

The Dynamics and Economy of Recommender Systems

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Recommender System (RS)

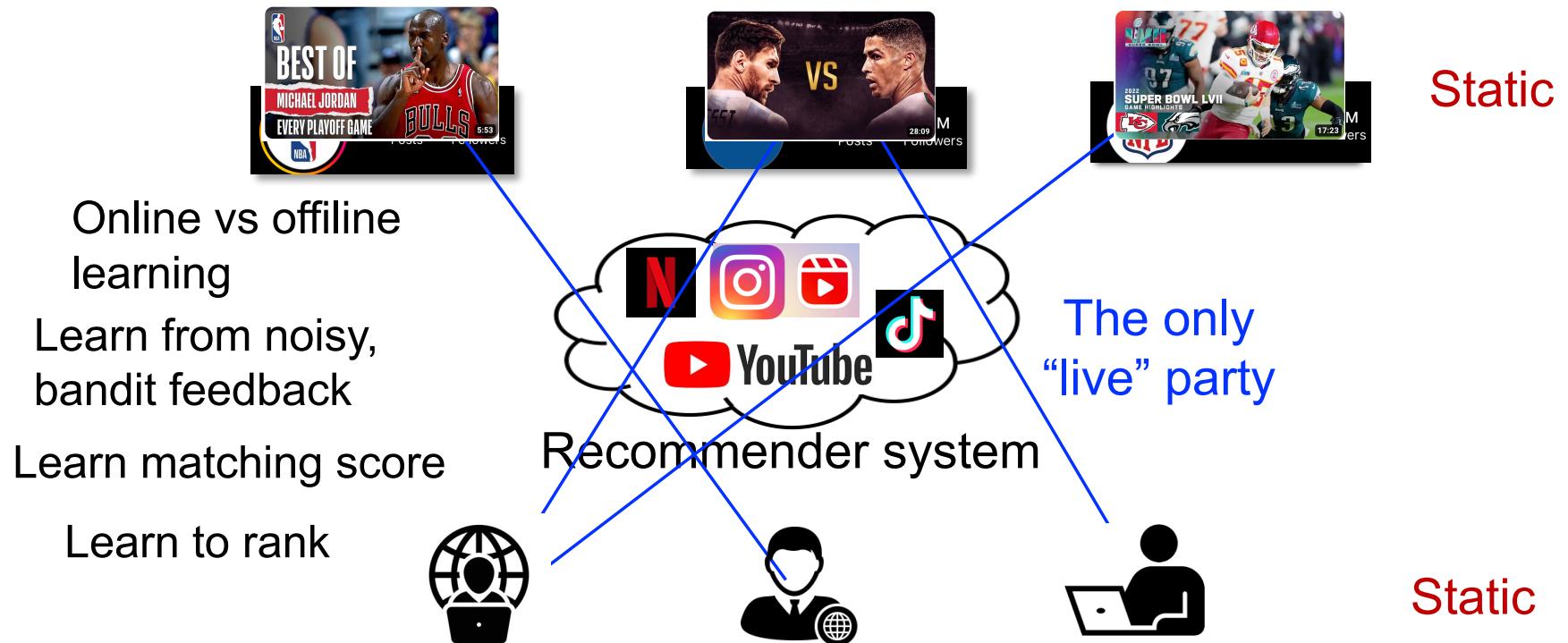
- An indispensable component of modern information systems

Google Revenue Breakdown (2021)

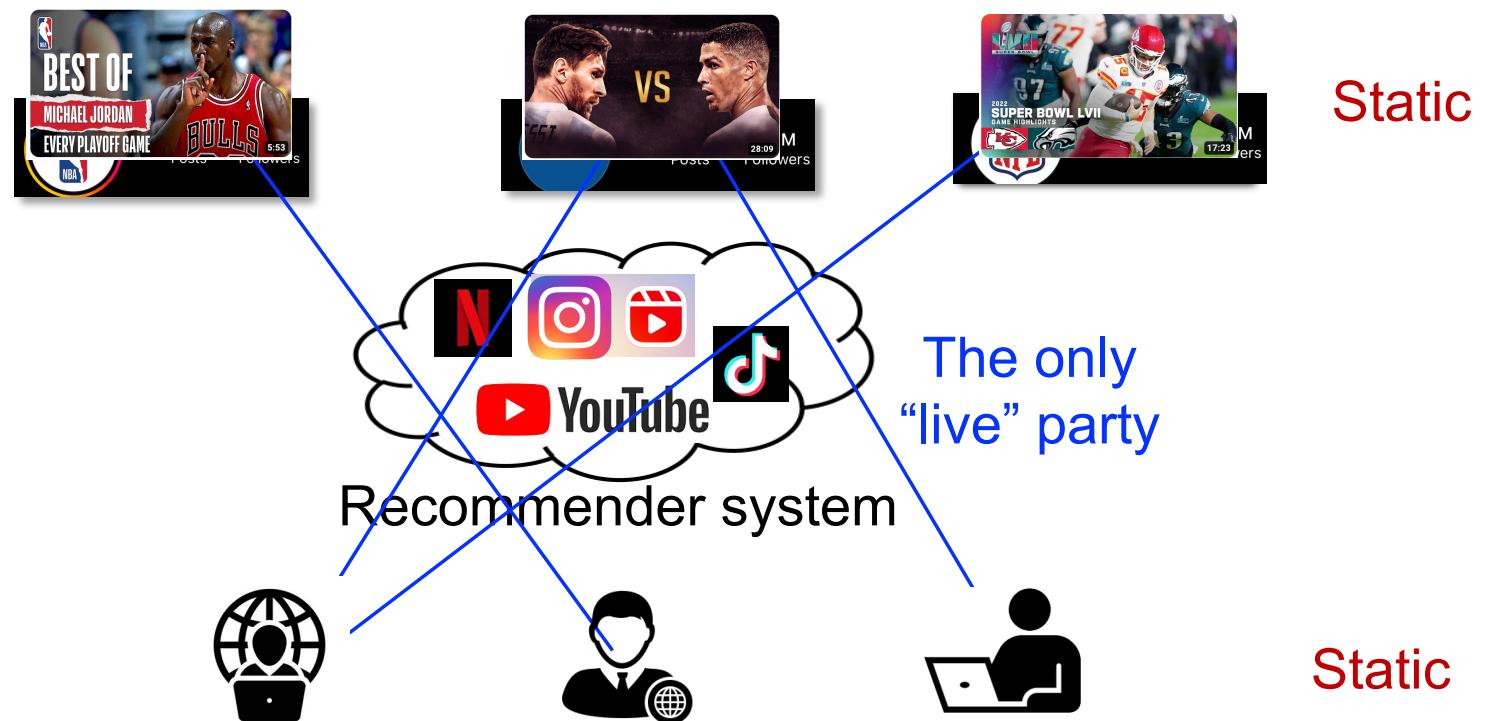
| Category | Revenue (\$ billion) | Percentage |
|--|----------------------|------------|
| Ads (Google Search & other properties) | \$148.95 billion | 58% |
| Google Network ads | \$31.7 billion | 12.3% |
| YouTube ads | \$28.85 billion | 11.2% |
| Apps, hardware, and content | \$28.03 billion | 10.9% |
| Google Cloud | \$19.21 billion | 7.5% |

Classic Research Paradigm in RSs

System learning
in
static environments

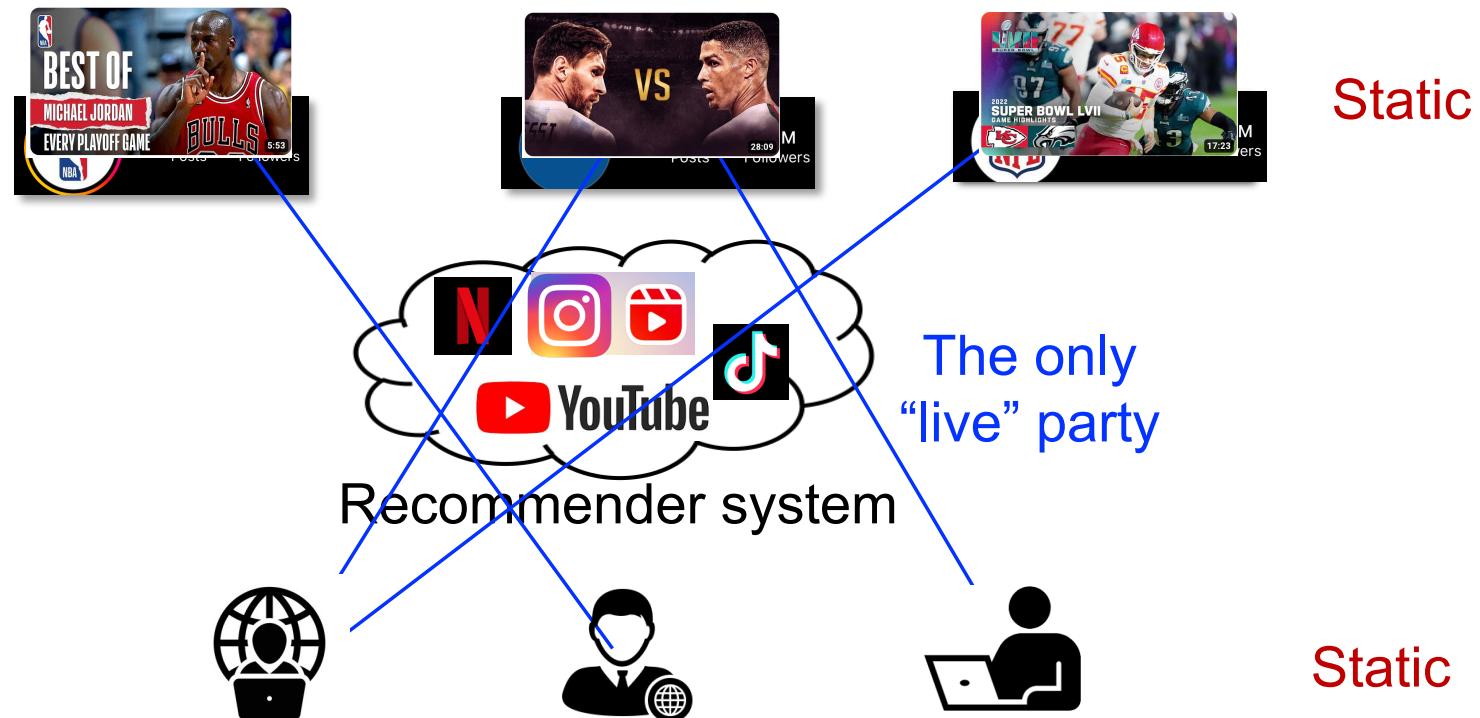


However...Numerous Evidence Supports Dynamic (Often Adaptive) Creator and User Behaviors



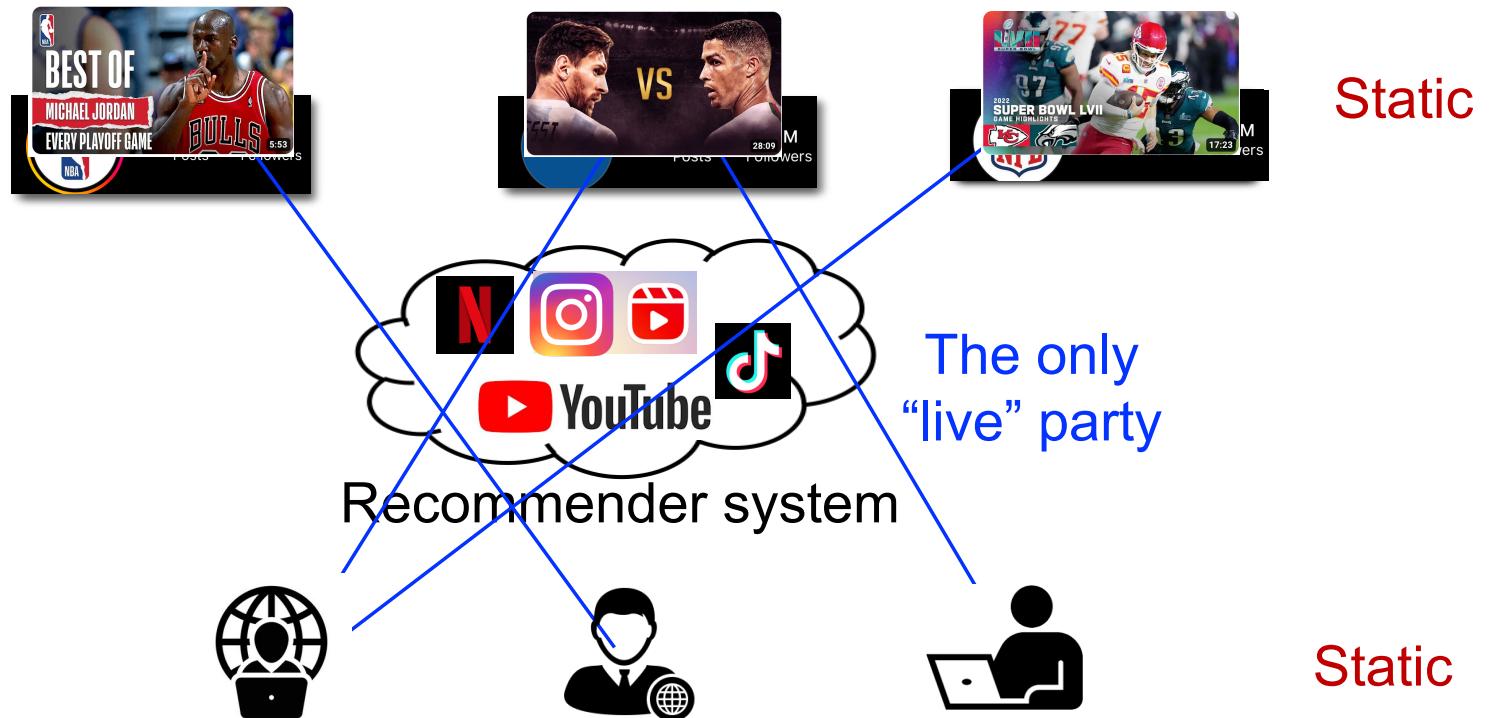
However...Numerous Evidence Supports Dynamic (Often Adaptive) Creator and User Behaviors

- **Creators** create longer videos after Youtube switches to use view duration to evaluate quality [MC'23]
- **RS users** are explorative at beginning (shown in many behavioral studies); Their feedback becomes more accurate only after sufficient experience



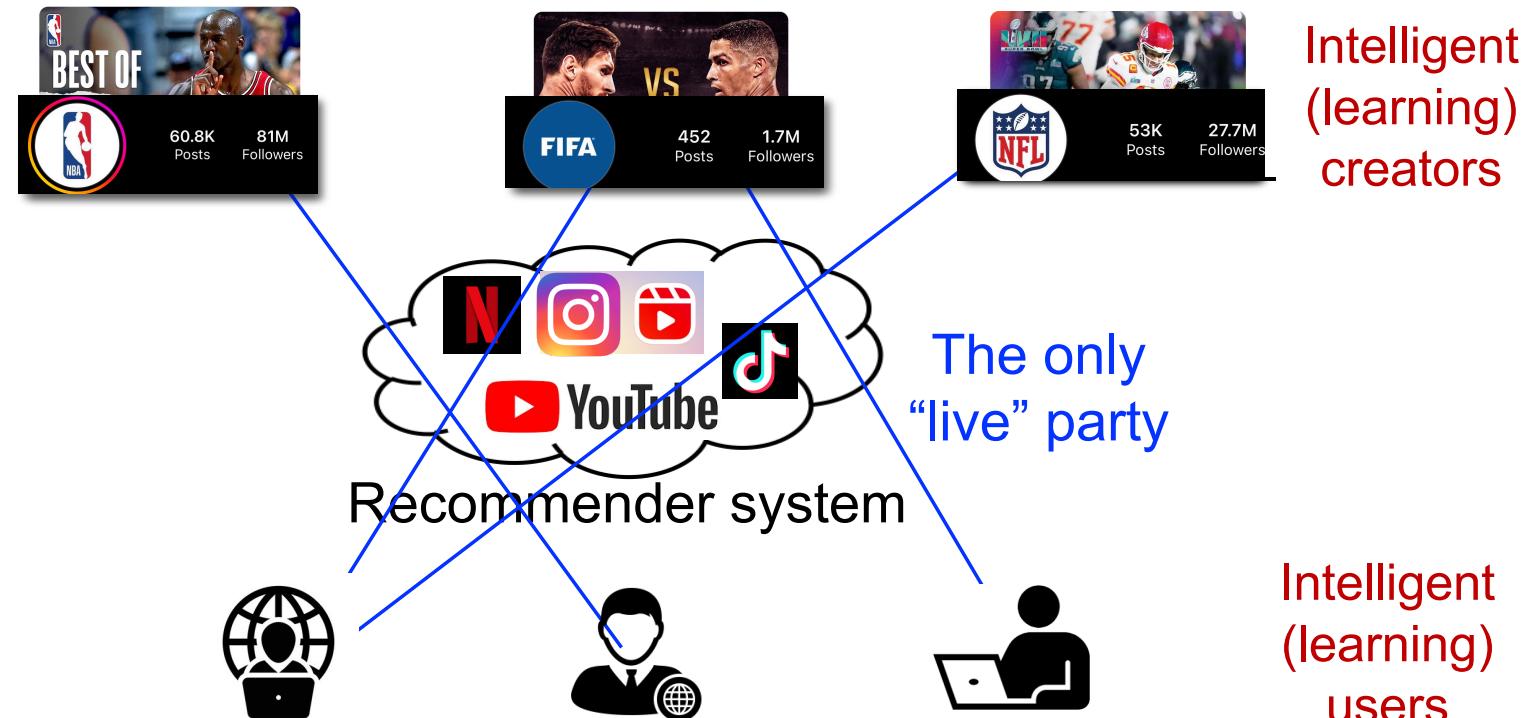
Rethinking this modeling paradigm....

System learning in static environments



Rethinking this modeling paradigm....

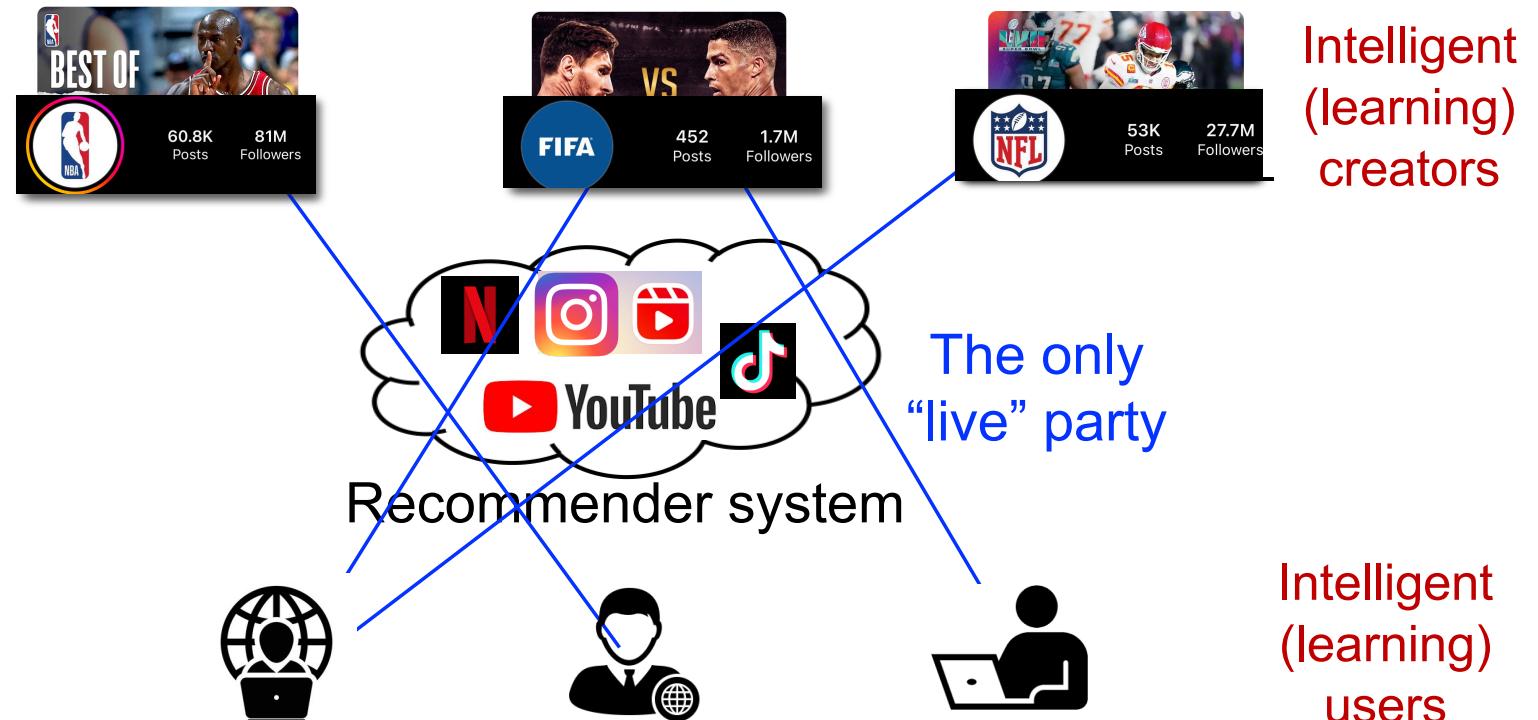
System learning in static environments



Theme of This Talk

(multi-agent) economic modeling and optimization
of recommender systems

Multi-agent — System learning
Rethinking this modeling paradigm.... in
non-stationary — static environments



Outline



Intelligent

Part 1: Interacting with Strategic Creators



Part 2: Learning from Learning Users



Intelligent
(learning)
users

Utility maximizing
(learning) agent



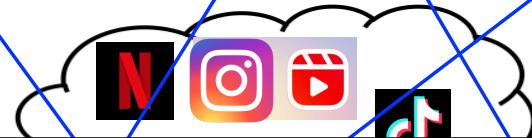
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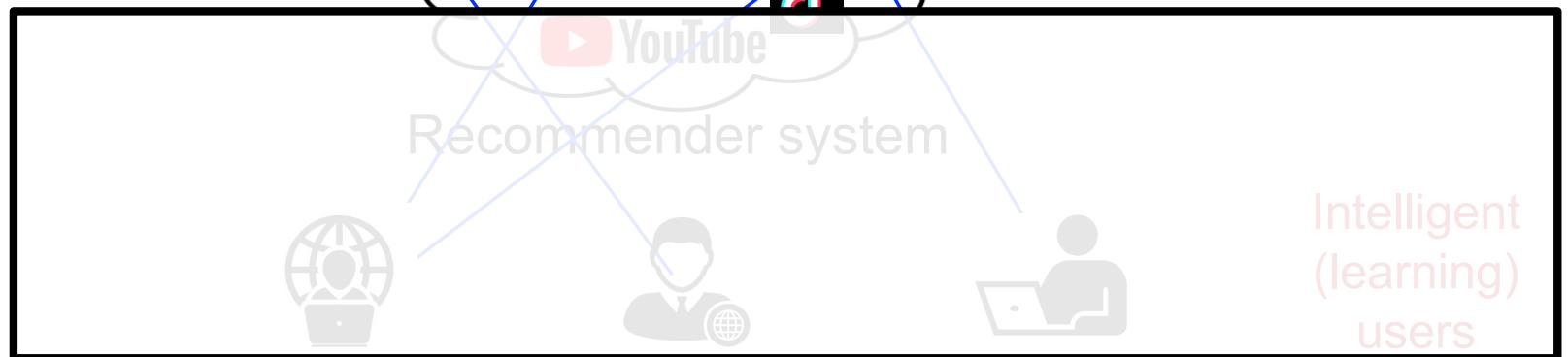
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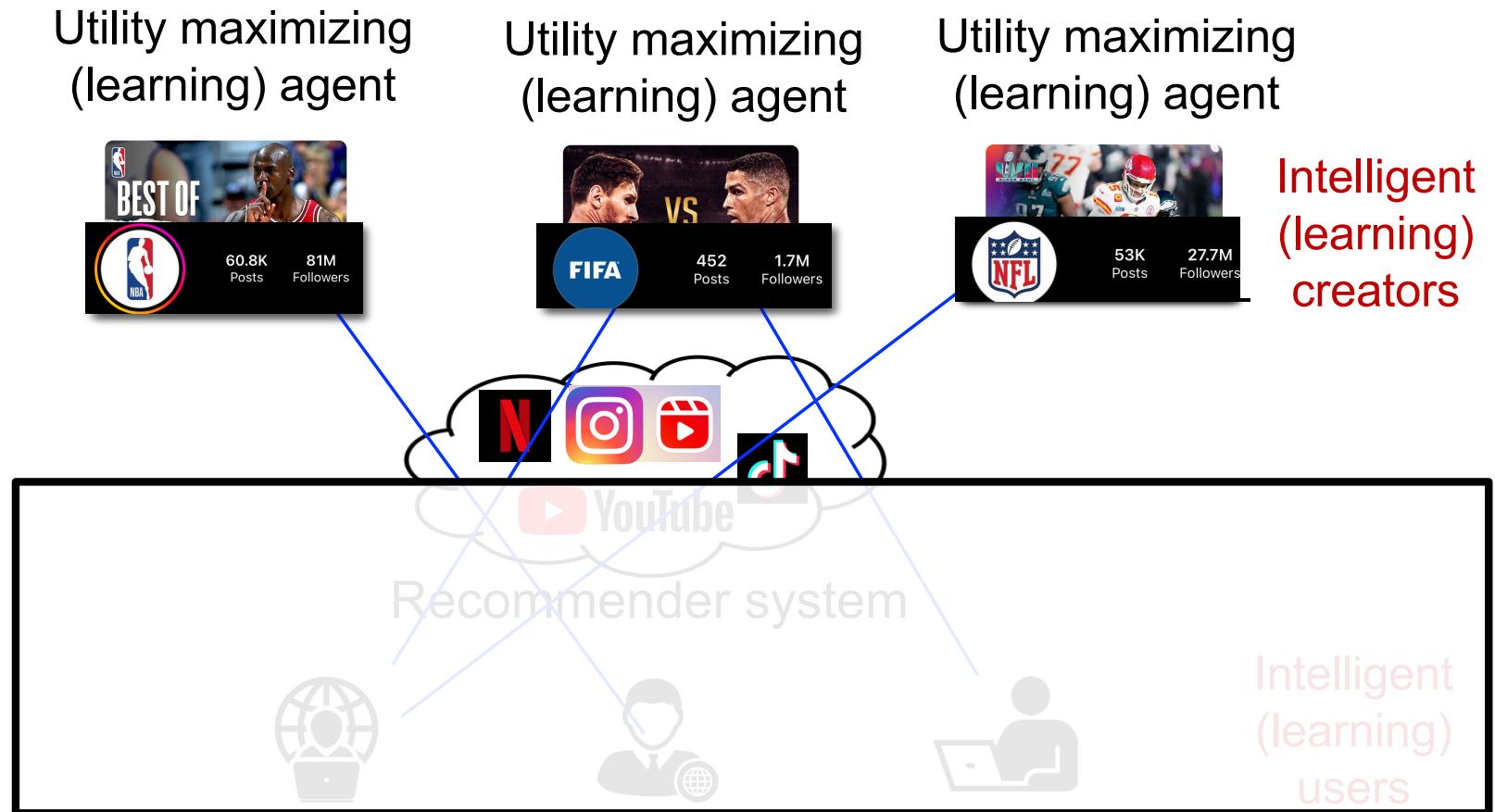
Intelligent
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creators



Recommender system



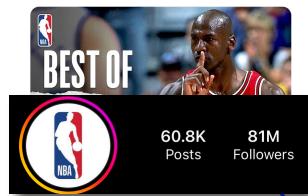
Q: do creators' learning dynamics converge to good or bad outcome?



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The Competing Content Creation (C3) Game

Utility maximizing
(learning) agent



Utility maximizing
(learning) agent



Utility maximizing
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Intelligent
(learning)
creators



Reward Generating Environments



content
(learning)
users

Q: do creators' learning dynamics converge to good or bad outcome?

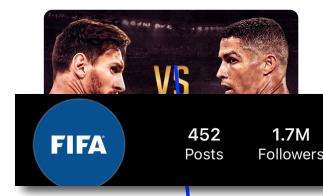
The Competing Content Creation (C3) Game

Contents
(actions)

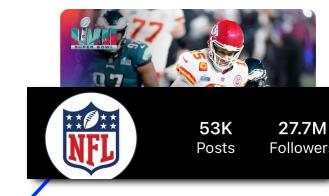
$$s_1 \in S_1$$



$$s_2 \in S_2$$



$$s_3 \in S_3$$



Estimated matching score: $\sigma(s_1, x)$

$\sigma(s_2, x)$

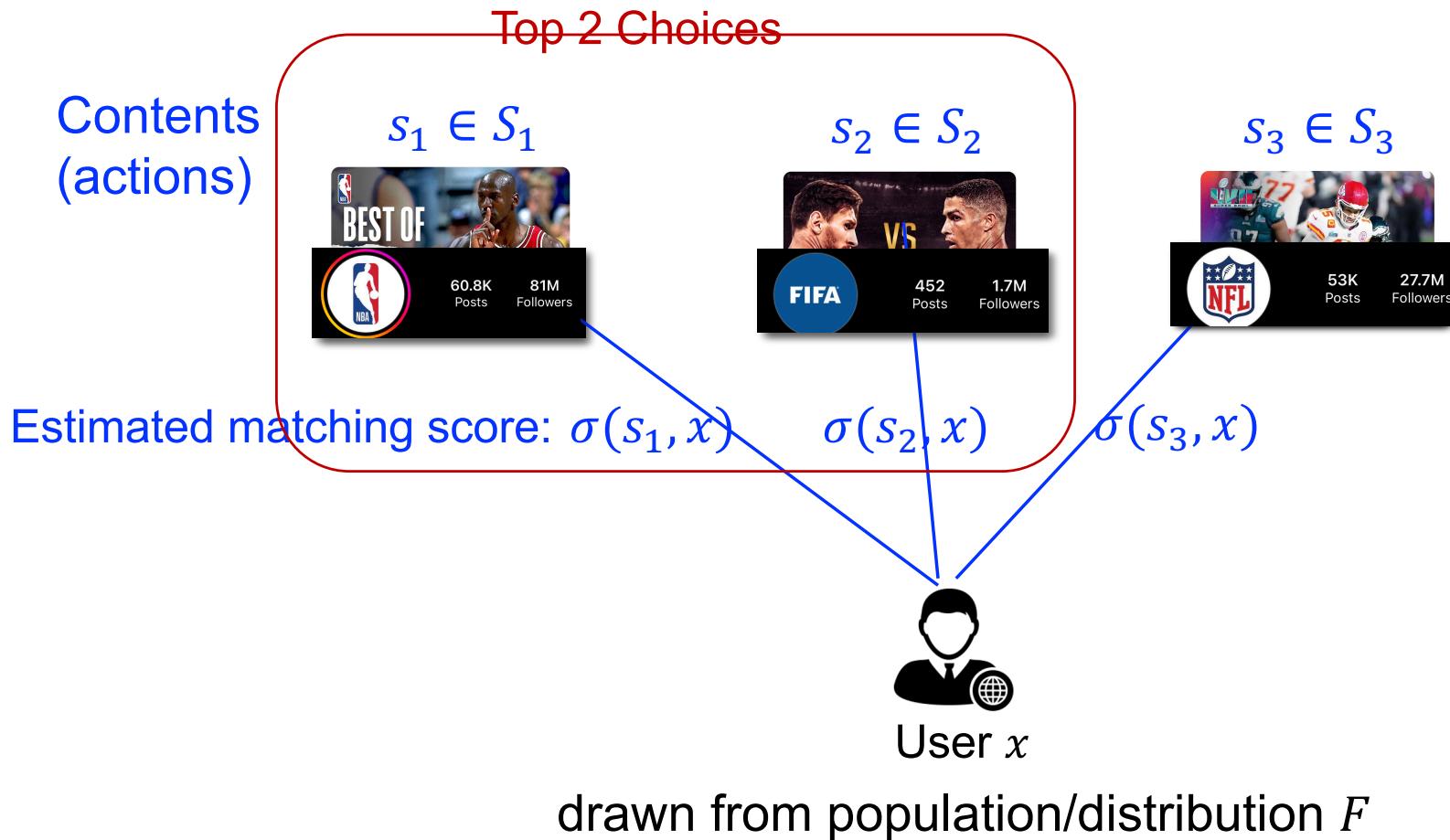
$\sigma(s_3, x)$



drawn from population/distribution F

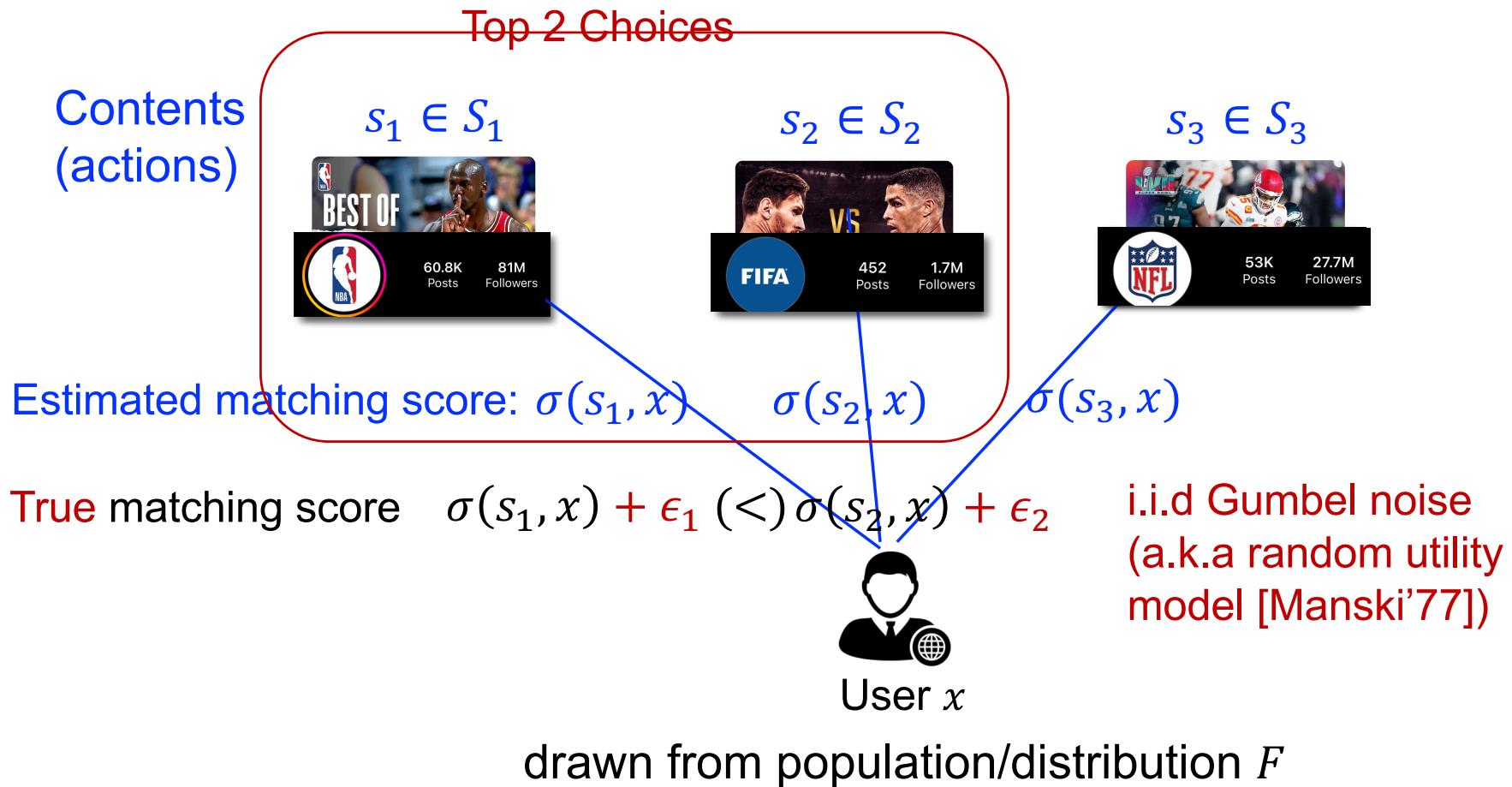
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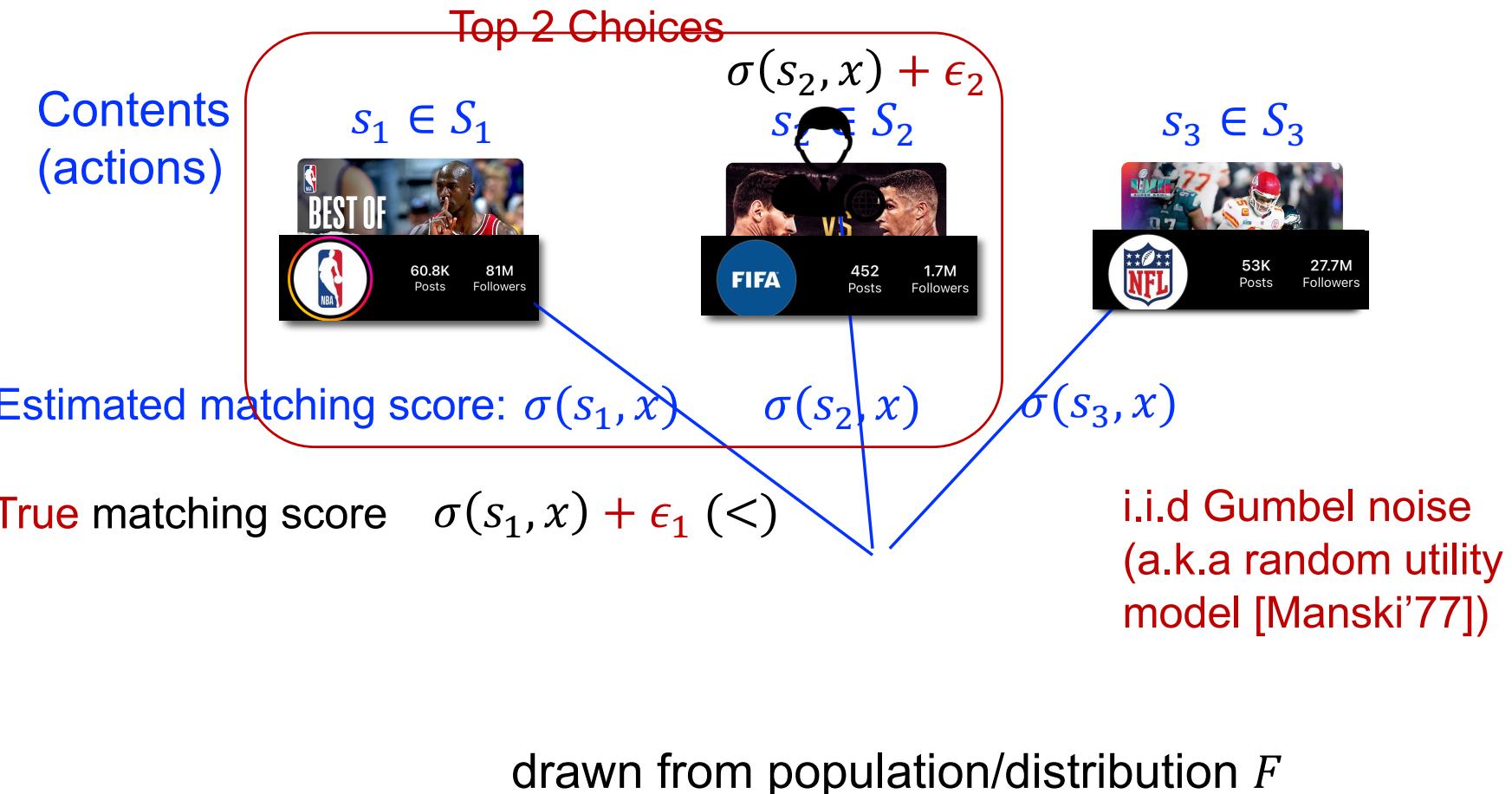
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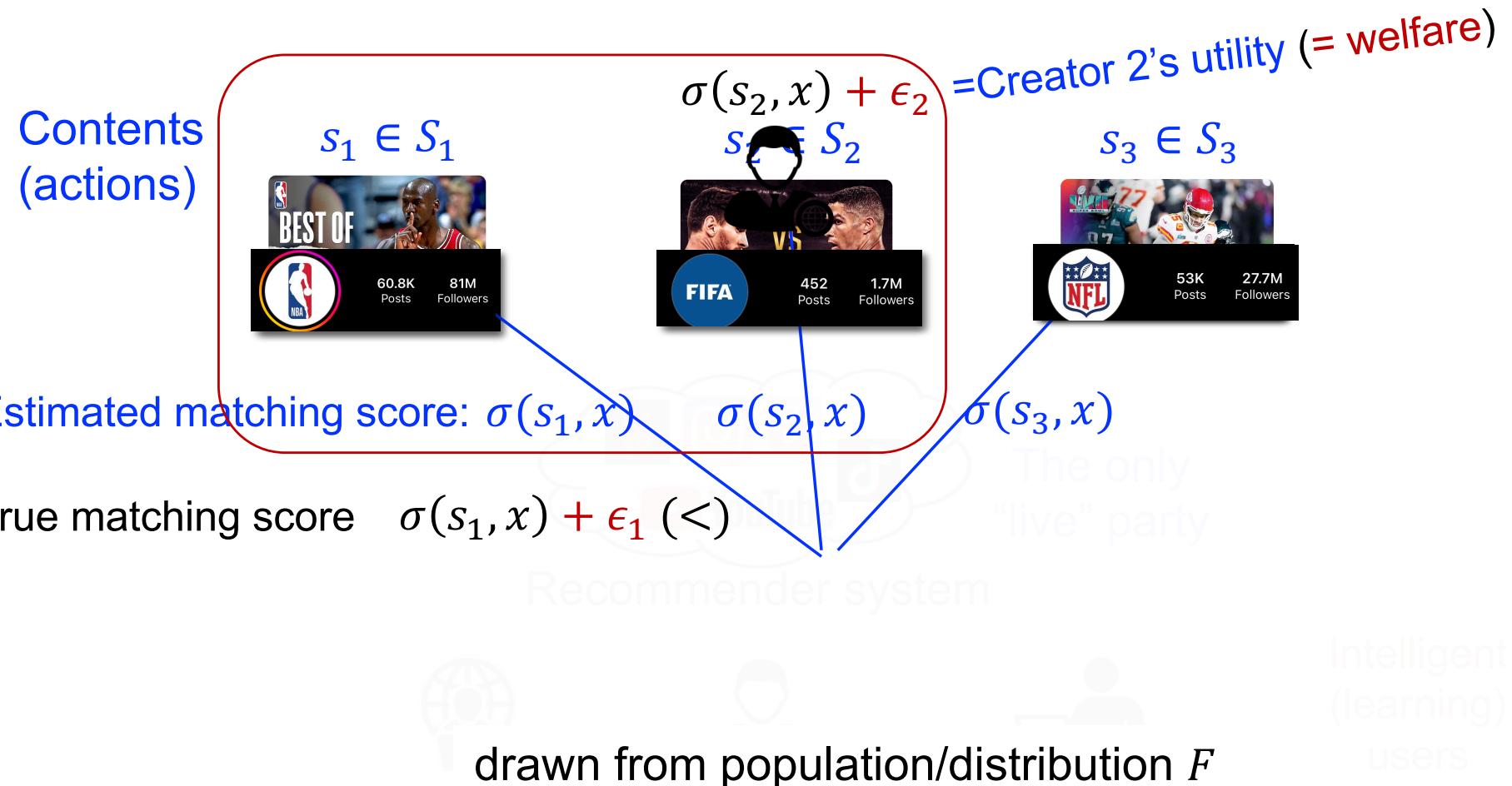
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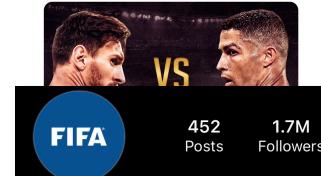
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Q: do creators' learning dynamics converge to good or bad outcome?

The Competing Content Creation (C3) Game

$$\sigma(s_2, x) + \epsilon_2 = \text{Creator 2's utility} (= \text{welfare})$$
$$s_2 \in S_2$$



$$\sigma(s_2, x)$$

How to model each content creator's behavior in the system?

→ Simple – they are just *any* “reasonable” (no-regret) learners who learn to maximize their own users' welfare/happiness

$$\mathbb{E}_{x \sim F} [(\sigma(s_2, x) + \epsilon_2) \cdot \mathbb{I}(x \text{ visits the creator})]$$

Q: do creators' learning dynamics converge to good or bad outcome?

The Competing Content Creation (C3) Game

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- The goal here is NOT to learn $\sigma(s, x)$ or set S_i 's
- Goal is to study **convergence property** in C3 under (non-stationary) creator learning dynamics, and resultant **system welfare**

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- The goal here is NOT to learn $\sigma(s, x)$ or set S_i 's
 - Goal is to study **convergence property** in C3 under (non-stationary) creator learning dynamics, and resultant **system welfare**
 - We do not directly consider revenue, but RS's revenue is often aligned with total user welfare
- Simple – they are just *any* “reasonable” (no-regret) learners who learn to maximize their own users' welfare/happiness

$$\mathbb{E}_{x \sim F} [(\sigma(s_2, x) + \epsilon_2) \cdot \mathbb{I}(x \text{ visits the creator})]$$

Q: do creators' learning dynamics converge to good or bad outcome?

Theorem [YLNWX, ICML'23]. In any C3 games, if each creator generates contents via *any* no regret learning algorithms, then w.h.p.

$$\frac{\text{Accumulated total welfare}}{\text{Idealized Maximum Welfare}} \geq 1 - \frac{1}{1 + (1 + \beta) \log(K)}$$

$K = \# \text{ of recommendation slots}$

$\beta^2 = \text{variance of Gumbel noise}$

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Remark

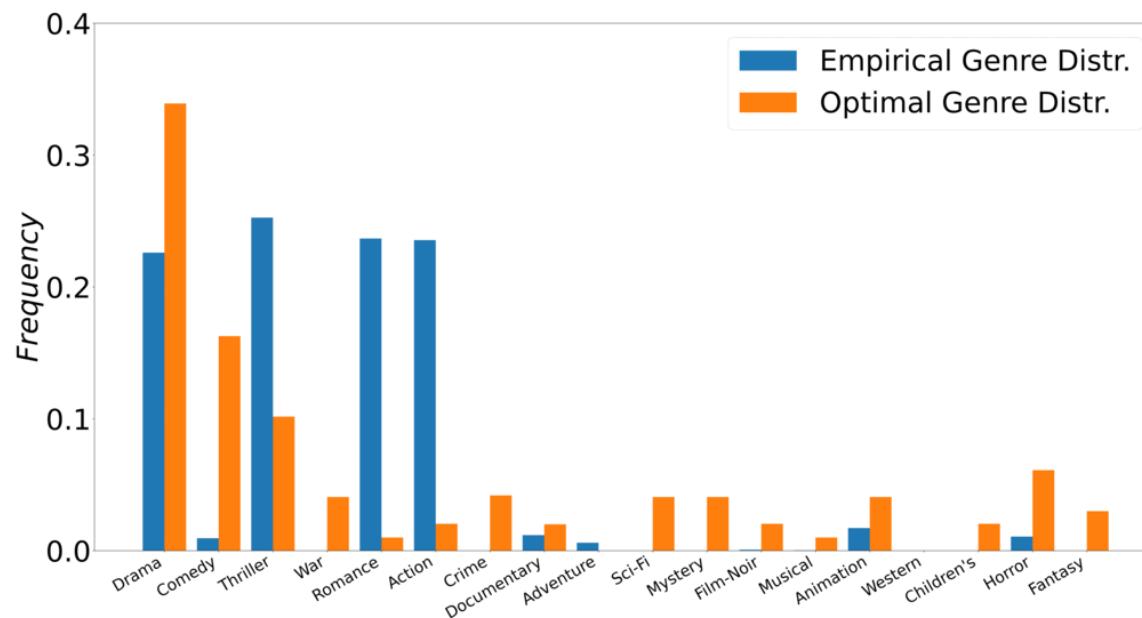
- Also known as the *price of anarchy (PoA)*
 - A very plausible and robust prediction about welfare [Blum et al.'08]
- The bound is an intrinsic property of content competition and user choices
 - Independent of matching score function $\sigma(s, x)$ and #users

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Simulation on MovieLens dataset between **empirical** and **ideal** content distributions



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This bound is (order-wise) tight

Prop 1. There exists C3 games such that is PoA (even for Nash) satisfies

$$\frac{\text{Accumulated total welfare}}{\text{Idealized Maximum Welfare}} \leq 1 - \frac{1}{2 + 5\beta \log(K)}$$

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Proof Sketch

- Core insight – C3 is a smooth game [Roughgarden'12]
- Proof turns out to be quite involved
 - Hinges on various analytical properties about the C3 game
 - E.g., total welfare is submodular in the set of contents

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- Proof turns out to be quite involved
 - Hinges on various analytical properties about the C3 game
 - E.g., total welfare is submodular in the set of contents
- **Fun fact:** smoothness technique for C3 yields (order-wise) tight PoA
 - Before this, only 3 classes of games are known to satisfy this (linear congestion game, second price auction and valid utility games)

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Economic insights:

- More recommendation slots (K large), more efficient the system is

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Economic insights:

- More recommendation slots (K large), more efficient the system is
- Setting proper creator incentives matters a lot!

In previous model

Creator's utility \sim True user matching score

$$= \sigma(s_2, x) + \epsilon_2$$

\approx user engagement

What if

Creator's utility \sim Pr(being matched to user)

\approx user traffic

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Prop 2. Suppose creators' utilities are propositional to **user traffic** in C3 games, then there are C3 games such that

$$\frac{\text{Accumulated total welfare}}{\text{Idealized Maximum Welfare}} \leq \frac{1}{2}$$

What if

Creator's utility $\sim \Pr(\text{being matched to user})$
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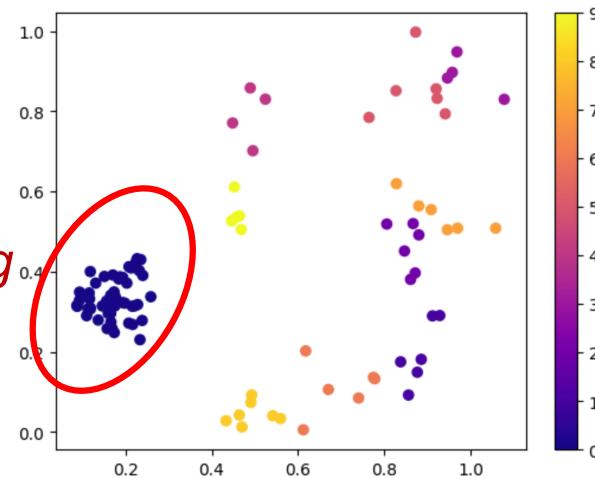
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What situation is worrisome?

Trend-vs-Niche!

A dominating user group



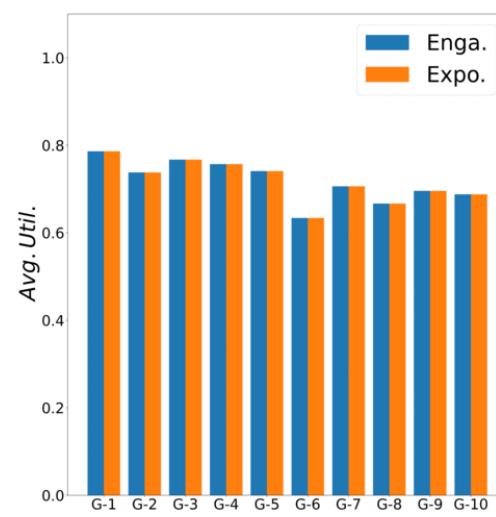
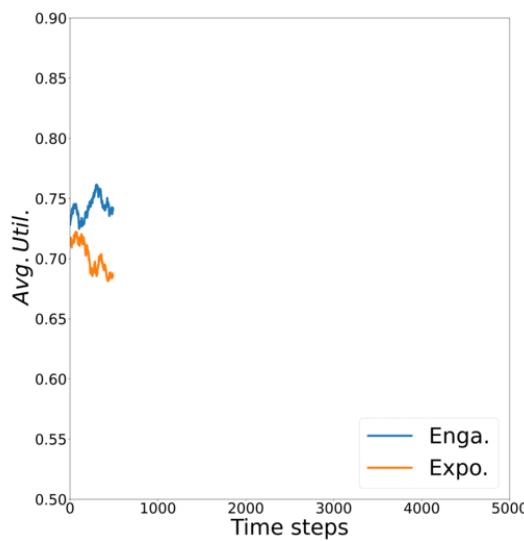
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Simulations of no-regret creators on synthetic data

— user engagement
— user traffic

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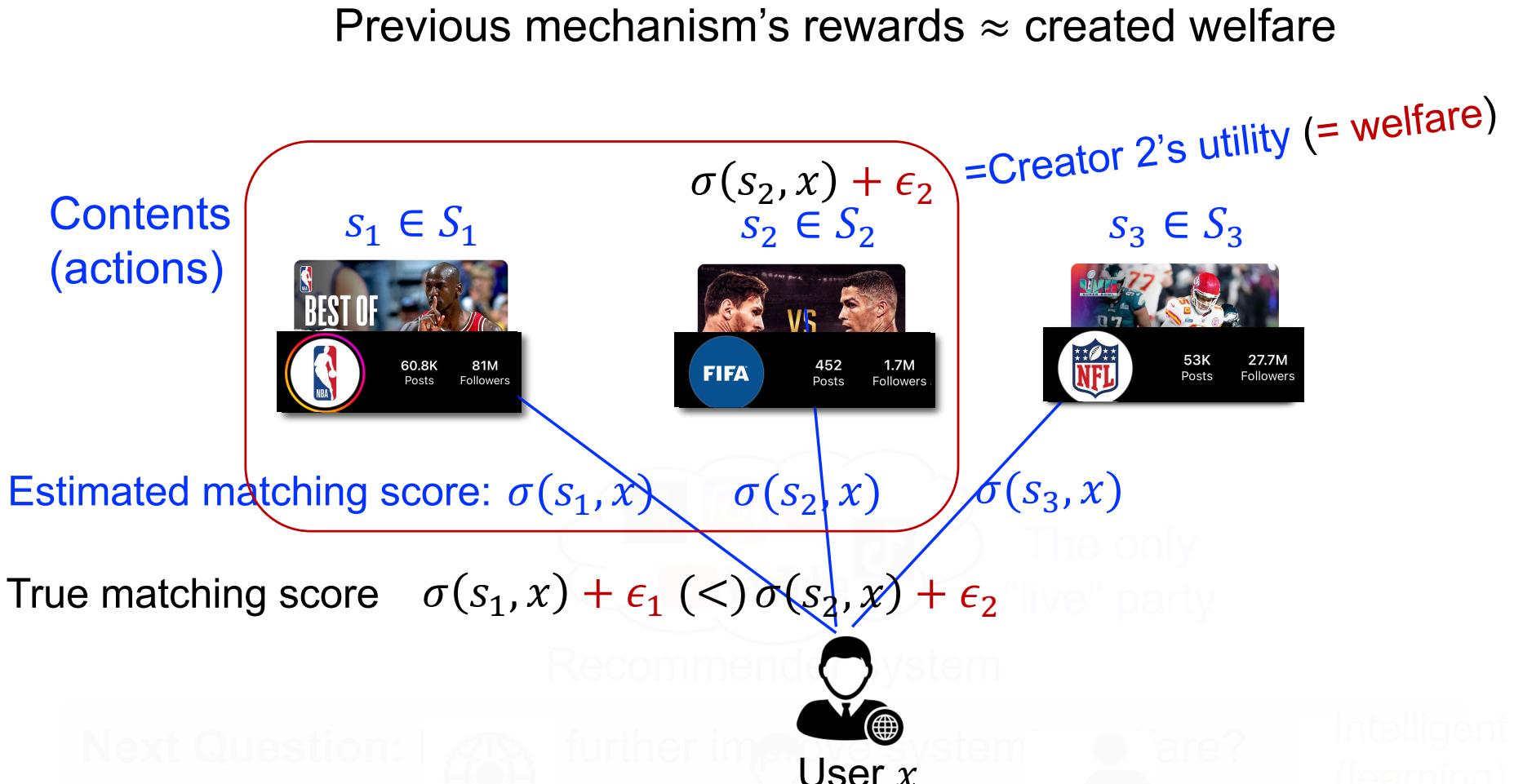
- More recommendation slots (K large), more efficient the system is
- Setting proper creator incentives matters a lot!
- Larger β – users are more explorative – increases efficiency
- In practice, still constant fraction loss since $K \leq 12$

Next Question: how to further improve system's welfare?

Incentive Design for Rewarding Creation

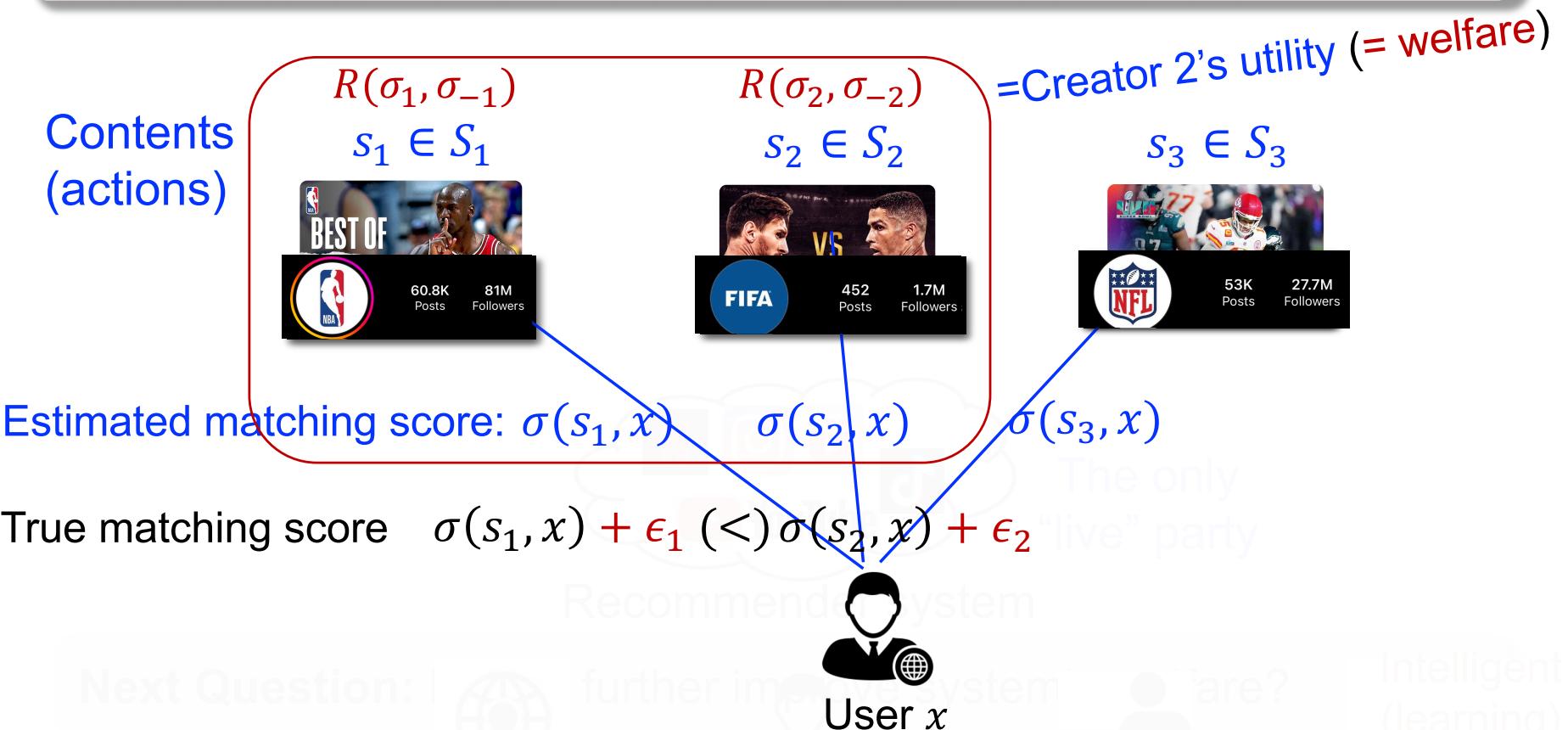
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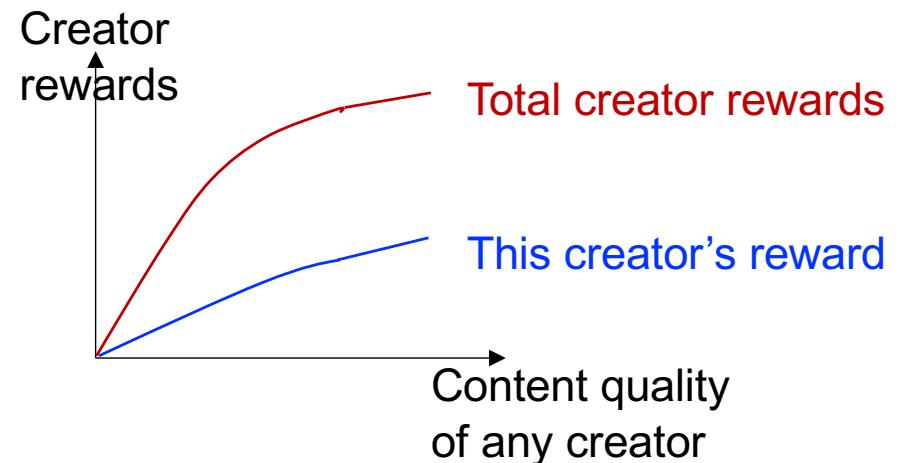
Incentive Design for Rewarding Creation

Q: Can we design/optimize the reward values R to “steer”/incentivize creators’ collective behaviors towards better total welfare?



Why current rewarding mechanism may not be good?

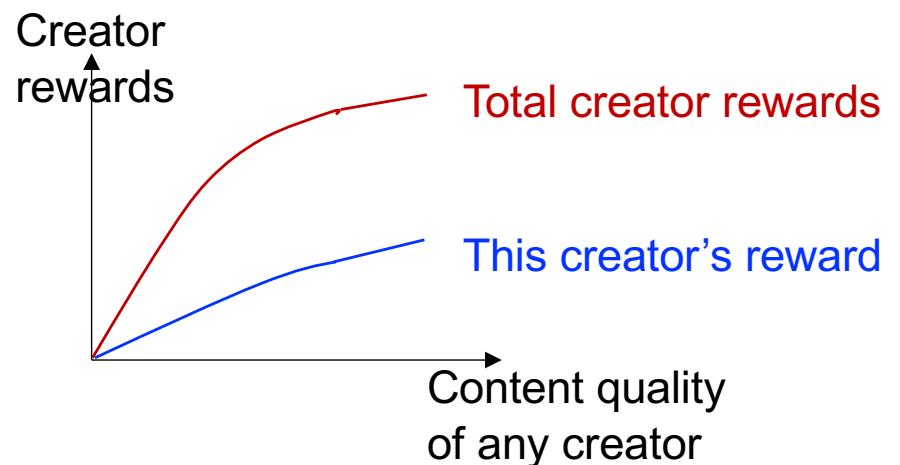
Theorem [Yao et al.'23]. If a rewarding mechanism R are **both individual-monotone** (better contents get more rewards) and **group-monotone**, then it necessarily suffer at least $1/K$ fraction of welfare loss at equilibrium



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- *User engagement and user traffic* do satisfy both; so do many natural rewarding mechanisms in real-world

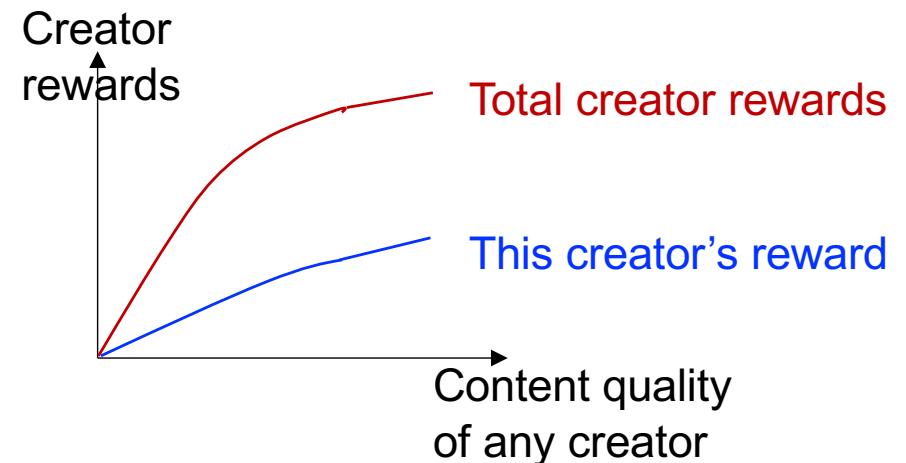


“Rethinking Incentives in Recommender Systems”

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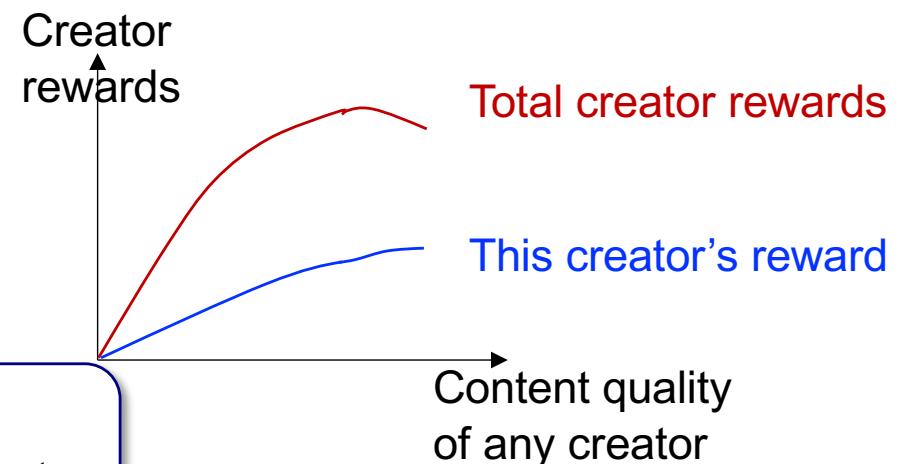
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- *User engagement and user traffic* do satisfy both; so do many natural rewarding mechanisms in real-world
- To overcome this limitation, we **drop group-monotonicity**

Why reasonable?

Group-monotonicity is generally not satisfied in economic markets!



“Rethinking Incentives in Recommender Systems”

Our new mechanism. We designed a new rewarding mechanism that drops group-monotonicity, but provably achieves optimal welfare

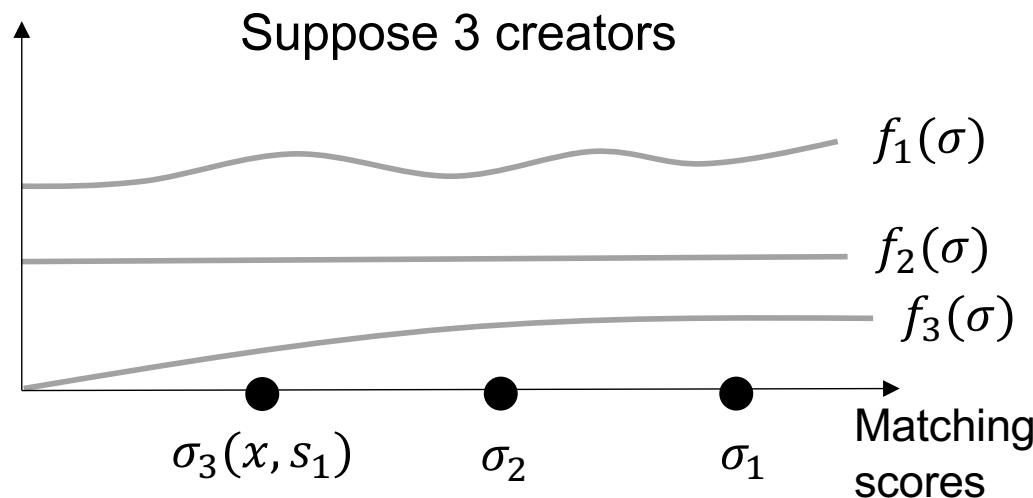
Core idea: reward based on how much you are better than the next

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- Mechanism is fully described by functions f_1, f_2, f_3

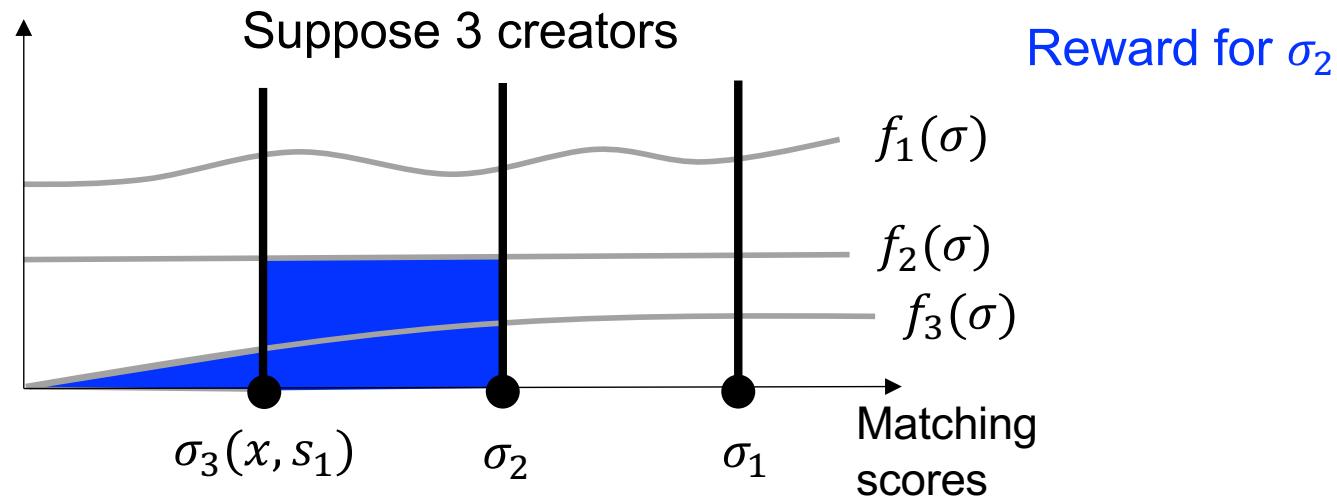


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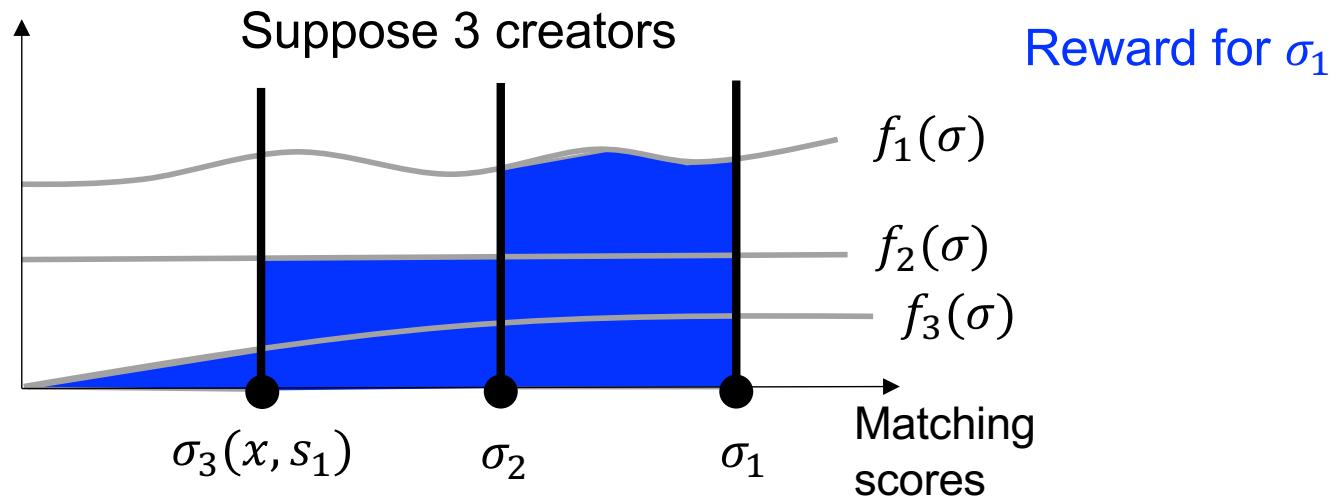


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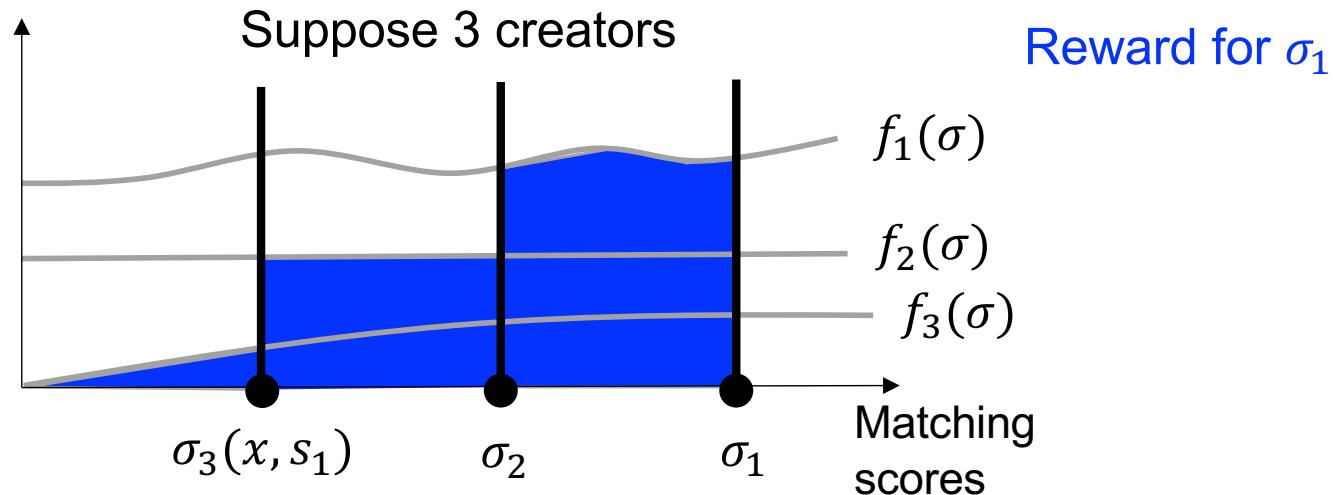
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Advantages

- ✓ σ_1 's reward decreases when σ_2 becomes better (i.e., competition reduces rewards)



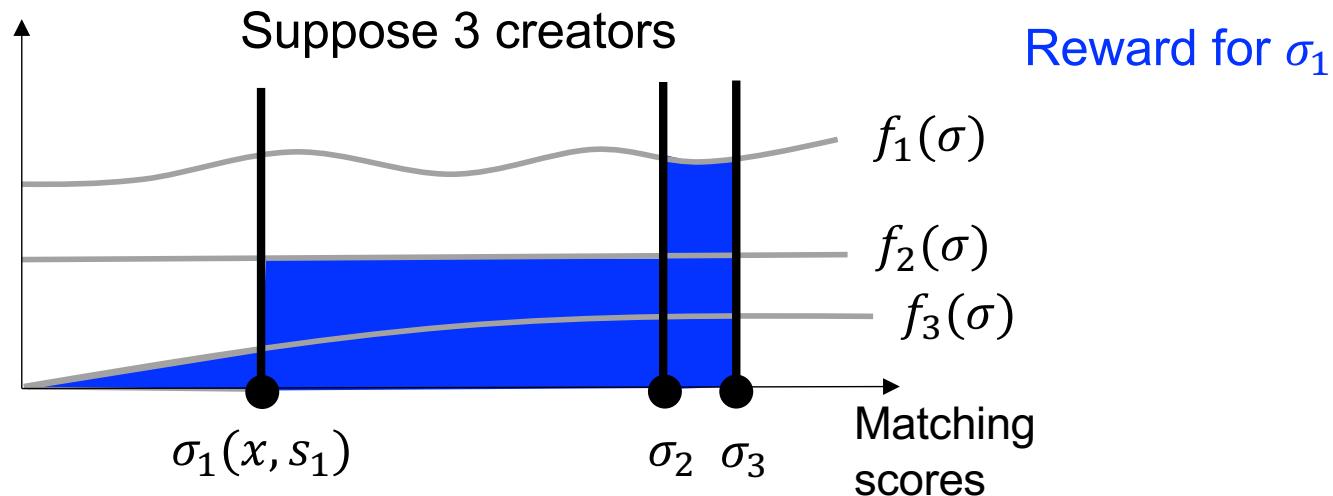
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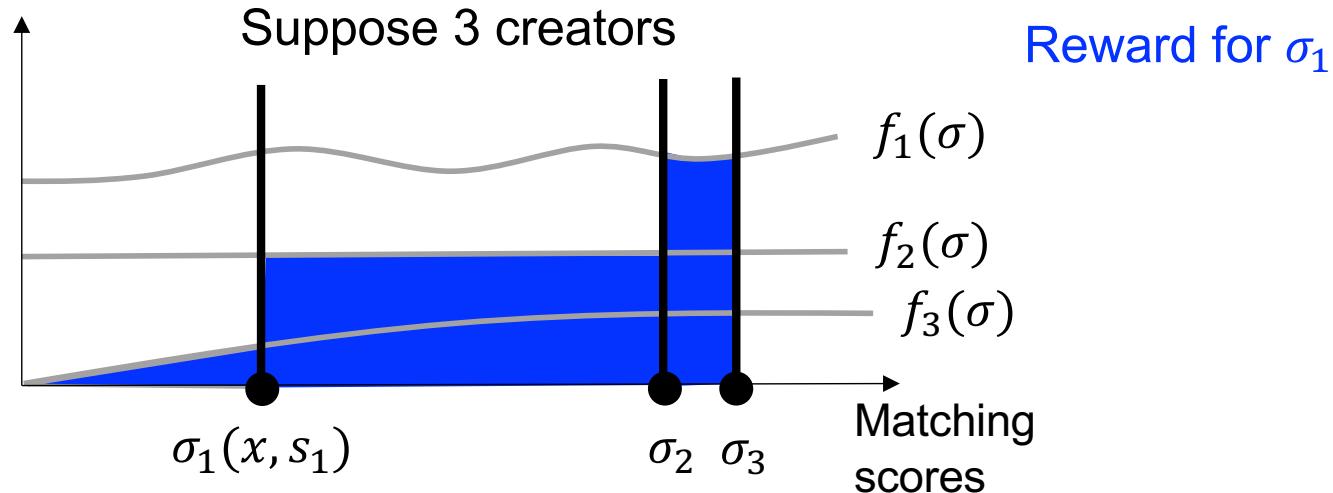
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- ✓ Naturally handles top- K selection by setting $f_{K+1} = \dots = f_n = 0$



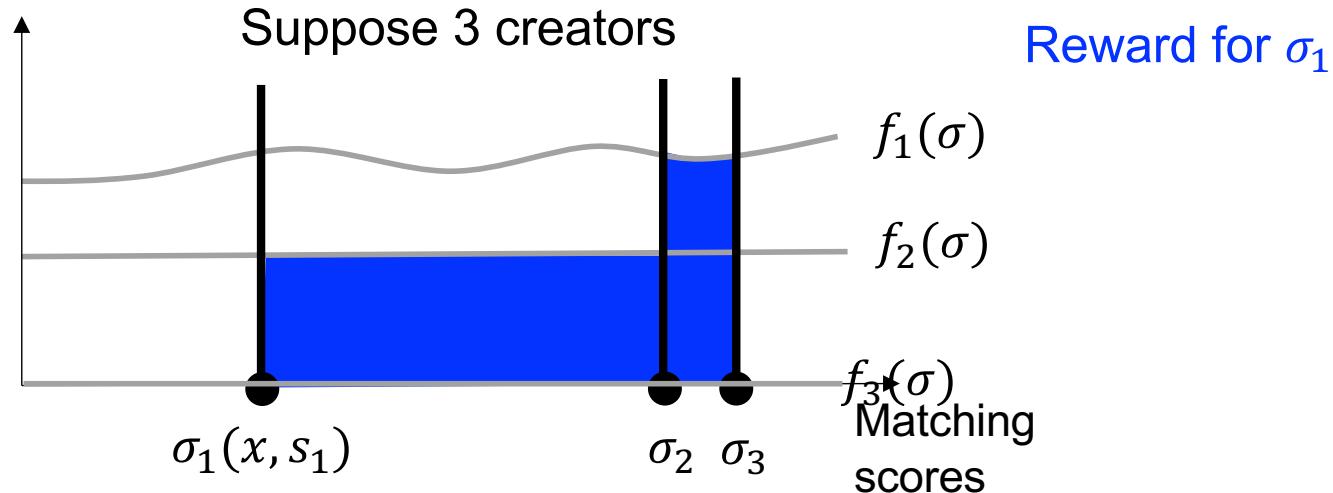
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- Proof idea: the reward mechanism above induce a potential game among creators, such that potential function = welfare function

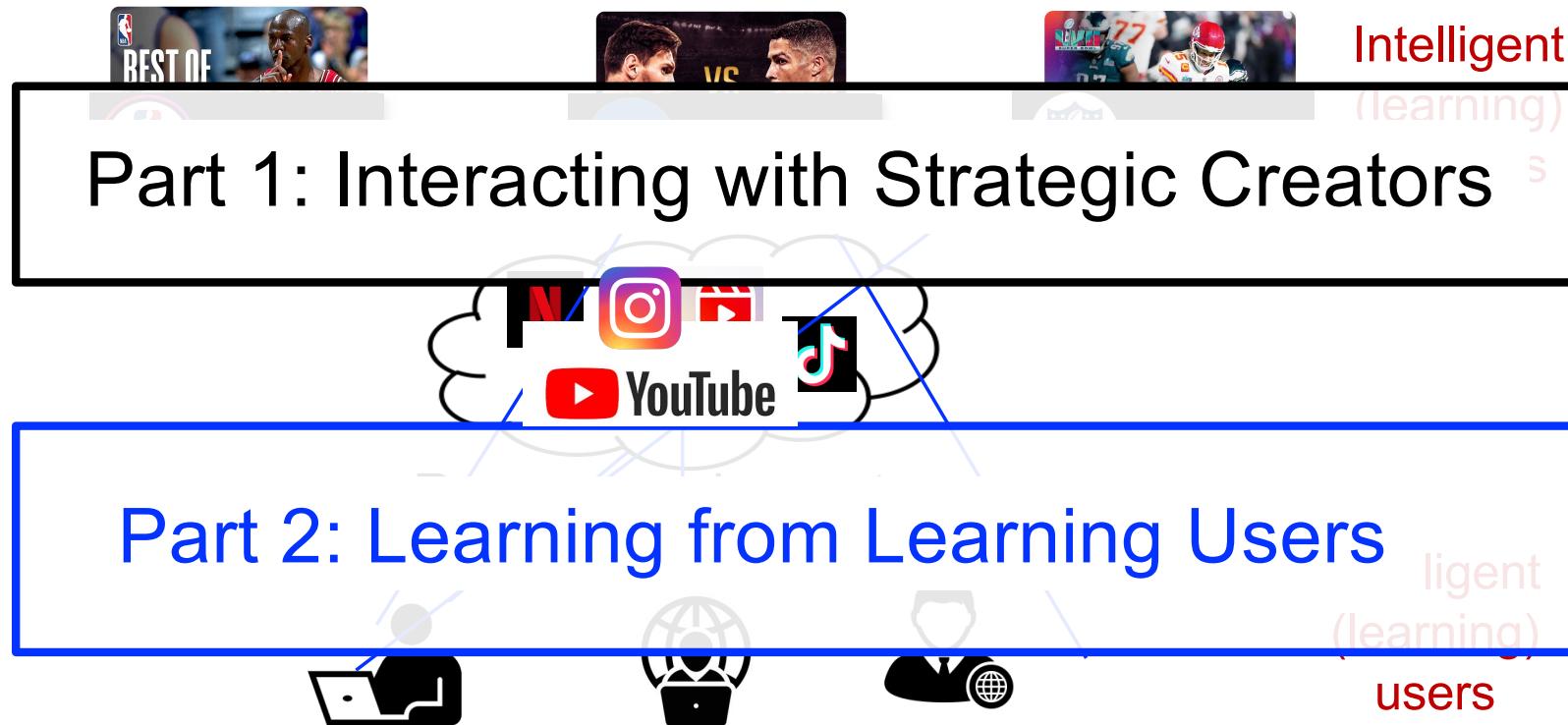
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- Project done in collaboration with researchers at Meta
- Under live experiments on Instagram for >1month now
 - Disclaimer: the deployed algorithm is inspired by, but different from the exact design above

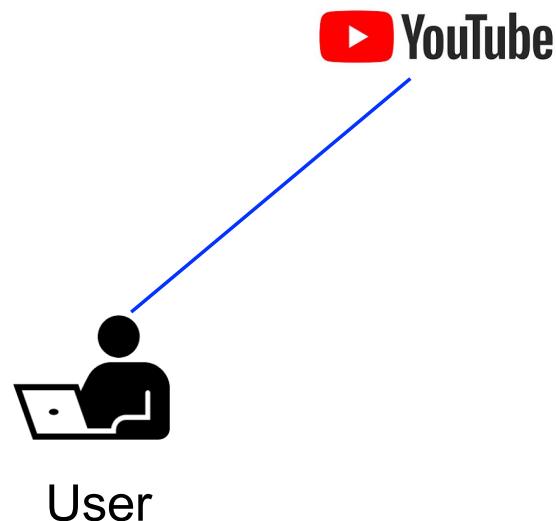


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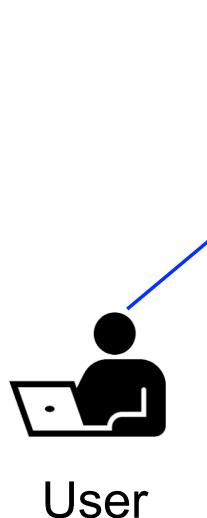
Different Research Challenges

| | Creator side | User side |
|-----------|------------------------------------|----------------------------------|
| Difficult | Incentives, Strategic behaviors | User preferences |
| Easy | Contents' embedding | Incentive (typically aligned) |



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| Difficult | Incentives, Strategic behaviors | User preferences |
| Easy | Contents' embedding | Incentive (typically aligned) |

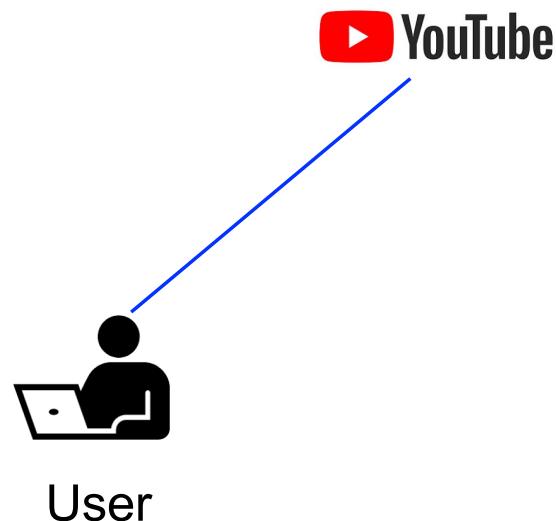


- Very often, users themselves even do not know what they like the most
 - ❖ uninformative/misleading feedback at beginning
- Many behavioral/marketing studies show
 - ❖ RS users are explorative at beginning;
 - ❖ Their feedback becomes more accurate only after sufficient experience
 - ❖ (see more discussions in [Yao et al., ICML22])

Different Research Challenges

Q: how to learn user preferences from evolving/non-stationary behaviors?

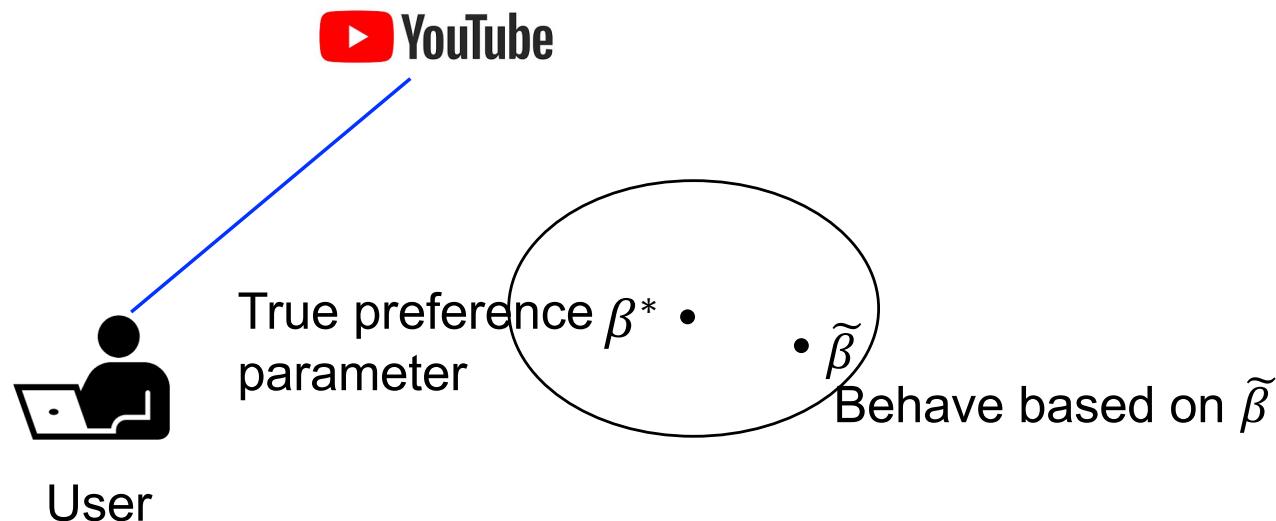
- ❖ Learning from learning users



Different Research Challenges

Q: how to learn user preferences from evolving/non-stationary behaviors?

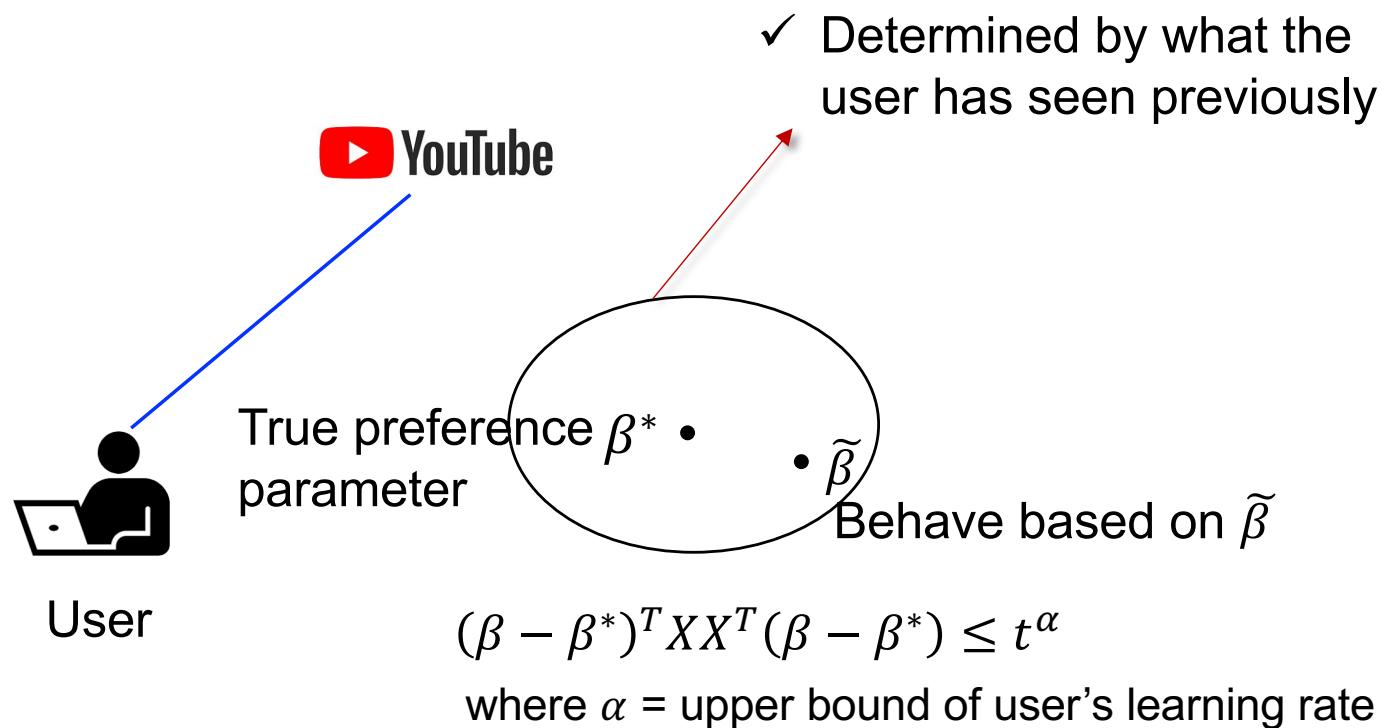
- ❖ Learning from learning users



Different Research Challenges

Q: how to learn user preferences from evolving/non-stationary behaviors?

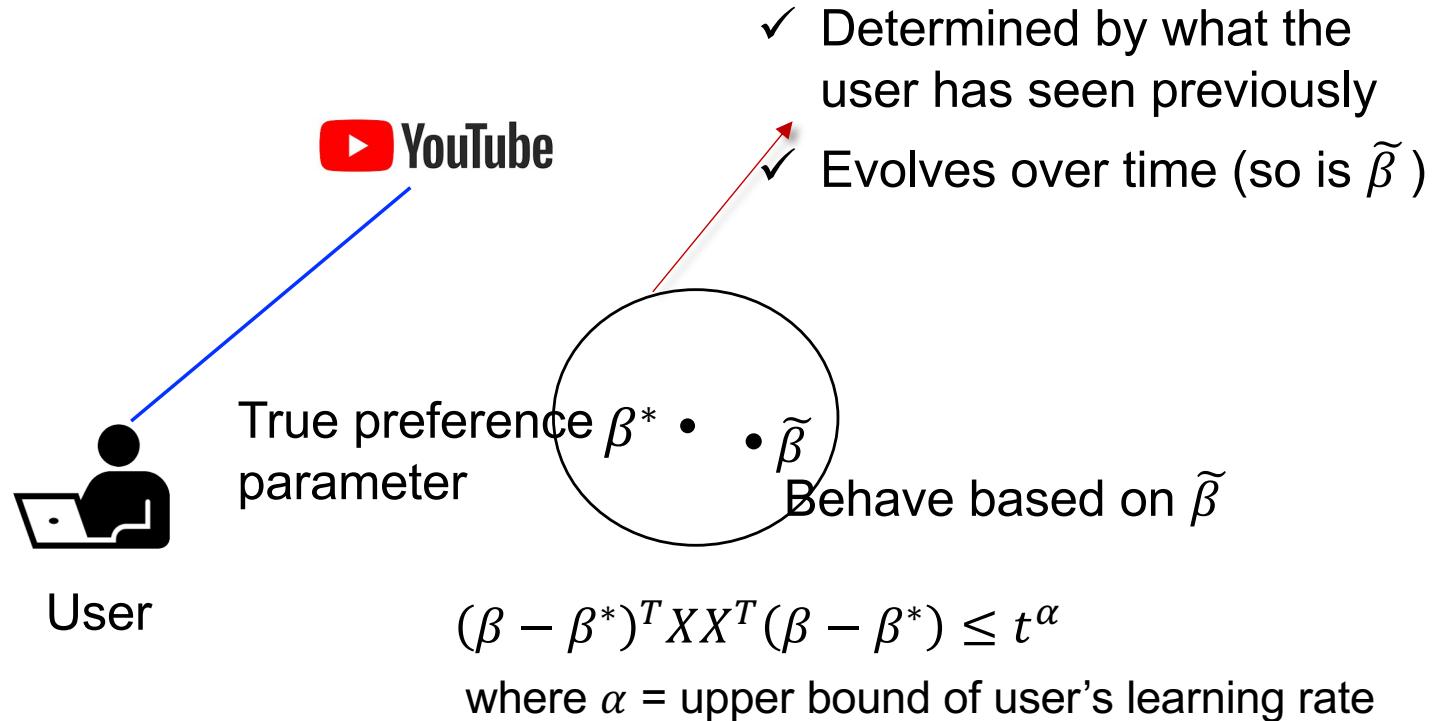
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Different Research Challenges

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Different Research Challenges

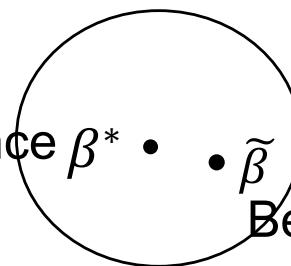
Q: how to learn user preferences from evolving/non-stationary behaviors?

Can design algorithm to effectively learn from such non-stationary user feedback (driven by user's own learning)



User

True preference
parameter



Behave based on $\tilde{\beta}$

Different Research Challenges

Q: how to learn user preferences from evolving/non-stationary behaviors?

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Core ideas

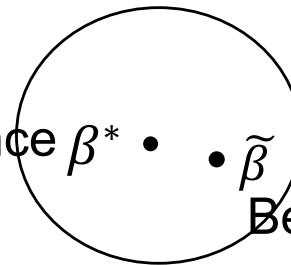
- ✓ Cultivate user's own learning at first with more aggressive exploration

⚠ Challenge: tailor exploration time based on user's learning rate α



User

True preference
parameter



Behave based on $\tilde{\beta}$

Different Research Challenges

Q: how to learn user preferences from evolving/non-stationary behaviors?

Can design algorithm to effectively learn from such non-stationary user feedback (driven by user's own learning)

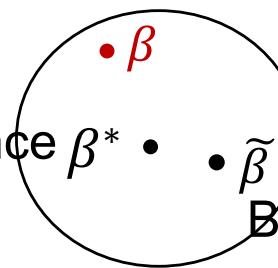
Core ideas

- ✓ Cultivate user's own learning at first with more aggressive exploration
- ✓ Robustify the use of user's reward feedback, since it is never perfect though gradually improving



User

True preference
parameter



Behave based on $\tilde{\beta}$



Challenge: robustify the learning for
arbitrary β in the confidence region

Different Research Challenges

Q: how to learn user preferences from evolving/non-stationary behaviors?

Can design algorithm to effectively learn from such non-stationary user feedback (driven by user's own learning)

Overall, it is good news!

Theorem [informal]. There is an algorithm that learns optimal user preferences with regret $O(T^{0.5+\alpha})$ where α is user's own learning rate.

Different Research Challenges

Q: how to learn user preferences from evolving/non-stationary behaviors?

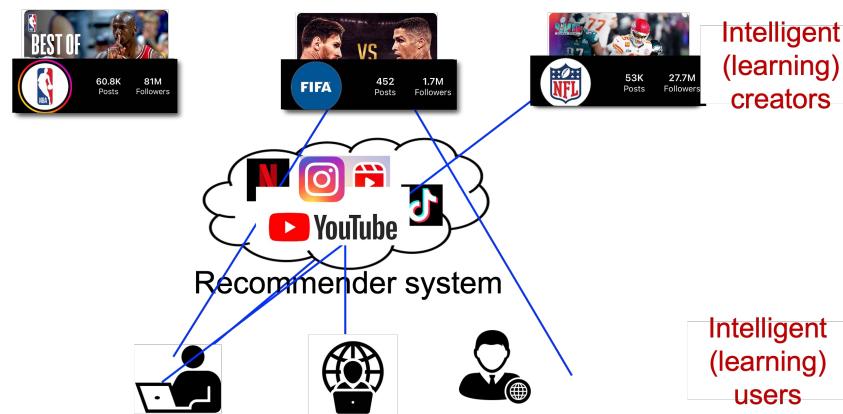
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Overall, it is good news!

Theorem [informal]. There is an algorithm that learns optimal user preferences with regret $O(T^{0.5+\alpha})$ where α is user's own learning rate.

- $\alpha = 0 \rightarrow$ perfect user, in which case we recover optimal regret for standard setups
- Generally, learning efficiency degrades gracefully as user less efficient

Conclusions



- A framework for economic modeling of **contemporary system-creator-user** learning + optimization
- Examined some basic questions during system-creator and system-user interactions
- Many open questions
 - What if three parties are learning contemporarily?
 - What if user preference is contextual as well? (e.g., $\theta(x) = \Theta \cdot x$ where x is a search query)

Acknowledgment



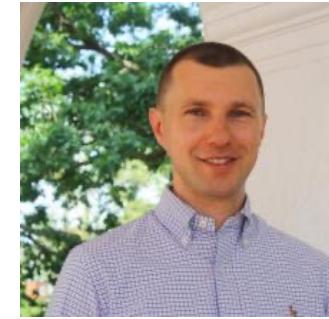
Fan Yao



Hongning Wang



Chuanhao Li



Denis Nekipelov



Karthik
Sankararaman



Yiming Liao



Yan Zhu



Qifan Wang

References

Learning from a Learning User for Optimal Recommendations

Fan Yao, Chuanhao Li, Denis Nekipelov, Hongning Wang and Haifeng Xu ICML 2022

How Bad is Top-K Recommendation under Competing Content Creators?

Fan Yao, Chuanhao Li, Denis Nekipelov, Hongning Wang and Haifeng Xu. ICML 2023

Rethinking Incentives in Recommender Systems: Are Monotone Rewards Always Beneficial?

Fan Yao, Chuanhao Li, Karthik Abinav Sankararaman, Yiming Liao, Yan Zhu, Qifan Wang, Hongning Wang and Haifeng Xu, working paper

And many references therein!

Thank You
Questions?

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