CO 789, Homework 1

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1 First section

Definition 1.1 (Lattice). A lattice is a discrete subgroup of \mathbb{R}^n

Theorem 1.1 (Minkowski's bound). let $\mathcal{L}(B)$ be a full-rank lattice with basis $B \in \mathbb{R}^{n \times n}$, and $B^* = [\mathbf{b}_1^*, \mathbf{b}_2^*, \dots, \mathbf{b}_n^*]$ be the Gram-Schmidt orthogonalization of B, then

$$\lambda_1(\mathcal{L}(B)) \ge \min_{1 \le i \le n} |\mathbf{b}_i^*| \tag{1}$$

Algorithm 1 An algorithm with caption

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Require: n \ge 0
Ensure: y = x^n
y \leftarrow 1
X \leftarrow x
N \leftarrow n
while N \ne 0 do
if N is even then
X \leftarrow X \times X
N \leftarrow \frac{N}{2}
else if N is odd then
y \leftarrow y \times X
N \leftarrow N - 1
end if
end while
```

Here is some citation[1]

References

[1] Eiichiro Fujisaki and Tatsuaki Okamoto. Secure integration of asymmetric and symmetric encryption schemes. In *Annual international cryptology conference*, pages 537–554. Springer, 1999.