Supplemental Figures

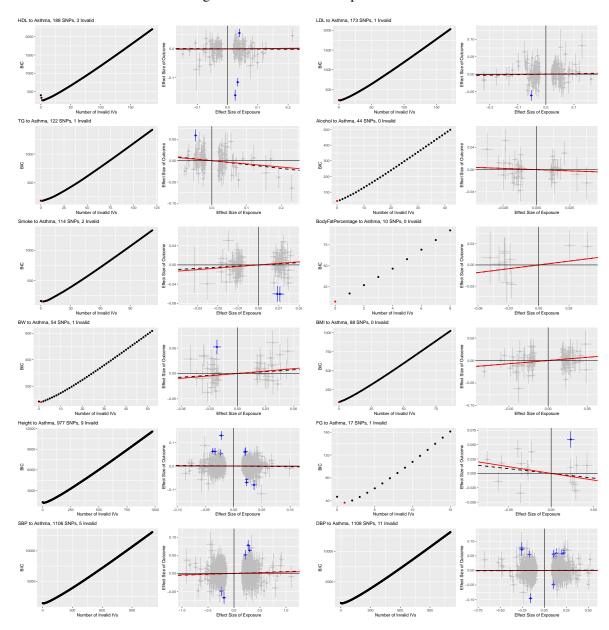


Figure S1: BIC and scatter plot: Asthma

Figure S2: BIC and scatter plot: CAD

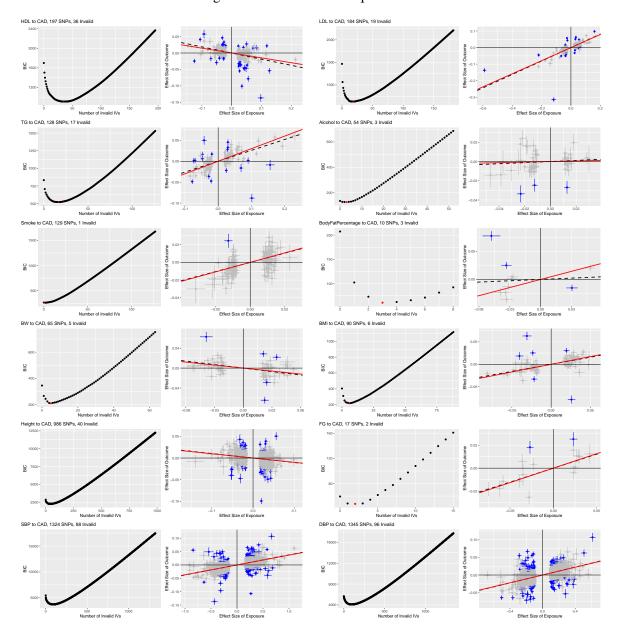


Figure S3: BIC and scatter plot: Stroke

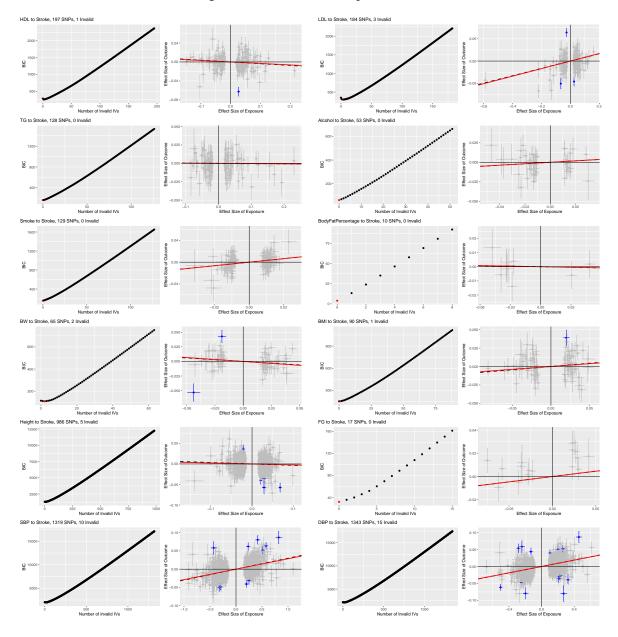


Figure S4: BIC and scatter plot: T2D

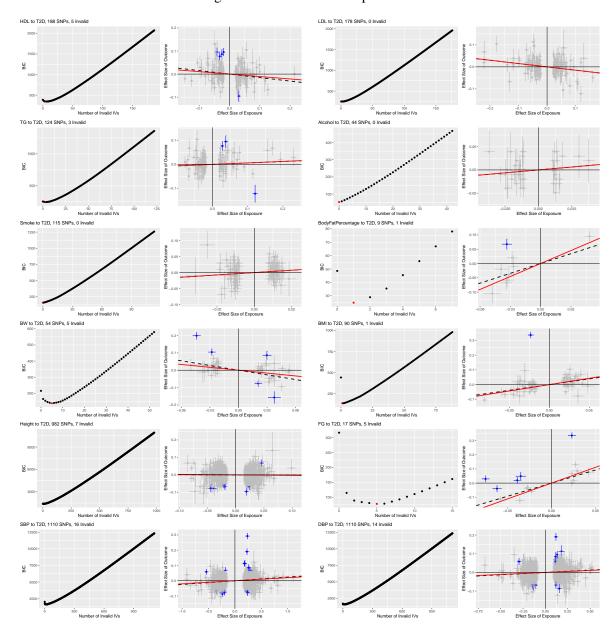


Figure S5: 53 trait pairs in secondary real data analysis: Q-Q plots for all 14 methods.

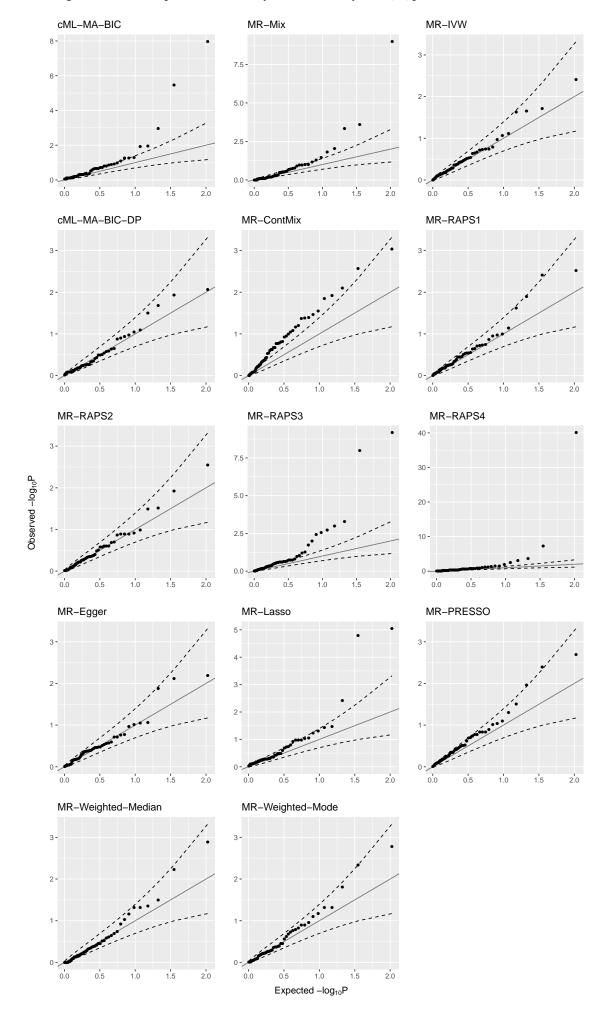


Figure S6: Main simulations: the empirical type-I error rates at the nominal level of 0.05 with sample size N = 50000 and with m = 10 or 100 SNPs, among which 0 to 60% were invalid IVs with the InSIDE assumption either holding or violated. The results were based on 10,000 simulations.

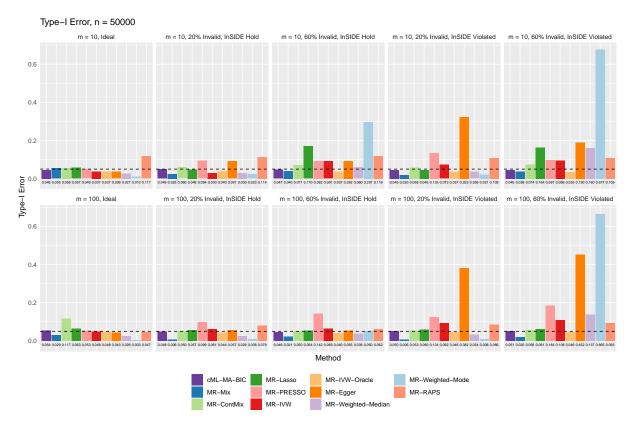


Figure S7: Secondary simulations: empirical type-I error rates (for $\theta = 0$) and power (for $\theta \neq 0$) with sample size N = 50000 or 100000, and with m = 10 or 100 exposure-associated SNPs. The p-value cutoff 0.001 was used for CAUSE to select IVs.

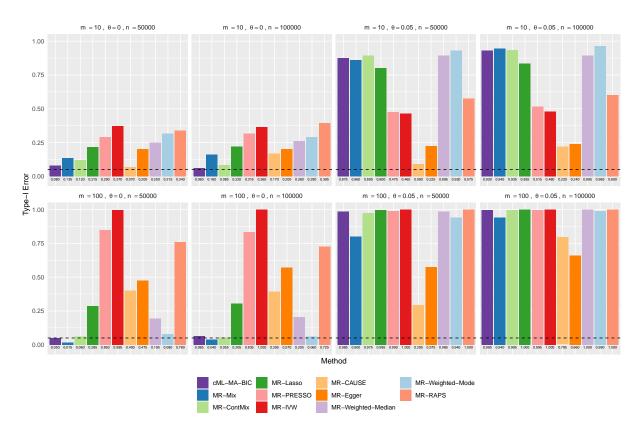
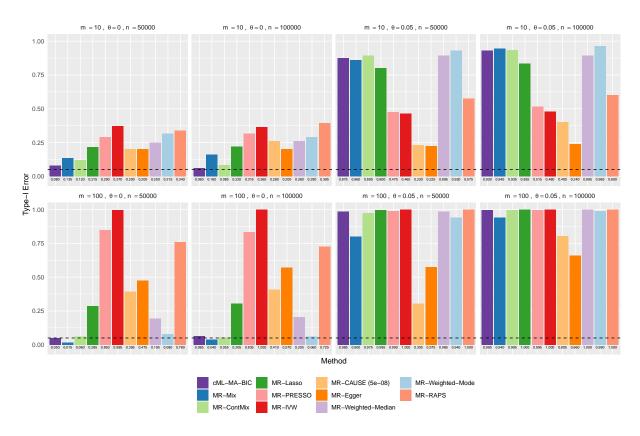


Figure S8: Secondary simulations: empirical type-I error rates (for $\theta=0$) and power (for $\theta\neq0$) with sample size N=50000 or 100000, and with m=10 or 100 exposure-associated SNPs. The p-value cutoff 5×10^{-8} was used for CAUSE to select IVs.



Supplemental Tables

Table S1: Inferring causal effects of 12 risk factors on Asthma, in each cell from top to bottom are p-value, estimated causal effect $\hat{\theta}$ and its standard error $SE(\hat{\theta})$. Cells with p-value less than Bonferroni adjusted significant cutoff 0.001 are marked with red.

| Exposure | HDL(188) | LDL(173) | TG(122) | Alcohol(44) | Smoke(114) | BF(10) | BW(54) | BMI(88) | Height(977) | FG(17) | SBP(1106) | DBP(1108 |
|------------------------|----------------------|-----------------------|-----------------------|-----------------------|----------------------|----------------------|----------------------|----------------------|------------------------|-----------------------|----------------------|-----------------------|
| cML-MA- AIC | 1.2e-02, | 4.1e-01, | 3.9e-01, | 3.0e-01, | 1.3e-01, | 8.3e-01, | 1.1e-02, | 7.4e-03, | 2.9e-01, | 1.8e-02, | 1.7e-01, | 9.7e-02, |
| | -9.2e-02, | 2.4e-02, | -3.8e-02, | -1.8e-01, | 2.4e-01, | 5.0e-02, | 2.6e-01, | 1.9e-01, | 2.2e-02, | -3.0e-01, | 2.9e-03, | -6.8e-03, |
| cML- AIC | 3.6e-02 3.2e-03, | 2.9e-02 5.7e-01, | 4.5e-02 9.5e-01, | 1.8e-01 2.9e-01, | 1.6e-01 2.2e-01, | 2.3e-01 3.8e-01, | 1.0e-01 1.1e-02, | 7.0e-02 1.4e-02, | 2.1e-02 2.6e-01, | 1.3e-01 6.2e-03, | 2.1e-03 1.1e-01, | 4.1e-03 4.8e-02, |
| CML- AIC | -9.4e-02, | 1.6e-02, | 2.5e-03, | -1.7e-01, | 1.8e-01, | 1.2e-01, | 2.3e-01, | 1.5e-01, | 2.3e-02, | -3.2e-01, | 3.2e-03, | -7.0e-03, |
| | 3.2e-02 | 2.8e-02 | 4.0e-02 | 1.6e-01 | 1.5e-01 | 1.4e-01 | 9.1e-02 | 6.2e-02 | 2.1e-02 | 1.2e-01 | 2.0e-03 | 3.6e-03 |
| cML-MA-BIC-max | 7.2e-01, | 9.1e-01, | 2.7e-02, | 5.7e-01, | 2.2e-02, | 3.8e-01, | 4.8e-02, | 1.5e-02, | 5.7e-01, | 1.7e-02, | 3.6e-02, | 9.8e-01, |
| | 9.6e-03, 2.7e-02 | 2.8e-03, 2.5e-02 | -7.5e-02, 3.4e-02 | -8.6e-02, 1.5e-01 | 3.1e-01, 1.3e-01 | 1.2e-01, 1.4e-01 | 1.5e-01, 7.8e-02 | 1.4e-01, 5.9e-02 | -1.1e-02, 1.9e-02 | -2.4e-01, 9.9e-02 | 3.8e-03, 1.8e-03 | -8.9e-05, 3.1e-03 |
| cML-BIC-max | 7.2e-01, | 8.6e-01, | 2.7e-02, | 5.5e-01, | 1.4e-02, | 3.8e-01, | 3.9e-02, | 1.6e-02, | 5.9e-02 | 1.7e-02, | 3.2e-02, | 1.0e+00, |
| CHIL DIC max | 9.7e-03, | 4.5e-03, | -7.4e-02, | -8.9e-02, | 3.3e-01, | 1.2e-01, | 1.6e-01, | 1.4e-01, | -1.0e-02, | -2.3e-01, | 3.9e-03, | 1.4e-05, |
| | 2.7e-02 | 2.5e-02 | 3.4e-02 | 1.5e-01 | 1.3e-01 | 1.4e-01 | 7.7e-02 | 5.9e-02 | 1.9e-02 | 9.8e-02 | 1.8e-03 | 3.1e-03 |
| cML-MA-BIC | 7.3e-01, | 9.2e-01, | 2.7e-02, | 5.9e-01, | 2.1e-02, | 3.8e-01, | 4.8e-02, | 1.5e-02, | 5.8e-01, | 1.6e-02, | 5.0e-02, | 1.0e+00, |
| | 9.4e-03, | 2.4e-03, | -7.5e-02, | -8.2e-02, | 3.1e-01, | 1.2e-01, | 1.5e-01, | 1.4e-01, | -1.1e-02, | -2.4e-01, | 3.6e-03, | 2.0e-06, |
| ML DIC | 2.7e-02 | 2.5e-02 | 3.4e-02 | 1.5e-01 | 1.3e-01 | 1.4e-01 | 7.8e-02 | 5.9e-02 | 1.9e-02 | 1.0e-01 | 1.8e-03 | 3.1e-03 |
| cML-BIC | 7.2e-01, 9.7e-03, | 8.6e-01, 4.5e-03, | 2.7e-02, -7.4e-02, | 5.5e-01, -8.9e-02, | 1.4e-02, 3.3e-01, | 3.8e-01, 1.2e-01, | 3.9e-02, 1.6e-01, | 1.6e-02, 1.4e-01, | 6.0e-01, -1.0e-02, | 1.7e-02, -2.3e-01, | 4.2e-02, 3.7e-03, | 9.8e-01, -7.0e-05, |
| | 2.7e-02 | 2.5e-02 | 3.4e-02 | 1.5e-01 | 1.3e-01 | 1.4e-01 | 7.7e-02 | 5.9e-02 | 1.9e-02 | 9.8e-02 | 1.8e-03 | 3.1e-03 |
| cML-MA-BIC-DP-Max | 7.9e-01, | 8.7e-01, | 6.8e-02, | 6.1e-01, | 4.2e-02, | 4.4e-01, | 1.0e-01, | 2.3e-02, | 6.8e-01, | 7.3e-02, | 9.4e-02, | 9.0e-01, |
| | 8.6e-03, | 4.7e-03, | -7.9e-02, | -8.3e-02, | 3.2e-01, | 1.1e-01, | 1.5e-01, | 1.5e-01, | -9.4e-03, | -2.3e-01, | 3.6e-03, | 4.5e-04, |
| | 3.2e-02 | 2.9e-02 | 4.3e-02 | 1.7e-01 | 1.6e-01 | 1.5e-01 | 9.5e-02 | 6.6e-02 | 2.3e-02 | 1.3e-01 | 2.1e-03 | 3.6e-03 |
| cML-BIC-DP-Max | 8.2e-01, | 8.9e-01, | 7.4e-02, | 6.2e-01, | 3.8e-02, | 4.3e-01, | 7.6e-02, | 1.9e-02, | 6.8e-01, | 5.1e-02, | 8.9e-02, | 8.8e-01, |
| | 7.5e-03, 3.3e-02 | 3.6e-03, 2.7e-02 | -8.1e-02, 4.6e-02 | -8.0e-02, 1.6e-01 | 3.3e-01, 1.6e-01 | 1.1e-01, 1.5e-01 | 1.5e-01, 8.6e-02 | 1.5e-01, 6.5e-02 | -8.9e-03, 2.2e-02 | -2.1e-01, 1.1e-01 | 3.6e-03, 2.1e-03 | 5.3e-04, 3.4e-03 |
| cML-MA-BIC-DP | 8.0e-01, | 8.8e-01, | 7.0e-02, | 6.2e-01, | 4.3e-02, | 4.4e-01, | 1.1e-01, | 2.4e-02, | 6.9e-01, | 7.9e-02, | 1.4e-01, | 9.2e-01, |
| und unit bio bi | 8.4e-03, | 4.5e-03, | -7.9e-02, | -8.5e-02, | 3.2e-01, | 1.1e-01, | 1.5e-01, | 1.5e-01, | -9.2e-03, | -2.4e-01, | 3.3e-03, | 3.8e-04, |
| | 3.3e-02 | 2.9e-02 | 4.4e-02 | 1.7e-01 | 1.6e-01 | 1.5e-01 | 9.5e-02 | 6.7e-02 | 2.3e-02 | 1.4e-01 | 2.3e-03 | 3.9e-03 |
| cML-BIC-DP | 8.2e-01, | 8.9e-01, | 7.4e-02, | 6.0e-01, | 3.8e-02, | 4.3e-01, | 7.6e-02, | 1.9e-02, | 6.8e-01, | 8.7e-02, | 1.5e-01, | 9.1e-01, |
| | 7.5e-03, | 3.6e-03, | -8.1e-02, | -8.9e-02, | 3.3e-01, | 1.1e-01, | 1.5e-01, | 1.5e-01, | -8.9e-03, | -2.5e-01, | 3.3e-03, | 4.5e-04, |
| cML-MA-AIC-Profile | 3.3e-02 1.2e-02, | 2.7e-02 4.1e-01, | 4.6e-02 4.0e-01, | 1.7e-01 3.1e-01, | 1.6e-01 1.4e-01, | 1.5e-01 8.3e-01, | 8.6e-02 1.3e-02, | 6.5e-02 8.2e-03, | 2.2e-02 3.0e-01, | 1.5e-01 1.9e-02, | 2.3e-03 1.8e-01, | 4.0e-03 1.0e-01, |
| CIVIL-IVIA-AIC-FIOINE | -9.2e-02, | 2.4e-02, | -3.8e-02, | -1.8e-01, | 2.4e-01, | 5.0e-02, | 2.6e-01, | 1.9e-01, | 2.3e-02, | -3.0e-01, | 2.9e-03, | -6.8e-03, |
| | 3.7e-02 | 3.0e-02 | 4.5e-02 | 1.8e-01 | 1.6e-01 | 2.4e-01 | 1.0e-01 | 7.0e-02 | 2.2e-02 | 1.3e-01 | 2.2e-03 | 4.2e-03 |
| cML-AIC-Profile | 3.5e-03, | 5.7e-01, | 9.5e-01, | 3.0e-01, | 2.4e-01, | 3.8e-01, | 1.3e-02, | 1.5e-02, | 2.7e-01, | 6.8e-03, | 1.2e-01, | 5.2e-02, |
| | -9.4e-02, | 1.6e-02, | 2.5e-03, | -1.7e-01, | 1.8e-01, | 1.2e-01, | 2.3e-01, | 1.5e-01, | 2.3e-02, | -3.2e-01, | 3.2e-03, | -7.0e-03, |
| | 3.2e-02 | 2.8e-02 | 4.1e-02 | 1.6e-01 | 1.5e-01 | 1.4e-01 | 9.3e-02 | 6.3e-02 | 2.1e-02 | 1.2e-01 | 2.1e-03 | 3.6e-03 |
| cML-MA-BIC-max-Profile | 7.2e-01, 9.6e-03, | 9.1e-01, 2.8e-03, | 2.7e-02, | 5.7e-01, | 2.4e-02, 3.1e-01, | 3.8e-01, 1.2e-01, | 4.8e-02, 1.5e-01, | 1.6e-02, | 5.7e-01, | 1.6e-02, -2.4e-01, | 3.7e-02, | 9.8e-01, -8.9e-05, |
| | 2.7e-02 | 2.5e-03, 2.5e-02 | -7.5e-02, 3.4e-02 | -8.6e-02, 1.5e-01 | 1.4e-01 | 1.2e-01, 1.4e-01 | 7.8e-02 | 1.4e-01, 6.0e-02 | -1.1e-02, 1.9e-02 | 9.9e-02 | 3.8e-03, 1.8e-03 | 3.1e-03 |
| cML-BIC-max-Profile | 7.2e-01, | 8.6e-01, | 2.7e-02, | 5.6e-01, | 1.5e-02, | 3.8e-01, | 4.0e-02, | 1.7e-02, | 5.9e-01, | 1.6e-02, | 3.3e-02, | 1.0e+00, |
| | 9.7e-03, | 4.5e-03, | -7.4e-02, | -8.9e-02, | 3.3e-01, | 1.2e-01, | 1.6e-01, | 1.4e-01, | -1.0e-02, | -2.3e-01, | 3.9e-03, | 1.4e-05, |
| | 2.7e-02 | 2.5e-02 | 3.4e-02 | 1.5e-01 | 1.3e-01 | 1.4e-01 | 7.7e-02 | 6.0e-02 | 1.9e-02 | 9.8e-02 | 1.8e-03 | 3.1e-03 |
| cML-MA-BIC-Profile | 7.3e-01, | 9.2e-01, | 2.7e-02, | 5.9e-01, | 2.3e-02, | 3.8e-01, | 4.8e-02, | 1.6e-02, | 5.8e-01, | 1.6e-02, | 5.2e-02, | 1.0e+00, |
| | 9.4e-03, | 2.4e-03, | -7.5e-02, | -8.2e-02, | 3.1e-01, | 1.2e-01, | 1.5e-01, | 1.4e-01, | -1.1e-02, | -2.4e-01, | 3.6e-03, | 2.0e-06, |
| cML-BIC-Profile | 2.7e-02 7.2e-01, | 2.5e-02 8.6e-01, | 3.4e-02 2.7e-02, | 1.5e-01 5.6e-01, | 1.4e-01 1.5e-02, | 1.4e-01 3.8e-01, | 7.8e-02 4.0e-02, | 6.0e-02 1.7e-02, | 1.9e-02 6.0e-01, | 1.0e-01 1.6e-02, | 1.8e-03 4.3e-02, | 3.1e-03 9.8e-01, |
| CML-BIC-FIGHE | 9.7e-03, | 4.5e-03, | -7.4e-02, | -8.9e-02, | 3.3e-01, | 1.2e-01, | 1.6e-01, | 1.7e-02, 1.4e-01, | -1.0e-02, | -2.3e-01, | 3.7e-03, | -7.0e-05, |
| | 2.7e-02 | 2.5e-02 | 3.4e-02 | 1.5e-01 | 1.3e-01 | 1.4e-01 | 7.7e-02 | 6.0e-02 | 1.9e-02 | 9.8e-02 | 1.8e-03 | 3.1e-03 |
| CAUSE | 1.0e+00, | 8.7e-01, | 1.7e-01, | 8.1e-01, | 5.0e-01, | 5.7e-01, | 7.3e-01, | 1.6e-01, | 1.0e+00, | 3.5e-01, | 7.6e-01, | 5.9e-01, |
| | 9.5e-03, | -1.8e-02, | -9.2e-02, | -7.1e-02, | 1.3e-01, | 9.6e-02, | 5.7e-02, | 1.3e-01, | -2.7e-03, | -2.0e-01, | 2.5e-03, | 3.9e-03, |
| 100 10° | NA | NA 47. 01 | NA 1.0 | NA O.5. O.1 | NA | NA | NA | NA | NA 10 100 | NA | NA NA | NA 10 00 |
| MR-Mix | 6.4e-01, 1.0e-02, | 4.7e-01, -1.0e-02, | 1.0e+00, 0.0e+00, | 9.5e-01, -3.0e-02, | 2.3e-01, 1.5e-01, | 3.4e-01, 4.0e-02, | 3.8e-01, 7.0e-02, | 1.4e-01, 4.5e-02, | 1.0e+00, 0.0e+00, | 7.3e-02, -5.0e-02, | 1.0e+00, 0.0e+00, | 1.0e+00, 0.0e+00, |
| | 2.1e-02 | 1.4e-02 | 4.9e-02 | 4.6e-01 | 1.3e-01, 1.3e-01 | 4.0e-02, 4.2e-02 | 8.0e-02 | 3.0e-02 | 1.2e-02 | 2.8e-02 | 2.0e-02 | 2.1e-02 |
| MR-ContMix | 3.2e-01, | 7.7e-01, | 1.5e-01, | 3.2e-01, | 1.6e-01, | 2.9e-01, | 2.4e-02, | 1.3e-02, | 4.6e-01, | 8.8e-02, | 2.0e-02 2.0e-01, | 1.6e-01, |
| | -3.9e-02, | -7.8e-03, | -7.4e-02, | -2.5e-01, | 5.0e-01, | 2.5e-01, | 4.0e-01, | 1.9e-01, | 2.1e-02, | -2.0e-01, | 6.9e-03, | -1.2e-02, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 8.7e-01, | 9.3e-01, | 6.4e-03, | 5.6e-01, | 1.0e-02, | 3.8e-01, | 6.0e-03, | 1.6e-02, | 7.1e-01, | 7.1e-02, | 8.1e-02, | 8.0e-01, |
| | -4.6e-03, | -2.2e-03, | -9.5e-02, | -8.7e-02, | 3.4e-01, | 1.2e-01, | 2.2e-01, | 1.4e-01, 5.9e-02 | -7.0e-03, | -2.3e-01, | 3.2e-03, | 8.2e-04, |
| MR-PRESSO | 2.8e-02 7.4e-01, | 2.5e-02 8.7e-01, | 3.5e-02 6.2e-02, | 1.5e-01 5.6e-01, | 1.3e-01 2.5e-02, | 1.3e-01 3.4e-01, | 8.2e-02 7.6e-02, | 5.9e-02 1.5e-02, | 1.9e-02 7.0e-01, | 1.3e-01 7.1e-02, | 1.8e-03 5.2e-02, | 3.2e-03 8.6e-01, |
| MIN I KLOOU | 9.6e-03, | 4.5e-03, | -7.4e-02, | -8.7e-02, | 2.3e-02, 3.2e-01, | 1.2e-01, | 1.5e-02, 1.5e-01, | 1.5e-02, 1.4e-01, | -7.9e-01, | -2.3e-01, | 3.2e-02, 3.8e-03, | 6.3e-04, |
| | 2.9e-02 | 2.8e-02 | 3.9e-02 | 1.5e-01 | 1.4e-01 | 1.2e-01 | 8.7e-02 | 5.8e-02 | 2.0e-02 | 1.3e-01 | 2.0e-03 | 3.5e-03 |
| MR-IVW | 8.6e-01, | 6.2e-01, | 2.9e-02, | 5.6e-01, | 1.4e-01, | 3.8e-01, | 2.2e-01, | 1.6e-02, | 2.0e-01, | 3.3e-01, | 1.6e-02, | 6.5e-01, |
| | -6.6e-03, | 1.4e-02, | -9.0e-02, | -8.7e-02, | 2.3e-01, | 1.2e-01, | 1.2e-01, | 1.4e-01, | -2.8e-02, | -1.6e-01, | 4.9e-03, | 1.6e-03, |
| MD E | 3.9e-02 | 2.9e-02 | 4.1e-02 | 1.5e-01 | 1.5e-01 | 1.3e-01 | 9.5e-02 | 5.9e-02 | 2.2e-02 | 1.6e-01 | 2.0e-03 | 3.6e-03 |
| MR-Egger | 9.9e-01, 7.5e-04, | 8.2e-01, -1.2e-02, | 5.1e-01, -4.8e-02, | 1.4e-01, -6.9e-01, | 4.9e-01, 5.1e-01, | 9.3e-01, 6.1e-02, | 8.5e-01, 6.7e-02, | 6.4e-02, 2.8e-01, | 5.6e-01, -3.9e-02, | 3.9e-01, -3.6e-01, | 8.5e-01, 1.2e-03, | 8.6e-02, -1.8e-02, |
| | 7.3e-04, 7.3e-02 | -1.2e-02, 5.3e-02 | -4.8e-02, 7.3e-02 | -6.9e-01, 4.7e-01 | 7.4e-01 | 6.7e-02, | 3.5e-01 | 2.8e-01, 1.5e-01 | -3.9e-02, 6.7e-02 | -3.6e-01, 4.1e-01 | 6.0e-03 | -1.8e-02, 1.1e-02 |
| MR-Weighted-Median | 5.1e-01, | 2.6e-01, | 9.4e-01, | 5.9e-01, | 1.4e-01, | 9.0e-01, | 1.5e-01, | 1.0e-02, | 4.2e-01, | 2.0e-02, | 8.6e-01, | 1.8e-01, |
| | 3.1e-02, | 4.7e-02, | -4.1e-03, | -1.2e-01, | 3.0e-01, | 2.3e-02, | 1.7e-01, | 2.5e-01, | -2.4e-02, | -3.2e-01, | 5.3e-04, | -6.9e-03, |
| | 4.7e-02 | 4.1e-02 | 5.7e-02 | 2.2e-01 | 2.0e-01 | 1.8e-01 | 1.2e-01 | 9.5e-02 | 3.0e-02 | 1.4e-01 | 2.9e-03 | 5.2e-03 |
| MR-Weighted-Mode | 9.3e-01, | 6.2e-01, | 3.5e-01, | 4.3e-01, | 9.4e-01, | 5.3e-01, | 4.5e-01, | 4.9e-02, | 1.3e-01, | 8.8e-02, | 3.4e-01, | 1.5e-01, |
| | 5.1e-03, | 2.3e-02, 4.6e-02 | -5.9e-02, | -2.8e-01, | 3.7e-02, | -1.7e-01, | 2.1e-01, | 2.4e-01, | -1.5e-01, | -2.7e-01, | -1.1e-02, | -2.9e-02, |
| MR-RAPS1 | 6.2e-02 9.9e-01, | 4.6e-02 5.9e-01, | 6.4e-02 2.0e-02, | 3.5e-01 5.6e-01, | 4.9e-01 1.6e-01, | 2.8e-01 3.8e-01, | 2.8e-01 1.8e-01, | 1.2e-01 1.6e-02, | 9.9e-02 2.4e-01, | 1.6e-01 3.5e-01, | 1.2e-02 2.2e-02, | 2.0e-02 7.1e-01, |
| WIN-NAF 31 | -4.9e-01, | 1.5e-02, | -9.4e-02, | -8.9e-02, | 2.3e-01, | 1.2e-01, | 1.3e-01, | 1.6e-02, 1.4e-01, | -2.4e-01, -2.6e-02, | -1.5e-01, | 4.7e-03, | 1.4e-03, |
| | 3.8e-02 | 2.9e-02 | 4.1e-02 | 1.5e-01 | 1.6e-01 | 1.4e-01 | 9.6e-02 | 6.0e-02 | 2.2e-02 | 1.6e-01 | 2.1e-03 | 3.7e-03 |
| MR-RAPS2 | 7.7e-01, | 8.0e-01, | 4.3e-02, | 6.2e-01, | 3.0e-02, | 4.1e-01, | 1.0e-01, | 1.4e-02, | 7.5e-01, | 2.3e-01, | 1.0e-01, | 9.8e-01, |
| | 9.3e-03, | 7.3e-03, | -8.4e-02, | -7.7e-02, | 3.2e-01, | 1.2e-01, | 1.5e-01, | 1.5e-01, | -6.8e-03, | -1.9e-01, | 3.4e-03, | 8.7e-05, |
| | 3.1e-02 | 2.9e-02 | 4.1e-02 | 1.5e-01 | 1.5e-01 | 1.4e-01 | 9.5e-02 | 6.2e-02 | 2.1e-02 | 1.6e-01 | 2.1e-03 | 3.6e-03 |
| MR-RAPS3 | 8.0e-01, | 5.7e-01, | 7.0e-03, | 5.6e-01, | 7.7e-02, | 3.8e-01, | 1.2e-01, | 1.6e-02, | 1.3e-01, | 9.5e-02, | 6.6e-03, | 5.9e-01, |
| | -6.7e-03, | 1.4e-02, | -9.1e-02, | -8.9e-02, | 2.4e-01, | 1.2e-01, | 1.2e-01, | 1.4e-01, | -2.9e-02, | -1.6e-01, | 5.0e-03, | 1.7e-03, |
| | 2.7e-02 8.7e-01, | 2.5e-02 8.7e-01, | 3.4e-02 3.7e-02, | 1.5e-01 6.2e-01, | 1.4e-01 1.6e-02, | 1.4e-01 4.0e-01, | 7.8e-02 3.2e-02, | 6.0e-02 1.4e-02, | 1.9e-02 7.3e-01, | 9.9e-02 1.1e-02, | 1.8e-03 8.6e-02, | 3.1e-03 1.0e+00, |
| MD_DADCA | | | 1. / C-U/ | 1 U. 4E-UI. | | 4.UC-U1. | 1 J.4C-U4. | 1.40-02, | 1.30-01, | 1.10-02, | 0.00-02, | 1.00+00, |
| MR-RAPS4 | 4.5e-03, | 4.2e-03, | -7.2e-02, | -7.7e-02, | 3.3e-01, | 1.2e-01, | 1.7e-01, | 1.5e-01, | -6.8e-03, | -2.5e-01, | 3.2e-03, | 2.0e-05, |

Table S2: Inferring causal effects of 12 risk factors on CAD, in each cell from top to bottom are p-value, estimated causal effect $\hat{\theta}$ and its standard error $SE(\hat{\theta})$. Cells with p-value less than Bonferroni adjusted significant cutoff 0.001 are marked with red.

| <u> </u> | | | | | | | | | | | | |
|--|---|---|---|---|--|--|---|--|--|---|---|---|
| Exposure | HDL(197) | LDL(184) | TG(128) | Alcohol(54) | Smoke(129) | BF(10) | BW(65) | BMI(90) | Height(986) | FG(17) | SBP(1324) | DBP(1345) |
| cML-MA- AIC | 3.4e-18, | 2.6e-132, | 6.0e-02, | 4.7e-04, | 6.1e-26, | 5.1e-07, | 4.6e-01, | 3.9e-28, | 4.7e-24, | 1.0e-07, | 3.9e-92, | 1.3e-153, |
| | -1.4e-01, | 4.4e-01, | 1.2e-01, | 2.4e-01, | 7.5e-01, | 4.8e-01, | -3.1e-02, | 3.7e-01, | -9.8e-02, | 2.6e-01, | 3.0e-02, | 5.2e-02, |
| | 1.6e-02 | 1.8e-02 | 6.4e-02 | 6.9e-02 | 7.1e-02 | 9.6e-02 | 4.2e-02 | 3.3e-02 | 9.6e-03 | 4.8e-02 | 1.5e-03 | 2.0e-03 |
| cML- AIC | 3.0e-23, | 1.1e-178, | 1.8e-14, | 8.0e-05, | 1.5e-33, | 7.2e-10, | 3.1e-01, | 8.2e-40, | 3.4e-25, | 3.6e-09, | 2.4e-247, | 1.7e-229, |
| | -1.4e-01, 1.4e-02 | 4.4e-01, 1.5e-02 | 1.6e-01, 2.1e-02 | 2.6e-01, 6.6e-02 | 7.4e-01, 6.2e-02 | 5.1e-01, 8.2e-02 | -3.8e-02, 3.8e-02 | 3.8e-01, 2.9e-02 | -9.6e-02, 9.3e-03 | 2.6e-01, 4.3e-02 | 3.0e-02, 8.9e-04 | 5.1e-02, 1.6e-03 |
| cML-MA-BIC-max | 3.3e-30, | 1.3e-02 1.3e-209, | 3.9e-55, | 3.4e-01, | 1.3e-23, | 2.4e-09, | 3.1e-11, | 9.8e-47, | 2.6e-36, | 3.1e-10, | 0.0e+00, | 0.0e+00, |
| CIVIL-IVIA-BIC-IIIAX | -1.4e-01, | 4.0e-01, | 2.9e-01, | 6.0e-02, | 5.4e-01, | 4.7e-01, | -2.0e-01, | 3.4e-01, | -1.0e-01, | 2.7e-01, | 3.7e-02, | 5.6e-02, |
| | 1.2e-02 | 1.3e-02 | 1.8e-02 | 6.3e-02 | 5.4e-02 | 7.8e-02 | 3.1e-02 | 2.4e-02 | 7.9e-03 | 4.2e-02 | 7.5e-04 | 1.4e-03 |
| cML-BIC-max | 2.9e-33, | 2.5e-306, | 1.6e-88, | 6.1e-01, | 1.9e-24, | 4.3e-12, | 1.6e-11, | 2.4e-48, | 2.7e-38, | 4.2e-12, | 0.0e+00, | 0.0e+00, |
| | -1.3e-01, | 4.0e-01, | 2.8e-01, | 2.9e-02, | 5.4e-01, | 4.8e-01, | -2.0e-01, | 3.4e-01, | -1.0e-01, | 2.8e-01, | 3.7e-02, | 5.5e-02, |
| NE MA DIC | 1.1e-02 | 1.1e-02 | 1.4e-02 | 5.8e-02 | 5.3e-02 | 7.0e-02 | 3.0e-02 | 2.4e-02 | 7.7e-03 | 4.0e-02 | 7.3e-04 | 1.2e-03 |
| cML-MA-BIC | 4.7e-27, -1.5e-01, | 1.4e-206, 4.1e-01, | 3.3e-70, 3.0e-01, | 3.6e-01, 5.8e-02, | 1.1e-23, 5.5e-01, | 1.1e-07, 4.6e-01, | 1.1e-10, -2.0e-01, | 1.6e-46, 3.4e-01, | 4.6e-36, -9.8e-02, | 1.4e-08, 2.5e-01, | 0.0e+00, 3.7e-02, | 0.0e+00, 5.6e-02, |
| | 1.4e-02 | 1.3e-02 | 1.7e-02 | 6.4e-02 | 5.4e-02 | 8.7e-02 | 3.1e-02 | 2.4e-02 | 7.8e-03 | 4.4e-02 | 7.5e-04 | 1.3e-03 |
| cML-BIC | 9.7e-40, | 2.9e-293, | 9.9e-96, | 6.1e-01, | 1.9e-24, | 4.3e-12, | 1.6e-11, | 2.4e-48, | 6.6e-37, | 3.2e-10, | 0.0e+00. | 0.0e+00, |
| | -1.5e-01, | 4.0e-01, | 3.0e-01, | 2.9e-02, | 5.4e-01, | 4.8e-01, | -2.0e-01, | 3.4e-01, | -9.9e-02, | 2.5e-01, | 3.7e-02, | 5.5e-02, |
| | 1.1e-02 | 1.1e-02 | 1.4e-02 | 5.8e-02 | 5.3e-02 | 7.0e-02 | 3.0e-02 | 2.4e-02 | 7.8e-03 | 4.0e-02 | 7.3e-04 | 1.3e-03 |
| cML-MA-BIC-DP-Max | 9.1e-08, | 9.9e-33, | 2.9e-10, | 1.9e-01, | 8.4e-14, | 3.7e-03, | 4.3e-05, | 2.7e-28, | 7.9e-18, | 5.3e-06, | 9.1e-134, | 2.6e-100, |
| | -1.6e-01, | 4.0e-01, | 2.6e-01, | 1.1e-01, | 5.5e-01, | 4.5e-01, | -1.9e-01, | 3.4e-01, | -9.7e-02, | 2.5e-01, | 3.6e-02, | 5.5e-02, |
| cML-BIC-DP-Max | 2.9e-02 8.4e-08, | 3.4e-02 4.1e-28, | 4.2e-02 2.6e-10, | 8.8e-02 1.9e-01, | 7.4e-02 4.0e-14, | 1.6e-01 4.7e-03, | 4.7e-02 3.3e-05, | 3.1e-02 8.1e-29, | 1.1e-02 8.1e-18, | 5.6e-02 5.6e-06, | 1.4e-03 2.4e-131, | 2.6e-03 1.8e-101, |
| CML-BIC-DF-Max | -1.6e-01, | 4.1e-28, 4.0e-01, | 2.6e-10, 2.6e-01, | 1.9e-01, 1.2e-01, | 5.6e-01, | 4.7e-03, 4.7e-01, | -2.0e-01, | 3.4e-01, | -9.8e-02, | 2.5e-00, | 3.6e-02, | 5.5e-02, |
| | 2.9e-02 | 3.7e-02 | 4.2e-02 | 8.8e-02 | 7.4e-02 | 1.6e-01 | 4.7e-02 | 3.1e-02 | 1.1e-02 | 5.5e-02 | 1.5e-03 | 2.6e-03 |
| cML-MA-BIC-DP | 5.7e-07, | 3.3e-28, | 7.2e-10, | 1.8e-01, | 1.1e-13, | 1.1e-02, | 8.3e-05, | 1.0e-27, | 1.0e-17, | 5.7e-06, | 4.4e-133, | 1.4e-100, |
| | -1.6e-01, | 4.0e-01, | 2.6e-01, | 1.2e-01, | 5.5e-01, | 4.5e-01, | -1.9e-01, | 3.4e-01, | -9.7e-02, | 2.5e-01, | 3.6e-02, | 5.5e-02, |
| | 3.2e-02 | 3.7e-02 | 4.3e-02 | 8.8e-02 | 7.4e-02 | 1.8e-01 | 4.8e-02 | 3.2e-02 | 1.1e-02 | 5.5e-02 | 1.5e-03 | 2.6e-03 |
| cML-BIC-DP | 8.4e-08, | 4.1e-28, | 2.6e-10, | 1.9e-01, | 2.8e-13, | 4.7e-03, | 8.4e-05, | 8.1e-29, | 1.8e-17, | 5.6e-06, | 2.4e-131, | 1.8e-101, |
| | -1.6e-01, 2.9e-02 | 4.0e-01, 3.7e-02 | 2.6e-01, 4.2e-02 | 1.2e-01, 8.8e-02 | 5.4e-01, 7.4e-02 | 4.7e-01, 1.6e-01 | -1.9e-01, 4.8e-02 | 3.4e-01, 3.1e-02 | -9.8e-02, 1.1e-02 | 2.5e-01, 5.5e-02 | 3.6e-02, 1.5e-03 | 5.5e-02, 2.6e-03 |
| cML-MA-AIC-Profile | 3.6e-15, | 6.7e-02 | 6.1e-02, | 6.1e-04, | 7.4e-02 7.5e-25, | 7.2e-07, | 4.8e-02 4.4e-01, | 1.7e-27, | 3.0e-23, | 1.3e-07, | 1.3e-03 1.2e-168, | 1.9e-168, |
| CIVIL-IVIA-AIC-FIUIIC | -1.5e-01, | 4.2e-01, | 1.2e-01, | 2.4e-01, | 7.5e-25, 7.5e-01, | 4.8e-01, | -3.3e-02, | 3.7e-27, 3.7e-01, | -9.8e-02, | 2.6e-01, | 3.1e-02, | 5.2e-02, |
| | 1.9e-02 | 1.9e-02 | 6.4e-02 | 7.0e-02 | 7.3e-02 | 9.8e-02 | 4.2e-02 | 3.4e-02 | 9.8e-03 | 4.8e-02 | 1.1e-03 | 1.9e-03 |
| cML-AIC-Profile | 6.5e-26, | 7.9e-161, | 3.4e-14, | 1.1e-04, | 1.2e-31, | 1.3e-09, | 3.2e-01, | 1.5e-38, | 1.8e-24, | 5.4e-09, | 8.2e-251, | 1.6e-224, |
| | -1.6e-01, | 4.2e-01, | 1.6e-01, | 2.6e-01, | 7.4e-01, | 5.1e-01, | -3.8e-02, | 3.8e-01, | -9.6e-02, | 2.6e-01, | 3.1e-02, | 5.2e-02, |
| | 1.5e-02 | 1.6e-02 | 2.1e-02 | 6.8e-02 | 6.3e-02 | 8.4e-02 | 3.9e-02 | 2.9e-02 | 9.4e-03 | 4.4e-02 | 9.2e-04 | 1.6e-03 |
| cML-MA-BIC-max-Profile | 1.0e-30, | 3.9e-274, | 4.1e-61, | 3.4e-01, | 3.1e-24, | 8.3e-10, | 1.2e-11, | 4.5e-47, | 4.2e-37, | 2.3e-10, | 0.0e+00, | 0.0e+00, |
| | -1.4e-01, 1.2e-02 | 4.0e-01, 1.1e-02 | 2.9e-01, 1.7e-02 | 6.0e-02, 6.3e-02 | 5.4e-01, 5.3e-02 | 4.7e-01, 7.6e-02 | -2.0e-01, 3.0e-02 | 3.4e-01, 2.4e-02 | -1.0e-01, 7.8e-03 | 2.7e-01, 4.2e-02 | 3.7e-02, 7.3e-04 | 5.6e-02, 1.3e-03 |
| cML-BIC-max-Profile | 2.6e-34, | 0.0e+00, | 6.6e-91, | 6.1e-01, | 3.8e-25, | 6.7e-13, | 5.9e-12, | 1.1e-48, | 7.2e-39, | 2.5e-12, | 0.0e+00, | 0.0e+00, |
| CIVIE BIC Max Frome | -1.3e-01, | 4.0e-01, | 2.8e-01, | 2.9e-02, | 5.4e-01, | 4.8e-01, | -2.0e-01, | 3.4e-01, | -1.0e-01, | 2.8e-01, | 3.7e-02, | 5.6e-02, |
| | 1.1e-02 | 1.1e-02 | 1.4e-02 | 5.8e-02 | 5.2e-02 | 6.7e-02 | 2.9e-02 | 2.3e-02 | 7.7e-03 | 3.9e-02 | 7.2e-04 | 1.2e-03 |
| cML-MA-BIC-Profile | 3.0e-25, | 2.2e-220, | 2.0e-76, | 3.6e-01, | 2.9e-24, | 6.0e-08, | 4.6e-11, | 7.6e-47, | 1.0e-36, | 1.3e-08, | 0.0e+00, | 0.0e+00, |
| | -1.5e-01, | 4.0e-01, | 2.9e-01, | 5.8e-02, | 5.5e-01, | 4.6e-01, | -2.0e-01, | 3.4e-01, | -9.8e-02, | 2.5e-01, | 3.7e-02, | 5.6e-02, |
| M. DIC D. CI | 1.4e-02 | 1.3e-02 | 1.6e-02 | 6.4e-02 | 5.4e-02 | 8.5e-02 | 3.0e-02 | 2.4e-02 | 7.8e-03 | 4.4e-02 | 7.3e-04 | 1.3e-03 |
| cML-BIC-Profile | 8.5e-41, -1.5e-01, | 8.5e-298, 3.9e-01, | 6.4e-96, 2.9e-01, | 6.1e-01, 2.9e-02, | 3.8e-25, 5.4e-01, | 6.7e-13, 4.8e-01, | 5.9e-12, -2.0e-01, | 1.1e-48, 3.4e-01, | 2.3e-37, -9.9e-02, | 2.8e-10, 2.5e-01, | 0.0e+00, 3.7e-02, | 0.0e+00, 5.6e-02, |
| | 1.1e-02 | 1.1e-02 | 1.4e-02 | 5.8e-02 | 5.4e-01, 5.2e-02 | 6.7e-02 | 2.9e-02 | 2.3e-02 | 7.7e-03 | 4.0e-02 | 7.2e-04 | 1.2e-03 |
| CAUSE | 4.4e-04, | 6.3e-12, | 8.5e-02, | 8.2e-01, | 9.2e-08, | 3.3e-01, | 1.4e-03, | 1.2e-04, | 1.8e-04, | 2.5e-01, | 6.6e-31, | 1.3e-26, |
| | -2.0e-01, | 3.6e-01, | 2.8e-01, | 3.7e-02, | 4.8e-01, | 1.3e-01, | -1.4e-01, | 2.5e-01, | -6.5e-02, | 1.1e-01, | 2.5e-02, | 3.7e-02, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Mix | 8.4e-04, | 2.4e-11, | 6.5e-30, | 1.1e-01, | 3.4e-06, | 7.3e-05, | 3.0e-01, | 8.0e-16, | 2.3e-06, | 1.5e-05, | 1.2e-59, | 2.8e-21, |
| | -5.0e-02, | 1.8e-01, | 2.1e-01, | 9.0e-02, 5.7e-02 | 3.5e-01, | 2.0e-01, | -4.0e-02, | 1.6e-01, | -3.0e-02, | 5.0e-02, | 2.0e-01, | 1.9e-01, |
| MR-ContMix | 1.5e-02 5.7e-08, | 2.7e-02 4.5e-43, | 1.8e-02 3.9e-06, | 5.4e-04, | 7.5e-02 9.8e-13, | 5.0e-02 3.8e-03, | 3.8e-02 1.3e-01, | 2.0e-02 1.8e-17, | 6.3e-03 2.4e-11, | 1.2e-02 1.7e-05, | 1.2e-02 7.5e-116, | 2.0e-02 1.6e-85, |
| WIK-COIIIWIX | -1.2e-01, | 4.8e-01, | 4.3e-00, | 2.6e-01, | 5.0e-01, | 5.0e-01, | -1.3e-01, | 3.4e-01, | -1.0e-01, | 2.7e-01, | 3.9e-02, | 6.4e-02, |
| | NA NA | NA | NA | NA NA | NA | NA | NA NA | NA | NA | NA | NA | NA |
| MR-Lasso | 2.3e-25, | 1.4e-178, | 9.8e-47, | 1.1e-01, | 1.1e-27, | 3.0e-03, | 7.3e-06, | 1.5e-40, | 1.0e-26, | 6.3e-07, | 0.0e+00, | 7.7e-275, |
| | -1.5e-01, | 4.0e-01, | 2.7e-01, | 1.1e-01, | 6.0e-01, | 3.7e-01, | -1.6e-01, | 3.2e-01, | -9.0e-02, | 2.2e-01, | 3.2e-02, | 5.1e-02, |
| 140 00000 | 1.4e-02 | 1.4e-02 | 1.8e-02 | 6.8e-02 | 5.5e-02 | 1.2e-01 | 3.5e-02 | 2.4e-02 | 8.4e-03 | 4.5e-02 | 8.0e-04 | 1.4e-03 |
| MR-PRESSO | 5.2e-16, | 3.6e-112, | 1.7e-25, | 1.1e-01, 1.1e-01, | 1.0e-12, | 7.5e-01, 5.7e-02, | 4.3e-05, | 1.9e-28, | 9.0e-21, | 6.3e-07, | 2.0e-246, 3.5e-02 | 2.3e-177, 5.2e-02 |
| | -1.5e-01, 1.9e-02 | 3.8e-01, 1.7e-02 | 2.6e-01, 2.5e-02 | 6.8e-02 | 4.8e-01, 6.8e-02 | 5.7e-02, 1.8e-01 | -1.9e-01, 4.6e-02 | 3.3e-01, 3.0e-02 | -9.8e-02, 1.0e-02 | 2.2e-01, 4.5e-02 | 3.5e-02, 1.0e-03 | 5.2e-02, 1.8e-03 |
| MR-IVW | 6.5e-10, | 4.6e-51, | 3.8e-14, | 5.4e-01, | 2.8e-11, | 8.9e-01, | 1.4e-03, | 7.1e-10, | 9.6e-15, | 1.6e-03, | 2.0e-138, | 2.7e-106, |
| | | | 2.4e-01, | 5.5e-02, | 4.9e-01, | 3.5e-02, | -2.1e-01, | 3.0e-01, | -9.8e-02, | 2.3e-01, | 3.5e-02, | 5.2e-02, |
| | -1.7e-01, | 3.7e-01, | | | | | | | | | | |
| MR-Egger | -1.7e-01, 2.8e-02 | 3.7e-01, 2.5e-02 | 3.2e-02 | 8.9e-02 | 7.3e-02 | 2.5e-01 | 6.5e-02 | 4.8e-02 | 1.3e-02 | 7.4e-02 | 1.4e-03 | 2.4e-03 |
| | 2.8e-02 5.5e-01, | 2.5e-02 5.6e-19, | 3.2e-02 2.3e-03, | 8.9e-02 5.4e-01, | 7.3e-02 1.4e-02, | 9.3e-01, | 6.5e-02 9.4e-01, | 4.8e-02 1.2e-01, | 1.3e-02 1.4e-01, | 2.4e-01, | 7.0e-18, | 5.9e-21, |
| | 2.8e-02 5.5e-01, -3.0e-02, | 2.5e-02 5.6e-19, 3.5e-01, | 3.2e-02 2.3e-03, 1.7e-01, | 8.9e-02 5.4e-01, 1.6e-01, | 7.3e-02 1.4e-02, 8.5e-01, | 9.3e-01, -1.1e-01, | 6.5e-02 9.4e-01, 1.6e-02, | 4.8e-02 1.2e-01, 2.0e-01, | 1.3e-02 1.4e-01, -5.5e-02, | 2.4e-01, 2.2e-01, | 7.0e-18, 3.5e-02, | 5.9e-21, 6.3e-02, |
| MP Waighted Medien | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 | 9.3e-01, -1.1e-01, 1.3e+00 | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 | 2.4e-01, 2.2e-01, 1.9e-01 | 7.0e-18, 3.5e-02, 4.1e-03 | 5.9e-21, 6.3e-02, 6.7e-03 |
| MR-Weighted-Median | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, |
| MR-Weighted-Median | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, 4.1e-01, | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, |
| MR-Weighted-Median MR-Weighted-Mode | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, |
| · | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-03 3.9e-08, 2.9e-02, | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, |
| MR-Weighted-Mode | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, 2.7e-02 | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-02 | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-03 3.9e-08, 2.9e-02, 5.4e-03 | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 |
| · | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, 2.7e-02 3.0e-10, | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 7.9e-51, | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 3.6e-01, | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 6.1e-12, | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-02 1.6e-03, | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 5.9e-07, | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 4.9e-15, | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 7.5e-04, | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-03 3.9e-08, 2.9e-02, 5.4e-03 1.9e-141, | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 4.3e-110, |
| MR-Weighted-Mode | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, 2.7e-02 3.0e-10, -1.8e-01, | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 7.9e-51, 3.8e-01, | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 2.8e-13, 2.2e-01, | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 3.6e-01, 8.0e-02, | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 6.1e-12, 5.2e-01, | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 5.0e-01, 7.9e-02, | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-02 1.6e-03, -2.1e-01, | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 5.9e-07, 2.6e-01, | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 4.9e-15, -1.0e-01, | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 7.5e-04, 2.4e-01, | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-03 3.9e-08, 2.9e-02, 5.4e-03 1.9e-141, 3.5e-02, | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 4.3e-110, 5.3e-02, |
| MR-Weighted-Mode MR-RAPS1 | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, 2.7e-02 3.0e-10, -1.8e-01, 2.8e-02 | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 7.9e-51, 3.8e-01, 2.5e-02 | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 2.8e-13, 2.2e-01, 3.0e-02 | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 3.6e-01, 8.0e-02, 8.7e-02 | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 6.1e-12, 5.2e-01, 7.5e-02 | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 5.0e-01, 7.9e-02, 1.2e-01 | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-02 1.6e-03, -2.1e-01, 6.5e-02 | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 5.9e-07, 2.6e-01, 5.3e-02 | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 4.9e-15, -1.0e-01, 1.3e-02 | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 7.5e-04, 2.4e-01, 7.1e-02 | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-03 3.9e-08, 2.9e-02, 5.4e-03 1.9e-141, 3.5e-02, 1.4e-03 | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 4.3e-110, 5.3e-02, 2.4e-03 |
| MR-Weighted-Mode | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, 2.7e-02 3.0e-10, -1.8e-01, 2.8e-02 1.8e-09, | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 7.9e-51, 3.8e-01, 2.5e-02 0.0e+00, | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 2.8e-13, 2.2e-01, 3.0e-02 6.1e-94, | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 3.6e-01, 8.0e-02, 8.7e-02 2.0e-01, | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 6.1e-12, 5.2e-01, 7.5e-02 | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 5.0e-01, 7.9e-02, 1.2e-01 | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-02 1.6e-03, -2.1e-01, 6.5e-02 2.7e-03, | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 5.9e-07, 2.6e-01, 5.3e-02 0.0e+00, | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 4.9e-15, -1.0e-01, 1.3e-02 1.2e-17, | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 7.5e-04, 2.4e-01, 7.1e-02 5.8e-04, | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-03 3.9e-08, 2.9e-02, 5.4e-03 1.9e-141, 3.5e-02, 1.4e-03 | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 4.3e-110, 5.3e-02, 2.4e-03 3.0e-147, |
| MR-Weighted-Mode MR-RAPS1 | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, 2.7e-02 3.0e-10, -1.8e-01, 2.8e-02 | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 7.9e-51, 3.8e-01, 2.5e-02 | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 2.8e-13, 2.2e-01, 3.0e-02 | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 3.6e-01, 8.0e-02, 8.7e-02 | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 6.1e-12, 5.2e-01, 7.5e-02 | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 5.0e-01, 7.9e-02, 1.2e-01 | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-02 1.6e-03, -2.1e-01, 6.5e-02 | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 5.9e-07, 2.6e-01, 5.3e-02 | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 4.9e-15, -1.0e-01, 1.3e-02 | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 7.5e-04, 2.4e-01, 7.1e-02 | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-03 3.9e-08, 2.9e-02, 5.4e-03 1.9e-141, 3.5e-02, 1.4e-03 | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 4.3e-110, 5.3e-02, 2.4e-03 |
| MR-Weighted-Mode MR-RAPS1 | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, 2.7e-02 3.0e-10, -1.8e-01, 2.8e-02 1.8e-09, -1.4e-01, | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 7.9e-51, 3.8e-01, 2.5e-02 0.0e+00, 4.1e-01, | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 2.8e-13, 2.2e-01, 3.0e-02 6.1e-94, 2.7e-01, | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 3.6e-01, 8.0e-02, 8.7e-02 2.0e-01, 1.1e-01, | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 6.1e-12, 5.2e-01, 7.5e-02 1.7e-13, 5.5e-01, | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 5.0e-01, 7.9e-02, 1.2e-01 2.7e-14, | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-02 1.6e-03, -2.1e-01, 6.5e-02 2.7e-03, -1.6e-01, | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 5.9e-07, 2.6e-01, 5.3e-02 0.0e+00, -2.9e+01, | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 4.9e-15, -1.0e-01, 1.3e-02 1.2e-17, -9.8e-02, | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 7.5e-04, 2.4e-01, 7.1e-02 5.8e-04, 2.4e-01, | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-03 3.9e-08, 2.9e-02, 5.4e-03 1.9e-141, 3.5e-02, 1.4e-03 1.5e-204, 3.5e-02, | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 4.3e-110, 5.3e-02, 2.4e-03 3.0e-147, 5.3e-02, |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.0e-10, -1.3e-01, 2.8e-02 1.8e-01, 2.8e-02 1.8e-01, 2.8e-02 6.1e-74, -1.9e-01, | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 7.9e-51, 3.8e-01, 2.5e-02 0.0e+40, 4.1e-01, 9.1e-03 | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 2.8e-13, 2.2e-01, 3.0e-02 6.1e-94, 2.7e-01, 1.3e-02 2.6e-84, 2.6e-01, | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 3.6e-01, 8.0e-02, 8.7e-02 2.0e-01, 1.1e-01, 8.2e-02 3.3e-01, 5.7e-02, | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 6.1e-12, 5.2e-01, 7.5e-02 1.7e-13, 5.5e-01, 7.5e-02 1.0e-21, 5.2e-01, | 9.3e-01, -1.1e-01, -1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 5.0e-01, 7.9e-02, 1.2e-01 2.7e-14, 4.9e-01, 6.5e-02 5.0e-01, 7.9e-02, | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-02 1.6e-03, -2.1e-01, 6.5e-02 2.7e-03, -1.6e-01, 5.3e-02 1.1e-13, -2.3e-01, | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 5.9e-07, 2.6e-01, 5.3e-02 0.0e+40, -2.9e+01, 4.4e-01 2.3e-39, 3.2e-01, | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 4.9e-15, -1.0e-01, 1.3e-02 1.2e-17, -9.8e-02, 1.1e-02 9.2e-40, -1.0e-01, | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 7.5e-04, 2.4e-01, 7.1e-02 1.1e-09, 2.4e-01, | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-03 3.9e-08, 2.9e-02, 5.4e-03 1.9e-141, 3.5e-02, 1.4e-03 1.5e-204, 3.5e-02, 1.1e-03 0.0e+00, 3.8e-02, | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 4.3e-110, 5.3e-02, 2.4e-03 3.0e-147, 5.3e-02, 2.1e-03 0.0e+00, 5.6e-02, |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 MR-RAPS3 | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, 2.7e-02 3.0e-10, -1.8e-01, 2.8e-02 1.8e-09, -1.4e-01, 2.3e-02 6.1e-74, -1.9e-01, 1.0e-02 | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 7.9e-51, 3.8e-01, 2.5e-02 0.0e+00, 4.1e-01, 9.1e-03 | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 2.8e-13, 2.2e-01, 3.0e-02 6.1e-94, 2.7e-01, 1.3e-02 2.6e-01, 1.3e-02 | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 8.0e-02, 8.7e-02 2.0e-01, 1.1e-01, 8.2e-02 3.3e-01, 5.7e-02, 5.9e-02 | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 6.1e-12, 5.2e-01, 7.5e-02 1.7e-13, 5.5e-01, 7.5e-02 1.0e-21, 5.2e-01, 5.2e-01, 5.5e-01, | 9.3e-01, -1.1e-01, -1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 5.0e-01, 7.9e-02, 1.2e-01 2.7e-14, 4.9e-01, 6.5e-02 5.0e-01, 7.9e-02, 1.2e-01 | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-02 1.6e-03, -2.1e-01, 6.5e-02 2.7e-03, -1.6e-01, 5.3e-02 1.1e-13, -2.3e-01, 3.1e-02 | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 5.9e-07, 2.6e-01, 5.3e-02 0.0e+00, -2.9e+01, 4.4e-01 2.3e-39, 3.2e-01, 2.4e-02 | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 4.9e-15, -1.0e-01, 1.3e-02 1.2e-17, -9.8e-02, 1.1e-02 9.2e-40, -1.0e-01, 7.8e-03 | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 7.5e-04, 2.4e-01, 7.1e-02 1.1e-09, 2.4e-01, 4.0e-02 | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-08, 2.9e-02, 5.4e-03 1.9e-141, 3.5e-02, 1.4e-03 1.5e-204, 3.5e-02, 1.1e-03 0.0e+00, 3.8e-02, 7.4e-04 | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 4.3e-110, 5.3e-02, 2.4e-03 3.0e-147, 5.3e-02, 2.1e-03 0.0e+00, 5.6e-02, 1.2e-03 |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, 2.7e-02 3.0e-10, -1.8e-01, 2.8e-02 1.8e-09, -1.4e-01, 2.3e-02 6.1e-74, -1.9e-01, 1.0e-02 3.2e-53, | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 7.9e-51, 3.8e-01, 2.5e-02 0.0e+00, 4.1e-01, 9.1e-03 0.0e+00, 4.1e-01, 9.4e-03 0.0e+00, | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 2.8e-13, 2.2e-01, 3.0e-02 6.1e-94, 2.7e-01, 1.3e-02 2.6e-84, 2.6e-01, 1.3e-02 6.1e-94, | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 3.6e-01, 8.0e-02, 8.7e-02 2.0e-01, 1.1e-01, 8.2e-02 3.3e-01, 5.7e-02, 5.9e-02 | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 6.1e-12, 5.2e-01, 7.5e-02 1.7e-13, 5.5e-01, 7.5e-02 1.0e-21, 5.2e-01, 5.4e-02 2.6e-27, | 9.3e-01, -1.1e-01, 1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 5.0e-01, 7.9e-02, 1.2e-01 2.7e-14, 4.9e-01, 6.5e-02 5.0e-01, 7.9e-02, 1.2e-01 | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-03, -2.1e-01, 6.5e-02 2.7e-03, -1.6e-01, 5.3e-02 1.1e-13, -2.3e-01, 3.1e-02 1.8e-09, | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 5.9e-07, 2.6e-01, 5.3e-02 0.0e+00, -2.9e+01, 4.4e-01 2.3e-39, 3.2e-01, 2.4e-02 | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 4.9e-15, -1.0e-01, 1.3e-02 1.2e-17, -9.8e-02, 1.1e-02 9.2e-40, -1.0e-01, -1.0e-0 | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 7.5e-04, 2.4e-01, 7.1e-02 1.1e-09, 2.4e-01, 4.0e-02 4.4e-10, | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-03 3.9e-08, 2.9e-02, 5.4e-03 1.9e-141, 3.5e-02, 1.4e-03 1.5e-204, 3.5e-02, 1.1e-03 0.0e+00, 3.8e-02, 7.4e-04 | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 4.3e-110, 5.3e-02, 2.4e-03 3.0e-147, 5.3e-02, 2.1e-03 0.0e+00, 5.6e-02, 1.2e-03 |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 MR-RAPS3 | 2.8e-02 5.5e-01, -3.0e-02, 5.1e-02 3.0e-11, -1.4e-01, 2.1e-02 3.4e-06, -1.3e-01, 2.7e-02 3.0e-10, -1.8e-01, 2.8e-02 1.8e-09, -1.4e-01, 2.3e-02 6.1e-74, -1.9e-01, 1.0e-02 | 2.5e-02 5.6e-19, 3.5e-01, 4.0e-02 2.8e-45, 2.7e-01, 1.9e-02 1.9e-49, 2.6e-01, 1.7e-02 7.9e-51, 3.8e-01, 2.5e-02 0.0e+00, 4.1e-01, 9.1e-03 | 3.2e-02 2.3e-03, 1.7e-01, 5.7e-02 3.2e-13, 2.1e-01, 2.8e-02 2.1e-07, 2.0e-01, 3.9e-02 2.8e-13, 2.2e-01, 3.0e-02 6.1e-94, 2.7e-01, 1.3e-02 2.6e-01, 1.3e-02 | 8.9e-02 5.4e-01, 1.6e-01, 2.6e-01 6.0e-02, 1.7e-01, 9.2e-02 3.6e-02, 2.7e-01, 1.3e-01 8.0e-02, 8.7e-02 2.0e-01, 1.1e-01, 8.2e-02 3.3e-01, 5.7e-02, 5.9e-02 | 7.3e-02 1.4e-02, 8.5e-01, 3.5e-01 2.0e-09, 5.0e-01, 8.4e-02 2.8e-04, 8.8e-01, 2.4e-01 6.1e-12, 5.2e-01, 7.5e-02 1.7e-13, 5.5e-01, 7.5e-02 1.0e-21, 5.2e-01, 5.2e-01, 5.5e-01, | 9.3e-01, -1.1e-01, -1.3e+00 6.8e-05, 4.1e-01, 1.0e-01 9.2e-05, 4.1e-01, 1.1e-01 5.0e-01, 7.9e-02, 1.2e-01 2.7e-14, 4.9e-01, 6.5e-02 5.0e-01, 7.9e-02, 1.2e-01 | 6.5e-02 9.4e-01, 1.6e-02, 2.3e-01 1.9e-02, -1.1e-01, 4.8e-02 2.9e-01, -8.0e-02, 7.6e-02 1.6e-03, -2.1e-01, 6.5e-02 2.7e-03, -1.6e-01, 5.3e-02 1.1e-13, -2.3e-01, 3.1e-02 | 4.8e-02 1.2e-01, 2.0e-01, 1.3e-01 9.3e-15, 3.0e-01, 3.8e-02 2.4e-12, 3.3e-01, 4.8e-02 5.9e-07, 2.6e-01, 5.3e-02 0.0e+00, -2.9e+01, 4.4e-01 2.3e-39, 3.2e-01, 2.4e-02 | 1.3e-02 1.4e-01, -5.5e-02, 3.7e-02 2.6e-11, -8.5e-02, 1.3e-02 2.8e-04, -1.6e-01, 4.5e-02 4.9e-15, -1.0e-01, 1.3e-02 1.2e-17, -9.8e-02, 1.1e-02 9.2e-40, -1.0e-01, 7.8e-03 | 2.4e-01, 2.2e-01, 1.9e-01 2.8e-06, 2.5e-01, 5.3e-02 8.4e-06, 2.6e-01, 5.8e-02 7.5e-04, 2.4e-01, 7.1e-02 1.1e-09, 2.4e-01, 4.0e-02 | 7.0e-18, 3.5e-02, 4.1e-03 1.5e-124, 3.1e-02, 1.3e-08, 2.9e-02, 5.4e-03 1.9e-141, 3.5e-02, 1.4e-03 1.5e-204, 3.5e-02, 1.1e-03 0.0e+00, 3.8e-02, 7.4e-04 | 5.9e-21, 6.3e-02, 6.7e-03 3.3e-113, 5.1e-02, 2.3e-03 3.6e-07, 5.9e-02, 1.2e-02 4.3e-110, 5.3e-02, 2.4e-03 3.0e-147, 5.3e-02, 2.1e-03 0.0e+00, 5.6e-02, 1.2e-03 |

Table S3: Inferring causal effects of 12 risk factors on Stroke, in each cell from top to bottom are p-value, estimated causal effect $\hat{\theta}$ and its standard error $SE(\hat{\theta})$. Cells with p-value less than Bonferroni adjusted significant cutoff 0.001 are marked with red.

| Exposure | HDL(197) | LDL(184) | TG(128) | Alcohol(53) | Smoke(129) | BF(10) | BW(65) | BMI(90) | Height(986) | | SBP(1319) | DBP(1343 |
|-------------------------|-----------------------|----------------------|-----------------------|-----------------------|----------------------|-----------------------|-----------------------|----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| cML-MA- AIC | 7.1e-05, -8.0e-02, | 1.3e-06, 8.1e-02, | 6.1e-01, 1.5e-02, | 3.3e-01, -1.4e-01, | 4.2e-04, 3.4e-01, | 8.1e-01, -2.4e-02, | 1.2e-04, -2.5e-01, | 6.8e-01, 2.1e-02, | 1.3e-01, -2.3e-02, | 4.6e-01, -6.7e-02, | 1.6e-86, 2.7e-02, | 4.4e-91, 4.7e-02, |
| | 2.0e-02, 2.0e-02 | 1.7e-02, | 3.1e-02 | 1.4e-01, 1.4e-01 | 9.7e-02 | 1.0e-01 | 6.4e-02 | 5.0e-02 | 1.5e-02 | 9.0e-02 | 1.4e-03 | 4.7e-02, 2.3e-03 |
| cML- AIC | 5.4e-05, | 3.5e-07, | 4.3e-01, | 7.5e-02, | 1.3e-04, | 6.1e-01, | 4.9e-06, | 6.6e-01, | 4.8e-02, | 5.5e-01, | 1.9e-94, | 8.2e-97, |
| | -7.6e-02, 1.9e-02 | 8.4e-02, 1.6e-02 | 2.0e-02, 2.5e-02 | -2.0e-01, 1.1e-01 | 3.6e-01, 9.3e-02 | -4.9e-02, 9.6e-02 | -2.5e-01, 5.5e-02 | 2.0e-02, 4.7e-02 | -2.9e-02, 1.5e-02 | -4.4e-02, 7.4e-02 | 2.7e-02, 1.3e-03 | 4.8e-02, 2.3e-03 |
| cML-MA-BIC-max | 5.8e-02, | 6.5e-08, | 8.6e-01, | 3.3e-01, | 1.2e-04, | 8.9e-01, | 2.0e-02, | 4.4e-02, | 5.3e-02, | 2.0e-01, | 8.8e-134, | 1.8e-124, |
| | -3.2e-02, | 8.4e-02, | -4.0e-03, | 9.3e-02, | 3.2e-01, | -1.3e-02, | -1.1e-01, | 8.2e-02, | -2.5e-02, | 9.0e-02, | 2.9e-02, | 4.7e-02, |
| cML-BIC-max | 1.7e-02 6.1e-02, | 1.6e-02 1.0e-08, | 2.2e-02 8.8e-01, | 9.5e-02 3.2e-01, | 8.4e-02 1.1e-04, | 9.3e-02 8.9e-01, | 4.9e-02 1.9e-02, | 4.1e-02 2.8e-02, | 1.3e-02 5.2e-02, | 7.0e-02 1.8e-01, | 1.2e-03 3.1e-135, | 2.0e-03 4.2e-126, |
| CIVIL-BIC-IIIAX | -3.2e-02, | 8.4e-02, | -3.3e-03, | 9.3e-02, | 3.3e-01, | -1.3e-02, | -1.1e-01, | 8.8e-02, | -2.5e-02, | 9.2e-02, | 2.8e-02, | 4.2e-120, 4.7e-02, |
| | 1.7e-02 | 1.5e-02 | 2.2e-02 | 9.4e-02 | 8.4e-02 | 9.3e-02 | 4.8e-02 | 4.0e-02 | 1.3e-02 | 6.9e-02 | 1.1e-03 | 2.0e-03 |
| cML-MA-BIC | 5.7e-02, | 3.9e-07, | 8.4e-01, | 3.3e-01, | 1.2e-04, | 8.8e-01, | 2.4e-02, | 4.6e-02, | 6.0e-02, | 2.2e-01, | 2.6e-134, | 9.3e-125, |
| | -3.2e-02, 1.7e-02 | 8.1e-02, 1.6e-02 | -4.3e-03, 2.2e-02 | 9.2e-02, 9.5e-02 | 3.2e-01, 8.4e-02 | -1.4e-02, 9.3e-02 | -1.1e-01, 4.9e-02 | 8.1e-02, 4.1e-02 | -2.4e-02, 1.3e-02 | 8.7e-02, 7.0e-02 | 2.9e-02, 1.2e-03 | 4.7e-02, 2.0e-03 |
| cML-BIC | 6.1e-02, | 1.0e-08, | 8.8e-01, | 3.2e-01, | 1.1e-04, | 8.9e-01, | 1.9e-02, | 5.6e-02, | 6.5e-02, | 1.8e-01, | 3.7e-136, | 2.5e-126, |
| | -3.2e-02, | 8.4e-02, | -3.3e-03, | 9.3e-02, | 3.3e-01, | -1.3e-02, | -1.1e-01, | 7.7e-02, | -2.4e-02, | 9.2e-02, | 2.9e-02, | 4.7e-02, |
| cML-MA-BIC-DP-Max | 1.7e-02 4.6e-02, | 1.5e-02 3.3e-05, | 2.2e-02 8.7e-01, | 9.4e-02 3.8e-01, | 8.4e-02 5.9e-04, | 9.3e-02 8.7e-01, | 4.8e-02 4.8e-02, | 4.0e-02 8.4e-02, | 1.3e-02 1.4e-01, | 6.9e-02 2.5e-01, | 1.1e-03 7.0e-103, | 2.0e-03 4.1e-88, |
| CIVIL-IVIA-DIC-DF-IVIAX | -3.6e-02, | 7.8e-02, | -3.6e-03, | 8.9e-02, | 3.3e-04, 3.3e-01, | -1.7e-02, | -1.3e-01, | 8.0e-02, | -2.3e-02, | 9.7e-02, | 2.9e-02, | 4.7e-02, |
| | 1.8e-02 | 1.9e-02 | 2.3e-02 | 1.0e-01 | 9.5e-02 | 1.0e-01 | 6.5e-02 | 4.6e-02 | 1.5e-02 | 8.4e-02 | 1.3e-03 | 2.4e-03 |
| cML-BIC-DP-Max | 4.1e-02, | 6.7e-05, | 8.7e-01, | 3.1e-01, | 5.9e-04, | 8.7e-01, | 4.2e-02, | 4.0e-02, | 1.4e-01, | 2.1e-01, | 7.0e-105, | 2.3e-89, |
| | -3.6e-02, 1.8e-02 | 7.8e-02, 1.9e-02 | -3.7e-03, 2.2e-02 | 9.3e-02, 9.2e-02 | 3.2e-01, 9.5e-02 | -1.7e-02, 1.0e-01 | -1.2e-01, 6.1e-02 | 8.3e-02, 4.1e-02 | -2.3e-02, 1.5e-02 | 9.7e-02, 7.8e-02 | 2.9e-02, 1.3e-03 | 4.7e-02, 2.4e-03 |
| cML-MA-BIC-DP | 4.6e-02, | 5.2e-05, | 8.8e-01, | 4.0e-01, | 7.8e-04, | 8.7e-01, | 5.1e-02, | 9.1e-02, | 1.4e-01, | 3.4e-01, | 4.5e-86, | 1.2e-79, |
| | -3.7e-02, | 7.8e-02, | -3.6e-03, | 8.7e-02, | 3.3e-01, | -1.7e-02, | -1.3e-01, | 8.0e-02, | -2.3e-02, | 9.3e-02, | 2.9e-02, | 4.7e-02, |
| aML DIC DD | 1.8e-02 | 1.9e-02 | 2.3e-02 | 1.0e-01 | 9.7e-02 | 1.0e-01 | 6.8e-02 | 4.7e-02 | 1.5e-02 | 9.9e-02 | 1.5e-03 | 2.5e-03 |
| cML-BIC-DP | 4.1e-02, -3.6e-02, | 6.7e-05, 7.8e-02, | 8.7e-01, -3.7e-03, | 4.2e-01, 8.8e-02, | 5.9e-04, 3.2e-01, | 8.7e-01, -1.7e-02, | 4.7e-02, -1.3e-01, | 1.2e-01, 7.9e-02, | 1.4e-01, -2.3e-02, | 2.1e-01, 9.7e-02, | 5.7e-77, 2.9e-02, | 1.2e-79, 4.7e-02, |
| | 1.8e-02 | 1.9e-02 | 2.2e-02 | 1.1e-01 | 9.5e-02 | 1.0e-01 | 6.5e-02 | 5.1e-02 | 1.5e-02 | 7.8e-02 | 1.5e-03 | 2.5e-03 |
| cML-MA-AIC-Profile | 8.4e-05, | 1.6e-06, | 6.2e-01, | 3.4e-01, | 6.3e-04, | 8.2e-01, | 1.5e-04, | 6.9e-01, | 1.3e-01, | 4.6e-01, | 1.0e-87, | 3.2e-88, |
| | -8.0e-02, 2.0e-02 | 8.1e-02, 1.7e-02 | 1.5e-02, 3.1e-02 | -1.4e-01, 1.4e-01 | 3.4e-01, 1.0e-01 | -2.4e-02, 1.0e-01 | -2.5e-01, 6.5e-02 | 2.1e-02, 5.1e-02 | -2.3e-02, 1.6e-02 | -6.7e-02, 9.0e-02 | 2.7e-02, 1.4e-03 | 4.7e-02, 2.4e-03 |
| cML-AIC-Profile | 6.3e-05, | 4.2e-07, | 4.4e-01, | 8.1e-02, | 2.1e-04, | 6.2e-01, | 8.2e-06, | 6.7e-02 | 5.2e-02, | 5.6e-01, | 3.0e-91, | 3.8e-95, |
| | -7.6e-02, | 8.4e-02, | 2.0e-02, | -2.0e-01, | 3.6e-01, | -4.9e-02, | -2.5e-01, | 2.0e-02, | -2.9e-02, | -4.4e-02, | 2.7e-02, | 4.8e-02, |
| | 1.9e-02 | 1.7e-02 | 2.6e-02 | 1.1e-01 | 9.6e-02 | 9.9e-02 | 5.7e-02 | 4.7e-02 | 1.5e-02 | 7.5e-02 | 1.3e-03 | 2.3e-03 |
| ML-MA-BIC-max-Profile | 5.9e-02, -3.2e-02, | 6.6e-08, 8.4e-02, | 8.6e-01, -4.0e-03, | 3.3e-01, 9.3e-02, | 1.4e-04, 3.2e-01, | 8.9e-01, -1.3e-02, | 2.0e-02, -1.1e-01, | 4.4e-02, 8.2e-02, | 5.4e-02, -2.5e-02, | 1.9e-01, 9.0e-02, | 1.8e-133, 2.9e-02, | 2.2e-124 4.7e-02, |
| | 1.7e-02 | 1.6e-02 | 2.2e-02 | 9.5e-02 | 8.5e-02 | 9.5e-02 | 4.9e-02 | 4.1e-02 | 1.3e-02 | 6.9e-02 | 1.2e-03 | 2.0e-03 |
| cML-BIC-max-Profile | 6.1e-02, | 1.1e-08, | 8.8e-01, | 3.3e-01, | 1.3e-04, | 8.9e-01, | 1.9e-02, | 2.8e-02, | 5.3e-02, | 1.8e-01, | 6.4e-135, | 5.0e-126 |
| | -3.2e-02, | 8.4e-02, | -3.3e-03, | 9.3e-02, | 3.3e-01, | -1.3e-02, | -1.1e-01, | 8.8e-02, | -2.5e-02, | 9.2e-02, | 2.8e-02, | 4.7e-02, |
| cML-MA-BIC-Profile | 1.7e-02 5.8e-02, | 1.5e-02 4.0e-07, | 2.2e-02 8.4e-01, | 9.5e-02 3.3e-01, | 8.5e-02 1.5e-04, | 9.5e-02 8.9e-01, | 4.8e-02 2.4e-02, | 4.0e-02 4.6e-02, | 1.3e-02 6.1e-02, | 6.9e-02 2.2e-01, | 1.1e-03 5.9e-134, | 2.0e-03 1.3e-124, |
| CME MIT DIC TIONIC | -3.2e-02, | 8.1e-02, | -4.3e-03, | 9.2e-02, | 3.2e-01, | -1.4e-02, | -1.1e-01, | 8.1e-02, | -2.4e-02, | 8.7e-02, | 2.9e-02, | 4.7e-02, |
| | 1.7e-02 | 1.6e-02 | 2.2e-02 | 9.5e-02 | 8.5e-02 | 9.5e-02 | 5.0e-02 | 4.1e-02 | 1.3e-02 | 7.0e-02 | 1.2e-03 | 2.0e-03 |
| cML-BIC-Profile | 6.1e-02, | 1.1e-08, | 8.8e-01, | 3.3e-01, | 1.3e-04, | 8.9e-01, | 1.9e-02, | 5.5e-02, | 6.6e-02, | 1.8e-01, | 8.4e-136, | 3.5e-126, 4.7e-02, |
| | -3.2e-02, 1.7e-02 | 8.4e-02, 1.5e-02 | -3.3e-03, 2.2e-02 | 9.3e-02, 9.5e-02 | 3.3e-01, 8.5e-02 | -1.3e-02, 9.5e-02 | -1.1e-01, 4.8e-02 | 7.7e-02, 4.0e-02 | -2.4e-02, 1.3e-02 | 9.2e-02, 6.9e-02 | 2.9e-02, 1.1e-03 | 4.7e-02, 2.0e-03 |
| CAUSE | 2.7e-01, | 4.6e-02, | 9.9e-01, | 2.5e-01, | 2.3e-02, | 1.0e+00, | 8.8e-02, | 2.3e-01, | 5.5e-01, | 9.9e-01, | 4.1e-09, | 1.1e-03, |
| | -3.5e-02, | 6.2e-02, | 8.1e-03, | 1.3e-01, | 2.9e-01, | 4.4e-03, | -1.1e-01, | 7.2e-02, | -1.6e-02, | 9.6e-03, | 2.2e-02, | 3.2e-02, |
| MR-Mix | NA 1.0e+00, | NA 1.5e-01, | NA 2.1e-02, | NA 1.0e+00, | NA 1.0e+00, | NA 1.0e+00, | NA 2.9e-01, | NA 1.0e+00, | NA 8.6e-02, | NA 8.2e-01, | NA 7.0e-11, | NA 1.7e-07, |
| IVIK-IVIIX | 0.0e+00, | 2.0e-02, | 8.0e-02, | 2.0e-17, | 2.0e-17, | 1.0e-10, 1.0e-17, | -4.0e-02, | 2.0e-17, | 1.0e-02, | -1.0e-02, | 1.0e-11, 1.0e-01, | 1.7e-07, 1.1e-01, |
| | 2.1e-02 | 1.4e-02 | 3.5e-02 | 4.6e-02 | 4.3e-02 | 2.3e-02 | 3.8e-02 | 2.0e-02 | 5.8e-03 | 4.4e-02 | 1.5e-02 | 2.1e-02 |
| MR-ContMix | 3.8e-03, | 6.8e-05, | 8.5e-01, | 3.3e-01, | 1.9e-03, | 6.1e-01, | 6.2e-04, | 7.1e-01, | 7.5e-01, | 5.5e-01, | 2.6e-63, | 5.4e-60, |
| | -6.5e-02, NA | 7.2e-02, NA | -4.6e-03, NA | -1.4e-01, NA | 5.0e-01, NA | -4.9e-02, NA | -2.8e-01, NA | 1.7e-02, NA | -6.6e-03, NA | -4.4e-02, NA | 3.9e-02, NA | 7.0e-02, NA |
| MR-Lasso | 4.6e-03, | 6.6e-06, | 6.8e-01, | 5.6e-01, | 3.5e-04, | 8.9e-01, | 2.3e-03, | 5.3e-02, | 1.6e-01, | 6.9e-01, | 1.6e-119, | 3.3e-108. |
| | -4.8e-02, | 6.9e-02, | -9.4e-03, | 5.6e-02, | 3.0e-01, | -1.3e-02, | -1.5e-01, | 8.1e-02, | -1.8e-02, | 3.3e-02, | 2.8e-02, | 4.5e-02, |
| MD DDEGGO | 1.7e-02 | 1.5e-02 | 2.3e-02 | 9.6e-02 | 8.4e-02 | 9.2e-02 | 4.9e-02 | 4.2e-02 | 1.3e-02 | 8.1e-02 | 1.2e-03 | 2.0e-03 |
| MR-PRESSO | 9.4e-02, -3.1e-02, | 2.9e-06, 8.2e-02, | 9.0e-01, -3.2e-03, | 3.7e-01, 9.1e-02, | 5.4e-04, 3.1e-01, | 8.3e-01, -1.3e-02, | 7.7e-02, -9.2e-02, | 1.4e-01, 7.5e-02, | 6.8e-02, -2.6e-02, | 3.6e-01, 9.0e-02, | 1.1e-93, 2.8e-02, | 6.0e-88, 4.6e-02, |
| | 1.9e-02 | 1.7e-02 | 2.5e-02 | 1.0e-01 | 9.0e-02 | 6.1e-02 | 5.2e-02 | 5.0e-02 | 1.4e-02 | 9.7e-02 | 1.3e-03 | 2.3e-03 |
| MR-IVW | 7.2e-02, | 6.0e-05, | 9.0e-01, | 3.7e-01, | 5.4e-04, | 8.9e-01, | 1.2e-01, | 9.9e-02, | 2.1e-02, | 3.6e-01, | 3.3e-95, | 1.9e-79, |
| | -3.6e-02, | 8.1e-02, | -3.2e-03, | 9.1e-02, 1.0e-01 | 3.1e-01, 9.0e-02 | -1.3e-02, 9.2e-02 | -9.6e-02, | 8.6e-02, | -3.4e-02, 1.5e-02 | 9.0e-02, | 2.9e-02, 1.4e-03 | 4.6e-02, |
| MR-Egger | 2.0e-02 4.8e-01, | 2.0e-02 3.2e-04, | 2.5e-02 1.0e-01, | 3.9e-01, | 6.2e-03, | 7.0e-01, | 6.1e-02 3.9e-02, | 5.2e-02 7.3e-01, | 5.3e-01, | 9.7e-02 3.1e-02, | 9.2e-25, | 2.4e-03 1.1e-17, |
| 255er | 2.6e-02, | 1.1e-01, | -7.1e-02, | -2.5e-01, | 1.2e+00, | -1.8e-01, | 4.3e-01, | -4.8e-02, | -2.7e-02, | -4.4e-01, | 4.2e-02, | 5.9e-02, |
| | 3.7e-02 | 3.2e-02 | 4.3e-02 | 3.0e-01 | 4.3e-01 | 4.6e-01 | 2.1e-01 | 1.4e-01 | 4.3e-02 | 2.0e-01 | 4.1e-03 | 6.9e-03 |
| MR-Weighted-Median | 7.2e-02, | 7.9e-03, | 8.0e-01, | 8.7e-01, | 2.9e-02, | 9.3e-01, | 1.2e-01, | 6.0e-01, | 2.3e-01, | 3.4e-01, | 5.6e-49, | 3.2e-53, |
| | -5.1e-02, 2.8e-02 | 7.3e-02, 2.7e-02 | 9.0e-03, 3.5e-02 | 2.3e-02, 1.4e-01 | 2.7e-01, 1.2e-01 | -9.5e-03, 1.2e-01 | -1.2e-01, 7.3e-02 | 3.7e-02, 7.0e-02 | -2.4e-02, 1.9e-02 | -9.4e-02, 9.8e-02 | 2.9e-02, 1.9e-03 | 5.0e-02, 3.2e-03 |
| MR-Weighted-Mode | 1.0e-01, | 1.6e-03, | 9.5e-01, | 7.8e-01, | 2.0e-01, | 9.4e-01, | 2.3e-01, | 8.1e-01, | 9.1e-01, | 4.5e-01, | 1.5e-07, | 2.1e-07, |
| | -4.6e-02, | 7.4e-02, | 2.5e-03, | -7.8e-02, | 3.8e-01, | 1.3e-02, | -2.2e-01, | 2.0e-02, | -9.1e-03, | -8.2e-02, | 3.0e-02, | 5.5e-02, |
| MR-RAPS1 | 2.8e-02 8.5e-02, | 2.3e-02 7.4e-06, | 3.8e-02 7.8e-01, | 2.8e-01 3.9e-01, | 3.0e-01 | 1.7e-01 | 1.9e-01 1.4e-01, | 8.3e-02 | 7.8e-02 2.0e-02, | 1.1e-01 3.3e-01, | 5.8e-03 | 1.1e-02 |
| WIK-KAP31 | 8.5e-02, -3.5e-02, | 7.4e-06, 8.6e-02, | 7.8e-01, -6.9e-03, | 3.9e-01, 8.8e-02, | 4.9e-04, 3.3e-01, | 8.9e-01, -1.3e-02, | -9.1e-02, | 1.5e-01, 7.6e-02, | 2.0e-02, -3.4e-02, | 3.3e-01, 9.3e-02, | 1.3e-97, 3.0e-02, | 1.5e-80, 4.6e-02, |
| | 2.0e-02 | 1.9e-02 | 2.5e-02 | 1.0e-01 | 9.3e-02 | 9.3e-02 | 6.2e-02 | 5.3e-02 | 1.5e-02 | 9.6e-02 | 1.4e-03 | 2.4e-03 |
| MR-RAPS2 | 3.0e-02, | 8.7e-06, | 7.9e-01, | 5.3e-01, | 6.5e-04, | 8.7e-01, | 2.9e-02, | 2.2e-01, | 1.3e-01, | 4.2e-01, | 8.6e-95, | 2.4e-83, |
| | -4.0e-02, 1.9e-02 | 7.9e-02, 1.8e-02 | -7.0e-03, 2.6e-02 | 6.8e-02, | 3.3e-01, 9.6e-02 | -1.6e-02, 9.6e-02 | -1.3e-01, 5.9e-02 | 6.7e-02, 5.5e-02 | -2.2e-02, 1.5e-02 | 8.3e-02, | 2.9e-02, 1.4e-03 | 4.7e-02, |
| MR-RAPS3 | 1.9e-02 3.0e-02, | 2.7e-08, | 8.8e-01, | 1.1e-01 3.3e-01, | 9.6e-02 1.5e-04, | 9.6e-02 8.9e-01, | 3.7e-02, | 3.0e-02, | 7.6e-03, | 1.0e-01 1.9e-01, | 3.6e-147, | 2.4e-03 2.2e-128 |
| | -3.7e-02, | 8.2e-02, | -3.3e-03, | 9.3e-02, | 3.3e-01, | -1.3e-02, | -1.0e-01, | 8.8e-02, | -3.4e-02, | 9.2e-02, | 3.0e-02, | 4.7e-02, |
| | 1.7e-02 | 1.5e-02 | 2.2e-02 | 9.6e-02 | 8.6e-02 | 9.3e-02 | 4.8e-02 | 4.1e-02 | 1.3e-02 | 7.0e-02 | 1.2e-03 | 2.0e-03 |
| MR-RAPS4 | 1.3e-02, -4.3e-02, | 5.2e-07, 7.6e-02, | 8.8e-01, | 4.7e-01, | 1.8e-04, | 8.7e-01, | 2.4e-03, | 9.4e-02, | 1.1e-01, | 3.9e-01, | 5.1e-130, | 3.1e-123, |
| | -4 3C-U/ | 7.0e-UZ. | -3.3e-03, | 7.2e-02, | 3.3e-01, | -1.6e-02, | -1.5e-01, | 7.0e-02, | -2.1e-02, | 6.1e-02, | 2.9e-02, | 4.7e-02, |

Table S4: Inferring causal effects of 12 risk factors on T2D, in each cell from top to bottom are p-value, estimated causal effect $\hat{\theta}$ and its standard error SE($\hat{\theta}$). Cells with p-value less than Bonferroni adjusted significant cutoff 0.001 are marked with red.

| Method | HDL(188) | LDL(178) | TG(124) | Alcohol(44) | Smoke(115) | BF(9) | BW(54) | BMI(90) | Height(982) | FG(17) | SBP(1110) | DBP(1110) |
|--|---|---|---|---|---|--|---|--|---|--|---|--|
| cML-MA- AIC | 1.0e-01, | 1.1e-04, | 5.7e-01, | 1.9e-01, | 6.8e-01, | 5.0e-11, | 2.1e-03, | 2.9e-19, | 9.9e-01, | 3.8e-12, | 8.2e-17, | 9.7e-10, |
| CINE IIII THE | -8.9e-02, | -1.6e-01, | 3.3e-02, | 3.3e-01, | 8.3e-02, | 1.9e+00, | -4.1e-01, | 9.5e-01, | -4.2e-04, | 2.1e+00, | 2.4e-02, | 3.1e-02, |
| | 5.4e-02 | 4.1e-02 | 5.8e-02 | 2.5e-01 | 2.0e-01 | 2.8e-01 | 1.3e-01 | 1.1e-01 | 3.0e-02 | 3.0e-01 | 2.8e-03 | 5.1e-03 |
| cML- AIC | 6.2e-02, | 1.7e-05, | 5.7e-01, | 3.9e-01, | 9.2e-01, | 1.4e-12, | 1.9e-04, | 8.0e-21, | 8.9e-01, | 9.2e-20, | 2.3e-16, | 5.5e-11, |
| | -8.2e-02, | -1.7e-01, | 3.2e-02, | 2.1e-01, | -1.9e-02, | 1.8e+00, | -4.7e-01, | 9.1e-01, | -4.1e-03, | 2.0e+00, | 2.3e-02, | 3.1e-02, |
| cML-MA-BIC-max | 4.4e-02 2.7e-03, | 3.9e-02 9.2e-06, | 5.7e-02 2.6e-01, | 2.4e-01 2.3e-01, | 1.9e-01 3.5e-02, | 2.6e-01 4.1e-11, | 1.3e-01 6.5e-07, | 9.7e-02 4.6e-27, | 2.9e-02 3.6e-01, | 2.2e-01 1.4e-16, | 2.8e-03 1.2e-17, | 4.7e-03 2.9e-08, |
| CME-MA-BIC-IIIAX | -1.1e-01, | -1.6e-01, | 5.4e-02, | 2.5e-01, 2.5e-01, | 3.6e-01, | 1.5e+00, | -5.7e-01, | 8.7e-01, | -2.3e-02, | 2.1e+00, | 2.1e-02, | 2.3e-08, 2.3e-02, |
| | 3.7e-02 | 3.5e-02 | 4.8e-02 | 2.1e-01 | 1.7e-01 | 2.3e-01 | 1.1e-01 | 8.0e-02 | 2.6e-02 | 2.5e-01 | 2.5e-03 | 4.2e-03 |
| cML-BIC-max | 4.0e-03, | 1.2e-05, | 1.8e-01, | 2.3e-01, | 3.1e-02, | 2.3e-11, | 2.8e-07, | 4.0e-27, | 3.7e-01, | 2.1e-27, | 2.7e-18, | 8.0e-09, |
| | -1.1e-01, | -1.5e-01, | 6.2e-02, | 2.5e-01, | 3.7e-01, | 1.5e+00, | -5.5e-01, | 8.6e-01, | -2.3e-02, | 2.2e+00, | 2.1e-02, | 2.4e-02, |
| | 3.7e-02 | 3.4e-02 | 4.7e-02 | 2.1e-01 | 1.7e-01 | 2.3e-01 | 1.1e-01 | 8.0e-02 | 2.5e-02 | 2.1e-01 | 2.4e-03 | 4.2e-03 |
| cML-MA-BIC | 2.3e-03, -1.1e-01, | 6.9e-06, | 2.2e-01, 5.8e-02, | 2.2e-01, 2.6e-01, | 4.5e-02, 3.5e-01, | 4.6e-11, | 1.5e-06, | 5.0e-27, | 3.2e-01, -2.6e-02, | 8.3e-18, | 2.2e-16, 2.0e-02, | 3.2e-07, 2.2e-02, |
| | 3.8e-02 | -1.6e-01, 3.6e-02 | 4.8e-02, | 2.0e-01, 2.1e-01 | 1.7e-01 | 1.5e+00, 2.3e-01 | -5.6e-01, 1.2e-01 | 8.7e-01, 8.1e-02 | 2.6e-02, | 2.1e+00, 2.5e-01 | 2.5e-02, 2.5e-03 | 4.2e-02, |
| cML-BIC | 4.0e-03, | 1.2e-05, | 1.8e-01, | 2.1c-01 2.3e-01, | 3.1e-02, | 2.3e-11, | 2.8e-07, | 4.0e-27, | 2.5e-01, | 2.1e-27, | 1.5e-16, | 2.3e-07, |
| | -1.1e-01, | -1.5e-01, | 6.2e-02, | 2.5e-01, | 3.7e-01, | 1.5e+00, | -5.5e-01, | 8.6e-01, | -2.9e-02, | 2.2e+00, | 2.0e-02, | 2.2e-02, |
| | 3.7e-02 | 3.4e-02 | 4.7e-02 | 2.1e-01 | 1.7e-01 | 2.3e-01 | 1.1e-01 | 8.0e-02 | 2.5e-02 | 2.1e-01 | 2.4e-03 | 4.2e-03 |
| cML-MA-BIC-DP-Max | 2.1e-02, | 2.3e-04, | 3.0e-01, | 2.9e-01, | 8.9e-02, | 6.2e-07, | 1.7e-03, | 3.6e-19, | 5.6e-01, | 2.1e-04, | 4.7e-12, | 3.5e-06, |
| | -1.2e-01, | -1.5e-01, | 6.8e-02, | 2.5e-01, | 3.4e-01, | 1.5e+00, | -5.5e-01, | 8.7e-01, | -1.7e-02, | 1.9e+00, | 2.1e-02, | 2.2e-02, |
| cML-BIC-DP-Max | 5.1e-02 3.4e-02, | 4.2e-02 8.0e-05, | 6.6e-02 | 2.4e-01 2.2e-01, | 2.0e-01 9.4e-02, | 3.0e-01 1.2e-08, | 1.8e-01 2.2e-03, | 9.7e-02 | 3.0e-02 4.7e-01, | 5.1e-01 3.9e-04, | 3.1e-03 5.2e-12, | 4.7e-03 2.6e-06, |
| CML-BIC-DF-Max | -1.1e-01, | -1.5e-01, | 3.4e-01, 6.3e-02, | 2.2e-01, 2.7e-01, | 9.4e-02, 3.4e-01, | 1.5e+00, | -5.5e-01, | 1.4e-23, 8.6e-01, | -1.9e-02, | 3.9e-04, 1.9e+00, | 2.1e-02, | 2.0e-00, 2.2e-02, |
| | 5.4e-02 | 3.9e-02 | 6.6e-02 | 2.2e-01 | 2.0e-01 | 2.6e-01 | 1.8e-01 | 8.6e-02 | 2.7e-02 | 5.3e-01 | 3.1e-03 | 4.7e-03 |
| cML-MA-BIC-DP | 3.4e-02, | 8.7e-04, | 3.1e-01, | 3.4e-01, | 1.2e-01, | 9.8e-07, | 2.3e-03, | 6.5e-15, | 7.2e-01, | 2.3e-04, | 4.6e-12, | 2.4e-05, |
| | -1.1e-01, | -1.5e-01, | 7.0e-02, | 2.5e-01, | 3.3e-01, | 1.5e+00, | -5.4e-01, | 8.7e-01, | -1.3e-02, | 1.9e+00, | 2.1e-02, | 2.2e-02, |
| | 5.4e-02 | 4.6e-02 | 6.8e-02 | 2.6e-01 | 2.1e-01 | 3.1e-01 | 1.8e-01 | 1.1e-01 | 3.5e-02 | 5.2e-01 | 3.1e-03 | 5.3e-03 |
| cML-BIC-DP | 3.4e-02, | 2.3e-03, | 3.2e-01, | 3.7e-01, | 9.4e-02, | 1.2e-08, | 2.2e-03, | 3.0e-14, | 7.3e-01, | 3.9e-04, | 1.6e-12, | 1.7e-05, |
| | -1.1e-01, 5.4e-02 | -1.5e-01, 5.1e-02 | 7.2e-02, 7.1e-02 | 2.3e-01, 2.6e-01 | 3.4e-01, 2.0e-01 | 1.5e+00, 2.6e-01 | -5.5e-01, 1.8e-01 | 8.7e-01, 1.1e-01 | -1.2e-02, 3.5e-02 | 1.9e+00, 5.3e-01 | 2.1e-02, 3.0e-03 | 2.2e-02, 5.2e-03 |
| cML-MA-AIC-Profile | 9.3e-02, | 1.2e-04, | 5.7e-01, | 2.0e-01, | 6.9e-01, | 1.2e-10, | 4.1e-03, | 6.8e-19, | 9.9e-01, | 6.0e-12, | 2.2e-16, | 1.5e-09, |
| CIME WITT THE TRAINE | -9.1e-02, | -1.6e-01, | 3.3e-02, | 3.3e-01, | 8.3e-02, | 1.9e+00, | -3.9e-01, | 9.5e-01, | -4.2e-04, | 2.1e+00, | 2.4e-02, | 3.1e-02, |
| | 5.4e-02 | 4.2e-02 | 5.9e-02 | 2.5e-01 | 2.1e-01 | 2.9e-01 | 1.4e-01 | 1.1e-01 | 3.1e-02 | 3.0e-01 | 2.9e-03 | 5.2e-03 |
| cML-AIC-Profile | 6.4e-02, | 2.0e-05, | 5.7e-01, | 4.0e-01, | 9.2e-01, | 4.9e-12, | 2.6e-04, | 4.0e-20, | 8.9e-01, | 2.4e-19, | 7.1e-16, | 1.1e-10, |
| | -8.2e-02, | -1.7e-01, | 3.2e-02, | 2.1e-01, | -1.9e-02, | 1.8e+00, | -4.7e-01, | 9.1e-01, | -4.1e-03, | 2.0e+00, | 2.3e-02, | 3.1e-02, |
| cML-MA-BIC-max-Profile | 4.4e-02 | 3.9e-02 | 5.7e-02 | 2.5e-01 | 2.0e-01 | 2.7e-01 | 1.3e-01 | 9.9e-02 | 2.9e-02 | 2.2e-01 | 2.8e-03 | 4.8e-03 |
| CML-MA-BIC-max-Profile | 2.6e-03, -1.1e-01, | 9.4e-06, -1.6e-01, | 2.6e-01, 5.4e-02, | 2.3e-01, 2.5e-01, | 3.5e-02, 3.6e-01, | 4.1e-11, 1.5e+00, | 5.8e-07, -5.7e-01, | 4.6e-27, 8.7e-01, | 3.6e-01, -2.3e-02, | 1.3e-16, 2.1e+00, | 1.4e-17, 2.1e-02, | 3.0e-08, 2.3e-02, |
| | 3.7e-02 | 3.5e-02 | 4.8e-02 | 2.1e-01 | 1.7e-01 | 2.3e-01 | 1.1e-01 | 8.0e-02 | 2.6e-02 | 2.5e-01 | 2.5e-03 | 4.2e-03 |
| cML-BIC-max-Profile | 4.0e-03, | 1.2e-05, | 1.8e-01, | 2.3e-01, | 3.2e-02, | 2.2e-11, | 2.4e-07, | 3.8e-27, | 3.7e-01, | 1.2e-27, | 3.1e-18, | 8.3e-09, |
| | -1.1e-01, | -1.5e-01, | 6.2e-02, | 2.5e-01, | 3.7e-01, | 1.5e+00, | -5.5e-01, | 8.6e-01, | -2.3e-02, | 2.2e+00, | 2.1e-02, | 2.4e-02, |
| | 3.7e-02 | 3.4e-02 | 4.6e-02 | 2.1e-01 | 1.7e-01 | 2.3e-01 | 1.1e-01 | 8.0e-02 | 2.5e-02 | 2.1e-01 | 2.4e-03 | 4.2e-03 |
| cML-MA-BIC-Profile | 2.3e-03, | 7.1e-06, | 2.2e-01, | 2.2e-01, | 4.5e-02, | 4.7e-11, | 1.4e-06, | 5.2e-27, | 3.2e-01, | 7.7e-18, | 2.6e-16, | 3.4e-07, |
| | -1.1e-01, 3.8e-02 | -1.6e-01, 3.6e-02 | 5.8e-02, 4.8e-02 | 2.6e-01, 2.1e-01 | 3.5e-01, 1.7e-01 | 1.5e+00, 2.3e-01 | -5.6e-01, 1.2e-01 | 8.7e-01, 8.1e-02 | -2.6e-02, 2.6e-02 | 2.1e+00, 2.5e-01 | 2.0e-02, 2.5e-03 | 2.2e-02, 4.3e-03 |
| cML-BIC-Profile | 4.0e-03, | 1.2e-05, | 1.8e-01, | 2.1e-01 2.3e-01, | 3.2e-02, | 2.2e-11, | 2.4e-07, | 3.8e-27, | 2.5e-02 2.5e-01, | 1.2e-27, | 1.7e-16, | 2.5e-07, |
| enia are frome | -1.1e-01, | -1.5e-01, | 6.2e-02, | 2.5e-01, | 3.7e-01, | 1.5e+00, | -5.5e-01, | 8.6e-01, | -2.9e-02, | 2.2e+00, | 2.0e-02, | 2.2e-02, |
| | 3.7e-02 | 3.4e-02 | 4.6e-02 | 2.1e-01 | 1.7e-01 | 2.3e-01 | 1.1e-01 | 8.0e-02 | 2.6e-02 | 2.1e-01 | 2.5e-03 | 4.2e-03 |
| CAUSE | 5.6e-02, | 3.2e-01, | 1.5e-01, | 9.9e-01, | 6.7e-01, | 1.0e+00, | 6.4e-02, | 4.8e-03, | 9.6e-01, | 1.3e-02, | 1.0e-02, | 2.0e-02, |
| | -1.6e-01, | -1.3e-01, | 1.8e-01, | 6.9e-02, | 1.5e-01, | 6.5e-02, | -2.7e-01, | 7.5e-01, | 1.3e-02, | 1.3e+00, | 1.4e-02, | 2.0e-02, |
| MD Mar | NA 1.6.01 | NA 1.5: 01 | NA 5.4: 01 | NA 1.000 | NA | NA | NA 1.0: 01 | NA | NA CO: 01 | NA | NA | NA |
| MR-Mix | 1.6e-01, -3.0e-02, | 1.5e-01, -7.0e-02, | 5.4e-01, 6.0e-02, | 1.0e+00, 2.0e-17, | 4.9e-01, -2.1e-01, | 2.9e-05, 5.1e-01, | 1.0e-01, -1.1e-01, | 1.1e-03, 3.0e-01, | 6.9e-01, 4.0e-02, | 2.0e-04, 3.3e-01, | 2.1e-03, 9.0e-02, | 8.2e-02, 4.0e-02, |
| | 2.2e-02 | 4.9e-02 | 9.8e-02 | 8.7e-02 | 3.1e-01 | 1.2e-01 | 6.7e-02 | 9.2e-02 | 1.0e-01 | 8.9e-02 | 2.9e-02 | 2.3e-02 |
| MR-ContMix | 4.1e-01, | 1.5e-03, | 1.9e-01, | 1.8e-01, | 7.9e-01, | 2.7e-01, | 2.5e-02, | 3.4e-09, | 7.6e-01, | 2.1e-01, | 3.2e-11, | 4.5e-06, |
| | -4.1e-02, | -1.5e-01, | 1.2e-01, | 4.7e-01, | 5.0e-02, | 4.4e-01, | -4.1e-01, | 5.0e-01, | 1.2e-02, | 5.0e-01, | 2.6e-02, | 3.4e-02, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA | NA | | |
| MR-Lasso | 1.5e-02, | 9.7e-06, | | | | | | 2.7e-21, | | | NA | NA |
| | | | 9.5e-02, | 1.5e-01, | 1.9e-01, | 2.1e-06, | 4.3e-05, | | 8.5e-01, | 1.8e-05, | 3.7e-17, | NA 5.1e-06, |
| | -9.6e-02, | -1.6e-01, | 8.5e-02, | 3.2e-01, | 2.3e-01, | 1.5e+00, | 4.3e-05, -4.9e-01, | 8.3e-01, | 4.9e-03, | 1.8e-05, 1.5e+00, | 3.7e-17, 2.1e-02, | NA 5.1e-06, 1.9e-02, |
| MR-PRESSO | -9.6e-02, 3.9e-02 | -1.6e-01, 3.6e-02 | 8.5e-02, 5.1e-02 | 3.2e-01, 2.2e-01 | 2.3e-01, 1.8e-01 | 1.5e+00, 3.1e-01 | 4.3e-05, -4.9e-01, 1.2e-01 | 8.7e-02 | 4.9e-03, 2.6e-02 | 1.8e-05, 1.5e+00, 3.6e-01 | 3.7e-17, 2.1e-02, 2.5e-03 | NA 5.1e-06, 1.9e-02, 4.3e-03 |
| MR-PRESSO | -9.6e-02, 3.9e-02 9.0e-03, | -1.6e-01, 3.6e-02 2.5e-04, | 8.5e-02, | 3.2e-01, | 2.3e-01, 1.8e-01 7.4e-02, | 1.5e+00, 3.1e-01 1.5e-03, | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, | 8.7e-02 2.1e-19, | 4.9e-03, 2.6e-02 3.3e-01, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, |
| MR-PRESSO | -9.6e-02, 3.9e-02 | -1.6e-01, 3.6e-02 | 8.5e-02, 5.1e-02 2.4e-01, | 3.2e-01, 2.2e-01 2.8e-01, | 2.3e-01, 1.8e-01 | 1.5e+00, 3.1e-01 | 4.3e-05, -4.9e-01, 1.2e-01 | 8.7e-02 | 4.9e-03, 2.6e-02 | 1.8e-05, 1.5e+00, 3.6e-01 | 3.7e-17, 2.1e-02, 2.5e-03 | NA 5.1e-06, 1.9e-02, 4.3e-03 |
| MR-PRESSO MR-IVW | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, | 8.7e-02 2.1e-19, 8.4e-01, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, |
| | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, |
| MR-IVW | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-02 | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 |
| | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-02 3.0e-01, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01 2.9e-01, | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, |
| MR-IVW | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, -1.1e+00, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, | 4.3e-05, -4.9e-01, 1.2e-01, 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-02 3.0e-01, 9.3e-02, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01 2.9e-01, -1.5e+00, | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, |
| MR-IVW MR-Egger | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, -1.1e+00, 9.1e-01 | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-02 3.0e-01, 9.3e-02, 9.0e-02 | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01 2.9e-01, -1.5e+00, 1.4e+00 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 |
| MR-IVW | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, -1.1e+00, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, | 4.3e-05, -4.9e-01, 1.2e-01, 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-02 3.0e-01, 9.3e-02, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01 2.9e-01, -1.5e+00, | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, |
| MR-IVW MR-Egger MR-Weighted-Median | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02, 7.8e-02 | 3.2e-01, 2.2e-01, 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, -1.1e+00, 9.1e-01 | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 4.6e-03, | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-01, 9.3e-02, 9.0e-02 | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01 2.9e-01, -1.5e+00, 1.4e+00 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, |
| MR-IVW MR-Egger | 9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 1.0e+00, 0.0e+00, 6.7e-02 8.2e-01, | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, | 3.2e-01, 2.2e-01 2.8e-01, 2.3e-01, 2.3e-01, 2.3e-01, 2.3e-01, 1.5e-01, 1.0e+00, 7.2e-01 2.6e-01, 3.7e-01, 3.3e-01 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, -1.1e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01 8.6e-01, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 2.5e-07, 1.8e+00, 3.4e-01 5.9e-08, | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 4.6e-03, -4.7e-01, 1.7e-01 2.4e-01, | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-02 3.0e-01, 9.3e-02, 9.0e-02 1.0e+00, 0.0e+00, 4.2e-02 9.0e-01, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01 2.9e-01, -1.5e+00, 1.3e-02, 7.3e-01, 2.9e-01 6.0e-01, | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, |
| MR-IVW MR-Egger MR-Weighted-Median | 9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 1.0e+00, 0.0e+00, 6.7e-02 8.2e-01, 1.5e-02, | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 2.6e-01, 3.7e-01, 3.3e-01 3.1e-01, 4.8e-01, | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 2.0e-01, 2.3e-01, -1.1e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01, 8.7e-02, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 2.5e-07, 1.8e+00, 3.4e-01 5.9e-08, 1.9e+00, | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 4.6e-03, -4.7e-01, 1.7e-01 2.4e-01, -2.7e-01, | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.3e-01, 1.3e-01 6.5e-09, 1.0e+00, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-01 9.3e-02, 9.0e-02 1.0e+00, 0.0e+00, 4.2e-02 9.0e-01, 1.9e-02, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01, 2.9e-01, -1.5e+00, 1.4e+00 1.3e-02, 7.3e-01, 2.9e-01 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 1.8e-02, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, |
| MR-IVW MR-Egger MR-Weighted-Median MR-Weighted-Mode | 9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 1.0e+00, 0.0e+00, 6.7e-02 8.2e-01, 1.5e-02, 6.6e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, 6.7e-02 | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, 8.8e-02 | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 2.6e-01, 3.7e-01, 3.3e-01 4.8e-01, 4.7e-01 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, -1.1e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01 8.6e-01, 8.7e-02, 5.1e-01 | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 3.4e-01 5.9e-08, 1.9e+00, 3.4e-01 | 4.3e-05, -4.9e-01, 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 4.6e-03, -4.7e-01, 1.7e-01 2.4e-01, -2.7e-01, 2.2e-01 | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, 1.0e+00, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-01, 9.3e-02, 9.0e-02 1.0e+00, 0.0e+400, 4.2e-02 9.0e-01, 1.9e-02, 1.5e-01 | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01 2.9e-01, -1.5e+00, 1.4e+00 1.3e-02, 7.3e-01, 2.9e-01 6.0e-01, 2.1e-01, 4.0e-01 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 1.8e-02, 8.9e-03 | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, 1.6e-02 |
| MR-IVW MR-Egger MR-Weighted-Median | 9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 1.0e+00, 6.7e-02 8.2e-01, 1.5e-02, 6.6e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, 6.7e-02 8.5e-05, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, 8.8e-02 3.3e-01, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 2.6e-01, 3.7e-01, 3.3e-01 3.1e-01, 4.8e-01, 4.7e-01 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, -1.1e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01, 8.6e-01, 8.7e-02, 5.1e-01 6.1e-02, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 2.5e-07, 1.8e+00, 3.4e-01 5.9e-08, 1.9e+00, 3.4e-01 | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 4.6e-03, -4.7e-01, 1.7e-01 2.4e-01, -2.7e-01, 2.2e-01 5.2e-05, | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, 1.0e+00, 1.8e-01 | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-01, 9.3e-02, 9.0e-02 1.0e+00, 0.0e+00, 4.2e-02 9.0e-01, 1.9e-02, 1.5e-01 6.3e-01, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01 2.9e-01, 1.5e+00, 1.3e-02, 7.3e-01, 2.9e-01 6.0e-01, 2.1e-01, 4.0e-01 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 1.8e-02, 8.9e-03 2.8e-12, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, 1.6e-02 2.2e-06, |
| MR-IVW MR-Egger MR-Weighted-Median MR-Weighted-Mode | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 1.0e+00, 6.7e-02 8.2e-01, 1.5e-02, 6.6e-02 4.6e-03, -1.5e-01, | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, 6.7e-02 8.5e-05, -1.6e-01, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, 8.8e-02 3.3e-01, 6.2e-02, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 3.7e-01, 3.3e-01 3.1e-01, 4.7e-01 2.9e-01, 2.5e-01, | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 2.0e-01 2.3e-01, -1.1e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01 8.6e-01, 8.7e-02, 5.1e-01 6.1e-02, 3.9e-01, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 2.5e-07, 1.8e+00, 3.4e-01 5.9e-08, 1.9e+00, 3.4e-01 | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 4.6e-03, -4.7e-01, 1.7e-01 2.2e-01, 2.2e-01, 5.2e-05, -8.3e-01, | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, 1.0e+00, 1.8e-01 6.1e-05, 7.1e-01, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-01 9.3e-02, 9.0e-02 1.0e+00, 4.2e-02 9.0e-01, 1.9e-02, 1.5e-01 6.3e-01, -1.5e-01 | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01, 2.9e-01, -1.5e+00, 1.3e-02, 7.3e-01, 2.9e-01, 2.9e-01, 2.9e-01, 3.9e-01 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 8.9e-03 2.8e-12, 2.3e-02, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, 1.6e-02 2.2e-06, 2.5e-02, |
| MR-IVW MR-Egger MR-Weighted-Median MR-Weighted-Mode | 9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 1.0e+00, 6.7e-02 8.2e-01, 1.5e-02, 6.6e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, 6.7e-02 8.5e-05, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, 8.8e-02 3.3e-01, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 2.6e-01, 3.7e-01, 3.3e-01 3.1e-01, 4.8e-01, 4.7e-01 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, -1.1e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01, 8.6e-01, 8.7e-02, 5.1e-01 6.1e-02, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 2.5e-07, 1.8e+00, 3.4e-01 5.9e-08, 1.9e+00, 3.4e-01 | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 4.6e-03, -4.7e-01, 1.7e-01 2.4e-01, -2.7e-01, 2.2e-01 5.2e-05, | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, 1.0e+00, 1.8e-01 | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-01, 9.3e-02, 9.0e-02 1.0e+00, 0.0e+00, 4.2e-02 9.0e-01, 1.9e-02, 1.5e-01 6.3e-01, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01 2.9e-01, 1.5e+00, 1.3e-02, 7.3e-01, 2.9e-01 6.0e-01, 2.1e-01, 4.0e-01 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 1.8e-02, 8.9e-03 2.8e-12, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, 1.6e-02 2.2e-06, |
| MR-IVW MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 1.0e+00, 0.0e+00, 6.7e-02 8.2e-01, 1.5e-02, 6.6e-02 4.6e-03, -1.5e-01, 5.3e-01 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, 6.7e-02 8.5e-05, -1.6e-01, 4.1e-02 | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, 8.8e-02 3.3e-01, 6.2e-02, 6.3e-02 | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, 1.5e-01, 1.0e-400, 7.2e-01 3.7e-01, 3.7e-01, 3.7e-01, 4.8e-01, 4.7e-01 2.9e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.4e-01 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, -1.1e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01, 8.7e-02, 5.1e-01 6.1e-02, 3.9e-01, 2.1e-01 | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 3.4e-01 5.9e-08, 1.9e+00, 3.4e-01 1.9e-02, 1.1e+00, 4.7e-01 | 4.3e-05, -4.9e-01, 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 4.6e-03, -4.7e-01, 1.7e-01 2.4e-01, -2.7e-01, 2.2e-01, 2 | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, 1.0e+00, 1.8e-01 6.1e-05, 7.1e-01, 1.8e-01 | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-02 9.0e-02 1.0e+00, 0.0e+00, 4.2e-02 9.0e-01, 1.9e-02, 1.5e-01 6.3e-01, -1.5e-02, 3.1e-02 | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.3e-02, 1.4e+00, 6.3e-01, 2.9e-01, -1.5e+00, 1.3e-02, 7.3e-01, 2.9e-01 6.0e-01, 2.1e-01, 4.0e-01, 2.7e-02, 1.3e+00, 6.0e-01 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 1.8e-02, 8.9e-03 2.8e-12, 2.3e-02, 3.3e-02, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, 1.6e-02 2.2e-06, 2.5e-02, 5.3e-03 |
| MR-IVW MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 1.0e+00, 0.0e+00, 6.7e-02 8.2e-01, 1.5e-01, 5.3e-02 1.5e-01, 5.3e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, 6.7e-02 8.5e-05, -1.6e-01, 4.1e-02 1.6e-04, -1.6e-01, 4.2e-02 | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, 8.8e-02 3.3e-01, 6.2e-02, 6.3e-02 2.0e-01, 8.2e-02, 6.4e-02 4.4e-02 | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, 1.5e-01, 1.0e-00, 7.2e-01 2.6e-01, 3.7e-01, 3.7e-01, 4.8e-01, 4.7e-01 2.5e-01, 2.5e-0 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 2.0e-01 2.3e-01, 2.1e-01 1.0e+00, 0.0e+00, 0.0e+00, 2.6e-01, 8.7e-02, 5.1e-01 6.1e-02, 3.9e-01, 2.1e-01 | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 3.4e-01 5.9e-08, 1.9e+00, 3.4e-01 1.9e-02, 1.1e+00, 4.7e-01 7.7e-03, 1.2e+00, 4.6e-01 | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 4.6e-03, -4.7e-01, 1.7e-01 2.2e-01, 2.2e-01, 2.2e-01, 2.2e-01, 2.1e-01 2.9e-04, -6.0e-01, 1.7e-01 | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, 1.0e+00, 1.8e-01 8.8e-27, 8.8e-01, 8.8e-27, 8.8e-01, 8.2e-02 | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-02 3.0e-01, 9.3e-02, 9.0e-02 1.0e+00, 0.0e+00, 4.2e-02 9.0e-01, 1.9e-02, 1.5e-01 6.3e-01, -1.5e-02, 3.1e-02 7.1e-01, -1.2e-02, 3.1e-02 | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01, 2.9e-01, -1.5e+00, 1.4e+00 1.3e-02, 7.3e-01, 2.9e-01 6.0e-01, 2.1e-01, 4.0e-01 2.7e-02, 1.3e-02, 7.3e-01, 2.9e-01 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 1.8e-02, 8.9e-03 2.8e-12, 2.3e-02, 3.3e-03 1.8e-12, 3.3e-03 | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, 1.6e-02 2.2e-06, 2.5e-02, 5.3e-03 6.6e-06, 2.3e-02, 5.1e-03 |
| MR-IVW MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | 9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 1.0e+00, 0.0e+00, 6.7e-02 8.2e-01, 1.5e-01, 5.3e-02 4.6e-03, -1.5e-01, 5.3e-02 1.1e-02, -1.3e-01, 5.3e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, 6.7e-02 8.5e-05, -1.6e-01, 4.1e-02 1.6e-04, -1.6e-04, -1.6e-01, -1.9e-01, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, 8.8e-02 3.3e-01, 6.2e-02, 6.3e-02 2.0e-01, 8.2e-02, 6.4e-02 1.9e-01, 9.5e-01, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 3.7e-01, 3.7e-01, 3.3e-01 4.8e-01, 4.7e-01 2.9e-01, 2.5e-01, | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 7.4e-02, 3.5e-01, 2.0e-01 2.3e-01, -1.1e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01 8.6e-01, 8.7e-02, 5.1e-01 6.1e-02, 3.9e-01, 2.1e-01 1.0e-01, 3.5e-01, 2.1e-01 3.5e-01, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 2.5e-07, 1.8e+00, 3.4e-01 1.9e-02, 1.1e+00, 4.7e-01 7.7e-03, 1.2e+00, 4.6e-01 6.1e-07, | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 2.4e-01, -2.7e-01, 2.2e-01 5.2e-05, -8.3e-01, 2.2e-01 5.2e-05, -8.3e-01, 1.2e-01 1.2e-01 1.2e-01 1.2e-01 1.2e-01 | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, 1.0e+00, 1.8e-01 1.8e-01 8.8e-27, 8.8e-01, 8.8e-27, 8.8e-01, 8.2e-02 6.4e-20, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-01, 9.3e-02, 9.0e-02 1.0e+00, 4.2e-02 9.0e-01, 1.9e-02, 1.5e-01 6.3e-01, -1.5e-02, 3.1e-02 7.1e-01, -1.2e-02, 3.1e-02 5.5e-01, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.3e-02, 1.4e+00, 6.3e-01 2.9e-01, -1.5e+00, 1.3e-02, 7.3e-01, 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 2.9e-01 3 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 1.8e-02, 8.9e-03 2.8e-12, 2.3e-02, 3.3e-03 1.8e-12, 2.1e-02, 3.3e-03 2.8e-12, 2.1e-02, 3.0e-03 2.2e-22, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, 1.6e-02 2.2e-06, 2.5e-02, 5.3e-03 6.6e-06, 2.3e-02, 5.1e-03 2.7e-09, |
| MR-IVW MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 1.0e+00, 0.0e+00, 6.7e-02 8.2e-01, 1.5e-01, 5.3e-02 4.6e-03, -1.5e-01, 5.3e-02 1.1e-02, -1.3e-01, 5.1e-02 4.1e-05, -1.5e-01, 5.1e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, 6.7e-02 8.5e-05, -1.6e-01, 4.1e-02 1.6e-04, -1.6e-01, 4.2e-02 1.3e-05, -1.5e-01, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, 8.8e-02 3.3e-01, 6.2e-02, 6.3e-02 2.0e-01, 8.2e-02, 6.4e-02 1.9e-01, 6.0e-02, 6.0e-02, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 2.6e-01, 3.7e-01, 3.3e-01 3.1e-01, 4.8e-01, 4.7e-01 2.9e-01, 2.5e-01, 2.4e-01 2.8e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, | 2.3e-01, 1.8e-01 1.8e-01 1.4e-02, 3.5e-01, 2.0e-01 1.4e-02, 3.5e-01, 2.0e-01 1.0e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01 8.7e-02, 5.1e-01 6.1e-02, 3.9e-01, 2.1e-01 1.0e-01, 3.5e-01, 3.5e-01, 3.5e-01, 3.7e-01, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 2.5e-07, 1.8e+00, 3.4e-01 1.9e+00, 3.4e-01 1.9e-02, 1.1e+00, 4.7e-01 7.7e-03, 1.2e+40, 4.6e-01 6.1e-07, 1.1e+00, | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, -1.0e+00, 71.e-01 4.6e-03, -4.7e-01, 1.7e-01 2.2e-01, 2.2e-01, 5.2e-05, -8.3e-01, 2.1e-01 2.9e-04, -6.0e-01, 1.7e-01 | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, 1.0e+00, 1.8e-01 6.1e-05, 7.1e-01, 1.8e-01 8.8e-27, 8.8e-01, 8.2e-02 6.4e-20, 7.7e-01, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-01, 9.3e-02 1.0e+00, 0.0e+00, 4.2e-02 9.0e-01, 1.9e-02, 1.5e-01 6.3e-01, -1.5e-02, 3.1e-02 7.1e-01, -1.2e-02, 3.1e-02 5.5e-01, -1.5e-02, 5.5e-01, -1.5e-02, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01, 2.9e-01, -1.5e+00, 1.4e+00 1.3e-02, 7.3e-01, 2.9e-01, 4.0e-01, 2.1e-01, 4.0e-01, 2.7e-02, 1.3e+00, 6.0e-01, 2.7e-02, 1.3e+00, 6.0e-01, 1.5e-01, | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 1.8e-02, 8.9e-03 2.8e-12, 2.3e-02, 3.3e-03 1.8e-12, 2.1e-02, 3.0e-03 2.2e-12, 2.2e-22, 2.4e-02, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, 1.6e-02 2.2e-06, 2.5e-02, 5.3e-03 6.6e-06, 2.3e-02, 5.1e-03 2.7e-09, 2.5e-02, |
| MR-IVW MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | -9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 6.0e-01, 5.0e-02, 9.7e-02 1.0e+00, 0.0e+00, 6.7e-02 8.2e-01, 1.5e-01, 5.3e-02 4.6e-03, -1.5e-01, 5.3e-02 4.1e-05, -1.3e-01, 5.1e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, 6.7e-02 8.5e-05, -1.6e-01, 4.1e-02 1.6e-04, -1.6e-01, 4.2e-02 1.3e-05, -1.5e-01, 3.5e-02 | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, 8.8e-02 3.3e-01, 6.2e-02, 6.3e-02 2.0e-01, 8.2e-02, 6.4e-02 1.9e-01, 6.0e-02, 4.6e-02 | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 2.6e-01, 3.7e-01, 3.3e-01 3.1e-01, 4.8e-01, 4.7e-01 2.9e-01, 2.5e-01, 2.4e-01 2.5e-01, 2.4e-01, 2.5e-01, 2.7e-01, 2.5e-01, 2.5e-01, 2.1e-01 | 2.3e-01, 1.8e-01 7.4e-02, 3.5e-01, 2.0e-01 2.0e-01 2.3e-01, -1.1e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01, 8.7e-02, 5.1e-01 1.0e-01, 3.5e-01, 2.1e-01 1.0e-01, 3.5e-01, 2.1e-01 | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 3.4e-01 5.9e-08, 1.9e+00, 3.4e-01 1.9e-02, 1.1e+00, 4.7e-01 7.7e-03, 1.2e+400, 4.6e-01 6.1e-07, 1.1e+00, 2.3e-01 | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, 2.0e-01 1.6e-01, -1.0e+00, 7.1e-01 4.6e-03, -4.7e-01, 1.7e-01 2.2e-01, 2.2e-01 5.2e-05, -8.3e-01, 2.1e-01 1.9e-04, -6.0e-01, 1.7e-01 1.6e-16, -9.0e-01, 1.1e-01 | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, 1.0e+00, 1.8e-01 8.8e-27, 8.8e-01, 8.8e-27, 8.8e-01, 8.2e-02 | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-01, 9.3e-02, 9.0e-02 1.0e+00, 0.0e+00, 4.2e-02 9.0e-01, 1.9e-02, 1.5e-01 6.3e-01, -1.5e-02, 3.1e-02 7.1e-01, -1.2e-02, 3.1e-02 5.5e-01, -1.5e-02, 2.6e-02 | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01, 2.9e-01, -1.5e+00, 1.4e+00 1.3e-02, 7.3e-01, 2.9e-01 6.0e-01, 2.1e-01, 4.0e-01 2.7e-02, 1.3e-40, 6.0e-01 1.3e-38, 2.0e+00, 1.5e-01 1.6e-23, 1.9e-01 | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 1.8e-02, 8.9e-03 2.8e-12, 2.3e-02, 3.3e-03 1.8e-12, 2.3e-02, 3.2e-02, 3.2e-02, 3.2e-03 2.2e-22, 2.2e-02, 2.2e-02, 2.2e-02, 3.2e-03 | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, 1.6e-02 2.2e-06, 2.3e-02, 5.3e-03 6.6e-06, 2.3e-02, 5.1e-03 2.7e-09, 2.5e-02, 4.2e-03 |
| MR-IVW MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 9.6e-02, 3.9e-02 9.0e-03, -1.2e-01, 4.6e-02 4.5e-03, -1.5e-01, 5.2e-02 1.0e+00, 0.0e+00, 6.7e-02 8.2e-01, 1.5e-01, 5.3e-02 4.6e-03, -1.5e-01, 5.3e-02 1.1e-02, -1.3e-01, 5.1e-02 4.1e-05, -1.5e-01, 5.1e-02 | -1.6e-01, 3.6e-02 2.5e-04, -1.5e-01, 4.1e-02 2.5e-04, -1.5e-01, 4.1e-02 6.8e-04, -2.7e-01, 7.8e-02 2.5e-02, -1.3e-01, 5.9e-02 4.9e-03, -1.9e-01, 6.7e-02 8.5e-05, -1.6e-01, 4.1e-02 1.6e-04, -1.6e-01, 4.2e-02 1.3e-05, -1.5e-01, | 8.5e-02, 5.1e-02 2.4e-01, 7.4e-02, 6.3e-02 3.7e-01, 5.9e-02, 6.5e-02 5.2e-01, 7.5e-02, 1.2e-01 2.3e-01, 9.5e-02, 7.8e-02 2.4e-01, 1.0e-01, 8.8e-02 3.3e-01, 6.2e-02, 6.3e-02 2.0e-01, 8.2e-02, 6.4e-02 1.9e-01, 6.0e-02, 6.0e-02, | 3.2e-01, 2.2e-01 2.8e-01, 2.5e-01, 2.3e-01 2.8e-01, 2.5e-01, 2.3e-01 1.5e-01, 1.0e+00, 7.2e-01 2.6e-01, 3.7e-01, 3.3e-01 3.1e-01, 4.8e-01, 4.7e-01 2.9e-01, 2.5e-01, 2.4e-01 2.8e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, 2.5e-01, | 2.3e-01, 1.8e-01 1.8e-01 1.4e-02, 3.5e-01, 2.0e-01 1.4e-02, 3.5e-01, 2.0e-01 1.0e+00, 9.1e-01 1.0e+00, 0.0e+00, 2.6e-01 8.7e-02, 5.1e-01 6.1e-02, 3.9e-01, 2.1e-01 1.0e-01, 3.5e-01, 3.5e-01, 3.5e-01, 3.7e-01, | 1.5e+00, 3.1e-01 1.5e-03, 1.2e+00, 3.7e-01 4.1e-02, 1.0e+00, 4.9e-01 2.6e-02, 5.1e+00, 2.3e+00 2.5e-07, 1.8e+00, 3.4e-01 1.9e+00, 3.4e-01 1.9e-02, 1.1e+00, 4.7e-01 7.7e-03, 1.2e+40, 4.6e-01 6.1e-07, 1.1e+00, | 4.3e-05, -4.9e-01, 1.2e-01 1.2e-05, -5.9e-01, 1.3e-01 4.4e-05, -8.3e-01, -1.0e+00, 71.e-01 4.6e-03, -4.7e-01, 1.7e-01 2.2e-01, 2.2e-01, 5.2e-05, -8.3e-01, 2.1e-01 2.9e-04, -6.0e-01, 1.7e-01 | 8.7e-02 2.1e-19, 8.4e-01, 9.3e-02 4.2e-05, 7.1e-01, 1.7e-01 8.9e-03, 1.2e+00, 4.5e-01 8.3e-11, 8.6e-01, 1.3e-01 6.5e-09, 1.0e+00, 1.8e-01 6.1e-05, 7.1e-01, 1.8e-01 8.8e-27, 8.8e-01, 8.2e-02 6.4e-20, 7.7e-01, | 4.9e-03, 2.6e-02 3.3e-01, -2.9e-02, 2.9e-02 6.2e-01, -1.5e-02, 3.0e-01, 9.3e-02 1.0e+00, 0.0e+00, 4.2e-02 9.0e-01, 1.9e-02, 1.5e-01 6.3e-01, -1.5e-02, 3.1e-02 7.1e-01, -1.2e-02, 3.1e-02 5.5e-01, -1.5e-02, 5.5e-01, -1.5e-02, | 1.8e-05, 1.5e+00, 3.6e-01 2.9e-10, 1.7e+00, 2.7e-01 2.3e-02, 1.4e+00, 6.3e-01, 2.9e-01, -1.5e+00, 1.4e+00 1.3e-02, 7.3e-01, 2.9e-01, 4.0e-01, 2.1e-01, 4.0e-01, 2.7e-02, 1.3e+00, 6.0e-01, 2.7e-02, 1.3e+00, 6.0e-01, 1.5e-01, | 3.7e-17, 2.1e-02, 2.5e-03 6.0e-13, 2.0e-02, 2.8e-03 5.8e-13, 2.3e-02, 3.2e-03 1.3e-01, 1.5e-02, 9.8e-03 1.3e-06, 2.0e-02, 4.0e-03 4.7e-02, 1.8e-02, 8.9e-03 2.8e-12, 2.3e-02, 3.3e-03 1.8e-12, 2.1e-02, 3.0e-03 2.2e-12, 2.2e-22, 2.4e-02, | NA 5.1e-06, 1.9e-02, 4.3e-03 5.1e-06, 2.2e-02, 4.8e-03 1.8e-06, 2.4e-02, 5.1e-03 2.5e-01, 1.7e-02, 1.5e-02 1.2e-03, 2.3e-02, 7.1e-03 6.1e-03, 4.5e-02, 1.6e-02 2.2e-06, 2.5e-02, 5.3e-03 6.6e-06, 2.3e-02, 5.1e-03 2.7e-09, 2.5e-02, |

Table S5: For each pair of exposure and outcome, from top to bottom are number of IVs used, number of invalid IVs detected by cML-BIC, and proportion of detected invalid IVs. Results are got with one starting point set at 0, and 100 randomly generated starting points.

| Exposure Outcome | HDL | LDL | TG | Alcohol | Smoke | BF | BW | BMI | Height | FG | SBP | DBP |
|------------------|--------|--------|--------|---------|-------|--------|-------|-------|--------|--------|-------|-------|
| Asthma | 188, | 173, | 122, | 44, | 114, | 10, | 54, | 88, | 977, | 17, | 1106, | 1108, |
| | 3, | 1, | 1, | 0, | 2, | 0, | 1, | 0, | 9, | 1, | 5, | 11, |
| | 1.60% | 0.58% | 0.82% | 0.00% | 1.75% | 0.00% | 1.85% | 0.00% | 0.92% | 5.88% | 0.45% | 0.99% |
| CAD | 197, | 184, | 128, | 54, | 129, | 10, | 65, | 90, | 986, | 17, | 1324, | 1345, |
| | 36, | 19, | 17, | 3, | 1, | 3, | 5, | 6, | 40, | 2, | 88, | 96, |
| | 18.27% | 10.33% | 13.28% | 5.56% | 0.78% | 30.00% | 7.69% | 6.67% | 4.06% | 11.76% | 6.65% | 7.14% |
| Stroke | 197, | 184, | 128, | 53, | 129, | 10, | 65, | 90, | 986, | 17, | 1319, | 1343, |
| | 1, | 3, | 0, | 0, | 0, | 0, | 2, | 1, | 5, | 0, | 10, | 15, |
| | 0.51% | 1.63% | 0.00% | 0.00% | 0.00% | 0.00% | 3.08% | 1.11% | 0.51% | 0.00% | 0.76% | 1.12% |
| T2D | 188, | 178, | 124, | 44, | 115, | 9, | 54, | 90, | 982, | 17, | 1110, | 1110, |
| | 5, | 0, | 3, | 0, | 0, | 1, | 5, | 1, | 7, | 5, | 16, | 14, |
| | 2.66% | 0.00% | 2.42% | 0.00% | 0.00% | 11.11% | 9.26% | 1.11% | 0.71% | 29.41% | 1.44% | 1.26% |

Table S6: For each pair of exposure and outcome, from top to bottom are number of IVs used, number of invalid IVs detected by cML-BIC, and proportion of detected invalid IVs. Results are got with one starting point set at 0.

| Exposure | HDL | LDL | TG | Alcohol | Smoke | BF | BW | BMI | Height | FG | SBP | DBP |
|----------|--------|--------|--------|---------|-------|--------|-------|-------|--------|--------|-------|-------|
| Outcome | IIDL | LDL | 10 | Alcohol | SHOKE | DI. | ВW | DIVII | Height | 10 | SDI | ומט |
| Asthma | 188, | 173, | 122, | 44, | 114, | 10, | 54, | 88, | 977, | 17, | 1106, | 1108, |
| | 3, | 1, | 1, | 0, | 2, | 0, | 1, | 0, | 9, | 1, | 5, | 11, |
| | 1.60% | 0.58% | 0.82% | 0.00% | 1.75% | 0.00% | 1.85% | 0.00% | 0.92% | 5.88% | 0.45% | 0.99% |
| CAD | 197, | 184, | 128, | 54, | 129, | 10, | 65, | 90, | 986, | 17, | 1324, | 1345, |
| | 37, | 19, | 15, | 3, | 1, | 4, | 5, | 6, | 41, | 2, | 89, | 96, |
| | 18.78% | 10.33% | 11.72% | 5.56% | 0.78% | 40.00% | 7.69% | 6.67% | 4.16% | 11.76% | 6.72% | 7.14% |
| Stroke | 197, | 184, | 128, | 53, | 129, | 10, | 65, | 90, | 986, | 17, | 1319, | 1343, |
| | 1, | 3, | 0, | 0, | 0, | 0, | 2, | 1, | 5, | 0, | 10, | 15, |
| | 0.51% | 1.63% | 0.00% | 0.00% | 0.00% | 0.00% | 3.08% | 1.11% | 0.51% | 0.00% | 0.76% | 1.12% |
| T2D | 188, | 178, | 124, | 44, | 115, | 9, | 54, | 90, | 982, | 17, | 1110, | 1110, |
| | 5, | 0, | 3, | 0, | 0, | 1, | 5, | 1, | 8, | 3, | 16, | 14, |
| | 2.66% | 0.00% | 2.42% | 0.00% | 0.00% | 11.11% | 9.26% | 1.11% | 0.81% | 17.65% | 1.44% | 1.26% |

Table S7: Goodness-of-fit tests for Asthma: the cells with the p-values less than the Bonferroni adjusted significance cutoff 0.001 are marked with red.

| Exposure | HDL | LDL | TG | Alcohol | Smoke | BF | BW | BMI | Height | FG | SBP | DBP |
|----------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| GOF1-Max | 6.1e-01 | 7.8e-02 | 3.6e-02 | 2.4e-01 | 2.9e-02 | 3.7e-01 | 8.0e-02 | 2.4e-01 | 2.6e-01 | 7.8e-02 | 4.0e-01 | 3.9e-02 |
| GOF2-Max | 6.4e-01 | 1.0e-01 | 5.2e-02 | 2.5e-01 | 3.0e-02 | 3.6e-01 | 7.2e-02 | 2.9e-01 | 2.7e-01 | 8.0e-02 | 4.0e-01 | 3.5e-02 |
| GOF1 | 6.1e-01 | 7.8e-02 | 3.6e-02 | 2.4e-01 | 2.9e-02 | 3.7e-01 | 8.0e-02 | 2.4e-01 | 2.5e-01 | 7.8e-02 | 4.8e-02 | 8.9e-03 |
| GOF2 | 6.4e-01 | 1.0e-01 | 5.2e-02 | 2.5e-01 | 3.0e-02 | 3.6e-01 | 7.2e-02 | 2.9e-01 | 2.6e-01 | 8.0e-02 | 5.9e-02 | 8.7e-03 |

Table S8: Goodness-of-fit tests for CAD: the cells with the p-values less than the Bonferroni adjusted significance cutoff 0.001 are marked with red.

| Exposure | HDL | LDL | TG | Alcohol | Smoke | BF | BW | BMI | Height | FG | SBP | DBP |
|----------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| GOF1-Max | 2.6e-14 | 1.1e-16 | 8.7e-13 | 1.2e-07 | 5.2e-01 | 8.2e-06 | 8.5e-06 | 6.9e-04 | 1.9e-03 | 1.6e-08 | 5.2e-14 | 3.1e-11 |
| GOF2-Max | 2.5e-16 | 4.7e-14 | 3.6e-16 | 4.3e-08 | 5.6e-01 | 1.4e-09 | 2.5e-06 | 2.2e-03 | 1.0e-03 | 2.1e-06 | 1.8e-12 | 4.8e-10 |
| GOF1 | 2.7e-14 | 1.6e-14 | 7.5e-18 | 1.2e-07 | 5.2e-01 | 8.2e-06 | 8.5e-06 | 6.9e-04 | 1.7e-07 | 4.5e-06 | 1.3e-12 | 9.8e-11 |
| GOF2 | 8.3e-19 | 2.3e-17 | 3.7e-18 | 4.3e-08 | 5.6e-01 | 1.4e-09 | 2.5e-06 | 2.2e-03 | 4.0e-07 | 8.4e-06 | 9.0e-11 | 2.8e-11 |

Table S9: Goodness-of-fit tests for Stroke: the cells with the p-values less than the Bonferroni adjusted significance cutoff 0.001 are marked with red.

| Exposure | HDL | LDL | TG | Alcohol | Smoke | BF | BW | BMI | Height | FG | SBP | DBP |
|----------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| GOF1-Max | 7.3e-01 | 3.0e-02 | 5.1e-01 | 6.7e-01 | 1.4e-01 | 2.0e-01 | 3.6e-05 | 7.2e-01 | 8.8e-01 | 5.6e-02 | 7.4e-04 | 4.6e-02 |
| GOF2-Max | 7.2e-01 | 3.6e-02 | 5.4e-01 | 6.6e-01 | 1.7e-01 | 1.7e-01 | 1.8e-04 | 7.1e-01 | 8.7e-01 | 5.5e-02 | 1.4e-03 | 3.8e-02 |
| GOF1 | 7.3e-01 | 3.0e-02 | 5.1e-01 | 6.7e-01 | 1.4e-01 | 2.0e-01 | 3.6e-05 | 8.4e-01 | 1.7e-01 | 5.6e-02 | 1.3e-02 | 6.9e-03 |
| GOF2 | 7.2e-01 | 3.6e-02 | 5.4e-01 | 6.6e-01 | 1.7e-01 | 1.7e-01 | 1.8e-04 | 8.5e-01 | 2.0e-01 | 5.5e-02 | 1.1e-02 | 2.4e-03 |

Table S10: Goodness-of-fit tests for T2D: the cells with the p-values less than the Bonferroni adjusted significance cutoff 0.001 are marked with red.

| Exposure | HDL | LDL | TG | Alcohol | Smoke | BF | BW | BMI | Height | FG | SBP | DBP |
|----------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| GOF1-Max | 5.2e-02 | 7.4e-02 | 3.5e-02 | 5.1e-01 | 1.5e-01 | 2.5e-01 | 9.8e-07 | 1.6e-02 | 7.2e-02 | 4.0e-12 | 3.7e-02 | 1.2e-01 |
| GOF2-Max | 5.6e-02 | 1.1e-01 | 1.5e-02 | 5.2e-01 | 1.7e-01 | 8.8e-02 | 2.4e-08 | 3.3e-02 | 8.4e-02 | 2.2e-16 | 5.5e-02 | 9.4e-02 |
| GOF1 | 5.2e-02 | 7.4e-02 | 3.5e-02 | 5.1e-01 | 1.5e-01 | 2.5e-01 | 9.8e-07 | 1.6e-02 | 2.3e-01 | 4.0e-12 | 2.6e-02 | 4.6e-03 |
| GOF2 | 5.6e-02 | 1.1e-01 | 1.5e-02 | 5.2e-01 | 1.7e-01 | 8.8e-02 | 2.4e-08 | 3.3e-02 | 2.3e-01 | 2.2e-16 | 2.2e-02 | 1.0e-02 |

Table S11: GWAS data used for 13 traits in secondary real data analysis.

| Trait Name | ID in TwoSampleMR | Sample Size | Ref. |
|------------|-------------------|-------------|------|
| FP | ebi-a-GCST001212 | 10,701 | [9] |
| Height | ieu-a-89 | 253,288 | [12] |
| HOMA | ebi-a-GCST005180 | 36,466 | [3] |
| LDL | ebi-a-GCST002222 | 94,595 | [11] |
| RA | ebi-a-GCST002318 | 58,284 | [7] |
| SCZ | ieu-b-42 | 77,096 | [8] |
| T2D | ieu-a-26 | 69,033 | [5] |
| ASmk | ieu-a-964 | 47,961 | [4] |
| ANRX | ieu-a-45 | 17,767 | [2] |
| CIQ | ieu-a-16 | 12,441 | [1] |
| ESmk | ieu-a-962 | 74,035 | [4] |
| FSmk | ieu-a-963 | 41,969 | [4] |
| IHC | ieu-a-28 | 10,768 | [10] |
| | | | |

Table S12: Secondary real data analysis, set 1.

| Exp/Out Method | FP/ASmk (6) | FP/ANRX (6) | FP/CIQ (4) | FP/ESmk (6) | FP/FSmk (6) | FP/Height (6) | FP/HOMA (6) | FP/IHC (6) | FP/LDL (5) |
|--------------------|-----------------------|----------------------|----------------------------------|-----------------------|-----------------------|----------------------|----------------------------------|-----------------------|----------------------|
| cML-MA-BIC-Max | 2.3e-01, | 6.1e-01, | 1.9e-01, | 6.7e-01, | 1.1e-01. | 4.3e-02, | 3.7e-08, | 4.5e-01, | 2.0e-01, |
| | -1.9e-02, | 9.0e-02, | -1.3e-01, | -3.5e-02, | 1.1e-01, -1.8e-01, | 4.8e-02, | -2.5e-01, | -7.3e-02, | 4.5e-02, |
| | 1.6e-02 | 1.8e-01 | 1.0e-01 | 8.3e-02 | 1.1e-01 | 2.4e-02 | 4.6e-02 | 9.6e-02 | 3.5e-02 |
| cML-BIC-Max | 2.3e-01, -1.9e-02, | 6.0e-01, | 1.9e-01, | 5.7e-01, | 1.1e-01, -1.8e-01, | 5.1e-02, | 5.4e-11, | 4.4e-01, | 3.5e-01, |
| | -1.9e-02, | 9.3e-02, | -1.3e-01, | -4.5e-02, | -1.8e-01, | 4.0e-02, | -2.8e-01, | -7.4e-02, | 2.6e-02, |
| | 1.6e-02 | 1.8e-01 | 1.0e-01 | 7.8e-02 | 1.1e-01 | 2.1e-02 | 4.2e-02 | 9.6e-02 | 2.7e-02 |
| cML-MA-BIC | 2.3e-01 | 6.2e-01, | 1.9e-01, | 7.9e-01, | 1.1e-01. | 5.2e-02, | 1.1e-08, | 4.5e-01, | 1.3e-01, |
| | -1.9e-02, | 8.9e-02, | -1.3e-01, | -2.3e-02, | -1.8e-01, | 4.2e-02, | -2.6e-01, | -7.3e-02, | 6.2e-02, |
| | 1.6e-02 2.3e-01, | 1.8e-01 | 1.0e-01 | 8.8e-02 | 1.1e-01 1.1e-01, | 2.2e-02 | 4.6e-02 5.4e-11, | 9.6e-02 | 4.1e-02 |
| cML-BIC | 2.3e-01, | 6.0e-01, | 1.9e-01, | 5.7e-01, | 1.1e-01, | 5.1e-02, | 5.4e-11, | 4.4e-01, | 4.3e-02, |
| | -1.9e-02, | 9.3e-02, | -1.3e-01, | -4.5e-02, | -1.8e-01. | 4.0e-02, | -2.8e-01. | -7.4e-02, | 5.9e-02, |
| | 1.6e-02 | 1.8e-01 | 1.0e-01 | 7.8e-02 | 1.1e-01 1.2e-01, | 2.1e-02 | 4.2e-02 4.5e-01, | 9.6e-02 | 2.9e-02 |
| :ML-MA-BIC-DP-Max | 2.5e-01, | 6.9e-01, | 2.2e-01, | 7.8e-01, | 1.2e-01, | 7.8e-02, | 4.5e-01, | 4.5e-01, | 2.9e-01, |
| | -2.0e-02, | 7.6e-02, | -1.3e-01, | -2.8e-02, | -1.8e-01, | 4.5e-02, | -1.3e-01, | -7.8e-02, | 4.9e-02. |
| | -2.0e-02, 1.7e-02 | 1.9e-01 | -1.3e-01, 1.0e-01 | 1.0e-01 | -1.8e-01, 1.2e-01 | 2.6e-02 | -1.3e-01, 1.7e-01 | 1.0e-01 | 4.7e-02 |
| cML-BIC-DP-Max | 2.4e-01, | 6.8e-01, | 2.2e-01, | 5.5e-01, | 1.1e-01, | 8.5e-02, | 3.7e-01. | 4.4e-01, | 2.4e-01, |
| | -2.0e-02, | 7.5e-02, | -1.3e-01, | -5.0e-02. | -1.8e-01, | 4.3e-02, | -1.4e-01, | -7.9e-02, | 5.0e-02, |
| | -2.0e-02, 1.7e-02 | 1.8e-01 | -1.3e-01, 1.0e-01 | 8.3e-02 | -1.8e-01, 1.2e-01 | 2.5e-02 | 1.5e-01 | 1.0e-01 | 4.2e-02 |
| cML-MA-BIC-DP | 2.6e-01, | 6.9e-01, | 2.2e-01, | 9.1e-01, | 1.3e-01, | 9.0e-02, | -1.4e-01, 1.5e-01 4.8e-01, | 4.5e-01, | 2.8e-01, |
| | -2.0e-02, | 7.6e-02, | -1.3e-01, 1.0e-01 2.2e-01, | -1.3e-02, | -1.8e-01. | 4.3e-02, | -1.2e-01. | -7.8e-02, | 6.0e-02, |
| | 1.8e-02 | 1.9e-01 | 1.0e-01 | 1.1e-01 | 1.2e-01 | 2.5e-02 | 1.7e-01 | 1.0e-01 | 5.6e-02 |
| cML-BIC-DP | 2.4e-01, | 6.8e-01, | 2.2e-01, | 9.2e-01, | 1.2e-01 1.1e-01, | 8.5e-02, | 5.5e-01, | 4.4e-01, | 2.4e-01, |
| | -2.0e-02. | 7.5e-02, | -1.3e-01, 1.0e-01 1.7e-01, | 1.2e-02, | -1.8e-01, | 4.3e-02, | -1.1e-01. | -7.9e-02, | 5.0e-02, |
| | 1.7e-02 | 1.8e-01 | 1.0e-01 | 1.2e-01 | -1.8e-01, 1.2e-01 | 2.5e-02 | 1.9e-01 | 1.0e-01 | 4.2e-02 |
| MR-Mix | 1.7e-02 2.0e-01, | 8.0e-01, | 1.7e-01. | 7.8e-01, | 1.1e-01, | 6.8e-02, | 1.9e-01 1.0e-09, | 4.7e-01, | 2.5e-04, |
| | -3.0e-02, | 1.0e-02, | -7.0e-02, | 1.0e-02, | -4.0e-02, | 2.0e-02, | -3.2e-01, | -3.5e-02, | 1.0e-01, |
| | 2.3e-02 | 3.8e-02 | 5.1e-02 | 3.7e-02 | 2.5e-02 | 1.1e-02 | 5.2e-02 | 4.9e-02 | 2.7e-02 |
| MR-ContMix | 2.5e-01, | 6.1e-01, | 2.4e-01, | 5.6e-01, | 1.7e-01, | 1.1e-01, | 1.4e-02, | 4.8e-01, | 2.3e-01, |
| mic commin | -1.7e-02, | 9.5e-02, | -1.3e-01, | 5.0e-02, | -2.1e-01, | 3.8e-02, | -2.7e-01, | -7.7e-02, | 1.4e-01, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 3.7e-01, | 8.0e-01, | 1.9e-01, | 6.7e-01, | 1.1e-01, | 5.0e-02, | 5.8e-02, | 4.4e-01, | 6.8e-01, |
| | -1.5e-02, | -5.3e-02, | -1.3e-01, | -4.4e-02, | -1.8e-01, | 4.0e-02, | -1.5e-01, | -7.4e-02, | 2.4e-02, |
| | 1.7e-02 | 2.1e-01 | 9.9e-02 | 1.0e-01 | 1.1e-01 | 2.1e-02 | 8.1e-02 | 9.6e-02 | 5.9e-02 |
| MR-PRESSO | 1.3e-01, | 5.5e-01, | 1.5e-01, | 6.9e-01, | 9.7e-02, | 8.0e-02, | 5.0e-02, | 1.7e-01, | 3.1e-01, |
| | -1.9e-02, | 9.2e-02, | -1.3e-01, | -4.4e-02, | -1.8e-01, | 4.0e-02, | 5.6e-02, | -7.4e-02, | 5.8e-02, |
| | 1.1e-02 | 1.4e-01 | 6.7e-02 | 1.0e-01 | 8.7e-02 | 1.7e-02 | 4.4e-03 | 4.6e-02 | 4.7e-02 |
| MR-IVW | 2.3e-01, | 6.1e-01, | 1.9e-01, | 6.7e-01, | 1.1e-01, | 7.6e-02, | 7.1e-01, | 4.4e-01, | 6.8e-01, |
| | -1.9e-02, | 9.2e-02, | -1.3e-01, | -4.4e-02, | -1.8e-01, | 6.5e-02, | -3.1e-02, | -7.4e-02, | 2.4e-02, |
| | 1.6e-02 | 1.8e-01 | 9.9e-02 | 1.0e-01 | 1.1e-01 | 3.6e-02 | 8.2e-02 | 9.6e-02 | 5.9e-02 |
| MR-Egger | 4.6e-01, | 8.9e-01, | 9.1e-01, | 1.9e-01, | 9.0e-01, | 7.0e-01, | 1.7e-01, | 9.6e-01, | 9.5e-01, |
| | -2.8e-02, 3.8e-02 | 5.5e-02, | -2.8e-02, 2.4e-01 | -2.9e-01, | 3.2e-02, | -3.0e-02, | 2.1e-01, | 1.2e-02, | -1.1e-02, |
| | 3.8e-02 | 3.9e-01 | 2.4e-01 | 2.2e-01 | 2.5e-01 | 7.8e-02 | 1.6e-01 | 2.2e-01 | 1.7e-01 |
| MR-Weighted-Median | 6.2e-01, | 9.4e-01, | 3.5e-01, | 9.6e-01, | 3.0e-01, | 1.2e-01, | 1.6e-01 6.9e-02, | 6.2e-01, | 4.1e-01, |
| | -9.5e-03, | 1.7e-02, | -1.1e-01, 1.2e-01 | 5.4e-03, | -1.4e-01, 1.3e-01 | 3.8e-02, | 6.8e-02, 3.8e-02 | -5.5e-02, | 2.8e-02, |
| | 1.9e-02 | 2.2e-01 | 1.2e-01 | 1.0e-01 | 1.3e-01 | 2.5e-02 | 3.8e-02 | 1.1e-01 | 3.4e-02 |
| MR-Weighted-Mode | 1.6e-01, | 6.0e-01, | 6.0e-01, | 8.9e-01, | 4.2e-01, | 1.9e-01, | 1.7e-03, | 6.7e-01, | 5.1e-01, |
| = | -3.3e-02, 2.4e-02 | -1.7e-01, | -6.9e-02, 1.3e-01 | 1.7e-02, | -1.2e-01, 1.6e-01 | 3.6e-02, | 9.8e-02, 3.1e-02 | -5.6e-02, | 2.4e-02, |
| | 2.4e-02 | 3.2e-01 | 1.3e-01 | 1.2e-01 | 1.6e-01 | 2.7e-02 | 3.1e-02 | 1.3e-01 | 3.7e-02 |
| MR-RAPS1 | 2.3e-01, | 6.1e-01, | 1.9e-01, | 5.7e-01, | 1.1e-01, | 1.0e-01, | 9.1e-01, | 4.4e-01, | 5.8e-01, |
| | -1.9e-02. | 9.3e-02, | -1.3e-01. | -4.5e-02, | -1.8e-01. | 5.1e-02, | 7.4e-03, | -7.4e-02, | 2.8e-02, |
| | 1.6e-02 | 1.8e-01 | 1.0e-01 | 8.0e-02 | 1.1e-01 | 3.1e-02 | 6.5e-02 | 9.6e-02 | 5.0e-02 |
| MR-RAPS2 | 2.5e-01, | 6.4e-01, | 2.1e-01, | 9.5e-01, | 1.2e-01, | 1.3e-01, | 8.5e-01, | 4.7e-01, | 6.0e-01, |
| | -1.9e-02, | 8.7e-02, | -1.3e-01, | -4.9e-03, | -1.8e-01, | 4.6e-02, | 1.3e-02, | -7.1e-02, | 2.9e-02, |
| | 1.6e-02 | 1.8e-01 | 1.0e-01 | 8.1e-02 | 1.1e-01 | 3.0e-02 | 7.2e-02 | 9.9e-02 | 5.5e-02 |
| MR-RAPS3 | | 6.1e-01, | 1.9e-01, | 5.7e-01, | 1.1e-01, | 1.0e-03, | 1.5e-01, | 4.4e-01, | 3.6e-01, |
| | 2.3e-01, -1.9e-02, | 9.3e-02, | -1.3e-01, | -4.5e-02, | -1.8e-01, | 6.7e-02, | -3.7e-02, | -7.4e-02, | 2.6e-02, |
| | 1.6e-02 2.5e-01, | 1.8e-01 | 1.0e-01 2.1e-01, | 8.0e-02 | 1.1e-01 1.2e-01, | 2.1e-02 | 2.6e-02 3.0e-03, | 9.6e-02 | 2.8e-02 1.0e-01, |
| | | | | | 1.0.01 | | 2.0.02 | | 1 0 01 |
| MR-RAPS4 | 2.5e-01, | 6.4e-01, | 2.1e-01, | 9.5e-01, | 1.2e-01, | 3.8e-02, | 3.0e-03, | 4./e-01, | 1.0e-01, |
| MR-RAPS4 | 2.5e-01, -1.9e-02, | 6.4e-01, 8.7e-02, | 2.1e-01, -1.3e-01, | 9.5e-01, -4.9e-03, | 1.2e-01, -1.8e-01, | 3.8e-02, 4.2e-02, | 3.0e-03, -6.9e-02, | 4.7e-01, -7.1e-02, | 1.0e-01, 4.7e-02, |

Table S13: Secondary real data analysis, set 2.

| Exp/Out Method | FP/RA (6) | FP/SCZ (6) | FP/T2D (6) | Height/ASmk (310) | Height/ESmk (310) | Height/FP (307) | Height/FSmk (310) | Height/HOMA (303) | Height/RA (306) |
|---------------------|-----------------------|----------------------|---------------------------------|----------------------|-----------------------|----------------------|-----------------------|----------------------|----------------------|
| cML-MA-BIC-Max | 5.6e-01, | 8.3e-02, | 2.2e-01, | 5.7e-01, | 1.4e-01 | 3.7e-01, | 7.4e-01 | 2.6e-01, | 1.3e-02 |
| CHILD HILL DIC HALL | -6.8e-02, | -1.2e-01, | -4.9e-01, | 3.0e-03, | 1.4e-01, -4.0e-02, | 1.4e-02, | 7.4e-01, -1.2e-02, | -8.3e-03, | 1.3e-02, 8.1e-02, |
| | 1.2e-01 | 6.7e-02 | 4.0e-01 | 5.2e-03 | 2.7e-02 | 1.6e-02 | 3.6e-02 | 7.4e-03 | 3.3e-02 |
| cML-BIC-Max | 2.7e-01 | 8.6e-02, | 3.3e-05, | 6.5e-01, | 1.20-01 | 3.4e-01, | 8.5e-01 | 2.4e-01, | 1.3e-02, |
| CIVIL-DIC-IVIAX | 2.7e-01, -1.1e-01, | -1.1e-01, | -6.8e-01, | 2.3e-03, | 1.2e-01, -4.1e-02, | 1.5e-02, | 8.5e-01, -6.9e-03, | -8.6e-03, | 8.1e-02, |
| | 9.9e-02 | 6.6e-02 | 1.6e-01 | 5.0e-03 | 2.6e-02 | 1.6e-02 | 3.6e-02 | 7.3e-03 | 3.2e-02 |
| cML-MA-BIC | 7.7e-01, | 8.0e-02, | 6.9e-01, | 5.0e-01, | 1.2e-01, | 4.7e-01, | 6.4e-01, | 2.8e-01, | 1.1e-02, |
| CIVIL-IVIA-BIC | -3.7e-02, | -1.2e-01, | -2.8e-01, | 3.6e-03, | -4.1e-02, | 1.1e-02, | -1.7e-02, | -8.1e-03, | 8.6e-02, |
| | 1.20.01 | 6.8e-02 | 7.00.01 | 5.3e-03 | 2.70.02 | 1.6e-02 | 2 60 02 | 7.4e-03 | 3.40.02 |
| cML-BIC | 1.2e-01 2.7e-01, | 8.6e-02, | 7.0e-01 3.3e-05, | 6.5e-01, | 2.7e-02 1.2e-01, | 4.9e-01, | 3.6e-02 5.9e-01, | 3.1e-01, | 3.4e-02 8.6e-03, |
| CIVIL-DIC | -1.1e-01, | -1.1e-01, | -6.8e-01, | 2.3e-03, | -4.1e-02, | 1.1e-02, | -1.9e-02, | -7.5e-03, | 8.5e-02, |
| | 9.9e-02 | 6.6e-02 | -0.8e-01, | 5.0e-03 | -4.1e-02, | | -1.96-02, | 7.4e-03 | 3.2e-02, |
| M. MA DIC DD M | 9.9e-02 | | 1.6e-01 8.2e-01, | | 2.6e-02 1.9e-01, | 1.6e-02 | 3.6e-02 7.1e-01, | | 3.2e-02 |
| ML-MA-BIC-DP-Max | 6.3e-01, | 9.1e-02, | 8.2e-01, | 6.0e-01, | 1.9e-01, | 4.0e-01, | /.1e-01, | 4.6e-01, | 2.8e-02, |
| | -7.5e-02, 1.6e-01 | -1.2e-01, | 2.2e-01, 9.6e-01 | 3.0e-03, | -3.9e-02, 3.0e-02 | 1.4e-02, | -1.5e-02, 3.9e-02 | -6.6e-03, | 9.7e-02, |
| | 1.6e-01 | 7.3e-02 | 9.6e-01 | 5.8e-03 | 3.0e-02 | 1.6e-02 | 3.9e-02 | 9.0e-03 | 4.4e-02 |
| cML-BIC-DP-Max | 8.3e-01, | 7.7e-02, | 8.2e-01, | 6.8e-01, | 1.5e-01, | 3.8e-01, | 6.1e-01, | 5.6e-01, | 2.1e-02, |
| | -3.7e-02, | -1.2e-01, | 2.1e-01, 9.1e-01 | 2.3e-03, | -4.3e-02, 2.9e-02 | 1.4e-02, | -2.0e-02, 3.8e-02 | -5.2e-03, | 9.7e-02, |
| | 1.8e-01 | 6.8e-02 | 9.1e-01 | 5.5e-03 | 2.9e-02 | 1.5e-02 | 3.8e-02 | 9.0e-03 | 4.2e-02 |
| cML-MA-BIC-DP | 7.5e-01, | 1.1e-01, | 8.2e-01, | 5.6e-01, | 2.3e-01, | 5.4e-01, | 8.2e-01, | 5.4e-01, | 3.1e-02, |
| | -5.6e-02, | -1.3e-01, | 2.3e-01, | 3.5e-03, | -3.7e-02, | 1.2e-02, | -9.9e-03, | -5.5e-03, | 1.0e-01, |
| | 1.8e-01 | 7.9e-02 | 1.0e+00 | 6.0e-03 | 3.1e-02 2.1e-01, | 1.9e-02 | 4.3e-02 | 9.1e-03 | 4.7e-02 |
| cML-BIC-DP | 8.3e-01, | 7.7e-02, | 8.2e-01, | 5.3e-01, | 2.1e-01, | 5.9e-01, | 8.3e-01, | 5.6e-01, | 4.8e-02, |
| | -3.7e-02, | -1.2e-01, | 2.1e-01, 9.1e-01 3.4e-02, | 3.7e-03, | -3.8e-02, 3.0e-02 | 1.1e-02, | -9.7e-03. | -5.2e-03, | 9.8e-02, |
| | 1.8e-01 | 6.8e-02 | 9.1e-01 | 6.0e-03 | 3.0e-02 | 2.0e-02 | 4.5e-02 | 9.0e-03 | 5.0e-02 |
| MR-Mix | 1.8e-01 3.3e-01, | 6.6e-01, | 3.4e-02. | 8.0e-01, | 1.1e-01, | 8.5e-01, | 4.5e-02 3.1e-01, | 6.4e-01, | 2.6e-01, |
| | 4.0e-02, | -7.0e-02, | -1.3e-01, | 5.0e-02, | -4.0e-02, | -8.0e-02, | -3.0e-02, | 6.0e-02, | 3.0e-02, |
| | 4.1e-02 | 1.6e-01 | 6.1e-02 | 2.0e-01 | 2.5e-02 | 4.3e-01 | 3.0e-02 | 1.3e-01 | 2.7e-02 |
| MR-ContMix | 2.1e-01, | 3.4e-02, | 4.0e-02, | 6.1e-01, | 8.4e-01, | 2.9e-01, | 8.5e-01 | 8.2e-01, | 2.7e-03, |
| WIK-COIIIWIIX | 1.8e-01, | -1.5e-01, | -9.1e-01, | 2.2e-03, | 9.3e-03, | 2.8e-02, | 8.5e-01, 1.3e-02, | -7.9e-03, | 2.0e-01, |
| | NA | NA | NA | NA | NA | NA | NA | NA I | NA |
| MR-Lasso | 5.6e-01, | 1.8e-01, | 2.1e-01, 7.6e-01, | 3.3e-01, | 9.3e-02, | 4.9e-01, | 6.0e-01, | 4.7e-01, | 1.6e-05, |
| | -1.0e-01, | -1.1e-01, | 7.6e-01, | 5.0e-03, | -4.4e-02, | 1.1e-02, | -1.9e-02. | -5.4e-03, | 1.5e-01, |
| | 1.8e-01 | 8.4e-02 | 6.0e-01 | 5.1e-03 | 2.6e-02 | 1.6e-02 | 3.6e-02 | 7.5e-03 | 3.4e-02 |
| MR-PRESSO | 8.8e-01, | 2.4e-01, | 4.2e-01, | 6.6e-01, | 3.0e-01, | 3.6e-01, | 6.1e-01, | 3.1e-01, | 3.1e-02, |
| | 2.4e-02, | -1.1e-01, | 6.5e-01, | 2.2e-03, | -2.8e-02, | 1.5e-02, | -1.9e-02, | -8.4e-03, | 8.6e-02, |
| | 1.5e-01 | 8.4e-02 | 5.1e-01 | 5.0e-03 | 2.7e-02 | 1.6e-02 | 3.7e-02 | 8.3e-03 | 4.0e-02 |
| MR-IVW | 5.6e-01, | 1.8e-01, | 4.2e-01, | 6.6e-01, | 3.0e-01, | 3.6e-01, | 8.6e-01, | 3.1e-01, | 1.9e-02, |
| IVIIX-I V VV | -1.0e-01, | -1.1e-01, | 7.7e-01, | 2.2e-03, | -2.8e-02, | 1.5e-02, | -6.8e-03, | -8.4e-03, | 1.1e-01, |
| | 1.8e-01 | 8.4e-02 | 9.6e-01 | 5.0e-03 | 2.7e-02 | 1.6e-02 | 3.8e-02 | 8.3e-03 | 4.7e-02 |
| MR-Egger | 5.7e-01, | 4.0e-01, | 6.8e-01, | 6.5e-01, | 9.1e-01, | 9.3e-01, | 4.3e-01, | 2.8e-01, | 1.7e-02 |
| MR-Egger | 2.3e-01, | | 0.86-01, | | | | | | |
| | 2.3e-01, 4.0e-01 | -1.7e-01, | -9.3e-01, 2.2e+00 | 6.1e-03, 1.3e-02 | -7.7e-03, 7.2e-02 | -3.7e-03, 4.3e-02 | -8.1e-02, | -2.4e-02, | 1.6e-01, 1.2e-01 |
| | | 2.0e-01 | 2.2e+00 | | | | 1.0e-01 | 2.3e-02 | |
| MR-Weighted-Median | 3.9e-01, | 3.2e-02, | 5.9e-03, | 1.0e+00, | 6.9e-01, | 4.3e-01, | 1.0e+00, | 5.7e-01, | 4.8e-01, |
| | 1.2e-01, | -1.8e-01, | -7.5e-01, 2.7e-01 | 0.0e+00, | -1.7e-02, 4.1e-02 | 1.9e-02, | 9.2e-05, 5.8e-02 | -6.6e-03, | 4.0e-02, |
| | 1.4e-01 | 8.3e-02 | 2.7e-01 | 8.1e-03 | 4.1e-02 | 2.4e-02 | 5.8e-02 | 1.2e-02 | 5.7e-02 |
| MR-Weighted-Mode | 4.1e-01, | 1.1e-01, | 1.6e-02, | 6.1e-01, | 9.7e-01, | 8.0e-01, | 6.9e-01, | 5.5e-01, | 6.7e-02, |
| | 1.2e-01, 1.5e-01 | -1.6e-01, | -4.3e-01, 1.8e-01 | -1.2e-02, | -3.1e-03, 7.8e-02 | 1.3e-02, | 4.8e-02, 1.2e-01 | 1.5e-02, | 1.8e-01, |
| | 1.5e-01 | 1.0e-01 | 1.8e-01 | 2.3e-02 | 7.8e-02 | 5.3e-02 | 1.2e-01 | 2.6e-02 | 9.6e-02 |
| MR-RAPS1 | 8.1e-01, | 1.4e-01, | 5.6e-01, | 6.5e-01, | 3.0e-01, | 3.6e-01, | 8.6e-01, | 2.9e-01, | 1.3e-02, |
| | -3.6e-02. | -1.1e-01, | 4.1e-01. | 2.3e-03, | -2.9e-02. | 1.5e-02, | -6.8e-03. | -8.7e-03, | 1.2e-01, |
| | 1.5e-01 | 7.7e-02 | 7.0e-01 | 5.2e-03 | 2.8e-02 | 1.6e-02 | 3.8e-02 | 8.2e-03 | 4.8e-02 |
| MR-RAPS2 | 9.4e-01, | 1.3e-01, | 6.9e-01, | 4.6e-01, | 2.0e-01, | 4.3e-01, | 8.1e-01, | 4.4e-01, | 3.1e-02, |
| | -1.2e-02, | -1.2e-01, | 2.9e-01, | 3.9e-03, | -3.6e-02, | 1.3e-02, | -9.1e-03, | -6.4e-03, | 9.4e-02, |
| | 1.6e-01 | 8.1e-02 | 7.1e-01 | 5.3e-03 | 2.8e-02 | 1.6e-02 | 3.8e-02 | 8.3e-03 | 4.4e-02 |
| MR-RAPS3 | | 9.1e-02, | 6.8e-10, | 6.5e-01, | 2.8e-01, | 3.5e-01, | 8.5e-01, | 2.5e-01, | 5.1e-04, |
| THE REAL OF | 2.7e-01, -1.1e-01, | -1.1e-01, | 2.1e+00, | 2.3e-03, | -2.8e-02, | 1.5e-02, | -6.9e-03, | -8.6e-03, | 1.1e-04, |
| | 1.10 01, 1.0e-01 | 6.7e-02 | 3.4e_01 | 5.1e-03 | 2.6c-02, | 1.6e-02 | 3.6e-02 | 7.4e-03 | 3.2e-02 |
| MR-RAPS4 | 1.0e-01 9.6e-01, | 6.0e-02, | 3.4e-01 3.8e-02, | 4.4e-01, | 2.6e-02 1.9e-01, | 4.3e-01, | 3.6e-02 7.9e-01, | 7.4e-03 4.2e-01, | 3.2e-02 9.2e-04, |
| WIK-KAP34 | 5.00-U1, | | 3.66-02, | | 1.96-01, | | -9.6e-03, | 4.26-01, | 7.20-04, 1.1 a 01 |
| | -5.1e-03, 1.0e-01 | -1.3e-01, 6.9e-02 | 2.6e-01, 1.3e-01 | 4.0e-03, 5.2e-03 | -3.6e-02, 2.7e-02 | 1.3e-02, 1.6e-02 | -9.6e-03, 3.7e-02 | -6.1e-03, 7.6e-03 | 1.1e-01, 3.3e-02 |
| | | | | | | | | | |

Table S14: Secondary real data analysis, set 3.

| Exp/Out Method | Height/SCZ | Height/T2D | HOMA/ASmk | HOMA/ESmk | HOMA/FP | HOMA/FSmk | HOMA/Height | HOMA/IHC | HOMA/LD |
|--------------------|-----------------------|---------------------|----------------------|---------------------|---------------------|---------------------|----------------------|---------------------|----------------------|
| | (288) | (307) | (2) | (2) | (2) | (2) | (2) | (2) | (2) |
| cML-MA-BIC-Max | 1.3e-01, | 7.8e-01, | 3.3e-01, | 6.8e-01, | 1.6e-01, | 2.3e-02, | 3.3e-02, | 1.8e-01, | 7.7e-01, |
| | -3.8e-02, | -1.1e-02, | -5.3e-02, | 1.2e-01, | 2.4e-01, | 8.8e-01, | -1.6e-01, | 4.6e-01, | -2.8e-02, |
| | 2.5e-02 | 4.0e-02 | 5.5e-02 | 2.8e-01 | 1.7e-01 | 3.9e-01 | 7.3e-02 3.3e-02, | 3.4e-01 | 9.5e-02 |
| cML-BIC-Max | 1.1e-01, | 9.7e-01, | 3.3e-01, | 6.8e-01, | 1.6e-01, | 2.3e-02, | 3.3e-02, | 1.8e-01, | 7.7e-01, |
| | -3.9e-02, | -1.7e-03, | -5.3e-02, 5.5e-02 | 1.2e-01, | 2.4e-01, | 8.8e-01, | -1.6e-01, | 4.6e-01, | -2.8e-02, |
| | 2.5e-02 | 4.0e-02 | 5.5e-02 | 2.8e-01 | 1.7e-01 | 3.9e-01 | 7.3e-02 | 3.4e-01 | 9.5e-02 |
| cML-MA-BIC | 1.4e-01, | 7.4e-01, | 3.3e-01, | 6.8e-01, | 1.6e-01, | 2.3e-02, | 3.3e-02, | 1.8e-01, | 7.7e-01, |
| | -3.7e-02, | -1.4e-02, | -5.3e-02, | 1.2e-01, | 2.4e-01, | 8.8e-01, | -1.6e-01, | 4.6e-01, | -2.8e-02, |
| | 2.5e-02 | 4.1e-02 | 5.5e-02 | 2.8e-01 | 1.7e-01 | 3.9e-01 | 7.3e-02 3.3e-02, | 3.4e-01 | 9.5e-02 |
| cML-BIC | 9.3e-02, | 5.8e-01, | 3.3e-01, | 6.8e-01, | 1.6e-01, | 2.3e-02, | 3.3e-02, | 1.8e-01, | 7.7e-01, |
| | -4.1e-02, | -2.2e-02, | -5.3e-02. | 1.2e-01, | 2.4e-01. | 8.8e-01, | -1.6e-01. | 4.6e-01, | -2.8e-02, |
| | 2.5e-02 | 4.0e-02 | 5.5e-02 | 2.8e-01 | 1.7e-01 2.1e-01, | 3.9e-01 | 7.3e-02 7.1e-02, | 3.4e-01 | 9.5e-02 |
| ML-MA-BIC-DP-Max | 3.9e-01, | 9.2e-01, | 4.3e-01, | 6.8e-01, | 2.1e-01, | 4.8e-02, | 7.1e-02, | 2.3e-01, | 8.3e-01, |
| | -3.3e-02, | 5.0e-03, | -5.0e-02, | 1.3e-01, | 2.5e-01, | 9.1e-01, | -1.5e-01, | 4.8e-01, | -2.5e-02, |
| | 3.8e-02 | 5.0e-02 | 6.4e-02 | 3.2e-01 | 2.0e-01 | 4.6e-01 | 8.5e-02 | 4.1e-01 | 1.1e-01 |
| cML-BIC-DP-Max | 4.3e-01, | 9.2e-01, | 4.3e-01, | 6.8e-01, | 2.1e-01, | 4.8e-02, | 7.1e-02, | 2.3e-01, | 8.3e-01, |
| DIO DI MMA | -3.1e-02, | 5.1e-03, | -5.0e-02 | 1.3e-01, | 2.5e-01, | 9.1e-01, | -1.5e-01, | 4.8e-01, | -2.5e-02, |
| | 3.9e-02 | 4.9e-02 | -5.0e-02, 6.4e-02 | 3.2e-01 | 2.0e-01 | 4.6e-01 | 8.5e-02 | 4.1e-01 | 1.1e-01 |
| cML-MA-BIC-DP | 3.7e-02 | 9.3e-01, | 4.3e-01, | 6.8e-01, | 2.1e-01, | 4.8e-02, | 7.1e-02, | 2.3e-01, | 8.3e-01, |
| CML-MA-BIC-DF | | | | | | 4.0C-02, | | | |
| | -3.7e-02, 4.1e-02 | 4.7e-03, 5.3e-02 | -5.0e-02, 6.4e-02 | 1.3e-01, 3.2e-01 | 2.5e-01, 2.0e-01 | 9.1e-01, 4.6e-01 | -1.5e-01, 8.5e-02 | 4.8e-01, 4.1e-01 | -2.5e-02, 1.1e-01 |
| M. DIG DD | | | 0.46-02 | | 2.06-01 | | 8.36-02 | | |
| cML-BIC-DP | 3.2e-01, | 9.2e-01, | 4.3e-01, | 6.8e-01, | 2.1e-01, | 4.8e-02, | 7.1e-02, | 2.3e-01, | 8.3e-01, |
| | -4.2e-02, | 5.1e-03, | -5.0e-02, | 1.3e-01, | 2.5e-01, | 9.1e-01, | -1.5e-01, | 4.8e-01, | -2.5e-02, |
| | 4.2e-02 | 4.9e-02 | 6.4e-02 | 3.2e-01 NA | 2.0e-01 | 4.6e-01 NA | 8.5e-02 | 4.1e-01 | 1.1e-01 |
| MR-Mix | 7.1e-01, | 7.0e-01, | NA | NA | NA | NA NA | NA | NA | NA |
| | -7.0e-02, | 4.0e-02, | | | | | | | |
| | 1.9e-01 | 1.1e-01 | | | | | | | |
| MR-ContMix | 2.8e-02, | 6.7e-01, | NA | NA | NA | NA | NA | NA | NA |
| | -1.0e-01, | 3.4e-02, | | | | | | | |
| | NA | NA | | | | | | | |
| MR-Lasso | 3.7e-02, | 9.3e-01, | NA | NA | NA | NA | NA | NA | NA |
| | -5.6e-02, | 4.0e-03, | | | | | | | |
| | 2.7e-02 | 4.3e-02 | | | | | | | |
| MR-PRESSO | 4.5e-01, | 7.6e-01, | NA | NA | NA | NA | NA | NA | NA |
| MR TRESSO | -2.5e-02, | -1.5e-02, | | | | 1 | 1 | 1111 | 1 |
| | 3.3e-02 | 4.9e-02 | | | | | | | |
| MR-IVW | 4.3e-01, | 1.0e+00, | NA | NA | NA | NA | NA | NA | NA |
| IVIK-I V VV | -3.0e-02, | 8.5e-05, | INA | INA | INA | INA | INA | INA | INA |
| | | | | | | | | | |
|) (D. E. | 3.7e-02 | 5.1e-02 | 27.6 | N/A | 27.4 | N/A | N/A | 27.4 | NT. |
| MR-Egger | 9.2e-01, | 3.1e-01, | NA | NA | NA | NA | NA | NA | NA |
| | 9.6e-03, | 1.4e-01, | | | | | | | 1 |
| | 1.0e-01 | 1.4e-01 | | | | | | | |
| MR-Weighted-Median | 4.1e-01, | 1.0e+00, | NA | NA | NA | NA | NA | NA | NA |
| | -3.5e-02, | 0.0e+00, | | | | | | | |
| | 4.3e-02 | 6.5e-02 | | | | | | | |
| MR-Weighted-Mode | 9.8e-01, | 9.8e-01, | NA | NA | NA | NA | NA | NA | NA |
| | 2.6e-03. | 3.9e-03, | | | | | | | |
| | 1.0e-01 | 1.9e-01 | | | | | | | |
| MR-RAPS1 | 3.5e-01, -3.5e-02, | 9.9e-01, | NA | NA | NA | NA | NA | NA | NA |
| ** | -3.5e-02, | -7.7e-04, | | | | | | | |
| | 3.7e-02 | 5.2e-02 | | | | | | | 1 |
| MR-RAPS2 | 3.3e-01, | 8.8e-01, | NA | NA | NA | NA | NA | NA | NA |
| 11.02 | -3.6e-02, | 8.1e-03, | | 1 | | 1 | - " - | - *** | 1 |
| | 3.7e-02 | 5.2e-02 | | | | | | | 1 |
| MR-RAPS3 | 2.1e-01, | | NA | NA | NA | NA | NA | NA | NA |
| MK-KAPS3 | | 1.0e+00, | INA | NA. | INA | INA. | INA | INA | INA |
| | -3.0e-02, | 8.7e-05, | | | | | | | 1 |
| | 2.4e-02 | 4.0e-02 | | | 27.1 | 1 | 27. | 37. | 1 |
| MR-RAPS4 | 1.5e-01, | 8.4e-01, | NA | NA | NA | NA | NA | NA | NA |
| | -3.6e-02, | 8.2e-03, | | | | | | | 1 |
| | 2.5e-02 | 4.1e-02 | 1 | 1 | | | | | |

Table S15: Secondary real data analysis, set 4.

| Exp/Out Method | HOMA/RA | HOMA/SCZ | HOMA/T2D | LDL/ASmk | LDL/ANRX | LDL/ESmk | LDL/FP (68) | LDL/FSmk | LDL/HOM/ |
|--------------------|---------------------|----------|---------------------|-----------|----------------------|-----------|-----------------------|----------|----------------------|
| - | (2) | (2) | (2) | (69) | (52) | (69) | 11.00 | (69) | (68) |
| cML-MA-BIC-Max | 3.8e-01, | 2.9e-01, | 3.8e-01, | 1.9e-01, | 5.3e-02, 1.6e-01, | 4.1e-01, | 1.1e-02, | 1.6e-01, | 8.1e-01, 2.3e-03, |
| | 3.4e-01, 3.9e-01 | 2.7e-01, | 3.5e-01, 4.0e-01 | -8.4e-03, | 1.0e-01, | -2.8e-02, | -5.3e-02, 2.1e-02 | 6.5e-02, | 9.4e-03 |
| \m nrg.1/ | 3.9e-01 | 2.6e-01 | 4.0e-01 | 6.5e-03 | 8.1e-02 | 3.4e-02 | 2.1e-02 | 4.6e-02 | 9.4e-03 |
| cML-BIC-Max | 3.8e-01, | 2.9e-01, | 3.8e-01, | 1.9e-01, | 5.2e-02, | 3.0e-01, | 1.1e-02, | 1.8e-01, | 8.2e-01, |
| | 3.4e-01, 3.9e-01 | 2.7e-01, | 3.5e-01, 4.0e-01 | -8.5e-03, | 1.6e-01, 8.1e-02 | -3.4e-02, | -5.3e-02, 2.1e-02 | 6.1e-02, | 2.0e-03, 9.2e-03 |
| M. M. DIG | 3.96-01 | 2.6e-01 | 4.0e-01 | 6.4e-03 | 8.1e-02 | 3.3e-02 | 2.1e-02 | 4.6e-02 | |
| cML-MA-BIC | 3.8e-01, | 2.9e-01, | 3.8e-01, | 1.9e-01, | 5.5e-02, | 4.2e-01, | 1.2e-02, | 1.5e-01, | 7.6e-01, |
| | 3.4e-01, | 2.7e-01, | 3.5e-01, | -8.4e-03, | 1.6e-01, | -2.7e-02, | -5.3e-02, | 6.6e-02, | 2.9e-03, |
| M. DIC | 3.9e-01 | 2.6e-01 | 4.0e-01 | 6.5e-03 | 8.1e-02 5.2e-02, | 3.4e-02 | 2.1e-02 | 4.6e-02 | 9.4e-03 |
| cML-BIC | 3.8e-01, | 2.9e-01, | 3.8e-01, | 1.9e-01, | 5.2e-02, | 4.8e-01, | 1.1e-02, | 1.8e-01, | 8.2e-01, |
| | 3.4e-01, | 2.7e-01, | 3.5e-01, | -8.5e-03, | 1.6e-01, | -2.4e-02, | -5.3e-02, | 6.1e-02, | 2.0e-03, |
| 10 11 DIG DD 11 | 3.9e-01 4.3e-01, | 2.6e-01 | 4.0e-01 4.2e-01, | 6.4e-03 | 8.1e-02 8.8e-02, | 3.3e-02 | 2.1e-02 1.9e-02, | 4.6e-02 | 9.2e-03 |
| cML-MA-BIC-DP-Max | 4.3e-01, | 3.4e-01, | 4.2e-01, | 2.9e-01, | 8.8e-02, | 6.5e-01, | 1.9e-02, | 1.3e-01, | 8.2e-01, |
| | 3.6e-01, | 2.9e-01, | 3.8e-01, | -7.9e-03, | 1.6e-01, | -1.7e-02, | -5.4e-02, | 7.3e-02, | 2.5e-03, |
| | 4.6e-01 | 3.0e-01 | 4.7e-01 | 7.5e-03 | 9.3e-02 | 3.7e-02 | 2.3e-02 | 4.9e-02 | 1.1e-02 |
| cML-BIC-DP-Max | 4.3e-01, | 3.4e-01, | 4.2e-01, | 3.4e-01, | 6.9e-02, | 7.2e-01, | 1.8e-02, | 1.3e-01, | 9.3e-01, |
| | 3.6e-01, 4.6e-01 | 2.9e-01, | 3.8e-01, | -7.5e-03, | 1.6e-01, | -1.4e-02, | -5.4e-02, 2.3e-02 | 7.3e-02, | 9.8e-04, |
| | 4.6e-01 | 3.0e-01 | 4.7e-01 4.2e-01, | 7.9e-03 | 8.9e-02 | 3.9e-02 | 2.3e-02 | 4.8e-02 | 1.1e-02 |
| cML-MA-BIC-DP | 4.3e-01, | 3.4e-01, | 4.2e-01, | 3.2e-01, | 1.2e-01, | 6.6e-01, | 2.1e-02, | 1.3e-01, | 7.5e-01, |
| | 3.6e-01, 4.6e-01 | 2.9e-01, | 3.8e-01, 4.7e-01 | -7.6e-03, | 1.6e-01, 9.9e-02 | -1.7e-02, | -5.5e-02, | 7.4e-02, | 3.4e-03, |
| | 4.6e-01 | 3.0e-01 | 4.7e-01 | 7.7e-03 | 9.9e-02 | 3.8e-02 | 2.4e-02 | 4.9e-02 | 1.1e-02 |
| cML-BIC-DP | 4.3e-01, | 3.4e-01, | 4.2e-01, | 3.4e-01, | 1.3e-01, | 7.2e-01, | 2.0e-02, | 1.3e-01, | 7.1e-01, |
| | 3.6e-01, | 2.9e-01, | 3.8e-01, | -7.5e-03, | 1.6e-01, | -1.4e-02, | -5.5e-02, | 7.3e-02, | 4.2e-03, |
| | 4.6e-01 | 3.0e-01 | 4.7e-01 | 7.9e-03 | 1.0e-01 | 3.9e-02 | 2.4e-02 | 4.8e-02 | 1.1e-02 |
| MR-Mix | NA | NA | NA | 3.1e-01, | 1.0e-01 5.1e-02, | 5.2e-01, | 2.4e-02 2.9e-01, | 3.4e-01, | 1.0e-01, |
| | | | | -1.5e-02, | 3.9e-01, | 1.0e-02, | -7.0e-02, | 2.0e-02, | 3.0e-02, |
| | | | | 1.5e-02 | 2.0e-01 | 1.6e-02 | 6.6e-02 | 2.1e-02 | 1.8e-02 |
| MR-ContMix | NA | NA | NA | 4.4e-01, | 8.9e-02, | 9.9e-01, | 7.9e-03, | 1.0e-01, | 3.8e-01, |
| | | | | -7.1e-03, | 1.6e-01, | -8.4e-05, | -6.5e-02, | 1.1e-01, | 6.9e-03, |
| | | | | NA | NA | NA | NA | NA | NA |
| MR-Lasso | NA | NA | NA | 2.5e-01, | 1.0e-01, | 5.2e-01, | 3.9e-03, -6.0e-02, | 9.1e-02, | 5.5e-01, |
| | | | | -7.4e-03, | 1.4e-01, | -2.3e-02, | -6.0e-02, | 7.7e-02, | 5.5e-03, |
| | | | | 6.4e-03 | 8.9e-02 | 3.6e-02 | 2.1e-02 | 4.6e-02 | 9.3e-03 |
| MR-PRESSO | NA | NA | NA | 1.4e-01, | 9.2e-02, | 3.8e-01, | 4.0e-03, | 1.8e-01, | 8.0e-01, |
| | | | | -8.5e-03, | 1.6e-01, | -3.4e-02, | -6.0e-02, | 6.1e-02, | -2.9e-03, |
| | | | | 5.7e-03 | 9.2e-02 | 3.8e-02 | 2.0e-02 | 4.5e-02 | 1.2e-02 |
| MR-IVW | NA | NA | NA | 1.9e-01, | 8.6e-02, | 3.8e-01, | 3.9e-03, | 1.8e-01, | 8.0e-01, |
| | | | | -8.5e-03, | 1.6e-01, | -3.4e-02, | -6.0e-02, | 6.1e-02, | -2.9e-03, |
| | | | | 6.4e-03 | 9.2e-02 | 3.8e-02 | 2.1e-02 | 4.5e-02 | 1.2e-02 |
| MR-Egger | NA | NA | NA | 3.7e-01, | 4.3e-01, | 6.5e-01, | 3.0e-01, | 3.4e-01, | 6.3e-01, |
| | | | | 9.8e-03, | 1 1e-01 | -2.9e-02. | -3.8e-02, 3.6e-02 | 7.4e-02, | -9.7e-03. |
| | | | | 1.1e-02 | 1.4e-01 | 6.4e-02 | 3.6e-02 | 7.7e-02 | 2.0e-02 |
| MR-Weighted-Median | NA | NA | NA | 6.9e-01, | 1.8e-01, | 2.0e-01, | 9.3e-02, | 3.1e-01, | 8.1e-01, |
| Ü | | | | 4.3e-03, | 1.6e-01. | -6.6e-02, | -5.3e-02. | 6.9e-02, | 3.3e-03, |
| | | | | 1.1e-02 | 1.2e-01 | 5.2e-02 | 3.2e-02 | 6.7e-02 | 1.4e-02 |
| MR-Weighted-Mode | NA | NA | NA | 3.6e-01, | 1.5e-01, | 2.1e-01, | 1.3e-01, | 2.4e-01, | 8.3e-01, |
| | | | | 1.0e-02, | 1.5e-01, | -5.6e-02, | -4.8e-02. | 7.7e-02, | 2.7e-03, |
| | | | | 1.1e-02 | 1.0e-01 | 4.5e-02 | 3.1e-02 | 6.5e-02 | 1.3e-02 |
| MR-RAPS1 | NA | NA | NA | 1.9e-01, | 7.2e-02, | 3.6e-01, | 3.9e-03, | 1.9e-01, | 6.7e-01, |
| * | 1 | | | -8.5e-03, | 1.6e-01, | -3.5e-02, | -6.0e-02, | 6.2e-02, | -4.9e-03, |
| | | | | 6.5e-03 | 8.8e-02 | 3.8e-02 | 2.1e-02 | 4.8e-02 | 1.1e-02 |
| MR-RAPS2 | NA | NA | NA | 2.5e-01, | 1.0e-01, | 5.6e-01, | 1.2e-02, | 1.3e-01, | 9.5e-01, |
| | | | | -7.7e-03, | 1.5e-01, | -2.2e-02, | -5.4e-02, | 7.3e-02, | 7.2e-04, |
| | | | | 6.6e-03 | 9.4e-02 | 3.9e-02 | 2.1e-02 | 4.8e-02 | 1.1e-02 |
| MR-RAPS3 | NA | NA | NA | 1.9e-01, | 5.3e-02, | 3.1e-01, | 3.9e-03, | 1.8e-01, | 7.5e-01, |
| MIC IOI 05 | | . 1/1 | | -8.5e-03, | 1.6e-01, | -3.4e-02, | -6.0e-02, | 6.1e-02, | -3.0e-03, |
| | | | | 6.5e-03 | 8.2e-02 | 3.3e-02 | 2.1e-02 | 4.6e-02 | 9.2e-03 |
| MR-RAPS4 | NA | NA | NA | 2.5e-01, | 6.3e-02, | 5.9e-01, | 1.2e-02, | 1.2e-01, | 6.4e-01, |
| MIN IN I OT | 11/1 | 11/1 | 11/1 | -7.7e-03, | 1.6e-01, | -1.8e-02, | -5.4e-02, | 7.3e-02, | 4.4e-03, |
| | 1 | | | 6.6e-03 | 8.4e-02 | 3.4e-02 | 2.1e-02 | 4.7e-02 | 9.4e-03 |
| | 1 | 1 | 1 | 0.00-03 | 0.46-02 | J.4C-UZ | L.1C-UZ | H./C-UZ | 1 7.4C-U3 |

Table S16: Secondary real data analysis, set 5.

| Exp/Out Method | LDL/IHC (67) | LDL/RA (71) | LDL/SCZ (69) | LDL/T2D (67) | RA/SCZ (47) | SCZ/ASmk (35) | SCZ/CIQ (20) | SCZ/FP (34) | SCZ/FSmk |
|----------------------|-----------------------|-----------------------|---|-----------------------|----------------------|-----------------------|----------------------------------|-----------------------|----------------------|
| cML-MA-BIC-Max | | | | | 1.6.01 | | | 60.01 | 6.9e-01, |
| CML-MA-BIC-Max | 4.7e-01, -2.8e-02, | 7.9e-01, -9.9e-03, | 7.6e-01, -8.7e-03, | 1.2e-03, -1.7e-01, | 1.6e-01, 1.8e-02, | 5.0e-01, -3.8e-03, | 4.6e-01, -3.1e-02, | 6.0e-01, -9.7e-03, | -1.6e-02, |
| | 3.9e-02 | | 2.8e-02 | | 1.3e-02, 1.3e-02 | 5.6e-03 | 4.3e-02 | 1.9e-02 | 4.2e-02 |
| M. DICM | 5.9e-02 | 3.7e-02 | 2.8e-02 | 5.3e-02 | 1.3e-02 | | 4.3e-02 | | 4.2e-02 |
| cML-BIC-Max | 5.0e-01, -2.6e-02, | 8.2e-01, | 7.7e-01, -8.2e-03, | 1.9e-03, | 2.0e-01, 1.6e-02, | 5.1e-01, | 4.4e-01, -3.3e-02, | 5.1e-01, | 7.8e-01, |
| | -2.6e-02, | -8.6e-03, | -8.2e-03, | -1.6e-01, | 1.6e-02, | -3.7e-03, | -3.3e-02, | -1.2e-02, | -1.1e-02, |
| | 3.8e-02 | 3.7e-02 | 2.8e-02 | 5.0e-02 | 1.2e-02 | 5.6e-03 | 4.2e-02 | 1.8e-02 | 3.9e-02 |
| cML-MA-BIC | 4.8e-01, | 7.8e-01, | 7.6e-01, | 1.1e-03, | 1.6e-01, | 5.0e-01, | 5.0e-01, | 5.0e-01, | 6.7e-01, |
| | -2.7e-02, | -1.0e-02, | -8.5e-03, | -1.7e-01, | 1.8e-02, | -3.8e-03, | -2.9e-02, | -1.2e-02, | -1.8e-02, |
| | 3.8e-02 5.0e-01, | 3.7e-02 | 2.8e-02 7.7e-01, | 5.3e-02 | 1.3e-02 2.0e-01, | 5.6e-03 | 4.3e-02 4.4e-01, | 1.9e-02 | 4.2e-02 7.8e-01, |
| cML-BIC | 5.0e-01, | 8.2e-01, | 7.7e-01, | 6.4e-04, | 2.0e-01, | 5.1e-01, | 4.4e-01, | 5.1e-01, | 7.8e-01, |
| | -2.6e-02, | -8.6e-03, | -8.2e-03, | -1.7e-01, | 1.6e-02, | -3.7e-03, | -3.3e-02, | -1.2e-02, | -1.1e-02, |
| | 3.8e-02 5.4e-01, | 3.7e-02 | -8.2e-03, 2.8e-02 8.1e-01, | 5.1e-02 | 1.2e-02 3.2e-01, | 5.6e-03 | 4.2e-02 6.1e-01, | 1.8e-02 | 3.9e-02 |
| ML-MA-BIC-DP-Max | 5.4e-01, | 7.6e-01, | 8.1e-01, | 1.1e-02, | 3.2e-01, | 5.4e-01, | 6.1e-01, | 7.6e-01, | 6.6e-01, |
| | -2.9e-02, 4.7e-02 | -1.2e-02, 4.1e-02 | -7.6e-03, 3.1e-02 | -1.8e-01, | 1.6e-02, 1.6e-02 | -4.0e-03, | -2.6e-02, | -7.1e-03, | -2.3e-02, 5.3e-02 |
| | 4.7e-02 | | 3.1e-02 | 7.0e-02 | 1.6e-02 | 6.5e-03 | -2.6e-02, 5.0e-02 | 2.3e-02 | 5.3e-02 |
| cML-BIC-DP-Max | 4.7e-01, | 7.9e-01, | 8.2e-01, | 8.2e-03, | 3.4e-01, | 5.5e-01, | 6.1e-01, | 7.7e-01, | 5.9e-01, |
| | -2.9e-02, 4.1e-02 | -1.0e-02, | -7.2e-03, 3.2e-02 | -1.8e-01, | 1.4e-02, | -3.5e-03. | -2.6e-02, | -6.2e-03, | -2.9e-02, |
| | 4.1e-02 | 3.8e-02 | 3.2e-02 | 6.8e-02 | 1.5e-02 | 5.8e-03 | 5.2e-02 | 2.2e-02 | 5.5e-02 |
| cML-MA-BIC-DP | 5.8e-01, | 7.6e-01, | 8.1e-01, | 1.2e-02, | 1.5e-02 3.2e-01, | 5.4e-01, | -2.6e-02, 5.2e-02 6.6e-01, | 7.7e-01, | 6.5e-01, |
| | -2.8e-02, 5.2e-02 | -1.3e-02, | -7.6e-03, 3.1e-02 | -1.8e-01. | 1.6e-02. | -4.0e-03, | -2.4e-02, 5.5e-02 6.1e-01, | -7.1e-03, | -2.5e-02, |
| | 5.2e-02 | 4.2e-02 | 3.1e-02 | 7.1e-02 | 1.6e-02 | 6.6e-03 | 5.5e-02 | 2.4e-02 | 5.5e-02 |
| cML-BIC-DP | 5.8e-01, | 7.6e-01, | 8 2e-01 | 8.2e-03, | 3.4e-01, | 5.3e-01, | 6.1e-01, | 7.2e-01, | 5.9e-01, |
| | -2.7e-02. | -1.3e-02, | -7.2e-03, 3.2e-02 5.2e-01, -1.0e-02, | -1.8e-01, | 1.4e-02 | -4.4e-03, | -2.6e-02, 5.2e-02 1.0e+00, | -9.1e-03, | -2.9e-02, |
| | 4.9e-02 | 4.4e-02 | 3.2e-02 | 6.8e-02 | 1.5e-02 | 7.0e-03 | 5.2e-02 | 2.5e-02 | 5.5e-02 |
| MR-Mix | 4.9e-02 1.0e+00, | 7.8e-01, | 5.2e-01. | 1.5e-02, | 1.5e-02 9.7e-02, | 5.7e-01, | 1.0e+00. | 4.9e-01, | 1.3e-01, |
| | 0.0e+00, | 1.0e-02, | -1.0e-02. | -9.0e-02, | 3.0e-02, | -2.0e-02, | 2.0e-17, | -1.0e-01, | -1.0e-01, |
| | 3.6e-02 | 3.6e-02 | 1.6e-02 | 3.7e-02 | 1.8e-02 | 3.5e-02 | 9.9e-02 | 1.5e-01 | 6.6e-02 |
| MR-ContMix | 8.1e-01, | 3.7e-01, | 8.3e-01, | 4.2e-02, | 8.3e-02, | 6.9e-02, | 5.5e-01, | 9.3e-01, | 1.6e-01, |
| WIR COMMIN | -9.2e-03, | -3.4e-02, | -1.2e-02, | -1.4e-01, | 2.4e-02, | -1.4e-02, | -2.7e-02, | 8.4e-04, | -6.8e-02, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 5.2e-01, | 5.2e-01, | 7.3e-01, -9.5e-03, | 8.8e-06, | 1.2e-01, 2.0e-02, | 5.1e-01, | 8.1e-01, | 5.5e-01, | 1.1e-01, |
| | -2.6e-02, | -2.5e-02, | -9.5e-03, | -2.3e-01, | 2.0e-02, | -3.6e-03, | -1.1e-02, | -1.1e-02, | -6.7e-02, |
| | 4.0e-02 | 3.9e-02 | 2.8e-02 | 5.1e-02 | 1.3e-02 | 5.5e-03 | -1.1e-02, 4.6e-02 | 1.8e-02 | 4.2e-02 |
| MR-PRESSO | 3.3e-01, | 8.3e-01, | 9.8e-01, | 1.1e-02, | 1.7e-01, | 4.5e-01, | 5.3e-01, | 5.7e-01, | 8.1e-01, |
| | -4.3e-02. | -8.6e-03, | -7.5e-04, | -1.7e-01, | 2.0e-02. | -3.6e-03, | -3.2e-02. | -1.1e-02, | -1.0e-02, |
| | 4.4e-02 | 3.9e-02 | 3.2e-02 | 6.5e-02 | 1.4e-02 | 4.7e-03 | 5.0e-02 | 2.0e-02 | 4.4e-02 |
| MR-IVW | 3.3e-01, | 7.3e-01, | 7.9e-01, | 2.2e-02, | 6.0e-01, 9.7e-03, | 5.1e-01, | 5.2e-01, | 9.5e-01, | 8.1e-01, |
| | -4.3e-02, | 2.6e-02, | -1.0e-02. | -1.5e-01, | 9.7e-03, | -3.6e-03, | -3.2e-02, | -1.3e-03, | -1.0e-02, |
| | 4.4e-02 | 7.5e-02 | 3.8e-02 | 6.7e-02 | 1.8e-02 | 5.5e-03 | 5.0e-02 | 2.2e-02 | 4.4e-02 |
| MR-Egger | 3.3e-01, | 6.8e-01, | 4.1e-01, | 7.6e-03, | 8.6e-02, | 4.2e-01, | 6.50.03 | 2.7e-01, | 1.3e-02, |
| | 6.8e-02. | 5.0e-02, | 4.9e-02. | -3.2e-01, | 5.7e-02. | -1.9e-02, | 9.0e-01. | -9.7e-02, | 4.2e-01, |
| | 6.8e-02, 7.1e-02 | 1.2e-01 | 4.9e-02, 6.0e-02 | 1.2e-01 | 5.7e-02, 3.3e-02 | 2.4e-02 | 3.3e-01 | 8.8e-02 | 1.7e-01 |
| MR-Weighted-Median | 4.6e-01, | 1.0e+00, | 3.5e-01, | 4.4e-02, | 4.8e-02, | 2.5e-01, | 9.0e-01, 3.3e-01 4.5e-01, | 5.4e-01, | 2.6e-01, |
| wire weighted medium | -4 6e-02 | 0.0e+00, | 3.9e-02 | -1.7e-01, | 3.7e-02 | -8.7e-03, | -4 6e-02 | -1.7e-02, | -6.5e-02, |
| | -4.6e-02, 6.2e-02 | 5.4e-02 | 3.9e-02, 4.2e-02 | 8.4e-02 | 3.7e-02, 1.9e-02 | 7.6e-03 | -4.6e-02, 6.0e-02 | 2.7e-02 | 5.8e-02 |
| MR-Weighted-Mode | 8.9e-01, | 8.5e-01, | 5.1e-01, | 4.8e-02, | 8.0e-02, | 1.7e-01, | 6.3e-01, | 8.3e-01, | 4.3e-01, |
| WIK-Weighted-Wode | 8 20 02 | -9.8e-03, | 2.50.02 | -1.7e-01, | 3 30 02 | 1.70-01, | 4.70.02 | -9.0e-03, | -1.1e-01, |
| | 8.3e-03, 5.8e-02 | 5.3e-02 | 2.5e-02, 3.8e-02 | 8.4e-02 | 3.3e-02, 1.9e-02 | -1.9e-02, 1.4e-02 | -4.7e-02, 9.8e-02 | 4.1e-02 | 1.5e-01 |
| MR-RAPS1 | 3.6e-02 | 5.6e-01, | 8.2e-01, | 3.0e-03, | 4.6e-01, | 5.1e-01, | 5.4e-01, | 8.7e-01, | 8.2e-01, |
| WIK-KAP51 | -3.9e-02, | 5.6e-01, 4.2e-02, | 8.2e-01, -8.1e-03, | -2.0e-01, | 1.3e-02, | -3.7e-03, | -3.1e-02, | -3.6e-03, | -9.9e-03, |
| | -3.9e-02, 4.3e-02 | 4.2e-02, 7.2e-02 | -8.1e-03, 3.6e-02 | -2.0e-01, 6.6e-02 | 1.3e-02, 1.7e-02 | -3.7e-03, 5.6e-03 | -3.1e-02, 5.0e-02 | -3.6e-03, 2.2e-02 | -9.9e-03, 4.4e-02 |
| MR-RAPS2 | | | 9.0e-01, | | 2.1 - 01 | | 6.1e-01, | | 5.1e-01, |
| MK-KAPS2 | 4.4e-01, | 6.3e-01, | 9.0e-01, | 2.8e-03, | 3.1e-01, | 4.2e-01, | 0.1e-01, | 7.6e-01, | |
| | -3.1e-02, | -1.8e-02, | -3.7e-03, | -2.0e-01, | 1.7e-02, | -4.6e-03, | -2.7e-02, | -6.6e-03, | -2.9e-02, |
| 100 0 1000 | 4.0e-02 | 3.8e-02 | 3.1e-02 | 6.6e-02 | 1.7e-02 | 5.8e-03 | 5.2e-02 | 2.2e-02 | 4.4e-02 |
| MR-RAPS3 | 2.6e-01, -4.3e-02, | 4.7e-01, | 7.0e-01, | 1.9e-03, | 4.2e-01, | 5.1e-01, | 4.5e-01, | 9.4e-01, | 7.9e-01, |
| | -4.3e-02, | 2.7e-02, | -1.0e-02, | -1.6e-01, | 9.9e-03, | -3.7e-03, | -3.3e-02, | -1.4e-03, | -1.1e-02, |
| | 3.8e-02 | 3.8e-02 | -1.0e-02, 2.8e-02 8.7e-01, | 5.0e-02 | 1.2e-02 1.7e-01, | 5.6e-03 4.2e-01, | 4.3e-02 5.5e-01, | 1.8e-02 | 4.0e-02 4.3e-01, |
| MR-RAPS4 | 4.4e-01, | 6.3e-01, | 8.7e-01, | 2.5e-04, | 1.7e-01, | 4.2e-01, | 5.5e-01, | 6.9e-01, | 4.3e-01, |
| | -3.0e-02, | -1.8e-02, | -4.7e-03, 2.8e-02 | -1.9e-01, 5.2e-02 | 1.7e-02, 1.3e-02 | -4.6e-03, 5.8e-03 | -2.7e-02, 4.4e-02 | -7.3e-03, 1.8e-02 | -3.2e-02, 4.1e-02 |
| | 3.9e-02 | 3.8e-02 | | | | | | | |

Table S17: Secondary real data analysis, set 6.

| Exp/Out Method | SCZ/Height (35) | SCZ/HOMA (35) | SCZ/IHC (35) | SCZ/LDL (36) | SCZ/RA (69) | SCZ/T2D (35) | T2D/ASmk (10) | T2D/ANRX (6) | T2D/CIQ (|
|----------------------|--------------------|------------------|-----------------|-----------------|-------------|-----------------|----------------------|-----------------|-----------|
| cML-MA-BIC-Max | 3.6e-01, | 2.2e-01, | 8.0e-01, | 8.9e-01, | 3.0e-01, | 8.9e-01, | 7.6e-01, | 9.0e-01, | 6.6e-01, |
| CIVIL-IVIA-DIC-IVIAX | -8.1e-03, | 9.9e-03, | -9.2e-03, | -1.7e-03, | 2.7e-02, | 6.2e-03, | -1.8e-03, | 1.2e-02, | 1.7e-02, |
| | 8.9e-03 | 8.1e-03 | 3.6e-02 | 1.2e-02 | 2.6e-02 | 4.4e-02 | 5.8e-03 | 9.9e-02 | 3.8e-02 |
| cML-BIC-Max | 4.2e-01, | 2.2e-01, | 7.6e-01, | 9.5e-01, | 2.5e-01, | 9.1e-01, | 7.6e-01, | 8.9e-01, | 6.7e-01, |
| CML-DIC-Max | -6.2e-03, | 9.9e-03, | -1.1e-02, | -7.9e-04, | 2.9e-02, | 5.0e-03, | -1.8e-03, | 1.3e-02, | 1.6e-02, |
| | 7.7e-03 | 8.1e-03 | 3.5e-02 | 1.2e-02 | 2.6e-02 | 4.4e-02 | 5.8e-03 | 9.9e-02 | 3.8e-02 |
| cML-MA-BIC | 2.2e-01, | 2.2e-01, | 7.5e-01, | 8.9e-01, | 3.0e-01, | 8.9e-01, | 7.6e-01, | 9.1e-01, | 6.5e-01, |
| CIVIL-WIA-DIC | -1.1e-02, | 9.8e-03, | -1.2e-02, | -1.8e-03, | 2.7e-02, | 6.3e-03, | -1.8e-03, | 1.2e-02, | 1.8e-02, |
| | 8.6e-03 | 8.1e-03 | 3.6e-02 | 1.2e-02 | 2.6e-02 | 4.4e-02 | 5.8e-03 | 9.9e-02 | 3.8e-02 |
| cML-BIC | 6.5e-02, | 2.2e-01, | 7.6e-01, | 9.5e-01, | 2.5e-01, | 9.1e-01, | 7.6e-01, | 8.9e-01, | 6.7e-01, |
| | -1.4e-02, | 9.9e-03, | -1.1e-02, | -7.9e-04, | 2.9e-02, | 5.0e-03, | -1.8e-03, | 1.3e-02, | 1.6e-02, |
| | 7.9e-03 | 8.1e-03 | 3.5e-02 | 1.2e-02 | 2.6e-02 | 4.4e-02 | 5.8e-03 | 9.9e-02 | 3.8e-02 |
| cML-MA-BIC-DP-Max | 8.5e-01, | 2.5e-01, | 8.9e-01, | 9.7e-01, | 3.9e-01, | 8.5e-01, | 8.2e-01, | 8.3e-01, | 7.1e-01, |
| | -3.0e-03, | 1.0e-02, | -6.9e-03, | -6.3e-04, | 2.9e-02, | 1.0e-02, | -1.3e-03. | 2.5e-02, | 1.6e-02, |
| | 1.5e-02 | 8.8e-03 | 4.9e-02 | 1.8e-02 | 3.4e-02 | 5.5e-02 | -1.3e-03, 5.8e-03 | 1.2e-01 | 4.3e-02 |
| cML-BIC-DP-Max | 9.2e-01, | 2.2e-01, | 9.5e-01, | 9.8e-01, | 3.9e-01, | 8.4e-01, | 8.3e-01, | 8.2e-01, | 7.0e-01, |
| | -1.4e-03, | 1.0e-02, | -3.0e-03, | 5.3e-04, | 2.9e-02, | 1.1e-02, | -1.2e-03, | 2.7e-02, | 1.6e-02, |
| | 1.4e-02 | 8.5e-03 | 4.6e-02 | 1.8e-02 | 3.4e-02 | 5.4e-02 | 5.7e-03 | 1.2e-01 | 4.2e-02 |
| cML-MA-BIC-DP | 8.1e-01, | 2.6e-01, | 8.3e-01, | 9.7e-01, | 3.9e-01, | 8.5e-01, | 8.2e-01, | 8.4e-01, | 7.1e-01, |
| | -3.9e-03, | 9.9e-03, | -1.2e-02, | -6.4e-04, | 2.9e-02, | 1.0e-02, | -1.3e-03, | 2.4e-02, | 1.7e-02, |
| | 1.6e-02 | 8.9e-03 | 5.5e-02 | 1.8e-02 | 3.4e-02 | 5.5e-02 | 5.9e-03 | 1.2e-01 | 4.5e-02 |
| cML-BIC-DP | 8.6e-01, | 2.2e-01, | 8.1e-01, | 9.8e-01, | 3.9e-01, | 8.4e-01, | 8.3e-01, | 8.2e-01, | 7.0e-01, |
| CALL DIC DI | -3.3e-03, | 1.0e-02, | -1.5e-02, | 5.3e-04, | 2.9e-02, | 1.1e-02, | -1.2e-03, | 2.7e-02, | 1.6e-02, |
| | 1.9e-02 | 8.5e-03 | 6.0e-02 | 1.8e-02 | 3.4e-02 | 5.4e-02 | 5.7e-03 | 1.2e-01 | 4.2e-02 |
| MR-Mix | 1.9e-01, | 2.0e-01, | 8.1e-01, | 1.0e+00, | 8.9e-01, | 1.0e+00, | 7.9e-01, | 8.4e-01, | 1.0e+00, |
| | -4.0e-02, | 5.0e-02, | -1.2e-01, | 2.0e-17, | -2.0e-02, | 2.0e-17, | -1.5e-02, | 2.5e-02, | 2.0e-17, |
| | 3.0e-02 | 3.9e-02 | 5.1e-01 | 5.8e-02 | 1.5e-01 | 6.5e-02 | 5.5e-02 | 1.2e-01 | 2.0e-01 |
| MR-ContMix | 9.3e-01, | 2.9e-01, | 1.2e-02, | 1.5e-01, | 4.6e-01, | 6.3e-02, | 5.2e-01, | 6.4e-01, | 1.7e-01, |
| MIC COMMIN | 2.8e-04, | 1.1e-02, | -1.7e-01, | 2.1e-02, | 2.7e-02, | 1.4e-01, | -1.5e-02, | -5.1e-02, | 6.6e-02, |
| | NA | NA | NA | NA | NA | NA NA | NA | NA | NA |
| MR-Lasso | 6.0e-01, | 3.3e-01, | 7.9e-01, | 5.7e-01, | 7.6e-01, | 6.3e-01, | 7.6e-01, | 8.9e-01, | 7.2e-01, |
| THE EMOSO | -5.3e-03, | 7.8e-03, | -1.1e-02, | -7.7e-03, | 8.4e-03, | 2.5e-02, | -1.7e-03, | 1.3e-02, | 1.6e-02, |
| | 1.0e-02 | 8.1e-03 | 4.0e-02 | 1.4e-02 | 2.7e-02 | 5.2e-02 | 5.7e-03 | 9.8e-02 | 4.4e-02 |
| MR-PRESSO | 7.9e-01, | 1.5e-01, | 7.9e-01, | 9.6e-01, | 3.4e-01, | 9.3e-01, | 7.2e-01, | 8.7e-01, | 7.3e-01, |
| | 3.2e-03, | 9.8e-03, | -1.1e-02, | -7.5e-04, | 2.8e-02, | 4.8e-03, | -1.7e-03, | 1.3e-02, | 1.6e-02, |
| | 1.2e-02 | 6.6e-03 | 4.0e-02 | 1.6e-02 | 3.0e-02 | 5.3e-02 | 4.6e-03 | 7.5e-02 | 4.4e-02 |
| MR-IVW | 2.1e-01, | 2.2e-01, | 7.6e-01, | 9.6e-01, | 3.4e-01, | 9.3e-01, | 7.6e-01, | 8.9e-01, | 7.2e-01, |
| | 2.1e-02, | 9.8e-03, | 1.4e-02, | -7.5e-04, | 2.8e-02, | 4.8e-03, | -1.7e-03, | 1.3e-02, | 1.6e-02, |
| | 1.7e-02 | 8.0e-03 | 4.5e-02 | 1.6e-02 | 3.0e-02 | 5.3e-02 | 5.7e-03 | 9.8e-02 | 4.4e-02 |
| MR-Egger | 3.8e-01, | 7.7e-01, | 8.9e-01, | 6.6e-01, | 8.9e-02, | 8.7e-01, | 9.7e-02, | 6.6e-01, | 2.0e-01, |
| 00 | -6.3e-02, | -1.1e-02, | -2.6e-02, | 3.1e-02, | 2.3e-01, | 4.0e-02, | 5.3e-02, | -3.3e-01, | 3.2e-01, |
| | 7.3e-02 | 3.7e-02 | 2.0e-01 | 7.1e-02 | 1.4e-01 | 2.4e-01 | 3.2e-02 | 7.6e-01 | 2.5e-01 |
| MR-Weighted-Median | 7.1e-01, | 6.6e-01, | 8.3e-01, | 6.9e-01, | 1.0e+00, | 1.0e+00, | 9.8e-01, | 8.9e-01, | 5.9e-01, |
| | -4.5e-03, | 4.9e-03, | -1.2e-02, | 7.5e-03, | 0.0e+00, | 0.0e+00, | -2.3e-04, | -1.7e-02, | 2.7e-02, |
| | 1.2e-02 | 1.1e-02 | 5.3e-02 | 1.9e-02 | 4.0e-02 | 6.9e-02 | 7.6e-03 | 1.2e-01 | 5.0e-02 |
| MR-Weighted-Mode | 6.4e-01, | 9.0e-01, | 4.9e-02, | 5.6e-01, | 5.4e-01, | 9.2e-01, | 4.2e-01, | 8.0e-01, | 5.5e-01, |
| · · | -7.4e-03, | 2.3e-03, | -2.0e-01, | 1.8e-02, | 5.2e-02, | -1.3e-02, | 9.6e-03, | -4.4e-02, | 4.7e-02, |
| | 1.6e-02 | 1.9e-02 | 1.0e-01 | 3.2e-02 | 8.4e-02 | 1.4e-01 | 1.2e-02 | 1.8e-01 | 7.8e-02 |
| MR-RAPS1 | 2.8e-01, | 2.2e-01, | 7.2e-01, | 9.3e-01, | 2.8e-01, | 8.9e-01, | 7.6e-01, | 8.9e-01, | 6.6e-01, |
| | 1.8e-02, | 9.9e-03, | 1.6e-02, | -1.4e-03, | 3.3e-02, | 7.3e-03, | -1.8e-03, | 1.3e-02, | 1.7e-02, |
| | 1.7e-02 | 8.2e-03 | 4.5e-02 | 1.6e-02 | 3.1e-02 | 5.3e-02 | 5.8e-03 | 9.9e-02 | 4.0e-02 |
| MR-RAPS2 | 6.9e-01, | 2.6e-01, | 9.7e-01, | 9.4e-01, | 3.9e-01, | 8.0e-01, | 7.5e-01, | 9.6e-01, | 6.1e-01, |
| | 5.9e-03, | 9.4e-03, | -1.9e-03, | -1.3e-03, | 2.6e-02, | 1.5e-02, | -1.9e-03, | 4.9e-03, | 2.2e-02, |
| | 1.5e-02 | 8.4e-03 | 4.5e-02 | 1.7e-02 | 3.1e-02 | 5.8e-02 | 6.0e-03 | 1.0e-01 | 4.4e-02 |
| MR-RAPS3 | 2.7e-03, | 2.2e-01, | 6.9e-01, | 9.5e-01, | 2.6e-01, | 9.1e-01, | 7.6e-01, | 8.9e-01, | 6.7e-01, |
| | 2.4e-02, | 9.9e-03, | 1.4e-02, | -7.9e-04, | 2.9e-02, | 5.0e-03, | -1.8e-03, | 1.3e-02, | 1.6e-02, |
| | 8.1e-03 | 8.2e-03 | 3.5e-02 | 1.3e-02 | 2.6e-02 | 4.5e-02 | 5.8e-03 | 9.9e-02 | 3.8e-02 |
| MR-RAPS4 | 3.4e-01, | 2.6e-01, | 6.7e-01, | 9.6e-01, | 3.3e-01, | 6.8e-01, | 7.5e-01, | 9.6e-01, | 6.1e-01, |
| | -7.1e-03, | 9.4e-03, | -1.6e-02, | -6.7e-04, | 2.6e-02, | 1.9e-02, | -1.9e-03, | 4.9e-03, | 2.0e-02, |
| | | | | | 2.7e-02 | 4.6e-02 | 6.0e-03 | 1.0e-01 | 3.9e-02 |

Table S18: Secondary real data analysis, set 7.

| Exp/Out | T2D/ESmk | T2D/FP (10) | T2D/FSmk | T2D/Height | T2D/HOMA | T2D/IHC | T2D/LDL | T2D/RA (10) | T2D/SCZ (8) |
|--|---------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|-----------------------|
| Method | (10) | | (10) | (10) | (10) | (10) | (10) | | |
| cML-MA-BIC-Max | 6.4e-01, | 3.8e-01, | 7.5e-01, | 3.7e-01, | 6.2e-06, | 4.4e-01, | 5.8e-01, | 2.2e-01, | 5.5e-02, |
| | 1.4e-02, | 1.8e-02, | 1.3e-02, | -7.8e-03, | -5.0e-02, | -2.9e-02, | 5.4e-03, | -4.1e-02, | -5.9e-02, |
| | 3.0e-02 | 2.1e-02 | 4.1e-02 | 8.7e-03 | 1.1e-02 | 3.7e-02 | 9.8e-03 | 3.4e-02 | 3.1e-02 |
| cML-BIC-Max | 6.6e-01, | 2.7e-01, | 7.5e-01, | 2.6e-01, | 2.7e-07, | 4.1e-01, | 5.4e-01, 5.9e-03, | 2.4e-01, | 5.6e-02, |
| | 1.3e-02, | 2.2e-02, | 1.3e-02, | -9.1e-03, | -4.9e-02, | -3.0e-02, | 5.9e-03, | -3.9e-02, | -5.8e-02, |
| | 3.0e-02 | 1.9e-02 | 4.1e-02 | 8.1e-03 | 9.5e-03 | 3.6e-02 | 9.6e-03 | 3.3e-02 | 3.0e-02 |
| cML-MA-BIC | 6.4e-01, | 4.7e-01, | 7.5e-01, | 4.6e-01, | 3.5e-06, | 4.8e-01, | 5.9e-01, | 2.2e-01, | 5.5e-02, |
| | 1.4e-02, | 1.6e-02, | 1.3e-02, | -6.7e-03, | -5.1e-02, | -2.7e-02, | 5.3e-03, | -4.1e-02, | -5.9e-02, |
| | 3.0e-02 | 2.2e-02 | 4.1e-02 | 9.1e-03 | 1.1e-02 | 3.8e-02 | 9.9e-03 | 3.4e-02 | 3.1e-02 |
| cML-BIC | 6.6e-01, | 2.7e-01, | 7.5e-01, | 2.6e-01, | 2.7e-07, | 4.1e-01, | 5.4e-01, | 2.4e-01, | 5.6e-02, |
| | 1.3e-02, | 2.2e-02, | 1.3e-02, | -9.1e-03, | -4.9e-02, | -3.0e-02, | 5.9e-03, | -3.9e-02, | -5.8e-02, |
| | 3.0e-02 | 1.9e-02 | 4.1e-02 | 8.1e-03 | 9.5e-03 | 3.6e-02 | 9.6e-03 5.8e-01, | 3.3e-02 | 3.0e-02 |
| cML-MA-BIC-DP-Max | 5.8e-01, | 4.2e-01, | 6.9e-01, | 5.7e-01, | 8.7e-03, | 5.2e-01, | 5.8e-01, | 3.1e-01, | 8.0e-02, |
| | 1.7e-02, 3.1e-02 | 2.4e-02, | 1.7e-02, | -7.1e-03, | -4.8e-02, | -2.5e-02, | 5.8e-03, 1.1e-02 | -3.8e-02, | -5.8e-02, |
| 10 PIG PP 11 | | 3.1e-02 | 4.1e-02 | 1.3e-02 | 1.8e-02 | 3.8e-02 | 1.1e-02 | 3.7e-02 | 3.3e-02 |
| cML-BIC-DP-Max | 5.9e-01, | 4.3e-01, | 6.8e-01, | 6.5e-01, | 9.9e-03, | 4.7e-01, | 4.8e-01, | 3.0e-01, | 6.0e-02, |
| | 1.6e-02, | 2.5e-02, | 1.7e-02, 4.0e-02 | -6.3e-03, | -4.8e-02, 1.9e-02 | -2.6e-02, | 6.9e-03, 9.7e-03 | -3.6e-02, | -5.8e-02, |
| M. M. DIG DD | 3.0e-02 | 3.1e-02 | | 1.4e-02 | | 3.6e-02 | | 3.4e-02 | 3.1e-02 |
| cML-MA-BIC-DP | 5.8e-01, | 4.6e-01, | 6.9e-01, | 6.4e-01, | 8.5e-03, | 5.7e-01, | 6.0e-01, | 3.1e-01, | 8.1e-02, -5.8e-02, |
| | 1.7e-02, 3.2e-02 | 2.4e-02, 3.3e-02 | 1.6e-02, 4.1e-02 | -6.5e-03, 1.4e-02 | -4.8e-02, 1.8e-02 | -2.3e-02, 4.1e-02 | 5.7e-03, 1.1e-02 | -3.8e-02, 3.7e-02 | -5.8e-02, 3.3e-02 |
| cML-BIC-DP | 5.9e-01, | 4.3e-01, | 6.8e-01, | 6.5e-01, | 9.9e-03, | 4.7e-01, | 4.8e-01, | 3.0e-01, | 6.0e-02, |
| CML-DIC-DP | 1.6e-02, | 4.5e-01, 2.5e-02, | 1.7e-02, | -6.3e-03, | -4.8e-02, | -2.6e-02, | 6.9e-03, | -3.6e-02, | -5.8e-02, |
| | 3.0e-02 | 3.1e-02 | 4.0e-02 | 1.4e-02 | 1.9e-02 | 3.6e-02 | 9.7e-03 | 3.4e-02 | 3.1e-02 |
| MR-Mix | 7.6e-01, | 8.7e-01, | 8.0e-01, | 6.0e-01, | 8.8e-03, | 6.3e-01, | 8.3e-01, | 6.4e-01, | 4.7e-04, |
| WIIX-WIIX | 1.5e-02, | 6.0e-02, | 1.5e-02, | -3.0e-02, | -3.5e-01, | -1.0e-01, | 2.5e-02, | -1.8e-01, | -2.5e-01, |
| | 5.0e-02 | 3.6e-01 | 5.8e-02 | 5.7e-02 | 1.3e-01 | 2.1e-01 | 1.2e-01 | 3.9e-01 | 7.1e-02 |
| MR-ContMix | 1.5e-01, | 2.1e-01, | 9.0e-01, | 1.2e-01, | 9.1e-04, | 1.0e+00, | 7.8e-01, | 4.3e-01, | 4.3e-02, |
| WIK COMMIN | 5.8e-02, | 3.8e-02, | 1.5e-02, | 2.2e-02, | -5.2e-02, | -4.9e-03, | -2.5e-03, | -9.7e-02, | -1.3e-01, |
| | NA | NA | NA | NA | NA | NA NA | NA | NA NA | NA NA |
| MR-Lasso | 6.6e-01. | 5.0e-01, | 7.5e-01, | 3.3e-01, | 3.4e-02, | 4.3e-01, | 7.8e-01, | 3.7e-01, | 1.6e-01, |
| | 1.3e-02, | 2.0e-02, | 1.3e-02, | 1.1e-02, | -3.6e-02, | -3.0e-02, | -2.9e-03, | -3.8e-02, | -5.6e-02, |
| | 3.0e-02 | 3.0e-02 | 4.1e-02 | 1.1e-02 | 1.7e-02 | 3.8e-02 | 1.0e-02 | 4.2e-02 | 4.0e-02 |
| MR-PRESSO | 6.6e-01, | 2.0e-01, | 6.3e-01, | 5.0e-01, | 2.0e-03, | 4.5e-01, | 5.6e-01, | 3.9e-01, | 2.1e-01, |
| | 1.3e-02, | 3.8e-02, | 1.3e-02, | 9.3e-03, | -5.6e-02, | -3.0e-02, | 5.7e-03, | -3.8e-02, | -5.6e-02, |
| | 2.9e-02 | 2.7e-02 | 2.6e-02 | 1.3e-02 | 1.1e-02 2.4e-02, | 3.8e-02 | 9.5e-03 | 4.2e-02 | 4.0e-02 |
| MR-IVW | 6.6e-01, | 2.9e-01, | 7.5e-01, | 5.7e-01, | 2.4e-02, | 4.3e-01, | 5.5e-01, | 3.7e-01, | 1.6e-01, |
| | 1.3e-02, | 4.8e-02, | 1.3e-02, | 1.8e-02, | -5.0e-02, | -3.0e-02, | 5.7e-03, | -3.8e-02, | -5.6e-02, |
| | 3.0e-02 | 4.5e-02 | 4.1e-02 | 3.1e-02 | 2.2e-02 | 3.8e-02 | 9.5e-03 1.1e-01, | 4.2e-02 | 4.0e-02 3.5e-01, |
| MR-Egger | 4.1e-01, | 5.0e-01, | 6.2e-01, | 3.4e-01, | 9.9e-01, | 2.5e-01, | 1.1e-01, | 5.0e-01, | 3.5e-01, |
| | -1.3e-01, | 1.8e-01, | 1.1e-01, | -1.6e-01, | -1.5e-03, | -2.4e-01, | 8.3e-02, | 1.6e-01, | -2.3e-01, |
| | 1.6e-01 | 2.6e-01 | 2.2e-01 | 1.7e-01 | 1.3e-01 | 2.1e-01 | 5.1e-02 | 2.4e-01 | 2.5e-01 |
| MR-Weighted-Median | 8.2e-01, | 2.2e-01, | 7.5e-01, | 7.4e-01, | 1.3e-03, | 7.5e-01, | 5.2e-01, | 9.6e-01, | 4.8e-02, |
| | 9.5e-03, 4.2e-02 | 3.2e-02, | 1.7e-02, 5.3e-02 | -4.2e-03, | -4.1e-02, | -1.5e-02, | -8.3e-03, 1.3e-02 | -2.4e-03, | -8.5e-02, |
| 100 W. 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | | 2.6e-02 | | 1.3e-02 | 1.3e-02 | 4.8e-02 | | 4.8e-02 | 4.3e-02 |
| MR-Weighted-Mode | 2.7e-01, | 3.5e-01, | 9.2e-01, | 6.1e-01, | 4.7e-03, | 7.0e-01, | 4.4e-01, | 9.7e-01, | 1.3e-01, |
| | 9.3e-02, 8.5e-02 | 3.1e-02, 3.4e-02 | 7.0e-03, 7.0e-02 | 1.0e-02, 2.0e-02 | -4.4e-02, 1.6e-02 | -3.0e-02, 7.6e-02 | -1.6e-02, 2.1e-02 | -2.5e-03, 7.7e-02 | -1.1e-01, 7.1e-02 |
| MR-RAPS1 | 6.6e-01, | 1.8e-01, | 7.5e-01, | 7.0e-01, | 2.4e-02, | 4.1e-01, | 5.5e-01, | 3.1e-01, | 1.1e-02 |
| MK-KAPS1 | 1.3e-02, | 6.5e-02, | 1.3e-01, 1.3e-02, | 1.1e-02, | -4.8e-02, | -3.0e-02, | 5.9e-03, | -3.7e-02, | -5.9e-02, |
| | 3.0e-02 | 4.9e-02 | 4.1e-02 | 2.8e-02 | 2.1e-02 | 3.7e-02 | 9.8e-03 | 3.6e-02 | 3.7e-02 |
| MR-RAPS2 | 5.4e-01, | 2.5e-01, | 7.8e-01, | 4.9e-01, | 3.2e-02, | 5.5e-01, | 8.1e-01, | 2.6e-01, | 1.4e-01, |
| MIX-IXAI 52 | 1.9e-02, | 2.3e-01, 2.3e-02, | 1.2e-02, | -5.5e-03, | -4.7e-02, | -2.3e-02, | 2.4e-03, | -4.3e-02, | -6.2e-02, |
| | 3.1e-02 | 2.0e-02 | 4.2e-02 | 8.0e-03 | 2.2e-02 | 3.8e-02 | 1.0e-02 | 3.8e-02 | 4.1e-02 |
| MR-RAPS3 | 6.6e-01, | 9.8e-03, | 7.5e-01, | 1.8e-02, | 1.0e-08, | 4.1e-01, | 5.5e-01, | 2.5e-01, | 6.1e-02, |
| MIC ICH 05 | 1.3e-02, | 5.3e-02, | 1.3e-02, | 2.5e-02, | -5.7e-02, | -3.0e-02, | 5.9e-03, | -3.9e-02, | -5.8e-02, |
| | 3.0e-02 | 2.1e-02 | 4.1e-02 | 1.0e-02 | 1.0e-02 | 3.7e-02 | 9.8e-03 | 3.4e-02 | 3.1e-02 |
| MR-RAPS4 | 5.4e-01, | 2.5e-01, | 7.8e-01, | 9.2e-41, | 5.9e-08, | 5.5e-01, | 8.1e-01, | 2.0e-01, | 4.9e-02, |
| | 1.9e-02, | 2.3e-02, | 1.2e-02, | 1.7e-01, | -4.9e-02, | -2.3e-02, | 2.4e-03, | -4.5e-02, | -6.3e-02, |
| | 3.1e-02 | 2.0e-02 | 4.2e-02 | 1.2e-02 | 9.1e-03 | 3.8e-02 | 1.0e-02 | 3.5e-02 | 3.2e-02 |

Table S19: Goodness-of-fit tests for secondary real data analysis, set 1.

| Exp/Out Method | FP/ASmk (6) | FP/ANRX (6) | FP/CIQ (4) | FP/ESmk (6) | FP/FSmk (6) | FP/Height (6) | FP/HOMA (6) | FP/IHC (6) | FP/LDL (5) |
|-------------------|-------------|----------------|------------|-------------|-------------|---------------|----------------|------------|------------|
| GOF1-Max | 4.5e-01 | 7.5e-01 | 7.2e-01 | 4.6e-01 | 4.4e-01 | 3.4e-02 | 2.3e-130 | 4.1e-01 | 1.1e-01 |
| GOF2-Max | 4.3e-01 | 7.5e-01 | 7.2e-01 | 4.4e-01 | 4.4e-01 | 1.5e-02 | 1.0e-20 | 4.0e-01 | 9.7e-02 |
| GOF1 | 4.5e-01 | 7.5e-01 | 7.2e-01 | 4.6e-01 | 4.4e-01 | 3.4e-02 | 2.3e-130 | 4.1e-01 | 1.0e-04 |
| GOF2 | 4.3e-01 | 7.5e-01 | 7.2e-01 | 4.4e-01 | 4.4e-01 | 1.5e-02 | 1.0e-20 | 4.0e-01 | 1.0e-04 |

Table S20: Goodness-of-fit tests for secondary real data analysis, set 2.

| Exp/Out Method | FP/RA (6) | FP/SCZ (6) | FP/T2D (6) | Height/ASmk (310) | Height/ESmk (310) | Height/FP (307) | Height/FSmk (310) | Height/HOMA (303) | Height/RA (306) |
|-------------------|-----------|------------|------------|----------------------|----------------------|--------------------|----------------------|----------------------|--------------------|
| GOF1-Max | 4.3e-01 | 7.2e-01 | 1.6e-28 | 2.5e-01 | 1.4e-01 | 2.0e-01 | 2.7e-01 | 3.6e-01 | 1.7e-03 |
| GOF2-Max | 4.4e-01 | 7.2e-01 | 9.4e-21 | 2.0e-01 | 1.8e-01 | 2.6e-01 | 2.2e-01 | 3.6e-01 | 1.8e-03 |
| GOF1 | 4.3e-01 | 7.2e-01 | 1.6e-28 | 2.5e-01 | 1.4e-01 | 2.4e-01 | 6.6e-02 | 1.9e-01 | 1.5e-02 |
| GOF2 | 4.4e-01 | 7.2e-01 | 9.4e-21 | 2.0e-01 | 1.8e-01 | 2.4e-01 | 3.9e-02 | 2.0e-01 | 1.2e-02 |

Table S21: Goodness-of-fit tests for secondary real data analysis, set 3.

| Exp/Out Method | Height/SCZ (288) | Height/T2D (307) | HOMA/ASmk (2) | HOMA/ESmk (2) | HOMA/FP (2) | HOMA/FSmk (2) | HOMA/Height (2) | HOMA/IHC (2) | HOMA/LDL (2) |
|-------------------|---------------------|---------------------|------------------|------------------|----------------|------------------|-----------------|-----------------|-----------------|
| GOF1-Max | 3.4e-05 | 3.7e-04 | 1.4e-01 | 1.5e-01 | 1.2e-01 | 1.0e-01 | 1.1e-01 | 8.7e-02 | 7.1e-02 |
| GOF2-Max | 5.2e-05 | 1.9e-03 | 1.4e-01 | 1.5e-01 | 1.2e-01 | 1.0e-01 | 1.1e-01 | 8.9e-02 | 7.4e-02 |
| GOF1 | 1.4e-04 | 2.9e-04 | 1.4e-01 | 1.5e-01 | 1.2e-01 | 1.0e-01 | 1.1e-01 | 8.7e-02 | 7.1e-02 |
| GOF2 | 1.0e-04 | 5.3e-05 | 1.4e-01 | 1.5e-01 | 1.2e-01 | 1.0e-01 | 1.1e-01 | 8.9e-02 | 7.4e-02 |

Table S22: Goodness-of-fit tests for secondary real data analysis, set 4.

| Exp/Out Method | HOMA/RA (2) | HOMA/SCZ (2) | HOMA/T2D (2) | LDL/ASmk (69) | LDL/ANRX (52) | LDL/ESmk (69) | LDL/FP (68) | LDL/FSmk (69) | LDL/HOMA (68) |
|-------------------|----------------|-----------------|-----------------|------------------|------------------|------------------|-------------|------------------|------------------|
| GOF1-Max | 1.4e-01 | 1.2e-01 | 1.3e-01 | 5.5e-01 | 4.7e-01 | 5.6e-01 | 1.2e-01 | 5.8e-01 | 3.3e-02 |
| GOF2-Max | 1.4e-01 | 1.2e-01 | 1.2e-01 | 5.6e-01 | 4.7e-01 | 5.7e-01 | 1.2e-01 | 5.9e-01 | 3.7e-02 |
| GOF1 | 1.4e-01 | 1.2e-01 | 1.3e-01 | 5.5e-01 | 4.7e-01 | 5.4e-01 | 1.2e-01 | 5.8e-01 | 3.3e-02 |
| GOF2 | 1.4e-01 | 1.2e-01 | 1.2e-01 | 5.6e-01 | 4.7e-01 | 5.0e-01 | 1.2e-01 | 5.9e-01 | 3.7e-02 |

Table S23: Goodness-of-fit tests for secondary real data analysis, set 5.

| Method Exp/Out | LDL/IHC (67) | LDL/RA (71) | LDL/SCZ (69) | LDL/T2D (67) | RA/SCZ (47) | SCZ/ASmk (35) | SCZ/CIQ (20) | SCZ/FP (34) | SCZ/FSmk (35) |
|----------------|-----------------|----------------|-----------------|-----------------|-------------|------------------|-----------------|-------------|------------------|
| GOF1-Max | 1.7e-01 | 1.9e-01 | 3.1e-01 | 8.8e-01 | 2.9e-03 | 3.7e-01 | 9.4e-01 | 3.8e-03 | 1.9e-01 |
| GOF2-Max | 2.0e-01 | 1.7e-01 | 3.2e-01 | 8.9e-01 | 3.0e-03 | 3.8e-01 | 9.4e-01 | 3.7e-03 | 2.0e-01 |
| GOF1 | 1.7e-01 | 1.9e-01 | 3.1e-01 | 6.8e-03 | 2.9e-03 | 3.7e-01 | 9.4e-01 | 3.8e-03 | 1.9e-01 |
| GOF2 | 2.0e-01 | 1.7e-01 | 3.2e-01 | 1.4e-02 | 3.0e-03 | 3.8e-01 | 9.4e-01 | 3.7e-03 | 2.0e-01 |

Table S24: Goodness-of-fit tests for secondary real data analysis, set 6.

| Exp/Out Method | SCZ/Height (35) | SCZ/HOMA (35) | SCZ/IHC (35) | SCZ/LDL (36) | SCZ/RA (69) | SCZ/T2D (35) | T2D/ASmk (10) | T2D/ANRX (6) | T2D/CIQ (7) |
|-------------------|-----------------|------------------|-----------------|-----------------|-------------|-----------------|------------------|-----------------|-------------|
| GOF1-Max | 4.8e-08 | 4.4e-01 | 4.8e-05 | 3.5e-02 | 7.1e-01 | 2.2e-01 | 8.7e-01 | 3.4e-02 | 1.4e-01 |
| GOF2-Max | 3.1e-11 | 4.6e-01 | 4.9e-05 | 4.7e-02 | 7.5e-01 | 2.2e-01 | 8.6e-01 | 4.4e-02 | 1.7e-01 |
| GOF1 | 1.6e-07 | 4.4e-01 | 4.8e-05 | 3.5e-02 | 7.1e-01 | 2.2e-01 | 8.7e-01 | 3.4e-02 | 1.4e-01 |
| GOF2 | 1.1e-13 | 4.6e-01 | 4.9e-05 | 4.7e-02 | 7.5e-01 | 2.2e-01 | 8.6e-01 | 4.4e-02 | 1.7e-01 |

Table S25: Goodness-of-fit tests for secondary real data analysis, set 7.

| Exp/Out Method | T2D/ESmk (10) | T2D/FP (10) | T2D/FSmk (10) | T2D/Height (10) | T2D/HOMA (10) | T2D/IHC (10) | T2D/LDL (10) | T2D/RA (10) | T2D/SCZ (8) |
|-------------------|------------------|-------------|------------------|--------------------|------------------|-----------------|-----------------|-------------|-------------|
| GOF1-Max | 1.0e+00 | 1.8e-03 | 9.1e-01 | 5.2e-01 | 7.2e-11 | 9.6e-01 | 9.4e-01 | 8.1e-01 | 8.7e-01 |
| GOF2-Max | 1.0e+00 | 6.0e-04 | 9.0e-01 | 5.2e-01 | 2.0e-12 | 9.6e-01 | 9.4e-01 | 8.0e-01 | 8.6e-01 |
| GOF1 | 1.0e+00 | 1.8e-03 | 9.1e-01 | 5.2e-01 | 7.2e-11 | 9.6e-01 | 9.4e-01 | 8.1e-01 | 8.7e-01 |
| GOF2 | 1.0e+00 | 6.0e-04 | 9.0e-01 | 5.2e-01 | 2.0e-12 | 9.6e-01 | 9.4e-01 | 8.0e-01 | 8.6e-01 |

Table S26: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, ideal case, q=0, N=50000.

| θ | , <u>, </u> | 1 | T | 7 1 7 | | T | | T | |
|--------------------|--|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|
| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.817, | 0.261, | 0.086, | 0.023, | 0.014, | 0.023, | 0.084, | 0.233, | 0.728, |
| | -0.0867, | -0.0394, | -0.0227, | -0.0078, | -0.0007, | 0.0067, | 0.0215, | 0.0382, | 0.0847, |
| | 0.0292, | 0.0262, | 0.0243, | 0.0228, | 0.0228, | 0.0231, | 0.0253, | 0.0279, | 0.0319, |
| | 0.03 | 0.0298 | 0.0295 | 0.0294 | 0.0295 | 0.0297 | 0.0304 | 0.0312 | 0.0331 |
| cML-MA-AIC-Profile | 0.810, | 0.254, | 0.083, | 0.023, | 0.014, | 0.023, | 0.084, | 0.231, | 0.728, |
| | -0.0869, 0.0292, | -0.0395, 0.0262, | -0.0228, | -0.0078, | -0.0007, | 0.0067, 0.0232, | 0.0215, 0.0253, | 0.0382, 0.0280, | 0.0849, |
| | 0.0292, | 0.0202, | 0.0244, 0.0297 | 0.0228, 0.0296 | 0.0228, 0.0297 | 0.0232, | 0.0233, | 0.0280, | 0.0319, 0.0333 |
| cML-AIC | 0.904, | 0.0299 | 0.0297 | 0.0250 | 0.0297 | 0.0233 | 0.0300 | 0.0314 | 0.872, |
| CML-AIC | -0.0932, | -0.0446, | -0.0263, | -0.0094, | -0.0009, | 0.0079, | 0.0251, | 0.0436, | 0.0922, |
| | 0.0321, | 0.0307, | 0.0297, | 0.0288, | 0.0290, | 0.0292, | 0.0310, | 0.0323, | 0.0343, |
| | 0.0246 | 0.025 | 0.0257 | 0.0255 | 0.0257 | 0.0258 | 0.0261 | 0.0264 | 0.0271 |
| cML-AIC-Profile | 0.906, | 0.474, | 0.234, | 0.081, | 0.080, | 0.083, | 0.203, | 0.407, | 0.871, |
| | -0.0935, | -0.0447, | -0.0263, | -0.0094, | -0.0009, | 0.0079, | 0.0251, | 0.0436, | 0.0923, |
| | 0.0321, | 0.0307, | 0.0298, | 0.0288, | 0.0290, | 0.0292, | 0.0310, | 0.0324, | 0.0343, |
| | 0.0248 | 0.0252 | 0.0255 | 0.0257 | 0.0258 | 0.026 | 0.0263 | 0.0265 | 0.0273 |
| cML-MA-BIC | 0.991, | 0.589, | 0.252, | 0.062, | 0.050, | 0.068, | 0.222, | 0.531, | 0.976, |
| | -0.1004, | -0.0504, | -0.0304, | -0.0105, | -0.0005, | 0.0095, | 0.0294, | 0.0493, | 0.0993, |
| | 0.0229, | 0.0232, | 0.0234, | 0.0235, | 0.0236, | 0.0238, | 0.0240, | 0.0243, | 0.0251, |
| | 0.023 | 0.0234 | 0.0236 | 0.0239 | 0.024 | 0.0241 | 0.0244 | 0.0246 | 0.0254 |
| cML-MA-BIC-Profile | 0.991, | 0.583, | 0.248, | 0.061, | 0.049, | 0.068, | 0.219, | 0.525, | 0.976, |
| | -0.1004, | -0.0504, | -0.0304, | -0.0105, | -0.0005, | 0.0095, | 0.0294, | 0.0493, | 0.0993, |
| | 0.0229, | 0.0232, | 0.0234, | 0.0235, | 0.0236, | 0.0238, | 0.0241, | 0.0243, | 0.0251, |
| 10.510 | 0.0231 | 0.0235 | 0.0237 | 0.0239 | 0.0241 | 0.0242 | 0.0244 | 0.0247 | 0.0255 |
| cML-BIC | 0.991, | 0.608, | 0.262, | 0.073, | 0.054, | 0.072, | 0.235, | 0.546, | 0.979, |
| | -0.1005, | -0.0505, | -0.0305, | -0.0105, | -0.0005, | 0.0095, | 0.0295, | 0.0495, | 0.0995, |
| | 0.0229, | 0.0233, | 0.0235, | 0.0237, | 0.0238, | 0.0239, | 0.0242, | 0.0245, | 0.0251, |
| «MI DIC DCI- | 0.0227 | 0.0231 | 0.0233 | 0.0235 | 0.0236 | 0.0238 | 0.024 | 0.0243 | 0.025 |
| cML-BIC-Profile | 0.991, | 0.607, | 0.260, | 0.069, | 0.053, | 0.072, | 0.234, 0.0295, | 0.543, | 0.979, |
| | -0.1005, 0.0229, | -0.0505, 0.0233, | -0.0305, 0.0235, | -0.0105, 0.0237, | -0.0005, 0.0238, | 0.0095, 0.0239, | 0.0295, 0.0242, | 0.0495, 0.0245, | 0.0995, 0.0251, |
| | 0.0229, | 0.0233, | 0.0233, | 0.0237, | 0.0238, | 0.0239, | 0.0242, | 0.0243, | 0.0251, |
| MR-Mix | 0.728, | 0.405, | 0.0234 | 0.063, | 0.0257 | 0.070, | 0.165, | 0.358, | 0.710, |
| WIK-WIX | -0.1007, | -0.0488, | -0.0291, | -0.0101, | -0.0004, | 0.0089, | 0.103, | 0.0456, | 0.0888, |
| | 0.0461, | 0.0398, | 0.0381, | 0.0376, | 0.0372, | 0.0370, | 0.0376, | 0.0392, | 0.0448, |
| | 0.1046 | 0.0826 | 0.0675 | 0.0854 | 0.0551 | 0.0592 | 0.0715 | 0.0901 | 0.083 |
| MR-ContMix | 0.938, | 0.468, | 0.210, | 0.067, | 0.045, | 0.064, | 0.181, | 0.398, | 0.900, |
| | -0.1216, | -0.0689, | -0.0434, | -0.0151, | -0.0016, | 0.0126, | 0.0419, | 0.0674, | 0.1221, |
| | 0.0323, | 0.0391, | 0.0419, | 0.0455, | 0.0460, | 0.0458, | 0.0432, | 0.0406, | 0.0349, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.975, | 0.544, | 0.244, | 0.078, | 0.056, | 0.078, | 0.222, | 0.488, | 0.957, |
| | -0.0998, | -0.0504, | -0.0305, | -0.0105, | -0.0006, | 0.0095, | 0.0296, | 0.0487, | 0.0991, |
| | 0.0246, | 0.0251, | 0.0254, | 0.0260, | 0.0257, | 0.0260, | 0.0261, | 0.0261, | 0.0267, |
| | 0.0241 | 0.0246 | 0.0248 | 0.0251 | 0.0252 | 0.0253 | 0.0256 | 0.0258 | 0.0266 |
| MR-PRESSO | 0.969, | 0.511, | 0.225, | 0.075, | 0.052, | 0.067, | 0.200, | 0.457, | 0.936, |
| | -0.1001, | -0.0503, | -0.0304, | -0.0105, | -0.0005, | 0.0094, | 0.0292, | 0.0491, | 0.0989, |
| | 0.0230, | 0.0234, | 0.0236, | 0.0237, | 0.0239, | 0.0240, | 0.0243, | 0.0245, | 0.0253, |
| MD WWY | 0.0217 | 0.0221 | 0.0223 | 0.0225 | 0.0226 | 0.0227 | 0.023 | 0.0232 | 0.0239 |
| MR-IVW | 0.983, | 0.531, | 0.225, | 0.047, | 0.039, | 0.056, | 0.195, | 0.488, | 0.966, |
| | -0.1001, 0.0226, | -0.0503, 0.0229, | -0.0304, 0.0231, | -0.0105, 0.0233, | -0.0005, 0.0234, | 0.0094, 0.0235, | 0.0293, 0.0238, | 0.0492, 0.0240, | 0.0990, 0.0247, |
| | 0.0220, | 0.0229, | 0.0251, | 0.0253, | 0.0254, | 0.0256 | 0.0258 | 0.0240, | 0.0247, |
| MR-IVW-Oracle | 0.983, | 0.531, | 0.0251 | 0.0233 | 0.0233 | 0.056, | 0.0258 | 0.488, | 0.966, |
| WIK-IV W-Oldele | -0.1001, | -0.0503, | -0.0304, | -0.0105, | -0.0005, | 0.0094, | 0.193, | 0.488, | 0.990, |
| | 0.0226, | 0.0229, | 0.0231, | 0.0233, | 0.0234, | 0.0235, | 0.0238, | 0.0240, | 0.0247, |
| | 0.0244 | 0.0249 | 0.0251 | 0.0253 | 0.0255 | 0.0256 | 0.0258 | 0.0240, | 0.0269 |
| MR-Egger | 0.106, | 0.058, | 0.047, | 0.045, | 0.039, | 0.043, | 0.043, | 0.049, | 0.082, |
| 1556 | -0.0841, | -0.0403, | -0.0228, | -0.0052, | 0.0035, | 0.0123, | 0.0299, | 0.0474, | 0.0912, |
| | 0.1285, | 0.1307, | 0.1317, | 0.1328, | 0.1335, | 0.1341, | 0.1354, | 0.1368, | 0.1407, |
| | 0.1343 | 0.1372 | 0.1385 | 0.1398 | 0.1405 | 0.1413 | 0.1427 | 0.1443 | 0.1484 |
| MR-Weighted-Median | 0.924, | 0.374, | 0.127, | 0.029, | 0.025, | 0.027, | 0.114, | 0.298, | 0.851, |
| - | -0.0992, | -0.0502, | -0.0307, | -0.0110, | -0.0012, | 0.0086, | 0.0282, | 0.0478, | 0.0969, |
| | 0.0265, | 0.0270, | 0.0273, | 0.0275, | 0.0276, | 0.0277, | 0.0280, | 0.0284, | 0.0293, |
| | 0.0304 | 0.0309 | 0.0312 | 0.0315 | 0.0316 | 0.0318 | 0.0321 | 0.0324 | 0.0334 |
| MR-Weighted-Mode | 0.640, | 0.142, | 0.050, | 0.013, | 0.007, | 0.008, | 0.044, | 0.122, | 0.519, |
| | -0.0992, | -0.0505, | -0.0312, | -0.0115, | -0.0015, | 0.0082, | 0.0279, | 0.0475, | 0.0964, |
| | 0.0355, | 0.0365, | 0.0369, | 0.0373, | 0.0376, | 0.0377, | 0.0379, | 0.0381, | 0.0392, |
| 140 D 1 201 | 0.0448 | 0.0457 | 0.046 | 0.0465 | 0.0467 | 0.0469 | 0.0475 | 0.048 | 0.0494 |
| MR-RAPS1 | 0.988, | 0.557, | 0.233, | 0.053, | 0.042, | 0.059, | 0.201, | 0.498, | 0.966, |
| | -0.1005, | -0.0505, | -0.0305, | -0.0105, | -0.0005, | 0.0094, | 0.0294, | 0.0494, | 0.0994, |
| | 0.0226, 0.024 | 0.0230, 0.0244 | 0.0232, | 0.0234, | 0.0235, 0.025 | 0.0236, | 0.0238, 0.0254 | 0.0241, | 0.0248, 0.0265 |
| MD DADCO | | | 0.0247 | 0.0249 | | 0.0251 | | 0.0257 | |
| MR-RAPS2 | 0.982, | 0.603, | 0.306, | 0.141, | 0.128, | 0.143, | 0.283, 0.2962, | 0.554, | 0.963, 0.2696, |
| | 0.2085, 4.1153, | 0.3626, 4.1546, | -0.0550, 3.7213, | 0.3252, 3.3704, | 0.3278, 3.3292, | 0.1586, 2.9538, | 0.2962, 4.1884, | 0.0538, 4.9955, | 0.2696, 4.5346, |
| | 0.0831 | 0.0897 | 0.076 | 0.0641 | 0.0602 | 0.0586 | 0.0748 | 4.9955, 0.0979 | 4.5346, 0.1002 |
| MR-RAPS3 | 0.0831 | 0.607, | 0.076 | 0.070, | 0.050, | 0.0380 | 0.0748 | 0.0979 | 0.1002 |
| MIN-IVAL 93 | -0.1006, | -0.0506, | -0.0306, | -0.0105, | -0.0005, | 0.008, | 0.232, 0.0295, | 0.0495, | 0.981, |
| | 0.0227, | 0.0230, | 0.0232, | 0.0234, | 0.0235, | 0.0033, | 0.0233, | 0.0493, | 0.0333, |
| | 0.0227, | 0.0230, | 0.0232, | 0.0236 | 0.0233, | 0.0236, | 0.0239, | 0.0241, | 0.0248, |
| MR-RAPS4 | 0.987, | 0.587, | 0.0254 | 0.0230 | 0.0237 | 0.067, | 0.0241 | 0.513, | 0.975, |
| | | | -0.0305, | -0.0105, | -0.0005, | 0.007, | 0.217, | 0.0495, | 0.973, |
| | -(),1006 | | | | | | | | |
| MIC IC II D | -0.1006, 0.0232, | -0.0506, 0.0236, | 0.0238, | 0.0240, | 0.0241, | 0.0242, | 0.0245, | 0.0247, | 0.0255, |

Table S27: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the ideal case of q=0, and N=100000.

| θ | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|--------------------------|---|---|--|---|--|--|--|---|--|
| Methods cML-MA-AIC | 0.963, | 0.491, | | 0.023, | 0.012, | 0.032, | | | |
| CML-MA-AIC | -0.0897, | -0.0404, | 0.173, -0.0225, | -0.0065, | 0.012, 0.0004, | 0.032, | 0.185, 0.0233, | 0.469, 0.0413, | 0.937, 0.0898, |
| | 0.0207, | 0.0200, | 0.0182, | 0.0164, | 0.0004, | 0.0166, | 0.0233, | 0.0413, | 0.0333, |
| | 0.0213 | 0.0213 | 0.021 | 0.0207 | 0.0208 | 0.0209 | 0.0216 | 0.0223 | 0.0235 |
| cML-MA-AIC-Profile | 0.962, | 0.490, | 0.170, | 0.023, | 0.012, | 0.032, | 0.184, | 0.469, | 0.936, |
| | -0.0899, | -0.0405, | -0.0225, | -0.0065, | 0.0004, | 0.0076, | 0.0234, | 0.0413, | 0.0899, |
| | 0.0208, | 0.0200, | 0.0182, | 0.0164, | 0.0161, | 0.0166, | 0.0187, | 0.0210, | 0.0232, |
| NG ATO | 0.0213 | 0.0213 | 0.021 | 0.0208 | 0.0208 | 0.021 | 0.0217 | 0.0224 | 0.0235 |
| cML-AIC | 0.986, -0.0947, | 0.688, -0.0446, | 0.349, | 0.103, -0.0071, | 0.079, | 0.120, 0.0089, | 0.356, 0.0263, | 0.664, | 0.976, |
| | 0.0221, | 0.0224, | -0.0255, 0.0215, | 0.0208, | 0.0007, 0.0206, | 0.0089, | 0.0203, | 0.0455, 0.0237, | 0.0950, 0.0252, |
| | 0.0221, | 0.0224, | 0.0213, | 0.0208, | 0.0200, | 0.0210, | 0.0222, | 0.0237, | 0.0232, |
| cML-AIC-Profile | 0.986, | 0.684, | 0.350, | 0.102, | 0.079, | 0.118, | 0.355, | 0.664, | 0.975, |
| | -0.0948, | -0.0446, | -0.0255, | -0.0071, | 0.0007, | 0.0089, | 0.0264, | 0.0456, | 0.0951, |
| | 0.0222, | 0.0224, | 0.0215, | 0.0208, | 0.0206, | 0.0210, | 0.0222, | 0.0237, | 0.0252, |
| | 0.0174 | 0.0178 | 0.0179 | 0.0182 | 0.0183 | 0.0183 | 0.0185 | 0.0187 | 0.0193 |
| cML-MA-BIC | 1.000, | 0.857, | 0.425, | 0.074, | 0.047, | 0.096, | 0.429, | 0.834, | 1.000, |
| | -0.0997, | -0.0496, | -0.0296, | -0.0096, | 0.0004, | 0.0104, | 0.0304, | 0.0504, | 0.1005, |
| | 0.0158, 0.0161 | 0.0161, 0.0165 | 0.0162, 0.0166 | 0.0163, 0.0168 | 0.0164, 0.0168 | 0.0165, 0.0169 | 0.0167, 0.0171 | 0.0169, 0.0173 | 0.0174, 0.0178 |
| cML-MA-BIC-Profile | 1.000, | 0.856, | 0.422, | 0.074, | 0.0108 | 0.0109 | 0.427, | 0.0173 | 1.000, |
| CIVIL-IVIA-DIC-FIOINE | -0.0997, | -0.0496, | -0.0296, | -0.0096, | 0.047, | 0.093, | 0.427, 0.0304, | 0.0504, | 0.1005, |
| | 0.0158, | 0.0161, | 0.0162, | 0.0163, | 0.0004, | 0.0165, | 0.0167, | 0.0169, | 0.1003, |
| | 0.0162 | 0.0165 | 0.0166 | 0.0168 | 0.0169 | 0.017 | 0.0171 | 0.0173 | 0.0174, |
| cML-BIC | 1.000, | 0.863, | 0.436, | 0.077, | 0.052, | 0.098, | 0.444, | 0.843, | 1.000, |
| | -0.0998, | -0.0497, | -0.0297, | -0.0097, | 0.0004, | 0.0104, | 0.0304, | 0.0504, | 0.1005, |
| | 0.0158, | 0.0161, | 0.0162, | 0.0164, | 0.0165, | 0.0166, | 0.0168, | 0.0169, | 0.0175, |
| M. DIC 7. C. | 0.016 | 0.0163 | 0.0164 | 0.0166 | 0.0167 | 0.0167 | 0.0169 | 0.0171 | 0.0176 |
| cML-BIC-Profile | 1.000, | 0.863, | 0.436, | 0.077, | 0.052, | 0.096, | 0.444, | 0.843, | 1.000, |
| | -0.0998, 0.0158, | -0.0497, 0.0161, | -0.0297, 0.0162, | -0.0097, 0.0164, | 0.0004, 0.0165, | 0.0104, 0.0166, | 0.0304, 0.0168, | 0.0504, 0.0169, | 0.1005, 0.0175, |
| | 0.0158, | 0.0161, | 0.0162, | 0.0164, | 0.0165, | 0.0166, | 0.0168, | 0.0169, | 0.0175, |
| MR-Mix | 0.784, | 0.562, | 0.0103 | 0.070 | 0.062, | 0.0108 | 0.017 | 0.555, | 0.780, |
| | -0.0965, | -0.0466, | -0.0271, | -0.0086, | 0.0007, | 0.0101, | 0.0282, | 0.0461, | 0.0886, |
| | 0.0400, | 0.0298, | 0.0277, | 0.0267, | 0.0266, | 0.0268, | 0.0278, | 0.0297, | 0.0387, |
| | 0.0397 | 0.0788 | 0.0689 | 0.0939 | 0.1207 | 0.05 | 0.0602 | 0.1415 | 0.0599 |
| MR-ContMix | 1.000, | 0.703, | 0.321, | 0.070, | 0.051, | 0.093, | 0.333, | 0.680, | 0.994, |
| | -0.1137, | -0.0644, | -0.0404, | -0.0138, | 0.0010, | 0.0152, | 0.0423, | 0.0658, | 0.1163, |
| | 0.0202, | 0.0248, | 0.0284, | 0.0314, | 0.0321, | 0.0319, | 0.0293, | 0.0261, | 0.0217, |
| MR-Lasso | NA 1.000, | NA 0.795, | NA 0.394, | NA 0.080, | NA 0.050, | NA 0.092, | NA 0.403, | NA 0.783, | NA 1.000, |
| WIK-Lasso | -0.0994, | -0.0493, | -0.0296, | -0.0093, | 0.0005, | 0.0103, | 0.0303, | 0.0505, | 0.1003, |
| | 0.0171, | 0.0171, | 0.0175, | 0.0179, | 0.0176, | 0.0178, | 0.0179, | 0.0183, | 0.0187, |
| | 0.017 | 0.0174 | 0.0176 | 0.0178 | 0.0178 | 0.0179 | 0.0181 | 0.0183 | 0.0188 |
| MR-PRESSO | 1.000, | 0.781, | 0.374, | 0.077, | 0.056, | 0.092, | 0.351, | 0.746, | 0.999, |
| | -0.0996, | -0.0496, | -0.0296, | -0.0096, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0160, | 0.0162, | 0.0164, | 0.0165, | 0.0166, | 0.0167, | 0.0169, | 0.0170, | 0.0175, |
| MD TUTY | 0.0154 | 0.0157 | 0.0159 | 0.016 | 0.0161 | 0.0162 | 0.0163 | 0.0165 | 0.017 |
| MR-IVW | 1.000, -0.0995, | 0.818, -0.0496, | 0.371, -0.0296, | 0.055, -0.0096, | 0.041, 0.0004, | 0.077, 0.0104, | 0.382, 0.0304, | 0.795, 0.0504, | 1.000, 0.1004, |
| | 0.0158, | 0.0160, | 0.0161, | 0.0163, | 0.0004, | 0.0164, | 0.0304, | 0.0304, | 0.1004, |
| | 0.0172 | 0.0175 | 0.0177 | 0.0179 | 0.0179 | 0.018 | 0.0182 | 0.0184 | 0.019 |
| MR-IVW-Oracle | 1.000, | 0.818, | 0.371, | 0.055, | 0.041, | 0.077, | 0.382, | 0.795, | 1.000, |
| | -0.0995, | -0.0496, | -0.0296, | -0.0096, | 0.0004, | 0.0104, | 0.0304, | 0.0504, | 0.1004, |
| | 0.0158, | 0.0160, | 0.0161, | 0.0163, | 0.0164, | 0.0164, | 0.0166, | 0.0168, | 0.0173, |
| | 0.0172 | 0.0175 | 0.0177 | 0.0179 | 0.0179 | 0.018 | 0.0182 | 0.0184 | 0.019 |
| MR-Egger | 0.161, | 0.079, | 0.050, | 0.035, | 0.032, | 0.029, | 0.034, | 0.059, | 0.142, |
| | -0.0938, | -0.0469, | -0.0282, | -0.0094, | 0.0000, | 0.0093, | 0.0281, | 0.0469, | 0.0938, |
| | 0.0886, 0.0965 | 0.0900, 0.0986 | 0.0907, 0.0995 | 0.0914, 0.1005 | 0.0918, 0.101 | 0.0922, 0.1015 | 0.0931, 0.1026 | 0.0940, 0.1038 | 0.0967, 0.1068 |
| MR-Weighted-Median | 0.0903 | 0.627, | 0.0993 | 0.1003 | 0.101 | 0.1013 | 0.1026 | 0.1038 | 0.1008 |
| 1711C- Weighten-Wiethall | -0.0991, | -0.0495, | -0.0297, | -0.0098, | 0.028, | 0.040, | 0.232, 0.0300, | 0.002, | 0.993, |
| | 0.0187, | 0.0191, | 0.0192, | 0.0194, | 0.0195, | 0.0196, | 0.0199, | 0.0201, | 0.0206, |
| | 0.0214 | 0.0218 | 0.022 | 0.0222 | 0.0223 | 0.0224 | 0.0226 | 0.0229 | 0.0236 |
| MR-Weighted-Mode | 0.912, | 0.316, | 0.090, | 0.011, | 0.006, | 0.012, | 0.097, | 0.327, | 0.854, |
| | -0.0986, | -0.0489, | -0.0290, | -0.0091, | 0.0008, | 0.0107, | 0.0303, | 0.0502, | 0.0997, |
| | 0.0251, | 0.0254, | 0.0256, | 0.0259, | 0.0261, | 0.0262, | 0.0266, | 0.0270, | 0.0280, |
| 1 | | | 0.0326 | 0.0329 | 0.0331 | 0.0332 | 0.0336 | 0.034 | 0.035 |
| MD D + DC - | 0.0317 | 0.0323 | | 0.001 | | 0.000 | 0.402 | | |
| MR-RAPS1 | 0.0317 1.000, | 0.834, | 0.392, | 0.061, | 0.041, | 0.082, | 0.403, | 0.816, | 1.000, |
| MR-RAPS1 | 0.0317 1.000, -0.0998, | 0.834, -0.0497, | 0.392, -0.0297, | -0.0096, | 0.0004, | 0.0104, | 0.0304, | 0.0505, | 0.1006, |
| MR-RAPS1 | 0.0317 1.000, -0.0998, 0.0158, | 0.834, -0.0497, 0.0161, | 0.392, -0.0297, 0.0162, | -0.0096, 0.0163, | 0.0004, 0.0164, | 0.0104, 0.0165, | 0.0304, 0.0166, | 0.0505, 0.0168, | 0.1006, 0.0173, |
| | 0.0317 1.000, -0.0998, 0.0158, 0.0169 | 0.834, -0.0497, 0.0161, 0.0172 | 0.392, -0.0297, 0.0162, 0.0173 | -0.0096, 0.0163, 0.0175 | 0.0004, 0.0164, 0.0176 | 0.0104, 0.0165, 0.0177 | 0.0304, 0.0166, 0.0178 | 0.0505, 0.0168, 0.018 | 0.1006, 0.0173, 0.0186 |
| MR-RAPS1 MR-RAPS2 | 0.0317 1.000, -0.0998, 0.0158, | 0.834, -0.0497, 0.0161, | 0.392, -0.0297, 0.0162, | -0.0096, 0.0163, | 0.0004, 0.0164, | 0.0104, 0.0165, | 0.0304, 0.0166, | 0.0505, 0.0168, | 0.1006, 0.0173, |
| | 0.0317 1.000, -0.0998, 0.0158, 0.0169 1.000, 0.1027, 1.0726, | 0.834, -0.0497, 0.0161, 0.0172 0.853, -0.0015, 2.4214, | 0.392, -0.0297, 0.0162, 0.0173 0.492, 0.1487, 2.5566, | -0.0096, 0.0163, 0.0175 0.184, 0.1367, 2.4835, | 0.0004, 0.0164, 0.0176 0.131, 0.1945, 2.1665, | 0.0104, 0.0165, 0.0177 0.176, 0.1989, 2.4643, | 0.0304, 0.0166, 0.0178 0.470, 0.3043, 2.6780, | 0.0505, 0.0168, 0.018 0.829, 0.1506, 2.5923, | 0.1006, 0.0173, 0.0186 0.999, 0.2744, 1.5985, |
| MR-RAPS2 | 0.0317 1.000, -0.0998, 0.0158, 0.0169 1.000, 0.1027, 1.0726, 0.0351 | 0.834, -0.0497, 0.0161, 0.0172 0.853, -0.0015, 2.4214, 0.0583 | 0.392, -0.0297, 0.0162, 0.0173 0.492, 0.1487, 2.5566, 0.0549 | -0.0096, 0.0163, 0.0175 0.184, 0.1367, 2.4835, 0.049 | 0.0004, 0.0164, 0.0176 0.131, 0.1945, 2.1665, 0.0422 | 0.0104, 0.0165, 0.0177 0.176, 0.1989, 2.4643, 0.0461 | 0.0304, 0.0166, 0.0178 0.470, 0.3043, 2.6780, 0.0576 | 0.0505, 0.0168, 0.018 0.829, 0.1506, 2.5923, 0.0593 | 0.1006, 0.0173, 0.0186 0.999, 0.2744, 1.5985, 0.0441 |
| | 0.0317 1.000, -0.0998, 0.0158, 0.0169 1.000, 0.1027, 1.0726, 0.0351 1.000, | 0.834, -0.0497, 0.0161, 0.0172 0.853, -0.0015, 2.4214, 0.0583 0.864, | 0.392, -0.0297, 0.0162, 0.0173 0.492, 0.1487, 2.5566, 0.0549 0.435, | -0.0096, 0.0163, 0.0175 0.184, 0.1367, 2.4835, 0.049 0.075, | 0.0004, 0.0164, 0.0176 0.131, 0.1945, 2.1665, 0.0422 0.050, | 0.0104, 0.0165, 0.0177 0.176, 0.1989, 2.4643, 0.0461 0.096, | 0.0304, 0.0166, 0.0178 0.470, 0.3043, 2.6780, 0.0576 | 0.0505, 0.0168, 0.018 0.829, 0.1506, 2.5923, 0.0593 | 0.1006, 0.0173, 0.0186 0.999, 0.2744, 1.5985, 0.0441 1.000, |
| MR-RAPS2 | 0.0317 1.000, -0.0998, 0.0158, 0.0169 1.000, 0.1027, 1.0726, 0.0351 1.000, -0.0998, | 0.834, -0.0497, 0.0161, 0.0172 0.853, -0.0015, 2.4214, 0.0583 0.864, -0.0497, | 0.392, -0.0297, 0.0162, 0.0173 0.492, 0.1487, 2.5566, 0.0549 0.435, -0.0296, | -0.0096, 0.0163, 0.0175 0.184, 0.1367, 2.4835, 0.049 0.075, -0.0096, | 0.0004, 0.0164, 0.0176 0.131, 0.1945, 2.1665, 0.0422 0.050, 0.0004, | 0.0104, 0.0165, 0.0177 0.176, 0.1989, 2.4643, 0.0461 0.096, 0.0104, | 0.0304, 0.0166, 0.0178 0.470, 0.3043, 2.6780, 0.0576 0.445, 0.0305, | 0.0505, 0.0168, 0.018 0.829, 0.1506, 2.5923, 0.0593 0.844, 0.0505, | 0.1006, 0.0173, 0.0186 0.999, 0.2744, 1.5985, 0.0441 1.000, 0.1006, |
| MR-RAPS2 | 0.0317 1.000, -0.0998, 0.0158, 0.0169 1.000, 0.1027, 1.0726, 0.0351 1.000, -0.0998, 0.0158, | 0.834, -0.0497, 0.0161, 0.0172 0.853, -0.0015, 2.4214, 0.0583 0.864, -0.0497, 0.0161, | 0.392, -0.0297, 0.0162, 0.0173 0.492, 0.1487, 2.5566, 0.0549 0.435, -0.0296, 0.0162, | -0.0096, 0.0163, 0.0175 0.184, 0.1367, 2.4835, 0.049 0.075, -0.0096, 0.0163, | 0.0004, 0.0164, 0.0176 0.131, 0.1945, 2.1665, 0.0422 0.050, 0.0004, 0.0164, | 0.0104, 0.0165, 0.0177 0.176, 0.1989, 2.4643, 0.0461 0.096, 0.0104, 0.0165, | 0.0304, 0.0166, 0.0178 0.470, 0.3043, 2.6780, 0.0576 0.445, 0.0305, 0.0166, | 0.0505, 0.0168, 0.018 0.829, 0.1506, 2.5923, 0.0593 0.844, 0.0505, 0.0168, | 0.1006, 0.0173, 0.0186 0.999, 0.2744, 1.5985, 0.0441 1.000, 0.1006, 0.0173, |
| MR-RAPS2 MR-RAPS3 | 0.0317 1.000, -0.0998, 0.0158, 0.0169 1.000, 0.1027, 1.0726, 0.0351 1.000, -0.0998, 0.0158, 0.016 | 0.834, -0.0497, 0.0161, 0.0172 0.853, -0.0015, 2.4214, 0.0583 0.864, -0.0497, 0.0161, 0.0163 | 0.392, -0.0297, 0.0162, 0.0173 0.492, 0.1487, 2.5566, 0.0549 0.435, -0.0296, 0.0162, 0.0164 | -0.0096, 0.0163, 0.0175 0.184, 0.1367, 2.4835, 0.049 0.075, -0.0096, 0.0163, 0.0166 | 0.0004, 0.0164, 0.0176 0.131, 0.1945, 2.1665, 0.0422 0.050, 0.0004, 0.0164, 0.0167 | 0.0104, 0.0165, 0.0177 0.176, 0.1989, 2.4643, 0.0461 0.096, 0.0104, 0.0165, 0.0168 | 0.0304, 0.0166, 0.0178 0.470, 0.3043, 2.6780, 0.0576 0.445, 0.0305, 0.0166, 0.0169 | 0.0505, 0.0168, 0.018 0.829, 0.1506, 2.5923, 0.0593 0.844, 0.0505, 0.0168, 0.0171 | 0.1006, 0.0173, 0.0186 0.999, 0.2744, 1.5985, 0.0441 1.000, 0.1006, 0.0173, 0.0177 |
| MR-RAPS2 | 0.0317 1.000, -0.0998, 0.0158, 0.0169 1.000, 0.1027, 1.0726, 0.0351 1.000, -0.0998, 0.0158, 0.016 1.000, | 0.834, -0.0497, 0.0161, 0.0172 0.853, -0.0015, 2.4214, 0.0583 0.864, -0.0497, 0.0161, 0.0163 | 0.392, -0.0297, 0.0162, 0.0173 0.492, 0.1487, 2.5566, 0.0549 0.435, -0.0296, 0.0162, 0.0164 | -0.0096, 0.0163, 0.0175 0.184, 0.1367, 2.4835, 0.049 0.075, -0.0096, 0.0163, 0.0166 | 0.0004, 0.0164, 0.0176 0.131, 0.1945, 2.1665, 0.0422 0.050, 0.0004, 0.0164, 0.0167 | 0.0104, 0.0165, 0.0177 0.176, 0.1989, 2.4643, 0.0461 0.096, 0.0104, 0.0165, 0.0168 | 0.0304, 0.0166, 0.0178 0.470, 0.3043, 2.6780, 0.0576 0.445, 0.0305, 0.0166, 0.0169 | 0.0505, 0.0168, 0.018 0.829, 0.1506, 2.5923, 0.0593 0.844, 0.0505, 0.0168, 0.0171 | 0.1006, 0.0173, 0.0186 0.999, 0.2744, 1.5985, 0.0441 1.000, 0.1006, 0.0173, 0.0177 |
| MR-RAPS2 MR-RAPS3 | 0.0317 1.000, -0.0998, 0.0158, 0.0169 1.000, 0.1027, 1.0726, 0.0351 1.000, -0.0998, 0.0158, 0.016 | 0.834, -0.0497, 0.0161, 0.0172 0.853, -0.0015, 2.4214, 0.0583 0.864, -0.0497, 0.0161, 0.0163 | 0.392, -0.0297, 0.0162, 0.0173 0.492, 0.1487, 2.5566, 0.0549 0.435, -0.0296, 0.0162, 0.0164 | -0.0096, 0.0163, 0.0175 0.184, 0.1367, 2.4835, 0.049 0.075, -0.0096, 0.0163, 0.0166 | 0.0004, 0.0164, 0.0176 0.131, 0.1945, 2.1665, 0.0422 0.050, 0.0004, 0.0164, 0.0167 | 0.0104, 0.0165, 0.0177 0.176, 0.1989, 2.4643, 0.0461 0.096, 0.0104, 0.0165, 0.0168 | 0.0304, 0.0166, 0.0178 0.470, 0.3043, 2.6780, 0.0576 0.445, 0.0305, 0.0166, 0.0169 | 0.0505, 0.0168, 0.018 0.829, 0.1506, 2.5923, 0.0593 0.844, 0.0505, 0.0168, 0.0171 | 0.1006, 0.0173, 0.0186 0.999, 0.2744, 1.5985, 0.0441 1.000, 0.1006, 0.0173, 0.0177 |

Table S28: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the ideal case of q=0, and N=200000.

| | , , | 1 | 1 | | - | 1 | 1 | | |
|---------------------|---------------------|---------------------|---------------------|---------------------|-------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|
| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| | 0.000 | 0.000 | 0.402 | 0.052 | 0.020 | 0.045 | 0.220 | 0.720 | T 0.000 |
| cML-MA-AIC | 0.999, -0.0942, | 0.809, -0.0443, | 0.402, -0.0252, | 0.053, -0.0082, | 0.020, -0.0008, | 0.045, 0.0065, | 0.338, 0.0232, | 0.739, 0.0420, | 0.990, 0.0915, |
| | 0.0147, | 0.0148, | 0.0232, | 0.0120, | 0.0116, | 0.0063, | 0.0232, | 0.0420, | 0.0913, |
| | 0.015 | 0.0152 | 0.015 | 0.0146 | 0.0147 | 0.0148 | 0.0154 | 0.016 | 0.0166 |
| cML-MA-AIC-Profile | 0.999, | 0.809, | 0.402, | 0.053, | 0.020, | 0.045, | 0.337, | 0.739, | 0.990, |
| | -0.0944, | -0.0443, | -0.0252, | -0.0082, | -0.0008, | 0.0065, | 0.0232, | 0.0420, | 0.0916, |
| | 0.0148, | 0.0148, | 0.0139, | 0.0120, | 0.0116, | 0.0119, | 0.0138, | 0.0152, | 0.0163, |
| | 0.0151 | 0.0152 | 0.015 | 0.0147 | 0.0147 | 0.0148 | 0.0155 | 0.016 | 0.0166 |
| cML-AIC | 1.000, | 0.925, | 0.600, | 0.146, | 0.071, | 0.127, | 0.536, | 0.876, | 0.996, |
| | -0.0978, 0.0156, | -0.0478, 0.0159, | -0.0282, 0.0156, | -0.0095, 0.0146, | -0.0009, 0.0145, | 0.0076, 0.0147, | 0.0260, 0.0156, | 0.0453, 0.0167, | 0.0952, 0.0175, |
| | 0.0136, | 0.0139, | 0.0136, | 0.0146, | 0.0143, | 0.0147, | 0.0136, | 0.0107, | 0.0175, |
| cML-AIC-Profile | 1.000, | 0.925, | 0.601, | 0.147, | 0.071, | 0.126, | 0.535, | 0.877, | 0.996, |
| | -0.0980, | -0.0478, | -0.0282, | -0.0096, | -0.0009, | 0.0076, | 0.0260, | 0.0453, | 0.0953, |
| | 0.0156, | 0.0159, | 0.0156, | 0.0146, | 0.0145, | 0.0147, | 0.0156, | 0.0167, | 0.0175, |
| | 0.0123 | 0.0125 | 0.0126 | 0.0128 | 0.0128 | 0.0129 | 0.013 | 0.0131 | 0.0135 |
| cML-MA-BIC | 1.000, | 0.991, | 0.738, | 0.132, | 0.053, | 0.120, | 0.692, | 0.986, | 1.000, |
| | -0.1004, | -0.0504, | -0.0304, | -0.0104, | -0.0004, | 0.0096, | 0.0296, | 0.0496, | 0.0996, |
| | 0.0111, 0.0114 | 0.0114, 0.0116 | 0.0115, 0.0117 | 0.0116, 0.0118 | 0.0116, 0.0119 | 0.0117, 0.0119 | 0.0119, 0.0121 | 0.0120, 0.0122 | 0.0124, 0.0126 |
| cML-MA-BIC-Profile | 1.000, | 0.0110 | 0.738, | 0.0118 | 0.0119 | 0.0119 | 0.691, | 0.986, | 1.000, |
| CML-MA-DIC-HOME | -0.1004, | -0.0504, | -0.0304, | -0.0104, | -0.0004, | 0.0096, | 0.0296, | 0.0496, | 0.0996, |
| | 0.0111, | 0.0114, | 0.0115, | 0.0116, | 0.0116, | 0.0117, | 0.0119, | 0.0120, | 0.0124, |
| | 0.0114 | 0.0116 | 0.0117 | 0.0118 | 0.0119 | 0.0119 | 0.0121 | 0.0122 | 0.0126 |
| cML-BIC | 1.000, | 0.991, | 0.747, | 0.138, | 0.056, | 0.127, | 0.700, | 0.986, | 1.000, |
| | -0.1004, | -0.0504, | -0.0304, | -0.0104, | -0.0004, | 0.0096, | 0.0296, | 0.0496, | 0.0997, |
| | 0.0112, | 0.0114, | 0.0115, | 0.0116, | 0.0117, | 0.0118, | 0.0119, | 0.0120, | 0.0124, |
| aML DIC Description | 0.0113 | 0.0115 | 0.0116 | 0.0117 | 0.0118 | 0.0118 | 0.012 | 0.0121 | 0.0125 |
| cML-BIC-Profile | 1.000, -0.1004, | 0.991, -0.0504, | 0.746, -0.0304, | 0.138, -0.0104, | 0.056, -0.0004, | 0.126, 0.0096, | 0.699, 0.0296, | 0.986, 0.0496, | 1.000, 0.0997, |
| | 0.0112, | 0.0114, | 0.0304, | 0.0104, | 0.0117, | 0.0096, | 0.0296, 0.0119, | 0.0496, 0.0120, | 0.0997, 0.0124, |
| | 0.0113 | 0.0115 | 0.0116 | 0.0117 | 0.0117, | 0.0118 | 0.012 | 0.0121 | 0.0125 |
| MR-Mix | 0.843, | 0.734, | 0.528, | 0.103, | 0.050, | 0.094, | 0.464, | 0.712, | 0.836, |
| | -0.0985, | -0.0484, | -0.0293, | -0.0102, | -0.0008, | 0.0085, | 0.0267, | 0.0447, | 0.0889, |
| | 0.0333, | 0.0222, | 0.0188, | 0.0168, | 0.0167, | 0.0167, | 0.0187, | 0.0217, | 0.0303, |
| | 0.0504 | 0.0459 | 0.0576 | 0.0535 | 0.0485 | 0.0696 | 0.0701 | 0.0583 | 0.0313 |
| MR-ContMix | 1.000, | 0.955, | 0.606, | 0.128, | 0.051, | 0.107, | 0.527, | 0.911, | 1.000, |
| | -0.1081, | -0.0617, | -0.0410, 0.0179, | -0.0159, 0.0210, | -0.0010, 0.0219, | 0.0133, 0.0217, | 0.0392, | 0.0605, | 0.1080, |
| | 0.0137, NA | 0.0156, NA | 0.0179, NA | 0.0210, NA | 0.0219, NA | 0.0217, NA | 0.0192, NA | 0.0169, NA | 0.0150, NA |
| MR-Lasso | 1.000, | 0.982, | 0.690, | 0.136, | 0.049, | 0.115, | 0.642, | 0.964, | 1.000, |
| THE LABOU | -0.1004, | -0.0506, | -0.0306, | -0.0105, | -0.0006, | 0.0094, | 0.0294, | 0.0494, | 0.0994, |
| | 0.0120, | 0.0122, | 0.0124, | 0.0125, | 0.0124, | 0.0126, | 0.0129, | 0.0128, | 0.0133, |
| | 0.012 | 0.0123 | 0.0124 | 0.0125 | 0.0126 | 0.0126 | 0.0128 | 0.0129 | 0.0132 |
| MR-PRESSO | 1.000, | 0.973, | 0.679, | 0.132, | 0.048, | 0.113, | 0.616, | 0.951, | 1.000, |
| | -0.1004, | -0.0504, | -0.0304, | -0.0105, | -0.0005, | 0.0095, | 0.0295, | 0.0495, | 0.0995, |
| | 0.0112, | 0.0115, | 0.0116, | 0.0117, | 0.0118, | 0.0118, | 0.0120, 0.0114 | 0.0121, | 0.0125, |
| MR-IVW | 0.0108 1.000, | 0.011 0.986, | 0.0111 0.696, | 0.0112 0.120, | 0.0112 0.042, | 0.0113 0.100, | 0.651, | 0.0116 0.969, | 0.0119 1.000, |
| IVIIX-I V VV | -0.1003, | -0.0504, | -0.0304, | -0.0104, | -0.0004, | 0.100, | 0.031, | 0.909, | 0.0995, |
| | 0.0112, | 0.0114, | 0.0115, | 0.0116, | 0.0117, | 0.0117, | 0.0119, | 0.0120, | 0.0124, |
| | 0.0121 | 0.0124 | 0.0125 | 0.0126 | 0.0127 | 0.0127 | 0.0129 | 0.013 | 0.0134 |
| MR-IVW-Oracle | 1.000, | 0.986, | 0.696, | 0.120, | 0.042, | 0.100, | 0.651, | 0.969, | 1.000, |
| | -0.1003, | -0.0504, | -0.0304, | -0.0104, | -0.0004, | 0.0095, | 0.0295, | 0.0495, | 0.0995, |
| | 0.0112, | 0.0114, | 0.0115, | 0.0116, | 0.0117, | 0.0117, | 0.0119, | 0.0120, | 0.0124, |
| 1 m F | 0.0121 | 0.0124 | 0.0125 | 0.0126 | 0.0127 | 0.0127 | 0.0129 | 0.013 | 0.0134 |
| MR-Egger | 0.283, -0.0936, | 0.091, -0.0455, | 0.061, -0.0263, | 0.039, -0.0070, | 0.039, 0.0026, | 0.041, 0.0122, | 0.058, 0.0314, | 0.085, 0.0507, | 0.257, 0.0988, |
| | 0.0641, | 0.0653, | 0.0658, | 0.0664, | 0.0668, | 0.0122, | 0.0514, 0.0678, | 0.0307, | 0.0988, |
| | 0.0691 | 0.0705 | 0.0711 | 0.0718 | 0.0721 | 0.0725 | 0.0732 | 0.074 | 0.0761 |
| MR-Weighted-Median | 1.000, | 0.918, | 0.516, | 0.065, | 0.029, | 0.058, | 0.442, | 0.883, | 1.000, |
| - | -0.1004, | -0.0506, | -0.0307, | -0.0108, | -0.0008, | 0.0091, | 0.0290, | 0.0488, | 0.0985, |
| | 0.0134, | 0.0137, | 0.0138, | 0.0139, | 0.0140, | 0.0140, | 0.0142, | 0.0143, | 0.0148, |
| MD W/ 1 - 127 / | 0.0151 | 0.0154 | 0.0155 | 0.0157 | 0.0157 | 0.0158 | 0.016 | 0.0162 | 0.0166 |
| MR-Weighted-Mode | 0.995, | 0.662, | 0.229, | 0.032, | 0.013, | 0.025, | 0.184, | 0.564, | 0.979, |
| | -0.1006, 0.0176, | -0.0509, 0.0181, | -0.0311, 0.0184, | -0.0112, 0.0186, | -0.0013, 0.0187, | 0.0086, 0.0188, | 0.0284, 0.0190, | 0.0483, 0.0192, | 0.0976, 0.0197, |
| | 0.0176, | 0.0181, | 0.0184, | 0.0186, | 0.0187, | 0.0188, | 0.0190, | 0.0192, | 0.0197, |
| MR-RAPS1 | 1.000, | 0.988, | 0.706, | 0.0233 | 0.0233 | 0.106, | 0.670, | 0.974, | 1.000, |
| | -0.1005, | -0.0504, | -0.0304, | -0.0104, | -0.0004, | 0.0096, | 0.0296, | 0.0496, | 0.0996, |
| | 0.0112, | 0.0114, | 0.0115, | 0.0116, | 0.0117, | 0.0117, | 0.0119, | 0.0120, | 0.0124, |
| | 0.0119 | 0.0121 | 0.0122 | 0.0124 | 0.0124 | 0.0125 | 0.0126 | 0.0127 | 0.0131 |
| MR-RAPS2 | 1.000, | 0.984, | 0.753, | 0.239, | 0.151, | 0.213, | 0.714, | 0.971, | 1.000, |
| | -0.0155, | 0.0743, | 0.0333, | 0.1931, | 0.0831, | 0.1960, | 0.1130, | 0.1235, | 0.1630, |
| | 0.3022, | 1.0341, | 1.4742, | 2.2589, 0.0358 | 1.8815, | 2.0820, | 1.8206, | 1.1682, | 0.4813, |
| MD_DADC2 | 0.0151 1.000, | 0.0308 | 0.0393 | 0.0358 | 0.0335 0.055, | 0.0336 0.124, | 0.0418 | 0.0342 0.986, | 0.0201 1.000, |
| MR-RAPS3 | -0.1005, | -0.0505, | -0.0305, | -0.0105, | -0.0004, | 0.124, 0.0096, | 0.099, | 0.986, | 0.0996, |
| | 0.0112, | 0.0114, | 0.0115, | 0.0116, | 0.0117, | 0.0030, | 0.0119, | 0.0120, | 0.0124, |
| | 0.0113 | 0.0115 | 0.0116 | 0.0117 | 0.0117, | 0.0118 | 0.012 | 0.0120, | 0.0125 |
| | | 0.992, | 0.726, | 0.132, | 0.053, | 0.118, | 0.683, | 0.978, | 1.000, |
| MR-RAPS4 | 1.000, | 0.552, | | | | | | | |
| MR-RAPS4 | -0.1006, | -0.0505, | -0.0280, | -0.0103, | -0.0005, | 0.0099, | 0.0299, | 0.0504, | 0.0995, |
| MR-RAPS4 | | | | | -0.0005, 0.0118, 0.0121 | 0.0099, 0.0158, 0.0122 | 0.0299, 0.0145, 0.0123 | 0.0504, 0.0240, 0.0124 | 0.0995, 0.0126, 0.0128 |

Table S29: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE satisfied, q=0.2, and N=50000.

| , , | <i>' '</i> | | | | | | | | |
|--------------------|---------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.680, | 0.204, | 0.072, | 0.020, | 0.022, | 0.023, | 0.065, | 0.164, | 0.607, |
| | -0.0831, | -0.0371, | -0.0216, | -0.0075, | -0.0004, | 0.0065, | 0.0207, | 0.0368, | 0.0818, |
| | 0.0338, | 0.0304, | 0.0277, | 0.0261, | 0.0259, | 0.0261, | 0.0278, | 0.0303, | 0.0357, |
| | 0.0347 | 0.0341 | 0.0338 | 0.0338 | 0.0339 | 0.034 | 0.0348 | 0.0356 | 0.0379 |
| cML-MA-AIC-Profile | 0.670, | 0.199, | 0.070, | 0.020, | 0.021, | 0.023, | 0.063, | 0.163, | 0.604, |
| | -0.0833, | -0.0372, | -0.0216, | -0.0075, | -0.0004, | 0.0065, | 0.0207, | 0.0368, | 0.0820, |
| | 0.0338, | 0.0305, | 0.0278, | 0.0261, | 0.0259, | 0.0261, | 0.0278, | 0.0303, | 0.0358, |
|) // LIC | 0.0349 | 0.0343 | 0.034 | 0.034 | 0.0341 | 0.0342 | 0.035 | 0.0358 | 0.0381 |
| cML-AIC | 0.828, | 0.380, | 0.205, | 0.090, | 0.073, | 0.098, | 0.175, | 0.355, | 0.772, |
| | -0.0908, | -0.0428, | -0.0250, | -0.0083, | -0.0004, | 0.0082, | 0.0245, | 0.0426, | 0.0903, |
| | 0.0381, 0.028 | 0.0360, 0.0284 | 0.0344, 0.0288 | 0.0333, 0.029 | 0.0332, 0.0292 | 0.0334, 0.0293 | 0.0349, 0.0296 | 0.0366, 0.03 | 0.0409, 0.0307 |
| cML-AIC-Profile | | | | 0.029 | | 0.0293 | | 0.05 | |
| CML-AIC-FIGHE | 0.827, -0.0911, | 0.375, -0.0428, | 0.201, -0.0251, | -0.0084, | 0.072, -0.0004, | 0.093, | 0.174, 0.0245, | 0.0426, | 0.772, 0.0904, |
| | 0.0381, | 0.0360, | 0.0345, | 0.0333, | 0.0332, | 0.0334, | 0.0243, | 0.0366, | 0.0410, |
| | 0.0282 | 0.0286 | 0.029 | 0.0292 | 0.0294 | 0.0295 | 0.0298 | 0.0301 | 0.0309 |
| cML-MA-BIC | 0.969, | 0.475, | 0.214, | 0.068, | 0.051, | 0.061, | 0.197, | 0.441, | 0.937, |
| | -0.1001, | -0.0501, | -0.0302, | -0.0102, | -0.0003, | 0.0097, | 0.0296, | 0.0495, | 0.0995, |
| | 0.0262, | 0.0266, | 0.0268, | 0.0270, | 0.0271, | 0.0273, | 0.0276, | 0.0280, | 0.0289, |
| | 0.0261 | 0.0266 | 0.0268 | 0.0271 | 0.0272 | 0.0273 | 0.0276 | 0.0279 | 0.0287 |
| cML-MA-BIC-Profile | 0.969, | 0.472, | 0.211, | 0.068, | 0.050, | 0.059, | 0.196, | 0.439, | 0.933, |
| | -0.1001, | -0.0501, | -0.0302, | -0.0102, | -0.0003, | 0.0097, | 0.0296, | 0.0495, | 0.0995, |
| | 0.0262, | 0.0266, | 0.0268, | 0.0270, | 0.0271, | 0.0273, | 0.0276, | 0.0280, | 0.0289, |
| | 0.0262 | 0.0267 | 0.0269 | 0.0272 | 0.0273 | 0.0274 | 0.0277 | 0.028 | 0.0289 |
| cML-BIC | 0.973, | 0.487, | 0.219, | 0.074, | 0.055, | 0.065, | 0.203, | 0.447, | 0.942, |
| | -0.1002, | -0.0503, | -0.0303, | -0.0103, | -0.0003, | 0.0097, | 0.0298, | 0.0498, | 0.0997, |
| | 0.0260, | 0.0266, | 0.0268, | 0.0271, | 0.0272, | 0.0274, | 0.0276, | 0.0280, | 0.0289, |
| | 0.0258 | 0.0262 | 0.0264 | 0.0267 | 0.0268 | 0.027 | 0.0272 | 0.0275 | 0.0284 |
| cML-BIC-Profile | 0.972, | 0.483, | 0.216, | 0.072, | 0.054, | 0.062, | 0.201, | 0.448, | 0.941, |
| | -0.1002, | -0.0503, | -0.0303, | -0.0103, | -0.0003, | 0.0097, | 0.0298, | 0.0498, | 0.0997, |
| | 0.0260, | 0.0266, | 0.0268, | 0.0271, | 0.0272, | 0.0274, | 0.0276, | 0.0280, | 0.0289, |
| | 0.0259 | 0.0263 | 0.0265 | 0.0268 | 0.0269 | 0.0271 | 0.0273 | 0.0276 | 0.0285 |
| MR-Mix | 0.870, | 0.280, | 0.110, | 0.035, | 0.023, | 0.032, | 0.099, | 0.265, | 0.799, |
| | -0.1053, | -0.0515, | -0.0308, | -0.0104, | -0.0002, | 0.0098, | 0.0295, | 0.0488, | 0.0952, |
| | 0.0296, | 0.0296, | 0.0294, | 0.0294, | 0.0294, | 0.0295, | 0.0294, | 0.0295, | 0.0296, |
| 100 C -16 | 0.0358 | 0.0357 | 0.0356 | 0.0356 | 0.0356 | 0.0357 | 0.0357 | 0.036 | 0.036 |
| MR-ContMix | 0.954, | 0.481, | 0.227, | 0.076, | 0.060, | 0.080, | 0.210, | 0.446, | 0.904, |
| | -0.1002, 0.0282, | -0.0503, 0.0288, | -0.0304, 0.0290, | -0.0104, 0.0294, | -0.0005, 0.0296, | 0.0094, 0.0298, | 0.0294, 0.0301, | 0.0493, 0.0305, | 0.0991, 0.0314, |
| | 0.0282, NA | 0.0288, NA | 0.0290, NA | 0.0294, NA | 0.0296, NA | 0.0298, NA | 0.0501, NA | 0.0303, NA | 0.0314, NA |
| MR-Lasso | 0.946, | 0.433, | 0.198, | 0.062, | 0.046, | 0.058, | 0.171, | 0.400, | 0.899, |
| WIK-Lasso | -0.0996, | -0.0500, | -0.0301, | -0.0101, | -0.0003, | 0.0095, | 0.0293, | 0.400, | 0.0993, |
| | 0.0271, | 0.0278, | 0.0278, | 0.0282, | 0.0280, | 0.0280, | 0.0295, | 0.0291, | 0.0298, |
| | 0.0276 | 0.0282 | 0.0284 | 0.0287 | 0.0288 | 0.029 | 0.0292 | 0.0295 | 0.0304 |
| MR-PRESSO | 0.525, | 0.257, | 0.154, | 0.106, | 0.107, | 0.114, | 0.159, | 0.261, | 0.522, |
| | -0.0803, | -0.0339, | -0.0150, | 0.0025, | 0.0114, | 0.0211, | 0.0380, | 0.0554, | 0.1011, |
| | 0.2115, | 0.2085, | 0.2073, | 0.2045, | 0.2046, | 0.2045, | 0.2024, | 0.1995, | 0.1943, |
| | 0.0929 | 0.0907 | 0.0897 | 0.0874 | 0.0873 | 0.087 | 0.0851 | 0.083 | 0.079 |
| MR-IVW | 0.112, | 0.055, | 0.043, | 0.032, | 0.025, | 0.027, | 0.037, | 0.050, | 0.113, |
| | -0.0890, | -0.0390, | -0.0191, | 0.0009, | 0.0109, | 0.0209, | 0.0409, | 0.0609, | 0.1108, |
| | 0.2471, | 0.2470, | 0.2470, | 0.2470, | 0.2470, | 0.2470, | 0.2470, | 0.2470, | 0.2470, |
| | 0.2342 | 0.2342 | 0.2342 | 0.2342 | 0.2342 | 0.2342 | 0.2342 | 0.2342 | 0.2342 |
| MR-IVW-Oracle | 0.949, | 0.422, | 0.187, | 0.054, | 0.040, | 0.051, | 0.164, | 0.393, | 0.900, |
| | -0.0998, | -0.0500, | -0.0301, | -0.0102, | -0.0002, | 0.0097, | 0.0296, | 0.0495, | 0.0993, |
| | 0.0258, | 0.0263, | 0.0266, | 0.0268, | 0.0270, | 0.0271, | 0.0274, | 0.0277, | 0.0285, |
| | 0.0278 | 0.0284 | 0.0286 | 0.0289 | 0.029 | 0.0292 | 0.0295 | 0.0298 | 0.0306 |
| MR-Egger | 0.081, | 0.079, | 0.080, | 0.081, | 0.083, | 0.083, | 0.085, | 0.087, | 0.087, |
| | -0.1124, | -0.0683, | -0.0507, | -0.0330, | -0.0242, | -0.0154, | 0.0022, | 0.0199, | 0.0639, |
| | 1.3324, | 1.3322, | 1.3321, | 1.3320, | 1.3319, | 1.3319, | 1.3318, | 1.3318, | 1.3317, |
| MD W ' 1 - 1 M P | 1.2673 | 1.2671 | 1.267 | 1.267 | 1.267 | 1.267 | 1.2669 | 1.2669 | 1.2669 |
| MR-Weighted-Median | 0.829, | 0.309, | 0.124, | 0.037, | 0.032, | 0.045, | 0.123, | 0.278, | 0.747, |
| | -0.0979, 0.0319, | -0.0492, 0.0325, | -0.0296, 0.0328, | -0.0101, 0.0331, | -0.0003, 0.0333, | 0.0095, 0.0334, | 0.0290, 0.0337, | 0.0484, | 0.0970, 0.0349, |
| | 0.0319, | 0.0325, | 0.0328, | 0.0351, | 0.0333, | 0.0354, | 0.0357, | 0.0341, 0.0361 | 0.0349, |
| MR-Weighted-Mode | 0.0557 | 0.0343 | 0.0346 | 0.033 | 0.0331 | 0.0333 | 0.0337 | 0.0361 | 0.674, |
| weighten-Mout | -0.0987, | -0.0496, | -0.0299, | -0.0105, | -0.0007, | 0.031, | 0.090, | 0.230, | 0.074, |
| | 0.0340, | 0.0347, | 0.0351, | 0.0355, | 0.0356, | 0.0358, | 0.0362, | 0.0367, | 0.0377, |
| | 0.0376 | 0.0383 | 0.0386 | 0.039 | 0.0392 | 0.0394 | 0.0398 | 0.0402 | 0.0377, |
| MR-RAPS1 | 0.136, | 0.078, | 0.058, | 0.043, | 0.040, | 0.040, | 0.048, | 0.066, | 0.147, |
| | -0.0889, | -0.0389, | -0.0189, | 0.0012, | 0.0112, | 0.0212, | 0.0412, | 0.0612, | 0.1113, |
| | 0.2410, | 0.2411, | 0.2411, | 0.2412, | 0.2412, | 0.2412, | 0.2413, | 0.2413, | 0.2414, |
| | 0.2238 | 0.2238 | 0.2238 | 0.2238 | 0.2238 | 0.2238 | 0.2238 | 0.2238 | 0.2239 |
| MR-RAPS2 | 0.901, | 0.757, | 0.672, | 0.629, | 0.623, | 0.624, | 0.690, | 0.749, | 0.896, |
| | -0.0764, | 0.0771, | 0.4224, | 0.5567, | 0.5403, | 0.7386, | 1.1735, | 1.1140, | 0.6427, |
| | 3.2138, | 2.5930, | 2.9590, | 3.7350, | 3.8176, | 4.7511, | 5.7913, | 5.2713, | 6.0397, |
| | 0.0776 | 0.0648 | 0.0665 | 0.079 | 0.074 | 0.0832 | 0.1106 | 0.1117 | 0.1136 |
| MR-RAPS3 | 0.899, | 0.810, | 0.797, | 0.794, | 0.785, | 0.795, | 0.791, | 0.818, | 0.886, |
| | -0.1889, | 0.0415, | 0.0731, | 0.0099, | 0.0260, | 0.0428, | 0.0768, | 0.1099, | 0.1877, |
| | 0.5604, | 3.8089, | 3.2619, | 0.4702, | 0.4535, | 0.4449, | 0.4335, | 0.4251, | 0.4064, |
| | 0.0732 | 14.8032 | 2.8162 | 0.0626 | 0.0582 | 0.0561 | 0.0538 | 0.0521 | 0.0495 |
| MR-RAPS4 | 0.995, | 0.907, | 0.858, | 0.810, | 0.798, | 0.795, | 0.824, | 0.873, | 0.991, |
| | -0.2234, | 0.0267, | 0.0880, | 0.2014, | 0.2672, | 0.3081, | 0.4070, | 0.4891, | 0.7079, |
| | | | | | | | | | |
| | 1.2807, 0.0503 | 1.2697, 0.0486 | 1.2736, 0.0484 | 1.2339, 0.0475 | 1.2305, 0.0477 | 1.1909, 0.0462 | 1.1715, 0.0467 | 1.1353, 0.0465 | 1.0264, 0.0464 |

Table S30: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE satisfied, q=0.2, and N=100000.

| | / / | | | | , <u>1</u> | | | | |
|--------------------|---------------------|----------|----------|----------|------------|---------|---------|---------|---------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.926, | 0.341, | 0.117, | 0.025, | 0.022, | 0.042, | 0.134, | 0.387, | 0.872, |
| | -0.0863, | -0.0378, | -0.0205, | -0.0057, | 0.0013, | 0.0081, | 0.0233, | 0.0407, | 0.0885, |
| | 0.0232, | 0.0217, | 0.0200, | 0.0183, | 0.0182, | 0.0188, | 0.0212, | 0.0235, | 0.0264, |
| | 0.0246 | 0.0245 | 0.024 | 0.0237 | 0.0237 | 0.024 | 0.0247 | 0.0255 | 0.0269 |
| cML-MA-AIC-Profile | 0.926, | 0.338, | 0.117, | 0.024, | 0.022, | 0.042, | 0.133, | 0.385, | 0.873, |
| | -0.0864, | -0.0378, | -0.0205, | -0.0058, | 0.0013, | 0.0081, | 0.0233, | 0.0407, | 0.0887, |
| | 0.0233, | 0.0217, | 0.0200, | 0.0183, | 0.0182, | 0.0188, | 0.0212, | 0.0235, | 0.0264, |
| | 0.0247 | 0.0245 | 0.0241 | 0.0238 | 0.0238 | 0.0241 | 0.0247 | 0.0256 | 0.027 |
| cML-AIC | 0.965, | 0.572, | 0.280, | 0.098, | 0.080, | 0.109, | 0.309, | 0.603, | 0.937, |
| | -0.0921, | -0.0428, | -0.0239, | -0.0069, | 0.0015, | 0.0097, | 0.0269, | 0.0455, | 0.0947, |
| | 0.0256, | 0.0251, | 0.0244, | 0.0232, | 0.0229, | 0.0235, | 0.0251, | 0.0269, | 0.0284, |
| | 0.0197 | 0.0201 | 0.0202 | 0.0204 | 0.0205 | 0.0206 | 0.0208 | 0.021 | 0.0217 |
| cML-AIC-Profile | 0.964, | 0.569, | 0.281, | 0.097, | 0.079, | 0.109, | 0.308, | 0.602, | 0.938, |
| | -0.0922, | -0.0428, | -0.0239, | -0.0069, | 0.0015, | 0.0097, | 0.0269, | 0.0455, | 0.0950, |
| | 0.0257, | 0.0251, | 0.0245, | 0.0232, | 0.0229, | 0.0235, | 0.0251, | 0.0269, | 0.0284, |
| | 0.0198 | 0.0201 | 0.0203 | 0.0205 | 0.0205 | 0.0207 | 0.0209 | 0.0211 | 0.0217 |
| cML-MA-BIC | 0.999, | 0.733, | 0.342, | 0.084, | 0.051, | 0.092, | 0.371, | 0.728, | 0.997, |
| | -0.0988, | -0.0488, | -0.0288, | -0.0089, | 0.0011, | 0.0110, | 0.0310, | 0.0510, | 0.1010, |
| | 0.0189, | 0.0192, | 0.0193, | 0.0195, | 0.0195, | 0.0196, | 0.0199, | 0.0202, | 0.0208, |
| | 0.0183 | 0.0187 | 0.0188 | 0.019 | 0.0191 | 0.0192 | 0.0194 | 0.0196 | 0.0202 |
| cML-MA-BIC-Profile | 0.999, | 0.730, | 0.341, | 0.083, | 0.051, | 0.092, | 0.369, | 0.727, | 0.997, |
| | -0.0988, | -0.0488, | -0.0288, | -0.0089, | 0.0011, | 0.0110, | 0.0310, | 0.0510, | 0.1010, |
| | 0.0189, | 0.0192, | 0.0193, | 0.0195, | 0.0195, | 0.0196, | 0.0199, | 0.0202, | 0.0208, |
| | 0.0184 | 0.0187 | 0.0188 | 0.019 | 0.0191 | 0.0192 | 0.0194 | 0.0196 | 0.0202 |
| cML-BIC | 1.000, | 0.743, | 0.353, | 0.088, | 0.055, | 0.094, | 0.376, | 0.740, | 0.997, |
| | -0.0990, | -0.0489, | -0.0289, | -0.0089, | 0.0011, | 0.0111, | 0.0310, | 0.0511, | 0.1011, |
| | 0.0189, | 0.0192, | 0.0193, | 0.0195, | 0.0196, | 0.0197, | 0.0200, | 0.0202, | 0.0207, |
| | 0.0181 | 0.0185 | 0.0186 | 0.0188 | 0.0189 | 0.019 | 0.0192 | 0.0194 | 0.02 |
| cML-BIC-Profile | 1.000, | 0.740, | 0.353, | 0.087, | 0.055, | 0.094, | 0.375, | 0.739, | 0.997, |
| | -0.0990, | -0.0490, | -0.0289, | -0.0089, | 0.0011, | 0.0111, | 0.0310, | 0.0511, | 0.1011, |
| | 0.0189, | 0.0192, | 0.0193, | 0.0195, | 0.0196, | 0.0197, | 0.0200, | 0.0202, | 0.0207, |
| | 0.0182 | 0.0185 | 0.0186 | 0.0188 | 0.0189 | 0.019 | 0.0192 | 0.0194 | 0.02 |
| MR-Mix | 0.988, | 0.539, | 0.189, | 0.034, | 0.026, | 0.048, | 0.214, | 0.524, | 0.964, |
| | -0.1047, | -0.0509, | -0.0301, | -0.0096, | 0.0006, | 0.0105, | 0.0302, | 0.0495, | 0.0958, |
| | 0.0219, | 0.0219, | 0.0219, | 0.0217, | 0.0218, | 0.0217, | 0.0219, | 0.0218, | 0.0220, |
| | 0.0254 | 0.0253 | 0.0254 | 0.0254 | 0.0254 | 0.0254 | 0.0254 | 0.0256 | 0.0255 |
| MR-ContMix | 0.997, | 0.731, | 0.356, | 0.103, | 0.065, | 0.105, | 0.390, | 0.740, | 0.991, |
| | -0.0984, | -0.0483, | -0.0283, | -0.0084, | 0.0016, | 0.0116, | 0.0315, | 0.0515, | 0.1013, |
| | 0.0197, | 0.0201, | 0.0204, | 0.0205, | 0.0208, | 0.0209, | 0.0212, | 0.0215, | 0.0221, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.996, | 0.673, | 0.307, | 0.075, | 0.051, | 0.083, | 0.344, | 0.690, | 0.989, |
| | -0.0985, | -0.0486, | -0.0286, | -0.0088, | 0.0012, | 0.0112, | 0.0312, | 0.0511, | 0.1010, |
| | 0.0193, | 0.0196, | 0.0197, | 0.0201, | 0.0202, | 0.0202, | 0.0205, | 0.0207, | 0.0215, |
| | 0.0194 | 0.0199 | 0.02 | 0.0202 | 0.0203 | 0.0204 | 0.0206 | 0.0209 | 0.0215 |
| MR-PRESSO | 0.517, | 0.318, | 0.176, | 0.072, | 0.065, | 0.091, | 0.210, | 0.338, | 0.525, |
| | -0.0953, | -0.0459, | -0.0263, | -0.0061, | 0.0034, | 0.0130, | 0.0328, | 0.0524, | 0.1007, |
| | 0.2290, | 0.2287, | 0.2285, | 0.2281, | 0.2278, | 0.2276, | 0.2277, | 0.2276, | 0.2264, |
| | 0.1123 | 0.1116 | 0.1113 | 0.111 | 0.1105 | 0.1102 | 0.1104 | 0.1105 | 0.1093 |
| MR-IVW | 0.106, | 0.038, | 0.029, | 0.020, | 0.019, | 0.024, | 0.034, | 0.048, | 0.107, |
| | -0.0966, | -0.0465, | -0.0264, | -0.0064, | 0.0036, | 0.0136, | 0.0337, | 0.0537, | 0.1037, |
| | 0.2365, | 0.2365, | 0.2365, | 0.2365, | 0.2364, | 0.2364, | 0.2364, | 0.2364, | 0.2364, |
| | 0.2336 | 0.2336 | 0.2336 | 0.2336 | 0.2336 | 0.2336 | 0.2336 | 0.2336 | 0.2336 |
| MR-IVW-Oracle | 0.998, | 0.673, | 0.302, | 0.069, | 0.044, | 0.075, | 0.331, | 0.686, | 0.993, |
| | -0.0988, | -0.0488, | -0.0289, | -0.0089, | 0.0011, | 0.0110, | 0.0310, | 0.0510, | 0.1009, |
| | 0.0187, | 0.0191, | 0.0193, | 0.0194, | 0.0195, | 0.0196, | 0.0198, | 0.0200, | 0.0206, |
| | 0.0196 | 0.02 | 0.0202 | 0.0204 | 0.0205 | 0.0206 | 0.0208 | 0.021 | 0.0216 |
| MR-Egger | 0.084, | 0.081, | 0.080, | 0.079, | 0.077, | 0.077, | 0.077, | 0.077, | 0.081, |
| | -0.0660, | -0.0187, | 0.0002, | 0.0191, | 0.0285, | 0.0379, | 0.0568, | 0.0757, | 0.1229, |
| | 1.4052, | 1.4047, | 1.4045, | 1.4043, | 1.4042, | 1.4041, | 1.4040, | 1.4038, | 1.4034, |
| | 1.3167 | 1.3167 | 1.3167 | 1.3167 | 1.3167 | 1.3167 | 1.3168 | 1.3168 | 1.3169 |
| MR-Weighted-Median | 0.990, | 0.513, | 0.203, | 0.046, | 0.031, | 0.062, | 0.225, | 0.534, | 0.970, |
| | -0.0975, | -0.0481, | -0.0283, | -0.0086, | 0.0012, | 0.0111, | 0.0308, | 0.0505, | 0.0997, |
| | 0.0222, | 0.0226, | 0.0228, | 0.0230, | 0.0232, | 0.0233, | 0.0236, | 0.0239, | 0.0246, |
| | 0.0237 | 0.0242 | 0.0244 | 0.0246 | 0.0247 | 0.0248 | 0.0251 | 0.0254 | 0.0261 |
| MR-Weighted-Mode | 0.959, | 0.422, | 0.171, | 0.033, | 0.023, | 0.045, | 0.176, | 0.458, | 0.925, |
| | -0.0977, | -0.0482, | -0.0284, | -0.0085, | 0.0014, | 0.0112, | 0.0310, | 0.0507, | 0.1003, |
| | 0.0243, | 0.0247, | 0.0247, | 0.0247, | 0.0249, | 0.0251, | 0.0254, | 0.0256, | 0.0262, |
| | 0.0266 | 0.0271 | 0.0273 | 0.0276 | 0.0277 | 0.0279 | 0.0281 | 0.0285 | 0.0293 |
| MR-RAPS1 | 0.148, | 0.055, | 0.042, | 0.033, | 0.031, | 0.033, | 0.040, | 0.058, | 0.142, |
| | -0.0954, | -0.0454, | -0.0254, | -0.0054, | 0.0046, | 0.0147, | 0.0347, | 0.0547, | 0.1047, |
| | 0.2296, | 0.2296, | 0.2296, | 0.2297, | 0.2297, | 0.2297, | 0.2297, | 0.2297, | 0.2298, |
| | 0.2225 | 0.2226 | 0.2226 | 0.2226 | 0.2226 | 0.2226 | 0.2226 | 0.2226 | 0.2227 |
| MR-RAPS2 | 0.926, | 0.756, | 0.420, | 0.187, | 0.160, | 0.200, | 0.485, | 0.755, | 0.924, |
| | -0.1293, | 0.0720, | 0.2497, | 0.2705, | 0.5470, | 0.6700, | 0.8761, | 1.0341, | 0.6349, |
| | 3.9699, | 2.9083, | 3.7601, | 3.6465, | 3.1943, | 8.0029, | 3.9672, | 4.2728, | 3.9908, |
| | 0.0665 | 0.0457 | 0.048 | 0.0536 | 0.0544 | 0.0618 | 0.0751 | 0.0865 | 0.084 |
| MR-RAPS3 | 0.929, | 0.859, | 0.842, | 0.829, | 0.836, | 0.836, | 0.846, | 0.851, | 0.918, |
| | -0.2029, | -0.0747, | -0.0463, | -0.0095, | 0.0088, | 0.0270, | 0.0626, | 0.0971, | 0.1775, |
| | 0.4917, | 0.5223, | 0.4329, | 0.4212, | 0.4169, | 0.4131, | 0.4058, | 0.3990, | 0.3834, |
| | 0.0509 | 0.0917 | 0.0418 | 0.0392 | 0.0386 | 0.038 | 0.0371 | 0.0363 | 0.0347 |
| MR-RAPS4 | 0.999, | 0.797, | 0.407, | 0.129, | 0.093, | 0.138, | 0.451, | 0.788, | 0.999, |
| MIC-ICAL 54 | 1 | -0.0488, | -0.0288, | -0.0088, | 0.0012, | 0.0112, | 0.0312, | 0.0513, | 0.1013, |
| WIK-KAI 54 | -0.0988, | | | | | | | | |
| WIK-KAI 54 | -0.0988, 0.0193, | 0.0197, | 0.0199, | 0.0200, | 0.0201, | 0.0202, | 0.0204, | 0.0207, | 0.0213, |

Table S31: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE satisfied, q=0.2, and N=200000.

| // | <i>'</i> | | | | , I | | | | |
|--------------------|---------------------|-------------------------------|-------------------------------|------------------------------|------------------------------|--------------------|------------------------------|--------------------|------------------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.990, | 0.665, | 0.255, | 0.040, | 0.024, | 0.033, | 0.247, | 0.609, | 0.975, |
| | -0.0916, | -0.0418, | -0.0231, | -0.0071, | -0.0003, | 0.0066, | 0.0224, | 0.0407, | 0.0898, |
| | 0.0166, | 0.0163, | 0.0151, | 0.0130, | 0.0129, | 0.0135, | 0.0157, | 0.0177, | 0.0191, |
| | 0.0175 | 0.0177 | 0.0174 | 0.017 | 0.0169 | 0.017 | 0.0178 | 0.0184 | 0.0192 |
| cML-MA-AIC-Profile | 0.990, | 0.665, | 0.255, | 0.040, | 0.024, | 0.033, | 0.246, | 0.609, | 0.975, |
| | -0.0917, | -0.0418, | -0.0231, | -0.0071, | -0.0003, | 0.0066, | 0.0224, | 0.0408, | 0.0899, |
| | 0.0167, 0.0176 | 0.0163, 0.0177 | 0.0151, 0.0174 | 0.0130, 0.017 | 0.0129, 0.0169 | 0.0135, 0.017 | 0.0157, 0.0178 | 0.0177, 0.0184 | 0.0191, 0.0192 |
| cML-AIC | 0.0176 | 0.845, | 0.0174 | 0.017 | 0.0169 | 0.017 | 0.0178 | 0.0184 | 0.0192 |
| CIVIL-AIC | -0.0959, | -0.0460, | -0.0265, | -0.0082, | -0.0002, | 0.0080, | 0.0258, | 0.0449, | 0.0943, |
| | 0.0182, | 0.0180, | 0.0175, | 0.0165, | 0.0165, | 0.0172, | 0.0184, | 0.0198, | 0.0207, |
| | 0.014 | 0.0142 | 0.0143 | 0.0144 | 0.0145 | 0.0146 | 0.0147 | 0.0149 | 0.0153 |
| cML-AIC-Profile | 0.993, | 0.845, | 0.497, | 0.126, | 0.076, | 0.124, | 0.477, | 0.788, | 0.987, |
| | -0.0960, | -0.0461, | -0.0265, | -0.0082, | -0.0002, | 0.0080, | 0.0258, | 0.0449, | 0.0944, |
| | 0.0183, | 0.0180, | 0.0175, | 0.0165, | 0.0165, | 0.0172, | 0.0184, | 0.0198, | 0.0207, |
| | 0.014 | 0.0142 | 0.0143 | 0.0144 | 0.0145 | 0.0146 | 0.0147 | 0.0149 | 0.0154 |
| cML-MA-BIC | 1.000, | 0.965, | 0.636, | 0.118, | 0.049, | 0.120, | 0.577, | 0.932, | 1.000, |
| | -0.1005, | -0.0505, | -0.0306, | -0.0106, | -0.0006, | 0.0094, | 0.0293, | 0.0493, | 0.0993, |
| | 0.0133, 0.0129 | 0.0135, 0.0131 | 0.0136, 0.0132 | 0.0137, 0.0134 | 0.0137, 0.0134 | 0.0138, 0.0135 | 0.0140, 0.0136 | 0.0141, 0.0138 | 0.0145, 0.0142 |
| cML-MA-BIC-Profile | 1.000, | 0.0131 | 0.636, | 0.0134 | 0.0134 | 0.0133 | 0.0136 | 0.0138 | 1.000, |
| CML-MA-DIC-FIORE | -0.1005, | -0.0505, | -0.0306, | -0.0106, | -0.0006, | 0.120, | 0.0293, | 0.932, | 0.0993, |
| | 0.0133, | 0.0135, | 0.0136, | 0.0137, | 0.0137, | 0.0138, | 0.0140, | 0.0141, | 0.0145, |
| | 0.0133, | 0.0131 | 0.0133 | 0.0134 | 0.0134 | 0.0135 | 0.0136 | 0.0138 | 0.0142 |
| cML-BIC | 1.000, | 0.966, | 0.643, | 0.121, | 0.053, | 0.122, | 0.584, | 0.935, | 1.000, |
| | -0.1006, | -0.0506, | -0.0306, | -0.0106, | -0.0006, | 0.0093, | 0.0293, | 0.0493, | 0.0993, |
| | 0.0133, | 0.0135, | 0.0136, | 0.0137, | 0.0138, | 0.0138, | 0.0140, | 0.0141, | 0.0145, |
| | 0.0128 | 0.013 | 0.0131 | 0.0133 | 0.0133 | 0.0134 | 0.0135 | 0.0137 | 0.0141 |
| cML-BIC-Profile | 1.000, | 0.966, | 0.643, | 0.122, | 0.053, | 0.122, | 0.584, | 0.935, | 1.000, |
| | -0.1006, | -0.0506, | -0.0306, | -0.0106, | -0.0006, | 0.0093, | 0.0293, | 0.0493, | 0.0993, |
| | 0.0133, 0.0128 | 0.0135, 0.013 | 0.0136, 0.0131 | 0.0137, 0.0133 | 0.0138, 0.0133 | 0.0138, 0.0134 | 0.0140, 0.0135 | 0.0141, 0.0137 | 0.0145, 0.0141 |
| MR-Mix | 0.0128 | 0.013 | 0.0131 | 0.0133 | 0.0133 | 0.0134 | 0.0133 | 0.769, | 0.994, |
| IVIIX-IVIIX | -0.1061, | -0.0526, | -0.0315, | -0.0111, | -0.0010, | 0.0090, | 0.0287, | 0.0479, | 0.0945, |
| | 0.0159, | 0.0158, | 0.0157, | 0.0157, | 0.0157, | 0.0157, | 0.0156, | 0.0158, | 0.0157, |
| | 0.0183 | 0.0182 | 0.0182 | 0.0182 | 0.0182 | 0.0182 | 0.0182 | 0.0182 | 0.0183 |
| MR-ContMix | 1.000, | 0.958, | 0.660, | 0.144, | 0.078, | 0.133, | 0.607, | 0.936, | 1.000, |
| | -0.1002, | -0.0504, | -0.0304, | -0.0104, | -0.0005, | 0.0095, | 0.0294, | 0.0494, | 0.0993, |
| | 0.0138, | 0.0140, | 0.0141, | 0.0142, | 0.0143, | 0.0143, | 0.0145, | 0.0146, | 0.0151, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.941, | 0.589, | 0.104, | 0.048, | 0.107, | 0.522, | 0.896, | 0.999, |
| | -0.1006, 0.0137, | -0.0506, 0.0139, | -0.0307, 0.0140, | -0.0108, 0.0141, | -0.0008, 0.0142, | 0.0092, 0.0143, | 0.0291, 0.0144, | 0.0491, 0.0146, | 0.0990, 0.0151, |
| | 0.0137, | 0.0139, | 0.0140, | 0.0141, | 0.0142, | 0.0145, | 0.0144, | 0.0148 | 0.0151, |
| MR-PRESSO | 0.493, | 0.387, | 0.243, | 0.088, | 0.066, | 0.0143 | 0.241, | 0.370, | 0.495, |
| MIC I RESSO | -0.1154, | -0.0654, | -0.0454, | -0.0255, | -0.0156, | -0.0055, | 0.0143, | 0.0342, | 0.0842, |
| | 0.2375, | 0.2371, | 0.2371, | 0.2370, | 0.2369, | 0.2369, | 0.2368, | 0.2367, | 0.2364, |
| | 0.1207 | 0.12 | 0.1198 | 0.1194 | 0.1192 | 0.1192 | 0.119 | 0.119 | 0.1184 |
| MR-IVW | 0.128, | 0.056, | 0.035, | 0.022, | 0.022, | 0.023, | 0.029, | 0.039, | 0.100, |
| | -0.1158, | -0.0657, | -0.0456, | -0.0256, | -0.0156, | -0.0056, | 0.0145, | 0.0345, | 0.0845, |
| | 0.2418, | 0.2417, | 0.2416, | 0.2416, | 0.2415, | 0.2415, | 0.2415, | 0.2414, | 0.2413, |
| MD MW/O 1 | 0.2338 | 0.2338 | 0.2338 | 0.2337 | 0.2337 | 0.2337 | 0.2337 | 0.2337 | 0.2337 |
| MR-IVW-Oracle | 1.000, -0.1004, | 0.942, -0.0505, | 0.581, -0.0306, | 0.093, -0.0106, | 0.036, -0.0006, | 0.102, 0.0094, | 0.522, 0.0293, | 0.903, 0.0493, | 0.999, 0.0992, |
| | 0.0132, | 0.0134, | 0.0135, | 0.0136, | 0.0137, | 0.0034, | 0.0233, | 0.0493, | 0.0144, |
| | 0.0132, | 0.0134, | 0.0143 | 0.0145 | 0.0137, | 0.0146 | 0.0137, | 0.0149 | 0.0153 |
| MR-Egger | 0.071, | 0.070, | 0.069, | 0.070, | 0.070, | 0.070, | 0.068, | 0.069, | 0.071, |
| 66 | -0.1706, | -0.1222, | -0.1028, | -0.0834, | -0.0737, | -0.0641, | -0.0447, | -0.0253, | 0.0231, |
| | 1.3437, | 1.3435, | 1.3434, | 1.3433, | 1.3432, | 1.3432, | 1.3431, | 1.3430, | 1.3428, |
| | 1.3309 | 1.3308 | 1.3307 | 1.3307 | 1.3307 | 1.3307 | 1.3306 | 1.3306 | 1.3306 |
| MR-Weighted-Median | 1.000, | 0.855, | 0.423, | 0.079, | 0.040, | 0.057, | 0.392, | 0.781, | 0.999, |
| | -0.0999, | -0.0503, | -0.0305, | -0.0106, | -0.0007, | 0.0092, | 0.0290, | 0.0489, | 0.0984, |
| | 0.0157, | 0.0160, | 0.0162, | 0.0164, | 0.0165, 0.0175 | 0.0166, 0.0176 | 0.0168, | 0.0171, | 0.0177, |
| MR-Weighted-Mode | 0.0168 1.000, | 0.0171 0.769, | 0.0173 0.337, | 0.0174 0.060, | 0.0175 | 0.0176 | 0.0178 0.322, | 0.018 0.707, | 0.0185 |
| wix- weighten-Mone | -0.0999, | -0.0502, | -0.0304, | -0.0105, | -0.0005, | 0.046, | 0.322, 0.0293, | 0.707, 0.0492, | 0.993, |
| | 0.0166, | 0.0170, | 0.0172, | 0.0173, | 0.0174, | 0.0093, | 0.0293, | 0.0492, | 0.0330, |
| | 0.0189 | 0.0193 | 0.0194 | 0.0196 | 0.0197 | 0.0198 | 0.02 | 0.0202 | 0.0208 |
| MR-RAPS1 | 0.171, | 0.069, | 0.044, | 0.030, | 0.030, | 0.024, | 0.036, | 0.058, | 0.126, |
| | -0.1144, | -0.0644, | -0.0444, | -0.0244, | -0.0144, | -0.0044, | 0.0156, | 0.0356, | 0.0855, |
| | 0.2336, | 0.2336, | 0.2336, | 0.2336, | 0.2336, | 0.2336, | 0.2336, | 0.2336, | 0.2336, |
| 100 0 (| 0.2223 | 0.2223 | 0.2223 | 0.2223 | 0.2223 | 0.2223 | 0.2223 | 0.2223 | 0.2224 |
| MR-RAPS2 | 0.939, | 0.923, | 0.731, | 0.335, | 0.264, | 0.350, | 0.678, | 0.904, | 0.943, |
| | 0.0667, | -0.0469, | 0.1500, | 0.1544, | -0.0108, | -0.0979, | -0.3080, | 0.0703, | 0.2736, |
| | 4.1364, 0.071 | 3.3717, 0.0709 | 4.0999, 0.0735 | 3.5386, 0.0687 | 3.5733, 0.0658 | 4.4794, 0.0763 | 5.0440, 0.0742 | 3.7687, 0.0663 | 3.4304, 0.0647 |
| MR-RAPS3 | 0.071 | 0.0709 | 0.0735 | 0.0687 | 0.0658 | 0.0763 | 0.0742 | 0.0663 | 0.0647 |
| WIN-NAP33 | -0.3156, | -0.1309, | -0.0820, | -0.0450, | -0.0266, | -0.0083, | 0.879, 0.0283, | 0.890, | 0.940, |
| | 2.7672, | 0.5608, | 0.4483, | 0.4358, | 0.4311, | 0.4268, | 0.0283, | 0.4128, | 0.1434, |
| | 0.4842 | 0.0832 | 0.0292 | 0.0277 | 0.0273 | 0.0272 | 0.0267 | 0.0256 | 0.0244 |
| | 1.000, | 0.973, | 0.705, | 0.189, | 0.104, | 0.171, | 0.642, | 0.957, | 1.000, |
| MR-RAPS4 | | | | | | | | | |
| MR-RAPS4 | -0.1005, | -0.0493, | -0.0256, | 0.0035, | 0.0133, | 0.0194, | 0.0323, | 0.0503, | 0.0994, |
| MR-RAPS4 | | -0.0493, 0.0347, 0.0119 | -0.0256, 0.0647, 0.0121 | 0.0035, 0.1212, 0.0123 | 0.0133, 0.1092, 0.0123 | 0.0194, 0.0893, | 0.0323, 0.0504, 0.0124 | 0.0503, 0.0315, | 0.0994, 0.0148, 0.0129 |

Table S32: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE satisfied, q=0.4, and N=50000.

| // | <i>'</i> | | | | , I | | | | |
|---------------------------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.559, | 0.120, | 0.034, | 0.010, | 0.009, | 0.014, | 0.034, | 0.093, | 0.494, |
| | -0.0821, | -0.0364, | -0.0208, | -0.0061, | 0.0007, | 0.0073, | 0.0213, | 0.0365, | 0.0804, |
| | 0.0343, | 0.0303, | 0.0282, | 0.0267, | 0.0269, | 0.0273, | 0.0295, | 0.0324, | 0.0382, |
| | 0.0398 | 0.0392 | 0.039 | 0.0389 | 0.0391 | 0.0393 | 0.0402 | 0.0411 | 0.0434 |
| cML-MA-AIC-Profile | 0.553, | 0.117, | 0.034, | 0.008, | 0.009, | 0.014, | 0.034, | 0.093, | 0.493, |
| INIL-MA-AIC-I TOILE | -0.0822, | -0.0364, | -0.0208, | -0.0061, | 0.0007, | 0.0073, | 0.0213, | 0.0365, | 0.0806, |
| | 0.0344, | 0.0303, | 0.0282, | 0.0268, | 0.0007, | 0.0073, | 0.0213, | 0.0303, | 0.0383, |
| | 0.0344, | 0.0303, | 0.0282, | 0.0208, | 0.0209, | 0.0396 | 0.0293, | 0.0324, | 0.0383, |
| -MI AIC | | | | 0.0592 | | | | | |
| cML-AIC | 0.783, | 0.304, | 0.144, | | 0.045, | 0.060, | 0.134, | 0.273, | 0.707, |
| | -0.0906, | -0.0424, | -0.0249, | -0.0072, | 0.0008, | 0.0086, | 0.0251, | 0.0420, | 0.0889, |
| | 0.0382, | 0.0361, | 0.0350, | 0.0344, | 0.0349, | 0.0353, | 0.0373, | 0.0395, | 0.0441, |
| | 0.0324 | 0.033 | 0.0332 | 0.0336 | 0.0337 | 0.0339 | 0.0343 | 0.0347 | 0.0358 |
| cML-AIC-Profile | 0.780, | 0.295, | 0.140, | 0.054, | 0.043, | 0.056, | 0.130, | 0.269, | 0.706, |
| | -0.0907, | -0.0424, | -0.0249, | -0.0072, | 0.0008, | 0.0086, | 0.0251, | 0.0420, | 0.0891 |
| | 0.0383, | 0.0361, | 0.0350, | 0.0346, | 0.0349, | 0.0353, | 0.0373, | 0.0396, | 0.0442 |
| | 0.0326 | 0.0332 | 0.0335 | 0.0338 | 0.0339 | 0.0341 | 0.0345 | 0.035 | 0.036 |
| cML-MA-BIC | 0.914, | 0.361, | 0.152, | 0.052, | 0.042, | 0.045, | 0.135, | 0.315, | 0.855, |
| | -0.1004, | -0.0504, | -0.0305, | -0.0106, | -0.0007, | 0.0093, | 0.0291, | 0.0491, | 0.0990 |
| | 0.0293, | 0.0297, | 0.0299, | 0.0301, | 0.0302, | 0.0304, | 0.0307, | 0.0311, | 0.0321 |
| | 0.0304 | 0.031 | 0.0313 | 0.0315 | 0.0317 | 0.0318 | 0.0322 | 0.0325 | 0.0334 |
| ML-MA-BIC-Profile | 0.913, | 0.356, | 0.151, | 0.0515 | 0.041, | 0.044, | 0.133, | 0.314, | 0.852, |
| MIL-MA-DIC-PIONE | | | 0.131, | | | | | 0.514, | |
| | -0.1004, | -0.0504, | -0.0305, | -0.0106, | -0.0007, | 0.0093, | 0.0291, | 0.0491, | 0.0990 |
| | 0.0293, | 0.0297, | 0.0299, | 0.0301, | 0.0302, | 0.0304, | 0.0307, | 0.0311, | 0.0322 |
| | 0.0305 | 0.0311 | 0.0314 | 0.0317 | 0.0318 | 0.032 | 0.0323 | 0.0326 | 0.0336 |
| cML-BIC | 0.924, | 0.378, | 0.165, | 0.058, | 0.046, | 0.051, | 0.143, | 0.330, | 0.860, |
| | -0.1008, | -0.0507, | -0.0306, | -0.0106, | -0.0006, | 0.0094, | 0.0293, | 0.0493, | 0.0994 |
| | 0.0294, | 0.0299, | 0.0302, | 0.0304, | 0.0306, | 0.0308, | 0.0310, | 0.0314, | 0.0323 |
| | 0.03 | 0.0305 | 0.0308 | 0.0311 | 0.0312 | 0.0314 | 0.0317 | 0.032 | 0.033 |
| cML-BIC-Profile | 0.923, | 0.371, | 0.162, | 0.055, | 0.046, | 0.049, | 0.140, | | 0.859, |
| CAL DICTIONS | -0.1008, | -0.0507, | -0.0306, | -0.0106, | -0.0006, | 0.0094, | 0.0293, | 0.327, 0.0493, | 0.0994 |
| | 0.0294, | 0.0299, | | 0.0304, | 0.0306, | 0.0094, | 0.0293, | 0.0775, | 0.0334 |
| | | | 0.0302, | | | | | 0.0314, | 0.0323 |
| MD M | 0.0301 | 0.0307 | 0.0309 | 0.0312 | 0.0314 | 0.0315 | 0.0318 | 0.0322 | 0.0331 |
| MR-Mix | 0.845, | 0.288, | 0.105, | 0.038, | 0.024, | 0.039, | 0.095, | 0.235, | 0.743, |
| | -0.1057, | -0.0525, | -0.0318, | -0.0113, | -0.0012, | 0.0088, | 0.0283, | 0.0476, | 0.0935 |
| | 0.0329, | 0.0327, | 0.0325, | 0.0327, | 0.0327, | 0.0327, | 0.0328, | 0.0328, | 0.0329 |
| | 0.0376 | 0.0375 | 0.0373 | 0.0371 | 0.0371 | 0.037 | 0.0372 | 0.0372 | 0.0375 |
| MR-ContMix | 0.912, | 0.398, | 0.178, | 0.062, | 0.048, | 0.064, | 0.153, | 0.335, | 0.861, |
| | -0.1000, | -0.0503, | -0.0304, | -0.0106, | -0.0006, | 0.0093, | 0.0291, | 0.0489, | 0.0987 |
| | 0.0308, | 0.0314, | 0.0317, | 0.0319, | 0.0320, | 0.0322, | 0.0325, | 0.0329, | 0.0339 |
| | NA |
| MR-Lasso | 0.880, | 0.328, | 0.132, | 0.047, | 0.035, | 0.048, | 0.115, | 0.291, | 0.809, |
| WIK-Lasso | | -0.0490, | -0.0293, | -0.0094, | 0.0005, | 0.0105, | 0.0306, | 0.0506, | 0.1003 |
| | -0.0987, | | | | | | | | |
| | 0.0478, | 0.0505, | 0.0506, | 0.0507, | 0.0487, | 0.0509, | 0.0511, | 0.0513, | 0.0519 |
| | 0.0329 | 0.0335 | 0.0338 | 0.0341 | 0.0344 | 0.0345 | 0.0349 | 0.0352 | 0.0362 |
| MR-PRESSO | 0.396, | 0.212, | 0.154, | 0.128, | 0.125, | 0.127, | 0.161, | 0.234, | 0.391, |
| | -0.0857, | -0.0373, | -0.0177, | 0.0011, | 0.0108, | 0.0207, | 0.0399, | 0.0587, | 0.1063 |
| | 0.3268, | 0.3259, | 0.3262, | 0.3253, | 0.3251, | 0.3251, | 0.3244, | 0.3231, | 0.3219 |
| | 0.1621 | 0.1603 | 0.1606 | 0.1586 | 0.1581 | 0.1581 | 0.1559 | 0.1532 | 0.1516 |
| MR-IVW | 0.097, | 0.103, | 0.109, | 0.112, | 0.113, | 0.112, | 0.112, | 0.112, | 0.106, |
| | -0.0905, | -0.0403, | -0.0203, | -0.0002, | 0.0098, | 0.0198, | 0.0399, | 0.0599, | 0.1100 |
| | 0.3440, | 0.3439, | 0.3439, | 0.3439, | 0.3438, | 0.3438, | 0.3438, | 0.3438, | 0.3437 |
| | 0.3283 | 0.3283 | 0.3283 | 0.3283 | 0.3283 | 0.3283 | 0.3283 | 0.3283 | 0.3283 |
| MD IVIV Ol. | | | | | | | | | |
| MR-IVW-Oracle | 0.884, | 0.324, | 0.130, | 0.045, | 0.031, | 0.042, | 0.108, | 0.283, | 0.810, |
| | -0.1003, | -0.0505, | -0.0306, | -0.0107, | -0.0007, | 0.0092, | 0.0292, | 0.0491, | 0.0989 |
| | 0.0291, | 0.0296, | 0.0298, | 0.0301, | 0.0303, | 0.0304, | 0.0307, | 0.0311, | 0.0321 |
| | 0.0328 | 0.0335 | 0.0338 | 0.0341 | 0.0343 | 0.0344 | 0.0348 | 0.0351 | 0.0361 |
| MR-Egger | 0.079, | 0.079, | 0.080, | 0.082, | 0.082, | 0.082, | 0.081, | 0.080, | 0.080, |
| | -0.0580, | -0.0142, | 0.0033, | 0.0208, | 0.0296, | 0.0384, | 0.0559, | 0.0734, | 0.1171 |
| | 1.8427, | 1.8425, | 1.8424, | 1.8424, | 1.8423, | 1.8423, | 1.8422, | 1.8422, | 1.8421 |
| | 1.7924 | 1.7922 | 1.7921 | 1.7921 | 1.792 | 1.792 | 1.7919 | 1.7919 | 1.7918 |
| MR-Weighted-Median | 0.721, | 0.225, | 0.081, | 0.033, | 0.037, | 0.044, | 0.085, | 0.199, | 0.642, |
| · · · · · · · · · · · · · · · · · · · | -0.0969, | -0.0484, | -0.0291, | -0.0098, | -0.0002, | 0.0095, | 0.083, | 0.199, | 0.042, |
| | 0.0356, | 0.0362, | 0.0366, | 0.0370, | 0.0372, | | 0.0288, | 0.0480, | 0.0339 |
| | | | | | | 0.0375, | | | |
| 100 W/ 1 | 0.0384 | 0.0391 | 0.0394 | 0.0398 | 0.04 | 0.0402 | 0.0406 | 0.041 | 0.0422 |
| MR-Weighted-Mode | 0.872, | 0.300, | 0.120, | 0.047, | 0.044, | 0.052, | 0.104, | 0.271, | 0.795, |
| | -0.0988, | -0.0497, | -0.0302, | -0.0103, | -0.0005, | 0.0093, | 0.0289, | 0.0484, | 0.0978 |
| | 0.0309, | 0.0313, | 0.0315, | 0.0318, | 0.0321, | 0.0322, | 0.0325, | 0.0329, | 0.0337 |
| | 0.0331 | 0.0337 | 0.034 | 0.0343 | 0.0345 | 0.0346 | 0.035 | 0.0353 | 0.0364 |
| MR-RAPS1 | 0.105, | 0.116, | 0.120, | 0.119, | 0.118, | 0.115, | 0.117, | 0.114, | 0.111, |
| | -0.0930, | -0.0429, | -0.0229, | -0.0029, | 0.0072, | 0.0172, | 0.0372, | 0.0572, | 0.1073 |
| | 0.3354, | 0.3355, | 0.3355, | 0.3355, | 0.3355, | 0.3355, | 0.3355, | 0.3355, | 0.3356 |
| | 0.3142 | 0.3142 | 0.3142 | 0.3142 | 0.3142 | 0.3142 | 0.3142 | 0.3142 | 0.3143 |
| MR-RAPS2 | 0.078, | 0.076, | 0.084, | 0.086, | 0.092, | 0.092, | 0.087, | 0.087, | 0.079, |
| MIN-NAP32 | | | | | | | | | |
| | -0.0942, | -0.0450, | -0.0233, | -0.0028, | 0.0066, | 0.0167, | 0.0354, | 0.0570, | 0.1062 |
| | 0.3292, | 0.3300, | 0.3317, | 0.3293, | 0.3299, | 0.3302, | 0.3275, | 0.3269, | 0.3302 |
| | 0.327 | 0.3276 | 0.3279 | 0.3286 | 0.3291 | 0.3295 | 0.3285 | 0.3275 | 0.3301 |
| MR-RAPS3 | 0.896, | 0.864, | 0.857, | 0.856, | 0.862, | 0.859, | 0.861, | 0.877, | 0.896, |
| | -0.3241, | 0.1266, | 0.1445, | 2.4271, | 1.3950, | -0.3627, | -0.0916, | 0.3121, | 0.6502 |
| | 13.0930, | 20.7751, | 19.5143, | 49.5897, | 42.3294, | 10.3500, | 7.1335, | 6.6967, | 12.823 |
| | 12.7633 | 38.25 | 35.1805 | 195.9921 | 42.5294, | 10.5500, | 57.192 | 7.4227 | 18.253 |
| MD D / PG / | | | | | | | | | |
| MR-RAPS4 | 0.986, | 0.983, | 0.974, | 0.961, | 0.952, | 0.953, | 0.963, | 0.971, | 0.990, |
| | 0.3623, | 0.3262, | 0.3552, | 0.3088, | 0.3373, | 0.2926, | 0.2641, | 0.2457, | 0.1394 |
| | | | | | | | | | |
| | 1.5807, 0.1621 | 1.6056, 0.1149 | 1.5778, 0.1227 | 1.6007, 0.8658 | 1.6014, 0.1237 | 1.5770, 0.1079 | 1.6315, 0.1217 | 1.6184, 0.1786 | 1.6111, 0.1694 |

Table S33: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE satisfied, q=0.4, and N=100000.

| θ | | | | | | | | | |
|--|---|--|---|---|---|--|--|--|--|
| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.838, | 0.256, | 0.076, | 0.012, | 0.012, | 0.023, | 0.082, | 0.240, | 0.774, |
| CIVIL WITTING | -0.0857, | -0.0378, | -0.0209, | -0.0064, | 0.0005, | 0.0071, | 0.0217, | 0.0379, | 0.0850 |
| | 0.0257, | 0.0235, | 0.0212, | 0.0195, | 0.0195, | 0.0200, | 0.0224, | 0.0253, | 0.0288 |
| | 0.0237, | 0.0233, | 0.0212, | 0.0193, | 0.0193, | 0.0200, | 0.0224, | 0.0233, | 0.0288 |
| MI MA AIC D. GI. | | | | | | | | | |
| cML-MA-AIC-Profile | 0.838, | 0.255, | 0.073, | 0.011, | 0.012, | 0.021, | 0.082, | 0.238, | 0.774, |
| | -0.0858, | -0.0378, | -0.0209, | -0.0064, | 0.0005, | 0.0071, | 0.0217, | 0.0379, | 0.0851 |
| | 0.0258, | 0.0235, | 0.0213, | 0.0195, | 0.0195, | 0.0200, | 0.0225, | 0.0253, | 0.0288 |
| | 0.0287 | 0.0285 | 0.0281 | 0.0279 | 0.028 | 0.0282 | 0.029 | 0.0298 | 0.0314 |
| cML-AIC | 0.920, | 0.509, | 0.224, | 0.078, | 0.069, | 0.085, | 0.214, | 0.470, | 0.890, |
| | -0.0921, | -0.0428, | -0.0245, | -0.0082, | 0.0003, | 0.0084, | 0.0249, | 0.0427, | 0.0916 |
| | 0.0286, | 0.0278, | 0.0265, | 0.0253, | 0.0252, | 0.0259, | 0.0280, | 0.0297, | 0.0317 |
| | 0.023 | 0.0235 | 0.0236 | 0.0239 | 0.024 | 0.0241 | 0.0243 | 0.0246 | 0.0252 |
| cML-AIC-Profile | | | | | | | 0.211, | | |
| CML-AIC-FIGHE | 0.920, | 0.508, | 0.222, | 0.077, | 0.067, | 0.085, | | 0.468, | 0.890, |
| | -0.0921, | -0.0428, | -0.0245, | -0.0082, | 0.0003, | 0.0084, | 0.0249, | 0.0427, | 0.0916 |
| | 0.0287, | 0.0278, | 0.0265, | 0.0253, | 0.0252, | 0.0259, | 0.0280, | 0.0297, | 0.0317 |
| | 0.0231 | 0.0235 | 0.0237 | 0.0239 | 0.0241 | 0.0241 | 0.0244 | 0.0246 | 0.0253 |
| cML-MA-BIC | 0.992, | 0.646, | 0.278, | 0.076, | 0.045, | 0.070, | 0.260, | 0.581, | 0.984, |
| | -0.0997, | -0.0497, | -0.0298, | -0.0099, | 0.0001, | 0.0100, | 0.0300, | 0.0499, | 0.0999 |
| | 0.0213, | 0.0217, | 0.0219, | 0.0221, | 0.0222, | 0.0223, | 0.0226, | 0.0229, | 0.0236 |
| | 0.0214 | 0.0218 | 0.022 | 0.0222 | 0.0223 | 0.0224 | 0.0226 | 0.0229 | 0.0235 |
| ML-MA-BIC-Profile | 0.992, | 0.644, | 0.275, | 0.074, | 0.045, | 0.069, | 0.259, | 0.581, | 0.984, |
| CWIE-WIA-BIC-1 TOILIC | -0.0997, | -0.0497, | -0.0298, | -0.0099, | 0.0001, | 0.0100, | 0.0300, | 0.0499, | 0.0999 |
| | | | | | | | | | |
| | 0.0213, | 0.0217, | 0.0219, | 0.0221, | 0.0222, | 0.0223, | 0.0226, | 0.0229, | 0.0236 |
| | 0.0215 | 0.0218 | 0.022 | 0.0222 | 0.0223 | 0.0224 | 0.0227 | 0.0229 | 0.0236 |
| cML-BIC | 0.992, | 0.654, | 0.286, | 0.081, | 0.050, | 0.075, | 0.268, | 0.595, | 0.988, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001 |
| | 0.0213, | 0.0218, | 0.0220, | 0.0222, | 0.0223, | 0.0225, | 0.0227, | 0.0230, | 0.0237 |
| | 0.0212 | 0.0215 | 0.0217 | 0.0219 | 0.022 | 0.0221 | 0.0224 | 0.0226 | 0.0233 |
| cML-BIC-Profile | 0.992, | 0.654, | 0.284, | 0.080, | 0.050, | 0.075, | 0.267, | 0.594, | 0.988, |
| CAL DICTIONS | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.207, 0.0301, | 0.0501, | 0.1001 |
| | | | | | | | | | |
| | 0.0213, | 0.0218, | 0.0220, | 0.0222, | 0.0223, | 0.0225, | 0.0227, | 0.0230, | 0.0237 |
| 100.10 | 0.0212 | 0.0216 | 0.0218 | 0.022 | 0.0221 | 0.0222 | 0.0224 | 0.0226 | 0.0233 |
| MR-Mix | 0.971, | 0.502, | 0.197, | 0.053, | 0.035, | 0.052, | 0.173, | 0.441, | 0.943, |
| | -0.1040, | -0.0511, | -0.0303, | -0.0100, | -0.0001, | 0.0098, | 0.0293, | 0.0485, | 0.0945 |
| | 0.0241, | 0.0240, | 0.0242, | 0.0242, | 0.0243, | 0.0243, | 0.0243, | 0.0243, | 0.0243 |
| | 0.0273 | 0.027 | 0.027 | 0.0276 | 0.0276 | 0.0277 | 0.0276 | 0.0278 | 0.0273 |
| MR-ContMix | 0.992, | 0.667, | 0.312, | 0.100, | 0.071, | 0.096, | 0.295, | 0.607, | 0.985, |
| mit commi | -0.0998, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0502, | 0.1001 |
| | 0.0225, | 0.0228, | 0.0230, | 0.0232, | 0.0233, | 0.0234, | 0.0236, | 0.0239, | 0.0246 |
| | | 0.0228, NA | | | 0.0233, NA | | 0.0230, NA | | |
|) III I | NA 0.000 | | NA | NA 0.067 | | NA | | NA 0.520 | NA |
| MR-Lasso | 0.980, | 0.582, | 0.244, | 0.067, | 0.039, | 0.066, | 0.232, | 0.539, | 0.969, |
| | -0.0994, | -0.0495, | -0.0296, | -0.0095, | 0.0004, | 0.0104, | 0.0304, | 0.0505, | 0.1002 |
| | 0.0224, | 0.0227, | 0.0229, | 0.0232, | 0.0234, | 0.0235, | 0.0236, | 0.0239, | 0.0250 |
| | 0.0232 | 0.0236 | 0.0239 | 0.0241 | 0.0242 | 0.0243 | 0.0246 | 0.0248 | 0.0256 |
| MR-PRESSO | 0.394, | 0.256, | 0.173, | 0.132, | 0.120, | 0.122, | 0.170, | 0.244, | 0.402, |
| | -0.0834, | -0.0338, | -0.0142, | 0.0057, | 0.0159, | 0.0260, | 0.0456, | 0.0657, | 0.1150 |
| | 0.3375, | 0.3374, | 0.3373, | 0.3373, | 0.3373, | 0.3373, | 0.3368, | 0.3363, | 0.3353 |
| | 0.2048 | 0.2043 | 0.2034 | 0.2034 | 0.2031 | 0.2031 | 0.2008 | 0.1987 | 0.1947 |
| MR-IVW | 0.108, | 0.113, | | 0.120, | 0.2031 | 0.122, | 0.120, | 0.121, | |
| MK-IVW | 0.108, | | 0.116, | | | | | | 0.113, |
| | 0.0055 | | -0.0154, | 0.0046, | 0.0147, | 0.0247, | 0.0447, | 0.0648, | 0.1149 |
| | -0.0857, | -0.0355, | | 0.3424, | 0.3424, | 0.3424, | 0.3424, | 0.3424, | 0.3423 |
| | 0.3425, | 0.3425, | 0.3425, | | | | | | |
| | 0.3425, 0.3298 | | | 0.3298 | 0.3298 | 0.3298 | 0.3298 | 0.3297 | |
| MR-IVW-Oracle | 0.3425, | 0.3425, | 0.3425, | | | | | | 0.3297 |
| MR-IVW-Oracle | 0.3425, 0.3298 0.989, | 0.3425, 0.3298 | 0.3425, 0.3298 0.237, | 0.3298 0.059, | 0.3298 0.033, | 0.3298 0.057, | 0.3298 | 0.3297 0.526, | 0.3297 0.970, |
| MR-IVW-Oracle | 0.3425, 0.3298 0.989, -0.0997, | 0.3425, 0.3298 0.586, -0.0498, | 0.3425, 0.3298 0.237, -0.0299, | 0.3298 0.059, -0.0099, | 0.3298 0.033, 0.0001, | 0.3298 0.057, 0.0101, | 0.3298 0.220, 0.0300, | 0.3297 0.526, 0.0500, | 0.3297 0.970, 0.0998 |
| MR-IVW-Oracle | 0.3425, 0.3298 0.989, -0.0997, 0.0212, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, | 0.3298 0.059, -0.0099, 0.0220, | 0.3298 0.033, 0.0001, 0.0222, | 0.3298 0.057, 0.0101, 0.0223, | 0.3298 0.220, 0.0300, 0.0225, | 0.3297 0.526, 0.0500, 0.0228, | 0.3297 0.970, 0.0998 0.0235 |
| | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 | 0.3298 0.220, 0.0300, 0.0225, 0.0246 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 | 0.3297 0.970, 0.0998 0.0235 0.0255 |
| MR-IVW-Oracle MR-Egger | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, | 0.3297 0.970, 0.0998 0.0235 0.0255 |
| | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 |
| | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 |
| MR-Egger | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 |
| MR-Egger | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, |
| MR-Egger | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, |
| MR-Egger | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0989 |
| MR-Egger | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0989 0.0287 |
| MR-Egger MR-Weighted-Median | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, 0.0282 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0989 0.0287 0.0298 |
| MR-Egger MR-Weighted-Median | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, 0.0282 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.02284 | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0988 0.0298 0.0298 |
| MR-Egger MR-Weighted-Median | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0259, 0.0271 0.985, -0.0991, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, 0.0282 0.042, 0.0000, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.1282 1.9314 1.859 0.912, 0.0988 0.0287 0.0287 0.0280 0.0968, 0.0990 |
| MR-Egger MR-Weighted-Median | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0282 0.042, 0.0000, 0.0235, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0989 0.0287 0.0298 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.024 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, 0.0269, 0.0282 0.042, 0.0000, 0.0235, 0.0243 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0988 0.0287 0.0298 0.0968, 0.0908 0.0250 |
| MR-Egger MR-Weighted-Median | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.024 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, 0.0282 0.0042, 0.0000, 0.0235, 0.0243 0.126, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.8559 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0239, 0.0239, 0.0247 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0988 0.0256 0.0298 0.0255 0.0298 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.024 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0282 0.042, 0.0023, 0.0243 0.126, 0.0107, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0287 0.219, 0.0239, 0.0239, 0.0247 0.127, 0.0407, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0988 0.0287 0.0298 0.0255 0.0 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, 0.3356, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.024 0.123, -0.0193, 0.3356, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.9324, 1.9324, 0.0008, 0.0269, 0.0269, 0.0223, 0.0000, 0.0235, 0.0243 0.126, 0.0107, 0.3356, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0270, 0.0236, 0.0245 0.129, 0.0207, 0.3356, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.8559 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, 0.3356, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0988 0.0287 0.0298 0.0255 0.0 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.024 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0282 0.042, 0.0000, 0.0235, 0.0243 0.1126, 0.0107, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0287 0.219, 0.0239, 0.0239, 0.0247 0.127, 0.0407, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0988 0.0287 0.0298 0.0255 0.0 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0232, 0.0393, 0.3356, 0.3135 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.0193, -0.0193, 0.3356, 0.3136 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.3136 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, 0.0282 0.042, 0.0000, 0.0235, 0.0243 0.126, 0.0107, 0.3356, 0.3136 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.8559 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0207, 0.0207, 0.0207, 0.0207, 0.0356, 0.0336, 0. | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.8559 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, 0.3136 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.3136 | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0287 0.0287 0.0298 0.0968, 0.0999 0.0250 0.0255 0.115, 0.1100 0.3355 0.3136 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.995, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 0.079, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, 0.3356, 0.3135 0.089, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.024 0.123, -0.0193, 0.3356, 0.3136 0.095, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.3136 0.097, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0282 0.042, 0.00243 0.126, 0.0107, 0.3356, 0.3136 0.098, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.3356, 0.3356, 0.091, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, 0.3136 0.090, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.3136 0.088, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0988 0.0288 0.0298 0.0257 0.1155, 0.1106 0.3357 0.1106 0.3357 0.1106 0.3357 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, 0.3356, 0.3135 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.024 0.123, -0.0193, 0.3356, 0.3136 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, -0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.3136 0.097, -0.0004, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, 0.0282 0.042, 0.0000, 0.0235, 0.0243 0.126, 0.0107, 0.3356, 0.3136 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.3356, 0.3136 0.091, 0.0212, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, 0.3136 0.090, 0.0389, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.3136 0.088, 0.0607, | 0.3297 0.970, 0.0998 0.0235 0.0955, 0.1282 1.9314 1.859 0.912, 0.0988 0.0287 0.0298 0.0255 0.055, 0.1000 0.0257 0.0100 0.03357 0.115, 0.1100 0.3357 0.3133 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 0.079, -0.0884, 0.3207, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0232, 0.3135 0.0393, 0.3356, 0.3135 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.0193, 0.3356, 0.3136 0.095, -0.0200, 0.3234, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.3136 0.097, -0.0004, 0.3248, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, 0.0282 0.042, 0.0000, 0.0235, 0.0243 0.126, 0.0107, 0.3356, 0.3136 0.098, 0.098, 0.0090, 0.3245, | 0.3298 0.057, 0.01011, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.8559 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.33566, 0.3136 0.091, 0.0212, 0.3291, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.8559 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, 0.3136 0.090, 0.0389, 0.03249, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.3136 0.088, 0.0607, 0.3264, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0985 0.0287 0.1050 0.0257 0.115, 0.1106 0.33575 0.3136 0.082, 0.082, 0.082, 0.1082, 0.1082, |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 0.079, -0.0884, 0.3207, 0.3192 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, 0.3356, 0.3135 0.089, -0.0376, 0.3234, 0.3238 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.0193, 0.3356, 0.3136 0.095, -0.0200, 0.3234, 0.3236 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.0136, 0.0097, -0.0004, 0.3248, 0.3244 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0282 0.042, 0.0023, 0.00243 0.126, 0.0107, 0.3356, 0.3136 0.098, 0.0090, 0.3245, 0.3247 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.3356, 0.091, 0.0212, 0.3291, 0.3251 | 0.3298 0.220, 0.0300, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0299, 0.0239, 0.0247 0.127, 0.0407, 0.3136, 0.3136 0.090, 0.0389, 0.03249, 0.3255 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.088, 0.0607, 0.3275 | 0.3297 0.970, 0.0998 0.0235 0.0255 0.1282 1.9314 1.859 0.912, 0.0985 0.0257 0.0257 0.0257 0.0257 0.0257 0.0257 0.0257 0.0257 0.115. 0.1106 0.3357 0.082, 0.1090 0.3266 0.3275 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 0.079, -0.0884, 0.3207, 0.3192 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0232, 0.0238 0.119, -0.0393, 0.3356, 0.3135 0.089, -0.0376, 0.3234, 0.3238 0.916, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0294, 0.024 0.123, -0.0193, 0.3356, 0.3136 0.095, -0.0200, 0.3234, 0.3236 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, -0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.3136 0.097, -0.0004, 0.3248, 0.324 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, 0.0282 0.042, 0.0000, 0.0235, 0.0243 0.126, 0.0107, 0.3356, 0.3136 0.099, 0.3245, 0.3247 0.887, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.3356, 0.3136 0.091, 0.0212, 0.3291, 0.3251 0.891, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, 0.3136 0.090, 0.0389, 0.3249, 0.3255 0.898, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.3356, 0.3136 0.088, 0.0607, 0.3264, 0.3275 0.907, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0989 0.0287 0.0298 0.0250 0.0257 0.115, 0.1106 0.3357 0.3136 0.082, 0.1090 0.3269 0.3279 0.926, |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 0.079, -0.0884, 0.3207, 0.3192 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, 0.3356, 0.3135 0.089, -0.0376, 0.3234, 0.3238 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.0193, 0.3356, 0.3136 0.095, -0.0200, 0.3234, 0.3236 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.0136, 0.0097, -0.0004, 0.3248, 0.3244 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0282 0.042, 0.0023, 0.00243 0.126, 0.0107, 0.3356, 0.3136 0.098, 0.0090, 0.3245, 0.3247 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.3356, 0.091, 0.0212, 0.3291, 0.3251 | 0.3298 0.220, 0.0300, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0299, 0.0239, 0.0247 0.127, 0.0407, 0.3136, 0.3136 0.090, 0.0389, 0.03249, 0.3255 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.088, 0.0607, 0.3275 | 0.3297 0.970, 0.0998 0.0235 0.095, 0.1282 1.9314 1.859 0.912, 0.0988 0.0287 0.0258 0.095, 0.1000 0.3357 0.3156 0.3357 0.3160 0.3269 0.3279 0.926, |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.03355, 0.3135 0.079, -0.0884, 0.3207, 0.3192 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.03356, 0.3135 0.089, -0.0334, 0.3238 0.916, -0.3338, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.0193, 0.3356, 0.3136 0.095, -0.0200, 0.3234, 0.3236 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.3136 0.097, -0.0004, 0.3248, 0.324 0.899, -1.2781, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0269, 0.0282 0.042, 0.0000, 0.0235, 0.0243 0.126, 0.0107, 0.3356, 0.3136 0.098, 0.0098, 0.0245 0.098, 0.099, 0.3245, 0.3247 0.887, -0.5316, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.3356, 0.3136 0.091, 0.0212, 0.3291, 0.3251 0.891, 0.1034, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1,9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, 0.3136 0.090, 0.0389, 0.3249, 0.3255 0.898, -1.7426, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.3136 0.088, 0.0607, 0.3264, 0.3275 0.907, 0.3672, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.0955, 0.1282 1.9314 1.859 0.912, 0.0989 0.0257 0.115, 0.1106 0.03577 0.3136 0.082, 0.10900 0.3269 0.3279 0.9228 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 0.079, -0.0884, 0.3207, 0.3192 0.942, -15.7267, 585.1517, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, 0.3356, 0.3234, 0.3238 0.916, -0.3338, 10.4566, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.0244, -0.0297, 0.0234, 0.0193, 0.3136 0.095, -0.0200, 0.3234, 0.3236 0.908, 0.1956, 25.4131, | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.007, 0.3356, 0.0242 0.125, 0.0097, 0.0342, 0.097, -0.0004, 0.3248, 0.324 0.899, -1.2781, 45.5970, | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0282 0.042, 0.0023, 0.0243 0.126, 0.0107, 0.3356, 0.016, 0.3136 0.098, 0.0090, 0.3245, 0.3247 0.887, -0.5316, 40.8729, | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.3356, 0.091, 0.0212, 0.3291, 0.3251 0.891, 0.1034, 28.1294, | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, 0.3136 0.090, 0.0389, 0.3249, 0.3255 0.898, -1.7426, 58.0315, | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.3136 0.088, 0.0607, 0.3264, 0.3275 0.997, 0.5672, 9.1414, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.1282 1.9314 1.859 0.912, 0.0988 0.0287 0.0298 0.0287 0.0250 0.0257 0.115, 0.1106 0.3357 0.115, 0.1106 0.3357 0.015, 0.11090 0.3269 0.3279 0.926, 0.2282 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 0.3192 0.942, -15.7267, 585,1517, 13300 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, 0.3356, 0.3234, 0.3234, 0.3238 0.916, -0.3338, 10.4566, 26.03 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.024 0.123, -0.0193, 0.3356, 0.3136 0.095, -0.0200, 0.3234, 0.0295, -0.0200, 0.3234, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.254, 1131, 45.07 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, -0.0095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.3136 0.097, -0.0004, 0.3248, 0.3244 0.899, -1.2781, 45.5970, 1116.2 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0282 0.042, 0.0000, 0.0235, 0.0243 0.126, 0.0107, 0.3356, 0.3136 0.099, 0.3245, 0.3247 0.887, -0.5316, 40.8729, 182 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.3356, 0.3136 0.091, 0.0212, 0.3251 0.891, 0.1034, 28.1294, 39.4 | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, 0.3136 0.090, 0.0389, 0.3249, 0.3255 0.898, -1.7426, 58.0315, 1103 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.3136 0.088, 0.0607, 0.3264, 0.3275 0.907, 0.5672, 9.1414, 6.23 | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0989 0.0287 0.0298 0.0258 0.0950 0.0257 0.1150 0.3357 0.3136 0.3357 0.31090 0.3269 0.3279 0.926, 0.2286 5.0424 5.0425 |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 0.079, -0.0884, 0.3207, 0.3192 0.942, -15.7267, 585.1517, 13300 0.972, | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, 0.3356, 0.3135 0.089, -0.0376, 0.3234, 0.3238, 0.916, -0.3338, 10.4566, 26.03 0.983, | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.024 0.123, -0.0193, 0.3356, 0.3136 0.095, -0.0200, 0.3234, 0.908, 0.1956, 25.4131, 45.07 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.3136 0.097, -0.0004, 0.3248, 0.324 0.899, -1.2781, 45.5970, 116.2 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.9324, 0.0008, 0.0269, 0.0282 0.042, 0.0000, 0.0235, 0.0243 0.126, 0.0107, 0.3356, 0.3136 0.098, 0.0090, 0.3245, 0.3247 0.887, -0.5316, 40.8729, 182 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.3356, 0.3136 0.091, 0.0212, 0.3291, 0.3251 0.891, 0.1034, 28.1294, 39.4 | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.8559 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, 0.3136 0.090, 0.0389, 0.3249, 0.3255 0.898, -1.7426, 58.0315, 1103 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.3136 0.088, 0.0607, 0.3264, 0.3275 0.907, 0.5672, 9.1414, 6.23 0.993, | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0988 0.0257 0.015, 0.1000 0.0257 0.115, 0.1106 0.3357 0.3136 0.082, 0.1090 0.3269 0.3279 0.926, 0.2286 5.0424 2.527 0.998, |
| MR-Egger MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.3425, 0.3298 0.989, -0.0997, 0.0212, 0.0232 0.094, -0.0602, 1.9334, 1.859 0.948, -0.0974, 0.0259, 0.0271 0.985, -0.0991, 0.0226, 0.0234 0.112, -0.0893, 0.3355, 0.3135 0.3192 0.942, -15.7267, 585,1517, 13300 | 0.3425, 0.3298 0.586, -0.0498, 0.0216, 0.0237 0.092, -0.0130, 1.9329, 1.859 0.436, -0.0483, 0.0264, 0.0276 0.563, -0.0496, 0.0232, 0.0238 0.119, -0.0393, 0.3356, 0.3234, 0.3234, 0.3238 0.916, -0.3338, 10.4566, 26.03 | 0.3425, 0.3298 0.237, -0.0299, 0.0218, 0.0239 0.092, 0.0058, 1.9327, 1.859 0.161, -0.0287, 0.0266, 0.0278 0.244, -0.0297, 0.0234, 0.024 0.123, -0.0193, 0.3356, 0.3136 0.095, -0.0200, 0.3234, 0.0295, -0.0200, 0.3234, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.1956, 0.254, 1131, 45.07 | 0.3298 0.059, -0.0099, 0.0220, 0.0241 0.095, -0.0095, 0.0246, 1.9325, 1.859 0.044, -0.0090, 0.0268, 0.0281 0.066, -0.0100, 0.0235, 0.0242 0.125, 0.0007, 0.3356, 0.3136 0.097, -0.0004, 0.3248, 0.3244 0.899, -1.2781, 45.5970, 1116.2 | 0.3298 0.033, 0.0001, 0.0222, 0.0242 0.095, 0.0341, 1.9324, 1.859 0.043, 0.0008, 0.0282 0.042, 0.0000, 0.0235, 0.0243 0.126, 0.0107, 0.3356, 0.3136 0.099, 0.3245, 0.3247 0.887, -0.5316, 40.8729, 182 | 0.3298 0.057, 0.0101, 0.0223, 0.0243 0.095, 0.0435, 1.9323, 1.859 0.052, 0.0107, 0.0270, 0.0284 0.054, 0.0100, 0.0236, 0.0245 0.129, 0.0207, 0.3356, 0.3136 0.091, 0.0212, 0.3251 0.891, 0.1034, 28.1294, 39.4 | 0.3298 0.220, 0.0300, 0.0225, 0.0246 0.095, 0.0623, 1.9320, 1.859 0.181, 0.0303, 0.0273, 0.0287 0.219, 0.0298, 0.0239, 0.0247 0.127, 0.0407, 0.3356, 0.3136 0.090, 0.0389, 0.3249, 0.3255 0.898, -1.7426, 58.0315, 1103 | 0.3297 0.526, 0.0500, 0.0228, 0.0248 0.095, 0.0812, 1.9318, 1.859 0.411, 0.0499, 0.0277, 0.029 0.527, 0.0496, 0.0245, 0.025 0.126, 0.0607, 0.3356, 0.3136 0.088, 0.0607, 0.3264, 0.3275 0.907, 0.5672, 9.1414, 6.23 | 0.3297 0.970, 0.0998 0.0235 0.0255 0.095, 0.1282 1.9314 1.859 0.912, 0.0989 0.0287 0.0298 0.0258 0.0950 0.0257 0.1150 0.3357 0.3136 0.3357 0.31090 0.3269 0.3279 0.926, 0.2286 5.0424 5.0425 |

Table S34: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE satisfied, q=0.4, and N=200000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|-------------------|----------|-------------------|----------|---------------------|----------|----------|----------|---------|---------|
| cML-MA-AIC | 0.979, | 0.557, | 0.170, | 0.022, | 0.013, | 0.029, | 0.168, | 0.495, | 0.946, |
| | -0.0906, | -0.0409, | -0.0227, | -0.0072, | -0.0003, | 0.0066, | 0.0220, | 0.0399, | 0.0889, |
| | 0.0187, | 0.0182, | 0.0165, | 0.0144, | 0.0139, | 0.0145, | 0.0170, | 0.0194, | 0.0210, |
| M M MG D CI | 0.0203 | 0.0205 | 0.0202 | 0.0198 | 0.0198 | 0.0199 | 0.0206 | 0.0213 | 0.0223 |
| ML-MA-AIC-Profile | 0.979, | 0.556, | 0.171, | 0.022, | 0.013, | 0.028, | 0.168, | 0.492, | 0.946, |
| | -0.0907, | -0.0410, | -0.0227, | -0.0072, | -0.0004, | 0.0066, | 0.0220, | 0.0399, | 0.0890, |
| | 0.0188, | 0.0182, | 0.0165, | 0.0143, | 0.0139, | 0.0145, | 0.0170, | 0.0194, | 0.0210, |
| -MI AIC | 0.0203 | 0.0205 | 0.0202 | 0.0198 | 0.0198 | 0.0199 | 0.0207 | 0.0214 | 0.0223 |
| cML-AIC | 0.986, | 0.739, | 0.412, | 0.103, | 0.068, | 0.107, | 0.368, | 0.698, | 0.977, |
| | -0.0950, | -0.0450, | -0.0261, | -0.0086, | -0.0005, | 0.0075, | 0.0250, | 0.0439, | 0.0937 |
| | 0.0210, | 0.0209, | 0.0200, | 0.0186, | 0.0183, | 0.0187, | 0.0204, | 0.0222, | 0.0231 |
| M. AICD CI | 0.0163 | 0.0166 | 0.0167 | 0.0169 | 0.0169 | 0.0171 | 0.0173 | 0.0174 | 0.0179 |
| cML-AIC-Profile | 0.986, | 0.738, | 0.412, | 0.103, | 0.068, | 0.106, | 0.368, | 0.698, | 0.977, |
| | -0.0950, | -0.0451, | -0.0261, | -0.0086, | -0.0005, | 0.0075, | 0.0250, | 0.0439, | 0.0937 |
| | 0.0210, | 0.0209, | 0.0200, | 0.0186, | 0.0183, | 0.0187, | 0.0204, | 0.0222, | 0.0231 |
| M. M. DIG | 0.0163 | 0.0167 | 0.0168 | 0.0169 | 0.017 | 0.0171 | 0.0173 | 0.0175 | 0.018 |
| cML-MA-BIC | 1.000, | 0.894, | 0.516, | 0.097, | 0.055, | 0.101, | 0.466, | 0.861, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0098, | 0.0298, | 0.0498, | 0.0998 |
| | 0.0152, | 0.0155, | 0.0156, | 0.0157, | 0.0158, | 0.0159, | 0.0161, | 0.0163, | 0.0168 |
| | 0.0151 | 0.0154 | 0.0155 | 0.0157 | 0.0158 | 0.0158 | 0.016 | 0.0162 | 0.0166 |
| ML-MA-BIC-Profile | 1.000, | 0.894, | 0.515, | 0.097, | 0.055, | 0.100, | 0.466, | 0.861, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0098, | 0.0298, | 0.0498, | 0.0998 |
| | 0.0152, | 0.0155, | 0.0156, | 0.0157, | 0.0158, | 0.0159, | 0.0161, | 0.0163, | 0.0168 |
| M. DIG | 0.0152 | 0.0154 | 0.0156 | 0.0157 | 0.0158 | 0.0159 | 0.016 | 0.0162 | 0.0167 |
| cML-BIC | 1.000, | 0.899, | 0.525, | 0.102, | 0.057, | 0.103, | 0.473, | 0.863, | 1.000, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0099, | 0.0298, | 0.0499, | 0.0999 |
| | 0.0152, | 0.0155, | 0.0157, | 0.0158, | 0.0159, | 0.0160, | 0.0162, | 0.0164, | 0.0168 |
| MI DICE C | 0.015 | 0.0153 | 0.0154 | 0.0156 | 0.0156 | 0.0157 | 0.0159 | 0.0161 | 0.0165 |
| cML-BIC-Profile | 1.000, | 0.899, | 0.524, | 0.102, | 0.057, | 0.102, | 0.473, | 0.863, | 1.000, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0099, | 0.0298, | 0.0499, | 0.0999 |
| | 0.0152, | 0.0155, | 0.0157, | 0.0158, | 0.0159, | 0.0160, | 0.0162, | 0.0164, | 0.0168 |
| MD M | 0.015 | 0.0153 | 0.0154 | 0.0156 | 0.0157 | 0.0157 | 0.0159 | 0.0161 | 0.0165 |
| MR-Mix | 0.995, | 0.785, | 0.348, | 0.061, | 0.033, | 0.061, | 0.337, | 0.725, | 0.998, |
| | -0.1042, | -0.0512, | -0.0305, | -0.0102, | -0.0002, | 0.0098, | 0.0294, | 0.0486, | 0.0948 |
| | 0.0170, | 0.0168, | 0.0168, | 0.0169, | 0.0169, | 0.0169, | 0.0169, | 0.0170, | 0.0171 |
| | 0.0196 | 0.0196 | 0.0196 | 0.0194 | 0.0193 | 0.0193 | 0.0192 | 0.0192 | 0.0193 |
| MR-ContMix | 1.000, | 0.899, | 0.547, | 0.137, | 0.081, | 0.121, | 0.515, | 0.878, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0498, | 0.0998 |
| | 0.0157, | 0.0159, | 0.0161, | 0.0162, | 0.0163, | 0.0164, | 0.0165, | 0.0167, | 0.0173 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.850, | 0.454, | 0.092, | 0.052, | 0.082, | 0.409, | 0.815, | 0.999, |
| | -0.1002, | -0.0501, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0997 |
| | 0.0158, | 0.0159, | 0.0160, | 0.0161, | 0.0163, | 0.0163, | 0.0165, | 0.0167, | 0.0171 |
| | 0.0164 | 0.0168 | 0.0169 | 0.0171 | 0.0172 | 0.0173 | 0.0175 | 0.0176 | 0.0181 |
| MR-PRESSO | 0.356, | 0.286, | 0.195, | 0.120, | 0.107, | 0.110, | 0.172, | 0.254, | 0.350, |
| | -0.1064, | -0.0563, | -0.0364, | -0.0161, | -0.0062, | 0.0039, | 0.0241, | 0.0442, | 0.0944 |
| | 0.3365, | 0.3362, | 0.3362, | 0.3361, | 0.3360, | 0.3360, | 0.3359, | 0.3359, | 0.3356 |
| | 0.226 | 0.2244 | 0.2241 | 0.2229 | 0.2225 | 0.2226 | 0.222 | 0.2217 | 0.2197 |
| MR-IVW | 0.103, | 0.106, | 0.106, | 0.108, | 0.108, | 0.108, | 0.108, | 0.101, | 0.095, |
| | -0.1078, | -0.0575, | -0.0373, | -0.0172, | -0.0071, | 0.0029, | 0.0230, | 0.0432, | 0.0934 |
| | 0.3387, | 0.3386, | 0.3385, | 0.3385, | 0.3385, | 0.3384, | 0.3384, | 0.3384, | 0.3383 |
| | 0.3312 | 0.3311 | 0.3311 | 0.3311 | 0.3311 | 0.3311 | 0.3311 | 0.3311 | 0.331 |
| MR-IVW-Oracle | 1.000, | 0.851, | 0.447, | 0.084, | 0.048, | 0.078, | 0.411, | 0.820, | 1.000, |
| | -0.1000, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999 |
| | 0.0151, | 0.0154, | 0.0156, | 0.0157, | 0.0158, | 0.0158, | 0.0160, | 0.0162, | 0.0166 |
| 100.5 | 0.0165 | 0.0168 | 0.0169 | 0.0171 | 0.0172 | 0.0172 | 0.0174 | 0.0176 | 0.0181 |
| MR-Egger | 0.088, | 0.088, | 0.087, | 0.085, | 0.084, | 0.083, | 0.086, | 0.087, | 0.089, |
| | -0.1355, | -0.0867, | -0.0672, | -0.0476, 1.9648, | -0.0379, | -0.0281, | -0.0086, | 0.0109, | 0.0597 |
| | 1.9662, | 1.9654, | 1.9651, | 1.9048, | 1.9646, | 1.9644, | 1.9641, | 1.9638, | 1.9630 |
| D W | 1.8909 | 1.8908 | 1.8907 | 1.8907 | 1.8906 | 1.8906 | 1.8905 | 1.8905 | 1.8904 |
| R-Weighted-Median | 0.999, | 0.759, | 0.337, | 0.070, | 0.045, | 0.070, | 0.294, | 0.672, | 0.990, |
| | -0.0996, | -0.0501, | -0.0303, | -0.0105, | -0.0007, | 0.0092, | 0.0290, | 0.0487, | 0.0981 |
| | 0.0187, | 0.0190, | 0.0192, | 0.0194, | 0.0195, | 0.0196, | 0.0198, | 0.0200, | 0.0206 |
| (D. W.:.ba. 134 1 | 0.0192 | 0.0195 | 0.0197 | 0.0199 | 0.02 | 0.0201 | 0.0203 | 0.0205 | 0.0211 |
| MR-Weighted-Mode | 1.000, | 0.822, | 0.423, | 0.084, | 0.058, | 0.090, | 0.388, | 0.799, | 1.000, |
| | -0.0998, | -0.0500, | -0.0300, | -0.0101, | -0.0001, | 0.0098, | 0.0297, | 0.0496, | 0.0995 |
| | 0.0165, | 0.0168, | 0.0171, | 0.0171, | 0.0172, | 0.0173, | 0.0174, | 0.0176, | 0.0182 |
| MD DARGS | 0.0167 | 0.017 | 0.0171 | 0.0173 | 0.0174 | 0.0175 | 0.0176 | 0.0178 | 0.0183 |
| MR-RAPS1 | 0.105, | 0.116, | 0.116, | 0.116, | 0.117, | 0.117, | 0.112, | 0.106, | 0.100, |
| | -0.1065, | -0.0565, | -0.0365, | -0.0164, | -0.0064, | 0.0036, | 0.0236, | 0.0436, | 0.0936 |
| | 0.3270, | 0.3270, 0.3145 | 0.3270, | 0.3270, | 0.3270, | 0.3270, | 0.3270, | 0.3270, | 0.3271 |
| MD DARGO | 0.3145 | | 0.3145 | 0.3145 | 0.3145 | 0.3145 | 0.3145 | 0.3145 | 0.3145 |
| MR-RAPS2 | 0.069, | 0.038, | 0.036, | 0.035, | 0.035, | 0.035, | 0.036, | 0.039, | 0.060, |
| | -0.1094, | -0.0573, | -0.0387, | -0.0184, | -0.0093, | -0.0001, | 0.0206, | 0.0407, | 0.0914 |
| | 0.2086, | 0.2082, | 0.2110, | 0.2088, | 0.2095, | 0.2102, | 0.2158, | 0.2213, | 0.2214 |
| 14D D 1 222 | 0.1913 | 0.193 | 0.1936 | 0.1954 | 0.1972 | 0.1985 | 0.202 | 0.2035 | 0.1992 |
| MR-RAPS3 | 0.959, | 0.933, | 0.921, | 0.921, | 0.925, | 0.927, | 0.945, | 0.936, | 0.947, |
| | -2.1700, | -0.2074, | 0.1424, | 1.3643, | 0.6899, | 0.4231, | -0.0315, | 0.1685, | 0.3789 |
| | 46.0090, | 39.5875, | 7.9004, | 48.5633, | 30.4514, | 10.0749, | 10.7542, | 5.9607, | 3.6643 |
| MD D 4 700 f | 67.0966 | 69.0319 | 4.7066 | 443.2405 | 80.3419 | 6.9016 | 7.7096 | 2.5978 | 0.6306 |
| MR-RAPS4 | 1.000, | 0.957, | 0.720, | 0.309, | 0.276, | 0.321, | 0.671, | 0.940, | 1.000, |
| | -0.0757, | -0.0192, | 0.0050, | 0.0384, | 0.0538, | 0.0572, | 0.0539, | 0.0684, | 0.1080, |
| | 0.1110, | 0.1537, | 0.1726, | 0.2149, | 0.2296, | 0.2080, | 0.1540, | 0.1307, | 0.0930, |

Table S35: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE satisfied, q=0.6, and N=50000.

| ((| / / | | | | ′ 1 | | | | |
|--------------------|---------------------|---------------------|---------------------|---------------------|---------------------|--------------------|-------------------|--------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.438, | 0.100, | 0.044, | 0.013, | 0.012, | 0.014, | 0.026, | 0.078, | 0.364, |
| | -0.0821, | -0.0375, | -0.0219, | -0.0078, | -0.0006, | 0.0064, | 0.0206, | 0.0360, | 0.0806, |
| | 0.0416, | 0.0373, | 0.0348, | 0.0334, | 0.0335, | 0.0336, | 0.0352, | 0.0382, | 0.0440, |
| | 0.0468 | 0.0468 | 0.0469 | 0.0472 | 0.0473 | 0.0475 | 0.0482 | 0.0491 | 0.0511 |
| cML-MA-AIC-Profile | 0.433, | 0.098, | 0.043, | 0.013, | 0.012, | 0.012, | 0.025, | 0.077, | 0.361, |
| | -0.0820, | -0.0374, | -0.0219, | -0.0078, | -0.0005, | 0.0065, | 0.0207, | 0.0361, | 0.0809, |
| | 0.0417, | 0.0374, | 0.0351, | 0.0336, | 0.0337, | 0.0338, | 0.0354, | 0.0385, | 0.0446, |
| | 0.0472 | 0.0472 | 0.0473 | 0.0476 | 0.0477 | 0.048 | 0.0487 | 0.0495 | 0.0517 |
| cML-AIC | 0.621, | 0.229, | 0.119, | 0.056, | 0.039, | 0.042, | 0.098, | 0.202, | 0.553, |
| | -0.0881, | -0.0422, | -0.0251, | -0.0095, | -0.0010, | 0.0073, | 0.0233, | 0.0400, | 0.0867, |
| | 0.0479, | 0.0445, | 0.0427, | 0.0416, | 0.0419, | 0.0422, | 0.0435, | 0.0459, | 0.0499, |
| | 0.0401 | 0.0407 | 0.0409 | 0.0413 | 0.0415 | 0.0418 | 0.0423 | 0.0427 | 0.0439 |
| cML-AIC-Profile | 0.617, | 0.227, | 0.116, | 0.056, | 0.038, | 0.042, | 0.096, | 0.200, | 0.550, |
| | -0.0881, | -0.0422, | -0.0252, | -0.0095, | -0.0010, | 0.0073, | 0.0233, | 0.0400, | 0.0869, |
| | 0.0479, 0.0403 | 0.0445, 0.0409 | 0.0428, 0.0412 | 0.0416, 0.0416 | 0.0419, 0.0418 | 0.0422, 0.0421 | 0.0435, 0.0426 | 0.0459, 0.043 | 0.0502, 0.0442 |
| cML-MA-BIC | 0.0403 | 0.0409 | 0.0412 | 0.0410 | 0.0418 | 0.0421 | 0.0420 | 0.043 | 0.686, |
| CML-MA-DIC | -0.0979, | -0.0480, | -0.0297, | -0.0098, | 0.041, | 0.0100, | 0.0286, | 0.0497, | 0.0997, |
| | 0.0633, | 0.0638, | 0.0373, | 0.0375, | 0.0377, | 0.0379, | 0.0566, | 0.0390, | 0.0403, |
| | 0.0378 | 0.0385 | 0.0387 | 0.0391 | 0.0393 | 0.0395 | 0.0403 | 0.0403 | 0.0414 |
| cML-MA-BIC-Profile | 0.754, | 0.255, | 0.124, | 0.056, | 0.044, | 0.046, | 0.111, | 0.248, | 0.680, |
| cone mar bio riome | -0.0995, | -0.0488, | -0.0276, | -0.0060, | 0.0042, | 0.0143, | 0.0346, | 0.0549, | 0.1060, |
| | 0.1219, | 0.1231, | 0.1272, | 0.1212, | 0.1225, | 0.1232, | 0.1246, | 0.1260, | 0.1298, |
| | 0.0411 | 0.0416 | 0.0426 | 0.0429 | 0.043 | 0.0432 | 0.0435 | 0.044 | 0.0455 |
| cML-BIC | 0.774, | 0.258, | 0.126, | 0.058, | 0.044, | 0.049, | 0.120, | 0.262, | 0.696, |
| | -0.0985, | -0.0484, | -0.0300, | -0.0099, | 0.0001, | 0.0101, | 0.0286, | 0.0500, | 0.1002, |
| | 0.0642, | 0.0646, | 0.0377, | 0.0381, | 0.0382, | 0.0385, | 0.0644, | 0.0395, | 0.0406, |
| | 0.0372 | 0.0379 | 0.0382 | 0.0385 | 0.0387 | 0.0389 | 0.0393 | 0.0397 | 0.0409 |
| cML-BIC-Profile | 0.773, | 0.262, | 0.131, | 0.065, | 0.050, | 0.056, | 0.123, | 0.265, | 0.693, |
| | -0.0996, | -0.0482, | -0.0266, | -0.0052, | 0.0049, | 0.0149, | 0.0349, | 0.0548, | 0.1067, |
| | 0.1275, | 0.1351, | 0.1437, | 0.1371, | 0.1371, | 0.1372, | 0.1372, | 0.1374, | 0.1480, |
| | 0.0375 | 0.0381 | 0.0385 | 0.0388 | 0.039 | 0.0392 | 0.0396 | 0.04 | 0.0412 |
| MR-Mix | 0.707, | 0.218, | 0.099, | 0.043, | 0.035, | 0.039, | 0.087, | 0.218, | 0.625, |
| | -0.1028, | -0.0503, | -0.0300, | -0.0099, | -0.0001, | 0.0097, | 0.0289, | 0.0479, | 0.0936, |
| | 0.0389, | 0.0387, | 0.0384, | 0.0384, | 0.0385, | 0.0385, | 0.0384, | 0.0387, | 0.0391, |
| | 0.043 | 0.044 | 0.0424 | 0.0423 | 0.0423 | 0.0422 | 0.0422 | 0.0424 | 0.0429 |
| MR-ContMix | 0.786, | 0.291, | 0.152, | 0.069, | 0.060, | 0.072, | 0.148, | 0.278, | 0.713, |
| | -0.0998, | -0.0499, | -0.0298, | -0.0099, | 0.0001, | 0.0102, | 0.0299, | 0.0499, | 0.0996, |
| | 0.0382, | 0.0387, | 0.0389, | 0.0395, | 0.0397, | 0.0401, | 0.0403, | 0.0409, | 0.0423, |
|) ID I | NA 0.702 | NA 0.202 | NA 0.202 | NA 0.154 | NA | NA 0.151 | NA 0.200 | NA 0.206 | NA 0.621 |
| MR-Lasso | 0.703, | 0.302, | 0.203, | 0.154, | 0.146, | 0.151, | 0.200, | 0.296, | 0.631, |
| | -0.0857, | -0.0358, | -0.0166, | 0.0044, | 0.0146, | 0.0242, | 0.0450, | 0.0636, | 0.1136, |
| | 0.4348, 0.0723 | 0.4330, 0.0738 | 0.4338, | 0.4358, 0.0741 | 0.4363, 0.0743 | 0.4356, 0.0744 | 0.4353, 0.0749 | 0.4374, | 0.4372, 0.0768 |
| MR-PRESSO | 0.0723 | 0.0738 | 0.0744 | 0.0741 | 0.0743 | 0.0744 | 0.0749 | 0.0754 0.131, | 0.0768 |
| WIK-PKESSO | -0.0997, | -0.0508, | 0.115, -0.0310, | -0.0114, | -0.0018, | 0.091, | 0.103, | 0.131, 0.0473, | 0.220, |
| | 0.4016, | 0.4012, | 0.4008, | 0.4007, | 0.4005, | 0.4003, | 0.3999, | 0.3995, | 0.0907, |
| | 0.2312 | 0.2291 | 0.2277 | 0.2275 | 0.2262 | 0.4003, | 0.2245 | 0.2228 | 0.2216 |
| MR-IVW | 0.088, | 0.083, | 0.083, | 0.084, | 0.084, | 0.087, | 0.090, | 0.091, | 0.093, |
| 14114 1 4 44 | -0.1052, | -0.0548, | -0.0347, | -0.0145, | -0.0045, | 0.0056, | 0.0257, | 0.0459, | 0.0961, |
| | 0.4102, | 0.4102, | 0.4102, | 0.4101, | 0.4101, | 0.4101, | 0.4101, | 0.4101, | 0.4100, |
| | 0.4031 | 0.4031 | 0.4031 | 0.4031 | 0.4031 | 0.4031 | 0.4031 | 0.4031 | 0.4031 |
| MR-IVW-Oracle | 0.688, | 0.220, | 0.102, | 0.045, | 0.032, | 0.036, | 0.091, | 0.205, | 0.607, |
| | -0.0997, | -0.0498, | -0.0298, | -0.0099, | 0.0001, | 0.0101, | 0.0300, | 0.0500, | 0.0998, |
| | 0.0362, | 0.0369, | 0.0373, | 0.0376, | 0.0378, | 0.0380, | 0.0384, | 0.0389, | 0.0401, |
| | 0.0414 | 0.0422 | 0.0426 | 0.043 | 0.0432 | 0.0434 | 0.0438 | 0.0443 | 0.0455 |
| MR-Egger | 0.098, | 0.098, | 0.097, | 0.096, | 0.097, | 0.098, | 0.099, | 0.099, | 0.099, |
| 50 | -0.0259, | 0.0183, | 0.0359, | 0.0536, | 0.0624, | 0.0712, | 0.0888, | 0.1065, | 0.1505, |
| | 2.2979, | 2.2978, | 2.2978, | 2.2977, | 2.2977, | 2.2977, | 2.2977, | 2.2977, | 2.2977, |
| | 2.164 | 2.164 | 2.164 | 2.164 | 2.164 | 2.164 | 2.164 | 2.164 | 2.164 |
| MR-Weighted-Median | 0.575, | 0.191, | 0.093, | 0.055, | 0.049, | 0.051, | 0.089, | 0.168, | 0.493, |
| | -0.0933, | -0.0467, | -0.0281, | -0.0094, | -0.0001, | 0.0094, | 0.0278, | 0.0461, | 0.0919, |
| | 0.0590, | 0.0605, | 0.0619, | 0.0635, | 0.0645, | 0.0655, | 0.0681, | 0.0709, | 0.0792, |
| | 0.0462 | 0.047 | 0.0474 | 0.0478 | 0.0481 | 0.0483 | 0.0489 | 0.0494 | 0.0511 |
| MR-Weighted-Mode | 0.542, | 0.351, | 0.306, | 0.291, | 0.282, | 0.298, | 0.321, | 0.363, | 0.508, |
| | -0.0841, | -0.0419, | -0.0254, | -0.0083, | 0.0001, | 0.0088, | 0.0254, | 0.0422, | 0.0836, |
| | 0.1044, | 0.1062, | 0.1078, | 0.1087, | 0.1099, | 0.1106, | 0.1125, | 0.1142, | 0.1206, |
| MD D / PG1 | 0.0469 | 0.0477 | 0.0482 | 0.0487 | 0.049 | 0.0494 | 0.0501 | 0.0508 | 0.053 |
| MR-RAPS1 | 0.096, | 0.099, | 0.099, -0.0356, | 0.098, | 0.099, | 0.100, | 0.101, 0.0245, | 0.102, | 0.112, |
| | -0.1058, 0.4038, | -0.0557, 0.4038, | -0.0356, 0.4038, | -0.0156, 0.4038, | -0.0056, 0.4039, | 0.0044, 0.4039, | 0.0245, 0.4039, | 0.0445, 0.4039, | 0.0946, 0.4040, |
| | 0.4038, 0.3858 | 0.4038, 0.3859 | 0.4038, 0.3859 | 0.4038, 0.3859 | 0.4039, | 0.4039, 0.3859 | 0.4039, 0.3859 | 0.4039, | 0.4040, |
| MR-RAPS2 | 0.3838 | 0.3839 | 0.3839 | 0.3839 | 0.3839 | 0.3839 | 0.3839 | 0.386 | 0.386 |
| MIN-INAL 97 | -0.103, | -0.0558, | -0.0349, | -0.0165, | -0.0048, | 0.111, | 0.111, | 0.111, | 0.123, |
| | 0.4391, | 0.4367, | 0.4374, | 0.4373, | 0.4382, | 0.0033, | 0.0239, | 0.4368, | 0.0963, |
| | 0.4391, | 0.4307, | 0.4374, | 0.4373, | 0.4382, | 0.419 | 0.4399, | 0.4308, | 0.4409, |
| MR-RAPS3 | 0.4183 | 0.4189 | 0.866, | 0.4180 | 0.882, | 0.419 | 0.4169 | 0.4191 | 0.4183 |
| mic ich 33 | 63.3358, | -4.0102, | 4.2910, | 1.5637, | 0.8245, | -2.7847, | -4.4656, | 0.4654, | 0.3751, |
| | 2058.7795, | 151.7719, | 146.2623, | 43.2247, | 26.2799, | 109.0332, | 86.2928, | 12.9018, | 36.3773 |
| | 128300 | 794.4 | 1424 | 75.2 | 33.74 | 475.1 | 335.6 | 7.783 | 60.93 |
| MR-RAPS4 | 0.988, | 0.988, | 0.980, | 0.983, | 0.976, | 0.978, | 0.982, | 0.981, | 0.975, |
| | 0.3407, | 0.2469, | 0.2280, | 0.1159, | 0.0777, | 0.0733, | -0.0743, | -0.1083, | -0.4070 |
| | | | , | , | , | | | , | |
| | 1.5671, | 1.6003, | 1.6874, | 1.7280, | 1.8078, | 1.7938, | 1.7813, | 1.7991, | 1.8125, |

Table S36: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE satisfied, q=0.6, and N=100000.

| // | <i>'</i> | | | | ′ 1 | | | | |
|----------------------|----------|-----------|-----------|-----------|----------|----------------|----------------|----------------|---------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.725, | 0.197, | 0.062, | 0.011, | 0.012, | 0.020, | 0.070, | 0.187, | 0.677, |
| | -0.0854, | -0.0374, | -0.0208, | -0.0061, | 0.0007, | 0.0074, | 0.0216, | 0.0382, | 0.0860, |
| | 0.0307, | 0.0279, | 0.0256, | 0.0239, | 0.0244, | 0.0249, | 0.0276, | 0.0301, | 0.0333, |
| | 0.0333 | 0.0336 | 0.0336 | 0.0336 | 0.0341 | 0.0342 | 0.0347 | 0.0354 | 0.0366 |
| cML-MA-AIC-Profile | 0.723, | 0.197, | 0.062, | 0.010, | 0.011, | 0.020, | 0.070, | 0.187, | 0.676, |
| onie mirrino riome | -0.0857, | -0.0376, | -0.0209, | -0.0062, | 0.0009, | 0.0075, | 0.0217, | 0.0384, | 0.0863, |
| | 0.0317, | 0.0287, | 0.0263, | 0.0246, | 0.0247, | 0.0252, | 0.0280, | 0.0306, | 0.0340, |
| | 0.034 | 0.0343 | 0.0344 | 0.0343 | 0.0344 | 0.0345 | 0.0351 | 0.0358 | 0.0370, |
| cML-AIC | 0.825, | 0.372, | 0.165, | 0.060, | 0.0344 | 0.072, | 0.168, | 0.338, | 0.811, |
| CML-AIC | -0.0896, | -0.0409, | -0.0230, | -0.0071, | 0.040, | 0.072, | 0.108, | 0.0425, | 0.0912, |
| | 0.0345, | 0.0326, | 0.0230, | 0.0302, | 0.0012, | 0.0307, | 0.0244, | 0.0423, | 0.0372, |
| | 0.0343, | 0.0326, | 0.0313, | 0.0302, | 0.0303, | 0.0307, | 0.0330, | 0.0348, | 0.0372, |
| M. AIC D. Cl | | | | | | | | | |
| cML-AIC-Profile | 0.825, | 0.368, | 0.165, | 0.060, | 0.046, | 0.072, | 0.166, | 0.336, | 0.810, |
| | -0.0896, | -0.0409, | -0.0231, | -0.0071, | 0.0012, | 0.0090, | 0.0244, | 0.0425, | 0.0912, |
| | 0.0345, | 0.0326, | 0.0314, | 0.0302, | 0.0303, | 0.0307, | 0.0330, | 0.0349, | 0.0372 |
| | 0.0284 | 0.029 | 0.0293 | 0.0295 | 0.0296 | 0.0297 | 0.0299 | 0.0303 | 0.0312 |
| cML-MA-BIC | 0.959, | 0.468, | 0.191, | 0.064, | 0.048, | 0.073, | 0.197, | 0.415, | 0.936, |
| | -0.0994, | -0.0495, | -0.0296, | -0.0097, | -0.0013, | 0.0087, | 0.0285, | 0.0484, | 0.0984 |
| | 0.0263, | 0.0268, | 0.0270, | 0.0272, | 0.0535, | 0.0536, | 0.0538, | 0.0540, | 0.0546 |
| | 0.0266 | 0.027 | 0.0273 | 0.0276 | 0.0277 | 0.0278 | 0.0281 | 0.0284 | 0.0292 |
| ML-MA-BIC-Profile | 0.958, | 0.465, | 0.193, | 0.064, | 0.049, | 0.074, | 0.196, | 0.409, | 0.932, |
| | -0.1011, | -0.0494, | -0.0294, | -0.0094, | 0.0006, | 0.0106, | 0.0306, | 0.0507, | 0.1012, |
| | 0.1011, | 0.0861, | 0.0860, | 0.0860, | 0.0860, | 0.0861, | 0.0866, | 0.0873, | 0.0910 |
| | 0.0276 | 0.0279 | 0.0282 | 0.0285 | 0.0287 | 0.0288 | 0.0292 | 0.0296 | 0.0305 |
| cML-BIC | 0.960, | 0.477, | 0.199, | 0.068, | 0.049, | 0.076, | 0.202, | 0.427, | 0.939, |
| | -0.0997, | -0.0498, | -0.0298, | -0.0098, | -0.0013, | 0.0087, | 0.0286, | 0.0486, | 0.0986 |
| | 0.0263, | 0.0269, | 0.0271, | 0.0274, | 0.0537, | 0.0537, | 0.0539, | 0.0541, | 0.0546 |
| | 0.0263 | 0.0268 | 0.0271, | 0.0273 | 0.0274 | 0.0337, | 0.0278 | 0.0281 | 0.0289 |
| cML-BIC-Profile | 0.0203 | 0.0208 | 0.027 | 0.0273 | 0.0274 | 0.0273 | 0.0278 | 0.0281 | 0.0289 |
| CIVIL-DIC-PIOIIIE | -0.1008, | -0.0492, | -0.0292, | -0.0092, | 0.0008, | 0.077, 0.0108, | 0.203, 0.0308, | 0.423, 0.0507, | 0.938, |
| | | | | | | | | 0.0307, | |
| | 0.1006, | 0.0846, | 0.0848, | 0.0849, | 0.0850, | 0.0850, | 0.0852, | | 0.1028 |
| MD M | 0.0264 | 0.0269 | 0.0271 | 0.0274 | 0.0275 | 0.0276 | 0.0279 | 0.0282 | 0.029 |
| MR-Mix | 0.930, | 0.419, | 0.160, | 0.053, | 0.046, | 0.061, | 0.162, | 0.357, | 0.893, |
| | -0.1028, | -0.0502, | -0.0298, | -0.0097, | 0.0002, | 0.0099, | 0.0291, | 0.0480, | 0.0940 |
| | 0.0279, | 0.0279, | 0.0279, | 0.0279, | 0.0280, | 0.0280, | 0.0280, | 0.0281, | 0.0284 |
| | 0.0299 | 0.0297 | 0.0298 | 0.0298 | 0.0298 | 0.0299 | 0.03 | 0.0299 | 0.0301 |
| MR-ContMix | 0.958, | 0.525, | 0.236, | 0.094, | 0.069, | 0.094, | 0.249, | 0.467, | 0.939, |
| | -0.0992, | -0.0494, | -0.0296, | -0.0097, | 0.0004, | 0.0103, | 0.0302, | 0.0502, | 0.1001 |
| | 0.0270, | 0.0274, | 0.0279, | 0.0284, | 0.0285, | 0.0286, | 0.0290, | 0.0294, | 0.0303 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.901, | 0.465, | 0.253, | 0.159, | 0.141, | 0.161, | 0.263, | 0.423, | 0.880, |
| | -0.0983, | -0.0476, | -0.0279, | -0.0083, | 0.0021, | 0.0125, | 0.0323, | 0.0524, | 0.1026 |
| | 0.4216, | 0.4222, | 0.4218, | 0.4232, | 0.4220, | 0.4234, | 0.4241, | 0.4240, | 0.4253 |
| | 0.059 | 0.0593 | 0.0593 | 0.0594 | 0.0592 | 0.0596 | 0.0596 | 0.06 | 0.0605 |
| MR-PRESSO | 0.251, | 0.135, | 0.099, | 0.081, | 0.080, | 0.079, | 0.090, | 0.138, | 0.254, |
| WIK I KLOSO | -0.0992, | -0.0490, | -0.0288, | -0.0089, | 0.0010, | 0.0112, | 0.0310, | 0.0507, | 0.0992 |
| | 0.3925, | 0.3924, | 0.3923, | 0.3923, | 0.3923, | 0.3922, | 0.3922, | 0.3920, | 0.3916 |
| | 0.3923, | 0.3924, | 0.3923, | 0.3923, | 0.3923, | 0.3922, | 0.3922, | 0.3920, | 0.2662 |
| MD IVW | | | | | | | | | |
| MR-IVW | 0.087, | 0.080, | 0.079, | 0.077, | 0.077, | 0.077, | 0.075, | 0.080, | 0.089, |
| | -0.1006, | -0.0501, | -0.0299, | -0.0098, | 0.0003, | 0.0104, | 0.0305, | 0.0507, | 0.1010 |
| | 0.3958, | 0.3958, | 0.3958, | 0.3958, | 0.3958, | 0.3958, | 0.3958, | 0.3957, | 0.3957 |
| | 0.4046 | 0.4046 | 0.4046 | 0.4046 | 0.4046 | 0.4046 | 0.4046 | 0.4045 | 0.4045 |
| MR-IVW-Oracle | 0.919, | 0.406, | 0.162, | 0.055, | 0.039, | 0.057, | 0.166, | 0.361, | 0.885, |
| | -0.0995, | -0.0496, | -0.0297, | -0.0097, | 0.0003, | 0.0102, | 0.0302, | 0.0501, | 0.1000 |
| | 0.0262, | 0.0268, | 0.0270, | 0.0273, | 0.0274, | 0.0276, | 0.0279, | 0.0282, | 0.0291 |
| | 0.0292 | 0.0298 | 0.03 | 0.0303 | 0.0304 | 0.0306 | 0.0309 | 0.0312 | 0.032 |
| MR-Egger | 0.088, | 0.086, | 0.086, | 0.086, | 0.085, | 0.086, | 0.087, | 0.088, | 0.090, |
| 50 | -0.0091, | 0.0379, | 0.0567, | 0.0755, | 0.0849, | 0.0943, | 0.1130, | 0.1318, | 0.1787 |
| | 2.3970, | 2.3968, | 2.3967, | 2.3966, | 2.3966, | 2.3965, | 2.3964, | 2.3964, | 2.3962 |
| | 2.2796 | 2.2795 | 2.2794 | 2.2794 | 2.2794 | 2.2794 | 2.2793 | 2.2793 | 2.2793 |
| MR-Weighted-Median | 0.822, | 0.339, | 0.151, | 0.057, | 0.045, | 0.065, | 0.162, | 0.312, | 0.777, |
| | -0.0956, | -0.0476, | -0.0283, | -0.0091, | 0.0003, | 0.0100, | 0.0291, | 0.0483, | 0.0956 |
| | 0.0335, | 0.0343, | 0.0347, | 0.0352, | 0.0355, | 0.0359, | 0.0367, | 0.0377, | 0.0425 |
| | 0.0333, | 0.0332 | 0.0347, | 0.0332, | 0.0339 | 0.0339, | 0.0345 | 0.0349 | 0.0361 |
| MR-Weighted-Mode | 0.670, | 0.0552 | 0.0333 | 0.0558 | 0.0339 | 0.0341 | 0.0343 | 0.0349 | 0.673, |
| wix- weighted-iviode | | | | | | | | | |
| | -0.0826, | -0.0392, | -0.0225, | -0.0053, | 0.0033, | 0.0118, | 0.0290, | 0.0461, | 0.0884 |
| | 0.0899, | 0.0909, | 0.0921, | 0.0935, | 0.0944, | 0.0950, | 0.0968, | 0.0988, | 0.1051 |
| 14D D : DC : | 0.0335 | 0.0341 | 0.0344 | 0.0348 | 0.035 | 0.0352 | 0.0357 | 0.0362 | 0.0377 |
| MR-RAPS1 | 0.091, | 0.080, | 0.078, | 0.076, | 0.077, | 0.078, | 0.083, | 0.093, | 0.097, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1002 |
| | 0.3860, | 0.3860, | 0.3860, | 0.3861, | 0.3861, | 0.3861, | 0.3861, | 0.3862, | 0.3862 |
| | 0.3857 | 0.3857 | 0.3858 | 0.3858 | 0.3858 | 0.3858 | 0.3858 | 0.3858 | 0.3858 |
| MR-RAPS2 | 0.135, | 0.121, | 0.116, | 0.131, | 0.128, | 0.127, | 0.131, | 0.128, | 0.135, |
| | -0.1038, | -0.0380, | -0.0207, | -0.0120, | 0.0058, | 0.0138, | 0.0278, | 0.0490, | 0.0976 |
| | 0.5051, | 0.4751, | 0.4889, | 0.4854, | 0.4772, | 0.4746, | 0.4822, | 0.4713, | 0.4618 |
| | 0.4046 | 0.408 | 0.4078 | 0.4057 | 0.4081 | 0.4076 | 0.4094 | 0.4106 | 0.4109 |
| MR-RAPS3 | 0.923, | 0.907, | 0.908, | 0.905, | 0.902, | 0.903, | 0.910, | 0.906, | 0.916, |
| MIN-IVAL 93 | 0.923, | -6.2997, | 4.0412, | 1.2127, | -1.5129, | 0.903, | -1.9248, | -2.4762, | 0.916, |
| | | | 104.8374, | | | | | | |
| | 30.6220, | 193.5672, | | 130.9044, | 46.1664, | 41.6720, | 71.7011, | 61.1978, | 56.798 |
| | 30.4642 | 1076.2517 | 348.2075 | 593.1527 | 73.9518 | 51.7658 | 140.9863 | 144.338 | 162.87 |
| | | | 0.992, | 0.986, | 0.989, | 0.986, | 0.983, | 0.983, | 0.987, |
| MR-RAPS4 | 0.997, | 0.994, | | | | | | | |
| MR-RAPS4 | 0.6986, | 0.5614, | 0.4942, | 0.4093, | 0.3672, | 0.3656, | 0.1688, | 0.1251, | -0.0863 |
| MR-RAPS4 | | | | | | | | | |

Table S37: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE satisfied, q=0.6, and N=200000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|--------------------|---------------------|--------------------|-----------|-------------------|-------------------|-------------------|-------------------|-----------|---------|
| cML-MA-AIC | 0.949, | 0.434, | 0.156, | 0.025, | 0.019, | 0.024, | 0.137, | 0.366, | 0.904, |
| | -0.0915, | -0.0417, | -0.0233, | -0.0076, | -0.0007, | 0.0062, | 0.0216, | 0.0395, | 0.0882, |
| | 0.0225, | 0.0221, | 0.0203, | 0.0180, | 0.0177, | 0.0180, | 0.0203, | 0.0224, | 0.0249, |
| M M MG D G | 0.0235 | 0.0238 | 0.0238 | 0.0237 | 0.0238 | 0.0239 | 0.0246 | 0.0251 | 0.0259 |
| cML-MA-AIC-Profile | 0.949, | 0.433, | 0.155, | 0.025, | 0.018, | 0.024, | 0.136, | 0.366, | 0.904, |
| | -0.0916, | -0.0417, | -0.0233, | -0.0076, | -0.0007, | 0.0062, | 0.0216, | 0.0395, | 0.0882, |
| | 0.0226, | 0.0221, | 0.0203, | 0.0180, | 0.0177, | 0.0180, | 0.0203, | 0.0224, | 0.0249 |
| -MI AIC | 0.0235 | 0.0238 | 0.0239 | 0.0237 | 0.0238 | 0.024 | 0.0246 | 0.0251 | 0.0259 |
| cML-AIC | 0.960, | 0.617, | 0.306, | 0.083, | 0.057, | 0.076, | 0.266, | 0.539, | 0.924, |
| | -0.0942, | -0.0446, | -0.0256, | -0.0085, | -0.0008, | 0.0067, | 0.0238, | 0.0423, | 0.0912 |
| | 0.0254, | 0.0251, | 0.0239, | 0.0222, 0.0206 | 0.0220, | 0.0224, 0.021 | 0.0241, | 0.0256, | 0.0280 |
| M. AICD CI | 0.0201 | 0.0204 | 0.0206 | | 0.0208 | | 0.0212 | 0.0215 | 0.0221 |
| cML-AIC-Profile | 0.960, | 0.617, | 0.305, | 0.082, | 0.057, | 0.076, | 0.266, | 0.538, | 0.924, |
| | -0.0943, | -0.0446, | -0.0256, | -0.0085, | -0.0008, | 0.0067, | 0.0238, | 0.0423, | 0.0912 |
| | 0.0255, | 0.0251, | 0.0239, | 0.0222, | 0.0220, | 0.0224, | 0.0241, | 0.0256, | 0.0280 |
| cML-MA-BIC | 0.0201 | 0.0204 0.762, | 0.0206 | 0.0207 | 0.0209 | 0.021 | 0.0213 0.326, | 0.0215 | 0.0221 |
| CIVIL-IVIA-DIC | 0.999, | -0.0508, | 0.372, | 0.086, | 0.056, | 0.085, | 0.320, | 0.670, | 0.992, |
| | -0.1009, | | -0.0308, | -0.0108, | -0.0009, | 0.0091, | | 0.0490, | 0.0991 |
| | 0.0194, | 0.0197, | 0.0198, | 0.0199, 0.0194 | 0.0199, | 0.0200, 0.0196 | 0.0203, | 0.0205, | 0.0210 |
| W MA DIC D CI | 0.0188 | 0.0191 | 0.0193 | | 0.0195 | | 0.0198 | 0.02 | 0.0206 |
| ML-MA-BIC-Profile | 0.999, | 0.762, | 0.369, | 0.085, | 0.056, | 0.085, | 0.326, | 0.669, | 0.992, |
| | -0.1009, | -0.0508, | -0.0308, | -0.0108, | -0.0009, | 0.0091, | 0.0290, | 0.0490, | 0.0991 |
| | 0.0194, | 0.0197, | 0.0198, | 0.0199, 0.0195 | 0.0199, | 0.0200, | 0.0203, | 0.0205, | 0.0210 |
| »ML DIC | 0.0188 | 0.0191 | 0.0193 | | 0.0195 | 0.0196 | 0.0198 | 0.02 | 0.0206 |
| cML-BIC | 1.000, | 0.767, | 0.375, | 0.089, | 0.058, | 0.088, | 0.331, | 0.678, | 0.993, |
| | -0.1010, | -0.0509, | -0.0309, | -0.0109, | -0.0009, | 0.0091, | 0.0292, | 0.0492, | 0.0993 |
| | 0.0194, 0.0187 | 0.0196, 0.019 | 0.0198, | 0.0199, 0.0193 | 0.0200, 0.0194 | 0.0201, 0.0195 | 0.0203, 0.0197 | 0.0205, | 0.0210 |
| »ML DIC D CI | | | 0.0191 | | | | | 0.0199 | 0.0205 |
| cML-BIC-Profile | 1.000, | 0.767, | 0.374, | 0.088, | 0.058, | 0.088, | 0.331, | 0.677, | 0.993, |
| | -0.1010, | -0.0509, | -0.0309, | -0.0109, | -0.0009, | 0.0091, | 0.0292, | 0.0492, | 0.0993 |
| | 0.0194, | 0.0196, | 0.0198, | 0.0199, | 0.0200, | 0.0201, | 0.0203, | 0.0205, | 0.0210 |
| MD M | 0.0187 | 0.019 | 0.0192 | 0.0193 | 0.0194 | 0.0195 | 0.0197 | 0.0199 | 0.0205 |
| MR-Mix | 0.997, | 0.705, | 0.318, | 0.069, | 0.048, | 0.069, | 0.282, | 0.601, | 0.985, |
| | -0.1042, | -0.0516, | -0.0310, | -0.0108, | -0.0009, | 0.0089, | 0.0283, | 0.0472, | 0.0930 |
| | 0.0205, | 0.0206, | 0.0207, | 0.0207, | 0.0207, | 0.0208, | 0.0206, | 0.0205, | 0.0207 |
| | 0.0214 | 0.0212 | 0.0212 | 0.0212 | 0.0212 | 0.0212 | 0.0212 | 0.0213 | 0.0214 |
| MR-ContMix | 0.999, | 0.791, | 0.423, | 0.117, | 0.085, | 0.115, | 0.388, | 0.709, | 0.992, |
| | -0.1009, | -0.0509, | -0.0309, | -0.0109, | -0.0009, | 0.0091, | 0.0291, | 0.0491, | 0.0991 |
| | 0.0197, | 0.0200, | 0.0201, | 0.0203, | 0.0204, | 0.0205, | 0.0206, | 0.0209, | 0.0214 |
| 100 1 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.963, | 0.708, | 0.395, | 0.208, | 0.181, | 0.201, | 0.367, | 0.649, | 0.955, |
| | -0.0991, | -0.0476, | -0.0285, | -0.0080, | 0.0024, | 0.0131, | 0.0337, | 0.0539, | 0.1056 |
| | 0.4737, | 0.4753, | 0.4741, | 0.4744, | 0.4747, | 0.4752, | 0.4750, | 0.4753, | 0.4766 |
| | 0.0564 | 0.0561 | 0.0561 | 0.056 | 0.0563 | 0.0564 | 0.057 | 0.0571 | 0.058 |
| MR-PRESSO | 0.227, | 0.129, | 0.097, | 0.067, | 0.068, | 0.069, | 0.085, | 0.131, | 0.222, |
| | -0.1135, | -0.0627, | -0.0425, | -0.0226, | -0.0125, | -0.0025, | 0.0176, | 0.0377, | 0.0881 |
| | 0.4187, | 0.4185, | 0.4185, | 0.4184, | 0.4184, | 0.4184, | 0.4183, | 0.4183, | 0.4181 |
| | 0.3124 | 0.3112 | 0.3109 | 0.3106 | 0.3106 | 0.3103 | 0.3103 | 0.3103 | 0.3076 |
| MR-IVW | 0.089, | 0.088, | 0.089, | 0.095, | 0.100, | 0.099, | 0.096, | 0.097, | 0.105, |
| | -0.1143, | -0.0638, | -0.0436, | -0.0234, | -0.0133, | -0.0032, | 0.0170, | 0.0372, | 0.0876 |
| | 0.4198, | 0.4197, | 0.4196, | 0.4196, | 0.4196, | 0.4196, | 0.4195, | 0.4195, | 0.4194 |
| | 0.4009 | 0.4009 | 0.4009 | 0.4008 | 0.4008 | 0.4008 | 0.4008 | 0.4008 | 0.4008 |
| MR-IVW-Oracle | 0.996, | 0.688, | 0.306, | 0.073, | 0.045, | 0.068, | 0.267, | 0.607, | 0.986, |
| | -0.1008, | -0.0508, | -0.0308, | -0.0108, | -0.0008, | 0.0092, | 0.0292, | 0.0492, | 0.0992 |
| | 0.0193, | 0.0196, | 0.0198, | 0.0199, | 0.0200, | 0.0201, | 0.0203, | 0.0205, | 0.0210 |
| 100.5 | 0.0207 | 0.0211 | 0.0213 | 0.0215 | 0.0216 | 0.0217 | 0.0219 | 0.0222 | 0.0228 |
| MR-Egger | 0.079, | 0.079, | 0.079, | 0.079, | 0.079, | 0.080, | 0.080, | 0.080, | 0.081, |
| | -0.1149, | -0.0662, | -0.0468, | -0.0273, | -0.0176, | -0.0078, | 0.0116, | 0.0310, | 0.0796 |
| | 2.3920, | 2.3914, | 2.3912, | 2.3910, | 2.3908, | 2.3907, | 2.3905, | 2.3903, | 2.3898 |
| D W. L. 135 V | 2.295 | 2.295 | 2.295 | 2.295 | 2.295 | 2.295 | 2.295 | 2.295 | 2.295 |
| IR-Weighted-Median | 0.969, | 0.591, | 0.285, | 0.076, | 0.065, | 0.086, | 0.239, | 0.523, | 0.937, |
| | -0.0985, | -0.0499, | -0.0305, | -0.0112, | -0.0015, | 0.0082, | 0.0275, | 0.0469, | 0.0948 |
| | 0.0258, | 0.0265, | 0.0270, | 0.0278, | 0.0282, | 0.0287, | 0.0298, | 0.0312, | 0.0352 |
| (D. W.:.) - 125 -: | 0.0233 | 0.0236 | 0.0238 | 0.0241 | 0.0242 | 0.0243 | 0.0247 | 0.0251 | 0.0263 |
| MR-Weighted-Mode | 0.786, | 0.599, | 0.550, | 0.535, | 0.527, | 0.519, | 0.550, | 0.586, | 0.722, |
| | -0.0894, | -0.0465, | -0.0287, | -0.0119, | -0.0030, | 0.0057, | 0.0229, | 0.0404, | 0.0817 |
| | 0.0842, | 0.0856, | 0.0865, | 0.0878, | 0.0882, | 0.0891, | 0.0908, | 0.0926, | 0.0985 |
| MD D 4 DC1 | 0.0241 | 0.0246 | 0.0248 | 0.0251 | 0.0252 | 0.0254 | 0.0258 | 0.0261 | 0.0272 |
| MR-RAPS1 | 0.108, | 0.106, | 0.104, | 0.098, | 0.097, | 0.100, | 0.100, | 0.106, | 0.113, |
| | -0.1113, | -0.0612, | -0.0412, | -0.0212, | -0.0112, | -0.0012, | 0.0188, | 0.0388, | 0.0888 |
| | 0.4084, | 0.4084, | 0.4084, | 0.4084, | 0.4084, | 0.4084, | 0.4084, | 0.4084, | 0.4083 |
| MD D + DGC | 0.3813 | 0.3813 | 0.3814 | 0.3814 | 0.3814 | 0.3814 | 0.3814 | 0.3814 | 0.3814 |
| MR-RAPS2 | 0.275, | 0.245, | 0.237, | 0.244, | 0.224, | 0.236, | 0.228, | 0.224, | 0.228, |
| | -0.1105, | -0.0540, | -0.0308, | -0.0168, | 0.0039, | 0.0008, | 0.0170, | 0.0563, | 0.0987 |
| | 0.6861, | 0.6572, | 0.6357, | 0.6418, | 0.6283, | 0.6400, | 0.6296, | 0.6160, | 0.5859 |
| | 0.2873 | 0.2963 | 0.3002 | 0.3003 | 0.3083 | 0.3106 | 0.3108 | 0.3171 | 0.331 |
| MR-RAPS3 | 0.943, | 0.943, | 0.941, | 0.929, | 0.934, | 0.937, | 0.941, | 0.948, | 0.944, |
| | -1.4311, | -0.0468, | 27.5745, | -0.4064, | 3.4743, | -3.0060, | 3.5392, | 6.9374, | 4.2169 |
| | 34.1674, | 32.6704, | 921.1527, | 32.4517, | 138.5109, | 88.5082, | 70.1783, | 157.8841, | 73.4382 |
| | 27.9 | 22.82 | 16430 | 25.7 | 321.6 | 181.1 | 119.4 | 569.6 | 161.5 |
| MR-RAPS4 | 1.000, | 0.993, | 0.976, | 0.960, | 0.985, | 0.947, | 0.974, | 0.985, | 1.000, |
| | 0.1405 | 1 0 2222 | 0.3997, | 0.3748, | 0.5552, | 0.4655, | 0.4762, | 0.4427, | 0.2559 |
| | -0.1495, 0.4334, | 0.3332, 1.3073, | 1.3479, | 1.3709, | 1.8731, | 1.3436, | 1.3067, | 1.2900, | 0.2574 |

Table S38: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE violated, q=0.2, and N=50000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|--------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|-------------------|--------------------|--------------------|
| cML-MA-AIC | 0.712, | 0.189, | 0.055, | 0.012, | 0.009, | 0.018, | 0.058, | 0.150, | 0.644, |
| | -0.0846, | -0.0379, | -0.0214, | -0.0065, | 0.0005, | 0.0076, | 0.0220, | 0.0380, | 0.0839, |
| | 0.0303, 0.0339 | 0.0273, 0.0334 | 0.0254, | 0.0238, 0.0331 | 0.0236, 0.0332 | 0.0240, | 0.0256, | 0.0281, | 0.0325, 0.0374 |
| | 0.0339 | 0.0334 | 0.0331 | 0.0331 | 0.009, | 0.0334 | 0.0342 | 0.0352 0.149, | 0.640, |
| | -0.0848, | -0.0380, | -0.0214, | -0.0065, | 0.009, | 0.016, | 0.037, | 0.149, | 0.040, |
| | 0.0304, | 0.0274, | 0.0254, | 0.0238, | 0.0236, | 0.0240, | 0.0256, | 0.0281, | 0.0326, |
| | 0.0341 | 0.0336 | 0.0333 | 0.0333 | 0.0334 | 0.0336 | 0.0344 | 0.0354 | 0.0376 |
| cML-AIC | 0.873, | 0.396, | 0.191, | 0.063, | 0.059, | 0.066, | 0.163, | 0.349, | 0.830, |
| | -0.0926, | -0.0440, | -0.0258, | -0.0079, | 0.0004, | 0.0090, | 0.0256, | 0.0436, | 0.0917 |
| | 0.0337, | 0.0319, | 0.0309, | 0.0303, | 0.0301, | 0.0306, | 0.0315, | 0.0331, | 0.0363, |
| | 0.0277 | 0.0282 | 0.0284 | 0.0287 | 0.0289 | 0.029 | 0.0293 | 0.0296 | 0.0305 |
| cML-AIC-Profile | 0.872, | 0.393, | 0.188, | 0.063, | 0.057, | 0.065, | 0.159, | 0.342, | 0.829, |
| | -0.0928, | -0.0440, | -0.0258, | -0.0079, | 0.0004, | 0.0090, | 0.0256, | 0.0436, | 0.0918 |
| | 0.0338, | 0.0319, | 0.0309, | 0.0304, | 0.0301, | 0.0306, | 0.0315, | 0.0332, | 0.0363 |
| | 0.0278 | 0.0284 | 0.0286 | 0.0289 | 0.0291 | 0.0292 | 0.0295 | 0.0298 | 0.0307 |
| cML-MA-BIC | 0.974, | 0.499, | 0.185, | 0.046, | 0.036, | 0.052, | 0.176, | 0.439, | 0.957, |
| | -0.0998, | -0.0497, | -0.0297, | -0.0098, | 0.0002, | 0.0101, | 0.0301, | 0.0501, | 0.1002 |
| | 0.0244, | 0.0249, | 0.0250, | 0.0252, | 0.0253, | 0.0255, | 0.0258, | 0.0261, | 0.0271 |
| MI MA DIC D. GI. | 0.026 | 0.0264 | 0.0267 | 0.0269 | 0.027 | 0.0272 | 0.0275 | 0.0278 | 0.0286 |
| ML-MA-BIC-Profile | 0.974, | 0.491, | 0.182, | 0.045, | 0.034, | 0.050, | 0.175, | 0.432, | 0.956, |
| | -0.0998, | -0.0497, | -0.0297, | -0.0098, 0.0252, | 0.0002, | 0.0101, | 0.0301, | 0.0501, | 0.1002 |
| | 0.0244, 0.0261 | 0.0249, 0.0265 | 0.0250, 0.0268 | 0.0252, | 0.0253, 0.0271 | 0.0255, 0.0273 | 0.0258, 0.0276 | 0.0261, 0.0279 | 0.0271 0.0287 |
| cML-BIC | 0.0261 | 0.0203 | 0.0208 | 0.027 | 0.0271 | 0.0273 | 0.0276 | 0.0279 | 0.0287 |
| CIVIL-DIC | -0.1001, | -0.0499, | -0.0299, | -0.0099, | 0.0044, | 0.032, | 0.183, | 0.455, | 0.1003 |
| | 0.0246, | 0.0250, | 0.0253, | 0.0255, | 0.0002, | 0.0102, | 0.0302, | 0.0303, | 0.1003 |
| | 0.0246, | 0.0250, | 0.0263 | 0.0255, | 0.0250, | 0.0268 | 0.0200, | 0.0203, | 0.0272 |
| cML-BIC-Profile | 0.973, | 0.501, | 0.195, | 0.051, | 0.043, | 0.052, | 0.179, | 0.447, | 0.958, |
| Die Home | -0.1001, | -0.0499, | -0.0299, | -0.0099, | 0.0002, | 0.0102, | 0.0302, | 0.0503, | 0.1003 |
| | 0.0246, | 0.0250, | 0.0253, | 0.0255, | 0.0256, | 0.0257, | 0.0260, | 0.0263, | 0.0272 |
| | 0.0257 | 0.0262 | 0.0264 | 0.0267 | 0.0268 | 0.0269 | 0.0272 | 0.0275 | 0.0283 |
| MR-Mix | 0.877, | 0.300, | 0.101, | 0.034, | 0.024, | 0.032, | 0.093, | 0.270, | 0.818, |
| | -0.1053, | -0.0516, | -0.0306, | -0.0102, | 0.0000, | 0.0100, | 0.0298, | 0.0491, | 0.0958 |
| | 0.0295, | 0.0295, | 0.0294, | 0.0294, | 0.0294, | 0.0294, | 0.0293, | 0.0293, | 0.0295 |
| | 0.0356 | 0.0353 | 0.0353 | 0.0353 | 0.0353 | 0.0354 | 0.0354 | 0.0354 | 0.0358 |
| MR-ContMix | 0.955, | 0.485, | 0.191, | 0.051, | 0.042, | 0.061, | 0.188, | 0.436, | 0.941, |
| | -0.0993, | -0.0496, | -0.0298, | -0.0100, | -0.0001, | 0.0099, | 0.0298, | 0.0497, | 0.0995 |
| | 0.0258, | 0.0259, | 0.0261, | 0.0262, | 0.0263, | 0.0265, | 0.0269, | 0.0272, | 0.0280 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.951, | 0.447, | 0.169, | 0.039, | 0.035, | 0.048, | 0.154, | 0.409, | 0.934, |
| | -0.0994, | -0.0497, | -0.0299, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0501, | 0.0995 |
| | 0.0251, | 0.0254, | 0.0258, | 0.0260, | 0.0260, | 0.0260, | 0.0264, | 0.0268, | 0.0278 |
| | 0.0274 | 0.028 | 0.0282 | 0.0285 | 0.0286 | 0.0287 | 0.029 | 0.0293 | 0.0302 |
| MR-PRESSO | 0.576, | 0.293, | 0.182, | 0.132, | 0.126, | 0.132, | 0.202, | 0.311, | 0.592, |
| | -0.0696, | -0.0224, | -0.0037, | 0.0139, | 0.0239, | 0.0338, | 0.0529, | 0.0725, | 0.1192 |
| | 0.2056, | 0.2042, | 0.2038, | 0.2030, 0.0791 | 0.2029, | 0.2029, | 0.2010, | 0.1993, | 0.1960 |
| MR-IVW | 0.0827 0.098, | 0.0807 0.090, | 0.0803 | 0.0791 | 0.0791 | 0.0792 0.083, | 0.0775 0.089, | 0.0764 0.099, | 0.0744 |
| MK-IVW | -0.0820, | -0.0320, | 0.083, | 0.086, | 0.082, 0.0180, | 0.083, | 0.089, | | 0.132, |
| | 0.2459, | 0.2459, | -0.0120, 0.2459, | 0.0080, | 0.0180, | 0.0280, | 0.0480, | 0.0680, 0.2458, | 0.1179 |
| | 0.2323 | 0.2439, | 0.2323 | 0.2439, | 0.2439, | 0.2323 | 0.2438, | 0.2438, | 0.2323 |
| MR-IVW-Oracle | 0.954, | 0.439, | 0.165, | 0.035, | 0.032, | 0.042, | 0.145, | 0.403, | 0.938, |
| IT IT OTACIC | -0.0995, | -0.0497, | -0.0297, | -0.0098, | 0.002, | 0.0101, | 0.0301, | 0.403, | 0.0999, |
| | 0.0243, | 0.0247, | 0.0250, | 0.0252, | 0.0002, | 0.0255, | 0.0351, | 0.0261, | 0.0269 |
| | 0.0276 | 0.0282 | 0.0284 | 0.0287 | 0.0288 | 0.029 | 0.0293 | 0.0296 | 0.0304 |
| MR-Egger | 0.319, | 0.314, | 0.310, | 0.302, | 0.303, | 0.304, | 0.302, | 0.308, | 0.314, |
| 66. | 0.2228, | 0.2689, | 0.2873, | 0.3057, | 0.3149, | 0.3241, | 0.3425, | 0.3609, | 0.4068 |
| | 1.4474, | 1.4474, | 1.4474, | 1.4474, | 1.4474, | 1.4474, | 1.4474, | 1.4475, | 1.4476 |
| | 0.941 | 0.9411 | 0.9412 | 0.9413 | 0.9413 | 0.9413 | 0.9414 | 0.9415 | 0.9418 |
| IR-Weighted-Median | 0.842, | 0.304, | 0.110, | 0.039, | 0.027, | 0.029, | 0.092, | 0.233, | 0.754, |
| - | -0.0991, | -0.0504, | -0.0309, | -0.0115, | -0.0019, | 0.0078, | 0.0272, | 0.0467, | 0.0952 |
| | 0.0304, | 0.0307, | 0.0309, | 0.0312, | 0.0314, | 0.0315, | 0.0319, | 0.0324, | 0.0336 |
| | 0.0336 | 0.0342 | 0.0345 | 0.0348 | 0.035 | 0.0352 | 0.0355 | 0.036 | 0.0371 |
| MR-Weighted-Mode | 0.770, | 0.223, | 0.079, | 0.023, | 0.013, | 0.023, | 0.073, | 0.196, | 0.700, |
| | -0.0976, | -0.0486, | -0.0290, | -0.0094, | 0.0005, | 0.0110, | 0.0303, | 0.0500, | 0.0989 |
| | 0.0317, | 0.0324, | 0.0327, | 0.0331, | 0.0333, | 0.0363, | 0.0365, | 0.0367, | 0.0377 |
| 100 P : 20: | 0.0377 | 0.0384 | 0.0388 | 0.0391 | 0.0393 | 0.0395 | 0.04 | 0.0404 | 0.0416 |
| MR-RAPS1 | 0.122, | 0.098, | 0.095, | 0.095, | 0.102, | 0.101, | 0.105, | 0.126, | 0.159, |
| | -0.0833, | -0.0332, | -0.0132, | 0.0069, | 0.0169, | 0.0269, | 0.0469, | 0.0670, | 0.1170 |
| | 0.2428, 0.2224 | 0.2428, | 0.2428, | 0.2428, | 0.2428, 0.2225 | 0.2428, | 0.2429, | 0.2429, | 0.2429 |
| MD DADGO | | 0.2225 | 0.2225 | 0.2225 | | 0.2226 | 0.2226 | 0.2226 | 0.2227 |
| MR-RAPS2 | 0.927, | 0.769, | 0.661, | 0.618, | 0.612, | 0.613, | 0.676, | 0.776, | 0.915, |
| | -0.0474, 5.0000 | 0.0560, | 0.3383, | 0.0578, | 0.3082, | 0.2456, | 0.1217, | 0.3031, | 0.1242 |
| | 5.9000, | 7.7647, | 6.2639, | 3.0608, | 4.9676, | 4.0430, | 5.2827, | 4.8627, | 4.7136 |
| MD DADG2 | 0.2051 | 0.2415 | 0.1445 | 0.0725 | 0.0968 | 0.0937 | 0.0964 | 0.1029 | 0.484 |
| MR-RAPS3 | 0.883, | 0.866, -0.0560, | 0.865, | 0.856, | 0.852, | 0.853, | 0.848, 0.0592, | 0.835, | 0.878, |
| | -0.1674, 2.0258, | -0.0560, 0.8177, | -0.0563, 1.2277, | 0.0360, 1.2228, | 0.0318, 0.7947, | 0.0392, 0.6982, | 0.0592, 0.6803, | 0.0688, 0.9214, | 1.2930, 32.7490 |
| | 2.0258, 0.825 | 0.8177, 0.1021 | 0.174 | 0.1773 | 0.7947, 0.0931 | 0.6982, | 0.6803, | 0.9214, 0.1387 | 32.7490 |
| MR-RAPS4 | | | | | | | | | |
| WIK-KAP34 | 0.994, -0.2322, | 0.903, -0.0262, | 0.827, 0.0720, | 0.795, 0.0055, | 0.773, -0.0142, | 0.768, 0.0085, | 0.809, 0.0703, | 0.896, 0.1224, | 0.988, 0.3060, |
| | | 5.7965, | 4.9655, | 1.7865, | 2.3852, | 2.1923, | 2.1411, | 2.0957, | 2.9404 |
| | 5.2930, | | | | | | | | |

Table S39: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m = 10, the InSIDE violated, q = 0.2, and N = 100000.

| <i>'</i> ' ' | · / | | | | | | | | |
|------------------------|---------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.917, | 0.379, | 0.121, | 0.021, | 0.017, | 0.032, | 0.121, | 0.351, | 0.877, |
| CIVIL-IVIA-AIC | -0.0878, | -0.0393, | -0.0217, | -0.0065, | 0.017, | 0.0076, | 0.121, | 0.0395, | 0.0872, |
| | 0.0229, | 0.0213, | 0.0193, | 0.0177, | 0.0006, | 0.0076, | 0.0223, | 0.0228, | 0.0372, |
| | 0.0245 | 0.0243 | 0.024 | 0.0237 | 0.0237 | 0.0239 | 0.0247 | 0.0255 | 0.0269 |
| cML-MA-AIC-Profile | 0.917, | 0.374, | 0.120, | 0.020, | 0.017, | 0.032, | 0.117, | 0.351, | 0.877, |
| | -0.0879, | -0.0393, | -0.0217, | -0.0065, | 0.0006, | 0.0076, | 0.0223, | 0.0395, | 0.0873, |
| | 0.0230, | 0.0213, | 0.0193, | 0.0177, | 0.0176, | 0.0178, | 0.0202, | 0.0228, | 0.0254, |
| | 0.0245 | 0.0244 | 0.0241 | 0.0238 | 0.0238 | 0.024 | 0.0248 | 0.0255 | 0.027 |
| cML-AIC | 0.965, | 0.600, | 0.297, | 0.087, | 0.075, | 0.099, | 0.284, | 0.589, | 0.947, |
| | -0.0934, 0.0253, | -0.0441, 0.0246, | -0.0252, | -0.0077, 0.0225, | 0.0007, 0.0226, | 0.0088, 0.0228, | 0.0256, | 0.0444, | 0.0935, |
| | 0.0233, | 0.0246, | 0.0237, 0.0202 | 0.0223, | 0.0226, | 0.0228, | 0.0248, 0.0207 | 0.0262, 0.021 | 0.0279, 0.0216 |
| cML-AIC-Profile | 0.964, | 0.602, | 0.296, | 0.086, | 0.074, | 0.099, | 0.283, | 0.587, | 0.947, |
| | -0.0936, | -0.0442, | -0.0252, | -0.0077, | 0.0007, | 0.0088, | 0.0256, | 0.0444, | 0.0935, |
| | 0.0253, | 0.0247, | 0.0237, | 0.0225, | 0.0226, | 0.0228, | 0.0248, | 0.0262, | 0.0279, |
| | 0.0197 | 0.02 | 0.0202 | 0.0204 | 0.0205 | 0.0206 | 0.0208 | 0.021 | 0.0217 |
| cML-MA-BIC | 0.999, | 0.776, | 0.369, | 0.085, | 0.045, | 0.068, | 0.323, | 0.734, | 0.998, |
| | -0.1000, | -0.0500, | -0.0301, | -0.0101, | -0.0002, | 0.0098, | 0.0297, | 0.0497, | 0.0996, |
| | 0.0181, | 0.0185, | 0.0186, | 0.0188, | 0.0189, | 0.0190, | 0.0192, | 0.0195, | 0.0201, |
| cML-MA-BIC-Profile | 0.0182 0.999, | 0.0186 0.776, | 0.0187 0.368, | 0.0189 0.085, | 0.019 0.045, | 0.0191 0.068, | 0.0193 0.323, | 0.0195 0.734, | 0.0201 |
| CIVIL-IVIA-DIC-PTOILLE | -0.1000, | -0.0500, | -0.0301, | -0.0101, | -0.0002, | 0.008, | 0.323, 0.0297, | 0.734, 0.0497, | 0.998, |
| | 0.0181, | 0.0185, | 0.0186, | 0.0188, | 0.0189, | 0.0190, | 0.0192, | 0.0195, | 0.0201, |
| | 0.0183 | 0.0186 | 0.0188 | 0.019 | 0.019 | 0.0191 | 0.0193 | 0.0195 | 0.0201 |
| cML-BIC | 0.999, | 0.783, | 0.375, | 0.090, | 0.047, | 0.072, | 0.329, | 0.736, | 0.998, |
| | -0.1001, | -0.0501, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0181, | 0.0185, | 0.0186, | 0.0188, | 0.0189, | 0.0190, | 0.0192, | 0.0194, | 0.0201, |
| M DIC 2 2 | 0.018 | 0.0184 | 0.0185 | 0.0187 | 0.0188 | 0.0189 | 0.0191 | 0.0193 | 0.0199 |
| cML-BIC-Profile | 0.999, | 0.783, -0.0501, | 0.375, | 0.090, | 0.047, | 0.072, | 0.329, | 0.736, | 0.998, |
| | -0.1001, 0.0181, | -0.0501, 0.0185, | -0.0302, 0.0186, | -0.0102, 0.0188, | -0.0002, 0.0189, | 0.0098, 0.0190, | 0.0298, 0.0192, | 0.0498, 0.0194, | 0.0998, 0.0201, |
| | 0.0181 | 0.0184 | 0.0186 | 0.0187 | 0.0188 | 0.0189 | 0.0191 | 0.0193 | 0.0199 |
| MR-Mix | 0.986, | 0.577, | 0.209, | 0.042, | 0.020, | 0.031, | 0.182, | 0.492, | 0.960, |
| | -0.1057, | -0.0520, | -0.0312, | -0.0106, | -0.0006, | 0.0095, | 0.0291, | 0.0483, | 0.0948, |
| | 0.0212, | 0.0212, | 0.0211, | 0.0213, | 0.0213, | 0.0213, | 0.0212, | 0.0212, | 0.0214, |
| 1000 10 | 0.0254 | 0.0253 | 0.0253 | 0.0252 | 0.0252 | 0.0252 | 0.0253 | 0.0253 | 0.0254 |
| MR-ContMix | 0.998, | 0.781, | 0.388, | 0.100, -0.0100, | 0.066, | 0.090, 0.0099, | 0.356, | 0.729, | 0.993, |
| | -0.0998, 0.0193, | -0.0500, 0.0196, | -0.0300, 0.0197, | 0.0199, | -0.0001, 0.0200, | 0.0099, | 0.0298, 0.0204, | 0.0497, 0.0206, | 0.0996, 0.0212, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.997, | 0.727, | 0.324, | 0.075, | 0.047, | 0.062, | 0.297, | 0.682, | 0.992, |
| | -0.0999, | -0.0500, | -0.0302, | -0.0102, | -0.0002, | 0.0097, | 0.0297, | 0.0497, | 0.0995, |
| | 0.0186, | 0.0191, | 0.0191, | 0.0193, | 0.0194, | 0.0196, | 0.0199, | 0.0200, | 0.0208, |
| MD DDEGGO | 0.0194 | 0.0198 | 0.02 | 0.0202 | 0.0203 | 0.0204 | 0.0206 | 0.0208 | 0.0214 |
| MR-PRESSO | 0.476, -0.0771, | 0.310, -0.0285, | 0.193, -0.0090, | 0.112, 0.0108, | 0.114, 0.0206, | 0.120, 0.0306, | 0.215, 0.0501, | 0.348, 0.0696, | 0.519, 0.1180, |
| | 0.2305, | 0.2295, | 0.2291, | 0.0108, | 0.0200, | 0.0300, | 0.0301, | 0.0090, | 0.1180, |
| | 0.118 | 0.1157 | 0.1142 | 0.1142 | 0.1139 | 0.1139 | 0.1129 | 0.1124 | 0.1107 |
| MR-IVW | 0.098, | 0.074, | 0.066, | 0.066, | 0.061, | 0.060, | 0.066, | 0.085, | 0.123, |
| | -0.0766, | -0.0266, | -0.0066, | 0.0134, | 0.0234, | 0.0334, | 0.0534, | 0.0734, | 0.1233, |
| | 0.2444, | 0.2445, | 0.2445, | 0.2445, | 0.2445, | 0.2445, | 0.2445, | 0.2445, | 0.2446, |
| 100 WW. 0 1 | 0.2346 | 0.2346 | 0.2346 | 0.2346 | 0.2346 | 0.2346 | 0.2346 | 0.2346 | 0.2346 |
| MR-IVW-Oracle | 0.997, -0.0999, | 0.728, -0.0501, | 0.315, -0.0302, | 0.068, -0.0102, | 0.038, -0.0003, | 0.053, 0.0097, | 0.288, 0.0297, | 0.679, 0.0496, | 0.995, 0.0994, |
| | 0.0179, | 0.0183, | 0.0302, | 0.0102, | 0.0187, | 0.0097, | 0.0297, | 0.0193, | 0.0199, |
| | 0.0196 | 0.02 | 0.0201 | 0.0203 | 0.0204 | 0.0205 | 0.0207 | 0.0209 | 0.0215 |
| MR-Egger | 0.330, | 0.337, | 0.336, | 0.336, | 0.336, | 0.336, | 0.337, | 0.338, | 0.336, |
| | 0.3324, | 0.3804, | 0.3995, | 0.4187, | 0.4283, | 0.4379, | 0.4570, | 0.4762, | 0.5241, |
| | 1.4737, | 1.4737, | 1.4736, | 1.4736, | 1.4736, | 1.4735, | 1.4735, | 1.4735, | 1.4734, |
| MD Well-le 134 P | 0.9709 | 0.971 | 0.971 | 0.9711 | 0.9711 | 0.9711 | 0.9712 | 0.9712 | 0.9714 |
| MR-Weighted-Median | 0.985, -0.0992, | 0.559, -0.0501, | 0.241, -0.0305, | 0.059, -0.0109, | 0.043, -0.0010, | 0.060, 0.0088, | 0.202, 0.0285, | 0.496, 0.0481, | 0.960, 0.0971, |
| | 0.0230, | 0.0235, | 0.0237, | 0.0239, | 0.0240, | 0.0088, | 0.0283, | 0.0481, | 0.0971, 0.0257, |
| | 0.0237 | 0.0241 | 0.0243 | 0.0245 | 0.0247 | 0.0248 | 0.025 | 0.0253 | 0.0261 |
| MR-Weighted-Mode | 0.963, | 0.459, | 0.172, | 0.033, | 0.027, | 0.037, | 0.155, | 0.418, | 0.920, |
| - | -0.0991, | -0.0498, | -0.0301, | -0.0103, | -0.0004, | 0.0096, | 0.0296, | 0.0493, | 0.0986, |
| | 0.0247, | 0.0247, | 0.0249, | 0.0251, | 0.0253, | 0.0253, | 0.0257, | 0.0260, | 0.0270, |
| 1 m n i nai | 0.0272 | 0.0276 | 0.0278 | 0.0281 | 0.0282 | 0.0283 | 0.0286 | 0.0289 | 0.0298 |
| MR-RAPS1 | 0.111, | 0.095, -0.0311, | 0.088, | 0.080, 0.0089, | 0.080, | 0.080, | 0.090, 0.0489, | 0.098, | 0.144, |
| | -0.0810, 0.2376, | 0.2377, | -0.0111, 0.2377, | 0.0089, | 0.0189, 0.2378, | 0.0289, 0.2378, | 0.0489, 0.2378, | 0.0689, 0.2379, | 0.1189, 0.2380, |
| | 0.2231 | 0.2231 | 0.2231 | 0.2232 | 0.2232 | 0.2232 | 0.2232 | 0.2232 | 0.2232 |
| MR-RAPS2 | 0.933, | 0.774, | 0.438, | 0.179, | 0.140, | 0.173, | 0.431, | 0.746, | 0.937, |
| | 0.0234, | 0.1909, | 0.2053, | 0.3617, | 0.3763, | 0.6863, | 0.4991, | 0.5010, | 0.4110, |
| | 5.5185, | 2.7853, | 2.5708, | 3.6355, | 8.3796, | 3.6344, | 3.2395, | 3.6159, | 3.9224, |
| 14D D : 200 | 0.0626 | 0.0453 | 0.0425 | 0.0503 | 0.0575 | 0.0574 | 0.0608 | 0.0629 | 0.08 |
| MR-RAPS3 | 0.900, | 0.907, 0.0097, | 0.905, | 0.907, 0.0090, | 0.907, 0.0602, | 0.903, 0.0591, | 0.911, 0.1050, | 0.902, | 0.911, |
| | -0.1626, 1.3875, | 1.1390, | 0.0080, 0.7449, | 1.0339, | 0.0602, 0.7714, | 0.0591, | 0.1050, | 0.1287, 0.5444, | 0.2049, 0.4986, |
| | 0.2522 | 0.1243 | 0.0664 | 0.1888 | 0.7714, | 0.7535, | 0.0552 | 0.046 | 0.4980, |
| | | | | | | | | 0.787, | 1.000, |
| MR-RAPS4 | 0.999, | 0.823, | 0.449, | 0.130, | 0.084, | 0.127, | 0.418, | 0.767, | 1.000, |
| MR-RAPS4 | 0.999, -0.1000, | -0.0501, | -0.0313, | -0.0141, | -0.0034, | 0.0068, | 0.0257, | 0.0493, | 0.1702, |
| MR-RAPS4 | 0.999, | | | | | | | | |

Table S40: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE violated, q=0.2, and N=200000.

| // | <i>'</i> | | | | , I | | | | |
|--------------------|---------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.999, | 0.675, | 0.282, | 0.037, | 0.013, | 0.036, | 0.244, | 0.618, | 0.981, |
| | -0.0919, | -0.0421, | -0.0233, | -0.0073, | -0.0004, | 0.0066, | 0.0226, | 0.0411, | 0.0902, |
| | 0.0163, | 0.0163, | 0.0150, | 0.0129, | 0.0124, | 0.0129, | 0.0154, | 0.0171, | 0.0184, |
| | 0.0174 | 0.0176 | 0.0172 | 0.0168 | 0.0167 | 0.017 | 0.0177 | 0.0184 | 0.0192 |
| cML-MA-AIC-Profile | 0.999, | 0.674, | 0.282, | 0.037, | 0.013, | 0.037, | 0.242, | 0.617, | 0.981, |
| | -0.0920, | -0.0421, | -0.0233, | -0.0073, | -0.0004, | 0.0066, | 0.0226, | 0.0411, | 0.0903, |
| | 0.0163, 0.0175 | 0.0163, 0.0176 | 0.0150, 0.0173 | 0.0129, 0.0168 | 0.0124, 0.0168 | 0.0130, 0.017 | 0.0154, 0.0177 | 0.0171, 0.0184 | 0.0184, 0.0192 |
| cML-AIC | 0.999, | 0.848, | 0.503, | 0.0108 | 0.073, | 0.124, | 0.453, | 0.810, | 0.0192 |
| CML-AIC | -0.0964, | -0.0463, | -0.0267, | -0.0086, | -0.0005, | 0.0076, | 0.0255, | 0.0451, | 0.0948, |
| | 0.0179, | 0.0181, | 0.0175, | 0.0164, | 0.0159, | 0.0165, | 0.0179, | 0.0193, | 0.0202, |
| | 0.0139 | 0.0142 | 0.0143 | 0.0144 | 0.0145 | 0.0145 | 0.0147 | 0.0149 | 0.0153 |
| cML-AIC-Profile | 0.999, | 0.847, | 0.503, | 0.127, | 0.073, | 0.124, | 0.453, | 0.806, | 0.989, |
| | -0.0965, | -0.0464, | -0.0267, | -0.0086, | -0.0005, | 0.0076, | 0.0255, | 0.0451, | 0.0949, |
| | 0.0180, | 0.0181, | 0.0175, | 0.0164, | 0.0159, | 0.0165, | 0.0179, | 0.0193, | 0.0202, |
| | 0.0139 | 0.0142 | 0.0143 | 0.0144 | 0.0145 | 0.0146 | 0.0147 | 0.0149 | 0.0154 |
| cML-MA-BIC | 1.000, | 0.956, | 0.637, | 0.122, | 0.053, | 0.119, | 0.593, | 0.945, | 1.000, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0097, | 0.0297, | 0.0497, | 0.0997, |
| | 0.0130, 0.0129 | 0.0132, 0.0131 | 0.0133, 0.0132 | 0.0134, 0.0134 | 0.0135, 0.0134 | 0.0136, 0.0135 | 0.0138, 0.0136 | 0.0139, 0.0138 | 0.0144, 0.0142 |
| cML-MA-BIC-Profile | 1.000, | 0.0131 | 0.638, | 0.0134 | 0.0134 | 0.0133 | 0.590, | 0.0138 | 1.000, |
| CML-MA-DIC-FIGHE | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0097, | 0.0297, | 0.0497, | 0.0997, |
| | 0.0130, | 0.0132, | 0.0133, | 0.0134, | 0.0135, | 0.0136, | 0.0138, | 0.0139, | 0.0144, |
| | 0.0129 | 0.0131 | 0.0133 | 0.0134 | 0.0135 | 0.0135 | 0.0136, | 0.0138 | 0.0144, |
| cML-BIC | 1.000, | 0.960, | 0.644, | 0.123, | 0.057, | 0.122, | 0.600, | 0.946, | 1.000, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0130, | 0.0132, | 0.0133, | 0.0135, | 0.0135, | 0.0136, | 0.0138, | 0.0139, | 0.0144, |
| | 0.0128 | 0.013 | 0.0132 | 0.0133 | 0.0133 | 0.0134 | 0.0135 | 0.0137 | 0.0141 |
| cML-BIC-Profile | 1.000, | 0.960, | 0.644, | 0.122, | 0.057, | 0.122, | 0.600, | 0.945, | 1.000, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0130, 0.0128 | 0.0132, 0.0131 | 0.0133, 0.0132 | 0.0135, 0.0133 | 0.0135, 0.0133 | 0.0136, 0.0134 | 0.0138, 0.0136 | 0.0139, 0.0137 | 0.0144, 0.0141 |
| MR-Mix | 0.0128 | 0.0131 | 0.0132 | 0.0133 | 0.0133 | 0.0134 | 0.0136 | 0.0137 | 0.998, |
| IVIIX-IVIIX | -0.1052, | -0.0516, | -0.0307, | -0.0102, | -0.0001, | 0.071, | 0.0297, | 0.791, | 0.998, |
| | 0.0152, | 0.0151, | 0.0151, | 0.0151, | 0.0151, | 0.0151, | 0.0152, | 0.0152, | 0.0154, |
| | 0.0183 | 0.0183 | 0.0183 | 0.0182 | 0.0182 | 0.0183 | 0.0183 | 0.0183 | 0.0183 |
| MR-ContMix | 1.000, | 0.957, | 0.665, | 0.153, | 0.071, | 0.144, | 0.615, | 0.944, | 1.000, |
| | -0.1001, | -0.0501, | -0.0302, | -0.0102, | -0.0002, | 0.0097, | 0.0297, | 0.0497, | 0.0996, |
| | 0.0133, | 0.0135, | 0.0136, | 0.0137, | 0.0138, | 0.0139, | 0.0140, | 0.0142, | 0.0147, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.935, | 0.580, | 0.109, | 0.056, | 0.102, | 0.539, | 0.919, | 1.000, |
| | -0.1001, 0.0132, | -0.0501, 0.0134, | -0.0301, 0.0135, | -0.0102, 0.0136, | -0.0002, 0.0138, | 0.0098, 0.0138, | 0.0297, 0.0140, | 0.0497, 0.0141, | 0.0997, 0.0146, |
| | 0.0132, | 0.0134, | 0.0133, | 0.0130, | 0.0138, | 0.0138, | 0.0146 | 0.0141, | 0.0140, |
| MR-PRESSO | 0.402, | 0.309, | 0.209, | 0.100, | 0.089, | 0.097, | 0.207, | 0.328, | 0.436, |
| | -0.0816, | -0.0320, | -0.0122, | 0.0078, | 0.0178, | 0.0278, | 0.0478, | 0.0679, | 0.1175, |
| | 0.2386, | 0.2384, | 0.2384, | 0.2383, | 0.2382, | 0.2382, | 0.2382, | 0.2376, | 0.2371, |
| | 0.1461 | 0.1447 | 0.1448 | 0.1448 | 0.1442 | 0.1442 | 0.1439 | 0.1416 | 0.1396 |
| MR-IVW | 0.099, | 0.084, | 0.074, | 0.071, | 0.071, | 0.075, | 0.083, | 0.087, | 0.125, |
| | -0.0822, | -0.0321, | -0.0120, | 0.0080, | 0.0181, | 0.0281, | 0.0481, | 0.0682, | 0.1183, |
| | 0.2431, | 0.2431, | 0.2431, | 0.2431, | 0.2431, | 0.2431, | 0.2431, | 0.2430, | 0.2430, |
| MD IVW Ol. | 0.2356 | 0.2356 | 0.2356 | 0.2356 0.105, | 0.2356 | 0.2356 | 0.2355 | 0.2355 | 0.2355 |
| MR-IVW-Oracle | 1.000, -0.1001, | 0.936, -0.0501, | 0.579, -0.0301, | -0.0102, | 0.049, -0.0002, | 0.097, 0.0098, | 0.537, 0.0298, | 0.921, 0.0498, | 1.000, 0.0997, |
| | 0.0129, | 0.0131, | 0.0133, | 0.0134, | 0.0135, | 0.0135, | 0.0230, | 0.0138, | 0.0143, |
| | 0.0129, | 0.0141 | 0.0143 | 0.0144 | 0.0145 | 0.0145 | 0.0137, | 0.0148 | 0.0152 |
| MR-Egger | 0.341, | 0.347, | 0.347, | 0.345, | 0.345, | 0.347, | 0.348, | 0.348, | 0.353, |
| 66 | 0.3442, | 0.3933, | 0.4129, | 0.4326, | 0.4424, | 0.4522, | 0.4718, | 0.4914, | 0.5405, |
| | 1.5425, | 1.5424, | 1.5424, | 1.5423, | 1.5423, | 1.5423, | 1.5423, | 1.5422, | 1.5422, |
| | 0.9761 | 0.9761 | 0.9761 | 0.9761 | 0.9761 | 0.9761 | 0.9761 | 0.9761 | 0.9762 |
| MR-Weighted-Median | 1.000, | 0.848, | 0.440, | 0.081, | 0.041, | 0.075, | 0.376, | 0.768, | 1.000, |
| | -0.1003, | -0.0506, | -0.0308, | -0.0110, | -0.0011, | 0.0088, | 0.0285, | 0.0483, | 0.0977, |
| | 0.0161, 0.0168 | 0.0165, | 0.0167, | 0.0169, | 0.0169, | 0.0170, | 0.0173, | 0.0175, | 0.0180, |
| MR-Weighted-Mode | 0.0168 | 0.0171 0.747, | 0.0173 0.341, | 0.0174 0.049, | 0.0175 0.026, | 0.0176 0.052, | 0.0178 0.312, | 0.018 0.687, | 0.0185 0.995, |
| wix-weighten-Mone | -0.1003, | -0.0503, | -0.0302, | -0.0103, | -0.0004, | 0.032, | 0.312, 0.0295, | 0.087, | 0.995, |
| | 0.0194, | 0.0197, | 0.0200, | 0.0201, | 0.0203, | 0.0090, | 0.0293, | 0.0498, | 0.0300, |
| | 0.0194 | 0.0198 | 0.0199 | 0.0201 | 0.0202 | 0.0203 | 0.0205 | 0.0207 | 0.0213 |
| MR-RAPS1 | 0.109, | 0.098, | 0.101, | 0.097, | 0.093, | 0.090, | 0.099, | 0.106, | 0.133, |
| | -0.0823, | -0.0323, | -0.0123, | 0.0078, | 0.0178, | 0.0278, | 0.0478, | 0.0678, | 0.1178, |
| | 0.2365, | 0.2365, | 0.2365, | 0.2365, | 0.2365, | 0.2365, | 0.2366, | 0.2366, | 0.2366, |
| | 0.2234 | 0.2235 | 0.2235 | 0.2235 | 0.2235 | 0.2235 | 0.2235 | 0.2235 | 0.2235 |
| MR-RAPS2 | 0.945, | 0.906, | 0.691, | 0.311, | 0.229, | 0.262, | 0.661, | 0.882, | 0.942, |
| | 0.3227, | -0.1949, | 0.4203, | -0.1507, | 0.4714, | 0.2704, | 0.0532, | 0.2976, | 0.5987, |
| | 4.0103, | 11.4382, 0.0628 | 4.6843, | 15.9910, | 4.1526, | 3.1951, | 4.0533, | 3.0651, | 5.4713, |
| MR-RAPS3 | 0.0599 | | 0.052 | 0.0727 | 0.0643 | 0.0513 | 0.0578 | 0.0495 | 0.0614 |
| WIK-KAPSS | 0.936, -22.1268, | 0.945, -0.0436, | 0.932, -0.0903, | 0.917, 0.1199, | 0.914, 0.0685, | 0.913, 0.0690, | 0.916, 0.0437, | 0.923, 0.1284, | 0.943, 0.1937, |
| | 693.8632, | 1.4025, | 1.6370, | 3.1922, | 0.0083, | 0.7006, | 1.8048, | 0.1284, | 0.1937, |
| | 20170 | 0.0965 | 0.2188 | 1.347 | 0.0696 | 0.0502 | 0.4863 | 0.0368 | 0.0333 |
| | | | | 0.203, | 0.114, | 0.182, | 0.680, | 0.958, | 1.000, |
| MR-RAPS4 | 1.000, | 0.970, | 0.708, | | | | | | |
| MR-RAPS4 | 1.000, -0.1009, | 0.970, -0.0514, | -0.0292, | -0.0037, | 0.0035, | 0.0154, | 0.0294, | 0.0488, | 0.1002, |
| MR-RAPS4 | | | | | | | | | |

Table S41: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE violated, q=0.4, and N=50000.

| // | <i>'</i> | | | | , I | | | | |
|--------------------|---------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.561, | 0.126, | 0.042, | 0.015, | 0.016, | 0.013, | 0.050, | 0.116, | 0.491, |
| | -0.0808, | -0.0353, | -0.0198, | -0.0055, | 0.0015, | 0.0080, | 0.0218, | 0.0375, | 0.0817, |
| | 0.0344, | 0.0312, | 0.0292, | 0.0286, | 0.0282, | 0.0285, | 0.0306, | 0.0330, | 0.0385, |
| | 0.0398 | 0.0392 | 0.0391 | 0.039 | 0.0393 | 0.0395 | 0.0402 | 0.0412 | 0.0436 |
| cML-MA-AIC-Profile | 0.557, | 0.123, | 0.040, | 0.015, | 0.016, | 0.013, | 0.050, | 0.114, | 0.489, |
| | -0.0808, | -0.0353, | -0.0198, | -0.0055, | 0.0015, | 0.0080, | 0.0218, | 0.0375, | 0.0818, |
| | 0.0345, | 0.0313, | 0.0292, | 0.0286, | 0.0282, | 0.0285, | 0.0306, | 0.0330, | 0.0386, |
| | 0.04 | 0.0395 | 0.0393 | 0.0393 | 0.0395 | 0.0398 | 0.0405 | 0.0414 | 0.0438 |
| cML-AIC | 0.755, | 0.283, | 0.136, | 0.066, | 0.057, | 0.077, | 0.146, | 0.302, | 0.708, |
| | -0.0882, | -0.0402, | -0.0227, | -0.0060, | 0.0022, | 0.0101, | 0.0261, | 0.0436, | 0.0908, |
| | 0.0387, | 0.0376, | 0.0365, | 0.0362, | 0.0362, | 0.0365, | 0.0377, 0.0344 | 0.0398, | 0.0438, |
| M AIG D CI | 0.0324 | 0.033 | 0.0333 | 0.0337 | 0.0339 | 0.034 | | 0.0348 | 0.0357 |
| cML-AIC-Profile | 0.751, | 0.281, -0.0403, | 0.135, | 0.063, -0.0060, | 0.056, | 0.072, 0.0101, | 0.144, | 0.298, | 0.706, |
| | -0.0883, 0.0389, | 0.0376, | -0.0227, 0.0365, | 0.0362, | 0.0022, 0.0362, | 0.0101, | 0.0261, 0.0377, | 0.0436, 0.0398, | 0.0908, 0.0438, |
| | 0.0389, | 0.0370, | 0.0336 | 0.0302, | 0.0302, | 0.0343 | 0.0377, | 0.035 | 0.0458, |
| cML-MA-BIC | 0.898, | 0.363, | 0.149, | 0.056, | 0.036, | 0.0545 | 0.156, | 0.351, | 0.864, |
| CHILD HILL DIC | -0.0990, | -0.0490, | -0.0291, | -0.0092, | 0.0007, | 0.0107, | 0.0305, | 0.0505, | 0.1005, |
| | 0.0299, | 0.0304, | 0.0305, | 0.0308, | 0.0309, | 0.0311, | 0.0314, | 0.0318, | 0.0328, |
| | 0.0304 | 0.031 | 0.0313 | 0.0315 | 0.0317 | 0.0318 | 0.0322 | 0.0325 | 0.0334 |
| cML-MA-BIC-Profile | 0.897, | 0.361, | 0.148, | 0.055, | 0.036, | 0.052, | 0.152, | 0.347, | 0.862, |
| | -0.0990, | -0.0490, | -0.0291, | -0.0092, | 0.0007, | 0.0107, | 0.0305, | 0.0505, | 0.1005, |
| | 0.0299, | 0.0304, | 0.0305, | 0.0308, | 0.0309, | 0.0311, | 0.0314, | 0.0318, | 0.0328, |
| | 0.0306 | 0.0311 | 0.0314 | 0.0317 | 0.0318 | 0.032 | 0.0323 | 0.0326 | 0.0336 |
| cML-BIC | 0.907, | 0.375, | 0.157, | 0.060, | 0.042, | 0.062, | 0.162, | 0.361, | 0.874, |
| | -0.0994, | -0.0493, | -0.0293, | -0.0093, | 0.0008, | 0.0108, | 0.0308, | 0.0508, | 0.1007, |
| | 0.0299, | 0.0305, | 0.0307, | 0.0309, | 0.0312, | 0.0314, | 0.0317, | 0.0321, | 0.0329, |
| M DIC P 21 | 0.03 | 0.0306 | 0.0308 | 0.0311 | 0.0313 | 0.0314 | 0.0317 | 0.0321 | 0.033 |
| cML-BIC-Profile | 0.906, | 0.372, | 0.156, | 0.059, | 0.042, | 0.058, | 0.159, | 0.355, | 0.871, |
| | -0.0994, | -0.0493, | -0.0293, | -0.0093, | 0.0008, | 0.0108, | 0.0308, | 0.0508, | 0.1007, |
| | 0.0299, 0.0302 | 0.0305, 0.0307 | 0.0307, 0.031 | 0.0309, 0.0312 | 0.0312, 0.0314 | 0.0314, 0.0316 | 0.0317, 0.0319 | 0.0321, 0.0322 | 0.0329, 0.0332 |
| MR-Mix | 0.0302 | 0.0307 | 0.031 | 0.0312 | 0.0314 | 0.0316 | 0.0319 | 0.0322 | 0.0532 |
| IVIK-IVIIX | -0.1038, | -0.0505, | -0.0301, | -0.0097, | 0.030, | 0.036, | 0.099, | 0.237, 0.0488, | 0.739, |
| | 0.0327, | 0.0325, | 0.0325, | 0.0326, | 0.0325, | 0.0326, | 0.0257, | 0.0327, | 0.0325, |
| | 0.0377 | 0.0325, | 0.0375 | 0.0374 | 0.0373 | 0.0372 | 0.0372 | 0.0373 | 0.0374 |
| MR-ContMix | 0.903, | 0.393, | 0.179, | 0.073, | 0.056, | 0.071, | 0.179, | 0.381, | 0.862, |
| mit commi | -0.0988, | -0.0488, | -0.0289, | -0.0090, | 0.0009, | 0.0108, | 0.0306, | 0.0505, | 0.1007, |
| | 0.0313, | 0.0321, | 0.0323, | 0.0326, | 0.0328, | 0.0331, | 0.0335, | 0.0338, | 0.0351, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.868, | 0.327, | 0.139, | 0.053, | 0.037, | 0.056, | 0.142, | 0.328, | 0.818, |
| | -0.0971, | -0.0471, | -0.0270, | -0.0071, | 0.0029, | 0.0129, | 0.0327, | 0.0527, | 0.1026, |
| | 0.0538, | 0.0540, | 0.0542, | 0.0543, | 0.0544, | 0.0545, | 0.0535, | 0.0538, | 0.0543, |
| | 0.033 | 0.0337 | 0.034 | 0.0343 | 0.0344 | 0.0346 | 0.0349 | 0.0352 | 0.0362 |
| MR-PRESSO | 0.366, | 0.200, | 0.154, | 0.130, | 0.121, | 0.131, | 0.164, | 0.240, | 0.416, |
| | -0.0568, | -0.0085, | 0.0111, | 0.0306, | 0.0401, | 0.0498, | 0.0683, | 0.0882, | 0.1365, |
| | 0.3305, | 0.3300, 0.162 | 0.3298, | 0.3296, 0.1605 | 0.3295, | 0.3294, | 0.3284, | 0.3275, 0.1556 | 0.3253, 0.1499 |
| MR-IVW | 0.1626 0.119, | 0.102 | 0.1613 0.111, | 0.1005 | 0.1599 0.106, | 0.1598 0.106, | 0.1578 0.106, | 0.1556 | 0.1499 |
| IVIIX-I V VV | -0.0575, | -0.0073, | 0.111, | 0.103, | 0.100, | 0.0528, | 0.100, | 0.104, | 0.108, |
| | 0.3493, | 0.3493, | 0.3493, | 0.0328, | 0.0428, | 0.3493, | 0.0729, | 0.0929, | 0.1430, |
| | 0.325 | 0.325 | 0.325 | 0.325 | 0.325 | 0.325 | 0.325 | 0.325 | 0.3251 |
| MR-IVW-Oracle | 0.875, | 0.320, | 0.132, | 0.043, | 0.027, | 0.046, | 0.131, | 0.312, | 0.817, |
| mit i monute | -0.0991, | -0.0493, | -0.0293, | -0.0094, | 0.0005, | 0.0105, | 0.0304, | 0.0503, | 0.1001, |
| | 0.0295, | 0.0300, | 0.0303, | 0.0305, | 0.0307, | 0.0308, | 0.0311, | 0.0315, | 0.0324, |
| | 0.0327 | 0.0333 | 0.0336 | 0.0339 | 0.034 | 0.0342 | 0.0345 | 0.0349 | 0.0358 |
| MR-Egger | 0.198, | 0.205, | 0.208, | 0.208, | 0.209, | 0.210, | 0.211, | 0.213, | 0.216, |
| | 0.3768, | 0.4239, | 0.4428, | 0.4616, | 0.4710, | 0.4804, | 0.4992, | 0.5180, | 0.5649, |
| | 1.5720, | 1.5718, | 1.5717, | 1.5717, | 1.5717, | 1.5716, | 1.5716, | 1.5715, | 1.5714, |
| | 1.169 | 1.17 | 1.17 | 1.17 | 1.17 | 1.17 | 1.17 | 1.17 | 1.171 |
| MR-Weighted-Median | 0.743, | 0.287, | 0.138, | 0.069, | 0.058, | 0.060, | 0.106, | 0.205, | 0.591, |
| | -0.1006, | -0.0532, | -0.0343, | -0.0153, | -0.0058, | 0.0037, | 0.0227, | 0.0415, | 0.0884, |
| | 0.0437, | 0.0457, | 0.0466, | 0.0476, | 0.0482, | 0.0489, | 0.0503, | 0.0521, | 0.0569, |
| MD Walaka 134 | 0.0391 | 0.0399 | 0.0402 | 0.0406 | 0.0408 | 0.041 | 0.0415 | 0.042 | 0.0433 |
| MR-Weighted-Mode | 0.831, | 0.281, | 0.113, | 0.043, | 0.039, | 0.048, | 0.115, | 0.273, | 0.761, |
| | -0.0975, 0.0649, | -0.0489, 0.0679, | -0.0291, 0.0684, | -0.0102, 0.0731, | -0.0004, 0.0732, | 0.0093, 0.0733, | 0.0284, 0.0745, | 0.0483, | 0.0939, 0.0913, |
| | 0.0349, | 0.0079, | 0.0394 | 0.0731, | 0.0732, | 0.0733, | 0.0743, | 0.0750, 0.0414 | 0.0913, |
| MR-RAPS1 | 0.0382 | 0.0389 | 0.0394 | 0.0397 | 0.0398 | 0.04 | 0.0406 | 0.0414 | 0.043 |
| MIX IXII DI | -0.0553, | -0.0052, | 0.122, | 0.0348, | 0.110, | 0.0549, | 0.111, | 0.0950, | 0.110, |
| | 0.3416, | 0.3417, | 0.3417, | 0.3417, | 0.3417, | 0.3417, | 0.3418, | 0.3418, | 0.3419, |
| | 0.3099 | 0.31 | 0.31 | 0.31 | 0.3101 | 0.3101 | 0.3101 | 0.3101 | 0.3102 |
| MR-RAPS2 | 0.115, | 0.089, | 0.088, | 0.080, | 0.078, | 0.083, | 0.087, | 0.086, | 0.093, |
| ** | -0.0818, | -0.0160, | 0.0027, | 0.0335, | 0.0346, | 0.0448, | 0.0459, | 0.0865, | 0.1109, |
| | 0.5677, | 0.3351, | 0.3285, | 0.4325, | 0.3329, | 0.3348, | 0.8315, | 0.3255, | 0.8306, |
| | 0.3129 | 0.3139 | 0.3138 | 0.3138 | 0.3134 | 0.3136 | 0.316 | 0.3141 | 0.3169 |
| MR-RAPS3 | 0.885, | 0.884, | 0.897, | 0.905, | 0.909, | 0.914, | 0.916, | 0.916, | 0.914, |
| | 1.3579, | 0.5522, | -0.0384, | 35.0963, | 0.3326, | 0.4553, | 0.8766, | -0.5582, | 0.5238, |
| | 44.4267, | 13.3942, | 16.5791, | 819.6598, | 7.6864, | 18.7536, | 9.9464, | 21.6160, | 5.7278, |
| | 165.6 | 13.21 | 17.56 | 49490 | 3.564 | 38.44 | 13.95 | 51.22 | 2.47 |
| MR-RAPS4 | 0.983, | 0.953, | 0.935, | 0.925, | 0.919, | 0.911, | 0.924, | 0.944, | 0.980, |
| | -0.1091, | -0.2614, | 0.0849, | -0.0260, | -0.2501, | -0.2434, | -0.1388, | -0.1657, | 0.0310, |
| | | | | | | | | | |
| | 3.6669, 0.5702 | 11.5315, 1.389 | 3.9536, 0.8077 | 7.6959, 1.438 | 8.8183, 0.4624 | 7.5444, 0.4677 | 8.6924, 0.7604 | 7.6694, 0.5314 | 7.2304, 0.4874 |

Table S42: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE violated, q=0.4, and N=100000.

| , , | <i>'</i> | | | | , <u>1</u> | | | | |
|--------------------|---------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.851, | 0.258, | 0.092, | 0.015, | 0.013, | 0.019, | 0.081, | 0.238, | 0.769, |
| | -0.0861, | -0.0379, | -0.0215, | -0.0063, | 0.0002, | 0.0070, | 0.0215, | 0.0379, | 0.0850, |
| | 0.0267, | 0.0247, | 0.0221, | 0.0205, | 0.0200, | 0.0205, | 0.0226, | 0.0253, | 0.0288, |
| | 0.0284 | 0.0283 | 0.0279 | 0.0277 | 0.0278 | 0.028 | 0.0287 | 0.0297 | 0.0314 |
| cML-MA-AIC-Profile | 0.851, | 0.258, | 0.092, | 0.015, | 0.012, | 0.018, | 0.080, | 0.236, | 0.766, |
| | -0.0862, | -0.0379, | -0.0215, | -0.0063, | 0.0002, | 0.0070, | 0.0215, | 0.0380, | 0.0851, |
| | 0.0269, | 0.0247, | 0.0221, | 0.0205, | 0.0200, | 0.0205, | 0.0226, | 0.0253, | 0.0288, |
|) // LIC | 0.0285 | 0.0284 | 0.028 | 0.0278 | 0.0279 | 0.0281 | 0.0288 | 0.0298 | 0.0315 |
| cML-AIC | 0.921, | 0.477, | 0.240, | 0.089, | 0.077, | 0.078, | 0.231, | 0.480, | 0.883, |
| | -0.0918, | -0.0428, | -0.0248, | -0.0073, | 0.0004, | 0.0083, | 0.0248, | 0.0427, | 0.0916, |
| | 0.0302, 0.0231 | 0.0290, 0.0235 | 0.0273, 0.0236 | 0.0264, 0.0238 | 0.0262, 0.0239 | 0.0266, 0.0241 | 0.0280, 0.0242 | 0.0301, 0.0246 | 0.0321, 0.0252 |
| aML AIC Duafila | | | | 0.0238 | | | 0.0242 | | |
| cML-AIC-Profile | 0.921, -0.0920, | 0.476, -0.0428, | 0.240, -0.0248, | -0.0073, | 0.076, 0.0004, | 0.078, 0.0083, | 0.229, | 0.478, 0.0427, | 0.883, 0.0916, |
| | 0.0304, | 0.0290, | 0.0248, | 0.0264, | 0.0004, | 0.0266, | 0.0248, | 0.0427, | 0.0310, |
| | 0.0231 | 0.0235 | 0.0237 | 0.0239 | 0.024 | 0.0241 | 0.0243 | 0.0247 | 0.0253 |
| cML-MA-BIC | 0.995, | 0.624, | 0.284, | 0.067, | 0.047, | 0.072, | 0.276, | 0.600, | 0.983, |
| | -0.0998, | -0.0498, | -0.0299, | -0.0100, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0216, | 0.0220, | 0.0221, | 0.0224, | 0.0225, | 0.0226, | 0.0229, | 0.0232, | 0.0239, |
| | 0.0214 | 0.0218 | 0.022 | 0.0222 | 0.0223 | 0.0225 | 0.0227 | 0.0229 | 0.0236 |
| cML-MA-BIC-Profile | 0.995, | 0.622, | 0.282, | 0.067, | 0.048, | 0.072, | 0.275, | 0.597, | 0.983, |
| | -0.0998, | -0.0498, | -0.0299, | -0.0100, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0216, | 0.0220, | 0.0221, | 0.0224, | 0.0225, | 0.0226, | 0.0229, | 0.0232, | 0.0239, |
| | 0.0215 | 0.0219 | 0.0221 | 0.0223 | 0.0224 | 0.0225 | 0.0227 | 0.023 | 0.0236 |
| cML-BIC | 0.995, | 0.636, | 0.292, | 0.070, | 0.051, | 0.073, | 0.293, | 0.606, | 0.985, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0100, | 0.0001, | 0.0101, | 0.0301, | 0.0500, | 0.1000, |
| | 0.0216, | 0.0220, | 0.0222, | 0.0226, | 0.0227, | 0.0228, | 0.0230, | 0.0232, | 0.0240, |
| | 0.0212 | 0.0216 | 0.0217 | 0.0219 | 0.022 | 0.0222 | 0.0224 | 0.0226 | 0.0233 |
| cML-BIC-Profile | 0.995, | 0.635, | 0.292, | 0.070, | 0.051, | 0.073, | 0.291, | 0.605, | 0.986, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0100, | 0.0001, | 0.0101, | 0.0301, | 0.0500, | 0.1000, |
| | 0.0216, | 0.0220, | 0.0222, | 0.0226, | 0.0227, | 0.0228, | 0.0230, | 0.0232, | 0.0240, |
| | 0.0212 | 0.0216 | 0.0218 | 0.022 | 0.0221 | 0.0222 | 0.0224 | 0.0227 | 0.0233 |
| MR-Mix | 0.973, | 0.487, | 0.191, | 0.044, | 0.029, | 0.050, | 0.188, | 0.468, | 0.937, |
| | -0.1043, | -0.0509, | -0.0303, | -0.0101, | 0.0000, | 0.0099, | 0.0294, | 0.0487, | 0.0946, |
| | 0.0241, | 0.0240, | 0.0240, | 0.0241, | 0.0240, | 0.0241, | 0.0241, | 0.0241, | 0.0240, |
| 100 C -16 | 0.027 | 0.0269 | 0.0269 | 0.027 | 0.0272 | 0.0297 | 0.0275 | 0.0275 | 0.0273 |
| MR-ContMix | 0.992, | 0.658, | 0.330, | 0.098, | 0.069, | 0.102, | 0.316, | 0.628, | 0.980, |
| | -0.1001, 0.0224, | -0.0502, 0.0228, | -0.0303, 0.0229, | -0.0103, 0.0232, | -0.0003, 0.0233, | 0.0097, 0.0234, | 0.0296, 0.0237, | 0.0496, 0.0239, | 0.0996, 0.0247, |
| | 0.0224, NA | 0.0228, NA | 0.0229, NA | 0.0232, NA | 0.0255, NA | 0.0254, NA | 0.0237, NA | 0.0239, NA | 0.0247, NA |
| MR-Lasso | 0.987, | 0.565, | 0.247, | 0.060, | 0.044, | 0.066, | 0.241, | 0.544, | 0.957, |
| WIK-Lasso | -0.0991, | -0.0492, | -0.0293, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1000, |
| | 0.0450, | 0.0452, | 0.0453, | 0.0370, | 0.0370, | 0.0372, | 0.0373, | 0.0375, | 0.0382, |
| | 0.0237 | 0.0242 | 0.0244 | 0.0247 | 0.0248 | 0.0249 | 0.0251 | 0.0254 | 0.026 |
| MR-PRESSO | 0.313, | 0.197, | 0.145, | 0.111, | 0.111, | 0.114, | 0.164, | 0.228, | 0.357, |
| | -0.0449, | 0.0051, | 0.0254, | 0.0450, | 0.0551, | 0.0650, | 0.0849, | 0.1044, | 0.1534, |
| | 0.3250, | 0.3247, | 0.3243, | 0.3242, | 0.3240, | 0.3240, | 0.3237, | 0.3237, | 0.3231, |
| | 0.2057 | 0.2028 | 0.2015 | 0.2006 | 0.2002 | 0.1999 | 0.198 | 0.1971 | 0.1931 |
| MR-IVW | 0.091, | 0.089, | 0.084, | 0.085, | 0.085, | 0.085, | 0.090, | 0.090, | 0.095, |
| | -0.0440, | 0.0062, | 0.0263, | 0.0464, | 0.0565, | 0.0665, | 0.0866, | 0.1067, | 0.1568, |
| | 0.3323, | 0.3323, | 0.3323, | 0.3323, | 0.3323, | 0.3323, | 0.3323, | 0.3324, | 0.3324, |
| | 0.3299 | 0.3299 | 0.3299 | 0.3299 | 0.3299 | 0.3299 | 0.3299 | 0.3298 | 0.3298 |
| MR-IVW-Oracle | 0.990, | 0.561, | 0.237, | 0.053, | 0.037, | 0.058, | 0.229, | 0.540, | 0.964, |
| | -0.0998, | -0.0499, | -0.0299, | -0.0099, | 0.0000, | 0.0100, | 0.0300, | 0.0499, | 0.0998, |
| | 0.0215, | 0.0219, | 0.0221, | 0.0223, | 0.0224, | 0.0225, | 0.0227, | 0.0230, | 0.0236, |
| | 0.0233 | 0.0238 | 0.024 | 0.0242 | 0.0244 | 0.0245 | 0.0247 | 0.025 | 0.0257 |
| MR-Egger | 0.235, | 0.237, | 0.240, | 0.240, | 0.240, | 0.239, | 0.239, | 0.243, | 0.238, |
| | 0.4847, | 0.5332, | 0.5526, | 0.5720, | 0.5816, | 0.5913, | 0.6107, | 0.6300, | 0.6784, |
| | 1.5839, | 1.5840, | 1.5840, | 1.5840, | 1.5840, | 1.5841, | 1.5841, | 1.5841, | 1.5842, |
| MD Walake 134 3 | 1.191 | 1.191 | 1.191 | 1.191 | 1.191 | 1.191 | 1.191 | 1.191 | 1.192 |
| MR-Weighted-Median | 0.941, | 0.461, | 0.214, | 0.093, | 0.072, | 0.080, | 0.171, 0.0244, | 0.388, | 0.851, |
| | -0.1013, 0.0325, | -0.0528, 0.0341, | -0.0335, 0.0350, | -0.0141, 0.0359, | -0.0045, 0.0364, | 0.0051, 0.0369, | 0.0244, 0.0380, | 0.0437, | 0.0916, |
| | 0.0325, | 0.0341, | 0.0330, | 0.0339, | 0.0364, | 0.0369, | 0.0380, | 0.0394, 0.0296 | 0.0427, 0.0306 |
| MR-Weighted-Mode | 0.0276 | 0.0281 | 0.0284 | 0.0286 | 0.0288 | 0.0289 | 0.0293 | 0.0296 | 0.0306 |
| mergineu-ivioue | -0.0995, | -0.0501, | -0.0304, | -0.0106, | -0.0008, | 0.036, | 0.212, 0.0291, | 0.322, 0.0488, | 0.943, |
| | 0.0328, | 0.0329, | 0.0328, | 0.0330, | 0.0330, | 0.0031, | 0.0231, | 0.0336, | 0.0400, |
| | 0.0284 | 0.0289 | 0.0291 | 0.0293 | 0.0295 | 0.0297 | 0.0299 | 0.0301 | 0.0311 |
| MR-RAPS1 | 0.099, | 0.097, | 0.092, | 0.088, | 0.087, | 0.088, | 0.087, | 0.089, | 0.101, |
| | -0.0479, | 0.0022, | 0.0222, | 0.0422, | 0.0522, | 0.0622, | 0.0822, | 0.1022, | 0.1523, |
| | 0.3240, | 0.3240, | 0.3241, | 0.3241, | 0.3241, | 0.3241, | 0.3241, | 0.3242, | 0.3243, |
| | 0.3135 | 0.3135 | 0.3135 | 0.3135 | 0.3135 | 0.3135 | 0.3135 | 0.3135 | 0.3136 |
| MR-RAPS2 | 0.106, | 0.088, | 0.086, | 0.079, | 0.078, | 0.077, | 0.074, | 0.078, | 0.085, |
| | -0.0890, | -0.0380, | -0.0171, | 0.0049, | 0.0542, | 0.0408, | 0.0507, | 0.0725, | 0.1242, |
| | 0.3025, | 0.2975, | 0.2906, | 0.2950, | 0.9588, | 0.4487, | 0.2983, | 0.3025, | 0.3063, |
| | 0.2722 | 0.2783 | 0.2816 | 0.2842 | 0.2888 | 0.2898 | 0.292 | 0.2951 | 0.3023 |
| MR-RAPS3 | 0.922, | 0.919, | 0.922, | 0.929, | 0.937, | 0.936, | 0.931, | 0.938, | 0.935, |
| | -2.5105, | 0.4746, | 1.8887, | -1.3272, | 30.6530, | 0.6059, | -2.4818, | 0.1966, | 0.2288, |
| | 56.1160, | 27.9686, | 57.6319, | 50.4485, | 894.6462, | 7.9225, | 58.5677, | 11.4127, | 9.1694, |
| | 128.2 | 42.39 | 167.6 | 126.7 | 30780 | 2.882 | 539 | 7.026 | 4.466 |
| MR-RAPS4 | 0.978, | 0.970, | 0.963, | 0.950, | 0.952, | 0.948, | 0.960, | 0.965, | 0.985, |
| | -0.1546, | 0.0731, | 0.1687, | -0.0474, | -0.0736, | -0.0663, | -0.0506, | -0.0820, | -0.2449 |
| | | | | | | | | | |
| | 10.1909, 0.471 | 8.2261, 0.712 | 7.9969, 2.363 | 4.9448, 0.452 | 5.1400, 0.5624 | 5.1935, 2.667 | 5.2175, 0.7871 | 5.2784, 1.371 | 8.5402, 0.3131 |

Table S43: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE violated, q=0.4, and N=200000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|--------------------|---------------------|----------|----------|-------------------|----------|----------|----------|-----------------|---------|
| cML-MA-AIC | 0.977, | 0.538, | 0.193, | 0.025, | 0.011, | 0.028, | 0.183, | 0.479, | 0.957, |
| | -0.0903, | -0.0408, | -0.0224, | -0.0068, | 0.0001, | 0.0070, | 0.0222, | 0.0402, | 0.0893, |
| | 0.0189, | 0.0184, | 0.0169, | 0.0147, | 0.0143, | 0.0147, | 0.0173, | 0.0194, | 0.0210, |
| M M MG D CI | 0.0202 | 0.0203 | 0.02 | 0.0197 | 0.0196 | 0.0199 | 0.0207 | 0.0213 | 0.0222 |
| ML-MA-AIC-Profile | 0.977, | 0.536, | 0.192, | 0.025, | 0.011, | 0.027, | 0.182, | 0.479, | 0.957, |
| | -0.0905, | -0.0408, | -0.0224, | -0.0068, | 0.0001, | 0.0070, | 0.0222, | 0.0402, | 0.0894, |
| | 0.0189, | 0.0184, | 0.0169, | 0.0147, | 0.0143, | 0.0147, | 0.0173, | 0.0194, | 0.0211, |
| cML-AIC | 0.0202 | 0.0203 | 0.02 | 0.0197 | 0.0197 | 0.0199 | 0.0207 | 0.0213 | 0.0222 |
| cML-AIC | 0.989, | 0.749, | 0.413, | 0.101, | 0.062, | 0.094, | 0.365, | 0.707, | 0.971, |
| | -0.0949, | -0.0452, | -0.0258, | -0.0083, | 0.0002, | 0.0083, | 0.0254, | 0.0442, | 0.0938 |
| | 0.0208, | 0.0206, | 0.0199, | 0.0186, | 0.0182, | 0.0185, | 0.0205, | 0.0219, | 0.0235 |
| M. AICD CI | 0.0162 | 0.0165 | 0.0166 | 0.0168 | 0.0169 | 0.017 | 0.0172 | 0.0175 | 0.0179 |
| cML-AIC-Profile | 0.989, | 0.749, | 0.413, | 0.101, | 0.062, | 0.093, | 0.362, | 0.706, | 0.971, |
| | -0.0952, | -0.0452, | -0.0258, | -0.0083, | 0.0002, | 0.0083, | 0.0254, | 0.0442, | 0.0939 |
| | 0.0206, | 0.0206, | 0.0199, | 0.0186, | 0.0182, | 0.0185, | 0.0205, | 0.0219, | 0.0235 |
| M. M. DIG | 0.0162 | 0.0165 | 0.0167 | 0.0168 | 0.0169 | 0.017 | 0.0173 | 0.0175 | 0.0179 |
| cML-MA-BIC | 1.000, | 0.891, | 0.503, | 0.101, | 0.044, | 0.099, | 0.468, | 0.870, | 1.000, |
| | -0.0998, | -0.0499, | -0.0299, | -0.0100, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0998 |
| | 0.0154, | 0.0156, | 0.0157, | 0.0159, | 0.0159, | 0.0160, | 0.0162, | 0.0163, | 0.0168 |
| | 0.0151 | 0.0154 | 0.0155 | 0.0157 | 0.0157 | 0.0158 | 0.016 | 0.0161 | 0.0166 |
| ML-MA-BIC-Profile | 1.000, | 0.891, | 0.501, | 0.101, | 0.044, | 0.099, | 0.467, | 0.870, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0100, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0998 |
| | 0.0154, | 0.0156, | 0.0157, | 0.0159, | 0.0159, | 0.0160, | 0.0162, | 0.0163, | 0.0168 |
| 10.00 | 0.0151 | 0.0154 | 0.0155 | 0.0157 | 0.0157 | 0.0158 | 0.016 | 0.0162 | 0.0166 |
| cML-BIC | 1.000, | 0.894, | 0.508, | 0.105, | 0.045, | 0.103, | 0.480, | 0.874, | 1.000, |
| | -0.0999, | -0.0500, | -0.0300, | -0.0100, | -0.0001, | 0.0100, | 0.0300, | 0.0500, | 0.0999 |
| | 0.0153, | 0.0156, | 0.0157, | 0.0158, 0.0155 | 0.0159, | 0.0161, | 0.0162, | 0.0164, | 0.0170 |
| | 0.015 | 0.0153 | 0.0154 | 0.0155 | 0.0156 | 0.0157 | 0.0158 | 0.016 | 0.0165 |
| cML-BIC-Profile | 1.000, | 0.893, | 0.508, | 0.105, | 0.045, | 0.102, | 0.479, | 0.874, | 1.000, |
| | -0.0999, | -0.0500, | -0.0300, | -0.0100, | -0.0001, | 0.0100, | 0.0300, | 0.0500, | 0.0999 |
| | 0.0153, | 0.0156, | 0.0157, | 0.0158, | 0.0159, | 0.0161, | 0.0162, | 0.0164, | 0.0170 |
| | 0.015 | 0.0153 | 0.0154 | 0.0155 | 0.0156 | 0.0157 | 0.0158 | 0.016 | 0.0165 |
| MR-Mix | 0.999, | 0.782, | 0.361, | 0.071, | 0.032, | 0.068, | 0.346, | 0.729, | 0.996, |
| | -0.1042, | -0.0513, | -0.0305, | -0.0102, | -0.0001, | 0.0099, | 0.0293, | 0.0483, | 0.0943 |
| | 0.0176, | 0.0174, | 0.0174, | 0.0174, | 0.0174, | 0.0175, | 0.0175, | 0.0174, | 0.0173 |
| | 0.0191 | 0.0191 | 0.019 | 0.0191 | 0.0191 | 0.0191 | 0.0191 | 0.0191 | 0.0192 |
| MR-ContMix | 0.999, | 0.900, | 0.550, | 0.126, | 0.058, | 0.135, | 0.510, | 0.880, | 1.000, |
| | -0.0998, | -0.0499, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0498, | 0.0997 |
| | 0.0158, | 0.0161, | 0.0163, | 0.0164, | 0.0164, | 0.0165, | 0.0167, | 0.0169, | 0.0174 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.997, | 0.843, | 0.450, | 0.095, | 0.046, | 0.085, | 0.400, | 0.815, | 0.996, |
| | -0.0998, | -0.0496, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0302, | 0.0502, | 0.1002 |
| | 0.0480, | 0.0470, | 0.0470, | 0.0471, | 0.0471, | 0.0471, | 0.0472, | 0.0473, | 0.0475 |
| | 0.0173 | 0.0175 | 0.0177 | 0.0178 | 0.0179 | 0.018 | 0.0182 | 0.0183 | 0.0188 |
| MR-PRESSO | 0.306, | 0.234, | 0.169, | 0.112, | 0.103, | 0.112, | 0.175, | 0.239, | 0.322, |
| | -0.0679, | -0.0180, | 0.0022, | 0.0219, | 0.0319, | 0.0419, | 0.0621, | 0.0823, | 0.1322 |
| | 0.3504, | 0.3504, | 0.3504, | 0.3503, | 0.3503, | 0.3503, | 0.3502, | 0.3501, | 0.3500 |
| | 0.239 | 0.2378 | 0.2378 | 0.2368 | 0.2368 | 0.2368 | 0.2353 | 0.2351 | 0.2328 |
| MR-IVW | 0.107, | 0.101, | 0.101, | 0.102, | 0.102, | 0.104, | 0.107, | 0.110, | 0.119, |
| | -0.0671, | -0.0168, | 0.0033, | 0.0234, | 0.0334, | 0.0435, | 0.0636, | 0.0837, | 0.1339 |
| | 0.3524, | 0.3524, | 0.3524, | 0.3524, | 0.3524, | 0.3524, | 0.3524, | 0.3524, | 0.3524 |
| | 0.3309 | 0.3309 | 0.3308 | 0.3308 | 0.3308 | 0.3308 | 0.3308 | 0.3308 | 0.3307 |
| MR-IVW-Oracle | 0.999, | 0.844, | 0.447, | 0.090, | 0.039, | 0.079, | 0.403, | 0.819, | 0.999, |
| Oracle | -0.0998, | -0.0499, | -0.0300, | -0.0100, | 0.0000, | 0.0099, | 0.0299, | 0.0499, | 0.0998 |
| | 0.0153, | 0.0155, | 0.0156, | 0.0158, | 0.0158, | 0.0159, | 0.0161, | 0.0162, | 0.0167 |
| | 0.0155, | 0.0155, | 0.0168 | 0.0136, | 0.0138, | 0.0172 | 0.0101, | 0.0102, | 0.018 |
| MR-Egger | 0.240, | 0.244, | 0.248, | 0.248, | 0.249, | 0.248, | 0.0173 | 0.251, | 0.254, |
| 25501 | 0.4842, | 0.5335, | 0.5533, | 0.5730, | 0.5828, | 0.5927, | 0.6124, | 0.6321, | 0.6813 |
| | 1.6226, | 1.6225, | 1.6224, | 1.6224, | 1.6224, | 1.6223, | 1.6223, | 1.6222, | 1.6221 |
| | 1.1645 | 1.1645 | 1.1645 | 1.1646 | 1.1646 | 1.1646 | 1.1646 | 1.1646 | 1.1646 |
| IR-Weighted-Median | 0.997, | 0.748, | 0.402, | 0.124, | 0.070, | 0.084, | 0.285, | 0.610, | 0.965, |
| | -0.1018, | -0.0534, | -0.0340, | -0.0147, | -0.0050, | 0.0047, | 0.0240, | 0.0434, | 0.0916 |
| | 0.0297, | 0.0301, | 0.0308, | 0.0317, | 0.0322, | 0.0327, | 0.0337, | 0.0350, | 0.0389 |
| | 0.0297, | 0.0201 | 0.0203 | 0.0205 | 0.0322, | 0.0327, | 0.0337, | 0.0330, | 0.0219 |
| MR-Weighted-Mode | 0.996, | 0.817, | 0.420, | 0.0203 | 0.039, | 0.080, | 0.378, | 0.788, | 0.991, |
| | -0.1005, | -0.0504, | -0.0307, | -0.0109. | -0.0009, | 0.0090, | 0.0286. | 0.0492, | 0.0961 |
| | 0.0238, | 0.0240, | 0.0240, | 0.0241, | 0.0243, | 0.0244, | 0.0248, | 0.0252, | 0.0497 |
| | 0.0238, | 0.0185 | 0.0186 | 0.0241, | 0.0243, | 0.019 | 0.0192 | 0.0195 | 0.0201 |
| MR-RAPS1 | 0.0101 | 0.0185 | 0.112, | 0.108, | 0.013 | 0.111, | 0.0132 | 0.115, | 0.126, |
| MIX IX II OI | -0.0692, | -0.0192, | 0.0008, | 0.108, | 0.0308, | 0.0408, | 0.0608, | 0.0808, | 0.120, |
| | 0.3419, | 0.3420, | 0.3420, | 0.0208, | 0.0308, | 0.3421, | 0.3421, | 0.3421, | 0.1308 |
| | 0.3419, | 0.3420, | 0.3420, | 0.3420, | 0.3420, | 0.3421, | 0.3421, | 0.3421, | 0.3422 |
| MR-RAPS2 | 0.162, | 0.314 | 0.089, | 0.080, | 0.073, | 0.067, | 0.073, | 0.071, | 0.077, |
| MIN-INAL DZ | -0.1226, | -0.0766, | -0.0552, | -0.0318, | -0.0226, | -0.0219, | 0.075, | 0.071, | 0.077, |
| | 0.1226, | 0.2639, | 0.2345, | 0.2336, | 0.2395, | 0.3510, | 0.0055, | 0.0248, 0.2619, | 0.0748 |
| | 0.2282, 0.1941 | | | 0.2336, | 0.2395, | 0.3510, | | | 0.2411 |
| MD DARGO | | 0.1937 | 0.1949 | | | | 0.2016 | 0.2009 | |
| MR-RAPS3 | 0.940, | 0.948, | 0.953, | 0.939, | 0.934, | 0.932, | 0.953, | 0.956, | 0.955, |
| | -2.8247, 45.2076 | 1.3487, | 0.3711, | 2.7406, | -1.7006, | 0.0982, | 0.1190, | -5.8855, | 0.9751, |
| | 45.3076, | 37.0838, | 16.2788, | 82.6052, | 55.5342, | 11.3167, | 17.1701, | 174.8939, | 17.468 |
| MD D (DG) | 52.1233 | 38.0906 | 7.362 | 127.3877 | 167.3854 | 6.5138 | 9.3429 | 804.4194 | 7.0265 |
| MR-RAPS4 | 1.000, | 0.965, | 0.735, | 0.399, | 0.344, | 0.399, | 0.723, | 0.959, | 1.000, |
| | -0.0657, | -0.0174, | 0.0086, | 0.0330, | 0.0416, | 0.0602, | 0.0560, | 0.0701, | 0.1159 |
| | 0.1245, | 0.2065, | 0.2540, | 0.2728, | 0.2802, | 0.2599, | 0.2086, | 0.1616, | 0.1038, |

Table S44: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE violated, q=0.6, and N=50000.

| ((| <i>'</i> | | | | , I | | | | |
|---------------------|---------------------|---------------------|---------------------|-----------|----------|----------|----------------|----------------|---------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.448, | 0.084, | 0.036, | 0.013, | 0.008, | 0.014, | 0.033, | 0.076, | 0.363, |
| | -0.0825, | -0.0367, | -0.0208, | -0.0064, | 0.0001, | 0.0069, | 0.0214, | 0.0363, | 0.0801, |
| | 0.0411, | 0.0369, | 0.0348, | 0.0334, | 0.0335, | 0.0339, | 0.0358, | 0.0392, | 0.0455, |
| | 0.047 | 0.0473 | 0.0473 | 0.0475 | 0.0477 | 0.048 | 0.0487 | 0.0495 | 0.0515 |
| cML-MA-AIC-Profile | 0.445, | 0.084, | 0.035, | 0.013, | 0.008, | 0.013, | 0.032, | 0.076, | 0.363, |
| AND MILL THE FIGURE | -0.0826, | -0.0367, | -0.0208, | -0.0064, | 0.0001, | 0.0069, | 0.0214, | 0.0363, | 0.0801, |
| | 0.0412, | 0.0369, | 0.0348, | 0.0334, | 0.0001, | 0.0009, | 0.0214, | 0.0394, | 0.0455, |
| | 0.0412, | 0.0309, | 0.0348, | 0.0334, | 0.0333, | 0.0339, | 0.0338, | 0.0394, | 0.0433 |
| -ML AIC | | | | 0.0478 | | | | | |
| cML-AIC | 0.639, | 0.210, | 0.112, | | 0.050, | 0.051, | 0.087, | 0.181, | 0.558, |
| | -0.0889, | -0.0416, | -0.0241, | -0.0076, | 0.0002, | 0.0080, | 0.0241, | 0.0401, | 0.0864 |
| | 0.0469, | 0.0441, | 0.0429, | 0.0422, | 0.0425, | 0.0430, | 0.0444, | 0.0472, | 0.0523 |
| | 0.04 | 0.0407 | 0.0411 | 0.0416 | 0.0418 | 0.042 | 0.0423 | 0.0429 | 0.0441 |
| cML-AIC-Profile | 0.638, | 0.205, | 0.111, | 0.056, | 0.049, | 0.049, | 0.085, | 0.178, | 0.551, |
| | -0.0890, | -0.0416, | -0.0241, | -0.0076, | 0.0002, | 0.0080, | 0.0241, | 0.0401, | 0.0864 |
| | 0.0470, | 0.0441, | 0.0429, | 0.0422, | 0.0425, | 0.0430, | 0.0444, | 0.0474, | 0.0523 |
| | 0.0403 | 0.041 | 0.0414 | 0.0419 | 0.0421 | 0.0423 | 0.0426 | 0.0432 | 0.0444 |
| cML-MA-BIC | 0.768, | 0.259, | 0.124, | 0.055, | 0.044, | 0.044, | 0.095, | 0.219, | 0.673, |
| | -0.1008, | -0.0506, | -0.0307, | -0.0107, | -0.0008, | 0.0091, | 0.0291, | 0.0488, | 0.0989 |
| | 0.0372, | 0.0377, | 0.0379, | 0.0382, | 0.0384, | 0.0386, | 0.0391, | 0.0395, | 0.0410 |
| | 0.0379 | 0.0386 | 0.0389 | 0.0392 | 0.0394 | 0.0396 | 0.04 | 0.0404 | 0.0415 |
| ML-MA-BIC-Profile | | 0.256, | | 0.056, | 0.0354 | 0.045, | 0.096, | 0.217, | 0.667, |
| ML-MA-BIC-PIOINE | 0.766, | | 0.125, | | | | | | |
| | -0.0993, | -0.0490, | -0.0290, | -0.0090, | 0.0009, | 0.0109, | 0.0309, | 0.0507, | 0.1008 |
| | 0.0591, | 0.0634, | 0.0648, | 0.0661, | 0.0667, | 0.0672, | 0.0683, | 0.0693, | 0.0713 |
| | 0.0388 | 0.0393 | 0.0395 | 0.0398 | 0.0399 | 0.0401 | 0.0405 | 0.0408 | 0.0419 |
| cML-BIC | 0.783, | 0.267, | 0.132, | 0.058, | 0.047, | 0.050, | 0.102, | 0.229, | 0.682, |
| | -0.1012, | -0.0509, | -0.0309, | -0.0108, | -0.0008, | 0.0093, | 0.0293, | 0.0492, | 0.0995 |
| | 0.0374, | 0.0381, | 0.0383, | 0.0386, | 0.0388, | 0.0391, | 0.0395, | 0.0396, | 0.0408 |
| | 0.0375 | 0.0381 | 0.0384 | 0.0388 | 0.0389 | 0.0391 | 0.0395 | 0.0399 | 0.0411 |
| cML-BIC-Profile | 0.781, | 0.264, | 0.132, | 0.059, | 0.047, | 0.050, | 0.102, | 0.228, | 0.677, |
| CIAIT-DIC-LIQUIC | -0.0992, | -0.0490, | -0.0290, | -0.0089, | 0.047, | 0.030, | 0.102, 0.0313, | 0.228, 0.0512, | 0.077, |
| | | | | | | | | | 0.1014 |
| | 0.0717, | 0.0721, | 0.0722, | 0.0724, | 0.0726, | 0.0727, | 0.0729, | 0.0730, | 0.0737 |
| 100 1 | 0.0377 | 0.0383 | 0.0386 | 0.039 | 0.0392 | 0.0393 | 0.0397 | 0.0401 | 0.0413 |
| MR-Mix | 0.726, | 0.219, | 0.100, | 0.051, | 0.041, | 0.044, | 0.093, | 0.195, | 0.628, |
| | -0.1045, | -0.0516, | -0.0313, | -0.0111, | -0.0010, | 0.0089, | 0.0283, | 0.0472, | 0.0931 |
| | 0.0395, | 0.0396, | 0.0395, | 0.0397, | 0.0397, | 0.0396, | 0.0395, | 0.0394, | 0.0399 |
| | 0.0423 | 0.0419 | 0.0419 | 0.042 | 0.0419 | 0.0419 | 0.0419 | 0.0419 | 0.0421 |
| MR-ContMix | 0.801, | 0.305, | 0.171, | 0.086, | 0.070, | 0.076, | 0.128, | 0.266, | 0.714, |
| | -0.1011, | -0.0510, | -0.0310, | -0.0111, | -0.0011, | 0.0090, | 0.0287, | 0.0487, | 0.0988 |
| | 0.0385, | 0.0394, | 0.0400, | 0.0403, | 0.0406, | 0.0408, | 0.0440, | 0.0444, | 0.0462 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.736, | 0.321, | 0.229, | 0.174, | 0.168, | 0.163, | 0.194, | 0.272, | 0.613, |
| MR-Lasso | | | | 0.174, | 0.106, | | | | |
| | -0.0499, | -0.0003, | 0.0195, | 0.0390, | 0.0497, | 0.0597, | 0.0799, | 0.1004, | 0.1503 |
| | 0.3745, | 0.3767, | 0.3775, | 0.3741, | 0.3746, | 0.3753, | 0.3755, | 0.3785, | 0.3794 |
| | 0.0678 | 0.0682 | 0.0688 | 0.0691 | 0.0697 | 0.0699 | 0.07 | 0.0708 | 0.0725 |
| MR-PRESSO | 0.246, | 0.140, | 0.122, | 0.110, | 0.110, | 0.107, | 0.117, | 0.143, | 0.246, |
| | -0.0304, | 0.0183, | 0.0382, | 0.0584, | 0.0678, | 0.0776, | 0.0978, | 0.1169, | 0.1663 |
| | 0.4048, | 0.4046, | 0.4042, | 0.4039, | 0.4038, | 0.4037, | 0.4040, | 0.4034, | 0.4028 |
| | 0.2281 | 0.2254 | 0.2248 | 0.2243 | 0.2234 | 0.223 | 0.2217 | 0.2195 | 0.2172 |
| MR-IVW | 0.105, | 0.100, | 0.103, | 0.101, | 0.099, | 0.103, | 0.102, | 0.104, | 0.111, |
| | -0.0306, | 0.0198, | 0.0400, | 0.0601, | 0.0702, | 0.0803, | 0.1004, | 0.1205, | 0.1708 |
| | 0.4136, | 0.4136, | 0.4136, | 0.4136, | 0.4136, | 0.4136, | 0.4136, | 0.4136, | 0.4135 |
| | 0.4028 | 0.4027 | 0.4027 | 0.4027 | 0.4027 | 0.4027 | 0.4027 | 0.4026 | 0.4026 |
| MD WWY O I | | | | | | | | | |
| MR-IVW-Oracle | 0.713, | 0.212, | 0.105, | 0.044, | 0.036, | 0.038, | 0.081, | 0.181, | 0.609, |
| | -0.1010, | -0.0510, | -0.0310, | -0.0110, | -0.0010, | 0.0090, | 0.0290, | 0.0490, | 0.0991 |
| | 0.0366, | 0.0373, | 0.0376, | 0.0380, | 0.0382, | 0.0384, | 0.0388, | 0.0392, | 0.0404 |
| | 0.0413 | 0.0422 | 0.0425 | 0.0429 | 0.0431 | 0.0433 | 0.0437 | 0.0442 | 0.0454 |
| MR-Egger | 0.201, | 0.201, | 0.205, | 0.205, | 0.205, | 0.205, | 0.204, | 0.204, | 0.216, |
| | 0.6599, | 0.7079, | 0.7271, | 0.7463, | 0.7559, | 0.7655, | 0.7846, | 0.8038, | 0.8517 |
| | 1.5413, | 1.5412, | 1.5411, | 1.5410, | 1.5410, | 1.5410, | 1.5409, | 1.5409, | 1.5408 |
| | 1.2434 | 1.2435 | 1.2436 | 1.2437 | 1.2437 | 1.2437 | 1.2438 | 1.2439 | 1.2441 |
| MP Weighted Medica | 0.638, | 0.314, | 0.226, | 0.187, | 0.174, | 0.178, | 0.199, | 0.255, | 0.484, |
| MR-Weighted-Median | | -0.0676, | -0.0507, | | | | | | |
| | -0.1093, | | | -0.0342, | -0.0256, | -0.0175, | -0.0013, | 0.0155, | 0.0572 |
| | 0.1281, | 0.1306, | 0.1323, | 0.1346, | 0.1360, | 0.1366, | 0.1388, | 0.1421, | 0.1501 |
| | 0.0502 | 0.0509 | 0.0513 | 0.0517 | 0.0519 | 0.0522 | 0.0527 | 0.0532 | 0.0547 |
| MR-Weighted-Mode | 0.749, | 0.718, | 0.704, | 0.691, | 0.694, | 0.688, | 0.680, | 0.681, | 0.690, |
| | -0.1287, | -0.0924, | -0.0779, | -0.0635, | -0.0561, | -0.0488, | -0.0341, | -0.0204, | 0.0166 |
| | 0.2185, | 0.2217, | 0.2227, | 0.2247, | 0.2257, | 0.2265, | 0.2280, | 0.2307, | 0.2373 |
| | 0.0473 | 0.0476 | 0.0479 | 0.048 | 0.0481 | 0.0482 | 0.0485 | 0.049 | 0.05 |
| MR-RAPS1 | 0.107, | 0.106, | 0.108, | 0.109, | 0.105, | 0.106, | 0.106, | 0.114, | 0.117, |
| 1011 01 | -0.0264, | 0.100, | 0.108, | 0.103, | 0.103, | 0.100, | 0.1039, | 0.114, | 0.117, |
| | | | | | | | | | |
| | 0.4036, | 0.4037, | 0.4037, | 0.4037, | 0.4037, | 0.4037, | 0.4037, | 0.4037, | 0.4037 |
| | 0.3842 | 0.3842 | 0.3842 | 0.3842 | 0.3842 | 0.3842 | 0.3842 | 0.3842 | 0.3843 |
| MR-RAPS2 | 0.115, | 0.104, | 0.107, | 0.114, | 0.109, | 0.107, | 0.109, | 0.112, | 0.120, |
| | -0.0310, | 0.0159, | 0.0380, | 0.0582, | 0.0663, | 0.0794, | 0.0988, | 0.1225, | 0.1701 |
| | 0.4253, | 0.4241, | 0.4250, | 0.4379, | 0.4368, | 0.4374, | 0.4382, | 0.4263, | 0.4255 |
| | 0.4102 | 0.41 | 0.4108 | 0.4104 | 0.4102 | 0.4118 | 0.4115 | 0.4126 | 0.4117 |
| MR-RAPS3 | 0.881, | 0.893, | 0.902, | 0.900, | 0.905, | 0.904, | 0.889, | 0.893, | 0.882, |
| MIN-IVAL 93 | 2.0639, | -1.6022, | | | | | -2.0102, | 7.2212, | |
| | | | -6.0948, | 7.5128, | 1.6741, | 3.6396, | | | 4.9987 |
| | 93.7912, | 54.9780, | 259.1498, | 202.9000, | 71.2527, | 88.6035, | 33.9409, | 169.8092, | 77.200 |
| | 252.4835 | 106.569 | 2527.0841 | 2281.6167 | 148.85 | 721.006 | 48.2306 | 1117.9699 | 953.60 |
| | 0.979, | 0.963, | 0.960, | 0.952, | 0.942, | 0.948, | 0.942, | 0.940, | 0.959, |
| MR-RAPS4 | | | | -0.3806, | -0.3676, | -0.2913, | -0.4679, | -0.2870, | -0.207 |
| MR-RAPS4 | -0.7163, | -0.7850, | -0.5914, | -0.5600, | -0.3070, | | -0.4077. | -0.2070, | -0.207 |
| MR-RAPS4 | -0.7163, 7.9742, | -0.7850, 9.7173, | -0.5914, 8.6282, | 7.5705, | 9.3461, | 9.6837, | 8.5193, | 8.0767, | 9.8532. |

Table S45: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE violated, q=0.6, and N=100000.

| Methods θ | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|---------------------|-----------------------|------------------------|------------------------|-----------------------|------------------------|------------------------|------------------------|------------------------|----------------------|
| cML-MA-AIC | 0.723, | 0.196, | 0.061, | 0.012, | 0.005, | 0.014, | 0.054, | 0.184, | 0.669, |
| | -0.0850, 3.100e- | -0.0374, 2.800e- | -0.0209, 2.580e- | -0.0062, 2.380e- | 0.0007, 2.360e- | 0.0073, 2.430e- | 0.0216, 2.620e- | 0.0380, 2.930e- | 0.0848, 3.360e- |
| | 02, 0.0335 | 02, 0.0338 | 02, 0.0337 | 02, 0.0338 | 02, 0.0339 | 02, 0.0341 | 02, 0.0348 | 02, 0.0355 | 02, 0.036 |
| cML-MA-AIC-Profile | 0.722, | 0.194, | 0.060, | 0.012, | 0.005, | 0.013, | 0.053, | 0.184, | 0.668, |
| | -0.0851, | -0.0374, | -0.0209, | -0.0062, 2.380e- | 0.0007, | 0.0072, | 0.0216, | 0.0380, | 0.0850, |
| | 3.100e- 02, 0.0336 | 2.800e- 02, 0.0339 | 2.580e- 02, 0.0338 | 02, 0.0339 | 2.360e- 02, 0.034 | 2.420e- 02, 0.0342 | 2.620e- 02, 0.0349 | 2.930e- 02, 0.0356 | 3.370e- 02, 0.037 |
| cML-AIC | 0.816, | 0.360, | 0.163, | 0.049, | 0.036, | 0.049, | 0.163, | 0.344, | 0.788, |
| | -0.0888, | -0.0410, | -0.0235, | -0.0071, | 0.0010, | 0.0083, | 0.0242, | 0.0419, | 0.0892, |
| | 3.560e- | 3.280e- | 3.150e- | 3.010e- | 2.990e- | 3.050e- | 3.210e- | 3.380e- | 3.770e- |
| cML-AIC-Profile | 02, 0.0286 0.817, | 02, 0.0291 0.359, | 02, 0.0293 0.161, | 02, 0.0295 0.049, | 02, 0.0297 0.035, | 02, 0.0299 0.046, | 02, 0.0302 0.161, | 02, 0.0305 0.340, | 02, 0.031 |
| CML-AIC-FIOIRE | -0.0889, | -0.0410, | -0.0235, | -0.0071, | 0.0010, | 0.040, | 0.101, | 0.0419, | 0.787, |
| | 3.550e- | 3.280e- | 3.150e- | 3.010e- | 2.990e- | 3.050e- | 3.210e- | 3.380e- | 3.790e- |
| | 02, 0.0287 | 02, 0.0292 | 02, 0.0294 | 02, 0.0297 | 02, 0.0298 | 02, 0.03 | 02, 0.0303 | 02, 0.0306 | 02, 0.03 |
| cML-MA-BIC | 0.955, | 0.451, | 0.188, | 0.050, | 0.036, | 0.053, | 0.202, | 0.446, | 0.935, |
| | -0.0988, 2.600e- | -0.0488, 2.650e- | -0.0288, 2.660e- | -0.0089, 2.680e- | 0.0010, 2.700e- | 0.0109, 2.710e- | 0.0308, 2.750e- | 0.0507, 2.790e- | 0.1007, 2.880e- |
| | 02, 0.0267 | 02, 0.0272 | 02, 0.0274 | 02, 0.0276 | 02, 0.0278 | 02, 0.0279 | 02, 0.0281 | 02, 0.0284 | 02, 0.02 |
| cML-MA-BIC-Profile | 0.954, | 0.448, | 0.188, | 0.050, | 0.036, | 0.053, | 0.201, | 0.445, | 0.935, |
| | -0.0988, | -0.0488, | -0.0288, | -0.0089, | 0.0010, | 0.0109, | 0.0308, | 0.0507, | 0.1007, |
| | 2.600e- 02, 0.0268 | 2.650e- 02, 0.0272 | 2.660e- 02, 0.0275 | 2.680e- 02, 0.0277 | 2.700e- | 2.710e- 02, 0.0279 | 2.750e- 02, 0.0282 | 2.790e- | 2.880e- 02, 0.029 |
| cML-BIC | 0.960, | 0.466, | 0.198, | 0.055, | 02, 0.0278 0.039, | 0.056, | 0.208, | 02, 0.0285 0.457, | 0.938, |
| CIVIL DIC | -0.0991. | -0.0491, | -0.0291, | -0.0091, | 0.0009, | 0.0109, | 0.0310, | 0.0510, | 0.1010, |
| | 2.600e- | 2.650e- | 2.670e- | 2.700e- 02, 0.0273 | 2.710e- | 2.730e- | 2.760e- | 2.790e- | 2.880e- |
| | 02, 0.0264 | 02, 0.0269 | 02, 0.0271 | 02, 0.0273 | 02, 0.0275 | 02, 0.0276 | 02, 0.0279 | 02, 0.0282 | 02, 0.02 |
| cML-BIC-Profile | 0.960, | 0.464, -0.0491, | 0.197, -0.0291, | 0.054, -0.0091, | 0.039, 0.0009, | 0.054, 0.0109, | 0.207, | 0.455, 0.0510, | 0.937, |
| | -0.0991, 2.600e- | 2.650e- | 2.670e- | 2.700e- | 2.710e- | 2.730e- | 0.0310, 2.760e- | 2.790e- | 0.1010, 2.880e- |
| | 02, 0.0265 | 02, 0.0269 | 02, 0.0272 | 02, 0.0274 | 02, 0.0275 | 02, 0.0277 | 02, 0.0279 | 02, 0.0282 | 02, 0.02 |
| MR-Mix | 0.929, | 0.395, | 0.161, | 0.047, | 0.027, | 0.046, | 0.171, | 0.388, | 0.886, |
| | -0.1019, | -0.0491, | -0.0287, | -0.0086, | 0.0013, | 0.0111, | 0.0302, | 0.0494, | 0.0951, |
| | 2.770e- 02, 0.031 | 2.770e- 02, 0.0301 | 2.780e- 02, 0.0301 | 2.790e- 02, 0.0303 | 2.790e- 02, 0.0304 | 2.800e- 02, 0.0306 | 2.810e- 02, 0.0304 | 2.810e- 02, 0.0303 | 2.830e- 02, 0.03 |
| MR-ContMix | 0.955, | 0.507, | 0.244, | 0.091, | 0.071, | 0.081, | 0.252, | 0.494, | 0.937, |
| WIN COMMIN | -0.0989, | -0.0489, | -0.0290, | -0.0090, | 0.0010, | 0.0110, | 0.0310, | 0.0510, | 0.1010, |
| | 2.750e- | 2.770e- | 2.790e- | 2.820e- | 2.830e- | 2.850e- | 2.870e- | 2.910e- | 3.000e- |
| 1 m 1 | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA |
| MR-Lasso | 0.888, -0.0570, | 0.461, -0.0077, | 0.264, 0.0119, | 0.169, 0.0320, | 0.155, 0.0421, | 0.164, 0.0521, | 0.258, 0.0717, | 0.435, 0.0917, | 0.826, 0.1416, |
| | 3.792e- | 3.800e- | 3.795e- | 3.792e- | 3.791e- | 3.791e- | 3.789e- | 3.785e- | 3.787e- |
| | 01, 0.0598 | 01, 0.06 | 01, 0.0604 | 01, 0.0604 | 01, 0.0606 | 01, 0.0607 | 01, 0.0609 | 01, 0.0611 | 01, 0.06 |
| MR-PRESSO | 0.207, | 0.121, | 0.097, | 0.081, | 0.085, | 0.088, | 0.105, | 0.135, | 0.226, |
| | -0.0344, | 0.0164, | 0.0366, | 0.0569, | 0.0671, | 0.0769, | 0.0968, | 0.1170, | 0.1662, |
| | 4.203e- 01, 0.2848 | 4.200e- 01, 0.2828 | 4.199e- 01, 0.282 | 4.197e- 01, 0.2805 | 4.195e- 01, 0.2798 | 4.195e- 01, 0.2792 | 4.194e- 01, 0.278 | 4.195e- 01, 0.2769 | 4.195e- 01, 0.27 |
| MR-IVW | 0.105, | 0.099, | 0.099, | 0.102, | 0.105, | 0.106, | 0.108, | 0.111, | 0.116, |
| | -0.0360, | 0.0145, | 0.0346, | 0.0548, | 0.0649, | 0.0750, | 0.0951, | 0.1152, | 0.1655, |
| | 4.230e- | 4.229e- | 4.229e- | 4.229e- | 4.229e- | 4.229e- | 4.228e- | 4.228e- | 4.228e- |
| 100 00000 | 01, 0.3961 | 01, 0.3961 | 01, 0.3961 | 01, 0.396 | 01, 0.396 | 01, 0.396 | 01, 0.396 | 01, 0.396 | 01, 0.39 |
| MR-IVW-Oracle | 0.915, -0.0989, | 0.381, -0.0489, | 0.152, -0.0290, | 0.043, -0.0090, | 0.028, 0.0010, | 0.040, 0.0110, | 0.162, 0.0310, | 0.385, 0.0509, | 0.886, 0.1009, |
| | 2.580e- | 2.630e- | 2.660e- | 2.680e- | 2.700e- | 2.710e- | 2.740e- | 2.770e- | 2.860e- |
| | 02, 0.0297 | 02, 0.0302 | 02, 0.0305 | 02, 0.0307 | 02, 0.0309 | 02, 0.031 | 02, 0.0313 | 02, 0.0316 | 02, 0.03 |
| MR-Egger | 0.164, | 0.172, | 0.172, | 0.174, | 0.175, | 0.174, | 0.175, | 0.183, | 0.189, |
| | 0.5210, | 0.5700, | 0.5896, | 0.6092, | 0.6190, | 0.6287, | 0.6483, | 0.6679, | 0.7167, |
| | 1.514e+00, 1.282 | 1.514e+00, 1.282 | 1.514e+00, 1.282 | 1.514e+00, 1.282 | 1.514e+00, 1.282 | 1.514e+00, 1.282 | 1.514e+00, 1.282 | 1.514e+00, 1.282 | 1.513e+ 1.282 |
| //R-Weighted-Median | 0.842, | 0.426, | 0.260, | 0.167, | 0.151, | 0.153, | 0.206, | 0.328, | 0.714, |
| | -0.1081, | -0.0644, | -0.0473, | -0.0301, | -0.0216, | -0.0131, | 0.0035, | 0.0200, | 0.0613, |
| | 1.070e- | 1.095e- | 1.104e- | 1.124e- | 1.134e- | 1.150e- | 1.183e- | 1.221e- | 1.327e- |
| MD Welster J Medi | 01, 0.0363 | 01, 0.037 | 01, 0.0372 | 01, 0.0376 | 01, 0.0377 | 01, 0.0379 | 01, 0.0382 | 01, 0.0386 | 01, 0.03 |
| MR-Weighted-Mode | 0.807, -0.1414, | 0.760, -0.1037, | 0.750, -0.0886, | 0.745, -0.0738, | 0.739, -0.0660, | 0.729, -0.0590, | 0.731, -0.0460, | 0.733, -0.0311, | 0.724, 0.0032, |
| | 2.083e- | 2.086e- | 2.099e- | 2.106e- | 2.117e- | 2.130e- | 2.107e- | 2.122e- | 2.169e- |
| | 01, 0.0364 | 01, 0.0368 | 01, 0.0371 | 01, 0.0375 | 01, 0.0376 | 01, 0.038 | 01, 0.0383 | 01, 0.039 | 01, 0.04 |
| MR-RAPS1 | 0.105, | 0.115, | 0.116, | 0.116, | 0.120, | 0.119, | 0.118, | 0.119, | 0.131, |
| | -0.0345, | 0.0156, | 0.0356, | 0.0556, | 0.0656, | 0.0756, | 0.0957, | 0.1157, | 0.1657, |
| | 4.127e- 01, 0.3761 | 4.128e- 01, 0.3761 | 4.128e- 01, 0.3761 | 4.128e- 01, 0.376 | 4.128e- 01, 0.376 | 4.128e- 01, 0.376 | 4.129e- 01, 0.376 | 4.129e- 01, 0.376 | 4.129e- 01, 0.37 |
| MR-RAPS2 | 0.175, | 0.165, | 0.166, | 0.162, | 0.155, | 0.151, | 0.154, | 0.138, | 0.143, |
| | -0.0739, | -0.0255, | -0.0044, | 0.0230, | 0.0331, | 0.0370, | 0.0575, | 0.0872, | 0.1348, |
| | 4.584e- | 4.459e- | 4.529e- | 4.746e- | 4.536e- | 4.456e- | 4.658e- | 4.503e- | 4.528e- |
| MD DARGO | 01, 0.3739 | 01, 0.3791 | 01, 0.3781 | 01, 0.3808 | 01, 0.3814 | 01, 0.3816 | 01, 0.3823 | 01, 0.3849 | 01, 0.38 |
| MR-RAPS3 | 0.925, -1.4125, | 0.930, -1.5231, | 0.931, -19.4827, | 0.937, 1.1305, | 0.934, - 344.3808, | 0.931, 0.2234, | 0.931, -0.7363, | 0.932, 0.4207, | 0.931, 1.2562, |
| | 5.300e+01, | 7.782e+01, | 7.148e+02, | 1.1305, 1.432e+02, | 1.077e+04, | 0.2234, 2.287e+01, | -0.7363, 4.346e+01, | 0.4207, 2.871e+01, | 1.2362, 2.377e+ |
| | 120.8 | 137.5 | 11950 | 535.1 | 3045000 | 14.1 | 577 | 29.4 | 15.51 |
| MR-RAPS4 | 0.977, | 0.969, | 0.967, | 0.973, | 0.973, | 0.967, | 0.980, | 0.977, | 0.976, |
| | -0.5602, | -0.1700, 6.251e+00, | -0.2526, 5.066e+00, | 0.5137, 2.408e+01, | -0.1766, 4.869e+00, | -0.1216, 4.848e+00, | -0.0620, 4.982e+00, | -0.0546, 4.927e+00, | -0.0612 7.837e+ |
| | 7.266e+00, | | | | | | | | |

Table S46: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE violated, q=0.6, and N=200000.

| | . , | | | | | | | | |
|--------------------|-----------------------|------------------------|------------------------|-----------------------|---------------------|---------------------|------------------------|---------------------|---------------------|
| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.927, | 0.417, | 0.132, | 0.027, | 0.016, | 0.024, | 0.121, | 0.369, | 0.903, |
| CNIL-MA-AIC | -0.0895, | -0.0400, | -0.0220, | -0.0069, | -0.0002, | 0.024, | 0.121, 0.0220, | 0.0400, | 0.903, |
| | 0.0228, | 0.0221, | 0.0220, | 0.0180, | 0.0176, | 0.0178, | 0.0201, | 0.0224, | 0.0241, |
| | 0.0239 | 0.0242 | 0.0242 | 0.0239 | 0.0239 | 0.024 | 0.0246 | 0.0251 | 0.0259 |
| cML-MA-AIC-Profile | 0.926, | 0.412, | 0.132, | 0.026, | 0.016, | 0.023, | 0.120, | 0.367, | 0.903, |
| | -0.0896, | -0.0399, | -0.0220, | -0.0069, | -0.0003, | 0.0066, | 0.0220, | 0.0400, | 0.0890, |
| | 0.0228, | 0.0221, | 0.0203, | 0.0180, | 0.0176, | 0.0178, | 0.0201, | 0.0224, | 0.0241, |
| cML-AIC | 0.0239 0.941, | 0.0243 0.609, | 0.0242 0.264, | 0.024 | 0.0239 0.061, | 0.0241 0.083, | 0.0247 0.240, | 0.0252 0.558, | 0.026 0.925, |
| CIVIL-AIC | -0.0922, | -0.0426, | -0.0240, | -0.0080, | -0.0004, | 0.0075, | 0.0240, | 0.0428, | 0.923, |
| | 0.0257, | 0.0253, | 0.0240, | 0.0222, | 0.0218, | 0.0219, | 0.0237, | 0.0254, | 0.0268, |
| | 0.0203 | 0.0207 | 0.0208 | 0.0209 | 0.021 | 0.0211 | 0.0213 | 0.0215 | 0.0221 |
| cML-AIC-Profile | 0.941, | 0.608, | 0.265, | 0.068, | 0.060, | 0.083, | 0.239, | 0.558, | 0.925, |
| | -0.0922, | -0.0426, | -0.0241, | -0.0080, | -0.0004, | 0.0075, | 0.0241, | 0.0428, | 0.0921, |
| | 0.0257, | 0.0253, | 0.0242, | 0.0222, | 0.0218, | 0.0219, | 0.0237, | 0.0254, | 0.0268, |
| cML-MA-BIC | 0.0203 | 0.0207 0.748, | 0.0208 | 0.021 0.076, | 0.021 | 0.0211 | 0.0213 0.325, | 0.0216 | 0.0222 |
| CIVIL-IVIA-DIC | 0.998, -0.0999, | -0.0499, | 0.334, -0.0299, | -0.0100, | -0.0001, | 0.079, | 0.323, 0.0298, | 0.709, 0.0498, | 0.997, |
| | 0.0187, | 0.0190, | 0.0191, | 0.0192, | 0.0193, | 0.0093, | 0.0196, | 0.0498, | 0.0203, |
| | 0.0189 | 0.0192 | 0.0194 | 0.0196 | 0.0197 | 0.0197 | 0.0199 | 0.0202 | 0.0207 |
| cML-MA-BIC-Profile | 0.997, | 0.748, | 0.334, | 0.076, | 0.048, | 0.079, | 0.324, | 0.709, | 0.996, |
| | -0.0999, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0504, | 0.1008, |
| | 0.0187, | 0.0191, | 0.0195, | 0.0201, | 0.0207, | 0.0215, | 0.0239, | 0.0272, | 0.0379, |
| 10.010 | 0.0189 | 0.0193 | 0.0196 | 0.0199 | 0.0201 | 0.0202 | 0.0206 | 0.0209 | 0.0214 |
| cML-BIC | 0.998, | 0.756, | 0.347, | 0.079, -0.0100, | 0.051, | 0.086, 0.0100, | 0.335, 0.0300, | 0.714, | 0.998, 0.1000, |
| | -0.1001, 0.0187, | -0.0501, 0.0189, | -0.0301, 0.0191, | -0.0100, 0.0193, | 0.0000, 0.0194, | 0.0100, 0.0195, | 0.0300, 0.0196, | 0.0500, 0.0198, | 0.1000, 0.0204, |
| | 0.0187, | 0.0189, | 0.0191, | 0.0193, | 0.0194, | 0.0193, | 0.0196, | 0.0198, | 0.0204, |
| cML-BIC-Profile | 0.998, | 0.755, | 0.348, | 0.079, | 0.050, | 0.086, | 0.334, | 0.714, | 0.998, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1016, |
| | 0.0187, | 0.0189, | 0.0191, | 0.0193, | 0.0194, | 0.0195, | 0.0196, | 0.0198, | 0.0527, |
| | 0.0187 | 0.0191 | 0.0192 | 0.0194 | 0.0195 | 0.0196 | 0.0198 | 0.02 | 0.0206 |
| MR-Mix | 0.997, | 0.667, | 0.271, | 0.064, | 0.049, | 0.066, | 0.263, | 0.646, | 0.989, |
| | -0.1032, | -0.0503, | -0.0300, | -0.0099, | 0.0000, | 0.0099, | 0.0293, | 0.0483, | 0.0939, |
| | 0.0200, 0.0218 | 0.0199, 0.0217 | 0.0199, 0.0216 | 0.0201, 0.0217 | 0.0200, 0.0217 | 0.0201, 0.0217 | 0.0199, 0.0218 | 0.0200, 0.0219 | 0.0205, 0.0223 |
| MR-ContMix | 0.0218 | 0.789, | 0.0210 | 0.0217 | 0.0217 | 0.0217 | 0.397, | 0.0219 | 0.0223 |
| WIK COMMIX | -0.1001, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0192, | 0.0195, | 0.0196, | 0.0198, | 0.0198, | 0.0199, | 0.0200, | 0.0202, | 0.0208, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.967, | 0.695, | 0.355, | 0.179, | 0.153, | 0.171, | 0.328, | 0.639, | 0.927, |
| | -0.0560, | -0.0055, | 0.0154, | 0.0358, | 0.0457, | 0.0560, | 0.0756, | 0.0955, | 0.1466, |
| | 0.3638, 0.0485 | 0.3633, 0.0487 | 0.3634, 0.0493 | 0.3634, 0.0493 | 0.3630, 0.0494 | 0.3633, 0.0494 | 0.3635, 0.0498 | 0.3635, 0.0501 | 0.3633, 0.0506 |
| MR-PRESSO | 0.0483 | 0.122, | 0.0493 | 0.0493 | 0.0494 | 0.076, | 0.108, | 0.0501 | 0.0300 |
| WIK-I KESSO | -0.0300, | 0.0206, | 0.0407, | 0.0604, | 0.0704, | 0.0806, | 0.1008, | 0.132, | 0.1706, |
| | 0.4156, | 0.4155, | 0.4155, | 0.4155, | 0.4155, | 0.4154, | 0.4154, | 0.4154, | 0.4152, |
| | 0.3195 | 0.3188 | 0.3177 | 0.3164 | 0.3164 | 0.3161 | 0.3158 | 0.3151 | 0.3123 |
| MR-IVW | 0.091, | 0.093, | 0.091, | 0.091, | 0.092, | 0.094, | 0.095, | 0.100, | 0.116, |
| | -0.0309, | 0.0196, | 0.0397, | 0.0599, | 0.0700, | 0.0801, | 0.1002, | 0.1204, | 0.1707, |
| | 0.4167, | 0.4167, | 0.4166, | 0.4166, | 0.4166, | 0.4166, | 0.4166, | 0.4166, | 0.4165, |
| MR-IVW-Oracle | 0.4016 0.992, | 0.4016 0.668, | 0.4016 0.274, | 0.4016 0.060, | 0.4015 0.042, | 0.4015 0.069, | 0.4015 0.258, | 0.4015 0.630, | 0.4015 0.986, |
| WIK-IV W-Oracie | -0.1000, | -0.0500, | -0.0300, | -0.0100, | -0.0001, | 0.009, | 0.238, 0.0299, | 0.030, | 0.986, |
| | 0.0187, | 0.0189, | 0.0191, | 0.0192, | 0.0193, | 0.0194, | 0.0196, | 0.0197, | 0.0203, |
| | 0.0211 | 0.0215 | 0.0217 | 0.0219 | 0.022 | 0.0221 | 0.0224 | 0.0226 | 0.0232 |
| MR-Egger | 0.209, | 0.215, | 0.217, | 0.218, | 0.220, | 0.220, | 0.219, | 0.221, | 0.229, |
| | 0.7085, | 0.7579, | 0.7777, | 0.7974, | 0.8073, | 0.8171, | 0.8369, | 0.8566, | 0.9059, |
| | 1.6364, | 1.6364, | 1.6365, | 1.6365, | 1.6365, | 1.6365, | 1.6365, | 1.6366, | 1.6366, |
| MD Waighted Medico | 1.2704 0.948, | 1.2704 0.633, | 1.2704 0.375, | 1.2704 0.189, | 1.2704 0.154, | 1.2704 0.178, | 1.2704 0.292, | 1.2704 0.515, | 1.2704 0.848, |
| MR-Weighted-Median | -0.1024, | -0.0589, | -0.0415, | -0.0241, | -0.0155, | -0.0067, | 0.292, 0.0106, | 0.515, 0.0275, | 0.848, 0.0697, |
| | 0.1330, | 0.1344, | 0.1356, | 0.1370, | 0.1379, | 0.1387, | 0.1409, | 0.0275, | 0.1512, |
| | 0.0275 | 0.0277 | 0.0279 | 0.0281 | 0.0282 | 0.0284 | 0.0287 | 0.0289 | 0.0297 |
| MR-Weighted-Mode | 0.872, | 0.831, | 0.823, | 0.817, | 0.822, | 0.821, | 0.815, | 0.816, | 0.804, |
| | -0.1220, | -0.0855, | -0.0708, | -0.0560, | -0.0485, | -0.0416, | -0.0267, | -0.0119, | 0.0238, |
| | 0.2271, | 0.2311, | 0.2335, | 0.2350, | 0.2361, | 0.2379, | 0.2390, | 0.2415, | 0.2505, |
| MD D i Dor | 0.0257 | 0.0257 | 0.0258 | 0.0261 | 0.0263 | 0.0264 | 0.0264 | 0.0266 | 0.027 |
| MR-RAPS1 | 0.105, | 0.107, -1.5332, | 0.109, | 0.106, 0.0648, | 0.104, | 0.102, | 0.108, 0.1075, | 0.111, | 0.125, |
| | -0.2502, 8.2147, | -1.5552, 44.5248, | 0.1187, 3.3341, | 2.2694, | 0.0459, 2.4359, | 0.0153, 3.1656, | 1.2322, | 0.1199, 1.3024, | 0.1771, 0.7752, |
| | 1.3504 | 22.2417 | 0.4994 | 0.4349 | 0.4454 | 0.4957 | 0.3949 | 0.4015 | 0.3858 |
| MR-RAPS2 | 0.281, | 0.240, | 0.233, | 0.198, | 0.188, | 0.187, | 0.180, | 0.171, | 0.174, |
| | -0.0856, | -0.0360, | -0.0273, | -0.0010, | 0.0019, | 0.0129, | 0.0209, | 0.0543, | 0.1114, |
| | 0.4947, | 0.4766, | 0.4684, | 0.4759, | 0.4607, | 0.4854, | 0.7618, | 0.4452, | 0.4689, |
| | 0.2646 | 0.2679 | 0.2643 | 0.2757 | 0.2742 | 0.2731 | 0.2786 | 0.2824 | 0.2928 |
| MR-RAPS3 | 0.948, | 0.944, | 0.946, | 0.944, | 0.946, | 0.948, | 0.949, | 0.950, | 0.947, |
| | -3.9798, | 27.6247, | -2.8912, | -5.1822, | 1.0330, | -0.5791, 57.5046 | -15.4647, 752.0266 | 0.1444, | -1.0000, 28.1072 |
| | 133.1913, 265.2621 | 703.6228, 8354.1716 | 149.4389, 3683.3129 | 141.8313, 587.2076 | 56.3390, 57.5573 | 57.5046, 67.6878 | 752.9266, 8713.9481 | 36.8795, 25.6024 | 38.1072, 57.7633 |
| MR-RAPS4 | 0.989, | 0.976, | 0.969, | 0.973, | 0.980, | 0.981, | 0.975, | 0.975, | 1.000, |
| | | | 0.1306, | 0.1374, | 0.1847, | 0.1272, | 0.3318, | 0.1738, | 0.2699, |
| | 0.0094. | 0.0977. | 0.1300. | 0.1374. | 0.1047. | 0.1272. | | | |
| MICRO I | 0.0094, 3.2157, | 0.0977, 3.3890, | 3.4094, | 4.1508, | 4.3370, | 4.2599, | 8.0901, | 4.1473, | 0.2967, |

Table S47: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the ideal case of q=0, and N=50000.

| | <u> </u> | | | | . , | 1 | | 1 | 1 |
|----------------------|---|---|--|--|--|---|---|---|---|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.969, | 0.559, | 0.239, | 0.054, | 0.046, | 0.071, | 0.244, | 0.518, | 0.957, |
| | -0.0915, | -0.0424, | -0.0240, | -0.0070, | 0.0010, | 0.0089, | 0.0256, | 0.0436, | 0.0921, |
| | 0.0221, | 0.0217, | 0.0206, | 0.0192, | 0.0190, | 0.0194, | 0.0210, | 0.0228, | 0.0248, |
| | 0.0201 | 0.0203 | 0.0202 | 0.0201 | 0.0202 | 0.0204 | 0.0208 | 0.0213 | 0.0223 |
| cML-MA-AIC-Profile | 0.969, | 0.554, | 0.238, | 0.053, | 0.045, | 0.070, | 0.241, | 0.517, | 0.957, |
| | -0.0918, | -0.0425, | -0.0240, | -0.0070, | 0.0010, | 0.0089, | 0.0256, | 0.0436, | 0.0924, |
| | 0.0223, | 0.0217, | 0.0206, | 0.0192, | 0.0190, | 0.0194, | 0.0210, | 0.0228, | 0.0249, |
| | 0.0203 | 0.0204 | 0.0203 | 0.0202 | 0.0203 | 0.0205 | 0.0209 | 0.0215 | 0.0224 |
| cML-AIC | 0.990, | 0.699, | 0.380, | 0.146, | 0.117, | 0.152, | 0.389, | 0.672, | 0.987, |
| | -0.0954, | -0.0458, | -0.0265, | -0.0079, | 0.0011, | 0.0101, | 0.0284, | 0.0474, | 0.0968, |
| | 0.0237, | 0.0240, | 0.0235, | 0.0230, | 0.0231, | 0.0233, | 0.0238, | 0.0248, | 0.0258, |
| -MI AIC D. GI | 0.0174 | 0.0177 | 0.0178 | 0.018 | 0.0181 | 0.0182 | 0.0184 | 0.0186 | 0.0191 |
| cML-AIC-Profile | 0.989, -0.0958, | 0.696, -0.0459, | 0.376, | 0.141, -0.0079, | 0.114, 0.0011, | 0.149, 0.0101, | 0.386, 0.0284, | 0.666, | 0.987, 0.0969, |
| | 0.0239, | 0.0240, | -0.0265, 0.0236, | 0.0230, | 0.0011, | 0.0101, | 0.0284, 0.0238, | 0.0475, 0.0248, | 0.0969, |
| | 0.0239, | 0.0240, | 0.0230, | 0.0230, | 0.0231, | 0.0233, | 0.0238, | 0.0248, | 0.0239, |
| cML-MA-BIC | 1.000, | 0.855, | 0.430, | 0.090, | 0.052, | 0.097, | 0.417, | 0.831, | 1.000, |
| CHIL HIT DIC | -0.0995, | -0.0496, | -0.0296, | -0.0097, | 0.0003, | 0.0102, | 0.0301, | 0.0501, | 0.1000, |
| | 0.0162, | 0.0165, | 0.0167, | 0.0168, | 0.0169, | 0.0170, | 0.0172, | 0.0174, | 0.0180, |
| | 0.0161 | 0.0164 | 0.0166 | 0.0167 | 0.0168 | 0.0169 | 0.0171 | 0.0173 | 0.0178 |
| cML-MA-BIC-Profile | 1.000, | 0.854, | 0.426, | 0.088, | 0.049, | 0.094, | 0.414, | 0.831, | 1.000, |
| | -0.0996, | -0.0496, | -0.0296, | -0.0097, | 0.0003, | 0.0102, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0162, | 0.0165, | 0.0167, | 0.0168, | 0.0169, | 0.0170, | 0.0172, | 0.0174, | 0.0180, |
| | 0.0162 | 0.0165 | 0.0166 | 0.0168 | 0.0169 | 0.017 | 0.0171 | 0.0173 | 0.0179 |
| cML-BIC | 1.000, | 0.862, | 0.443, | 0.097, | 0.057, | 0.101, | 0.433, | 0.840, | 1.000, |
| | -0.0996, | -0.0497, | -0.0297, | -0.0097, | 0.0002, | 0.0102, | 0.0302, | 0.0502, | 0.1001, |
| | 0.0162, | 0.0165, | 0.0166, | 0.0168, | 0.0169, | 0.0170, | 0.0172, | 0.0174, | 0.0180, |
| | 0.0159 | 0.0162 | 0.0164 | 0.0165 | 0.0166 | 0.0167 | 0.0169 | 0.0171 | 0.0176 |
| cML-BIC-Profile | 1.000, | 0.861, | 0.442, | 0.095, | 0.054, | 0.099, | 0.432, | 0.838, | 1.000, |
| | -0.0996, | -0.0497, | -0.0297, | -0.0097, | 0.0002, | 0.0102, | 0.0302, | 0.0502, | 0.1001, |
| | 0.0162, | 0.0165, | 0.0166, | 0.0168, | 0.0169, | 0.0170, | 0.0172, | 0.0174, | 0.0180, |
| | 0.016 | 0.0163 | 0.0164 | 0.0166 | 0.0167 | 0.0167 | 0.0169 | 0.0171 | 0.0176 |
| MR-Mix | 0.751, | 0.540, | 0.263, | 0.075, | 0.065, | 0.072, | 0.242, | 0.501, | 0.728, |
| | -0.0990, | -0.0484, | -0.0289, | -0.0095, | -0.0001, | 0.0094, | 0.0281, | 0.0461, | 0.0901, |
| | 0.0417, | 0.0315, | 0.0294, | 0.0284, | 0.0284, | 0.0283, | 0.0295, | 0.0312, | 0.0387, |
| 1 m a 1 m | 0.1318 | 0.2585 | 0.1924 | 0.1854 | 0.0845 | 0.1963 | 0.0754 | 0.2309 | 0.0609 |
| MR-ContMix | 0.996, | 0.714, | 0.360, | 0.104, | 0.092, | 0.114, | 0.376, | 0.673, | 0.996, |
| | -0.1212, | -0.0681, | -0.0426, | -0.0138, | 0.0009, | 0.0155, | 0.0445, | 0.0697, | 0.1237, |
| | 0.0233, | 0.0296, | 0.0331, | 0.0363, | 0.0367, | 0.0360, NA | 0.0331, | 0.0304, | 0.0257, |
| MR-Lasso | NA 1.000, | NA 0.824, | NA 0.412, | NA 0.098, | NA 0.062, | 0.103, | NA 0.401, | NA 0.790, | NA 1.000, |
| WIK-Lasso | -0.0991, | -0.0495, | -0.0295, | -0.0098, | 0.002, | 0.103, | 0.401, | 0.750, | 0.0996, |
| | 0.0171, | 0.0178, | 0.0179, | 0.0180, | 0.0002, | 0.0103, | 0.0297, | 0.0300, | 0.0390, |
| | 0.0171, | 0.0169 | 0.0171 | 0.0172 | 0.0173 | 0.0174 | 0.0175 | 0.0177 | 0.0183 |
| MR-PRESSO | 1.000, | 0.823, | 0.411, | 0.095, | 0.062, | 0.089, | 0.395, | 0.794, | 1.000, |
| mit i italooo | -0.0991, | -0.0494, | -0.0296, | -0.0097, | 0.0002, | 0.0101, | 0.0300, | 0.0499, | 0.0995, |
| | 0.0161, | 0.0164, | 0.0166, | 0.0168, | 0.0168, | 0.0169, | 0.0171, | 0.0173, | 0.0179, |
| | 0.0156 | 0.0159 | 0.016 | 0.0162 | 0.0163 | 0.0163 | 0.0165 | 0.0167 | 0.0172 |
| MR-IVW | 1.000, | 0.831, | 0.402, | 0.082, | 0.046, | 0.085, | 0.387, | 0.804, | 1.000, |
| | -0.0991, | -0.0495, | -0.0296, | -0.0098, | 0.0002, | 0.0101, | 0.0300, | 0.0498, | 0.0995, |
| | 0.0161, | 0.0164, | 0.0166, | 0.0167, | 0.0168, | 0.0169, | 0.0171, | 0.0173, | 0.0179, |
| | 0.0167 | 0.0171 | 0.0172 | 0.0174 | 0.0175 | 0.0176 | 0.0178 | 0.018 | 0.0185 |
| MR-IVW-Oracle | 1.000, | 0.831, | 0.402, | 0.082, | 0.046, | 0.085, | 0.387, | 0.804, | 1.000, |
| | -0.0991, | -0.0495, | -0.0296, | -0.0098, | 0.0002, | 0.0101, | 0.0300, | 0.0498, | 0.0995, |
| | 0.0161, | 0.0164, | 0.0166, | 0.0167, | 0.0168, | 0.0169, | 0.0171, | 0.0173, | 0.0179, |
| | 0.0167 | 0.0171 | 0.0172 | 0.0174 | 0.0175 | 0.0176 | 0.0178 | 0.018 | 0.0185 |
| MR-Egger | 0.183, | 0.061, | 0.041, | 0.037, | 0.039, | 0.039, | 0.052, | 0.067, | 0.134, |
| | -0.0863, | -0.0433, | -0.0261, | -0.0090, | -0.0004, | 0.0082, | 0.0254, | 0.0426, | 0.0855, |
| | 0.0826, | 0.0840, | 0.0847, | 0.0855, | 0.0859, | 0.0863, | 0.0871, | 0.0880, | 0.0905, |
| MD Wainht-1 M. 1. | 0.086 | 0.0878 | 0.0886 | 0.0895 | 0.0899 | 0.0904 | 0.0914 | 0.0924 | 0.095 |
| MR-Weighted-Median | 0.997, | 0.555, | 0.210, | 0.031, | 0.025, | 0.050, | 0.205, | 0.564, | 0.994, |
| | -0.0969, 0.0192, | -0.0481, 0.0195, | -0.0286, 0.0197, | -0.0090, 0.0199, | 0.0008, 0.0199, | 0.0106, 0.0201, | 0.0302, 0.0203, | 0.0498, 0.0205, | 0.0985, |
| | 0.0192, | 0.0195, | 0.0197, | 0.0199, | 0.0199, | 0.0201, | 0.0203, | 0.0205, | 0.0210, 0.0247 |
| MR-Weighted-Mode | 0.0225 | 0.0229 | 0.0231 | 0.0233 | 0.0234 | 0.0235 | 0.0237 | 0.024 | 0.0247 |
| 1711X- Weighted-Word | -0.0960, | -0.0469, | -0.0272, | -0.007, | 0.000, | 0.010, | 0.030, | 0.203, | 0.720, |
| | 0.0287, | 0.0293, | 0.0272, | 0.0298, | 0.0020, | 0.0118, | 0.0310, | 0.0306, | 0.0991, |
| | 0.0237, | 0.0253, | 0.0293, | 0.0298, | 0.0386 | 0.0388 | 0.0392 | 0.0397 | 0.0408 |
| MR-RAPS1 | 1.000, | 0.838, | 0.415, | 0.0364 | 0.051, | 0.0388 | 0.392, | 0.808, | 1.000, |
| | -0.0996, | -0.0497, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0301, | 0.0501, | 0.1000, |
| | 0.0161, | 0.0165, | 0.0166, | 0.0168, | 0.0169, | 0.0170, | 0.0172, | 0.0174, | 0.0180, |
| | | 0.017 | 0.0171 | 0.0173 | 0.0174 | 0.0175 | 0.0177 | 0.0179 | 0.0184 |
| I | 0.0167 | 1 | 0.412, | 0.104, | 0.061, | 0.096, | 0.391, | 0.792, | 1.000, |
| MR-RAPS2 | 0.0167 1.000, | 0.828, | | | 0.0310, | 0.0627, | 0.0225, | 0.1562, | 0.2590, |
| MR-RAPS2 | 1.000, | 0.828, 0.0252, | -0.0232, | 0.0619, | | | | | |
| MR-RAPS2 | | | -0.0232, 4.4364, | 1.9884, | 2.0792, | 2.2456, | 4.1872, | 4.7615, | 4.6551, |
| MR-RAPS2 | 1.000, -0.1574, | 0.0252, | | | | 2.2456, 0.0275 | 4.1872, 0.0417 | 4.7615, 0.0565 | 4.6551, 0.0613 |
| MR-RAPS2 MR-RAPS3 | 1.000, -0.1574, 4.1595, | 0.0252, 4.4121, | 4.4364, | 1.9884, | 2.0792, | | | | |
| | 1.000, -0.1574, 4.1595, 0.0565 | 0.0252, 4.4121, 0.0556 | 4.4364, 0.0418 | 1.9884, 0.0269 | 2.0792, 0.0254 | 0.0275 | 0.0417 | 0.0565 | 0.0613 |
| | 1.000, -0.1574, 4.1595, 0.0565 1.000, | 0.0252, 4.4121, 0.0556 0.860, -0.0498, 0.0165, | 4.4364, 0.0418 0.443, -0.0298, 0.0167, | 1.9884, 0.0269 0.099, -0.0098, 0.0168, | 2.0792, 0.0254 0.057, 0.0002, 0.0169, | 0.0275 0.100, | 0.0417 0.432, 0.0301, 0.0172, | 0.0565 0.837, | 0.0613 1.000, 0.1000, 0.0180, |
| MR-RAPS3 | 1.000, -0.1574, 4.1595, 0.0565 1.000, -0.0997, 0.0162, 0.016 | 0.0252, 4.4121, 0.0556 0.860, -0.0498, 0.0165, 0.0163 | 4.4364, 0.0418 0.443, -0.0298, 0.0167, 0.0164 | 1.9884, 0.0269 0.099, -0.0098, 0.0168, 0.0166 | 2.0792, 0.0254 0.057, 0.0002, 0.0169, 0.0166 | 0.0275 0.100, 0.0102, 0.0170, 0.0167 | 0.0417 0.432, 0.0301, 0.0172, 0.0169 | 0.0565 0.837, 0.0501, | 0.0613 1.000, 0.1000, 0.0180, 0.0176 |
| | 1.000, -0.1574, 4.1595, 0.0565 1.000, -0.0997, 0.0162, 0.016 1.000, | 0.0252, 4.4121, 0.0556 0.860, -0.0498, 0.0165, 0.0163 | 4.4364, 0.0418 0.443, -0.0298, 0.0167, 0.0164 0.418, | 1.9884, 0.0269 0.099, -0.0098, 0.0168, 0.0166 0.096, | 2.0792, 0.0254 0.057, 0.0002, 0.0169, 0.0166 0.053, | 0.0275 0.100, 0.0102, 0.0170, 0.0167 0.099, | 0.0417 0.432, 0.0301, 0.0172, 0.0169 0.412, | 0.0565 0.837, 0.0501, 0.0174, 0.0171 0.817, | 0.0613 1.000, 0.1000, 0.0180, 0.0176 1.000, |
| MR-RAPS3 | 1.000, -0.1574, 4.1595, 0.0565 1.000, -0.0997, 0.0162, 0.016 1.000, -0.0996, | 0.0252, 4.4121, 0.0556 0.860, -0.0498, 0.0165, 0.0163 0.848, -0.0497, | 4.4364, 0.0418 0.443, -0.0298, 0.0167, 0.0164 0.418, -0.0297, | 1.9884, 0.0269 0.099, -0.0098, 0.0168, 0.0166 0.096, -0.0097, | 2.0792, 0.0254 0.057, 0.0002, 0.0169, 0.0166 0.053, 0.0003, | 0.0275 0.100, 0.0102, 0.0170, 0.0167 0.099, 0.0103, | 0.0417 0.432, 0.0301, 0.0172, 0.0169 0.412, 0.0302, | 0.0565 0.837, 0.0501, 0.0174, 0.0171 0.817, 0.0502, | 0.0613 1.000, 0.1000, 0.0180, 0.0176 1.000, 0.1002, |
| MR-RAPS3 | 1.000, -0.1574, 4.1595, 0.0565 1.000, -0.0997, 0.0162, 0.016 1.000, | 0.0252, 4.4121, 0.0556 0.860, -0.0498, 0.0165, 0.0163 | 4.4364, 0.0418 0.443, -0.0298, 0.0167, 0.0164 0.418, | 1.9884, 0.0269 0.099, -0.0098, 0.0168, 0.0166 0.096, | 2.0792, 0.0254 0.057, 0.0002, 0.0169, 0.0166 0.053, | 0.0275 0.100, 0.0102, 0.0170, 0.0167 0.099, | 0.0417 0.432, 0.0301, 0.0172, 0.0169 0.412, | 0.0565 0.837, 0.0501, 0.0174, 0.0171 0.817, | 0.0613 1.000, 0.1000, 0.0180, 0.0176 1.000, |

Table S48: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the ideal case of q=0, and N=100000.

| | , , | | | | | | , | | |
|--------------------|------------------------------|------------------------------|------------------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|
| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| | | | | 0.054 | | | 0.006 | | |
| cML-MA-AIC | 0.998, | 0.823, | 0.419, | 0.074, | 0.039, | 0.080, | 0.386, | 0.795, | 0.996, |
| | -0.0942, 0.0155, | -0.0445, 0.0156, | -0.0252, 0.0149, | -0.0080, 0.0133, | -0.0001, 0.0129, | 0.0076, 0.0135, | 0.0250, 0.0154, | 0.0441, 0.0165, | 0.0936, 0.0173, |
| | 0.0133, | 0.0130, | 0.0149, | 0.0133, | 0.0129, | 0.0135, | 0.0134, | 0.0163, | 0.0173, |
| cML-MA-AIC-Profile | 0.998, | 0.822, | 0.420, | 0.075, | 0.039, | 0.080, | 0.385, | 0.796, | 0.996, |
| | -0.0945, | -0.0445, | -0.0253, | -0.0080, | -0.0001, | 0.0077, | 0.0250, | 0.0441, | 0.0938, |
| | 0.0155, | 0.0156, | 0.0149, | 0.0133, | 0.0129, | 0.0135, | 0.0155, | 0.0166, | 0.0173, |
| | 0.0145 | 0.0147 | 0.0146 | 0.0144 | 0.0144 | 0.0145 | 0.015 | 0.0153 | 0.0159 |
| cML-AIC | 1.000, | 0.901, | 0.580, | 0.162, | 0.104, | 0.163, | 0.535, | 0.874, | 1.000, |
| | -0.0972, 0.0167, | -0.0474, 0.0171, | -0.0277, 0.0166, | -0.0090, 0.0158, | 0.0000, 0.0157, | 0.0086, 0.0159, | 0.0270, 0.0172, | 0.0468, 0.0178, | 0.0967, 0.0183, |
| | 0.0107, | 0.0171, | 0.0100, | 0.0138, | 0.0137, | 0.0139, | 0.0172, | 0.0178, | 0.0185, |
| cML-AIC-Profile | 1.000, | 0.900, | 0.579, | 0.162, | 0.103, | 0.162, | 0.533, | 0.874, | 1.000, |
| | -0.0975, | -0.0475, | -0.0278, | -0.0090, | 0.0000, | 0.0086, | 0.0270, | 0.0468, | 0.0968, |
| | 0.0168, | 0.0172, | 0.0166, | 0.0158, | 0.0157, | 0.0159, | 0.0172, | 0.0178, | 0.0183, |
| | 0.0124 | 0.0126 | 0.0127 | 0.0129 | 0.0129 | 0.013 | 0.0131 | 0.0132 | 0.0137 |
| cML-MA-BIC | 1.000, | 0.993, | 0.739, | 0.129, | 0.039, | 0.114, | 0.686, | 0.983, | 1.000, |
| | -0.1001, 0.0110, | -0.0501, 0.0112, | -0.0301, | -0.0102, 0.0114, | -0.0002, 0.0114, | 0.0098, 0.0115, | 0.0298, 0.0116, | 0.0498, 0.0118, | 0.0997, 0.0121, |
| | 0.0110, | 0.0112, | 0.0113, 0.0117 | 0.0114, | 0.0114, | 0.0115, | 0.0116, | 0.0118, | 0.0121, |
| cML-MA-BIC-Profile | 1.000, | 0.993, | 0.738, | 0.129, | 0.038, | 0.113, | 0.683, | 0.983, | 1.000, |
| CHE HIT BIC Frome | -0.1001, | -0.0501, | -0.0301, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0110, | 0.0112, | 0.0113, | 0.0114, | 0.0114, | 0.0115, | 0.0116, | 0.0118, | 0.0121, |
| | 0.0114 | 0.0116 | 0.0117 | 0.0118 | 0.0119 | 0.012 | 0.0121 | 0.0122 | 0.0126 |
| cML-BIC | 1.000, | 0.992, | 0.748, | 0.134, | 0.039, | 0.116, | 0.696, | 0.983, | 1.000, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0110, | 0.0112, | 0.0113, | 0.0114, | 0.0115, | 0.0115, | 0.0117, | 0.0118, | 0.0122, |
| cML-BIC-Profile | 0.0113 1.000, | 0.0115 0.992, | 0.0116 0.748, | 0.0117 0.133, | 0.0118 | 0.0118 0.116, | 0.0119 0.694, | 0.0121 0.983, | 0.0124 1.000, |
| CIVIL-DIC-PTOILE | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.116, 0.0098, | 0.694, 0.0298, | 0.983, 0.0498, | 0.0998, |
| | 0.0110, | 0.0112, | 0.0113, | 0.0102, | 0.0115, | 0.0038, | 0.0238, | 0.0498, | 0.0338, |
| | 0.0113 | 0.0115 | 0.0116 | 0.0117 | 0.0118 | 0.0118 | 0.012 | 0.0121 | 0.0125 |
| MR-Mix | 0.791, | 0.656, | 0.440, | 0.089, | 0.050, | 0.090, | 0.428, | 0.647, | 0.763, |
| | -0.0984, | -0.0480, | -0.0285, | -0.0091, | 0.0004, | 0.0096, | 0.0282, | 0.0463, | 0.0901, |
| | 0.0371, | 0.0252, | 0.0220, | 0.0205, | 0.0202, | 0.0205, | 0.0222, | 0.0248, | 0.0342, |
| 1000 10 | 0.0869 | 0.0907 | 0.1039 | 0.058 | 0.0482 | 0.0588 | 0.0654 | 0.0866 | 0.066 |
| MR-ContMix | 1.000, | 0.923, | 0.596, | 0.145, | 0.085, | 0.131, | 0.546, | 0.905, | 1.000, |
| | -0.1146, 0.0152, | -0.0663, 0.0186, | -0.0433, 0.0217, | -0.0158, 0.0249, | -0.0004, 0.0255, | 0.0147, 0.0252, | 0.0425, 0.0220, | 0.0668, 0.0191, | 0.1168, 0.0161, |
| | 0.0132, NA | NA | 0.0217, NA | 0.0249, NA | 0.0255, NA | 0.0232, NA | NA | 0.0191, NA | NA |
| MR-Lasso | 1.000, | 0.985, | 0.697, | 0.135, | 0.047, | 0.133, | 0.654, | 0.974, | 1.000, |
| | -0.0998, | -0.0501, | -0.0300, | -0.0102, | -0.0001, | 0.0098, | 0.0297, | 0.0495, | 0.0996, |
| | 0.0120, | 0.0121, | 0.0122, | 0.0124, | 0.0124, | 0.0124, | 0.0126, | 0.0125, | 0.0130, |
| | 0.0118 | 0.012 | 0.0121 | 0.0122 | 0.0123 | 0.0124 | 0.0125 | 0.0126 | 0.013 |
| MR-PRESSO | 1.000, | 0.988, | 0.693, | 0.113, | 0.039, | 0.118, | 0.654, | 0.978, | 1.000, |
| | -0.0999, 0.0111, | -0.0501, 0.0113, | -0.0301, | -0.0102, 0.0114, | -0.0002, 0.0115, | 0.0098, 0.0115, | 0.0297, 0.0117, | 0.0496, | 0.0995, 0.0122, |
| | 0.0111, | 0.0113, | 0.0113, 0.0115 | 0.0114, | 0.0115, | 0.0115, | 0.0117, | 0.0118, 0.0119 | 0.0122, |
| MR-IVW | 1.000, | 0.988, | 0.694, | 0.108, | 0.032, | 0.100, | 0.654, | 0.977, | 1.000, |
| | -0.0999, | -0.0501, | -0.0301, | -0.0102, | -0.0002, | 0.0098, | 0.0297, | 0.0497, | 0.0995, |
| | 0.0110, | 0.0111, | 0.0112, | 0.0113, | 0.0114, | 0.0115, | 0.0116, | 0.0117, | 0.0121, |
| | 0.012 | 0.0122 | 0.0123 | 0.0124 | 0.0125 | 0.0126 | 0.0127 | 0.0128 | 0.0132 |
| MR-IVW-Oracle | 1.000, | 0.988, | 0.694, | 0.108, | 0.032, | 0.100, | 0.654, | 0.977, | 1.000, |
| | -0.0999, | -0.0501, | -0.0301, | -0.0102, | -0.0002, | 0.0098, | 0.0297, | 0.0497, | 0.0995, |
| | 0.0110, | 0.0111, | 0.0112, | 0.0113, | 0.0114, | 0.0115, | 0.0116, | 0.0117, | 0.0121, |
| MD Eggar | 0.012 | 0.0122 | 0.0123 0.067, | 0.0124 0.045, | 0.0125 0.045, | 0.0126 0.049, | 0.0127 | 0.0128 | 0.0132 0.284, |
| MR-Egger | 0.309, -0.0922, | 0.109, -0.0456, | -0.0270, | -0.0084, | 0.045, | 0.049, 0.0102, | 0.064, 0.0288, | 0.113, 0.0475, | 0.284, 0.0940, |
| | 0.0622, | 0.0633, | 0.0639, | 0.0645, | 0.0648, | 0.0651, | 0.0658, | 0.0665, | 0.0685, |
| | 0.0637 | 0.065 | 0.0656 | 0.0662 | 0.0665 | 0.0669 | 0.0675 | 0.0683 | 0.0702 |
| MR-Weighted-Median | 1.000, | 0.895, | 0.435, | 0.050, | 0.018, | 0.067, | 0.405, | 0.848, | 1.000, |
| | -0.0990, | -0.0495, | -0.0297, | -0.0100, | -0.0001, | 0.0098, | 0.0296, | 0.0494, | 0.0989, |
| | 0.0138, | 0.0140, | 0.0141, | 0.0142, | 0.0143, | 0.0144, | 0.0146, | 0.0148, | 0.0153, |
| MD Waisher J M. J | 0.016 | 0.0162 | 0.0164 | 0.0165 | 0.0166 | 0.0167 | 0.0169 | 0.0171 | 0.0176 |
| MR-Weighted-Mode | 0.973, -0.0990, | 0.456, -0.0494, | 0.131, -0.0298, | 0.015, -0.0099, | 0.005, 0.0000, | 0.012, 0.0099, | 0.121, 0.0297, | 0.429, 0.0493, | 0.942, 0.0985, |
| | 0.0207, | 0.0209, | 0.0298, | 0.0099, | 0.0000, | 0.0099, | 0.0297, 0.0217, | 0.0493, 0.0219, | 0.0985, |
| | 0.0267 | 0.0209, | 0.0210, | 0.0212, | 0.0213, | 0.0214, | 0.0217, | 0.0219, | 0.0220, |
| MR-RAPS1 | 1.000, | 0.989, | 0.709, | 0.114, | 0.033, | 0.101, | 0.661, | 0.978, | 1.000, |
| ** | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0997, |
| | 0.0110, | 0.0112, | 0.0113, | 0.0114, | 0.0114, | 0.0115, | 0.0116, | 0.0118, | 0.0121, |
| | 0.0119 | 0.0121 | 0.0122 | 0.0123 | 0.0124 | 0.0124 | 0.0126 | 0.0127 | 0.0131 |
| MR-RAPS2 | 1.000, | 0.986, | 0.698, | 0.128, | 0.046, | 0.131, | 0.653, | 0.974, | 1.000, |
| | 0.1615, | 0.0071, | 0.0861, 2.9466, | 0.0990, | -0.0036, | 0.1293, | 0.1774, | 0.1085, | 0.2511, |
| | 1.2017, 0.0237 | 2.4534, 0.0363 | 2.9466, 0.0348 | 1.5865, 0.0199 | 1.0167, 0.016 | 1.6882, 0.0217 | 2.6544, 0.0358 | 2.3809, 0.0362 | 1.7903, 0.0319 |
| MR-RAPS3 | 1.000, | 0.0363 | 0.0348 | 0.0199 | 0.016 | 0.0217 | 0.0338 | 0.0362 | 1.000, |
| MIX-IXAL 93 | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.116, | 0.099, | 0.983, | 0.0998, |
| | | | 0.0113, | 0.0114, | 0.0114, | 0.0115, | 0.0116, | 0.0118, | 0.0121, |
| | 0.0110, | 0.0112, | | | | | | | |
| | 0.0110, 0.0113 | 0.0112, | 0.0116 | 0.0117 | 0.0118 | 0.0118 | 0.012 | 0.0121 | 0.0125 |
| MR-RAPS4 | 0.0113 1.000, | 0.0115 0.991, | 0.0116 0.725, | 0.128, | 0.040, | 0.118, | 0.667, | 0.983, | 1.000, |
| MR-RAPS4 | 0.0113 1.000, -0.1002, | 0.0115 0.991, -0.0502, | 0.0116 0.725, -0.0302, | 0.128, -0.0102, | 0.040, -0.0002, | 0.118, 0.0098, | 0.667, 0.0298, | 0.983, 0.0498, | 1.000, 0.0998, |
| MR-RAPS4 | 0.0113 1.000, | 0.0115 0.991, | 0.0116 0.725, | 0.128, | 0.040, | 0.118, | 0.667, | 0.983, | 1.000, |

Table S49: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the ideal case of q=0, and N=200000.

| | <i>'</i> | | | | <u> </u> | | | | |
|----------------------|--|---|---|---|---|---|---|---|---|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.981, | 0.703, | 0.130, | 0.031, | 0.140, | 0.686, | 0.963, | 0.999, |
| COME THE THE | -0.0963, | -0.0464, | -0.0265, | -0.0080, | 0.0001, | 0.0083, | 0.0266, | 0.0464, | 0.0961, |
| | 0.0110, | 0.0112, | 0.0111, | 0.0099, | 0.0094, | 0.0099, | 0.0113, | 0.0117, | 0.0121, |
| | 0.0101 | 0.0102 | 0.0103 | 0.0101 | 0.0101 | 0.0102 | 0.0106 | 0.0108 | 0.0111 |
| cML-MA-AIC-Profile | 1.000, | 0.981, | 0.702, | 0.130, | 0.030, | 0.139, | 0.685, | 0.963, | 0.999, |
| | -0.0965, | -0.0464, | -0.0265, | -0.0080, | 0.0001, | 0.0083, | 0.0266, | 0.0464, | 0.0963, |
| | 0.0110, | 0.0113, | 0.0112, | 0.0099, | 0.0094, | 0.0099, | 0.0114, | 0.0117, | 0.0122, |
| | 0.0101 | 0.0103 | 0.0103 | 0.0101 | 0.0101 | 0.0102 | 0.0106 | 0.0108 | 0.0112 |
| cML-AIC | 1.000, | 0.989, | 0.808, | 0.242, | 0.107, | 0.259, | 0.793, | 0.984, | 1.000, |
| | -0.0983, | -0.0482, | -0.0282, | -0.0089, | 0.0002, | 0.0093, | 0.0285, | 0.0484, | 0.0983, |
| | 0.0116, | 0.0119, | 0.0121, | 0.0116, | 0.0113, | 0.0117, | 0.0125, | 0.0127, | 0.0129, |
|) // | 0.0087 | 0.0088 | 0.0089 | 0.009 | 0.009 | 0.0091 | 0.0092 | 0.0093 | 0.0096 |
| cML-AIC-Profile | 1.000, | 0.989, | 0.808, | 0.242, -0.0089, | 0.106, | 0.259, | 0.793, | 0.984, | 1.000, |
| | -0.0984, 0.0117, | -0.0483, 0.0119, | -0.0282, 0.0121, | -0.0089, 0.0116, | 0.0002, 0.0113, | 0.0093, 0.0117, | 0.0285, 0.0125, | 0.0484, 0.0126, | 0.0984, 0.0130, |
| | 0.0117, | 0.0119, | 0.0121, | 0.0116, | 0.0113, | 0.0117, | 0.0123, | 0.0126, | 0.0130, |
| cML-MA-BIC | 1.000, | 1.000, | 0.967, | 0.234, | 0.0091 | 0.0091 | 0.0092 | 1.000, | 1.000, |
| CML-MA-DIC | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0078, | 0.0080, | 0.0081, | 0.0081, | 0.0082, | 0.0082, | 0.0083, | 0.0084, | 0.0087, |
| | 0.008 | 0.0082 | 0.0082 | 0.0083 | 0.0084 | 0.0084 | 0.0085 | 0.0086 | 0.0089 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.967, | 0.233, | 0.041, | 0.226, | 0.946, | 1.000, | 1.000, |
| cond out a pro-trome | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0078, | 0.0080, | 0.0081, | 0.0081, | 0.0082, | 0.0082, | 0.0083, | 0.0084, | 0.0087, |
| | 0.008 | 0.0082 | 0.0083 | 0.0083 | 0.0084 | 0.0084 | 0.0085 | 0.0086 | 0.0089 |
| cML-BIC | 1.000, | 1.000, | 0.968, | 0.238, | 0.046, | 0.231, | 0.948, | 1.000, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0079, | 0.0080, | 0.0081, | 0.0081, | 0.0082, | 0.0082, | 0.0083, | 0.0084, | 0.0087, |
| | 0.008 | 0.0081 | 0.0082 | 0.0083 | 0.0083 | 0.0083 | 0.0084 | 0.0085 | 0.0088 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.968, | 0.238, | 0.046, | 0.231, | 0.948, | 1.000, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0079, | 0.0080, | 0.0081, | 0.0081, | 0.0082, | 0.0082, | 0.0083, | 0.0084, | 0.0087, |
| | 0.008 | 0.0081 | 0.0082 | 0.0083 | 0.0083 | 0.0083 | 0.0084 | 0.0085 | 0.0088 |
| MR-Mix | 0.828, | 0.751, | 0.606, | 0.140, | 0.061, | 0.157, | 0.627, | 0.736, | 0.829, |
| | -0.0985, | -0.0476, | -0.0283, | -0.0094, | 0.0002, | 0.0095, | 0.0281, | 0.0462, | 0.0894, |
| | 0.0335, | 0.0201, | 0.0159, | 0.0138, | 0.0135, | 0.0137, | 0.0161, | 0.0198, | 0.0319, |
| | 0.0296 | 0.1742 | 0.379 | 0.0608 | 0.0518 | 0.0487 | 0.0422 | 0.0668 | 0.0301 |
| MR-ContMix | 1.000, | 0.997, | 0.836, | 0.205, | 0.071, | 0.223, | 0.817, | 0.996, | 1.000, |
| | -0.1073, | -0.0613, | -0.0407, | -0.0145, | 0.0003, | 0.0149, | 0.0402, | 0.0612, | 0.1086, |
| | 0.0094, | 0.0118, NA | 0.0139, | 0.0169, | 0.0175, NA | 0.0166, NA | 0.0138, NA | 0.0119, | 0.0102, NA |
| MR-Lasso | NA 1.000, | 0.999, | NA 0.936, | NA 0.234, | 0.050, | 0.223, | 0.929, | NA 1.000, | 1.000, |
| WIK-Lasso | -0.1000, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.223, | 0.929, | 0.0499, | 0.0998, |
| | 0.0084, | 0.0086, | 0.0085, | 0.0087, | 0.0088, | 0.0099, | 0.0299, | 0.0088, | 0.0998, |
| | 0.0083 | 0.0084 | 0.0085 | 0.0086 | 0.0086 | 0.0087 | 0.0088 | 0.0089 | 0.0091 |
| MR-PRESSO | 1.000, | 1.000, | 0.945, | 0.221, | 0.039, | 0.219, | 0.921, | 1.000, | 1.000, |
| MR TRESSO | -0.1000, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0098, | 0.0298, | 0.0498, | 0.0997, |
| | 0.0079, | 0.0080, | 0.0081, | 0.0082, | 0.0082, | 0.0083, | 0.0083, | 0.0084, | 0.0087, |
| | 0.0078 | 0.0079 | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0083 | 0.0083 | 0.0086 |
| MR-IVW | 1.000, | 1.000, | 0.949, | 0.211, | 0.033, | 0.210, | 0.929, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0498, | 0.0998, |
| | 0.0078, | 0.0080, | 0.0081, | 0.0081, | 0.0082, | 0.0082, | 0.0083, | 0.0084, | 0.0087, |
| | 0.0084 | 0.0086 | 0.0086 | 0.0087 | 0.0088 | 0.0088 | 0.0089 | 0.009 | 0.0093 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.949, | 0.211, | 0.033, | 0.210, | 0.929, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0498, | 0.0998, |
| | 0.0078, | 0.0080, | 0.0081, | 0.0081, | 0.0082, | 0.0082, | 0.0083, | 0.0084, | 0.0087, |
| | 0.0084 | 0.0086 | 0.0086 | 0.0087 | 0.0088 | 0.0088 | 0.0089 | 0.009 | 0.0093 |
| MR-Egger | 0.562, | 0.185, | 0.095, | 0.044, | 0.042, | 0.049, | 0.080, | 0.174, | 0.492, |
| | -0.0964, | -0.0482, | -0.0290, | -0.0097, | -0.0001, | 0.0096, | 0.0288, | 0.0481, | 0.0962, |
| | 0.0443, | 0.0452, | 0.0457, | 0.0462, | 0.0464, | 0.0467, | 0.0472, | 0.0478, | 0.0493, |
| MD Walakt J.M. P. | 0.0455 | 0.0464 | 0.0469 | 0.0473 | 0.0476 | 0.0478 | 0.0483 | 0.0488 | 0.0502 |
| MR-Weighted-Median | 1.000, | 0.996, | 0.756, | 0.114, | 0.019, | 0.117, | 0.724, | 0.994, | 1.000, |
| | -0.0997, 0.0099, | -0.0499, 0.0101, | -0.0300, 0.0102, | -0.0101, 0.0103, | -0.0002, 0.0103, | 0.0098, 0.0104, | 0.0297, 0.0105, | 0.0496, 0.0106, | 0.0994, 0.0109, |
| | 0.0099, | 0.0101, | 0.0102, | 0.0103, | 0.0103, | 0.0104, | 0.0105, | 0.0106, | 0.0109, |
| MR-Weighted-Mode | 1.000, | 0.0114 | 0.0115 | 0.0116 | 0.0117 | 0.0117 | 0.0119 | 0.012 | 0.0124 |
| MIN- Weighten-Mode | -0.0994, | -0.0498, | -0.0299, | -0.0102, | -0.0004, | 0.026, | 0.303, | 0.740, | 0.999, |
| | 0.0144, | 0.0147, | 0.0299, | 0.0102, | 0.0151, | 0.0093, | 0.0293, | 0.0494, | 0.0993, |
| | 0.0187 | 0.0147, | 0.0192 | 0.0194 | 0.0195 | 0.0196 | 0.0198 | 0.0133, | 0.0206 |
| MR-RAPS1 | 1.000, | 1.000, | 0.952, | 0.219, | 0.0155 | 0.0150 | 0.930, | 1.000, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0079, | 0.0080, | 0.0081, | 0.0082, | 0.0082, | 0.0082, | 0.0083, | 0.0084, | 0.0087, |
| | 0.0083 | 0.0085 | 0.0086 | 0.0086 | 0.0087 | 0.0087 | 0.0088 | 0.0089 | 0.0092 |
| MR-RAPS2 | 1.000, | 1.000, | 0.943, | 0.235, | 0.052, | 0.238, | 0.925, | 1.000, | 1.000, |
| | -0.0230, | -0.0397, | 0.0841, | 0.1322, | 0.1164, | 0.0919, | 0.0723, | 0.0851, | 0.1477, |
| | 0.2890, | 1.0738, | 3.4025, | 2.6761, | 1.2820, | 1.9255, | 1.5577, | 1.1493, | 0.4888, |
| | 0.2070, | 0.0202 | 0.025 | 0.0189 | 0.0128 | 0.0197 | 0.0239 | 0.021 | 0.0138 |
| | 0.0105 | 0.0202 | | | 0.046, | 0.230, | 0.947, | 1.000, | 1.000, |
| MR-RAPS3 | 0.0105 1.000, | 1.000, | 0.967, | 0.239, | | | | | |
| MR-RAPS3 | 0.0105 1.000, -0.1001, | 1.000, -0.0501, | 0.967, -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| MR-RAPS3 | 0.0105 1.000, -0.1001, 0.0078, | 1.000, -0.0501, 0.0080, | 0.967, -0.0301, 0.0081, | -0.0101, 0.0081, | -0.0001, 0.0082, | 0.0099, 0.0082, | 0.0299, 0.0083, | 0.0499, 0.0084, | 0.0999, 0.0087, |
| | 0.0105 1.000, -0.1001, 0.0078, 0.008 | 1.000, -0.0501, 0.0080, 0.0081 | 0.967, -0.0301, 0.0081, 0.0082 | -0.0101, 0.0081, 0.0083 | -0.0001, 0.0082, 0.0083 | 0.0099, 0.0082, 0.0083 | 0.0299, 0.0083, 0.0084 | 0.0499, 0.0084, 0.0085 | 0.0999, 0.0087, 0.0088 |
| MR-RAPS3 MR-RAPS4 | 0.0105 1.000, -0.1001, 0.0078, 0.008 1.000, | 1.000, -0.0501, 0.0080, 0.0081 1.000, | 0.967, -0.0301, 0.0081, 0.0082 0.956, | -0.0101, 0.0081, 0.0083 0.224, | -0.0001, 0.0082, 0.0083 0.039, | 0.0099, 0.0082, 0.0083 0.221, | 0.0299, 0.0083, 0.0084 0.943, | 0.0499, 0.0084, 0.0085 1.000, | 0.0999, 0.0087, 0.0088 1.000, |
| | 0.0105 1.000, -0.1001, 0.0078, 0.008 1.000, -0.1001, | 1.000, -0.0501, 0.0080, 0.0081 1.000, -0.0501, | 0.967, -0.0301, 0.0081, 0.0082 0.956, -0.0301, | -0.0101, 0.0081, 0.0083 0.224, -0.0101, | -0.0001, 0.0082, 0.0083 0.039, -0.0001, | 0.0099, 0.0082, 0.0083 0.221, 0.0099, | 0.0299, 0.0083, 0.0084 0.943, 0.0299, | 0.0499, 0.0084, 0.0085 1.000, 0.0499, | 0.0999, 0.0087, 0.0088 1.000, 0.0999, |
| | 0.0105 1.000, -0.1001, 0.0078, 0.008 1.000, | 1.000, -0.0501, 0.0080, 0.0081 1.000, | 0.967, -0.0301, 0.0081, 0.0082 0.956, | -0.0101, 0.0081, 0.0083 0.224, | -0.0001, 0.0082, 0.0083 0.039, | 0.0099, 0.0082, 0.0083 0.221, | 0.0299, 0.0083, 0.0084 0.943, | 0.0499, 0.0084, 0.0085 1.000, | 0.0999, 0.0087, 0.0088 1.000, |

Table S50: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE satisfied, q=0.2, and N=50000.

| // | <i>'</i> | | | | , I | | | | |
|-------------------------|---------------------|---------------------|----------|--------------------|----------|---------|---------|---------|------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.941, | 0.460, | 0.178, | 0.044, | 0.033, | 0.046, | 0.153, | 0.404, | 0.886, |
| CIVIL IVIT THE | -0.0908, | -0.0423, | -0.0244, | -0.0080, | -0.0004, | 0.0070, | 0.0231, | 0.0405, | 0.0884, |
| | 0.0249, | 0.0236, | 0.0221, | 0.0204, | 0.0202, | 0.0207, | 0.0225, | 0.0248, | 0.0275, |
| | 0.0249, | 0.0234 | 0.0221, | 0.0232 | 0.0233 | 0.0234 | 0.0223, | 0.0245 | 0.0273, |
| cML-MA-AIC-Profile | 0.941, | 0.458, | 0.177, | 0.044, | 0.031, | 0.045, | 0.151, | 0.399, | 0.884, |
| CIVIL-IVIA-AIC-I TOILIC | -0.0911, | -0.0423, | -0.0244, | -0.0080, | -0.0004, | 0.0070, | 0.0231, | 0.0406, | 0.0886, |
| | 0.0250, | 0.0236, | 0.0221, | 0.0204, | 0.0202, | 0.0070, | 0.0231, | 0.0400, | 0.0336, |
| | 0.0236, | 0.0236 | 0.0221, | 0.0233 | 0.0202, | 0.0207, | 0.0223, | 0.0246 | 0.0270, |
| cML-AIC | 0.0233 | 0.638, | 0.0234 | 0.0255 | 0.0234 | 0.0236 | 0.024 | 0.0246 | 0.0239 |
| CIVIL-AIC | | | | | | | | | |
| | -0.0956, | -0.0467, | -0.0278, | -0.0095, | -0.0009, | 0.0077, | 0.0258, | 0.0444, | 0.0934, |
| | 0.0267, | 0.0260, | 0.0254, | 0.0247, | 0.0248, | 0.0252, | 0.0264, | 0.0277, | 0.0290, |
| | 0.0198 | 0.0202 | 0.0204 | 0.0206 | 0.0207 | 0.0208 | 0.021 | 0.0212 | 0.0218 |
| cML-AIC-Profile | 0.966, | 0.636, | 0.328, | 0.115, | 0.098, | 0.122, | 0.277, | 0.548, | 0.951, |
| | -0.0958, | -0.0468, | -0.0279, | -0.0095, | -0.0009, | 0.0078, | 0.0258, | 0.0444, | 0.0936, |
| | 0.0268, | 0.0261, | 0.0254, | 0.0247, | 0.0248, | 0.0253, | 0.0264, | 0.0277, | 0.0291, |
| | 0.02 | 0.0203 | 0.0205 | 0.0207 | 0.0208 | 0.0209 | 0.0211 | 0.0213 | 0.022 |
| cML-MA-BIC | 1.000, | 0.753, | 0.367, | 0.086, | 0.052, | 0.083, | 0.341, | 0.702, | 0.997, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0101, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0998 |
| | 0.0189, | 0.0192, | 0.0193, | 0.0195, | 0.0196, | 0.0197, | 0.0199, | 0.0202, | 0.0208 |
| | 0.0185 | 0.0188 | 0.0189 | 0.0191 | 0.0192 | 0.0193 | 0.0195 | 0.0197 | 0.0203 |
| ML-MA-BIC-Profile | 1.000, | 0.749, | 0.364, | 0.083, | 0.052, | 0.083, | 0.339, | 0.701, | 0.997, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0101, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0998 |
| | 0.0189, | 0.0192, | 0.0193, | 0.0195, | 0.0196, | 0.0197, | 0.0199, | 0.0202, | 0.0208. |
| | 0.0185 | 0.0188 | 0.019 | 0.0192 | 0.0193 | 0.0193 | 0.0195 | 0.0198 | 0.0203 |
| cML-BIC | 1.000, | 0.754, | 0.372, | 0.091, | 0.053, | 0.092, | 0.357, | 0.716, | 0.997, |
| 5.0 | -0.1000, | -0.0499, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1000 |
| | 0.0189, | 0.0193, | 0.0194, | 0.0196, | 0.0000, | 0.0100, | 0.0300, | 0.0300, | 0.1000 |
| | 0.0189, | 0.0193, | 0.0194, | 0.0196, | 0.0197, | 0.0198, | 0.0200, | 0.0202, | 0.0208 |
| oMI DIC Dangle | | | | | | | | | |
| cML-BIC-Profile | 1.000, | 0.751, | 0.371, | 0.091, -0.0100, | 0.053, | 0.092, | 0.355, | 0.715, | 0.997, 0.1000 |
| | -0.1000, | -0.0499, | -0.0300, | | 0.0000, | 0.0100, | 0.0300, | 0.0500, | |
| | 0.0189, | 0.0193, | 0.0194, | 0.0196, | 0.0197, | 0.0198, | 0.0200, | 0.0202, | 0.0208 |
| 100 1 | 0.0183 | 0.0186 | 0.0188 | 0.0189 | 0.019 | 0.0191 | 0.0193 | 0.0195 | 0.0201 |
| MR-Mix | 0.934, | 0.387, | 0.119, | 0.017, | 0.013, | 0.030, | 0.127, | 0.378, | 0.924, |
| | -0.1049, | -0.0508, | -0.0297, | -0.0091, | 0.0010, | 0.0111, | 0.0309, | 0.0503, | 0.0973 |
| | 0.0237, | 0.0234, | 0.0234, | 0.0233, | 0.0232, | 0.0232, | 0.0233, | 0.0233, | 0.0233, |
| | 0.0311 | 0.0308 | 0.0307 | 0.0307 | 0.0307 | 0.0307 | 0.0306 | 0.0306 | 0.0305 |
| MR-ContMix | 1.000, | 0.725, | 0.358, | 0.098, | 0.059, | 0.089, | 0.327, | 0.677, | 0.993, |
| | -0.0997, | -0.0502, | -0.0303, | -0.0104, | -0.0005, | 0.0095, | 0.0294, | 0.0492, | 0.0989 |
| | 0.0200, | 0.0204, | 0.0205, | 0.0206, | 0.0207, | 0.0209, | 0.0211, | 0.0214, | 0.0222 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.730, | 0.334, | 0.085, | 0.050, | 0.080, | 0.318, | 0.668, | 0.996, |
| | -0.0997, | -0.0499, | -0.0300, | -0.0101, | -0.0002, | 0.0098, | 0.0296, | 0.0496, | 0.0994 |
| | 0.0192, | 0.0197, | 0.0197, | 0.0199, | 0.0199, | 0.0201, | 0.0204, | 0.0206, | 0.0212 |
| | 0.0191 | 0.0194 | 0.0196 | 0.0198 | 0.0199 | 0.02 | 0.0202 | 0.0204 | 0.021 |
| MR-PRESSO | 0.877, | 0.652, | 0.461, | 0.303, | 0.258, | 0.286, | 0.409, | 0.599, | 0.867, |
| MIK-FKESSO | -0.1010, | -0.0522, | -0.0324, | -0.0130, | -0.0036, | 0.0058, | 0.0258, | 0.0457, | 0.0953 |
| | | 0.0626, | 0.0324, | 0.0617, | 0.0620, | | | | |
| | 0.0629, | | 0.0610, | | | 0.0611, | 0.0604, | 0.0593, | 0.0581 |
| 1 CD 17 1777 | 0.0209 | 0.021 | 0.0208 | 0.021 | 0.0211 | 0.0211 | 0.0211 | 0.0212 | 0.0214 |
| MR-IVW | 0.107, | 0.089, | 0.083, | 0.088, | 0.085, | 0.086, | 0.083, | 0.082, | 0.097, |
| | -0.1078, | -0.0579, | -0.0379, | -0.0179, | -0.0079, | 0.0020, | 0.0220, | 0.0420, | 0.0919 |
| | 0.1697, | 0.1696, | 0.1696, | 0.1696, | 0.1696, | 0.1696, | 0.1696, | 0.1696, | 0.1696 |
| | 0.1654 | 0.1654 | 0.1654 | 0.1654 | 0.1654 | 0.1654 | 0.1654 | 0.1654 | 0.1654 |
| MR-IVW-Oracle | 1.000, | 0.722, | 0.318, | 0.073, | 0.041, | 0.071, | 0.314, | 0.667, | 0.996, |
| | -0.0994, | -0.0497, | -0.0298, | -0.0099, | 0.0000, | 0.0100, | 0.0298, | 0.0497, | 0.0995 |
| | 0.0186, | 0.0190, | 0.0191, | 0.0193, | 0.0194, | 0.0195, | 0.0197, | 0.0199, | 0.0205 |
| | 0.0193 | 0.0197 | 0.0198 | 0.02 | 0.0201 | 0.0202 | 0.0204 | 0.0206 | 0.0212 |
| MR-Egger | 0.071, | 0.074, | 0.075, | 0.075, | 0.075, | 0.076, | 0.076, | 0.076, | 0.072, |
| 30 | -0.0209, | 0.0223, | 0.0396, | 0.0568, | 0.0655, | 0.0741, | 0.0914, | 0.1086, | 0.1518 |
| | 0.8701, | 0.8701, | 0.8702, | 0.8702, | 0.8702, | 0.8703, | 0.8703, | 0.8704, | 0.8705 |
| | 0.8466 | 0.8466 | 0.8466 | 0.8466 | 0.8466 | 0.8467 | 0.8467 | 0.8467 | 0.8468 |
| MR-Weighted-Median | 0.973, | 0.487, | 0.175, | 0.041, | 0.025, | 0.043, | 0.158, | 0.432, | 0.949, |
| | -0.0974, | -0.0489, | -0.0294, | -0.0100, | -0.0003, | 0.0094, | 0.0289, | 0.432, | 0.949, |
| | 0.0226, | 0.0230, | 0.0232, | 0.0235, | 0.0236, | 0.0034, | 0.0239, | 0.0484, | 0.0252 |
| | 0.0226, | 0.0258 | 0.0232, | 0.0253, | 0.0256, | 0.0257, | 0.0259, | 0.0242, | 0.0232 |
| MR-Weighted-Mode | 0.0234 | 0.0238 | | 0.0203 | 0.0204 | 0.0263 | 0.0268 | 0.0271 | 0.0279 |
| wix-weighten-Mode | | | 0.123, | | | | | | |
| | -0.0980, | -0.0490, | -0.0297, | -0.0100, | -0.0001, | 0.0097, | 0.0292, | 0.0488, | 0.0977 |
| | 0.0263, | 0.0268, | 0.0272, | 0.0274, | 0.0277, | 0.0277, | 0.0283, | 0.0285, | 0.0296 |
| 100 0 1 | 0.0308 | 0.0314 | 0.0316 | 0.0319 | 0.0321 | 0.0322 | 0.0326 | 0.0329 | 0.0339 |
| MR-RAPS1 | 0.105, | 0.086, | 0.096, | 0.099, | 0.101, | 0.100, | 0.090, | 0.080, | 0.092, |
| | -0.1083, | -0.0583, | -0.0382, | -0.0182, | -0.0082, | 0.0018, | 0.0218, | 0.0418, | 0.0918 |
| | 0.1668, | 0.1669, | 0.1669, | 0.1669, | 0.1669, | 0.1669, | 0.1670, | 0.1670, | 0.1671 |
| | 0.1618 | 0.1618 | 0.1618 | 0.1619 | 0.1619 | 0.1619 | 0.1619 | 0.1619 | 0.162 |
| MR-RAPS2 | 0.991, | 0.905, | 0.778, | 0.636, | 0.646, | 0.658, | 0.782, | 0.907, | 0.994, |
| | 0.2414, | 0.2583, | 0.2497, | 0.3900, | 0.5145, | 0.3228, | 0.5106, | 0.3514, | 0.2625 |
| | 3.4866, | 3.3666, | 2.7536, | 3.9040, | 5.0016, | 3.0375, | 3.2553, | 3.7643, | 3.8922 |
| | 0.0498 | 0.035 | 0.036 | 0.0362 | 0.0405 | 0.0341 | 0.0388 | 0.0422 | 0.0483 |
| MR-RAPS3 | | | | | | | | | |
| WIK-KAPSS | 0.901, | 0.848, | 0.829, | 0.828, | 0.831, | 0.829, | 0.847, | 0.871, | 0.889, |
| | -0.2260, | -0.1187, | -0.0770, | -0.0363, | -0.0164, | 0.0032, | 0.0414, | 0.0784, | 0.1649 |
| | 0.3464, | 0.3423, | 0.3387, | 0.3341, | 0.3315, | 0.3287, | 0.3227, | 0.3162, | 0.2989 |
| | 0.0404 | 0.0393 | 0.0387 | 0.0382 | 0.038 | 0.0377 | 0.0372 | 0.0366 | 0.0355 |
| | 1.000, | 0.968, | 0.901, | 0.849, | 0.837, | 0.847, | 0.898, | 0.956, | 1.000, |
| MR-RAPS4 | | | 0.0073, | 0.1234, | 0.1738, | 0.2090, | 0.3159, | 0.3864, | 0.5563 |
| MR-RAPS4 | -0.2182, | -0.0554, | | | | | | | |
| MR-RAPS4 | -0.2182, 1.1830, | -0.0554, 1.1372, | 1.1520, | 1.1165, | 1.0960, | 1.0959, | 1.1012, | 1.0980, | 1.0458 |

Table S51: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE satisfied, q=0.2, and N=100000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|-------------------|----------|----------|----------|----------|----------|---------|---------|---------|---------|
| cML-MA-AIC | 0.993, | 0.718, | 0.335, | 0.070, | 0.044, | 0.076, | 0.323, | 0.681, | 0.983, |
| | -0.0933, | -0.0436, | -0.0248, | -0.0079, | -0.0003, | 0.0076, | 0.0246, | 0.0434, | 0.0925, |
| | 0.0183, | 0.0183, | 0.0173, | 0.0157, | 0.0156, | 0.0160, | 0.0177, | 0.0193, | 0.0206, |
| | 0.0166 | 0.0168 | 0.0166 | 0.0164 | 0.0164 | 0.0166 | 0.0171 | 0.0175 | 0.0182 |
| ML-MA-AIC-Profile | 0.993, | 0.715, | 0.333, | 0.070, | 0.044, | 0.074, | 0.322, | 0.680, | 0.983, |
| | -0.0935, | -0.0437, | -0.0248, | -0.0079, | -0.0003, | 0.0076, | 0.0247, | 0.0434, | 0.0927, |
| | 0.0184, | 0.0184, | 0.0173, | 0.0157, | 0.0156, | 0.0160, | 0.0177, | 0.0193, | 0.0207 |
| 10.110 | 0.0167 | 0.0168 | 0.0167 | 0.0165 | 0.0165 | 0.0166 | 0.0171 | 0.0176 | 0.0183 |
| cML-AIC | 0.996, | 0.837, | 0.505, | 0.173, | 0.124, | 0.175, | 0.476, | 0.788, | 0.995, |
| | -0.0968, | -0.0472, | -0.0277, | -0.0094, | -0.0007, | 0.0084, | 0.0271, | 0.0465, | 0.0962 |
| | 0.0195, | 0.0198, | 0.0195, | 0.0188, | 0.0188, | 0.0190, | 0.0199, | 0.0210, | 0.0219 |
| | 0.014 | 0.0143 | 0.0144 | 0.0146 | 0.0146 | 0.0147 | 0.0148 | 0.015 | 0.0154 |
| cML-AIC-Profile | 0.996, | 0.835, | 0.505, | 0.172, | 0.123, | 0.173, | 0.475, | 0.787, | 0.994, |
| | -0.0970, | -0.0473, | -0.0277, | -0.0094, | -0.0007, | 0.0084, | 0.0271, | 0.0465, | 0.0963 |
| | 0.0195, | 0.0198, | 0.0195, | 0.0188, | 0.0188, | 0.0190, | 0.0199, | 0.0210, | 0.0219 |
| | 0.0141 | 0.0143 | 0.0145 | 0.0146 | 0.0147 | 0.0148 | 0.0149 | 0.0151 | 0.0155 |
| cML-MA-BIC | 1.000, | 0.960, | 0.612, | 0.123, | 0.050, | 0.120, | 0.586, | 0.939, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0102, | -0.0002, | 0.0098, | 0.0297, | 0.0497, | 0.0997 |
| | 0.0134, | 0.0137, | 0.0138, | 0.0139, | 0.0140, | 0.0141, | 0.0143, | 0.0144, | 0.0149 |
| | 0.013 | 0.0133 | 0.0134 | 0.0135 | 0.0136 | 0.0136 | 0.0138 | 0.0139 | 0.0143 |
| ML-MA-BIC-Profile | 1.000, | 0.960, | 0.610, | 0.122, | 0.050, | 0.120, | 0.585, | 0.938, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0102, | -0.0002, | 0.0098, | 0.0297, | 0.0497, | 0.0997 |
| | 0.0134, | 0.0137, | 0.0138, | 0.0139, | 0.0140, | 0.0141, | 0.0143, | 0.0144, | 0.0149 |
| | 0.0134, | 0.0137, | 0.0134 | 0.0135 | 0.0136 | 0.0137 | 0.0143, | 0.0139 | 0.0144 |
| cML-BIC | 1.000, | 0.966, | 0.621, | 0.130, | 0.056, | 0.124, | 0.5138 | 0.941, | 1.000, |
| CIVIL DIC | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.941, | 0.0997 |
| | 0.0134, | 0.0137, | 0.0138, | 0.0102, | 0.0140, | 0.0098, | 0.0298, | 0.0497, | 0.0997 |
| | 0.0134, | 0.0137, | 0.0138, | 0.0140, | 0.0140, | 0.0141, | 0.0143, | 0.0144, | 0.0148 |
| aML DIC B CL. | | | | | | | | | |
| cML-BIC-Profile | 1.000, | 0.965, | 0.621, | 0.130, | 0.053, | 0.124, | 0.597, | 0.941, | 1.000, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0497, | 0.0997 |
| | 0.0134, | 0.0137, | 0.0138, | 0.0140, | 0.0140, | 0.0141, | 0.0143, | 0.0144, | 0.0148 |
| 1 m | 0.0129 | 0.0132 | 0.0133 | 0.0134 | 0.0134 | 0.0135 | 0.0137 | 0.0138 | 0.0142 |
| MR-Mix | 0.997, | 0.700, | 0.259, | 0.036, | 0.013, | 0.040, | 0.246, | 0.662, | 0.990, |
| | -0.1062, | -0.0522, | -0.0311, | -0.0104, | -0.0002, | 0.0098, | 0.0296, | 0.0492, | 0.0958 |
| | 0.0171, | 0.0171, | 0.0172, | 0.0173, | 0.0172, | 0.0172, | 0.0172, | 0.0171, | 0.0172 |
| | 0.0223 | 0.0221 | 0.0224 | 0.0221 | 0.0221 | 0.022 | 0.022 | 0.022 | 0.0221 |
| MR-ContMix | 1.000, | 0.943, | 0.604, | 0.133, | 0.068, | 0.132, | 0.586, | 0.920, | 1.000, |
| | -0.0997, | -0.0498, | -0.0299, | -0.0100, | 0.0000, | 0.0099, | 0.0299, | 0.0498, | 0.0997 |
| | 0.0141, | 0.0144, | 0.0145, | 0.0147, | 0.0148, | 0.0148, | 0.0150, | 0.0152, | 0.0158 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.952, | 0.587, | 0.121, | 0.062, | 0.119, | 0.559, | 0.916, | 1.000, |
| | -0.0998, | -0.0501, | -0.0302, | -0.0102, | -0.0003, | 0.0097, | 0.0297, | 0.0495, | 0.0994 |
| | 0.0138, | 0.0142, | 0.0144, | 0.0146, | 0.0147, | 0.0146, | 0.0147, | 0.0149, | 0.0154 |
| | 0.0135 | 0.0138 | 0.0139 | 0.0141 | 0.0147, | 0.0142 | 0.0147, | 0.0145 | 0.0134 |
| MR-PRESSO | 0.849, | 0.714, | 0.540, | 0.363, | 0.336, | 0.357, | 0.540, | 0.689, | 0.825, |
| WIK-FKESSO | -0.1053, | -0.0573, | -0.0375, | -0.0177, | -0.0080, | 0.0018, | 0.0219, | 0.0419, | 0.0898 |
| | 0.1180, | 0.1173, | | 0.1160, | 0.1154, | 0.1153, | 0.0219, | 0.0419, | 0.1090 |
| | | | 0.1166, | | | | | | |
| MR-IVW | 0.0314 | 0.0312 | 0.0308 | 0.0306 | 0.0305 | 0.0306 | 0.0303 | 0.0299 | 0.0285 |
| MR-IVW | 0.108, | 0.081, | 0.079, | 0.077, | 0.078, | 0.087, | 0.079, | 0.074, | 0.081, |
| | -0.1096, | -0.0596, | -0.0396, | -0.0196, | -0.0096, | 0.0004, | 0.0204, | 0.0404, | 0.0904 |
| | 0.1680, | 0.1680, | 0.1680, | 0.1679, | 0.1679, | 0.1679, | 0.1679, | 0.1679, | 0.1679 |
| | 0.1661 | 0.166 | 0.166 | 0.166 | 0.166 | 0.166 | 0.166 | 0.166 | 0.166 |
| MR-IVW-Oracle | 1.000, | 0.952, | 0.580, | 0.108, | 0.045, | 0.109, | 0.552, | 0.917, | 1.000, |
| | -0.0998, | -0.0500, | -0.0301, | -0.0102, | -0.0002, | 0.0098, | 0.0297, | 0.0496, | 0.0995 |
| | 0.0133, | 0.0136, | 0.0137, | 0.0138, | 0.0139, | 0.0140, | 0.0141, | 0.0143, | 0.0147 |
| | 0.0137 | 0.0139 | 0.0141 | 0.0142 | 0.0143 | 0.0143 | 0.0145 | 0.0146 | 0.0151 |
| MR-Egger | 0.053, | 0.050, | 0.052, | 0.049, | 0.049, | 0.047, | 0.046, | 0.047, | 0.051, |
| | -0.0970, | -0.0504, | -0.0318, | -0.0132, | -0.0039, | 0.0054, | 0.0240, | 0.0426, | 0.0891 |
| | 0.8833, | 0.8830, | 0.8828, | 0.8827, | 0.8826, | 0.8826, | 0.8824, | 0.8823, | 0.8820 |
| | 0.8867 | 0.8866 | 0.8866 | 0.8865 | 0.8865 | 0.8865 | 0.8865 | 0.8865 | 0.8865 |
| R-Weighted-Median | 1.000, | 0.787, | 0.357, | 0.060, | 0.026, | 0.058, | 0.343, | 0.749, | 1.000, |
| - | -0.0987, | -0.0493, | -0.0296, | -0.0098, | 0.0000, | 0.0099, | 0.0295, | 0.0491, | 0.0983 |
| | 0.0165, | 0.0168, | 0.0169, | 0.0171, | 0.0172, | 0.0173, | 0.0175, | 0.0177, | 0.0182 |
| | 0.018 | 0.0183 | 0.0185 | 0.0186 | 0.0187 | 0.0188 | 0.019 | 0.0192 | 0.0198 |
| MR-Weighted-Mode | 0.995, | 0.609, | 0.240, | 0.043, | 0.019, | 0.039, | 0.228, | 0.577, | 0.985, |
| | -0.0987, | -0.0495, | -0.0295, | -0.0099, | -0.0001, | 0.0099, | 0.0295. | 0.0493, | 0.0987 |
| | 0.0194, | 0.0197, | 0.0198, | 0.0200, | 0.0202, | 0.0203, | 0.0295, | 0.0208, | 0.0214 |
| | 0.0194, | 0.0197, | 0.0198, | 0.0200, | 0.0202, | 0.0203, | 0.0203, | 0.0208, | 0.0214 |
| MR-RAPS1 | 0.0221 | 0.0223 | 0.0227 | 0.0228 | 0.023 | 0.0231 | 0.0255 | 0.0230 | 0.0243 |
| MIN-NAP31 | -0.1072, | | | | | | 0.085, | | |
| | | -0.0572, | -0.0372, | -0.0172, | -0.0073, | 0.0027, | | 0.0427, | 0.0927 |
| | 0.1634, | 0.1634, | 0.1635, | 0.1635, | 0.1635, | 0.1635, | 0.1635, | 0.1635, | 0.1636 |
| 14D D 1 222 | 0.1619 | 0.1619 | 0.1619 | 0.1619 | 0.1619 | 0.1619 | 0.162 | 0.162 | 0.162 |
| MR-RAPS2 | 0.997, | 0.983, | 0.867, | 0.706, | 0.680, | 0.728, | 0.884, | 0.977, | 0.993, |
| | 0.6928, | 0.2831, | 0.4724, | 0.3816, | 0.2261, | 0.2819, | 0.8065, | 0.3940, | 0.7312 |
| | 3.3134, | 2.9407, | 4.6226, | 2.2356, | 3.4411, | 2.4180, | 8.6537, | 4.7269, | 8.8020 |
| | 0.0357 | 0.0227 | 0.0231 | 0.0231 | 0.0228 | 0.0246 | 0.0295 | 0.0299 | 0.0378 |
| MR-RAPS3 | 0.925, | 0.918, | 0.887, | 0.873, | 0.868, | 0.884, | 0.887, | 0.900, | 0.923, |
| | -0.2304, | -0.1214, | -0.0792, | -0.0381, | -0.0180, | 0.0018, | 0.0404, | 0.0776, | 0.1648 |
| | 0.3460, | 0.3421, | 0.3384, | 0.3338, | 0.3312, | 0.3284, | 0.3224, | 0.3158, | 0.2985, |
| | 0.0293 | 0.0282 | 0.0278 | 0.0274 | 0.0272 | 0.027 | 0.0266 | 0.0262 | 0.0253 |
| MR-RAPS4 | 1.000, | 0.999, | 0.971, | 0.932, | 0.931, | 0.928, | 0.974, | 0.994, | 1.000, |
| | 0.3571, | 0.4107, | 0.4326, | 0.4616, | 0.4855, | 0.5026, | 0.5353, | 0.5806, | 0.6787 |
| | | | | | | | | | |
| | 1.0738, | 1.0289, | 1.0006, | 0.9527, | 0.9528, | 0.9786, | 0.9597, | 0.9693, | 1.0068, |

Table S52: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE satisfied, q=0.2, and N=200000.

| // | <i>' '</i> | | | | , I | | | | |
|--------------------|------------------------------|------------------------------|------------------------------|------------------------------|---------------------|--------------------|------------------------------|--------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.999, | 0.929, | 0.560, | 0.094, | 0.034, | 0.090, | 0.530, | 0.897, | 1.000, |
| | -0.0951, | -0.0452, | -0.0255, | -0.0079, | -0.0002, | 0.0076, | 0.0251, | 0.0447, | 0.0945, |
| | 0.0124, | 0.0125, | 0.0122, | 0.0108, | 0.0103, | 0.0108, | 0.0127, | 0.0133, | 0.0139, |
| | 0.0119 | 0.0121 | 0.012 | 0.0117 | 0.0117 | 0.0119 | 0.0123 | 0.0126 | 0.013 |
| cML-MA-AIC-Profile | 0.999, | 0.929, | 0.558, | 0.094, | 0.034, | 0.089, | 0.530, | 0.897, | 1.000, |
| | -0.0953, | -0.0452, | -0.0255, | -0.0079, | -0.0002, | 0.0076, | 0.0251, | 0.0448, | 0.0946, |
| | 0.0124, | 0.0126, | 0.0122, | 0.0108, | 0.0103, | 0.0108, | 0.0127, | 0.0134, | 0.0139, |
|) // LTC | 0.0119 | 0.0121 | 0.012 | 0.0118 | 0.0117 | 0.0119 | 0.0124 | 0.0127 | 0.013 |
| cML-AIC | 1.000, | 0.962, | 0.721, | 0.211, | 0.108, | 0.206, | 0.702, | 0.949, | 1.000, |
| | -0.0979, 0.0132, | -0.0477, 0.0137, | -0.0278, 0.0136, | -0.0091, 0.0130, | -0.0004, 0.0129, | 0.0085, 0.0130, | 0.0275, 0.0139, | 0.0473, 0.0142, | 0.0973, 0.0145, |
| | 0.0132, | 0.0137, | 0.0136, | 0.0130, | 0.0129, | 0.0130, | 0.0139, | 0.0142, | 0.0143, |
| cML-AIC-Profile | 1.000, | 0.962, | 0.721, | 0.0103 | 0.108, | 0.205, | 0.702, | 0.949, | 1.000, |
| CIVIL THE Frome | -0.0979, | -0.0477, | -0.0278, | -0.0091, | -0.0004, | 0.0085, | 0.0275, | 0.0474, | 0.0974, |
| | 0.0132, | 0.0137, | 0.0137, | 0.0130, | 0.0129, | 0.0130, | 0.0139, | 0.0142, | 0.0146, |
| | 0.01 | 0.0102 | 0.0102 | 0.0103 | 0.0104 | 0.0104 | 0.0105 | 0.0106 | 0.0109 |
| cML-MA-BIC | 1.000, | 1.000, | 0.890, | 0.179, | 0.049, | 0.184, | 0.869, | 0.997, | 1.000, |
| | -0.1000, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0100, | 0.0300, | 0.0500, | 0.1001, |
| | 0.0091, | 0.0093, | 0.0094, | 0.0095, | 0.0095, | 0.0096, | 0.0097, | 0.0098, | 0.0101, |
| | 0.0092 | 0.0093 | 0.0094 | 0.0095 | 0.0095 | 0.0096 | 0.0097 | 0.0098 | 0.0101 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.889, | 0.177, | 0.049, | 0.184, | 0.868, | 0.997, | 1.000, |
| | -0.1000, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0100, | 0.0300, | 0.0500, | 0.1001, |
| | 0.0091, | 0.0093, | 0.0094, | 0.0095, | 0.0095, | 0.0096, | 0.0097, | 0.0098, | 0.0101, |
| | 0.0092 | 0.0094 | 0.0094 | 0.0095 | 0.0096 | 0.0096 | 0.0097 | 0.0098 | 0.0101 |
| cML-BIC | 1.000, | 1.000, | 0.897, | 0.181, | 0.050, | 0.191, | 0.874, | 0.997, | 1.000, |
| | -0.1000, | -0.0500, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0091, | 0.0093, | 0.0094, | 0.0095, | 0.0095, | 0.0096, | 0.0097, | 0.0098, | 0.0101, |
| M. DIG P. 21 | 0.0091 | 0.0093 | 0.0093 | 0.0094 | 0.0095 | 0.0095 | 0.0096 | 0.0097 | 0.01 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.897, | 0.181, | 0.050, | 0.190, | 0.874, | 0.997, | 1.000, |
| | -0.1000, | -0.0500, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0091, 0.0091 | 0.0093, 0.0093 | 0.0094, 0.0094 | 0.0095, 0.0094 | 0.0095, 0.0095 | 0.0096, 0.0095 | 0.0097, 0.0096 | 0.0098, 0.0097 | 0.0101, 0.01 |
| MR-Mix | 1.000, | 0.0093 | 0.0094 | 0.0094 | 0.0093 | 0.0093 | 0.0096 | 0.888, | 0.01 |
| IVIIX-IVIIX | -0.1062, | -0.0517, | -0.0307, | -0.0101, | 0.0000, | 0.031, | 0.437, | 0.0496, | 0.9966, |
| | 0.0126, | 0.0126, | 0.0124, | 0.0101, | 0.0000, | 0.0101, | 0.0300, | 0.0490, | 0.0300, |
| | 0.0120, | 0.0120, | 0.0124, | 0.0123, | 0.0124, | 0.0124, | 0.0124, | 0.0123, | 0.0124, |
| MR-ContMix | 1.000, | 0.999, | 0.892, | 0.188, | 0.065, | 0.196, | 0.861, | 0.998, | 1.000, |
| mic Commin | -0.0998, | -0.0498, | -0.0299, | -0.0099, | 0.0001, | 0.0100, | 0.0300, | 0.0500, | 0.0999, |
| | 0.0095, | 0.0096, | 0.0097, | 0.0097, | 0.0098, | 0.0098, | 0.0100, | 0.0101, | 0.0104, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.999, | 0.866, | 0.173, | 0.048, | 0.168, | 0.845, | 0.995, | 1.000, |
| | -0.0998, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0094, | 0.0096, | 0.0097, | 0.0097, | 0.0098, | 0.0098, | 0.0099, | 0.0100, | 0.0103, |
| | 0.0096 | 0.0098 | 0.0099 | 0.01 | 0.01 | 0.0101 | 0.0102 | 0.0103 | 0.0106 |
| MR-PRESSO | 0.671, | 0.599, | 0.528, | 0.320, | 0.268, | 0.305, | 0.507, | 0.608, | 0.726, |
| | -0.0931, | -0.0440, | -0.0243, | -0.0049, | 0.0042, | 0.0139, | 0.0335, | 0.0531, | 0.1037, |
| | 0.1512, | 0.1501, | 0.1496, | 0.1491, | 0.1484, | 0.1479, | 0.1473, | 0.1465, | 0.1439, |
| MD WWY | 0.0583 | 0.0566 | 0.056 | 0.0555 | 0.0546 | 0.054 | 0.053 | 0.0522 | 0.0492 |
| MR-IVW | 0.087, | 0.077, | 0.084, | 0.086, | 0.087, | 0.087, | 0.087, | 0.090, | 0.110, |
| | -0.0969, 0.1706, | -0.0468, 0.1706, | -0.0267, 0.1706, | -0.0067, 0.1706, | 0.0034, 0.1706, | 0.0134, 0.1706, | 0.0334, 0.1705, | 0.0535, 0.1705, | 0.1036, 0.1705, |
| | 0.1706, | 0.1700, | 0.1706, | 0.1700, | 0.1700, | 0.1700, | 0.1703, | 0.1703, | 0.1703, |
| MR-IVW-Oracle | 1.000, | 0.999, | 0.1633 | 0.1633 | 0.1033 | 0.1633 | 0.1033 | 0.1055 | 1.000, |
| WIK-IV W-Oldele | -0.0998, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0300, | 0.0500, | 0.1000, |
| | 0.0091, | 0.0093, | 0.0094, | 0.0095, | 0.0095, | 0.0096, | 0.0097, | 0.0098, | 0.0101, |
| | 0.0097 | 0.0099 | 0.0054, | 0.0101 | 0.0101 | 0.0102 | 0.0103 | 0.0104 | 0.0107 |
| MR-Egger | 0.077, | 0.078, | 0.077, | 0.077, | 0.076, | 0.075, | 0.075, | 0.072, | 0.077, |
| | -0.0769, | -0.0286, | -0.0093, | 0.0100, | 0.0197, | 0.0294, | 0.0487, | 0.0680, | 0.1163, |
| | 0.9564, | 0.9563, | 0.9562, | 0.9562, | 0.9561, | 0.9561, | 0.9561, | 0.9560, | 0.9559, |
| | 0.8961 | 0.896 | 0.896 | 0.896 | 0.8959 | 0.8959 | 0.8959 | 0.8959 | 0.8958 |
| MR-Weighted-Median | 1.000, | 0.981, | 0.634, | 0.083, | 0.027, | 0.087, | 0.625, | 0.964, | 1.000, |
| | -0.0992, | -0.0495, | -0.0297, | -0.0099, | 0.0000, | 0.0099, | 0.0298, | 0.0496, | 0.0992, |
| | 0.0114, | 0.0117, | 0.0118, | 0.0118, | 0.0119, | 0.0119, | 0.0120, | 0.0122, | 0.0126, |
| | 0.0127 | 0.013 | 0.0131 | 0.0132 | 0.0132 | 0.0133 | 0.0134 | 0.0136 | 0.014 |
| MR-Weighted-Mode | 1.000, | 0.895, | 0.457, | 0.060, | 0.017, | 0.061, | 0.433, | 0.879, | 1.000, |
| | -0.0994, | -0.0495, | -0.0297, | -0.0098, | 0.0002, | 0.0101, | 0.0300, | 0.0499, | 0.0997, |
| | 0.0134, | 0.0137, | 0.0138, | 0.0141, | 0.0142, | 0.0140, | 0.0142, | 0.0143, | 0.0148, |
| MR-RAPS1 | 0.0157 | 0.016 | 0.0161 | 0.0162 0.097, | 0.0163 0.100, | 0.0164 | 0.0166 | 0.0167 | 0.0172 |
| IVIN-KAP31 | 0.080, -0.0973, | -0.0473, | 0.086, -0.0273, | -0.0073, | 0.100, 0.0027, | 0.097, 0.0127, | 0.088, 0.0327, | 0.081, 0.0527, | 0.102, 0.1027, |
| | 0.1657, | 0.1658, | 0.1658, | 0.1658, | 0.0027, | 0.0127, | 0.0327, | 0.0527, | 0.1659, |
| | 0.1637, | 0.1638, | 0.1638, | 0.1638, | 0.1638, | 0.1638, | 0.1638, | 0.1607 | 0.1639, |
| MR-RAPS2 | 0.997, | 0.995, | 0.960, | 0.756, | 0.706, | 0.760, | 0.953, | 0.992, | 0.995, |
| 1411 02 | 0.4018, | 0.4899, | 0.5570, | 0.736, | 0.700, | 0.760, | 0.4676, | 0.5156, | 1.0016, |
| | 2.9379, | 2.6637, | 3.2538, | 3.1360, | 2.3930, | 5.9183, | 2.5363, | 2.6431, | 2.9849, |
| | 0.0301 | 0.0277 | 0.0277 | 0.0269 | 0.0252 | 0.0271 | 0.0262 | 0.025 | 0.0319 |
| MR-RAPS3 | 0.970, | 0.940, | 0.917, | 0.917, | 0.910, | 0.898, | 0.907, | 0.921, | 0.952, |
| | -0.2056, | -0.0977, | -0.0556, | -0.0144, | 0.0057, | 0.0254, | 0.0637, | 0.1004, | 0.1861, |
| | 0.3506, | 0.3434, | 0.3384, | 0.3326, | 0.3297, | 0.3267, | 0.3204, | 0.3137, | 0.2963, |
| | 0.0203 | 0.0198 | 0.0196 | 0.0193 | 0.0191 | 0.0189 | 0.0186 | 0.0183 | 0.0177 |
| | 1.000, | 1.000, | 0.995, | 0.965, | 0.953, | 0.962, | 0.993, | 1.000, | 1.000, |
| MR-RAPS4 | | | | | | | 0.6407, | 0.6812, | 0.7718, |
| MR-RAPS4 | 0.3556, | 0.4648, | 0.4820, | 0.5276, | 0.5601, | 0.5651, | 0.0407, | 0.0612, | 0.7710, |
| MR-RAPS4 | 0.3556, 1.0514, 0.0168 | 0.4648, 1.0059, 0.0162 | 0.4820, 0.9893, 0.0169 | 0.5276, 0.9934, 0.0168 | 0.5601, 0.9828, | 0.9625, 0.0156 | 0.0407, 0.9894, 0.0163 | 0.9645, | 0.9746, 0.0166 |

Table S53: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE satisfied, q=0.4, and N=50000.

| ((| <i>' '</i> | | | | , I | | | | |
|--------------------|---------------------|----------------------|----------------------|----------------------|---------------------|---------------------|---------------------|---------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.834, | 0.317, | 0.132, | 0.033, | 0.023, | 0.029, | 0.095, | 0.265, | 0.765, |
| | -0.0882, | -0.0410, | -0.0241, | -0.0090, | -0.0017, | 0.0058, | 0.0210, | 0.0378, | 0.0845, |
| | 0.0294, | 0.0270, | 0.0254, | 0.0237, | 0.0234, | 0.0235, | 0.0252, | 0.0273, | 0.0310, |
| | 0.0286 | 0.0283 | 0.0279 | 0.0278 | 0.0279 | 0.028 | 0.0286 | 0.0293 | 0.0309 |
| cML-MA-AIC-Profile | 0.833, | 0.311, | 0.131, | 0.033, | 0.021, | 0.030, | 0.095, | 0.263, | 0.762, |
| | -0.0884, | -0.0410, | -0.0241, | -0.0090, | -0.0017, | 0.0058, | 0.0210, | 0.0378, | 0.0847, |
| | 0.0295, | 0.0270, | 0.0254, | 0.0237, | 0.0234, | 0.0235, | 0.0252, | 0.0274, | 0.0311, |
|) // LTC | 0.0288 | 0.0284 | 0.0281 | 0.028 | 0.028 | 0.0281 | 0.0287 | 0.0294 | 0.0311 |
| cML-AIC | 0.929, | 0.501, | 0.273, | 0.121, | 0.094, | 0.101, | 0.224, | 0.437, | 0.879, |
| | -0.0945, 0.0316, | -0.0460, 0.0308, | -0.0274, 0.0303, | -0.0103, 0.0294, | -0.0017, 0.0294, | 0.0072, 0.0292, | 0.0239, 0.0308, | 0.0422, 0.0317, | 0.0909, 0.0336, |
| | 0.0316, | 0.0308, | 0.0303, | 0.0294, | 0.0294, | 0.0292, | 0.0308, | 0.0317, | 0.0336, |
| cML-AIC-Profile | 0.925, | 0.499, | 0.0242 | 0.0244 | 0.0243 | 0.0240 | 0.0246 | 0.432, | 0.875, |
| CIME THE Frome | -0.0947, | -0.0460, | -0.0275, | -0.0103, | -0.0017, | 0.0072, | 0.0240, | 0.0423, | 0.0910, |
| | 0.0318, | 0.0309, | 0.0303, | 0.0294, | 0.0294, | 0.0292, | 0.0309, | 0.0317, | 0.0337, |
| | 0.0237 | 0.0241 | 0.0243 | 0.0245 | 0.0246 | 0.0247 | 0.025 | 0.0252 | 0.0259 |
| cML-MA-BIC | 0.996, | 0.631, | 0.295, | 0.061, | 0.039, | 0.068, | 0.246, | 0.549, | 0.982, |
| | -0.1007, | -0.0508, | -0.0308, | -0.0109, | -0.0010, | 0.0090, | 0.0289, | 0.0488, | 0.0987, |
| | 0.0220, | 0.0223, | 0.0224, | 0.0225, | 0.0226, | 0.0227, | 0.0229, | 0.0233, | 0.0238, |
| | 0.0219 | 0.0223 | 0.0225 | 0.0226 | 0.0227 | 0.0229 | 0.0231 | 0.0233 | 0.024 |
| cML-MA-BIC-Profile | 0.996, | 0.626, | 0.294, | 0.061, | 0.039, | 0.067, | 0.245, | 0.548, | 0.981, |
| | -0.1007, | -0.0508, | -0.0308, | -0.0109, | -0.0010, | 0.0090, | 0.0289, | 0.0488, | 0.0987, |
| | 0.0220, | 0.0223, | 0.0224, | 0.0225, | 0.0226, | 0.0227, | 0.0229, | 0.0233, | 0.0238, |
| AH DIG | 0.022 | 0.0224 | 0.0225 | 0.0227 | 0.0228 | 0.0229 | 0.0232 | 0.0234 | 0.0241 |
| cML-BIC | 0.996, | 0.640, | 0.308, | 0.067, | 0.043, | 0.074, | 0.254, | 0.564, | 0.985, |
| | -0.1009, | -0.0509, | -0.0309, | -0.0109, | -0.0009, | 0.0091, | 0.0291, | 0.0490, | 0.0990, |
| | 0.0219, 0.0216 | 0.0222, 0.022 | 0.0225, 0.0222 | 0.0226, 0.0224 | 0.0227, 0.0225 | 0.0228, 0.0226 | 0.0230, 0.0228 | 0.0232, 0.023 | 0.0238, 0.0237 |
| cML-BIC-Profile | 0.0216 | 0.022 | 0.0222 | 0.0224 | 0.0225 | 0.0226 | 0.0228 | 0.023 | 0.0237 |
| CIVIL-DIC-FIOIRE | -0.1009, | -0.0509, | -0.0309, | -0.0109, | -0.0009, | 0.074, 0.0091, | 0.253, 0.0291, | 0.559, | 0.985, |
| | 0.0219, | 0.0222, | 0.0225, | 0.0226, | 0.0227, | 0.0031, | 0.0231, | 0.0490, | 0.0238, |
| | 0.0217 | 0.0222, | 0.0223, | 0.0224 | 0.0227, | 0.0226 | 0.0229 | 0.0232, | 0.0238 |
| MR-Mix | 0.939, | 0.389, | 0.128, | 0.020, | 0.016, | 0.027, | 0.120, | 0.337, | 0.901, |
| | -0.1039, | -0.0510, | -0.0304, | -0.0102, | -0.0002, | 0.0096, | 0.0291, | 0.0480, | 0.0941, |
| | 0.0246, | 0.0246, | 0.0245, | 0.0245, | 0.0244, | 0.0244, | 0.0244, | 0.0243, | 0.0242, |
| | 0.0978 | 0.0314 | 0.0313 | 0.031 | 0.031 | 0.0309 | 0.031 | 0.0307 | 0.0309 |
| MR-ContMix | 0.993, | 0.633, | 0.308, | 0.079, | 0.059, | 0.083, | 0.248, | 0.550, | 0.973, |
| | -0.1005, | -0.0509, | -0.0311, | -0.0113, | -0.0014, | 0.0085, | 0.0283, | 0.0483, | 0.0980, |
| | 0.0231, | 0.0234, | 0.0237, | 0.0240, | 0.0241, | 0.0242, | 0.0244, | 0.0247, | 0.0255, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.983, | 0.597, | 0.274, | 0.065, | 0.043, | 0.064, | 0.227, | 0.508, | 0.961, |
| | -0.1004, | -0.0509, | -0.0312, | -0.0114, | -0.0014, | 0.0085, | 0.0284, | 0.0482, | 0.0982, |
| | 0.0229, | 0.0229, | 0.0231, | 0.0235, | 0.0235, | 0.0236, | 0.0237, | 0.0241, | 0.0251, |
| MD DDECCO | 0.023 | 0.0235 | 0.0237 | 0.0239 | 0.024 | 0.0241 | 0.0243 | 0.0245 | 0.0251 |
| MR-PRESSO | 0.753, -0.0916, | 0.488, -0.0435, | 0.327, -0.0255, | 0.249, -0.0068, | 0.233, 0.0032, | 0.254, 0.0127, | 0.339, 0.0298, | 0.478, 0.0479, | 0.762, 0.0967, |
| | 0.1689, | 0.1662, | 0.1652, | 0.1635, | 0.0032, | 0.0127, | 0.0298, | 0.0479, | 0.0507, |
| | 0.1085, | 0.0472 | 0.1032, | 0.1033, | 0.1020, | 0.1032, | 0.1000, | 0.0445 | 0.1330, |
| MR-IVW | 0.089, | 0.072, | 0.073, | 0.070, | 0.068, | 0.065, | 0.064, | 0.068, | 0.079, |
| | -0.0974, | -0.0473, | -0.0272, | -0.0072, | 0.0028, | 0.0128, | 0.0328, | 0.0528, | 0.1028, |
| | 0.2377, | 0.2376, | 0.2376, | 0.2376, | 0.2376, | 0.2376, | 0.2375, | 0.2375, | 0.2375, |
| | 0.2347 | 0.2347 | 0.2347 | 0.2347 | 0.2347 | 0.2347 | 0.2347 | 0.2347 | 0.2347 |
| MR-IVW-Oracle | 0.988, | 0.592, | 0.257, | 0.044, | 0.029, | 0.055, | 0.224, | 0.502, | 0.974, |
| | -0.1003, | -0.0506, | -0.0307, | -0.0109, | -0.0009, | 0.0090, | 0.0289, | 0.0488, | 0.0985, |
| | 0.0217, | 0.0220, | 0.0221, | 0.0223, | 0.0224, | 0.0225, | 0.0226, | 0.0228, | 0.0234, |
| | 0.0232 | 0.0236 | 0.0238 | 0.024 | 0.0242 | 0.0243 | 0.0245 | 0.0247 | 0.0254 |
| MR-Egger | 0.067, | 0.064, | 0.065, | 0.065, | 0.066, | 0.067, | 0.067, | 0.067, | 0.066, |
| | -0.0648, | -0.0214, | -0.0041, | 0.0133, | 0.0219, | 0.0306, | 0.0480, | 0.0653, | 0.1086, |
| | 1.2200, | 1.2197, | 1.2196, | 1.2195, | 1.2195, | 1.2194, | 1.2193, | 1.2192, | 1.2190, |
| MD Walaka 134 P | 1.2119 | 1.2119 | 1.2119 | 1.2119 | 1.2119 | 1.2119 | 1.2119 | 1.2119 | 1.212 |
| MR-Weighted-Median | 0.917, | 0.388, | 0.150, | 0.034, | 0.021, | 0.033, | 0.121, | 0.306, | 0.846, |
| | -0.0976, 0.0270, | -0.0496, 0.0273, | -0.0305, 0.0275, | -0.0112, 0.0276, | -0.0016, 0.0277, | 0.0080, 0.0278, | 0.0273, 0.0282, | 0.0465, 0.0285, | 0.0943, 0.0291, |
| | 0.0270, | 0.0273, | 0.0275, | 0.0276, 0.0306 | 0.0277, | 0.0278, | 0.0282, | 0.0285, | 0.0291, |
| MR-Weighted-Mode | 0.966, | 0.0301 | 0.0303 | 0.0300 | 0.0307 | 0.0309 | 0.0312 | 0.388, | 0.0324 |
| g.med mode | -0.0991, | -0.0503, | -0.0307, | -0.0113, | -0.0014, | 0.0082, | 0.0276, | 0.0473, | 0.0959, |
| | 0.0244, | 0.0250, | 0.0252, | 0.0253, | 0.0254, | 0.0256, | 0.0258, | 0.0261, | 0.0267, |
| | 0.0265 | 0.027 | 0.0272 | 0.0275 | 0.0276 | 0.0277 | 0.028 | 0.0283 | 0.029 |
| MR-RAPS1 | 0.095, | 0.076, | 0.074, | 0.070, | 0.068, | 0.065, | 0.061, | 0.065, | 0.083, |
| | -0.0993, | -0.0493, | -0.0293, | -0.0093, | 0.0007, | 0.0107, | 0.0307, | 0.0507, | 0.1006, |
| | 0.2340, | 0.2340, | 0.2340, | 0.2340, | 0.2340, | 0.2340, | 0.2340, | 0.2340, | 0.2340, |
| | 0.2292 | 0.2292 | 0.2292 | 0.2292 | 0.2292 | 0.2292 | 0.2292 | 0.2292 | 0.2293 |
| MR-RAPS2 | 0.085, | 0.063, | 0.053, | 0.053, | 0.056, | 0.051, | 0.055, | 0.054, | 0.072, |
| | -0.0999, | -0.0492, | -0.0285, | -0.0088, | 0.0006, | 0.0116, | 0.0300, | 0.0509, | 0.1014, |
| | 0.2354, | 0.2340, | 0.2317, | 0.2337, | 0.2326, | 0.2334, | 0.2340, | 0.2337, | 0.2348, |
| 1 m p 1 mm | 0.2385 | 0.2376 | 0.2369 | 0.237 | 0.2372 | 0.2378 | 0.2379 | 0.2379 | 0.2387 |
| MR-RAPS3 | 0.888, | 0.895, | 0.888, | 0.897, | 0.896, | 0.894, | 0.887, | 0.884, | 0.894, |
| | -2.9695, 58.2053 | -0.7341, 19.9493, | 1.5759, | -0.5554, 17.9349, | -0.4997, 12.1421 | -0.4092, 17.3224 | 0.1299, | 0.3781, | 1.5471, |
| | 58.2053, 314.389 | 19.9493, 42.8006 | 57.7885, 294.0363 | 24.6186 | 12.1421, 14.5071 | 17.3224, 23.2788 | 9.1446, 10.8243 | 11.4410, 10.2028 | 20.6127 47.8447 |
| | 0.992, | 0.993, | 0.987, | 0.982, | 0.970, | 0.977, | 0.978, | 0.991, | 1.000, |
| MR_R A DQA | 0.224 | | | | | | | | -0.3085 |
| MR-RAPS4 | | 0.1808 | 0.1103 | () () () () () | 0.07/01 | | | | |
| MR-RAPS4 | 0.3520, 1.4681, | 0.1808, 1.5481, | 0.1103, 1.5868, | 0.0891, 1.5686, | 0.0791, 1.5665, | 0.0371, 1.5944, | -0.1037, 1.6249, | -0.1298, 1.5901, | 1.5074, |

Table S54: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE satisfied, q=0.4, and N=100000.

| // | <i>' '</i> | | | | , <u>1</u> | | | | |
|----------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.978, | 0.541, | 0.208, | 0.042, | 0.028, | 0.045, | 0.228, | 0.541, | 0.950, |
| | -0.0906, | -0.0413, | -0.0229, | -0.0069, | 0.0004, | 0.0079, | 0.0238, | 0.0420, | 0.0905, |
| | 0.0201, | 0.0197, | 0.0183, | 0.0166, | 0.0165, | 0.0171, | 0.0192, | 0.0212, | 0.0230, |
| | 0.02 | 0.02 | 0.0197 | 0.0195 | 0.0195 | 0.0197 | 0.0202 | 0.0209 | 0.0219 |
| cML-MA-AIC-Profile | 0.977, | 0.538, | 0.208, | 0.041, | 0.028, | 0.045, | 0.227, | 0.540, | 0.950, |
| | -0.0908, | -0.0413, | -0.0229, | -0.0069, | 0.0004, | 0.0079, | 0.0239, | 0.0420, | 0.0906, |
| | 0.0202, | 0.0197, | 0.0183, | 0.0166, | 0.0165, | 0.0171, | 0.0192, | 0.0212, | 0.0231, |
|) // LIC | 0.0201 | 0.0201 | 0.0198 | 0.0195 | 0.0196 | 0.0197 | 0.0203 | 0.021 | 0.0219 |
| cML-AIC | 0.993, | 0.730, | 0.377, | 0.113, | 0.096, | 0.134, | 0.384, | 0.699, | 0.980, |
| | -0.0954, | -0.0456, | -0.0262, | -0.0079, | 0.0003, | 0.0089, | 0.0266, | 0.0461, | 0.0954, |
| | 0.0216, 0.0164 | 0.0219, 0.0167 | 0.0213, 0.0169 | 0.0204, 0.017 | 0.0204, 0.0171 | 0.0210, 0.0172 | 0.0222, 0.0174 | 0.0233, 0.0176 | 0.0243, 0.0181 |
| cML-AIC-Profile | 0.993, | 0.0107 | 0.0109 | 0.017 | 0.0171 | 0.0172 | 0.384, | 0.699, | 0.980, |
| CIVIL-AIC-I TOILIC | -0.0955, | -0.0457, | -0.0262, | -0.0079, | 0.0003, | 0.0089, | 0.0266, | 0.0462, | 0.0955, |
| | 0.0217, | 0.0220, | 0.0213, | 0.0204, | 0.0204, | 0.0210, | 0.0222, | 0.0233, | 0.0244, |
| | 0.0165 | 0.0168 | 0.0169 | 0.0171 | 0.0172 | 0.0173 | 0.0174 | 0.0176 | 0.0181 |
| cML-MA-BIC | 1.000, | 0.887, | 0.480, | 0.083, | 0.050, | 0.092, | 0.471, | 0.877, | 1.000, |
| | -0.0996, | -0.0495, | -0.0295, | -0.0095, | 0.0005, | 0.0104, | 0.0304, | 0.0504, | 0.1005, |
| | 0.0149, | 0.0152, | 0.0153, | 0.0154, | 0.0155, | 0.0156, | 0.0158, | 0.0160, | 0.0164, |
| | 0.0153 | 0.0156 | 0.0157 | 0.0159 | 0.0159 | 0.016 | 0.0162 | 0.0163 | 0.0168 |
| cML-MA-BIC-Profile | 1.000, | 0.887, | 0.479, | 0.083, | 0.049, | 0.091, | 0.469, | 0.877, | 1.000, |
| | -0.0996, | -0.0495, | -0.0295, | -0.0095, | 0.0005, | 0.0104, | 0.0304, | 0.0504, | 0.1005, |
| | 0.0149, | 0.0152, | 0.0153, | 0.0154, | 0.0155, | 0.0156, | 0.0158, | 0.0160, | 0.0164, |
| | 0.0154 | 0.0156 | 0.0157 | 0.0159 | 0.016 | 0.016 | 0.0162 | 0.0164 | 0.0168 |
| cML-BIC | 1.000, | 0.895, | 0.487, | 0.092, | 0.055, | 0.094, | 0.482, | 0.884, | 1.000, |
| | -0.0997, | -0.0496, | -0.0296, | -0.0096, | 0.0004, | 0.0104, | 0.0304, | 0.0505, | 0.1005, |
| | 0.0149, | 0.0152, | 0.0153, | 0.0154, | 0.0155, | 0.0156, | 0.0157, | 0.0159, | 0.0164, |
| aML DIG D. Cl | 0.0152 | 0.0154 | 0.0155 | 0.0157 | 0.0157 | 0.0158 | 0.016 | 0.0161 | 0.0166 |
| cML-BIC-Profile | 1.000, -0.0997, | 0.895, | 0.487, | 0.091, -0.0096, | 0.055, | 0.093, 0.0104, | 0.481, | 0.884, | 1.000, |
| | -0.0997, 0.0149, | -0.0496, 0.0152, | -0.0296, 0.0153, | -0.0096, 0.0154, | 0.0004, 0.0155, | 0.0104, 0.0156, | 0.0304, 0.0157, | 0.0505, 0.0159, | 0.1005, 0.0164, |
| | 0.0149, | 0.0152, | 0.0156 | 0.0154, | 0.0153, | 0.0150, | 0.0157, | 0.0159, | 0.0166 |
| MR-Mix | 0.993, | 0.676, | 0.0130 | 0.035, | 0.017, | 0.0139 | 0.244, | 0.644, | 0.988, |
| IVIIX-IVIIX | -0.1033, | -0.0506, | -0.0300, | -0.0097, | 0.0003, | 0.0102, | 0.0297, | 0.0488, | 0.0952, |
| | 0.0174, | 0.0174, | 0.0174, | 0.0174, | 0.0175, | 0.0175, | 0.0175, | 0.0175, | 0.0176, |
| | 0.0225 | 0.0223 | 0.0223 | 0.0223 | 0.0223 | 0.0223 | 0.0223 | 0.0222 | 0.0223 |
| MR-ContMix | 1.000, | 0.883, | 0.480, | 0.102, | 0.065, | 0.109, | 0.480, | 0.869, | 1.000, |
| | -0.0993, | -0.0493, | -0.0294, | -0.0094, | 0.0006, | 0.0105, | 0.0305, | 0.0505, | 0.1005, |
| | 0.0157, | 0.0160, | 0.0162, | 0.0163, | 0.0164, | 0.0165, | 0.0166, | 0.0168, | 0.0171, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.999, | 0.867, | 0.432, | 0.077, | 0.047, | 0.089, | 0.431, | 0.840, | 0.999, |
| | -0.0996, | -0.0494, | -0.0295, | -0.0096, | 0.0004, | 0.0103, | 0.0303, | 0.0500, | 0.1001, |
| | 0.0159, | 0.0159, | 0.0162, | 0.0163, | 0.0162, | 0.0163, | 0.0164, | 0.0167, | 0.0170, |
| | 0.0161 | 0.0164 | 0.0166 | 0.0167 | 0.0168 | 0.0169 | 0.0171 | 0.0172 | 0.0177 |
| MR-PRESSO | 0.669, | 0.508, | 0.369, | 0.244, | 0.225, | 0.251, | 0.366, | 0.512, | 0.671, |
| | -0.1132, | -0.0636, | -0.0445, | -0.0249, | -0.0154, | -0.0056, | 0.0145, | 0.0331, | 0.0827, |
| | 0.2158, 0.0802 | 0.2152, 0.0796 | 0.2143, 0.0784 | 0.2137, 0.0774 | 0.2138, 0.0774 | 0.2135, 0.0771 | 0.2132, 0.0768 | 0.2119, | 0.2105, |
| MR-IVW | 0.0802 | 0.0796 | 0.0784 | 0.0774 | 0.0774 | 0.0771 | 0.0768 | 0.0755 0.076, | 0.0738 |
| IVIIX-I V VV | -0.1134, | -0.0631, | -0.0430, | -0.0229, | -0.0128, | -0.0028, | 0.077, | 0.070, | 0.091, |
| | 0.2438, | 0.2438, | 0.2437, | 0.2437, | 0.2437, | 0.2437, | 0.0173, | 0.0374, | 0.0870, |
| | 0.2328 | 0.2328 | 0.2328 | 0.2328 | 0.2328 | 0.2328 | 0.2328 | 0.2328 | 0.2327 |
| MR-IVW-Oracle | 1.000, | 0.873, | 0.426, | 0.065, | 0.035, | 0.074, | 0.429, | 0.840, | 1.000, |
| WINCE TO WE OF GROOM | -0.0994, | -0.0495, | -0.0295, | -0.0096, | 0.0004, | 0.0104, | 0.0304, | 0.0503, | 0.1003, |
| | 0.0147, | 0.0150, | 0.0151, | 0.0153, | 0.0153, | 0.0154, | 0.0156, | 0.0157, | 0.0162, |
| | 0.0163 | 0.0166 | 0.0167 | 0.0168 | 0.0169 | 0.017 | 0.0172 | 0.0173 | 0.0178 |
| MR-Egger | 0.075, | 0.079, | 0.081, | 0.080, | 0.080, | 0.080, | 0.079, | 0.080, | 0.082, |
| - | -0.1044, | -0.0576, | -0.0389, | -0.0203, | -0.0109, | -0.0016, | 0.0171, | 0.0357, | 0.0824, |
| | 1.2836, | 1.2832, | 1.2831, | 1.2829, | 1.2829, | 1.2828, | 1.2826, | 1.2825, | 1.2822, |
| | 1.2414 | 1.2413 | 1.2413 | 1.2413 | 1.2412 | 1.2412 | 1.2412 | 1.2412 | 1.2411 |
| MR-Weighted-Median | 0.999, | 0.668, | 0.260, | 0.057, | 0.030, | 0.059, | 0.253, | 0.614, | 0.989, |
| | -0.0976, | -0.0488, | -0.0292, | -0.0097, | 0.0000, | 0.0098, | 0.0293, | 0.0488, | 0.0977, |
| | 0.0189, | 0.0193, | 0.0194, | 0.0197, | 0.0199, | 0.0200, | 0.0202, | 0.0205, | 0.0212, |
| MD W. 1. 125 1 | 0.0208 | 0.0211 | 0.0213 | 0.0215 | 0.0216 | 0.0217 | 0.0219 | 0.0221 | 0.0227 |
| MR-Weighted-Mode | 1.000, | 0.740, | 0.315, | 0.052, | 0.037, | 0.063, | 0.339, | 0.728, | 1.000, |
| | -0.0984, | -0.0487, 0.0176, | -0.0288, 0.0175, | -0.0091, 0.0176, | 0.0008, | 0.0105, 0.0178, | 0.0303, 0.0179, | 0.0503, 0.0181, | 0.0996, 0.0187, |
| | 0.0171, 0.0188 | 0.0176, | 0.0175, | 0.0176, | 0.0177, 0.0195 | 0.0178, | 0.0179, | 0.0181, | 0.0187, |
| MR-RAPS1 | 0.0188 | 0.0191 | 0.0192 | 0.0194 | 0.0193 | 0.0193 | 0.0198 | 0.02 | 0.0203 |
| MIC ICH 91 | -0.1123, | -0.0623, | -0.0423, | -0.0223, | -0.0123, | -0.0023, | 0.071, | 0.0377, | 0.093, |
| | 0.2371, | 0.2371, | 0.2371, | 0.2371, | 0.2371, | 0.2371, | 0.2371, | 0.2371, | 0.2372, |
| | 0.2272 | 0.2272 | 0.2272 | 0.2272 | 0.2272 | 0.2272 | 0.2272 | 0.2272 | 0.2273 |
| MR-RAPS2 | 0.103, | 0.073, | 0.071, | 0.067, | 0.067, | 0.066, | 0.062, | 0.063, | 0.069, |
| ** | -0.1130, | -0.0628, | -0.0433, | -0.0228, | -0.0131, | -0.0030, | 0.0176, | 0.0362, | 0.0872, |
| | 0.2373, | 0.2369, | 0.2370, | 0.2355, | 0.2373, | 0.2364, | 0.2358, | 0.2373, | 0.2379, |
| | 0.2359 | 0.2361 | 0.2363 | 0.2359 | 0.2364 | 0.2361 | 0.2359 | 0.2366 | 0.2368 |
| MR-RAPS3 | 0.925, | 0.932, | 0.922, | 0.920, | 0.917, | 0.914, | 0.925, | 0.931, | 0.925, |
| | -0.8929, | 0.7958, | 0.0503, | 0.0199, | 0.2883, | 1.4861, | 0.1574, | 0.7047, | 0.8846, |
| | 18.0217, | 38.0980, | 7.6305, | 16.1430, | 11.2263, | 46.0627, | 11.9014, | 11.9321, | 16.3970 |
| | 19.6811 | 93.2854 | 4.0117 | 30.3805 | 6.7844 | 123.241 | 21.7929 | 9.4141 | 13.1956 |
| MR-RAPS4 | 0.979, | 0.985, | 0.983, | 0.980, | 0.981, | 0.983, | 0.985, | 0.999, | 0.998, |
| | 0.8757, | 0.6696, | 0.5895, | 0.4293, | 0.3695, | 0.2996, | 0.1714, | 0.0820, | -0.1306, |
| | | | | | | | | | |
| | 1.5868, 0.1991 | 1.6607, 0.2606 | 1.6646, 0.0987 | 1.7081, 0.0749 | 1.7272, 0.105 | 1.7692, 0.0683 | 1.6743, 0.0583 | 1.7151, 0.055 | 1.6148, 0.0519 |

Table S55: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE satisfied, q=0.4, and N=200000.

| | // | | | | , 1 | | | | |
|--|---|---|--|--|---|---|---|--|--|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.842, | 0.412, | 0.054, | 0.022, | 0.057, | 0.414, | 0.801, | 0.997, |
| CIVIL WITTING | -0.0936, | -0.0437, | -0.0245, | -0.0074, | 0.0002, | 0.0077, | 0.0246, | 0.0437, | 0.0933, |
| | 0.0142, | 0.0142, | 0.0134, | 0.0117, | 0.0115, | 0.0121, | 0.0140, | 0.0152, | 0.0160, |
| | 0.0143 | 0.0145 | 0.0143 | 0.0139 | 0.0139 | 0.014 | 0.0146 | 0.0151 | 0.0156 |
| cML-MA-AIC-Profile | 1.000, | 0.841, | 0.411, | 0.054, | 0.022, | 0.057, | 0.412, | 0.801, | 0.997, |
| CIVIL IVITE THE FIGURE | -0.0937, | -0.0437, | -0.0245, | -0.0074, | 0.0002, | 0.0077, | 0.0246, | 0.0437, | 0.0934, |
| | 0.0142, | 0.0142, | 0.0134, | 0.0117, | 0.0115, | 0.0121, | 0.0140, | 0.0152, | 0.0160, |
| | 0.0143 | 0.0145 | 0.0143 | 0.0139 | 0.0139 | 0.0121, | 0.0146 | 0.0151 | 0.0156 |
| cML-AIC | 1.000, | 0.925, | 0.612, | 0.0139 | 0.0139 | 0.163, | 0.595, | 0.911, | 0.999, |
| CIVIL-AIC | -0.0970, | -0.0471, | -0.0274, | -0.0088, | 0.092, | 0.103, | 0.0272, | 0.911, | |
| | 0.0151, | 0.0153, | 0.0152, | 0.0145, | 0.0000, | 0.0087, | 0.0272, | 0.0470, | 0.0968, 0.0168, |
| | 0.0131, | 0.0133, | 0.0132, | 0.0143, | 0.0143, | 0.0147, | 0.0139, | 0.0105, | 0.0108, |
| MI AIC D. GI. | | | | | | | | | |
| cML-AIC-Profile | 1.000, | 0.925, | 0.612, | 0.151, | 0.092, | 0.161, | 0.596, | 0.911, | 0.999, |
| | -0.0970, | -0.0471, | -0.0274, | -0.0088, | 0.0000, | 0.0087, | 0.0272, | 0.0470, | 0.0969, |
| | 0.0151, | 0.0153, | 0.0152, | 0.0145, | 0.0143, | 0.0147, | 0.0159, | 0.0163, | 0.0169, |
| M. M. DIG | 0.0118 | 0.0119 | 0.012 | 0.0122 | 0.0122 | 0.0123 | 0.0124 | 0.0125 | 0.0129 |
| cML-MA-BIC | 1.000, | 0.991, | 0.768, | 0.139, | 0.051, | 0.142, | 0.741, | 0.986, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0109, | 0.0111, | 0.0111, | 0.0112, | 0.0112, | 0.0113, | 0.0114, | 0.0115, | 0.0118, |
| | 0.0109 | 0.0111 | 0.0112 | 0.0113 | 0.0113 | 0.0114 | 0.0115 | 0.0116 | 0.0119 |
| CML-MA-BIC-Profile | 1.000, | 0.991, | 0.767, | 0.139, | 0.051, | 0.142, | 0.741, | 0.986, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0109, | 0.0111, | 0.0111, | 0.0112, | 0.0112, | 0.0113, | 0.0114, | 0.0115, | 0.0118, |
| | 0.0109 | 0.0111 | 0.0112 | 0.0113 | 0.0113 | 0.0114 | 0.0115 | 0.0116 | 0.0119 |
| cML-BIC | 1.000, | 0.992, | 0.771, | 0.146, | 0.055, | 0.150, | 0.748, | 0.989, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0998, |
| | 0.0109, | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0113, | 0.0114, | 0.0115, | 0.0118, |
| | 0.0108 | 0.011 | 0.0111 | 0.0111 | 0.0112 | 0.0113 | 0.0114 | 0.0115 | 0.0118 |
| cML-BIC-Profile | 1.000, | 0.992, | 0.769, | 0.145, | 0.055, | 0.150, | 0.746, | 0.989, | 1.000, |
| 10 1101110 | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0998 |
| | 0.0109, | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0033, | 0.0255, | 0.0115, | 0.0118, |
| | 0.0109, | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0113, | 0.0114, | 0.0115, | 0.0118 |
| MR-Mix | 0.999, | 0.901, | 0.473, | 0.0712 | 0.0112 | 0.0113 | 0.442, | 0.875, | 0.997, |
| IVIIX-IVIIX | -0.1041, | -0.0510, | -0.0305, | -0.0104, | -0.0005, | 0.0095, | 0.0290, | 0.0483, | 0.0945, |
| | 0.0136, | 0.0135, | | | 0.0134, | 0.0033, | 0.0230, | 0.0483, | 0.0943, |
| | 0.0136, | 0.0135, | 0.0135, | 0.0134, 0.0163 | 0.0134, | 0.0134, | 0.0134, 0.0163 | | 0.0133, |
| 100 C - 10 | | | 0.0164 | | | | | 0.0163 | |
| MR-ContMix | 1.000, | 0.990, | 0.776, | 0.160, | 0.069, | 0.166, | 0.757, | 0.985, | 1.000, |
| | -0.0999, | -0.0500, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0997, |
| | 0.0113, | 0.0114, | 0.0115, | 0.0116, | 0.0116, | 0.0117, | 0.0118, | 0.0119, | 0.0123 |
| 1 m 1 | NA | NA | NA | NA | NA NA | NA | NA 0.60# | NA | NA |
| MR-Lasso | 1.000, | 0.986, | 0.732, | 0.127, | 0.050, | 0.127, | 0.695, | 0.978, | 1.000, |
| | -0.0999, | -0.0500, | -0.0300, | -0.0101, | -0.0001, | 0.0099, | 0.0298, | 0.0497, | 0.0997, |
| | 0.0112, | 0.0114, | 0.0115, | 0.0115, | 0.0115, | 0.0115, | 0.0117, | 0.0119, | 0.0121, |
| | 0.0114 | 0.0117 | 0.0117 | 0.0119 | 0.0119 | 0.012 | 0.0121 | 0.0122 | 0.0126 |
| MR-PRESSO | 0.530, | 0.449, | 0.364, | 0.214, | 0.187, | 0.206, | 0.373, | 0.476, | 0.560, |
| | -0.1029, | -0.0532, | -0.0330, | -0.0131, | -0.0031, | 0.0064, | 0.0260, | 0.0462, | 0.0944, |
| | 0.2321, | 0.2317, | 0.2312, | 0.2310, | 0.2309, | 0.2306, | 0.2305, | 0.2299, | 0.2287 |
| | 0.1158 | 0.1145 | 0.1129 | 0.1122 | 0.1118 | 0.1109 | 0.1108 | 0.1094 | 0.1068 |
| MR-IVW | 0.097, | 0.073, | 0.067, | 0.068, | 0.069, | 0.073, | 0.071, | 0.073, | 0.084, |
| | -0.1017, | -0.0513, | -0.0312, | -0.0111, | -0.0010, | 0.0090, | 0.0292, | 0.0493, | 0.0995, |
| | 0.2428, | 0.2427, | 0.2427, | 0.2427, | 0.2427, | 0.2427, | 0.2427, | 0.2426, | 0.2426, |
| | 0.2339 | 0.2339 | 0.2339 | 0.2339 | 0.2339 | 0.2339 | 0.2338 | 0.2338 | 0.2338 |
| MR-IVW-Oracle | 1.000, | 0.989, | 0.728, | 0.119, | 0.043, | 0.119, | 0.695, | 0.983, | 1.000, |
| mic i v v Gracie | -0.1000, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0997 |
| | 0.0108, | 0.0109, | 0.0110, | 0.0111, | 0.0111, | 0.0055, | 0.0238, | 0.0438, | 0.0117 |
| | 0.0108, | 0.0109, | 0.0110, | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0114, | 0.0117 |
| MR-Egger | | 0.0118 | 0.0119 | 0.012 | 0.012 | | | 0.0123 | |
| | | | U.UO9. | | | | | | 0.070 |
| WINC Egger | 0.072, | | | | | 0.069, | 0.067, | | 0.070, |
| WIK Egger | -0.0795, | -0.0310, | -0.0116, | 0.0077, | 0.0174, | 0.0271, | 0.0465, | 0.0658, | 0.1142 |
| Mic Eggei | -0.0795, 1.2766, | -0.0310, 1.2764, | -0.0116, 1.2763, | 0.0077, 1.2762, | 0.0174, 1.2762, | 0.0271, 1.2761, | 0.0465, 1.2760, | 0.0658, 1.2760, | 0.1142 1.2758 |
| | -0.0795, 1.2766, 1.257 | -0.0310, 1.2764, 1.2569 | -0.0116, 1.2763, 1.2568 | 0.0077, 1.2762, 1.2568 | 0.0174, 1.2762, 1.2567 | 0.0271, 1.2761, 1.2567 | 0.0465, 1.2760, 1.2567 | 0.0658, 1.2760, 1.2566 | 0.1142 1.2758 1.2565 |
| | -0.0795, 1.2766, 1.257 1.000, | -0.0310, 1.2764, 1.2569 0.924, | -0.0116, 1.2763, 1.2568 0.518, | 0.0077, 1.2762, 1.2568 0.072, | 0.0174, 1.2762, 1.2567 0.032, | 0.0271, 1.2761, 1.2567 0.068, | 0.0465, 1.2760, 1.2567 0.470, | 0.0658, 1.2760, 1.2566 0.901, | 0.1142 1.2758 1.2565 1.000, |
| | -0.0795, 1.2766, 1.257 1.000, -0.0989, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, | -0.0116, 1.2763, 1.2568 0.518, -0.0298, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, | 0.0658, 1.2760, 1.2566 0.901, 0.0492, | 0.1142 1.2758 1.2565 1.000, 0.0985 |
| | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 |
| MR-Weighted-Median | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 |
| | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, |
| MR-Weighted-Median | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, 0.0098, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 |
| ИR-Weighted-Median | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, 0.0098, 0.0129, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 |
| MR-Weighted-Median MR-Weighted-Mode | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.0090, 0.0098, 0.0129, 0.014 | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 0.0147 |
| ИR-Weighted-Median | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, 0.0098, 0.0129, 0.014 | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 0.0147 |
| MR-Weighted-Median MR-Weighted-Mode | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.099, 0.0098, 0.0129, 0.014 0.066, 0.0073, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 0.0147 0.098, 0.0973 |
| MR-Weighted-Median MR-Weighted-Mode | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2379, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 0.077, -0.0527, 0.2379, | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2380, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, 0.2380, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, 0.0098, 0.0129, 0.014 0.066, 0.0073, 0.2380, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2380, | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 0.0147 0.098, 0.0973 0.2380 |
| MR-Weighted-Median MR-Weighted-Mode | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.099, 0.0098, 0.0129, 0.014 0.066, 0.0073, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 0.0147 0.098, 0.0973 |
| MR-Weighted-Median MR-Weighted-Mode | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2379, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 0.077, -0.0527, 0.2379, 0.2278 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2380, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, 0.2380, 0.2279 | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, 0.0098, 0.0129, 0.014 0.066, 0.0073, 0.2380, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2380, 0.2279 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2380, 0.2279 | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 0.0147 0.098, 0.0973 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2379, 0.2278 | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 -0.0527, 0.2379, 0.2278 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 0.035, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2279 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, 0.2380, 0.2279 | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0154 0.090, 0.0129, 0.0129, 0.0166, 0.0073, 0.2279 | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2279 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2279 | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149, 0.0161 1.000, 0.0993, 0.0135, 0.0147 0.098, 0.0973 0.2380 0.2279 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2379, 0.2278 0.184, -0.1014, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 0.077, -0.0527, 0.2278 0.02278 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 0.035, -0.0310, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2380, 0.2279 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, 0.2380, 0.2279 0.029, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, 0.0129, 0.014 0.066, 0.0073, 0.2380, 0.2279 | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2380, 0.2279 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2380, 0.2279 | 0.1142 1.2758 1.2565 1.000, 0.0985, 0.0149, 0.0161 1.000, 0.0993, 0.0135 0.0147 0.098, 0.0973 0.2279 0.185, 0.0992 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2379, 0.2278 0.184, -0.1014, 0.1316, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 0.077, -0.0527, 0.2379, 0.2278 0.062, -0.0525, 0.1360, | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 0.035, -0.0310, 0.1417, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2380, 0.2279 0.027, -0.0124, 0.1515, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, 0.2380, 0.2279 0.029, -0.0025, 0.1554, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, 0.0098, 0.0129, 0.014 0.066, 0.0073, 0.2380, 0.2279 0.034, 0.0080, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2380, 0.2279 0.047, 0.0281, 0.1553, | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2380, 0.2279 0.063, 0.0482, 0.1489, | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 0.0147 0.098, 0.0973 0.2380 0.2279 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2278 0.184, -0.1014, 0.1316, 0.1226 | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 -0.0527, 0.2278 0.062, -0.0525, 0.1360, 0.1264 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 0.035, -0.0310, 0.1417, 0.1305 | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2279 0.027, -0.0124, 0.1515, 0.134 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, 0.2279 0.029, -0.0025, 0.1554, 0.1346 | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0154 0.090, 0.0129, 0.014 0.066, 0.0073, 0.2279 0.034, 0.0080, 0.1578, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2279 0.047, 0.0281, 0.1553, 0.1351 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2279 0.063, 0.0482, 0.1489, 0.1301 | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 0.0147 0.098, 0.0973 0.2380 0.2279 0.185, 0.0992 0.1609 0.141 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2379, 0.2278 0.184, -0.1014, 0.1316, 0.1226 | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 -0.0527, 0.2379, 0.2278 0.062, -0.0525, 0.1360, 0.1264 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 0.035, -0.0310, 0.1417, 0.1305 0.953, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2380, 0.2279 0.027, -0.0124, 0.1515, 0.134 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, 0.2380, 0.2279 0.029, -0.0025, 0.1554, 0.1346 0.939, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0154 0.090, 0.0129, 0.0129, 0.014 0.066, 0.0073, 0.2380, 0.2279 0.034, 0.0080, 0.1578, 0.136 | 0.0465, 1.2760, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2380, 0.2279 0.047, 0.0281, 0.1553, 0.1351 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2380, 0.2279 0.063, 0.0482, 0.1489, 0.1301 0.951, | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 0.0147 0.098, 0.0973 0.2279 0.185, 0.0992 0.1609 0.141 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2379, 0.2278 0.184, -0.1014, 0.1316, 0.1226 0.955, -0.4771, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 0.077, -0.0527, 0.2379, 0.2278 0.062, -0.0525, 0.1360, 0.1264 0.943, -3.2576, | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 0.035, -0.0310, 0.1417, 0.1305 0.953, -0.2303, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2380, 0.2279 0.027, -0.0124, 0.1515, 0.134 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, 0.2380, 0.2279 0.029, -0.0025, 0.1554, 0.1346 0.939, -9.5439, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, 0.0129, 0.014 0.066, 0.0073, 0.2380, 0.2279 0.034, 0.0080, 0.1578, 0.136 | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2380, 0.2279 0.047, 0.0281, 0.1553, 0.1351 0.951, -0.3191, | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2380, 0.2279 0.063, 0.0482, 0.1489, 0.1301 | 0.1142 1.2758 1.2565 1.000, 0.0985 0.0149 0.0161 1.000, 0.0993 0.0135 0.0147 0.098, 0.0973 0.2279 0.185, 0.0993 0.141 0.090, 0.000, 0.0 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | -0.0795, 1.2766, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2278 0.184, -0.1014, 0.1136, 0.1226 0.955, -0.4771, 12.4874, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 -0.0527, 0.2278 0.062, -0.0525, 0.1360, 0.1264 0.943, -3.2576, 82.3207, | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 0.035, -0.0310, 0.1417, 0.1305 0.953, -0.2303, 8.2856, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2279 0.027, -0.0124, 0.1515, 0.134 0.941, 0.1716, 11.3534, | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, 0.2279 0.029, -0.0025, 0.1346 0.934, 9.5439, 229,1913, | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0154 0.090, 0.0129, 0.014 0.066, 0.0073, 0.2279 0.034, 0.0080, 0.1578, 0.136 | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2279 0.047, 0.0281, 0.1351 0.951, -0.3191, 17.9694, | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2279 0.063, 0.0482, 0.1489, 0.1301 0.951, 0.2955, 24.1995, | 0.1142, 1.2758, 1.2565 1.000, 0.0985, 0.0149, 0.0161 1.000, 0.0993, 0.0135, 0.0147 0.098, 0.0973, 0.2380, 0.2279 0.185, 0.0992, 0.1609, 0.1609, 0.1610, 0.4838, 6.9566 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 MR-RAPS3 | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2379, 0.2278 0.184, -0.1014, 0.1316, 0.1226 0.955, -0.4771, 12.4874, 5.8058 | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 -0.0527, 0.2379, 0.2278 0.062, -0.0525, 0.1264 0.943, -3.2576, 82.3207, 686.8739 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 0.035, -0.0310, 0.1417, 0.1305 0.953, -0.2303, 8.2856, 3.4314 | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2380, 0.2279 0.027, -0.0124, 0.1515, 0.134 0.941, 0.1716, 11.3534, 6.0882 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0028, 0.0128, 0.014 0.068, -0.0027, 0.2380, 0.2279 0.029, -0.0025, 0.1554, 0.1346 0.939, -9.5439, 229,1913, 1847,4207 | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, 0.0098, 0.0129, 0.014 0.066, 0.0073, 0.2380, 0.2279 0.034, 0.0080, 0.1578, 0.136 0.947, -0.7703, 19.8328, 26.7187 | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2380, 0.2279 0.047, 0.0281, 0.1553, 0.1351 0.951, -0.3191, 17,9694, 13,7273 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2380, 0.2279 0.063, 0.0482, 0.1301 0.951, 0.951, 0.955, 24.1995, 30.1402 | 0.1142, 1.2758, 1.2365 1.000, 0.0985, 0.0149, 0.0161 1.000, 0.0993, 0.0135, 0.0135, 0.0279 0.185, 0.0992, 0.1609, 0.141 0.950, 0.4838, 6.9566, |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2379, 0.2278 0.1316, 0.1316, 0.1326 0.955, -0.4771, 12.4874, 5.8058 0.982, | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 0.077, -0.0527, 0.2278 0.062, -0.0525, 0.1360, 0.1264 0.943, -3.2576, 82.3207, 686.8739 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 0.035, -0.0310, 0.1417, 0.1305 0.953, -0.2303, 8.2856, 3.4314 0.986, | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2380, 0.2279 0.027, -0.0124, 0.1515, 0.134 0.941, 0.1716, 11.3534, 6.0882 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0002, 0.0128, 0.014 0.068, -0.0027, 0.2380, 0.2279 0.029, -0.0025, 0.1554, 0.1346 0.939, -9.5439, 229,1913, 1847,4207 | 0.0271, 1.2761, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.099, 0.0129, 0.014 0.066, 0.0073, 0.2380, 0.2279 0.034, 0.0080, 0.1578, 0.136 0.947, -0.7703, 19.8328, 26.7187 0.987, | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2380, 0.2279 0.047, 0.0281, 0.1553, 0.1351 0.951, 1.79694, 13.7273 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2380, 0.2279 0.063, 0.1489, 0.1301 0.951, 0.2955, 24,1995, 30,1402 | 0.1142, 1.2758, 1.2565 1.000, 0.0985, 0.0149, 0.0161 1.000, 0.0993, 0.0135, 0.0147 0.098, 0.2279 0.185, 0.0973, 0.0993, 0.485, 0.6993, 0.4996, 0.4996, 0.4838, 6.9566, 3.6628 1.000, |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 MR-RAPS3 | -0.0795, 1.2766, 1.257 1.000, -0.0989, 0.0135, 0.0148 1.000, -0.0995, 0.0124, 0.0135 0.111, -0.1027, 0.2379, 0.2278 0.184, -0.1014, 0.1316, 0.1226 0.955, -0.4771, 12.4874, 5.8058 | -0.0310, 1.2764, 1.2569 0.924, -0.0496, 0.0138, 0.015 0.963, -0.0498, 0.0125, 0.0137 -0.0527, 0.2379, 0.2278 0.062, -0.0525, 0.1264 0.943, -3.2576, 82.3207, 686.8739 | -0.0116, 1.2763, 1.2568 0.518, -0.0298, 0.0140, 0.0151 0.598, -0.0299, 0.0125, 0.0138 0.072, -0.0327, 0.2379, 0.2279 0.035, -0.0310, 0.1417, 0.1305 0.953, -0.2303, 8.2856, 3.4314 | 0.0077, 1.2762, 1.2568 0.072, -0.0101, 0.0141, 0.0153 0.094, -0.0101, 0.0128, 0.0139 0.068, -0.0127, 0.2380, 0.2279 0.027, -0.0124, 0.1515, 0.134 0.941, 0.1716, 11.3534, 6.0882 | 0.0174, 1.2762, 1.2567 0.032, -0.0003, 0.0141, 0.0153 0.028, -0.0028, 0.0128, 0.014 0.068, -0.0027, 0.2380, 0.2279 0.029, -0.0025, 0.1554, 0.1346 0.939, -9.5439, 229,1913, 1847,4207 | 0.0271, 1.2761, 1.2567 0.068, 0.0096, 0.0142, 0.0154 0.090, 0.0098, 0.0129, 0.014 0.066, 0.0073, 0.2380, 0.2279 0.034, 0.0080, 0.1578, 0.136 0.947, -0.7703, 19.8328, 26.7187 | 0.0465, 1.2760, 1.2567 0.470, 0.0294, 0.0143, 0.0155 0.547, 0.0297, 0.0130, 0.0142 0.063, 0.0273, 0.2380, 0.2279 0.047, 0.0281, 0.1553, 0.1351 0.951, -0.3191, 17,9694, 13,7273 | 0.0658, 1.2760, 1.2566 0.901, 0.0492, 0.0144, 0.0157 0.948, 0.0497, 0.0133, 0.0143 0.067, 0.0473, 0.2380, 0.2279 0.063, 0.0482, 0.1301 0.951, 0.951, 0.955, 24.1995, 30.1402 | 0.1142, 1.2758, 1.2565 1.000, 0.0985, 0.0149, 0.0161 1.000, 0.0993, 0.0135, 0.0147 0.098, 0.2380, 0.2380, 0.2380, 0.973, 0.2380, 0.950, 0.441 0.950, 0.444 0.950, 0.466, 0.666, 0.666, 0.6628 |

Table S56: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE satisfied, q=0.6, and N=50000.

| , mean (SΣ(σ) | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|--------------------|-----------------------|-----------------------|----------------------|-----------------------|-----------------------|-----------------------|----------------------|-----------------------|--------------------|
| cML-MA-AIC | 0.660, | 0.176, | 0.056, | 0.018, | 0.014, | 0.022, | 0.062, | 0.159, | 0.607, |
| | -0.0828, 3.400e- | -0.0369, 3.040e- | -0.0213, 2.750e- | -0.0063, 2.610e- | 0.0007, 2.590e- | 0.0077, 2.600e- | 0.0221, 2.810e- | 0.0379, 3.050e- | 0.0832, 3.610e- |
| | 02, 0.0356 | 02, 0.0351 | 02, 0.0348 | 02, 0.0348 | 02, 0.0349 | 02, 0.0351 | 02, 0.0359 | 02, 0.0368 | 02, 0.03 |
| cML-MA-AIC-Profile | 0.655, | 0.172, | 0.056, | 0.018, | 0.014, | 0.020, | 0.062, | 0.156, | 0.606, |
| | -0.0830, | -0.0370, | -0.0213, | -0.0063, | 0.0008, | 0.0077, | 0.0221, | 0.0380, | 0.0833, |
| | 3.420e- | 3.050e- | 2.760e- | 2.610e- | 2.590e- | 2.600e- | 2.810e- | 3.060e- | 3.620e- |
| MLAIC | 02, 0.0358 | 02, 0.0354 | 02, 0.035 | 02, 0.035 | 02, 0.0351 | 02, 0.0353 | 02, 0.0361 | 02, 0.037 | 02, 0.03 |
| cML-AIC | 0.825, -0.0902, | 0.353, -0.0420, | 0.169, -0.0248, | 0.078, -0.0075, | 0.069, 0.0009, | 0.094, 0.0090, | 0.172, 0.0259, | 0.327, 0.0433, | 0.790, 0.0911, |
| | 3.760e- | 3.600e- | 3.420e- | 3.360e- | 3.330e- | 3.350e- | 3.520e- | 3.660e- | 4 080e- |
| | 02, 0.0291 | 02, 0.0296 | 02, 0.0298 | 02, 0.03 | 02, 0.0302 | 02, 0.0303 | 02, 0.0307 | 02, 0.031 | 02, 0.03 |
| cML-AIC-Profile | 0.825, | 0.351, | 0.169, | 0.075, | 0.068, | 0.091, | 0.168, | 0.317, | 0.790, |
| | -0.0905, | -0.0420, | -0.0248, | -0.0075, | 0.0009, | 0.0090, | 0.0259, | 0.0433, | 0.0912, |
| | 3.780e- | 3.600e- | 3.420e- | 3.360e- | 3.330e- | 3.350e- | 3.520e- | 3.660e- | 4.080e- |
| cML-MA-BIC | 02, 0.0293 | 02, 0.0298 | 02, 0.03 | 02, 0.0302 | 02, 0.0304 | 02, 0.0305 | 02, 0.0309 | 02, 0.0312 | 02, 0.03 |
| CML-MA-BIC | 0.946, -0.0991, | 0.429, -0.0490, | 0.187, -0.0290, | 0.065, -0.0090, | 0.053, 0.0009, | 0.076, 0.0109, | 0.191, 0.0308, | 0.412, 0.0508, | 0.920, 0.1009, |
| | 2.790e- | 2.830e- | 2.850e- | 2.870e- | 2.880e- | 2.900e- | 2.930e- | 2.960e- | 3.050e- |
| | 02, 0.0273 | 02, 0.0277 | 02, 0.0279 | 02, 0.0282 | 02, 0.0283 | 02, 0.0284 | 02, 0.0287 | 02, 0.029 | 02, 0.02 |
| ML-MA-BIC-Profile | 0.945, | 0.425, | 0.186, | 0.065, | 0.053, | 0.076, | 0.190, | 0.406, | 0.920, |
| | -0.0991, | -0.0490, | -0.0290, | -0.0090, | 0.0009, | 0.0109, | 0.0308, | 0.0508, | 0.1009, |
| | 2.790e- | 2.830e- | 2.850e- | 2.870e- | 2.880e- | 2.900e- | 2.930e- | 2.960e- | 3.050e- |
| | 02, 0.0274 | 02, 0.0278 | 02, 0.0281 | 02, 0.0283 | 02, 0.0284 | 02, 0.0285 | 02, 0.0288 | 02, 0.0291 | 02, 0.02 |
| cML-BIC | 0.949, | 0.444, | 0.193, | 0.069, | 0.057, | 0.080, | 0.199, | 0.422, | 0.927, |
| | -0.0993, 2.790e- | -0.0492, 2.840e- | -0.0291, 2.870e- | -0.0090, 2.890e- | 0.0010, | 0.0110, 2.920e- | 0.0310, 2.940e- | 0.0511, 2.980e- | 0.1012, 3.060e- |
| | 2.790e- 02, 0.0269 | 2.840e- 02, 0.0274 | 02, 0.0276 | 2.890e- 02, 0.0278 | 2.910e- 02, 0.028 | 02, 0.0281 | 02, 0.0283 | 02, 0.0286 | 02, 0.02 |
| cML-BIC-Profile | 0.948, | 0.443, | 0.192. | 0.068, | 0.056, | 0.079, | 0.198, | 0.416, | 0.927, |
| civil Bio Frome | -0.0993, | -0.0492, | 0.192, -0.0291, | -0.0090, | 0.0010, | 0.0110, | 0.0310, | 0.0511, | 0.1012, |
| | 2.790e- | 2.840e- | 2.870e- | 2.890e- | 2.910e- | 2.920e- | 2.940e- | 2.980e- | 3.060e- |
| | 02, 0.0271 | 02, 0.0275 | 02, 0.0277 | 02, 0.0279 | 02, 0.0281 | 02, 0.0282 | 02, 0.0285 | 02, 0.0288 | 02, 0.02 |
| MR-Mix | 0.879, | 0.337, | 0.141, | 0.038, | 0.036, | 0.053, | 0.146, | 0.306, | 0.854, |
| | -0.1008, | -0.0489, | -0.0289, | -0.0090, | 0.0009, | 0.0105, | 0.0297, | 0.0485, | 0.0937, |
| | 2.970e- 02, 0.0329 | 2.960e- 02, 0.0325 | 2.950e- | 2.950e- 02, 0.0325 | 2.960e- 02, 0.0325 | 2.960e- 02, 0.0327 | 2.960e- | 2.960e- 02, 0.0325 | 2.990e- |
| MR-ContMix | 0.948, | 0.455, | 02, 0.0326 0.204, | 0.081, | 0.067, | 0.089, | 02, 0.0327 0.211, | 0.437, | 02, 0.03 |
| WIK-COIRWIIX | -0.0986, | -0.0487, | -0.0287, | -0.0088, | 0.007, | 0.009, | 0.0311, | 0.457, | 0.1006, |
| | 2.860e- | 2.900e- | 2.930e- | 2.940e- | 2.960e- | 2.970e- | 3.010e- | 3.040e- | 3.130e- |
| | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA |
| MR-Lasso | 0.905, | 0.416, | 0.196, | 0.100, | 0.094, | 0.105, | 0.198, | 0.396, | 0.879, |
| | -0.1064, | -0.0559, | -0.0361, | -0.0160, | -0.0058, | 0.0036, | 0.0239, | 0.0437, | 0.0939, |
| | 2.198e- | 2.212e- | 2.213e- | 2.207e- | 2.213e- | 2.217e- | 2.211e- | 2.208e- | 2.183e- |
| MR-PRESSO | 01, 0.0363 0.574, | 01, 0.0364 0.329, | 01, 0.0366 | 01, 0.0368 0.170, | 01, 0.037 0.169, | 01, 0.0373 0.183, | 01, 0.0377 | 01, 0.0379 0.341, | 01, 0.03 |
| MK-PKESSO | -0.0951, | -0.0483, | 0.208, -0.0290, | -0.0101, | -0.0005, | 0.183, | 0.239, 0.0274, | 0.0473, | 0.391, |
| | 2.535e- | 2.509e- | 2.507e- | 2.510e- | 2.511e- | 2.505e- | 2.493e- | 2.486e- | 2.450e- |
| | 01, 0.0923 | 01, 0.0897 | 01, 0.0894 | 01, 0.0894 | 01, 0.0895 | 01, 0.0888 | 01, 0.0879 | 01, 0.0871 | 01, 0.08 |
| MR-IVW | 0.091, | 0.082, | 0.080, | 0.080, | 0.078, | 0.075, | 0.081, | 0.086, | 0.090, |
| | -0.0984, | -0.0481, | -0.0280, | -0.0079, | 0.0021, | 0.0122, | 0.0323, | 0.0523, | 0.1025, |
| | 2.956e- | 2.956e- | 2.955e- | 2.955e- | 2.955e- | 2.955e- | 2.955e- | 2.955e- | 2.955e- |
| MR-IVW-Oracle | 01, 0.2851 0.925, | 01, 0.285 0.394, | 01, 0.285 0.162, | 01, 0.285 0.058, | 01, 0.285 0.051, | 01, 0.285 0.064, | 01, 0.285 0.165, | 01, 0.285 0.377, | 01, 0.28 0.897, |
| WIK-I V W-Oracle | -0.0987, | -0.0489, | -0.0290, | -0.0091, | 0.001, | 0.004, | 0.103, | 0.377, 0.0507, | 0.897, |
| | 2.760e- | 2.810e- | 2.830e- | 2.860e- | 2.870e- | 2.880e- | 2.910e- | 2.940e- | 3.020e- |
| | 02, 0.0289 | 02, 0.0294 | 02, 0.0296 | 02, 0.0299 | 02, 0.03 | 02, 0.0301 | 02, 0.0304 | 02, 0.0307 | 02, 0.03 |
| MR-Egger | 0.077, | 0.074, | 02, 0.0296 0.071, | 0.071, | 02, 0.03 0.071, | 0.072, | 0.072, | 02, 0.0307 0.074, | 0.076, |
| - | -0.1458, | -0.1022, | -0.0847, | -0.0673, | -0.0586, | -0.0499, | -0.0324, | -0.0150, | 0.0285, |
| | 1.534e+00, | 1.534e+00, | 1.534e+00, | 1.534e+00, | 1.534e+00, | 1.533e+00, | 1.533e+00, | 1.533e+00, | 1.533e+ |
| ID Wainhtad M. di- | 1.465 | 1.465 | 1.465 | 1.465 | 1.465 | 1.465 | 1.464 | 1.464 | 1.464 |
| IR-Weighted-Median | 0.754, -0.0940, | 0.256, -0.0467, | 0.103, -0.0278, | 0.050, -0.0090, | 0.049, 0.0005, | 0.058, 0.0099, | 0.113, 0.0286, | 0.240, 0.0473, | 0.697, 0.0940, |
| | 3.560e- | 3.600e- | 3.630e- | 3.650e- | 3.660e- | 3.680e- | 3.730e- | 0.0473, 3.780e- | 3.910e- |
| | 02, 0.0358 | 02, 0.0363 | 02, 0.0366 | 02, 0.0368 | 02, 0.037 | 02, 0.0372 | 02, 0.0375 | 02, 0.0379 | 02, 0.03 |
| MR-Weighted-Mode | 0.715, | 0.381, | 0.287, | 0.239, | 0.225, | 0.223, | 0.275, | 0.367, | 0.616, |
| - | -0.0912, | -0.0462, | -0.0283, | -0.0104, | -0.0013, | 0.0077, | 0.0258, | 0.0433, | 0.0874, |
| | 5.560e- | 5.670e- | 5.700e- | 5.750e- | 5.780e- | 5.830e- | 5.920e- | 5.990e- | 6.310e- |
| 100 0 1 | 02, 0.0331 | 02, 0.0337 | 02, 0.034 | 02, 0.0344 | 02, 0.0346 | 02, 0.0348 | 02, 0.0352 | 02, 0.0357 | 02, 0.03 |
| MR-RAPS1 | 0.092, | 0.087, | 0.082, | 0.085, | 0.081, | 0.083, | 0.080, | 0.084, | 0.093, |
| | -0.0942, 2.912e- | -0.0442, 2.912e- | -0.0242, 2.912e- | -0.0042, 2.912e- | 0.0058, 2.912e- | 0.0158, 2.912e- | 0.0358, 2.912e- | 0.0558, 2.912e- | 0.1058, 2.913e- |
| | 01, 0.2794 | 01, 0.2794 | 01, 0.2795 | 01, 0.2795 | 01, 0.2795 | 01, 0.2795 | 01, 0.2795 | 01, 0.2795 | 01, 0.2 |
| MR-RAPS2 | 0.101, | 0.097, | 0.092, | 0.096, | 0.091, | 0.089, | 0.092, | 0.095, | 0.105, |
| | -0.0929, | -0.0438, | -0.0226, | -0.0038, | 0.0062, | 0.0162, | 0.0365, | 0.0562, | 0.1066, |
| | 3.263e- | 3.234e- | 3.275e- | 3.234e- | 3.234e- | 3.234e- | 3.238e- | 3.296e- | 3.253e- |
| | 01, 0.3038 | 01, 0.3041 | 01, 0.3033 | 01, 0.3041 | 01, 0.3041 | 01, 0.3041 | 01, 0.3039 | 01, 0.3037 | 01, 0.30 |
| MR-RAPS3 | 0.889, | 0.901, - | 0.896, | 0.897, | 0.899, | 0.893, | 0.887, | 0.893, | 0.889, |
| | -8.6896, | 327.3507, | 2.5442, | -6.6228, | -2.0052, | 2.2011, | 0.8221, | 2.3586, | 0.8809, |
| | 1.977e+02, | 1.020e+04, 3105000 | 1.350e+02, 564.2 | 1.083e+02, 335.5 | 1.216e+02, 774.8 | 1.417e+02, 1037 | 1.075e+02, 419.4 | 4.626e+01, | 7.284e- 315.5 |
| MR-RAPS4 | 1147 0.998, | 0.997, | 0.994, | 0.994, | 0.993, | 0.990, | 0.989, | 97.77 0.990, | 0.990, |
| WIN-KAP34 | 0.998, | 0.997, | 0.994, 0.2539, | 0.994, | 0.993, 0.0353, | 0.990, | -0.1278, | -0.2992, | -0.6071 |
| | 1.427e+00, | 1.605e+00, | 1.718e+00, | 1.752e+00, | 1.701e+00, | 1.710e+00, | 1.714e+00, | 1.782e+00, | 1.718e- |
| | 1.42/0+00 | | | | | | | | |

Table S57: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE satisfied, q=0.6, and N=100000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|-------------------|---------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|
| cML-MA-AIC | 0.888, | 0.330, | 0.102, | 0.030, | 0.015, | 0.022, | 0.108, | 0.295, | 0.853, |
| | -0.0874, | -0.0390, | -0.0221, | -0.0076, | -0.0009, | 0.0062, | 0.0211, | 0.0381, | 0.0858, |
| | 0.0242, | 0.0227, | 0.0204, | 0.0188, | 0.0186, | 0.0191, | 0.0214, | 0.0238, | 0.0269, |
| M. M. HOD CL | 0.0262 | 0.0259 | 0.0253 | 0.025 | 0.025 | 0.0252 | 0.0259 | 0.0267 | 0.0281 |
| ML-MA-AIC-Profile | 0.888, | 0.328, | 0.101, | 0.030, | 0.015, | 0.022, | 0.108, | 0.293, | 0.853, |
| | -0.0875, 0.0243, | -0.0390, 0.0227, | -0.0221, 0.0204, | -0.0076, 0.0188, | -0.0009, 0.0186, | 0.0062, 0.0191, | 0.0211, 0.0214, | 0.0381, 0.0238, | 0.0859, 0.0269, |
| | 0.0243, | 0.0227, | 0.0204, | 0.0188, | 0.0180, | 0.0191, | 0.0214, | 0.0258, | 0.0289, |
| cML-AIC | 0.0203 | 0.567, | 0.0234 | 0.0231 | 0.0231 | 0.0233 | 0.0239 | 0.539, | 0.0282 |
| CWIL-AIC | -0.0932, | -0.0441, | -0.0257, | -0.0092, | -0.0009, | 0.094, | 0.232, | 0.0428, | 0.927, |
| | 0.0271, | 0.0269, | 0.0252, | 0.0244, | 0.0240, | 0.0074, | 0.0264, | 0.0428, | 0.0296, |
| | 0.0271, | 0.0212 | 0.0232, | 0.0244, | 0.0216 | 0.0217 | 0.0219 | 0.0279, | 0.0227 |
| cML-AIC-Profile | 0.943, | 0.567, | 0.270, | 0.0213 | 0.083, | 0.094, | 0.249, | 0.534, | 0.927, |
| CIVIL THE FIGURE | -0.0935, | -0.0441, | -0.0257, | -0.0092, | -0.0009, | 0.0074, | 0.0242, | 0.0429, | 0.0922, |
| | 0.0272, | 0.0269, | 0.0252, | 0.0244, | 0.0240, | 0.0245, | 0.0264, | 0.0279, | 0.0296, |
| | 0.0209 | 0.0213 | 0.0214 | 0.0216 | 0.0217 | 0.0217 | 0.022 | 0.0222 | 0.0228 |
| cML-MA-BIC | 0.998, | 0.718, | 0.322, | 0.078, | 0.052, | 0.071, | 0.320, | 0.699, | 0.993, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0099, | 0.0299, | 0.0499, | 0.0999 |
| | 0.0192, | 0.0195, | 0.0196, | 0.0198, | 0.0199, | 0.0200, | 0.0203, | 0.0205, | 0.0211 |
| | 0.0193 | 0.0196 | 0.0197 | 0.0199 | 0.02 | 0.0201 | 0.0203 | 0.0205 | 0.0211 |
| ML-MA-BIC-Profile | 0.998, | 0.717, | 0.322, | 0.078, | 0.051, | 0.071, | 0.319, | 0.697, | 0.993, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0099, | 0.0299, | 0.0499, | 0.0999 |
| | 0.0192, | 0.0195, | 0.0196, | 0.0198, | 0.0199, | 0.0200, | 0.0203, | 0.0205, | 0.0211 |
| | 0.0193 | 0.0196 | 0.0198 | 0.02 | 0.02 | 0.0201 | 0.0203 | 0.0205 | 0.0211 |
| cML-BIC | 0.998, | 0.723, | 0.328, | 0.083, | 0.057, | 0.074, | 0.333, | 0.711, | 0.993, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1001 |
| | 0.0192, | 0.0195, | 0.0197, | 0.0199. | 0.0200, | 0.0201, | 0.0203, | 0.0205, | 0.0212 |
| | 0.0191 | 0.0194 | 0.0195 | 0.0199, 0.0197 | 0.0198 | 0.0199 | 0.02 | 0.0203 | 0.0208 |
| cML-BIC-Profile | 0.998, | 0.723, | 0.327, | 0.083, | 0.055, | 0.074, | 0.332, | 0.709, | 0.993, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1001 |
| | 0.0192, | 0.0195, | 0.0197, | 0.0199, | 0.0200, | 0.0201, | 0.0203, | 0.0205, | 0.0212 |
| | 0.0191 | 0.0194 | 0.0196 | 0.0197 | 0.0198 | 0.0199 | 0.0201 | 0.0203 | 0.0208 |
| MR-Mix | 0.976, | 0.562, | 0.224, | 0.051, | 0.030, | 0.040, | 0.212, | 0.554, | 0.970, |
| | -0.1017, | -0.0499, | -0.0298, | -0.0099, | -0.0001, | 0.0097, | 0.0288, | 0.0476, | 0.0932 |
| | 0.0210, | 0.0209, | 0.0209, | 0.0209, | 0.0208, | 0.0209, | 0.0209, | 0.0208, | 0.0209 |
| | 0.0245 | 0.0243 | 0.0242 | 0.0243 | 0.0243 | 0.0244 | 0.0243 | 0.0243 | 0.024 |
| MR-ContMix | 0.998, | 0.740, | 0.367, | 0.098, | 0.070, | 0.091, | 0.356, | 0.726, | 0.994, |
| | -0.1000, | -0.0501, | -0.0301, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0997 |
| | 0.0198, | 0.0201, | 0.0203, | 0.0205, | 0.0206, | 0.0206, | 0.0209, | 0.0212, | 0.0217 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.984, | 0.662, | 0.295, | 0.098, | 0.073, | 0.089, | 0.302, | 0.638, | 0.974, |
| | -0.1014, | -0.0515, | -0.0314, | -0.0114, | -0.0012, | 0.0086, | 0.0284, | 0.0485, | 0.0990 |
| | 0.1710, | 0.1705, | 0.1705, | 0.1705, | 0.1716, | 0.1724, | 0.1735, | 0.1731, | 0.1679 |
| | 0.0261 | 0.0264 | 0.0266 | 0.0268 | 0.0269 | 0.0271 | 0.0272 | 0.0273 | 0.0278 |
| MR-PRESSO | 0.528, | 0.349, | 0.229, | 0.159, | 0.143, | 0.152, | 0.229, | 0.350, | 0.524, |
| | -0.1065, | -0.0569, | -0.0375, | -0.0179, | -0.0078, | 0.0019, | 0.0209, | 0.0406, | 0.0907, |
| | 0.2693, | 0.2691, | 0.2690, | 0.2685, | 0.2685, | 0.2684, | 0.2681, | 0.2674, | 0.2659 |
| | 0.1301 | 0.129 | 0.1288 | 0.1277 | 0.1277 | 0.1272 | 0.1263 | 0.1248 | 0.1215 |
| MR-IVW | 0.082, | 0.074, | 0.066, | 0.066, | 0.067, | 0.065, | 0.067, | 0.071, | 0.074, |
| | -0.1106, | -0.0601, | -0.0399, | -0.0198, | -0.0097, | 0.0004, | 0.0205, | 0.0407, | 0.0910 |
| | 0.2861, | 0.2861, | 0.2861, | 0.2861, | 0.2861, | 0.2861, | 0.2861, | 0.2861, | 0.2860 |
| | 0.2863 | 0.2863 | 0.2863 | 0.2863 | 0.2863 | 0.2863 | 0.2863 | 0.2863 | 0.2863 |
| MR-IVW-Oracle | 0.997, | 0.664, | 0.278, | 0.067, | 0.044, | 0.055, | 0.281, | 0.638, | 0.990, |
| | -0.0998, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0499, | 0.0998 |
| | 0.0191, | 0.0195, | 0.0196, | 0.0198, | 0.0199, | 0.0200, | 0.0202, | 0.0205, | 0.0211 |
| | 0.0207 | 0.0211 | 0.0213 | 0.0215 | 0.0216 | 0.0217 | 0.0219 | 0.0221 | 0.0227 |
| MR-Egger | 0.095, | 0.097, | 0.099, | 0.099, | 0.099, | 0.100, | 0.099, | 0.098, | 0.095, |
| - | -0.1206, | -0.0738, | -0.0550, | -0.0363, | -0.0270, | -0.0176, | 0.0011, | 0.0198, | 0.0665 |
| | 1.6542, | 1.6538, | 1.6537, | 1.6536, | 1.6535, | 1.6534, | 1.6533, | 1.6532, | 1.6529 |
| | 1.5192 | 1.5191 | 1.5191 | 1.5191 | 1.5191 | 1.5191 | 1.5191 | 1.5191 | 1.5191 |
| R-Weighted-Median | 0.960, | 0.485, | 0.201, | 0.075, | 0.054, | 0.067, | 0.193, | 0.442, | 0.919, |
| | -0.0974, | -0.0488, | -0.0294, | -0.0101, | -0.0006, | 0.0091, | 0.0284, | 0.0476, | 0.0955 |
| | 0.0253, | 0.0258, | 0.0261, | 0.0266, | 0.0268, | 0.0270, | 0.0275, | 0.0281, | 0.0295 |
| | 0.0254 | 0.0258 | 0.026 | 0.0262 | 0.0263 | 0.0264 | 0.0266 | 0.0269 | 0.0276 |
| MR-Weighted-Mode | 0.840, | 0.521, | 0.395, | 0.300, | 0.313, | 0.317, | 0.392, | 0.516, | 0.796, |
| | -0.0914, | -0.0462, | -0.0282, | -0.0100, | -0.0009, | 0.0082, | 0.0264, | 0.0446, | 0.0896 |
| | 0.0476, | 0.0482, | 0.0488, | 0.0494, | 0.0496, | 0.0498, | 0.0508, | 0.0518, | 0.0542 |
| 100 7 : | 0.0236 | 0.0241 | 0.0243 | 0.0245 | 0.0247 | 0.0248 | 0.0251 | 0.0254 | 0.0264 |
| MR-RAPS1 | 0.083, | 0.076, | 0.070, | 0.065, | 0.063, | 0.064, | 0.069, | 0.071, | 0.079, |
| | -0.1084, | -0.0583, | -0.0383, | -0.0183, | -0.0083, | 0.0017, | 0.0217, | 0.0417, | 0.0917 |
| | 0.2792, | 0.2792, | 0.2792, | 0.2793, | 0.2793, | 0.2793, | 0.2793, | 0.2793, | 0.2793 |
| 14D D 1702 | 0.2796 | 0.2796 | 0.2796 | 0.2796 | 0.2796 | 0.2796 | 0.2796 | 0.2796 | 0.2797 |
| MR-RAPS2 | 0.098, | 0.080, | 0.080, | 0.080, | 0.083, | 0.087, | 0.080, | 0.084, | 0.094, |
| | -0.1111, | -0.0585, | -0.0395, | -0.0215, | -0.0096, | -0.0062, | 0.0205, | 0.0349, | 0.0917 |
| | 0.3274, | 0.3159, | 0.3162, | 0.3202, | 0.3236, | 0.3322, | 0.3171, | 0.3305, | 0.3196 |
| | 0.3027 | 0.3038 | 0.304 | 0.3033 | 0.3035 | 0.3023 | 0.304 | 0.3024 | 0.3036 |
| MR-RAPS3 | 0.906, | 0.920, | 0.915, | 0.911, | 0.917, | 0.920, | 0.928, | 0.932, | 0.926, |
| | -2.7927, | 8.5127, | 5.1277, | -2.1372, | 14.4961, | -0.8176, | -16.2561, | 1.2652, | -3.7158 |
| | 89.2482, | 256.4422, | 111.1046, | 63.7077, | 301.0921, | 32.4694, | 487.8015, | 18.5049, | 103.97 |
| | 172.8403 | 1436.1815 | 317.4877 | 88.3011 | 2142.2384 | 26.1085 | 8034.2503 | 9.8629 | 262.35 |
| MR-RAPS4 | 0.992, | 0.996, | 0.995, | 0.995, | 0.992, | 0.993, | 0.985, | 0.984, | 0.986, |
| | 0.6529, | 0.4470, | 0.3015, | 0.2050, | 0.1195, | 0.0096, | -0.2416, | -0.3876, | -0.7337 |
| | 1.6028, | 1.7693, | 1.7968, | 1.7899, | 1.8489, | 1.8731, | 1.9026, | 1.9715, | 1.7963, |
| | 0.1007 | 0.1051 | 0.1154 | 0.1383 | 0.0914 | 0.096 | 0.3056 | 0.1785 | 0.143 |

Table S58: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE satisfied, q=0.6, and N=200000.

| // | / / | | | | , I | | | | |
|--|-----------------------|----------------------|-----------------------|-----------------------|------------------------------|------------------------------|-------------------------------|-------------------------------|-------------------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.987, | 0.631, | 0.241, | 0.031, | 0.012, | 0.033, | 0.227, | 0.604, | 0.973, |
| | -0.0908, | -0.0411, | -0.0227, | -0.0067, | 0.0003, | 0.0073, | 0.0227, | 0.0412, | 0.0903, |
| | 0.0174, | 0.0170, | 0.0156, | 0.0136, | 0.0132, | 0.0137, | 0.0163, | 0.0180, | 0.0192, |
| | 0.0183 | 0.0183 | 0.018 | 0.0177 | 0.0177 | 0.0179 | 0.0186 | 0.0192 | 0.0201 |
| cML-MA-AIC-Profile | 0.987, | 0.630, | 0.239, | 0.030, | 0.012, | 0.033, | 0.226, | 0.603, | 0.973, |
| | -0.0909, | -0.0411, | -0.0227, | -0.0067, | 0.0003, | 0.0073, | 0.0227, | 0.0412, | 0.0904, |
| | 0.0174, | 0.0170, | 0.0156, | 0.0135, | 0.0132, | 0.0137, | 0.0163, | 0.0180, | 0.0192, |
| MLAIC | 0.0183 | 0.0184 | 0.018 | 0.0177 | 0.0177 | 0.0179 | 0.0186 | 0.0193 | 0.0201 |
| cML-AIC | 0.998, | 0.798, | 0.445, | 0.123, -0.0079, | 0.079, | 0.114, | 0.444, | 0.774, | 0.985, |
| | -0.0951, 0.0189, | -0.0451, 0.0191, | -0.0257, 0.0185, | 0.0173, | 0.0002, 0.0170, | 0.0085, 0.0175, | 0.0260, 0.0191, | 0.0455, 0.0200, | 0.0950, 0.0209, |
| | 0.0189, | 0.0151, | 0.0183, | 0.0173, | 0.0170, | 0.0173, | 0.0154 | 0.0200, | 0.0209, |
| cML-AIC-Profile | 0.998, | 0.796, | 0.445, | 0.122, | 0.078, | 0.114, | 0.442, | 0.774, | 0.985, |
| cond the frome | -0.0952, | -0.0451, | -0.0257, | -0.0079, | 0.0002, | 0.0085, | 0.0260, | 0.0455, | 0.0951, |
| | 0.0189, | 0.0191, | 0.0185, | 0.0173, | 0.0170, | 0.0175, | 0.0191, | 0.0200, | 0.0210, |
| | 0.0147 | 0.015 | 0.0151 | 0.0152 | 0.0153 | 0.0153 | 0.0154 | 0.0156 | 0.016 |
| cML-MA-BIC | 1.000, | 0.949, | 0.575, | 0.112, | 0.043, | 0.103, | 0.560, | 0.926, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0134, | 0.0137, | 0.0138, | 0.0139, | 0.0139, | 0.0140, | 0.0142, | 0.0144, | 0.0148, |
| | 0.0136 | 0.0138 | 0.0139 | 0.0141 | 0.0141 | 0.0142 | 0.0143 | 0.0145 | 0.0149 |
| cML-MA-BIC-Profile | 1.000, | 0.948, | 0.575, | 0.112, | 0.043, | 0.103, | 0.559, | 0.926, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0134, 0.0136 | 0.0137, 0.0138 | 0.0138, | 0.0139, 0.0141 | 0.0139, 0.0141 | 0.0140, 0.0142 | 0.0142, 0.0143 | 0.0144, | 0.0148, |
| cML-BIC | 1.000, | 0.0138 | 0.014 0.584, | 0.0141 | 0.0141 | 0.0142 | 0.566, | 0.0145 0.929, | 0.0149 1.000, |
| CIVIL-DIC | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.044, | 0.105, 0.0100, | 0.300, | 0.929, | 0.1000, |
| | 0.0134, | 0.0136, | 0.0137, | 0.0139, | 0.0000, | 0.0100, | 0.0300, | 0.0300, | 0.1000, |
| | 0.0134, | 0.0130, | 0.0137, | 0.0139, | 0.0140, | 0.0140, | 0.0142, | 0.0143, | 0.0148, |
| cML-BIC-Profile | 1.000, | 0.949, | 0.584, | 0.117. | 0.044, | 0.104, | 0.565, | 0.929, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1000, |
| | 0.0134, | 0.0136, | 0.0137, | 0.0139, | 0.0140, | 0.0140, | 0.0142, | 0.0143, | 0.0148, |
| | 0.0135 | 0.0137 | 0.0138 | 0.0139 | 0.014 | 0.0141 | 0.0142 | 0.0143 | 0.0147 |
| MR-Mix | 0.993, | 0.826, | 0.410, | 0.063, | 0.024, | 0.058, | 0.381, | 0.809, | 0.989, |
| | -0.1019, | -0.0500, | -0.0300, | -0.0100, | -0.0001, | 0.0096, | 0.0288, | 0.0476, | 0.0931, |
| | 0.0151, | 0.0149, | 0.0148, | 0.0149, | 0.0149, | 0.0149, | 0.0150, | 0.0149, | 0.0151, |
| 100 C 11 | 0.0177 | 0.0178 | 0.0178 | 0.0178 | 0.0178 | 0.018 | 0.0178 | 0.0179 | 0.0176 |
| MR-ContMix | 1.000, -0.0998, | 0.949, -0.0499, | 0.618, | 0.147, -0.0099, | 0.068, | 0.130, 0.0101, | 0.591, 0.0301, | 0.930, | 1.000, 0.0999, |
| | 0.0137, | 0.0140, | -0.0299, 0.0141, | 0.0143, | 0.0001, 0.0144, | 0.0101, | 0.0301, | 0.0500, 0.0149, | 0.0999, |
| | 0.0137, NA | 0.0140, NA | 0.0141, NA | 0.0143, NA | 0.0144, NA | NA | 0.0146, NA | 0.0149, NA | 0.0154, NA |
| MR-Lasso | 0.998, | 0.920, | 0.537, | 0.136, | 0.074, | 0.124, | 0.497, | 0.886, | 0.996, |
| THE EMODE | -0.1096, | -0.0598, | -0.0399, | -0.0199, | -0.0099, | 0.0001, | 0.0202, | 0.0402, | 0.0905, |
| | 0.2275, | 0.2284, | 0.2284, | 0.2296, | 0.2296, | 0.2296, | 0.2294, | 0.2294, | 0.2315, |
| | 0.0205 | 0.0207 | 0.0208 | 0.021 | 0.021 | 0.0211 | 0.0212 | 0.0213 | 0.0215 |
| MR-PRESSO | 0.435, | 0.358, | 0.244, | 0.143, | 0.127, | 0.145, | 0.235, | 0.355, | 0.451, |
| | -0.1182, | -0.0684, | -0.0486, | -0.0285, | -0.0183, | -0.0082, | 0.0119, | 0.0322, | 0.0831, |
| | 0.2976, | 0.2975, | 0.2975, | 0.2974, | 0.2974, | 0.2972, | 0.2972, | 0.2970, | 0.2967, |
| MD WWY | 0.1707 | 0.1701 | 0.1701 | 0.1697 | 0.1694 | 0.169 | 0.1686 | 0.1678 | 0.166 |
| MR-IVW | 0.101, | 0.087, | 0.087, | 0.082, | 0.084, | 0.084, | 0.087, | 0.093, | 0.098, |
| | -0.1186, 0.3029, | -0.0681, 0.3029, | -0.0479, 0.3029, | -0.0277, 0.3029, | -0.0176, 0.3029, | -0.0075, 0.3029, | 0.0126, 0.3029, | 0.0328, 0.3028, | 0.0832, 0.3028, |
| | 0.3029, | 0.3029, | 0.3029, | 0.3029, | 0.3029, | 0.3029, | 0.3029, | 0.3028, | 0.3028, |
| MR-IVW-Oracle | 1.000, | 0.930, | 0.518, | 0.098, | 0.033, | 0.084, | 0.499, | 0.896, | 1.000, |
| MICTY W Gracie | -0.0998, | -0.0499, | -0.0299, | -0.0099, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.0999, |
| | 0.0133, | 0.0135, | 0.0137, | 0.0138, | 0.0139, | 0.0139, | 0.0141, | 0.0143, | 0.0147, |
| | 0.0147 | 0.0149 | 0.015 | 0.0152 | 0.0152 | 0.0153 | 0.0154 | 0.0156 | 0.016 |
| MR-Egger | 0.074, | 0.073, | 0.074, | 0.073, | 0.073, | 0.074, | 0.071, | 0.068, | 0.068, |
| | -0.0935, | -0.0448, | -0.0254, | -0.0059, | 0.0038, | 0.0135, | 0.0329, | 0.0524, | 0.1009, |
| | 1.6365, | 1.6361, | 1.6359, | 1.6358, | 1.6357, | 1.6356, | 1.6355, | 1.6353, | 1.6349, |
| A CONTRACTOR OF THE CONTRACTOR | 1.5486 | 1.5485 | 1.5485 | 1.5485 | 1.5484 | 1.5484 | 1.5484 | 1.5483 | 1.5482 |
| MR-Weighted-Median | 0.997, | 0.776, | 0.351, | 0.075, | 0.047, | 0.077, | 0.349, | 0.733, | 0.993, |
| | -0.0976, | -0.0488, | -0.0292, | -0.0097, | 0.0000, | 0.0098, | 0.0292, | 0.0487, | 0.0972, |
| | 0.0180, 0.018 | 0.0182, 0.0182 | 0.0183, 0.0184 | 0.0185, 0.0185 | 0.0186, 0.0186 | 0.0187, 0.0187 | 0.0189, 0.0188 | 0.0192, 0.019 | 0.0201, 0.0195 |
| MR-Weighted-Mode | 0.018 | 0.652, | 0.0184 | 0.0185 | 0.0186 | 0.0187 | 0.0188 | 0.645, | 0.0195 |
| wiv- weignien-mone | -0.0922, | -0.0465, | -0.0282, | -0.0099, | -0.0007, | 0.423, 0.0084, | 0.495, | 0.045, | 0.893, |
| | 0.0427, | 0.0431, | 0.0435, | 0.0445, | 0.0447, | 0.0054, | 0.0200, | 0.0451, | 0.0490, |
| | 0.0172 | 0.0175 | 0.0176 | 0.0178 | 0.0178 | 0.018 | 0.0182 | 0.0184 | 0.019 |
| MR-RAPS1 | 0.099, | 0.092, | 0.091, | 0.089, | 0.083, | 0.085, | 0.083, | 0.085, | 0.091, |
| | -0.1177, | -0.0676, | -0.0476, | -0.0276, | -0.0176, | -0.0076, | 0.0124, | 0.0324, | 0.0824, |
| | 0.2950, | 0.2950, | 0.2950, | 0.2950, | 0.2950, | 0.2950, | 0.2950, | 0.2950, | 0.2951, |
| | 0.2782 | 0.2782 | 0.2782 | 0.2782 | 0.2782 | 0.2782 | 0.2782 | 0.2782 | 0.2782 |
| MR-RAPS2 | 0.242, | 0.184, | 0.175, | 0.169, | 0.163, | 0.158, | 0.161, | 0.158, | 0.154, |
| | -0.1225, | -0.0638, | -0.0462, | -0.0294, | -0.0199, | -0.0021, | 0.0142, | 0.0296, | 0.0795, |
| | 0.4831, | 0.4537, | 0.4579, | 0.4508, | 0.4538, | 0.4483, | 0.4291, | 0.4320, | 0.4158, |
| MD D + DGG | 0.222 | 0.2304 | 0.232 | 0.2384 | 0.2375 | 0.2433 | 0.2463 | 0.2519 | 0.2681 |
| MR-RAPS3 | 0.944, | 0.934, | 0.943, | 0.945, | 0.937, | 0.934, | 0.939, | 0.940, | 0.952, |
| | -4.0115, 106.3931, | 1.0247, 115.9425, | -7.7396, 283.5044, | -9.6841, 302.9734, | 1.1517, 45.2390, | -9.9359, 206.3759, | 2.0667, 72.1215, | -2.4343, 39.6826, | -0.5707, 32.6778, |
| | 100.3931, | | 1403.6719 | 1208.8483 | 45.2390, 52.2286 | 898.1968 | 138.1285 | 34.3873 | 22.666 |
| | 231 2400 | 205 4114 | | | 34.4400 | 020.1700 | 130.1403 | JT.J0/J | 44.000 |
| MR_RADSA | 231.2409 | 205.4114 | | | 0.995 | 0.992 | 0.991 | 0.992 | 0.003 |
| MR-RAPS4 | 0.998, | 0.995, | 0.993, | 0.993, | 0.995, 0.1680. | 0.992, 0.1248. | 0.991, -0.0159. | 0.992, -0.2282. | 0.993, -0.5607. |
| MR-RAPS4 | | | | | 0.995, 0.1680, 1.9255, | 0.992, 0.1248, 1.9509, | 0.991, -0.0159, 2.0202, | 0.992, -0.2282, 1.9963, | 0.993, -0.5607, 1.9078, |

Table S59: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE violated, q=0.2, and N=50000.

| θ flethods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|-------------------|-------------|--------------|---------------------|-------------------|--------------|--------------------|--------------------|--------------------|------------------|
| cML-MA-AIC | 0.932, | 0.453, | 0.178, | 0.058, | 0.039, | 0.040, | 0.145, | 0.389, | 0.892, |
| | -0.0908, | -0.0424, | -0.0245, | -0.0087, | -0.0011, | 0.0064, | 0.0223, | 0.0400, | 0.0881, |
| | 0.0251, | 0.0240, | 0.0224, | 0.0209, | 0.0205, | 0.0208, | 0.0223, | 0.0244, | 0.0271, |
| M M MG D CI | 0.0237 | 0.0236 | 0.0234 | 0.0233 | 0.0233 | 0.0235 | 0.0239 | 0.0246 | 0.0258 |
| ML-MA-AIC-Profile | 0.933, | 0.449, | 0.177, | 0.055, | 0.039, | 0.040, | 0.144, | 0.385, | 0.890, |
| | -0.0911, | -0.0425, | -0.0246, | -0.0087, | -0.0011, | 0.0064, | 0.0223, | 0.0401, | 0.0883, |
| | 0.0253, | 0.0241, | 0.0225, | 0.0209, | 0.0205, | 0.0208, | 0.0224, | 0.0244, | 0.0272, |
| 10.110 | 0.0238 | 0.0237 | 0.0235 | 0.0234 | 0.0235 | 0.0236 | 0.0241 | 0.0247 | 0.0259 |
| cML-AIC | 0.965, | 0.611, | 0.344, | 0.133, | 0.098, | 0.115, | 0.278, | 0.560, | 0.948, |
| | -0.0956, | -0.0464, | -0.0275, | -0.0099, | -0.0009, | 0.0078, | 0.0252, | 0.0443, | 0.0935 |
| | 0.0268, | 0.0269, | 0.0260, | 0.0254, | 0.0253, | 0.0254, | 0.0262, | 0.0275, | 0.0293 |
| | 0.0199 | 0.0203 | 0.0205 | 0.0207 | 0.0207 | 0.0208 | 0.021 | 0.0213 | 0.0219 |
| cML-AIC-Profile | 0.965, | 0.608, | 0.337, | 0.131, | 0.098, | 0.114, | 0.274, | 0.558, | 0.947, |
| | -0.0959, | -0.0464, | -0.0275, | -0.0099, | -0.0009, | 0.0078, | 0.0252, | 0.0443, | 0.0936 |
| | 0.0270, | 0.0270, | 0.0260, | 0.0254, | 0.0253, | 0.0255, | 0.0263, | 0.0275, | 0.0293 |
| | 0.02 | 0.0204 | 0.0206 | 0.0208 | 0.0209 | 0.021 | 0.0212 | 0.0214 | 0.022 |
| cML-MA-BIC | 1.000, | 0.778, | 0.366, | 0.083, | 0.042, | 0.078, | 0.315, | 0.677, | 0.996, |
| | -0.1006, | -0.0506, | -0.0307, | -0.0107, | -0.0008, | 0.0092, | 0.0291, | 0.0490, | 0.0990 |
| | 0.0184, | 0.0187, | 0.0189, | 0.0190, | 0.0191, | 0.0192, | 0.0194, | 0.0197, | 0.0203 |
| | 0.0185 | 0.0188 | 0.019 | 0.0192 | 0.0192 | 0.0193 | 0.0195 | 0.0197 | 0.0203 |
| ML-MA-BIC-Profile | 1.000, | 0.773, | 0.365, | 0.082, | 0.041, | 0.077, | 0.313, | 0.674, | 0.996, |
| | -0.1006, | -0.0506, | -0.0307, | -0.0107, | -0.0008, | 0.0092, | 0.0291, | 0.0490, | 0.0990 |
| | 0.0185, | 0.0187, | 0.0189, | 0.0190, | 0.0191, | 0.0192, | 0.0194, | 0.0197, | 0.0203 |
| | 0.0186 | 0.0189 | 0.019 | 0.0192 | 0.0193 | 0.0194 | 0.0196 | 0.0198 | 0.0204 |
| cML-BIC | 1.000, | 0.787, | 0.384, | 0.089, | 0.045, | 0.085, | 0.320, | 0.697, | 0.996, |
| | -0.1007, | -0.0508, | -0.0308, | -0.0108, | -0.0008, | 0.0092, | 0.0292, | 0.0491, | 0.0991 |
| | 0.0184, | 0.0187, | 0.0189, | 0.0190. | 0.0191, | 0.0192, | 0.0194, | 0.0196, | 0.0202 |
| | 0.0183 | 0.0186 | 0.0188 | 0.0190, 0.0189 | 0.019 | 0.0191 | 0.0193 | 0.0195 | 0.0201 |
| cML-BIC-Profile | 1.000, | 0.783, | 0.382, | 0.088, | 0.043, | 0.085, | 0.319, | 0.696, | 0.996, |
| | -0.1007, | -0.0508, | -0.0308, | -0.0108, | -0.0008, | 0.0092, | 0.0292, | 0.0491, | 0.0991 |
| | 0.0184, | 0.0187, | 0.0189, | 0.0190, | 0.0191, | 0.0192, | 0.0194, | 0.0196, | 0.0202 |
| | 0.0183 | 0.0187, | 0.0189, | 0.0190, | 0.0191, | 0.0192 | 0.0194, | 0.0196 | 0.0202 |
| MR-Mix | 0.952, | 0.399, | 0.135, | 0.024, | 0.0151 | 0.025, | 0.116, | 0.355, | 0.906, |
| WIIK WIIK | -0.1064, | -0.0524, | -0.0314, | -0.0107, | -0.0005, | 0.0096, | 0.0294, | 0.0488, | 0.0953 |
| | 0.0233, | 0.0231, | 0.0231, | 0.0229, | 0.0229, | 0.0228, | 0.0224, | 0.0230, | 0.0229 |
| | 0.0233, | 0.0231, | 0.0304 | 0.0229, | 0.0229, | 0.0305 | 0.0228, | 0.0230, | 0.0229 |
| MR-ContMix | 1.000, | 0.0303 | | 0.0304 | 0.0504 | 0.0303 | 0.0303 | | 0.0307 |
| MR-Continix | -0.1002, | -0.0505, | 0.375, | -0.0107, | -0.0008, | 0.082, | | 0.678, | |
| | 0.0194, | 0.0303, | -0.0307, 0.0199, | 0.0200, | 0.0201, | 0.0092, | 0.0290, 0.0204, | 0.0488, 0.0206, | 0.0984 0.0213 |
| | | | | | | | | | |
| MD I | NA 0.000 | NA 0.737, | NA 0.242 | NA 0.077, | NA 0.042, | NA 0.071, | NA 0.200 | NA 0.650 | NA 0.005 |
| MR-Lasso | 0.999, | 0.737, | 0.343, | 0.077, | | | 0.290, | 0.659, | 0.995, |
| | -0.1000, | -0.0504, | -0.0305, | -0.0106, | -0.0007, | 0.0092, | 0.0290, | 0.0488, | 0.0983 |
| | 0.0187, | 0.0191, | 0.0193, | 0.0195, | 0.0195, | 0.0196, | 0.0198, | 0.0200, | 0.0206 |
| | 0.0192 | 0.0195 | 0.0197 | 0.0199 | 0.02 | 0.0201 | 0.0203 | 0.0205 | 0.0211 |
| MR-PRESSO | 0.851, | 0.627, | 0.438, | 0.289, | 0.283, | 0.306, | 0.434, | 0.634, | 0.874, |
| | -0.0864, | -0.0388, | -0.0188, | 0.0008, | 0.0098, | 0.0192, | 0.0377, | 0.0571, | 0.1054 |
| | 0.0864, | 0.0823, | 0.0816, | 0.0815, | 0.0790, | 0.0784, | 0.0749, | 0.0741, | 0.0711 |
| | 0.0239 | 0.0233 | 0.0233 | 0.0233 | 0.0231 | 0.0231 | 0.0228 | 0.0228 | 0.0226 |
| MR-IVW | 0.125, | 0.107, | 0.102, | 0.088, | 0.085, | 0.085, | 0.084, | 0.095, | 0.136, |
| | -0.0745, | -0.0246, | -0.0047, | 0.0153, | 0.0253, | 0.0352, | 0.0552, | 0.0751, | 0.1250 |
| | 0.1795, | 0.1795, | 0.1794, | 0.1794, | 0.1794, | 0.1794, | 0.1794, | 0.1793, | 0.1793 |
| | 0.1673 | 0.1673 | 0.1673 | 0.1673 | 0.1673 | 0.1673 | 0.1673 | 0.1673 | 0.1673 |
| MR-IVW-Oracle | 1.000, | 0.738, | 0.336, | 0.066, | 0.035, | 0.064, | 0.281, | 0.647, | 0.995, |
| | -0.1002, | -0.0505, | -0.0306, | -0.0108, | -0.0008, | 0.0091, | 0.0290, | 0.0488, | 0.0985 |
| | 0.0183, | 0.0186, | 0.0187, | 0.0189, | 0.0190, | 0.0190, | 0.0192, | 0.0194, | 0.0200 |
| | 0.0194 | 0.0197 | 0.0199 | 0.0201 | 0.0202 | 0.0203 | 0.0205 | 0.0207 | 0.0212 |
| MR-Egger | 0.299, | 0.300, | 0.302, | 0.308, | 0.308, | 0.311, | 0.312, | 0.320, | 0.326, |
| | 0.3418, | 0.3876, | 0.4059, | 0.4242, | 0.4334, | 0.4425, | 0.4608, | 0.4791, | 0.5248 |
| | 1.0256, | 1.0259, | 1.0260, | 1.0261, | 1.0262, | 1.0263, | 1.0264, | 1.0265, | 1.0269 |
| | 0.6476 | 0.6478 | 0.6479 | 0.648 | 0.648 | 0.6481 | 0.6482 | 0.6483 | 0.6486 |
| R-Weighted-Median | 0.976, | 0.529, | 0.212, | 0.069, | 0.036, | 0.028, | 0.135, | 0.382, | 0.918, |
| | -0.1001, | -0.0518, | -0.0324, | -0.0131, | -0.0034, | 0.0063, | 0.0256, | 0.0450, | 0.0933 |
| | 0.0234, | 0.0239, | 0.0240, | 0.0243, | 0.0244, | 0.0246, | 0.0248, | 0.0252, | 0.0260 |
| | 0.0255 | 0.026 | 0.0262 | 0.0264 | 0.0265 | 0.0267 | 0.0269 | 0.0272 | 0.028 |
| MR-Weighted-Mode | 0.917, | 0.327, | 0.111, | 0.034, | 0.023, | 0.028, | 0.084, | 0.259, | 0.836, |
| J | -0.0988, | -0.0500, | -0.0306, | -0.0111, | -0.0015, | 0.0083, | 0.0275, | 0.0473, | 0.0958 |
| | 0.0286, | 0.0291, | 0.0292, | 0.0294, | 0.0295, | 0.0295, | 0.0295, | 0.0297, | 0.0304 |
| | 0.0324 | 0.033 | 0.0333 | 0.0336 | 0.0337 | 0.0338 | 0.0342 | 0.0345 | 0.0355 |
| MR-RAPS1 | 0.129, | 0.100, | 0.096, | 0.088, | 0.088, | 0.082, | 0.083, | 0.095, | 0.146, |
| | -0.0762, | -0.0262, | -0.0062, | 0.0138, | 0.0238, | 0.0338, | 0.0537, | 0.0737, | 0.1237 |
| | 0.1737, | 0.1736, | 0.1736, | 0.0136, | 0.0236, | 0.1736, | 0.0337, | 0.1736, | 0.1736 |
| | 0.1737, | 0.1730, | 0.1730, | 0.1730, | 0.1730, | 0.1730, | 0.1730, | 0.1730, | 0.1730 |
| MR-RAPS2 | 0.993, | 0.921, | 0.763, | 0.634, | 0.626, | 0.639, | 0.752, | 0.895, | 0.1033 |
| MIN-INAL DZ | | 0.921, | 0.763, | 0.3564, | 0.020, | | 0.732, | 0.893, | 0.594, |
| | 0.0501, | 2.4769, | | 5.7200, | 3.0576, | 0.1485, 3.4577, | 2.6805, | | 3.9835 |
| | 3.2512, | | 3.5239, | | | | | 3.0321, | |
| MD D + DGC | 0.0463 | 0.0546 | 0.0847 | 0.3273 | 0.0839 | 0.0648 | 0.0536 | 0.0481 | 0.043 |
| MR-RAPS3 | 0.868, | 0.865, | 0.866, | 0.863, | 0.855, | 0.866, | 0.857, | 0.881, | 0.888, |
| | -0.3884, | -0.0426, | -0.3797, | 0.0463, | 0.0616, | 0.3869, | 0.1258, | 0.1597, | 0.2408 |
| | 5.7295, | 0.5098, | 12.1020, | 0.4602, | 0.4663, | 9.4974, | 0.3945, | 0.3779, | 0.3489, |
| | | | | 0.0553 | 0.0599 | 31.1292 | 0.0452 | 0.042 | 0.0391 |
| | 12.3079 | 0.062 | 26.2886 | | | | | | |
| MR-RAPS4 | 1.000, | 0.955, | 0.862, | 0.796, | 0.788, | 0.789, | 0.854, | 0.935, | 1.000, |
| MR-RAPS4 | | | | | | | | | |

Table S60: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE violated, q=0.2, and N=100000.

| // | <i>' '</i> | | | | , I | | | | |
|---------------------------------------|-------------------------------|------------------------------|------------------------------|-------------------|-------------------|-------------------|-------------------|------------------|-------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.996, | 0.712, | 0.298, | 0.068, | 0.033, | 0.077, | 0.310, | 0.685, | 0.983, |
| CIVIL MITTING | -0.0929, | -0.0432, | -0.0241, | -0.0072, | 0.0005, | 0.0082, | 0.0251, | 0.0436, | 0.0928, |
| | 0.0175, | 0.0175, | 0.0166, | 0.0150, | 0.0149, | 0.0152, | 0.0170, | 0.0185, | 0.0197, |
| | 0.0175, | 0.0173, | 0.0166 | 0.0150, | 0.0145, | 0.0152, | 0.0170, | 0.0176 | 0.0197, |
| cML-MA-AIC-Profile | 0.996, | 0.711, | 0.298, | 0.067, | 0.033, | 0.076, | 0.310, | 0.683, | 0.983, |
| CIVIL-IVIA-AIC-FIOIIIE | -0.0931, | -0.0432, | -0.0241, | -0.0072, | 0.0005, | 0.076, | 0.0251, | 0.0437, | 0.983, |
| | 0.0176, | 0.0175, | | | | 0.0082, | 0.0231, 0.0170, | | |
| | | | 0.0166, | 0.0150, | 0.0149, | | | 0.0185, | 0.0198, |
| M. ATC | 0.0166 | 0.0168 | 0.0167 | 0.0165 | 0.0165 | 0.0167 | 0.0172 | 0.0177 | 0.0184 |
| cML-AIC | 0.998, | 0.831, | 0.483, | 0.149, | 0.111, | 0.168, | 0.489, | 0.805, | 0.991, |
| | -0.0963, | -0.0466, | -0.0271, | -0.0084, | 0.0005, | 0.0094, | 0.0279, | 0.0473, | 0.0967, |
| | 0.0189, | 0.0189, | 0.0187, | 0.0180, | 0.0180, | 0.0181, | 0.0190, | 0.0199, | 0.0209, |
| | 0.014 | 0.0143 | 0.0144 | 0.0145 | 0.0146 | 0.0147 | 0.0148 | 0.015 | 0.0154 |
| cML-AIC-Profile | 0.998, | 0.831, | 0.482, | 0.148, | 0.107, | 0.168, | 0.486, | 0.804, | 0.991, |
| | -0.0964, | -0.0467, | -0.0271, | -0.0084, | 0.0005, | 0.0094, | 0.0279, | 0.0473, | 0.0968, |
| | 0.0189, | 0.0189, | 0.0187, | 0.0180, | 0.0180, | 0.0181, | 0.0190, | 0.0200, | 0.0210, |
| | 0.0141 | 0.0143 | 0.0145 | 0.0146 | 0.0147 | 0.0147 | 0.0149 | 0.015 | 0.0155 |
| cML-MA-BIC | 1.000, | 0.959, | 0.599, | 0.096, | 0.053, | 0.122, | 0.611, | 0.952, | 1.000, |
| | -0.0994, | -0.0494, | -0.0293, | -0.0093, | 0.0006, | 0.0106, | 0.0306, | 0.0506, | 0.1006, |
| | 0.0130, | 0.0132, | 0.0133, | 0.0134, | 0.0134, | 0.0135, | 0.0137, | 0.0138, | 0.0142, |
| | 0.0130, | 0.0132, | 0.0133, | 0.0135 | 0.0135 | 0.0136 | 0.0137, | 0.0139 | 0.0142, |
| M. M. DIG D. Cl | | | | | | | | | |
| cML-MA-BIC-Profile | 1.000, | 0.959, | 0.597, | 0.095, | 0.052, | 0.119, | 0.609, | 0.952, | 1.000, |
| | -0.0994, | -0.0494, | -0.0293, | -0.0093, | 0.0006, | 0.0106, | 0.0306, | 0.0506, | 0.1006, |
| | 0.0130, | 0.0132, | 0.0133, | 0.0134, | 0.0134, | 0.0135, | 0.0137, | 0.0138, | 0.0142, |
| | 0.013 | 0.0133 | 0.0134 | 0.0135 | 0.0136 | 0.0136 | 0.0138 | 0.0139 | 0.0143 |
| cML-BIC | 1.000, | 0.963, | 0.610, | 0.106, | 0.053, | 0.127, | 0.617, | 0.952, | 1.000, |
| | -0.0995, | -0.0495, | -0.0294, | -0.0094, | 0.0006, | 0.0106, | 0.0306, | 0.0507, | 0.1007, |
| | 0.0130, | 0.0132, | 0.0133, | 0.0134, | 0.0135, | 0.0136, | 0.0137, | 0.0138, | 0.0142, |
| | 0.0129 | 0.0131 | 0.0132 | 0.0133 | 0.0134 | 0.0135 | 0.0136 | 0.0138 | 0.0142 |
| cML-BIC-Profile | 1.000, | 0.962, | 0.606, | 0.105, | 0.053, | 0.126, | 0.617, | 0.952, | 1.000, |
| CHIL-DIC-LIGHE | -0.0995, | -0.0495, | -0.0294, | -0.0094, | 0.0006, | 0.120, 0.0106, | 0.017, | 0.952, | 0.1007, |
| | | | | | | | | | |
| | 0.0130, | 0.0132, | 0.0133, | 0.0134, | 0.0135, | 0.0136, | 0.0137, | 0.0138, | 0.0142, |
| 100.1 | 0.0129 | 0.0131 | 0.0132 | 0.0134 | 0.0134 | 0.0135 | 0.0136 | 0.0138 | 0.0142 |
| MR-Mix | 0.996, | 0.690, | 0.235, | 0.027, | 0.015, | 0.035, | 0.256, | 0.672, | 0.994, |
| | -0.1054, | -0.0513, | -0.0302, | -0.0096, | 0.0006, | 0.0106, | 0.0305, | 0.0501, | 0.0968, |
| | 0.0167, | 0.0168, | 0.0167, | 0.0166, | 0.0166, | 0.0167, | 0.0166, | 0.0168, | 0.0167, |
| | 0.0222 | 0.0221 | 0.022 | 0.022 | 0.022 | 0.0219 | 0.0219 | 0.0219 | 0.022 |
| MR-ContMix | 1.000, | 0.950, | 0.590, | 0.113, | 0.068, | 0.140, | 0.617, | 0.937, | 1.000, |
| | -0.0991, | -0.0492, | -0.0292, | -0.0093, | 0.0007, | 0.0107, | 0.0306, | 0.0506, | 0.1006, |
| | 0.0135, | 0.0138, | 0.0139, | 0.0140, | 0.0141, | 0.0141, | 0.0143, | 0.0145, | 0.0149, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.942, | 0.560, | 0.089, | 0.045, | 0.117, | 0.571, | 0.934, | 1.000, |
| MR-Lasso | | | | | 0.043, | | 0.371, 0.0307, | | |
| | -0.0992, | -0.0492, | -0.0292, | -0.0093, | 0.0007, | 0.0107, | | 0.0506, | 0.1006, |
| | 0.0133, | 0.0133, | 0.0134, | 0.0136, | 0.0136, | 0.0137, | 0.0139, | 0.0141, | 0.0146, |
| | 0.0136 | 0.0139 | 0.014 | 0.0141 | 0.0142 | 0.0142 | 0.0144 | 0.0145 | 0.0149 |
| MR-PRESSO | 0.797, | 0.681, | 0.503, | 0.325, | 0.309, | 0.341, | 0.542, | 0.709, | 0.846, |
| | -0.0817, | -0.0332, | -0.0138, | 0.0049, | 0.0146, | 0.0244, | 0.0444, | 0.0627, | 0.1112, |
| | 0.1256, | 0.1245, | 0.1241, | 0.1228, | 0.1219, | 0.1209, | 0.1198, | 0.1174, | 0.1142, |
| | 0.0349 | 0.0342 | 0.0337 | 0.0331 | 0.0326 | 0.0321 | 0.0317 | 0.0308 | 0.0295 |
| MR-IVW | 0.122, | 0.082, | 0.076, | 0.065, | 0.067, | 0.068, | 0.074, | 0.090, | 0.133, |
| | -0.0825, | -0.0324, | -0.0124, | 0.0077, | 0.0177, | 0.0277, | 0.0477, | 0.0677, | 0.1177, |
| | 0.1737, | 0.1736, | 0.1736, | 0.1736, | 0.1736, | 0.1736, | 0.1736, | 0.1736, | 0.1736. |
| | 0.1665 | 0.1665 | 0.1665 | 0.1665 | 0.1665 | 0.1665 | 0.1665 | 0.1665 | 0.1665 |
| MD IVW OI- | | | | | | | | | |
| MR-IVW-Oracle | 1.000, | 0.947, | 0.556, | 0.084, | 0.040, | 0.107, | 0.560, | 0.938, | 1.000, |
| | -0.0992, | -0.0493, | -0.0293, | -0.0094, | 0.0006, | 0.0106, | 0.0306, | 0.0505, | 0.1004, |
| | 0.0129, | 0.0131, | 0.0132, | 0.0133, | 0.0133, | 0.0134, | 0.0135, | 0.0137, | 0.0140, |
| | 0.0137 | 0.0139 | 0.0141 | 0.0142 | 0.0143 | 0.0143 | 0.0145 | 0.0146 | 0.0151 |
| MR-Egger | 0.296, | 0.297, | 0.294, | 0.296, | 0.295, | 0.298, | 0.303, | 0.308, | 0.317, |
| | 0.3378, | 0.3856, | 0.4047, | 0.4238, | 0.4334, | 0.4430, | 0.4621, | 0.4812, | 0.5289, |
| | 1.0560, | 1.0560, | 1.0560, | 1.0560, | 1.0560, | 1.0560, | 1.0559, | 1.0559, | 1.0559 |
| | 0.6644 | 0.6645 | 0.6645 | 0.6645 | 0.6645 | 0.6645 | 0.6646 | 0.6646 | 0.6647 |
| MR-Weighted-Median | 1.000, | 0.794, | 0.362, | 0.071, | 0.034, | 0.057, | 0.332, | 0.715, | 0.997, |
| · · · · · · · · · · · · · · · · · · · | -0.0991, | -0.0501, | -0.0304, | -0.0108, | -0.0010, | 0.0089, | 0.0285, | 0.713, | 0.997, |
| | 0.0166, | 0.0169, | 0.0170, | 0.0172, | 0.0173, | 0.0089, | | | |
| | | | | | 0.0173, | | 0.0176, | 0.0178, | 0.0184, |
| MD Welsha 136 1 | 0.018 | 0.0183 | 0.0185 | 0.0186 | | 0.0188 | 0.019 | 0.0192 | 0.0198 |
| MR-Weighted-Mode | 0.988, | 0.583, | 0.221, | 0.035, | 0.011, | 0.035, | 0.228, | 0.575, | 0.978, |
| | -0.0982, | -0.0487, | -0.0289, | -0.0094, | 0.0006, | 0.0107, | 0.0303, | 0.0499, | 0.0999, |
| | 0.0200, | 0.0197, | 0.0197, | 0.0198, | 0.0200, | 0.0202, | 0.0203, | 0.0204, | 0.0212, |
| | 0.0247 | 0.0251 | 0.0253 | 0.0255 | 0.0256 | 0.0257 | 0.0259 | 0.0262 | 0.0269 |
| MR-RAPS1 | 0.128, | 0.086, | 0.075, | 0.074, | 0.075, | 0.075, | 0.072, | 0.085, | 0.130, |
| | -0.0825, | -0.0325, | -0.0124, | 0.0076, | 0.0176, | 0.0276, | 0.0476, | 0.0676, | 0.1176 |
| | 0.1704, | 0.1704, | 0.1705, | 0.1705, | 0.1705, | 0.1705, | 0.1705, | 0.1705, | 0.1705 |
| | 0.1621 | 0.1621 | 0.1621 | 0.1621 | 0.1621 | 0.1621 | 0.1622 | 0.1622 | 0.1622 |
| MR-RAPS2 | 0.994, | 0.984, | 0.885, | 0.709, | 0.682, | 0.739, | 0.891, | 0.985, | 0.997, |
| MIN-INAL 97 | | | | | | | | | |
| | 0.0931, | 0.1847, | -0.0938, | 0.1946, | 0.1062, | 0.1451, | 0.1144, | 0.3700, | 0.3341, |
| | 3.3651, | 4.0240, | 4.1144, | 5.7829, | 2.4081, | 3.0307, | 2.1872, | 2.9876, | 3.2080, |
| | 0.0343 | 0.0349 | 0.0378 | 0.0463 | 0.0797 | 0.0632 | 0.0382 | 0.036 | 0.1277 |
| MR-RAPS3 | 0.916, | 0.896, | 0.885, | 0.892, | 0.896, | 0.910, | 0.914, | 0.892, | 0.907, |
| | -0.1917, | -0.0748, | 0.0073, | 0.0149, | 0.0345, | 0.0539, | 0.0918, | 0.1284, | 0.2169, |
| | 0.4577, | 0.4362, | 1.2245, | 0.3966, | 0.3894, | 0.3838, | 0.3736, | 0.3631, | 0.3328, |
| | 0.0382 | 0.0356 | 0.336 | 0.033 | 0.0309 | 0.0302 | 0.0293 | 0.0287 | 0.0293 |
| | | | | | | | | | |
| MD DADC4 | 1.000, | 0.992, | 0.959, | 0.884, | 0.871, 0.1198, | 0.886, | 0.963, 0.1920, | 0.996, | 0.999, 0.3337, |
| MR-RAPS4 | 0.0000 | | | | I DILIUX | 0.1617, | | 0.2335, | 1 113337 |
| MR-RAPS4 | -0.0389, | 0.0334, | 0.0483, | 0.2189, | | | | | |
| MR-RAPS4 | -0.0389, 1.7384, 0.0325 | 0.0334, 1.7535, 0.0376 | 0.0483, 1.7108, 0.0339 | 3.5802, 0.0813 | 1.6998, 0.0805 | 1.6979, 0.0614 | 1.7682, 0.0387 | 1.6196, 0.033 | 1.5870, 0.1237 |

Table S61: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE violated, q=0.2, and N=200000.

| | <i>')</i> | | | | , I | | | | |
|--|--|---|--|--|--|---|---|--|---|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.927, | 0.546, | 0.086, | 0.039, | 0.104, | 0.576, | 0.911, | 1.000, |
| CIVIL IVIT THE | -0.0947, | -0.0447, | -0.0251, | -0.0073, | 0.0006, | 0.0084, | 0.0262, | 0.0458, | 0.0955, |
| | 0.0124, | 0.0125, | 0.0121, | 0.0108, | 0.0106, | 0.0113, | 0.0131, | 0.0138, | 0.0141, |
| | 0.0118 | 0.012 | 0.0119 | 0.0117 | 0.0117 | 0.0118 | 0.0122 | 0.0125 | 0.0129 |
| cML-MA-AIC-Profile | 1.000, | 0.927, | 0.546, | 0.086, | 0.039, | 0.103, | 0.576, | 0.911, | 1.000, |
| CIVIL WITT THE I TOME | -0.0948, | -0.0448, | -0.0251, | -0.0073, | 0.0005, | 0.0084, | 0.0262, | 0.0458, | 0.0956, |
| | 0.0124, | 0.0125, | 0.0121, | 0.0108, | 0.0106, | 0.0113, | 0.0202, | 0.0138, | 0.0141, |
| | 0.0124, | 0.0125, | 0.0121, | 0.0108, | 0.0100, | 0.0118 | 0.0131, | 0.0135, | 0.0141, |
| cML-AIC | 1.000, | 0.964, | 0.725, | 0.188, | 0.104, | 0.204, | 0.725, | 0.957, | 1.000, |
| CIVIL-AIC | -0.0971, | -0.0473, | -0.0273, | -0.0085, | 0.104, | 0.204, | 0.723, | 0.937, | 0.0981, |
| | 0.0130, | 0.0473, | 0.0132, | 0.0127, | 0.0003, | 0.0033, | 0.0284, | | 0.0381, |
| | 0.0130, | 0.0131, | 0.0132, | 0.0127, | 0.0127, | 0.0131, | 0.0142, | 0.0147, | 0.0149, |
| M. AIC D. CI | | | | | | | | 0.0106 | |
| cML-AIC-Profile | 1.000, | 0.964, | 0.725, | 0.188, | 0.102, | 0.204, | 0.724, | 0.957, | 1.000, |
| | -0.0972, | -0.0473, | -0.0273, | -0.0085, | 0.0005, | 0.0095, | 0.0284, | 0.0482, | 0.0982, |
| | 0.0130, | 0.0132, | 0.0132, | 0.0127, | 0.0127, | 0.0131, | 0.0142, | 0.0146, | 0.0149, |
| 10. 10. Dra | 0.01 | 0.0101 | 0.0102 | 0.0103 | 0.0104 | 0.0104 | 0.0105 | 0.0107 | 0.011 |
| cML-MA-BIC | 1.000, | 0.999, | 0.881, | 0.188, | 0.050, | 0.183, | 0.870, | 1.000, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0095, | 0.0096, | 0.0097, | 0.0097, | 0.0098, | 0.0098, | 0.0099, | 0.0100, | 0.0102, |
| | 0.0092 | 0.0094 | 0.0095 | 0.0095 | 0.0096 | 0.0096 | 0.0097 | 0.0098 | 0.0101 |
| cML-MA-BIC-Profile | 1.000, | 0.999, | 0.881, | 0.188, | 0.050, | 0.183, | 0.869, | 1.000, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0095, | 0.0096, | 0.0097, | 0.0097, | 0.0098, | 0.0098, | 0.0099, | 0.0100, | 0.0102, |
| | 0.0092 | 0.0094 | 0.0095 | 0.0096 | 0.0096 | 0.0096 | 0.0097 | 0.0098 | 0.0101 |
| cML-BIC | 1.000, | 0.999, | 0.886, | 0.192, | 0.053, | 0.189, | 0.872, | 1.000, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0095, | 0.0096, | 0.0097, | 0.0098, | 0.0098, | 0.0098, | 0.0099, | 0.0100, | 0.0103, |
| | 0.0091 | 0.0093 | 0.0094 | 0.0095 | 0.0095 | 0.0096 | 0.0097 | 0.0098 | 0.01 |
| cML-BIC-Profile | 1.000, | 0.999, | 0.886, | 0.192, | 0.053, | 0.188, | 0.871, | 1.000, | 1.000, |
| 10 1101110 | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0095, | 0.0096, | 0.0097, | 0.0098, | 0.0001, | 0.0098, | 0.0099, | 0.0100, | 0.01001, |
| | 0.0093, | 0.0090, | 0.0097, | 0.0098, | 0.0098, | 0.0096 | 0.0099, | 0.0100, | 0.0103, |
| MR-Mix | 1.000, | 0.0093 | 0.522, | 0.062, | 0.0093 | 0.065, | 0.476, | 0.890, | 1.000, |
| IVIIX-IVIIX | -0.1060, | -0.0522, | -0.0311, | -0.0104, | -0.0003, | 0.003, | 0.0297, | 0.0491, | 0.0960, |
| | 0.0128, | 0.0322, | 0.0128, | 0.0128, | 0.0128, | 0.0038, | 0.0237, | 0.0491, | 0.0300, |
| | 0.0128, | 0.0129, | 0.0128, | 0.0128, 0.0159 | 0.0128, | 0.0128, | 0.0128, | 0.0129, | 0.0128, |
| 100 C - 10 | | | | | | | | | |
| MR-ContMix | 1.000, | 0.999, | 0.876, | 0.204, | 0.069, | 0.195, | 0.873, | 1.000, | 1.000, |
| | -0.0996, | -0.0497, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0502, | 0.1001, |
| | 0.0098, | 0.0099, | 0.0099, | 0.0100, | 0.0100, | 0.0100, | 0.0101, | 0.0102, | 0.0104, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.998, | 0.857, | 0.170, | 0.049, | 0.159, | 0.836, | 1.000, | 1.000, |
| | -0.0997, | -0.0498, | -0.0298, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1000, |
| | 0.0097, | 0.0098, | 0.0099, | 0.0100, | 0.0100, | 0.0100, | 0.0100, | 0.0101, | 0.0105, |
| | 0.0096 | 0.0098 | 0.0099 | 0.01 | 0.0101 | 0.0101 | 0.0102 | 0.0103 | 0.0106 |
| MR-PRESSO | 0.703, | 0.614, | 0.515, | 0.314, | 0.261, | 0.314, | 0.511, | 0.625, | 0.756, |
| | -0.0815, | -0.0330, | -0.0130, | 0.0071, | 0.0168, | 0.0269, | 0.0465, | 0.0656, | 0.1136, |
| | 0.1538, | 0.1534, | 0.1533, | 0.1530, | 0.1528, | 0.1527, | 0.1521, | 0.1512, | 0.1497, |
| | 0.0583 | 0.0573 | 0.0572 | 0.0568 | 0.0566 | 0.0565 | 0.0557 | 0.0544 | 0.0522 |
| MR-IVW | 0.109, | 0.080, | 0.076, | 0.077, | 0.081, | 0.081, | 0.083, | 0.089, | 0.119, |
| | -0.0832, | -0.0331, | -0.0130, | 0.0070, | 0.0170, | 0.0271, | 0.0471, | 0.0671, | 0.1172, |
| | 0.1742, | 0.1742, | 0.1742, | 0.1742, | 0.1742, | 0.1742, | 0.1742, | 0.1742, | 0.1742, |
| | 0.1672 | 0.1671 | 0.1671 | 0.1671 | 0.1671 | 0.1671 | 0.1671 | 0.1671 | 0.1671 |
| MR-IVW-Oracle | 1.000, | 0.999, | 0.862, | 0.161, | 0.042, | 0.153, | 0.837, | 1.000, | 1.000, |
| mit i monucio | -0.0997, | -0.0498, | -0.0298, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0500, | 0.1000, |
| | 0.0094, | 0.0095, | 0.0096, | 0.0096, | 0.0001, | 0.0097, | 0.0098, | 0.0099, | 0.0101, |
| | 0.0094, | 0.0093, | 0.0090, | 0.0090, | 0.0097, | 0.0097, | 0.0098, | 0.0099, | 0.0101, |
| MP Egga- | | 0.0099 | 0.01 | 0.0101 | 0.0101 | 0.0102 | 0.0103 | | |
| MR-Egger | 0.311, | | | | | | | 0.320, | 0.334, |
| | 0.2987, | 0.3476, | 0.3671, | 0.3866, | 0.3964, | 0.4062, | 0.4257, | 0.4452, | 0.4940, |
| | 1.0869, | 1.0867, 0.663 | 1.0866, | 1.0865, | 1.0865, | 1.0864, 0.663 | 1.0864, | 1.0863, | 1.0861, |
| | | | 0.663 | 0.663 | 0.663 | I U.DD.5 | 0.663 | 0.663 | 0.663 1.000, |
| 4D W/ 1 | 0.663 | | | 0.112 | 0.007 | | 0.500 | | 1 1 000 |
| MR-Weighted-Median | 1.000, | 0.976, | 0.652, | 0.113, | 0.035, | 0.087, | 0.590, | 0.949, | |
| MR-Weighted-Median | 1.000, -0.0995, | 0.976, -0.0502, | 0.652, -0.0304, | -0.0106, | -0.0007, | 0.087, 0.0092, | 0.0290, | 0.0489, | 0.0983, |
| MR-Weighted-Median | 1.000, -0.0995, 0.0118, | 0.976, -0.0502, 0.0121, | 0.652, -0.0304, 0.0122, | -0.0106, 0.0123, | -0.0007, 0.0124, | 0.087, 0.0092, 0.0125, | 0.0290, 0.0126, | 0.0489, 0.0127, | 0.0983, 0.0132, |
| | 1.000, -0.0995, 0.0118, 0.0128 | 0.976, -0.0502, 0.0121, 0.013 | 0.652, -0.0304, 0.0122, 0.0131 | -0.0106, 0.0123, 0.0132 | -0.0007, 0.0124, 0.0133 | 0.087, 0.0092, 0.0125, 0.0133 | 0.0290, 0.0126, 0.0135 | 0.0489, 0.0127, 0.0136 | 0.0983, 0.0132, 0.014 |
| | 1.000, -0.0995, 0.0118, 0.0128 | 0.976, -0.0502, 0.0121, 0.013 | 0.652, -0.0304, 0.0122, 0.0131 0.446, | -0.0106, 0.0123, 0.0132 0.063, | -0.0007, 0.0124, 0.0133 0.014, | 0.087, 0.0092, 0.0125, 0.0133 | 0.0290, 0.0126, 0.0135 0.459, | 0.0489, 0.0127, 0.0136 0.860, | 0.0983, 0.0132, 0.014 0.994, |
| | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, | -0.0106, 0.0123, 0.0132 0.063, -0.0093, | -0.0007, 0.0124, 0.0133 0.014, 0.0007, | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, | 0.0290, 0.0126, 0.0135 0.459, 0.0305, | 0.0489, 0.0127, 0.0136 0.860, 0.0503, | 0.0983, 0.0132, 0.014 0.994, 0.0999, |
| | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, |
| MR-Weighted-Mode | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, 0.0171 | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.018 |
| | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, 0.0171 0.073, | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.018 |
| MR-Weighted-Mode | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, 0.0171 0.073, 0.0159, | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.018 0.126, 0.1160, |
| MR-Weighted-Mode | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1685, | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1685, | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1685, | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, 0.0171 0.073, 0.0159, 0.1685, | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1685, | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, 0.1685, | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.018 0.126, 0.1160, 0.1686, |
| MR-Weighted-Mode | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, 0.0171 0.073, 0.0159, | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.018 0.126, 0.1160, |
| MR-Weighted-Mode | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1685, 0.1628 | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1685, | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1685, | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, 0.0171 0.073, 0.0159, 0.1685, | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1685, | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, 0.1685, 0.1628 | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, 0.1629 | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.018 0.126, 0.1160, 0.1686, |
| MR-Weighted-Mode MR-RAPS1 | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1685, 0.1628 | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1685, 0.1628 | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1685, 0.1628 | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, 0.0171 0.073, 0.0159, 0.1685, 0.1628 | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1628 | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, 0.1685, 0.1628 | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, 0.1629 | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.018 0.126, 0.1160, 0.1686, 0.1629 |
| MR-Weighted-Mode MR-RAPS1 | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1628 0.997, 0.4776, | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1628 0.997, 0.2965, | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 0.967, 0.3959, | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.0077, 0.0059, 0.1685, 0.1628 0.773, | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, 0.0171 0.073, 0.0159, 0.1685, 0.1628 0.719, 0.4960, | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1685, 0.1628 0.769, 0.2048, | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, 0.1685, 0.1628 0.958, 0.4515, | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, 0.1629 0.996, 0.6053, | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.018 0.126, 0.1160, 0.1686, 0.1629 0.995, 0.8674, |
| MR-Weighted-Mode MR-RAPS1 | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1685, 0.1628 0.997, 0.4776, 4.6454, | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1628 0.997, 0.2965, 3.0003, | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 0.967, 0.3959, 3.3803, | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1688, 0.1628 0.773, 0.8531, 9.3107, | -0.0007, 0.0124, 0.0133 -0.014, 0.0007, 0.0149, 0.0171 -0.073, 0.0159, 0.1685, 0.1628 -0.719, 0.4960, 5.4037, | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1685, 0.1628 0.769, 0.2048, 3.4138, | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, 0.1685, 0.1628 0.958, 0.4515, 2.6366, | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, 0.1629 0.996, 0.6053, 3.2164, | 0.0983 0.0132 0.014 0.994, 0.0999 0.0156 0.018 0.126, 0.1160 0.1686 0.1629 0.995, 0.8674 4.8518 |
| MR-RAPS1 MR-RAPS2 | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1685, 0.1628 0.997, 0.4776, 4.6454, 0.0282 | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1685, 0.1628 0.997, 0.2965, 3.0003, 0.0224 | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 0.967, 0.3959, 3.3803, 0.0243 | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1628 0.773, 0.8531, 9.3107, | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, 0.0171 0.073, 0.0159, 0.1628 0.719, 0.4960, 5.4037, 0.0258 | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1685, 0.1628 0.769, 0.2048, 3.4138, 0.0246 | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, 0.1628 0.958, 0.4515, 2.6366, 0.0234 | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, 0.1629 0.996, 0.6053, 3.2164, 0.0272 | 0.0983, 0.0132, 0.014 0.9994, 0.0999, 0.0156, 0.118 0.126, 0.1160, 0.1686, 0.1629 0.995, 0.8674, 4.8518, 0.0311 |
| MR-Weighted-Mode MR-RAPS1 | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1685, 0.1628 0.997, 0.4776, 4.6454, 0.0282 | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1628 0.997, 0.2965, 3.0003, 0.0224 | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 0.967, 0.3959, 3.3803, 0.0243 | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1685, 0.1628 0.773, 0.8531, 9.3107, 0.0277 | -0.0007, 0.0124, 0.0133 -0.014, 0.0007, 0.0149, 0.0171 -0.073, 0.0159, 0.1628 -0.719, 0.4960, 5.4037, 0.0258 | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1685, 0.1628 0.769, 0.2048, 3.4138, 0.0246 | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.1628 0.1628 0.958, 0.4515, 2.6366, 0.0234 | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, 0.1629 0.996, 0.6053, 3.2164, 0.0272 | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.018 0.126, 0.1160, 0.1686, 0.1629 0.995, 0.8674, 4.8518, 0.0311 0.935, |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1685, 0.1628 0.997, 4.6454, 0.0282 0.947, -0.1950, | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1628 0.997, 0.2965, 3.0003, 0.0224 0.931, -0.0634, | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 0.967, 0.3959, 3.3803, 0.0243 0.923, -0.0266, | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1628 0.773, 0.8531, 9.3107, 0.0277 0.939, 0.0233, | -0.0007, 0.0124, 0.0133 -0.014, 0.0007, 0.0149, 0.0171 -0.073, 0.01685, 0.1628 -0.719, 0.4960, 5.4037, 0.0258 -0.939, 0.0436, | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1685, 0.1628 0.769, 0.2048, 3.4138, 0.0246 0.935, 0.0649, | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, 0.1628 0.958, 0.4515, 2.6366, 0.0234 0.915, 0.1013, | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1629 0.996, 0.6053, 3.2164, 0.0272 0.920, 0.1335, | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.1160, 0.1686, 0.1629 0.995, 0.8674, 4.8518, 0.0311 |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1685, 0.1628 0.997, 0.4776, 4.6454, 0.0282 0.947, -0.1950, 0.8378, | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1685, 0.1628 0.997, 0.2965, 3.0003, 0.0224 0.931, -0.0634, 0.4513, | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 0.967, 0.3959, 3.3803, 0.0243 0.923, -0.0266, 0.4709, | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1685, 0.1628 0.773, 0.8531, 9.3107, 0.0277 0.939, 0.0233, 0.4192, | -0.0007, 0.0124, 0.0133 0.014, 0.0007, 0.0149, 0.0171 0.073, 0.1628 0.719, 0.4960, 5.4037, 0.0258 0.939, 0.0496, 0.4097, | 0.087, 0.0092, 0.0125, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1685, 0.1628 0.769, 0.2048, 3.4138, 0.0246 0.935, 0.0649, 0.4030, | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, 0.1628 0.958, 0.4515, 2.6366, 0.0234 0.915, 0.1013, 0.3925, | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, 0.1629 0.996, 0.6053, 3.2164, 0.0272 0.920, 0.1335, 0.4270, | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.1160, 0.1180, 0.1629 0.995, 0.8674, 4.8518, 0.0311 |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 MR-RAPS3 | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1685, 0.1628 0.997, 0.4776, 4.6454, 0.0282 0.947, -0.1950, 0.8378, 0.1869 | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1685, 0.1628 0.997, 0.2965, 3.0003, 0.0224 0.931, -0.0634, 0.4513, 0.0268 | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 0.967, 0.3959, 3.3803, 0.0243 0.923, -0.0266, 0.4709, 0.0366 | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1685, 0.1628 0.773, 0.8531, 9.3107, 0.0277 0.939, 0.0233, 0.4192, 0.0267 | -0.0007, 0.0124, 0.0133 -0.014, 0.0007, 0.0149, 0.0171 -0.073, 0.1685, 0.1628 -0.719, 0.4960, 5.4037, 0.0258 -0.939, 0.0436, 0.4097, 0.0269 | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1685, 0.1628 0.769, 0.2048, 3.4138, 0.0246 0.935, 0.0649, 0.4030, 0.0475 | 0.0290, 0.0126, 0.0135 0.459, 0.0135 0.0151, 0.0173 0.082, 0.0459, 0.1628 0.958, 0.4515, 2.6366, 0.0234 0.915, 0.1013, 0.3925, 0.0231 | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, 0.1629 0.996, 0.6053, 3.2164, 0.0272 0.920, 0.1335, 0.4270, | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.1160, 0.1629 0.995, 0.8674, 4.8518, 0.0311 0.935, 0.2275, 0.3409, 0.0199 |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1628 0.997, 4.6454, 0.0282 0.947, -0.1950, 0.8378, 0.1869 | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1628 0.997, 0.2965, 3.0003, 0.0224 0.931, -0.0634, 0.4513, 0.0268 | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 0.967, 0.3959, 3.3803, 0.0243 0.923, -0.0266, 0.4709, 0.0366 | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1685, 0.1628 0.773, 0.8531, 9.3107, 0.0277 0.939, 0.0233, 0.4192, 0.0267 0.956, | -0.0007, 0.0124, 0.0133 -0.014, 0.0007, 0.0149, 0.0171 -0.073, 0.0159, 0.1685, 0.1628 -0.719, 0.4960, 5.4037, 0.0258 0.939, 0.0436, 0.4097, 0.0269 | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1628 0.769, 0.2048, 3.4138, 0.0246 0.935, 0.0649, 0.4030, 0.0475 | 0.0290, 0.0126, 0.0135 0.459, 0.0305, 0.0151, 0.0173 0.082, 0.0459, 0.1685, 0.1628 0.958, 0.4515, 2.6366, 0.0234 0.915, 0.01013, 0.3925, 0.0231 | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, 0.1629 0.996, 0.6053, 3.2164, 0.0272 0.920, 0.1335, 0.4270, 0.0352 | 0.0983, 0.0132, 0.0114 0.994, 0.0999, 0.0156, 0.1160, 0.1629 0.995, 0.8674, 4.8518, 0.0311 0.935, 0.2275, 0.3409, 0.0199 |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 MR-RAPS3 | 1.000, -0.0995, 0.0118, 0.0128 0.997, -0.0992, 0.0148, 0.0165 0.109, -0.0841, 0.1685, 0.1628 0.997, 0.4776, 4.6454, 0.0282 0.947, -0.1950, 0.8378, 0.1869 | 0.976, -0.0502, 0.0121, 0.013 0.890, -0.0493, 0.0147, 0.0167 0.082, -0.0341, 0.1685, 0.1628 0.997, 0.2965, 3.0003, 0.0224 0.931, -0.0634, 0.4513, 0.0268 | 0.652, -0.0304, 0.0122, 0.0131 0.446, -0.0292, 0.0147, 0.0169 0.082, -0.0141, 0.1685, 0.1628 0.967, 0.3959, 3.3803, 0.0243 0.923, -0.0266, 0.4709, 0.0366 | -0.0106, 0.0123, 0.0132 0.063, -0.0093, 0.0149, 0.017 0.077, 0.0059, 0.1685, 0.1628 0.773, 0.8531, 9.3107, 0.0277 0.939, 0.0233, 0.4192, 0.0267 | -0.0007, 0.0124, 0.0133 -0.014, 0.0007, 0.0149, 0.0171 -0.073, 0.1685, 0.1628 -0.719, 0.4960, 5.4037, 0.0258 -0.939, 0.0436, 0.4097, 0.0269 | 0.087, 0.0092, 0.0125, 0.0133 0.059, 0.0106, 0.0149, 0.0172 0.076, 0.0259, 0.1685, 0.1628 0.769, 0.2048, 3.4138, 0.0246 0.935, 0.0649, 0.4030, 0.0475 | 0.0290, 0.0126, 0.0135 0.459, 0.0135 0.0151, 0.0173 0.082, 0.0459, 0.1628 0.958, 0.4515, 2.6366, 0.0234 0.915, 0.1013, 0.3925, 0.0231 | 0.0489, 0.0127, 0.0136 0.860, 0.0503, 0.0150, 0.0175 0.088, 0.0659, 0.1686, 0.1629 0.996, 0.6053, 3.2164, 0.0272 0.920, 0.1335, 0.4270, | 0.0983, 0.0132, 0.014 0.994, 0.0999, 0.0156, 0.1160, 0.1629 0.995, 0.8674, 4.8518, 0.0311 0.935, 0.2275, 0.3409, 0.0199 |

Table S62: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE violated, q=0.4, and N=50000.

| // | <i>' '</i> | | | | , <u>1</u> | | | | |
|--------------------|------------------------------|--------------------------------|---------------------|---------------------|--------------------|--------------------|--------------------|----------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.855, | 0.295, | 0.109, | 0.027, | 0.019, | 0.031, | 0.105, | 0.287, | 0.785, |
| | -0.0875, | -0.0394, | -0.0221, | -0.0067, | 0.0005, | 0.0080, | 0.0232, | 0.0404, | 0.0873, |
| | 0.0272, | 0.0254, | 0.0235, | 0.0223, | 0.0225, | 0.0229, | 0.0250, | 0.0274, | 0.0311, |
| | 0.0283 | 0.028 | 0.0277 | 0.0276 | 0.0277 | 0.0279 | 0.0285 | 0.0292 | 0.0308 |
| cML-MA-AIC-Profile | 0.853, | 0.293, | 0.102, | 0.027, | 0.019, | 0.029, | 0.101, | 0.287, | 0.783, |
| | -0.0878, | -0.0395, | -0.0221, | -0.0067, | 0.0005, | 0.0080, | 0.0233, | 0.0404, | 0.0874, |
| | 0.0274, | 0.0254, | 0.0236, | 0.0223, | 0.0225, | 0.0229, | 0.0251, | 0.0274, | 0.0312, |
| | 0.0284 | 0.0282 | 0.0279 | 0.0278 | 0.0279 | 0.0281 | 0.0287 | 0.0294 | 0.031 |
| cML-AIC | 0.939, | 0.498, | 0.242, | 0.098, | 0.076, | 0.100, | 0.248, | 0.477, | 0.893, |
| | -0.0941, | -0.0449, | -0.0260, | -0.0082, | 0.0006, | 0.0092, | 0.0268, | 0.0454, | 0.0940, |
| | 0.0296, | 0.0291, | 0.0280, | 0.0278, | 0.0278, | 0.0281, | 0.0295, | 0.0309, | 0.0333, |
| MI AIC D. GI. | 0.0234 | 0.0238 | 0.024 | 0.0243 | 0.0244 | 0.0245 | 0.0247 | 0.025 | 0.0257 |
| cML-AIC-Profile | 0.938, -0.0943, | 0.490, -0.0449, | 0.240, -0.0260, | 0.096, -0.0082, | 0.075, 0.0006, | 0.097, 0.0092, | 0.242, 0.0268, | 0.471, 0.0455, | 0.893, 0.0940, |
| | 0.0297, | 0.0291, | 0.0280, | 0.0082, | 0.0008, | 0.0092, | 0.0208, | 0.0433, | 0.0334, |
| | 0.0237, | 0.024 | 0.0242 | 0.0276, | 0.0276, | 0.0247 | 0.0249 | 0.0252 | 0.0259 |
| cML-MA-BIC | 0.992, | 0.624, | 0.249, | 0.066, | 0.045, | 0.067, | 0.242, | 0.593, | 0.987, |
| | -0.0995, | -0.0495, | -0.0295, | -0.0096, | 0.0003, | 0.0103, | 0.0302, | 0.0502, | 0.1001, |
| | 0.0217, | 0.0220, | 0.0222, | 0.0223, | 0.0224, | 0.0226, | 0.0228, | 0.0231, | 0.0239, |
| | 0.0218 | 0.0222 | 0.0224 | 0.0226 | 0.0227 | 0.0228 | 0.023 | 0.0233 | 0.0239 |
| cML-MA-BIC-Profile | 0.992, | 0.622, | 0.248, | 0.066, | 0.045, | 0.067, | 0.242, | 0.590, | 0.987, |
| | -0.0995, | -0.0495, | -0.0295, | -0.0096, | 0.0003, | 0.0103, | 0.0302, | 0.0502, | 0.1001, |
| | 0.0217, | 0.0220, | 0.0222, | 0.0223, | 0.0224, | 0.0226, | 0.0228, | 0.0231, | 0.0239, |
| | 0.0219 | 0.0223 | 0.0225 | 0.0227 | 0.0228 | 0.0229 | 0.0231 | 0.0233 | 0.024 |
| cML-BIC | 0.992, | 0.638, | 0.257, | 0.072, | 0.048, | 0.071, | 0.246, | 0.605, | 0.990, |
| | -0.0996, | -0.0497, | -0.0297, | -0.0096, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0216, | 0.0220, | 0.0221, | 0.0223, | 0.0224, | 0.0225, | 0.0228, | 0.0231, | 0.0239, |
| 10 Pro | 0.0215 | 0.0219 | 0.0221 | 0.0223 | 0.0224 | 0.0225 | 0.0227 | 0.023 | 0.0236 |
| cML-BIC-Profile | 0.992, | 0.633, | 0.257, | 0.071, | 0.046, | 0.071, | 0.244, | 0.597, | 0.990, |
| | -0.0996, | -0.0497, | -0.0297, | -0.0096, | 0.0003, | 0.0103, | 0.0303, 0.0228, | 0.0503, | 0.1003, |
| | 0.0216, | 0.0220, | 0.0221, | 0.0223, 0.0224 | 0.0224, | 0.0225, | | 0.0231, | 0.0239, |
| MD Min | 0.0216 | 0.022 | 0.0222 | | 0.0225 | 0.0226 | 0.0228 | 0.023 | 0.0237 |
| MR-Mix | 0.943, | 0.396, -0.0505, | 0.136, | 0.025, | 0.022, 0.0002, | 0.036, 0.0101, | 0.131, 0.0295, | 0.334, 0.0484, | 0.910, |
| | -0.1034, 0.0248, | 0.0248, | -0.0299, 0.0248, | -0.0097, 0.0247, | 0.0002, | 0.0101, | 0.0293, | 0.0484, | 0.0944, 0.0248, |
| | 0.0248, | 0.0303 | 0.0248, | 0.0301 | 0.0247, | 0.0301 | 0.0248, | 0.0248, | 0.0248, |
| MR-ContMix | 0.993, | 0.632, | 0.276, | 0.079, | 0.056, | 0.083, | 0.270, | 0.603, | 0.984, |
| WIK-CORONIX | -0.0992, | -0.0494, | -0.0296, | -0.0096, | 0.0003, | 0.0102, | 0.0301, | 0.0499, | 0.0996, |
| | 0.0227, | 0.0229, | 0.0231, | 0.0233, | 0.0234, | 0.0235, | 0.0238, | 0.0241, | 0.0250, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.989, | 0.600, | 0.237, | 0.061, | 0.042, | 0.069, | 0.231, | 0.548, | 0.971, |
| | -0.0992, | -0.0495, | -0.0297, | -0.0098, | 0.0001, | 0.0101, | 0.0300, | 0.0499, | 0.0994, |
| | 0.0222, | 0.0226, | 0.0229, | 0.0230, | 0.0231, | 0.0233, | 0.0236, | 0.0238, | 0.0247, |
| | 0.0228 | 0.0232 | 0.0234 | 0.0236 | 0.0237 | 0.0239 | 0.0241 | 0.0243 | 0.025 |
| MR-PRESSO | 0.727, | 0.477, | 0.333, | 0.249, | 0.240, | 0.255, | 0.355, | 0.511, | 0.777, |
| | -0.0733, | -0.0278, | -0.0082, | 0.0109, | 0.0200, | 0.0290, | 0.0480, | 0.0670, | 0.1140, |
| | 0.1774, | 0.1750, | 0.1748, | 0.1728, | 0.1721, | 0.1713, | 0.1703, | 0.1686, | 0.1629, |
| V 00 17 17 17 | 0.0515 | 0.0496 | 0.0494 | 0.0486 | 0.0483 | 0.0482 | 0.0478 | 0.0473 | 0.0455 |
| MR-IVW | 0.086, | 0.069, | 0.068, | 0.066, | 0.067, | 0.067, | 0.076, | 0.080, | 0.108, |
| | -0.0690, | -0.0188, | 0.0012, | 0.0213, | 0.0313, 0.2408, | 0.0413, 0.2408, | 0.0614, | 0.0814, | 0.1315, |
| | 0.2407, 0.2341 | 0.2407, 0.234 | 0.2407, 0.234 | 0.2408, 0.234 | 0.2408, | 0.2408, | 0.2408, 0.234 | 0.2408, 0.234 | 0.2408, 0.234 |
| MR-IVW-Oracle | 0.2341 | 0.593, | 0.234 | 0.254 | 0.234 | 0.254 | 0.234 | 0.234 | 0.234 |
| WIK-IV W-Oldele | -0.0991, | -0.0494, | -0.0295, | -0.0096, | 0.0003, | 0.0103, | 0.220, | 0.0500, | 0.0998, |
| | 0.0215, | 0.0218, | 0.0220, | 0.0222, | 0.0223, | 0.0224, | 0.0226, | 0.0229, | 0.0236, |
| | 0.0229 | 0.0233 | 0.0235 | 0.0237 | 0.0238 | 0.024 | 0.0242 | 0.0244 | 0.0250, |
| MR-Egger | 0.206, | 0.212, | 0.213, | 0.221, | 0.222, | 0.222, | 0.224, | 0.229, | 0.250, |
| DD | 0.5169, | 0.5640, | 0.5828, | 0.6016, | 0.6110, | 0.6204, | 0.6392, | 0.6580, | 0.7050, |
| | 1.0543, | 1.0541, | 1.0541, | 1.0541, | 1.0540, | 1.0540, | 1.0540, | 1.0539, | 1.0539, |
| | 0.7834 | 0.7835 | 0.7835 | 0.7836 | 0.7836 | 0.7837 | 0.7837 | 0.7838 | 0.784 |
| MR-Weighted-Median | 0.922, | 0.444, | 0.203, | 0.079, | 0.060, | 0.053, | 0.129, | 0.272, | 0.786, |
| | -0.1010, | -0.0534, | -0.0343, | -0.0154, | -0.0059, | 0.0036, | 0.0227, | 0.0418, | 0.0894, |
| | 0.0297, | 0.0307, | 0.0311, | 0.0317, | 0.0320, | 0.0323, | 0.0328, | 0.0333, | 0.0349, |
| NO WILL : | 0.0297 | 0.0302 | 0.0305 | 0.0307 | 0.0309 | 0.031 | 0.0313 | 0.0317 | 0.0326 |
| MR-Weighted-Mode | 0.932, | 0.410, | 0.149, | 0.037, | 0.025, | 0.042, | 0.152, | 0.383, | 0.901, |
| | -0.1023, | -0.0534, | -0.0323, | -0.0130, | -0.0033, | 0.0065, | 0.0258, | 0.0454, | 0.0945, |
| | 0.1260, | 0.1259, | 0.1286, | 0.1285, | 0.1284, | 0.1283, | 0.1282, | 0.1280, | 0.1276, |
| MD DARGI | 0.0497 | 0.0502 | 0.0505 | 0.0507 | 0.0507 | 0.0509 | 0.0512 | 0.0515 | 0.0526 |
| MR-RAPS1 | 0.083, | 0.067, | 0.068, | 0.068, | 0.065, | 0.064, 0.0409, | 0.072, | 0.081, | 0.106, |
| | -0.0692, 0.2329, | -0.0191, 0.2330, | 0.0009, 0.2330, | 0.0209, 0.2330, | 0.0309, 0.2330, | 0.0409, 0.2330, | 0.0610, 0.2331, | 0.0810, 0.2331, | 0.1310, 0.2332, |
| | 0.2329, 0.2292 | 0.2330, | 0.2330, | 0.2330, 0.2292 | 0.2330, 0.2292 | 0.2330, | 0.2331, 0.2292 | 0.2331, 0.2292 | 0.2332, |
| MR-RAPS2 | 0.2292 | 0.2292 | 0.2292 | 0.2292 | 0.2292 | 0.2292 | 0.2292 | 0.2292 | 0.2293 |
| 1711X-1X711 32 | -0.0864, | -0.0379, | -0.0177, | 0.000, | 0.039, | 0.000, | 0.066, | 0.073, | 0.088, |
| | 0.2243, | 0.2284, | 0.2281, | 0.2283, | 0.0124, | 0.2300, | 0.0412, | 0.0020, | 0.1146, |
| | 0.2299 | 0.2308 | 0.2305 | 0.2306 | 0.2309 | 0.2314 | 0.2305 | 0.231 | 0.2312 |
| MR-RAPS3 | 0.896, | 0.895, | 0.890, | 0.897, | 0.895, | 0.890, | 0.899, | 0.896, | 0.895, |
| | -0.5866, | -1.1754, | 0.1021, | -2.1821, | 2.4716, | -3.1800, | 0.3914, | -0.0317, | 0.8791, |
| | 21.0060, | 34.1200, | 11.9450, | 65.0454, | 58.1470, | 102.3099, | 9.2434, | 50.8193, | 12.6109, |
| | 62.3479 | 83.9749 | 8.2491 | 156.102 | 216.8516 | 716.7582 | 6.128 | 85.8968 | 12.2244 |
| MR-RAPS4 | 0.989, | 0.974, | 0.949, | 0.911, | 0.906, | 0.907, | 0.929, | 0.969, | 0.998, |
| MIK-KAP54 | | | | -0.0919, | -0.1390, | -0.0308, | -0.2430, | -1.2295, | -0.0585, |
| MR-RAP54 | -0.0482, | -0.2519, | -0.1746, | -0.0919, | -0.1350, | -0.0306, | -0.2430, | -1.2293, | |
| WK-KAP34 | -0.0482, 6.6462, 0.387 | -0.2519, 11.6099, 0.3825 | 9.5661, 0.2742 | 9.2975, 0.2694 | 9.0784, 0.2925 | 9.6594, 0.4394 | 10.4690, 0.5783 | 47.9748, 201.0763 | 5.2586, 0.3555 |

Table S63: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE violated, q=0.4, and N=100000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|---------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|-------------------|
| cML-MA-AIC | 0.979, | 0.569, | 0.209, | 0.050, | 0.036, | 0.044, | 0.217, | 0.525, | 0.948, |
| | -0.0914, | -0.0419, | -0.0235, | -0.0071, | 0.0002, | 0.0077, | 0.0238, | 0.0421, | 0.0908, |
| | 0.0203, 0.0198 | 0.0200, 0.0199 | 0.0185, 0.0197 | 0.0169, 0.0195 | 0.0165, 0.0195 | 0.0169, 0.0197 | 0.0191, 0.0203 | 0.0208, 0.0209 | 0.0228, 0.0219 |
| ML-MA-AIC-Profile | 0.0198 | 0.568, | 0.0197 | 0.0193 | 0.0193 | 0.0197 | 0.0203 | 0.523, | 0.0219 |
| WIL-WA-AIC-I TOILIC | -0.0915, | -0.0419, | -0.0235, | -0.0071, | 0.0002, | 0.0077, | 0.0239, | 0.0422, | 0.0910, |
| | 0.0204, | 0.0200, | 0.0185, | 0.0169, | 0.0165, | 0.0169, | 0.0191, | 0.0209, | 0.0229 |
| | 0.0199 | 0.0199 | 0.0197 | 0.0196 | 0.0196 | 0.0197 | 0.0204 | 0.021 | 0.022 |
| cML-AIC | 0.992, | 0.733, | 0.391, | 0.140, | 0.101, | 0.139, | 0.399, | 0.708, | 0.975, |
| | -0.0958, | -0.0458, | -0.0265, | -0.0082, | 0.0001, | 0.0089, | 0.0269, | 0.0463, | 0.0954 |
| | 0.0217, | 0.0219, | 0.0213, | 0.0209, | 0.0207, | 0.0207, | 0.0222, | 0.0232, | 0.0247 |
| | 0.0165 | 0.0168 | 0.017 | 0.0172 | 0.0172 | 0.0173 | 0.0175 | 0.0177 | 0.0181 |
| cML-AIC-Profile | 0.992, | 0.732, | 0.389, | 0.140, | 0.100, | 0.137, | 0.396, | 0.707, | 0.975, |
| | -0.0959, | -0.0458, | -0.0265, | -0.0082, | 0.0002, | 0.0089, | 0.0269, | 0.0463, | 0.0956 |
| | 0.0217, | 0.0219, | 0.0213, | 0.0209, | 0.0208, | 0.0207, | 0.0223, | 0.0232, | 0.0248 |
| M. M. DIG | 0.0166 | 0.0169 | 0.017 | 0.0172 | 0.0173 | 0.0173 | 0.0175 | 0.0177 | 0.0182 |
| cML-MA-BIC | 1.000, | 0.884, | 0.476, | 0.098, | 0.058, | 0.099, 0.0101, | 0.467, | 0.857, | 1.000, |
| | -0.0998, 0.0156, | -0.0498, 0.0159, | -0.0298, 0.0160, | -0.0098, 0.0161, | 0.0002, 0.0162, | 0.0101, | 0.0301, 0.0165, | 0.0501, 0.0167, | 0.1001 0.0173 |
| | 0.0156, | 0.0156 | 0.0166, | 0.0151, | 0.0162, | 0.016 | 0.0163, | 0.0164 | 0.0173 |
| ML-MA-BIC-Profile | 1.000, | 0.882, | 0.470, | 0.0139 | 0.058, | 0.096, | 0.463, | 0.857, | 1.000, |
| VIL-WIA-DIC-TIONIC | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0101, | 0.0301, | 0.0501, | 0.1002 |
| | 0.0156, | 0.0159, | 0.0160, | 0.0161, | 0.0162, | 0.0163, | 0.0165, | 0.0167, | 0.0173 |
| | 0.0154 | 0.0157 | 0.0158 | 0.0159 | 0.0162, | 0.0161 | 0.0162 | 0.0164 | 0.0169 |
| cML-BIC | 1.000, | 0.889, | 0.485, | 0.105, | 0.062, | 0.101, | 0.475, | 0.865, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0502, | 0.1002 |
| | 0.0156, | 0.0159, | 0.0160, | 0.0162, | 0.0163, | 0.0164, | 0.0165, | 0.0167, | 0.0174 |
| | 0.0152 | 0.0155 | 0.0156 | 0.0157 | 0.0158 | 0.0159 | 0.016 | 0.0162 | 0.0167 |
| cML-BIC-Profile | 1.000, | 0.887, | 0.485, | 0.105, | 0.061, | 0.099, | 0.473, | 0.863, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0502, | 0.1002 |
| | 0.0156, | 0.0159, | 0.0160, | 0.0162, | 0.0163, | 0.0164, | 0.0165, | 0.0167, | 0.0174 |
| 1 m 1 c | 0.0152 | 0.0155 | 0.0156 | 0.0158 | 0.0158 | 0.0159 | 0.0161 | 0.0162 | 0.0167 |
| MR-Mix | 0.994, | 0.662, | 0.243, | 0.055, | 0.028, | 0.039, | 0.233, | 0.611, | 0.980, |
| | -0.1039, | -0.0508, | -0.0302, | -0.0100, | -0.0001, | 0.0098, | 0.0292, | 0.0483, | 0.0943 |
| | 0.0188, | 0.0188, | 0.0188, | 0.0188, | 0.0189, | 0.0189, | 0.0188, | 0.0186, | 0.0187 |
| MD CMG | 0.0225 | 0.0224 | 0.0224 | 0.0224 | 0.0224 | 0.0224 | 0.0223 | 0.0223 | 0.0225 |
| MR-ContMix | 1.000, -0.0995, | 0.889, -0.0497, | 0.506, -0.0297, | 0.124, -0.0097, | 0.071, 0.0003, | 0.120, 0.0103, | 0.490, 0.0302, | 0.874, 0.0502, | 1.000, 0.1000 |
| | 0.0159, | 0.0163, | 0.0164, | 0.0166, | 0.0003, | 0.0168, | 0.0302, | 0.0302, | 0.1000 |
| | 0.0139, NA | 0.0105, NA | 0.0104, NA | 0.0100, NA | 0.0107, NA | NA | 0.0170, NA | NA | NA |
| MR-Lasso | 1.000, | 0.853, | 0.448, | 0.091, | 0.060, | 0.090, | 0.427, | 0.836, | 1.000, |
| THE EMBOO | -0.0997, | -0.0497, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.0999 |
| | 0.0157, | 0.0161, | 0.0163, | 0.0165, | 0.0166, | 0.0167, | 0.0168, | 0.0170, | 0.0176 |
| | 0.0162 | 0.0165 | 0.0166 | 0.0167 | 0.0168 | 0.0169 | 0.0171 | 0.0172 | 0.0177 |
| MR-PRESSO | 0.639, | 0.488, | 0.338, | 0.224, | 0.216, | 0.260, | 0.410, | 0.565, | 0.738, |
| | -0.0397, | 0.0083, | 0.0265, | 0.0457, | 0.0556, | 0.0656, | 0.0855, | 0.1050, | 0.1534 |
| | 0.2136, | 0.2132, | 0.2127, | 0.2119, | 0.2117, | 0.2118, | 0.2107, | 0.2102, | 0.2091 |
| | 0.0829 | 0.0812 | 0.0795 | 0.0778 | 0.0776 | 0.0776 | 0.0764 | 0.0756 | 0.0741 |
| MR-IVW | 0.082, | 0.088, | 0.085, | 0.091, | 0.090, | 0.089, | 0.098, | 0.106, | 0.130, |
| | -0.0323, | 0.0180, | 0.0381, | 0.0582, | 0.0682, | 0.0783, | 0.0983, | 0.1184, | 0.1686 |
| | 0.2371, | 0.2371, | 0.2371, | 0.2371, | 0.2371, | 0.2371, | 0.2371, | 0.2371, | 0.2371 |
| 1 m mm o 1 | 0.2328 | 0.2328 | 0.2328 | 0.2328 | 0.2328 | 0.2328 | 0.2328 | 0.2328 | 0.2327 |
| MR-IVW-Oracle | 1.000, | 0.849, | 0.438, | 0.085, | 0.053, | 0.084, | 0.423, | 0.834, | 1.000, |
| | -0.0996, | -0.0498, | -0.0298, | -0.0098, | 0.0001, 0.0162, | 0.0101, | 0.0301, | 0.0500, | 0.0999 |
| | 0.0155, 0.0163 | 0.0158, 0.0166 | 0.0160, 0.0167 | 0.0161, 0.0169 | 0.0162, | 0.0163, 0.017 | 0.0165, 0.0172 | 0.0167, 0.0173 | 0.0172 0.0178 |
| MR-Egger | 0.0103 | 0.0100 | 0.0107 | 0.0169 | 0.0109 | 0.017 | 0.0172 | 0.0173 | 0.0178 |
| mix Lagor | 0.5207, | 0.5694, | 0.5889, | 0.6084, | 0.6181, | 0.6278, | 0.232, | 0.238, | 0.203, |
| | 1.1342, | 1.1340, | 1.1339, | 1.1339, | 1.1339, | 1.1338, | 1.1338, | 1.1337, | 1.1336 |
| | 0.8026 | 0.8027 | 0.8027 | 0.8028 | 0.8028 | 0.8028 | 0.8028 | 0.8029 | 0.8029 |
| IR-Weighted-Median | 0.997, | 0.678, | 0.326, | 0.091, | 0.061, | 0.075, | 0.248, | 0.548, | 0.973, |
| - | -0.1000, | -0.0514, | -0.0318, | -0.0123, | -0.0026, | 0.0072, | 0.0266, | 0.0460, | 0.0945 |
| | 0.0214, | 0.0219, | 0.0222, | 0.0226, | 0.0228, | 0.0229, | 0.0233, | 0.0237, | 0.0248 |
| | 0.021 | 0.0213 | 0.0215 | 0.0217 | 0.0218 | 0.0219 | 0.0221 | 0.0224 | 0.023 |
| MR-Weighted-Mode | 0.989, | 0.702, | 0.283, | 0.058, | 0.035, | 0.059, | 0.304, | 0.679, | 0.983, |
| | -0.0966, | -0.0473, | -0.0271, | -0.0073, | 0.0023, | 0.0120, | 0.0312, | 0.0511, | 0.0999 |
| | 0.0365, | 0.0364, | 0.0361, | 0.0359, | 0.0359, | 0.0359, | 0.0406, | 0.0405, | 0.0408 |
| MD D + DG: | 0.0346 | 0.035 | 0.0351 | 0.0354 | 0.0354 | 0.0355 | 0.0357 | 0.0359 | 0.0366 |
| MR-RAPS1 | 0.084, | 0.083, | 0.089, | 0.089, | 0.087, | 0.086, | 0.092, | 0.097, | 0.132, |
| | -0.0360, 0.2307, | 0.0141, 0.2307, | 0.0341, 0.2307, | 0.0541, 0.2307, | 0.0641, 0.2308, | 0.0741, 0.2308, | 0.0941, 0.2308, | 0.1141, | 0.1642 0.2308 |
| | 0.2307, 0.2271 | 0.2307, | 0.2307, | 0.2307, 0.2271 | 0.2308, | 0.2308, | 0.2308, | 0.2308, 0.2271 | 0.2308 |
| MR-RAPS2 | 0.142, | 0.108, | 0.2271 | 0.2271 | 0.086, | 0.092, | 0.090, | 0.2271 | 0.2272 |
| MIX IX II 92 | -0.0780, | -0.0258, | -0.0058, | 0.003, | 0.080, | 0.032, | 0.0613, | 0.0833, | 0.110, |
| | 0.2208, | 0.2251, | 0.2236, | 0.2229, | 0.0273, | 0.0381, | 0.2304, | 0.0833, | 0.1333 |
| | 0.2200, | 0.2251, | 0.2250, | 0.2177 | 0.2207, | 0.2199 | 0.2213 | 0.2233 | 0.2225 |
| MR-RAPS3 | 0.933, | 0.924, | 0.921, | 0.913, | 0.910, | 0.906, | 0.915, | 0.920, | 0.929, |
| | -2.3384, | 0.3391, | 1.6787, | 0.6886, | 1.1393, | 1.7040, | -0.0513, | 0.4360, | 0.3862 |
| | 70.7258, | 10.2598, | 27.3294, | 41.4050, | 22.0445, | 18.2553, | 9.0579, | 11.9486, | 7.3367. |
| | 191.3771 | 5.3413 | 32.6694 | 104.7941 | 29.3033 | 17.7291 | 3.8172 | 11.6837 | 3.6125 |
| MR-RAPS4 | 0.984, | 0.986, | 0.970, | 0.940, | 0.929, | 0.938, | 0.954, | 0.991, | 0.993, |
| | 0.2999, | 0.4626, | 0.7042, | 0.6981, | 0.4933, | 0.6048, | 0.3249, | 0.3620, | 0.3066 |
| | 9.8559, | 7.5855, | 9.4893, | 10.1499, | 7.5349, | 8.7619, | 2.5576, | 2.5130, | 2.0239 |
| | 0.517 | 0.1915 | 0.1727 | 0.1708 | 0.1882 | 0.3101 | 0.1281 | 0.1438 | 0.0938 |

Table S64: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE violated, q=0.4, and N=200000.

| ((| / / | | | | , I | | | | |
|---------------------|--------------------|--------------------|----------------|----------|----------------|-----------|----------|---------|---------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.997, | 0.836, | 0.418, | 0.069, | 0.024, | 0.068, | 0.410, | 0.815, | 0.997, |
| COLD MIN MIC | -0.0936, | -0.0438, | -0.0245, | -0.0073, | 0.0002, | 0.0078, | 0.0248, | 0.0440, | 0.0934, |
| | 0.0145, | 0.0145, | 0.0138, | 0.0121, | 0.0117, | 0.0121, | 0.0141, | 0.0152, | 0.0161, |
| | 0.0142 | 0.0143 | 0.0141 | 0.0138 | 0.0138 | 0.014 | 0.0145 | 0.015 | 0.0155 |
| cML-MA-AIC-Profile | 0.998, | 0.836, | 0.417, | 0.066, | 0.024, | 0.067, | 0.409, | 0.815, | 0.997, |
| cond our rate frome | -0.0937, | -0.0438, | -0.0245, | -0.0073, | 0.0002, | 0.0078, | 0.0248, | 0.0440, | 0.0936, |
| | 0.0145, | 0.0146, | 0.0138, | 0.0120, | 0.0117, | 0.0121, | 0.0141, | 0.0152, | 0.0162, |
| | 0.0142 | 0.0143 | 0.0142 | 0.0138 | 0.0138 | 0.014 | 0.0146 | 0.015 | 0.0155 |
| cML-AIC | 1.000, | 0.922, | 0.610, | 0.164, | 0.102, | 0.161, | 0.605, | 0.908, | 0.999, |
| CIVIL THE | -0.0970, | -0.0468, | -0.0271, | -0.0083, | 0.0004, | 0.0090, | 0.0275, | 0.0472, | 0.0968, |
| | 0.0151, | 0.0155, | 0.0154, | 0.0146, | 0.0146, | 0.0147, | 0.0273, | 0.0164, | 0.0308, |
| | 0.0131, | 0.0133, | 0.0134, | 0.0121 | 0.0122 | 0.0122 | 0.0133, | 0.0125 | 0.0172, |
| cML-AIC-Profile | 1.000, | 0.922, | 0.610, | 0.163, | 0.101, | 0.160, | 0.605, | 0.907, | 0.999, |
| CML-AIC-HOMC | -0.0970, | -0.0469, | -0.0271, | -0.0083, | 0.0004, | 0.0090, | 0.003, | 0.0472, | 0.0968, |
| | 0.0151, | 0.0155, | 0.0154, | 0.0146, | 0.0146, | 0.0090, | 0.0273, | 0.0164, | 0.0308, |
| | 0.0131, | 0.0133, | 0.0134, | 0.0121 | 0.0140, | 0.0122 | 0.0139, | 0.0104, | 0.0173, |
| cML-MA-BIC | 1.000, | 0.996, | 0.012 | 0.144, | 0.0122 | 0.140, | 0.0124 | 0.989, | 1.000, |
| CML-MA-BIC | -0.1000, | -0.0500, | -0.0300, | -0.0100, | | 0.140, | 0.731, | 0.989, | 0.0999, |
| | | | | | 0.0000, | | | | |
| | 0.0108, | 0.0110, | 0.0111, | 0.0111, | 0.0112, | 0.0112, | 0.0114, | 0.0115, | 0.0118, |
| 111 111 PIG P GI | 0.0108 | 0.011 | 0.0111 | 0.0112 | 0.0113 | 0.0113 | 0.0114 | 0.0116 | 0.0119 |
| ML-MA-BIC-Profile | 1.000, | 0.996, | 0.775, | 0.144, | 0.051, | 0.138, | 0.751, | 0.989, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0108, | 0.0110, | 0.0111, | 0.0111, | 0.0112, | 0.0112, | 0.0114, | 0.0115, | 0.0118, |
| | 0.0108 | 0.011 | 0.0111 | 0.0112 | 0.0113 | 0.0113 | 0.0114 | 0.0116 | 0.0119 |
| cML-BIC | 1.000, | 0.997, | 0.780, | 0.148, | 0.052, | 0.146, | 0.758, | 0.990, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999 |
| | 0.0108, | 0.0110, | 0.0110, | 0.0111, | 0.0112, | 0.0112, | 0.0113, | 0.0115, | 0.0118 |
| | 0.0107 | 0.0109 | 0.011 | 0.0111 | 0.0112 | 0.0112 | 0.0113 | 0.0115 | 0.0118 |
| cML-BIC-Profile | 1.000, | 0.997, | 0.779, | 0.147, | 0.052, | 0.145, | 0.758, | 0.990, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999 |
| | 0.0108, | 0.0110, | 0.0110, | 0.0111, | 0.0112, | 0.0112, | 0.0113, | 0.0115, | 0.0118 |
| | 0.0108 | 0.0109 | 0.011 | 0.0111 | 0.0112 | 0.0112 | 0.0113 | 0.0115 | 0.0118 |
| MR-Mix | 0.999, | 0.914, | 0.476, | 0.064, | 0.016, | 0.057, | 0.455, | 0.878, | 0.996, |
| | -0.1041, | -0.0509, | -0.0303, | -0.0102, | -0.0002, | 0.0098, | 0.0292, | 0.0483, | 0.0944 |
| | 0.0132, | 0.0131, | 0.0129, | 0.0129, | 0.0128, | 0.0128, | 0.0129, | 0.0130, | 0.0130 |
| | 0.0164 | 0.0163 | 0.0164 | 0.0163 | 0.0163 | 0.0163 | 0.0163 | 0.0163 | 0.0167 |
| MR-ContMix | 1.000, | 0.995, | 0.793, | 0.164, | 0.072, | 0.168, | 0.770, | 0.987, | 1.000, |
| | -0.0999, | -0.0500, | -0.0300, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0498, | 0.0997 |
| | 0.0110, | 0.0113, | 0.0114, | 0.0114, | 0.0115, | 0.0116, | 0.0117, | 0.0118, | 0.0121 |
| | NA NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.986, | 0.733, | 0.130, | 0.047, | 0.126, | 0.704, | 0.978, | 0.999, |
| | -0.0998, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0099, | 0.0299, | 0.0499, | 0.0997 |
| | 0.0112, | 0.0114, | 0.0115, | 0.0115, | 0.0115, | 0.0116, | 0.0116, | 0.0118, | 0.0121 |
| | 0.0115 | 0.0117 | 0.0118 | 0.0119 | 0.0119 | 0.012 | 0.0121 | 0.0122 | 0.0126 |
| MR-PRESSO | 0.537, | 0.459, | 0.354, | 0.219, | 0.200, | 0.233, | 0.402, | 0.498, | 0.608, |
| WIK I KESSO | -0.0499, | -0.0003, | 0.0192, | 0.0394, | 0.0490, | 0.0589, | 0.0786, | 0.0984, | 0.1473, |
| | 0.2351, | 0.2349, | 0.2348, | 0.2347, | 0.2347, | 0.2346, | 0.2341, | 0.2337, | 0.2329 |
| | 0.1138 | 0.113 | 0.1122 | 0.112 | 0.1117 | 0.1115 | 0.1101 | 0.1089 | 0.1056 |
| MR-IVW | 0.091, | 0.086, | 0.087, | 0.085, | 0.082, | 0.079, | 0.090, | 0.095, | 0.116, |
| IVIIC-I V VV | -0.0465, | 0.0038, | 0.0239, | 0.0440, | 0.0541, | 0.0642, | 0.0843, | 0.1043, | 0.110, |
| | 0.2446, | 0.2445, | 0.0239, | 0.2444, | 0.0341, | 0.2444, | 0.2444, | 0.1043, | 0.1340 |
| | 0.2440, | 0.234 | 0.234 | 0.234 | 0.234 | 0.2339 | 0.2339 | 0.2339 | 0.2339 |
| MR-IVW-Oracle | | 0.234 | 0.732, | 0.234 | 0.234 | 0.2339 | 0.2339 | 0.2339 | 1.000, |
| MR-IV W-Oracie | 1.000, | | | | | | | | |
| | -0.0999, | -0.0499, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0499, | 0.0998 |
| | 0.0107, | 0.0109, | 0.0110, | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0114, | 0.0117 |
| 1 (D. F. | 0.0115 | 0.0117 | 0.0118 | 0.0119 | 0.012 | 0.012 | 0.0122 | 0.0123 | 0.0126 |
| MR-Egger | 0.254, | 0.258, | 0.258, | 0.265, | 0.267, | 0.272, | 0.272, | 0.278, | 0.289, |
| | 0.5503, | 0.5997, | 0.6194, | 0.6391, | 0.6490, | 0.6588, | 0.6785, | 0.6982, | 0.7474 |
| | 1.1351, | 1.1350, | 1.1350, | 1.1350, | 1.1350, | 1.1350, | 1.1350, | 1.1350, | 1.1350 |
| en with the second | 0.7866 | 0.7865 | 0.7865 | 0.7865 | 0.7865 | 0.7865 | 0.7865 | 0.7865 | 0.7865 |
| MR-Weighted-Median | 1.000, | 0.927, | 0.543, | 0.133, | 0.062, | 0.079, | 0.434, | 0.832, | 0.996, |
| | -0.1005, | -0.0514, | -0.0318, | -0.0121, | -0.0023, | 0.0074, | 0.0270, | 0.0466, | 0.0954 |
| | 0.0153, | 0.0157, | 0.0159, | 0.0163, | 0.0165, | 0.0167, | 0.0171, | 0.0177, | 0.0191 |
| | 0.0148 | 0.0151 | 0.0152 | 0.0153 | 0.0154 | 0.0155 | 0.0156 | 0.0158 | 0.0163 |
| MR-Weighted-Mode | 0.990, | 0.919, | 0.530, | 0.094, | 0.037, | 0.085, | 0.515, | 0.901, | 0.992, |
| | -0.0992, | -0.0493, | -0.0296, | -0.0096, | 0.0004, | 0.0102, | 0.0301, | 0.0497, | 0.0996 |
| | 0.0158, | 0.0157, | 0.0159, | 0.0160, | 0.0160, | 0.0159, | 0.0159, | 0.0160, | 0.0162 |
| | 0.0157 | 0.0159 | 0.016 | 0.0161 | 0.0161 | 0.0162 | 0.0163 | 0.0165 | 0.0168 |
| MR-RAPS1 | 0.094, | 0.092, | 0.086, | 0.084, | 0.077, | 0.084, | 0.092, | 0.100, | 0.125, |
| | -0.0472, | 0.0028, | 0.0228, | 0.0428, | 0.0528, | 0.0628, | 0.0828, | 0.1028, | 0.1528 |
| | 0.2392, | 0.2391, | 0.2391, | 0.2391, | 0.2391, | 0.2391, | 0.2391, | 0.2391, | 0.2390 |
| | 0.228 | 0.228 | 0.228 | 0.228 | 0.228 | 0.228 | 0.228 | 0.228 | 0.228 |
| MR-RAPS2 | 0.284, | 0.177, | 0.136, | 0.095, | 0.082, | 0.078, | 0.065, | 0.063, | 0.103, |
| | -0.1275, | -0.0790, | -0.0575, | -0.0431, | -0.0327, | -0.0206, | -0.0012, | 0.0160, | 0.0688 |
| | 0.1607, | 0.1635, | 0.1710, | 0.1589, | 0.1597, | 0.1602, | 0.1626, | 0.1605, | 0.1729 |
| | 0.136 | 0.137 | 0.1386 | 0.1374 | 0.1378 | 0.1373 | 0.137 | 0.1354 | 0.1418 |
| MR-RAPS3 | 0.932, | 0.930, | 0.926, | 0.944, | 0.951, | 0.955, | 0.954, | 0.950, | 0.947, |
| | -4.5043, | -2.8573, | 0.2790, | 0.2108, | -0.6234, | -11.2173, | 1.1095, | 0.2982, | 0.3811 |
| | 133.2929, | 108.8086, | 20.2050, | 44.2770, | 19.5964, | 378.1344, | 15.8975, | 9.1370, | 11.320 |
| | 459.1634 | 278.2873 | 12.2365 | 83.1364 | 11.7936 | 6799.6057 | 8.7751 | 4.4133 | 4.5942 |
| MD DADC4 | 0.990, | 0.993, | 0.986, | 0.960, | 0.946, | 0.955, | 0.993, | 0.999, | 0.998, |
| | | | 0.986, 0.1421, | 0.960, | 0.946, 0.1670, | 0.955, | 0.993, | 0.999, | 0.998, |
| MR-RAPS4 | 0.0260 | | | | | | | | |
| MR-RAPS4 | 0.0360, 2.5810, | 0.0936, 2.5583, | 2.6249, | 2.6864, | 2.6504, | 2.6050, | 2.5032, | 2.5032, | 2.3370 |

Table S65: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m = 20, the InSIDE violated, q = 0.6, and N = 50000.

| | | | | | - | | | | |
|--|---|---|--|---|--|---|---|---|--|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.621, | 0.170, | 0.060, | 0.023, | 0.016, | 0.010, | 0.049, | 0.138, | 0.557, |
| CWIL-WIA-AIC | -0.0822, | -0.0372, | -0.0215, | -0.0072, | -0.0005, | 0.010, | 0.049, | 0.136, | 0.0799, |
| | 0.0340, | 0.0302, | 0.0282, | 0.0265, | 0.0259, | 0.0263, | 0.0279, | 0.0304, | 0.0359, |
| | 0.0363 | 0.0357 | 0.0355 | 0.0354 | 0.0354 | 0.0356 | 0.0364 | 0.0373 | 0.0396 |
| cML-MA-AIC-Profile | 0.618, | 0.170, | 0.059, | 0.022, | 0.016, | 0.010, | 0.047, | 0.136, | 0.554, |
| | -0.0823, | -0.0372, | -0.0215, | -0.0072, | -0.0005, | 0.0064, | 0.0203, | 0.0360, | 0.0801, |
| | 0.0342, | 0.0302, | 0.0282, | 0.0265, | 0.0259, | 0.0263, | 0.0279, | 0.0304, | 0.0360, |
| cML-AIC | 0.0365 0.811, | 0.0359 | 0.0357 0.178, | 0.0356 0.080, | 0.0356 0.073, | 0.0358 0.076, | 0.0367 0.157, | 0.0375 0.331, | 0.0399 0.750, |
| CML-AIC | -0.0907, | -0.0429, | -0.0258, | -0.0084, | -0.0008, | 0.070, | 0.137, | 0.0410, | 0.730, |
| | 0.0375, | 0.0358, | 0.0346, | 0.0343, | 0.0337, | 0.0339, | 0.0360, | 0.0379, | 0.0412, |
| | 0.0293 | 0.03 | 0.0302 | 0.0305 | 0.0305 | 0.0307 | 0.0311 | 0.0315 | 0.0323 |
| cML-AIC-Profile | 0.806, | 0.356, | 0.173, | 0.080, | 0.071, | 0.075, | 0.156, | 0.326, | 0.745, |
| | -0.0909, | -0.0429, | -0.0258, | -0.0084, | -0.0007, | 0.0078, | 0.0237, | 0.0410, | 0.0876, |
| | 0.0377, | 0.0359, | 0.0346, | 0.0343, | 0.0338, | 0.0339, | 0.0360, | 0.0379, | 0.0413, |
| cML-MA-BIC | 0.0295 0.957, | 0.0302 0.435, | 0.0304 0.194, | 0.0307 0.063, | 0.0307 0.037, | 0.0309 0.053, | 0.0313 0.165, | 0.0317 0.401, | 0.0325 0.917, |
| CML-MA-DIC | -0.1000, | -0.0500, | -0.0301, | -0.0102, | -0.0002, | 0.003, | 0.103, | 0.401, | 0.917, |
| | 0.0265, | 0.0270, | 0.0271, | 0.0273, | 0.0274, | 0.0275, | 0.0279, | 0.0282, | 0.0291, |
| | 0.0274 | 0.0279 | 0.0281 | 0.0284 | 0.0285 | 0.0286 | 0.0289 | 0.0292 | 0.03 |
| cML-MA-BIC-Profile | 0.955, | 0.433, | 0.193, | 0.063, | 0.036, | 0.052, | 0.164, | 0.399, | 0.916, |
| | -0.1000, | -0.0500, | -0.0301, | -0.0102, | -0.0002, | 0.0097, | 0.0296, | 0.0496, | 0.0996, |
| | 0.0265, | 0.0270, | 0.0271, | 0.0273, | 0.0274, | 0.0275, | 0.0279, | 0.0282, | 0.0291, |
| M. DIC | 0.0276 | 0.028 | 0.0283 | 0.0285 | 0.0286 | 0.0288 | 0.029 | 0.0293 | 0.0301 |
| cML-BIC | 0.957, -0.1002, | 0.446, -0.0502, | 0.200, -0.0302, | 0.065, -0.0102, | 0.042, -0.0002, | 0.060, 0.0098, | 0.180, 0.0298, | 0.423, 0.0498, | 0.922, 0.0998, |
| | 0.0266, | 0.0302, | 0.0274, | 0.0277, | 0.0277, | 0.0098, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0200, | 0.0275 | 0.0277 | 0.028 | 0.0281 | 0.0282 | 0.0285 | 0.0288 | 0.0292, |
| cML-BIC-Profile | 0.953, | 0.442, | 0.199, | 0.065, | 0.039, | 0.059, | 0.178, | 0.419, | 0.921, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0266, | 0.0272, | 0.0274, | 0.0277, | 0.0277, | 0.0279, | 0.0281, | 0.0284, | 0.0292, |
| 100.10 | 0.0272 | 0.0276 | 0.0278 | 0.0281 | 0.0282 | 0.0283 | 0.0286 | 0.0289 | 0.0297 |
| MR-Mix | 0.869, | 0.335, | 0.140, | 0.038, | 0.023, | 0.040, | 0.110, | 0.292, | 0.816, |
| | -0.1021, 0.0287, | -0.0503, 0.0286, | -0.0301, 0.0285, | -0.0102, 0.0284, | -0.0004, 0.0284, | 0.0094, 0.0285, | 0.0286, 0.0284, | 0.0472, 0.0286, | 0.0925, 0.0286, |
| | 0.0339 | 0.0338 | 0.0283, | 0.0337 | 0.0335 | 0.0335 | 0.0334 | 0.0334 | 0.0236 |
| MR-ContMix | 0.957, | 0.477, | 0.229, | 0.079, | 0.061, | 0.077, | 0.209, | 0.440, | 0.920, |
| | -0.0996, | -0.0499, | -0.0300, | -0.0102, | -0.0002, | 0.0097, | 0.0296, | 0.0495, | 0.0994, |
| | 0.0275, | 0.0279, | 0.0281, | 0.0283, | 0.0284, | 0.0286, | 0.0288, | 0.0291, | 0.0302, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.908, | 0.417, | 0.218, | 0.099, | 0.081, | 0.086, | 0.176, | 0.357, | 0.854, |
| | -0.0774, 0.2046, | -0.0273, 0.2045, | -0.0074, 0.2045, | 0.0127, 0.2046, | 0.0226, 0.2046, | 0.0327, 0.2049, | 0.0521, 0.2036, | 0.0722, 0.2052, | 0.1223, 0.2062, |
| | 0.035 | 0.0356 | 0.0359 | 0.0361 | 0.0363 | 0.0364 | 0.037 | 0.0375 | 0.0382 |
| MR-PRESSO | 0.545, | 0.302, | 0.209, | 0.173, | 0.170, | 0.185, | 0.259, | 0.349, | 0.627, |
| | -0.0251, | 0.0216, | 0.0397, | 0.0577, | 0.0659, | 0.0743, | 0.0936, | 0.1131, | 0.1596, |
| | 0.2518, | 0.2505, | 0.2501, | 0.2490, | 0.2482, | 0.2473, | 0.2469, | 0.2465, | 0.2440, |
| | 0.0918 | 0.0896 | 0.0888 | 0.0871 | 0.086 | 0.0848 | 0.0842 | 0.0834 | 0.0816 |
| MR-IVW | 0.072, | 0.074, | 0.075, | 0.080, | 0.083, | 0.082, | 0.093, | 0.098, | 0.117, |
| | -0.0121, 0.2894, | 0.0382, 0.2895, | 0.0583, 0.2895, | 0.0784, 0.2895, | 0.0885, 0.2895, | 0.0985, 0.2895, | 0.1186, 0.2895, | 0.1387, 0.2895, | 0.1889, 0.2896, |
| | 0.2894, | 0.2893, | 0.2893, | 0.2893, | 0.2893, | 0.2893, | 0.2893, | 0.2893, | 0.2890, |
| MR-IVW-Oracle | 0.922, | 0.386, | 0.171, | 0.048, | 0.033, | 0.043, | 0.134, | 0.346, | 0.881, |
| | -0.0996, | -0.0499, | -0.0300, | -0.0101, | -0.0001, | 0.0098, | 0.0297, | 0.0496, | 0.0994, |
| | 0.0261, | 0.0265, | 0.0268, | 0.0270, | 0.0271, | 0.0273, | 0.0276, | 0.0279, | 0.0287, |
| | 0.0296 | 0.0301 | 0.0304 | 0.0306 | 0.0308 | 0.0309 | 0.0312 | 0.0315 | 0.0323 |
| MR-Egger | | 0.187, | 0.192, | 0.194, | | | | | |
| | 0.185, | | | | 0.196, | 0.199, | 0.200, | 0.203, | 0.219, |
| | 0.5815, | 0.6295, | 0.6487, | 0.6678, | 0.6774, | 0.6870, | 0.7062, | 0.7253, | 0.7731, |
| | 0.5815, 1.0311, | 0.6295, 1.0311, | 0.6487, 1.0311, | 0.6678, 1.0311, | 0.6774, 1.0311, | 0.6870, 1.0311, | 0.7062, 1.0311, | 0.7253, 1.0311, | 0.7731, 1.0311, |
| MR-Weighted-Median | 0.5815, | 0.6295, | 0.6487, | 0.6678, | 0.6774, | 0.6870, | 0.7062, | 0.7253, | 0.7731, |
| MR-Weighted-Median | 0.5815, 1.0311, 0.8485 | 0.6295, 1.0311, 0.8486 | 0.6487, 1.0311, 0.8486 | 0.6678, 1.0311, 0.8487 | 0.6774, 1.0311, 0.8487 | 0.6870, 1.0311, 0.8487 | 0.7062, 1.0311, 0.8488 | 0.7253, 1.0311, 0.8488 | 0.7731, 1.0311, 0.849 |
| MR-Weighted-Median | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, |
| | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 |
| MR-Weighted-Median MR-Weighted-Mode | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 |
| | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, |
| | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, |
| MR-Weighted-Mode | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 |
| | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, |
| MR-Weighted-Mode | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.084, -0.0149, 0.2856, | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.0352, 0.2857, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2857, | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.0752, 0.2857, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.084, 0.0852, 0.2857, | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2857, | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, |
| MR-Weighted-Mode MR-RAPS1 | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.084, -0.0149, 0.2856, 0.2745 | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.0352, 0.2857, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2857, 0.2746 | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.0752, 0.2857, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.084, 0.0852, 0.2857, 0.2746 | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2857, 0.2746 | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, 0.2746 | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, 0.2747 |
| MR-Weighted-Mode | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.2856, 0.2745 | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.0352, 0.2746 | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2746 | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.0752, 0.2746 0.080, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.0852, 0.2552, 0.2746 | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2746 0.086, | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, 0.2746 | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, 0.2746 | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, 0.2747 |
| MR-Weighted-Mode MR-RAPS1 | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.084, -0.0149, 0.2856, 0.2745 0.096, -0.0232, | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.0352, 0.2857, 0.2746 0.086, 0.0260, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2857, 0.2746 0.080, | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.0752, 0.2857, 0.2746 0.080, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.084, 0.0852, 0.2746 0.085, 0.0778, | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2577, 0.2746 | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, 0.2746 | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, 0.2746 | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, 0.2747 0.110, |
| MR-Weighted-Mode MR-RAPS1 | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.084, -0.0149, 0.2856, 0.2745 0.096, -0.0232, 0.3100, | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.2857, 0.2746 0.086, 0.0260, 0.3104, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2857, 0.2746 0.080, 0.0469, 0.3095, | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.0752, 0.2857, 0.2746 0.080, 0.0658, 0.3109, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.084, 0.0852, 0.2857, 0.2746 0.085, 0.0778, 0.3104, | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2857, 0.2746 0.086, 0.0875, 0.3115, | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, 0.2746 0.090, 0.1071, 0.3123, | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, 0.2746 0.094, 0.1234, 0.3102, | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, 0.2747 0.110, 0.1778, |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.2836, 0.2745 0.096, -0.0232, 0.3100, 0.2948 | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.0352, 0.2746 0.086, 0.0260, 0.3104, 0.2943 | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2746 0.080, 0.0469, 0.3095, 0.2949 | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.0752, 0.2746 0.080, 0.0658, 0.3109, 0.2946 | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.0852, 0.2746 0.085, 0.0778, 0.3104, 0.2947 | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2746 0.086, 0.0875, 0.3115, 0.2947 | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, 0.2746 0.090, 0.1071, 0.3123, 0.2949 | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, 0.2746 0.094, 0.1234, 0.3102, 0.2936 | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, 0.2747 0.110, 0.1778, 0.3106, 0.2951 |
| MR-Weighted-Mode MR-RAPS1 | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.084, -0.0149, 0.2856, 0.2745 0.096, -0.0232, 0.3100, 0.2948 | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.0352, 0.2857, 0.2746 0.0960, 0.3104, 0.2943 | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2857, 0.2746 0.0469, 0.3095, 0.2949 | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.2746 0.085, 0.2857, 0.2746 0.080, 0.0658, 0.3109, 0.2946 | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.084, 0.0852, 0.2857, 0.2746 0.0778, 0.3104, 0.2947 | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2857, 0.2746 0.0875, 0.3115, 0.2947 | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, 0.2746 0.090, 0.1071, 0.3123, | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, 0.2746 0.094, 0.1234, 0.3102, 0.2936 0.898, | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, 0.2747 0.110, 0.1778, 0.3106, |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.2836, 0.2745 0.096, -0.0232, 0.3100, 0.2948 | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.0352, 0.2746 0.086, 0.0260, 0.3104, 0.2943 | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2746 0.080, 0.0469, 0.3095, 0.2949 | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.0752, 0.2746 0.080, 0.0658, 0.3109, 0.2946 | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.0852, 0.2746 0.085, 0.0778, 0.3104, 0.2947 | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2746 0.086, 0.0875, 0.3115, 0.2947 | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, 0.2746 0.090, 0.1071, 0.3123, 0.2949 | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, 0.2746 0.094, 0.1234, 0.3102, 0.2936 | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, 0.2747 0.110, 0.1778, 0.3106, 0.2951 |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.084, -0.0149, 0.2856, 0.2745 0.096, -0.0232, 0.3100, 0.2948 0.895, -0.3470, | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.2857, 0.2746 0.086, 0.0260, 0.3104, 0.2943 0.887, 0.9905, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2857, 0.2746 0.080, 0.3095, 0.2949 0.887, -3.5865, | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.0752, 0.2857, 0.2746 0.080, 0.0658, 0.3109, 0.2946 0.896, -0.4220, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.084, 0.0852, 0.2857, 0.2746 0.085, 0.0778, 0.3104, 0.2947 0.889, 10.5151, | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2857, 0.2746 0.088, 0.0875, 0.3115, 0.2947 0.899, 0.5375, | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, 0.2746 0.090, 0.1071, 0.3123, 0.2949 0.894, -0.1168, | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, 0.2746 0.094, 0.1234, 0.3102, 0.2936 0.898, -6.1403, | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, 0.2747 0.110, 0.1778, 0.3106, 0.2951 0.897, -2.8103, |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.084, -0.0149, 0.2856, 0.2745 0.096, -0.0232, 0.3100, 0.2948 0.895, -0.3470, 49.8288, 77.0998 | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.0352, 0.2857, 0.2746 0.086, 0.0260, 0.3104, 0.2943 0.887, 0.9905, 66.5783, 112.6095 0.989, | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2857, 0.2746 0.080, 0.3095, 0.2949 0.887, -3.5865, 163.6478, 892.9504 | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.0752, 0.2857, 0.2746 0.080, 0.3109, 0.2946 0.896, -0.4220, 35.3251, 53.739 0.976, | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.084, 0.0852, 0.2746 0.085, 0.3104, 0.2947 0.889, 10.5151, 220.5876, 1339.5784 0.971, | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2857, 0.2746 0.0875, 0.3115, 0.2947 0.899, 0.5375, 97.1229, 306.5017 0.978, | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, 0.2746 0.090, 0.1071, 0.3123, 0.2949 0.894, -0.1168, 67.8534, 199.5718 | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, 0.2746 0.094, 0.1234, 0.3102, 0.2936 0.898, -6.1403, 197-4045, 2342,1774 | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, 0.2747 0.110, 0.1778, 0.3106, 0.2951 0.897, -2.8103, 115.7327, 743.884 0.986, |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 MR-RAPS3 | 0.5815, 1.0311, 0.8485 0.791, -0.1045, 0.0564, 0.0375 0.784, -0.1529, 0.1378, 0.0419 0.084, -0.0149, 0.2856, 0.2745 0.096, -0.0232, 0.3100, 0.2948 0.895, -0.3470, 49.8288, 77.0998 | 0.6295, 1.0311, 0.8486 0.385, -0.0593, 0.0572, 0.0383 0.718, -0.1164, 0.1377, 0.0421 0.081, 0.0352, 0.2857, 0.2746 0.0260, 0.3104, 0.2943 0.887, 0.9905, 66.5783, 112.6095 | 0.6487, 1.0311, 0.8486 0.219, -0.0415, 0.0582, 0.0386 0.690, -0.1020, 0.1391, 0.0422 0.081, 0.0552, 0.2857, 0.2746 0.080, 0.3095, 0.2949 0.887, -3.5865, 163.6478, 892.9504 | 0.6678, 1.0311, 0.8487 0.139, -0.0237, 0.0600, 0.039 0.678, -0.0869, 0.1402, 0.0423 0.085, 0.0752, 0.2857, 0.2746 0.080, 0.0658, 0.3109, 0.2946 0.896, -0.4220, 35.3251, 53.739 | 0.6774, 1.0311, 0.8487 0.117, -0.0148, 0.0608, 0.0392 0.676, -0.0799, 0.1411, 0.0423 0.084, 0.0852, 0.2857, 0.2746 0.085, 0.0778, 0.3104, 0.2947 0.889, 10.5151, 220.5876, 1339.5784 | 0.6870, 1.0311, 0.8487 0.098, -0.0059, 0.0617, 0.0394 0.665, -0.0724, 0.1419, 0.0424 0.086, 0.0952, 0.2857, 0.2746 0.086, 0.0875, 0.3115, 0.2947 0.899, 0.5375, 97.1229, 306.5017 | 0.7062, 1.0311, 0.8488 0.133, 0.0117, 0.0642, 0.0399 0.657, -0.0583, 0.1440, 0.0426 0.092, 0.1153, 0.2857, 0.2746 0.090, 0.1071, 0.3123, 0.2949 0.894, -0.1168, 67.8534, 199.5718 | 0.7253, 1.0311, 0.8488 0.203, 0.0292, 0.0668, 0.0404 0.645, -0.0441, 0.1448, 0.0429 0.095, 0.1353, 0.2858, 0.2746 0.094, 0.1234, 0.3102, 0.2936 0.898, -6.1403, 197.4045, 2342.1774 | 0.7731, 1.0311, 0.849 0.530, 0.0727, 0.0748, 0.0417 0.625, -0.0085, 0.1488, 0.0436 0.113, 0.1853, 0.2858, 0.2747 0.110, 0.1778, 0.3106, 0.2951 0.897, -28103, 115.7327, 743.884 |

Table S66: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m = 20, the InSIDE violated, q = 0.6, and N = 100000.

| | . , | | | | | | | | |
|--------------------|----------------------|----------------------|-----------------------|---------------------|---------------------|---------------------|--------------------|---------------------|---------------------|
| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.885, | 0.351, | 0.118, | 0.033, | 0.020, | 0.025, | 0.114, | 0.327, | 0.865, |
| CIVIL-IVIA-AIC | -0.0874, | -0.0391, | -0.0217, | -0.0066, | 0.020, | 0.023, | 0.114, | 0.0396, | 0.0876, |
| | 0.0250, | 0.0231, | 0.0217, | 0.0192, | 0.0188, | 0.0191, | 0.0212, | 0.0237, | 0.0263, |
| | 0.0258 | 0.0254 | 0.025 | 0.0248 | 0.0248 | 0.025 | 0.0257 | 0.0266 | 0.028 |
| cML-MA-AIC-Profile | 0.884, | 0.352, | 0.116, | 0.032, | 0.020, | 0.024, | 0.113, | 0.327, | 0.863, |
| | -0.0875, | -0.0391, | -0.0217, | -0.0066, | 0.0006, | 0.0075, | 0.0227, | 0.0396, | 0.0877, |
| | 0.0251, | 0.0232, | 0.0212, | 0.0191, | 0.0188, | 0.0191, | 0.0212, | 0.0237, | 0.0264, |
| cML-AIC | 0.0258 0.949, | 0.0255 0.564, | 0.0251 0.275, | 0.0249 0.097, | 0.0249 0.080, | 0.0251 0.093, | 0.0258 0.280, | 0.0267 0.562, | 0.0281 0.938, |
| CML-AIC | -0.0932, | -0.0437, | -0.0255, | -0.0076, | 0.000, | 0.0093, | 0.260, | 0.362, | 0.938, |
| | 0.0273, | 0.0263, | 0.0251, | 0.0242, | 0.0241, | 0.0239, | 0.0256, | 0.0271, | 0.0289, |
| | 0.0207 | 0.0211 | 0.0212 | 0.0214 | 0.0215 | 0.0215 | 0.0217 | 0.022 | 0.0226 |
| cML-AIC-Profile | 0.949, | 0.562, | 0.273, | 0.095, | 0.078, | 0.091, | 0.279, | 0.557, | 0.938, |
| | -0.0934, | -0.0437, | -0.0255, | -0.0076, | 0.0009, | 0.0093, | 0.0262, | 0.0450, | 0.0941, |
| | 0.0273, | 0.0263, | 0.0251, | 0.0241, | 0.0241, | 0.0239, | 0.0256, | 0.0271, | 0.0290, |
| cML-MA-BIC | 0.0208 | 0.0211 0.700, | 0.0213 | 0.0215 0.078, | 0.0215 | 0.0216 | 0.0218 | 0.022 | 0.0227 |
| CIVIL-IVIA-DIC | 0.999, -0.0996, | -0.0495, | 0.330, -0.0295, | -0.0095, | 0.051, 0.0004, | 0.086, 0.0104, | 0.332, | 0.695, 0.0504, | 0.997, 0.1005, |
| | 0.0195, | 0.0198, | 0.0199, | 0.0201, | 0.0201, | 0.0202, | 0.0204, | 0.0207, | 0.0212, |
| | 0.0193 | 0.0196 | 0.0198 | 0.0199 | 0.02 | 0.0201 | 0.0203 | 0.0205 | 0.0211 |
| cML-MA-BIC-Profile | 0.999, | 0.700, | 0.329, | 0.075, | 0.050, | 0.086, | 0.331, | 0.692, | 0.997, |
| | -0.0996, | -0.0495, | -0.0295, | -0.0095, | 0.0004, | 0.0104, | 0.0304, | 0.0504, | 0.1005, |
| | 0.0195, | 0.0198, | 0.0199, | 0.0201, | 0.0201, | 0.0202, | 0.0204, | 0.0207, | 0.0212, |
| 10.010 | 0.0193 | 0.0197 | 0.0198 | 0.02 | 0.0201 | 0.0202 | 0.0203 | 0.0206 | 0.0211 |
| cML-BIC | 0.999, | 0.711, -0.0496, | 0.338, | 0.080, | 0.055, | 0.091, 0.0105, | 0.342, | 0.703, | 0.997, 0.1005, |
| | -0.0996, 0.0195, | -0.0496, 0.0198, | -0.0296, 0.0199, | -0.0096, 0.0201, | 0.0004, 0.0202, | 0.0105, 0.0203, | 0.0305, 0.0205, | 0.0505, 0.0207, | 0.1005, 0.0212, |
| | 0.0193, | 0.0198, | 0.0199, | 0.0201, | 0.0202, | 0.0203, | 0.0203, | 0.0207, | 0.0212, |
| cML-BIC-Profile | 0.999, | 0.710, | 0.335, | 0.080, | 0.055, | 0.091, | 0.341, | 0.700, | 0.997, |
| | -0.0996, | -0.0496, | -0.0296, | -0.0096, | 0.0004, | 0.0105, | 0.0305, | 0.0505, | 0.1005, |
| | 0.0195, | 0.0198, | 0.0199, | 0.0201, | 0.0202, | 0.0203, | 0.0205, | 0.0207, | 0.0212, |
| | 0.0191 | 0.0194 | 0.0196 | 0.0198 | 0.0198 | 0.0199 | 0.0201 | 0.0203 | 0.0209 |
| MR-Mix | 0.982, | 0.564, | 0.232, | 0.042, | 0.022, | 0.048, | 0.211, | 0.544, | 0.955, |
| | -0.1016, 0.0212, | -0.0495, 0.0212, | -0.0292, 0.0210, | -0.0093, 0.0209, | 0.0004, 0.0209, | 0.0100, 0.0210, | 0.0292, 0.0210, | 0.0482, 0.0211, | 0.0933, 0.0213, |
| | 0.0212, | 0.0212, | 0.0210, | 0.0209, | 0.0209, | 0.0210, | 0.0210, | 0.0211, | 0.0213, |
| MR-ContMix | 0.998, | 0.731, | 0.367, | 0.098, | 0.072, | 0.106, | 0.373, | 0.716, | 0.997, |
| mit commi | -0.0994, | -0.0495, | -0.0296, | -0.0096, | 0.0004, | 0.0104, | 0.0304, | 0.0504, | 0.1003, |
| | 0.0198, | 0.0201, | 0.0202, | 0.0205, | 0.0205, | 0.0206, | 0.0207, | 0.0210, | 0.0216, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.984, | 0.653, | 0.302, | 0.095, | 0.079, | 0.101, | 0.315, | 0.646, | 0.976, |
| | -0.0953, | -0.0455, | -0.0252, | -0.0042, | 0.0058, | 0.0158, | 0.0357, | 0.0558, | 0.1059, |
| | 0.1476, 0.0237 | 0.1465, 0.0243 | 0.1469, 0.0245 | 0.1502, 0.025 | 0.1506, 0.0251 | 0.1506, 0.0252 | 0.1505, 0.0251 | 0.1503, 0.0254 | 0.1509, 0.026 |
| MR-PRESSO | 0.0237 | 0.0243 | 0.0243 | 0.023 | 0.0231 | 0.0232 | 0.0231 | 0.0234 | 0.572, |
| MIK I KESSO | -0.0309, | 0.0183, | 0.0378, | 0.0579, | 0.0680, | 0.0779, | 0.0971, | 0.1166, | 0.1649, |
| | 0.2713, | 0.2705, | 0.2702, | 0.2704, | 0.2702, | 0.2702, | 0.2697, | 0.2692, | 0.2676, |
| | 0.1347 | 0.1324 | 0.1312 | 0.1312 | 0.1311 | 0.1309 | 0.1293 | 0.1277 | 0.1228 |
| MR-IVW | 0.062, | 0.072, | 0.079, | 0.080, | 0.082, | 0.087, | 0.091, | 0.096, | 0.120, |
| | -0.0259, | 0.0246, | 0.0447, | 0.0649, | 0.0750, | 0.0850, | 0.1052, | 0.1253, | 0.1756, |
| | 0.2859, 0.2806 | 0.2858, 0.2806 | 0.2858, 0.2806 | 0.2858, 0.2806 | 0.2858, 0.2806 | 0.2858, 0.2806 | 0.2858, 0.2806 | 0.2858, 0.2806 | 0.2857, 0.2806 |
| MR-IVW-Oracle | 0.2800 | 0.2800 | 0.286, | 0.2800 | 0.2806 | 0.2806 | 0.284, | 0.2800 | 0.2806 |
| WIK-IV W-Olacie | -0.0995, | -0.0495, | -0.0296, | -0.0096, | 0.040, | 0.0104, | 0.0304, | 0.0503, | 0.1002, |
| | 0.0193, | 0.0196, | 0.0198, | 0.0199, | 0.0200, | 0.0201, | 0.0203, | 0.0204, | 0.0210, |
| | 0.0207 | 0.021 | 0.0212 | 0.0214 | 0.0215 | 0.0216 | 0.0218 | 0.022 | 0.0226 |
| MR-Egger | 0.178, | 0.192, | 0.199, | 0.201, | 0.204, | 0.204, | 0.206, | 0.210, | 0.224, |
| | 0.5209, | 0.5700, | 0.5896, | 0.6092, | 0.6190, | 0.6288, | 0.6484, | 0.6679, | 0.7168, |
| | 1.0486, | 1.0486, | 1.0487, | 1.0487, | 1.0487, | 1.0487, | 1.0488, | 1.0488, | 1.0489, |
| MP_Weighted Medies | 0.849 0.957, | 0.8491 | 0.8491 | 0.8492 0.153, | 0.8492 0.115, | 0.8492 | 0.8492 0.181, | 0.8492 0.382, | 0.8493 0.812, |
| MR-Weighted-Median | -0.1052, | -0.0587, | -0.0404, | -0.0220, | -0.0129, | -0.0037, | 0.181, 0.0142, | 0.382, 0.0323, | 0.812, 0.0764, |
| | 0.0392, | 0.0432, | 0.0460, | 0.0485, | 0.0499, | 0.0510, | 0.0544, | 0.0569, | 0.0674, |
| | 0.0263 | 0.0268 | 0.0271 | 0.0274 | 0.0275 | 0.0277 | 0.028 | 0.0284 | 0.0293 |
| MR-Weighted-Mode | 0.866, | 0.813, | 0.784, | 0.767, | 0.766, | 0.756, | 0.743, | 0.726, | 0.729, |
| | -0.1558, | -0.1189, | -0.1033, | -0.0890, | -0.0819, | -0.0740, | -0.0610, | -0.0461, | -0.0105, |
| | 0.1479, | 0.1488, | 0.1501, | 0.1505, | 0.1512, | 0.1516, | 0.1525, | 0.1536, | 0.1590, |
| MD D A DOI | 0.0513 | 0.0514 | 0.0514 | 0.0515 | 0.0516 | 0.0517 | 0.0519 | 0.0521 | 0.0523 |
| MR-RAPS1 | 0.072, -0.0241, | 0.072, 0.0259, | 0.075, 0.0459, | 0.078, 0.0660, | 0.077, 0.0760, | 0.079, 0.0860, | 0.085, 0.1060, | 0.099, 0.1260, | 0.118, 0.1760, |
| | 0.2779, | 0.0239, | 0.0439, | 0.0000, | 0.0700, | 0.0800, | 0.1000, | 0.1200, | 0.1700, |
| | 0.2739 | 0.2739 | 0.2739 | 0.2739 | 0.2779 | 0.2739 | 0.274 | 0.274 | 0.274 |
| MR-RAPS2 | 0.098, | 0.088, | 0.094, | 0.096, | 0.091, | 0.099, | 0.098, | 0.101, | 0.119, |
| | -0.0333, | 0.0105, | 0.0282, | 0.0470, | 0.0566, | 0.0701, | 0.0894, | 0.1141, | 0.1613, |
| | 0.3180, | 0.3091, | 0.3075, | 0.3073, | 0.3081, | 0.3136, | 0.3120, | 0.3116, | 0.3073, |
| 1 m n : | 0.2903 | 0.2915 | 0.2909 | 0.2911 | 0.2917 | 0.2901 | 0.2906 | 0.2919 | 0.2915 |
| MR-RAPS3 | 0.926, | 0.922, | 0.922, | 0.909, | 0.909, | 0.916, | 0.928, 1.9973, | 0.931, | 0.939, |
| | 5.3303, 130.5940, | 3.7135, 168.1767, | -1.4269, 141.4856, | 5.3399, 85.1299, | 1.3724, 40.2535, | 1.3301, 74.8899, | 73.1478, | 2.0407, 29.8844, | 0.3029, 31.9163, |
| | 445.4344 | 566.857 | 401.2783 | 189.6383 | 40.2535, | 191.5282 | 181.7078 | 30.6823 | 39.36 |
| MR-RAPS4 | 0.984, | 0.988, | 0.987, | 0.984, | 0.980, | 0.978, | 0.979, | 0.986, | 0.982, |
| | | 0.6937, | 0.7010, | 0.7561, | 0.9548, | 0.7176, | 0.4522, | 0.4824, | 0.4537, |
| | 0.1080, | 0.0957, | 0.7010, | 0.7501, | 0.2340, | 0.7170, | 0.4522, | | |
| | 0.1080, 12.4816, | 10.4543, | 11.1183, | 11.5701, | 15.3063, | 9.5789, | 8.1870, | 8.1668, | 2.7776, |

Table S67: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE violated, q=0.6, and N=200000.

| ((| / / | | | | , I | | | | |
|--------------------|---------------------|---------------------|----------|-----------|----------|----------|----------|-----------|---------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.979, | 0.605, | 0.235, | 0.039, | 0.022, | 0.031, | 0.217, | 0.590, | 0.982, |
| COLD THE THE | -0.0905, | -0.0409, | -0.0227, | -0.0071, | -0.0004, | 0.0066, | 0.0226, | 0.0410, | 0.0901, |
| | 0.0185, | 0.0180, | 0.0165, | 0.0141, | 0.0136, | 0.0141, | 0.0165, | 0.0181, | 0.0194, |
| | 0.0186 | 0.0186 | 0.0182 | 0.0178 | 0.0177 | 0.0179 | 0.0186 | 0.0192 | 0.02 |
| cML-MA-AIC-Profile | 0.979, | 0.605, | 0.234, | 0.039, | 0.021, | 0.030, | 0.217, | 0.588, | 0.982, |
| COME MATTING FROME | -0.0906, | -0.0409, | -0.0227, | -0.0071, | -0.0004, | 0.0066, | 0.0226, | 0.0410, | 0.0902, |
| | 0.0184, | 0.0180, | 0.0165, | 0.0141, | 0.0136, | 0.0141, | 0.0165, | 0.0181, | 0.0194, |
| | 0.0186 | 0.0186 | 0.0183 | 0.0178 | 0.0178 | 0.0179 | 0.0186 | 0.0192 | 0.0201 |
| cML-AIC | 0.990, | 0.807, | 0.467, | 0.124, | 0.079, | 0.129, | 0.424, | 0.785, | 0.995, |
| | -0.0950, | -0.0452, | -0.0259, | -0.0085, | -0.0003, | 0.0078, | 0.0258, | 0.0453, | 0.0950, |
| | 0.0199, | 0.0198, | 0.0193, | 0.0174, | 0.0171, | 0.0174, | 0.0191, | 0.0198, | 0.0208, |
| | 0.0147 | 0.015 | 0.0151 | 0.0152 | 0.0152 | 0.0153 | 0.0155 | 0.0156 | 0.0161 |
| cML-AIC-Profile | 0.990, | 0.808, | 0.464, | 0.121, | 0.079, | 0.127, | 0.423, | 0.783, | 0.995, |
| | -0.0952, | -0.0452, | -0.0259, | -0.0085, | -0.0003, | 0.0078, | 0.0258, | 0.0454, | 0.0950, |
| | 0.0199, | 0.0199, | 0.0193, | 0.0174, | 0.0171, | 0.0174, | 0.0191, | 0.0199, | 0.0208, |
| | 0.0148 | 0.015 | 0.0151 | 0.0152 | 0.0153 | 0.0153 | 0.0155 | 0.0156 | 0.0161 |
| cML-MA-BIC | 1.000, | 0.944, | 0.567, | 0.122, | 0.052, | 0.110, | 0.564, | 0.916, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0143, | 0.0145, | 0.0146, | 0.0147, | 0.0147, | 0.0148, | 0.0149, | 0.0151, | 0.0154, |
| | 0.0136 | 0.0139 | 0.014 | 0.0141 | 0.0142 | 0.0142 | 0.0144 | 0.0145 | 0.0149 |
| cML-MA-BIC-Profile | 1.000, | 0.944, | 0.567, | 0.121, | 0.052, | 0.110, | 0.564, | 0.916, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0143, | 0.0145, | 0.0146, | 0.0147, | 0.0147, | 0.0148, | 0.0149, | 0.0151, | 0.0154, |
| | 0.0137 | 0.0139 | 0.014 | 0.0141 | 0.0142 | 0.0142 | 0.0144 | 0.0145 | 0.0149 |
| cML-BIC | 1.000, | 0.946, | 0.573, | 0.125, | 0.054, | 0.115, | 0.572, | 0.919, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0098, | 0.0001, | 0.0101, | 0.0301, | 0.0502, | 0.1002, |
| | 0.0143, | 0.0145, | 0.0146, | 0.0147, | 0.0147, | 0.0148, | 0.0149, | 0.0150, | 0.0154, |
| | 0.0135 | 0.0138 | 0.0139 | 0.014 | 0.014 | 0.0141 | 0.0142 | 0.0144 | 0.0148 |
| cML-BIC-Profile | 1.000, | 0.946, | 0.573, | 0.125, | 0.053, | 0.113, | 0.570, | 0.919, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0098, | 0.0001, | 0.0101, | 0.0301, | 0.0502, | 0.1002, |
| | 0.0143, | 0.0145, | 0.0146, | 0.0147, | 0.0147, | 0.0148, | 0.0149, | 0.0150, | 0.0154, |
| | 0.0135 | 0.0138 | 0.0139 | 0.014 | 0.014 | 0.0141 | 0.0143 | 0.0144 | 0.0148 |
| MR-Mix | 0.993, | 0.829, | 0.398, | 0.057, | 0.030, | 0.077, | 0.389, | 0.793, | 0.992, |
| | -0.1015, | -0.0496, | -0.0293, | -0.0095, | 0.0003, | 0.0100, | 0.0290, | 0.0478, | 0.0932, |
| | 0.0160, | 0.0157, | 0.0156, | 0.0156, | 0.0155, | 0.0157, | 0.0157, | 0.0155, | 0.0159, |
| | 0.0186 | 0.0185 | 0.0187 | 0.0184 | 0.0185 | 0.0184 | 0.0184 | 0.0181 | 0.0185 |
| MR-ContMix | 1.000, | 0.953, | 0.614, | 0.158, | 0.072, | 0.151, | 0.602, | 0.927, | 1.000, |
| | -0.0998, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0300, | 0.0499, | 0.0999, |
| | 0.0147, | 0.0148, | 0.0148, | 0.0149, | 0.0150, | 0.0151, | 0.0152, | 0.0154, | 0.0158, |
| | NA | NA | NA NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.996, | 0.908, | 0.516, | 0.130, | 0.072, | 0.122, | 0.507, | 0.869, | 0.988, |
| | -0.0901, | -0.0401, | -0.0204, | -0.0001, | 0.0099, | 0.0199, | 0.0398, | 0.0598, | 0.1099, |
| | 0.1634, | 0.1635, | 0.1631, | 0.1644, | 0.1644, | 0.1649, | 0.1647, | 0.1647, | 0.1647, |
| | 0.0195 | 0.0197 | 0.0199 | 0.0199 | 0.02 | 0.0199 | 0.02 | 0.0202 | 0.0206 |
| MR-PRESSO | 0.414, | 0.332, | 0.230, | 0.134, | 0.122, | 0.140, | 0.241, | 0.343, | 0.472, |
| | -0.0315, | 0.0179, | 0.0379, | 0.0578, | 0.0679, | 0.0778, | 0.0977, | 0.1175, | 0.1668, |
| | 0.2885, | 0.2885, | 0.2884, | 0.2884, | 0.2884, | 0.2884, | 0.2882, | 0.2881, | 0.2876, |
| | 0.1714 | 0.1698 | 0.1693 | 0.1691 | 0.1691 | 0.1685 | 0.1678 | 0.1668 | 0.1632 |
| MR-IVW | 0.084, | 0.083, | 0.079, | 0.079, | 0.078, | 0.079, | 0.088, | 0.096, | 0.124, |
| | -0.0302, | 0.0203, | 0.0405, | 0.0607, | 0.0708, | 0.0808, | 0.1010, | 0.1212, | 0.1715, |
| | 0.2936, | 0.2936, | 0.2936, | 0.2935, | 0.2935, | 0.2935, | 0.2935, | 0.2935, | 0.2935, |
| | 0.2806 | 0.2805 | 0.2805 | 0.2805 | 0.2805 | 0.2805 | 0.2805 | 0.2805 | 0.2804 |
| MR-IVW-Oracle | 1.000, | 0.915, | 0.505, | 0.097, | 0.039, | 0.092, | 0.507, | 0.892, | 1.000, |
| * *** | -0.0998, | -0.0498, | -0.0298, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1000, |
| | 0.0142, | 0.0144, | 0.0145, | 0.0146, | 0.0147, | 0.0147, | 0.0148, | 0.0150, | 0.0154, |
| | 0.0147 | 0.015 | 0.0151 | 0.0152 | 0.0153 | 0.0154 | 0.0155 | 0.0157 | 0.0161 |
| MR-Egger | 0.178, | 0.190, | 0.195, | 0.198, | 0.201, | 0.204, | 0.211, | 0.217, | 0.224, |
| 30 | 0.6026, | 0.6523, | 0.6722, | 0.6920, | 0.7019, | 0.7118, | 0.7316, | 0.7515, | 0.8009, |
| | 1.0480, | 1.0479, | 1.0479, | 1.0478, | 1.0478, | 1.0478, | 1.0477, | 1.0477, | 1.0476, |
| | 0.861 | 0.861 | 0.861 | 0.861 | 0.861 | 0.861 | 0.861 | 0.861 | 0.861 |
| MR-Weighted-Median | 0.996, | 0.825, | 0.489, | 0.162, | 0.118, | 0.112, | 0.302, | 0.600, | 0.941, |
| <u> </u> | -0.1057, | -0.0585, | -0.0398, | -0.0212, | -0.0119, | -0.0026, | 0.0158, | 0.0342, | 0.0800, |
| | 0.0355, | 0.0423, | 0.0456, | 0.0491, | 0.0508, | 0.0526, | 0.0562, | 0.0596, | 0.0668, |
| | 0.0188 | 0.0191 | 0.0193 | 0.0195 | 0.0196 | 0.0197 | 0.0199 | 0.0201 | 0.0209 |
| MR-Weighted-Mode | 0.903, | 0.853, | 0.827, | 0.821, | 0.818, | 0.824, | 0.811, | 0.807, | 0.792, |
| - | -0.1554, | -0.1182, | -0.1033, | -0.0881, | -0.0805, | -0.0731, | -0.0587, | -0.0439, | -0.0087 |
| | 0.1328, | 0.1342, | 0.1355, | 0.1365, | 0.1369, | 0.1374, | 0.1392, | 0.1404, | 0.1460, |
| | 0.02 | 0.0201 | 0.0201 | 0.0202 | 0.0202 | 0.0202 | 0.0203 | 0.0204 | 0.0207 |
| MR-RAPS1 | 0.082, | 0.077, | 0.084, | 0.085, | 0.091, | 0.091, | 0.093, | 0.105, | 0.128, |
| | -0.0314, | 0.0186, | 0.0387, | 0.0587, | 0.0687, | 0.0787, | 0.0987, | 0.1187, | 0.1687, |
| | 0.2870, | 0.2870, | 0.2870, | 0.2870, | 0.2870, | 0.2870, | 0.2870, | 0.2870, | 0.2870, |
| | 0.2733 | 0.2733 | 0.2733 | 0.2733 | 0.2733 | 0.2733 | 0.2733 | 0.2733 | 0.2733 |
| MR-RAPS2 | 0.336, | 0.263, | 0.233, | 0.208, | 0.197, | 0.188, | 0.172, | 0.151, | 0.149, |
| * | -0.1246, | -0.0631, | -0.0415, | -0.0216, | -0.0147, | 0.0027, | 0.0271, | 0.0403, | 0.0989, |
| | 0.4235, | 0.3437, | 0.3206, | 0.3156, | 0.3100, | 0.3270, | 0.3306, | 0.3146, | 0.3201, |
| | 0.192 | 0.1986 | 0.2012 | 0.2038 | 0.2053 | 0.2067 | 0.2081 | 0.2138 | 0.2239 |
| MR-RAPS3 | 0.951, | 0.948, | 0.940, | 0.948, | 0.952, | 0.956, | 0.951, | 0.947, | 0.949, |
| | -37.8104, | -4.2250, | -1.7704, | -5.5316, | 4.7789, | 0.0180, | 0.6276, | -4.7526, | -16.313 |
| | 941.3561, | 101.5375, | 34.4377, | 130.4426, | 55.2695, | 18.2874, | 97.0454, | 147.4679, | 508.277 |
| | 10820 | 205.8 | 26.5 | 241.9 | 38.82 | 6.667 | 205.2 | 499.1 | 6162 |
| MR-RAPS4 | 0.990, | 0.984, | 0.980, | 0.977, | 0.981, | 0.985, | 0.984, | 0.987, | 0.990, |
| | | | -0.1244, | -0.1260, | -0.1665, | -0.1443, | -0.1504, | -0.0510, | -0.0178 |
| MIC-KAI 54 | -0.1036 | | | | | | | -U.U.JIU. | -U.UI/0 |
| WIK-KAI 54 | -0.1036, 3.4325, | -0.1812, 6.9522, | 7.6520, | 7.5668, | 7.7123, | 7.6815, | 7.7571, | 7.2657, | 7.4870, |

Table S68: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the ideal case of q=0, and N=50000.

| | · / | | | | | | | | |
|--------------------|---------------------|---------------------|---------------------|---------------------|------------------------------|--------------------|--------------------|--------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000 | 0.996, | 0.941 | 0.206 | 0.099, | 0.241 | 0.946 | 0.991, | 1.000, |
| CML-MA-AIC | 1.000, -0.0973, | -0.0478, | 0.841, -0.0279, | 0.206, -0.0085, | 0.099, | 0.241, 0.0097, | 0.846, 0.0290, | 0.991, | 0.0983, |
| | 0.0105, | 0.0107, | 0.0108, | 0.0102, | 0.0100, | 0.0104, | 0.0230, | 0.0435, | 0.0117, |
| | 0.0084 | 0.0085 | 0.0086 | 0.0086 | 0.0086 | 0.0087 | 0.0089 | 0.009 | 0.0093 |
| cML-MA-AIC-Profile | 1.000, | 0.996, | 0.840, | 0.204, | 0.097, | 0.238, | 0.846, | 0.991, | 1.000, |
| | -0.0980, | -0.0479, | -0.0279, | -0.0085, | 0.0006, | 0.0097, | 0.0291, | 0.0490, | 0.0989, |
| | 0.0106, | 0.0108, | 0.0108, | 0.0102, | 0.0100, | 0.0105, | 0.0113, | 0.0115, | 0.0118, |
| cML-AIC | 0.0085 | 0.0086 | 0.0087 | 0.0087 0.280, | 0.0087 | 0.0088 | 0.0089 0.887, | 0.0091 | 0.0094 |
| CML-AIC | 1.000, -0.0985, | 0.998, -0.0487, | 0.882, -0.0287, | -0.0089, | 0.156, 0.0007, | 0.325, 0.0103, | 0.887, 0.0300, | 0.997, 0.0499, | 1.000, 0.0995, |
| | 0.0109, | 0.0111, | 0.0111, | 0.0111, | 0.0007, | 0.0103, | 0.0116, | 0.0117, | 0.0121, |
| | 0.0077 | 0.0079 | 0.0079 | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0083 | 0.0085 |
| cML-AIC-Profile | 1.000, | 0.998, | 0.880, | 0.274, | 0.154, | 0.316, | 0.886, | 0.997, | 1.000, |
| | -0.0989, | -0.0487, | -0.0287, | -0.0089, | 0.0007, | 0.0103, | 0.0300, | 0.0500, | 0.0998, |
| | 0.0111, | 0.0111, | 0.0112, | 0.0111, | 0.0110, | 0.0113, | 0.0116, | 0.0118, | 0.0122, |
| cML-MA-BIC | 0.0078 | 0.0079 1.000, | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0082 0.978, | 0.0083 | 0.0086 1.000, |
| CML-MA-BIC | 1.000, -0.0997, | -0.0497, | 0.985, -0.0297, | -0.0097, | 0.050, 0.0003, | 0.277, 0.0103, | 0.978, 0.0303, | 1.000, 0.0503, | 0.1003, |
| | 0.0073, | 0.0074, | 0.0074, | 0.0075, | 0.0005, | 0.0075, | 0.0076, | 0.0077, | 0.0079, |
| | 0.0072 | 0.0073 | 0.0074 | 0.0074 | 0.0075 | 0.0075 | 0.0076 | 0.0077 | 0.0079 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.985, | 0.255, | 0.048, | 0.272, | 0.976, | 1.000, | 1.000, |
| | -0.0997, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0073, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0075, | 0.0076, | 0.0077, | 0.0079, |
| M. DIG | 0.0072 | 0.0073 | 0.0074 | 0.0075 | 0.0075 | 0.0075 | 0.0076 | 0.0077 | 0.008 |
| cML-BIC | 1.000, -0.0997, | 1.000, -0.0497, | 0.985, -0.0297, | 0.263, -0.0097, | 0.051, 0.0003, | 0.287, 0.0103, | 0.979, 0.0303, | 1.000, 0.0503, | 1.000, 0.1003, |
| | 0.0073, | 0.0074, | -0.0297, 0.0074, | 0.0097, | 0.0003, | 0.0103, 0.0076, | 0.0303, 0.0076, | 0.0503, 0.0077, | 0.1003, 0.0079, |
| | 0.0073, | 0.0074, | 0.0074, | 0.0073, | 0.0073, | 0.0076, | 0.0076, | 0.0077, | 0.0079 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.985, | 0.258, | 0.050, | 0.285, | 0.979, | 1.000, | 1.000, |
| | -0.0997, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0073, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0076, | 0.0076, | 0.0077, | 0.0079, |
| | 0.0072 | 0.0073 | 0.0073 | 0.0074 | 0.0074 | 0.0075 | 0.0076 | 0.0076 | 0.0079 |
| MR-Mix | 0.818, | 0.703, | 0.564, | 0.117, | 0.023, | 0.134, | 0.568, | 0.692, | 0.790, |
| | -0.1121, 0.0361, | -0.0548, 0.0211, | -0.0331, 0.0169, | -0.0110, 0.0145, | -0.0003, 0.0141, | 0.0105, 0.0145, | 0.0322, 0.0163, | 0.0528, 0.0198, | 0.1027, 0.0316, |
| | 0.0501, | 0.0211, | 2.7381 | 0.0145, | 0.0141, | 0.0143, | 0.0103, | 0.0198, | 0.0316, |
| MR-ContMix | 1.000, | 0.998, | 0.876, | 0.234, | 0.125, | 0.275, | 0.878, | 0.997, | 1.000, |
| | -0.1212, | -0.0687, | -0.0436, | -0.0149, | 0.0009, | 0.0162, | 0.0449, | 0.0701, | 0.1240, |
| | 0.0102, | 0.0132, | 0.0156, | 0.0176, | 0.0181, | 0.0177, | 0.0162, | 0.0142, | 0.0116, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 1.000, | 0.980, | 0.266, | 0.058, | 0.288, | 0.972, | 1.000, | 1.000, |
| | -0.0990, | -0.0494, 0.0077, | -0.0296, | -0.0097, 0.0077, | 0.0002, 0.0077, | 0.0101, 0.0078, | 0.0301, 0.0078, | 0.0498, 0.0078, | 0.0994, 0.0082, |
| | 0.0075, 0.0071 | 0.0077, | 0.0076, 0.0073 | 0.0077, | 0.0077, | 0.0078, | 0.0078, | 0.0076 | 0.0082, |
| MR-PRESSO | 1.000, | 1.000, | 0.986, | 0.259, | 0.043, | 0.282, | 0.980, | 1.000, | 1.000, |
| | -0.0989, | -0.0493, | -0.0295, | -0.0096, | 0.0003, | 0.0102, | 0.0301, | 0.0499, | 0.0996, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0076, | 0.0078, |
| | 0.0071 | 0.0072 | 0.0072 | 0.0073 | 0.0073 | 0.0074 | 0.0074 | 0.0075 | 0.0078 |
| MR-IVW | 1.000, | 1.000, | 0.984, | 0.244, | 0.043, | 0.267, | 0.980, | 1.000, | 1.000, |
| | -0.0990, | -0.0493, | -0.0295, | -0.0096, | 0.0003, | 0.0102, | 0.0301, | 0.0499, | 0.0996, |
| | 0.0072, 0.0073 | 0.0073, 0.0074 | 0.0073, 0.0075 | 0.0074, 0.0075 | 0.0074, 0.0076 | 0.0074, 0.0076 | 0.0075, 0.0077 | 0.0076, 0.0078 | 0.0078, 0.008 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.984, | 0.244, | 0.043, | 0.267, | 0.980, | 1.000, | 1.000, |
| mit I v m Gracie | -0.0990, | -0.0493, | -0.0295, | -0.0096, | 0.0003, | 0.0102, | 0.0301, | 0.0499, | 0.0996, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0076, | 0.0078, |
| | 0.0073 | 0.0074 | 0.0075 | 0.0075 | 0.0076 | 0.0076 | 0.0077 | 0.0078 | 0.008 |
| MR-Egger | 0.637, | 0.208, | 0.093, | 0.047, | 0.042, | 0.050, | 0.100, | 0.194, | 0.566, |
| | -0.0824, | -0.0410, | -0.0245, | -0.0079, | 0.0004, | 0.0087, | 0.0252, | 0.0418, | 0.0831, |
| | 0.0345, 0.0355 | 0.0352, 0.0361 | 0.0355, 0.0365 | 0.0359, 0.0368 | 0.0361, 0.037 | 0.0363, 0.0372 | 0.0367, 0.0376 | 0.0372, 0.038 | 0.0384, 0.0391 |
| MR-Weighted-Median | 1.000, | 0.0301 | 0.811, | 0.0308 | 0.037 | 0.0372 | 0.801, | 0.038 | 1.000, |
| | -0.0971, | -0.0485, | -0.0291, | -0.0096, | 0.0002, | 0.0099, | 0.0294, | 0.0488, | 0.0976, |
| | 0.0091, | 0.0093, | 0.0095, | 0.0096, | 0.0096, | 0.0096, | 0.0098, | 0.0099, | 0.0103, |
| | 0.0104 | 0.0106 | 0.0106 | 0.0107 | 0.0108 | 0.0108 | 0.011 | 0.0111 | 0.0114 |
| MR-Weighted-Mode | 0.994, | 0.499, | 0.130, | 0.016, | 0.008, | 0.013, | 0.147, | 0.450, | 0.982, |
| | -0.0963, | -0.0480, | -0.0287, | -0.0094, | 0.0002, | 0.0098, | 0.0290, | 0.0485, | 0.0969, |
| | 0.0184, | 0.0190, | 0.0191, | 0.0194, 0.0255 | 0.0195, | 0.0197, 0.0258 | 0.0198, | 0.0199, 0.0264 | 0.0204, |
| MR-RAPS1 | 0.0247 1.000, | 0.0251 1.000, | 0.0253 0.984, | 0.0255 | 0.0257 0.041, | 0.0258 | 0.0261 0.980, | 1.000, | 0.0272 1.000, |
| WIN-IXAL 91 | -0.0996, | -0.0497, | -0.0297, | -0.0097, | 0.001, | 0.266, | 0.980, | 0.0503, | 0.1003, |
| | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0076, | 0.0076, | 0.0079, |
| | 0.0073 | 0.0074 | 0.0075 | 0.0076 | 0.0076 | 0.0076 | 0.0077 | 0.0078 | 0.0081 |
| MR-RAPS2 | 1.000, | 1.000, | 0.974, | 0.237, | 0.048, | 0.255, | 0.967, | 1.000, | 1.000, |
| | -0.1032, | -0.0266, | -0.0860, | -0.0016, | 0.0003, | 0.0103, | 0.0303, | 0.0354, | 0.1237, |
| | 1.1696, | 0.7274, | 2.2136, | 0.2561, | 0.0076, | 0.0077, | 0.0078, | 0.4716, | 1.0524, |
| MD DADG2 | 0.0085 1.000, | 0.0079 1.000, | 0.0085 | 0.0079 0.259, | 0.0078 | 0.0079 | 0.0079 | 0.0084 | 0.009 |
| MR-RAPS3 | -0.0997, | -0.0497, | -0.0297, | -0.0097, | 0.047, 0.0003, | 0.283, 0.0103, | 0.981, 0.0303, | 1.000, 0.0503, | 1.000, 0.1003, |
| | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0005, | 0.0103, | 0.0303, | 0.0076, | 0.1003, |
| | 0.0073, | 0.0073 | 0.0073 | 0.0074 | 0.0074 | 0.0075 | 0.0075 | 0.0076 | 0.0079 |
| MR-RAPS4 | 1.000, | 1.000, | 0.979, | 0.249, | 0.054, | 0.279, | 0.970, | 1.000, | 1.000, |
| | | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | -0.0997, | | | | | | | | |
| | 0.0075, 0.0073 | 0.0075, 0.0075 | 0.0076, 0.0075 | 0.0076, 0.0076 | 0.0003, 0.0077, 0.0076 | 0.0077, 0.0077 | 0.0078, 0.0077 | 0.0079, 0.0078 | 0.0081, 0.0081 |

Table S69: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the ideal case of q=0, and N=100000.

| CML-MA-AIC | | | 1 , | | | | |
|--|---------------------|----------------------------|---------------|---------|--------------------|--------------------|--------------------|
| -0.0988, | -0.03 | -0.05 -0.03 -0.01 | 1 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| O.00988 O.00491 O.0076 O.0075 O.0076 O.0076 O.0061 O.0059 O.0061 O.0059 O.0061 O.0059 O.0061 O.0075 O.0076 O.0077 O.0077 O.0077 O.0077 O.0077 O.0078 O.0055 O.0056 O.0055 O.0056 O.0055 O.0056 O.0058 O.0055 O.0056 O.0058 O.0078 O.0055 O.0056 O.0051 O.0051 O.0051 O.0051 O.0052 O.0051 O.0051 O.0052 O.0051 O.0051 O.0052 O.0051 O.0051 O.0052 O.0051 O.0051 O.0051 O.0052 O.0051 O.0052 O.0051 O.0052 | 0.986, | 00, 1.000, 0.986, 0.358 | 58, 0.087, | 0.344, | 0.980, | 1.000, | 1.000, |
| CML-MA-AIC-Profile | -0.0292, | | | | 0.0287, | 0.0486, | 0.0984, |
| cML-MA-AIC-Profile 1.000, -0.0992, -0.0492, -0.0492, -0.0006 0.00076, -0.0006 0.0006 0.0061 0.0061 0.0061 0.0061 0.0061 0.0061 0.0061 0.0061 0.0061 0.0061 0.0061 0.0061 0.0061 0.0061 0.0061 0.0076, -0.0097, -0.0078, -0.0077, -0.0078, -0.0098, -0.0498, -0.0098, -0.0498, -0.0099, -0.0099, | 0.0077, | | | | 0.0079, | 0.0080, | 0.0082, |
| -0.0992, | 0.0061 | | | | 0.0063 | 0.0064 | 0.0066 |
| CML-AIC 1.000, | 0.986, | | | | 0.980, | 1.000, | 1.000, |
| CML-AIC 1.000, | -0.0292, | | | | 0.0287, | 0.0487, | 0.0987, |
| CML-AIC 1.000, | 0.0077, | | | | 0.0079, | 0.0080, | 0.0083, |
| -0.0995, | 0.0061 | | | | 0.0063 | 0.0064 | 0.0066 |
| CML-AIC-Profile | 0.992, | | | | 0.988, | 1.000, | 1.000, |
| CML-AIC-Profile | -0.0298, 0.0079, | | | | 0.0294, 0.0082, | 0.0494, 0.0084, | 0.0992, 0.0085, |
| cML-AIC-Profile 1.000, -0.0998, -0.0498, -0.00978, 0.0078, 0.0078, 0.0078, 0.0075 -0.0078, 0.0078, 0.0056 0.0055 cML-MA-BIC 1.000, -0.0501, -0.0501, 0.0051, 0.0051, 0.0052, 0.0051 0.0051, 0.0052, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0055, 0.0051, 0.0055, 0.0051, 0.0055, 0.0051, 0.0055, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0051, 0.0052, 0.0051, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0053, 0.0053, 0.0054, 0.0064, 0.0068, 0.0064, 0.0068, 0.0064, 0.0068, 0.0064, 0.0068, 0.0064, 0.0068, 0.0064, 0. | 0.0079, | | | | 0.0082, | 0.0084, | 0.0083, |
| -0.0998, | 0.992, | | | | 0.986, | 1.000, | 1.000, |
| O.0078, | -0.0298, | | | | 0.0294, | 0.0494, | 0.0995, |
| CML-MA-BIC | 0.0079, | | | | 0.0082, | 0.0084, | 0.0085, |
| CML-MA-BIC | 0.0056 | | | | 0.0058 | 0.0059 | 0.0061 |
| -0.1001, | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| O.0051 | -0.0301, | | 101, -0.0001, | 0.0099, | 0.0299, | 0.0498, | 0.0998, |
| cML-MA-BIC-Profile 1.000, -0.1001, -0.0501, -0.0051, 0.0052, 0.0051 1.000, -0.0501, -0.0052, 0.0052 cML-BIC 1.000, -0.1001, -0.0501, -0.0051, 0.0052, 0.0051 0.0052, 0.0051 cML-BIC 1.000, -0.1001, -0.0501, 0.0052, 0.0051 0.005 cML-BIC-Profile 1.000, -0.0051, 0.0052, 0.0051 0.005 cML-BIC-Profile 1.000, -0.1001, -0.0501, 0.0052, 0.0051 0.0051, 0.0052, 0.0051 cMR-Mix 0.834, -0.746, -0.1131, -0.0556, 0.0034 0.0343, 0.0195, 0.0054 cMR-ContMix 1.000, -1.000, -1.000, -0.0049, -0.0064, 0.0080, 0.0064, 0.0080, 0.0064, 0.0080, 0.0064, 0.0080, 0.0064, 0.0080, 0.0051, 0.0052, 0.0053, 0.0054, 0.0052, 0.0053, 0.0054, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0053, 0.0051, 0.0052, 0.0053, 0.0052, 0.0053, 0.0051, 0.0052, 0.0053, 0.0051, 0.0052, 0.0053, 0.0052, 0.0053, 0.0052, 0.0053, 0.0052, 0.0053, 0.0052, 0.0053, 0.0054, | 0.0052, | | | | 0.0054, | 0.0054, | 0.0056, |
| -0.1001, | 0.0052 | | | | 0.0054 | 0.0054 | 0.0056 |
| CML-BIC 1.000, 1 | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| CML-BIC | -0.0301, | | | | 0.0299, | 0.0498, | 0.0998, |
| CML-BIC 1.000, | 0.0052, | | | | 0.0054, | 0.0054, | 0.0056, |
| -0.1001, | 0.0052 | | | | 0.0054 | 0.0054 | 0.0056 |
| CML-BIC-Profile | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| CML-BIC-Profile | -0.0301, | | | | 0.0299, | 0.0499, | 0.0998, |
| cML-BIC-Profile 1.000, -0.1001, -0.0501, -0.0501, 0.0051, 0.0051, 0.0051, 0.0051, 0.0051 0.0051, 0.0052, 0.0051 MR-Mix 0.834, -0.746, -0.1131, -0.0556, -0.0034, 0.0195, 0.0346 0.2241 -0.0063, -0.0064, 0.0080, 0.0142, -0.0064, 0.0080, 0.0064, 0.0080, 0.0064, 0.0080, 0.0064, 0.0080, 0.0064, 0.0083, 0.0053, 0.0053, 0.0053, 0.0053, 0.0053, 0.0053, 0.0054, 0.0051, 0.0052, 0.0051, 0.0051, 0.0052, 0.0051, 0.0051, 0.0052, 0.0051, 0.0051, 0.0052, 0.0051, 0.0051, 0.0052, 0.0051, 0.0052, 0.0052, 0.0051, 0.0052, 0.0053, 0.0054, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0053, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0053, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0053, 0.0052, 0.005 | 0.0052, 0.0052 | | | | 0.0054, 0.0053 | 0.0054, 0.0054 | 0.0056, 0.0056 |
| -0.1001, | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| 0.0051, 0.0052, 0.0051 | -0.0301, | | | | 0.0299, | 0.0499, | 0.0998, |
| 0.0051 0.0051 0.0051 0.0051 0.0051 0.0051 0.0051 0.0051 0.0054 0.0054 0.00556 0.00343 0.0195 0.00346 0.2241 0.0054 0.0064 0.0080 0.0064 0.0080 0.0064 0.0080 0.0064 0.0053 0.0053 0.0053 0.0055 0.0051 0.0052 0.0064 0.0065 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 0.0051 0.0052 | 0.0052, | | | | 0.0255, | 0.0455, | 0.0956, |
| MR-Mix | 0.0052, | | | | 0.0054, | 0.0054 | 0.0056 |
| -0.1131, -0.0556, -0.0343, 0.0195, 0.0343, 0.0195, 0.0343, 0.0195, 0.0346, 0.2241 0.0 0.0061, 0.0063, -0.0663, -0.0064, 0.0080, 0.0080, 0.0080, 0.0080, 0.0080, 0.0080, 0.0080, 0.0080, 0.0080, 0.0080, 0.0080, 0.0080, 0.0080, 0.0080, 0.0081, 0.0097, -0.0499, -0.00997, -0.0499, -0.00951, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, 0.0051, 0.0052, | 0.641, | | | | 0.643, | 0.727, | 0.834, |
| MR-ContMix | -0.0335, | | | | 0.0315, | 0.0522, | 0.1019, |
| MR-ContMix | 0.0148, | | | | 0.0150, | 0.0191, | 0.0312, |
| -0.1142, | 0.0725 | | | | 0.1184 | 0.0797 | 0.1323 |
| 0.0064, NA | 0.991, | 00, 1.000, 0.991, 0.391 | 0.114, | 0.393, | 0.989, | 1.000, | 1.000, |
| NA | -0.0435, | | | | 0.0429, | 0.0660, | 0.1159, |
| MR-Lasso | 0.0097, | | | | 0.0104, | 0.0090, | 0.0072, |
| 0.0997, 0.0499, 0.0054, 0.0055, 0.0051, 0.0051 0.0052 0.0051 0.0051 0.0052 0.0051 0.0051 0.0052 0.0051 0.0051 0.0052 0.0051 0.0051 0.0052 0.0051 0.0052 0.0053 0.0054 0.0054 0.0054 0.0055 0.0052 0.0055 | NA | | NA | | NA | NA | NA |
| MR-PRESSO | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| MR-PRESSO | -0.0300, | | | | 0.0298, | 0.0497, | 0.0994, |
| MR-PRESSO 1.000, 1.000, -0.0997, -0.0499, -0.0051, 0.0051, 0.0051, 0.0051, 0.0051, 0.0051, 0.0051, 0.0051, 0.0052, 0.0051, 0.0051, 0.0052, 0.0 | 0.0054, | | | | 0.0056, | 0.0057, | 0.0059, |
| -0.0997, | 0.0052 | | | | 0.0054 | 0.0054 | 0.0056 |
| MR-IVW | 1.000, | | | | 1.000, 0.0298, | 1.000, 0.0497, | 1.000, 0.0995, |
| MR-IVW | -0.0300, 0.0052, | | | | 0.0298, | 0.0497, | 0.0993, |
| MR-IVW 1.000, | 0.0052, | | | | 0.0054, | 0.0054, | 0.0056, |
| -0.0997, | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| 0.0051, 0.0052, 0.0052 0.0055 0.0052 0.0052 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0054 0.0064 0.0068 0.0064 0.0068 0.0064 0.0068 0.0064 0.0068 0.0064 0.0068 0.0052 0.0051 0.0052 0.0053 0.0054 0.0064 0.0068 0.0064 0.0068 0.0051 0.0051 0.00552 0.00551 0.00551 0.00551 0.00551 0.00551 0.00551 0.00551 0.00551 0.00552 0.00551 0.00551 0.00551 0.00551 0.00551 0.00552 0.00551 0.00551 0.00551 0.00552 0.00551 0.00551 0.00552 0.00551 0.00552 0.00551 0.0 | -0.0300, | | | | 0.0298, | 0.0497, | 0.0995, |
| MR-IVW-Oracle | 0.0052, | | 0.0053, | | 0.0054, | 0.0054, | 0.0056, |
| MR-IVW-Oracle 1.000, -0.0997, -0.0499, -0.0051, -0.0052, -0.0052 | 0.0053 | | | | 0.0055 | 0.0055 | 0.0057 |
| 0.0997, 0.0499, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0261, 0.0263, 0.0268, 0.0268, 0.0263, 0.0268, 0.0064, 0.0065, 0.0064, 0.0065, 0.0073, 0.0075, 0.0073, 0.0075, 0.0073, 0.0075, 0.0052, 0.0051, 0.0051, 0.0051, 0.0051, 0.0051, 0.0051, 0.0052, 0.00 | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| 0.0051, 0.0052, 0.0052 0.0052 0.0052 0.0052 0.0052 0.0052 0.0052 0.0052 0.0052 0.0052 0.0052 0.0052 0.0064 0.0261, 0.0265, 0.0265 0.0263 0.0268 0.0263 0.0268 0.0064 0.0064, 0.0065, 0.0064, 0.0065, 0.0064 0.0065, 0.0073 0.0075 0.0064 0.0065, 0.0064 0.0065, 0.0073 0.0075 0.0064 0.0065, 0.0064 0.0065, 0.0064 0.0065, 0.0064 0.0065, 0.0064 0.0052 0.00132, 0.0132, 0.0130, 0.0132, 0.0177 0.018 0.0077 0.018 0.0077 0.018 0.0052 0.0064 0.0068 0.0064 0.0068 0.0064 0.0068 0.0064 0.0065 0.0052 0.0051 0.0052 0.00551 0.0052 0.00551 0.0052 0.00551 0.0052 0.00551 0.0052 0.00551 0.0052 0.00551 0.00551 0.00551 0.0052 0.00551 0.005 | -0.0300, | | | | 0.0298, | 0.0497, | 0.0995, |
| MR-Egger 0.934, 0.406, 0. 0.0919, -0.0466, 0. 0.0261, 0.0265, 0. 0.0263 0.0268 0.0 MR-Weighted-Median 1.000, 1.000, -0. 0.0989, -0.0496, 0. 0.0064, 0.0065, 0. 0.0073 0.0075 0. MR-Weighted-Mode 1.000, 0.856, 00.0992, -0.0499, -0. 0.0130, 0.0132, 0. 0.0177 0.018 0.0 MR-RAPS1 1.000, 1.000, 1.0 -0.1001, -0.0501, 0.0052, 0.0052, 0.0052 0.0052 0.0053 0.0 MR-RAPS2 1.000, 1.000, 10.0354, 0.0342, 10.0254, 0.0342, 10.0064 0.0068 0.0 MR-RAPS3 1.000, 1.000, 10.1001, -0.0501, -0.0068 MR-RAPS3 1.000, 1.000, 1.000, 10.1001, -0.0501, -0.0552, 0.0052, 0.0052 | 0.0052, | | 0.0053, | 0.0053, | 0.0054, | 0.0054, | 0.0056, |
| -0.0919, -0.0466, -0.00261, -0.0265, -0.02661, -0.0268, -0.0268, -0.0263, -0.0268, -0.0263, -0.0268, -0.0263, -0.0268, -0.0268, -0.0268, -0.0268, -0.0268, -0.0268, -0.0064, -0.0065, -0.0064, -0.0065, -0.0073, -0.0075, -0.0075, -0.0075, -0.0075, -0.0075, -0.0075, -0.00130, -0.0132, -0.0130, -0.0132, -0.0130, -0.0132, -0.0177, -0.018, -0.0017, -0.0051, -0.0051, -0.0051, -0.0052, -0.0051, -0.0051, -0.0051, -0.0051, -0.0051, -0.0051, -0.0052, | 0.0053 | | | | 0.0055 | 0.0055 | 0.0057 |
| 0.0261, 0.0265, 0.0 0.0263 | 0.185, | 34, 0.406, 0.185, 0.062 | 52, 0.045, | 0.059, | 0.162, | 0.350, | 0.876, |
| 0.0263 | -0.0286, | | | | 0.0257, | 0.0438, | 0.0890, |
| MR-Weighted-Median 1.000, | 0.0267, | | | | 0.0275, | 0.0279, | 0.0288, |
| 0.0989, 0.0496, 0.0064, 0.00052, 0.0064, 0.0073 0.0075 0.0064, 0.0065, 0.0063, 0.0073 0.0075 0.0064, 0.0064, 0.0064, 0.0064, 0.0064, 0.0130, 0.0130, 0.0132, 0.0177 0.018 0.0072, 0.0051, 0.0051, 0.0052, 0.0051, 0.0052, 0.0053 0.0053 0.0053, 0.0054, 0.0064, 0.0068, 0.0064, 0.0068, 0.0064, 0.0068, 0.0064, 0.0068, 0.0064, 0.0065, 0.0052, 0.00051, 0.00052, 0.00 | 0.027 | | | | 0.0278 | 0.0281 | 0.029 |
| 0.0064, 0.0065, 0.0073 0.0075 0.0073 0.0075 0.0051 0.0051 0.0052 0.0053 0.0075 0.0 | 0.991, | | | | 0.982, | 1.000, | 1.000, |
| 0.0073 0.0075 0.0078 0.0078 0.0078 0.0078 0.0078 0.0078 0.0080 0.0085 0.0092 0.0130 0.0132 0.0130 0.0177 0.018 0.0077 0.018 0.0077 0.0081 0.0051 0.0051 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.00551 0.0052 0.00551 0.00551 0.00552 0. | -0.0299, | | | | 0.0293, | 0.0491, | 0.0983, |
| MR-Weighted-Mode 1.000, -0.0992, -0.0499, -0.0499, -0.0130, 0.0132, 0.0 0.0130, 0.0132, 0.0 MR-RAPS1 1.000, -0.1001, -0.0501, -0.0051, 0.0052, 0.0051, 0.0052, 0.0053 0.0 MR-RAPS2 1.000, -1.000, -1.000, 1.000, -1.000, -1.000, -1.0027, 1.0272, 0.0053, -0.0052, 0.0053 0.0 MR-RAPS2 1.000, -1.000, -1.000, -1.000, -1.0072, 0.0064, 0.0068, 0.0 0.0 MR-RAPS3 1.000, -1.000, -1.000, -0.0501, -0.000, -0.001, -0.0501, -0.0501, -0.0052, 0.0052, 0.0 | 0.0065, 0.0075 | | | | 0.0066, 0.0078 | 0.0067, 0.0079 | 0.0069, 0.0081 |
| 0.0992, 0.0499, 0.0130, 0.0132, 0.0137, 0.018 0.0177 0.018 0.0177 0.018 0.0177 0.018 0.0177 0.018 0.0177 0.018 0.0051, 0.0051, 0.0052, 0.0053 0.0052, 0.0053 0.0052 0.0053 0.0052, 0.0053 0.0052, 0.0053 0.0052, 0.0053 0.0052, 0.0053 0.0052, 0.0053 0.0052, 0.0053 0.0052, 0.0054 0.0064 0.0068 0.0064 0.0068 0.0064 0.0068 0.0064 0.0068 0.0064 0.0068 0.0064 0.0051, 0.0051, 0.0052, 0.0052, 0.00551, 0.0052, 0.0052, 0.005 | 0.0075 | | | | 0.0078 | 0.0079 | 1.000, |
| 0.0130, 0.0132, 0.0 | -0.0303, | | | | 0.303, 0.0290, | 0.810, 0.0487, | 0.0977, |
| 0.0177 0.018 0.018 0.018 0.0177 0.018 0.018 0.000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.00052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.0052 0.0053 0.00000 1.0000 1.0000 1.0072 1.0272 1.1871 1.00064 0.0068 0.0064 0.0068 0.0064 0.0068 0.000000 0.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.0000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.00000 1.000000 1.000000 1.000000 1.000000 1.000000 1.000000 1.0000000 1.0000000 1.00000000 1.000000000 1.0000000000 | 0.0133, | | | | 0.0230, | 0.0487, | 0.0377, |
| MR-RAPS1 1.000, 1.000, -0.1001, -0.0501, -0.0051, -0.0051, -0.0052, -0.0052, -0.0052, -0.0052, -0.0052, -0.0052, -0.0052, -0.0053, -0.0052, -0.0052, -0.0052, -0.0052, -0.0052, -0.0052, -0.0064, -0.0068, -0.0064, -0.0068, -0.0064, -0.0068, -0.0064, -0.0068, -0.0064, -0.0061, -0.0051, -0.0051, -0.0051, -0.0052, -0.0052, -0.0052, -0.0052, -0.0051, -0.0051, -0.0052, -0.0052, -0.0051, -0.0051, -0.0051, -0.0052, -0.0052, -0.0052, -0.0051, -0.0051, -0.0051, -0.0052, -0.0052, -0.0051, -0.0051, -0.0051, -0.0052, -0.0052, -0.0052, -0.0051, -0.0051, -0.0051, -0.0051, -0.0052 | 0.0181 | | | | 0.0187 | 0.0189 | 0.0141, |
| 0.1001, -0.0501, -0.0501, 0.0051, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.0054, 0.0342, 1.0272, 1.1871, 1. 0.0064 0.0068 0.0068 0.0068 0.0068 0.0068 0.0068 0.0068 0.0051, 0.0051, 0.0052, 0.0051, 0.0052, | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| 0.0051, 0.0052, 0.0053 | -0.0301, | | | | 0.0299, | 0.0499, | 0.0998, |
| MR-RAPS2 1.000, | 0.0052, | 051, 0.0052, 0.0052, 0.005 | 0.0053, | 0.0053, | 0.0054, | 0.0054, | 0.0056, |
| MR-RAPS3 1.000, 1.000, 1.000, 0.0051, 0.0052, 0.0052, 0.0052, 0.0052, 0.0052, 0.00342, -0.00342, -0.00342, -0.0068 | 0.0053 | | | | 0.0055 | 0.0055 | 0.0057 |
| 1.0272, 1.1871, 1. 0.0064 0.0068 0.1 0.0068 0.1 | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| 0.0064 0.0068 0.0 MR-RAPS3 1.000, 1.000, 1.0 -0.1001, -0.0501, -0 0.0051, 0.0052, 0.0 | -0.0082, | | | | 0.0318, | 0.1437, | 0.0740, |
| MR-RAPS3 1.000, 1.000, 1.000, -0.1001, -0.0501, -0.0051, 0.0052, 0.005 | 1.1961, | | | | 0.5447, | 2.2004, | 0.7759, |
| -0.1001, -0.0501, -0 0.0051, 0.0052, 0.0 | 0.0066 | | | | 0.0061 | 0.007 | 0.0065 |
| 0.0051, 0.0052, 0. | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| | -0.0301, | | | | 0.0299, | 0.0499, | 0.0999, |
| 0.005 | 0.0052, | | | | 0.0054, | 0.0055, | 0.0056, |
| | 0.0052 | | | | 0.0053 | 0.0054 | 0.0056 |
| | 1.000, | | | | 1.000, | 1.000, | 1.000, |
| | -0.0301, | | | | 0.0299, | 0.0499, | 0.0998, |
| | 0.0053, 0.0053 | | | | 0.0055, 0.0055 | 0.0056, 0.0055 | 0.0058, 0.0057 |

Table S70: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the ideal case of q=0, and N=200000.

| ` | / / | | <u> </u> | | 1 / | | | | |
|--------------------|---------------------|-------------------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 1.000, | 1.000, | 0.536, | 0.081, | 0.551, | 0.999, | 1.000, | 1.000, |
| | -0.0989, | -0.0491, | -0.0291, | -0.0092, | 0.0000, | 0.0094, | 0.0292, | 0.0492, | 0.0990, |
| | 0.0053, | 0.0054, | 0.0055, | 0.0054, | 0.0050, | 0.0054, | 0.0055, | 0.0056, | 0.0057, |
| | 0.0042 | 0.0043 | 0.0043 | 0.0044 | 0.0043 | 0.0044 | 0.0045 | 0.0045 | 0.0046 |
| cML-MA-AIC-Profile | 1.000, | 1.000, | 1.000, | 0.536, | 0.081, | 0.551, | 0.999, | 1.000, | 1.000, |
| | -0.0992, | -0.0492, | -0.0292, | -0.0092, | 0.0000, | 0.0094, | 0.0293, | 0.0492, | 0.0992, |
| | 0.0053, | 0.0054, | 0.0055, | 0.0054, | 0.0050, | 0.0054, | 0.0055, | 0.0056, | 0.0058, |
| MAIC | 0.0042 | 0.0043 | 0.0043 | 0.0044 | 0.0043 | 0.0044 | 0.0045 | 0.0045 | 0.0047 |
| cML-AIC | 1.000, | 1.000, -0.0496, | 1.000, | 0.618, | 0.152, | 0.623, | 0.999, | 1.000, | 1.000, |
| | -0.0995, 0.0054, | 0.0056, | -0.0296, 0.0057, | -0.0096, 0.0057, | 0.0001, 0.0055, | 0.0098, 0.0057, | 0.0297, 0.0058, | 0.0497, 0.0058, | 0.0995, 0.0060, |
| | 0.0034, | 0.0030, | 0.0037, | 0.0037, | 0.0033, | 0.0037, | 0.0038, | 0.0038, | 0.0043 |
| cML-AIC-Profile | 1.000, | 1.000, | 1.000, | 0.618, | 0.152, | 0.622, | 0.999, | 1.000, | 1.000, |
| CALL THE TIOME | -0.0996, | -0.0496. | -0.0296, | -0.0096, | 0.0001, | 0.0098, | 0.0297, | 0.0498, | 0.0997, |
| | 0.0055, | 0.0057, | 0.0057, | 0.0057, | 0.0055, | 0.0057, | 0.0058, | 0.0058, | 0.0060, |
| | 0.0039 | 0.0039 | 0.004 | 0.004 | 0.004 | 0.0041 | 0.0041 | 0.0041 | 0.0043 |
| cML-MA-BIC | 1.000, | 1.000, | 1.000, | 0.788, | 0.048, | 0.760, | 1.000, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0036, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0038, | 0.0039, |
| | 0.0036 | 0.0036 | 0.0037 | 0.0037 | 0.0037 | 0.0037 | 0.0038 | 0.0038 | 0.0039 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 1.000, | 0.788, | 0.047, | 0.759, | 1.000, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0036, 0.0036 | 0.0037, 0.0036 | 0.0037, 0.0037 | 0.0037, 0.0037 | 0.0037, 0.0037 | 0.0037, 0.0037 | 0.0037, 0.0038 | 0.0038, 0.0038 | 0.0039, 0.004 |
| cML-BIC | 1.000, | 1.000, | 1.000, | 0.0037 | 0.0037 | 0.764, | 1.000, | 1.000, | 1.000, |
| CIVIL-DIC | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.704, | 0.0300, | 0.0500, | 0.0999, |
| | 0.0036, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0038, | 0.0039, |
| | 0.0036 | 0.0036 | 0.0036 | 0.0037 | 0.0037, | 0.0037 | 0.0038 | 0.0038 | 0.0039 |
| cML-BIC-Profile | 1.000, | 1.000, | 1.000, | 0.791, | 0.048, | 0.764, | 1.000, | 1.000, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0100, | 0.0300, | 0.0500, | 0.0999, |
| | 0.0036, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0038, | 0.0039, |
| | 0.0036 | 0.0036 | 0.0037 | 0.0037 | 0.0037 | 0.0037 | 0.0038 | 0.0038 | 0.0039 |
| MR-Mix | 0.859, | 0.809, | 0.731, | 0.404, | 0.072, | 0.361, | 0.725, | 0.806, | 0.844, |
| | -0.1121, | -0.0549, | -0.0326, | -0.0105, | 0.0004, | 0.0110, | 0.0321, | 0.0527, | 0.1021, |
| | 0.0340, | 0.0175, | 0.0120, | 0.0083, | 0.0075, | 0.0081, | 0.0120, | 0.0171, | 0.0307, |
| MD C MC | 0.1045 | 0.0315 | 0.0487 | 0.0341 | 0.1511 | 0.0297 | 0.0291 | 0.0874 | 0.123 |
| MR-ContMix | 1.000, -0.1074, | 1.000, -0.0616, | 1.000, -0.0411, | 0.597, -0.0156, | 0.106, 0.0001, | 0.613, 0.0156, | 1.000, 0.0414, | 1.000, 0.0623, | 1.000, 0.1091, |
| | 0.0042, | 0.0050, | 0.0062, | 0.0084, | 0.0001, | 0.0130, | 0.0064, | 0.0023, | 0.1091, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 1.000, | 1.000, | 0.766, | 0.061, | 0.745, | 1.000, | 1.000, | 1.000, |
| | -0.0998, | -0.0499, | -0.0300, | -0.0100, | 0.0000, | 0.0099, | 0.0299, | 0.0499, | 0.0998, |
| | 0.0038, | 0.0038, | 0.0038, | 0.0038, | 0.0039, | 0.0039, | 0.0039, | 0.0039, | 0.0040, |
| | 0.0036 | 0.0036 | 0.0037 | 0.0037 | 0.0037 | 0.0038 | 0.0038 | 0.0038 | 0.0039 |
| MR-PRESSO | 1.000, | 1.000, | 1.000, | 0.759, | 0.048, | 0.758, | 1.000, | 1.000, | 1.000, |
| | -0.0999, | -0.0499, | -0.0300, | -0.0100, | 0.0000, | 0.0099, | 0.0299, | 0.0499, | 0.0998, |
| | 0.0036, | 0.0036, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0038, |
| MR-IVW | 0.0036 1.000, | 0.0036 1.000, | 0.0036 1.000, | 0.0037 0.761, | 0.0037 0.043, | 0.0037 0.750, | 0.0037 1.000, | 0.0038 1.000, | 0.0039 1.000, |
| IVIIX-I V VV | -0.0999, | -0.0500, | -0.0300, | -0.0100, | -0.0001, | 0.730, | 0.0299, | 0.0499, | 0.0998, |
| | 0.0036, | 0.0036, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0233, | 0.0037, | 0.0038, |
| | 0.0036 | 0.0037 | 0.0037 | 0.0038 | 0.0038 | 0.0038 | 0.0039 | 0.0039 | 0.004 |
| MR-IVW-Oracle | 1.000, | 1.000, | 1.000, | 0.761, | 0.043, | 0.750, | 1.000, | 1.000, | 1.000, |
| | -0.0999, | -0.0500, | -0.0300, | -0.0100, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0998, |
| | 0.0036, | 0.0036, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0038, |
| | 0.0036 | 0.0037 | 0.0037 | 0.0038 | 0.0038 | 0.0038 | 0.0039 | 0.0039 | 0.004 |
| MR-Egger | 1.000, | 0.702, | 0.320, | 0.086, | 0.050, | 0.073, | 0.285, | 0.644, | 0.997, |
| | -0.0958, | -0.0481, | -0.0291, | -0.0100, | -0.0005, | 0.0091, | 0.0281, | 0.0472, | 0.0948, |
| | 0.0190, | 0.0193, | 0.0195, | 0.0197, | 0.0197, | 0.0198, | 0.0201, | 0.0203, | 0.0209, |
| MD Weighted Medico | 0.019 1.000, | 0.0194 1.000, | 0.0195 1.000, | 0.0197 0.435, | 0.0198 0.028, | 0.0199 0.466, | 0.0201 1.000, | 0.0204 1.000, | 0.021 1.000, |
| MR-Weighted-Median | -0.0993, | -0.0496, | -0.0297, | -0.0099, | 0.028, 0.0000, | 0.466, 0.0100, | 0.0298, | 0.0497, | 0.0993, |
| | 0.0046, | 0.0047, | 0.0047, | 0.0048. | 0.0000, | 0.0100, | 0.0298, | 0.0497, | 0.0993, |
| | 0.0040, | 0.0053 | 0.0047, | 0.0048, | 0.0048, | 0.0049, | 0.0049, | 0.0056 | 0.0050, |
| MR-Weighted-Mode | 1.000, | 0.988, | 0.661, | 0.053, | 0.0034 | 0.049, | 0.651, | 0.981, | 1.000, |
| | -0.0987, | -0.0492, | -0.0295, | -0.0097, | 0.0003, | 0.0102, | 0.0299, | 0.0496, | 0.0991, |
| | 0.0096, | 0.0098, | 0.0100, | 0.0101, | 0.0100, | 0.0101, | 0.0101, | 0.0101, | 0.0102, |
| | 0.0126 | 0.0128 | 0.013 | 0.0131 | 0.0131 | 0.0132 | 0.0134 | 0.0135 | 0.014 |
| MR-RAPS1 | 1.000, | 1.000, | 1.000, | 0.769, | 0.045, | 0.752, | 1.000, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0499, | 0.0999, |
| | 0.0036, | 0.0036, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0038, | 0.0038, |
| MD DADGS | 0.0037 | 0.0037 | 0.0037 | 0.0038 | 0.0038 | 0.0038 | 0.0039 | 0.0039 | 0.004 |
| MR-RAPS2 | 1.000, | 1.000, | 1.000, | 0.742, | 0.049, | 0.725, | 1.000, | 1.000, | 1.000, |
| | -0.0878, 0.1467, | -0.0640, 0.4223, | -0.0505, 0.9665, | -0.0100, 0.0038, | 0.0000, 0.0038, | 0.0100, 0.0038, | 0.0179, 0.7288, | 0.0693, 0.5024, | 0.0963, 0.2849, |
| | 0.1467, 0.0039 | 0.4223, | 0.9665, | 0.0038, | 0.0038, | 0.0038, | 0.7288, 0.0048 | 0.5024, | 0.2849, |
| MR-RAPS3 | 1.000, | 1.000, | 1.000, | 0.0039 | 0.0039 | 0.763, | 1.000, | 1.000, | 1.000, |
| CC TEXT-NIN | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.703, | 0.0300, | 0.0500, | 0.1000, |
| | 0.0036, | 0.0036, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0037, | 0.0038, | 0.1000, |
| | 0.0036 | 0.0036 | 0.0036 | 0.0037 | 0.0037, | 0.0037 | 0.0038 | 0.0038 | 0.0039 |
| 1 (D. D. 1 DC 1 | 1.000, | 1.000, | 1.000, | 0.761, | 0.055, | 0.740, | 1.000, | 1.000, | 1.000, |
| MR-RAPS4 | | | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1000, |
| MR-RAPS4 | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | | 0.0500, | | |
| MR-RAPS4 | -0.1000, 0.0037, | -0.0500, 0.0037, 0.0037 | 0.0037, | 0.0038, | 0.0038, | 0.0038, | 0.0038, | 0.0038, | 0.0039, |

Table S71: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE satisfied, q=0.2, and N=50000.

| // | <i>' '</i> | | | | , 1 | | | | |
|--------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|-------------------|--------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.975, | 0.695, | 0.157, | 0.077, | 0.182, | 0.704, | 0.974, | 1.000, |
| | -0.0970, | -0.0473, | -0.0274, | -0.0083, | 0.0008, | 0.0097, | 0.0288, | 0.0487, | 0.0985, |
| | 0.0128, | 0.0129, | 0.0128, | 0.0120, | 0.0118, | 0.0123, | 0.0133, | 0.0134, | 0.0136, |
| | 0.0104 | 0.0105 | 0.0106 | 0.0106 | 0.0106 | 0.0107 | 0.0109 | 0.011 | 0.0113 |
| cML-MA-AIC-Profile | 1.000, | 0.975, | 0.693, | 0.155, | 0.075, | 0.179, | 0.699, | 0.974, | 1.000, |
| | -0.0975, | -0.0474, | -0.0274, | -0.0083, | 0.0008, | 0.0097, | 0.0289, | 0.0488, | 0.0990, |
| | 0.0130, | 0.0130, | 0.0128, | 0.0120, | 0.0118, | 0.0123, | 0.0133, | 0.0135, | 0.0138, |
| | 0.0105 | 0.0106 | 0.0107 | 0.0107 | 0.0107 | 0.0108 | 0.011 | 0.0111 | 0.0114 |
| cML-AIC | 1.000, | 0.985, | 0.750, | 0.243, | 0.142, | 0.261, | 0.773, | 0.981, | 1.000, |
| | -0.0983, | -0.0486, | -0.0285, | -0.0090, | 0.0006, | 0.0101, | 0.0299, | 0.0500, | 0.0999, |
| | 0.0134, | 0.0135, | 0.0136, | 0.0133, | 0.0132, | 0.0135, | 0.0140, | 0.0141, | 0.0143, |
| M. AIG D. CI | 0.0095 | 0.0097 | 0.0097 | 0.0098 | 0.0098 | 0.0099 | 0.01 | 0.0101 | 0.0104 |
| cML-AIC-Profile | 1.000, -0.0986, | 0.984, -0.0486, | 0.747, | 0.240, -0.0090, | 0.139, 0.0006, | 0.259, 0.0101, | 0.767, 0.0299, | 0.981, 0.0501, | 1.000, 0.1003, |
| | 0.0135, | 0.0135, | -0.0286, 0.0137, | 0.0090, | 0.0006, | 0.0101, | 0.0299, | 0.0301, | 0.1003, |
| | 0.0133, | 0.0133, | 0.0137, | 0.0133, | 0.0132, | 0.0133, | 0.0140, | 0.0141, | 0.0144, |
| cML-MA-BIC | 1.000, | 0.999, | 0.915, | 0.182, | 0.053, | 0.192, | 0.910, | 1.000, | 1.000, |
| cine init bio | -0.0997, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0087, | 0.0088, | 0.0088, | 0.0089, | 0.0089, | 0.0090, | 0.0091, | 0.0091, | 0.0094, |
| | 0.0088 | 0.009 | 0.009 | 0.0091 | 0.0091 | 0.0092 | 0.0093 | 0.0093 | 0.0096 |
| cML-MA-BIC-Profile | 1.000, | 0.999, | 0.913, | 0.182, | 0.052, | 0.189, | 0.910, | 1.000, | 1.000, |
| | -0.0997, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0087, | 0.0088, | 0.0088, | 0.0089, | 0.0089, | 0.0090, | 0.0091, | 0.0091, | 0.0094, |
| | 0.0089 | 0.009 | 0.0091 | 0.0091 | 0.0092 | 0.0092 | 0.0093 | 0.0094 | 0.0096 |
| cML-BIC | 1.000, | 0.999, | 0.924, | 0.189, | 0.053, | 0.197, | 0.912, | 1.000, | 1.000, |
| | -0.0997, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0087, | 0.0088, | 0.0089, | 0.0089, | 0.0090, | 0.0090, | 0.0091, | 0.0092, | 0.0094, |
| | 0.0088 | 0.0089 | 0.009 | 0.009 | 0.0091 | 0.0091 | 0.0092 | 0.0093 | 0.0095 |
| cML-BIC-Profile | 1.000, | 0.999, | 0.922, | 0.188, | 0.052, | 0.196, | 0.912, | 1.000, | 1.000, |
| | -0.0997, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0087, | 0.0088, | 0.0089, | 0.0089, | 0.0090, | 0.0090, | 0.0091, | 0.0092, | 0.0094, |
| | 0.0088 | 0.0089 | 0.009 | 0.0091 | 0.0091 | 0.0091 | 0.0092 | 0.0093 | 0.0096 |
| MR-Mix | 1.000, | 0.899, | 0.384, | 0.031, | 0.011, | 0.024, | 0.340, | 0.858, | 1.000, |
| | -0.1108, | -0.0545, | -0.0327, | -0.0113, | -0.0007, | 0.0099, | 0.0308, | 0.0513, | 0.1009, |
| | 0.0129, | 0.0128, | 0.0128, | 0.0128, | 0.0129, | 0.0129, | 0.0131, | 0.0131, | 0.0130, |
| .m.cu. | 0.0193 | 0.0191 | 0.019 | 0.0189 | 0.0189 | 0.0189 | 0.0188 | 0.0187 | 0.0186 |
| MR-ContMix | 1.000, | 0.999, | 0.874, | 0.154, | 0.045, | 0.182, | 0.881, | 1.000, | 1.000, |
| | -0.0987, | -0.0491, | -0.0292, | -0.0094, | 0.0006, | 0.0105, | 0.0303, | 0.0502, | 0.0999, |
| | 0.0093, | 0.0093, | 0.0094, | 0.0095, | 0.0095, | 0.0095, | 0.0097, | 0.0098, | 0.0100, |
| MR-Lasso | NA 1.000, | NA 0.999, | NA 0.908, | NA 0.183, | NA 0.060, | NA 0.194, | NA 0.904, | NA 1.000, | NA 1.000, |
| WIX-Lasso | -0.0989, | -0.0492, | -0.0293, | -0.0095, | 0.000, | 0.194, | 0.904, | 0.0501, | 0.0997, |
| | 0.0089, | 0.0091, | 0.0090, | 0.0093, | 0.0004, | 0.0103, | 0.0302, | 0.0001, | 0.0997, |
| | 0.0088 | 0.0091, | 0.009 | 0.0091 | 0.0091 | 0.0092 | 0.0093 | 0.0093 | 0.0096 |
| MR-PRESSO | 1.000, | 0.995, | 0.878, | 0.236, | 0.094, | 0.239, | 0.885, | 0.997, | 1.000, |
| MIK I KLOSO | -0.0988, | -0.0492, | -0.0294, | -0.0095, | 0.0004, | 0.0103, | 0.0301, | 0.0499, | 0.0995, |
| | 0.0105, | 0.0106, | 0.0105, | 0.0106, | 0.0106, | 0.0106, | 0.0106, | 0.0106, | 0.0107, |
| | 0.0085 | 0.0086 | 0.0087 | 0.0088 | 0.0088 | 0.0088 | 0.0089 | 0.009 | 0.0093 |
| MR-IVW | 0.269, | 0.116, | 0.074, | 0.054, | 0.057, | 0.056, | 0.069, | 0.114, | 0.274, |
| | -0.0992, | -0.0494, | -0.0294, | -0.0095, | 0.0005, | 0.0104, | 0.0304, | 0.0503, | 0.1001, |
| | 0.0755, | 0.0755, | 0.0755, | 0.0755, | 0.0755, | 0.0755, | 0.0755, | 0.0755, | 0.0755, |
| | 0.074 | 0.074 | 0.074 | 0.074 | 0.074 | 0.074 | 0.074 | 0.074 | 0.0741 |
| MR-IVW-Oracle | 1.000, | 0.999, | 0.905, | 0.179, | 0.051, | 0.182, | 0.900, | 1.000, | 1.000, |
| | -0.0991, | -0.0494, | -0.0296, | -0.0097, | 0.0002, | 0.0102, | 0.0300, | 0.0499, | 0.0995, |
| | 0.0086, | 0.0087, | 0.0087, | 0.0088, | 0.0088, | 0.0089, | 0.0089, | 0.0090, | 0.0093, |
| | 0.009 | 0.0091 | 0.0092 | 0.0092 | 0.0093 | 0.0093 | 0.0094 | 0.0095 | 0.0097 |
| MR-Egger | 0.074, | 0.071, | 0.072, | 0.069, | 0.068, | 0.067, | 0.067, | 0.069, | 0.071, |
| | -0.0853, | -0.0437, | -0.0270, | -0.0103, | -0.0020, | 0.0063, | 0.0230, | 0.0396, | 0.0812, |
| | 0.3835, | 0.3834, | 0.3834, | 0.3834, | 0.3834, | 0.3834, | 0.3834, | 0.3834, | 0.3834, |
| MD Walle 136 P | 0.3612 | 0.3612 | 0.3612 | 0.3612 | 0.3612 | 0.3612 | 0.3612 | 0.3613 | 0.3613 |
| MR-Weighted-Median | 1.000, | 0.978, | 0.610, | 0.076, -0.0094, | 0.019, | 0.073, | 0.606, | 0.968, | 1.000, |
| | -0.0963, 0.0110, | -0.0480, 0.0109, | -0.0287, 0.0110, | -0.0094, 0.0110, | 0.0004, 0.0111, | 0.0101, 0.0112, | 0.0294, 0.0114, | 0.0488, | 0.0971, 0.0119, |
| | 0.0110, | 0.0109, | 0.0110, | 0.0110, | 0.0111, | 0.0112, | 0.0114, | 0.0116, 0.0135 | 0.0119, |
| MR-Weighted-Mode | 0.0128 | 0.0129 | 0.013 | 0.0131 | 0.0132 | 0.0132 | 0.0134 | 0.0133 | 0.0139 |
| WIK-Weighted-Wode | -0.0963, | -0.0480, | -0.0288, | -0.0095, | 0.009, | 0.023, | 0.0295, | 0.0489, | 0.990, |
| | 0.0173, | 0.0173, | 0.0176, | 0.0093, | 0.0004, | 0.0100, | 0.0293, | 0.0489, | 0.0974, |
| | 0.0173, | 0.0224 | 0.0176, | 0.0227 | 0.0179, | 0.0178, | 0.0231 | 0.0233 | 0.0133, |
| MR-RAPS1 | 0.265, | 0.0224 | 0.0220 | 0.049, | 0.0228 | 0.0229 | 0.063, | 0.108, | 0.265, |
| | -0.0994, | -0.0494, | -0.0294, | -0.0094, | 0.0006, | 0.0106, | 0.0306, | 0.0506, | 0.1006, |
| | 0.0735, | 0.0735, | 0.0735, | 0.0735, | 0.0735, | 0.0735, | 0.0736, | 0.0736, | 0.0736, |
| | 0.074 | 0.074 | 0.074 | 0.074 | 0.074 | 0.074 | 0.074 | 0.074 | 0.074 |
| MR-RAPS2 | 1.000, | 1.000, | 0.972, | 0.704, | 0.620, | 0.699, | 0.970, | 1.000, | 1.000, |
| | 0.0598, | 0.1228, | 0.1311, | 0.0071, | 0.0196, | 0.0482, | -0.0728, | -0.0804, | -0.0340, |
| | 1.5440, | 2.1237, | 1.8903, | 0.7392, | 0.8700, | 1.5487, | 2.4757, | 2.9620, | 1.5029, |
| | 0.0137 | 0.0138 | 0.0134 | 0.0123 | 0.0125 | 0.0132 | 0.0137 | 0.0139 | 0.0144 |
| MR-RAPS3 | 0.924, | 0.885, | 0.847, | 0.837, | 0.837, | 0.833, | 0.843, | 0.876, | 0.926, |
| | -0.2649, | -0.1287, | -0.0753, | -0.0235, | 0.0016, | 0.0261, | 0.0733, | 0.1178, | 0.2178, |
| | 0.1863, | 0.1926, | 0.1915, | 0.1886, | 0.1866, | 0.1843, | 0.1789, | 0.1728, | 0.1564, |
| | 0.0226 | 0.0222 | 0.0219 | 0.0215 | 0.0213 | 0.0211 | 0.0207 | 0.0203 | 0.0192 |
| MR-RAPS4 | 1.000, | 1.000, | 0.988, | 0.848, | 0.807, | 0.831, | 0.985, | 1.000, | 1.000, |
| MIK-IKAI 54 | | 0.0905, | 0.0856, | 0.0637, | 0.0443, | 0.0755, | 0.0051, | -0.0316, | -0.0231, |
| WIK-KAI 54 | 0.1534, | 0.0903, | 0.0050, | | | | | | |
| MK-KAI 54 | 0.1534, 0.9997, | 0.0903, | 0.9108, | 0.8849, | 0.8960, | 0.8876, | 0.9049, | 0.9254, | 0.9971, |

Table S72: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE satisfied, q=0.2, and N=100000.

| ((| <i>' '</i> | | <i>'</i> | | , I | | | | |
|-------------------------|--------------------|--------------------|--------------------|--------------------|----------|----------------|----------|-------------------|----------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 1.000, | 0.919, | 0.254, | 0.081, | 0.258, | 0.915, | 0.999, | 1.000, |
| | -0.0982, | -0.0484, | -0.0285, | -0.0090, | 0.0000, | 0.0091, | 0.0286, | 0.0485, | 0.0982, |
| | 0.0090, | 0.0091, | 0.0092, | 0.0087, | 0.0084, | 0.0088, | 0.0095, | 0.0096, | 0.0098, |
| | 0.0074 | 0.0075 | 0.0075 | 0.0075 | 0.0075 | 0.0076 | 0.0077 | 0.0078 | 0.008 |
| cML-MA-AIC-Profile | 1.000, | 1.000, | 0.918, | 0.251, | 0.080, | 0.257, | 0.914, | 0.999, | 1.000, |
| LIVIL-IVIA-AIC-I TOILIC | -0.0985, | -0.0485, | -0.0285, | -0.0090, | 0.0000, | 0.0091, | 0.0286, | 0.0486, | 0.0986, |
| | 0.0091, | 0.0092, | 0.0092, | 0.0087, | 0.0000, | 0.0088, | 0.0280, | 0.0480, | 0.0099, |
| | 0.0091, | 0.0092, | 0.0075 | 0.0087, | 0.0084, | 0.0038, | 0.0093, | 0.0078 | 0.0099, |
| -MI AIC | | | | | | | | | |
| cML-AIC | 1.000, | 1.000, | 0.949, | 0.337, | 0.132, | 0.346, | 0.939, | 0.999, | 1.000, |
| | -0.0992, | -0.0493, | -0.0294, | -0.0096, | 0.0000, | 0.0096, | 0.0294, | 0.0494, | 0.0992, |
| | 0.0095, | 0.0095, | 0.0096, | 0.0094, | 0.0093, | 0.0095, | 0.0099, | 0.0100, | 0.0104 |
| | 0.0068 | 0.0068 | 0.0069 | 0.0069 | 0.007 | 0.007 | 0.0071 | 0.0071 | 0.0073 |
| cML-AIC-Profile | 1.000, | 1.000, | 0.948, | 0.336, | 0.128, | 0.343, | 0.938, | 0.999, | 1.000, |
| | -0.0995, | -0.0493, | -0.0294, | -0.0096, | 0.0000, | 0.0096, | 0.0294, | 0.0494, | 0.0994 |
| | 0.0095, | 0.0095, | 0.0096, | 0.0094, | 0.0093, | 0.0095, | 0.0099, | 0.0100, | 0.0104 |
| | 0.0068 | 0.0069 | 0.0069 | 0.007 | 0.007 | 0.007 | 0.0071 | 0.0072 | 0.0074 |
| cML-MA-BIC | 1.000, | 1.000, | 0.999, | 0.365, | 0.048, | 0.343, | 0.998, | 1.000, | 1.000, |
| | -0.0999, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0499, | 0.0999 |
| | 0.0063, | 0.0063, | 0.0064, | 0.0064, | 0.0064, | 0.0065, | 0.0065, | 0.0066, | 0.0068 |
| | 0.0062 | 0.0063 | 0.0064 | 0.0064 | 0.0064 | 0.0065 | 0.0065 | 0.0066 | 0.0068 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.998, | 0.364, | 0.048, | 0.340, | 0.998, | | 1.000, |
| MIL-MA-DIC-PIONE | | | 0.998, | | | | | 1.000, | |
| | -0.0999, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0499, | 0.0999 |
| | 0.0063, | 0.0063, | 0.0064, | 0.0064, | 0.0064, | 0.0065, | 0.0065, | 0.0066, | 0.0068 |
| | 0.0063 | 0.0063 | 0.0064 | 0.0064 | 0.0065 | 0.0065 | 0.0065 | 0.0066 | 0.0068 |
| cML-BIC | 1.000, | 1.000, | 0.999, | 0.374, | 0.051, | 0.345, | 0.998, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0499, | 0.0999 |
| | 0.0062, | 0.0063, | 0.0063, | 0.0064, | 0.0064, | 0.0064, | 0.0065, | 0.0066, | 0.0068 |
| | 0.0062 | 0.0063 | 0.0063 | 0.0064 | 0.0064 | 0.0064 | 0.0065 | 0.0066 | 0.0067 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.999, | 0.373, | 0.051, | 0.343, | 0.998, | | 1.000, |
| CHIL-DIC-LIGHE | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.001, | 0.343, 0.0100, | 0.998, | 1.000, 0.0499, | 0.0999 |
| | | | | | | | | 0.0499, | 0.0999 |
| | 0.0062, | 0.0063, | 0.0063, | 0.0064, | 0.0064, | 0.0064, | 0.0065, | 0.0066, | 0.0068 |
| 100.10 | 0.0062 | 0.0063 | 0.0063 | 0.0064 | 0.0064 | 0.0064 | 0.0065 | 0.0066 | 0.0067 |
| MR-Mix | 1.000, | 0.983, | 0.629, | 0.041, | 0.004, | 0.036, | 0.603, | 0.973, | 1.000, |
| | -0.1107, | -0.0545, | -0.0326, | -0.0110, | -0.0003, | 0.0104, | 0.0313, | 0.0518, | 0.1014 |
| | 0.0095, | 0.0096, | 0.0096, | 0.0095, | 0.0094, | 0.0095, | 0.0095, | 0.0096, | 0.0099 |
| | 0.0152 | 0.015 | 0.015 | 0.015 | 0.0149 | 0.0149 | 0.0149 | 0.0149 | 0.0148 |
| MR-ContMix | 1.000, | 1.000, | 0.997, | 0.332, | 0.056, | 0.327, | 0.991, | 1.000, | 1.000, |
| mit commix | -0.0995, | -0.0498, | -0.0299, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0498, | 0.0996 |
| | 0.0066, | 0.0067, | 0.0068, | 0.0068, | 0.0068, | 0.0069, | 0.0069, | 0.0070, | 0.0072 |
| | | | | | | | | | |
| 100.1 | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 1.000, | 0.996, | 0.368, | 0.067, | 0.341, | 0.998, | 1.000, | 1.000, |
| | -0.0996, | -0.0498, | -0.0299, | -0.0100, | 0.0000, | 0.0099, | 0.0298, | 0.0498, | 0.0996 |
| | 0.0066, | 0.0066, | 0.0066, | 0.0067, | 0.0068, | 0.0068, | 0.0068, | 0.0069, | 0.0070 |
| | 0.0062 | 0.0063 | 0.0064 | 0.0064 | 0.0065 | 0.0065 | 0.0066 | 0.0066 | 0.0068 |
| MR-PRESSO | 1.000, | 0.991, | 0.953, | 0.453, | 0.198, | 0.429, | 0.957, | 0.993, | 1.000, |
| WIR T RESSO | -0.0993, | -0.0496, | -0.0298, | -0.0099, | 0.0000, | 0.0100, | 0.0299, | 0.0497, | 0.0994 |
| | 0.0117, | 0.0116, | 0.0115, | 0.0114, | 0.0000, | 0.0100, | 0.0255, | 0.0113, | 0.0112 |
| | | | | | | | | | |
| | 0.006 | 0.0061 | 0.0061 | 0.0062 | 0.0062 | 0.0062 | 0.0063 | 0.0063 | 0.0065 |
| MR-IVW | 0.277, | 0.127, | 0.078, | 0.060, | 0.062, | 0.073, | 0.094, | 0.121, | 0.296, |
| | -0.0987, | -0.0487, | -0.0287, | -0.0087, | 0.0013, | 0.0112, | 0.0312, | 0.0512, | 0.1012 |
| | 0.0778, | 0.0777, | 0.0777, | 0.0777, | 0.0777, | 0.0777, | 0.0777, | 0.0777, | 0.0776 |
| | 0.0737 | 0.0737 | 0.0737 | 0.0737 | 0.0737 | 0.0737 | 0.0737 | 0.0737 | 0.0737 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.999, | 0.345, | 0.044, | 0.327, | 0.997, | 1.000, | 1.000, |
| min i v v oracie | -0.0996, | -0.0498, | -0.0299, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0498, | 0.0996 |
| | | 0.0062, | | | | | | | |
| | 0.0062, | | 0.0063, | 0.0063, | 0.0064, | 0.0064, | 0.0064, | 0.0065, | 0.0067 |
| 100.7 | 0.0063 | 0.0064 | 0.0065 | 0.0065 | 0.0066 | 0.0066 | 0.0067 | 0.0067 | 0.0069 |
| MR-Egger | 0.067, | 0.063, | 0.058, | 0.053, | 0.052, | 0.049, | 0.047, | 0.045, | 0.055, |
| | -0.1045, | -0.0589, | -0.0406, | -0.0224, | -0.0133, | -0.0041, | 0.0141, | 0.0323, | 0.0779 |
| | 0.3841, | 0.3840, | 0.3840, | 0.3839, | 0.3839, | 0.3839, | 0.3839, | 0.3839, | 0.3838 |
| | 0.3757 | 0.3757 | 0.3757 | 0.3757 | 0.3757 | 0.3757 | 0.3757 | 0.3757 | 0.3757 |
| MR-Weighted-Median | 1.000, | 1.000, | 0.922, | 0.153, | 0.033, | 0.142, | 0.898, | 1.000, | 1.000, |
| | -0.0982, | -0.0491, | -0.0295, | -0.0099, | -0.0001, | 0.0098, | 0.0294, | 0.0491, | 0.0981 |
| | 0.0080, | 0.0082, | 0.0082, | 0.0083, | 0.0083, | 0.0083, | 0.0084, | 0.0086, | 0.0088 |
| | 0.0080, | 0.0082, | 0.0082, | | 0.0083, | 0.0083, | 0.0084, | | 0.0088 |
| MD Walaka 136 1 | | | | 0.0093 | | | | 0.0095 | |
| MR-Weighted-Mode | 1.000, | 0.918, | 0.439, | 0.036, | 0.005, | 0.034, | 0.433, | 0.874, | 1.000, |
| | -0.0987, | -0.0493, | -0.0297, | -0.0101, | -0.0002, | 0.0098, | 0.0295, | 0.0492, | 0.0984 |
| | 0.0122, | 0.0122, | 0.0125, | 0.0124, | 0.0125, | 0.0127, | 0.0129, | 0.0130, | 0.0136 |
| | 0.0158 | 0.016 | 0.0161 | 0.0163 | 0.0163 | 0.0164 | 0.0165 | 0.0167 | 0.0172 |
| MR-RAPS1 | 0.280, | 0.112, | 0.075, | 0.060, | 0.058, | 0.063, | 0.077, | 0.118, | 0.290, |
| ** | -0.0983, | -0.0483, | -0.0283, | -0.0083, | 0.0017, | 0.0117, | 0.0317, | 0.0517, | 0.1017 |
| | 0.0751, | 0.0751, | 0.0751, | 0.0751, | 0.0751, | 0.0751, | 0.0751, | 0.0751, | 0.0751 |
| | 0.0731, | 0.0735 | 0.0735 | 0.0735 | 0.0735 | 0.0731, | 0.0731, | 0.0735 | 0.0736 |
| MD DARCO | | | | | | | | | |
| MR-RAPS2 | 0.999, | 1.000, | 0.999, | 0.810, | 0.702, | 0.808, | 1.000, | 1.000, | 1.000, |
| | 0.4861, | 0.1562, | 0.0588, | 0.0250, | 0.0143, | 0.0186, | -0.0578, | -0.0977, | -0.214 |
| | 2.3093, | 1.9727, | 1.2278, | 0.7413, | 0.7838, | 0.7571, | 1.3944, | 1.3736, | 1.8828 |
| | 0.0294 | 0.0089 | 0.0089 | 0.0088 | 0.0092 | 0.0089 | 0.0092 | 0.0092 | 0.0103 |
| MR-RAPS3 | 0.953, | 0.908, | 0.907, | 0.897, | 0.904, | 0.900, | 0.883, | 0.906, | 0.943, |
| MIN IN IN ISS | -0.2591, | -0.1249, | -0.0723, | -0.0214, | 0.0034, | 0.0276, | 0.0741, | 0.1182, | 0.2172 |
| | | | | | | | | | |
| | 0.1907, | 0.1963, | 0.1951, | 0.1920, | 0.1900, | 0.1876, | 0.1821, | 0.1760, | 0.1595 |
| | 0.0158 | 0.0155 | 0.0153 | 0.015 | 0.0149 | 0.0147 | 0.0145 | 0.0142 | 0.0135 |
| | 1.000, | 1.000, | 0.999, | 0.934, | 0.885, | 0.920, | 1.000, | 1.000, | 1.000, |
| MR-RAPS4 | | | | | 0.0572, | 0.0582, | -0.0247, | -0.0852, | -0.2750 |
| MR-RAPS4 | 0.4068. | 0.2108. | 0.1523. | 0.0743. | | | -0.0247. | -0.0632. | -0.27.30 |
| MR-RAPS4 | 0.4068, 0.7992, | 0.2108, 0.8180, | 0.1523, 0.8198, | 0.0743, 0.8509, | 0.8755, | 0.8647, | 0.8465, | 0.8816, | 0.8467, |

Table S73: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE satisfied, q=0.2, and N=200000.

| , , | ′ / | | | | , I | | | | |
|--------------------|---|--|---|--|--|--|--|--|--|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 1.000, | 0.995, | 0.438, | 0.075, | 0.413, | 0.991, | 1.000, | 1.000, |
| | -0.0988, | -0.0491, | -0.0291, | -0.0094, | -0.0002, | 0.0090, | 0.0288, | 0.0487, | 0.0985, |
| | 0.0064, | 0.0065, | 0.0066, | 0.0063, | 0.0059, | 0.0063, | 0.0067, | 0.0067, | 0.0069, |
| | 0.0052 | 0.0053 | 0.0053 | 0.0053 | 0.0053 | 0.0054 | 0.0055 | 0.0055 | 0.0057 |
| cML-MA-AIC-Profile | 1.000, | 1.000, | 0.995, | 0.438, | 0.075, | 0.413, | 0.991, | 1.000, | 1.000, |
| | -0.0991, | -0.0491, | -0.0292, | -0.0094, | -0.0002, | 0.0090, | 0.0288, | 0.0488, | 0.0987, |
| | 0.0065, | 0.0066, | 0.0066, | 0.0063, | 0.0059, | 0.0063, | 0.0067, | 0.0068, | 0.0069, |
| M. AIC | 0.0052 | 0.0053 | 0.0053 | 0.0053 | 0.0053 | 0.0054 | 0.0055 | 0.0055 | 0.0057 |
| cML-AIC | 1.000, | 1.000, | 0.996, | 0.507, | 0.151, | 0.495, | 0.995, | 1.000, | 1.000, |
| | -0.0995, 0.0067, | -0.0497, 0.0067, | -0.0297, 0.0069, | -0.0098, 0.0068, | -0.0002, 0.0066, | 0.0094, 0.0068, | 0.0293, 0.0070, | 0.0492, 0.0071, | 0.0991, 0.0072, |
| | 0.0067, | 0.0067, | 0.0069, | 0.0008, | 0.0066, | 0.0068, | 0.0070, | 0.0071, | 0.0072, |
| cML-AIC-Profile | 1.000, | 1.000, | 0.996, | 0.505, | 0.151, | 0.495, | 0.995, | 1.000, | 1.000, |
| CHE THE HOME | -0.0997, | -0.0497, | -0.0297, | -0.0098, | -0.0002, | 0.0094, | 0.0293, | 0.0493, | 0.0993, |
| | 0.0068, | 0.0067, | 0.0069, | 0.0068, | 0.0066, | 0.0068, | 0.0070, | 0.0071, | 0.0072, |
| | 0.0048 | 0.0049 | 0.0049 | 0.0049 | 0.0049 | 0.005 | 0.005 | 0.0051 | 0.0052 |
| cML-MA-BIC | 1.000, | 1.000, | 1.000, | 0.608, | 0.046, | 0.581, | 1.000, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0044, | 0.0044, | 0.0045, | 0.0045, | 0.0045, | 0.0046, | 0.0046, | 0.0047, | 0.0048, |
| | 0.0044 | 0.0045 | 0.0045 | 0.0045 | 0.0046 | 0.0046 | 0.0046 | 0.0047 | 0.0048 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 1.000, | 0.608, | 0.046, | 0.579, | 1.000, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0044, | 0.0044, | 0.0045, | 0.0045, | 0.0045, | 0.0046, | 0.0046, | 0.0047, | 0.0048, |
| Aff. DIC | 0.0044 | 0.0045 | 0.0045 | 0.0045 | 0.0046 | 0.0046 | 0.0046 | 0.0047 | 0.0048 |
| cML-BIC | 1.000, | 1.000, | 1.000, | 0.615, | 0.048, | 0.581, | 1.000, | 1.000, | 1.000, |
| | -0.1000, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0044, 0.0044 | 0.0045, 0.0044 | 0.0045, 0.0045 | 0.0045, 0.0045 | 0.0045, 0.0045 | 0.0046, 0.0045 | 0.0046, 0.0046 | 0.0047, 0.0046 | 0.0048, 0.0048 |
| cML-BIC-Profile | 1.000, | 1.000, | 1.000, | 0.613, | 0.0045 | 0.0045 | 1.000, | 1.000, | 1.000, |
| CMIT-DIC-LIGHIG | -0.1000, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.581, 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0044, | 0.0045, | 0.0045, | 0.0045, | 0.0001, | 0.0033, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0044 | 0.0045 | 0.0045 | 0.0045 | 0.0045 | 0.0046 | 0.0046 | 0.0046 | 0.0048 |
| MR-Mix | 0.998, | 0.993, | 0.866, | 0.083, | 0.005, | 0.091, | 0.842, | 0.994, | 1.000, |
| | -0.1105, | -0.0543, | -0.0324, | -0.0108, | 0.0000, | 0.0107, | 0.0318, | 0.0523, | 0.1018, |
| | 0.0079, | 0.0079, | 0.0079, | 0.0079, | 0.0079, | 0.0080, | 0.0081, | 0.0081, | 0.0081, |
| | 0.0119 | 0.0118 | 0.0118 | 0.0117 | 0.0117 | 0.0116 | 0.0116 | 0.0116 | 0.0115 |
| MR-ContMix | 1.000, | 1.000, | 1.000, | 0.589, | 0.051, | 0.559, | 1.000, | 1.000, | 1.000, |
| | -0.0999, | -0.0500, | -0.0300, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0498, | 0.0998, |
| | 0.0045, | 0.0045, | 0.0046, | 0.0046, | 0.0046, | 0.0047, | 0.0047, | 0.0048, | 0.0050, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 1.000, | 1.000, | 0.597, | 0.059, | 0.587, | 1.000, | 1.000, | 1.000, |
| | -0.0998, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0499, | 0.0997, |
| | 0.0046, | 0.0046, | 0.0046, | 0.0047, | 0.0047, | 0.0047, | 0.0047, | 0.0048, | 0.0050, |
| MD DDECCO | 0.0044 | 0.0045 | 0.0045 | 0.0046 0.646, | 0.0046 | 0.0046 | 0.0046 | 0.0047 | 0.0048 |
| MR-PRESSO | 0.998, -0.0996, | 0.982, -0.0498, | 0.941, -0.0299, | -0.0100, | 0.341, 0.0000, | 0.638, 0.0100, | 0.939, 0.0299, | 0.988, 0.0498, | 1.000, 0.0996, |
| | 0.0149, | 0.0145, | 0.0144, | 0.0144, | 0.0000, | 0.0100, | 0.0299, | 0.0498, | 0.0336, |
| | 0.0045 | 0.0045 | 0.0046 | 0.0046 | 0.0046 | 0.0046 | 0.0046 | 0.0047 | 0.0130, |
| MR-IVW | 0.304, | 0.116, | 0.084, | 0.055, | 0.054, | 0.063, | 0.075, | 0.113, | 0.272, |
| | -0.1005, | -0.0504, | -0.0304, | -0.0104, | -0.0003, | 0.0097, | 0.0297, | 0.0497, | 0.0998, |
| | 0.0758, | 0.0758, | 0.0758, | 0.0758, | 0.0758, | 0.0758, | 0.0758, | 0.0758, | 0.0758, |
| | 0.0739 | 0.0739 | 0.0739 | 0.0739 | 0.0739 | 0.0739 | 0.0739 | 0.0739 | 0.0739 |
| MR-IVW-Oracle | 1.000, | 1.000, | 1.000, | 0.594, | 0.042, | 0.563, | 1.000, | 1.000, | 1.000, |
| | -0.0999, | -0.0500, | -0.0300, | -0.0100, | -0.0001, | 0.0099, | 0.0299, | 0.0498, | 0.0997, |
| | 0.0044, | 0.0044, | 0.0045, | 0.0045, | 0.0045, | 0.0045, | 0.0046, | 0.0046, | 0.0048, |
| | 0.0045 | 0.0046 | 0.0046 | 0.0046 | 0.0047 | 0.0047 | 0.0047 | 0.0048 | 0.0049 |
| MR-Egger | 0.069, | 0.074, | 0.068, | 0.070, | 0.069, | 0.071, | 0.068, | 0.065, | 0.062, |
| | -0.1074, | -0.0596, | -0.0405, | -0.0214, | -0.0119, | -0.0023, | 0.0168, | 0.0358, | 0.0836, |
| | 0.3914, | 0.3913, | 0.3913, | 0.3912, | 0.3912, | 0.3912, | 0.3912, | 0.3911, | 0.3911, |
| 4D W | 0.3839 | 0.3838 | 0.3838 | 0.3838 | 0.3838 | 0.3838 | 0.3838 | 0.3838 | 0.3837 |
| MR-Weighted-Median | 1.000, | 1.000, | 0.998, | 0.310, | 0.017, | 0.297, | 0.998, | 1.000, | 1.000, |
| | -0.0991, | -0.0496, | -0.0298, | -0.0100, | 0.0000, | 0.0099, | 0.0297, | 0.0495, | 0.0990, |
| | 0.0056, 0.0064 | 0.0057, 0.0065 | 0.0057, 0.0065 | 0.0057, 0.0066 | 0.0058, 0.0066 | 0.0058, 0.0066 | 0.0058, 0.0067 | 0.0059, 0.0067 | 0.0061, 0.0069 |
| MR-Weighted-Mode | 1.000, | 0.0065 | 0.0065 | 0.0000 | 0.008, | 0.0000 | 0.765, | 0.0067 | 1.000, |
| WIK-Weighted-Wode | | | -0.0297, | -0.0100, | 0.0000, | 0.0100, | 0.703, | 0.0495, | 0.0991, |
| | | -0.0497 | | | 0.0000, | 0.0092, | | 0.0094, | 0.0093, |
| | -0.0992, | -0.0497, 0.0089, | | 0.0090. | 0.0090. | 0.0092. | 0.0093. | | |
| | | -0.0497, 0.0089, 0.0114 | 0.0089, 0.0115 | 0.0090, 0.0116 | 0.0090, | 0.0092, | 0.0093, 0.0118 | 0.0119 | 0.0122 |
| MR-RAPS1 | -0.0992, 0.0089, | 0.0089, | 0.0089, | | | | | | |
| MR-RAPS1 | -0.0992, 0.0089, 0.0113 | 0.0089, 0.0114 0.113, -0.0511, | 0.0089, 0.0115 | 0.0116 0.053, -0.0111, | 0.0116 | 0.0117 | 0.0118 | 0.0119 | 0.0122 |
| MR-RAPS1 | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, | 0.0089, 0.0114 0.113, -0.0511, 0.0741, | 0.0089, 0.0115 0.075, -0.0311, 0.0741, | 0.0116 0.053, -0.0111, 0.0741, | 0.0116 0.053, -0.0011, 0.0741, | 0.0117 0.055, 0.0089, 0.0741, | 0.0118 0.080, 0.0289, 0.0741, | 0.0119 0.105, 0.0489, 0.0741, | 0.0122 0.255, 0.0989, 0.0741, |
| | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 | 0.0089, 0.0114 0.113, -0.0511, 0.0741, 0.0735 | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 | 0.0116 0.053, -0.0111, 0.0741, 0.0735 | 0.0116 0.053, -0.0011, 0.0741, 0.0735 | 0.0117 0.055, 0.0089, 0.0741, 0.0735 | 0.0118 0.080, 0.0289, 0.0741, 0.0735 | 0.0119 0.105, 0.0489, 0.0741, 0.0735 | 0.0122 0.255, 0.0989, 0.0741, 0.0735 |
| MR-RAPS1 MR-RAPS2 | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 1.000, | 0.0089, 0.0114 0.113, -0.0511, 0.0741, 0.0735 1.000, | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 1.000, | 0.0116 0.053, -0.0111, 0.0741, 0.0735 0.890, | 0.0116 0.053, -0.0011, 0.0741, 0.0735 0.673, | 0.0117 0.055, 0.0089, 0.0741, 0.0735 0.872, | 0.0118 0.080, 0.0289, 0.0741, 0.0735 1.000, | 0.0119 0.105, 0.0489, 0.0741, 0.0735 1.000, | 0.0122 0.255, 0.0989, 0.0741, 0.0735 |
| | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 1.000, 0.4682, | 0.0089, 0.0114 0.113, -0.0511, 0.0741, 0.0735 1.000, 0.1663, | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 1.000, 0.1104, | 0.0116 0.053, -0.0111, 0.0741, 0.0735 0.890, 0.1789, | 0.0116 0.053, -0.0011, 0.0741, 0.0735 0.673, 0.2385, | 0.0117 0.055, 0.0089, 0.0741, 0.0735 0.872, 0.1537, | 0.0118 0.080, 0.0289, 0.0741, 0.0735 1.000, 0.2206, | 0.0119 0.105, 0.0489, 0.0741, 0.0735 1.000, 0.2140, | 0.0122 0.255, 0.0989, 0.0741, 0.0735 1.000, 0.1425, |
| | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 1.000, 0.4682, 2.3725, | 0.0089, 0.0114 0.113, -0.0511, 0.0741, 0.0735 1.000, 0.1663, 0.6543, | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 1.000, 0.1104, 0.9236, | 0.0116 0.053, -0.0111, 0.0741, 0.0735 0.890, 0.1789, 0.7864, | 0.0116 0.053, -0.0011, 0.0741, 0.0735 0.673, 0.2385, 1.1421, | 0.0117 0.055, 0.0089, 0.0741, 0.0735 0.872, 0.1537, 0.9202, | 0.0118 0.080, 0.0289, 0.0741, 0.0735 1.000, 0.2206, 1.0497, | 0.0119 0.105, 0.0489, 0.0741, 0.0735 1.000, 0.2140, 1.1501, | 0.0122 0.255, 0.0989, 0.0741, 0.0735 1.000, 0.1425, 1.4071, |
| MR-RAPS2 | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 1.000, 0.4682, 2.3725, 0.0083 | 0.0089, 0.0114 0.113, -0.0511, 0.0741, 0.0735 1.000, 0.1663, 0.6543, 0.0056 | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 1.000, 0.1104, 0.9236, 0.0057 | 0.0116 0.053, -0.0111, 0.0741, 0.0735 0.890, 0.1789, 0.7864, 0.0057 | 0.0116 0.053, -0.0011, 0.0741, 0.0735 0.673, 0.2385, 1.1421, 0.0062 | 0.0117 0.055, 0.0089, 0.0741, 0.0735 0.872, 0.1537, 0.9202, 0.0061 | 0.0118 0.080, 0.0289, 0.0741, 0.0735 1.000, 0.2206, 1.0497, 0.0063 | 0.0119 0.105, 0.0489, 0.0741, 0.0735 1.000, 0.2140, 1.1501, 0.0069 | 0.0122 0.255, 0.0989, 0.0741, 0.0735 1.000, 0.1425, 1.4071, 0.0069 |
| | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 1.000, 0.4682, 2.3725, 0.0083 | 0.0089, 0.0114 0.113, -0.0511, 0.0741, 0.0735 1.000, 0.1663, 0.6543, 0.0056 | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 1.000, 0.1104, 0.9236, 0.0057 | 0.0116 0.053, -0.0111, 0.0741, 0.0735 0.890, 0.1789, 0.7864, 0.0057 | 0.0116 0.053, -0.0011, 0.0741, 0.0735 0.673, 0.2385, 1.1421, 0.0062 0.927, | 0.0117 0.055, 0.0089, 0.0741, 0.0735 0.872, 0.1537, 0.9202, 0.0061 0.920, | 0.0118 0.080, 0.0289, 0.0741, 0.0735 1.000, 0.2206, 1.0497, 0.0063 0.937, | 0.0119 0.105, 0.0489, 0.0741, 0.0735 1.000, 0.2140, 1.1501, 0.0069 0.924, | 0.0122 0.255, 0.0989, 0.0741, 0.0735 1.000, 0.1425, 1.4071, 0.0069 |
| MR-RAPS2 | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 1.000, 0.4682, 2.3725, 0.0083 0.962, -0.2666, | 0.0089, 0.0114 0.113, -0.0511, 0.0735 1.000, 0.1663, 0.6543, 0.0056 0.929, -0.1304, | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 1.000, 0.1104, 0.9236, 0.0057 0.911, -0.0771, | 0.0116 0.053, -0.0111, 0.0741, 0.0735 0.890, 0.1789, 0.7864, 0.0057 0.924, -0.0253, | 0.0116 0.053, -0.0011, 0.0741, 0.0735 0.673, 0.2385, 1.1421, 0.0062 0.927, -0.0002, | 0.0117 0.055, 0.0089, 0.0741, 0.0735 0.872, 0.1537, 0.9202, 0.0061 0.920, 0.0243, | 0.0118 0.080, 0.0289, 0.0741, 0.0735 1.000, 0.2206, 1.0497, 0.0063 0.937, 0.0715, | 0.0119 0.105, 0.0489, 0.0741, 0.0735 1.000, 0.2140, 1.1501, 0.0069 0.924, 0.1161, | 0.0122 0.255, 0.0989, 0.0741, 0.0735 1.000, 0.1425, 1.4071, 0.0069 0.960, 0.2162, |
| MR-RAPS2 | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 1.000, 0.4682, 2.3725, 0.0083 0.962, -0.2666, 0.1861, | 0.0089, 0.0114 0.113, -0.0511, 0.0741, 0.0735 1.000, 0.1663, 0.6543, 0.0056 0.929, -0.1304, 0.1924, | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 1.000, 0.1104, 0.9236, 0.0057 0.911, -0.0771, 0.1914, | 0.0116 0.053, -0.0111, 0.0741, 0.0735 0.890, 0.1789, 0.7864, 0.0057 0.924, -0.0253, 0.1886, | 0.0116 0.053, -0.0011, 0.0741, 0.0735 0.673, 0.2385, 1.1421, 0.0062 0.927, -0.0002, 0.1866, | 0.0117 0.055, 0.0089, 0.0741, 0.0735 0.872, 0.1537, 0.9202, 0.0061 0.920, 0.0243, 0.1843, | 0.0118 0.080, 0.0289, 0.0741, 0.0735 1.000, 0.2206, 1.0497, 0.0063 0.937, 0.0715, 0.1789, | 0.0119 0.105, 0.0489, 0.0741, 0.0735 1.000, 0.2140, 1.1501, 0.0069 0.924, 0.1161, 0.1728, | 0.0122 0.255, 0.0989, 0.0741, 0.0735 1.000, 0.1425, 1.4071, 0.0069 0.960, 0.2162, 0.1563, |
| MR-RAPS2 MR-RAPS3 | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 1.000, 0.4682, 2.3725, 0.0083 0.962, -0.2666, 0.1861, 0.0113 | 0.0089, 0.0114 0.113, -0.0511, 0.0741, 0.0735 1.000, 0.1663, 0.6543, 0.0056 0.929, -0.1304, 0.1924, 0.0111 | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 1.000, 0.1104, 0.9236, 0.0057 0.911, -0.0771, 0.1914, 0.0109 | 0.0116 0.053, -0.0111, 0.0741, 0.0735 0.890, 0.1789, 0.7864, 0.0057 0.924, -0.0253, 0.1886, 0.0107 | 0.0116 0.053, -0.0011, 0.0741, 0.0735 0.673, 0.2385, 1.1421, 0.0062 0.927, -0.0002, 0.1866, 0.0106 | 0.0117 0.055, 0.0089, 0.0741, 0.0735 0.872, 0.1537, 0.9202, 0.0061 0.920, 0.0243, 0.1843, 0.0105 | 0.0118 0.080, 0.0289, 0.0741, 0.0735 1.000, 0.2206, 1.0497, 0.0063 0.937, 0.0715, 0.1789, 0.0103 | 0.0119 0.105, 0.0489, 0.0741, 0.0735 1.000, 0.2140, 1.1501, 0.0069 0.924, 0.1161, 0.1728, 0.0101 | 0.0122 0.255, 0.0989, 0.0741, 0.0735 1.000, 0.1425, 1.4071, 0.0069 0.2162, 0.1563, 0.0096 |
| MR-RAPS2 | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 1.000, 0.4682, 2.3725, 0.0083 0.962, -0.2666, 0.1861, 0.0113 | 0.0089, 0.0114 0.113, -0.0511, 0.0741, 0.0735 1.000, 0.1663, 0.05643, 0.0056 0.929, -0.1304, 0.1924, 0.0111 | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 1.000, 0.1104, 0.9236, 0.0057 0.911, -0.0771, 0.1914, 0.0109 | 0.0116 0.053, -0.0111, 0.0741, 0.0735 0.890, 0.1789, 0.7864, 0.0057 0.924, -0.0253, 0.1886, 0.0107 | 0.0116 0.053, -0.0011, 0.0741, 0.0735 0.673, 0.2385, 1.1421, 0.0062 0.927, -0.0002, 0.1866, 0.0106 | 0.0117 0.055, 0.0089, 0.0741, 0.0735 0.872, 0.1537, 0.9202, 0.0061 0.920, 0.0243, 0.1843, 0.0105 | 0.0118 0.080, 0.0289, 0.0741, 0.0735 1.000, 0.2206, 1.0497, 0.0063 0.937, 0.0715, 0.1789, 0.0103 | 0.0119 0.105, 0.0489, 0.0741, 0.0735 1.000, 0.2140, 1.1501, 0.0069 0.924, 0.1161, 0.1728, 0.0101 | 0.0122 0.255, 0.0989, 0.0741, 0.0735 1.000, 0.1425, 1.4071, 0.0069 0.2162, 0.1563, 0.0096 1.000, |
| MR-RAPS2 MR-RAPS3 | -0.0992, 0.0089, 0.0113 0.299, -0.1011, 0.0740, 0.0735 1.000, 0.4682, 2.3725, 0.0083 0.962, -0.2666, 0.1861, 0.0113 | 0.0089, 0.0114 0.113, -0.0511, 0.0741, 0.0735 1.000, 0.1663, 0.6543, 0.0056 0.929, -0.1304, 0.1924, 0.0111 | 0.0089, 0.0115 0.075, -0.0311, 0.0741, 0.0735 1.000, 0.1104, 0.9236, 0.0057 0.911, -0.0771, 0.1914, 0.0109 | 0.0116 0.053, -0.0111, 0.0741, 0.0735 0.890, 0.1789, 0.7864, 0.0057 0.924, -0.0253, 0.1886, 0.0107 | 0.0116 0.053, -0.0011, 0.0741, 0.0735 0.673, 0.2385, 1.1421, 0.0062 0.927, -0.0002, 0.1866, 0.0106 | 0.0117 0.055, 0.0089, 0.0741, 0.0735 0.872, 0.1537, 0.9202, 0.0061 0.920, 0.0243, 0.1843, 0.0105 | 0.0118 0.080, 0.0289, 0.0741, 0.0735 1.000, 0.2206, 1.0497, 0.0063 0.937, 0.0715, 0.1789, 0.0103 | 0.0119 0.105, 0.0489, 0.0741, 0.0735 1.000, 0.2140, 1.1501, 0.0069 0.924, 0.1161, 0.1728, 0.0101 | 0.0122 0.255, 0.0989, 0.0741, 0.0735 1.000, 0.1425, 1.4071, 0.0669 0.2162, 0.1563, 0.0096 |

Table S74: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE satisfied, q=0.4, and N=50000.

| // (/ | ') | | <u> </u> | | , I | | | | |
|--|---|---|--|--|--|--|---|--|--|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.886, | 0.516, | 0.136, | 0.079, | 0.155, | 0.533, | 0.870, | 1.000, |
| | -0.0964, | -0.0467, | -0.0270, | -0.0083, | 0.0005, | 0.0094, | 0.0280, | 0.0475, | 0.0971, |
| | 0.0164, | 0.0166, | 0.0163, | 0.0153, | 0.0151, | 0.0155, | 0.0167, | 0.0173, | 0.0176, |
| | 0.0132 | 0.0134 | 0.0134 | 0.0134 | 0.0134 | 0.0135 | 0.0137 | 0.0139 | 0.0142 |
| cML-MA-AIC-Profile | 1.000, | 0.884, | 0.509, | 0.133, | 0.076, | 0.151, | 0.525, | 0.868, | 1.000, |
| | -0.0969, | -0.0468, | -0.0271, | -0.0083, | 0.0005, | 0.0094, | 0.0280, | 0.0476, | 0.0975, |
| | 0.0165, | 0.0167, | 0.0163, | 0.0153, | 0.0151, | 0.0155, | 0.0168, | 0.0174, | 0.0177, |
| | 0.0134 | 0.0135 | 0.0135 | 0.0134 | 0.0135 | 0.0136 | 0.0138 | 0.014 | 0.0144 |
| cML-AIC | 1.000, | 0.924, | 0.609, | 0.227, | 0.154, | 0.234, | 0.611, | 0.917, | 1.000, |
| | -0.0983, | -0.0485, | -0.0285, | -0.0090, | 0.0006, | 0.0101, | 0.0296, | 0.0495, | 0.0990, |
| | 0.0169, | 0.0175, | 0.0175, | 0.0172, | 0.0172, | 0.0174, | 0.0180, | 0.0181, | 0.0184, |
| No. 170 P. O. | 0.012 | 0.0121 | 0.0122 | 0.0123 | 0.0123 | 0.0124 | 0.0125 | 0.0126 | 0.0129 |
| cML-AIC-Profile | 1.000, | 0.924, | 0.607, | 0.223, | 0.150, | 0.229, | 0.606, | 0.915, | 1.000, |
| | -0.0986, 0.0172, | -0.0486, 0.0176, | -0.0286, | -0.0090, 0.0172, | 0.0006, 0.0172, | 0.0101, 0.0174, | 0.0296, | 0.0496, 0.0182, | 0.0993, 0.0185, |
| | 0.0172, | 0.0176, | 0.0175, 0.0123 | 0.0172, | 0.0172, | 0.0174, | 0.0180, 0.0126 | 0.0182, | 0.0183, |
| cML-MA-BIC | 1.000, | 0.995, | 0.0123 | 0.0124 | 0.0124 | 0.0123 | 0.733, | 0.989, | 1.000, |
| CML-MA-DIC | -0.1000, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1002, |
| | 0.0113, | 0.0114, | 0.0115, | 0.0116, | 0.0116, | 0.0116, | 0.0118, | 0.0119, | 0.0121, |
| | 0.0111 | 0.0112 | 0.0113 | 0.0114 | 0.0114 | 0.0115 | 0.0115 | 0.0116 | 0.0119 |
| cML-MA-BIC-Profile | 1.000, | 0.995, | 0.738, | 0.145, | 0.051, | 0.148, | 0.732, | 0.989, | 1.000, |
| CIVIL MATERIC Frome | -0.1000, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1002, |
| | 0.0113, | 0.0114, | 0.0115, | 0.0116, | 0.0116, | 0.0116, | 0.0118, | 0.0119, | 0.0121, |
| | 0.0112 | 0.0113 | 0.0113 | 0.0114 | 0.0115 | 0.0115 | 0.0116 | 0.0117 | 0.012 |
| cML-BIC | 1.000, | 0.994, | 0.752, | 0.161, | 0.053, | 0.155, | 0.744, | 0.989, | 1.000, |
| | -0.1000, | -0.0500, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1002, |
| | 0.0113, | 0.0114, | 0.0115, | 0.0116, | 0.0116, | 0.0116, | 0.0117, | 0.0118, | 0.0121, |
| | 0.011 | 0.0111 | 0.0112 | 0.0113 | 0.0113 | 0.0114 | 0.0114 | 0.0115 | 0.0118 |
| cML-BIC-Profile | 1.000, | 0.994, | 0.749, | 0.158, | 0.052, | 0.153, | 0.744, | 0.989, | 1.000, |
| | -0.1000, | -0.0500, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1002, |
| | 0.0113, | 0.0114, | 0.0115, | 0.0116, | 0.0116, | 0.0116, | 0.0117, | 0.0118, | 0.0121, |
| | 0.0111 | 0.0112 | 0.0112 | 0.0113 | 0.0114 | 0.0114 | 0.0115 | 0.0116 | 0.0119 |
| MR-Mix | 1.000, | 0.886, | 0.403, | 0.042, | 0.012, | 0.034, | 0.391, | 0.873, | 0.999, |
| | -0.1019, | -0.0503, | -0.0300, | -0.0102, | -0.0002, | 0.0096, | 0.0291, | 0.0483, | 0.0945, |
| | 0.0128, | 0.0129, | 0.0128, | 0.0128, | 0.0128, | 0.0128, | 0.0128, | 0.0128, | 0.0129, |
| | 0.0168 | 0.0167 | 0.0166 | 0.0166 | 0.0166 | 0.0165 | 0.0165 | 0.0165 | 0.0164 |
| MR-ContMix | 1.000, | 0.985, | 0.704, | 0.146, | 0.052, | 0.161, | 0.696, | 0.983, | 1.000, |
| | -0.0991, | -0.0494, | -0.0295, | -0.0097, | 0.0003, | 0.0102, | 0.0301, | 0.0500, | 0.0996, |
| | 0.0120, | 0.0121, | 0.0122, | 0.0123, | 0.0124, | 0.0124, | 0.0126, | 0.0128, | 0.0131, |
|) (D. I | NA | NA 0.000 | NA 0.720 | NA 0.152 | NA | NA 0.162 | NA 0.725 | NA | NA 1.000 |
| MR-Lasso | 1.000, | 0.988, | 0.730, | 0.152, | 0.066, | 0.162, 0.0101, | 0.725, | 0.981, 0.0498, | 1.000, |
| | -0.0992, 0.0120, | -0.0496, 0.0121, | -0.0297, | -0.0098, 0.0122, | 0.0001, 0.0122, | 0.0101, 0.0122, | 0.0299, 0.0123, | 0.0498, 0.0123, | 0.0995, 0.0128, |
| | 0.0120, | 0.0121, | 0.0122, 0.0113 | 0.0122, | 0.0122, | 0.0122, | 0.0123, | 0.0123, | 0.0128, |
| MR-PRESSO | 1.000, | 0.962, | 0.713, | 0.215, | 0.0113 | 0.223, | 0.707, | 0.965, | 1.000, |
| WIK-F KESSO | -0.0987, | -0.0491, | -0.0293, | -0.0095, | 0.0004, | 0.223, | 0.0301, | 0.903, | 0.0995, |
| | 0.0160, | 0.0158, | 0.0158, | 0.0157, | 0.0157, | 0.0157, | 0.0156, | 0.0155, | 0.0155, |
| | 0.0107 | 0.0108 | 0.0109 | 0.0137, | 0.0137, | 0.0111 | 0.0112 | 0.0112 | 0.0135, |
| MR-IVW | 0.152, | 0.079, | 0.062, | 0.057, | 0.055, | 0.054, | 0.067, | 0.081, | 0.169, |
| | -0.0955, | -0.0454, | -0.0255, | -0.0055, | 0.0045, | 0.0145, | 0.0345, | 0.0545, | 0.1044, |
| | 0.1052, | 0.1051, | 0.1051, | 0.1051, | 0.1051, | 0.1051, | 0.1051, | 0.1051, | 0.1051, |
| | 0.1044 | 0.1044 | 0.1044 | 0.1044 | 0.1044 | 0.1044 | 0.1044 | 0.1044 | 0.1044 |
| MR-IVW-Oracle | 1.000, | 0.995, | 0.728, | 0.133, | 0.045, | 0.134, | 0.710, | 0.990, | 1.000, |
| | -0.0994, | -0.0497, | -0.0298, | -0.0099, | 0.0001, | 0.0100, | 0.0299, | 0.0498, | 0.0995, |
| | 0.0111, | 0.0112, | 0.0113, | 0.0114, | 0.0114, | 0.0115, | 0.0116, | 0.0117, | 0.0120, |
| | 0.0113 | 0.0115 | 0.0115 | 0.0116 | 0.0117 | 0.0117 | 0.0118 | 0.0119 | 0.0121 |
| MR-Egger | 0.054, | 0.055, | 0.056, | 0.054, | 0.055, | 0.054, | 0.058, | 0.060, | 0.062, |
| | -0.0669, | -0.0252, | -0.0086, | 0.0081, | 0.0164, | 0.0248, | 0.0414, | 0.0581, | 0.0997, |
| | 0.5198, | 0.5199, | 0.5199, | 0.5200, | 0.5200, | 0.5200, | 0.5201, | 0.5201, | 0.5202, |
| | 0.5085 | 0.5085 | 0.5085 | 0.5085 | 0.5085 | 0.5085 | 0.5086 | 0.5086 | 0.5086 |
| MR-Weighted-Median | 1.000, | 0.847, | 0.386, | 0.060, | 0.031, | 0.073, | 0.435, | 0.839, | 1.000, |
| | | | | | | | | 0.0486, | 0.0965, |
| | -0.0950, | -0.0470, | -0.0278, | -0.0086, | 0.0009, | 0.0105, | 0.0295, | | |
| | -0.0950, 0.0144, | 0.0147, | 0.0148, | 0.0149, | 0.0149, | 0.0150, | 0.0151, | 0.0153, | 0.0157, |
| | -0.0950, 0.0144, 0.016 | 0.0147, 0.0162 | 0.0148, 0.0163 | 0.0149, 0.0164 | 0.0149, 0.0164 | 0.0150, 0.0165 | 0.0151, 0.0166 | 0.0153, 0.0167 | 0.0157, 0.0171 |
| MR-Weighted-Mode | -0.0950, 0.0144, 0.016 0.999, | 0.0147, 0.0162 0.799, | 0.0148, 0.0163 0.337, | 0.0149, 0.0164 0.054, | 0.0149, 0.0164 0.022, | 0.0150, 0.0165 0.064, | 0.0151, 0.0166 0.381, | 0.0153, 0.0167 0.788, | 0.0157, 0.0171 1.000, |
| | -0.0950, 0.0144, 0.016 0.999, -0.0963, | 0.0147, 0.0162 0.799, -0.0481, | 0.0148, 0.0163 0.337, -0.0285, | 0.0149, 0.0164 0.054, -0.0092, | 0.0149, 0.0164 0.022, 0.0008, | 0.0150, 0.0165 0.064, 0.0107, | 0.0151, 0.0166 0.381, 0.0299, | 0.0153, 0.0167 0.788, 0.0493, | 0.0157, 0.0171 1.000, 0.0981, |
| | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, | 0.0147, 0.0162 0.799, -0.0481, 0.0154, | 0.0148, 0.0163 0.337, -0.0285, 0.0153, | 0.0149, 0.0164 0.054, -0.0092, 0.0156, | 0.0149, 0.0164 0.022, 0.0008, 0.0158, | 0.0150, 0.0165 0.064, 0.0107, 0.0159, | 0.0151, 0.0166 0.381, 0.0299, 0.0160, | 0.0153, 0.0167 0.788, 0.0493, 0.0158, | 0.0157, 0.0171 1.000, 0.0981, 0.0162, |
| MR-Weighted-Mode | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.018 | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 |
| | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.018 | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, |
| MR-Weighted-Mode | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 0.077, -0.0459, | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.018 0.055, 0.0041, | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, |
| MR-Weighted-Mode | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1040, | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 0.077, -0.0459, 0.1040, | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1040, | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.018 0.055, 0.0041, 0.1041, | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1041, | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, |
| MR-Weighted-Mode MR-RAPS1 | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1040, 0.1045 | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 0.077, -0.0459, 0.1040, 0.1045 | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1040, 0.1045 | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, 0.1045 | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.018 0.055, 0.0041, 0.1041, 0.1045 | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1041, 0.1045 | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, 0.1045 |
| MR-Weighted-Mode | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1040, 0.1045 | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 0.077, -0.0459, 0.1040, 0.1045 | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1040, 0.1045 | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, 0.1045 0.053, | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.018 0.055, 0.0041, 0.1041, 0.1045 0.049, | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.1042, 0.1041, 0.1045 | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, 0.1045 |
| MR-Weighted-Mode MR-RAPS1 | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1040, 0.1045 0.137, -0.0954, | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 -0.0459, 0.1040, 0.1045 0.065, -0.0454, | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1040, 0.1045 0.057, -0.0253, | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, 0.1045 0.053, -0.0053, | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.018 0.055, 0.0041, 0.1041, 0.1045 0.049, | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1041, 0.1045 0.051, 0.0147, | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 0.051, 0.0347, | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 0.070, | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, 0.1045 0.157, 0.1048, |
| MR-Weighted-Mode MR-RAPS1 | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1040, 0.1045 0.137, -0.0954, 0.1067, | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 -0.0459, 0.1040, 0.1045 0.065, -0.0454, 0.1067, | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1040, 0.1045 0.057, -0.0253, 0.1067, | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, 0.1045 0.053, -0.0053, 0.1067, | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.015, 0.0041, 0.1041, 0.1045 0.0047, 0.0047, | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1041, 0.1045 0.051, 0.0147, 0.1068, | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 0.051, 0.0347, 0.1068, | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 0.070, 0.0547, | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, 0.1045 0.157, 0.1048, 0.1068, |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1044, 0.1045 0.137, -0.0954, 0.1067, 0.1088 | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177, -0.0459, 0.1045, 0.1045, 0.065, -0.0454, 0.1067, 0.1088 | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1044, 0.1045 0.057, -0.0253, 0.1067, 0.1088 | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, 0.1045 0.053, -0.0053, 0.1067, 0.1088 | 0.0149, 0.0164 0.0222, 0.0008, 0.0158, 0.018 0.055, 0.0041, 0.1045 0.049, 0.0047, 0.1067, 0.1088 | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1045 0.051, 0.0147, 0.1068, 0.1088 | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 0.051, 0.0347, 0.1068, 0.1089 | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 0.070, 0.0547, 0.1068, 0.1089 | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, 0.1045 0.157, 0.1048, 0.1068, 0.1089 |
| MR-Weighted-Mode MR-RAPS1 | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1044, 0.1045 0.137, -0.0954, 0.1067, 0.1088 | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 -0.0459, 0.1040, 0.1045 0.065, -0.0454, 0.1067, 0.1088 | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1044, 0.057, -0.0253, 0.1067, 0.1088 | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, 0.053, -0.0053, 0.1067, 0.1088 | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.015, 0.0041, 0.1041, 0.1045 0.049, 0.0047, 0.1067, 0.1088 | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1041, 0.1045 0.051, 0.0147, 0.1068, 0.1088 | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 0.051, 0.0347, 0.1068, 0.1089 | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 0.070, 0.0547, 0.1068, 0.1089 | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, 0.1045 0.157, 0.1048, 0.1068, 0.1089 |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1040, 0.1045 0.137, -0.0954, 0.1067, 0.1088 | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 -0.0459, 0.10440, 0.1045 0.065, -0.0454, 0.1067, 0.1088 0.877, -2.7050, | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1040, 0.1045 0.057, -0.0253, 0.1067, 0.1088 0.871, 0.1730, | 0.0149, 0.0164 0.054, -0.0092, 0.0156, -0.0059, 0.1041, 0.1045 0.053, -0.0053, 0.1067, 0.1088 0.883, 0.2818, | 0.0149, 0.0164 0.0222, 0.0008, 0.0158, 0.018 0.055, 0.0041, 0.1045 0.049, 0.0047, 0.1067, 0.1067, 0.1088 | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1041, 0.1045 0.051, 0.0147, 0.1068, 0.1088 0.895, -0.8724, | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 0.051, 0.0347, 0.1068, 0.1089 | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 0.070, 0.0547, 0.1068, 0.1089 | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, 0.1045 0.157, 0.1048, 0.1068, 0.1089 |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1045 0.137, -0.0954, 0.1088 0.903, -1.6334, 20.9243, | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 -0.0459, 0.1045, 0.1045 0.065, -0.0454, 0.1067, 0.1088 0.877, -2.7050, 94.0318, | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1045 0.057, -0.0253, 0.1067, 0.1088 0.871, 0.1730, 21.7599, | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, 0.1045 0.053, -0.0053, 0.1067, 0.1088 0.883, 0.2818, 10.2006, | 0.0149, 0.0164 0.0222, 0.0008, 0.0158, 0.018 0.055, 0.0041, 0.1045 0.049, 0.0047, 0.1067, 0.1088 0.886, 265.5101, 8383.5654, | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1045 0.051, 0.1045 0.1047, 0.1068, 0.1088 0.895, -0.8724, 24.3864, | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 0.051, 0.0347, 0.1068, 0.1089 0.877, 1.3031, 27.4717, | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 0.070, 0.0547, 0.1068, 0.1089 0.878, -0.2543, 42.4199, | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, 0.1045 0.157, 0.1068, 0.1089 0.926, 0.7809, 3.4360, |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 MR-RAPS3 | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1040, 0.1045 0.137, -0.0954, 0.1067, 0.1088 0.903, -1.6334, 20.9243, 26.1 | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177, -0.0459, 0.1040, 0.1045 0.065, -0.0454, 0.1067, 0.1088 0.877, -2.7050, 94.0318, 1013 | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1044, 0.1045 0.057, -0.0253, 0.1067, 0.1088 0.871, 0.1730, 21,7599, 39.08 | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, 0.1045 0.053, -0.0053, 0.1067, 0.1088 0.883, 0.2818, 10.2006, 10.77 | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.018 0.055, 0.0041, 0.1041, 0.1045 0.049, 0.0047, 0.1067, 0.1088 0.886, 265.5101, 8383.5654, 29550000 | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1041, 0.1045 0.051, 0.0147, 0.1068, 0.1088 0.895, -0.8724, 24.3864, 209.2 | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 0.051, 0.0347, 0.1068, 0.1089 0.877, 1.3031, 27.4717, 70.51 | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 0.070, 0.0547, 0.1068, 0.1089 0.878, -0.2543, 42.4199, 183.8 | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, 0.1045 0.157, 0.1048, 0.1068, 0.1089 0.926, 0.7809, 3.4360, 3.107 |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1044, 0.1045 0.137, -0.0954, 0.1067, 0.1088 0.903, -1.6334, 20.9243, 26.1 1.000, | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0177 -0.0459, 0.1040, 0.1045 0.065, -0.0454, 0.1067, 0.1088 0.877, -2.7050, 94.0318, 1013 | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1040, 0.1045 0.057, -0.0253, 0.1067, 0.1088 0.871, 0.1730, 21.7599, 39.08 | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, 0.1045 0.053, -0.0053, 0.1067, 0.1088 0.2818, 10.2006, 10.77 | 0.0149, 0.0164 0.0222, 0.0008, 0.0158, 0.018 0.055, 0.0041, 0.1045 0.049, 0.0047, 0.1067, 0.1067, 0.1088 0.886, 265.5101, 8383.5654, 29550000 0.929, | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1041, 0.1045 0.051, 0.0147, 0.1068, 0.1088 0.895, -0.8724, 24,3864, 209.2 0.953, | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 0.051, 0.0347, 0.1068, 0.1089 0.877, 1.3031, 27,4717, 70.51 | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 0.070, 0.0547, 0.1068, 0.1089 0.878, -0.2543, 42,4199, 183,8 | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1045 0.157, 0.1048, 0.1068, 0.1089 0.926, 0.7809, 3.4360, 3.107 1.000, |
| MR-Weighted-Mode MR-RAPS1 MR-RAPS2 MR-RAPS3 | -0.0950, 0.0144, 0.016 0.999, -0.0963, 0.0152, 0.0175 0.150, -0.0960, 0.1040, 0.1045 0.137, -0.0954, 0.1067, 0.1088 0.903, -1.6334, 20.9243, 26.1 | 0.0147, 0.0162 0.799, -0.0481, 0.0154, 0.0157, -0.0459, 0.1040, 0.1045 0.065, -0.0454, 0.1067, 0.1088 0.877, -2.7050, 94.0318, 1013 | 0.0148, 0.0163 0.337, -0.0285, 0.0153, 0.0178 0.061, -0.0259, 0.1044, 0.1045 0.057, -0.0253, 0.1067, 0.1088 0.871, 0.1730, 21,7599, 39.08 | 0.0149, 0.0164 0.054, -0.0092, 0.0156, 0.0179 0.056, -0.0059, 0.1041, 0.1045 0.053, -0.0053, 0.1067, 0.1088 0.883, 0.2818, 10.2006, 10.77 | 0.0149, 0.0164 0.022, 0.0008, 0.0158, 0.018 0.055, 0.0041, 0.1041, 0.1045 0.049, 0.0047, 0.1067, 0.1088 0.886, 265.5101, 8383.5654, 29550000 | 0.0150, 0.0165 0.064, 0.0107, 0.0159, 0.0181 0.057, 0.0142, 0.1041, 0.1045 0.051, 0.1047, 0.1068, 0.1088 0.895, -0.8724, 24.3864, 209.2 | 0.0151, 0.0166 0.381, 0.0299, 0.0160, 0.0182 0.055, 0.0342, 0.1041, 0.1045 0.051, 0.0347, 0.1068, 0.1089 0.877, 1.3031, 27.4717, 70.51 | 0.0153, 0.0167 0.788, 0.0493, 0.0158, 0.0183 0.071, 0.0542, 0.1041, 0.1045 0.070, 0.0547, 0.1068, 0.1089 0.878, -0.2543, 42.4199, 183.8 | 0.0157, 0.0171 1.000, 0.0981, 0.0162, 0.0188 0.167, 0.1042, 0.1041, 0.1045 0.157, 0.1048, 0.1068, 0.1089 0.926, 0.7809, 3.4360, 3.107 |

Table S75: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE satisfied, q=0.4, and N=100000.

| ((| <i>')</i> | | <i>'</i> | | , I | | | | |
|--------------------|--------------------|--------------------|--------------------|--------------------|-------------------|-------------------------------|-------------------|-------------------------------|-------------------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.991, | 0.798, | 0.171, | 0.061, | 0.163, | 0.785, | 0.994, | 1.000, |
| | -0.0975, | -0.0478, | -0.0280, | -0.0088, | 0.0000, | 0.0089, | 0.0279, | 0.0478, | 0.0974, |
| | 0.0108, | 0.0109, | 0.0109, | 0.0102, | 0.0098, | 0.0102, | 0.0112, | 0.0114, | 0.0117, |
| | 0.0094 | 0.0095 | 0.0095 | 0.0095 | 0.0095 | 0.0096 | 0.0097 | 0.0098 | 0.0101 |
| cML-MA-AIC-Profile | 1.000, | 0.991, | 0.795, | 0.169, | 0.061, | 0.161, | 0.783, | 0.994, | 1.000, |
| | -0.0978, | -0.0479, | -0.0280, | -0.0088, | 0.0000, | 0.0089, | 0.0280, | 0.0479, | 0.0977, |
| | 0.0109, | 0.0110, | 0.0109, | 0.0102, | 0.0098, | 0.0102, | 0.0113, | 0.0115, | 0.0118, |
| | 0.0094 | 0.0095 | 0.0096 | 0.0095 | 0.0095 | 0.0096 | 0.0098 | 0.0099 | 0.0101 |
| cML-AIC | 1.000, | 0.994, | 0.864, | 0.248, | 0.123, | 0.261, | 0.841, | 0.996, | 1.000, |
| | -0.0988, | -0.0490, | -0.0291, | -0.0094, | 0.0001, | 0.0095, | 0.0291, | 0.0490, | 0.0987, |
| | 0.0114, | 0.0115, | 0.0115, | 0.0114, | 0.0112, | 0.0114, | 0.0119, | 0.0120, | 0.0123, |
| -MI AIC D. GI | 0.0085 | 0.0086 | 0.0086 | 0.0087 | 0.0087 | 0.0087 | 0.0088 | 0.0089 | 0.0091 |
| cML-AIC-Profile | 1.000, -0.0990, | 0.994, -0.0490, | 0.864, -0.0291, | 0.247, -0.0094, | 0.122, 0.0001, | 0.257, 0.0095, | 0.840, 0.0291, | 0.996, 0.0491, | 1.000, 0.0989, |
| | 0.0115, | 0.0115, | 0.0116, | 0.0094, | 0.0001, | 0.0093, | 0.0291, 0.0120, | 0.0491, | 0.0989, |
| | 0.0115, | 0.0113, | 0.0087 | 0.0114, | 0.0112, | 0.0114, | 0.0120, | 0.0120, | 0.0124, |
| cML-MA-BIC | 1.000, | 1.000, | 0.961, | 0.216, | 0.059, | 0.231, | 0.956, | 1.000, | 1.000, |
| COLD THE DIC | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0300, | 0.0500, | 0.1000, |
| | 0.0078, | 0.0079, | 0.0080, | 0.0080, | 0.0081, | 0.0081, | 0.0082, | 0.0083, | 0.0085, |
| | 0.0078 | 0.0079 | 0.008 | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0082 | 0.0084 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.961, | 0.215, | 0.058, | 0.230, | 0.956, | 1.000, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0300, | 0.0500, | 0.1000, |
| | 0.0078, | 0.0079, | 0.0080, | 0.0080, | 0.0081, | 0.0081, | 0.0082, | 0.0083, | 0.0085, |
| | 0.0079 | 0.0079 | 0.008 | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0082 | 0.0084 |
| cML-BIC | 1.000, | 1.000, | 0.965, | 0.226, | 0.061, | 0.237, | 0.961, | 1.000, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0078, | 0.0079, | 0.0080, | 0.0080, | 0.0081, | 0.0081, | 0.0082, | 0.0083, | 0.0085, |
| | 0.0078 | 0.0079 | 0.0079 | 0.008 | 0.008 | 0.008 | 0.0081 | 0.0082 | 0.0084 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.965, | 0.225, | 0.061, | 0.236, | 0.961, | 1.000, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0078, | 0.0079, | 0.0080, | 0.0080, | 0.0081, | 0.0081, | 0.0082, | 0.0083, | 0.0085, |
| | 0.0078 | 0.0079 | 0.0079 | 0.008 | 0.008 | 0.008 | 0.0081 | 0.0082 | 0.0084 |
| MR-Mix | 1.000, | 0.984, | 0.638, | 0.054, | 0.013, | 0.052, | 0.653, | 0.981, | 1.000, |
| | -0.1014, | -0.0497, | -0.0294, | -0.0095, | 0.0004, | 0.0103, | 0.0295, | 0.0486, | 0.0948, |
| | 0.0102, | 0.0101, | 0.0101, | 0.0101, | 0.0101, | 0.0101, | 0.0101, | 0.0101, | 0.0101, |
| \m a \n | 0.0131 | 0.013 | 0.013 | 0.013 | 0.013 | 0.013 | 0.013 | 0.013 | 0.0129 |
| MR-ContMix | 1.000, | 1.000, | 0.951, | 0.225, | 0.056, | 0.218, | 0.941, | 1.000, | 1.000, |
| | -0.0996, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0099, | 0.0298, | 0.0497, | 0.0996, |
| | 0.0081, | 0.0082, | 0.0082, | 0.0083, | 0.0083, | 0.0083, | 0.0084, NA | 0.0085, | 0.0087, |
| MR-Lasso | NA 1.000, | NA 1.000, | NA 0.953, | NA 0.219, | NA 0.062, | NA 0.236, | 0.945, | NA 1.000, | NA 1.000, |
| WIX-Lasso | -0.0996, | -0.0497, | -0.0298, | -0.0099, | 0.002, | 0.230, | 0.943, | 0.0498, | 0.0996, |
| | 0.0081, | 0.0083, | 0.0082, | 0.0083, | 0.0001, | 0.0100, | 0.0300, | 0.0498, | 0.0990, |
| | 0.0079 | 0.008 | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0082 | 0.0083 | 0.0085 |
| MR-PRESSO | 0.994, | 0.964, | 0.865, | 0.378, | 0.255, | 0.381, | 0.872, | 0.962, | 0.996, |
| WIR TRESSO | -0.0993, | -0.0497, | -0.0299, | -0.0100, | -0.0001, | 0.0099, | 0.0297, | 0.0495, | 0.0992, |
| | 0.0193, | 0.0191, | 0.0190, | 0.0189, | 0.0189, | 0.0188, | 0.0188, | 0.0187, | 0.0183, |
| | 0.0078 | 0.0078 | 0.0079 | 0.0079 | 0.0079 | 0.008 | 0.008 | 0.0081 | 0.0083 |
| MR-IVW | 0.173, | 0.089, | 0.065, | 0.054, | 0.051, | 0.054, | 0.065, | 0.081, | 0.182, |
| | -0.0974, | -0.0473, | -0.0272, | -0.0072, | 0.0028, | 0.0129, | 0.0329, | 0.0529, | 0.1030, |
| | 0.1075, | 0.1075, | 0.1075, | 0.1075, | 0.1075, | 0.1075, | 0.1075, | 0.1075, | 0.1075, |
| | 0.1046 | 0.1046 | 0.1046 | 0.1046 | 0.1046 | 0.1046 | 0.1046 | 0.1046 | 0.1046 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.957, | 0.205, | 0.054, | 0.212, | 0.952, | 1.000, | 1.000, |
| | -0.0995, | -0.0497, | -0.0298, | -0.0099, | 0.0001, | 0.0100, | 0.0299, | 0.0499, | 0.0997, |
| | 0.0078, | 0.0079, | 0.0079, | 0.0080, | 0.0080, | 0.0080, | 0.0081, | 0.0082, | 0.0084, |
| | 0.008 | 0.0081 | 0.0082 | 0.0082 | 0.0082 | 0.0083 | 0.0083 | 0.0084 | 0.0086 |
| MR-Egger | 0.058, | 0.056, | 0.059, | 0.060, | 0.061, | 0.062, | 0.061, | 0.062, | 0.070, |
| | -0.0666, | -0.0210, | -0.0028, | 0.0154, | 0.0245, | 0.0337, | 0.0519, | 0.0701, | 0.1157, |
| | 0.5538, | 0.5536, | 0.5536, | 0.5535, | 0.5535, | 0.5535, | 0.5534, | 0.5534, | 0.5532, |
| | 0.5323 | 0.5323 | 0.5323 | 0.5323 | 0.5323 | 0.5323 | 0.5323 | 0.5323 | 0.5323 |
| MR-Weighted-Median | 1.000, | 0.996, | 0.755, | 0.101, | 0.022, | 0.101, | 0.745, | 0.991, | 1.000, |
| | -0.0972, | -0.0485, | -0.0290, | -0.0096, | 0.0001, | 0.0099, | 0.0294, | 0.0489, | 0.0974, |
| | 0.0097, | 0.0098, | 0.0099, | 0.0100, | 0.0100, | 0.0101, | 0.0102, | 0.0103, | 0.0107, |
| MD Waight 1 M - 1 | 0.0113 | 0.0114 | 0.0115 | 0.0116 | 0.0116 | 0.0117 | 0.0118 | 0.0119 | 0.0121 |
| MR-Weighted-Mode | 1.000, | 0.985, -0.0492, | 0.659, | 0.073, | 0.016, 0.0000, | 0.063, | 0.631, | 0.980, | 1.000, |
| | -0.0985, | | -0.0296, | -0.0100, | | 0.0098, | 0.0295, | 0.0491, | 0.0982, |
| | 0.0105, 0.0127 | 0.0105, 0.0128 | 0.0106, 0.0129 | 0.0107, 0.013 | 0.0107, 0.0131 | 0.0108, 0.0131 | 0.0108, 0.0132 | 0.0109, 0.0133 | 0.0113, 0.0136 |
| MR-RAPS1 | 0.0127 | 0.0128 | 0.0129 | 0.013 | 0.0131 | 0.0131 | 0.0132 | 0.0133 | 0.0136 |
| IVIN-KAP31 | 0.160, -0.0971, | -0.0471, | -0.0271, | -0.0071, | 0.050, 0.0029, | 0.048, 0.0129, | 0.056, 0.0329, | 0.073, 0.0529, | 0.168, 0.1029, |
| | 0.1043, | 0.10471, | 0.1043, | 0.1043, | 0.0029, | 0.0129, | 0.0329, | 0.0329, | 0.1029, |
| | 0.1043, | 0.1043, | 0.1043, | 0.1043, | 0.1044, | 0.1044, | 0.1044, | 0.1044, | 0.1044, |
| MR-RAPS2 | 0.1042 | 0.1042 | 0.059, | 0.051, | 0.1042 | 0.1042 | 0.1042 | 0.1042 | 0.1542 |
| MIC ICH 52 | -0.0971, | -0.0471, | -0.0271, | -0.0071, | 0.043, | 0.043, | 0.048, | 0.071, | 0.138, |
| | 0.1066, | 0.1066, | 0.1067, | 0.1067, | 0.1067, | 0.1067, | 0.1067, | 0.0329, | 0.1029, |
| | 0.1086 | 0.1086 | 0.1086 | 0.1086 | 0.1007, | 0.1086 | 0.1086 | 0.1086 | 0.1086 |
| MR-RAPS3 | 0.1080 | 0.1080 | 0.1080 | 0.1080 | 0.1080 | 0.1080 | 0.1080 | 0.1080 | 0.1080 |
| MIC ICH SS | 1.0078, | -1.0769, | 0.0886, | -9.5900, | -0.2141, | 1.7566, | -1.6525, | 0.3291, | 0.5993, |
| | 54.5723, | 18.1137, | 16.8509, | 257.8822, | 18.4052, | 98.5441, | 58.2242, | 10.2074, | 7.0298, |
| | | | 35.9937 | 4776.09 | 23.2109 | 434.4651 | 227.5009 | 10.2074, | 4.1958 |
| | | 20,2496 | 33.9937 | | | | | | |
| MR-RAPS4 | 112.8361 | 20.2496 | | | | 0,957. | | 1,000. | 1.000 |
| MR-RAPS4 | 112.8361 1.000, | 1.000, | 1.000, | 0.954, | 0.940, | 0.957, -0.1988, | 0.997, | 1.000, -0.6596, | 1.000, -0.9944, |
| MR-RAPS4 | 112.8361 | | | | | 0.957, -0.1988, 1.4411, | | 1.000, -0.6596, 1.2877, | 1.000, -0.9944, 0.8920, |

Table S76: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE satisfied, q=0.4, and N=200000.

| Methods θ | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|--------------------|-----------|----------|----------|-----------|-----------|----------|----------|----------|---------|
| cML-MA-AIC | 1.000, | 1.000, | 0.970, | 0.301, | 0.068, | 0.279, | 0.955, | 1.000, | 1.000, |
| | -0.0988, | -0.0489, | -0.0290, | -0.0093, | -0.0003, | 0.0087, | 0.0282, | 0.0482, | 0.0979, |
| | 0.0078, | 0.0079, | 0.0079, | 0.0075, | 0.0071, | 0.0075, | 0.0081, | 0.0081, | 0.0084, |
| | 0.0066 | 0.0067 | 0.0067 | 0.0067 | 0.0067 | 0.0067 | 0.0069 | 0.0069 | 0.0071 |
| ML-MA-AIC-Profile | 1.000, | 1.000, | 0.970, | 0.300, | 0.068, | 0.278, | 0.955, | 1.000, | 1.000, |
| | -0.0990, | -0.0490, | -0.0290, | -0.0093, | -0.0003, | 0.0087, | 0.0283, | 0.0482, | 0.0981, |
| | 0.0079, | 0.0079, | 0.0079, | 0.0075, | 0.0071, | 0.0075, | 0.0081, | 0.0082, | 0.0084 |
| MI AIC | 0.0066 | 0.0067 | 0.0067 | 0.0067 | 0.0067 | 0.0068 | 0.0069 | 0.0069 | 0.0071 |
| cML-AIC | 1.000, | 1.000, | 0.982, | 0.409, | 0.146, | 0.379, | 0.969, | 1.000, | 1.000, |
| | -0.0996, | -0.0498, | -0.0298, | -0.0100, | -0.0004, | 0.0092, | 0.0290, | 0.0490, | 0.0988 |
| | 0.0082, | 0.0083, | 0.0085, | 0.0083, | 0.0081, | 0.0083, | 0.0085, | 0.0086, | 0.0088 |
| M AIG D GI | 0.006 | 0.0061 | 0.0061 | 0.0061 | 0.0062 | 0.0062 | 0.0062 | 0.0063 | 0.0064 |
| cML-AIC-Profile | 1.000, | 1.000, | 0.982, | 0.407, | 0.146, | 0.379, | 0.969, | 1.000, | 1.000, |
| | -0.0997, | -0.0498, | -0.0298, | -0.0100, | -0.0004, | 0.0092, | 0.0290, | 0.0490, | 0.0990 |
| | 0.0082, | 0.0083, | 0.0085, | 0.0083, | 0.0081, | 0.0083, | 0.0085, | 0.0086, | 0.0088 |
| M. M. DIC | 0.006 | 0.0061 | 0.0061 | 0.0061 | 0.0062 | 0.0062 | 0.0062 | 0.0063 | 0.0064 |
| cML-MA-BIC | 1.000, | 1.000, | 1.000, | 0.406, | 0.047, | 0.426, | 0.999, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1000 |
| | 0.0054, | 0.0055, | 0.0056, | 0.0056, | 0.0056, | 0.0057, | 0.0057, | 0.0058, | 0.0060 |
| # M. DIG D. 01 | 0.0055 | 0.0056 | 0.0056 | 0.0057 | 0.0057 | 0.0057 | 0.0058 | 0.0058 | 0.0059 |
| ML-MA-BIC-Profile | 1.000, | 1.000, | 1.000, | 0.405, | 0.047, | 0.426, | 0.999, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1000 |
| | 0.0054, | 0.0055, | 0.0056, | 0.0056, | 0.0056, | 0.0057, | 0.0057, | 0.0058, | 0.0060 |
| 1.00 P | 0.0055 | 0.0056 | 0.0056 | 0.0057 | 0.0057 | 0.0057 | 0.0058 | 0.0058 | 0.0059 |
| cML-BIC | 1.000, | 1.000, | 0.999, | 0.413, | 0.047, | 0.438, | 0.999, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1000 |
| | 0.0054, | 0.0055, | 0.0056, | 0.0056, | 0.0056, | 0.0057, | 0.0057, | 0.0058, | 0.0060 |
| | 0.0055 | 0.0056 | 0.0056 | 0.0056 | 0.0057 | 0.0057 | 0.0057 | 0.0058 | 0.0059 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.999, | 0.412, | 0.047, | 0.438, | 0.999, | 1.000, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1000 |
| | 0.0054, | 0.0055, | 0.0056, | 0.0056, | 0.0056, | 0.0057, | 0.0057, | 0.0058, | 0.0060 |
| | 0.0055 | 0.0056 | 0.0056 | 0.0056 | 0.0057 | 0.0057 | 0.0057 | 0.0058 | 0.0059 |
| MR-Mix | 1.000, | 0.999, | 0.896, | 0.147, | 0.024, | 0.171, | 0.870, | 0.998, | 1.000, |
| | -0.1016, | -0.0499, | -0.0297, | -0.0097, | 0.0002, | 0.0100, | 0.0294, | 0.0487, | 0.0950 |
| | 0.0076, | 0.0075, | 0.0075, | 0.0075, | 0.0076, | 0.0075, | 0.0075, | 0.0075, | 0.0077 |
| | 0.0103 | 0.0102 | 0.0102 | 0.0102 | 0.0102 | 0.0102 | 0.0101 | 0.0101 | 0.01 |
| MR-ContMix | 1.000, | 1.000, | 1.000, | 0.403, | 0.051, | 0.427, | 0.999, | 1.000, | 1.000, |
| | -0.0998, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.0999 |
| | 0.0056, | 0.0057, | 0.0057, | 0.0058, | 0.0058, | 0.0058, | 0.0059, | 0.0060, | 0.0061 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 1.000, | 0.998, | 0.402, | 0.053, | 0.423, | 0.996, | 1.000, | 1.000, |
| | -0.0997, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0499, | 0.0998 |
| | 0.0057, | 0.0058, | 0.0058, | 0.0059, | 0.0059, | 0.0059, | 0.0060, | 0.0061, | 0.0063 |
| | 0.0056 | 0.0056 | 0.0057 | 0.0057 | 0.0057 | 0.0058 | 0.0058 | 0.0059 | 0.006 |
| MR-PRESSO | 0.986, | 0.946, | 0.901, | 0.581, | 0.417, | 0.551, | 0.880, | 0.940, | 0.986, |
| | -0.1011, | -0.0514, | -0.0316, | -0.0117, | -0.0017, | 0.0083, | 0.0282, | 0.0481, | 0.0977 |
| | 0.0268, | 0.0268, | 0.0267, | 0.0265, | 0.0265, | 0.0265, | 0.0263, | 0.0261, | 0.0240 |
| | 0.0062 | 0.0063 | 0.0063 | 0.0063 | 0.0064 | 0.0064 | 0.0064 | 0.0064 | 0.0064 |
| MR-IVW | 0.178, | 0.088, | 0.072, | 0.062, | 0.056, | 0.058, | 0.060, | 0.067, | 0.139, |
| | -0.1085, | -0.0583, | -0.0382, | -0.0181, | -0.0081, | 0.0020, | 0.0220, | 0.0421, | 0.0923 |
| | 0.1047, | 0.1046, | 0.1046, | 0.1046, | 0.1046, | 0.1046, | 0.1046, | 0.1046, | 0.1046 |
| | 0.1045 | 0.1045 | 0.1045 | 0.1045 | 0.1045 | 0.1045 | 0.1045 | 0.1045 | 0.1045 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.999, | 0.392, | 0.046, | 0.407, | 0.998, | 1.000, | 1.000, |
| | -0.0998, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0499, | 0.0999 |
| | 0.0054, | 0.0055, | 0.0055, | 0.0056, | 0.0056, | 0.0056, | 0.0057, | 0.0058, | 0.0059 |
| | 0.0057 | 0.0057 | 0.0058 | 0.0058 | 0.0058 | 0.0058 | 0.0059 | 0.0059 | 0.0061 |
| MR-Egger | 0.052, | 0.052, | 0.049, | 0.048, | 0.051, | 0.051, | 0.056, | 0.057, | 0.060, |
| | -0.1017, | -0.0538, | -0.0346, | -0.0155, | -0.0059, | 0.0036, | 0.0228, | 0.0419, | 0.0897 |
| | 0.5651, | 0.5650, | 0.5650, | 0.5650, | 0.5650, | 0.5650, | 0.5649, | 0.5649, | 0.5649 |
| | 0.5433 | 0.5433 | 0.5432 | 0.5432 | 0.5432 | 0.5432 | 0.5432 | 0.5432 | 0.5432 |
| IR-Weighted-Median | 1.000, | 1.000, | 0.973, | 0.212, | 0.020, | 0.194, | 0.964, | 1.000, | 1.000, |
| - | -0.0988, | -0.0495, | -0.0297, | -0.0101, | -0.0002, | 0.0096, | 0.0293, | 0.0490, | 0.0981 |
| | 0.0069, | 0.0070, | 0.0071, | 0.0071, | 0.0072, | 0.0072, | 0.0073, | 0.0073, | 0.0075 |
| | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0082 | 0.0082 | 0.0083 | 0.0084 | 0.0086 |
| MR-Weighted-Mode | 1.000, | 1.000, | 0.939, | 0.169, | 0.018, | 0.129, | 0.892, | 1.000, | 1.000, |
| - | -0.0994, | -0.0499, | -0.0301, | -0.0102, | -0.0003, | 0.0096, | 0.0293, | 0.0494, | 0.0990 |
| | 0.0078, | 0.0078, | 0.0079, | 0.0081, | 0.0081, | 0.0083, | 0.0082, | 0.0083, | 0.0084 |
| | 0.0092 | 0.0093 | 0.0094 | 0.0094 | 0.0095 | 0.0095 | 0.0096 | 0.0096 | 0.0099 |
| MR-RAPS1 | 0.174, | 0.090, | 0.067, | 0.055, | 0.054, | 0.052, | 0.052, | 0.059, | 0.141, |
| | -0.1081, | -0.0580, | -0.0380, | -0.0180, | -0.0080, | 0.0020, | 0.0220, | 0.0420, | 0.0920 |
| | 0.1021, | 0.1021, | 0.1021, | 0.1021, | 0.1021, | 0.1021, | 0.1021, | 0.1021, | 0.1021 |
| | 0.1039 | 0.1039 | 0.1039 | 0.1039 | 0.1039 | 0.1039 | 0.1039 | 0.1039 | 0.104 |
| MR-RAPS2 | 0.235, | 0.099, | 0.068, | 0.050, | 0.049, | 0.049, | 0.054, | 0.069, | 0.145, |
| ** | -0.1037, | -0.0579, | -0.0379, | -0.0183, | -0.0071, | 0.0036, | 0.0226, | 0.0430, | 0.0928 |
| | 0.0920, | 0.0978, | 0.0994, | 0.0999, | 0.0999, | 0.1008, | 0.1020, | 0.1019, | 0.1029 |
| | 0.0941 | 0.1013 | 0.1031 | 0.1041 | 0.104 | 0.1042 | 0.1036 | 0.1033 | 0.1046 |
| MR-RAPS3 | 0.959, | 0.933, | 0.943, | 0.939, | 0.929, | 0.924, | 0.945, | 0.944, | 0.956, |
| | -11.1622, | 0.0348, | -1.2186, | 3.9690, | 6.1388, | 0.4160, | -0.0042, | 0.5246, | 0.7122 |
| | 305.9594, | 82.3958, | 27.7718, | 108.9560, | 132.5582, | 18.3534, | 6.3809, | 15.5979, | 3.7180 |
| | 4762.2712 | 192.1699 | 38.7595 | 642.0259 | 687.2719 | 16.9941 | 4.2503 | 41.5097 | 1.7861 |
| MR-RAPS4 | 0.999, | 1.000, | 1.000, | 0.974, | 0.959, | 0.976, | 1.000, | 1.000, | 1.000, |
| 1111 IAI 54 | 0.999, | 0.6188, | 0.3922, | 0.974, | -0.0907, | -0.2073, | -0.5334, | -0.7904, | -1.0600 |
| | | | | | | | | | 0.8739 |
| | 1.2784, | 1.4998, | 1.6113, | 1.6427, | 1.6392, | 1.6216, | 1.5125, | 1.3714, | |

Table S77: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE satisfied, q=0.6, and N=50000.

| // | <i>'</i> | | <u> </u> | | , 1 | | | | |
|--------------------|-------------------|------------------------------|------------------------------|------------------------------|------------------------------|-------------------|------------------------------|-------------------|-------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.995, | 0.698, | 0.331, | 0.114, | 0.068, | 0.093, | 0.352, | 0.672, | 0.983, |
| | -0.0953, | -0.0458, | -0.0266, | -0.0088, | -0.0004, | 0.0083, | 0.0261, | 0.0450, | 0.0941, |
| | 0.0211, | 0.0212, | 0.0205, | 0.0192, | 0.0190, | 0.0193, | 0.0207, | 0.0220, | 0.0229, |
| | 0.0176 | 0.0177 | 0.0176 | 0.0176 | 0.0176 | 0.0178 | 0.018 | 0.0183 | 0.0188 |
| cML-MA-AIC-Profile | 0.994, | 0.698, | 0.331, | 0.113, | 0.067, | 0.092, | 0.345, | 0.667, | 0.983, |
| | -0.0956, | -0.0459, | -0.0267, | -0.0088, | -0.0004, | 0.0083, | 0.0262, | 0.0451, | 0.0945, |
| | 0.0213, | 0.0213, | 0.0205, | 0.0193, | 0.0190, | 0.0193, | 0.0207, | 0.0220, | 0.0230, |
| | 0.0177 | 0.0178 | 0.0178 | 0.0177 | 0.0178 | 0.0179 | 0.0181 | 0.0184 | 0.0189 |
| cML-AIC | 0.999, | 0.786, | 0.431, | 0.197, | 0.139, | 0.163, | 0.460, | 0.740, | 0.994, |
| | -0.0979, | -0.0481, | -0.0286, | -0.0095, | -0.0003, | 0.0092, | 0.0282, | 0.0478, | 0.0972, |
| | 0.0225, | 0.0225, | 0.0223, | 0.0218, | 0.0218, | 0.0220, | 0.0228, | 0.0234, | 0.0236, |
| | 0.0157 | 0.0159 | 0.016 | 0.016 | 0.0161 | 0.0162 | 0.0163 | 0.0164 | 0.0167 |
| cML-AIC-Profile | 0.999, | 0.783, | 0.427, | 0.194, | 0.137, | 0.163, | 0.453, | 0.739, | 0.994, |
| | -0.0980, | -0.0482, | -0.0286, | -0.0095, | -0.0003, | 0.0092, | 0.0282, | 0.0478, | 0.0974, |
| | 0.0226, | 0.0226, | 0.0223, | 0.0218, | 0.0218, | 0.0220, | 0.0228, | 0.0235, | 0.0238, |
| | 0.0159 | 0.016 | 0.0161 | 0.0162 | 0.0162 | 0.0163 | 0.0164 | 0.0165 | 0.0168 |
| cML-MA-BIC | 1.000, | 0.924, | 0.524, | 0.112, | 0.059, | 0.112, | 0.506, | 0.892, | 1.000, |
| | -0.1003, | -0.0504, | -0.0304, | -0.0104, | -0.0005, | 0.0095, | 0.0294, | 0.0494, | 0.0993, |
| | 0.0151, | 0.0153, | 0.0154, | 0.0154, | 0.0155, | 0.0155, | 0.0157, | 0.0158, | 0.0162, |
| M M DIC D CI | 0.0146 | 0.0148 | 0.0148 | 0.0149 | 0.015 | 0.015 | 0.0151 | 0.0152 | 0.0155 |
| cML-MA-BIC-Profile | 1.000, | 0.923, | 0.521, | 0.111, | 0.059, | 0.109, | 0.504, | 0.891, | 1.000, |
| | -0.1003, | -0.0504, | -0.0304, | -0.0104, | -0.0005, | 0.0095, | 0.0294, | 0.0494, | 0.0994, |
| | 0.0151, 0.0147 | 0.0153, 0.0148 | 0.0154, 0.0149 | 0.0154, 0.015 | 0.0155, 0.015 | 0.0155, 0.0151 | 0.0157, 0.0152 | 0.0158, | 0.0162, |
| cML-BIC | 1.000, | 0.0148 | | 0.015 | | 0.0151 | 0.0152 | 0.0153 0.895, | 0.0156 1.000, |
| CIVIL-BIC | -0.1004, | -0.0504, | 0.533, | -0.0105, | 0.063, | 0.118, 0.0095, | 0.518, 0.0295, | | |
| | 0.0151, | | -0.0304, | | -0.0005, 0.0156 | | | 0.0495, | 0.0994, |
| | 0.0151, 0.0145 | 0.0153, 0.0146 | 0.0154, 0.0147 | 0.0155, 0.0148 | 0.0156, 0.0148 | 0.0156, 0.0148 | 0.0157, 0.015 | 0.0158, 0.0151 | 0.0162, 0.0154 |
| cML-BIC-Profile | 1.000, | 0.0146 | 0.529, | 0.0148 | 0.0148 | 0.0148 | 0.516, | 0.895, | 1.000, |
| CIVIL-DIC-PIONIC | -0.1004, | -0.0504, | -0.0304, | -0.0105, | -0.0005, | 0.118, 0.0095, | 0.516, 0.0295, | 0.895, | 0.0994, |
| | 0.0151, | 0.0153, | 0.0154, | 0.0155, | 0.0156, | 0.0055, | 0.0293, | 0.0493, | 0.0334, |
| | 0.0131, | 0.0133, | 0.0134, | 0.0133, | 0.0130, | 0.0130, | 0.0157, | 0.0158, | 0.0154 |
| MR-Mix | 1.000, | 0.803, | 0.334, | 0.054, | 0.033, | 0.050, | 0.312, | 0.758, | 0.997, |
| 11111 11111 | -0.0950, | -0.0473, | -0.0284, | -0.0095, | -0.0003, | 0.0087, | 0.0268, | 0.0445, | 0.0883, |
| | 0.0151, | 0.0149, | 0.0149, | 0.0148, | 0.0149, | 0.0148, | 0.0149, | 0.0151, | 0.0151, |
| | 0.0171 | 0.017 | 0.017 | 0.017 | 0.017 | 0.017 | 0.017 | 0.017 | 0.017 |
| MR-ContMix | 1.000, | 0.917, | 0.508, | 0.108, | 0.058, | 0.105, | 0.484, | 0.881, | 0.999, |
| | -0.0996, | -0.0501, | -0.0304, | -0.0105, | -0.0006, | 0.0094, | 0.0292, | 0.0491, | 0.0987, |
| | 0.0157, | 0.0158, | 0.0158, | 0.0159, | 0.0160, | 0.0160, | 0.0162, | 0.0163, | 0.0167, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.915, | 0.521, | 0.118, | 0.067, | 0.122, | 0.506, | 0.876, | 0.999, |
| | -0.0995, | -0.0502, | -0.0302, | -0.0103, | -0.0004, | 0.0095, | 0.0293, | 0.0491, | 0.0989, |
| | 0.0155, | 0.0161, | 0.0161, | 0.0162, | 0.0163, | 0.0164, | 0.0164, | 0.0165, | 0.0172, |
| | 0.0148 | 0.0149 | 0.015 | 0.0151 | 0.0151 | 0.0152 | 0.0153 | 0.0154 | 0.0157 |
| MR-PRESSO | 0.991, | 0.879, | 0.556, | 0.243, | 0.166, | 0.207, | 0.511, | 0.819, | 0.980, |
| | -0.1010, | -0.0517, | -0.0319, | -0.0121, | -0.0022, | 0.0077, | 0.0274, | 0.0472, | 0.0967, |
| | 0.0241, | 0.0241, | 0.0241, | 0.0241, | 0.0242, | 0.0241, | 0.0239, | 0.0239, | 0.0236, |
| | 0.0141 | 0.0143 | 0.0143 | 0.0144 | 0.0145 | 0.0145 | 0.0146 | 0.0147 | 0.015 |
| MR-IVW | 0.160, | 0.102, | 0.091, | 0.079, | 0.077, | 0.071, | 0.073, | 0.076, | 0.123, |
| | -0.1092, | -0.0591, | -0.0391, | -0.0191, | -0.0091, | 0.0009, | 0.0209, | 0.0409, | 0.0909, |
| | 0.1371, | 0.1371, | 0.1371, | 0.1371, | 0.1371, | 0.1371, | 0.1371, | 0.1371, | 0.1370, |
| | 0.1276 | 0.1276 | 0.1276 | 0.1276 | 0.1276 | 0.1276 | 0.1276 | 0.1276 | 0.1276 |
| MR-IVW-Oracle | 1.000, | 0.914, | 0.500, | 0.103, | 0.053, | 0.105, | 0.485, | 0.881, | 0.999, |
| | -0.0996, | -0.0500, | -0.0301, | -0.0103, | -0.0004, 0.0154 | 0.0095, | 0.0294, | 0.0492, | 0.0988, |
| | 0.0150, 0.015 | 0.0151, 0.0151 | 0.0152, 0.0152 | 0.0153, 0.0153 | 0.0154, 0.0154 | 0.0154, 0.0154 | 0.0155, 0.0155 | 0.0156, 0.0156 | 0.0160, 0.0159 |
| MP_Eggar | 0.015 | 0.0151 | 0.0152 | 0.0153 | 0.0154 | 0.0154 | 0.0155 | 0.0156 | 0.0159 |
| MR-Egger | -0.0827, | -0.0409, | -0.0242, | -0.0074, | 0.049, | 0.050, | 0.031, | 0.051, 0.0427, | 0.036, |
| | 0.6337, | 0.6338, | 0.6338, | 0.6338, | 0.6338, | 0.6339, | 0.0260, | 0.6339, | 0.0845, 0.6340, |
| | 0.6235 | 0.6235 | 0.6235 | 0.6235 | 0.6235 | 0.6235 | 0.6235 | 0.6235 | 0.6236 |
| MR-Weighted-Median | 0.0233 | 0.624, | 0.0233 | 0.0233 | 0.0233 | 0.0233 | 0.0233 | 0.558, | 0.0230 |
| mergineu-ivicuidii | -0.0936, | -0.0471, | -0.0285, | -0.0100, | -0.0008, | 0.0084, | 0.247, 0.0270, | 0.0455, | 0.982, |
| | 0.0203, | 0.0205, | 0.0205, | 0.0207, | 0.0208, | 0.0209, | 0.0211, | 0.0214, | 0.0223, |
| | 0.0208 | 0.0203, | 0.0211 | 0.0212 | 0.0213 | 0.0213 | 0.0211, | 0.0214, | 0.0223, |
| MR-Weighted-Mode | 1.000, | 0.787, | 0.383, | 0.097, | 0.058, | 0.086, | 0.345, | 0.732, | 0.999, |
| | -0.0966, | -0.0488, | -0.0295, | -0.0106, | -0.0011, | 0.0084, | 0.0278, | 0.0469, | 0.0948, |
| | 0.0179, | 0.0180, | 0.0177, | 0.0181, | 0.0183, | 0.0184, | 0.0188, | 0.0189, | 0.0195, |
| | 0.0176 | 0.0178 | 0.0179 | 0.018 | 0.018 | 0.0181 | 0.0182 | 0.0183 | 0.0188 |
| MR-RAPS1 | 0.158, | 0.095, | 0.079, | 0.068, | 0.064, | 0.060, | 0.063, | 0.064, | 0.106, |
| | -0.1095, | -0.0595, | -0.0395, | -0.0195, | -0.0095, | 0.0005, | 0.0205, | 0.0405, | 0.0905, |
| | 0.1323, | 0.1323, | 0.1323, | 0.1323, | 0.1323, | 0.1323, | 0.1323, | 0.1323, | 0.1323, |
| | 0.1278 | 0.1278 | 0.1278 | 0.1278 | 0.1278 | 0.1278 | 0.1278 | 0.1278 | 0.1278 |
| MR-RAPS2 | 0.154, | 0.099, | 0.085, | 0.072, | 0.071, | 0.067, | 0.071, | 0.067, | 0.100, |
| | -0.1105, | -0.0608, | -0.0405, | -0.0205, | -0.0105, | -0.0005, | 0.0195, | 0.0395, | 0.0894, |
| | 0.1474, | 0.1484, | 0.1474, | 0.1474, | 0.1474, | 0.1474, | 0.1474, | 0.1474, | 0.1474, |
| | 0.1398 | 0.1397 | 0.1398 | 0.1398 | 0.1398 | 0.1398 | 0.1398 | 0.1398 | 0.1398 |
| MR-RAPS3 | 0.910, | 0.886, | 0.863, | 0.854, | 0.865, | 0.867, | 0.890, | 0.885, | 0.923, |
| | -2.1143, | -0.7317, | -3.6738, | -2.4649, | -2.1861, | -2.4260, | 0.9557, | 7.6228, | -0.8295, |
| | 57.5230, | 115.9904, | 90.3998, | 190.1472, | 60.2495, | 127.6301, | 55.5136, | 250.1111, | 70.4745, |
| | 66.8294 | 275.8253 | 184.4749 | 847.3009 | 85.8505 | 441.303 | 75.8285 | 1644.7824 | 140.3801 |
| | 1.000, | 1.000, | 1.000, | 1.000, | 0.997, | 0.998, | 0.999, | 1.000, | 1.000, |
| MR-RAPS4 | | | | 0.1760 | 0.1605 | 1 0 1202 | 0.0207 | -0.0182, | -0.2419, |
| MR-RAPS4 | 0.6525, | 0.4226, | 0.3563, | 0.1760, | 0.1625, | 0.1393, | 0.0387, | | |
| MR-RAPS4 | | 0.4226, 1.4593, 0.0302 | 0.3563, 2.0883, 0.0538 | 0.1760, 1.5444, 0.0312 | 0.1625, 1.5643, 0.0316 | 1.5965, 0.0326 | 0.0387, 1.5797, 0.0309 | 1.4614, 0.028 | 1.3946, 0.0285 |

Table S78: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE satisfied, q=0.6, and N=100000.

| | · / | | | | | | | | |
|----------------------|---------------------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|------------------------|------------------------|-----------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.923, | 0.562, | 0.109, | 0.072, | 0.135, | 0.550, | 0.910, | 1.000, |
| | -0.0966, | -0.0467, | -0.0270, | -0.0084, | 0.0003, | 0.0089, | 0.0274, | 0.0471, | 0.0969, |
| | 1.460e- | 1.470e- | 1.430e- | 1.330e- | 1.310e- | 1.360e- | 1.490e- | 1.550e- | 1.600e- |
| cML-MA-AIC-Profile | 02, 0.0124 1.000, | 02, 0.0126 0.922, | 02, 0.0126 0.560, | 02, 0.0125 0.107, | 02, 0.0125 0.071, | 02, 0.0126 0.131, | 02, 0.0128 0.548, | 02, 0.013 | 02, 0.0133 1.000, |
| CWIL-WA-AIC-I TOILIC | -0.0968, | -0.0467, | -0.0270, | -0.0084, | 0.0003, | 0.0089, | 0.0274, | 0.0471, | 0.0971, |
| | 1.470e- | 1.470e- | 1.440e- | 1.330e- | 1.310e- | 1.360e- | 1.490e- | 1.560e- | 1.610e- |
| | 02, 0.0125 | 02, 0.0126 | 02, 0.0126 | 02, 0.0125 | 02, 0.0125 | 02, 0.0126 | 02, 0.0128 | 02, 0.013 | 02, 0.0133 |
| cML-AIC | 1.000, -0.0985, | 0.958, -0.0484, | 0.655, | 0.203, -0.0088, | 0.135, 0.0005, | 0.219, 0.0098, | 0.656, 0.0292, | 0.945, 0.0491, | 1.000, 0.0989, |
| | 1.520e- | 1.510e- | -0.0285, 1.510e- | 1.490e- | 1.480e- | 1.500e- | 1.580e- | 1.610e- | 1.680e- |
| | 02, 0.0111 | 02, 0.0112 | 02, 0.0113 | 02, 0.0114 | 02, 0.0114 | 02, 0.0114 | 02, 0.0115 | 02, 0.0116 | 02, 0.0119 |
| cML-AIC-Profile | 1.000, | 0.958, | 0.653, | 0.200, | 0.131, | 0.216, | 0.655, | 0.945, | 1.000, |
| | -0.0986, | -0.0485, | -0.0285, | -0.0088, | 0.0005, | 0.0098, | 0.0292, | 0.0492, | 0.0991, |
| | 1.520e- 02, 0.0112 | 1.510e- 02, 0.0113 | 1.510e- 02, 0.0113 | 1.490e- 02, 0.0114 | 1.480e- 02, 0.0114 | 1.500e- 02, 0.0115 | 1.580e- 02, 0.0116 | 1.620e- 02, 0.0116 | 1.680e- 02, 0.0119 |
| cML-MA-BIC | 1.000, | 0.999, | 0.803, | 0.162, | 0.042, | 0.167, | 0.798, | 0.996, | 1.000, |
| | -0.1000, | -0.0500, | -0.0300, | -0.0100, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 0.0999, |
| | 1.030e- | 1.050e- | 1.050e- | 1.060e- | 1.060e- | 1.070e- | 1.080e- | 1.090e- | 1.120e- |
| cML-MA-BIC-Profile | 02, 0.0103 1.000, | 02, 0.0104 0.999, | 02, 0.0105 0.801, | 02, 0.0105 0.161, | 02, 0.0106 0.042, | 02, 0.0106 0.165, | 02, 0.0107 0.797, | 02, 0.0107 0.996, | 02, 0.011 1.000, |
| CML-MA-BIC-Profile | -0.1000, | -0.0500, | -0.0300, | -0.0100, | -0.0001, | 0.165, 0.0099, | 0.797, 0.0299, | 0.996, 0.0499, | 0.0999, |
| | 1.030e- | 1.050e- | 1.050e- | 1.060e- | 1.060e- | 1.070e- | 1.080e- | 1.090e- | 1.120e- |
| | 02, 0.0103 | 02, 0.0104 | 02, 0.0105 | 02, 0.0105 | 02, 0.0106 | 02, 0.0106 | 02, 0.0107 | 02, 0.0108 | 02, 0.011 |
| cML-BIC | 1.000, | 0.999, | 0.806, | 0.167, | 0.043, | 0.176, | 0.806, | 0.996, | 1.000, |
| | -0.1001, 1.030e- | -0.0500, 1.040e- | -0.0300, 1.050e- | -0.0101, 1.060e- | -0.0001, 1.060e- | 0.0100, 1.070e- | 0.0299, 1.080e- | 0.0499, 1.090e- | 0.0999, 1.120e- |
| | 02, 0.0102 | 02, 0.0103 | 02, 0.0104 | 02, 0.0104 | 02, 0.0105 | 02, 0.0105 | 02, 0.0106 | 02, 0.0107 | 02, 0.0109 |
| cML-BIC-Profile | 1.000, | 0.999, | 0.804, | 0.167, | 0.043, | 0.176, | 0.804, | 0.996, | 1.000, |
| | -0.1001, | -0.0500, | -0.0300, | -0.0101, | -0.0001, | 0.0100, | 0.0299, | 0.0499, | 0.0999, |
| | 1.030e- | 1.040e- | 1.050e- | 1.060e- | 1.060e- | 1.070e- | 1.080e- | 1.090e- | 1.120e- |
| MR-Mix | 02, 0.0102 1.000, | 02, 0.0103 0.970, | 02, 0.0104 0.580, | 02, 0.0105 0.066, | 02, 0.0105 0.008, | 02, 0.0105 0.053, | 02, 0.0106 0.544, | 02, 0.0107 0.968, | 02, 0.0109 0.999, |
| IVIK-IVIIX | -0.0950, | -0.0468, | -0.0281, | -0.0095, | -0.0001, | 0.0033, | 0.0271, | 0.968, | 0.999, |
| | 1.060e- | 1.070e- | 1.080e- | 1.090e- | 1.090e- | 1.080e- | 1.070e- | 1.070e- | 1.100e- |
| | 02, 0.0131 | 02, 0.013 | 02, 0.0129 | 02, 0.0129 | 02, 0.0129 | 02, 0.0129 | 02, 0.0129 | 02, 0.0129 | 02, 0.0129 |
| MR-ContMix | 1.000, | 0.997, | 0.803, | 0.160, | 0.054, | 0.172, | 0.782, | 0.994, | 1.000, |
| | -0.0995, 1.070e- | -0.0498, 1.090e- | -0.0299, 1.090e- | -0.0100, 1.090e- | 0.0000, 1.100e- | 0.0099, 1.100e- | 0.0298, 1.120e- | 0.0497, 1.130e- | 0.0995, 1.160e- |
| | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA | 02, NA |
| MR-Lasso | 1.000, | 0.996, | 0.791, | 0.167, | 0.048, | 0.170, | 0.791, | 0.992, | 1.000, |
| | -0.0996, | -0.0499, | -0.0299, | -0.0100, | 0.0000, | 0.0099, | 0.0298, | 0.0498, | 0.0996, |
| | 1.080e- | 1.100e- | 1.090e- | 1.110e- | 1.120e- | 1.130e- | 1.140e- | 1.150e- | 1.160e- |
| MR-PRESSO | 02, 0.0105 0.977, | 02, 0.0106 0.917, | 02, 0.0106 0.711, | 02, 0.0107 0.347, | 02, 0.0107 0.294, | 02, 0.0108 0.355, | 02, 0.0108 0.734, | 02, 0.0109 0.908, | 02, 0.0111 0.980, |
| WIK-I KESSO | -0.0997, | -0.0500, | -0.0301, | -0.0103, | -0.0003, | 0.0096, | 0.0295, | 0.0497, | 0.0992, |
| | 3.090e- | 3.060e- | 3.040e- | 3.030e- | 3.030e- | 3.020e- | 3.010e- | 2.700e- | 2.650e- |
| | 02, 0.0107 | 02, 0.0107 | 02, 0.0108 | 02, 0.0108 | 02, 0.0108 | 02, 0.0109 | 02, 0.0109 | 02, 0.0109 | 02, 0.0111 |
| MR-IVW | 0.139, | 0.083, | 0.071, | 0.069, | 0.067, | 0.068, | 0.069, | 0.084, | 0.135, |
| | -0.1001, 1.356e- | -0.0499, 1.356e- | -0.0298, 1.356e- | -0.0097, 1.356e- | 0.0003, 1.356e- | 0.0104, 1.356e- | 0.0305, 1.356e- | 0.0505, 1.356e- | 0.1007, 1.355e- |
| | 01, 0.1277 | 01, 0.1277 | 01, 0.1277 | 01, 0.1277 | 01, 0.1277 | 01, 0.1277 | 01, 0.1277 | 01, 0.1277 | 01, 0.1277 |
| MR-IVW-Oracle | 1.000, | 0.999, | 0.786, | 0.150, | 0.033, | 0.147, | 0.783, | 0.995, | 1.000, |
| | -0.0997, | -0.0499, | -0.0299, | -0.0100, | -0.0001, | 0.0099, | 0.0298, | 0.0497, | 0.0995, |
| | 1.020e- 02, 0.0106 | 1.030e- 02, 0.0107 | 1.040e- 02, 0.0108 | 1.050e- 02, 0.0108 | 1.050e- 02, 0.0109 | 1.060e- 02, 0.0109 | 1.070e- 02, 0.011 | 1.080e- | 1.100e- 02, 0.0113 |
| MR-Egger | 0.058, | 0.057, | 0.059, | 0.060, | 0.063, | 0.062, | 0.062, | 02, 0.0111 | 0.066, |
| | -0.0848, | -0.0391, | -0.0208, | -0.0025, | 0.0066, | 0.0158, | 0.0340, | 0.0523, | 0.0979, |
| | 6.559e- | 6.559e- | 6.560e- | 6.560e- | 6.560e- | 6.561e- | 6.561e- | 6.561e- | 6.562e- |
| MD W ' 1. '27 " | 01, 0.6496 | 01, 0.6496 | 01, 0.6496 | 01, 0.6496 | 01, 0.6496 | 01, 0.6496 | 01, 0.6496 | 01, 0.6496 | 01, 0.6496 |
| MR-Weighted-Median | 1.000, -0.0955, | 0.898, -0.0476, | 0.471, -0.0285, | 0.088, -0.0093, | 0.038, 0.0003, | 0.097, 0.0098, | 0.466, 0.0288, | 0.872, 0.0479, | 1.000, 0.0955, |
| | -0.0955, 1.440e- | 1.460e- | 1.470e- | 1.470e- | 1.480e- | 0.0098, 1.490e- | 0.0288, 1.510e- | 0.0479, 1.520e- | 0.0933, 1.590e- |
| | 02, 0.0147 | 02, 0.0148 | 02, 0.0149 | 02, 0.015 | 02, 0.015 | 02, 0.0151 | 02, 0.0152 | 02, 0.0153 | 02, 0.0156 |
| MR-Weighted-Mode | 1.000, | 0.950, | 0.641, | 0.125, | 0.062, | 0.131, | 0.570, | 0.944, | 1.000, |
| | -0.0974, | -0.0487, | -0.0294, | -0.0098, | -0.0001, | 0.0096, | 0.0290, | 0.0484, | 0.0965, |
| | 1.320e- 02, 0.0127 | 1.360e- 02, 0.0128 | 1.350e- 02, 0.0129 | 1.370e- 02, 0.013 | 1.380e- 02, 0.013 | 1.380e- 02, 0.013 | 1.380e- 02, 0.0131 | 1.410e- 02, 0.0132 | 1.440e- 02, 0.0135 |
| MR-RAPS1 | 0.130, | 0.086, | 0.069, | 0.063, | 0.060, | 0.059, | 0.064, | 0.081, | 0.135, |
| WIK KAT ST | -0.1009, | -0.0509, | -0.0309, | -0.0109, | -0.0009, | 0.0091, | 0.0291, | 0.0491, | 0.0991, |
| | 1.324e- | 1.324e- | 1.324e- | 1.324e- | 1.324e- | 1.324e- | 1.324e- | 1.324e- | 1.324e- |
| 140 D : 222 | 01, 0.1274 | 01, 0.1274 | 01, 0.1274 | 01, 0.1274 | 01, 0.1274 | 01, 0.1274 | 01, 0.1274 | 01, 0.1274 | 01, 0.1274 |
| MR-RAPS2 | 0.122, -0.1012, | 0.088, -0.0512, | 0.072, -0.0312, | 0.070, -0.0112, | 0.062, -0.0012, | 0.062, 0.0088, | 0.067, | 0.085, 0.0488, | 0.125, 0.0988, |
| | -0.1012, 1.477e- | -0.0512, 1.476e- | -0.0312, 1.476e- | -0.0112, 1.476e- | -0.0012, 1.476e- | 0.0088, 1.476e- | 0.0288, 1.476e- | 0.0488, 1.476e- | 0.0988, 1.476e- |
| | 01, 0.1394 | 01, 0.1394 | 01, 0.1394 | 01, 0.1394 | 01, 0.1394 | 01, 0.1394 | 01, 0.1394 | 01, 0.1394 | 01, 0.1394 |
| MR-RAPS3 | 0.941, | 0.920, | 0.894, | 0.923, | 0.920, | 0.911, | 0.921, | 0.919, | 0.932, |
| | 503.2040, | 6.3746, | -11.3066, | -2.3240, | 2.8694, | -22.8691, | 2.4172, | 1.5489, | 7.4360, |
| | 1.594e+04, | 1.885e+02, | 2.174e+02, | 5.227e+01, | 8.390e+01, | 5.550e+02, | 9.464e+01, | 6.579e+01, | 1.186e+02 |
| | 3919000 | 570.8 | 725.9 1.000, | 46.58 0.997, | 134.1 0.997, | 5556 | 154.3 1.000, | 74.78 0.999, | 254.6 |
| MD DADCA | 1.000 | | | U.99/. | U.77/. | 0.999, | 1.000, | U.ソソソ, | 1.000, |
| MR-RAPS4 | 1.000, | 1.000, | | | | 0.0904 | | -0.2692 | -0.5520 |
| MR-RAPS4 | 1.000, 0.8504, 1.058e+00, | 0.6833, 1.392e+00, | 0.5158, 1.604e+00, | 0.2713, 1.657e+00, | 0.1822, 1.785e+00, | 0.0994, 1.724e+00, | -0.1098, 1.712e+00, | -0.2692, 1.694e+00, | -0.5520, 1.520e+00 |

Table S79: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE satisfied, q=0.6, and N=200000.

| ((| <i>')</i> | | <u>′</u> | | , I | | | | |
|----------------------|--|--|--|---|--|--|---|--|--|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.986, | 0.813, | 0.175, | 0.061, | 0.201, | 0.848, | 0.995, | 1.000, |
| | -0.0968, | -0.0470, | -0.0270, | -0.0080, | 0.0007, | 0.0093, | 0.0284, | 0.0482, | 0.0980, |
| | 0.0105, | 0.0107, | 0.0105, | 0.0097, | 0.0094, | 0.0099, | 0.0108, | 0.0110, | 0.0113, |
| | 0.0088 | 0.0089 | 0.009 | 0.0089 | 0.0088 | 0.0089 | 0.0091 | 0.0092 | 0.0094 |
| cML-MA-AIC-Profile | 1.000, | 0.986, | 0.812, | 0.173, | 0.060, | 0.197, | 0.847, | 0.993, | 1.000, |
| | -0.0970, | -0.0470, | -0.0270, | -0.0080, | 0.0007, | 0.0093, | 0.0284, | 0.0483, | 0.0982, |
| | 0.0106, | 0.0107, | 0.0105, | 0.0097, | 0.0094, | 0.0099, | 0.0108, | 0.0111, | 0.0113, |
| | 0.0089 | 0.009 | 0.009 | 0.0089 | 0.0089 | 0.0089 | 0.0091 | 0.0092 | 0.0094 |
| cML-AIC | 1.000, | 0.994, | 0.881, | 0.266, | 0.135, | 0.285, | 0.895, | 0.995, | 1.000, |
| | -0.0981, | -0.0483, | -0.0283, | -0.0087, | 0.0007, | 0.0101, | 0.0297, | 0.0495, | 0.0994, |
| | 0.0112, | 0.0115, | 0.0114, | 0.0109, | 0.0108, | 0.0110, | 0.0114, | 0.0115, | 0.0117, |
| | 0.0079 | 0.008 | 0.008 | 0.008 | 0.0081 | 0.0081 | 0.0081 | 0.0082 | 0.0084 |
| cML-AIC-Profile | 1.000, | 0.994, | 0.880, | 0.266, | 0.133, | 0.285, | 0.893, | 0.995, | 1.000, |
| | -0.0982, 0.0112, | -0.0483, 0.0115, | -0.0283, | -0.0087, 0.0109, | 0.0007, | 0.0101, 0.0110, | 0.0297, 0.0114, | 0.0496, | 0.0995, |
| | 0.0112, | 0.0113, | 0.0114, 0.008 | 0.0109, | 0.0108, 0.0081 | 0.0110, | 0.0114, | 0.0115, 0.0082 | 0.0118, 0.0084 |
| cML-MA-BIC | 1.000, | 1.000, | 0.983, | 0.260, | 0.0081 | 0.300, | 0.987, | 1.000, | 1.000, |
| CIVIL-IVIA-DIC | -0.0997, | -0.0496, | -0.0296, | -0.0096, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077, |
| | 0.0073 | 0.0073 | 0.0074 | 0.0074 | 0.0074 | 0.0075 | 0.0075 | 0.0076 | 0.0077 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.983, | 0.260, | 0.044, | 0.296, | 0.986, | 1.000, | 1.000, |
| cond mar bio riome | -0.0997, | -0.0496, | -0.0296, | -0.0096, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077, |
| | 0.0073 | 0.0074 | 0.0074 | 0.0074 | 0.0075 | 0.0075 | 0.0075 | 0.0076 | 0.0078 |
| cML-BIC | 1.000, | 1.000, | 0.985, | 0.270, | 0.045, | 0.297, | 0.985, | 1.000, | 1.000, |
| | -0.0997, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077, |
| | 0.0072 | 0.0073 | 0.0073 | 0.0074 | 0.0074 | 0.0074 | 0.0075 | 0.0075 | 0.0077 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.985, | 0.270, | 0.044, | 0.294, | 0.985, | 1.000, | 1.000, |
| | -0.0997, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077, |
| | 0.0072 | 0.0073 | 0.0073 | 0.0074 | 0.0074 | 0.0074 | 0.0075 | 0.0075 | 0.0077 |
| MR-Mix | 1.000, | 0.999, | 0.883, | 0.170, | 0.035, | 0.183, | 0.886, | 0.999, | 1.000, |
| | -0.0946, | -0.0466, | -0.0276, | -0.0089, | 0.0002, | 0.0094, | 0.0277, | 0.0456, | 0.0895, |
| | 0.0081, | 0.0079, | 0.0078, | 0.0080, | 0.0081, | 0.0081, | 0.0078, | 0.0079, | 0.0080, |
| | 0.0099 | 0.0099 | 0.0099 | 0.0098 | 0.0098 | 0.0098 | 0.0098 | 0.0098 | 0.0098 |
| MR-ContMix | 1.000, | 1.000, | 0.981, | 0.260, | 0.053, | 0.294, | 0.985, | 1.000, | 1.000, |
| | -0.0994, | -0.0495, | -0.0296, | -0.0096, | 0.0004, | 0.0103, | 0.0303, | 0.0503, | 0.1002, |
| | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0075, | 0.0075, | 0.0076, | 0.0077, | 0.0079, |
|) (D. I | NA | NA 1,000 | NA 0.072 | NA 0.250 | NA 0.055 | NA 0.200 | NA 0.072 | NA 1 000 | NA |
| MR-Lasso | 1.000, | 1.000, | 0.973, | 0.258, | 0.055, | 0.290, | 0.973, | 1.000, | 1.000, |
| | -0.0995, | -0.0496, | -0.0295, | -0.0095, | 0.0005, | 0.0105, | 0.0304, 0.0079, | 0.0503, | 0.1003, |
| | 0.0077, 0.0074 | 0.0077, 0.0075 | 0.0078, 0.0075 | 0.0078, 0.0076 | 0.0078, 0.0076 | 0.0078, 0.0076 | 0.0079, | 0.0080, 0.0077 | 0.0082, 0.0079 |
| MR-PRESSO | 0.964, | 0.0073 | 0.822, | 0.490, | 0.391, | 0.518, | 0.839, | | 0.0079 |
| MK-PKESSO | -0.0976, | -0.0485, | -0.0286, | -0.0088, | 0.391, | 0.0108, | 0.839, | 0.894, 0.0508, | 0.971, 0.1007, |
| | 0.0587, | 0.0568, | 0.0568, | 0.0566, | 0.0578, | 0.0578, | 0.0510, | 0.0557, | 0.0554, |
| | 0.0387, | 0.0308, | 0.0106 | 0.0106 | 0.0378, | 0.0107 | 0.0106 | 0.0105 | 0.0334, |
| MR-IVW | 0.129, | 0.084, | 0.074, | 0.065, | 0.065, | 0.060, | 0.065, | 0.071, | 0.138, |
| | -0.0973, | -0.0470, | -0.0269, | -0.0068, | 0.0033, | 0.0133, | 0.0335, | 0.0536, | 0.1038, |
| | 0.1332, | 0.1332, | 0.1332, | 0.1332, | 0.1332, | 0.1332, | 0.1332, | 0.1332, | 0.1332, |
| | 0.1278 | 0.1278 | 0.1278 | 0.1278 | 0.1278 | 0.1278 | 0.1278 | 0.1278 | 0.1278 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.982, | 0.242, | 0.039, | 0.275, | 0.980, | 1.000, | 1.000, |
| | -0.0995, | -0.0496, | -0.0296, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0502, | 0.1002, |
| | 0.0072, | 0.0072, | 0.0073, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0075, | 0.0076, |
| | 0.0075 | 0.0076 | 0.0076 | 0.0077 | 0.0077 | 0.0077 | 0.0078 | 0.0078 | 0.008 |
| MR-Egger | 0.060, | 0.053, | 0.053, | 0.051, | 0.052, | 0.052, | 0.053, | 0.056, | 0.054, |
| | -0.1015, | -0.0536, | -0.0344, | -0.0152, | -0.0057, | 0.0039, | 0.0231, | 0.0422, | 0.0901, |
| | 0.6714, | 0.6713, | 0.6713, | 0.6712, | 0.6712, | 0.6712, | 0.6712, | 0.6712, | 0.6711, |
| | 0.6652 | 0.6652 | 0.6652 | 0.6652 | 0.6652 | 0.6652 | 0.6652 | 0.6652 | 0.6652 |
| MR-Weighted-Median | 1.000, | 0.992, | 0.774, | 0.144, | 0.050, | 0.155, | 0.796, | 0.991, | 1.000, |
| | -0.0966, | -0.0480, | -0.0285, | -0.0091, | 0.0006, | 0.0103, | 0.0296, | 0.0490, | 0.0974, |
| | 0.0103, | 0.0104, | 0.0105, | 0.0106, | 0.0106, | 0.0107, | 0.0108, | 0.0109, | 0.0112, |
| | 0.0104 | 0.0105 | 0.0106 | 0.0106 | 0.0106 | 0.0107 | 0.0107 | 0.0108 | 0.0111 |
| MR-Weighted-Mode | 1.000, | 0.997, | 0.838, | 0.175, | 0.063, | 0.204, | 0.839, | 0.996, | 1.000, |
| | -0.0979, | -0.0489, | -0.0290, | -0.0093, | 0.0004, | 0.0104, | 0.0298, | 0.0491, | 0.0984, |
| | 0.0104, | 0.0102, | 0.0104, | 0.0104, | 0.0107, | 0.0107, | 0.0108, | 0.0107, | 0.0108, |
| MD D / PG1 | 0.0097 | 0.0097 | 0.0098 | 0.0098 | 0.0099 | 0.0099 | 0.0099 | 0.01 | 0.0101 |
| MR-RAPS1 | 0.130, | 0.072, | 0.062, | 0.054, | 0.051, | 0.051, | 0.062, | 0.072, | 0.132, |
| | | -0.0470, | -0.0270, 0.1289, | -0.0070, 0.1289, | 0.0030, 0.1289, | 0.0130, 0.1289, | 0.0330, 0.1289, | 0.0530, | 0.1030, 0.1289, |
| | -0.0970, | 0.1200 | | 0.1289, 0.1272 | 0.1289, 0.1272 | 0.1289, 0.1272 | 0.1289, 0.1272 | 0.1289, 0.1272 | 0.1289, |
| | 0.1289, | 0.1289, | 0.1272 | 0.1474 | | | | | 0.1273 |
| MP PADS2 | 0.1289, 0.1272 | 0.1272 | 0.1272 | | 0.057 | 0.050 | | | |
| MR-RAPS2 | 0.1289, 0.1272 0.135, | 0.1272 0.081, | 0.073, | 0.060, | 0.057, | 0.059, | 0.069, | 0.078, | |
| MR-RAPS2 | 0.1289, 0.1272 0.135, -0.0858, | 0.1272 0.081, -0.0419, | 0.073, -0.0247, | 0.060, -0.0068, | 0.0033, | 0.0126, | 0.0332, | 0.0525, | 0.1032, |
| MR-RAPS2 | 0.1289, 0.1272 0.135, -0.0858, 0.1858, | 0.1272 0.081, -0.0419, 0.1756, | 0.073, -0.0247, 0.1617, | 0.060, -0.0068, 0.1438, | 0.0033, 0.1438, | 0.0126, 0.1457, | 0.0332, 0.1439, | 0.0525, 0.1518, | 0.1032, 0.1439, |
| | 0.1289, 0.1272 0.135, -0.0858, 0.1858, 0.1382 | 0.1272 0.081, -0.0419, 0.1756, 0.1387 | 0.073, -0.0247, 0.1617, 0.1389 | 0.060, -0.0068, 0.1438, 0.1392 | 0.0033, 0.1438, 0.1391 | 0.0126, 0.1457, 0.1389 | 0.0332, 0.1439, 0.1393 | 0.0525, 0.1518, 0.1388 | 0.1032, 0.1439, 0.1393 |
| MR-RAPS2 MR-RAPS3 | 0.1289, 0.1272 0.135, -0.0858, 0.1858, 0.1382 0.954, | 0.1272 0.081, -0.0419, 0.1756, 0.1387 0.946, | 0.073, -0.0247, 0.1617, 0.1389 0.929, | 0.060, -0.0068, 0.1438, 0.1392 0.934, | 0.0033, 0.1438, 0.1391 0.942, | 0.0126, 0.1457, 0.1389 0.944, | 0.0332, 0.1439, 0.1393 0.933, | 0.0525, 0.1518, 0.1388 0.931, - | 0.1032, 0.1439, 0.1393 0.963, |
| | 0.1289, 0.1272 0.135, -0.0858, 0.1858, 0.1382 0.954, 12.3642, | 0.1272 0.081, -0.0419, 0.1756, 0.1387 0.946, 6.7734, | 0.073, -0.0247, 0.1617, 0.1389 0.929, -0.4972, | 0.060, -0.0068, 0.1438, 0.1392 0.934, -10.9033, | 0.0033, 0.1438, 0.1391 0.942, -2.8934, | 0.0126, 0.1457, 0.1389 0.944, -5.2507, | 0.0332, 0.1439, 0.1393 0.933, 0.3578, | 0.0525, 0.1518, 0.1388 0.931, - 316.9602, | 0.1032, 0.1439, 0.1393 0.963, 2.2182, |
| | 0.1289, 0.1272 0.135, -0.0858, 0.1858, 0.1382 0.954, 12.3642, 306.2539, | 0.1272 0.081, -0.0419, 0.1756, 0.1387 0.946, 6.7734, 240.0308, | 0.073, -0.0247, 0.1617, 0.1389 0.929, -0.4972, 82.9198, | 0.060, -0.0068, 0.1438, 0.1392 0.934, -10.9033, 354.2821, | 0.0033, 0.1438, 0.1391 0.942, -2.8934, 155.7400, | 0.0126, 0.1457, 0.1389 0.944, -5.2507, 189.0625, | 0.0332, 0.1439, 0.1393 0.933, 0.3578, 133.3709, | 0.0525, 0.1518, 0.1388 0.931, - 316.9602, 9703.3823, | 0.1032, 0.1439, 0.1393 0.963, 2.2182, 52.7535, |
| MR-RAPS3 | 0.1289, 0.1272 0.135, -0.0858, 0.1858, 0.1382 0.954, 12.3642, 306.2539, 912.4 | 0.1272 0.081, -0.0419, 0.1756, 0.1387 0.946, 6.7734, 240.0308, 678.1 | 0.073, -0.0247, 0.1617, 0.1389 0.929, -0.4972, 82.9198, 80.98 | 0.060, -0.0068, 0.1438, 0.1392 0.934, -10.9033, 354.2821, 1499 | 0.0033, 0.1438, 0.1391 0.942, -2.8934, 155.7400, 268.9 | 0.0126, 0.1457, 0.1389 0.944, -5.2507, 189.0625, 494.7 | 0.0332, 0.1439, 0.1393 0.933, 0.3578, 133.3709, 224.1 | 0.0525, 0.1518, 0.1388 0.931, - 316.9602, 9703.3823, 1083000 | 0.1032, 0.1439, 0.1393 0.963, 2.2182, 52.7535, 43.62 |
| | 0.1289, 0.1272 0.135, -0.0858, 0.1858, 0.1382 0.954, 12.3642, 306.2539, 912.4 | 0.1272 0.081, -0.0419, 0.1756, 0.1387 0.946, 6.7734, 240.0308, 678.1 | 0.073, -0.0247, 0.1617, 0.1389 0.929, -0.4972, 82.9198, 80.98 | 0.060, -0.0068, 0.1438, 0.1392 0.934, -10.9033, 354.2821, 1499 1.000, | 0.0033, 0.1438, 0.1391 0.942, -2.8934, 155.7400, 268.9 0.999, | 0.0126, 0.1457, 0.1389 0.944, -5.2507, 189.0625, 494.7 0.999, | 0.0332, 0.1439, 0.1393 0.933, 0.3578, 133.3709, 224.1 1.000, | 0.0525, 0.1518, 0.1388 0.931, - 316.9602, 9703.3823, 1083000 1.000, | 0.1032, 0.1439, 0.1393 0.963, 2.2182, 52.7535, 43.62 1.000, |
| MR-RAPS3 | 0.1289, 0.1272 0.135, -0.0858, 0.1858, 0.1382 0.954, 12.3642, 306.2539, 912.4 | 0.1272 0.081, -0.0419, 0.1756, 0.1387 0.946, 6.7734, 240.0308, 678.1 | 0.073, -0.0247, 0.1617, 0.1389 0.929, -0.4972, 82.9198, 80.98 | 0.060, -0.0068, 0.1438, 0.1392 0.934, -10.9033, 354.2821, 1499 | 0.0033, 0.1438, 0.1391 0.942, -2.8934, 155.7400, 268.9 | 0.0126, 0.1457, 0.1389 0.944, -5.2507, 189.0625, 494.7 | 0.0332, 0.1439, 0.1393 0.933, 0.3578, 133.3709, 224.1 | 0.0525, 0.1518, 0.1388 0.931, - 316.9602, 9703.3823, 1083000 | 0.1032, 0.1439, 0.1393 0.963, 2.2182, 52.7535, 43.62 |

Table S80: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m = 100, the InSIDE violated, q = 0.2, and N = 50000.

| | · / | | | | | | | | _ |
|--------------------|---------------------|------------------------------|------------------------------|-----------------------------|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.972, | 0.673, | 0.168, | 0.091, | 0.189, | 0.691, | 0.969, | 1.000, |
| CML-MA-AIC | -0.0969, | -0.0472, | -0.0274, | -0.0083, | 0.091, | 0.189, | 0.091, | 0.969, | 0.0982, |
| | 0.0132, | 0.0133, | 0.0133, | 0.0125, | 0.0123, | 0.0036, | 0.0136, | 0.0139, | 0.0382, |
| | 0.0105 | 0.0107 | 0.0107 | 0.0107 | 0.0107 | 0.0108 | 0.011 | 0.0111 | 0.0114 |
| cML-MA-AIC-Profile | 1.000, | 0.971, | 0.672, | 0.165, | 0.090, | 0.183, | 0.689, | 0.969, | 1.000, |
| | -0.0974, | -0.0474, | -0.0274, | -0.0083, | 0.0006, | 0.0096, | 0.0287, | 0.0487, | 0.0987, |
| | 0.0133, | 0.0134, | 0.0133, | 0.0125, | 0.0123, | 0.0126, | 0.0137, | 0.0139, | 0.0143, |
| cML-AIC | 0.0106 | 0.0107 0.984, | 0.0108 | 0.0107 | 0.0108 | 0.0108 | 0.011 | 0.0112 | 0.0115 |
| CML-AIC | 1.000, -0.0982, | -0.0485, | 0.744, -0.0285, | 0.247, -0.0087, | 0.156, 0.0008, | 0.268, 0.0102, | 0.763, 0.0299, | 0.980, 0.0499, | 1.000, 0.0998, |
| | 0.0137, | 0.0139, | 0.0139, | 0.0138, | 0.0008, | 0.0140, | 0.0143, | 0.0145, | 0.0147, |
| | 0.0096 | 0.0097 | 0.0098 | 0.0099 | 0.0099 | 0.01 | 0.01 | 0.0101 | 0.0104 |
| cML-AIC-Profile | 1.000, | 0.984, | 0.743, | 0.243, | 0.152, | 0.264, | 0.759, | 0.980, | 1.000, |
| | -0.0985, | -0.0486, | -0.0285, | -0.0087, | 0.0008, | 0.0102, | 0.0299, | 0.0499, | 0.1001, |
| | 0.0139, | 0.0140, | 0.0140, | 0.0138, | 0.0138, | 0.0140, | 0.0144, | 0.0145, | 0.0149, |
| cML-MA-BIC | 0.0097 | 0.0098 1.000, | 0.0099 | 0.0099 | 0.01 | 0.01 | 0.0101 | 0.0102 | 0.0105 |
| CML-MA-BIC | 1.000, -0.0998, | -0.0498, | 0.901, -0.0298, | -0.0098, | 0.055, | 0.200, 0.0102, | 0.893, 0.0302, | 1.000, 0.0502, | 1.000, 0.1003, |
| | 0.0090, | 0.0091, | 0.0092, | 0.0093, | 0.0002, | 0.0093, | 0.0094, | 0.0095, | 0.1003, |
| | 0.0089 | 0.009 | 0.0091 | 0.0091 | 0.0092 | 0.0092 | 0.0093 | 0.0094 | 0.0097 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.901, | 0.191, | 0.055, | 0.199, | 0.890, | 1.000, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0502, | 0.1003, |
| | 0.0090, | 0.0091, | 0.0092, | 0.0093, | 0.0093, | 0.0093, | 0.0094, | 0.0095, | 0.0098, |
| JH DIC | 0.0089 | 0.0091 | 0.0091 | 0.0092 | 0.0092 | 0.0093 | 0.0093 | 0.0094 | 0.0097 |
| cML-BIC | 1.000, | 1.000, -0.0499, | 0.906, | 0.196, | 0.061, 0.0002, | 0.203, 0.0102, | 0.897, 0.0302, | 1.000, | 1.000, |
| | -0.0999, 0.0091, | 0.0499, | -0.0298, 0.0092, | -0.0098, 0.0093, | 0.0002, 0.0093, | 0.0102, 0.0094, | 0.0302, 0.0094, | 0.0503, 0.0095, | 0.1003, 0.0098, |
| | 0.0091, | 0.0092, | 0.0092, | 0.0093, | 0.0093, | 0.0094, | 0.0094, | 0.0093 | 0.0096 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.903, | 0.193, | 0.059, | 0.203, | 0.897, | 1.000, | 1.000, |
| | -0.0999, | -0.0499, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0503, | 0.1003, |
| | 0.0091, | 0.0092, | 0.0092, | 0.0093, | 0.0093, | 0.0094, | 0.0094, | 0.0095, | 0.0098, |
| | 0.0089 | 0.009 | 0.009 | 0.0091 | 0.0091 | 0.0092 | 0.0093 | 0.0094 | 0.0096 |
| MR-Mix | 0.999, | 0.884, | 0.392, | 0.030, | 0.004, | 0.023, | 0.330, | 0.853, | 1.000, |
| | -0.1108, 0.0132, | -0.0548, 0.0130, | -0.0327, 0.0131, | -0.0111, 0.0131, | -0.0004, 0.0130, | 0.0103, 0.0131, | 0.0311, 0.0131, | 0.0517, 0.0132, | 0.1012, 0.0133, |
| | 0.0132, | 0.0130, | 0.0131, | 0.0131, | 0.0130, | 0.0131, | 0.0131, | 0.0132, | 0.0133, |
| MR-ContMix | 1.000, | 1.000, | 0.882, | 0.197, | 0.055, | 0.188, | 0.864, | 0.999, | 1.000, |
| mic commi | -0.0990, | -0.0494, | -0.0296, | -0.0097, | 0.0003, | 0.0102, | 0.0301, | 0.0499, | 0.0996, |
| | 0.0094, | 0.0095, | 0.0096, | 0.0096, | 0.0097, | 0.0097, | 0.0098, | 0.0099, | 0.0103, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 1.000, | 0.883, | 0.195, | 0.068, | 0.221, | 0.888, | 1.000, | 1.000, |
| | -0.0990, | -0.0493, 0.0095, | -0.0295, | -0.0096, 0.0097, | 0.0004, 0.0097, | 0.0103, 0.0098, | 0.0302, 0.0098, | 0.0500, | 0.0998, 0.0103, |
| | 0.0094, 0.0089 | 0.0095, | 0.0096, 0.0091 | 0.0097, | 0.0097, | 0.0098, | 0.0098, | 0.0099, 0.0094 | 0.0103, |
| MR-PRESSO | 1.000, | 0.982, | 0.834, | 0.214, | 0.138, | 0.310, | 0.895, | 0.999, | 1.000, |
| TREBBO | -0.0966, | -0.0471, | -0.0273, | -0.0075, | 0.0024, | 0.0124, | 0.0322, | 0.0520, | 0.1014, |
| | 0.0121, | 0.0120, | 0.0120, | 0.0120, | 0.0119, | 0.0119, | 0.0119, | 0.0118, | 0.0118, |
| | 0.0086 | 0.0087 | 0.0087 | 0.0088 | 0.0088 | 0.0089 | 0.009 | 0.009 | 0.0093 |
| MR-IVW | 0.168, | 0.084, | 0.078, | 0.091, | 0.100, | 0.101, | 0.143, | 0.208, | 0.420, |
| | -0.0692, | -0.0193, | 0.0006, | 0.0205, | 0.0305, | 0.0405, | 0.0604, | 0.0804, | 0.1302, |
| | 0.0809, 0.0749 | 0.0809, 0.0749 | 0.0809, 0.0749 | 0.0809, 0.0749 | 0.0809, 0.0749 | 0.0809, 0.0749 | 0.0809, 0.0749 | 0.0809, 0.0749 | 0.0809, 0.0749 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.901, | 0.184, | 0.053, | 0.0745 | 0.886, | 1.000, | 1.000, |
| mit i m onucio | -0.0992, | -0.0495, | -0.0296, | -0.0098, | 0.0002, | 0.0101, | 0.0300, | 0.0499, | 0.0995, |
| | 0.0089, | 0.0090, | 0.0091, | 0.0091, | 0.0092, | 0.0092, | 0.0093, | 0.0094, | 0.0097, |
| | 0.009 | 0.0092 | 0.0092 | 0.0093 | 0.0093 | 0.0094 | 0.0095 | 0.0095 | 0.0098 |
| MR-Egger | 0.349, | 0.366, | 0.380, | 0.382, | 0.385, | 0.392, | 0.409, | 0.422, | 0.456, |
| | 0.3253, | 0.3702, | 0.3882, | 0.4061, | 0.4151, | 0.4241, | 0.4420, | 0.4599, | 0.5047, |
| | 0.4658, 0.2819 | 0.4660, 0.282 | 0.4660, 0.282 | 0.4661, 0.2821 | 0.4661, 0.2821 | 0.4661, 0.2821 | 0.4662, 0.2822 | 0.4663, 0.2822 | 0.4664, 0.2823 |
| MR-Weighted-Median | 1.000, | 0.282 | 0.636, | 0.2821 | 0.2821 | 0.2821 | 0.2822 | 0.2822 | 1.000, |
| | -0.0980, | -0.0496, | -0.0303, | -0.0111, | -0.0014, | 0.0082, | 0.0275, | 0.0468, | 0.0950, |
| | 0.0118, | 0.0119, | 0.0120, | 0.0121, | 0.0122, | 0.0123, | 0.0124, | 0.0126, | 0.0130, |
| | 0.0129 | 0.013 | 0.0131 | 0.0132 | 0.0133 | 0.0133 | 0.0134 | 0.0136 | 0.0139 |
| MR-Weighted-Mode | 0.939, | 0.506, | 0.183, | 0.021, | 0.006, | 0.019, | 0.174, | 0.512, | 0.923, |
| | -0.0972, | -0.0486, | -0.0296, | -0.0097, | -0.0004, | 0.0096, | 0.0290, | 0.0492, | 0.0966, |
| | 0.0308, 0.048 | 0.0301, 0.0483 | 0.0296, 0.0484 | 0.0296, 0.0487 | 0.0287, 0.0488 | 0.0288, 0.0489 | 0.0295, 0.0491 | 0.0289, 0.0493 | 0.0298, 0.0501 |
| MR-RAPS1 | 0.048 | 0.0483 | 0.0484 | 0.0487 | 0.0488 | 0.0489 | 0.0491 | 0.0493 | 0.0501 |
| WIN-IXAL 91 | -0.0698, | -0.0198, | 0.009, | 0.074, 0.0203, | 0.083, | 0.0403, | 0.142, 0.0603, | 0.203, | 0.419, |
| | 0.0789, | 0.0789, | 0.0789, | 0.0789, | 0.0789, | 0.0789, | 0.0789, | 0.0789, | 0.0790, |
| | 0.0747 | 0.0747 | 0.0747 | 0.0747 | 0.0747 | 0.0747 | 0.0747 | 0.0748 | 0.0748 |
| MR-RAPS2 | 1.000, | 1.000, | 0.962, | 0.653, | 0.559, | 0.640, | 0.967, | 1.000, | 1.000, |
| | 0.0184, | 0.0428, | 0.0682, | 0.1387, | 0.1015, | 0.1526, | 0.1430, | 0.2281, | 0.2073, |
| | 0.7491, | 0.7641, | 0.7370, | 1.1355, | 1.3704, | 0.7543, | 0.8293, | 0.7863, | 1.9485, |
| MD DADG2 | 0.0125 0.887, | 0.0125 | 0.0122 | 0.0133 | 0.0126 | 0.0125 | 0.0134 | 0.0131 | 0.0145 |
| MR-RAPS3 | -0.1942, | 0.853, -0.0490, | 0.846, 0.0058, | 0.847, 0.0577, | 0.857, 0.0825, | 0.869, 0.1066, | 0.875, 0.1522, | 0.911, 0.1947, | 0.959, 0.2884, |
| | 0.2254, | 0.2245, | 0.2200, | 0.0377, | 0.0823, | 0.1000, | 0.1322, | 0.1947, | 0.2884, |
| | 0.0248 | 0.0238 | 0.0232 | 0.0227 | 0.0224 | 0.0221 | 0.0215 | 0.0209 | 0.0196 |
| | 1.000, | 1.000, | 0.975, | 0.753, | 0.675, | 0.737, | 0.985, | 1.000, | 1.000, |
| MR-RAPS4 | | | | | | | | | |
| MR-RAPS4 | 0.0747, | 0.0707, | 0.1220, | 0.1447, | 0.1786, | 0.1954, | 0.2146, | 0.2529, | 0.3087, |
| MR-RAPS4 | | 0.0707, 0.9559, 0.0147 | 0.1220, 0.8988, 0.0141 | 0.1447, 0.9533, 0.015 | 0.1786, 0.8948, 0.0141 | 0.1954, 0.9082, 0.0143 | 0.2146, 0.9771, 0.0159 | 0.2529, 0.9886, 0.0155 | 0.3087, 1.0549, 0.0161 |

Table S81: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.2, and N=100000.

| ((| <i>' '</i> | | | | ′ 1 | | | | |
|--------------------|--------------------|--------------------|---------------------|--------------------|-------------------|-------------------|-------------------|--------------------|-------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 1.000, | 0.925, | 0.252, | 0.083, | 0.248, | 0.916, | 0.998, | 1.000, |
| | -0.0980, | -0.0483, | -0.0284, | -0.0089, | 0.0001, | 0.0092, | 0.0287, | 0.0485, | 0.0982, |
| | 0.0090, | 0.0092, | 0.0093, | 0.0088, | 0.0085, | 0.0089, | 0.0095, | 0.0097, | 0.0099, |
| | 0.0074 | 0.0075 | 0.0076 | 0.0076 | 0.0076 | 0.0076 | 0.0078 | 0.0079 | 0.0081 |
| cML-MA-AIC-Profile | 1.000, | 1.000, | 0.925, | 0.248, | 0.081, | 0.248, | 0.916, | 0.998, | 1.000, |
| | -0.0984, | -0.0484, | -0.0284, | -0.0089, | 0.0001, | 0.0092, | 0.0287, | 0.0486, | 0.0985, |
| | 0.0091, | 0.0092, | 0.0093, | 0.0088, | 0.0085, | 0.0089, | 0.0096, | 0.0097, | 0.0100, |
| | 0.0075 | 0.0076 | 0.0076 | 0.0076 | 0.0076 | 0.0077 | 0.0078 | 0.0079 | 0.0081 |
| cML-AIC | 1.000, | 1.000, | 0.940, | 0.333, | 0.144, | 0.332, | 0.932, | 0.999, | 1.000, |
| | -0.0990, | -0.0492, | -0.0293, | -0.0094, | 0.0002, | 0.0098, | 0.0295, | 0.0495, | 0.0992, |
| | 0.0095, | 0.0096, | 0.0097, | 0.0096, | 0.0095, | 0.0097, | 0.0100, | 0.0101, | 0.0103, |
| ·ML AIC D. · Cl. | 0.0068 | 0.0069 | 0.0069 | 0.007 | 0.007 | 0.007 | 0.0071 | 0.0072 | 0.0074 |
| cML-AIC-Profile | 1.000, -0.0992, | 1.000, -0.0492, | 0.940, | 0.330, -0.0094, | 0.142, 0.0002, | 0.331, 0.0098, | 0.932, 0.0296, | 0.999, | 1.000, 0.0994, |
| | 0.0095, | 0.0096, | -0.0293, 0.0097, | 0.0094, | 0.0002, | 0.0098, | 0.0290, | 0.0495, 0.0101, | 0.0994, |
| | 0.0068 | 0.0090, | 0.0057, | 0.007 | 0.0093, | 0.0057, | 0.0101, | 0.0101, | 0.0104, |
| cML-MA-BIC | 1.000, | 1.000, | 0.995, | 0.335, | 0.048, | 0.335, | 0.992, | 1.000, | 1.000, |
| und mit bio | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0501, | 0.1001, |
| | 0.0063, | 0.0064, | 0.0064, | 0.0065, | 0.0065, | 0.0065, | 0.0066, | 0.0067, | 0.0069, |
| | 0.0063 | 0.0064 | 0.0064 | 0.0065 | 0.0065 | 0.0065 | 0.0066 | 0.0066 | 0.0068 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.995, | 0.333, | 0.048, | 0.334, | 0.992, | 1.000, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0501, | 0.1001, |
| | 0.0063, | 0.0064, | 0.0064, | 0.0065, | 0.0065, | 0.0065, | 0.0066, | 0.0067, | 0.0069, |
| | 0.0063 | 0.0064 | 0.0064 | 0.0065 | 0.0065 | 0.0065 | 0.0066 | 0.0067 | 0.0068 |
| cML-BIC | 1.000, | 1.000, | 0.995, | 0.347, | 0.053, | 0.340, | 0.993, | 1.000, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0502, | 0.1002, |
| | 0.0063, | 0.0064, | 0.0064, | 0.0065, | 0.0065, | 0.0065, | 0.0066, | 0.0067, | 0.0069, |
| | 0.0062 | 0.0063 | 0.0064 | 0.0064 | 0.0064 | 0.0065 | 0.0065 | 0.0066 | 0.0068 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.995, | 0.344, | 0.052, | 0.338, | 0.993, | 1.000, 0.0502, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0502, | 0.1002, |
| | 0.0063, | 0.0064, | 0.0064, | 0.0065, | 0.0065, | 0.0065, | 0.0066, | 0.0067, | 0.0069, |
| | 0.0062 | 0.0063 | 0.0064 | 0.0064 | 0.0065 | 0.0065 | 0.0065 | 0.0066 | 0.0068 |
| MR-Mix | 0.999, | 0.981, | 0.578, | 0.037, | 0.006, | 0.048, | 0.614, | 0.967, | 1.000, |
| | -0.1102, | -0.0539, | -0.0320, | -0.0102, | 0.0004, | 0.0111, | 0.0320, | 0.0527, | 0.1021, |
| | 0.0102, | 0.0099, | 0.0098, | 0.0099, | 0.0100, | 0.0100, | 0.0100, | 0.0100, | 0.0102, |
| 100 0 10 | 0.0155 | 0.0153 | 0.0153 | 0.0152 | 0.0152 | 0.0152 | 0.0152 | 0.0151 | 0.015 |
| MR-ContMix | 1.000, | 1.000, | 0.992, | 0.336, | 0.054, | 0.324, | 0.993, | 1.000, | 1.000, |
| | -0.0995, | -0.0497, | -0.0297, | -0.0098, | 0.0002, | 0.0101, | 0.0300, | 0.0500, | 0.0998, |
| | 0.0065, | 0.0066, | 0.0066, | 0.0066, | 0.0067, | 0.0067, | 0.0067, | 0.0068, | 0.0070, |
| MR-Lasso | NA 1.000, | NA 1.000, | NA 0.992, | NA 0.337, | NA 0.057, | NA 0.341, | NA 0.991, | NA 1.000, | NA 1.000, |
| WIK-Lasso | -0.0994, | -0.0496, | -0.0296, | -0.0097, | 0.0003, | 0.0102, | 0.0301, | 0.0500, | 0.0998, |
| | 0.0065, | 0.0066, | 0.0066, | 0.0067, | 0.0068, | 0.0102, | 0.0301, | 0.0300, | 0.0998, |
| | 0.0063 | 0.0064 | 0.0064 | 0.0065 | 0.0065 | 0.0065 | 0.0066 | 0.0067 | 0.0068 |
| MR-PRESSO | 0.997, | 0.964, | 0.891, | 0.385, | 0.249, | 0.507, | 0.964, | 0.998, | 1.000, |
| WIR TRESSO | -0.0952, | -0.0456, | -0.0258, | -0.0060, | 0.0039, | 0.0138, | 0.0336, | 0.0534, | 0.1030, |
| | 0.0142, | 0.0139, | 0.0137, | 0.0136, | 0.0135, | 0.0134, | 0.0133, | 0.0132, | 0.0129, |
| | 0.0062 | 0.0062 | 0.0063 | 0.0063 | 0.0063 | 0.0064 | 0.0064 | 0.0065 | 0.0066 |
| MR-IVW | 0.171, | 0.096, | 0.081, | 0.086, | 0.093, | 0.103, | 0.157, | 0.217, | 0.437, |
| | -0.0677, | -0.0177, | 0.0023, | 0.0223, | 0.0323, | 0.0423, | 0.0623, | 0.0823, | 0.1322, |
| | 0.0826, | 0.0826, | 0.0826, | 0.0826, | 0.0827, | 0.0827, | 0.0827, | 0.0827, | 0.0827, |
| | 0.075 | 0.0749 | 0.0749 | 0.0749 | 0.0749 | 0.0749 | 0.0749 | 0.0749 | 0.0749 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.995, | 0.317, | 0.046, | 0.317, | 0.993, | 1.000, | 1.000, |
| | -0.0994, | -0.0496, | -0.0297, | -0.0098, | 0.0002, | 0.0101, | 0.0300, | 0.0500, | 0.0998, |
| | 0.0062, | 0.0063, | 0.0064, | 0.0064, | 0.0065, | 0.0065, | 0.0066, | 0.0066, | 0.0068, |
| | 0.0064 | 0.0065 | 0.0065 | 0.0066 | 0.0066 | 0.0066 | 0.0067 | 0.0068 | 0.0069 |
| MR-Egger | 0.340, | 0.374, | 0.387, | 0.406, | 0.411, | 0.412, | 0.432, | 0.445, | 0.479, |
| | 0.3448, | 0.3922, | 0.4112, | 0.4301, | 0.4396, | 0.4491, | 0.4680, | 0.4869, | 0.5342, |
| | 0.4780, | 0.4780, | 0.4780, | 0.4780, | 0.4780, | 0.4780, | 0.4780, | 0.4780, | 0.4780, |
| | 0.29 | 0.29 | 0.29 | 0.2901 | 0.2901 | 0.2901 | 0.2901 | 0.2901 | 0.2902 |
| MR-Weighted-Median | 1.000, | 1.000, | 0.930, | 0.198, | 0.034, | 0.119, | 0.866, | 1.000, | 1.000, |
| | -0.0991, | -0.0501, | -0.0305, | -0.0110, | -0.0012, | 0.0086, | 0.0282, | 0.0478, | 0.0965, |
| | 0.0080, | 0.0081, | 0.0082, | 0.0083, | 0.0084, | 0.0085, | 0.0086, | 0.0087, | 0.0091, |
| MD W ' 1 . 135 ' | 0.0091 | 0.0092 | 0.0093 | 0.0094 | 0.0094 | 0.0094 | 0.0095 | 0.0096 | 0.0099 |
| MR-Weighted-Mode | 0.961, | 0.794, | 0.360, | 0.026, | 0.010, | 0.042, | 0.370, | 0.783, | 0.958, |
| | -0.0958, | -0.0462, | -0.0267, | -0.0074, | 0.0020, | 0.0119, | 0.0316, | 0.0516, | 0.1010, |
| | 0.0654, | 0.0656, | 0.0656, | 0.0657, | 0.0655, 0.0392 | 0.0655, | 0.0656, | 0.0655, | 0.0657, |
| MR-RAPS1 | 0.0386 | 0.0388 | 0.039 | 0.0391 | | 0.0393 | 0.0394 | 0.0396 | 0.0401 |
| NIK-KAPSI | 0.169, -0.0680, | 0.084, -0.0180, | 0.072, 0.0020, | 0.079, 0.0220, | 0.088, 0.0320, | 0.107, 0.0420, | 0.153, 0.0620, | 0.217, 0.0820, | 0.435, 0.1320, |
| | 0.0797, | 0.0797, | 0.0020, | 0.0220, | 0.0320, | 0.0420, | 0.0020, | 0.0820, | 0.1320, |
| | 0.0797, | 0.0797, | 0.0798, | 0.0798, | 0.0745 | 0.0798, | 0.0798, | 0.0798, | 0.0798, |
| MR-RAPS2 | 1.000, | 1.000, | 0.0743 | 0.0743 | 0.590, | 0.0745 | 0.0743 | 1.000, | 1.000, |
| 1711X IX III 02 | 0.0870, | 0.0671, | 0.0293, | -0.0223, | 0.390, | 0.740, | 0.333, | 0.1287, | 0.3490, |
| | 1.7760, | 1.1320, | 0.0293, | 2.7815, | 1.3610, | 0.7111, | 0.7095, | 0.7081, | 3.3538, |
| | 0.01 | 0.0085 | 0.0084 | 0.009 | 0.0086 | 0.0084 | 0.7093, | 0.0086 | 0.0108 |
| MR-RAPS3 | 0.929, | 0.905, | 0.902, | 0.908, | 0.899, | 0.894, | 0.910, | 0.947, | 0.969, |
| MIC ICH 93 | -0.1908, | -0.0452, | 0.902, | 0.0619, | 0.0868, | 0.1110, | 0.1568, | 0.1994, | 0.2930, |
| | 0.2315, | 0.2294, | 0.2241, | 0.2173, | 0.2134, | 0.2094, | 0.2011, | 0.1928, | 0.1732, |
| | 0.2313, | 0.017 | 0.0166 | 0.0162 | 0.016 | 0.0157 | 0.0153 | 0.0149 | 0.1732, |
| MR-RAPS4 | 1.000, | 1.000, | 0.999, | 0.858, | 0.786, | 0.870, | 0.999, | 1.000, | 1.000, |
| AV. AA 13T | 0.0490, | 0.0622, | 0.0779, | 0.0940, | 0.786, | 0.1029, | 0.1307, | 0.1300, | 0.0845, |
| | | | | | | | | | |
| | 0.0490, | 0.8915, | 0.8715, | 0.8595, | 0.8717, | 0.8807, | 0.8970, | 0.9079, | 0.9769, |

Table S82: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.2, and N=200000.

| | · / | | | | | | | | _ |
|--------------------|--------------------|--------------------|---------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 1.000, | 0.996, | 0.398, | 0.084, | 0.417, | 0.991, | 1.000, | 1.000, |
| CIVIL-IVIA-AIC | -0.0988, | -0.0489, | -0.0289, | -0.0091, | 0.084, | 0.417, 0.0092, | 0.991, | 0.0490, | 0.0987, |
| | 0.0063, | 0.0065, | 0.0066, | 0.0064, | 0.0060, | 0.0092, | 0.0290, | 0.0069, | 0.0070, |
| | 0.0053 | 0.0053 | 0.0054 | 0.0054 | 0.0053 | 0.0054 | 0.0055 | 0.0056 | 0.0057 |
| cML-MA-AIC-Profile | 1.000, | 1.000, | 0.996, | 0.398, | 0.084, | 0.417, | 0.991, | 1.000, | 1.000, |
| | -0.0990, | -0.0490, | -0.0289, | -0.0091, | 0.0000, | 0.0092, | 0.0290, | 0.0490, | 0.0990, |
| | 0.0064, | 0.0065, | 0.0066, | 0.0064, | 0.0060, | 0.0065, | 0.0068, | 0.0069, | 0.0071, |
| | 0.0053 | 0.0053 | 0.0054 | 0.0054 | 0.0053 | 0.0054 | 0.0055 | 0.0056 | 0.0057 |
| cML-AIC | 1.000, | 1.000, | 0.997, | 0.480, | 0.147, | 0.506, | 0.992, | 1.000, | 1.000, |
| | -0.0995, | -0.0495, | -0.0295, | -0.0095, | 0.0001, | 0.0097, | 0.0296, | 0.0496, | 0.0995, |
| | 0.0066, | 0.0067, | 0.0069, | 0.0068, | 0.0067, | 0.0069, | 0.0071, | 0.0071, | 0.0074, |
| | 0.0048 | 0.0049 | 0.0049 | 0.0049 | 0.005 | 0.005 | 0.005 | 0.0051 | 0.0052 |
| cML-AIC-Profile | 1.000, | 1.000, | 0.997, | 0.479, | 0.146, | 0.506, | 0.992, | 1.000, | 1.000, |
| | -0.0996, | -0.0495, | -0.0295, | -0.0096, | 0.0001, | 0.0097, | 0.0296, | 0.0496, | 0.0996, |
| | 0.0066, 0.0048 | 0.0068, 0.0049 | 0.0069, 0.0049 | 0.0068, 0.0049 | 0.0066, 0.005 | 0.0069, 0.005 | 0.0071, 0.005 | 0.0071, 0.0051 | 0.0074, 0.0052 |
| cML-MA-BIC | 1.000, | 1.000, | 1.000, | 0.579, | 0.003 | 0.595, | 1.000, | 1.000, | 1.000, |
| CME MIT DIC | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0043, | 0.0044, | 0.0044, | 0.0045, | 0.0045, | 0.0045, | 0.0046, | 0.0046, | 0.0048, |
| | 0.0044 | 0.0045 | 0.0045 | 0.0046 | 0.0046 | 0.0046 | 0.0046 | 0.0047 | 0.0048 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 1.000, | 0.578, | 0.049, | 0.590, | 1.000, | 1.000, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0043, | 0.0044, | 0.0044, | 0.0045, | 0.0045, | 0.0045, | 0.0046, | 0.0046, | 0.0048, |
| | 0.0044 | 0.0045 | 0.0045 | 0.0046 | 0.0046 | 0.0046 | 0.0046 | 0.0047 | 0.0048 |
| cML-BIC | 1.000, | 1.000, | 1.000, | 0.582, | 0.055, | 0.597, | 1.000, | 1.000, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0043, | 0.0044, | 0.0045, | 0.0045, | 0.0045, | 0.0046, | 0.0046, | 0.0047, | 0.0048, |
| M. DIC P. C. | 0.0044 | 0.0045 | 0.0045 | 0.0045 | 0.0045 | 0.0046 | 0.0046 | 0.0047 | 0.0048 |
| cML-BIC-Profile | 1.000, | 1.000, | 1.000, | 0.582, | 0.055, | 0.597, | 1.000, | 1.000, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0043, 0.0044 | 0.0044, 0.0045 | 0.0045, 0.0045 | 0.0045, 0.0045 | 0.0045, 0.0046 | 0.0046, 0.0046 | 0.0046, 0.0046 | 0.0047, 0.0047 | 0.0048, 0.0048 |
| MR-Mix | 0.999, | 0.994, | 0.847, | 0.064, | 0.0040 | 0.0040 | 0.819, | 0.991, | 0.999, |
| IVIIX-IVIIX | -0.1104, | -0.0543, | -0.0322, | -0.0105, | 0.011, | 0.0107, | 0.0315, | 0.991, | 0.333, |
| | 0.0080, | 0.0080, | 0.0079, | 0.0080, | 0.0080, | 0.0080, | 0.0080, | 0.0080, | 0.0081, |
| | 0.012 | 0.0119 | 0.0118 | 0.0118 | 0.0119 | 0.0119 | 0.0119 | 0.0118 | 0.0118 |
| MR-ContMix | 1.000, | 1.000, | 1.000, | 0.564, | 0.057, | 0.596, | 1.000, | 1.000, | 1.000, |
| | -0.0997, | -0.0498, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0300, | 0.0500, | 0.0999, |
| | 0.0044, | 0.0045, | 0.0045, | 0.0046, | 0.0046, | 0.0046, | 0.0047, | 0.0047, | 0.0049, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 1.000, | 1.000, | 0.565, | 0.055, | 0.593, | 1.000, | 1.000, | 1.000, |
| | -0.0997, | -0.0497, | -0.0298, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0500, | 0.0999, |
| | 0.0045, | 0.0046, | 0.0046, | 0.0046, | 0.0046, | 0.0047, | 0.0047, | 0.0048, | 0.0049, |
| 1 m pppggg | 0.0044 | 0.0045 | 0.0046 | 0.0046 | 0.0046 | 0.0046 | 0.0047 | 0.0047 | 0.0048 |
| MR-PRESSO | 0.994, -0.0950, | 0.956, -0.0455, | 0.889, | 0.601, -0.0057, | 0.354, 0.0042, | 0.691, 0.0142, | 0.969, 0.0340, | 0.991, 0.0539, | 1.000, 0.1036, |
| | 0.0178, | 0.0433, | -0.0256, 0.0158, | 0.0057, | 0.0042, | 0.0142, | 0.0340, | 0.0339, | 0.1036, |
| | 0.0047 | 0.0138, | 0.0047 | 0.0047 | 0.0047 | 0.0133, | 0.0047 | 0.0048 | 0.0049 |
| MR-IVW | 0.208, | 0.082, | 0.062, | 0.062, | 0.074, | 0.088, | 0.117, | 0.183, | 0.368, |
| | -0.0778, | -0.0277, | -0.0076, | 0.0124, | 0.0224, | 0.0324, | 0.0525, | 0.0725, | 0.1226, |
| | 0.0783, | 0.0783, | 0.0783, | 0.0783, | 0.0783, | 0.0783, | 0.0783, | 0.0784, | 0.0784, |
| | 0.0748 | 0.0748 | 0.0748 | 0.0748 | 0.0748 | 0.0748 | 0.0748 | 0.0748 | 0.0748 |
| MR-IVW-Oracle | 1.000, | 1.000, | 1.000, | 0.563, | 0.045, | 0.584, | 1.000, | 1.000, | 1.000, |
| | -0.0997, | -0.0498, | -0.0298, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0500, | 0.0999, |
| | 0.0043, | 0.0044, | 0.0044, | 0.0045, | 0.0045, | 0.0045, | 0.0046, | 0.0046, | 0.0048, |
| | 0.0045 | 0.0046 | 0.0046 | 0.0047 | 0.0047 | 0.0047 | 0.0047 | 0.0048 | 0.0049 |
| MR-Egger | 0.344, | 0.383, | 0.398, | 0.406, | 0.406, | 0.417, | 0.424, | 0.437, | 0.476, |
| | 0.3366, | 0.3854, | 0.4049, | 0.4244, | 0.4341, | 0.4438, | 0.4633, | 0.4828, | 0.5314, |
| | 0.4740, 0.2926 | 0.4739, 0.2926 | 0.4739, 0.2927 | 0.4739, 0.2927 | 0.4739, 0.2927 | 0.4739, 0.2927 | 0.4738, 0.2927 | 0.4738, 0.2927 | 0.4738, 0.2927 |
| MR-Weighted Medies | 1.000, | 1.000, | 0.2927 | 0.2927 | 0.2927 | 0.2927 | 0.2927 | 1.000, | 1.000, |
| MR-Weighted-Median | -0.0999, | -0.0504, | -0.0306, | -0.0108, | -0.0010, | 0.244, 0.0089, | 0.994, 0.0287, | 0.0484, | 0.0977, |
| | 0.0058, | 0.0058, | 0.0058, | 0.0058, | 0.0058, | 0.0059, | 0.0059, | 0.0060, | 0.0062, |
| | 0.0064 | 0.0065 | 0.0066 | 0.0066 | 0.0066 | 0.0067 | 0.0067 | 0.0068 | 0.007 |
| MR-Weighted-Mode | 0.967, | 0.906, | 0.625, | 0.061, | 0.002, | 0.064, | 0.632, | 0.913, | 0.971, |
| | -0.1036, | -0.0536, | -0.0338, | -0.0140, | -0.0042, | 0.0062, | 0.0262, | 0.0458, | 0.0962, |
| | 0.1158, | 0.1161, | 0.1162, | 0.1163, | 0.1163, | 0.1165, | 0.1167, | 0.1169, | 0.1173, |
| | 0.0315 | 0.0316 | 0.0316 | 0.0317 | 0.0317 | 0.0317 | 0.0318 | 0.0317 | 0.032 |
| MR-RAPS1 | 0.195, | 0.085, | 0.058, | 0.063, | 0.066, | 0.079, | 0.119, | 0.173, | 0.378, |
| | -0.0781, | -0.0280, | -0.0080, | 0.0120, | 0.0220, | 0.0320, | 0.0520, | 0.0720, | 0.1220, |
| | 0.0762, | 0.0762, | 0.0762, | 0.0762, | 0.0762, | 0.0763, | 0.0763, | 0.0763, | 0.0763, |
| MD D : PGG | 0.0742 | 0.0742 | 0.0742 | 0.0742 | 0.0742 | 0.0742 | 0.0742 | 0.0742 | 0.0742 |
| MR-RAPS2 | 1.000, | 1.000, | 1.000, | 0.853, | 0.609, | 0.857, | 1.000, | 1.000, | 1.000, |
| | -0.0155, | -0.0329, | -0.0271, | 0.0669, | 0.0317, | 0.0631, | 0.0686, | 0.0717, | 0.1832, |
| | 1.0781, | 2.2290, | 0.5893, | 0.9552, | 0.5726, | 0.9608, | 0.5920, | 1.4411, | 2.2115, |
| MD DADC2 | 0.0054 | 0.0061 | 0.0054 | 0.0056 0.922, | 0.0053 0.921, | 0.0061 | 0.0055 0.923, | 0.0062 | 0.0063 |
| MR-RAPS3 | 0.957, -0.2170, | -0.0715, | -0.0162, | 0.922, | 0.921, 0.0619, | 0.934, 0.0864, | 0.923, 0.1331, | 0.943, 0.1767, | 0.974, 0.2728, |
| | 0.2170, | 0.2171, | 0.2136, | 0.0300, | 0.0019, | 0.0864, | 0.1331, 0.1943, | 0.1767, 0.1865, | 0.2728, 0.1672, |
| | 0.2130, | 0.2171, | 0.2130, | 0.2084, | 0.2032, | 0.2018, | 0.1943, | 0.1805, | 0.1072, |
| | | 1.000, | 1.000, | 0.946, | 0.837, | 0.941, | 1.000, | 1.000, | 1.000, |
| MR-RAPS4 | 1.000. | | | | | | | | , |
| MR-RAPS4 | 1.000, -0.0865, | -0.0529, | -0.0219, | 0.0228, | 0.0387, | 0.0464, | 0.0730, | 0.1114, | 0.0825, |
| MR-RAPS4 | | | | | 0.0387, 0.7647, | 0.0464, 0.7928, | 0.0730, 0.8056, | 0.1114, 0.8503, | 0.0825, 0.9615, |

Table S83: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.4, and N=50000.

| θ Methods cML-MA-AIC | -0.1 1.000, -0.0970, 0.0166, | -0.05 0.879, -0.0474, | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|----------------------------|---|------------------------------|----------------------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|
| | -0.0970, | | 0.531 | - | | | | | |
| | -0.0970, | | | 0.142, | 0.085, | 0.132, | 0.493, | 0.848, | 0.998, |
| cML-MA-AIC-Profile | 0.0166, | | -0.0278, | -0.0092, | -0.0003, | 0.0085, | 0.0271, | 0.0466, | 0.0961, |
| cML-MA-AIC-Profile | | 0.0167, | 0.0164, | 0.0155, | 0.0152, | 0.0155, | 0.0167, | 0.0172, | 0.0179, |
| cML-MA-AIC-Profile | 0.0133 | 0.0135 | 0.0135 | 0.0135 | 0.0135 | 0.0136 | 0.0138 | 0.0141 | 0.0144 |
| | 1.000, | 0.879, | 0.527, | 0.141, | 0.083, | 0.130, | 0.486, | 0.847, | 0.998, |
| | -0.0975, | -0.0475, | -0.0279, | -0.0092, | -0.0003, | 0.0085, | 0.0271, | 0.0467, | 0.0965, |
| | 0.0167, | 0.0168, | 0.0165, | 0.0155, | 0.0152, | 0.0155, | 0.0167, | 0.0173, | 0.0180, |
| - N. C. A. T. C. | 0.0134 | 0.0136 | 0.0136 | 0.0136 | 0.0136 | 0.0137 | 0.0139 | 0.0142 | 0.0145 |
| cML-AIC | 1.000, | 0.923, | 0.612, | 0.222, | 0.156, | 0.212, | 0.591, | 0.908, | 0.999, |
| | -0.0988, | -0.0492, | -0.0293, | -0.0099, | -0.0004, | 0.0090, | 0.0284, | 0.0483, | 0.0980, |
| | 0.0172, 0.0121 | 0.0175, 0.0122 | 0.0175, 0.0123 | 0.0172, 0.0124 | 0.0172, 0.0124 | 0.0173, 0.0125 | 0.0178, 0.0126 | 0.0181, 0.0127 | 0.0186, 0.013 |
| cML-AIC-Profile | 1.000, | 0.0122 | 0.609, | 0.0124 | 0.0124 | 0.0123 | 0.590, | 0.0127 | 0.999, |
| CIVIL-AIC-FIOINE | -0.0991, | -0.0492, | -0.0294, | -0.0099, | -0.0004, | 0.208, | 0.0284, | 0.907, | 0.999, |
| | 0.0174, | 0.0175, | 0.0176, | 0.0172, | 0.0172, | 0.0050, | 0.0178, | 0.0182, | 0.0187, |
| | 0.0122 | 0.0173, | 0.0124 | 0.0172, | 0.0172, | 0.0126 | 0.0127 | 0.0128 | 0.0131 |
| cML-MA-BIC | 1.000, | 0.992, | 0.772, | 0.150, | 0.049, | 0.125, | 0.732, | 0.989, | 1.000, |
| | -0.1005, | -0.0504, | -0.0304, | -0.0104, | -0.0004, | 0.0096, | 0.0296, | 0.0496, | 0.0996, |
| | 0.0113, | 0.0114, | 0.0114, | 0.0115, | 0.0115, | 0.0115, | 0.0116, | 0.0117, | 0.0120, |
| | 0.0112 | 0.0113 | 0.0114 | 0.0115 | 0.0115 | 0.0115 | 0.0116 | 0.0117 | 0.012 |
| cML-MA-BIC-Profile | 1.000, | 0.991, | 0.771, | 0.148, | 0.048, | 0.122, | 0.731, | 0.989, | 1.000, |
| | -0.1005, | -0.0504, | -0.0304, | -0.0104, | -0.0004, | 0.0096, | 0.0296, | 0.0496, | 0.0996, |
| | 0.0113, | 0.0114, | 0.0114, | 0.0115, | 0.0115, | 0.0115, | 0.0116, | 0.0117, | 0.0120, |
| | 0.0112 | 0.0114 | 0.0114 | 0.0115 | 0.0115 | 0.0116 | 0.0117 | 0.0118 | 0.0121 |
| cML-BIC | 1.000, | 0.990, | 0.777, | 0.156, | 0.053, | 0.135, | 0.735, | 0.990, | 1.000, |
| | -0.1005, | -0.0505, | -0.0304, | -0.0104, | -0.0004, | 0.0096, | 0.0296, | 0.0496, | 0.0997, |
| | 0.0113, | 0.0114, | 0.0114, | 0.0115, | 0.0115, | 0.0115, | 0.0116, | 0.0117, | 0.0120, |
| | 0.0111 | 0.0112 | 0.0113 | 0.0114 | 0.0114 | 0.0114 | 0.0115 | 0.0116 | 0.0119 |
| cML-BIC-Profile | 1.000, | 0.990, | 0.776, | 0.156, | 0.049, | 0.132, | 0.731, | 0.989, | 1.000, |
| | -0.1005, | -0.0505, | -0.0304, | -0.0104, | -0.0004, | 0.0096, | 0.0296, | 0.0496, | 0.0997, |
| | 0.0113, | 0.0114, | 0.0114, | 0.0115, | 0.0115, | 0.0115, | 0.0116, | 0.0117, | 0.0120, |
| | 0.0111 | 0.0113 | 0.0113 | 0.0114 | 0.0114 | 0.0115 | 0.0116 | 0.0117 | 0.012 |
| MR-Mix | 1.000, | 0.894, | 0.393, | 0.041, | 0.019, | 0.040, | 0.352, | 0.830, | 1.000, |
| | -0.1025, | -0.0509, | -0.0306, | -0.0106, | -0.0006, | 0.0092, | 0.0286, | 0.0476, | 0.0940, |
| | 0.0132, | 0.0131, | 0.0131, | 0.0131, | 0.0132, | 0.0132, | 0.0131, | 0.0132, | 0.0130, |
| 100 C 16 | 0.017 | 0.0169 | 0.0168 | 0.0168 | 0.0168 | 0.0167 | 0.0167 | 0.0167 | 0.0166 |
| MR-ContMix | 1.000, | 0.993, | 0.755, | 0.151, | 0.054, | 0.133, | 0.717, | 0.986, | 1.000, |
| | -0.0997, 0.0116, | -0.0501, 0.0117, | -0.0302, 0.0117, | -0.0104, 0.0118, | -0.0004, 0.0118, | 0.0095, 0.0118, | 0.0294, 0.0119, | 0.0492, 0.0120, | 0.0989, 0.0123, |
| | 0.0116, NA | 0.0117, NA | 0.0117, NA | 0.0116, NA | 0.0118, NA | 0.0118, NA | 0.0119, NA | 0.0120, NA | 0.0123, NA |
| MR-Lasso | 1.000, | 0.990, | 0.752, | 0.161, | 0.060, | 0.137, | 0.722, | 0.986, | 1.000, |
| WIK-Lasso | -0.0997, | -0.0500, | -0.0302, | -0.0104, | -0.0005, | 0.0095, | 0.0293, | 0.0492, | 0.0989, |
| | 0.0118, | 0.0119, | 0.0119, | 0.0119, | 0.0120, | 0.0053, | 0.0120, | 0.0120, | 0.0125, |
| | 0.0112 | 0.0114 | 0.0114 | 0.0115 | 0.0116 | 0.0116 | 0.0117 | 0.0118 | 0.012 |
| MR-PRESSO | 0.997, | 0.922, | 0.625, | 0.178, | 0.143, | 0.283, | 0.785, | 0.981, | 1.000, |
| | -0.0942, | -0.0448, | -0.0251, | -0.0054, | 0.0045, | 0.0144, | 0.0341, | 0.0539, | 0.1032, |
| | 0.0168, | 0.0165, | 0.0163, | 0.0161, | 0.0160, | 0.0160, | 0.0158, | 0.0157, | 0.0155, |
| | 0.0108 | 0.011 | 0.011 | 0.0111 | 0.0111 | 0.0112 | 0.0113 | 0.0114 | 0.0116 |
| MR-IVW | 0.073, | 0.047, | 0.055, | 0.074, | 0.090, | 0.102, | 0.142, | 0.178, | 0.318, |
| | -0.0461, | 0.0039, | 0.0239, | 0.0439, | 0.0539, | 0.0639, | 0.0839, | 0.1039, | 0.1538, |
| | 0.1046, | 0.1046, | 0.1046, | 0.1046, | 0.1046, | 0.1046, | 0.1046, | 0.1046, | 0.1046, |
| | 0.104 | 0.104 | 0.104 | 0.104 | 0.104 | 0.104 | 0.104 | 0.104 | 0.104 |
| MR-IVW-Oracle | 1.000, | 0.991, | 0.760, | 0.139, | 0.042, | 0.117, | 0.706, | 0.984, | 1.000, |
| | -0.0998, | -0.0501, | -0.0302, | -0.0104, | -0.0004, | 0.0095, | 0.0293, | 0.0492, | 0.0989, |
| | 0.0112, | 0.0113, | 0.0113, | 0.0114, | 0.0114, | 0.0114, | 0.0115, | 0.0116, | 0.0118, |
| | 0.0114 | 0.0115 | 0.0116 | 0.0117 | 0.0117 | 0.0118 | 0.0119 | 0.012 | 0.0123 |
| MR-Egger | 0.341, | 0.376, | 0.390, | 0.404, | 0.413, | 0.420, | 0.440, | 0.456, | 0.498, |
| | 0.4698, | 0.5165, | 0.5352, | 0.5539, | 0.5632, | 0.5725, | 0.5912, | 0.6098, | 0.6564, |
| | 0.4515, | 0.4516, | 0.4516, | 0.4517, | 0.4517, | 0.4517, | 0.4517, | 0.4518, | 0.4519, |
| MD Weighted Madie | 0.3364 1.000, | 0.3364 | 0.3364 | 0.3365 | 0.3365 0.071, | 0.3365 | 0.3365 | 0.3366 | 0.3367 |
| MR-Weighted-Median | | 0.913, -0.0535, | 0.549, | 0.159, | | 0.048, 0.0032, | 0.267, | 0.694, 0.0410, | 0.995, |
| | -0.1008, 0.0158, | 0.0164, | -0.0346, 0.0165, | -0.0157, 0.0167, | -0.0063, 0.0168, | 0.0032, | 0.0221, 0.0170, | 0.0410, | 0.0878, 0.0177, |
| | 0.0138, | 0.0164, | 0.0163, | 0.0167, | 0.0166 | 0.0169, | 0.0170, | 0.0171, | 0.0177, |
| MR-Weighted-Mode | 0.848, | 0.540, | 0.230, | 0.033, | 0.017, | 0.036, | 0.192, | 0.489, | 0.839, |
| | -0.0868, | -0.0388, | -0.0186, | 0.0019, | 0.017, | 0.0206, | 0.0393, | 0.0577, | 0.1079, |
| | 0.3201, | 0.3211, | 0.3215, | 0.3219, | 0.3222, | 0.3223, | 0.3228, | 0.3231, | 0.3239, |
| | 0.185 | 0.1865 | 0.1867 | 0.1868 | 0.1868 | 0.1868 | 0.1868 | 0.1869 | 0.1871 |
| MR-RAPS1 | 0.078, | 0.044, | 0.051, | 0.067, | 0.080, | 0.100, | 0.133, | 0.168, | 0.310, |
| | -0.0472, | 0.0028, | 0.0228, | 0.0429, | 0.0529, | 0.0629, | 0.0829, | 0.1029, | 0.1529, |
| | 0.1023, | 0.1023, | 0.1023, | 0.1023, | 0.1023, | 0.1023, | 0.1024, | 0.1024, | 0.1024, |
| | 0.1039 | 0.1039 | 0.1039 | 0.1039 | 0.1039 | 0.1039 | 0.1039 | 0.1039 | 0.104 |
| MR-RAPS2 | 0.110, | 0.055, | 0.049, | 0.051, | 0.054, | 0.058, | 0.087, | 0.125, | 0.223, |
| | -0.0715, | -0.0215, | -0.0014, | 0.0186, | 0.0286, | 0.0386, | 0.0586, | 0.0786, | 0.1287, |
| | 0.1041, | 0.1041, | 0.1041, | 0.1041, | 0.1041, | 0.1041, | 0.1042, | 0.1042, | 0.1042, |
| | 0.1051 | 0.1051 | 0.1051 | 0.1051 | 0.1051 | 0.1051 | 0.1051 | 0.1051 | 0.1051 |
| | 0.064 | 0.893, | 0.884, | 0.887, | 0.889, | 0.885, | 0.911, | 0.915, | 0.952, |
| MR-RAPS3 | 0.864, | | -8.9530, | 0.0867, | 2.9726, | 1.4535, | 0.4151, | 1.2800, | 0.8816, |
| MR-RAPS3 | -1.2666, | 0.3820, | | | | | | | |
| MR-RAPS3 | -1.2666, 68.7670, | 10.4769, | 227.2274, | 13.0961, | 68.4385, | 29.6133, | 13.2447, | 7.4228, | 2.3314, |
| | -1.2666, 68.7670, 1087.3079 | 10.4769, 7.9368 | 227.2274, 4070.7404 | 11.3686 | 1234.79 | 158.5749 | 23.6993 | 6.3155 | 1.291 |
| MR-RAPS3 | -1.2666, 68.7670, 1087.3079 0.999, | 10.4769, 7.9368 0.999, | 227.2274, 4070.7404 0.980, | 11.3686 0.853, | 1234.79 0.836, | 158.5749 0.861, | 23.6993 0.972, | 6.3155 1.000, | 1.291 1.000, |
| | -1.2666, 68.7670, 1087.3079 | 10.4769, 7.9368 | 227.2274, 4070.7404 | 11.3686 | 1234.79 | 158.5749 | 23.6993 | 6.3155 | 1.291 |

Table S84: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.4, and N=100000.

| ((| // | | <u> </u> | | , <u>1</u> | | | | |
|----------------------|-----------|----------|------------------------------|------------------------------|------------------------------|------------------------------|------------------------------|--------------------|-----------------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.988, | 0.786, | 0.172, | 0.071, | 0.180, | 0.777, | 0.987, | 1.000, |
| | -0.0974, | -0.0476, | -0.0277, | -0.0087, | 0.0002, | 0.0090, | 0.0281, | 0.0480, | 0.0977, |
| | 0.0113, | 0.0113, | 0.0113, | 0.0104, | 0.0102, | 0.0106, | 0.0115, | 0.0117, | 0.0119, |
| | 0.0094 | 0.0095 | 0.0096 | 0.0095 | 0.0095 | 0.0096 | 0.0098 | 0.0099 | 0.0102 |
| cML-MA-AIC-Profile | 1.000, | 0.988, | 0.782, | 0.171, | 0.070, | 0.178, | 0.776, | 0.987, | 1.000, |
| INIL-MA-AIC-I IOIIIC | -0.0977, | -0.0477, | -0.0277, | -0.0087, | 0.0002, | 0.0090, | 0.0281, | 0.0480, | 0.0980, |
| | 0.0113, | 0.0114, | 0.0113, | 0.0104, | 0.0102, | 0.0106, | 0.0115, | 0.0117, | 0.0120, |
| | 0.00113, | 0.0014, | 0.0113, | 0.0104, | 0.0102, | 0.0100, | 0.00113, | 0.0117, | 0.0120, |
| -MI AIC | | | | | | | | | |
| cML-AIC | 1.000, | 0.997, | 0.844, | 0.259, | 0.135, | 0.266, | 0.837, | 0.998, | 1.000, |
| | -0.0985, | -0.0488, | -0.0289, | -0.0093, | 0.0002, | 0.0096, | 0.0294, | 0.0492, | 0.0991 |
| | 0.0117, | 0.0117, | 0.0118, | 0.0115, | 0.0115, | 0.0117, | 0.0121, | 0.0121, | 0.0123 |
| | 0.0085 | 0.0086 | 0.0087 | 0.0087 | 0.0088 | 0.0088 | 0.0089 | 0.0089 | 0.0092 |
| cML-AIC-Profile | 1.000, | 0.997, | 0.844, | 0.258, | 0.133, | 0.264, | 0.835, | 0.997, | 1.000, |
| | -0.0987, | -0.0488, | -0.0289, | -0.0093, | 0.0002, | 0.0096, | 0.0294, | 0.0493, | 0.0993 |
| | 0.0117, | 0.0117, | 0.0118, | 0.0115, | 0.0115, | 0.0117, | 0.0121, | 0.0121, | 0.0125 |
| | 0.0086 | 0.0087 | 0.0087 | 0.0088 | 0.0088 | 0.0088 | 0.0089 | 0.009 | 0.0092 |
| cML-MA-BIC | 1.000, | 1.000, | 0.946, | 0.239, | 0.058, | 0.245, | 0.951, | 1.000, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0301, | 0.0502, | 0.1002 |
| | 0.0082, | 0.0082, | 0.0083, | 0.0083, | 0.0083, | 0.0084, | 0.0084, | 0.0085, | 0.0087 |
| | 0.0079 | 0.008 | 0.008 | 0.0081 | 0.0081 | 0.0081 | 0.0082 | 0.0083 | 0.0085 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.946, | 0.236, | 0.058, | 0.241, | 0.951, | 1.000, | 1.000, |
| MIL-MA-DIC-PIONE | -0.0998, | -0.0498, | -0.0298, | -0.0098, | | 0.241, 0.0102, | 0.931, 0.0301, | 0.0502, | |
| | | | | | 0.0002, | | | | 0.1002 |
| | 0.0082, | 0.0082, | 0.0083, | 0.0083, | 0.0083, | 0.0084, | 0.0084, | 0.0085, | 0.0087 |
| | 0.0079 | 0.008 | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0082 | 0.0083 | 0.0085 |
| cML-BIC | 1.000, | 1.000, | 0.949, | 0.245, | 0.060, | 0.247, | 0.958, | 1.000, | 1.000, |
| | -0.0999, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0302, | 0.0502, | 0.1002 |
| | 0.0082, | 0.0082, | 0.0083, | 0.0083, | 0.0083, | 0.0084, | 0.0084, | 0.0085, | 0.0087 |
| | 0.0078 | 0.0079 | 0.008 | 0.008 | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0084 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.949, | 0.242, | 0.060, | 0.247, | 0.958, | 1.000, | 1.000, |
| CALL DIC TIONIC | -0.0999, | -0.0498, | -0.0298, | -0.0098, | 0.000, | 0.0102, | 0.938, | 0.0502, | 0.1002 |
| | 0.0082, | 0.00498, | | 0.0083, | 0.0002, | 0.0102, | | | |
| | | | 0.0083, | | | | 0.0084, | 0.0085, | 0.0087 |
| 100 100 | 0.0078 | 0.0079 | 0.008 | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0082 | 0.0084 |
| MR-Mix | 1.000, | 0.985, | 0.652, | 0.055, | 0.004, | 0.049, | 0.637, | 0.986, | 1.000, |
| | -0.1017, | -0.0501, | -0.0299, | -0.0099, | -0.0001, | 0.0097, | 0.0292, | 0.0484, | 0.0948 |
| | 0.0101, | 0.0099, | 0.0099, | 0.0099, | 0.0099, | 0.0099, | 0.0099, | 0.0099, | 0.0096 |
| | 0.0134 | 0.0133 | 0.0133 | 0.0132 | 0.0132 | 0.0132 | 0.0132 | 0.0132 | 0.0131 |
| MR-ContMix | 1.000, | 1.000, | 0.942, | 0.245, | 0.067, | 0.246, | 0.951, | 1.000, | 1.000, |
| | -0.0995, | -0.0496, | -0.0297, | -0.0098, | 0.0002, | 0.0102, | 0.0301, | 0.0500, | 0.0998 |
| | 0.0083, | 0.0084, | 0.0084, | 0.0085, | 0.0085, | 0.0085, | 0.0086, | 0.0086, | 0.0088 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 1.000, | 0.934, | 0.248, | 0.072, | 0.254, | 0.944, | 1.000, | 1.000, |
| MR-Lasso | | | | | 0.072, | | | | |
| | -0.0994, | -0.0496, | -0.0297, | -0.0097, | 0.0003, | 0.0102, | 0.0301, | 0.0501, | 0.0998 |
| | 0.0087, | 0.0087, | 0.0087, | 0.0087, | 0.0088, | 0.0088, | 0.0090, | 0.0090, | 0.0092 |
| | 0.0079 | 0.0081 | 0.0081 | 0.0082 | 0.0082 | 0.0082 | 0.0083 | 0.0083 | 0.0085 |
| MR-PRESSO | 0.973, | 0.877, | 0.775, | 0.409, | 0.337, | 0.477, | 0.918, | 0.987, | 0.999, |
| | -0.0904, | -0.0409, | -0.0211, | -0.0013, | 0.0085, | 0.0184, | 0.0382, | 0.0580, | 0.1074 |
| | 0.0242, | 0.0234, | 0.0232, | 0.0231, | 0.0229, | 0.0228, | 0.0225, | 0.0223, | 0.0217 |
| | 0.0082 | 0.0082 | 0.0082 | 0.0082 | 0.0083 | 0.0083 | 0.0083 | 0.0084 | 0.0085 |
| MR-IVW | 0.101, | 0.067, | 0.077, | 0.095, | 0.102, | 0.126, | 0.148, | 0.181, | 0.299, |
| | -0.0481, | 0.0020, | 0.0221, | 0.0421, | 0.0522, | 0.0622, | 0.0822, | 0.1023, | 0.1524 |
| | 0.1118, | 0.1118, | 0.1118, | 0.1118, | 0.1118, | 0.1118, | 0.1118, | 0.1023, | 0.1324 |
| | | 0.1118, | | | | | | | |
| | 0.1042 | | 0.1042 | 0.1042 | 0.1042 | 0.1042 | 0.1042 | 0.1042 | 0.1042 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.942, | 0.224, | 0.055, | 0.228, | 0.947, | 1.000, | 1.000, |
| | -0.0995, | -0.0496, | -0.0297, | -0.0098, | 0.0002, | 0.0102, | 0.0301, | 0.0500, | 0.0998 |
| | 0.0081, | 0.0082, | 0.0082, | 0.0082, | 0.0083, | 0.0083, | 0.0083, | 0.0084, | 0.0086 |
| | 0.0081 | 0.0082 | 0.0082 | 0.0083 | 0.0083 | 0.0084 | 0.0084 | 0.0085 | 0.0087 |
| MR-Egger | 0.351, | 0.388, | 0.404, | 0.419, | 0.426, | 0.430, | 0.445, | 0.464, | 0.503, |
| 36 | 0.5000, | 0.5484, | 0.5677, | 0.5870, | 0.5967, | 0.6063, | 0.6257, | 0.6450, | 0.6932 |
| | 0.4731, | 0.4731, | 0.4731, | 0.4731, | 0.4731, | 0.4731, | 0.4731, | 0.4731, | 0.4732 |
| | 0.3425 | 0.3425 | 0.3425 | 0.3426 | 0.3426 | 0.3426 | 0.3426 | 0.3426 | 0.3426 |
| MD Waighted Madie | 1.000, | | | | | | | | |
| MR-Weighted-Median | | 0.991, | 0.814, | 0.219, | 0.072, | 0.081, | 0.548, | 0.954, | 1.000, |
| | -0.1007, | -0.0524, | -0.0330, | -0.0136, | -0.0039, | 0.0058, | 0.0251, | 0.0443, | 0.0924 |
| | 0.0114, | 0.0115, | 0.0116, | 0.0118, | 0.0118, | 0.0119, | 0.0121, | 0.0123, | 0.0128 |
| | 0.0114 | 0.0115 | 0.0116 | 0.0117 | 0.0117 | 0.0118 | 0.0119 | 0.012 | 0.0123 |
| MR-Weighted-Mode | 0.924, | 0.734, | 0.396, | 0.048, | 0.018, | 0.052, | 0.374, | 0.749, | 0.916, |
| | -0.0893, | -0.0402, | -0.0215, | -0.0025, | 0.0079, | 0.0182, | 0.0369, | 0.0566, | 0.1059 |
| | 0.3770, | 0.3749, | 0.3746, | 0.3738, | 0.3734, | 0.3730, | 0.3722, | 0.3713, | 0.3692 |
| | 0.1024 | 0.1027 | 0.103 | 0.1031 | 0.1032 | 0.1032 | 0.1034 | 0.1037 | 0.1041 |
| MR-RAPS1 | 0.097, | 0.065, | 0.069, | 0.089, | 0.098, | 0.109, | 0.138, | 0.174, | 0.293, |
| 1711X 1X/11 () 1 | -0.0497, | 0.003, | 0.0203, | 0.089, | 0.0504, | 0.109, | 0.0804, | 0.174, | 0.253, |
| | | 0.0003, | | 0.1092, | | 0.0004, | | | |
| | 0.1092, | | 0.1092, | | 0.1092, | | 0.1092, | 0.1092, | 0.1092 |
| 1 m = : = - | 0.1037 | 0.1037 | 0.1037 | 0.1037 | 0.1037 | 0.1037 | 0.1037 | 0.1038 | 0.1038 |
| MR-RAPS2 | 0.127, | 0.076, | 0.063, | 0.072, | 0.080, | 0.085, | 0.104, | 0.132, | 0.226, |
| | -0.0731, | -0.0231, | -0.0035, | 0.0169, | 0.0266, | 0.0366, | 0.0566, | 0.0753, | 0.1257 |
| | 0.1112, | 0.1113, | 0.1111, | 0.1113, | 0.1108, | 0.1111, | 0.1111, | 0.1096, | 0.1104 |
| | 0.1047 | 0.1048 | 0.1048 | 0.1048 | 0.1047 | 0.1048 | 0.1048 | 0.1045 | 0.1046 |
| MR-RAPS3 | 0.920, | 0.916, | 0.908, | 0.910, | 0.909, | 0.914, | 0.920, | 0.953, | 0.970, |
| WIN-INAL OO | -4.2014, | 0.916, | 4.5525, | -14.1242, | 1.2589, | -5.5832, | 1.5148, | 0.933, | 0.970, |
| | | | | | | | | | |
| | 136.2241, | 14.6667, | 116.2892, | 501.7183, | 38.5047, | 202.6511, | 24.0154, | 2.1430, | 2.5321 |
| | | 14.1 | 264 | 10180 | 125.4 | 2083 | 19.03 | 0.5891 | 0.4719 |
| | 961.1 | | | | 0.000 | 0.007 | 0.000 | 1 000 | 1 0000 |
| MR-RAPS4 | 0.999, | 1.000, | 0.999, | 0.941, | 0.893, | 0.927, | 0.998, | 1.000, | 1.000, |
| MR-RAPS4 | 0.999, | 1.000, | | | | | | | |
| MR-RAPS4 | | | 0.999, 0.8381, 1.3410, | 0.941, 0.8566, 1.3580, | 0.893, 0.8719, 1.3516, | 0.927, 1.0403, 4.6978, | 0.998, 0.9122, 1.3008, | 0.9391, 1.2918, | 1.000, 1.0060, 1.2068 |

Table S85: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.4, and N=200000.

| | | | | | | _ | | | |
|--|--|--|---|---|--|---|--|---|---|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 1.000, | 0.959, | 0.278, | 0.086, | 0.286, | 0.953, | 1.000, | 1.000, |
| CIVIL-IVIA-AIC | -0.0984, | -0.0485, | -0.0285, | -0.0089, | 0.0001, | 0.280, | 0.933, | 0.0485, | 0.0983, |
| | 0.0081, | 0.0082, | 0.0083, | 0.0078, | 0.0001, | 0.0078, | 0.0280, | 0.0485, | 0.0983, |
| | 0.0066 | 0.0067 | 0.0067 | 0.0067 | 0.0067 | 0.0068 | 0.0069 | 0.0035, | 0.0037, |
| cML-MA-AIC-Profile | 1.000, | 1.000, | 0.957, | 0.277, | 0.085, | 0.285, | 0.953, | 1.000, | 1.000, |
| | -0.0986, | -0.0485, | -0.0286, | -0.0089, | 0.0001, | 0.0090, | 0.0286, | 0.0485, | 0.0985, |
| | 0.0081, | 0.0082, | 0.0083, | 0.0078, | 0.0074, | 0.0078, | 0.0084, | 0.0085, | 0.0087, |
| | 0.0067 | 0.0067 | 0.0068 | 0.0068 | 0.0067 | 0.0068 | 0.0069 | 0.007 | 0.0072 |
| cML-AIC | 1.000, | 1.000, | 0.968, | 0.387, | 0.145, | 0.370, | 0.973, | 1.000, | 1.000, |
| | -0.0993, | -0.0494, | -0.0294, | -0.0095, | 0.0001, | 0.0096, | 0.0295, | 0.0494, | 0.0993, |
| | 0.0085, | 0.0086, | 0.0086, | 0.0086, | 0.0084, | 0.0085, | 0.0087, | 0.0088, | 0.0091, |
| | 0.006 | 0.0061 | 0.0061 | 0.0062 | 0.0062 | 0.0062 | 0.0063 | 0.0063 | 0.0065 |
| cML-AIC-Profile | 1.000, | 1.000, | 0.968, | 0.381, | 0.144, | 0.369, | 0.973, | 1.000, | 1.000, |
| | -0.0994, | -0.0494, | -0.0294, | -0.0095, | 0.0001, | 0.0096, | 0.0295, | 0.0494, | 0.0994, |
| | 0.0086, 0.006 | 0.0086, 0.0061 | 0.0086, 0.0061 | 0.0086, 0.0062 | 0.0084, 0.0062 | 0.0085, 0.0062 | 0.0087, 0.0063 | 0.0089, 0.0063 | 0.0091, 0.0065 |
| cML-MA-BIC | 1.000, | 1.000, | 0.999, | 0.427, | 0.0052 | 0.412, | 1.000, | 1.000, | 1.000, |
| CHE HIT DIC | -0.1000, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1000, |
| | 0.0056, | 0.0056, | 0.0056, | 0.0057, | 0.0057, | 0.0057, | 0.0057, | 0.0058, | 0.0059, |
| | 0.0056 | 0.0056 | 0.0057 | 0.0057 | 0.0057 | 0.0057 | 0.0058 | 0.0058 | 0.006 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.999, | 0.426, | 0.045, | 0.411, | 1.000, | 1.000, | 1.000, |
| | -0.1001, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1000, |
| | 0.0056, | 0.0056, | 0.0056, | 0.0057, | 0.0057, | 0.0057, | 0.0057, | 0.0058, | 0.0059, |
| | 0.0056 | 0.0056 | 0.0057 | 0.0057 | 0.0057 | 0.0057 | 0.0058 | 0.0058 | 0.006 |
| cML-BIC | 1.000, | 1.000, | 0.998, | 0.431, | 0.045, | 0.418, | 1.000, | 1.000, | 1.000, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0299, | 0.0500, | 0.1000, |
| | 0.0056, | 0.0056, | 0.0057, | 0.0057, | 0.0057, | 0.0057, | 0.0058, | 0.0058, | 0.0059, |
| •ML DIC D.: Cl. | 0.0055 | 0.0056 | 0.0056 | 0.0057 | 0.0057 | 0.0057 | 0.0058 | 0.0058 | 0.0059 |
| cML-BIC-Profile | 1.000, -0.1001, | 1.000, -0.0501, | 0.998, | 0.431, -0.0101, | 0.045, | 0.417, 0.0099, | 1.000, | 1.000, | 1.000, |
| | 0.0056, | 0.0056, | -0.0301, 0.0057, | 0.0057, | -0.0001, 0.0057, | 0.0099, | 0.0299, 0.0058, | 0.0500, 0.0058, | 0.1000, 0.0059, |
| | 0.0055 | 0.0056 | 0.0057, | 0.0057, | 0.0057 | 0.0057 | 0.0058, | 0.0058, | 0.0059, |
| MR-Mix | 1.000, | 0.997, | 0.879, | 0.150, | 0.018, | 0.134, | 0.871, | 0.999, | 0.999, |
| | -0.1024, | -0.0505, | -0.0301, | -0.0101, | -0.0002, | 0.0097, | 0.0291, | 0.0482, | 0.0945, |
| | 0.0078, | 0.0076, | 0.0076, | 0.0075, | 0.0076, | 0.0076, | 0.0077, | 0.0075, | 0.0075, |
| | 0.0103 | 0.0102 | 0.0102 | 0.0102 | 0.0102 | 0.0101 | 0.0101 | 0.0101 | 0.0102 |
| MR-ContMix | 1.000, | 1.000, | 0.997, | 0.437, | 0.051, | 0.418, | 1.000, | 1.000, | 1.000, |
| | -0.0998, | -0.0499, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0499, | 0.0998, |
| | 0.0056, | 0.0057, | 0.0057, | 0.0057, | 0.0057, | 0.0058, | 0.0058, | 0.0059, | 0.0060, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 1.000, | 0.998, | 0.418, | 0.050, | 0.406, | 1.000, | 1.000, | 1.000, |
| | -0.0999, | -0.0500, | -0.0300, | -0.0100, | 0.0000, | 0.0100, | 0.0299, | 0.0499, | 0.0998, |
| | 0.0058, 0.0056 | 0.0058, 0.0057 | 0.0058, 0.0057 | 0.0058, 0.0058 | 0.0059, 0.0058 | 0.0059, 0.0058 | 0.0059, 0.0059 | 0.0060, 0.0059 | 0.0061, 0.006 |
| MR-PRESSO | 0.0036 | 0.826, | 0.0037 | 0.529, | 0.0038 | 0.667, | 0.0039 | 0.0039 | 0.006 |
| WIK-F KESSO | -0.0840, | -0.0349, | -0.0153, | 0.0043, | 0.401, | 0.007, | 0.939, | 0.0633, | 0.993, |
| | 0.0417, | 0.0397, | 0.0387, | 0.0377, | 0.0377, | 0.0377, | 0.0367, | 0.0377, | 0.0321, |
| | 0.0079 | 0.0077 | 0.0076 | 0.0076 | 0.0076 | 0.0076 | 0.0074 | 0.0075 | 0.0071 |
| MR-IVW | 0.076, | 0.069, | 0.092, | 0.105, | 0.127, | 0.138, | 0.169, | 0.202, | 0.353, |
| | -0.0409, | 0.0094, | 0.0295, | 0.0495, | 0.0596, | 0.0696, | 0.0897, | 0.1098, | 0.1600, |
| | 0.1104, | 0.1104, | 0.1104, | 0.1104, | 0.1104, | 0.1104, | 0.1104, | 0.1104, | 0.1104, |
| | 0.1038 | 0.1038 | 0.1038 | 0.1038 | 0.1038 | 0.1038 | 0.1038 | 0.1038 | 0.1038 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.998, | 0.404 | | | | | |
| | | | | 0.404, | 0.040, | 0.394, | 0.999, | 1.000, | 1.000, |
| | -0.0999, | -0.0500, | -0.0300, | -0.0100, | -0.0001, | 0.0099, | 0.0299, | 0.0499, | 1.000, 0.0998, |
| | 0.0056, | -0.0500, 0.0056, | -0.0300, 0.0056, | -0.0100, 0.0057, | -0.0001, 0.0057, | 0.0099, 0.0057, | 0.0299, 0.0057, | 0.0499, 0.0058, | 1.000, 0.0998, 0.0059, |
| MP Egger | 0.0056, 0.0057 | -0.0500, 0.0056, 0.0058 | -0.0300, 0.0056, 0.0058 | -0.0100, 0.0057, 0.0058 | -0.0001, 0.0057, 0.0059 | 0.0099, 0.0057, 0.0059 | 0.0299, 0.0057, 0.0059 | 0.0499, 0.0058, 0.006 | 1.000, 0.0998, 0.0059, 0.0061 |
| MR-Egger | 0.0056, 0.0057 0.370, | -0.0500, 0.0056, 0.0058 0.405, | -0.0300, 0.0056, 0.0058 0.421, | -0.0100, 0.0057, 0.0058 0.444, | -0.0001, 0.0057, 0.0059 0.452, | 0.0099, 0.0057, 0.0059 0.463, | 0.0299, 0.0057, 0.0059 0.476, | 0.0499, 0.0058, 0.006 0.494, | 1.000, 0.0998, 0.0059, 0.0061 0.539, |
| MR-Egger | 0.0056, 0.0057 0.370, 0.5112, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, | -0.0300, 0.0056, 0.0058 0.421, 0.5803, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, | -0.0001, 0.0057, 0.0059 0.452, 0.6098, | 0.0099, 0.0057, 0.0059 0.463, 0.6197, | 0.0299, 0.0057, 0.0059 0.476, 0.6393, | 0.0499, 0.0058, 0.006 0.494, 0.6590, | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, |
| MR-Egger | 0.0056, 0.0057 0.370, | -0.0500, 0.0056, 0.0058 0.405, | -0.0300, 0.0056, 0.0058 0.421, | -0.0100, 0.0057, 0.0058 0.444, | -0.0001, 0.0057, 0.0059 0.452, | 0.0099, 0.0057, 0.0059 0.463, | 0.0299, 0.0057, 0.0059 0.476, | 0.0499, 0.0058, 0.006 0.494, | 1.000, 0.0998, 0.0059, 0.0061 0.539, |
| | 0.0056, 0.0057 0.370, 0.5112, 0.4918, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, |
| MR-Egger MR-Weighted-Median | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 |
| | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0263, 0.0085, | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0086, | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, |
| MR-Weighted-Median | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083 | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0263, 0.0085, 0.0084 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0086, 0.0084 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, |
| | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083 | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0263, 0.0085, 0.0084 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0086, 0.0084 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 |
| MR-Weighted-Median | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081 0.862, -0.0457, | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.572, -0.0253, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.0339, -0.0128, 0.0083, 0.0082 | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083 | 0.0099, 0.0057, 0.00559 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0263, 0.0084, 0.588, 0.0349, | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0086, 0.0084 0.856, 0.0546, | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, |
| MR-Weighted-Median | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081 0.862, -0.0457, 0.1313, | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.572, -0.0253, 0.1312, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0082 0.091, -0.0048, 0.1315, | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083 0.016, 0.0053, 0.1314, | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0063, 0.0084 0.588, 0.0349, 0.1312, | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0084 0.856, 0.0546, 0.1309, | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, 0.1307, |
| MR-Weighted-Median MR-Weighted-Mode | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, 0.0516 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081 0.862, -0.0457, 0.1313, | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.0052, 0.0518 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0082 0.091, -0.0048, 0.1315, 0.0518 | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0063, 0.1016, 0.0053, 0.1314, | 0.0099, 0.0057, 0.00559 0.463, 0.6197, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.084, 0.0151, 0.1313, | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0263, 0.0084 0.588, 0.0349, 0.1312, | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0084 0.856, 0.0546, 0.1309, 0.0521 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, 0.1307, 0.0523 |
| MR-Weighted-Median | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.955, -0.0956, 0.1314, 0.0516 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0081, 0.862, -0.0457, 0.1313, 0.0517 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.572, -0.0253, 0.1312, 0.079, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0082 0.091, -0.0048, 0.1315, 0.0518 | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0063, 0.1314, 0.052, 0.122, | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.0151, 0.1313, 0.052 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0084 0.588, 0.0349, 0.1312, 0.0521 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0084 0.0084 0.856, 0.0546, 0.1309, 0.0521 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, 0.1307, 0.0523 |
| MR-Weighted-Median MR-Weighted-Mode | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.1314, 0.0516 0.078, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081 0.862, -0.0457, 0.1313, 0.0517 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.572, -0.0253, 0.1312, 0.0518 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 0.091, -0.0048, 0.1315, 0.0518 0.107, 0.0484, | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.1314, 0.052 | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0151, 0.1313, 0.052 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0084, 0.588, 0.0084 0.588, 0.0349, 0.1312, 0.0521 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0086, 0.0084 0.856, 0.0521 0.1309, 0.0521 0.195, | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0087 0.0087 0.1041, 0.1307, 0.0523 0.335, 0.1585, |
| MR-Weighted-Median MR-Weighted-Mode | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.955, -0.0956, 0.1314, 0.0516 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0081, 0.862, -0.0457, 0.1313, 0.0517 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.572, -0.0253, 0.1312, 0.079, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0082 0.091, -0.0048, 0.1315, 0.0518 | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0063, 0.1314, 0.052, 0.122, | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.0151, 0.1313, 0.052 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0084 0.588, 0.0349, 0.1312, 0.0521 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0084 0.0084 0.856, 0.0546, 0.1309, 0.0521 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, 0.1307, 0.0523 |
| MR-Weighted-Median MR-Weighted-Mode | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, 0.0516 0.078, -0.0416, 0.1086, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0081 0.862, -0.0457, 0.1313, 0.0517 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082 0.572, -0.0253, 0.1312, 0.0518 0.079, 0.0284, 0.1086, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 0.091, -0.0048, 0.1315, 0.0518 0.107, 0.0484, 0.1086, | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.016, 0.0053, 0.1314, 0.052 | 0.0099, 0.0057, 0.00559 0.463, 0.6197, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.084, 0.0151, 0.1313, 0.052 0.130, | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0263, 0.0084 0.588, 0.0349, 0.1312, 0.0521 0.154, 0.0884, | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0084 0.856, 0.0546, 0.1309, 0.0521 0.195, 0.1084, 0.1086, | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, 0.1307, 0.0523 0.335, 0.1585, 0.1086, |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, 0.0516 0.078, -0.0416, 0.1086, 0.1033 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081 0.862, -0.0457, 0.1313, 0.0517 0.065, 0.0084, 0.1033 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.0572, -0.0253, 0.1312, 0.079, 0.0284, 0.1086, 0.1033 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 0.091, -0.0048, 0.1315, 0.0518 0.107, 0.0484, 0.1086, 0.1033 0.327, -0.0523, | -0,0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.016, 0.0053, 0.1314, 0.052 0.122, 0.0584, 0.1033 | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.0151, 0.1313, 0.052 0.130, 0.0684, 0.1086, 0.1033 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0084 0.588, 0.0349, 0.1312, 0.0521 0.154, 0.0884, 0.1033 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0084 0.856, 0.0546, 0.1309, 0.1084, 0.1084, 0.1086, 0.1033 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, 0.1307, 0.0523 0.335, 0.1585, 0.1086, 0.1033 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.9056, 0.1314, 0.0516 0.1086, 0.1086, 0.1086, 0.1033 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081 0.862, -0.0457, 0.1313, 0.0517 0.065, 0.0084, 0.1086, 0.1086, 0.1083 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.572, -0.0253, 0.1312, 0.0518 0.079, 0.0284, 0.1086, 0.1086, 0.1083, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 0.091, -0.0048, 0.1315, 0.0518 0.107, 0.0484, 0.1086, 0.1033 0.327, | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.0083, 0.1314, 0.052 0.122, 0.0584, 0.1086, 0.1086, 0.1083, 0.1086, | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.084, 0.0151, 0.1313, 0.052 0.130, 0.0684, 0.1086, 0.1086, 0.1086, 0.1086, 0.1086, | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0084 0.588, 0.0349, 0.1312, 0.0521 0.154, 0.0884, 0.1086, 0.1086, | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0086, 0.0084 0.856, 0.0521 0.195, 0.1086, 0.1086, 0.1086, 0.1086, 0.1086, 0.1086, | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.1307, 0.1307, 0.1523, 0.1585, 0.1086, 0.1033 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, 0.0516 0.1086, 0.1086, 0.1033 0.789, -0.1567, 0.0695, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081 0.862, -0.0457, 0.1313, 0.0517 0.065, 0.1086, 0.1033 0.516, -0.1006, 0.0753, | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.00518 0.079, -0.0253, 0.1312, 0.0518 0.079, 0.0284, 0.1086, 0.1033 0.422, -0.0770, 0.0795, 0.0607 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 0.091, -0.0048, 0.1315, 0.0518 0.107, 0.0484, 0.1086, 0.1033 0.327, -0.0523, 0.0835, 0.0835, 0.064 | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.0083, 0.1314, 0.052 0.122, 0.0584, 0.1086, 0.1033, 0.281, -0.0398, 0.0850, 0.0850, | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0151, 0.1313, 0.052 0.130, 0.0684, 0.1086, 0.1086, 0.1033 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0085, 0.0084 0.588, 0.0349, 0.1312, 0.0521 0.154, 0.0884, 0.1086, 0.1033 0.165, -0.0049, 0.08666, | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0086, 0.0084 0.856, 0.0546, 0.1309, 0.1086, 0.1086, 0.1086, 0.1033 0.130, 0.0202, 0.0896, 0.0739 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, 0.1307, 0.0523 0.335, 0.1086, 0.1033 0.195, 0.0859, 0.0859, |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, 0.0516 0.078, -0.0416, 0.1033 0.789, -0.1567, 0.0695, 0.0695, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081, 0.862, -0.0457, 0.1313, 0.0517 0.0084, 0.1086, 0.1033 0.516, -0.1006, 0.0753, 0.0587 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.572, -0.0253, 0.1312, 0.0518 0.079, 0.0284, 0.1086, 0.1033 0.422, -0.0770, 0.0795, 0.0607 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 0.091, -0.0048, 0.1315, 0.0518 0.1086, 0.1036, 0.1036, 0.1036, 0.1036, 0.1036, 0.1037, 0.0484, 0.1086, 0.1038, 0.0082, 0.0945, 0.0644 0.945, | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.1314, 0.052 0.122, 0.1086, 0.1033, 0.281, -0.0398, 0.0850, 0.0850, | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.084, 0.0151, 0.1313, 0.052 0.1086, 0.1086, 0.1086, 0.1033 0.236, 0.0292, 0.0852, 0.067 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0084 0.588, 0.0084 0.521 0.1312, 0.0521 0.1086, 0.1033 0.165, -0.0049, 0.0866, 0.0707 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0086, 0.0084 0.856, 0.0521 0.1084, 0.1086, 0.1033 0.133, 0.0202, 0.896, 0.0739 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.1041, 0.1307, 0.0523 0.335, 0.1086, 0.1033 0.195, 0.0859, 0.0859, 0.0858, |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, 0.0516 0.1086, 0.1033 0.789, -0.1567, 0.0695, 0.0538 0.943, 0.0538 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0081 0.862, -0.0457, 0.1313, 0.0517 0.065, 0.0084, 0.1033 0.516, -0.1006, 0.0753, 0.0587 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082 0.572, -0.0253, 0.1312, 0.0518 0.079, 0.0284, 0.1086, 0.1033 0.422, -0.0770, 0.0795, 0.0607 0.941, -0.7208, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0082, 0.0082, 0.001315, 0.0518 0.107, 0.0484, 0.1033, 0.327, -0.0523, 0.0835, 0.064, 0.945, 0.0945, 0.4942, | -0,0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.016, 0.0053, 0.1314, 0.052 0.122, 0.0584, 0.1033 0.281, -0.0398, 0.0850, 0.0659 | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.084, 0.0151, 0.1313, 0.052 0.130, 0.0684, 0.1033 0.236, -0.0292, 0.0852, 0.067 0.948, 26.8984, | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.0263, 0.0084, 0.0349, 0.1312, 0.0521 0.154, 0.0884, 0.1033 0.165, -0.0049, 0.0866, 0.0707 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0084 0.856, 0.0546, 0.1309, 0.0521 0.195, 0.1084, 0.1033 0.130, 0.0202, 0.0896, 0.0739 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, 0.1337, 0.1585, 0.1086, 0.1033 0.195, 0.0828 0.0974, 0.0828 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, 0.0516 0.1086, 0.1033 0.789, -0.1567, 0.0538 0.943, 0.3306, 27.5748, | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081 0.862, -0.0457, 0.1313, 0.0517 0.065, 0.1086, 0.1086, 0.1033 0.516, -0.1006, 0.0753, 0.0587 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.0082, 0.0518 0.079, -0.0253, 0.1312, 0.0518 0.079, 0.0284, 0.1086, 0.1033 0.422, -0.0770, 0.0795, 0.0607 0.941, -0.7208, 26.6908, | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 0.091, -0.0048, 0.1315, 0.0518 0.107, 0.0484, 0.1086, 0.1033 0.327, -0.0523, 0.0825, 0.064 0.945, 0.4942, 14.3938, | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.0063, 0.1314, 0.052 0.122, 0.0584, 0.1033, 0.281, -0.0398, 0.0850, 0.0659 | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.084, 0.0151, 0.1313, 0.052 0.130, 0.0684, 0.1033 0.236, -0.0292, 0.0852, 0.067 0.948, 26.8984, 826.3173, \$2.0057 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0084, 0.0084, 0.1312, 0.0521 0.154, 0.0884, 0.1086, 0.1033 0.165, -0.0049, 0.0866, 0.0707 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0086, 0.0084 0.856, 0.0521 0.195, 0.1086, 0.1086, 0.1086, 0.1033 0.130, 0.0202, 0.0896, 0.0739 0.952, -2.1333, 68.5526, | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, 0.1307, 0.0523 0.335, 0.1585, 0.1086, 0.1033 0.195, 0.0859, 0.0974, 0.0828 0.974, 0.0435, 27.4894, |
| MR-Weighted-Mode MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, 0.0516 0.078, -0.0416, 0.1086, 0.1033 0.789, -0.1567, 0.0695, 0.0338 0.943, 0.3306, 27.5748, 21.53 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081, 0.862, -0.0457, 0.1313, 0.0517 0.065, 0.0084, 0.1086, 0.1033 0.516, -0.1006, 0.0753, 0.0587 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.0082, 0.0082, 0.00518 0.079, 0.0284, 0.1086, 0.1033 0.422, -0.0770, 0.0795, 0.0607 0.941, -0.7208, 26.6908, 23.05 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 0.091, -0.0048, 0.1315, 0.0518 0.107, 0.0484, 0.1086, 0.1033 0.327, -0.0523, 0.0835, 0.064 0.945, 0.4942, 14,3938, 6.016 | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.0083 0.016, 0.0052, 0.1314, 0.052 0.122, 0.0584, 0.1036, 0.1036, 0.0053, 0.1314, 0.0552 0.122, 0.0584, 0.1036, 0.0059, 0.0059, 0.0059, 0.0059, 0.0059, 0.0059, 0.0059, 0.0059, 0.00559, 0.00557, 7.132 | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.084, 0.0151, 0.1313, 0.052 0.130, 0.0684, 0.1086, 0.1033 0.236, -0.0292, 0.0852, 0.067 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0084, 0.588, 0.0084 0.588, 0.0349, 0.1312, 0.0521 0.154, 0.1086, 0.1033 0.165, -0.0049, 0.0866, 0.0707 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0086, 0.0084 0.856, 0.0521 0.1084, 0.1086, 0.1033 0.130, 0.0202, 0.896, 0.0739 0.952, -2.1333, 68.5526, 269.6 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.1041, 0.1307, 0.0523 0.335, 0.1585, 0.1086, 0.1033 0.195, 0.0859, 0.0974, 0.0828 0.974, 0.0435, 27,4894, 56.52 |
| MR-Weighted-Median MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, 0.0516 0.078, -0.0416, 0.1033 0.789, -0.1567, 0.0695, 0.0538 0.943, 0.3306, 27.5748, 21.53 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0081 0.862, -0.0457, 0.1313, 0.0517 0.065, 0.0084, 0.1033 0.516, -0.1006, 0.0753, 0.0587 0.944, 1.0042, 26.5163, 53.14 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.0082 0.572, -0.0253, 0.1312, 0.0133 0.422, -0.079, 0.0284, 0.1086, 0.1033 0.422, -0.0770, 0.0795, 0.0607 0.941, -0.7208, 26.6908, 23.05 1.000, 0.0058 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0082, 0.0082, 0.001315, 0.0518 0.107, 0.0484, 0.1315, 0.1086, 0.1033 0.327, -0.0523, 0.0835, 0.064 0.945, 0.4942, 14, 3938, 6.016 0.966, | -0,0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.016, 0.0053, 0.1314, 0.052 0.122, 0.0584, 0.1033 0.281, -0.0398, 0.0850, 0.0659 0.934, 0.9393, 10.2557, 7.132 0.937, | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0051, 0.1313, 0.052 0.130, 0.0684, 0.1033 0.236, -0.0292, 0.0852, 0.067 0.948, 26.8984, 826.3173, 20840 0.965, | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0084 0.588, 0.0084 0.588, 0.0349, 0.1312, 0.0521 0.1086, 0.1033 0.165, -0.0049, 0.0866, 0.0707 0.949, 1.1222, 16.4003, 10.52 1.000, | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0459, 0.0084 0.856, 0.0546, 0.1033 0.130, 0.1084, 0.1033 0.130, 0.0202, 0.0896, 0.0739 0.0739 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.957, 0.1041, 0.1337, 0.1585, 0.1086, 0.1033 0.195, 0.0828 0.974, 0.0828 0.974, 0.0435, 27,4894, 56.52 1.000, |
| MR-Weighted-Mode MR-Weighted-Mode MR-RAPS1 MR-RAPS2 | 0.0056, 0.0057 0.370, 0.5112, 0.4918, 0.3434 1.000, -0.1010, 0.0080, 0.008 0.955, -0.0956, 0.1314, 0.0516 0.078, -0.0416, 0.1086, 0.1033 0.789, -0.1567, 0.0695, 0.0338 0.943, 0.3306, 27.5748, 21.53 | -0.0500, 0.0056, 0.0058 0.405, 0.5606, 0.4917, 0.3435 1.000, -0.0520, 0.0082, 0.0081, 0.862, -0.0457, 0.1313, 0.0517 0.065, 0.0084, 0.1086, 0.1033 0.516, -0.1006, 0.0753, 0.0587 | -0.0300, 0.0056, 0.0058 0.421, 0.5803, 0.4917, 0.3435 0.978, -0.0324, 0.0082, 0.0082, 0.0082, 0.0082, 0.00518 0.079, 0.0284, 0.1086, 0.1033 0.422, -0.0770, 0.0795, 0.0607 0.941, -0.7208, 26.6908, 23.05 | -0.0100, 0.0057, 0.0058 0.444, 0.6000, 0.4917, 0.3435 0.339, -0.0128, 0.0083, 0.0082 0.091, -0.0048, 0.1315, 0.0518 0.107, 0.0484, 0.1086, 0.1033 0.327, -0.0523, 0.0835, 0.064 0.945, 0.4942, 14,3938, 6.016 | -0.0001, 0.0057, 0.0059 0.452, 0.6098, 0.4917, 0.3435 0.068, -0.0030, 0.0083, 0.0083, 0.0083 0.016, 0.0052, 0.1314, 0.052 0.122, 0.0584, 0.1036, 0.1036, 0.0053, 0.1314, 0.0552 0.122, 0.0584, 0.1036, 0.0059, 0.0059, 0.0059, 0.0059, 0.0059, 0.0059, 0.0059, 0.0059, 0.00559, 0.00557, 7.132 | 0.0099, 0.0057, 0.0059 0.463, 0.6197, 0.4917, 0.3435 0.129, 0.0068, 0.0084, 0.0083 0.084, 0.0151, 0.1313, 0.052 0.130, 0.0684, 0.1086, 0.1033 0.236, -0.0292, 0.0852, 0.067 | 0.0299, 0.0057, 0.0059 0.476, 0.6393, 0.4917, 0.3435 0.882, 0.0084, 0.588, 0.0084 0.588, 0.0349, 0.1312, 0.0521 0.154, 0.1086, 0.1033 0.165, -0.0049, 0.0866, 0.0707 | 0.0499, 0.0058, 0.006 0.494, 0.6590, 0.4917, 0.3435 0.997, 0.0086, 0.0084 0.856, 0.0521 0.1084, 0.1086, 0.1033 0.130, 0.0202, 0.896, 0.0739 0.952, -2.1333, 68.5526, 269.6 | 1.000, 0.0998, 0.0059, 0.0061 0.539, 0.7081, 0.4916, 0.3435 1.000, 0.0947, 0.0090, 0.0087 0.1041, 0.1307, 0.0523 0.335, 0.1585, 0.1086, 0.1033 0.195, 0.0859, 0.0974, 0.0828 0.974, 0.0435, 27,4894, 56.52 |

Table S86: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.6, and N=50000.

| , , | ′) | | <u></u> | | , 1 | | | | |
|----------------------|--|---|---|---|--|--|--|--|---|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 0.998, | 0.700, | 0.322, | 0.087, | 0.063, | 0.092, | 0.343, | 0.678, | 0.990, |
| | -0.0949, | -0.0452, | -0.0262, | -0.0082, | 0.0004, | 0.0089, | 0.0268, | 0.0459, | 0.0955, |
| | 0.0203, | 0.0203, | 0.0193, | 0.0181, | 0.0180, | 0.0183, | 0.0199, | 0.0209, | 0.0219, |
| | 0.0176 | 0.0178 | 0.0177 | 0.0177 | 0.0177 | 0.0178 | 0.0181 | 0.0184 | 0.0188 |
| cML-MA-AIC-Profile | 0.998, | 0.697, | 0.321, | 0.084, | 0.063, | 0.089, | 0.343, | 0.673, | 0.989, |
| | -0.0952, | -0.0453, | -0.0262, | -0.0082, | 0.0004, | 0.0089, | 0.0268, | 0.0460, | 0.0958, |
| | 0.0204, | 0.0204, | 0.0194, | 0.0182, | 0.0180, | 0.0184, | 0.0199, | 0.0210, | 0.0221, |
| M. AIG | 0.0178 | 0.0179 | 0.0179 | 0.0178 | 0.0178 | 0.0179 | 0.0182 | 0.0185 | 0.019 |
| cML-AIC | 0.998, | 0.795, | 0.442, | 0.158, | 0.125, | 0.155, | 0.433, | 0.774, | 0.994, |
| | -0.0978, 0.0210, | -0.0480, 0.0212, | -0.0283, 0.0209, | -0.0091, 0.0203, | 0.0003, 0.0204, | 0.0096, 0.0205, | 0.0287, 0.0215, | 0.0484, 0.0220, | 0.0982, 0.0229, |
| | 0.0210, | 0.0212, | 0.0209, | 0.0203, | 0.0204, | 0.0203, | 0.0213, | 0.0220, | 0.0229, |
| cML-AIC-Profile | 0.998, | 0.793, | 0.436, | 0.0102 | 0.126, | 0.152, | 0.431, | 0.769, | 0.994, |
| CIME THE FIGURE | -0.0979, | -0.0481, | -0.0283, | -0.0091, | 0.0003, | 0.0096, | 0.0288, | 0.0484, | 0.0985, |
| | 0.0211, | 0.0212, | 0.0209, | 0.0203, | 0.0204, | 0.0205, | 0.0215, | 0.0221, | 0.0231, |
| | 0.0159 | 0.0161 | 0.0162 | 0.0163 | 0.0163 | 0.0164 | 0.0165 | 0.0166 | 0.017 |
| cML-MA-BIC | 1.000, | 0.916, | 0.481, | 0.116, | 0.050, | 0.103, | 0.534, | 0.885, | 1.000, |
| | -0.0996, | -0.0496, | -0.0296, | -0.0096, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0150, | 0.0151, | 0.0152, | 0.0153, | 0.0153, | 0.0154, | 0.0155, | 0.0156, | 0.0160, |
| | 0.0147 | 0.0149 | 0.0149 | 0.015 | 0.0151 | 0.0151 | 0.0152 | 0.0154 | 0.0157 |
| cML-MA-BIC-Profile | 1.000, | 0.916, | 0.479, | 0.115, | 0.049, | 0.100, | 0.534, | 0.882, | 1.000, |
| | -0.0996, | -0.0496, | -0.0296, | -0.0096, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0150, | 0.0151, | 0.0152, | 0.0153, | 0.0153, | 0.0154, | 0.0155, | 0.0156, | 0.0160, |
| All Dic | 0.0148 | 0.0149 | 0.015 | 0.0151 | 0.0151 | 0.0152 | 0.0153 | 0.0154 | 0.0158 |
| cML-BIC | 1.000, | 0.923, | 0.495, | 0.123, | 0.054, | 0.110, | 0.543, | 0.888, | 1.000, |
| | -0.0996, | -0.0496, | -0.0296, | -0.0096, | 0.0004, | 0.0104, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0150, 0.0146 | 0.0151, 0.0147 | 0.0152, 0.0148 | 0.0153, 0.0149 | 0.0154, 0.0149 | 0.0154, 0.015 | 0.0155, 0.0151 | 0.0156, 0.0152 | 0.0160, 0.0155 |
| cML-BIC-Profile | 1.000, | 0.0147 | 0.492, | 0.0149 | 0.0149 | 0.015 | 0.541, | | 1.000, |
| CIVIL-DIC-PIONE | -0.0996, | -0.0496, | -0.0296, | -0.0096, | 0.034, 0.0004, | 0.106, 0.0104, | 0.0303, | 0.887, 0.0503, | 0.1003, |
| | 0.0150, | 0.0151, | 0.0152, | 0.0153, | 0.0004, | 0.0154, | 0.0303, | 0.0303, | 0.1003, |
| | 0.0136, | 0.0131, | 0.0132, | 0.0155, | 0.0154, | 0.015 | 0.0153, | 0.0150, | 0.0156 |
| MR-Mix | 1.000, | 0.780, | 0.324, | 0.057, | 0.020, | 0.047, | 0.317, | 0.750, | 0.999, |
| | -0.0946, | -0.0467, | -0.0278, | -0.0093, | -0.0002, | 0.0091, | 0.0273, | 0.0453, | 0.0887, |
| | 0.0152, | 0.0151, | 0.0151, | 0.0151, | 0.0149, | 0.0149, | 0.0150, | 0.0152, | 0.0151, |
| | 0.0172 | 0.0171 | 0.0171 | 0.0171 | 0.0171 | 0.017 | 0.017 | 0.017 | 0.017 |
| MR-ContMix | 1.000, | 0.910, | 0.496, | 0.123, | 0.057, | 0.110, | 0.531, | 0.879, | 1.000, |
| | -0.0989, | -0.0493, | -0.0295, | -0.0097, | 0.0002, | 0.0101, | 0.0300, | 0.0499, | 0.0995, |
| | 0.0152, | 0.0154, | 0.0155, | 0.0156, | 0.0156, | 0.0157, | 0.0158, | 0.0159, | 0.0164, |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.899, | 0.474, | 0.115, | 0.059, | 0.117, | 0.519, | 0.871, | 0.999, |
| | -0.0990, | -0.0493, | -0.0296, | -0.0097, | 0.0002, | 0.0103, | 0.0301, | 0.0501, | 0.0996, |
| | 0.0156, | 0.0157, | 0.0158, | 0.0158, | 0.0160, | 0.0162, | 0.0164, | 0.0163, | 0.0172, |
| MD DDEGGO | 0.0148 | 0.015 | 0.0151 | 0.0152 | 0.0153 | 0.0153 | 0.0154 | 0.0155 | 0.0158 |
| MR-PRESSO | 0.968, -0.0907, | 0.760, -0.0413, | 0.423, -0.0217, | 0.184, -0.0020, | 0.182, 0.0079, | 0.261, 0.0177, | 0.642, 0.0374, | 0.916, 0.0571, | 0.997, 0.1064, |
| | 0.0249, | 0.0243, | 0.0217, | 0.0241, | 0.0079, | 0.0177, | 0.0374, | 0.0371, 0.0237, | 0.1004, |
| | 0.0249, | 0.0243, | 0.0240, | 0.0241, | 0.0239, | 0.0239, | 0.0237, | 0.0237, | 0.0234, |
| MR-IVW | 0.060, | 0.057, | 0.071, | 0.086, | 0.107, | 0.125, | 0.152, | 0.185, | 0.293, |
| | -0.0262, | 0.0239, | 0.0439, | 0.0640, | 0.0740, | 0.0840, | 0.1040, | 0.1240, | 0.1741, |
| | 0.1298, | 0.1298, | 0.1298, | 0.1298, | 0.1298, | 0.1298, | 0.1298, | 0.1298, | 0.1298, |
| | 0.1256 | 0.1256 | 0.1256 | 0.1256 | 0.1256 | 0.1256 | 0.1256 | 0.1256 | 0.1256 |
| MR-IVW-Oracle | 1.000, | 0.904, | 0.460, | 0.105, | 0.047, | 0.094, | 0.508, | 0.879, | 1.000, |
| | -0.0989, | -0.0493, | -0.0294, | -0.0096, | 0.0004, | 0.0103, | 0.0301, | 0.0500, | 0.0996, |
| | 0.0148, | 0.0149, | 0.0150, | 0.0151, | 0.0151, | 0.0152, | 0.0153, | 0.0154, | 0.0158, |
| | 0.015 | 0.0152 | 0.0153 | 0.0154 | 0.0154 | 0.0155 | 0.0156 | 0.0157 | 0.016 |
| MR-Egger | 0.379, | 0.422, | 0.433, | 0.453, | 0.459, | 0.464, | 0.484, | 0.509, | 0.546, |
| | 0.5690, | 0.6165, | 0.6355, | 0.6545, | 0.6640, | 0.6735, | 0.6924, | 0.7114, | 0.7588, |
| | 0.4384, | 0.4385, | 0.4385, | 0.4385, | 0.4386, | 0.4386, | 0.4386, | 0.4386, | 0.4387, |
| MD Well 137 " | 0.3636 | 0.3636 | 0.3636 | 0.3637 | 0.3637 | 0.3637 | 0.3637 | 0.3638 | 0.3638 |
| MR-Weighted-Median | 0.995, | 0.774, | 0.497, | 0.201, | 0.123, | 0.094, | 0.130, | 0.314, | 0.868, |
| | -0.1045, | -0.0593, | -0.0413, | -0.0232, | -0.0142, | -0.0052, | 0.0127, | 0.0306, 0.0257, | 0.0750, |
| | 0.0234, 0.0211 | 0.0237, 0.0214 | 0.0240, 0.0215 | 0.0244, 0.0216 | 0.0246, 0.0217 | 0.0249, 0.0218 | 0.0253, 0.022 | 0.0257, 0.0222 | 0.0268, 0.0228 |
| MR-Weighted-Mode | 0.0211 | 0.0214 | 0.0215 | 0.0216 | 0.0217 | 0.622, | 0.022 | 0.0222 | 0.0228 |
| 11117- WOIGHICU-WOUC | -0.1783, | -0.1372, | -0.1250, | -0.1086, | -0.0994, | -0.0908, | -0.0752, | -0.0576, | -0.0176 |
| | 0.1960, | 0.1972, | 0.2041, | 0.2036, | 0.2034, | 0.2032, | 0.2025, | 0.2021, | 0.2026, |
| | 0.2919 | 0.2913 | 0.2915 | 0.2919 | 0.2925 | 0.2926 | 0.293 | 0.2933 | 0.2941 |
| MR-RAPS1 | 0.053, | 0.047, | 0.065, | 0.080, | 0.093, | 0.103, | 0.142, | 0.173, | 0.299, |
| ** | -0.0268, | 0.0233, | 0.0433, | 0.0633, | 0.0733, | 0.0833, | 0.1033, | 0.1234, | 0.1734, |
| | 0.1255, | 0.1255, | 0.1255, | 0.1255, | 0.1255, | 0.1255, | 0.1255, | 0.1255, | 0.1256, |
| | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1258 |
| | | 0.053, | 0.062, | 0.074, | 0.084, | 0.095, | 0.110, | 0.140, | 0.218, |
| MR-RAPS2 | 0.066, | | 0.0298, | 0.0498, | 0.0598, | 0.0698, | 0.0898, | 0.1094, | 0.1593, |
| MR-RAPS2 | -0.0402, | 0.0098, | | 1 0 1204 | 0.1394, | 0.1394, | 0.1394, | 0.1390, | 0.1391, |
| MR-RAPS2 | -0.0402, 0.1394, | 0.1394, | 0.1394, | 0.1394, | | | | | |
| | -0.0402, 0.1394, 0.1356 | 0.1394, 0.1356 | 0.1356 | 0.1356 | 0.1356 | 0.1356 | 0.1356 | 0.1356 | 0.1356 |
| MR-RAPS2 MR-RAPS3 | -0.0402, 0.1394, 0.1356 0.892, | 0.1394, 0.1356 0.866, - | 0.1356 0.876, | 0.1356 0.891, | 0.900, | 0.912, | 0.908, | 0.911, | 0.945, |
| | -0.0402, 0.1394, 0.1356 0.892, 1.2454, | 0.1394, 0.1356 0.866, - 209.9883, | 0.1356 0.876, 21.2117, | 0.1356 0.891, -26.3794, | 0.900, 3.3468, | 0.912, -4.3093, | 0.908, 0.0604, | 0.911, 4.9292, | 0.945, 1.4952, |
| | -0.0402, 0.1394, 0.1356 0.892, 1.2454, 171.6271, | 0.1394, 0.1356 0.866, - 209.9883, 6699.4141, | 0.1356 0.876, 21.2117, 534.7323, | 0.1356 0.891, -26.3794, 810.1790, | 0.900, 3.3468, 59.4460, | 0.912, -4.3093, 154.9911, | 0.908, 0.0604, 40.8081, | 0.911, 4.9292, 309.3501, | 0.945, 1.4952, 23.8250 |
| MR-RAPS3 | -0.0402, 0.1394, 0.1356 0.892, 1.2454, 171.6271, 697.2 | 0.1394, 0.1356 0.866, - 209.9883, 6699.4141, 1249000 | 0.1356 0.876, 21.2117, 534.7323, 6772 | 0.1356 0.891, -26.3794, 810.1790, 24370 | 0.900, 3.3468, 59.4460, 78.77 | 0.912, -4.3093, 154.9911, 725.9 | 0.908, 0.0604, 40.8081, 40.55 | 0.911, 4.9292, 309.3501, 2518 | 0.945, 1.4952, 23.8250 20.02 |
| | -0.0402, 0.1394, 0.1356 0.892, 1.2454, 171.6271, 697.2 0.997, | 0.1394, 0.1356 0.866, - 209.9883, 6699.4141, 1249000 0.995, | 0.1356 0.876, 21.2117, 534.7323, 6772 0.995, | 0.1356 0.891, -26.3794, 810.1790, 24370 0.986, | 0.900, 3.3468, 59.4460, 78.77 0.981, | 0.912, -4.3093, 154.9911, 725.9 0.984, | 0.908, 0.0604, 40.8081, 40.55 | 0.911, 4.9292, 309.3501, 2518 0.998, | 0.945, 1.4952, 23.8250 20.02 0.999, |
| MR-RAPS3 | -0.0402, 0.1394, 0.1356 0.892, 1.2454, 171.6271, 697.2 | 0.1394, 0.1356 0.866, - 209.9883, 6699.4141, 1249000 | 0.1356 0.876, 21.2117, 534.7323, 6772 | 0.1356 0.891, -26.3794, 810.1790, 24370 | 0.900, 3.3468, 59.4460, 78.77 | 0.912, -4.3093, 154.9911, 725.9 | 0.908, 0.0604, 40.8081, 40.55 | 0.911, 4.9292, 309.3501, 2518 | 0.945, 1.4952, 23.8250 20.02 |

Table S87: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.6, and N=100000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------|----------------------|--------------------|---------------------|--------------------|--------------------|---------------------|--------------------|--------------------|--------------------|
| cML-MA-AIC | 1.000, | 0.892, | 0.547, | 0.115, | 0.055, | 0.122, | 0.548, | 0.890, | 1.000, |
| | -0.0958, | -0.0459, | -0.0263, | -0.0081, | 0.0004, | 0.0090, | 0.0273, | 0.0470, | 0.0966, |
| | 0.0151, 0.0127 | 0.0152, 0.0128 | 0.0147, 0.0128 | 0.0134, 0.0126 | 0.0131, 0.0126 | 0.0135, 0.0127 | 0.0151, 0.013 | 0.0157, 0.0132 | 0.0159, 0.0135 |
| ML-MA-AIC-Profile | 1.000, | 0.892, | 0.544, | 0.0120 | 0.0120 | 0.0127 | 0.545, | 0.890, | 1.000, |
| ML-MA-AIC-I IOIIIC | -0.0961, | -0.0460, | -0.0263, | -0.0080, | 0.0004, | 0.0090, | 0.0273, | 0.0470, | 0.0969, |
| | 0.0153, | 0.0153, | 0.0147, | 0.0134, | 0.0131, | 0.0135, | 0.0151, | 0.0157, | 0.0160, |
| | 0.0127 | 0.0128 | 0.0128 | 0.0127 | 0.0127 | 0.0128 | 0.013 | 0.0132 | 0.0135 |
| cML-AIC | 1.000, | 0.939, | 0.661, | 0.207, | 0.117, | 0.213, | 0.659, | 0.931, | 1.000, |
| | -0.0978, | -0.0479, | -0.0282, | -0.0089, | 0.0005, | 0.0098, | 0.0290, | 0.0490, | 0.0988, |
| | 0.0157, | 0.0158, | 0.0156, | 0.0152, | 0.0151, | 0.0153, | 0.0161, | 0.0165, | 0.0167, |
| | 0.0112 | 0.0113 | 0.0114 | 0.0115 | 0.0115 | 0.0116 | 0.0116 | 0.0117 | 0.012 |
| cML-AIC-Profile | 1.000, | 0.939, | 0.660, | 0.206, | 0.114, | 0.212, | 0.657, | 0.930, | 1.000, |
| | -0.0980, 0.0158, | -0.0480, | -0.0282, | -0.0089, | 0.0004, | 0.0098, | 0.0290, | 0.0490, | 0.0990, |
| | 0.0158, | 0.0159, 0.0114 | 0.0157, 0.0115 | 0.0152, 0.0115 | 0.0151, 0.0116 | 0.0153, 0.0116 | 0.0161, 0.0117 | 0.0165, 0.0118 | 0.0168, 0.012 |
| cML-MA-BIC | 1.000, | 0.994, | 0.797, | 0.165, | 0.0116 | 0.0116 | 0.0117 | 0.0118 | 1.000, |
| CML-MA-DIC | -0.0998, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0108, | 0.0109, | 0.0110, | 0.0110, | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0116, |
| | 0.0104 | 0.0105 | 0.0106 | 0.0106 | 0.0107 | 0.0107 | 0.0108 | 0.0109 | 0.0111 |
| ML-MA-BIC-Profile | 1.000, | 0.994, | 0.797, | 0.164, | 0.057, | 0.168, | 0.781, | 0.994, | 1.000, |
| | -0.0998, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0108, | 0.0109, | 0.0110, | 0.0110, | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0116, |
| | 0.0104 | 0.0105 | 0.0106 | 0.0107 | 0.0107 | 0.0107 | 0.0108 | 0.0109 | 0.0111 |
| cML-BIC | 1.000, | 0.994, | 0.799, | 0.175, | 0.058, | 0.174, | 0.785, | 0.994, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0108, | 0.0109, | 0.0110, | 0.0110, | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0116, |
| | 0.0103 | 0.0104 | 0.0105 | 0.0106 | 0.0106 | 0.0106 | 0.0107 | 0.0108 | 0.011 |
| cML-BIC-Profile | 1.000, | 0.994, | 0.799, | 0.174, | 0.058, | 0.173, | 0.784, | 0.994, 0.0503, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0108, | 0.0109, 0.0105 | 0.0110, | 0.0110, 0.0106 | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0116, |
| MR-Mix | 0.0103 | | 0.0105 | 0.0106 | 0.0106 | 0.0106 | 0.0107 | 0.0108 | 0.011 |
| IVIK-IVIIX | 1.000, -0.0951, | 0.960, -0.0470, | 0.583, -0.0281, | -0.0093, | 0.024, 0.0000, | 0.071, 0.0092, | 0.554, 0.0274, | 0.959, 0.0453, | 1.000, 0.0892, |
| | 0.0111, | 0.0111, | 0.0110, | 0.0112, | 0.0000, | 0.0092, | 0.0274, | 0.0433, | 0.0392, |
| | 0.0132 | 0.0111, | 0.0110, | 0.0112, | 0.0113, | 0.0112, | 0.0105, | 0.0112, | 0.0112, |
| MR-ContMix | 1.000, | 0.994, | 0.806, | 0.173, | 0.066, | 0.184, | 0.790, | 0.992, | 1.000, |
| WIN COMMIN | -0.0994, | -0.0496, | -0.0296, | -0.0097, | 0.0003, | 0.0103, | 0.0302, | 0.0502, | 0.1000, |
| | 0.0110, | 0.0110, | 0.0111, | 0.0111, | 0.0112, | 0.0112, | 0.0113, | 0.0114, | 0.0117. |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.988, | 0.781, | 0.163, | 0.060, | 0.163, | 0.763, | 0.990, | 1.000, |
| | -0.0994, | -0.0495, | -0.0295, | -0.0097, | 0.0003, | 0.0102, | 0.0301, | 0.0501, | 0.1000 |
| | 0.0112, | 0.0113, | 0.0114, | 0.0114, | 0.0114, | 0.0114, | 0.0115, | 0.0116, | 0.0120 |
| | 0.0106 | 0.0107 | 0.0108 | 0.0108 | 0.0109 | 0.0109 | 0.011 | 0.011 | 0.0113 |
| MR-PRESSO | 0.933, | 0.792, | 0.632, | 0.314, | 0.323, | 0.441, | 0.845, | 0.966, | 0.996, |
| | -0.0854, | -0.0364, | -0.0166, | 0.0031, | 0.0129, | 0.0228, | 0.0425, | 0.0623, | 0.1119, |
| | 0.0336, | 0.0310, 0.0112 | 0.0307, | 0.0303, 0.0112 | 0.0300, 0.0112 | 0.0298, 0.0113 | 0.0294, | 0.0293, | 0.0289, |
| MR-IVW | 0.0112 0.073, | 0.0112 | 0.0112 0.087, | 0.0112 | 0.0112 | 0.0113 | 0.0113 0.163, | 0.0113 0.188, | 0.0115 |
| IVIIX-I V VV | -0.0242, | 0.076, | 0.087, | 0.100, | 0.121, 0.0762, | 0.0863, | 0.105, | 0.1364, | 0.289, |
| | 0.1347, | 0.1347, | 0.1347, | 0.1347, | 0.1347, | 0.1347, | 0.1347, | 0.1204, | 0.1760, |
| | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 |
| MR-IVW-Oracle | 1.000, | 0.994, | 0.775, | 0.152, | 0.047, | 0.154, | 0.767, | 0.991, | 1.000, |
| mic IV IV Gracie | -0.0994, | -0.0496, | -0.0296, | -0.0097, | 0.0003, | 0.0102, | 0.0302, | 0.0501, | 0.1000, |
| | 0.0107, | 0.0108, | 0.0109, | 0.0110, | 0.0110 | 0.0110, | 0.0111, | 0.0112, | 0.0115 |
| | 0.0107 | 0.0108 | 0.0109 | 0.0109 | 0.011 | 0.011 | 0.0111 | 0.0112 | 0.0114 |
| MR-Egger | 0.389, | 0.426, | 0.438, | 0.463, | 0.470, | 0.488, | 0.501, | 0.516, | 0.559, |
| | 0.5783, | 0.6271, | 0.6467, | 0.6662, | 0.6759, | 0.6857, | 0.7052, | 0.7247, | 0.7734, |
| | 0.4525, | 0.4525, | 0.4524, | 0.4524, | 0.4524, | 0.4524, | 0.4524, | 0.4524, | 0.4523 |
| m w | 0.3677 | 0.3678 | 0.3678 | 0.3678 | 0.3678 | 0.3678 | 0.3678 | 0.3678 | 0.3679 |
| IR-Weighted-Median | 1.000, | 0.930, | 0.699, | 0.302, | 0.167, | 0.125, | 0.248, | 0.621, | 0.993, |
| | -0.1042, 0.0182, | -0.0574, | -0.0386, | -0.0199, | -0.0105, | -0.0011, 0.0194, | 0.0175, | 0.0361, | 0.0827 |
| | 0.0182, | 0.0186, 0.0152 | 0.0188, 0.0153 | 0.0191, 0.0154 | 0.0192, 0.0154 | 0.0194, | 0.0197, 0.0156 | 0.0200, 0.0158 | 0.0207 0.0162 |
| MR-Weighted-Mode | 0.015 | 0.0152 | 0.0153 | 0.0154 | 0.0154 | 0.0155 | 0.0156 | 0.0158 | 0.0162 |
| ****- *** ergineu-Moue | -0.1861, | -0.1449, | -0.1278, | -0.1111, | -0.1027, | -0.0937, | -0.0775, | -0.0615, | -0.0194 |
| | 0.2148, | 0.2143, | 0.2145, | 0.2145, | 0.2143, | 0.2144, | 0.2144, | 0.2148, | 0.2149 |
| | 0.1606 | 0.1607 | 0.1602 | 0.1606 | 0.1607 | 0.1609 | 0.1609 | 0.1611 | 0.1617 |
| MR-RAPS1 | 0.066, | 0.068, | 0.086, | 0.098, | 0.108, | 0.120, | 0.153, | 0.184, | 0.300, |
| | -0.0237, | 0.0263, | 0.0463, | 0.0663, | 0.0763, | 0.0863, | 0.1063, | 0.1263, | 0.1763, |
| | 0.1311, | 0.1311, | 0.1311, | 0.1311, | 0.1311, | 0.1311, | 0.1311, | 0.1311, | 0.1311, |
| | 0.1253 | 0.1253 | 0.1253 | 0.1253 | 0.1253 | 0.1253 | 0.1253 | 0.1253 | 0.1253 |
| MR-RAPS2 | 0.079, | 0.071, | 0.078, | 0.091, | 0.096, | 0.113, | 0.128, | 0.157, | 0.240, |
| | -0.0369, | 0.0126, | 0.0332, | 0.0532, | 0.0632, | 0.0732, | 0.0932, | 0.1132, | 0.1632, |
| | 0.1455, | 0.1446, | 0.1455, | 0.1455, | 0.1455, | 0.1455, | 0.1455, | 0.1455, | 0.1455, |
| | 0.1352 | 0.1351 | 0.1352 | 0.1352 | 0.1352 | 0.1352 | 0.1352 | 0.1352 | 0.1352 |
| MR-RAPS3 | 0.917, | 0.919, | 0.918, | 0.924, | 0.922, | 0.921, | 0.930, | 0.939, | 0.956, |
| | 25.1174, | 2.3288, | 23.8104, | 0.9100, | 3.1148, | 0.6864, | -0.1778, | 5.7914, | -5.6541 |
| | 805.4906, | 179.6817, | 546.1389, | 40.5061, | 37.4361, | 41.8040, | 53.2802, | 65.8989, | 236.23 |
| MD DARGA | 8805.7142 | 550.0199 | 5379.2702 | 29.0598 | 25.0112 | 34.2991 | 71.1757 | 80.7173 | 1300.24 |
| MR-RAPS4 | 0.998, | 0.997, | 0.996, | 0.996, | 0.989, | 0.995, | 0.999, | 1.000, | 1.000, |
| | -0.2801, 16.3670, | 0.5836, 8.2056, | 0.7451, 13.5943, | 0.7734, 2.1873, | 0.8248, 2.1544, | 0.8971, 2.0181, | 0.9619, 2.2797, | 1.0511, 1.7062, | 1.1992, 1.5983, |
| | | | | | | | | | |

Table S88: Main simulations: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.6, and N=200000.

| , , | <i>'</i> | | - | | , I | | | | |
|---------------------|-------------------|-------------------|------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| cML-MA-AIC | 1.000, | 0.996, | 0.827, | 0.205, | 0.056, | 0.178, | 0.797, | 0.990, | 1.000, |
| | -0.0977, | -0.0479, | -0.0281, | -0.0090, | -0.0004, | 0.0083, | 0.0272, | 0.0471, | 0.0969, |
| | 0.0104, | 0.0106, | 0.0105, | 0.0097, | 0.0093, | 0.0097, | 0.0107, | 0.0109, | 0.0110, |
| | 0.0089 | 0.009 | 0.0091 | 0.0089 | 0.0089 | 0.009 | 0.0092 | 0.0093 | 0.0095 |
| cML-MA-AIC-Profile | 1.000, | 0.996, | 0.826, | 0.201, | 0.056, | 0.177, | 0.796, | 0.990, | 1.000, |
| AND MAY THE PROME | -0.0979, | -0.0480, | -0.0281, | -0.0090, | -0.0003, | 0.0083, | 0.0272, | 0.0471, | 0.0970, |
| | 0.0105, | 0.0106, | 0.0105, | 0.0097, | 0.0093, | 0.0097, | 0.0107, | 0.0109, | 0.0111 |
| | 0.0103, | 0.009 | 0.0091 | 0.0097, | 0.0093, | 0.0097, | 0.0092 | 0.0093 | 0.0095 |
| cML-AIC | 1.000, | 0.009 | | 0.286, | | | 0.859, | | 1.000, |
| CML-AIC | | | 0.883, | | 0.116, | 0.275, | | 0.993, | |
| | -0.0990, | -0.0492, | -0.0292, | -0.0096, | -0.0003, | 0.0089, | 0.0284, | 0.0484, | 0.0982 |
| | 0.0110, | 0.0112, | 0.0112, | 0.0108, | 0.0107, | 0.0111, | 0.0114, | 0.0115, | 0.0117 |
| | 0.0079 | 0.008 | 0.0081 | 0.0081 | 0.0081 | 0.0082 | 0.0082 | 0.0083 | 0.0085 |
| cML-AIC-Profile | 1.000, | 0.996, | 0.882, | 0.286, | 0.116, | 0.274, | 0.858, | 0.993, | 1.000, |
| | -0.0991, | -0.0492, | -0.0293, | -0.0096, | -0.0003, | 0.0089, | 0.0284, | 0.0484, | 0.0983 |
| | 0.0110, | 0.0112, | 0.0112, | 0.0108, | 0.0107, | 0.0111, | 0.0114, | 0.0115, | 0.0117 |
| | 0.008 | 0.008 | 0.0081 | 0.0081 | 0.0082 | 0.0082 | 0.0082 | 0.0083 | 0.0085 |
| cML-MA-BIC | 1.000, | 1.000, | 0.982, | 0.292, | 0.043, | 0.234, | 0.978, | 1.000, | 1.000, |
| | -0.1004, | -0.0504, | -0.0304, | -0.0104, | -0.0005, | 0.0095, | 0.0295, | 0.0495, | 0.0995 |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077 |
| | 0.0073 | 0.0074 | 0.0075 | 0.0075 | 0.0075 | 0.0076 | 0.0076 | 0.0077 | 0.0078 |
| cML-MA-BIC-Profile | 1.000, | 1.000, | 0.982, | 0.290, | 0.043, | 0.233, | 0.978, | 1.000, | 1.000, |
| ewiE-wia-Bie-i fome | -0.1004, | -0.0504, | -0.0304, | -0.0104, | -0.0005, | 0.0095, | 0.0295, | 0.0495, | 0.0995 |
| | | | | | | | | | |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077 |
| 10.50 | 0.0073 | 0.0074 | 0.0075 | 0.0075 | 0.0075 | 0.0076 | 0.0076 | 0.0077 | 0.0078 |
| cML-BIC | 1.000, | 1.000, | 0.981, | 0.301, | 0.046, | 0.239, | 0.977, | 1.000, | 1.000, |
| | -0.1004, | -0.0504, | -0.0304, | -0.0105, | -0.0005, | 0.0095, | 0.0295, | 0.0495, | 0.0995 |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077 |
| | 0.0073 | 0.0074 | 0.0074 | 0.0074 | 0.0075 | 0.0075 | 0.0076 | 0.0076 | 0.0078 |
| cML-BIC-Profile | 1.000, | 1.000, | 0.981, | 0.300, | 0.046, | 0.238, | 0.976, | 1.000, | 1.000, |
| | -0.1004, | -0.0504, | -0.0304, | -0.0105, | -0.0005, | 0.0095, | 0.0295, | 0.0495, | 0.0995 |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077 |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077 |
| MD M:- | | | | | | | | | |
| MR-Mix | 1.000, | 0.995, | 0.880, | 0.188, | 0.038, | 0.148, | 0.838, | 0.994, | 1.000, |
| | -0.0957, | -0.0474, | -0.0285, | -0.0098, | -0.0007, | 0.0085, | 0.0269, | 0.0451, | 0.0885 |
| | 0.0084, | 0.0081, | 0.0081, | 0.0081, | 0.0081, | 0.0081, | 0.0081, | 0.0083, | 0.0083 |
| | 0.0102 | 0.0102 | 0.0102 | 0.0101 | 0.0101 | 0.0101 | 0.01 | 0.01 | 0.01 |
| MR-ContMix | 1.000, | 1.000, | 0.981, | 0.325, | 0.049, | 0.245, | 0.979, | 1.000, | 1.000, |
| | -0.1002, | -0.0504, | -0.0304, | -0.0105, | -0.0005, | 0.0095, | 0.0294, | 0.0494, | 0.0992 |
| | 0.0073, | 0.0074, | 0.0075, | 0.0075, | 0.0075, | 0.0075, | 0.0076, | 0.0077, | 0.0078 |
| | NA | NA | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 1.000, | 0.973, | 0.280, | 0.043, | 0.228, | 0.966, | 1.000, | 1.000, |
| WIIC Eusso | -0.1002, | -0.0503, | -0.0304, | -0.0104, | -0.0004, | 0.0095, | 0.0295, | 0.0494, | 0.0994 |
| | | | | | | | | | |
| | 0.0075, | 0.0075, | 0.0076, | 0.0076, | 0.0077, | 0.0077, | 0.0077, | 0.0078, | 0.0080 |
| | 0.0075 | 0.0076 | 0.0076 | 0.0077 | 0.0077 | 0.0077 | 0.0078 | 0.0078 | 0.008 |
| MR-PRESSO | 0.897, | 0.763, | 0.683, | 0.444, | 0.436, | 0.587, | 0.929, | 0.958, | 0.981, |
| | -0.0709, | -0.0225, | -0.0027, | 0.0166, | 0.0265, | 0.0365, | 0.0556, | 0.0750, | 0.1225 |
| | 0.0746, | 0.0719, | 0.0718, | 0.0704, | 0.0704, | 0.0705, | 0.0685, | 0.0677, | 0.0611 |
| | 0.0138 | 0.0131 | 0.0131 | 0.013 | 0.013 | 0.013 | 0.0127 | 0.0125 | 0.0119 |
| MR-IVW | 0.070, | 0.069, | 0.083, | 0.102, | 0.112, | 0.124, | 0.168, | 0.202, | 0.319, |
| | -0.0162, | 0.0341, | 0.0542, | 0.0743, | 0.0844, | 0.0944, | 0.1145, | 0.1346, | 0.1848 |
| | 0.1297, | 0.1297, | 0.1297, | 0.1297, | 0.1297, | 0.1297, | 0.1297, | 0.1297, | 0.1297 |
| | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1257 | 0.1256 |
| MD IVIV O l . | | | | | | | | | |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.976, | 0.265, | 0.035, | 0.218, | 0.969, | 1.000, | 1.000, |
| | -0.1002, | -0.0503, | -0.0304, | -0.0104, | -0.0004, | 0.0095, | 0.0295, | 0.0494, | 0.0993 |
| | 0.0072, | 0.0073, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0077 |
| | 0.0076 | 0.0077 | 0.0077 | 0.0078 | 0.0078 | 0.0078 | 0.0079 | 0.0079 | 0.0081 |
| MR-Egger | 0.408, | 0.443, | 0.460, | 0.471, | 0.481, | 0.493, | 0.499, | 0.525, | 0.565, |
| | 0.6105, | 0.6600, | 0.6798, | 0.6996, | 0.7095, | 0.7194, | 0.7392, | 0.7589, | 0.8083 |
| | 0.4612, | 0.4612, | 0.4612, | 0.4612, | 0.4612, | 0.4612, | 0.4612, | 0.4612, | 0.4611 |
| | 0.37 | 0.37 | 0.37 | 0.37 | 0.37 | 0.37 | 0.3701 | 0.3701 | 0.3701 |
| MR-Weighted-Median | 1.000, | 0.996, | 0.903, | 0.350, | 0.136, | 0.088, | 0.504, | 0.916, | 0.999, |
| | -0.1032, | -0.0553, | -0.0361, | -0.0170, | -0.0075, | 0.0021, | 0.0211, | 0.0402, | 0.0878 |
| | 0.0117, | 0.0119, | 0.0121, | 0.0170, | 0.0124, | 0.0124, | 0.0211, | 0.0402, | 0.0378 |
| | 0.0117, | 0.0119, | 0.0121, | 0.0123, | 0.0124, | 0.0124, | 0.0126, | | 0.0133 |
| MD Waller 136 1 | | | | | | | | 0.0111 | |
| MR-Weighted-Mode | 0.945, | 0.913, | 0.887, | 0.858, | 0.829, | 0.802, | 0.708, | 0.625, | 0.436, |
| | -0.1606, | -0.1179, | -0.0995, | -0.0838, | -0.0766, | -0.0686, | -0.0535, | -0.0362, | 0.0047 |
| | 0.3591, | 0.3586, | 0.3583, | 0.3581, | 0.3580, | 0.3579, | 0.3565, | 0.3564, | 0.3562 |
| | 0.1746 | 0.1865 | 0.1764 | 0.1804 | 0.1781 | 0.1702 | 0.1689 | 0.1731 | 0.1647 |
| MR-RAPS1 | 0.060, | 0.057, | 0.073, | 0.094, | 0.103, | 0.118, | 0.162, | 0.202, | 0.310, |
| | -0.0170, | 0.0330, | 0.0530, | 0.0730, | 0.0830, | 0.0930, | 0.1130, | 0.1329, | 0.1829 |
| | 0.1265, | 0.1264, | 0.1264, | 0.1264, | 0.1264, | 0.1264, | 0.1264, | 0.1264, | 0.1264 |
| | 0.125 | 0.125 | 0.125 | 0.125 | 0.125 | 0.125 | 0.125 | 0.125 | 0.125 |
| MR-RAPS2 | 0.125 | 0.085, | 0.085, | 0.100, | 0.106, | 0.110, | 0.125 | 0.173, | 0.261, |
| WIN-NAP32 | | | | | | | | | |
| | -0.0399, | 0.0155, | 0.0356, | 0.0556, | 0.0693, | 0.0776, | 0.0996, | 0.1186, | 0.1703 |
| | 0.1520, | 0.1582, | 0.1477, | 0.1495, | 0.1541, | 0.1418, | 0.1484, | 0.1481, | 0.1479 |
| | 0.1311 | 0.1325 | 0.1332 | 0.1332 | 0.1336 | 0.1342 | 0.1342 | 0.134 | 0.1345 |
| MR-RAPS3 | 0.931, | 0.943, | 0.937, | 0.945, | 0.948, | 0.950, | 0.956, | 0.958, | 0.984, |
| | -4.3662, | -0.8313, | -0.3019, | 2.1165, | -0.6127, | 10.8055, | 3.4670, | 1.4311, | 3.0832 |
| | 120.3558, | 72.0796, | 214.2086, | 47.2097, | 103.8212, | 349.7168, | 134.0669, | 35.1436, | 17.763 |
| | 148.8028 | 59.7488 | 491.0617 | 27.6602 | 126.1302 | 1383.0164 | 228.6325 | 15.5759 | 5.1696 |
| MR-RAPS4 | | | | | 0.990, | | | | |
| WIK-KAPS4 | 1.000, | 0.999, | 0.999, | 0.999, | | 0.997, | 0.999, | 0.999, | 1.000, |
| | 0.3480, | 0.7353, | 0.6685, | 0.8426, | 0.9712, | 0.9250, | 0.9291, | 1.0774, | 1.1822 |
| | | | | | | | | | |
| | 2.6821, 0.0441 | 2.1236, 0.0389 | 2.4392, 0.068 | 3.0054, 0.0636 | 2.6826, 0.0492 | 2.1687, 0.0401 | 2.2197, 0.0372 | 1.7498, 0.0362 | 2.6545, 0.0505 |

Table S89: Main simulations: the relative frequencies of cML-BIC selecting $\hat{K} = K_0$ for m = 10 and the InSIDE satisfied.

| θ | | q = 0 | | | q = 0.2 | | | q = 0.4 | | | q = 0.6 | |
|-------|---------|----------|----------|---------|----------|----------|---------|----------|----------|---------|----------|----------|
| | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k |
| -0.1 | 0.992 | 0.998 | 0.996 | 0.994 | 0.996 | 0.998 | 0.996 | 0.997 | 0.998 | 0.997 | 1.000 | 0.999 |
| -0.05 | 0.989 | 0.997 | 0.996 | 0.994 | 0.997 | 0.998 | 0.994 | 0.996 | 0.997 | 0.997 | 0.998 | 0.998 |
| -0.03 | 0.988 | 0.997 | 0.996 | 0.994 | 0.997 | 0.998 | 0.994 | 0.996 | 0.997 | 0.998 | 0.998 | 0.998 |
| -0.01 | 0.989 | 0.995 | 0.996 | 0.994 | 0.997 | 0.998 | 0.994 | 0.996 | 0.997 | 0.998 | 0.998 | 0.998 |
| 0 | 0.989 | 0.995 | 0.996 | 0.994 | 0.996 | 0.998 | 0.994 | 0.996 | 0.997 | 0.998 | 0.997 | 0.998 |
| 0.01 | 0.989 | 0.995 | 0.996 | 0.994 | 0.996 | 0.998 | 0.994 | 0.996 | 0.997 | 0.998 | 0.997 | 0.998 |
| 0.03 | 0.987 | 0.994 | 0.996 | 0.994 | 0.995 | 0.998 | 0.994 | 0.996 | 0.996 | 0.997 | 0.998 | 0.998 |
| 0.05 | 0.987 | 0.994 | 0.996 | 0.994 | 0.995 | 0.997 | 0.994 | 0.996 | 0.996 | 0.996 | 0.998 | 0.998 |
| 0.1 | 0.988 | 0.993 | 0.995 | 0.993 | 0.995 | 0.997 | 0.994 | 0.996 | 0.996 | 0.997 | 0.998 | 0.998 |

Table S90: Main simulations: the relative frequencies of cML-BIC selecting $\hat{K} = K_0$ for m = 10 and the InSIDE violated.

| θ | | q = 0 | | | q = 0.2 | | | q = 0.4 | | | q = 0.6 | |
|-------|---------|----------|----------|---------|----------|----------|---------|----------|----------|---------|----------|----------|
| | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k |
| -0.1 | 0.992 | 0.998 | 0.996 | 0.991 | 0.994 | 0.996 | 0.997 | 0.998 | 0.998 | 0.995 | 0.998 | 0.999 |
| -0.05 | 0.989 | 0.997 | 0.996 | 0.994 | 0.994 | 0.996 | 0.996 | 0.997 | 0.998 | 0.995 | 0.999 | 0.999 |
| -0.03 | 0.988 | 0.997 | 0.996 | 0.993 | 0.995 | 0.996 | 0.995 | 0.996 | 0.999 | 0.996 | 0.999 | 0.998 |
| -0.01 | 0.989 | 0.995 | 0.996 | 0.992 | 0.994 | 0.996 | 0.997 | 0.996 | 0.999 | 0.996 | 0.999 | 0.999 |
| 0 | 0.989 | 0.995 | 0.996 | 0.992 | 0.994 | 0.996 | 0.996 | 0.995 | 0.999 | 0.996 | 0.999 | 0.999 |
| 0.01 | 0.989 | 0.995 | 0.996 | 0.992 | 0.994 | 0.996 | 0.996 | 0.995 | 0.998 | 0.996 | 0.999 | 0.999 |
| 0.03 | 0.987 | 0.994 | 0.996 | 0.992 | 0.995 | 0.996 | 0.996 | 0.995 | 0.999 | 0.996 | 0.999 | 0.999 |
| 0.05 | 0.987 | 0.994 | 0.996 | 0.992 | 0.995 | 0.996 | 0.996 | 0.996 | 0.999 | 0.998 | 0.999 | 0.999 |
| 0.1 | 0.988 | 0.993 | 0.995 | 0.993 | 0.994 | 0.996 | 0.998 | 0.995 | 0.997 | 0.998 | 0.999 | 0.999 |
| | | | | | | | | | | | | |

Table S91: Main simulations: the relative frequencies of cML-BIC selecting $\hat{K} = K_0$ for m = 20 and the InSIDE satisfied.

| θ | | q = 0 | | | q = 0.2 | | | q = 0.4 | | | q = 0.6 | |
|-------|---------|----------|----------|---------|----------|----------|---------|----------|----------|---------|----------|----------|
| | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k |
| -0.1 | 0.980 | 0.985 | 0.993 | 0.979 | 0.990 | 0.992 | 0.989 | 0.994 | 0.994 | 0.991 | 0.995 | 0.997 |
| -0.05 | 0.983 | 0.987 | 0.994 | 0.981 | 0.988 | 0.995 | 0.989 | 0.992 | 0.995 | 0.992 | 0.994 | 0.998 |
| -0.03 | 0.986 | 0.989 | 0.994 | 0.979 | 0.988 | 0.995 | 0.987 | 0.993 | 0.995 | 0.992 | 0.994 | 0.998 |
| -0.01 | 0.987 | 0.988 | 0.994 | 0.982 | 0.988 | 0.995 | 0.987 | 0.993 | 0.995 | 0.993 | 0.995 | 0.997 |
| 0 | 0.987 | 0.989 | 0.994 | 0.983 | 0.988 | 0.995 | 0.987 | 0.993 | 0.995 | 0.993 | 0.995 | 0.997 |
| 0.01 | 0.987 | 0.990 | 0.994 | 0.983 | 0.987 | 0.995 | 0.987 | 0.994 | 0.995 | 0.992 | 0.995 | 0.997 |
| 0.03 | 0.987 | 0.990 | 0.993 | 0.982 | 0.987 | 0.996 | 0.986 | 0.995 | 0.993 | 0.993 | 0.995 | 0.997 |
| 0.05 | 0.988 | 0.989 | 0.993 | 0.983 | 0.987 | 0.996 | 0.987 | 0.995 | 0.993 | 0.992 | 0.995 | 0.998 |
| 0.1 | 0.987 | 0.990 | 0.992 | 0.982 | 0.989 | 0.996 | 0.986 | 0.996 | 0.992 | 0.992 | 0.996 | 0.996 |

Table S92: Main simulations: the relative frequencies of cML-BIC selecting $\hat{K} = K_0$ for m = 20 and the InSIDE violated.

| А | | q = 0 | | | q = 0.2 | | | q = 0.4 | | | q = 0.6 | |
|-------|---------|----------|----------|---------|----------|----------|---------|----------|----------|---------|----------|----------|
| | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k |
| -0.1 | 0.980 | 0.985 | 0.993 | 0.990 | 0.993 | 0.989 | 0.995 | 0.998 | 0.996 | 0.988 | 0.995 | 0.997 |
| -0.05 | 0.983 | 0.987 | 0.994 | 0.988 | 0.993 | 0.989 | 0.993 | 0.995 | 0.994 | 0.984 | 0.995 | 0.997 |
| -0.03 | 0.986 | 0.989 | 0.994 | 0.988 | 0.991 | 0.989 | 0.993 | 0.994 | 0.995 | 0.984 | 0.994 | 0.997 |
| -0.01 | 0.987 | 0.988 | 0.994 | 0.987 | 0.991 | 0.989 | 0.993 | 0.994 | 0.994 | 0.984 | 0.995 | 0.997 |
| 0 | 0.987 | 0.989 | 0.994 | 0.986 | 0.990 | 0.989 | 0.992 | 0.993 | 0.994 | 0.985 | 0.995 | 0.998 |
| 0.01 | 0.987 | 0.990 | 0.994 | 0.986 | 0.990 | 0.989 | 0.991 | 0.993 | 0.994 | 0.985 | 0.995 | 0.998 |
| 0.03 | 0.987 | 0.990 | 0.993 | 0.987 | 0.990 | 0.989 | 0.992 | 0.993 | 0.994 | 0.986 | 0.995 | 0.998 |
| 0.05 | 0.988 | 0.989 | 0.993 | 0.986 | 0.990 | 0.989 | 0.994 | 0.992 | 0.994 | 0.985 | 0.995 | 0.998 |
| 0.1 | 0.987 | 0.990 | 0.992 | 0.986 | 0.990 | 0.990 | 0.992 | 0.988 | 0.993 | 0.986 | 0.996 | 0.998 |

Table S93: Main simulations: the relative frequencies of cML-BIC selecting $\hat{K} = K_0$ for m = 100 and the InSIDE satisfied.

| θ | | q = 0 | | | q = 0.2 | | | q = 0.4 | | | q = 0.6 | |
|-------|---------|----------|----------|---------|----------|----------|---------|----------|----------|---------|----------|----------|
| | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k |
| -0.1 | 0.897 | 0.928 | 0.958 | 0.931 | 0.945 | 0.957 | 0.945 | 0.957 | 0.974 | 0.963 | 0.965 | 0.988 |
| -0.05 | 0.906 | 0.937 | 0.957 | 0.936 | 0.944 | 0.955 | 0.942 | 0.964 | 0.975 | 0.963 | 0.973 | 0.989 |
| -0.03 | 0.906 | 0.936 | 0.956 | 0.936 | 0.945 | 0.958 | 0.939 | 0.967 | 0.974 | 0.964 | 0.973 | 0.988 |
| -0.01 | 0.903 | 0.935 | 0.950 | 0.940 | 0.945 | 0.957 | 0.938 | 0.964 | 0.976 | 0.963 | 0.971 | 0.988 |
| 0 | 0.903 | 0.937 | 0.949 | 0.942 | 0.947 | 0.957 | 0.940 | 0.964 | 0.976 | 0.964 | 0.970 | 0.986 |
| 0.01 | 0.908 | 0.939 | 0.950 | 0.940 | 0.945 | 0.957 | 0.940 | 0.964 | 0.976 | 0.964 | 0.971 | 0.986 |
| 0.03 | 0.909 | 0.937 | 0.952 | 0.942 | 0.945 | 0.956 | 0.942 | 0.965 | 0.977 | 0.963 | 0.971 | 0.986 |
| 0.05 | 0.913 | 0.932 | 0.952 | 0.941 | 0.950 | 0.956 | 0.940 | 0.963 | 0.978 | 0.961 | 0.970 | 0.986 |
| 0.1 | 0.912 | 0.928 | 0.955 | 0.943 | 0.947 | 0.961 | 0.941 | 0.969 | 0.975 | 0.963 | 0.970 | 0.984 |

Table S94: Main simulations: the relative frequencies of cML-BIC selecting $\hat{K} = K_0$ for m = 100 and the InSIDE violated.

| θ | | q = 0 | | | q = 0.2 | | | q = 0.4 | | | q = 0.6 | |
|-------|---------|----------|----------|---------|----------|----------|---------|----------|----------|---------|----------|----------|
| | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k | N = 50k | N = 100k | N = 200k |
| -0.1 | 0.897 | 0.928 | 0.958 | 0.930 | 0.946 | 0.961 | 0.943 | 0.948 | 0.965 | 0.971 | 0.975 | 0.987 |
| -0.05 | 0.906 | 0.937 | 0.957 | 0.916 | 0.944 | 0.967 | 0.946 | 0.952 | 0.971 | 0.968 | 0.975 | 0.988 |
| -0.03 | 0.906 | 0.936 | 0.956 | 0.915 | 0.951 | 0.966 | 0.948 | 0.951 | 0.973 | 0.965 | 0.976 | 0.986 |
| -0.01 | 0.903 | 0.935 | 0.950 | 0.913 | 0.951 | 0.966 | 0.947 | 0.952 | 0.971 | 0.965 | 0.976 | 0.985 |
| 0 | 0.903 | 0.937 | 0.949 | 0.914 | 0.951 | 0.967 | 0.949 | 0.953 | 0.972 | 0.965 | 0.977 | 0.985 |
| 0.01 | 0.908 | 0.939 | 0.950 | 0.913 | 0.951 | 0.966 | 0.952 | 0.952 | 0.972 | 0.966 | 0.978 | 0.985 |
| 0.03 | 0.909 | 0.937 | 0.952 | 0.915 | 0.954 | 0.966 | 0.949 | 0.952 | 0.973 | 0.964 | 0.978 | 0.985 |
| 0.05 | 0.913 | 0.932 | 0.952 | 0.917 | 0.955 | 0.963 | 0.949 | 0.955 | 0.972 | 0.962 | 0.978 | 0.985 |
| 0.1 | 0.912 | 0.928 | 0.955 | 0.912 | 0.951 | 0.962 | 0.947 | 0.956 | 0.974 | 0.958 | 0.978 | 0.984 |

Table S95: Comparison of cML-MA-BIC and cML-BIC with cML-MA-BIC-DP and cML-BIC-DP: in each cell, from top to bottom are empirical type-I error/power, $\operatorname{mean}(\hat{\theta})$, $\operatorname{SD}(\hat{\theta})$, $\operatorname{mean}(\operatorname{SE}(\hat{\theta}))$ when m=10, the InSIDE violated, q=0.6, N=50000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------|----------|----------|----------|----------|----------|---------|---------|---------|---------|
| cML-MA-BIC | 0.768, | 0.259, | 0.124, | 0.055, | 0.044, | 0.044, | 0.095, | 0.219, | 0.673, |
| | -0.1008, | -0.0506, | -0.0307, | -0.0107, | -0.0008, | 0.0091, | 0.0291, | 0.0488, | 0.0989, |
| | 0.0372, | 0.0377, | 0.0379, | 0.0382, | 0.0384, | 0.0386, | 0.0391, | 0.0395, | 0.0410, |
| | 0.0379 | 0.0386 | 0.0389 | 0.0392 | 0.0394 | 0.0396 | 0.0400 | 0.0404 | 0.0415 |
| cML-BIC | 0.783, | 0.267, | 0.132, | 0.058, | 0.047, | 0.050, | 0.102, | 0.229, | 0.682, |
| | -0.1012, | -0.0509, | -0.0309, | -0.0108, | -0.0008, | 0.0093, | 0.0293, | 0.0492, | 0.0995, |
| | 0.0374, | 0.0381, | 0.0383, | 0.0386, | 0.0388, | 0.0391, | 0.0395, | 0.0396, | 0.0408, |
| | 0.0375 | 0.0381 | 0.0384 | 0.0388 | 0.0389 | 0.0391 | 0.0395 | 0.0399 | 0.0411 |
| cML-MA-BIC-DP, T = 100 | 0.774, | 0.259, | 0.127, | 0.060, | 0.043, | 0.043, | 0.091, | 0.205, | 0.647, |
| | -0.1004, | -0.0505, | -0.0307, | -0.0110, | -0.0012, | 0.0086, | 0.0283, | 0.0480, | 0.0976, |
| | 0.0371, | 0.0374, | 0.0375, | 0.0377, | 0.0379, | 0.0381, | 0.0386, | 0.0392, | 0.0408, |
| | 0.0375 | 0.0382 | 0.0385 | 0.0389 | 0.0391 | 0.0394 | 0.0399 | 0.0405 | 0.0421 |
| cML-BIC-DP, $T = 100$ | 0.803, | 0.281, | 0.145, | 0.068, | 0.051, | 0.052, | 0.104, | 0.226, | 0.682, |
| | -0.1016, | -0.0514, | -0.0314, | -0.0113, | -0.0013, | 0.0087, | 0.0288, | 0.0487, | 0.0988, |
| | 0.0373, | 0.0379, | 0.0382, | 0.0385, | 0.0387, | 0.0389, | 0.0393, | 0.0398, | 0.0411, |
| | 0.0366 | 0.0375 | 0.0379 | 0.0383 | 0.0385 | 0.0388 | 0.0393 | 0.0398 | 0.0411 |
| cML-MA-BIC-DP, T = 200 | 0.756, | 0.258, | 0.119, | 0.058, | 0.041, | 0.045, | 0.091, | 0.202, | 0.654, |
| | -0.1002, | -0.0503, | -0.0305, | -0.0108, | -0.0010, | 0.0089, | 0.0285, | 0.0483, | 0.0979, |
| | 0.0372, | 0.0375, | 0.0376, | 0.0378, | 0.0380, | 0.0382, | 0.0387, | 0.0393, | 0.0409, |
| | 0.0378 | 0.0385 | 0.0388 | 0.0392 | 0.0394 | 0.0396 | 0.0401 | 0.0406 | 0.0422 |
| cML-BIC-DP, $T = 200$ | 0.785, | 0.278, | 0.138, | 0.064, | 0.052, | 0.050, | 0.104, | 0.227, | 0.684, |
| | -0.1014, | -0.0512, | -0.0311, | -0.0111, | -0.0010, | 0.0090, | 0.0290, | 0.0490, | 0.0992, |
| | 0.0374, | 0.0380, | 0.0383, | 0.0386, | 0.0388, | 0.0389, | 0.0394, | 0.0398, | 0.0410, |
| | 0.0369 | 0.0377 | 0.0381 | 0.0385 | 0.0387 | 0.0390 | 0.0394 | 0.0399 | 0.0412 |
| cML-MA-BIC-DP, T = 500 | 0.761, | 0.254, | 0.120, | 0.056, | 0.040, | 0.043, | 0.092, | 0.214, | 0.655, |
| | -0.1002, | -0.0503, | -0.0306, | -0.0108, | -0.0010, | 0.0088, | 0.0285, | 0.0483, | 0.0979, |
| | 0.0371, | 0.0374, | 0.0375, | 0.0377, | 0.0378, | 0.0380, | 0.0385, | 0.0391, | 0.0408, |
| | 0.0377 | 0.0384 | 0.0387 | 0.0390 | 0.0392 | 0.0394 | 0.0399 | 0.0405 | 0.0420 |
| cML-BIC-DP, $T = 500$ | 0.789, | 0.277, | 0.135, | 0.063, | 0.049, | 0.053, | 0.107, | 0.232, | 0.683, |
| | -0.1014, | -0.0512, | -0.0312, | -0.0111, | -0.0011, | 0.0089, | 0.0289, | 0.0490, | 0.0991, |
| | 0.0373, | 0.0379, | 0.0382, | 0.0385, | 0.0386, | 0.0388, | 0.0392, | 0.0397, | 0.0410, |
| | 0.0369 | 0.0376 | 0.0380 | 0.0384 | 0.0386 | 0.0388 | 0.0393 | 0.0398 | 0.0410 |

Table S96: Comparison of cML-MA-BIC and cML-BIC with cML-MA-BIC-DP and cML-BIC-DP: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE violated, q=0.6, N=100000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------|----------|----------|----------|----------|---------|---------|---------|---------|---------|
| cML-MA-BIC | 0.955, | 0.451, | 0.188, | 0.050, | 0.036, | 0.053, | 0.202, | 0.446, | 0.935, |
| | -0.0988, | -0.0488, | -0.0288, | -0.0089, | 0.0010, | 0.0109, | 0.0308, | 0.0507, | 0.1007, |
| | 0.0260, | 0.0265, | 0.0266, | 0.0268, | 0.0270, | 0.0271, | 0.0275, | 0.0279, | 0.0288, |
| | 0.0267 | 0.0272 | 0.0274 | 0.0276 | 0.0278 | 0.0279 | 0.0281 | 0.0284 | 0.0293 |
| cML-BIC | 0.960, | 0.466, | 0.198, | 0.055, | 0.039, | 0.056, | 0.208, | 0.457, | 0.938, |
| | -0.0991, | -0.0491, | -0.0291, | -0.0091, | 0.0009, | 0.0109, | 0.0310, | 0.0510, | 0.1010, |
| | 0.0260, | 0.0265, | 0.0267, | 0.0270, | 0.0271, | 0.0273, | 0.0276, | 0.0279, | 0.0288, |
| | 0.0264 | 0.0269 | 0.0271 | 0.0273 | 0.0275 | 0.0276 | 0.0279 | 0.0282 | 0.0290 |
| cML-MA-BIC-DP, T = 100 | 0.954, | 0.457, | 0.183, | 0.055, | 0.039, | 0.057, | 0.195, | 0.433, | 0.919, |
| | -0.0984, | -0.0485, | -0.0287, | -0.0090, | 0.0008, | 0.0107, | 0.0303, | 0.0501, | 0.1000, |
| | 0.0261, | 0.0264, | 0.0264, | 0.0266, | 0.0267, | 0.0269, | 0.0273, | 0.0278, | 0.0289, |
| | 0.0263 | 0.0268 | 0.0270 | 0.0273 | 0.0274 | 0.0276 | 0.0280 | 0.0284 | 0.0294 |
| cML-BIC-DP, T = 100 | 0.961, | 0.487, | 0.203, | 0.061, | 0.044, | 0.065, | 0.213, | 0.464, | 0.933, |
| | -0.0992, | -0.0492, | -0.0291, | -0.0091, | 0.0009, | 0.0108, | 0.0309, | 0.0509, | 0.1009, |
| | 0.0260, | 0.0265, | 0.0268, | 0.0270, | 0.0272, | 0.0273, | 0.0276, | 0.0280, | 0.0289, |
| | 0.0257 | 0.0263 | 0.0266 | 0.0269 | 0.0270 | 0.0272 | 0.0275 | 0.0278 | 0.0288 |
| cML-MA-BIC-DP, T = 200 | 0.957, | 0.449, | 0.184, | 0.051, | 0.038, | 0.056, | 0.195, | 0.444, | 0.928, |
| | -0.0984, | -0.0485, | -0.0287, | -0.0090, | 0.0008, | 0.0107, | 0.0304, | 0.0502, | 0.1000, |
| | 0.0260, | 0.0263, | 0.0264, | 0.0265, | 0.0266, | 0.0268, | 0.0273, | 0.0278, | 0.0289, |
| | 0.0265 | 0.0270 | 0.0272 | 0.0274 | 0.0275 | 0.0277 | 0.0281 | 0.0284 | 0.0295 |
| cML-BIC-DP, T = 200 | 0.964, | 0.472, | 0.206, | 0.058, | 0.044, | 0.061, | 0.213, | 0.468, | 0.938, |
| | -0.0992, | -0.0491, | -0.0291, | -0.0091, | 0.0009, | 0.0109, | 0.0309, | 0.0509, | 0.1010, |
| | 0.0261, | 0.0265, | 0.0267, | 0.0270, | 0.0271, | 0.0272, | 0.0276, | 0.0279, | 0.0288, |
| | 0.0259 | 0.0264 | 0.0267 | 0.0270 | 0.0271 | 0.0273 | 0.0276 | 0.0279 | 0.0288 |
| cML-MA-BIC-DP, T = 500 | 0.956, | 0.461, | 0.187, | 0.052, | 0.039, | 0.056, | 0.200, | 0.443, | 0.929, |
| | -0.0984, | -0.0485, | -0.0286, | -0.0089, | 0.0009, | 0.0107, | 0.0304, | 0.0502, | 0.1001, |
| | 0.0261, | 0.0264, | 0.0265, | 0.0266, | 0.0268, | 0.0269, | 0.0274, | 0.0279, | 0.0290, |
| | 0.0265 | 0.0269 | 0.0271 | 0.0273 | 0.0275 | 0.0276 | 0.0280 | 0.0284 | 0.0294 |
| cML-BIC-DP, T = 500 | 0.962, | 0.486, | 0.205, | 0.062, | 0.048, | 0.067, | 0.215, | 0.465, | 0.939, |
| | -0.0991, | -0.0491, | -0.0291, | -0.0091, | 0.0009, | 0.0109, | 0.0309, | 0.0509, | 0.1010, |
| | 0.0262, | 0.0266, | 0.0268, | 0.0271, | 0.0272, | 0.0274, | 0.0277, | 0.0280, | 0.0289, |
| | 0.0258 | 0.0264 | 0.0266 | 0.0269 | 0.0271 | 0.0272 | 0.0275 | 0.0278 | 0.0287 |

Table S97: Comparison of cML-MA-BIC and cML-BIC with cML-MA-BIC-DP and cML-BIC-DP: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=10, the InSIDE violated, q=0.6, N=200000.

| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------|----------|----------|----------|----------|----------|---------|---------|---------|---------|
| cML-MA-BIC | 0.998, | 0.748, | 0.334, | 0.076, | 0.048, | 0.079, | 0.325, | 0.709, | 0.997, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0100, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0187, | 0.0190, | 0.0191, | 0.0192, | 0.0193, | 0.0193, | 0.0196, | 0.0198, | 0.0203, |
| | 0.0189 | 0.0192 | 0.0194 | 0.0196 | 0.0197 | 0.0197 | 0.0199 | 0.0202 | 0.0207 |
| cML-BIC | 0.998, | 0.756, | 0.347, | 0.079, | 0.051, | 0.086, | 0.335, | 0.714, | 0.998, |
| | -0.1001, | -0.0501, | -0.0301, | -0.0100, | 0.0000, | 0.0100, | 0.0300, | 0.0500, | 0.1000, |
| | 0.0187, | 0.0189, | 0.0191, | 0.0193, | 0.0194, | 0.0195, | 0.0196, | 0.0198, | 0.0204, |
| | 0.0187 | 0.0190 | 0.0192 | 0.0194 | 0.0195 | 0.0196 | 0.0198 | 0.0200 | 0.0205 |
| cML-MA-BIC-DP, T = 100 | 0.996, | 0.752, | 0.343, | 0.077, | 0.054, | 0.082, | 0.324, | 0.703, | 0.995, |
| | -0.0997, | -0.0497, | -0.0298, | -0.0100, | -0.0001, | 0.0097, | 0.0295, | 0.0494, | 0.0994, |
| | 0.0188, | 0.0190, | 0.0190, | 0.0190, | 0.0191, | 0.0192, | 0.0195, | 0.0198, | 0.0204, |
| | 0.0186 | 0.0190 | 0.0191 | 0.0193 | 0.0194 | 0.0195 | 0.0198 | 0.0201 | 0.0208 |
| cML-BIC-DP, $T = 100$ | 0.997, | 0.771, | 0.373, | 0.085, | 0.061, | 0.088, | 0.341, | 0.720, | 0.997, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0999, |
| | 0.0187, | 0.0190, | 0.0191, | 0.0193, | 0.0193, | 0.0195, | 0.0197, | 0.0198, | 0.0204, |
| | 0.0182 | 0.0186 | 0.0188 | 0.0190 | 0.0192 | 0.0193 | 0.0195 | 0.0197 | 0.0204 |
| cML-MA-BIC-DP, T = 200 | 0.997, | 0.755, | 0.342, | 0.076, | 0.047, | 0.080, | 0.329, | 0.701, | 0.996, |
| | -0.0998, | -0.0497, | -0.0298, | -0.0100, | -0.0002, | 0.0097, | 0.0295, | 0.0494, | 0.0994, |
| | 0.0187, | 0.0190, | 0.0190, | 0.0190, | 0.0191, | 0.0192, | 0.0195, | 0.0198, | 0.0203, |
| | 0.0187 | 0.0191 | 0.0192 | 0.0194 | 0.0195 | 0.0196 | 0.0199 | 0.0201 | 0.0208 |
| cML-BIC-DP, T = 200 | 0.997, | 0.773, | 0.365, | 0.085, | 0.052, | 0.083, | 0.345, | 0.714, | 0.997, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0999, |
| | 0.0187, | 0.0190, | 0.0191, | 0.0192, | 0.0193, | 0.0194, | 0.0196, | 0.0197, | 0.0203, |
| | 0.0183 | 0.0187 | 0.0189 | 0.0191 | 0.0192 | 0.0194 | 0.0196 | 0.0198 | 0.0204 |
| cML-MA-BIC-DP, T = 500 | 0.998, | 0.758, | 0.341, | 0.076, | 0.046, | 0.078, | 0.321, | 0.709, | 0.997, |
| | -0.0997, | -0.0497, | -0.0298, | -0.0100, | -0.0001, | 0.0097, | 0.0295, | 0.0494, | 0.0994, |
| | 0.0187, | 0.0189, | 0.0190, | 0.0190, | 0.0191, | 0.0192, | 0.0195, | 0.0198, | 0.0203, |
| | 0.0186 | 0.0190 | 0.0191 | 0.0193 | 0.0194 | 0.0195 | 0.0198 | 0.0200 | 0.0207 |
| cML-BIC-DP, $T = 500$ | 0.998, | 0.773, | 0.362, | 0.080, | 0.048, | 0.090, | 0.341, | 0.723, | 0.998, |
| | -0.1002, | -0.0501, | -0.0301, | -0.0101, | -0.0001, | 0.0099, | 0.0298, | 0.0498, | 0.0999, |
| | 0.0187, | 0.0190, | 0.0191, | 0.0192, | 0.0193, | 0.0194, | 0.0196, | 0.0198, | 0.0203, |
| | 0.0183 | 0.0187 | 0.0188 | 0.0190 | 0.0192 | 0.0193 | 0.0195 | 0.0197 | 0.0203 |

Table S98: Comparison of cML-MA-BIC and cML-BIC with cML-MA-BIC-DP and cML-BIC-DP: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE violated, q=0.6, N=50000.

| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------|----------|----------|----------|----------|----------|---------|---------|---------|---------|
| cML-MA-BIC | 0.957, | 0.435, | 0.194, | 0.063, | 0.037, | 0.053, | 0.165, | 0.401, | 0.917, |
| | -0.1000, | -0.0500, | -0.0301, | -0.0102, | -0.0002, | 0.0097, | 0.0296, | 0.0496, | 0.0996, |
| | 0.0265, | 0.0270, | 0.0271, | 0.0273, | 0.0274, | 0.0275, | 0.0279, | 0.0282, | 0.0291, |
| | 0.0274 | 0.0279 | 0.0281 | 0.0284 | 0.0285 | 0.0286 | 0.0289 | 0.0292 | 0.0300 |
| cML-BIC | 0.957, | 0.446, | 0.200, | 0.065, | 0.042, | 0.060, | 0.180, | 0.423, | 0.922, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0102, | -0.0002, | 0.0098, | 0.0298, | 0.0498, | 0.0998, |
| | 0.0266, | 0.0272, | 0.0274, | 0.0277, | 0.0277, | 0.0279, | 0.0281, | 0.0284, | 0.0292, |
| | 0.0271 | 0.0275 | 0.0277 | 0.0280 | 0.0281 | 0.0282 | 0.0285 | 0.0288 | 0.0296 |
| cML-MA-BIC-DP, T = 100 | 0.929, | 0.385, | 0.162, | 0.052, | 0.031, | 0.041, | 0.138, | 0.353, | 0.880, |
| | -0.0986, | -0.0488, | -0.0292, | -0.0098, | -0.0001, | 0.0096, | 0.0290, | 0.0486, | 0.0981, |
| | 0.0266, | 0.0267, | 0.0267, | 0.0267, | 0.0268, | 0.0270, | 0.0274, | 0.0279, | 0.0292, |
| | 0.0291 | 0.0293 | 0.0294 | 0.0295 | 0.0296 | 0.0297 | 0.0301 | 0.0306 | 0.0317 |
| cML-BIC-DP, $T = 100$ | 0.950, | 0.425, | 0.189, | 0.065, | 0.037, | 0.060, | 0.165, | 0.406, | 0.899, |
| | -0.0998, | -0.0497, | -0.0298, | -0.0099, | 0.0000, | 0.0099, | 0.0297, | 0.0497, | 0.0995, |
| | 0.0267, | 0.0271, | 0.0272, | 0.0275, | 0.0276, | 0.0277, | 0.0281, | 0.0284, | 0.0295, |
| | 0.0278 | 0.0282 | 0.0284 | 0.0286 | 0.0287 | 0.0289 | 0.0291 | 0.0294 | 0.0304 |
| cML-MA-BIC-DP, T = 200 | 0.935, | 0.392, | 0.169, | 0.053, | 0.033, | 0.043, | 0.138, | 0.345, | 0.880, |
| | -0.0989, | -0.0492, | -0.0296, | -0.0101, | -0.0005, | 0.0092, | 0.0286, | 0.0482, | 0.0977, |
| | 0.0266, | 0.0267, | 0.0267, | 0.0267, | 0.0268, | 0.0269, | 0.0274, | 0.0279, | 0.0291, |
| | 0.0286 | 0.0289 | 0.0290 | 0.0292 | 0.0293 | 0.0294 | 0.0299 | 0.0303 | 0.0316 |
| cML-BIC-DP, T = 200 | 0.955, | 0.438, | 0.191, | 0.067, | 0.041, | 0.056, | 0.174, | 0.414, | 0.898, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0103, | -0.0004, | 0.0095, | 0.0294, | 0.0492, | 0.0991, |
| | 0.0266, | 0.0271, | 0.0272, | 0.0275, | 0.0276, | 0.0277, | 0.0281, | 0.0285, | 0.0294, |
| | 0.0273 | 0.0278 | 0.0281 | 0.0283 | 0.0284 | 0.0286 | 0.0289 | 0.0292 | 0.0302 |
| cML-MA-BIC-DP, T = 500 | 0.936, | 0.373, | 0.160, | 0.050, | 0.027, | 0.038, | 0.127, | 0.341, | 0.877, |
| | -0.0986, | -0.0489, | -0.0293, | -0.0099, | -0.0003, | 0.0094, | 0.0288, | 0.0483, | 0.0978, |
| | 0.0265, | 0.0266, | 0.0265, | 0.0265, | 0.0266, | 0.0268, | 0.0272, | 0.0278, | 0.0290, |
| | 0.0290 | 0.0293 | 0.0293 | 0.0295 | 0.0296 | 0.0297 | 0.0302 | 0.0306 | 0.0319 |
| cML-BIC-DP, T = 500 | 0.945, | 0.429, | 0.183, | 0.061, | 0.036, | 0.056, | 0.165, | 0.394, | 0.906, |
| | -0.0999, | -0.0499, | -0.0300, | -0.0101, | -0.0002, | 0.0097, | 0.0295, | 0.0494, | 0.0993, |
| | 0.0266, | 0.0269, | 0.0271, | 0.0273, | 0.0274, | 0.0276, | 0.0279, | 0.0283, | 0.0293, |
| | 0.0278 | 0.0282 | 0.0284 | 0.0287 | 0.0288 | 0.0289 | 0.0292 | 0.0295 | 0.0305 |

Table S99: Comparison of cML-MA-BIC and cML-BIC with cML-MA-BIC-DP and cML-BIC-DP: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE violated, q=0.6, N=100000.

| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------|----------|----------|----------|----------|---------|---------|---------|---------|---------|
| cML-MA-BIC | 0.999, | 0.700, | 0.330, | 0.078, | 0.051, | 0.086, | 0.332, | 0.695, | 0.997, |
| | -0.0996, | -0.0495, | -0.0295, | -0.0095, | 0.0004, | 0.0104, | 0.0304, | 0.0504, | 0.1005, |
| | 0.0195, | 0.0198, | 0.0199, | 0.0201, | 0.0201, | 0.0202, | 0.0204, | 0.0207, | 0.0212, |
| | 0.0193 | 0.0196 | 0.0198 | 0.0199 | 0.0200 | 0.0201 | 0.0203 | 0.0205 | 0.0211 |
| cML-BIC | 0.999, | 0.711, | 0.338, | 0.080, | 0.055, | 0.091, | 0.342, | 0.703, | 0.997, |
| | -0.0996, | -0.0496, | -0.0296, | -0.0096, | 0.0004, | 0.0105, | 0.0305, | 0.0505, | 0.1005, |
| | 0.0195, | 0.0198, | 0.0199, | 0.0201, | 0.0202, | 0.0203, | 0.0205, | 0.0207, | 0.0212, |
| | 0.0191 | 0.0194 | 0.0196 | 0.0197 | 0.0198 | 0.0199 | 0.0201 | 0.0203 | 0.0209 |
| cML-MA-BIC-DP, T = 100 | 0.998, | 0.663, | 0.296, | 0.066, | 0.040, | 0.070, | 0.299, | 0.659, | 0.994, |
| | -0.0989, | -0.0488, | -0.0290, | -0.0093, | 0.0005, | 0.0103, | 0.0299, | 0.0498, | 0.0997, |
| | 0.0196, | 0.0198, | 0.0198, | 0.0197, | 0.0198, | 0.0199, | 0.0202, | 0.0206, | 0.0212, |
| | 0.0201 | 0.0203 | 0.0204 | 0.0205 | 0.0205 | 0.0207 | 0.0209 | 0.0212 | 0.0219 |
| cML-BIC-DP, T = 100 | 0.999, | 0.698, | 0.337, | 0.081, | 0.054, | 0.089, | 0.333, | 0.706, | 0.994, |
| | -0.0996, | -0.0495, | -0.0295, | -0.0095, | 0.0005, | 0.0105, | 0.0305, | 0.0505, | 0.1005, |
| | 0.0196, | 0.0199, | 0.0200, | 0.0201, | 0.0202, | 0.0203, | 0.0205, | 0.0207, | 0.0213, |
| | 0.0193 | 0.0196 | 0.0198 | 0.0199 | 0.0200 | 0.0201 | 0.0203 | 0.0205 | 0.0211 |
| cML-MA-BIC-DP, T = 200 | 0.999, | 0.672, | 0.308, | 0.068, | 0.043, | 0.075, | 0.308, | 0.659, | 0.993, |
| | -0.0991, | -0.0490, | -0.0292, | -0.0095, | 0.0003, | 0.0101, | 0.0298, | 0.0496, | 0.0995, |
| | 0.0196, | 0.0198, | 0.0197, | 0.0197, | 0.0198, | 0.0198, | 0.0202, | 0.0205, | 0.0212, |
| | 0.0197 | 0.0200 | 0.0201 | 0.0202 | 0.0203 | 0.0204 | 0.0207 | 0.0211 | 0.0218 |
| cML-BIC-DP, T = 200 | 0.999, | 0.707, | 0.351, | 0.077, | 0.056, | 0.092, | 0.344, | 0.699, | 0.995, |
| | -0.0997, | -0.0496, | -0.0296, | -0.0096, | 0.0004, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0196, | 0.0199, | 0.0200, | 0.0201, | 0.0201, | 0.0202, | 0.0204, | 0.0207, | 0.0213, |
| | 0.0190 | 0.0193 | 0.0195 | 0.0197 | 0.0198 | 0.0199 | 0.0201 | 0.0204 | 0.0210 |
| cML-MA-BIC-DP, T = 500 | 0.998, | 0.662, | 0.297, | 0.061, | 0.039, | 0.065, | 0.299, | 0.649, | 0.993, |
| | -0.0989, | -0.0489, | -0.0290, | -0.0094, | 0.0004, | 0.0102, | 0.0298, | 0.0496, | 0.0996, |
| | 0.0195, | 0.0197, | 0.0197, | 0.0196, | 0.0197, | 0.0198, | 0.0201, | 0.0205, | 0.0211, |
| | 0.0200 | 0.0203 | 0.0204 | 0.0205 | 0.0205 | 0.0207 | 0.0210 | 0.0213 | 0.0220 |
| cML-BIC-DP, T = 500 | 0.999, | 0.709, | 0.338, | 0.075, | 0.050, | 0.084, | 0.330, | 0.693, | 0.997, |
| | -0.0996, | -0.0495, | -0.0295, | -0.0095, | 0.0004, | 0.0104, | 0.0304, | 0.0504, | 0.1005, |
| | 0.0195, | 0.0198, | 0.0199, | 0.0200, | 0.0201, | 0.0202, | 0.0204, | 0.0206, | 0.0212, |
| | 0.0193 | 0.0196 | 0.0198 | 0.0199 | 0.0200 | 0.0201 | 0.0204 | 0.0206 | 0.0212 |

Table S100: Comparison of cML-MA-BIC and cML-BIC with cML-MA-BIC-DP and cML-BIC-DP: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=20, the InSIDE violated, q=0.6, N=200000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------|----------|----------|----------|----------|---------|---------|---------|---------|---------|
| cML-MA-BIC | 1.000, | 0.944. | 0.567. | 0.122, | 0.052. | 0.110. | 0.564. | 0.916. | 1.000. |
| | -0.0998. | -0.0498, | -0.0298, | -0.0098, | 0.0001, | 0.0101. | 0.0301, | 0.0501, | 0.1001, |
| | 0.0143, | 0.0145, | 0.0146, | 0.0147, | 0.0147. | 0.0148, | 0.0149, | 0.0151, | 0.0154, |
| | 0.0136 | 0.0139 | 0.0140 | 0.0141 | 0.0142 | 0.0142 | 0.0144 | 0.0145 | 0.0149 |
| cML-BIC | 1.000, | 0.946, | 0.573, | 0.125, | 0.054, | 0.115, | 0.572, | 0.919, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0098, | 0.0001, | 0.0101, | 0.0301, | 0.0502, | 0.1002, |
| | 0.0143, | 0.0145, | 0.0146, | 0.0147, | 0.0147, | 0.0148, | 0.0149, | 0.0150, | 0.0154, |
| | 0.0135 | 0.0138 | 0.0139 | 0.0140 | 0.0140 | 0.0141 | 0.0142 | 0.0144 | 0.0148 |
| cML-MA-BIC-DP, T = 100 | 1.000, | 0.932, | 0.531, | 0.116, | 0.048, | 0.099, | 0.528, | 0.899, | 1.000, |
| | -0.0995, | -0.0495, | -0.0296, | -0.0098, | 0.0000, | 0.0099, | 0.0297, | 0.0496, | 0.0996, |
| | 0.0144, | 0.0145, | 0.0146, | 0.0145, | 0.0146, | 0.0146, | 0.0149, | 0.0151, | 0.0155, |
| | 0.0140 | 0.0143 | 0.0143 | 0.0144 | 0.0144 | 0.0145 | 0.0147 | 0.0149 | 0.0153 |
| cML-BIC-DP, T = 100 | 1.000, | 0.939, | 0.563, | 0.129, | 0.053, | 0.116, | 0.567, | 0.912, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0101, | 0.0300, | 0.0501, | 0.1001, |
| | 0.0144, | 0.0146, | 0.0147, | 0.0147, | 0.0148, | 0.0148, | 0.0149, | 0.0151, | 0.0154, |
| | 0.0136 | 0.0138 | 0.0139 | 0.0141 | 0.0141 | 0.0142 | 0.0143 | 0.0145 | 0.0148 |
| cML-MA-BIC-DP, T = 200 | 1.000, | 0.936, | 0.546, | 0.111, | 0.048, | 0.100, | 0.541, | 0.900, | 1.000, |
| | -0.0996, | -0.0495, | -0.0296, | -0.0098, | 0.0000, | 0.0099, | 0.0297, | 0.0496, | 0.0996, |
| | 0.0144, | 0.0146, | 0.0146, | 0.0146, | 0.0146, | 0.0147, | 0.0149, | 0.0151, | 0.0155, |
| | 0.0138 | 0.0141 | 0.0142 | 0.0142 | 0.0143 | 0.0144 | 0.0146 | 0.0148 | 0.0153 |
| cML-BIC-DP, T = 200 | 1.000, | 0.944, | 0.578, | 0.132, | 0.055, | 0.115, | 0.573, | 0.914, | 1.000, |
| | -0.0999, | -0.0499, | -0.0299, | -0.0099, | 0.0001, | 0.0100, | 0.0300, | 0.0500, | 0.1000, |
| | 0.0144, | 0.0146, | 0.0147, | 0.0148, | 0.0148, | 0.0148, | 0.0150, | 0.0151, | 0.0155, |
| | 0.0134 | 0.0137 | 0.0138 | 0.0139 | 0.0140 | 0.0141 | 0.0142 | 0.0144 | 0.0148 |
| cML-MA-BIC-DP, T = 500 | 1.000, | 0.931, | 0.535, | 0.107, | 0.047, | 0.097, | 0.530, | 0.899, | 1.000, |
| | -0.0995, | -0.0494, | -0.0295, | -0.0097, | 0.0001, | 0.0099, | 0.0297, | 0.0496, | 0.0996, |
| | 0.0143, | 0.0145, | 0.0145, | 0.0145, | 0.0145, | 0.0146, | 0.0149, | 0.0151, | 0.0154, |
| | 0.0140 | 0.0143 | 0.0143 | 0.0144 | 0.0144 | 0.0145 | 0.0148 | 0.0150 | 0.0154 |
| cML-BIC-DP, T = 500 | 1.000, | 0.943, | 0.564, | 0.121, | 0.052, | 0.106, | 0.565, | 0.916, | 1.000, |
| | -0.0999, | -0.0499, | -0.0298, | -0.0099, | 0.0001, | 0.0101, | 0.0301, | 0.0501, | 0.1001, |
| | 0.0143, | 0.0145, | 0.0146, | 0.0147, | 0.0147, | 0.0148, | 0.0149, | 0.0150, | 0.0154, |
| | 0.0136 | 0.0138 | 0.0140 | 0.0141 | 0.0142 | 0.0142 | 0.0144 | 0.0145 | 0.0149 |

Table S101: Comparison of cML-MA-BIC and cML-BIC with cML-MA-BIC-DP and cML-BIC-DP: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.6, N=50000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|--------------------------|----------|----------|----------|----------|---------|---------|---------|---------|---------|
| cML-MA-BIC | 1.000, | 0.916, | 0.481, | 0.116, | 0.050, | 0.103, | 0.534, | 0.885, | 1.000, |
| | -0.0996, | -0.0496, | -0.0296, | -0.0096, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0150, | 0.0151, | 0.0152, | 0.0153, | 0.0153, | 0.0154, | 0.0155, | 0.0156, | 0.0160, |
| | 0.0147 | 0.0149 | 0.0149 | 0.0150 | 0.0151 | 0.0151 | 0.0152 | 0.0154 | 0.0157 |
| cML-BIC | 1.000, | 0.923, | 0.495, | 0.123, | 0.054, | 0.110, | 0.543, | 0.888, | 1.000, |
| | -0.0996, | -0.0496, | -0.0296, | -0.0096, | 0.0004, | 0.0104, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0150, | 0.0151, | 0.0152, | 0.0153, | 0.0154, | 0.0154, | 0.0155, | 0.0156, | 0.0160, |
| | 0.0146 | 0.0147 | 0.0148 | 0.0149 | 0.0149 | 0.0150 | 0.0151 | 0.0152 | 0.0155 |
| cML-MA-BIC-DP, T = 100 | 1.000, | 0.861, | 0.391, | 0.074, | 0.031, | 0.063, | 0.419, | 0.822, | 1.000, |
| | -0.0988, | -0.0489, | -0.0290, | -0.0094, | 0.0003, | 0.0100, | 0.0295, | 0.0493, | 0.0992, |
| | 0.0151, | 0.0152, | 0.0151, | 0.0150, | 0.0150, | 0.0151, | 0.0154, | 0.0157, | 0.0161, |
| | 0.0163 | 0.0165 | 0.0165 | 0.0163 | 0.0164 | 0.0165 | 0.0168 | 0.0171 | 0.0175 |
| cML-BIC-DP, T = 100 | 1.000, | 0.861, | 0.407, | 0.088, | 0.037, | 0.072, | 0.444, | 0.845, | 1.000, |
| | -0.0989, | -0.0489, | -0.0291, | -0.0094, | 0.0003, | 0.0100, | 0.0297, | 0.0495, | 0.0994, |
| | 0.0152, | 0.0152, | 0.0152, | 0.0151, | 0.0151, | 0.0152, | 0.0155, | 0.0157, | 0.0161, |
| | 0.0160 | 0.0162 | 0.0162 | 0.0161 | 0.0161 | 0.0162 | 0.0165 | 0.0168 | 0.0172 |
| cML-MA-BIC-DP, $T = 200$ | 1.000, | 0.865, | 0.400, | 0.073, | 0.034, | 0.060, | 0.429, | 0.831, | 1.000, |
| | -0.0987, | -0.0488, | -0.0290, | -0.0094, | 0.0003, | 0.0100, | 0.0295, | 0.0493, | 0.0992, |
| | 0.0150, | 0.0152, | 0.0151, | 0.0150, | 0.0150, | 0.0151, | 0.0154, | 0.0157, | 0.0161, |
| | 0.0163 | 0.0164 | 0.0164 | 0.0163 | 0.0163 | 0.0164 | 0.0167 | 0.0170 | 0.0174 |
| cML-BIC-DP, T = 200 | 1.000, | 0.872, | 0.417, | 0.088, | 0.035, | 0.078, | 0.453, | 0.843, | 1.000, |
| | -0.0988, | -0.0489, | -0.0290, | -0.0094, | 0.0004, | 0.0101, | 0.0297, | 0.0496, | 0.0994, |
| | 0.0151, | 0.0153, | 0.0152, | 0.0151, | 0.0151, | 0.0152, | 0.0155, | 0.0158, | 0.0161, |
| | 0.0159 | 0.0160 | 0.0160 | 0.0160 | 0.0160 | 0.0161 | 0.0164 | 0.0166 | 0.0170 |
| cML-MA-BIC-DP, $T = 500$ | 1.000, | 0.860, | 0.401, | 0.065, | 0.033, | 0.062, | 0.425, | 0.828, | 1.000, |
| | -0.0987, | -0.0488, | -0.0290, | -0.0094, | 0.0003, | 0.0100, | 0.0295, | 0.0493, | 0.0992, |
| | 0.0150, | 0.0152, | 0.0151, | 0.0150, | 0.0150, | 0.0150, | 0.0154, | 0.0157, | 0.0160, |
| | 0.0163 | 0.0165 | 0.0164 | 0.0163 | 0.0163 | 0.0164 | 0.0168 | 0.0171 | 0.0175 |
| cML-BIC-DP, $T = 500$ | 1.000, | 0.868, | 0.418, | 0.090, | 0.040, | 0.078, | 0.454, | 0.838, | 1.000, |
| | -0.0989, | -0.0490, | -0.0291, | -0.0094, | 0.0003, | 0.0101, | 0.0298, | 0.0496, | 0.0995, |
| | 0.0151, | 0.0152, | 0.0152, | 0.0151, | 0.0151, | 0.0152, | 0.0155, | 0.0157, | 0.0161, |
| | 0.0159 | 0.0161 | 0.0160 | 0.0160 | 0.0160 | 0.0161 | 0.0164 | 0.0166 | 0.0170 |

Table S102: Comparison of cML-MA-BIC and cML-BIC with cML-MA-BIC-DP and cML-BIC-DP: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.6, N=100000.

| θ | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------|----------|----------|----------|----------|---------|---------|---------|---------|---------|
| Methods | 0.1 | 0.05 | 0.03 | 0.01 | | 0.01 | 0.03 | 0.03 | 0.1 |
| cML-MA-BIC | 1.000, | 0.994, | 0.797, | 0.165, | 0.057, | 0.168, | 0.783, | 0.994, | 1.000, |
| | -0.0998, | -0.0497, | -0.0297, | -0.0097, | 0.0003, | 0.0103, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0108, | 0.0109, | 0.0110, | 0.0110, | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0116, |
| | 0.0104 | 0.0105 | 0.0106 | 0.0106 | 0.0107 | 0.0107 | 0.0108 | 0.0109 | 0.0111 |
| cML-BIC | 1.000, | 0.994, | 0.799, | 0.175, | 0.058, | 0.174, | 0.785, | 0.994, | 1.000, |
| | -0.0998, | -0.0498, | -0.0298, | -0.0098, | 0.0002, | 0.0102, | 0.0303, | 0.0503, | 0.1003, |
| | 0.0108, | 0.0109, | 0.0110, | 0.0110, | 0.0111, | 0.0111, | 0.0112, | 0.0113, | 0.0116, |
| | 0.0103 | 0.0104 | 0.0105 | 0.0106 | 0.0106 | 0.0106 | 0.0107 | 0.0108 | 0.0110 |
| cML-MA-BIC-DP, T = 100 | 1.000, | 0.989, | 0.732, | 0.121, | 0.034, | 0.125, | 0.720, | 0.988, | 1.000, |
| | -0.0992, | -0.0492, | -0.0293, | -0.0095, | 0.0002, | 0.0100, | 0.0298, | 0.0497, | 0.0997, |
| | 0.0109, | 0.0110, | 0.0110, | 0.0109, | 0.0109, | 0.0110, | 0.0113, | 0.0114, | 0.0116, |
| | 0.0113 | 0.0115 | 0.0115 | 0.0114 | 0.0114 | 0.0115 | 0.0117 | 0.0118 | 0.0121 |
| cML-BIC-DP, T = 100 | 1.000, | 0.988, | 0.731, | 0.130, | 0.048, | 0.136, | 0.732, | 0.988, | 1.000, |
| | -0.0993, | -0.0493, | -0.0293, | -0.0095, | 0.0003, | 0.0101, | 0.0299, | 0.0499, | 0.0998, |
| | 0.0110, | 0.0111, | 0.0111, | 0.0110, | 0.0110, | 0.0111, | 0.0113, | 0.0114, | 0.0117, |
| | 0.0111 | 0.0112 | 0.0112 | 0.0112 | 0.0112 | 0.0113 | 0.0114 | 0.0116 | 0.0118 |
| cML-MA-BIC-DP, T = 200 | 1.000, | 0.989, | 0.724, | 0.121, | 0.034, | 0.128, | 0.718, | 0.988, | 1.000, |
| | -0.0992, | -0.0492, | -0.0292, | -0.0095, | 0.0003, | 0.0100, | 0.0298, | 0.0498, | 0.0997, |
| | 0.0108, | 0.0110, | 0.0110, | 0.0109, | 0.0108, | 0.0109, | 0.0112, | 0.0113, | 0.0116, |
| | 0.0113 | 0.0114 | 0.0114 | 0.0113 | 0.0113 | 0.0114 | 0.0117 | 0.0118 | 0.0120 |
| cML-BIC-DP, $T = 200$ | 1.000, | 0.988, | 0.739, | 0.142, | 0.047, | 0.135, | 0.736, | 0.991, | 1.000, |
| | -0.0993, | -0.0494, | -0.0294, | -0.0096, | 0.0002, | 0.0101, | 0.0299, | 0.0499, | 0.0999, |
| | 0.0109, | 0.0110, | 0.0111, | 0.0110, | 0.0110, | 0.0111, | 0.0113, | 0.0114, | 0.0117, |
| | 0.0110 | 0.0111 | 0.0111 | 0.0111 | 0.0111 | 0.0112 | 0.0114 | 0.0115 | 0.0117 |
| cML-MA-BIC-DP, T = 500 | 1.000, | 0.991, | 0.732, | 0.123, | 0.037, | 0.120, | 0.726, | 0.987, | 1.000, |
| | -0.0992, | -0.0493, | -0.0293, | -0.0095, | 0.0002, | 0.0100, | 0.0298, | 0.0498, | 0.0997, |
| | 0.0108, | 0.0110, | 0.0110, | 0.0108, | 0.0108, | 0.0109, | 0.0112, | 0.0113, | 0.0116, |
| | 0.0113 | 0.0114 | 0.0114 | 0.0113 | 0.0113 | 0.0114 | 0.0117 | 0.0118 | 0.0120 |
| cML-BIC-DP, T = 500 | 1.000, | 0.991, | 0.758, | 0.140, | 0.048, | 0.136, | 0.753, | 0.989, | 1.000, |
| | -0.0994, | -0.0494, | -0.0294, | -0.0096, | 0.0003, | 0.0101, | 0.0300, | 0.0500, | 0.0999, |
| | 0.0109, | 0.0110, | 0.0110, | 0.0109, | 0.0109, | 0.0110, | 0.0112, | 0.0113, | 0.0116, |
| | 0.0109 | 0.0110 | 0.0111 | 0.0110 | 0.0111 | 0.0111 | 0.0113 | 0.0114 | 0.0116 |
| | | | | | | | | | |

Table S103: Comparison of cML-MA-BIC and cML-BIC with cML-MA-BIC-DP and cML-BIC-DP: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when m=100, the InSIDE violated, q=0.6, N=200000.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------|----------|----------|----------|----------|----------|---------|---------|---------|---------|
| cML-MA-BIC | 1.000, | 1.000, | 0.982, | 0.292, | 0.043, | 0.234, | 0.978, | 1.000, | 1.000, |
| | -0.1004, | -0.0504, | -0.0304, | -0.0104, | -0.0005, | 0.0095, | 0.0295, | 0.0495, | 0.0995, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077, |
| | 0.0073 | 0.0074 | 0.0075 | 0.0075 | 0.0075 | 0.0076 | 0.0076 | 0.0077 | 0.0078 |
| cML-BIC | 1.000, | 1.000, | 0.981, | 0.301, | 0.046, | 0.239, | 0.977, | 1.000, | 1.000, |
| | -0.1004, | -0.0504, | -0.0304, | -0.0105, | -0.0005, | 0.0095, | 0.0295, | 0.0495, | 0.0995, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0074, | 0.0074, | 0.0074, | 0.0075, | 0.0075, | 0.0077, |
| | 0.0073 | 0.0074 | 0.0074 | 0.0074 | 0.0075 | 0.0075 | 0.0076 | 0.0076 | 0.0078 |
| cML-MA-BIC-DP, T = 100 | 1.000, | 1.000, | 0.969, | 0.234, | 0.027, | 0.192, | 0.960, | 1.000, | 1.000, |
| | -0.1001, | -0.0502, | -0.0302, | -0.0103, | -0.0005, | 0.0093, | 0.0292, | 0.0492, | 0.0991, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0073, | 0.0073, | 0.0073, | 0.0075, | 0.0076, | 0.0077, |
| | 0.0078 | 0.0079 | 0.0080 | 0.0079 | 0.0079 | 0.0080 | 0.0081 | 0.0082 | 0.0084 |
| cML-BIC-DP, T = 100 | 1.000, | 1.000, | 0.973, | 0.267, | 0.038, | 0.220, | 0.963, | 1.000, | 1.000, |
| | -0.1002, | -0.0502, | -0.0302, | -0.0103, | -0.0004, | 0.0094, | 0.0293, | 0.0493, | 0.0992, |
| | 0.0073, | 0.0073, | 0.0074, | 0.0073, | 0.0073, | 0.0074, | 0.0075, | 0.0076, | 0.0077, |
| | 0.0076 | 0.0077 | 0.0077 | 0.0077 | 0.0077 | 0.0078 | 0.0079 | 0.0080 | 0.0082 |
| cML-MA-BIC-DP, T = 200 | 1.000, | 1.000, | 0.970, | 0.230, | 0.026, | 0.195, | 0.958, | 1.000, | 1.000, |
| | -0.1001, | -0.0501, | -0.0302, | -0.0103, | -0.0005, | 0.0093, | 0.0292, | 0.0492, | 0.0991, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0073, | 0.0073, | 0.0073, | 0.0075, | 0.0076, | 0.0077, |
| | 0.0078 | 0.0079 | 0.0079 | 0.0079 | 0.0079 | 0.0079 | 0.0081 | 0.0082 | 0.0083 |
| cML-BIC-DP, T = 200 | 1.000, | 1.000, | 0.970, | 0.263, | 0.040, | 0.225, | 0.964, | 1.000, | 1.000, |
| | -0.1002, | -0.0502, | -0.0303, | -0.0103, | -0.0005, | 0.0094, | 0.0293, | 0.0493, | 0.0992, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0073, | 0.0073, | 0.0074, | 0.0075, | 0.0076, | 0.0078, |
| | 0.0076 | 0.0077 | 0.0077 | 0.0077 | 0.0077 | 0.0077 | 0.0079 | 0.0079 | 0.0081 |
| cML-MA-BIC-DP, T = 500 | 1.000, | 1.000, | 0.971, | 0.227, | 0.028, | 0.191, | 0.961, | 1.000, | 1.000, |
| | -0.1001, | -0.0501, | -0.0302, | -0.0103, | -0.0005, | 0.0093, | 0.0292, | 0.0492, | 0.0991, |
| | 0.0072, | 0.0073, | 0.0073, | 0.0073, | 0.0073, | 0.0073, | 0.0075, | 0.0075, | 0.0077, |
| | 0.0078 | 0.0079 | 0.0080 | 0.0079 | 0.0079 | 0.0080 | 0.0081 | 0.0082 | 0.0084 |
| cML-BIC-DP, T = 500 | 1.000, | 1.000, | 0.971, | 0.265, | 0.038, | 0.214, | 0.968, | 1.000, | 1.000, |
| | -0.1003, | -0.0503, | -0.0303, | -0.0104, | -0.0005, | 0.0094, | 0.0293, | 0.0493, | 0.0993, |
| | 0.0073, | 0.0073, | 0.0074, | 0.0073, | 0.0073, | 0.0074, | 0.0075, | 0.0076, | 0.0078, |
| | 0.0076 | 0.0077 | 0.0077 | 0.0077 | 0.0077 | 0.0077 | 0.0079 | 0.0079 | 0.0081 |

Table S104: Relative frequencies of goodness-of-fit tests' rejecting the null at the p-value cutoff 0.05 when m = 10, the InSIDE violated, q = 0.6.

| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| GOF1, N = 50k, T = 100 | 0.009 | 0.007 | 0.006 | 0.004 | 0.004 | 0.004 | 0.005 | 0.001 | 0.003 |
| GOF2, N = 50k, T = 100 | 0.012 | 0.009 | 0.008 | 0.005 | 0.006 | 0.005 | 0.006 | 0.001 | 0.004 |
| GOF1, N = 50k, T = 200 | 0.002 | 0.002 | 0.002 | 0.003 | 0.003 | 0.003 | 0.003 | 0.001 | 0.003 |
| GOF2, N = 50k, T = 200 | 0.002 | 0.002 | 0.003 | 0.003 | 0.003 | 0.004 | 0.003 | 0.001 | 0.004 |
| GOF1, N = 50k, T = 500 | 0.002 | 0.003 | 0.003 | 0.003 | 0.004 | 0.004 | 0.003 | 0.001 | 0.005 |
| GOF2, N = 50k, T = 500 | 0.002 | 0.003 | 0.003 | 0.003 | 0.004 | 0.004 | 0.003 | 0.001 | 0.005 |
| GOF1, N = 100k, T = 100 | 0.014 | 0.007 | 0.006 | 0.004 | 0.004 | 0.003 | 0.001 | 0.000 | 0.000 |
| GOF2, N = 100k, T = 100 | 0.019 | 0.012 | 0.010 | 0.008 | 0.006 | 0.004 | 0.002 | 0.002 | 0.000 |
| GOF1, N = 100k, T = 200 | 0.002 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 |
| GOF2, N = 100k, T = 200 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.000 | 0.000 |
| GOF1, N = 100k, T = 500 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.000 | 0.001 |
| GOF2, N = 100k, T = 500 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.000 | 0.001 |
| GOF1, N = 200k, T = 100 | 0.029 | 0.022 | 0.019 | 0.015 | 0.014 | 0.012 | 0.010 | 0.009 | 0.003 |
| GOF2, N = 200k, T = 100 | 0.032 | 0.024 | 0.020 | 0.016 | 0.015 | 0.014 | 0.012 | 0.009 | 0.006 |
| GOF1, N = 200k, T = 200 | 0.015 | 0.004 | 0.003 | 0.002 | 0.002 | 0.001 | 0.001 | 0.001 | 0.001 |
| GOF2, N = 200k, T = 200 | 0.013 | 0.004 | 0.002 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 |
| GOF1, N = 200k, T = 500 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 |
| GOF2, $N = 200k$, $T = 500$ | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 |

Table S105: Relative frequencies of goodness-of-fit tests' rejecting the null at p-value cutoff 0.05 when m = 20, the InSIDE violated, q = 0.6.

| θ Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
|------------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| GOF1, N = 50k, T = 100 | 0.047 | 0.056 | 0.055 | 0.052 | 0.051 | 0.051 | 0.056 | 0.055 | 0.057 |
| GOF2, N = 50k, T = 100 | 0.035 | 0.039 | 0.039 | 0.041 | 0.039 | 0.039 | 0.039 | 0.042 | 0.054 |
| GOF1, N = 50k, T = 200 | 0.046 | 0.053 | 0.053 | 0.052 | 0.052 | 0.053 | 0.050 | 0.049 | 0.051 |
| GOF2, N = 50k, T = 200 | 0.045 | 0.051 | 0.052 | 0.050 | 0.047 | 0.049 | 0.045 | 0.045 | 0.053 |
| GOF1, $N = 50k$, $T = 500$ | 0.050 | 0.053 | 0.052 | 0.053 | 0.050 | 0.049 | 0.048 | 0.046 | 0.048 |
| GOF2, N = 50k, T = 500 | 0.048 | 0.049 | 0.050 | 0.048 | 0.047 | 0.046 | 0.043 | 0.042 | 0.051 |
| GOF1, N = 100k, T = 100 | 0.062 | 0.068 | 0.076 | 0.078 | 0.082 | 0.084 | 0.085 | 0.087 | 0.092 |
| GOF2, $N = 100k$, $T = 100$ | 0.045 | 0.052 | 0.059 | 0.062 | 0.064 | 0.067 | 0.069 | 0.075 | 0.079 |
| GOF1, N = 100k, T = 200 | 0.068 | 0.064 | 0.064 | 0.064 | 0.065 | 0.064 | 0.064 | 0.065 | 0.064 |
| GOF2, N = 100k, T = 200 | 0.065 | 0.063 | 0.065 | 0.063 | 0.063 | 0.063 | 0.062 | 0.062 | 0.067 |
| GOF1, N = 100k, T = 500 | 0.043 | 0.040 | 0.037 | 0.031 | 0.030 | 0.030 | 0.031 | 0.028 | 0.025 |
| GOF2, N = 100k, T = 500 | 0.036 | 0.033 | 0.032 | 0.030 | 0.028 | 0.028 | 0.028 | 0.025 | 0.025 |
| GOF1, N = 200k, T = 100 | 0.066 | 0.071 | 0.075 | 0.079 | 0.080 | 0.083 | 0.086 | 0.088 | 0.101 |
| GOF2, N = 200k, T = 100 | 0.052 | 0.061 | 0.064 | 0.064 | 0.065 | 0.066 | 0.070 | 0.074 | 0.087 |
| GOF1, N = 200k, T = 200 | 0.072 | 0.074 | 0.072 | 0.073 | 0.072 | 0.072 | 0.071 | 0.072 | 0.074 |
| GOF2, N = 200k, T = 200 | 0.067 | 0.068 | 0.065 | 0.066 | 0.065 | 0.066 | 0.066 | 0.065 | 0.066 |
| GOF1, N = 200k, T = 500 | 0.049 | 0.047 | 0.048 | 0.048 | 0.049 | 0.050 | 0.050 | 0.047 | 0.045 |
| GOF2, N = 200k, T = 500 | 0.042 | 0.043 | 0.044 | 0.044 | 0.043 | 0.043 | 0.042 | 0.042 | 0.044 |

Table S106: Relative frequencies of goodness-of-fit tests' rejecting the null at p-value cutoff 0.05 when m = 100, the InSIDE violated, q = 0.6.

| • | | | | | | | | | |
|-------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| Methods | -0.1 | -0.05 | -0.03 | -0.01 | 0 | 0.01 | 0.03 | 0.05 | 0.1 |
| GOF1, N = 50k, T = 100 | 0.083 | 0.085 | 0.080 | 0.079 | 0.077 | 0.075 | 0.078 | 0.082 | 0.084 |
| GOF2, N = 50k, T = 100 | 0.063 | 0.068 | 0.063 | 0.059 | 0.060 | 0.062 | 0.059 | 0.065 | 0.075 |
| GOF1, N = 50k, T = 200 | 0.057 | 0.057 | 0.057 | 0.054 | 0.051 | 0.051 | 0.057 | 0.059 | 0.074 |
| GOF2, N = 50k, T = 200 | 0.048 | 0.050 | 0.050 | 0.048 | 0.046 | 0.045 | 0.052 | 0.058 | 0.077 |
| GOF1, N = 50k, T = 500 | 0.057 | 0.057 | 0.056 | 0.054 | 0.051 | 0.048 | 0.059 | 0.081 | 0.105 |
| GOF2, N = 50k, T = 500 | 0.057 | 0.057 | 0.058 | 0.056 | 0.053 | 0.050 | 0.065 | 0.079 | 0.110 |
| GOF1, N = 100k, T = 100 | 0.082 | 0.074 | 0.075 | 0.073 | 0.071 | 0.074 | 0.067 | 0.068 | 0.066 |
| GOF2, N = 100k, T = 100 | 0.065 | 0.060 | 0.061 | 0.058 | 0.056 | 0.056 | 0.055 | 0.054 | 0.053 |
| GOF1, N = 100k, T = 200 | 0.059 | 0.065 | 0.062 | 0.058 | 0.057 | 0.056 | 0.059 | 0.060 | 0.059 |
| GOF2, N = 100k, T = 200 | 0.054 | 0.051 | 0.051 | 0.053 | 0.049 | 0.048 | 0.050 | 0.050 | 0.050 |
| GOF1, N = 100k, T = 500 | 0.061 | 0.062 | 0.061 | 0.063 | 0.059 | 0.058 | 0.059 | 0.061 | 0.060 |
| GOF2, N = 100k, T = 500 | 0.059 | 0.059 | 0.060 | 0.058 | 0.056 | 0.055 | 0.057 | 0.059 | 0.060 |
| GOF1, N = 200k, T = 100 | 0.082 | 0.081 | 0.083 | 0.081 | 0.074 | 0.076 | 0.077 | 0.073 | 0.075 |
| GOF2, N = 200k, T = 100 | 0.072 | 0.073 | 0.071 | 0.067 | 0.063 | 0.063 | 0.066 | 0.069 | 0.066 |
| GOF1, N = 200k, T = 200 | 0.082 | 0.084 | 0.084 | 0.086 | 0.084 | 0.084 | 0.087 | 0.086 | 0.094 |
| GOF2, N = 200k, T = 200 | 0.080 | 0.080 | 0.080 | 0.081 | 0.077 | 0.078 | 0.079 | 0.080 | 0.081 |
| GOF1, N = 200k, T = 500 | 0.066 | 0.064 | 0.066 | 0.066 | 0.063 | 0.063 | 0.064 | 0.064 | 0.067 |
| GOF2, N = 200k, T = 500 | 0.062 | 0.063 | 0.063 | 0.064 | 0.065 | 0.065 | 0.066 | 0.067 | 0.066 |
| | | | | | | | | | |

Table S107: Simulations with weak invalid IVs: in each cell, from top to bottom are empirical type-I error/power, $mean(\hat{\theta})$, $SD(\hat{\theta})$, $mean(SE(\hat{\theta}))$ when $h_y = 0.1$ and $h_u = 0$.

| | · · | | 1 | | | 1 | |
|----------------------------|---------------------|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|
| Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
| cML-MA-BIC | 0.997, | 0.974, | 0.766, | 0.228, | 0.777, | 0.978, | 0.999, |
| CME MIT DIC | -0.1943, | -0.0955, | -0.0468, | -0.0002, | 0.0470, | 0.0963, | 0.1953, |
| | 0.0330, | 0.0296, | 0.0273, | 0.0245, | 0.0263, | 0.0283, | 0.0311, |
| | 0.0145 | 0.0143 | 0.0142 | 0.0142 | 0.0143 | 0.0143 | 0.0145 |
| cML-BIC | 0.998, | 0.982, | 0.811, | 0.299, | 0.814, | 0.984, | 1.000, |
| | -0.1956, | -0.0966, | -0.0474, | -0.0001, | 0.0482, | 0.0975, | 0.1966, |
| | 0.0333, | 0.0302, | 0.0284, | 0.0263, | 0.0273, | 0.0290, | 0.0317, |
| cML-MA-BIC-DP, T = 100 | 0.0131 0.952, | 0.0130 0.830, | 0.0129 0.454, | 0.0129 0.047, | 0.0129 0.447, | 0.0130 0.846, | 0.0131 |
| CML-MA-BIC-DP, I = 100 | -0.1804, | -0.0872, | -0.0421, | 0.047, | 0.447, 0.0424, | 0.846, | 0.938, |
| | 0.0359, | 0.0275, | 0.0232, | 0.0204, | 0.0231, | 0.0271, | 0.0342, |
| | 0.0311 | 0.0266 | 0.0233 | 0.0208 | 0.0232 | 0.0264 | 0.0313 |
| cML-BIC-DP, T = 100 | 0.953, | 0.833, | 0.477, | 0.050, | 0.455, | 0.851, | 0.960, |
| | -0.1809, | -0.0876, | -0.0423, | 0.0000, | 0.0427, | 0.0885, | 0.1824, |
| | 0.0362, | 0.0277, | 0.0234, | 0.0208, | 0.0233, | 0.0272, | 0.0339, |
| cML-MA-BIC-DP, T = 200 | 0.0303 0.951, | 0.0263 0.833, | 0.0230 0.462, | 0.0206 0.046, | 0.0230 | 0.0259 0.845, | 0.0305 0.956, |
| CML-MA-BIC-DF, 1 = 200 | -0.1800, | -0.0870, | -0.0421, | -0.0001, | 0.440, | 0.043, | 0.930, |
| | 0.0361, | 0.0276, | 0.0232, | 0.0204, | 0.0231, | 0.0271, | 0.0345, |
| | 0.0314 | 0.0267 | 0.0234 | 0.0209 | 0.0233 | 0.0265 | 0.0316 |
| cML-BIC-DP, T = 200 | 0.953, | 0.835, | 0.466, | 0.052, | 0.450, | 0.850, | 0.960, |
| | -0.1807, | -0.0874, | -0.0423, | 0.0000, | 0.0426, | 0.0882, | 0.1820, |
| | 0.0360, | 0.0277, | 0.0235, | 0.0208, | 0.0233, | 0.0273, | 0.0343, |
| cML-MA-BIC-DP, T = 500 | 0.0307 0.948, | 0.0263 0.829, | 0.0231 | 0.0207 0.042, | 0.0230 0.442, | 0.0262 0.844, | 0.0309 |
| CIVIL-IVIA-DIC-DF, I = 300 | -0.1797, | -0.0869, | 0.454, -0.0420, | -0.0001, | 0.442, 0.0422, | 0.844, 0.0875, | 0.953, |
| | 0.0363, | 0.0275, | 0.0231, | 0.0203, | 0.0422, | 0.0373, | 0.1807, |
| | 0.0317 | 0.0269 | 0.0235 | 0.0209 | 0.0234 | 0.0267 | 0.0319 |
| cML-BIC-DP, T = 500 | 0.951, | 0.836, | 0.467, | 0.048, | 0.456, | 0.849, | 0.958, |
| | -0.1804, | -0.0873, | -0.0422, | -0.0001, | 0.0424, | 0.0879, | 0.1814, |
| | 0.0361, | 0.0276, | 0.0233, | 0.0205, | 0.0231, | 0.0271, | 0.0344, |
| MD MC- | 0.0311 | 0.0264 | 0.0232 | 0.0207 | 0.0231 | 0.0263 | 0.0313 |
| MR-Mix | 0.984, -0.2001, | 0.904, -0.0995, | 0.574, -0.0495, | 0.121, 0.0008, | 0.565, 0.0510, | 0.904, 0.1011, | 0.985, 0.2009, |
| | 0.0337, | 0.0346, | 0.0346, | 0.0008, | 0.0310, | 0.1011, | 0.2009, |
| | 0.0270 | 0.0262 | 0.0290 | 0.0266 | 0.0281 | 0.0271 | 0.0289 |
| MR-ContMix | 0.999, | 0.985, | 0.829, | 0.313, | 0.831, | 0.989, | 1.000, |
| | -0.1990, | -0.0993, | -0.0492, | 0.0006, | 0.0506, | 0.1004, | 0.1995, |
| | 0.0298, | 0.0297, | 0.0293, | 0.0293, | 0.0291, | 0.0295, | 0.0289, |
| 160.1 | NA 1 000 | NA 0.000 | NA | NA 0.215 | NA 0.700 | NA | NA 1,000 |
| MR-Lasso | 1.000, -0.1987, | 0.989, -0.0992, | 0.806, -0.0497, | 0.215, 0.0000, | 0.799, 0.0496, | 0.986, 0.0993, | 1.000, 0.1990, |
| | 0.0261, | 0.0254, | 0.0254, | 0.0000, | 0.0496, | 0.0993, | 0.1990, |
| | 0.0153 | 0.0153 | 0.0153 | 0.0153 | 0.0153 | 0.0153 | 0.0154 |
| MR-PRESSO | 1.000, | 0.967, | 0.702, | 0.201, | 0.688, | 0.968, | 1.000, |
| | -0.1994, | -0.0998, | -0.0498, | 0.0000, | 0.0497, | 0.0995, | 0.1990, |
| | 0.0312, | 0.0309, | 0.0306, | 0.0305, | 0.0305, | 0.0306, | 0.0306, |
| | 0.0182 | 0.0179 | 0.0178 | 0.0178 | 0.0179 | 0.0179 | 0.0182 |
| MR-IVW | 0.963, | 0.533, | 0.179, | 0.054, | 0.171, | 0.509, | 0.962, |
| | -0.1998, 0.0499, | -0.1003, 0.0498, | -0.0506, 0.0498, | -0.0008, 0.0498, | 0.0489, 0.0499, | 0.0986, 0.0499, | 0.1981, 0.0499, |
| | 0.0502 | 0.0502 | 0.0501 | 0.0501 | 0.0502 | 0.0502 | 0.0502 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.804, | 0.041, | 0.815, | 0.999, | 1.000, |
| | -0.1983, | -0.0988, | -0.0491, | 0.0006, | 0.0504, | 0.1001, | 0.1995, |
| | 0.0173, | 0.0171, | 0.0170, | 0.0170, | 0.0170, | 0.0170, | 0.0173, |
| 100.5 | 0.0176 | 0.0175 | 0.0174 | 0.0174 | 0.0174 | 0.0175 | 0.0176 |
| MR-Egger | 0.658, | 0.234, | 0.100, | 0.053, | 0.099, | 0.237, | 0.632, |
| | -0.2008, 0.0841, | -0.1014, 0.0841, | -0.0517, 0.0842, | -0.0020, 0.0842, | 0.0477, 0.0842, | 0.0974, 0.0843, | 0.1969, 0.0844, |
| | 0.0844 | 0.0844 | 0.0844 | 0.0844 | 0.0844 | 0.0844 | 0.0845 |
| MR-Weighted-Median | 0.999, | 0.959, | 0.685, | 0.140, | 0.643, | 0.955, | 0.998, |
| - | -0.1928, | -0.0972, | -0.0494, | -0.0012, | 0.0468, | 0.0948, | 0.1910, |
| | 0.0309, | 0.0297, | 0.0294, | 0.0293, | 0.0294, | 0.0297, | 0.0310, |
| MD Webb 134 | 0.0204 | 0.0201 | 0.0200 | 0.0200 | 0.0201 | 0.0201 | 0.0204 |
| MR-Weighted-Mode | 0.718, -0.1953, | 0.551, -0.1038, | 0.323, -0.0491, | 0.096, | 0.325, 0.0438, | 0.561, | 0.720, 0.1857, |
| | 0.1955, | 0.1629, | 0.1451, | 0.1448, | 0.0438, 0.1440, | 0.0911, 0.1528, | 0.1857, |
| | 1.0123 | 1.0020 | 1.0032 | 0.9972 | 0.9936 | 0.9987 | 0.9929 |
| MR-RAPS1 | 0.965, | 0.539, | 0.186, | 0.057, | 0.177, | 0.517, | 0.964, |
| | -0.2008, | -0.1008, | -0.0508, | -0.0009, | 0.0491, | 0.0991, | 0.1991, |
| | 0.0501, | 0.0501, | 0.0501, | 0.0501, | 0.0501, | 0.0501, | 0.0502, |
| MD DADGO | 0.0499 | 0.0499 | 0.0499 | 0.0499 | 0.0499 | 0.0499 | 0.0500 |
| MR-RAPS2 | 0.985, | 0.681, -0.1007, | 0.299, -0.0506, | 0.087, | 0.289, 0.0494, | 0.655, 0.0994, | 0.985, 0.1996, |
| | -0.2011, 0.0428, | 0.1007, | 0.0506, | 0.0006, | 0.0494, 0.0429, | 0.0994, 0.0429, | 0.1996, 0.0432, |
| | 0.0428, | 0.0430, | 0.0430, | 0.0431, | 0.0429, | 0.0429, | 0.0432, |
| MR-RAPS3 | 1.000, | 0.951, | 0.821, | 0.687, | 0.806, | 0.948, | 1.000, |
| | -0.2275, | -0.1148, | -0.0580, | -0.0010, | 0.0560, | 0.1128, | 0.2256, |
| | 0.0578, | 0.0579, | 0.0579, | 0.0578, | 0.0578, | 0.0577, | 0.0575, |
| | 0.0118 | 0.0117 | 0.0117 | 0.0117 | 0.0117 | 0.0117 | 0.0118 |
| MR-RAPS4 | 0.999, | 0.992, | 0.898, | 0.393, | 0.900, | 0.999, | 1.000, |
| | -0.2027, 0.0494, | -0.1008, 0.0371, | -0.0509, 0.0315, | 0.0006, 0.0347, | 0.0516, 0.0295, | 0.1001, 0.0440, | 0.2038, 0.0546, |
| | 0.0494, | 0.0371, | 0.0313, | 0.0347, | 0.0293, | 0.0440, | 0.0346, |
| | 1 2.2.407 | 1 2.32.00 | 1 2.3.00 | 1 222.07 | 1 2.3103 | 1 2.3103 | |

Table S108: Simulations with weak invalid IVs: in each cell, from top to bottom are empirical type-I error/power, $mean(\hat{\theta})$, $SD(\hat{\theta})$, $mean(SE(\hat{\theta}))$ when $h_y = 0.2$ and $h_u = 0$.

| Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
|--------------------------|--------------------|--------------------|---------------------|-------------------|-------------------|-------------------|-------------------|
| cML-MA-BIC | 0.996, | 0.980, | 0.784, | 0.196, | 0.784, | 0.978, | 0.997, |
| CIAL MIT DIE | -0.1952, | -0.0966, | -0.0477, | 0.0000, | 0.0480, | 0.0975, | 0.1963, |
| | 0.0320, | 0.0281, | 0.0260, | 0.0243, | 0.0257, | 0.0273, | 0.0301, |
| | 0.0151 | 0.0149 | 0.0149 | 0.0148 | 0.0149 | 0.0150 | 0.0151 |
| cML-BIC | 0.999, | 0.986, | 0.816, | 0.269, | 0.823, | 0.983, | 0.997, |
| | -0.1963, | -0.0974, | -0.0482, | -0.0001, | 0.0488, | 0.0984, | 0.1973, |
| | 0.0325, | 0.0290, | 0.0269, | 0.0259, | 0.0267, | 0.0281, | 0.0309, |
| cML-MA-BIC-DP, T = 100 | 0.0139 | 0.0137 | 0.0137 0.485, | 0.0136 0.042, | 0.0137 0.484, | 0.0137 0.849, | 0.0139 0.941, |
| CML-MA-BIC-DP, $I = 100$ | -0.1810, | -0.0882, | -0.0430, | 0.042, | 0.484, | 0.849, | 0.941, |
| | 0.0355, | 0.0270, | 0.0228, | 0.0203, | 0.0432, | 0.0260, | 0.0349, |
| | 0.0315 | 0.0263 | 0.0230 | 0.0206 | 0.0229 | 0.0261 | 0.0320 |
| cML-BIC-DP, T = 100 | 0.947, | 0.851, | 0.497, | 0.050, | 0.494, | 0.859, | 0.947, |
| | -0.1818, | -0.0886, | -0.0432, | 0.0000, | 0.0435, | 0.0895, | 0.1825, |
| | 0.0355, | 0.0272, | 0.0231, | 0.0208, | 0.0228, | 0.0261, | 0.0349, |
| | 0.0308 | 0.0259 | 0.0227 | 0.0203 | 0.0225 | 0.0256 | 0.0310 |
| cML-MA-BIC-DP, T = 200 | 0.943, | 0.829, | 0.472, | 0.045, | 0.471, | 0.846, | 0.940, |
| | -0.1805, | -0.0879, | -0.0428, | 0.0000, | 0.0431, | 0.0889, | 0.1811, |
| | 0.0359, | 0.0271, 0.0266 | 0.0227, | 0.0203, | 0.0225, | 0.0260, | 0.0351, |
| cML-BIC-DP, T = 200 | 0.0320 | 0.0200 | 0.0231 | 0.0207 0.054, | 0.0231 | 0.0263 0.850, | 0.0325 |
| CML-BIC-DP, 1 = 200 | -0.1813, | -0.0884, | -0.0431, | 0.0000, | 0.490, | 0.830, | 0.1820, |
| | 0.0358, | 0.0270, | 0.0229, | 0.0000, | 0.0435, | 0.0394, | 0.1820, |
| | 0.0312 | 0.0262 | 0.0228 | 0.0205 | 0.0228 | 0.0259 | 0.0316 |
| cML-MA-BIC-DP, T = 500 | 0.940, | 0.827, | 0.471, | 0.039, | 0.474, | 0.848, | 0.940, |
| | -0.1803, | -0.0878, | -0.0428, | 0.0000, | 0.0430, | 0.0888, | 0.1810, |
| | 0.0360, | 0.0270, | 0.0227, | 0.0202, | 0.0224, | 0.0259, | 0.0351, |
| | 0.0322 | 0.0266 | 0.0231 | 0.0207 | 0.0231 | 0.0264 | 0.0326 |
| cML-BIC-DP, T = 500 | 0.947, | 0.839, | 0.490, | 0.046, | 0.484, | 0.850, | 0.943, |
| | -0.1810, | -0.0882, | -0.0431, | 0.0000, | 0.0432, | 0.0892, | 0.1817, |
| | 0.0359, | 0.0271, 0.0262 | 0.0229, | 0.0204, | 0.0226, | 0.0259, | 0.0348, |
| MR-Mix | 0.0315 | 0.0262 | 0.0228 | 0.0205 | 0.0228 | 0.0260 | 0.0319 |
| WIK-WIX | -0.1997, | -0.0997, | 0.598, -0.0496, | 0.111, 0.0004, | 0.594, 0.0503, | 0.907, 0.1003, | 0.983, 0.2005, |
| | 0.0314, | 0.0301, | 0.0299, | 0.0004, | 0.0303, | 0.0300, | 0.0297, |
| | 0.0250 | 0.0258 | 0.0261 | 0.0258 | 0.1315 | 0.0272 | 0.0266 |
| MR-ContMix | 1.000, | 0.991, | 0.840. | 0.279, | 0.834, | 0.990, | 1.000. |
| | -0.1990, | -0.0993, | -0.0495, | 0.0003, | 0.0498, | 0.0997, | 0.1993, |
| | 0.0284, | 0.0276, | 0.0276, | 0.0274, | 0.0274, | 0.0273, | 0.0275, |
| | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 1.000, | 0.986, | 0.803, | 0.198, | 0.796, | 0.979, | 1.000, |
| | -0.1986, | -0.0992, | -0.0498, | -0.0001, | 0.0499, | 0.0995, | 0.1991, |
| | 0.0268, | 0.0265, | 0.0262, | 0.0265, | 0.0261, | 0.0264, | 0.0273, |
| MR-PRESSO | 0.0161 | 0.0161 | 0.0160 | 0.0160 | 0.0160 | 0.0161 | 0.0162 |
| WR-PRESSO | -0.1986, | -0.0992, | -0.0499, | -0.0003, | 0.071, | 0.933, | 0.998, |
| | 0.0391, | 0.0388, | 0.0388, | 0.0389, | 0.0387, | 0.0387, | 0.0390, |
| | 0.0192 | 0.0189 | 0.0189 | 0.0189 | 0.0189 | 0.0190 | 0.0193 |
| MR-IVW | 0.814, | 0.301, | 0.113, | 0.048, | 0.118, | 0.312, | 0.798, |
| | -0.2000, | -0.1006, | -0.0508, | -0.0011, | 0.0486, | 0.0984, | 0.1979, |
| | 0.0695, | 0.0695, | 0.0695, | 0.0695, | 0.0695, | 0.0695, | 0.0695, |
| | 0.0702 | 0.0702 | 0.0702 | 0.0702 | 0.0702 | 0.0702 | 0.0702 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.804, | 0.041, | 0.815, | 0.999, | 1.000, |
| | -0.1983, | -0.0988, | -0.0491, | 0.0006, | 0.0504, | 0.1001, | 0.1995, |
| | 0.0173, 0.0176 | 0.0171, 0.0175 | 0.0170, 0.0174 | 0.0170, 0.0174 | 0.0170, 0.0174 | 0.0170, 0.0175 | 0.0173, 0.0176 |
| MR-Egger | 0.420, | 0.0173 | 0.068, | 0.0174 | 0.0174 | 0.0173 | 0.396, |
| 125501 | -0.2013, | -0.1018, | -0.0521, | -0.0024, | 0.0473, | 0.0970, | 0.1964, |
| | 0.1176, | 0.1176, | 0.1177, | 0.1177, | 0.1177, | 0.1178, | 0.1179, |
| | 0.1181 | 0.1181 | 0.1181 | 0.1181 | 0.1181 | 0.1181 | 0.1182 |
| MR-Weighted-Median | 0.997, | 0.942, | 0.655, | 0.135, | 0.625, | 0.946, | 0.993, |
| | -0.1906, | -0.0963, | -0.0489, | -0.0013, | 0.0463, | 0.0939, | 0.1892, |
| | 0.0342, | 0.0325, | 0.0325, | 0.0327, | 0.0331, | 0.0336, | 0.0344, |
| MD Waight 1M-1 | 0.0213 | 0.0210 | 0.0209 | 0.0209 | 0.0209 | 0.0210 | 0.0213 |
| MR-Weighted-Mode | 0.672, -0.1951, | 0.503, -0.1026, | 0.278, -0.0545, | 0.109, -0.0033, | 0.285, 0.0438, | 0.511, 0.0892, | 0.676, 0.1770, |
| | 0.1951, | 0.1026, | -0.0545, 0.1760, | 0.1779, | 0.0438, 0.1903, | 0.0892, 0.2169, | 0.1770, 0.1952, |
| | 1.3382 | 1.3283 | 1.3229 | 1.3167 | 1.3139 | 1.3198 | 1.3048 |
| MR-RAPS1 | 0.820, | 0.313, | 0.117, | 0.052, | 0.121, | 0.314, | 0.805, |
| | -0.2011, | -0.1011, | -0.0511, | -0.0011, | 0.0489, | 0.0989, | 0.1989, |
| | 0.0699, | 0.0699, | 0.0699, | 0.0699, | 0.0699, | 0.0699, | 0.0699, |
| | 0.0698 | 0.0698 | 0.0698 | 0.0698 | 0.0698 | 0.0698 | 0.0699 |
| MR-RAPS2 | 0.902, | 0.469, | 0.248, | 0.095, | 0.237, | 0.459, | 0.886, |
| | -0.2015, | -0.1014, | -0.0512, | -0.0013, | 0.0466, | 0.0988, | 0.1995, |
| | 0.0580, | 0.0582, | 0.0582, | 0.0582, | 0.0898, | 0.0584, | 0.0585, |
| MD D A DG2 | 0.0552 | 0.0550 | 0.0550 | 0.0552 | 0.0551 | 0.0550 | 0.0555 |
| MR-RAPS3 | 0.994, -0.2629, | 0.925, | 0.838, -0.0680, | 0.778, -0.0017, | 0.808, 0.0647, | 0.920, 0.1307, | 1.000, 0.2600, |
| | 0.0957. | 0.0964. | 0.0965, | 0.0963, | 0.0647, 0.0959, | 0.1307, 0.0954. | 0.2600, |
| | 0.0937, | 0.0904, | 0.0963, | 0.0963, | 0.0939, | 0.0934, | 0.0943, |
| MR-RAPS4 | 1.000, | 0.998, | 0.907, | 0.379, | 0.903, | 0.999, | 1.000, |
| | -0.2039, | -0.1016, | -0.0517, | -0.0004, | 0.0508, | 0.1016, | 0.2049, |
| | 0.0807, | 0.0322, | 0.0464, | 0.0454, | 0.0392, | 0.0437, | 0.0944, |
| | 0.0107 | 0.0105 | 0.0105 | 0.0104 | 0.0105 | 0.0105 | 0.0108 |
| | | | | | | | |

Table S109: Simulations with weak invalid IVs: in each cell, from top to bottom are empirical type-I error/power, $mean(\hat{\theta})$, $SD(\hat{\theta})$, $mean(SE(\hat{\theta}))$ when $h_y = 0.4$ and $h_u = 0$.

| Methods | | | | | | | | |
|--|--------------------------|----------|----------|----------|----------|---------|---------|---------|
| MIL-MA-BIC 1996, | Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
| 0.1940, 0.0978, 0.0284, 0.0000, 0.0486, 0.0982, 0.1978, 0.0264, 0.0272, 0.0288, 0.0284, 0.0264, 0.0272, 0.0288, 0.0284, 0.0264, 0.0155 0.0156 0.0154 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0146 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0144 0.0145 0.0 | | 0.996 | 0.983 | 0.787 | 0.153 | 0.795 | 0.985 | 0 998 |
| CML_BIC | CME MAY BIC | | | | | | | |
| CML_BIC | | | | | | | | |
| -0.1971, -0.0987, -0.0942, -0.0041, -0.0994, -0.0991, -0.1989, -0.00146 -0.0144 -0.0143 -0.0143 -0.0145 -0.0146 -0.014 | | | | | | | 0.0155 | |
| MR-RAPS 0.0315, 0.0261, 0.0261, 0.0241, 0.0143 | cML-BIC | | | | | | | |
| cML.MA.BIC.DP, T = 100 0.0146 0.0143 0.0143 0.0143 0.0144 0.0146 0.0146 cML.MA.BIC.DP, T = 100 0.0503, 0.0837, 0.037, 0.037, 0.031, 0.0902, 0.0148, 0.00904, 0.1880, 0.0006 0.0216, 0.00246, 0.0014, 0.0188, 0.0006, 0.0222, 0.0008, 0.00216, 0.00244, 0.0015, 0.0026, 0.00216, 0.00244, 0.0015, 0.0026, 0.0022, 0.00216, 0.0024, 0.0013, 0.0006, 0.0022, 0.0018, 0.0024, 0.0013, 0.0006, 0.0 | | | | | | | | |
| CML-MA-BIC-DP, T = 100 | | | | | | | | |
| | MI MA DIC DD T - 100 | | | | | | | |
| CML_BIC-DP, T = 100 | CML-MA-BIC-DP, I = 100 | | | | | | | |
| cML_BIC.DP, T = 100 | | | | | | | | |
| CML-BIC-DP, T = 100 | | | | | | | | |
| CML-MA-BIC-DP, T = 200 | cML-BIC-DP, T = 100 | | | 0.539, | | | 0.898, | 0.969, |
| CML-MA-BIC-DP, T = 200 | | | | | | | | |
| cML-MA-BIC-DP, T = 200 0.9512, 0.952, 0.909, 0.0437, 0.0002, 0.0442, 0.0908, 0.0351, 0.0234, 0.0235, 0.0225 0.0202 0.00223 0.0251, 0.0234, 0.0313, 0.0235, 0.0225 0.0202 0.0222 0.0223 0.0251, 0.0308 0.0908, 0.01845, 0.0034, 0.0019, 0.0216, 0.0244, 0.0313, 0.00308 0.0351, 0.0234, 0.0033, 0.0415, 0.0216, 0.0244, 0.0313, 0.0348, 0.0234, 0.0333, 0.0019, 0.0415, 0.0415, 0.0244, 0.0312, 0.0348, 0.0234, 0.0234, 0.0217, 0.0197, 0.0218, 0.0244, 0.0312, 0.0348, 0.0234, 0.0234, 0.0217, 0.0197, 0.0218, 0.0244, 0.0312, 0.0348, 0.0234, 0.0234, 0.0217, 0.0197, 0.0218, 0.0244, 0.0312, 0.0352, 0.024, 0.0234, 0.0215, 0.0195, 0.0246, 0.0352, 0.024, 0.0234, 0.0215, 0.0195, 0.0246, 0.0352, 0.024, 0.0234, 0.0215, 0.0195, 0.0216, 0.0244, 0.0315, 0.0352, 0.0249, 0.0215, 0.0195, 0.0216, 0.0244, 0.0315, 0.0351, 0.0249, 0.0215, 0.0195, 0.0246, 0.0351, 0.0314, 0.0334, 0.0249, 0.0215, 0.0195, 0.0246, 0.0353, 0.0354, 0.0249, 0.0215, 0.0199, 0.0219, 0.0244, 0.0313, 0.0354, 0.0249, 0.0221, 0.0001, 0.0443, 0.0910, 0.1850, 0.0354, 0.0354, 0.0249, 0.0221, 0.0199, 0.0219, 0.0244, 0.0313, 0.0304, 0.0249, 0.0221, 0.0199, 0.0219, 0.0244, 0.0313, 0.0304, 0.0249, 0.0221, 0.0199, 0.0219, 0.0244, 0.0313, 0.0304, 0.0266, | | | | | | | | |
| -0.1826, -0.0899, -0.0437, -0.0002, -0.0442, -0.0028, -0.0244, -0.0313, -0.0351, -0.0349, -0.0215, -0.0202, -0.0223, -0.0221, -0.0313, -0.0301, -0.0503, -0.0301, | M. M. DIG DD T. 200 | | | | | | | |
| O.0351, O.0249, O.0215, O.0216, O.02214, O.0318 | cML-MA-BIC-DP, $T = 200$ | | | | | | | |
| MIL-BIC-DR T = 200 | | | | | | | | |
| CML-BIC-DP, T = 200 | | | | | | | | |
| -0.1834, | cML-BIC-DP, T = 200 | | | | | | | |
| MR-Mix | , | | | | | | | |
| CML-MA-BIC-DP, T = 500 | | 0.0348, | 0.0250, | 0.0217, | 0.0197, | 0.0218, | | 0.0312, |
| -0.1824, -0.0899, -0.0438, 0.0001, 0.0042, 0.0094, 0.0315, 0.0311 | | | | | | | | |
| CML-BIC-DP, T = 500 | cML-MA-BIC-DP, T = 500 | | | | | | | |
| CMI_BIC_DP, T = 500 | | | | | | | | |
| CML-BIC-DP, T = 500 | | | | | | | | |
| O.1832, O.0904, O.0441, O.0001, O.0443, O.0910, O.1850, O.0351, O.0249, O.0215, O.0196, O.0217, O.0244, O.0313, O.0304, O.0249, O.0212, O.0199, O.0217, O.0247, O.0303, O.0303, O.0904, O.0202, O.0205, O.0205, O.0206, O.0205, O.0206, O.0206, O.0266, O.0265, O.0206, O.0266, O.0266, O.0266, O.0255, O.0272, O.0259, O.0259, O.0260, O.0263, O.0266, O.0266, O.0255, O.0272, O.0257, O.0259, O.0260, O.0813, O.0274, O.0263, O.0255, O.0272, O.0257, O.0259, O.0494, O.0255, O.0258, O.0258, O.0298, O.0258, O.02 | cMI_RIC_DP T = 500 | | | | | | | |
| 0.0351, 0.0249, 0.0215, 0.0199, 0.0217, 0.0244, 0.0313, 0.0304 0.0924 0.0221 0.0999, 0.0304 0.0992, 0.0304 0.0992, 0.0908, 0.0000, 0.0000, 0.0500, 0.1001, 0.0205, 0.0266, 0.0267, 0.0991, 0.0261, 0.0813, 0.0274, 0.0263, 0.0255, 0.0258, 0.0258, 0.0258, 0.0258, 0.0258, 0.0258, 0.0258, 0.0258, 0.0258, 0.0258, 0.0261, 0.080, 0.0994, 0.0267, 0.0264, 0.0266, 0.0266, 0.0266, 0.0267, 0.0264, 0.0266, 0.0267, 0.0264, 0.0266, 0.0267, 0.0264, 0.0266, 0.0277, 0.0168, 0.0167, 0.0166, 0.0167, 0.0166, 0.0167, 0.0166, 0.0167, 0.0166, 0.0167, 0.0168, 0.0167, 0.0166, 0.0167, 0.0168, 0.0167, 0.0269, 0.0251, 0.0550, 0.0014, 0.0489, 0.0984, 0.1978, 0.0675, 0.0975, 0. | CWIE-BIC-BI, 1 = 300 | | | | | | | |
| MR-Mix | | | | | | | | |
| -0.2004, | | 0.0304 | | 0.0221 | | | | |
| 0.0269, 0.0256, 0.0266, 0.0263, 0.0274, 0.0263 0.0255 | MR-Mix | 0.992, | | | 0.094, | 0.602, | 0.929, | 0.989, |
| MR-ContMix | | | | | | | | |
| MR-ContMix | | | | | | | | |
| -0.1991, -0.0995, -0.0494, 0.0002, 0.0500, 0.0998, 0.1994, 0.0257, 0.0258, 0.0258, 0.0258, 0.0258, NA | 160 G 216 | | | | | | | |
| 0.0257, 0.0254, 0.0256, 0.0258, 0.0258, 0.0258, 0.0261, NA | MR-ContMix | | | | | | | |
| NA | | | | | | | | |
| MR-Lasso | | | | | | | | |
| -0.1989, | MR-Lasso | | | | | | | |
| MR-PRESSO | | -0.1989, | -0.0999, | -0.0502, | -0.0003, | 0.0489, | 0.0989, | |
| MR-PRESSO | | | | | | | | |
| -0.1985, -0.0995, -0.0499, -0.0004, 0.0489, 0.0984, 0.1978, 0.0550, 0.0550, 0.0550, 0.0550, 0.0547, 0.0548, 0.0549, 0.0206 0.0208 | | | | | | | | |
| 0.0550, 0.0550, 0.0550, 0.0547, 0.0548, 0.0549, 0.0208 | MR-PRESSO | | | | | | | |
| MR-IVW | | | | | | | | |
| MR-IVW 0.548, 0.168, 0.085, 0.047, 0.081, 0.179, 0.523, 0.09075, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0987, 0.0988, 0.0173, 0.0170, 0.0170, 0.0170, 0.0170, 0.0170, 0.0173, 0.0176, 0.0175, 0.0175, 0.0174, 0.0174, 0.0174, 0.0174, 0.0174, 0.0175, 0.0175, 0.0175, 0.0175, 0.0175, 0.0175, 0.0175, 0.0175, 0.01653, 0.1654, 0.1654, 0.1655, 0.1655, 0.1655, 0.1656, 0.1661, 0.0386, 0.0342, 0.0339, 0.03 | | | | | | | | |
| -0.2004, | MR-IVW | | | | | | | |
| MR-IVW-Oracle | | | | | | | | |
| MR-IVW-Oracle | | | | | | | | |
| -0.1983, | | | | | | | | |
| 0.0173, 0.0171, 0.0170, 0.0170, 0.0170, 0.0170, 0.0170, 0.0176, 0.0176 0.0176 0.0175 0.0174 0.0174 0.0174 0.0175 0.0176 0.0176 0.0176 0.0176 0.0175 0.0176 0.0174 0.0174 0.0175 0.0176 0.0176 0.0176 0.0176 0.0174 0.0174 0.0174 0.0176 0.0177 0. | MR-IVW-Oracle | | | | | | | |
| MR-Egger 0.0176 0.0175 0.0174 0.0174 0.0175 0.0176 | | | | | | | | |
| MR-Egger 0.238, -0.2019, -0.1025, -0.053, -0.0031, 0.048, 0.0667, 0.102, 0.242, 0.1653, 0.1653, 0.1654, 0.1654, 0.1655, 0.1655, 0.1655, 0.1655, 0.1655, 0.1656, 0.1661 0.0031, 0.0466, 0.0964, 0.0964, 0.1958, 0.1655, 0.1655, 0.1655, 0.1655, 0.1655, 0.1656, 0.1661 0.1661 0.1661 0.1661 0.1661 0.1661 0.1661 0.1661 0.1651, 0.1654, 0.1654, 0.1655, 0.1655, 0.1655, 0.1655, 0.1656, 0.1661 MR-Weighted-Median 0.991, 0.937, 0.630, 0.138, 0.0606, 0.935, 0.990, 0.0366, 0.0342, 0.0339, 0.0339, 0.0339, 0.0349, 0.0358, 0.0380, 0.0221 0.0218 0.0217 0.0216 0.0216 0.0217 0.0221 0.0366, 0.0342, 0.0339, 0.0339, 0.0349, 0.0358, 0.0380, 0.0221 0.0218 0.0217 0.0216 0.0216 0.0217 0.0221 MR-Weighted-Mode 0.611, 0.433, 0.238, 0.116, 0.242, 0.437, 0.626, 0.1957, -0.1032, -0.0531, -0.0174, 0.0212, 0.0724, 0.1641, 0.2474, 0.2596, 0.2733, 0.2997, 0.2746, 0.2637, 0.2735, 1.7626 1.7570 1.7426 1.7348 1.7399 1.7390 1.7241 MR-RAPS1 0.555, 0.181, 0.088, 0.053, 0.085, 0.085, 0.180, 0.534, 0.0986, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0982, 0.0982 0.0982 0.0982 0.0982 0.0982 0.0982 0.0982 0.0982 0.0982 MR-RAPS2 0.709, 0.348, 0.211, 0.094, 0.214, 0.348, 0.687, 0.0094, 0.00945, 0.0096, 0.0086, 0.0834, 0.0823, 0.0813, 0.0898, 0.0815, 0.00757 0.0760 0.0756 0.0758 0.0758 0.0756 0.0760 0.0756 0.0758 0.0758 0.0756 0.0760 0.0756 0.0758 0.0366, 0.2052, 0.1165, 0.0112, 0.4931, 0.2063, 0.3540, 0.2224, 0.2224, 0.2254, 0.2554, 0.3253, 0.3343, 0.0545, 0.0112, 0.0489, 0.0220 0.0233 0.0334 0.0265 12.8425 0.0321 0.0580 0.0111, 0.0472, 0.0204, 0.1136, 0.0637, 0.0549, 0.1311, 0.0266, 0.1177, 0.0472, 0.0774, 0.01136, 0.0637, 0.0549, 0.1311, 0.0266, 0.11311, | | | | | | | | |
| -0.2019, -0.1025, -0.0528, -0.0031, 0.0466, 0.0964, 0.1958, 0.1653, 0.16653, 0.16654, 0.16654, 0.16655, 0.1655, 0.1655, 0.1656, 0.16661 0.1661 | MP Eggar | | | | | | | |
| 0.1653, 0.1654, 0.1655, 0.1655, 0.1655, 0.1655, 0.1656, 0.1661 0.1661 | MIX-Egger | | | | | | | |
| MR-Weighted-Median | | | | | | | | |
| -0.1893, -0.0955, -0.0483, -0.0011, 0.0460, 0.0932, 0.1876, | | | | | | | | |
| -0.1893, -0.0955, -0.0483, -0.0011, 0.0460, 0.0932, 0.1876, | MR-Weighted-Median | 0.991, | | | 0.138, | | 0.935, | |
| MR-Weighted-Mode | | | | | | | | |
| MR-Weighted-Mode 0.611, 0.433, 0.238, 0.116, 0.242, 0.437, 0.626, 0.1957, 0.1957, -0.1032, -0.0531, -0.0174, 0.0212, 0.0724, 0.1641, 0.2274, 0.2296, 0.2733, 0.2997, 0.2746, 0.2637, 0.2735, 1.7626 1.7570 1.7426 1.7348 1.7399 1.7390 1.7241 MR-RAPS1 0.555, 0.181, 0.088, 0.053, 0.085, 0.180, 0.980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0982, 0.0982, 0.0982, 0.0982, 0.0982, 0.0982, 0.0982, 0.00982, 0. | | | | | | | | |
| -0.1957, -0.1032, -0.0531, -0.0174, 0.0212, 0.0724, 0.1641, 0.2474, 0.2596, 0.2733, 0.2997, 0.2746, 0.2637, 0.2735, 1.7626 1.7570 1.7426 1.7349 1.7390 1.7241 | MD Weight 1M-1 | | | | | | | |
| 0.2474, 0.2596, 0.2733, 0.2997, 0.2746, 0.2637, 0.2735, 1.7626 | MK-weighted-Mode | | | | | | | |
| 1.7626 1.7570 1.7426 1.7348 1.7399 1.7390 1.7241 MR-RAPS1 0.555, 0.181, 0.088, 0.053, 0.085, 0.180, 0.534, -0.2014, -0.1014, -0.0014, -0.0014, 0.0486, 0.0986, 0.1985, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0982 0.0982 0.0982 0.0982 0.0982 0.0982 MR-RAPS2 0.709, 0.348, 0.211, 0.094, 0.214, 0.348, 0.687, -0.2033, -0.1019, -0.0529, -0.0013, 0.0487, 0.1000, 0.1993, 0.0945, 0.0806, 0.0834, 0.0823, 0.0813, 0.0898, 0.0815, 0.0757 0.0760 0.0756 0.0758 0.0756 0.0760 0.0760 MR-RAPS3 0.978, 0.916, 0.862, 0.842, 0.830, 0.911, 0.975, 0.3806, -0.2052, -0.1165, -0.0112, -0.4931, 0.2063, 0.3540, 0.2224, 0.2554, 0.3253, 0.3403, 15.5916, 0.3738, 0.7622, 0.0220 0.0233 0.0334 0.0265 12.8425 0.0321 0.0580 MR-RAPS4 1.000, 0.999, 0.917, 0.377, 0.922, 0.997, 0.999, -0.2024, -0.1026, -0.0498, 0.0033, 0.0545, 0.1012, 0.2066, 0.1117, 0.0472, 0.0774, 0.1136, 0.0637, 0.5549, 0.1311, | | | | | | | | |
| MR-RAPS1 0.555, -0.2014, -0.1014, -0.0514, -0.0014, -0.0014, 0.0486, 0.0986, 0.0986, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0982, 0.0982 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0980, 0.0982 0.0980, 0.0982, 0.0982, 0.0982, 0.0982, 0.0982, 0.0982 0.0982, 0 | | | | | | | | |
| -0.2014, | MR-RAPS1 | | | | | | | |
| 0.0982 0.0982 0.0982 0.0982 0.0982 0.0982 0.0982 0.0982 | | -0.2014, | -0.1014, | -0.0514, | -0.0014, | 0.0486, | 0.0986, | 0.1985, |
| MR-RAPS2 0.709, -0.2033, 0.0945, 0.0945, 0.0945, 0.0946, 0.0757 0.348, 0.0806, 0.0834, 0.0758 0.211, 0.00529, 0.0823, 0.0813, 0.0813, 0.0813, 0.0813, 0.0756 0.0487, 0.0100, 0.0813, 0.0813, 0.0756 0.0898, 0.0756 0.0898, 0.0756 0.0815, 0.0760 MR-RAPS3 0.978, 0.2224, 0.2224, 0.2224, 0.0220 0.916, 0.3253, 0.3343, 0.3343 0.842, 0.3403, 0.3403, 0.3403, 0.3403, 0.3540, 0.3253, 0.3403, 0.3540, 0.3253, 0.3403, 0.3253, 0.3403, 0.3540, 0.3253, 0.3403, 0.3540, 0.3253, 0.3403, 0.3540, 0.3253, 0.3403, 0.3540, 0.3752, 0.0220 0.0933, 0.0334, 0.0265 0.0321, 0.0545, 0.0545, 0.0112, 0.0549, 0.1131, | | 0.0980, | | | | | | |
| -0.2033, -0.1019, -0.0529, -0.0013, 0.0487, 0.1000, 0.1993, 0.0945, 0.0806, 0.0834, 0.0823, 0.0813, 0.0898, 0.0815, 0.0757 0.0760 0.0756 0.0758 0.0756 0.0758 0.0756 0.0756 0.0758 0.0756 0.0758 0.0758 0.02524, 0.2554, 0.3253, 0.3403, 0.3540, 0.3553 0.3403, 0.0555 0.0321 0.0580 0.0220 0.0233 0.0334 0.0265 12.8425 0.0321 0.0580 0.0580 0.0549 0.0034 0.0037, 0.0549, 0.1177, 0.0472, 0.0774, 0.1136, 0.0637, 0.0549, 0.1311, 0.0754 0.11311, 0.0559 0.0034, 0.0637, 0.0549, 0.1311, 0.00556 0.00574, 0.00549, 0.1311, 0.00575 0.00549, 0.1311, 0.00575 0.00549, 0.1311, 0.00575 0.00549, 0.1311, 0.00575 0.00549, 0.1311, 0.00575 0.00549, 0.1311, 0.00575 0.00549, 0.00575 0.00549, 0.00575 0.00549, 0.00575 0.00549, 0.00575 0.00549, 0.00575 0 | | | | | | | | |
| 0.0945, 0.0806, 0.0834, 0.0823, 0.0813, 0.0898, 0.0815, 0.0757 0.0760 0.0756 0.0758 0.0756 0.0756 0.0760 0.0760 MR-RAPS3 0.978, 0.916, 0.862, 0.842, 0.830, 0.911, 0.975, 0.3806, -0.2052, -0.1165, -0.0112, -0.4931, 0.2063, 0.3540, 0.2224, 0.2254, 0.3253, 0.3403, 15.5916, 0.3738, 0.7622, 0.0220 0.0233 0.0334 0.0265 12.8425 0.0321 0.0580 MR-RAPS4 1.000, 0.999, 0.917, 0.377, 0.922, 0.997, 0.999, -0.2024, -0.1026, -0.0498, 0.0033, 0.0545, 0.1012, 0.2060, 0.1177, 0.0472, 0.0774, 0.1136, 0.0637, 0.0549, 0.1311, | MR-RAPS2 | | | | | | | |
| 0.0757 0.0760 0.0756 0.0758 0.0756 0.0760 0.0760 0.0760 | | | | | | | | |
| MR-RAPS3 0.978, 0.916, 0.862, 0.842, 0.830, 0.911, 0.975, 0.3268, 0.2052, 0.1165, 0.3012, 0.4931, 0.2063, 0.3540, 0.2224, 0.2554, 0.3253, 0.3403, 15.5916, 0.3738, 0.7622, 0.0220 0.0233 0.0334 0.0265 12.8425 0.0321 0.0580 MR-RAPS4 1.000, 0.999, 0.917, 0.377, 0.922, 0.997, 0.999, 0.2024, 0.1026, 0.0498, 0.0033, 0.0545, 0.1012, 0.2066, 0.1177, 0.0472, 0.0774, 0.1136, 0.0637, 0.0549, 0.1311, | | | | | | | | |
| -0.3806, -0.2052, -0.1165, -0.0112, -0.4931, 0.2063, 0.3540, 0.2224, 0.2554, 0.3253, 0.3403, 15.5916, 0.3738, 0.7622, 0.0220 0.0233 0.0334 0.0265 12.8425 0.0321 0.0580 | MP_PADC2 | | | | | | | |
| 0.2224, 0.0220 0.2554, 0.0233 0.3253, 0.0334 0.3403, 0.0265 15.5916, 12.8425 0.3738, 0.0321 0.7622, 0.0580 MR-RAPS4 1.000, -0.2024, 0.1177, 0.999, 0.917, 0.0498, 0.0033, 0.0545, 0.1136, 0.997, 0.0545, 0.1136, 0.0637, 0.0637, 0.0549, 0.1131, 0.999, 0.1311, | WIN-KAP33 | | | | | | | |
| 0.0220 0.0233 0.0334 0.0265 12.8425 0.0321 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0.0580 0 | | | | | | | | |
| MR-RAPS4 1.000, 0.999, 0.917, 0.377, 0.922, 0.997, 0.999, 0.0177, 0.02024, 0.0177, 0.0472, 0.0774, 0.1136, 0.0637, 0.0549, 0.1311, | | | | | | | | |
| -0.2024, -0.1026, -0.0498, 0.0033, 0.0545, 0.1012, 0.2060, 0.1177, 0.0472, 0.0774, 0.1136, 0.0637, 0.0549, 0.1311, | MR-RAPS4 | | | | | | | |
| | | -0.2024, | -0.1026, | -0.0498, | 0.0033, | 0.0545, | 0.1012, | 0.2060, |
| 0.0108 0.0105 0.0105 0.0105 0.0105 0.0105 0.0109 | | | | | | | | |
| | | 0.0108 | 0.0105 | 0.0105 | 0.0105 | 0.0105 | 0.0105 | 0.0109 |

Table S110: Simulations with weak invalid IVs: in each cell, from top to bottom are empirical type-I error/power, $mean(\hat{\theta})$, $SD(\hat{\theta})$, $mean(SE(\hat{\theta}))$ when $h_y = 0.6$ and $h_u = 0$.

| , | · · | | · · · | | | 1 | |
|---|---------------------|---------------------|---------------------|--------------------|--------------------|--------------------|--------------------|
| Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
| cML-MA-BIC | 0.996, | 0.987, | 0.792, | 0.152, | 0.799, | 0.985, | 0.999, |
| eme mir bre | -0.1968, | -0.0982, | -0.0485, | 0.0002, | 0.0489, | 0.0986, | 0.1980, |
| | 0.0294, | 0.0242, | 0.0233, | 0.0223, | 0.0233, | 0.0241, | 0.0266, |
| | 0.0161 | 0.0157 | 0.0157 | 0.0156 | 0.0156 | 0.0157 | 0.0158 |
| cML-BIC | 0.999, | 0.992, | 0.820, | 0.185, | 0.827, | 0.992, | 0.999, |
| | -0.1977, | -0.0990, | -0.0491, | 0.0001, | 0.0495, | 0.0993, | 0.1986, |
| | 0.0295, | 0.0246, | 0.0238, | 0.0233, | 0.0238, | 0.0245, | 0.0272, |
| cML-MA-BIC-DP, T = 100 | 0.0149 0.953, | 0.0147 0.900, | 0.0146 0.544, | 0.0146 | 0.0146 0.575, | 0.0147 0.913, | 0.0149 0.965, |
| CML-MA-BIC-DP, I = 100 | -0.1853, | -0.0914, | -0.0444, | 0.029, 0.0002, | 0.373, | 0.913, 0.0922, | 0.963, |
| | 0.0324, | 0.0239, | 0.0211, | 0.0002, | 0.0212, | 0.0236, | 0.0297, |
| | 0.0291 | 0.0242 | 0.0217 | 0.0197 | 0.0215 | 0.0239 | 0.0285 |
| cML-BIC-DP, T = 100 | 0.959, | 0.906, | 0.559, | 0.036, | 0.582, | 0.916, | 0.967, |
| | -0.1860, | -0.0918, | -0.0447, | 0.0002, | 0.0453, | 0.0927, | 0.1877, |
| | 0.0321, | 0.0240, | 0.0214, | 0.0195, | 0.0212, | 0.0238, | 0.0295, |
| | 0.0284 | 0.0237 | 0.0214 | 0.0194 | 0.0211 | 0.0234 | 0.0278 |
| cML-MA-BIC-DP, $T = 200$ | 0.953, | 0.897, | 0.530, | 0.025, | 0.557, | 0.912, | 0.964, |
| | -0.1848, | -0.0911, | -0.0443, | 0.0002, | 0.0449, | 0.0919, | 0.1866, |
| | 0.0326, 0.0296 | 0.0238, 0.0245 | 0.0210, | 0.0191, 0.0199 | 0.0211, 0.0218 | 0.0236, | 0.0300, |
| cML-BIC-DP, T = 200 | 0.0296 | 0.0243 | 0.0220 0.542, | 0.0199 | 0.0218 | 0.0243 0.912, | 0.0291 |
| CML-BIC-DP, $T = 200$ | -0.1855, | -0.0915, | -0.0445, | 0.032, | 0.363, | 0.912, 0.0923, | 0.966, 0.1871, |
| | 0.0326, | 0.0238, | 0.0212, | 0.0193, | 0.0213, | 0.0237, | 0.0301, |
| | 0.0320, | 0.0230, | 0.0212, | 0.0196 | 0.0213, | 0.0237, | 0.0283 |
| cML-MA-BIC-DP, T = 500 | 0.950, | 0.900, | 0.536, | 0.025, | 0.560, | 0.913, | 0.965, |
| | -0.1847, | -0.0911, | -0.0443, | 0.0002, | 0.0448, | 0.0919, | 0.1864, |
| | 0.0327, | 0.0238, | 0.0210, | 0.0191, | 0.0211, | 0.0237, | 0.0301, |
| | 0.0297 | 0.0245 | 0.0219 | 0.0198 | 0.0218 | 0.0242 | 0.0293 |
| cML-BIC-DP, T = 500 | 0.952, | 0.902, | 0.548, | 0.032, | 0.572, | 0.914, | 0.967, |
| | -0.1855, | -0.0914, | -0.0444, | 0.0003, | 0.0452, | 0.0923, | 0.1871, |
| | 0.0325, | 0.0238, | 0.0211, | 0.0194, | 0.0212, | 0.0237, | 0.0298, 0.0286 |
| MR-Mix | 0.0290 | 0.0240 0.926, | 0.0215 | 0.0195 | 0.0214 0.616, | 0.0238 | 0.0286 |
| WIK-WIIX | -0.2003, | -0.1001, | 0.619, -0.0502, | 0.095, 0.0000, | 0.010, | 0.929, 0.0998, | 0.987, |
| | 0.0259, | 0.0260, | 0.0259, | 0.0000, | 0.0499, | 0.0264, | 0.1990, |
| | 0.0254 | 0.0244 | 0.0246 | 0.0252 | 0.0241 | 0.0247 | 0.0280 |
| MR-ContMix | 1.000, | 0.998, | 0.827, | 0.225, | 0.844, | 0.992, | 1.000, |
| | -0.1988, | -0.0995, | -0.0497, | 0.0002, | 0.0499, | 0.0997, | 0.1991, |
| | 0.0252, | 0.0248, | 0.0251, | 0.0251, | 0.0252, | 0.0250, | 0.0252, |
| | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.999, | 0.985, | 0.781, | 0.161, | 0.777, | 0.982, | 1.000, |
| | -0.1989, | -0.0994, | -0.0497, | -0.0001, | 0.0496, | 0.0993, | 0.1984, |
| | 0.0275, 0.0170 | 0.0268, 0.0170 | 0.0269, 0.0169 | 0.0270, 0.0169 | 0.0272, 0.0169 | 0.0268, 0.0170 | 0.0273, |
| MR-PRESSO | 0.0170 | 0.886, | 0.694, | 0.0109 | 0.682, | 0.0170 | 0.0171 |
| WIK-I KESSO | -0.1988, | -0.0997, | -0.0499, | -0.0004, | 0.0491, | 0.0986, | 0.1980, |
| | 0.0676, | 0.0677, | 0.0682, | 0.0685, | 0.0688, | 0.0689, | 0.0697, |
| | 0.0222 | 0.0220 | 0.0219 | 0.0219 | 0.0220 | 0.0221 | 0.0224 |
| MR-IVW | 0.396, | 0.135, | 0.075, | 0.048, | 0.066, | 0.134, | 0.383, |
| | -0.2006, | -0.1012, | -0.0514, | -0.0017, | 0.0480, | 0.0978, | 0.1973, |
| | 0.1190, | 0.1190, | 0.1190, | 0.1190, | 0.1190, | 0.1190, | 0.1191, |
| | 0.1206 | 0.1206 | 0.1206 | 0.1206 | 0.1206 | 0.1206 | 0.1207 |
| MR-IVW-Oracle | 1.000, | 1.000, | 0.804, | 0.041, | 0.815, | 0.999, | 1.000, |
| | -0.1983, 0.0173, | -0.0988, 0.0171, | -0.0491, 0.0170, | 0.0006, 0.0170, | 0.0504, 0.0170, | 0.1001, 0.0170, | 0.1995, 0.0173, |
| | 0.0175, | 0.0171, | 0.0170, | 0.0170, | 0.0170, | 0.0176, | 0.0175, |
| MR-Egger | 0.174, | 0.076, | 0.050, | 0.046, | 0.065, | 0.088, | 0.180, |
| | -0.2024, | -0.1030, | -0.0533, | -0.0036, | 0.0462, | 0.0959, | 0.1953, |
| | 0.2021, | 0.2021, | 0.2022, | 0.2022, | 0.2023, | 0.2023, | 0.2024, |
| | 0.2030 | 0.2030 | 0.2030 | 0.2030 | 0.2030 | 0.2030 | 0.2031 |
| MR-Weighted-Median | 0.991, | 0.939, | 0.622, | 0.136, | 0.599, | 0.934, | 0.989, |
| | -0.1889, | -0.0951, | -0.0480, | -0.0008, | 0.0463, | 0.0930, | 0.1870, |
| | 0.0377, | 0.0348, | 0.0345, | 0.0345, | 0.0354, 0.0220 | 0.0376, | 0.0408, 0.0224 |
| MR-Weighted-Mode | 0.0225 0.579, | 0.0221 | 0.0220 | 0.0220 0.123, | 0.0220 | 0.0221 | 0.0224 |
| MIX- weighted-Mode | -0.1987, | -0.1091, | -0.0514, | -0.0277, | 0.208, 0.0177, | 0.390, | 0.584, 0.1556, |
| | 0.3192, | 0.3490, | 0.3560, | 0.3437, | 0.0177, 0.3348, | 0.3432, | 0.1550, |
| | 2.0935 | 2.0830 | 2.0716 | 2.0523 | 2.0355 | 2.0462 | 2.0312 |
| MR-RAPS1 | 0.400, | 0.139, | 0.079, | 0.051, | 0.069, | 0.137, | 0.390, |
| | -0.2017, | -0.1017, | -0.0517, | -0.0017, | 0.0483, | 0.0983, | 0.1983, |
| | 0.1196, | 0.1196, | 0.1196, | 0.1197, | 0.1197, | 0.1197, | 0.1197, |
| | 0.1201 | 0.1201 | 0.1201 | 0.1201 | 0.1201 | 0.1201 | 0.1201 |
| MR-RAPS2 | 0.576, | 0.300, | 0.179, | 0.096, | 0.191, | 0.282, | 0.558, |
| | -0.2012, | -0.1017, | -0.0503, | -0.0021, | 0.0499, | 0.1002, | 0.2006, |
| | 0.1014, | 0.1009, | 0.1007, | 0.1060, | 0.0996, 0.0928 | 0.1182, | 0.1152, |
| MR-RAPS3 | 0.0923 0.966, | 0.0921 | 0.0926 | 0.0922 | 0.0928 | 0.0927 0.914, | 0.0918 |
| WIK-KAPSS | -0.7063, | -0.3195, | -1.1323, | -0.1304, | 0.860, 0.2791, | 0.914, 3.7189, | 0.963, 0.4145, |
| | 1.9905, | 7.6792, | 19.2401, | 5.9349. | 9.7956, | 114.1616, | 5.1670, |
| | 0.2124 | 3.5350 | 20.4664 | 2.4806 | 6.5607 | 912.8000 | 0.8545 |
| MR-RAPS4 | 1.000, | 0.999, | 0.917, | 0.370, | 0.930, | 0.997, | 0.999, |
| • | -0.2078, | -0.0994, | -0.0432, | 0.0033, | 0.0593, | 0.1127, | 0.2148, |
| | 0.1447, | 0.1253, | 0.1208, | 0.1853, | 0.1198, | 0.1408, | 0.1713, |
| | 0.0110 | 0.0107 | 0.0106 | 0.0109 | 0.0106 | 0.0108 | 0.0112 |
| | | | | | | | |

Table S111: Simulations with weak invalid IVs: in each cell, from top to bottom are empirical type-I error/power, $mean(\hat{\theta})$, $SD(\hat{\theta})$, $mean(SE(\hat{\theta}))$ when $h_y = 0.1$ and $h_u = 0.1$.

| | | . ' / / | | | | | |
|--------------------------|----------|-------------------|----------|----------|-----------------|-----------------|-----------------|
| θ Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
| cML-MA-BIC | 0.980. | 0.961. | 0.720, | 0.230, | 0.799, | 0.988, | 0.998, |
| COME THE BIC | -0.1857, | -0.0919, | -0.0440, | 0.0028, | 0.0507, | 0.1001, | 0.1998, |
| | 0.0415, | 0.0288, | 0.0259, | 0.0240, | 0.0256, | 0.0270, | 0.0283, |
| | 0.0150 | 0.0149 | 0.0237, | 0.0147 | 0.0230, | 0.0270, | 0.0283, |
| cML-MA-BIC-DP, T = 200 | 0.826, | 0.746, | 0.387, | 0.043, | 0.532, | 0.895, | 0.980, |
| CML-MA-BIC-DP, $I = 200$ | -0.1615, | -0.0806, | -0.0384, | 0.043, | 0.332, | 0.893, | 0.980, |
| | 0.0467, | 0.0284, | 0.0227, | 0.0032, | 0.0407, | 0.0259, | 0.1898, |
| | 0.0407, | 0.0284, | 0.0227, | 0.0202, | 0.0229, | 0.0259, | 0.0302, |
| MR-Mix | 0.0404 | 0.0280 | 0.594. | 0.0206 | 0.0228 | 0.0233 | 0.0282 |
| MIK-MIX | | | | | | | |
| | -0.2005, | -0.1005, | -0.0502, | -0.0001, | 0.0499, | 0.0999, | 0.2004, |
| | 0.0286, | 0.0276, 0.0293 | 0.0275, | 0.0276, | 0.0277, | 0.0277, | 0.0293, |
| | 0.0269 | | 0.0267 | 0.0268 | 0.0270 | 0.0264 | 0.0265 |
| MR-ContMix | 0.999, | 0.989, | 0.803, | 0.321, | 0.848, | 0.992, | 1.000, |
| | -0.1959, | -0.0960, | -0.0466, | 0.0031, | 0.0528, | 0.1026, | 0.2021, |
| | 0.0284, | 0.0283, | 0.0280, | 0.0279, | 0.0279, | 0.0279, | 0.0285, |
| | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.986, | 0.884, | 0.560, | 0.375, | 0.927, | 0.998, | 1.000, |
| | -0.1734, | -0.0743, | -0.0245, | 0.0252, | 0.0750, | 0.1255, | 0.2251, |
| | 0.0396, | 0.0390, | 0.0394, | 0.0394, | 0.0390, | 0.0403, | 0.0401, |
| | 0.0170 | 0.0169 | 0.0169 | 0.0168 | 0.0168 | 0.0168 | 0.0169 |
| MR-PRESSO | 0.884, | 0.613, | 0.423, | 0.585, | 0.940, | 0.996, | 1.000, |
| | -0.1360, | -0.0370, | 0.0125, | 0.0619, | 0.1114, | 0.1608, | 0.2602, |
| | 0.0597, | 0.0595, | 0.0597, | 0.0598, | 0.0598, | 0.0592, | 0.0589, |
| | 0.0220 | 0.0218 | 0.0217 | 0.0217 | 0.0218 | 0.0219 | 0.0220 |
| MR-IVW | 0.312, | 0.079, | 0.160, | 0.378, | 0.676, | 0.863, | 0.994, |
| | -0.0930, | 0.0066, | 0.0564, | 0.1062, | 0.1560, | 0.2057, | 0.3053, |
| | 0.0690, | 0.0690, | 0.0690, | 0.0690, | 0.0690, | 0.0690, | 0.0690, |
| | 0.0649 | 0.0648 | 0.0649 | 0.0649 | 0.0649 | 0.0649 | 0.0649 |
| MR-IVW-Oracle | 1.000, | 0.998, | 0.818, | 0.038, | 0.819, | 0.999, | 1.000, |
| | -0.1985, | -0.0989, | -0.0492, | 0.0006, | 0.0503, | 0.1001, | 0.1996, |
| | 0.0172, | 0.0169, | 0.0168, | 0.0168, | 0.0167, | 0.0168, | 0.0170, |
| | 0.0176 | 0.0175 | 0.0174 | 0.0174 | 0.0174 | 0.0175 | 0.0176 |
| MR-Egger | 0.145, | 0.076, | 0.115, | 0.206, | 0.350, | 0.502, | 0.790, |
| 66 | -0.0862, | 0.0135, | 0.0633, | 0.1131, | 0.1629, | 0.2127, | 0.3124, |
| | 0.1164, | 0.1163, | 0.1163, | 0.1163, | 0.1163, | 0.1162, | 0.1162, |
| | 0.1091 | 0.1091 | 0.1091 | 0.1091 | 0.1091 | 0.1091 | 0.1092 |
| MR-Weighted-Median | 0.918, | 0.751, | 0.409, | 0.367, | 0.861, | 0.992, | 1.000, |
| | -0.1440, | -0.0535, | -0.0081, | 0.0378, | 0.0841, | 0.1308, | 0.2247, |
| | 0.0631, | 0.0569, | 0.0534, | 0.0508, | 0.0486, | 0.0473, | 0.0446, |
| | 0.0224 | 0.0221 | 0.0219 | 0.0218 | 0.0217 | 0.0217 | 0.0218 |
| MR-Weighted-Mode | 0.635, | 0.386, | 0.229, | 0.191, | 0.422, | 0.598, | 0.726, |
| | -0.1477, | -0.0612, | -0.0095, | 0.0272, | 0.0719, | 0.1180, | 0.2192, |
| | 0.2699, | 0.2838, | 0.2803, | 0.2852, | 0.2822, | 0.2650, | 0.2635, |
| | 0.8810 | 0.9130 | 0.9292 | 0.9340 | 0.9462 | 0.9544 | 0.9867 |
| MR-RAPS1 | 0.322, | 0.081, | 0.169, | 0.383, | 0.684, | 0.867, | 0.994, |
| | -0.0934, | 0.0066, | 0.0566, | 0.1067, | 0.1567, | 0.2067, | 0.3068, |
| | 0.0693, | 0.0693, | 0.0693, | 0.0693, | 0.0693, | 0.0693, | 0.0693, |
| | 0.0645 | 0.0645 | 0.0645 | 0.0645 | 0.0645 | 0.0645 | 0.0646 |
| MR-RAPS2 | 0.563, | 0.203, | 0.226, | 0.354, | 0.690, | 0.901, | 0.995, |
| | -0.1214, | -0.0201, | 0.0285, | 0.0798, | 0.1302, | 0.1785, | 0.2807, |
| | 0.0670, | 0.0719, | 0.0792, | 0.0705, | 0.0712, | 0.0778, | 0.0703, |
| | 0.0522 | 0.0522 | 0.0522 | 0.0522 | 0.0522 | 0.0521 | 0.0525 |
| MR-RAPS3 | 0.919, | 0.777, | 0.863, | 0.923, | 0.979, | 0.999, | 1.000, |
| Mic Rai 55 | -0.1172, | 0.0091, | 0.0723, | 0.1351, | 0.1972, | 0.2585, | 0.3779, |
| | 0.0880, | 0.0892, | 0.0895, | 0.0897, | 0.1372, | 0.0897, | 0.0891, |
| | 0.0123 | 0.0123 | 0.0123 | 0.0124 | 0.0898, | 0.0897, | 0.0126 |
| MR-RAPS4 | 0.998, | 0.996, | 0.892, | 0.0124 | 0.926, | 0.998, | 1.000, |
| WIN-ICAL 94 | -0.1898, | -0.0936, | -0.0243, | 0.444, | 0.926, 0.0577, | 0.998, | 0.2433, |
| | 0.0823, | 0.0682, | 0.1124, | 0.0133, | 0.0377, 0.0458, | 0.1061, 0.1458, | 0.2433, 0.1837, |
| | 0.0823, | 0.0082, | 0.0099 | 0.0904, | 0.0438, | 0.1438, | 0.1837, |
| | 0.0101 | 0.0027 | 0.0027 | 0.0027 | 0.0077 | 0.0120 | 0.0104 |

Table S112: Simulations with weak invalid IVs: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when $h_y = 0.2$ and $h_u = 0.1$.

| Methods | | , | . ' / / | , | | | | |
|--|--------------------------|----------|----------|----------|---------|---------|---------|---------|
| -0.1900, -0.0944, -0.0456, 0.0018, 0.0093, 0.0992, 0.1979, 0.0776, 0.0275, 0.0275, 0.0264, 0.0258, 0.0267, 0.00151 0.0152 0.0153 0.0155 0.0153 0.0152 0.0151 0.0151 0.0152 0.0153 0.0158, 0.0878, 0.0979, 0.427, 0.038, 0.0518, 0.0884, 0.0647, 0.0276, 0.0225, 0.0199, 0.0025, 0.0254, 0.0918, 0.1861, 0.0074, 0.0074, 0.0073, 0.0030, 0.0019, 0.0052, 0.0025, 0.0254, 0.0034, 0.0074, 0.0073, 0.0205, 0.0205, 0.0227, 0.0223, 0.0299, 0.0205, 0.0284, 0.0284, 0.0281, 0.0278, 0.0277, 0.0274, 0.0275, 0.0284, 0.02 | Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
| -0.1900, -0.0944, -0.0456, 0.0018, 0.0093, 0.0992, 0.1979, 0.0776, 0.0275, 0.0275, 0.0264, 0.0258, 0.0267, 0.00151 0.0152 0.0153 0.0155 0.0153 0.0152 0.0151 0.0151 0.0152 0.0153 0.0158, 0.0878, 0.0979, 0.427, 0.038, 0.0518, 0.0884, 0.0647, 0.0276, 0.0225, 0.0199, 0.0025, 0.0254, 0.0918, 0.1861, 0.0074, 0.0074, 0.0073, 0.0030, 0.0019, 0.0052, 0.0025, 0.0254, 0.0034, 0.0074, 0.0073, 0.0205, 0.0205, 0.0227, 0.0223, 0.0299, 0.0205, 0.0284, 0.0284, 0.0281, 0.0278, 0.0277, 0.0274, 0.0275, 0.0284, 0.02 | cML-MA-RIC | 0.990 | 0.972 | 0.746 | 0.205 | 0.791 | 0.983 | 0.996 |
| MIL-MA-BIC-DP.T = 200 | CME MIT BIC | | | | | | | |
| CMIL-MA-BIC-DP, T = 200 | | | 0.0276 | | | | | |
| CMIL-MA-BIC-DP, T = 200 | | | | | | | | |
| O.1698, O.0839, O.0403, O.017, O.0452, O.0918, O.1861, O.0417, O.0374, O.0273, O.025, O.0225, O.0225, O.0225, O.0299, | 10.10. PIG.PP. 0.00 | | | | | | | |
| 0.0417, 0.0276, 0.0225, 0.0254, 0.0324, 0.0374, 0.0673, 0.0273, 0.0205, 0.0272, 0.0253, 0.0299, 0.0281, 0.0291, 0.0282, 0.0281, 0.0281, 0.0281, 0.0282, 0.0281, 0.0281, 0.0282, 0.0281, 0.0285, 0.0267, 0.0264, 0.0282, 0.0281, 0.0284, 0.0281, 0.0284, 0.0281, 0.0284, 0.0288, 0.0265, 0.0267, 0.0264, 0.0282, 0.0285, 0.0267, 0.0264, 0.0282, 0.0280, 0.0265, 0.0267, 0.0264, 0.0282, 0.0265, 0.0267, 0.0264, 0.0288, 0.0265, 0.0267, 0.0274, 0.02 | cML-MA-BIC-DP, $I = 200$ | | | | | | | |
| MR-Mix | | | | | | | | |
| MR-Mix | | | | | | | | |
| -0.2004, -0.1002, -0.0502, -0.0002. 0.0500, 0.1003, 0.2003, 0.0284, 0.0284, 0.0288, 0.0282 0.0280 0.0265 0.0267 0.0264, 0.0284, 0.0288, 0.0285 0.0265 0.0267 0.0264, 0.0284, 0.0288, 0.0265 0.0267 0.0264, 0.0258, 0.0265, 0.0267, 0.0274, 0.0278, 0.0277, 0.0274, 0.0274, 0.0275, 0.0275, 0.0274, 0.0275, | | | | | | | | |
| 0.0284 | MR-Mix | | | | | | | |
| MR-ContMix | | | | | | | | |
| MR-ContMix | | | | | | | | |
| -0.1969, -0.0974, -0.0476, -0.0022, -0.0517, -0.1023, -0.0276, -0.0277, NA NA NA NA NA NA NA N | | | | | | | | |
| NA NA NA NA NA NA NA NA | MR-ContMix | | | | | | | |
| NA | | | -0.0974, | | 0.0022, | 0.0517, | 0.1013, | |
| MR-Lasso | | 0.0278, | 0.0277, | 0.0274, | 0.0275, | 0.0274, | 0.0276, | 0.0277, |
| -0.1780, | | NA | NA | NA | NA | NA | NA | NA |
| -0.1780, | MR-Lasso | 0.984, | 0.891, | 0.591, | 0.327, | 0.895, | 0.995, | 1.000, |
| 0.0395, 0.0391, 0.0385, 0.0396, 0.0397, 0.0401, 0.0404, | | -0.1780. | -0.0792. | -0.0291. | 0.0210. | 0.0710. | 0.1206. | |
| MR-PRESSO 0.861, 0.652, 0.436, 0.551, 0.918, 0.999, 0.0068, 0.0666, 0.0611, 0.0672, 0.0622, 0.0628, 0.0666, 0.0666, 0.0666, 0.0661, 0.0629, 0.0228, 0.0227, 0.0227, 0.0228, 0.0563, 0.1661, 0.1559, 0.0845, 0.098, 0.0798, 0.0798, 0.0798, 0.0798, 0.0798, 0.0798, 0.0798, 0.0798, 0.0798, 0.0798, 0.0798, 0.0798, 0.0176, 0.0174, 0.0174, 0.0175, 0.0174, | | | | | | | | |
| MR-PRESSO | | | | | | | | |
| -0.1369, -0.0382, 0.0113, 0.0606, 0.1104, 0.1601, 0.2588, 0.0668, 0.0661, 0.00229 | MR-PRESSO | | | | | | | |
| MR-IVW O.237 | MIK I KESSO | | | | | | | |
| MR-IVW | | | | | | | | |
| MR-IVW 0.237, 0.070, 0.130, 0.284, 0.506, 0.729, 0.953, 0.0846, 0.0845, 0.0846, 0.0798 0.0799 0.00175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0175 0.0174 | | | | | | | | |
| -0.0931, | MD IVW | | | | | | | |
| MR-IVW-Oracle | IVIK-I V VV | | | | | | | |
| MR-IVW-Oracle 0.0798 0.0798 0.0798 0.0798 0.0798 0.0798 0.0798 0.0798 0.0798 0.0798 0.0798 0.0798 MR-IVW-Oracle 1.000, | | | | | | | | |
| MR-IVW-Oracle | | | | | | | | |
| -0.1985, -0.0989, -0.0492, 0.0006, 0.0503, 0.1001, 0.1996, 0.0172, 0.0169, 0.0168, 0.0168, 0.0167, 0.0168, 0.0175 0.0176 | | | | | | | | |
| 0.0172, | MR-IVW-Oracle | | | | | | | |
| MR-Egger | | | | | | | | |
| MR-Egger 0.120, -0.0864, -0.0132, -0.0631, -0.0661, -0.01627, -0.2125, -0.3122, -0.1440, -0.1440, -0.1439, -0.1439, -0.1439, -0.1438, -0.1438, -0.1438, -0.1341 -0.1341 -0.1341 -0.1341 -0.1341 -0.1342 -0.1342 -0.1342 -0.1342 MR-Weighted-Median 0.926, -0.774, -0.0603, -0.0145, -0.0315, -0.0776, -0.1239, -0.2173, -0.0647, -0.0583, -0.0550, -0.0527, -0.0514, -0.0498, -0.0469, -0.0228 -0.0224 -0.0222 -0.0221 -0.0220 -0.0219 -0.0220 -0.0219 -0.0220 -0.0618, -0.1636, -0.0720, -0.0274, -0.0274, -0.0231, -0.073, -0.1206, -0.1206, -0.1206, -0.0274, -0.0274, -0.0231, -0.0761, -0.1206, -0.2167, -0.3395, -0.3339, -0.3384, -0.3240, -0.3268, -0.3301, -0.2906, -0.1046 -0.0146 -0.0146 -0.0793, -0.0793 -0. | | | | | | | | |
| -0.0864, 0.0132, 0.0631, 0.1129, 0.1627, 0.2125, 0.3122, 0.1440, 0.1439, 0.1438, 0.1448, 0.1464, 0.1467, 0.0447, 0.0447, 0.0447, 0.0447, 0.0447, 0.0583, 0.0550, 0.05527, 0.0514, 0.0219, 0.0219, 0.0220, 0.0228, 0.0228, 0.0224, 0.0222, 0.0221, 0.0220, 0.0219, 0.0220, 0.0220, 0.0220, 0.0221, 0.0220, 0.0224, 0.0221, 0.0224, 0.0224, 0.0224, 0.0224, 0.0224, 0.0224, 0.0224, 0.0224, 0.0224, 0.0226, 0.0244, 0.0284, 0.0284, 0.0284, 0.0326, 0.03301, 0.2906, 0.0339, 0.0393, 0.0393, 0.0393, 0.0393, 0.0393, 0.0394, 0.0349, 0.0346, 0.0346, 0.0346, 0.0346, 0.0346, 0.0346, 0.0346, 0.0346, 0.0 | | | | | | | | |
| MR-Weighted-Median | MR-Egger | | | | | | | |
| MR-Weighted-Median | | | | | | | | |
| MR-Weighted-Median 0.926, -0.1508, -0.0603, -0.0145, 0.0315, 0.0776, 0.1239, 0.2173, 0.0647, 0.06847, 0.0583, 0.0550, 0.0527, 0.0514, 0.0469, 0.0228 0.0224 0.0222 0.0221 0.0220 0.0219 0.0220 0.02173, 0.0649, 0.0220 0.0221 0.0220 0.0219 0.0220 MR-Weighted-Mode 0.618, 0.367, 0.199, 0.173, 0.355, 0.549, 0.693, 0.0339, -0.1636, -0.0720, 0.3394, 0.3240, 0.3268, 0.3301, 0.2906, 1.0469 1.0773 1.0939 1.0998 1.0959 1.1169 1.1571 0.0720, 0.3395, 0.3339, 0.3384, 0.3240, 0.3268, 0.3301, 0.2906, 1.0469 1.0773 1.0939 1.0998 1.0959 1.1169 1.1571 MR-RAPS1 0.244, 0.073, 0.1311, 0.289, 0.516, 0.737, 0.956, 0.0935, 0.0065, 0.0566, 0.1066, 0.1566, 0.2066, 0.3067, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0793 0.0793 0.0793 0.0793 0.0793 0.0794 0.0794 0.0794 0.0794 0.0794 MR-RAPS2 0.485, 0.213, 0.225, 0.287, 0.564, 0.784, 0.976, 0.9320, 0.0903, 0.0903, 0.0905, 0.0801, 0.0807, 0.0866, 0.0934, 0.0629 0.0624 0.0625 0.0622 0.0623 0.0622 0.0626 0.0629 0.0624 0.0625 0.0622 0.0623 0.0622 0.0626 MR-RAPS3 0.995, 0.804, 0.865, 0.917, 0.972, 0.988, 0.998, 0.0136, 0.1308, 0.1304, 0.1304, 0.1296, 0.1271, 0.1120, 0.1288, 0.1304, 0.1304, 0.1304, 0.1296, 0.1271, 0.0146 0.00621, 0.0621, 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, 0.00621, 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, 0.00621, 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, 0.00621, 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, 0.00621 | | | | | | | | |
| -0.1508, -0.0603, -0.0145, 0.0315, 0.0776, 0.1239, 0.2173, 0.0647, 0.0583, 0.0550, 0.0527, 0.0514, 0.0498, 0.0469, 0.0428, 0.0224, 0.0222, 0.0221, 0.0220, 0.0219, 0.0220, 0.0228, 0.0224, 0.0222, 0.0221, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0219, 0.0220, 0.0218, 0.0260, 0.03268, 0.03268, 0.03201, 0.02906, 0.03268, 0.03395, 0.3384, 0.3240, 0.03268, 0.03301, 0.2906, 0.03395, 0.3384, 0.3240, 0.3268, 0.3301, 0.2906, 0.03395, 0.3384, 0.3240, 0.03268, 0.3301, 0.2906, 0.0340, 0.0650, 0.0665, 0.0665, 0.0666, 0.0666, 0.0666, 0.0666, 0.0666, 0.0662, 0.0666, 0.0662, 0.0662, 0.0662, 0.0624, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0794, | | | | | | | | |
| MR-Weighted-Mode | MR-Weighted-Median | | 0.774, | 0.447, | 0.342, | 0.822, | 0.981, | 0.999, |
| MR-Weighted-Mode | | -0.1508, | -0.0603, | -0.0145, | 0.0315, | 0.0776, | 0.1239, | 0.2173, |
| MR-Weighted-Mode 0.618, -0.1636, -0.0720, -0.0274, -0.0231, -0.0761, -0.1206, -0.2167, -0.3395, -0.3384, -0.3244, -0.3246, -0.3268, -0.3301, -0.2906, -0.03395, -0.3384, -0.3244, -0.3246, -0.0931, -0.0988, -0.0998, -0.0935, -0.0065, -0.0956, -0.0566, -0.1066, -0.1566, -0.2066, -0.3067, -0.0935, -0.0065, -0.0566, -0.1066, -0.1566, -0.2066, -0.3067, -0.0850, -0.0849, -0.0849, -0.0849, -0.0849, -0.0849, -0.0849, -0.0934, -0.0793, -0.0793, -0.0793, -0.0794, -0.0794, -0.0794, -0.0794 MR-RAPS2 0.485, -0.213, -0.225, -0.287, -0.564, -0.784, -0.976, -0.1517, -0.0195, -0.0922, -0.0783, -0.1286, -0.1772, -0.2808, -0.9320, -0.0903, -0.0905, -0.0801, -0.0807, -0.0866, -0.0934, -0.0629, -0.0624, -0.0625, -0.0622, -0.0623, -0.0623, -0.0623, -0.0624, -0.1588, -0.1358, -0.1111, -0.0848, -0.1575, -0.2287, -0.2977, -0.4291, -0.1288, -0.1368, -0.0146, -0.00621, -0.0782, -0.1117, -0.1100, -0.0712, -0.0512, -0.0512, -0.1993, -0.00621, -0.0782, -0.1117, -0.1100, -0.0712, -0.0512, -0.1993, -0.00621, -0.0782, -0.1117, -0.1100, -0.0712, -0.0512, -0.1993, -0.00621, -0.0621, -0.0782, -0.1117, -0.1100, -0.0712, -0.0512, -0.0512, -0.1993, -0.00621, -0.0782, -0.1117, -0.1100, -0.0712, -0.0512, -0.0512, -0.0512, -0.0512, -0.0512, -0.0512, -0.00621, -0.0782, -0.1117, -0.1100, -0.0712, -0.0512, -0.0512, -0.0512, -0.0512, -0.0512, -0.0512, -0.0512, -0.0512, -0.0512, -0.051 | | 0.0647, | 0.0583, | 0.0550, | 0.0527, | 0.0514, | 0.0498, | 0.0469, |
| -0.1636, -0.0720, -0.0274, 0.0231, 0.0761, 0.1206, 0.2167, 0.3395, 0.3393, 0.3384, 0.3240, 0.3268, 0.3301, 0.2906, 0.2906, 1.0469 1.0773 1.0939 1.0998 1.0959 1.1169 1.1571 MR-RAPS1 0.244, 0.073, 0.131, 0.289, 0.516, 0.737, 0.956, 0.0850, 0.0850, 0.0865, 0.05666, 0.1066, 0.1566, 0.2066, 0.3067, 0.0850, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0793 0.0793 0.0793 0.0794 0.0794 0.0794 0.0794 0.0794 0.0794 MR-RAPS2 0.485, 0.213, 0.225, 0.287, 0.564, 0.784, 0.976, 0.1517, -0.0195, 0.0292, 0.0783, 0.1286, 0.1772, 0.2808, 0.9320, 0.0903, 0.0905, 0.0801, 0.0807, 0.0866, 0.0934, 0.0629 0.0624 0.0625 0.0622 0.0623 0.0622 0.0626 MR-RAPS3 0.905, 0.804, 0.865, 0.917, 0.972, 0.988, 0.998, 0.1288, 0.1308, 0.1304, 0.1288, 0.1308, 0.1308, 0.1304, 0.1296, 0.1271, 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0148, 0.2364, 0.0621, 0.0782, 0.0111, 0.1100, 0.0570, 0.0570, 0.1048, 0.2364, 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, | | 0.0228 | 0.0224 | 0.0222 | 0.0221 | 0.0220 | 0.0219 | 0.0220 |
| -0.1636, -0.0720, -0.0274, 0.0231, 0.0761, 0.1206, 0.2167, 0.3395, 0.3393, 0.3384, 0.3240, 0.3268, 0.3301, 0.2906, 0.2906, 1.0469 1.0773 1.0939 1.0998 1.0959 1.1169 1.1571 MR-RAPS1 0.244, 0.073, 0.131, 0.289, 0.516, 0.737, 0.956, 0.0850, 0.0850, 0.0865, 0.05666, 0.1066, 0.1566, 0.2066, 0.3067, 0.0850, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0793 0.0793 0.0793 0.0794 0.0794 0.0794 0.0794 0.0794 0.0794 MR-RAPS2 0.485, 0.213, 0.225, 0.287, 0.564, 0.784, 0.976, 0.1517, -0.0195, 0.0292, 0.0783, 0.1286, 0.1772, 0.2808, 0.9320, 0.0903, 0.0905, 0.0801, 0.0807, 0.0866, 0.0934, 0.0629 0.0624 0.0625 0.0622 0.0623 0.0622 0.0626 MR-RAPS3 0.905, 0.804, 0.865, 0.917, 0.972, 0.988, 0.998, 0.1288, 0.1308, 0.1304, 0.1288, 0.1308, 0.1308, 0.1304, 0.1296, 0.1271, 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0148, 0.2364, 0.0621, 0.0782, 0.0111, 0.1100, 0.0570, 0.0570, 0.1048, 0.2364, 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, | MR-Weighted-Mode | 0.618, | 0.367, | 0.199, | 0.173, | 0.355, | 0.549, | 0.693, |
| 0.3395, 0.33384, 0.3240, 0.3268, 0.3301, 0.2906, 1.0469 1.0773 1.0939 1.0998 1.0959 1.1169 1.1571 1.1571 1.0939 1.0939 1.0959 1.0959 1.0950 1.0956, 1.0956, 0.0844, 0.073, 0.0956, 0.0850, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0850, 0.0793 0.0793 0.0793 0.0793 0.0793 0.0794 | Č . | | | | | | | |
| 1.0469 | | | | | 0.3240, | 0.3268, | | 0.2906, |
| MR-RAPS1 0.244, -0.0935, -0.0065, -0.0566, -0.0566, -0.1566, -0.2066, -0.3067, -0.0935, -0.0965, -0.0566, -0.1066, -0.1566, -0.2066, -0.3067, -0.0850, -0.0849, -0.0849, -0.0849, -0.0849, -0.0849, -0.0849, -0.0849, -0.0793, -0.0793, -0.0793, -0.0794, -0.0784, -0.0794, -0.0903, -0.0801, -0.0807, -0.0866, -0.0934, -0.0629, -0.0624, -0.0625, -0.0622, -0.0623, -0.0622, -0.0626, -0.0624, -0.0629, -0.0624, -0.0625, -0.0622, -0.0623, -0.0622, -0.0626, -0.0794, - | | | | | | | | |
| -0.0935, 0.0065, 0.0566, 0.1066, 0.1566, 0.2066, 0.3067, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0850, 0.0793 0.0793 0.0794 0.0783, 0.1286, 0.1772, 0.2808, 0.9320, 0.0903, 0.0905, 0.0801, 0.0807, 0.0866, 0.0934, 0.0629 0.0624 0.0625 0.0622 0.0623 0.0622 0.0626 0.0626 0.0629 0.0624 0.0625 0.0622 0.0623 0.0622 0.0626 0.0626 0.0838, 0.111, 0.0848, 0.1575, 0.2287, 0.2977, 0.4291, 0.1288, 0.1307, 0.1309, 0.1308, 0.1304, 0.1296, 0.1271, 0.0146 0.01 | MR-RAPS1 | | | | | | | |
| 0.0850, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0849, 0.0794 | | | | | | | | |
| 0.0793 0.0793 0.0793 0.0794 0.0794 0.0794 0.0794 0.0794 | | | | | | | | |
| MR-RAPS2 0.485, -0.1517, -0.0195, 0.0292, 0.0783, 0.1286, 0.1772, 0.2808, 0.9320, 0.9033, 0.0905, 0.0801, 0.0807, 0.0866, 0.0934, 0.0629 0.0624 0.0625 0.06622 0.06623 0.0622 0.0626 0.0529, 0.0624 0.0625 0.06622 0.0623 0.0622 0.0626 MR-RAPS3 0.905, 0.804, 0.865, 0.917, 0.972, 0.988, 0.998, -0.1358, 0.111, 0.0848, 0.1575, 0.2287, 0.2977, 0.4291, 0.1288, 0.1304, 0.1304, 0.1296, 0.1271, 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 0.0146 MR-RAPS4 0.998, 0.996, 0.910, 0.425, 0.931, 0.998, 0.998, 0.1906, 0.1906, 0.0570, 0.1048, 0.2364, 0.0621, 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, 0.0793, 0.00512, 0.1993, 0.00512, 0.1993, 0.00521, 0.0512, 0.1993, 0.00521, 0.00512, 0.1993, 0.00520, 0.00521, 0.00512, 0.1993, 0.00520, 0.00521, 0.00521, 0.1993, 0.00520, 0.00520, 0.00521, 0.1993, 0.00520, 0.00520, 0.00520, 0.00520, 0.00520, 0.00520, 0.00520, 0.00520, 0.00520, 0.00521, 0.1993, 0.00520, 0.005 | | | | | | | | |
| -0.1517, -0.0195, 0.0292, 0.0783, 0.1286, 0.1772, 0.2808, 0.9320, 0.0903, 0.0905, 0.0801, 0.0807, 0.0866, 0.0934, 0.0629 0.0624 0.0625 0.0622 0.0623 0.0623 0.0622 0.0626 | MR-RAPS2 | | | | | | | |
| 0.9320, 0.0903, 0.0905, 0.0801, 0.0807, 0.0866, 0.0934, 0.0629 0.0624 0.0625 0.0622 0.0623 0.0622 0.0626 | MIC IO II DZ | | | | | | | |
| 0.0629 0.0624 0.0625 0.0622 0.0623 0.0622 0.0626 | | | | | | | | |
| MR-RAPS3 0.905, 0.804, 0.865, 0.917, 0.972, 0.988, 0.998, 0.1358, 0.0111, 0.0848, 0.1575, 0.2287, 0.2977, 0.4291, 0.1218, 0.1288, 0.1304, 0.1304, 0.1304, 0.1304, 0.1296, 0.1271, 0.0146 | | | | | | | | |
| -0.1358, 0.0111, 0.0848, 0.1575, 0.2287, 0.2977, 0.4291, 0.1288, 0.1307, 0.1309, 0.1308, 0.1304, 0.1296, 0.1271, 0.0146 0.0918, 0.0918, 0.0918, 0.0918, 0.0918, 0.0918, 0.0918, 0.0510, 0.0148, 0.2364, 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, 0.0018, | MD DADC2 | | | | | | | |
| MR-RAPS4 0.1986, -0.1966, -0.0931, -0.0821, 0.0621, 0.0621, 0.0621, 0.0621, 0.0782, 0.0782, 0.0621, 0.0782, 0. | WIK-KAPSS | | | | | | | |
| 0.0146 0 | | | | | | | | |
| MR-RAPS4 0.998, 0.996, 0.910, 0.425, 0.931, 0.998, 1.000, 0.1966, 0.0931, 0.0358, 0.0149, 0.0570, 0.1048, 0.2364, 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, | | | | | | | | |
| -0.1966, -0.0931, -0.0358, 0.0149, 0.0570, 0.1048, 0.2364, 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, | Am Pingi | | | | | | | |
| 0.0621, 0.0782, 0.1117, 0.1100, 0.0712, 0.0512, 0.1993, | MR-RAPS4 | | | | | | | |
| | | | | | | | | |
| 0.0101 0.0100 0.0099 0.0099 0.0099 0.0099 0.0104 | | | | | | | | |
| | | 0.0101 | 0.0100 | 0.0099 | 0.0099 | 0.0099 | 0.0099 | 0.0104 |

Table S113: Simulations with weak invalid IVs: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when $h_y = 0.4$ and $h_u = 0.1$.

| ,(*), 22 (*), | | | y | | -и | | |
|------------------------|----------------|----------|-----------------|-----------------|--------------------|-----------------|-----------------|
| Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
| cML-MA-BIC | 0.995, | 0.979, | 0.767, | 0.173, | 0.799, | 0.982, | 0.999, |
| | -0.1937, | -0.0953, | -0.0466, | 0.0018, | 0.0499, | 0.0995, | 0.1986, |
| | 0.0289, | 0.0258, | 0.0235, | 0.0225, | 0.0238, | 0.0251, | 0.0289, |
| | 0.0156 | 0.0155 | 0.0155 | 0.0155 | 0.0155 | 0.0156 | 0.0157 |
| cML-MA-BIC-DP, T = 200 | 0.920, | 0.850, | 0.473, | 0.035, | 0.527, | 0.904, | 0.968. |
| , | -0.1772, | -0.0870, | -0.0420, | 0.0014, | 0.0454, | 0.0921, | 0.1865, |
| | 0.0361, | 0.0257, | 0.0214, | 0.0191, | 0.0213, | 0.0245, | 0.0313, |
| | 0.0337 | 0.0259 | 0.0222 | 0.0200 | 0.0221 | 0.0246 | 0.0292 |
| MR-Mix | 0.990, | 0.922, | 0.573, | 0.102, | 0.615, | 0.929, | 0.991, |
| | -0.1990, | -0.0988, | -0.0485, | 0.0016, | 0.0516, | 0.1016, | 0.2017, |
| | 0.0263, | 0.0257, | 0.0259, | 0.0259, | 0.0265, | 0.0264, | 0.0268, |
| | 0.0256 | 0.0254 | 0.0269 | 0.0251 | 0.0248 | 0.0258 | 0.0259 |
| MR-ContMix | 1.000. | 0.993. | 0.818, | 0.260, | 0.855, | 0.990, | 1.000, |
| MIC COMMIX | -0.1978, | -0.0984, | -0.0487, | 0.0012, | 0.0510, | 0.1008, | 0.2002, |
| | 0.0249, | 0.0248, | 0.0250, | 0.0251, | 0.0252, | 0.0254, | 0.0258, |
| | NA | NA | NA NA | NA NA | NA | NA NA | NA NA |
| MR-Lasso | 0.988, | 0.916, | 0.636, | 0.260, | 0.865, | 0.993, | 1.000, |
| WIK-Lasso | -0.1827, | -0.0838, | -0.0341, | 0.200, | 0.0651, | 0.1147, | 0.2145, |
| | 0.0390, | 0.0383, | 0.0386, | 0.0382, | 0.0379, | 0.0381, | 0.0394, |
| | 0.0175 | 0.0383, | 0.0174 | 0.0382, | 0.0379, | 0.0381, | 0.0374, |
| MR-PRESSO | 0.856, | 0.670, | 0.0174 | 0.520, | 0.879, | 0.0173 | 0.996, |
| WIK-FKE33O | -0.1394, | -0.0409, | 0.0088, | 0.0585, | 0.1080, | 0.1574, | 0.2567, |
| | 0.0800, | 0.0791, | 0.0088, | 0.0383, | 0.1080, | 0.0783, | 0.2307, |
| | 0.0800, | 0.0791, | 0.0793, | 0.0789, | 0.0780, | 0.0783, | 0.0784, |
| MR-IVW | 0.0242 | 0.0242 | 0.0242 | 0.0242 | 0.0242 | 0.0242 | 0.0244 |
| IVIK-I V W | -0.0932, | 0.0064, | 0.106, | 0.200, | | 0.321, 0.2056, | 0.822, 0.3051, |
| | 0.1091, | 0.1091, | 0.0362, | 0.1000, | 0.1558, 0.1091, | 0.2036, 0.1091, | 0.3031, |
| | 0.1031, | 0.1031, | 0.1031, | 0.1031, | 0.1031, | 0.1031, | 0.1031, |
| MR-IVW-Oracle | 1.000, | 0.1033 | 0.1033 | 0.1033 | 0.1033 | 0.1034 | 1.000, |
| WIK-I V W-Oracle | -0.1985, | -0.0989, | -0.0492, | 0.0006, | 0.0503, | 0.1001, | 0.1996, |
| | 0.0172, | 0.0169, | 0.0168, | 0.0168, | 0.0303, | 0.0168, | 0.0170, |
| | 0.0172, | 0.0105, | 0.0174 | 0.0103, | 0.0174 | 0.0175 | 0.0176 |
| MR-Egger | 0.101, | 0.0173 | 0.087, | 0.124, | 0.195, | 0.267, | 0.454, |
| WIK-Eggei | -0.0867, | 0.0129, | 0.0628, | 0.124, | 0.1624, | 0.2122, | 0.3119, |
| | 0.1873, | 0.0123, | 0.1872, | 0.1120, | 0.1872, | 0.1871, | 0.1871, |
| | 0.1737 | 0.1737 | 0.1737 | 0.1737 | 0.1737 | 0.1738 | 0.1738 |
| MR-Weighted-Median | 0.941, | 0.828, | 0.448, | 0.271, | 0.773, | 0.964, | 0.997, |
| WIK- Weighted-Wedian | -0.1571, | -0.0680, | -0.0227, | 0.0232, | 0.0690, | 0.1153, | 0.2085, |
| | 0.0675, | 0.0580, | 0.0541, | 0.0232, | 0.0090, | 0.0483, | 0.0472, |
| | 0.0233 | 0.0330, | 0.0225 | 0.0313, | 0.0491, | 0.0483, | 0.0472, |
| MR-Weighted-Mode | 0.575, | 0.366, | 0.0223 | 0.166, | 0.299, | 0.473, | 0.645, |
| Mix- weighted-widde | -0.1704, | -0.0765, | -0.0339, | 0.100, | 0.255, | 0.0983, | 0.1921, |
| | 0.3591, | 0.3536, | 0.3342, | 0.3400, | 0.3489, | 0.3429, | 0.3487, |
| | 1.3495 | 1.3530 | 1.3557 | 1.3582 | 1.3552 | 1.3698 | 1.4165 |
| MR-RAPS1 | 0.173, | 0.070, | 0.110, | 0.205, | 0.356, | 0.528, | 0.826, |
| WIN-KAF 51 | -0.0936, | 0.070, | 0.110, | 0.205, 0.1065, | 0.336, | 0.328, 0.2065, | 0.826, |
| | 0.1096, | 0.1096, | 0.1096, | 0.1005, | 0.1096, | 0.1096, | 0.1096, |
| | 0.1030, | 0.1028 | 0.1028 | 0.1028 | 0.1028 | 0.1030, | 0.1028 |
| MR-RAPS2 | 0.377, | 0.210, | 0.198, | 0.224, | 0.422, | 0.618, | 0.879, |
| WIN-KAF 32 | -0.1229, | -0.0263, | 0.198, | 0.224, 0.0791, | 0.422, | 0.018, | 0.879, |
| | 0.1229, | 0.1735, | 0.0274, 0.1032, | 0.0791, | 0.1310, | 0.1811, | 0.2830, |
| | 0.0803 | 0.1733, | 0.0803 | 0.0998, | 0.1038, | 0.0799 | 0.0805 |
| MR-RAPS3 | 0.0803 | 0.0803 | 0.0803 | 0.0802 | 0.0806 | 0.0799 | 0.0803 |
| MK-KAF33 | -0.1952, | -0.0018, | 0.886, | 0.922, 0.2390, | 0.949, | 0.978, 0.4322, | 0.5802, |
| | 0.4104, | 0.5471, | 0.1124, 0.6015, | 1.0189, | 1.3282, | 0.4322, 0.2918, | 0.5802, 0.2460, |
| | 0.4104, 0.0433 | 0.5471, | 0.0015, | 0.5774 | 0.1987 | 0.2918, | 0.2460, |
| MR-RAPS4 | 1.000, | 0.0322 | 0.0421 | 0.3774 | 0.1987 | 0.0241 | 1.000, |
| MK-KAF54 | -0.1990, | -0.0883, | -0.0338, | 0.415, 0.0277, | 0.952, 0.0657, | 0.998, | 0.2256, |
| | 0.1049, | 0.1092, | 0.1397, | 0.0277, 0.1423, | 0.0657, | 0.1060, | 0.2256, 0.1793, |
| | 0.1049, | 0.1092, | 0.1397, | 0.1423, | 0.1178, | 0.0979, | 0.1793, |
| | 0.0103 | 0.0100 | 0.0100 | 0.0100 | 0.0100 | 0.0100 | 0.0104 |

Table S114: Simulations with weak invalid IVs: in each cell, from top to bottom are empirical type-I error/power, mean($\hat{\theta}$), SD($\hat{\theta}$), mean(SE($\hat{\theta}$)) when $h_y = 0.6$ and $h_u = 0.1$.

| $\frac{110011(0),02(0),}{\theta}$ | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
|-----------------------------------|---------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| Methods | | | | | | | |
| cML-MA-BIC | 0.996, | 0.988, | 0.784, | 0.165, | 0.794, | 0.994, | 0.997, |
| | -0.1956, | -0.0970, | -0.0474, | 0.0012, | 0.0497, | 0.0993, | 0.1986, |
| | 0.0284, | 0.0238, | 0.0226, | 0.0217, | 0.0227, | 0.0233, | 0.0264, |
| | 0.0159 | 0.0156 | 0.0156 | 0.0156 | 0.0156 | 0.0157 | 0.0158 |
| cML-MA-BIC-DP, T = 200 | 0.942, | 0.886, | 0.509, | 0.037, | 0.533, | 0.904, | 0.959, |
| | -0.1814, | -0.0894, | -0.0433, | 0.0007, | 0.0451, | 0.0920, | 0.1864, |
| | 0.0346, | 0.0244, | 0.0210, | 0.0188, | 0.0209, | 0.0237, | 0.0309, |
| | 0.0314 | 0.0249 | 0.0218 | 0.0196 | 0.0217 | 0.0242 | 0.0286 |
| MR-Mix | 0.991, | 0.930, | 0.583, | 0.087, | 0.620, | 0.933, | 0.991, |
| | -0.1991, | -0.0988, | -0.0486, | 0.0016, | 0.0515, | 0.1015, | 0.2017, |
| | 0.0253, | 0.0247, | 0.0249, | 0.0247, | 0.0246, | 0.0248, | 0.0252, |
| | 0.0255 | 0.0245 | 0.0243 | 0.0366 | 0.0239 | 0.0243 | 0.0250 |
| MR-ContMix | 0.999, | 0.998, | 0.829, | 0.252, | 0.835, | 1.000, | 1.000, |
| | -0.1977, | -0.0981, | -0.0482, | 0.0015, | 0.0513, | 0.1010, | 0.2005, |
| | 0.0243, | 0.0238, | 0.0236, | 0.0235, | 0.0234, | 0.0236, | 0.0238, |
| | NA | NA | NA | NA | NA | NA | NA |
| MR-Lasso | 0.987, | 0.929, | 0.676, | 0.221, | 0.835, | 0.993, | 1.000, |
| | -0.1863, | -0.0871, | -0.0372, | 0.0126, | 0.0626, | 0.1126, | 0.2118, |
| | 0.0384, | 0.0377, | 0.0373, | 0.0380, | 0.0378, | 0.0378, | 0.0377, |
| | 0.0177 | 0.0176 | 0.0176 | 0.0176 | 0.0177 | 0.0177 | 0.0178 |
| MR-PRESSO | 0.830, | 0.696, | 0.528, | 0.511, | 0.844, | 0.969, | 0.991, |
| | -0.1379, | -0.0393, | 0.0105, | 0.0597, | 0.1087, | 0.1577, | 0.2561, |
| | 0.0932, | 0.0925, | 0.0928, | 0.0923, | 0.0918, | 0.0906, | 0.0894, |
| | 0.0259 | 0.0256 | 0.0256 | 0.0257 | 0.0257 | 0.0256 | 0.0258 |
| MR-IVW | 0.140, | 0.067, | 0.088, | 0.159, | 0.271, | 0.415, | 0.705, |
| | -0.0933, | 0.0063, | 0.0561, | 0.1059, | 0.1557, | 0.2055, | 0.3051, |
| | 0.1289, | 0.1289, | 0.1289, | 0.1289, | 0.1289, | 0.1289, | 0.1290, |
| | 0.1224 | 0.1224 | 0.1224 | 0.1225 | 0.1225 | 0.1225 | 0.1225 |
| MR-IVW-Oracle | 1.000, | 0.998, | 0.818, | 0.038, | 0.819, | 0.999, | 1.000, |
| | -0.1985, | -0.0989, | -0.0492, | 0.0006, | 0.0503, | 0.1001, | 0.1996, |
| | 0.0172, | 0.0169, | 0.0168, | 0.0168, | 0.0167, | 0.0168, | 0.0170, |
| - Im F | 0.0176 | 0.0175 | 0.0174 | 0.0174 | 0.0174 | 0.0175 | 0.0176 |
| MR-Egger | 0.095, | 0.076, | 0.081, | 0.110, | 0.155, | 0.220, | 0.348, |
| | -0.0869, 0.2223, | 0.0127, 0.2223, | 0.0625, 0.2223, | 0.1124, 0.2222, | 0.1622, 0.2222, | 0.2120, 0.2222, | 0.3116, 0.2222, |
| | 0.2223, | 0.2223, | 0.2223, | 0.2222, | 0.2222, | 0.2222, | 0.2222, |
| MD Waighted Medica | 0.2038 | 0.2038 | 0.2038 | 0.2038 | 0.2039 | 0.2039 | 0.2039 |
| MR-Weighted-Median | -0.1619, | -0.0728, | -0.0273, | 0.245, 0.0183, | 0.739, 0.0645, | 0.954, 0.1105, | 0.993, |
| | 0.0686, | 0.0583, | 0.0555, | 0.0183, | 0.0043, | 0.1103, | 0.2030, |
| | 0.0036 | 0.0383, | 0.0333, | 0.0334, | 0.0319, | 0.0493, | 0.0484, |
| MR-Weighted-Mode | 0.550, | 0.339, | 0.200, | 0.160, | 0.0224 | 0.440, | 0.627, |
| WIK-Weighted-Wiode | -0.1718, | -0.0669, | -0.0152, | 0.0234, | 0.270, | 0.1162, | 0.2027, |
| | 0.4068, | 0.4114, | 0.4135, | 0.4037, | 0.3903, | 0.3854, | 0.3928, |
| | 1.5883 | 1.6090 | 1.6105 | 1.6022 | 1.5991 | 1.6165 | 1.6543 |
| MR-RAPS1 | 0.147, | 0.069, | 0.091, | 0.163, | 0.279, | 0.423, | 0.707, |
| Mil Oi | -0.0937, | 0.0063, | 0.0564, | 0.1064, | 0.1564, | 0.2064, | 0.3065, |
| | 0.1296, | 0.1296, | 0.1296, | 0.1296, | 0.1296, | 0.1296, | 0.1296, |
| | 0.1218 | 0.1218 | 0.1218 | 0.1218 | 0.1218 | 0.1218 | 0.1218 |
| MR-RAPS2 | 0.332, | 0.204, | 0.176, | 0.190, | 0.348, | 0.503, | 0.783, |
| | -0.1226, | -0.0244, | 0.0264, | 0.0782, | 0.1285, | 0.1791, | 0.2809, |
| | 0.1175, | 0.1195, | 0.1152, | 0.1199, | 0.1298, | 0.1255, | 0.1351, |
| | 0.0949 | 0.0945 | 0.0947 | 0.0947 | 0.0944 | 0.0950 | 0.0948 |
| MR-RAPS3 | 0.906, | 0.857, | 0.898, | 0.918, | 0.947, | 0.958, | 0.992, |
| | -0.4046, | 2.3722, | 0.3082, | 1.6598, | 0.4372, | 0.5583, | 0.8442, |
| | 4.5092, | 74.5197, | 4.0494, | 39.1988, | 4.3331, | 5.8561, | 0.5724, |
| | 2.0607 | 769.0805 | 0.8431 | 36.9932 | 0.9291 | 1.4798 | 0.0473 |
| MR-RAPS4 | 1.000, | 0.998, | 0.926, | 0.480, | 0.944, | 1.000, | 0.999, |
| | -0.2004, | -0.0789, | -0.0140, | 0.0309, | 0.0873, | 0.1306, | 0.2198, |
| | 0.1303, | 0.1614, | 0.1828, | 0.2152, | 0.2288, | 0.2075, | 0.1919, |
| | 0.0105 | 0.0102 | 0.0102 | 0.0103 | 0.0104 | 0.0104 | 0.0106 |
| | | | | | | | |

Table S115: Relative frequencies of goodness-of-fit tests' rejecting the null at p-value cutoff 0.05 when $h_y = 0.1$ and $h_u = 0$.

| θ Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
|---------------|-------|-------|-------|-------|-------|-------|-------|
| GOF1, T = 100 | 0.941 | 0.950 | 0.946 | 0.898 | 0.942 | 0.952 | 0.949 |
| GOF2, T = 100 | 0.965 | 0.958 | 0.954 | 0.906 | 0.948 | 0.958 | 0.966 |
| GOF1, T = 200 | 0.976 | 0.987 | 0.986 | 0.967 | 0.981 | 0.984 | 0.981 |
| GOF2, T = 200 | 0.987 | 0.988 | 0.989 | 0.969 | 0.983 | 0.989 | 0.990 |
| GOF1, T = 500 | 0.998 | 0.998 | 0.999 | 0.996 | 1.000 | 1.000 | 0.999 |
| GOF2, T = 500 | 0.999 | 0.999 | 0.999 | 0.997 | 1.000 | 1.000 | 0.999 |

Table S116: Relative frequencies of goodness-of-fit tests' rejecting the null at p-value cutoff 0.05 when $h_y = 0.2$ and $h_u = 0$.

| Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
|---------------|-------|-------|-------|-------|-------|-------|-------|
| GOF1, T = 100 | 0.915 | 0.926 | 0.915 | 0.819 | 0.906 | 0.919 | 0.901 |
| GOF2, T = 100 | 0.935 | 0.936 | 0.921 | 0.833 | 0.909 | 0.934 | 0.941 |
| GOF1, T = 200 | 0.971 | 0.982 | 0.980 | 0.947 | 0.973 | 0.977 | 0.965 |
| GOF2, T = 200 | 0.981 | 0.985 | 0.982 | 0.953 | 0.971 | 0.978 | 0.984 |
| GOF1, T = 500 | 0.995 | 0.996 | 0.994 | 0.977 | 0.987 | 0.992 | 0.992 |
| GOF2, T = 500 | 0.996 | 0.997 | 0.994 | 0.979 | 0.987 | 0.992 | 0.995 |

Table S117: Relative frequencies of goodness-of-fit tests' rejecting the null at p-value cutoff 0.05 when $h_y = 0.4$ and $h_u = 0$.

| θ Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
|---------------|-------|-------|-------|-------|-------|-------|-------|
| GOF1, T = 100 | 0.817 | 0.829 | 0.804 | 0.669 | 0.810 | 0.840 | 0.819 |
| GOF2, T = 100 | 0.867 | 0.847 | 0.813 | 0.697 | 0.821 | 0.864 | 0.876 |
| GOF1, T = 200 | 0.912 | 0.929 | 0.916 | 0.846 | 0.917 | 0.929 | 0.930 |
| GOF2, T = 200 | 0.929 | 0.930 | 0.917 | 0.867 | 0.928 | 0.942 | 0.954 |
| GOF1, T = 500 | 0.976 | 0.975 | 0.969 | 0.940 | 0.975 | 0.977 | 0.979 |
| GOF2, T = 500 | 0.979 | 0.976 | 0.972 | 0.946 | 0.976 | 0.982 | 0.983 |

Table S118: Relative frequencies of goodness-of-fit tests' rejecting the null at p-value cutoff 0.05 when $h_v = 0.6$ and $h_u = 0$.

| Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
|---------------|-------|-------|-------|-------|-------|-------|-------|
| GOF1, T = 100 | 0.746 | 0.766 | 0.731 | 0.579 | 0.737 | 0.764 | 0.756 |
| GOF2, T = 100 | 0.809 | 0.795 | 0.735 | 0.595 | 0.754 | 0.786 | 0.808 |
| GOF1, T = 200 | 0.872 | 0.885 | 0.867 | 0.764 | 0.874 | 0.889 | 0.878 |
| GOF2, T = 200 | 0.900 | 0.904 | 0.878 | 0.787 | 0.881 | 0.901 | 0.909 |
| GOF1, T = 500 | 0.944 | 0.948 | 0.942 | 0.900 | 0.942 | 0.960 | 0.952 |
| GOF2, T = 500 | 0.955 | 0.952 | 0.945 | 0.902 | 0.947 | 0.963 | 0.964 |

Table S119: Relative frequencies of goodness-of-fit tests' rejecting the null at p-value cutoff 0.05 with T = 200 when $h_u = 0.1$.

| θ Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
|-------------------|-------|-------|-------|-------|-------|-------|-------|
| GOF1, $h_V = 0.1$ | 0.983 | 0.989 | 0.982 | 0.939 | 0.976 | 0.978 | 0.973 |
| GOF2, $h_v = 0.1$ | 0.995 | 0.991 | 0.981 | 0.947 | 0.978 | 0.979 | 0.980 |
| GOF1, $h_y = 0.2$ | 0.955 | 0.969 | 0.958 | 0.887 | 0.941 | 0.943 | 0.938 |
| GOF2, $h_y = 0.2$ | 0.980 | 0.976 | 0.965 | 0.898 | 0.947 | 0.953 | 0.956 |
| GOF1, $h_y = 0.4$ | 0.915 | 0.923 | 0.902 | 0.815 | 0.887 | 0.901 | 0.893 |
| GOF2, $h_y = 0.4$ | 0.949 | 0.940 | 0.911 | 0.828 | 0.899 | 0.922 | 0.922 |
| GOF1, $h_y = 0.6$ | 0.887 | 0.886 | 0.854 | 0.758 | 0.840 | 0.869 | 0.851 |
| GOF2, $h_y = 0.6$ | 0.906 | 0.898 | 0.862 | 0.771 | 0.852 | 0.891 | 0.885 |

Table S120: Simulation results with valid and weaker IVs and $h_y = 0.2$, $h_u = 0$.

| Methods | -0.2 | -0.1 | -0.05 | 0 | 0.05 | 0.1 | 0.2 |
|------------------------|----------|----------|----------|---------|---------|---------|---------|
| cML-MA-BIC | 1.000, | 1.000, | 0.823, | 0.054, | 0.828, | 0.998, | 1.000, |
| | -0.1991, | -0.0992, | -0.0492, | 0.0007, | 0.0504, | 0.1004, | 0.2004, |
| | 0.0176, | 0.0173, | 0.0173, | 0.0171, | 0.0173, | 0.0174, | 0.0176, |
| | 0.0171 | 0.0169 | 0.0168 | 0.0168 | 0.0168 | 0.0169 | 0.0171 |
| cML-BIC | 1.000, | 0.999, | 0.835, | 0.057, | 0.835, | 0.999, | 1.000, |
| | -0.1993, | -0.0993, | -0.0493, | 0.0006, | 0.0506, | 0.1005, | 0.2005, |
| | 0.0177, | 0.0175, | 0.0174, | 0.0173, | 0.0174, | 0.0174, | 0.0177, |
| | 0.0169 | 0.0166 | 0.0165 | 0.0165 | 0.0165 | 0.0166 | 0.0168 |
| cML-MA-BIC-DP, T = 200 | 1.000, | 0.996, | 0.698, | 0.027, | 0.733, | 0.996, | 1.000, |
| | -0.1965, | -0.0969, | -0.0472, | 0.0007, | 0.0487, | 0.0984, | 0.1980, |
| | 0.0176, | 0.0175, | 0.0172, | 0.0163, | 0.0172, | 0.0174, | 0.0176, |
| | 0.0195 | 0.0192 | 0.0190 | 0.0182 | 0.0189 | 0.0191 | 0.0193 |
| cML-BIC-DP, T = 200 | 1.000, | 0.997, | 0.712, | 0.034, | 0.750, | 0.994, | 1.000, |
| | -0.1968, | -0.0972, | -0.0474, | 0.0007, | 0.0489, | 0.0987, | 0.1983, |
| | 0.0179, | 0.0176, | 0.0174, | 0.0165, | 0.0174, | 0.0176, | 0.0177, |
| | 0.0190 | 0.0189 | 0.0187 | 0.0180 | 0.0185 | 0.0187 | 0.0188 |
| GOF1, T = 200 | 0.063 | 0.066 | 0.065 | 0.054 | 0.062 | 0.065 | 0.057 |
| GOF2, T = 200 | 0.059 | 0.06 | 0.061 | 0.053 | 0.056 | 0.056 | 0.051 |

Table S121: Comparison of computational times (in seconds) of different MR methods as averaged over 10 simulations for m IV s.

| Methods | 10 | 20 | 50 | 70 | 100 |
|-------------------------------|---------|---------|----------|----------|---------|
| cML-MA-BIC, 0 Random Start | 0.0151 | 0.0272 | 0.0964 | 0.1548 | 0.2282 |
| cML-MA-BIC, 5 Random Start | 0.2237 | 0.6305 | 1.7965 | 2.7234 | 4.0821 |
| cML-MA-BIC-DP, 0 Random Start | 1.5327 | 3.0729 | 10.9926 | 15.803 | 24.9949 |
| cML-MA-BIC-DP, 5 Random Start | 18.5582 | 53.7983 | 170.9803 | 267.4588 | 408.589 |
| MR-Mix | 3.6973 | 4.667 | 6.1285 | 6.7372 | 7.6673 |
| MR-ContMix | 0.1198 | 0.1327 | 0.1695 | 0.2237 | 0.2388 |
| MR-Lasso | 0.0386 | 0.041 | 0.0536 | 0.0582 | 0.0673 |
| MR-PRESSO | 3.4478 | 5.5814 | 11.6707 | 15.9898 | 22.4874 |
| MR-IVW | 0.0012 | 0.001 | 0.0011 | 0.0011 | 0.001 |
| MR-Egger | 0.0012 | 0.0016 | 0.0014 | 0.0017 | 0.0013 |
| MR-Weighted-Median | 0.0489 | 0.0531 | 0.0582 | 0.0632 | 0.0697 |
| MR-Weighted-Mode | 2.3047 | 2.2967 | 2.3596 | 2.3546 | 2.3933 |
| MR-RAPS | 0.0809 | 0.1237 | 0.1035 | 0.2068 | 0.1276 |

Supplemental Methods and Results

S1 Proof of Theorem 1

Theorem 1. With Assumptions 1 and 2 satisfied, if $K_0 \in \mathcal{K}$, we have $P(\hat{K} = K_0) \to 1$ and $P(\hat{B}_{\hat{K}} = B_0) \to 1$ as $N_1, N_2 \to \infty$.

Proof. First, we show $P(\hat{B}_{K_0} = B_0) \to 1$, which is equivalent to show for any $B_1 \subseteq \{1, \dots, m\}$ such that $|B_1| = K_0$ and $B_1 \neq B_0$, $P(\hat{B}_{K_0} = B_1) \to 0$ as $N_1, N_2 \to \infty$. We have

$$\begin{split} &P(\hat{B}_{K_0} = B_1) \\ &\leq P(\min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in B_1^c} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta}\tilde{b}_{Xi})^2}{\hat{\sigma}_{Yi}^2} \right) \leq \min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in B_0^c} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta}\tilde{b}_{Xi})^2}{\hat{\sigma}_{Yi}^2} \right)) \\ &\leq P(\min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in B_1^c} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta}\tilde{b}_{Xi})^2}{\hat{\sigma}_{Yi}^2} \right) \leq \sum_{i \in B_0^c} \left(\frac{(\hat{\beta}_{Xi} - \beta_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \theta\beta_{Xi})^2}{\hat{\sigma}_{Yi}^2} \right)). \end{split}$$

Note that, for $i \in B_0^c$, $\frac{\hat{\beta}_{Xi} - \beta_{Xi}}{\hat{\sigma}_{Xi}} \sim N(0,1)$ and $\frac{\hat{\beta}_{Yi} - \theta_{Xi}}{\hat{\sigma}_{Yi}} \sim N(0,1)$. So for any $\varepsilon > 0$, there exists C > 0 such that

$$P\left(\sum_{i \in B_0^c} \left(\frac{(\hat{\beta}_{Xi} - \beta_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \theta \beta_{Xi})^2}{\hat{\sigma}_{Yi}^2} \right) > C\right) < \frac{\varepsilon}{2}.$$
(1)

And we have

$$\begin{split} &P(\min_{\tilde{\theta},\tilde{b}_{Xi}}\sum_{i\in B_1^c}\left(\frac{(\hat{\beta}_{Xi}-\tilde{b}_{Xi})^2}{\hat{\sigma}_{Xi}^2}+\frac{(\hat{\beta}_{Yi}-\tilde{\theta}\tilde{b}_{Xi})^2}{\hat{\sigma}_{Yi}^2}\right)\leq\sum_{i\in B_0^c}\left(\frac{(\hat{\beta}_{Xi}-\beta_{Xi})^2}{\hat{\sigma}_{Xi}^2}+\frac{(\hat{\beta}_{Yi}-\theta\beta_{Xi})^2}{\hat{\sigma}_{Yi}^2}\right))\\ &\leq P(\min_{\tilde{\theta},\tilde{b}_{Xi}}\sum_{i\in B_1^c}\left(\frac{(\hat{\beta}_{Xi}-\tilde{b}_{Xi})^2}{\hat{\sigma}_{Xi}^2}+\frac{(\hat{\beta}_{Yi}-\tilde{\theta}\tilde{b}_{Xi})^2}{\hat{\sigma}_{Yi}^2}\right)\leq C)+P(\sum_{i\in B_0^c}\left(\frac{(\hat{\beta}_{Xi}-\beta_{Xi})^2}{\hat{\sigma}_{Xi}^2}+\frac{(\hat{\beta}_{Yi}-\theta\beta_{Xi})^2}{\hat{\sigma}_{Yi}^2}\right)>C). \end{split}$$

After profiling out \tilde{b}_{Xi} 's, we get

$$\min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in B_1^c} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta} \tilde{b}_{Xi})^2}{\hat{\sigma}_{Yi}^2} \right) = \min_{\tilde{\theta}} \sum_{i \in B_1^c} \frac{(\hat{\beta}_{Yi} - \tilde{\theta} \cdot \hat{\beta}_{Xi})^2}{\hat{\sigma}_{Yi}^2 + \tilde{\theta}^2 \hat{\sigma}_{Xi}^2},$$

so

$$\begin{split} &P(\min_{\tilde{\theta},\tilde{b}_{Xi}}\sum_{i\in B_{1}^{c}}\left(\frac{(\hat{\beta}_{Xi}-\tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Xi}^{2}}+\frac{(\hat{\beta}_{Yi}-\tilde{\theta}\tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Yi}^{2}}\right)\leq C)\\ &=P(\min_{\tilde{\theta}}\sum_{i\in B^{c}}\frac{(\hat{\beta}_{Yi}-\tilde{\theta}\cdot\hat{\beta}_{Xi})^{2}}{\hat{\sigma}_{Yi}^{2}+\tilde{\theta}^{2}\hat{\sigma}_{Xi}^{2}}\leq C). \end{split}$$

We have $\frac{\hat{\beta}_{Yi} - \tilde{\theta} \cdot \hat{\beta}_{Xi}}{\sqrt{\hat{\sigma}_{Yi}^2 + \tilde{\theta}^2 \hat{\sigma}_{Xi}^2}} \sim N(\frac{\theta \cdot \beta_{Xi} + r_i - \tilde{\theta} \cdot \beta_{Xi}}{\sqrt{\hat{\sigma}_{Yi}^2 + \tilde{\theta}^2 \hat{\sigma}_{Xi}^2}}, 1)$, so $\sum_{i \in B_1^c} \frac{(\hat{\beta}_{Yi} - \tilde{\theta} \cdot \hat{\beta}_{Xi})^2}{\hat{\sigma}_{Yi}^2 + \tilde{\theta}^2 \hat{\sigma}_{Xi}^2}$ follows non-central χ^2 distribution with degrees of freedom $(m - K_0)$ and non-centrality parameter $\lambda_{\tilde{\theta}}$ depending on $\tilde{\theta}$

$$\lambda_{ ilde{ heta}} = \sum_{i \in B_i^c} rac{(heta \cdot eta_{Xi} + r_i - ilde{ heta} \cdot eta_{Xi})^2}{\hat{\sigma}_{Yi}^2 + ilde{ heta}^2 \hat{\sigma}_{Xi}^2}.$$

With Assumption 2, we get

$$\lambda_{\tilde{\theta}} \geq \sum_{i \in B_1^c} \frac{(\theta \cdot \beta_{Xi} + r_i - \tilde{\theta} \cdot \beta_{Xi})^2}{\frac{u_Y}{N_2} + \tilde{\theta}^2 \cdot \frac{u_X}{l_N \cdot N_2}} = N_2 \cdot \sum_{i \in B_1^c} \frac{(\theta \cdot \beta_{Xi} + r_i - \tilde{\theta} \cdot \beta_{Xi})^2}{u_Y + \tilde{\theta}^2 \cdot \frac{u_X}{l_N}}.$$

With Assumption 1, we know

$$\min_{\tilde{\theta}} \sum_{i \in B_i^c} \frac{(\theta \cdot \beta_{Xi} + r_i - \tilde{\theta} \cdot \beta_{Xi})^2}{u_Y + \tilde{\theta}^2 \cdot \frac{u_X}{l_N}} = v > 0,$$

here v is a constant. This is because, with Assumption 1, there is no $\tilde{\theta}$ making $\theta \cdot \beta_{Xi} + r_i - \tilde{\theta} \cdot \beta_{Xi} = 0$ for all $i \in B_1^c$ simultaneously. So we have $\min_{\tilde{\theta}} \lambda_{\tilde{\theta}} \geq N_2 \cdot v$. Then as N_2 large enough, we have

$$P(\min_{\tilde{\theta}} \sum_{i \in B_i^c} \frac{(\hat{\beta}_{Yi} - \tilde{\theta} \cdot \hat{\beta}_{Xi})^2}{\hat{\sigma}_{Yi}^2 + \tilde{\theta}^2 \hat{\sigma}_{Xi}^2} \le C) \le \frac{\varepsilon}{2}.$$
 (2)

Combining (1) and (2), we get $P(\hat{B}_{K_0} = B_0) \to 1$ as $N_1, N_2 \to \infty$.

Next, we show $P(\hat{K} = K_0) \rightarrow 1$. For any $K_1 < K_0$, we have

$$\begin{split} P(\hat{K} = K_1) &\leq P\left(\mathrm{BIC}(K_1) \leq \mathrm{BIC}(K_0)\right) \\ &= P\left(-2 \cdot L\left(\hat{\theta}(K_1), \hat{b}_{Xi}(K_1), \hat{r}_i(K_1)\right) + \log(N) \cdot K_1 \leq -2 \cdot L\left(\hat{\theta}(K_0), \hat{b}_{Xi}(K_0), \hat{r}_i(K_0)\right) + \log(N) \cdot K_0\right) \\ &= P\left(2 \cdot L\left(\hat{\theta}(K_0), \hat{b}_{Xi}(K_0), \hat{r}_i(K_0)\right) - 2 \cdot L\left(\hat{\theta}(K_1), \hat{b}_{Xi}(K_1), \hat{r}_i(K_1)\right) \leq \log(N)(K_0 - K_1)\right). \end{split}$$

As we have shown $P(\hat{B}_{K_0} = B_0) \to 1$, with probability goes to 1 we have

$$\begin{split} & 2 \cdot L\left(\hat{\theta}(K_{0}), \hat{b}_{Xi}(K_{0}), \hat{r}_{i}(K_{0})\right) - 2 \cdot L\left(\hat{\theta}(K_{1}), \hat{b}_{Xi}(K_{1}), \hat{r}_{i}(K_{1})\right) \\ &= \min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in \hat{B}_{K_{1}}^{c}} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Xi}^{2}} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta}\tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Yi}^{2}}\right) - \min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in B_{0}^{c}} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Xi}^{2}} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta}\tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Yi}^{2}}\right) \\ &\geq \min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in \hat{B}_{K_{1}}^{c}} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Xi}^{2}} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta}\tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Yi}^{2}}\right) - \sum_{i \in B_{0}^{c}} \left(\frac{(\hat{\beta}_{Xi} - \beta_{Xi})^{2}}{\hat{\sigma}_{Xi}^{2}} + \frac{(\hat{\beta}_{Yi} - \theta\beta_{Xi})^{2}}{\hat{\sigma}_{Yi}^{2}}\right). \end{split}$$

Then we get

$$\begin{split} &P(\hat{K} = K_{1}) \\ &\leq P\left(\min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in \hat{B}_{K_{1}}^{c}} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Xi}^{2}} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta}\tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Yi}^{2}}\right) \leq \sum_{i \in B_{0}^{c}} \left(\frac{(\hat{\beta}_{Xi} - \beta_{Xi})^{2}}{\hat{\sigma}_{Xi}^{2}} + \frac{(\hat{\beta}_{Yi} - \theta\beta_{Xi})^{2}}{\hat{\sigma}_{Yi}^{2}}\right) + \log(N)(K_{0} - K_{1})\right) \\ &\leq \sum_{|B| = K_{1}} P\left(\min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in B^{c}} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Xi}^{2}} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta}\tilde{b}_{Xi})^{2}}{\hat{\sigma}_{Yi}^{2}}\right) \leq \sum_{i \in B_{0}^{c}} \left(\frac{(\hat{\beta}_{Xi} - \beta_{Xi})^{2}}{\hat{\sigma}_{Xi}^{2}} + \frac{(\hat{\beta}_{Yi} - \theta\beta_{Xi})^{2}}{\hat{\sigma}_{Yi}^{2}}\right) + \log(N)(K_{0} - K_{1}).\right) \end{split}$$

Similar as above, we get

$$\min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in B^c} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta} \tilde{b}_{Xi})^2}{\hat{\sigma}_{Yi}^2} \right) = \min_{\tilde{\theta}} \sum_{i \in B^c} \frac{(\hat{\beta}_{Yi} - \tilde{\theta} \cdot \hat{\beta}_{Xi})^2}{\hat{\sigma}_{Yi}^2 + \tilde{\theta}^2 \hat{\sigma}_{Xi}^2},$$

and $\sum_{i \in B^c} \frac{(\hat{\beta}_{Yi} - \tilde{\theta} \cdot \hat{\beta}_{Xi})^2}{\hat{\sigma}_{Yi}^2 + \tilde{\theta}^2 \hat{\sigma}_{Xi}^2}$ follows non-central χ^2 distribution with degrees of freedom $(m - K_1)$ and non-centrality parameter $\lambda_{\tilde{\theta}}$ depending on $\tilde{\theta}$

$$\lambda_{ ilde{ heta}} = \sum_{i \in B^c} rac{(heta \cdot eta_{Xi} + r_i - ilde{ heta} \cdot eta_{Xi})^2}{\hat{\sigma}_{Yi}^2 + ilde{ heta}^2 \hat{\sigma}_{Xi}^2}.$$

Similarly, since $K_1 < K_0$, with Assumption 2 we have $\lambda_{\tilde{\theta}} \ge N_2 \cdot v$ for some constant v, so for any $|B| = K_1$, we get

$$P\left(\min_{\tilde{\theta},\tilde{b}_{Xi}}\sum_{i\in B^c}\left(\frac{(\hat{\beta}_{Xi}-\tilde{b}_{Xi})^2}{\hat{\sigma}_{Xi}^2}+\frac{(\hat{\beta}_{Yi}-\tilde{\theta}\tilde{b}_{Xi})^2}{\hat{\sigma}_{Yi}^2}\right)\leq \sum_{i\in B_0^c}\left(\frac{(\hat{\beta}_{Xi}-\beta_{Xi})^2}{\hat{\sigma}_{Xi}^2}+\frac{(\hat{\beta}_{Yi}-\theta\beta_{Xi})^2}{\hat{\sigma}_{Yi}^2}\right)+\log\left(N\right)(K_0-K_1)\right)\to 0.$$

This gives us $P(\hat{K} = K_1) \to 0$ for any $K_1 < K_0$. For any $K_1 > K_0$, we have

$$P(\hat{K}=K_1)$$

$$\leq P\left(\log(N)(K_1 - K_0) \leq \sum_{i \in B_0^c} \left(\frac{(\hat{\beta}_{Xi} - \beta_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \theta \beta_{Xi})^2}{\hat{\sigma}_{Yi}^2}\right) - \min_{\tilde{\theta}, \tilde{b}_{Xi}} \sum_{i \in \hat{B}_{K_1}^c} \left(\frac{(\hat{\beta}_{Xi} - \tilde{b}_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \tilde{\theta} \tilde{b}_{Xi})^2}{\hat{\sigma}_{Yi}^2}\right)\right)$$

$$\leq P\left(\log(N)(K_1 - K_0) \leq \sum_{i \in B_0^c} \left(\frac{(\hat{\beta}_{Xi} - \beta_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \theta \beta_{Xi})^2}{\hat{\sigma}_{Yi}^2}\right)\right)$$

Since $\sum_{i \in B_0^c} \left(\frac{(\hat{\beta}_{Xi} - \beta_{Xi})^2}{\hat{\sigma}_{Xi}^2} + \frac{(\hat{\beta}_{Yi} - \theta\beta_{Xi})^2}{\hat{\sigma}_{Yi}^2} \right)$ is a central χ^2 distribution with degrees of freedom $2(m - K_0)$, we get $P(\hat{K} = K_1) \to 0$ for any $K_1 > K_0$. So we have $P(\hat{K} = K_0) \to 1$ as $N_1, N_2 \to \infty$.

S2 Standard Error of $\hat{\theta}$

For any given K, denote the index set of K non-zero \hat{r}_i 's as \hat{B}_K . The (m-K+1) by (m-K+1) Fisher information matrix is

$$\mathscr{I} = \begin{pmatrix} \frac{\partial^2(-l)}{\partial \theta^2} & \frac{\partial^2(-l)}{\partial \theta \partial \beta_{XB}'} \\ \frac{\partial^2(-l)}{\partial \theta \partial \beta_{XB}} & \frac{\partial^2(-l)}{\partial \beta_{XB} \partial \beta_{XB}'} \end{pmatrix}, \tag{3}$$

where β_{XB} is a vector of elements β_{Xi} with $i \in \hat{B}_K^c$. Plug $\hat{\theta}$, \hat{b}_{Xi} 's into \mathscr{I} , we obtain the standard error of $\hat{\theta}$ as $SE(\hat{\theta}) = \sqrt{(\mathscr{I}^{-1})_{11}}$.

We have

$$\frac{\partial^{2}(-l)}{\partial \theta^{2}}\Big|_{\hat{\theta},\hat{b}_{Xi}} = \sum_{i \in \hat{B}_{K}^{c}} \frac{\hat{b}_{Xi}^{2}}{\hat{\sigma}_{Yi}^{2}},$$

$$\frac{\partial^{2}(-l)}{\partial \beta_{Xi}^{2}}\Big|_{\hat{\theta},\hat{b}_{Xi}} = \frac{1}{\hat{\sigma}_{Xi}^{2}} + \frac{\hat{\theta}^{2}}{\hat{\sigma}_{Yi}^{2}}$$

$$\frac{\partial^{2}(-l)}{\partial \theta \partial \beta_{Xi}}\Big|_{\hat{\theta},\hat{b}_{Xi}} = \frac{2\hat{b}_{Xi}\hat{\theta} - \hat{\beta}_{Yi}}{\hat{\sigma}_{Yi}^{2}}.$$
(4)

And

$$SE(\hat{\theta}) = \sqrt{(\mathscr{I}^{-1})_{11}} = \frac{1}{V},$$

$$V = \sum_{i \in \hat{B}_{K}^{c}} \frac{\hat{b}_{Xi}^{2}}{\hat{\sigma}_{Yi}^{2}} - \sum_{i \in \hat{B}_{K}^{c}} \left(\frac{2\hat{b}_{Xi}\hat{\theta} - \hat{\beta}_{Yi}}{\hat{\sigma}_{Yi}^{2}}\right)^{2} \cdot \frac{1}{\frac{1}{\hat{\sigma}_{Xi}^{2}} + \frac{\hat{\theta}^{2}}{\hat{\sigma}_{Yi}^{2}}}.$$
(5)

From our Assumption 2, we get N_1, N_2 are O(N) for some N, and $\hat{\sigma}_{Xi}^2$, $\hat{\sigma}_{Yi}^2$ are both O(1/N). And as $N \to \infty$, $\hat{\beta}_{Xi} \to \beta_{Xi}$ with probability 1, and from the IV Assumption A1 we have $\beta_{Xi} \neq 0$. So in Theorem 3.3 of [13], as $N_1, N_2 \to \infty$, i.e. $N \to \infty$, $\hat{\sigma}_{Xi}$ and $\hat{\sigma}_{Yi}$ are both $o_p(\hat{\beta}_{Xi})$, we have asymptotic variance of $\hat{\theta}$ as $1/V^*$ and

$$V^* = \sum_{i \in \hat{B}_V^c} \frac{\hat{\beta}_{Xi}^2 \hat{\sigma}_{Yi}^2 + \hat{\beta}_{Yi}^2 \hat{\sigma}_{Xi}^2}{(\hat{\theta}^2 \hat{\sigma}_{Xi}^2 + \hat{\sigma}_{Yi}^2)^2}.$$
 (6)

Since we have

$$\hat{b}_{Xi} = \frac{\frac{\hat{\beta}_{Xi}}{\hat{\sigma}_{Xi}^2} + \frac{\hat{\theta}\hat{\beta}_{Yi}}{\hat{\sigma}_{Yi}^2}}{\frac{1}{\hat{\sigma}_{Yi}^2} + \frac{\hat{\theta}^2}{\hat{\sigma}_{Yi}^2}}.$$
(7)

Plug (7) in (5), we get

$$V - V^* = \sum_{i \in \hat{B}_K^c} -\frac{4\hat{\sigma}_{Xi}^2 \hat{\sigma}_{Yi}^2 (\hat{\beta}_{Yi} - \hat{\theta} \hat{\beta}_{Xi})^2}{(\hat{\theta}^2 \hat{\sigma}_{Xi}^2 + \hat{\sigma}_{Yi}^2)^3} + \frac{2\hat{\sigma}_{Xi}^2 \hat{\beta}_{Yi} (\hat{\beta}_{Yi} - \hat{\theta} \hat{\beta}_{Xi})}{(\hat{\theta}^2 \hat{\sigma}_{Xi}^2 + \hat{\sigma}_{Yi}^2)^2}.$$
 (8)

With our Theorem 1 we have $P(\hat{K} = K_0) \to 1$ and $P(\hat{B}_{\hat{K}} = B_0) \to 1$, and when $\hat{B}_{\hat{K}} = B_0$, we have $\hat{\beta}_{Yi} - \hat{\theta}\hat{\beta}_{Xi} \to 0$ for $i \in \hat{B}^c_{\hat{K}}$. For the first part in (8), divided by the corresponding part in (6), because $\hat{\sigma}^2_{Xi}, \hat{\sigma}^2_{Yi}, \hat{\theta}^2\hat{\sigma}^2_{Xi} + \hat{\sigma}^2_{Yi}, \hat{\beta}^2_{Xi}\hat{\sigma}^2_{Yi} + \hat{\beta}^2_{Yi}\hat{\sigma}^2_{Xi}$ are all $O_p(1/N)$ and $\hat{\beta}_{Yi} - \hat{\theta}\hat{\beta}_{Xi} \to 0$, we get

$$-\frac{4\hat{\sigma}_{Xi}^2\hat{\sigma}_{Yi}^2(\hat{\beta}_{Yi}-\hat{\theta}\hat{\beta}_{Xi})^2}{(\hat{\theta}^2\hat{\sigma}_{Xi}^2+\hat{\sigma}_{Yi}^2)^3}\bigg/\frac{\hat{\beta}_{Xi}^2\hat{\sigma}_{Yi}^2+\hat{\beta}_{Yi}^2\hat{\sigma}_{Xi}^2}{(\hat{\theta}^2\hat{\sigma}_{Xi}^2+\hat{\sigma}_{Yi}^2)^2}=-\frac{4\hat{\sigma}_{Xi}^2\hat{\sigma}_{Yi}^2(\hat{\beta}_{Yi}-\hat{\theta}\hat{\beta}_{Xi})^2}{(\hat{\theta}^2\hat{\sigma}_{Xi}^2+\hat{\sigma}_{Yi}^2)(\hat{\beta}_{Xi}^2\hat{\sigma}_{Yi}^2+\hat{\beta}_{Yi}^2\hat{\sigma}_{Xi}^2)}\to 0.$$

Similarly, for the second part in (8), divided by the corresponding part in (6), because $\hat{\sigma}_{Xi}^2$, $\hat{\sigma}_{Yi}^2$ are both $O_p(1/N)$ and $\hat{\beta}_{Yi} - \hat{\theta}\hat{\beta}_{Xi} \to 0$, we get

$$\frac{2\hat{\sigma}_{Xi}^2\hat{\beta}_{Yi}(\hat{\beta}_{Yi}-\hat{\theta}\,\hat{\beta}_{Xi})}{(\hat{\theta}^2\hat{\sigma}_{Xi}^2+\hat{\sigma}_{Yi}^2)^2}\bigg/\frac{\hat{\beta}_{Xi}^2\hat{\sigma}_{Yi}^2+\hat{\beta}_{Yi}^2\hat{\sigma}_{Xi}^2}{(\hat{\theta}^2\hat{\sigma}_{Xi}^2+\hat{\sigma}_{Yi}^2)^2} = \frac{2\hat{\sigma}_{Xi}^2\hat{\beta}_{Yi}(\hat{\beta}_{Yi}-\hat{\theta}\,\hat{\beta}_{Xi})}{\hat{\beta}_{Xi}^2\hat{\sigma}_{Yi}^2+\hat{\beta}_{Yi}^2\hat{\sigma}_{Xi}^2} \to 0.$$

Hence we have $V - V^* = o_p(V^*)$, implying that V and V^* are asymptotically equivalent. This shows that our cMLE and the MPLE asymptotically share the same variance; this was also confirmed in our simulations and real data examples.

S3 Full Real Data Results

S3.1 Inference and Estimation Results of All Methods

Here we show the full real data results estimating and inferring causal effects of 12 risk factors on 4 common diseases from Table S1 to S4. We implemented cML methods, CAUSE, MR-Mix, MR-ContMix, MR-Lasso, MR-PRESSO, MR-IVW, MR-Egger, MR-Weighted-Median, MR-Weighted-Mode, and MR-RAPS. For cML method with BIC, we could use the smaller one of sample sizes of exposure and outcome (denoted by cML-BIC, cML-MA-BIC, cML-BIC-DP, cML-MA-BIC-DP), or we could use the larger one of them (denoted by cML-BIC-max, cML-MA-BIC-max, cML-BIC-DP-Max, cML-MA-BIC-DP-Max). These two choices give essentially the same results. We can also get $\hat{\theta}$ and SE($\hat{\theta}$) with profile likelihood as described in [13] (denoted by cML-MA-AIC-Profile, cML-AIC-Profile, cML-MA-BIC-max-Profile, cML-BIC-max-Profile, cML-MA-BIC-Profile, and cML-BIC-Profile). These two estimation approaches give almost the same results. For CAUSE, we extract its original results from Supplementary Table 3 of [6].

CAUSE and MR-ContMix do not provide the standard error of estimate, so we show their standard errors as NA.

S3.2 BIC and Scatter Plots

Table S5 shows the number of IVs used, number of invalid IVs detected by cML-BIC, and the proportion of detected invalid IVs for each exposure-outcome pair, with one default starting point set at 0 and

another 100 randomly generated starting points. Table S6 shows the results for only using the default starting point set at 0. There are 7 pairs giving different numbers of invalid IVs for the two runs with different starting points.

Figure S1 to S4 show BIC and scatter plots for each exposure-outcome pair in primary real data examples.

S3.3 Goodness-of-Fit Test Results

Tables S7 to S10 show the goodness-of-fit (GOF) test results for the 48 trait pairs. Each cell in each table shows the *p*-value of the corresponding GOF test. To calculate the BIC, we could use either the smaller one of the sample sizes for the exposure and the outcome (denoted by GOF1 and GOF2), or we could use the larger one of them (denoted by GOF1-Max and GOF2-Max). These two choices gave essentially the same results.

S4 Full Secondary Real Data Results

S4.1 GWAS Data and IV Selection

Table S11 shows the details of GWAS summary data used for the 13 traits in secondary real data examples. For each exposure-outcome pair, we used R package TwoSampleMR to select IVs and extract summary statistics following the standard procedure in the package. Here we show the example code for fasting proinsulin as the exposure and age at smoking as the outcome.

```
library(TwoSampleMR)
# ID of Fasting Proinsulin as exposure, ID of Age at Smoking as outcome
exp_id = "ebi-a-GCST001212"
out_id = "ieu-a-964"
# Extract IVs for exposure
exposure_dat <- extract_instruments(exp_id)</pre>
# LD-clumping of extracted IVs
exposure_dat <- clump_data(exposure_dat)</pre>
# Extract summary statistics of outcome, do not use proxy
outcome_dat <- extract_outcome_data(exposure_dat$SNP, out_id, proxies = 0)</pre>
# Harmonize data: correct strand for non-palindromic SNPs, drop all palindromic SNPs
dat <- harmonise_data(exposure_dat, outcome_dat, action = 3)</pre>
final_dat = dat[dat$mr_keep,]
# Get final estimates and standard errors for exposure and outcome
b_exp = final_dat$beta.exposure
b_out = final_dat$beta.outcome
se_exp =final_dat$se.exposure
se_out = final_dat$se.outcome
```

S4.2 Inference and Estimation Results of All Methods

See Table S12 to S18 and Figure S5.

S4.3 Goodness-of-fit Tests Results

See Table S19 to S25.

S5 Full Main Simulation Results

In our main simulations, we implemented our proposed cML method, MR-Mix, MR-ContMix, MR-Lasso, MR-PRESSO, MR-IVW, MR-IVW-Oracle, MR-Egger, MR-Weighted-Median, MR-Weighted-Mode and MR-RAPS. For cML methods, we could use AIC or BIC to select the best K (denoted by cML-AIC and cML-BIC), or generate AIC- or BIC-based weights for model averaging (denoted by cML-MA-AIC and cML-MA-BIC). We could use our iterative algorithm to get the constrained maximum likelihood estimate $\hat{\theta}$, and its standard error SE($\hat{\theta}$) with Fisher's information matrix as described in Section 4.4 (denoted by cML-MA-AIC, cML-AIC, cML-MA-BIC, and cML-BIC); or get $\hat{\theta}$ and SE($\hat{\theta}$) with the profile likelihood as described in [13] (denoted by cML-MA-AIC-Profile, cML-AIC-Profile, cML-MA-BIC-Profile, and cML-BIC-Profile). The two likelihood approaches gave almost the same results.

S5.1 Inference and Estimation Results

Table S26 to S88 show the inference and estimation results for the main simulations for m = 10, 20, 100, the ideal case with q = 0, and q = 0.2, 0.4, 0.6 with the InSIDE assumption holding or violated, and N = 50000, 100000, 200000.

MR-ContMix does not provide the standard error of an estimate, so we show its mean standard error as NA.

S5.2 Selection Results

Tables S89 to S94 show the relative frequencies of cML-BIC's selecting $\hat{K} = K_0$. We can see that, for each set-up, as N increased from 50000 to 200000, the relative frequencies of the correct selection also increased.

S5.3 Type-I Errors Based on 10,000 Simulations

In Figure 2 of the main text, we showed type-I errors of different methods for 10 setups based on 1000 simulations. We increased the number of simulations for each of these 10 setups to 10,000 and calculated the empirical type-I errors of different methods as shown in Figure S6.

S5.4 Data Perturbation Results

S5.4.1 Inference and Estimation Results

See Table S95 to S103.

S5.4.2 Goodness-of-Fit Test Results

See Table S104 to S106.

S6 Full Secondary Simulation Results

See Figure S7 and S8.

S7 Full Simulation Results with Weak Invalid IVs

S7.1 Inference and Estimation Results

See Table S107 to S114.

S7.2 Goodness-of-Fit Test Results

See Table S115 to S119.

S7.3 cML-MA-BIC and cML-MA-BIC-DP with Valid IVs

In the simulation setup 30 of 50 SNPs were invalid IVs while the other 20 were valid IVs. For valid IVs, their effects γ_i 's on X were generated from $N(0, h_x/m)$, where $h_x = 0.5$, m = 50, and pleiotropic effects α_i 's and ϕ_i 's were 0. We can see that the IV effects γ_i 's were weaker than in those in the Main simulations.

We applied cML-MA-BIC, cML-BIC, cML-MA-BIC-DP and cML-BIC-DP (with T=200) to the simulated data with only 20 valid IVs. Note that, since h_y only affected α_i 's of invalid IVs, the results were the same for $h_y=0.1,0.2,0.4,0.6$ as we only used 20 valid IVs. Table S120 shows the results. For cML-MA-BIC, cML-BIC, cML-MA-BIC-DP and cML-BIC-DP, in each cell from top to bottom are power/type-I error, Mean($\hat{\theta}$), SD($\hat{\theta}$), and Mean(SE($\hat{\theta}$)). For GOF1 and GOF2, the cells show the relative frequencies of their rejecting the null. The methods appeared to perform well.

S8 Computational Time

We compared the computational time taken by different methods. For cML-MA-BIC we tried with 0 or 5 random starting points (in addition to the single default starting point). For cML-MA-BIC-DP we set the number of data perturbations T=200 and tried with 0 or 5 random starting points (in addition to the single default starting point) for each perturbed dataset. For MR-ContMix we set CIMin = -0.5, CIMax = 0.5, CIStep = 0.0001. For MR-RAPS we set over dispersion = TRUE, loss function = "tukey". All other methods were implemented with their default parameters. Since CAUSE took a much longer running time, we did not include it for comparison.

We generated the simulated data following Section 2.9.3 in the Main text. We tried different numbers of IVs m = 10, 20, 50, 70 and 100, and set $h_y = 0.2$, $\theta = 0$, and 60% IVs as invalid IVs. For each m we did 10 simulations and applied different methods, counted each one's average running time over the 10 simulations. Table S121 shows the results. All methods were run on a 2016 MacBook Pro with a 2.7 GHz Intel Core i5 processor and 8 GB memory.

Supplemental References

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