## CO 789, Homework 1

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## 1 First section

**Definition 1.1** (Lattice). A lattice is a discrete subgroup of  $\mathbb{R}^n$ 

**Theorem 1.1** (Minkowski's bound). let  $\mathcal{L}(B)$  be a full-rank lattice with basis  $B \in \mathbb{R}^{n \times n}$ , and  $B^* = [\mathbf{b}_1^*, \mathbf{b}_2^*, \dots, \mathbf{b}_n^*]$  be the Gram-Schmidt orthogonalization of B, then

$$\lambda_1(\mathcal{L}(B)) \ge \min_{1 \le i \le n} \|\mathbf{b}_i^*\| \tag{1}$$

## Algorithm 1 Caption for the algorithm

Require: This input, and that input

- 1: Make some statement with the "State" command
- 2: for Wrap for loop condition within the "For" command  $\mathbf{do}$
- 3: end for
- 4: while Wrap while loop condition within "While" command do
- 5: end while
- 6: if Wrap if else in the "If" command then
- 7: else if Another condition then
- 8: **else**
- 9: end if

return Return the output using the "Return" command