

# Faster generic IND-CCA2 secure KEM using “encrypt-then-MAC”

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**Abstract.** The modular Fujisaki-Okamoto (FO) transformation takes public-key encryption with weaker security and constructs a key encapsulation mechanism (KEM) with indistinguishability under adaptive chosen ciphertext attacks. While the modular FO transform enjoys tight security bound and quantum resistance, it also suffers from computational inefficiency and vulnerabilities to side-channel attacks due to using de-randomization and re-encryption for providing ciphertext integrity. In this work, we propose an alternative KEM construction that achieves ciphertext integrity using a message authentication code (MAC) and instantiate a concrete instance using Kyber. Our experimental results showed that where the encryption routine incurs heavy computational cost, replacing re-encryption with MAC provides substantial performance improvements at comparable security level.

**Keywords:** Key encapsulation mechanism, post-quantum cryptography, lattice cryptography, Fujisaki-Okamoto transformation

## 1 Introduction

The Fujisaki-Okamoto transformation [FO99] is a generic construction that takes cryptographic primitives of lesser security and constructs a public-key encryption scheme with indistinguishability under adaptive chosen ciphertext attacks. Later works [HHK17][HHM22] extended the original transformation to the construction of key encapsulation mechanism, which has been adopted by many post-quantum schemes such as Kyber [BDK<sup>+</sup>18] (later standardized into ML-KEM [Nat24]), FrodoKEM [BCD<sup>+</sup>16], and SABER [DKRV18].

The current state of the FO transformation enjoys proven tight security bound and quantum resistance, but also leaves many open problems. One such problem is the substantial computational cost of using *de-randomization* and *re-encryption* [BP18] for providing ciphertext integrity. In many post-quantum schemes, including ML-KEM, the input encryption routine is substantially more expensive than the input decryption routine, so running the encryption as a subroutine substantially increases the runtime cost of the decapsulation routine. While not the focus of this project, *re-encryption* also introduces risks of side-channel vulnerabilities that may expose the plaintext or the secret key, as demonstrated in [RRCB19] and [UXT<sup>+</sup>22].

We are inspired by how ciphertext integrity is achieved in symmetric cryptography: given a semantically secure symmetric cipher and an existentially unforgeable message authentication code, combining them using in a pattern called “encrypt-then-MAC” provides proven authenticated encryption [BN00]. “encrypt-then-MAC” is now the most widely accepted method for doing symmetric encryption as AES-GCM [MV04] and ChaCha20-Poly1305 [NL15].

The main challenge in applying “encrypt-then-MAC” to public-key cryptography is the lack of a pre-shared symmetric key. Inspired by hybrid public-key encryption schemes such as [FO99] and [CS98], we proposed to derive the symmetric key by hashing the plaintext message. In section 3, we prove that under the random oracle model, if the input public-key encryption scheme is one-way secure against plaintext-checking attack

and the input message authentication code is one-time existentially unforgeable, then the transformed key encapsulation mechanism is IND-CCA2 secure.

In section 4, we instantiate concrete instances of our constructions using ML-KEM. Our experimental results showed that replacing re-encryption with computing authenticator leads to significant performance improvements in the decapsulation routine while incurring only minimal runtime overhead in the encapsulation routine and a small increase in ciphertext size.

## 2 Preliminaries and previous results

### 2.1 Public-key encryption scheme

**Syntax.** A public-key encryption scheme  $\text{PKE}(\text{KeyGen}, \text{Enc}, \text{Dec})$  is a collection of three routines defined over some plaintext space  $\mathcal{M}$  and some ciphertext space  $\mathcal{C}$ .  $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{KeyGen}()$  is a randomized routine that returns a keypair. The encryption routine  $\text{Enc} : (\text{pk}, m) \mapsto c$  encrypts the input plaintext under the input public key. The decryption routine  $\text{Dec} : (\text{sk}, c) \mapsto m$  decrypts the input ciphertext under the input secret key. Where the encryption routine is randomized, we denote the randomness by  $r \in \mathcal{R}$ , where  $\mathcal{R}$  is called the coin space. The decryption routine is assumed to always be deterministic. Some decryption routines can detect malformed ciphertext and output the rejection symbol  $\perp$  accordingly.

**Correctness.** Following the definition in [DNR04] and [HHK17], a PKE is  $\delta$ -correct if:

$$E \left[ \max_{m \in \mathcal{M}} P \left[ \text{Dec}(\text{sk}, c) \neq m \mid c \xleftarrow{\$} \text{Enc}(\text{pk}, m) \right] \right] \leq \delta$$

Where the expectation is taken with respect to the probability distribution of all possible keypairs  $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{PKE}.\text{KeyGen}()$ . For many lattice-based cryptosystems, including ML-KEM, decryption failures could leak information about the secret key, although the probability of a decryption failure is low enough that classical adversaries cannot exploit decryption failure more than they can defeat the underlying lattice problem (see table 1).

Table 1: Estimated probability of decryption failure in ML-KEM

	ML-KEM-512	ML-KEM-768	ML-KEM-1024
$\delta$	???	???	???

On the other hand, a quantum adversary may be able to exploit decryption failure in reasonable runtime by efficiently searching through all possible inputs using Grover’s search algorithm. For that, ML-KEM made slight modifications in its KEM construction to prevent quantum adversary from precomputing large lookup table. We refer readers to [ABD<sup>+</sup>19] and [BDK<sup>+</sup>18] for the details.

**Security.** We discuss the security of a PKE using the sequence of games described in [Sho04]. Specifically, we first define the OW-ATK as they pertain to a public key encryption scheme. In later section we will define the IND-CCA game as it pertains to a key encapsulation mechanism.

The OW-ATK game	
1: $(\mathbf{pk}, \mathbf{sk}) \xleftarrow{\$} \text{KeyGen}(1^\lambda)$	
2: $m^* \xleftarrow{\$} \mathcal{M}$	
3: $c^* \xleftarrow{\$} \text{Enc}(\mathbf{pk}, m^*)$	
4: $\hat{m} \xleftarrow{\$} \mathcal{A}^{\mathcal{O}_{\text{ATK}}}(1^\lambda, \mathbf{pk}, c^*)$	$\text{PCO}(m \in \mathcal{M}, c \in \mathcal{C})$
5: <b>return</b> $\llbracket m^* = \hat{m} \rrbracket$	1: <b>return</b> $\llbracket \text{Dec}(\mathbf{sk}, c) = m \rrbracket$

Figure 1: One-way security game of PKE (left) and plaintext-checking oracle (right)

77 In the OW-ATK game (see figure 1), an adversary's goal is to recover the decryption of a  
 78 randomly generated ciphertext. A challenger randomly samples a keypair and a challenge  
 79 plaintext  $m^*$ , encrypts the challenge plaintext  $c^* \xleftarrow{\$} \text{Enc}(\mathbf{pk}, m^*)$ , then gives  $\mathbf{pk}$  and  $c^*$   
 80 to the adversary  $A$ . The adversary  $A$ , with access to some oracle  $\mathcal{O}_{\text{ATK}}$ , outputs a guess  
 81 decryption  $\hat{m}$ .  $A$  wins the game if its guess  $\hat{m}$  is equal to the challenge plaintext  $m^*$ . The  
 82 *advantage*  $\text{Adv}_{\text{OW-ATK}}$  of an adversary in this game is the probability that it wins the game:

$$\text{Adv}_{\text{OW-ATK}}(A) = P \left[ A(\mathbf{pk}, c^*) = m^* \mid (\mathbf{pk}, \mathbf{sk}) \xleftarrow{\$} \text{KeyGen}(); m^* \xleftarrow{\$} \mathcal{M}; c^* \xleftarrow{\$} \text{Enc}(\mathbf{pk}, m^*) \right]$$

83 The capabilities of the oracle  $\mathcal{O}_{\text{ATK}}$  depends on the choice of security goal ATK. Particu-  
 84 larly relevant to our result is security against plaintext-checking attack (PCA), for which  
 85 the adversary has access to a plaintext-checking oracle (PCO) (see figure 1). A PCO takes  
 86 as input a plaintext-ciphertext pair  $(m, c)$  and returns **True** if  $m$  is the decryption of  $c$  or  
 87 **False** otherwise.

## 88 2.2 Key encapsulation mechanism (KEM)

89 A key encapsulation mechanism is a collection of three routines (**KeyGen**, **Encap**, **Decap**)  
 90 defined over some ciphertext space  $\mathcal{C}$  and some key space  $\mathcal{K}$ . The key generation routine  
 91 takes the security parameter  $1^\lambda$  and outputs a keypair  $(\mathbf{pk}, \mathbf{sk}) \xleftarrow{\$} \text{KeyGen}(1^\lambda)$ . **Encap**( $\mathbf{pk}$ )  
 92 is a probabilistic routine that takes a public key  $\mathbf{pk}$  and outputs a pair of values  $(c, K)$   
 93 where  $c \in \mathcal{C}$  is the ciphertext (also called encapsulation) and  $K \in \mathcal{K}$  is the shared secret  
 94 (also called session key). **Decap**( $\mathbf{sk}, c$ ) is a deterministic routine that takes the secret key  
 95  $\mathbf{sk}$  and the encapsulation  $c$  and returns the shared secret  $K$  if the ciphertext is valid. Some  
 96 KEM constructions use explicit rejection, where if  $c$  is invalid then **Decap** will return a  
 97 rejection symbol  $\perp$ ; other KEM constructions use implicit rejection, where if  $c$  is invalid  
 98 then **Decap** will return a fake session key that depends on the ciphertext and some other  
 99 secret values.

100 The IND-CCA security of a KEM is defined by an adversarial game in which an  
 101 adversary's goal is to distinguish pseudorandom shared secret (generated by running the  
 102 **Encap** routine) and a truly random value.

KEM-IND-CCA2 game	
1: $(\mathbf{pk}, \mathbf{sk}) \xleftarrow{\$} \text{KeyGen}(1^\lambda)$	
2: $(c^*, K_0) \xleftarrow{\$} \text{Encap}(\mathbf{pk})$	
3: $K_1 \xleftarrow{\$} \mathcal{K}$	
4: $b \xleftarrow{\$} \{0, 1\}$	
5: $\hat{b} \xleftarrow{\$} A^{\mathcal{O}_{\text{Decap}}}(1^\lambda, \mathbf{pk}, c^*, K_b)$	$\mathcal{O}_{\text{Decap}}(c)$
6: <b>return</b> $[\hat{b} = b]$	1: <b>return</b> $\text{Decap}(\mathbf{sk}, c)$

Figure 2: IND-CCA2 game for KEM (left) and decapsulation oracle (right)

103 The decapsulation oracle  $\mathcal{O}^{\text{Decap}}$  takes a ciphertext  $c$  and returns the output of the  
 104 **Decap** routine using the secret key. The advantage  $\epsilon_{\text{IND-CCA}}$  of an IND-CCA adversary  
 105  $\mathcal{A}_{\text{IND-CCA}}$  is defined by

$$\text{Adv}_{\text{IND-CCA}}(A) = \left| P[A^{\mathcal{O}_{\text{Decap}}}(a^\lambda, \mathbf{pk}, c^*, K_b) = b] - \frac{1}{2} \right|$$

## 106 2.3 Message authentication code (MAC)

107 A message authentication code **MAC** is a collection of routines (**Sign**, **Verify**) defined over  
 108 some key space  $\mathcal{K}$ , some message space  $\mathcal{M}$ , and some tag space  $\mathcal{T}$ . The signing routine  
 109 **Sign**( $k, m$ ) takes the secret key  $k \in \mathcal{K}$  and some message, and outputs a tag  $t$ . The  
 110 verification routine **Verify**( $k, m, t$ ) takes the triplet of secret key, message, and tag, and  
 111 outputs 1 if the message-tag pair is valid under the secret key, or 0 otherwise. Many MAC  
 112 constructions are deterministic. For these constructions it is simpler to denote the signing  
 113 routine by  $t \leftarrow \text{MAC}(k, m)$  and perform verification using a simple comparison.

114 The security of a MAC is defined in an adversarial game in which an adversary, with  
 115 access to some signing oracle  $\mathcal{O}_{\text{Sign}}(m)$ , tries to forge a new valid message-tag pair that  
 116 has never been queried before. The existential unforgeability under chosen message attack  
 117 (EUF-CMA) game is shown below:

EUF-CMA game	
1: $k^* \xleftarrow{\$} \mathcal{K}$	
2: $(\hat{m}, \hat{t}) \xleftarrow{\$} \mathcal{A}^{\mathcal{O}_{\text{Sign}}}()$	
3: <b>return</b> $[\text{Verify}(k^*, \hat{m}, \hat{t}) \wedge (\hat{m}, \hat{t}) \notin \mathcal{O}_{\text{Sign}}]$	

Figure 3: The existential forgery game

118 The advantage  $\text{Adv}_{\text{EUF-CMA}}$  of the existential forgery adversary is the probability that it  
 119 wins the EUF-CMA game.

## 120 2.4 Related works

121 The modular Fujisaki-Okamoto transformation [HHK17] is a family of generic transforma-  
 122 tions that takes as input a PKE with weaker security, such as OW-CPA, and outputs a  
 123 PKE or KEM with IND-CCA2 security. The key ingredient in achieving ciphertext non-  
 124 malleability is with *de-randomization* and *re-encryption*, which first transform a OW-CPA  
 125 PKE into a *rigid* PKE, then transform the rigid PKE into a KEM. More specifically:

1. *de-randomization* means that a randomized encryption routine  $c \xleftarrow{\$} \text{Enc}(\text{pk}, m)$  is made into a deterministic encryption routine by deriving randomization coin pseudorandomly:  $c \leftarrow \text{Enc}(\text{pk}, m, r = H(m))$  for some hash function  $H$
2. *re-encryption* means that the transformed decryption routine will run the transformed encryption routine to verify the integrity of the ciphertext. Because after *de-randomization*, each plaintext strictly corresponds exactly one ciphertext, tempering with a ciphertext means that even if the ciphertext decrypts back to the same plaintext, the re-encryption will detect that the ciphertext has been tempered with.
3. *rigidity* means that the decryption routine is a perfect inverse of the encryption routine:  $c = \text{Enc}(\text{pk}, m) \Leftrightarrow m = \text{Dec}(\text{sk}, c)$ . Converting a one-way secure rigid PKE (which is essentially a trapdoor function) into a IND-CCA2 KEM is well solved problem.

let  $\text{PKE} = (\text{KeyGen}_{\text{PKE}}, \text{Enc}, \text{Dec})$  be defined over message space  $\mathcal{M}$  and ciphertext space  $\mathcal{C}$ . Let  $G : \mathcal{M} \rightarrow \mathcal{R}$  hash plaintexts into coins, and let  $H : \{0, 1\}^* \rightarrow \{0, 1\}^*$  hash byte stream into session keys. Depending on whether the constructed KEM uses implicit or explicit rejection, and the security property of the PKE, [HHK17] described four variations. They are summarized in table 2 and figure 4.

Table 2: Variants of modular FO transforms

name	rejection	PKE security
$U^\perp$	explicit	OW-PCVA
$U^\perp$	implicit	OW-PCA
$U_m^\perp$	explicit	OW-VA + rigid
$U_m^\perp$	implicit	OW-CPA + rigid

KEM.KeyGen()	KEM.Decap(sk, c)
1: $(\text{pk}, \text{sk}') \xleftarrow{\$} \text{PKE.KeyGen}()$ 2: $z \xleftarrow{\$} \mathcal{M}$ 3: $\text{sk} \leftarrow (\text{sk}', z)$ 4: $\text{sk} \leftarrow \text{sk}'$ 5: <b>return</b> (pk, sk)	<b>Ensure:</b> $\text{sk} = (\text{sk}', z)$ <b>Ensure:</b> $\text{sk}'$ is valid PKE secret key <b>Ensure:</b> $z$ is valid PKE plaintext 1: $\hat{m} \leftarrow \text{PKE.Dec}(\text{sk}', c)$ 2: $\hat{r} \leftarrow G(\hat{m})$ 3: $\hat{c} \leftarrow \text{PKE.Enc}(\text{pk}, \hat{m}, \hat{r})$ 4: <b>if</b> $\hat{c} = c$ <b>then</b> 5: $K \leftarrow H(\hat{m})$ 6: $K \leftarrow H(\hat{m}, c)$ 7: <b>else</b> 8: $K \leftarrow H(z, c)$ 9: $K \leftarrow \perp$ 10: <b>end if</b> 11: <b>return</b> K
KEM.Encap(pk)	
1: $m \xleftarrow{\$} \mathcal{M}$ 2: $r \leftarrow G(m)$ 3: $c \leftarrow \text{PKE.Enc}(\text{pk}, m, r)$ 4: $K \leftarrow H(m, c)$ 5: $K \leftarrow H(m)$ 6: <b>return</b> (c, K)	1: $\hat{m} \leftarrow \text{PKE.Dec}(\text{sk}', c)$ 2: $\hat{r} \leftarrow G(\hat{m})$ 3: $\hat{c} \leftarrow \text{PKE.Enc}(\text{pk}, \hat{m}, \hat{r})$ 4: <b>if</b> $\hat{c} = c$ <b>then</b> 5: $K \leftarrow H(\hat{m})$ 6: $K \leftarrow H(\hat{m}, c)$ 7: <b>else</b> 8: $K \leftarrow H(z, c)$ 9: $K \leftarrow \perp$ 10: <b>end if</b> 11: <b>return</b> K

Figure 4: Summary of the modular Fujisaki-Okamoto transformation variations

The modular FO transformations enjoy tight security bounds and proven quantum resistance. Variations have been deployed to many post-quantum KEMs submitted to NIST's post-quantum cryptography competition. Kyber, one of the round 3 finalists, uses

the  $U^\perp$  transformation. When it was later standardized into FIPS-203, it changed to use the  $U_m^\perp$  transformation for computational efficiencies.

### 3 The “encrypt-then-MAC” transformation

Let  $\mathcal{B}^*$  denote the set of finite bit strings. Let  $\text{PKE}(\text{KeyGen}, \text{Enc}, \text{Dec})$  be a public-key encryption scheme defined over message space  $\mathcal{M}$  and ciphertext space  $\mathcal{C}$ . Let  $\text{MAC} : \mathcal{K}_{\text{MAC}} \times \mathcal{B}^* \rightarrow \mathcal{T}$  be a deterministic message authentication code that takes a key  $k \in \mathcal{K}_{\text{MAC}}$ , some message  $m \in \mathcal{B}^*$ , and outputs a digest  $t \in \mathcal{T}$ . Let  $G : \mathcal{M} \rightarrow \mathcal{K}_{\text{MAC}}$  be a hash function that maps from PKE’s plaintext space to MAC’s key space. Let  $H : \mathcal{B}^* \rightarrow \mathcal{K}_{\text{KEM}}$  be a hash function that maps bit strings into the set of possible shared secrets. The “encrypt-then-MAC” transformation  $\text{EtM}[\text{PKE}, \text{MAC}, G, H]$  constructs a key encapsulation mechanism  $\text{KEM}_{\text{EtM}}(\text{KeyGen}_{\text{KEM}}, \text{Encap}, \text{Decap})$ , whose routines are described in figure 5.

$\text{KEM}_{\text{EtM}}.\text{KeyGen}()$	$\text{KEM}_{\text{EtM}}.\text{Decap}(\text{sk}, c)$
1: $(\text{pk}, \text{sk}') \xleftarrow{\$} \text{PKE}.\text{KeyGen}()$ 2: $z \xleftarrow{\$} \mathcal{M}$ 3: $\text{sk} \leftarrow \text{sk}' \  z$ 4: <b>return</b> $(\text{pk}, \text{sk})$	<b>Require:</b> $c = c' \  t, \text{sk} = \text{sk}' \  z$ <b>Ensure:</b> $c'$ is some PKE ciphertext <b>Ensure:</b> $t$ is some MAC tag <b>Ensure:</b> $\text{sk}'$ is some PKE secret key <b>Ensure:</b> $z$ is some PKE plaintext 1: $(c', t) \leftarrow c$ 2: $(\text{sk}', z) \leftarrow \text{sk}$ 3: $\hat{m} \leftarrow \text{PKE}.\text{Dec}(\text{sk}', c')$ 4: $\hat{k} \leftarrow G(\hat{m})$ 5: <b>if</b> $\text{MAC}(\hat{k}, c') \neq t$ <b>then</b> 6: $K \leftarrow H(z, c')$ 7: <b>else</b> 8: $K \leftarrow H(\hat{m}, c')$ 9: <b>end if</b> 10: <b>return</b> $K$
$\text{KEM}_{\text{EtM}}.\text{Encap}(\text{pk})$	
<b>Ensure:</b> $\text{pk}$ is some PKE public key 1: $m \xleftarrow{\$} \mathcal{M}$ 2: $k \leftarrow G(m)$ 3: $c' \xleftarrow{\$} \text{PKE}.\text{Enc}(\text{pk}, m)$ 4: $t \leftarrow \text{MAC}(k, c')$ 5: $K \leftarrow H(m, c')$ 6: $c \leftarrow c' \  t$ 7: <b>return</b> $(c, K)$	

Figure 5:  $\text{KEM}_{\text{EtM}}$  routines

The key generation routine of  $\text{KEM}_{\text{EtM}}$  is largely identical to that of the PKE, only a secret value  $z$  is sampled as the implicit rejection symbol. In the encapsulation routine, a MAC key is derived from the randomly sampled plaintext  $k \leftarrow G(m)$ , then used to sign the unauthenticated ciphertext  $c'$ . Because the encryption routine might be randomized, the session key is derived from both the message and the ciphertext. Finally, the unauthenticated ciphertext  $c'$  and the tag  $t$  combine into the authenticated ciphertext  $c$  that would be transmitted to the peer. In the decapsulation routine, the decryption  $\hat{m}$  of the unauthenticated ciphertext is used to re-derive the MAC key  $\hat{k}$ , which is then used to re-compute the tag  $\hat{t}$ . The ciphertext is considered valid if and only if the recomputed tag is identical to the input tag.

For an adversary  $A$  to produce a valid tag  $t$  for some unauthenticated ciphertext  $c'$  under the symmetric key  $k \leftarrow G(\text{Dec}(\text{sk}', c'))$  implies that  $A$  must either know the symmetric key  $k$  or produce a forgery. Under the random oracle model,  $A$  also cannot know  $k$  without knowing its preimage  $\text{Dec}(\text{sk}', c')$ , so  $A$  must either have produced  $c'$  honestly, or have broken the one-way security of PKE. This means that the decapsulation

oracle will not give out information on decryptions that the adversary does not already know.

$\text{PCO}(m, c)$
1: $k \leftarrow G(m)$
2: $t \leftarrow \text{MAC}(k, c)$
3: <b>return</b> $\llbracket \mathcal{O}^{\text{Decap}}((c, t)) = H(m, c) \rrbracket$

Figure 6: Every decapsulation oracle can be converted into a plaintext-checking oracle

However, a decapsulation oracle can still give out some information: for a known plaintext  $m$ , all possible encryptions  $c' \xleftarrow{\$} \text{Enc}(\text{pk}, m)$  can be correctly signed, while ciphertexts that don't decrypt back to  $m$  cannot be correctly signed. This means that a decapsulation oracle can be converted into a plaintext-checking oracle (see figure 6), so every chosen-ciphertext attack against the KEM can be converted into a plaintext-checking attack against the underlying PKE.

On the other hand, if the underlying PKE is one-way secure against plaintext-checking attack that makes  $q$  plaintext-checking queries, then “encrypt-then-MAC” KEM is semantically secure under chosen ciphertext attacks making the same number of decapsulation queries:

**Theorem 1.** *For every IND-CCA2 adversary  $A$  against  $\text{KEM}_{\text{EtM}}$  that makes  $q$  decapsulation queries, there exists an OW-PCA adversary  $B$  who makes at least  $q$  plaintext-checking queries against the underlying PKE, and an one-time existential forgery adversary  $C$  against the underlying MAC such that*

$$\text{Adv}_{\text{IND-CCA2}}(A) \leq q \cdot \text{Adv}_{\text{OT-MAC}}(C) + 2 \cdot \text{Adv}_{\text{OW-PCA}}(B)$$

Theorem 1 naturally flows into an equivalence relationship between the security of the KEM and the security of the PKE:

**Lemma 1.**  *$\text{KEM}_{\text{EtM}}$  is IND-CCA2 secure if and only if the input PKE is OW-PCA secure*

### 3.1 Proof of theorem 1

We will prove theorem 1 using a sequence of game. A summary of the the sequence of games can be found in figure 7 and 8. From a high level we made three incremental modifications to the IND-CCA2 game for  $\text{KEM}_{\text{EtM}}$ : replace true decapsulation with simulated decapsulation, replace the pseudorandom MAC key  $k^* \leftarrow G(m^*)$  with a truly random MAC key  $k^* \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ , and finally replace pseudorandom shared secret  $K_0 \leftarrow H(m^*, c')$  with a truly random shared secret  $K_0 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ . A OW-PCA adversary can then simulate the modified IND-CCA2 game for the KEM adversary, and the advantage of the OW-PCA adversary is associated with the probability of certain behaviors of the KEM adversary.

*Proof.* *Game 0* is the standard IND-CCA2 game for KEMs. The decapsulation oracle  $\mathcal{O}^{\text{Decap}}$  executes the decapsulation routine using the challenge keypair and return the results faithfully. The queries made to the hash oracles  $\mathcal{O}^G, \mathcal{O}^H$  are recorded to their respective tapes  $\mathcal{L}^G, \mathcal{L}^H$ .

*Game 1* is identical to game 0 except that the true decapsulation oracle  $\mathcal{O}^{\text{Decap}}$  is replaced with a simulated oracle  $\mathcal{O}_1^{\text{Decap}}$ . Instead of directly decrypting  $c'$  as in the decapsulation routine, the simulated oracle searches through the tape  $\mathcal{L}^G$  to find a matching query  $(\tilde{m}, \tilde{k})$

IND-CCA2 game for $\text{KEM}_{\text{EtM}}$	$\mathcal{O}^{\text{Decap}}(c)$
1: $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{KEM}_{\text{EtM}}.\text{KeyGen}()$ 2: $m^* \xleftarrow{\$} \mathcal{M}$ 3: $c' \xleftarrow{\$} \text{PKE}.\text{Enc}(\text{pk}, m^*)$ 4: $k^* \leftarrow G(m^*)$ $\triangleright$ Game 0-1 5: $k^* \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ $\triangleright$ Game 2-3 6: $t \leftarrow \text{MAC}(k^*, c')$ 7: $c^* \leftarrow c'    t$ 8: $K_0 \leftarrow H(m^*, c')$ $\triangleright$ Game 0-2 9: $K_0 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ $\triangleright$ Game 3 10: $K_1 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ 11: $b \xleftarrow{\$} \{0, 1\}$ 12: $\hat{b} \leftarrow A^{\mathcal{O}^{\text{Decap}}}(\text{pk}, c^*, K_b)$ $\triangleright$ Game 0 13: $\hat{b} \leftarrow A^{\mathcal{O}_1^{\text{Decap}}}(\text{pk}, c^*, K_b)$ $\triangleright$ Game 1-3 14: <b>return</b> $\llbracket \hat{b} = b \rrbracket$	1: $(c', t) \leftarrow c$ 2: $\hat{m} = \text{Dec}(\text{sk}', c')$ 3: $\hat{k} \leftarrow G(\hat{m})$ 4: <b>if</b> $\text{MAC}(\hat{k}, c') = t$ <b>then</b> 5: $K \leftarrow H(\hat{m}, c')$ 6: <b>else</b> 7: $K \leftarrow H(z, c')$ 8: <b>end if</b> 9: <b>return</b> $K$
$\mathcal{O}^G(m)$	$\mathcal{O}_1^{\text{Decap}}(c)$
1: <b>if</b> $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = m$ <b>then</b> 2: <b>return</b> $\tilde{k}$ 3: <b>end if</b> 4: $k \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ 5: $\mathcal{L}^G \leftarrow \mathcal{L}^G \cup \{(m, k)\}$ 6: <b>return</b> $k$	1: $(c', t) \leftarrow c$ 2: <b>if</b> $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = \text{Dec}(\text{sk}', c') \wedge \text{MAC}(\tilde{k}, c') = t$ <b>then</b> 3: $K \leftarrow H(\tilde{m}, c')$ 4: <b>else</b> 5: $K \leftarrow H(z, c')$ 6: <b>end if</b> 7: <b>return</b> $K$
	$\mathcal{O}^H(m, c)$
	1: <b>if</b> $\exists(\tilde{m}, \tilde{c}, \tilde{K}) \in \mathcal{L}^H : \tilde{m} = m \wedge \tilde{c} = c$ <b>then</b> 2: <b>return</b> $\tilde{K}$ 3: <b>end if</b> 4: $K \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ 5: $\mathcal{L}^H \leftarrow \mathcal{L}^H \cup \{(m, c, K)\}$ 6: <b>return</b> $K$

Figure 7: Sequence of games

such that  $\tilde{m}$  is the decryption of  $c'$ . The simulated oracle then uses  $\tilde{k}$  to validate the tag  $t$  against  $c'$ .

If the simulated oracle accepts the queried ciphertext as valid, then there is a matching query that also validates the tag, which means that the queried ciphertext is honestly generated. Therefore, the true oracle must also accept the queried ciphertext. On the other hand, if the true oracle rejects the queried ciphertext (and output the implicit rejection  $H(z, c')$ ), then the tag is simply invalid under the MAC key  $k = G(\text{Dec}(\text{sk}', c'))$ . Therefore, there could not have been a matching query that also validates the tag, and the simulated oracle must also reject the queried ciphertext.

This means that from the adversary  $A$ 's perspective, game 1 and game 0 differ only when the true oracle accepts while the simulated oracle rejects, which means that  $t$  is a valid tag for  $c'$  under  $k = G(\text{Dec}(\text{sk}', c'))$ , but  $k$  has never been queried. Under the random oracle model, such  $k$  is a uniformly random sample of  $\mathcal{K}_{\text{MAC}}$  that the adversary does not know, so for  $A$  to produce a valid tag is to produce a forgery against the MAC under an unknown and uniformly random key. Furthermore, the security game does not include a signing oracle, so this is a zero-time forgery. While zero-time forgery is not a standard security definition for a MAC, we can bound it by the advantage of a one-time forgery



adversary  $C$ :

$$P \left[ \mathcal{O}^{\text{Decap}}(c) \neq \mathcal{O}_1^{\text{Decap}}(c) \right] \leq \text{Adv}_{\text{OT-MAC}}(C)$$

Across all  $q$  decapsulation queries, the probability that at least one query is a forgery is thus at most  $q \cdot P \left[ \mathcal{O}^{\text{Decap}}(c) \neq \mathcal{O}_1^{\text{Decap}}(c) \right]$ . By the difference lemma:

$$\text{Adv}_{G_0}(A) - \text{Adv}_{G_1}(A) \leq q \cdot \text{Adv}_{\text{OT-MAC}}(C)$$

*Game 2* is identical to game 1, except that the challenger samples a uniformly random MAC key  $k^* \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$  instead of deriving it from  $m^*$ . From  $A$ 's perspective the two games are indistinguishable, unless  $A$  queries  $G$  with the value of  $m^*$ . Denote the probability that  $A$  queries  $G$  with  $m^*$  by  $P[\text{QUERY } G]$ , then:

$$\text{Adv}_{G_1}(A) - \text{Adv}_{G_2}(A) \leq P[\text{QUERY } G]$$

*Game 3* is identical to game 2, except that the challenger samples a uniformly random shared secret  $K_0 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$  instead of deriving it from  $m^*$  and  $c'$ . From  $A$ 's perspective the two games are indistinguishable, unless  $A$  queries  $H$  with  $(m^*, \cdot)$ . Denote the probability that  $A$  queries  $H$  with  $(m^*, \cdot)$  by  $P[\text{QUERY } H]$ , then:

$$\text{Adv}_{G_2}(A) - \text{Adv}_{G_3}(A) \leq P[\text{QUERY } H]$$

Since in game 3, both  $K_0$  and  $K_1$  are uniformly random and independent of all other variables, no adversary can have any advantage:  $\text{Adv}_{G_3}(A) = 0$ .

$B(\text{pk}, c'^*)$	$\mathcal{O}_B^{\text{Decap}}(c)$
1: $z \xleftarrow{\$} \mathcal{M}$ 2: $k \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ 3: $t \leftarrow \text{MAC}(k, c'^*)$ 4: $c^* \leftarrow (c'^*, t)$ 5: $K \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ 6: $\hat{b} \leftarrow A^{\mathcal{O}_B^{\text{Decap}}, \mathcal{O}_B^G, \mathcal{O}_B^H}(\text{pk}, c^*, K)$ 7: <b>if</b> $\text{ABORT}(m)$ <b>then</b> 8: <b>return</b> $m$ 9: <b>end if</b>	1: $(c', t) \leftarrow c$ 2: <b>if</b> $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \text{PCO}(c', \tilde{m}) = 1 \wedge \text{MAC}(\tilde{k}, c') = t$ <b>then</b> 3: $K \leftarrow H(\tilde{m}, c')$ 4: <b>else</b> 5: $K \leftarrow H(z, c')$ 6: <b>end if</b> 7: <b>return</b> $K$
$\mathcal{O}_B^H(m, c)$	$\mathcal{O}_B^G(m)$
<b>if</b> $\text{PCO}(m, c'^*) = 1$ <b>then</b> $\text{ABORT}(m)$ <b>end if</b> <b>if</b> $\exists(\tilde{m}, \tilde{c}, \tilde{K}) \in \mathcal{L}^H : \tilde{m} = m \wedge \tilde{c} = c$ <b>then</b> <b>return</b> $\tilde{K}$ <b>end if</b> $K \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ $\mathcal{L}^H \leftarrow \mathcal{L}^H \cup \{(m, c, K)\}$ <b>return</b> $K$	1: <b>if</b> $\text{PCO}(m, c'^*) = 1$ <b>then</b> 2: $\text{ABORT}(m)$ 3: <b>end if</b> 4: <b>if</b> $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = m$ <b>then</b> 5: <b>return</b> $\tilde{k}$ 6: <b>end if</b> 7: $k \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ 8: $\mathcal{L}^G \leftarrow \mathcal{L}^G \cup \{(m, k)\}$ 9: <b>return</b> $k$

Figure 8: OW-PCA adversary  $B$  simulates game 3 for IND-CCA2 adversary  $A$

We will bound  $P[\text{QUERY } \mathcal{G}]$  and  $P[\text{QUERY } \mathcal{H}]$  by constructing a OW-PCA adversary  $B$  against the underlying PKE that uses  $A$  as a sub-routine.  $B$ 's behaviors are summarized in figure 8.

$B$  simulates game 3 for  $A$ : receiving the public key  $\text{pk}$  and challenge encryption  $c^*$ ,  $B$  samples random MAC key and session key to produce the challenge encapsulation, then feeds it to  $A$ . When simulating the decapsulation oracle,  $B$  uses the plaintext-checking oracle to look for matching queries in  $\mathcal{L}^G$ . When simulating the hash oracles,  $B$  uses the plaintext-checking oracle to detect when  $m^* = \text{Dec}(\text{sk}', c^*)$  has been queried. When  $m^*$  is queried,  $B$  terminates  $A$  and returns  $m^*$  to win the OW-PCA game. In other words:

$$P[\text{QUERY } \mathcal{G}] \leq \text{Adv}_{\text{OW-PCA}}(B)$$

$$P[\text{QUERY } \mathcal{H}] \leq \text{Adv}_{\text{OW-PCA}}(B)$$

Combining all equations above produce the desired security bound.  $\square$

### 3.2 Instantiation with ElGamal cryptosystem

In this section we instantiate our “encrypt-then-MAC” construction with the ElGamal cryptosystem, then prove that the output KEM is IND-CCA2 secure.

The ElGamal cryptosystem [Gam85] (see figure 9) bases its security on the conjectured intractability of the computational Diffie-Hellman problem and the decisional Diffie-Hellman problem.

KeyGen()	Enc(pk, m)	Dec(sk, c)
1: $x \xleftarrow{\$} \mathbb{Z}_q$	<b>Require:</b> $\text{pk}, m \in \mathbb{Z}_q$	<b>Require:</b> $\text{sk} \in \mathbb{Z}_q$
2: $\text{sk} \leftarrow x$	1: $y \xleftarrow{\$} \mathbb{Z}_q$	<b>Require:</b> $c = (u, v) \in \mathbb{Z}_q^2$
3: $\text{pk} \leftarrow g^x$	2: $u \leftarrow g^y$	1: <b>return</b> $(u^{\text{sk}})^{-1} \cdot v$
4: <b>return</b> (pk, sk)	3: $v \leftarrow m \cdot (\text{pk})^y$	
	4: <b>return</b> (u, v)	

Figure 9: The ElGamal cryptosystem

**Definition 1** (Computational Diffie-Hellman (CDH) problem). Let  $G = \langle g \rangle$  be a cyclic group with prime order  $g$ , let  $x, y \xleftarrow{\$} \mathbb{Z}_q$  be uniformly random samples. Given  $G, g, g^x, g^y$ , compute  $g^{xy}$

**Definition 2** (Decisional Diffie-Hellman (DDH) problem). Let  $G = \langle g \rangle$  be a cyclic group with prime order  $g$ , let  $x, y, z \xleftarrow{\$} \mathbb{Z}_q$  be uniformly random samples, let  $h$  be a random variable with probability distribution:

$$P[h = g^{xy}] = P[h = g^z] = \frac{1}{2}$$

Given  $G, g, g^x, g^y, h$ , distinguish whether  $h = g^{xy}$  or  $h = g^z$

It is well known that if the CDH problem is intractable, then the ElGamal cryptosystem is OW-CPA secure, and if the DDH problem is intractable, then the ElGamal cryptosystem is IND-CPA secure. It is easy to show that the DDH problem reduces to the CDH problem. However, it is conjectured that the CDH problem remains intractable even if the DDH problem can be solved efficiently.

**Definition 3** (Interactive computational Diffie-Hellman (ICDH) problem). Let  $G = \langle g \rangle$  be a cyclic group with prime order  $q$ . Let  $x, y \xleftarrow{\$} \mathbb{Z}_q$  be uniformly random sample. Let  $\mathcal{O}^{\text{DDH}}$  be a DDH oracle such that:

$$\mathcal{O}^{\text{DDH}} : (u, v) \in \mathbb{Z}_q^2 \mapsto \llbracket u^x = v \rrbracket$$

Given  $G, g, g^x, g^y$  and access to  $\mathcal{O}^{\text{DDH}}$ , compute  $g^{xy}$

**Theorem 2.** For every OW-PCA adversary  $A$  against the ElGamal cryptosystem, there exists an ICDH adversary  $B$  such that:

$$\text{Adv}(A) \leq \text{Adv}(B)$$

In other words, for cyclic group  $G$  where the ICDH assumption holds, the ElGamal cryptosystem is OW-PCA secure. From theorem 1, we naturally conclude that combining “encrypt-then-MAC” with the ElGamal cryptosystem gives us an IND-CCA2 secure KEM. It remains to prove theorem 2:

*Proof.* For a sketch of proof, we will construct an ICDH adversary  $B$  that uses the OW-PCA adversary  $A$  as a sub-routine. The main challenge is simulating the plaintext-checking oracle, which can be overcome because  $B$  has access to a DDH oracle  $\mathcal{O}^{\text{DDH}}$ . See figure 10 for how  $B$  simulates OW-PCA game for  $A$ :

OW-PCA game for ElGamal cryptosystem	ICDH adversary $B^{\mathcal{O}^{\text{DDH}}}(g^x, g^y)$
1: $x \xleftarrow{\$} \mathbb{Z}_q$	1: $\text{pk} \leftarrow g^x$
2: $(\text{pk}, \text{sk}) \leftarrow (g^x, x)$	2: $u \leftarrow g^y$
3: $m^* \xleftarrow{\$} \mathbb{Z}_q$	3: $v \xleftarrow{\$} \mathbb{Z}_q$
4: $y \xleftarrow{\$} \mathbb{Z}_q$	4: $c^* = (u, v)$
5: $(u, v) \leftarrow (g^y, m \cdot (g^x)^y)$	5: $\hat{m} \leftarrow A^{\mathcal{O}_1^{\text{PCO}}}(\text{pk}, c^*)$
6: $c^* \leftarrow (u, v)$	6: <b>return</b> $\hat{m}^{-1} \cdot v^*$
7: $\hat{m} \leftarrow A^{\text{PCO}}(\text{pk}, c^*)$	
8: <b>return</b> $\llbracket \hat{m} = m^* \rrbracket$	
	Simulated PCO: $\mathcal{O}_1^{\text{PCO}}(m, c)$
	<b>Require:</b> $c = (u, v) \in \mathbb{Z}_q^2$
	<b>Require:</b> $m \in \mathbb{Z}_q$
	1: <b>return</b> $\mathcal{O}^{\text{DDH}}(u, m^{-1}v)$

Figure 10: ICDH adversary  $B$  can perfectly simulate the OW-PCA game for  $A$

First observe that the simulated PCO is exactly the same as a true PCO:

$$\begin{aligned}
 \text{PCO}(m, c = (u, v)) &= 1 \\
 \Leftrightarrow m &= \text{Dec}(\text{sk}, c = (u, v)) \\
 \Leftrightarrow m &= u^{-x}v \\
 \Leftrightarrow u^x &= m^{-1}v \\
 \Leftrightarrow \mathcal{O}^{\text{DDH}}(u, m^{-1}v) &= 1
 \end{aligned}$$

Second notice that in the OW-PCA game,  $m^* \xleftarrow{\$} \mathbb{Z}_q$  is a uniformly random element in  $\mathbb{Z}_q$ , which means that  $v \leftarrow m \cdot (g^x)^y$  is a uniformly random element in  $\mathbb{Z}_q$ . When  $B$  simulates the OW-PCA game for  $A$ , it can simply sample a random value for  $v$  in the

challenge ciphertext, and  $A$  will have retained its advantage in recovering the correct decryption without the secret key.

If  $A$  succeeds in recovering the correct decryption while being run by  $B$ , then  $\hat{m} = u^{-x}v$ , which means that  $\hat{m}^{-1}v = u^x \cdot v^{-1} \cdot v = u^x = (g^y)x = g^{xy}$ . In this case,  $B$  successfully computes  $g^{xy}$  and wins the ICDH game. Therefore, the advantage of  $A$  is at most the advantage of  $B$ .  $\square$

## 4 Implementation

ML-KEM is an IND-CCA2 secure key encapsulation mechanism standardized by NIST in FIPS 203. The IND-CCA2 security of ML-KEM is achieved in two steps. First, ML-KEM constructs an IND-CPA secure public key encryption scheme K-PKE(KeyGen, Enc, Dec) whose security is based on the conjectured intractability of the module learning with error (MLWE) problems against both classical and quantum adversaries. Then, the  $U_m^x$  variant of the Fujisaki-Okamoto transformation [HHK17] is used to construct the KEM MLKEM(KeyGen, Encap, Decap) by calling K-PKE(KeyGen, Enc, Dec) as sub-routines. Because K-PKE.Enc includes substantially more arithmetics than K-PKE.Dec, by using *re-encryption* and *de-randomization*, ML-KEM’s decapsulation routine incurs significant computational cost.

We implemented the “encrypt-then-MAC” KEM construction using K-PKE as the input PKE and compared its performance against ML-KEM under a variety of scenarios. The experimental data showed that while the “encrypt-then-MAC” construction adds a small amount of computational overhead to the encapsulation routine and a small increase in ciphertext size when compared with ML-KEM, it boasts enormous runtime savings in the decapsulation routine, which makes it particularly suitable for deployment in constrained environment. See appendix 6.1 for comparison with Kyber’s third round submission to NIST’s PQC competition.

A detailed description of K-PKE’s routines can be found in FIPS 203 (TODO: citation). The “encrypt-then-MAC” routines are described in figure 11.

ML-KEM <sup>+</sup> .KeyGen()	ML-KEM <sup>+</sup> .Decap(sk, c)
1: $z \xleftarrow{\$} \{0, 1\}^{256}$ 2: $(pk, sk') \xleftarrow{\$} \text{K-PKE.KeyGen}()$ 3: $h \leftarrow H(pk)$ 4: $sk \leftarrow (sk'    pk    h    z)$ 5: <b>return</b> (pk, sk)	<b>Require:</b> Secret key $sk = (sk'    pk    h    z)$ <b>Require:</b> Ciphertext $c = (c'    t)$ 1: $(sk', pk, h, z) \leftarrow sk$ 2: $(c', t) \leftarrow c$ 3: $\hat{m} \leftarrow \text{K-PKE.Dec}(sk', c')$ 4: $(\bar{K}, \hat{r}, \hat{k}) \leftarrow \text{XOF}(\hat{m}    h)$ 5: $\hat{t} \leftarrow \text{MAC}(\hat{k}, c')$ 6: <b>if</b> $\hat{t} = t$ <b>then</b> 7: $K \leftarrow \text{KDF}(\bar{K}    t)$ 8: <b>else</b> 9: $K \leftarrow \text{KDF}(z    t)$ 10: <b>end if</b> 11: <b>return</b> $K$
ML-KEM <sup>+</sup> .Encap(pk)	
<b>Require:</b> Public key pk 1: $m \xleftarrow{\$} \{0, 1\}^{256}$ 2: $(\bar{K}, r, k) \leftarrow \text{XOF}(m    H(pk))$ 3: $c' \leftarrow \text{K-PKE.Enc}(pk, m, r)$ 4: $t \leftarrow \text{MAC}(k, c')$ 5: $K \leftarrow \text{KDF}(\bar{K}    c')$ 6: $c \leftarrow (c', t)$ 7: <b>return</b> (c, K)	

Figure 11: ML-KEM<sup>+</sup> routines

Our implementation extended from the reference implementation by the PQCrystals team (<https://github.com/pq-crystals/kyber>). All C code is compiled with GCC 11.4.1 and OpenSSL 3.0.8. All binaries are executed on an AWS c7a.medium instance with an AMD EPYC 9R14 CPU at 3.7 GHz and 1 GB of RAM.

#### 4.1 Choosing a message authenticator

For the ML-KEM<sup>+</sup> implementation, we instantiated MAC with a selection that covered a wide range of MAC designs, including Poly1305 [Ber05], GMAC [MV04], CMAC [IK03][BR05], and KMAC [KCP16].

Poly1305 and GMAC are both Carter-Wegman style authenticators that compute the tag using finite field arithmetic. Generically speaking, Carter-Wegman MAC is parameterized by some finite field  $\mathbb{F}$  and the maximal message length  $L > 0$ . Each symmetric key  $k = (k_1, k_2) \xleftarrow{\$} \mathbb{F}^2$  is a pair of uniformly random field elements, and the message is parsed into tuples of field elements up to length  $L$ :  $m = (m_1, m_2, \dots, m_l) \in \mathbb{F}^{\leq L}$ . The tag  $t$  is computed by evaluating a polynomial whose coefficients are the message blocks and whose indeterminate is the key:

$$\text{MAC}((k_1, k_2), m) = H_{\text{xpoly}}(k_1, m) + k_2 \quad (1)$$

Where  $H_{\text{xpoly}}$  is given by:

$$H_{\text{xpoly}}(k_1, m) = k_1^{l+1} + k_1^l \cdot m_1 + k_1^{l-1} \cdot m_2 + \dots + k_1 \cdot m_l$$

The authenticator formulated in equation 1 is a one-time MAC. To make the construction many-time secure, a non-repeating nonce  $r$  and a PRF is needed:

$$\text{MAC}((k_1, k_2), m, r) = H_{\text{xpoly}}(k_1, m) \oplus \text{PRF}(k_2, r)$$

Specifically, Poly1305 operates in the prime field  $\mathbb{F}_q$  where  $q = 2^{130} - 5$  whereas GMAC operates in the binary field  $\mathbb{F}_{2^{128}}$ . In OpenSSL's implementation, standalone Poly1305 is a one-time secure MAC, whereas GMAC uses a nonce and AES as the PRF and is thus many-time secure (in OpenSSL GMAC is AES-256-GCM except all data is fed into the "associated data" section and thus not encrypted).

CMAC is based on the CBC-MAC with the block cipher instantiated from AES-256. To compute a CMAC tag, the message is first broken into 128-bit blocks with appropriate padding. Each block is first XOR'd with the previous block's output, then encrypted under AES using the symmetric key. The final output is XOR'd with a sub key derived from the symmetric key, before being encrypted for one last time. A summary of the computation can be found in figure 12

KMAC is defined in NIST SP 800-185 to be based on the family of sponge functions with Keccak permutation as the underlying function. We chose KMAC-256, which uses Shake256 as the underlying extendable output functions. KMAC allows variable-length key and tag, but we chose the 256 bits for key length and 128 bits for tag size for consistency with other authenticators.

To isolate the performance characteristics of each authenticator in our instantiation of ML-KEM<sup>+</sup>, we measured the CPU cycles needed for each authenticator to compute a tag on random inputs whose sizes correspond to the ciphertext sizes of ML-KEM. The measurements are summarized in table 3.

Sub-key derivation	CMAC(k, m)
<b>Require:</b> 256-bit key $k$ <b>Require:</b> $\text{const\_Rb} = 0x87$ 1: $l \leftarrow \text{AES-256}(k, 0^{128})$ 2: <b>if</b> $\text{MostSignificantBit}(l) = 0$ <b>then</b> 3: $k_1 \leftarrow 1 \ll 1$ 4: <b>else</b> 5: $k_1 \leftarrow 1 \ll 1 \oplus \text{const\_Rb}$ 6: <b>end if</b> 7: <b>if</b> $\text{MostSignificantBit}(k_1) = 0$ <b>then</b> 8: $k_2 \leftarrow k_1 \ll 1$ 9: <b>else</b> 10: $k_2 \leftarrow k_1 \ll 1 \oplus \text{const\_Rb}$ 11: <b>end if</b> 12: <b>return</b> $k_1, k_2$	<b>Require:</b> 256-bit symmetric key $k$ 1: $(k_1, k_2) \leftarrow \text{deriveSubKey}(k)$ 2: $n \leftarrow \lceil \text{bytesLen}(m)/16 \rceil$ 3: <b>if</b> $n = 0$ <b>then</b> 4: $n \leftarrow 1$ 5: $m_{\text{last}} \leftarrow m_n \oplus k_2$ 6: <b>else if</b> $\text{bytesLen}(m) \bmod 16 = 0$ <b>then</b> 7: $m_{\text{last}} \leftarrow m_n \oplus k_1$ 8: <b>else</b> 9: $m_{\text{last}} \leftarrow m_n \oplus k_2$ 10: <b>end if</b> 11: $x = 0^{128}$ 12: <b>for</b> $i \in \{1, 2, \dots, n-1\}$ <b>do</b> 13: $y \leftarrow x \oplus m_i$ 14: $x \leftarrow \text{AES-256}(k, y)$ 15: <b>end for</b> 16: $y \leftarrow m_{\text{last}} \oplus x$ 17: $t \leftarrow \text{AES-256}(k, y)$ 18: <b>return</b> $t$

Figure 12: AES-256 CMAC

Table 3: CPU cycles needed to compute tag on various input sizes

Input size: 768 bytes			Input size: 1088 bytes			Input size: 1568 bytes		
MAC	Median	Average	MAC	Median	Average	MAC	Median	Average
Poly1305	909	2823	Poly1305	961	2704	Poly1305	1065	1809
GMAC	3899	4859	GMAC	3899	4827	GMAC	4055	5026
CMAC	6291	6373	CMAC	7305	7588	CMAC	8735	8772
KMAC	6373	7791	KMAC	9697	9928	KMAC	11647	12186

## 4.2 KEM performance

Compared to the  $U_m^{\mathcal{K}}$  variant of Fujisaki-Okamoto transformed used in ML-KEM, the “encrypt-then-MAC” transformation the following trade-off when given the same input sub-routines:

- Both encapsulation and decapsulation add a small amount of overhead for needing to hash both the PKE plaintext and the PKE ciphertext when deriving the shared secret, where as the  $U_m^{\mathcal{K}}$  transformation only needs to hash the PKE plaintext.
- The encapsulation routine adds a small amount of run-time overhead for computing the authenticator
- The decapsulation routine enjoys substantial runtime speedup because *re-encryption* is replaced with computing an authenticator
- Ciphertext size increases by the size of an authenticator

Since  $\text{K-PKE.Enc}$  carries significantly more computational complexity than  $\text{K-PKE.Dec}$  or any MAC we chose, the performance advantage of the “encrypt-then-MAC” transformation over the  $U_m^{\mathcal{K}}$  transformation is dominated by the runtime saving gained from replacing *re-encryption* with MAC. A comparison between ML-KEM and variations of the ML-KEM-ETM can be found in table 4

Table 4: CPU cycles of each KEM routine

128-bit security		KEM variant	Encap cycles/tick		Decap cycles/tick	
size parameters (bytes)			Median	Average	Median	Average
pk size	800	ML-KEM-512	91467	92065	121185	121650
sk size	1632	Kyber512	97811	98090	119937	120299
ct size	768	ML-KEM-512 <sup>+</sup> w/ Poly1305	93157	93626	33733	33908
KeyGen cycles/tick		ML-KEM-512 <sup>+</sup> w/ GMAC	97369	97766	37725	37831
Median	75945	ML-KEM-512 <sup>+</sup> w/ CMAC	99739	99959	40117	39943
Average	76171	ML-KEM-512 <sup>+</sup> w/ KMAC	101009	101313	40741	40916

  

192-bit security		KEM variant	Encap cycles/tick		Decap cycles/tick	
size parameters (bytes)			Median	Average	Median	Average
pk size	1184	ML-KEM-768	136405	147400	186445	187529
sk size	2400	Kyber768	153061	153670	182129	182755
ct size	1088	ML-KEM-768 <sup>+</sup> w/ Poly1305	146405	146860	43315	43463
KeyGen cycles/tick		ML-KEM-768 <sup>+</sup> w/ GMAC	149525	150128	46513	46706
Median	129895	ML-KEM-768 <sup>+</sup> w/ CMAC	153139	153735	49841	50074
Average	130650	ML-KEM-768 <sup>+</sup> w/ KMAC	155219	155848	52415	52611

  

256-bit security		KEM variant	Encap cycles/tick		Decap cycles/tick	
size parameters (bytes)			Median	Average	Median	Average
pk size	1568	ML-KEM-1024	199185	199903	246245	247320
sk size	3168	Kyber1024	222351	223260	258231	259067
ct size	1568	ML-KEM-1024 <sup>+</sup> w/ Poly1305	205763	206499	51375	51562
KeyGen cycles/tick		ML-KEM-1024 <sup>+</sup> w/ GMAC	208805	209681	54573	54780
Median	194921	ML-KEM-1024 <sup>+</sup> w/ CMAC	213667	214483	59175	59408
Average	195465	ML-KEM-1024 <sup>+</sup> w/ KMAC	216761	217468	62269	62516

### 4.3 Key exchange protocols

A common application of key encapsulation mechanism is key exchange protocols, where two parties establish a shared secret using a public channel. [BDK<sup>+</sup>18] described three key exchange protocols: unauthenticated key exchange (KE), unilaterally authenticated key exchange (UAKE), and mutually authenticated key exchange (AKE). We instantiated an implementation for each of the three key exchange protocols using different variations of the “encrypt-then-MAC” KEM and compared round trip time with implementations instantiated using ML-KEM.

For clarity, we denote the party who sends the first message to be the client and the other party to be the server. Round trip time (RTT) is defined to be the time interval between the moment before the client starts generating ephemeral keypairs and the moment after the client derives the final session key. All experiments are run on a pair of AWS c7a.medium instances both located in the us-west-2 region. For each experiment, a total of 10,000 rounds of key exchange are performed, with the median and average round trip time (measured in microsecond) recorded.

#### 4.3.1 Unauthenticated key exchange (KE)

In unauthenticated key exchange, a single pair of ephemeral keypair  $(pk_e, sk_e) \xleftarrow{\$} \text{KeyGen}()$  is generated by the client. The client transmits the ephemeral public key  $pk_e$  to the server, who runs the encapsulation routine  $(c_e, K_e) \xleftarrow{\$} \text{Encap}(pk_e)$  and transmits the ciphertext  $c_e$  back to the client. The client finally decapsulates the ciphertext to recover the shared secret  $K_e \leftarrow \text{Decap}(sk_e, c_e)$ . The key exchange routines are summarized in figure 13.

Note that in our implementation, a key derivation function (KDF) is applied to the ephemeral shared secret to derive the final session key. This step is added to maintain consistency with other authenticated key exchange protocols, where the final session key is derived from multiple shared secrets. The key derivation function is instantiated using Shake256, and the final session key is 256 bits in length.

$\text{KE}_C()$	$\text{KE}_S()$
1: $(\text{pk}_e, \text{sk}_e) \xleftarrow{\$} \text{KeyGen}()$	1: $\text{pk}_e \leftarrow \text{read}()$
2: $\text{send}(\text{pk}_e)$	2: $(c_e, K_e) \xleftarrow{\$} \text{Encap}(\text{pk}_e)$
3: $c_e \leftarrow \text{read}()$	3: $\text{send}(c_e)$
4: $K_e \leftarrow \text{Decap}(\text{sk}_e, c_e)$	4: $K \leftarrow \text{KDF}(K_e)$
5: $K \leftarrow \text{KDF}(K)$	5: <b>return</b> $K$
6: <b>return</b> $K$	

Figure 13: Unauthenticated key exchange (KE) routines

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The RTT comparison is summarized in table 5

Table 5: KE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-512	800	768	92	97
ML-KEM-512 <sup>+</sup> w/ Poly1305	800	784	70	72
ML-KEM-512 <sup>+</sup> w/ GMAC	800	784	73	76
ML-KEM-512 <sup>+</sup> w/ CMAC	800	784	75	79
ML-KEM-512 <sup>+</sup> w/ KMAC	800	784	76	78

  

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-768	1184	1088	135	140
ML-KEM-768 <sup>+</sup> w/ Poly1305	1184	1104	99	104
ML-KEM-768 <sup>+</sup> w/ GMAC	1184	1104	101	105
ML-KEM-768 <sup>+</sup> w/ CMAC	1184	1104	103	109
ML-KEM-768 <sup>+</sup> w/ KMAC	1184	1104	103	107

  

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-1024	1568	1568	193	199
ML-KEM-1024 <sup>+</sup> w/ Poly1305	1568	1584	138	141
ML-KEM-1024 <sup>+</sup> w/ GMAC	1568	1584	140	145
ML-KEM-1024 <sup>+</sup> w/ CMAC	1568	1584	143	148
ML-KEM-1024 <sup>+</sup> w/ KMAC	1568	1584	144	149

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### 4.3.2 Unilaterally authenticated key exchange (UAKE)

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In unilaterally authenticated key exchange, the authenticating party proves its identity to the other party by demonstrating possession of a secret key that corresponds to a published long-term public key. In this implementation, the client possesses the long-term public key  $\text{pk}_S$  of the server, and the server authenticates itself by demonstrating possession of the corresponding long-term secret key  $\text{sk}_S$ . UAKE routines are summarized in figure 14.

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In addition to the long-term key, the client will also generate an ephemeral keypair as it does in an unauthenticated key exchange, and the session key is derived by applying the KDF to the concatenation of both the ephemeral shared secret and the shared secret encapsulated under server’s long-term key. This helps the key exchange to achieve weak forward secrecy (citation needed).

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Using KEM for authentication is especially interesting within the context of post-quantum cryptography: post-quantum KEM schemes usually enjoy better performance characteristics than post-quantum signature schemes with faster runtime, smaller memory

406



407 footprint, and smaller communication sizes. KEMTLS was proposed in 2020 as an  
 408 alternative to existing TLS handshake protocols, and many experimental implementations  
 409 have demonstrated the performance advantage. (citation needed).

UAKE <sub>c</sub> (pk <sub>S</sub> )	UAKE <sub>s</sub> (sk <sub>S</sub> )
<b>Require:</b> Server's long-term pk <sub>S</sub>	<b>Require:</b> Server's long-term sk <sub>S</sub>
1: (pk <sub>e</sub> , sk <sub>e</sub> ) $\xleftarrow{\$}$ KeyGen()	1: (pk <sub>e</sub> , c <sub>S</sub> ) $\leftarrow$ read()
2: (c <sub>S</sub> , K <sub>S</sub> ) $\xleftarrow{\$}$ Encap(pk <sub>S</sub> )	2: K <sub>S</sub> $\leftarrow$ Decap(sk <sub>S</sub> , c <sub>S</sub> )
3: send(pk <sub>e</sub> , c <sub>S</sub> )	3: (c <sub>e</sub> , K <sub>e</sub> ) $\xleftarrow{\$}$ Encap(pk <sub>e</sub> )
4: c <sub>e</sub> $\leftarrow$ read()	4: send(c <sub>e</sub> )
5: K <sub>e</sub> $\leftarrow$ Decap(sk <sub>e</sub> , c <sub>e</sub> )	5: K $\leftarrow$ KDF(K <sub>e</sub>   K <sub>S</sub> )
6: K $\leftarrow$ KDF(K <sub>e</sub>   K <sub>S</sub> )	6: return K
7: return K	

Figure 14: Unilaterally authenticated key exchange (UAKE) routines

Table 6: UAKE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-512	1568	768	145	151
ML-KEM-512 <sup>+</sup> w/ Poly1305	1584	784	103	106
ML-KEM-512 <sup>+</sup> w/ GMAC	1584	784	106	110
ML-KEM-512 <sup>+</sup> w/ CMAC	1584	784	108	112
ML-KEM-512 <sup>+</sup> w/ KMAC	1584	784	109	113

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-768	2272	1088	215	222
ML-KEM-768 <sup>+</sup> w/ Poly1305	2288	1104	144	150
ML-KEM-768 <sup>+</sup> w/ GMAC	2288	1104	149	156
ML-KEM-768 <sup>+</sup> w/ CMAC	2288	1104	153	160
ML-KEM-768 <sup>+</sup> w/ KMAC	2288	1104	154	159

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-1024	3136	1568	310	318
ML-KEM-1024 <sup>+</sup> w/ Poly1305	3152	1584	202	209
ML-KEM-1024 <sup>+</sup> w/ GMAC	3152	1584	212	228
ML-KEM-1024 <sup>+</sup> w/ CMAC	3152	1584	212	218
ML-KEM-1024 <sup>+</sup> w/ KMAC	3152	1584	213	220

### 410 4.3.3 Mutually authenticated key exchange (AKE)

411 Mutually authenticated key exchange is largely identical to unilaterally authenticated  
 412 key exchange, except for that client authentication is required. This means that client  
 413 possesses server's long-term public key and its own long-term secret key, while the server  
 414 possesses client's long-term public key and its own long-term secret key. The session key  
 415 is derived by applying KDF onto the concatenation of shared secrets produced under the  
 416 ephemeral keypair, server's long-term keypair, and client's long-term keypair, in this order.

$\text{AKE}_C(\text{pk}_S, \text{sk}_C)$	$\text{AKE}_S(\text{sk}_S, \text{pk}_C)$
<b>Require:</b> Server’s long-term $\text{pk}_S$	<b>Require:</b> Server’s long-term $\text{sk}_S$
<b>Require:</b> Client’s long-term $\text{sk}_C$	<b>Require:</b> Client’s long-term $\text{pk}_C$
1: $(\text{pk}_e, \text{sk}_e) \xleftarrow{\$} \text{KeyGen}()$	1: $(\text{pk}_e, c_S) \leftarrow \text{read}()$
2: $(c_S, K_S) \xleftarrow{\$} \text{Encap}(\text{pk}_S)$	2: $K_S \leftarrow \text{Decap}(\text{sk}_S, c_S)$
3: <b>send</b> $(\text{pk}_e, c_S)$	3: $(c_e, K_e) \xleftarrow{\$} \text{Encap}(\text{pk}_e)$
4: $(c_e, c_C) \leftarrow \text{read}()$	4: $(c_C, K_C) \xleftarrow{\$} \text{Encap}(\text{pk}_C)$
5: $K_e \leftarrow \text{Decap}(\text{sk}_e, c_e)$	5: <b>send</b> $(c_e, c_C)$
6: $K_C \leftarrow \text{Decap}(\text{sk}_e, c_C)$	6: $K \leftarrow \text{KDF}(K_e \  K_S \  K_C)$
7: $K \leftarrow \text{KDF}(K_e \  K_S \  K_C)$	7: <b>return</b> $K$
8: <b>return</b> $K$	

Figure 15: Mutually authenticated key exchange (AKE) routines

Table 7: AKE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-512	1568	1536	220	213
ML-KEM-512 <sup>+</sup> w/ Poly1305	1584	1568	133	138
ML-KEM-512 <sup>+</sup> w/ GMAC	1584	1568	139	143
ML-KEM-512 <sup>+</sup> w/ CMAC	1584	1568	143	148
ML-KEM-512 <sup>+</sup> w/ KMAC	1584	1568	145	151

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-768	2272	2176	294	301
ML-KEM-768 <sup>+</sup> w/ Poly1305	2288	2208	190	196
ML-KEM-768 <sup>+</sup> w/ GMAC	2288	2208	197	210
ML-KEM-768 <sup>+</sup> w/ CMAC	2288	2208	202	208
ML-KEM-768 <sup>+</sup> w/ KMAC	2288	2208	204	210

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-1024	3136	3136	512	511
ML-KEM-1024 <sup>+</sup> w/ Poly1305	3152	3168	266	273
ML-KEM-1024 <sup>+</sup> w/ GMAC	3152	3168	273	282
ML-KEM-1024 <sup>+</sup> w/ CMAC	3152	3168	280	287
ML-KEM-1024 <sup>+</sup> w/ KMAC	3152	3168	282	288

## 5 Conclusions and future works

The “encrypt-then-MAC” transformation is a generic KEM construction that achieves IND-CCA2 security under the random oracle model if the input PKE is OW-PCA secure. Compared to the Fujisaki-Okamoto transformation, our construction replaced *de-randomization* and *re-encryption* with a message authenticator. At the cost of some minimal increase in communication size and encapsulation runtime, our construction achieves significant efficiency gains in the decapsulation routine. In practical key exchange protocols, our construction saves between 35-45% in round trip time.

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## 6 Appendix

### 6.1 Performance comparison between ML-KEM<sup>+</sup> and Kyber

ML-KEM directly evolved from CRYSTALS-Kyber’s third round submission to NIST’s post quantum cryptography competition. While their IND-CPA subroutines (see figure 16) are identical, ML-KEM deviated from Kyber by choosing a different variant of the Fujisaki-Okamoto transformation.

K-PKE.KeyGen()	K-PKE.Enc(pk, m)	K-PKE.Dec(sk, c)
1: $A \xleftarrow{\$} R_q^{k \times k}$	<b>Ensure:</b> $\text{pk} = (A, \mathbf{t})$	<b>Ensure:</b> $c = (c_1, c_2)$
2: $\mathbf{s} \xleftarrow{\$} \mathcal{X}_{\eta_1}^k$	<b>Ensure:</b> $m \in R_2$	<b>Ensure:</b> $\text{sk} = \mathbf{s}$
3: $\mathbf{e} \xleftarrow{\$} \mathcal{X}_{\eta_1}^k$	1: $\mathbf{r} \xleftarrow{\$} \mathcal{X}_{\eta_1}^k$	1: $\hat{m} \leftarrow c_2 - \mathbf{c}_1^\top \cdot \mathbf{s}$
4: $\mathbf{t} \leftarrow A\mathbf{s} + \mathbf{e}$	2: $\mathbf{e}_1 \xleftarrow{\$} \mathcal{X}_{\eta_2}^k$	2: $\hat{m} \leftarrow \text{Round}(\hat{m})$
5: $\text{pk} \leftarrow (A, \mathbf{t})$	3: $e_2 \xleftarrow{\$} \mathcal{X}_{\eta_2}$	3: <b>return</b> $\hat{m}$
6: $\text{sk} \leftarrow \mathbf{s}$	4: $\mathbf{c}_1 \leftarrow A\mathbf{r} + \mathbf{e}_1$	
7: <b>return</b> (pk, sk)	5: $c_2 \leftarrow \mathbf{t}^\top \mathbf{r} + e_2 + m \cdot \lfloor \frac{q}{2} \rfloor$	
	6: <b>return</b> (c <sub>1</sub> , c <sub>2</sub> )	

Figure 16: K-PKE routines are identical between Kyber and ML-KEM

CRYSTALS-Kyber uses the  $U^\perp$  variant, where the shared secret is derived from both the plaintext and the ciphertext. On the other hand, because by using *re-encryption* and *de-randomization*, the PKE is already made *rigid*, the CRYSTALS-Kyber team decided to use the  $U_m^\perp$  variant, where the shared secret is derived from the plaintext alone.

KEM.KeyGen()	KEM.Decap(sk, c)
1: $z \xleftarrow{\$} \{0, 1\}^{256}$ 2: $(pk, sk') \xleftarrow{\$} \text{PKE.KeyGen}()$ 3: $sk \leftarrow (sk'    pk    H(pk)    z)$ 4: <b>return</b> (pk, sk)	<b>Ensure:</b> $sk = (sk'    pk    H(pk)    z)$ 1: $\hat{m} \leftarrow \text{PKE.Dec}(sk', c)$ 2: $(\bar{K}, \hat{r}) \leftarrow G(\hat{m}    H(pk))$ 3: <b>if</b> $\text{PKE.Enc}(pk, \hat{m}, \hat{r}) = c$ <b>then</b> 4: $K \leftarrow \text{KDF}(\bar{K}, H(c)) \quad \triangleright U^\mathcal{X}$ 5: $K \leftarrow \bar{K} \quad \triangleright U_m^\mathcal{X}$ 6: <b>else</b> 7: $K \leftarrow \text{KDF}(z    H(c))$ 8: <b>end if</b> 9: <b>return</b> K
KEM.Encap(pk)	
1: $m \xleftarrow{\$} \{0, 1\}^{256}$ 2: $(\bar{K}, r) \leftarrow G(m    H(pk))$ 3: $c \leftarrow \text{PKE.Enc}(pk, m, r)$ 4: $K \leftarrow \text{KDF}(\bar{K}    H(c)) \quad \triangleright U^\mathcal{X}$ 5: $K \leftarrow \bar{K} \quad \triangleright U_m^\mathcal{X}$ 6: <b>return</b> (c, K)	

Figure 17: Kyber uses  $U^\mathcal{X}$  variant. ML-KEM uses  $U_m^\mathcal{X}$  variant.

532 The reason for ML-KEM to use a different variant of the Fujisaki-Okamoto trans-  
533 formation is two-fold. The first reason is performance: using the  $U_m^\mathcal{X}$  trans-  
534 formation saves the need to hash the ciphertext, and since Kyber/ML-KEM’s performance is mainly  
535 bottlenecked by the symmetric components, omitting the hash leads to significant runtime  
536 savings (up to 17% in AVX-2 optimized implementations). The second reason is the  
537 simplified security proof and tighter security bounds of the  $U_m^\mathcal{X}$  variant compared to the  
538  $U^\mathcal{X}$  variant. We will omit the details of the security proof and refer readers to [HHK17].

539 In section 4, we mainly compared ML-KEM<sup>+</sup> with ML-KEM, but we would like to point  
540 out that, because Kyber uses the  $U^\mathcal{X}$  variant and needs to hash the ciphertext for deriving  
541 the shared secret, the performance advantage of ML-KEM<sup>+</sup> over Kyber will be even greater.