

# Faster generic IND-CCA2 secure KEM using “encrypt-then-MAC”

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**Abstract.** The modular Fujisaki-Okamoto (FO) transformation takes public-key encryption with weaker security and constructs a key encapsulation mechanism (KEM) with indistinguishability under adaptive chosen ciphertext attacks. While the modular FO transform enjoys tight security bound and quantum resistance, it also suffers from computational inefficiency and vulnerabilities to side-channel attacks due to using de-randomization and re-encryption for providing ciphertext integrity. In this work, we propose an alternative KEM construction that achieves ciphertext integrity using a message authentication code (MAC) and instantiate a concrete instance using Kyber. Our experimental results showed that where the encryption routine incurs heavy computational cost, replacing re-encryption with MAC provides substantial performance improvements at comparable security level.

**Keywords:** Key encapsulation mechanism, post-quantum cryptography, lattice cryptography, Fujisaki-Okamoto transformation

## 1 Introduction

Key encapsulation mechanism (KEM) is a cryptographic primitive that allows two parties to establish a shared secret over an insecure channel. The combination of KEM and some data encapsulation mechanism (DEM), such as AES-GCM and ChaCha20-Poly1305, is the foundation of many of today’s most popular secure communication protocols such as Transport Layer Security (TLS) and Secure Shell (SSH). The commonly accepted security standard of a KEM is *Indistinguishability under adaptive chosen-ciphertext attack* (IND-CCA2): no efficient adversary can distinguish a shared secret obtained by running the encapsulation routine from random noise, even with access to a decapsulation oracle throughout the attack. KEM is related to another important cryptographic primitive called public-key encryption (PKE), and their security standards are similar. The desired security standard for PKE, also called IND-CCA2, requires that no efficient adversary can distinguish the encryption of two adversarially chosen messages even with access to decryption oracle.

It is difficult to build a provably IND-CCA2 secure KEM from scratch. Instead, secure KEMs are usually built on top of a PKE with weaker security property (e.g. being only OW-CPA or IND-CPA secure, not IND-CCA2). One such construction is the Fujisaki-Okamoto transformation, proposed in 1999 by Fujisaki Eiichiro and Okamoto Tetsuyuki in their seminal paper [FO99][FO13]. The first Fujisaki-Okamoto transformation combines an OW-CPA secure PKE with an IND-CPA secure symmetric cipher into a hybrid PKE (HPKE) with proven IND-CCA2 security under the random oracle model. Subsequent proposals such as [OP01], [CHJ<sup>+</sup>02], and [Den03] improved on the original proposal and adapted it to build KEM instead of HPKE. This line of work culminated in a landmark publication in 2017 by Hofheinz, Hovelmann, and Kiltz [HHK17a][HHM22], where the authors provided a versatile variety of modular KEM constructions with tight security reduction in the random oracle model and non-tight security reduction in the quantum random oracle model.

The modular Fujisaki-Okamoto KEM transformation is remarkably successful. It was adopted by many submissions to NIST’s post-quantum cryptography competition, including Kyber [BDK<sup>+</sup>18a], Saber [DKRV18], FrodoKEM [BCD<sup>+</sup>16], and classic McEliece [ABC<sup>+</sup>20] among others. When Kyber was standardized by NIST in FIPS 203 “Module-lattice key-encapsulation mechanism” (ML-KEM) [oST24], it kept the Fujisaki-Okamoto transformation in its KEM construction. However, the Fujisaki-Okamoto transformation is not perfect. Among its shortcomings is the use of *de-randomization* (transform a randomized encryption routine into a deterministic routine by using a pseudorandom coin derived from the input message) and *re-encryption* (the decapsulation routine of the output KEM runs the encryption routine of the input PKE to ensure ciphertext integrity), which causes two problems:

- **computational inefficiency:** where the PKE’s encryption routine is substantially more expensive than the decryption routine, using re-encryption causes the decapsulation routine in the output KEM to become computationally expensive
- **side-channel vulnerability:** running the input PKE’s encryption routine in the output KEM’s decapsulation routine introduces risk of side-channel vulnerabilities not found in the input PKE’s decryption routine alone. In fact, many practical attacks [UXT<sup>+</sup>22][RRCB19] exploit re-encryption to decrypt ciphertext or recover secret keys. Countermeasures such as masking have been proposed to address these side channels, but they inevitably carry substantial performance penalty.

## 1.1 Our contributions

Our main contribution is a novel generic construction that combines a PKE with weaker security property and a one-time secure message authentication code (MAC) into an IND-CCA2 secure KEM in the random oracle model. Specifically, we require the input PKE to be one-way secure against plaintext-checking attacks (OW-PCA): no efficient adversary can recover the decryption of a random encryption with access to a plaintext-checking oracle (PCO) that, when queried on a plaintext-ciphertext pair  $(m, c)$ , answers  $m$  is the decryption of  $c$ . While OW-PCA is not a standard security definition, it has appeared useful in past IND-CCA2 KEM constructions [OP01][CHJ<sup>+</sup>02], and plays an important role in the modularity of the Fujisaki-Okamoto KEM transformation.

Our KEM construction is inspired by how symmetric cryptography achieves IND-CCA2 security (or equivalently, authenticated encryption [Kra01]) using the “encrypt-then-MAC” pattern. We applied “encrypt-then-MAC” to the construction of the KEM: at encapsulation, a symmetric key is derived from hashing a random PKE plaintext, then used to compute an authenticator against the PKE ciphertext; at decapsulation, the same symmetric key is derived from hashing the decryption of the PKE ciphertext, then used to verify the authenticator. Intuitively, for an adversary to be able to produce a valid authenticator, it must know the correct symmetric key and thus the corresponding PKE plaintext. In other words, the adversary either produced the ciphertext honestly, or have broken the one-wayness of the input PKE.

### 1.1.1 Performance improvements

The main advantage of our KEM construction over the Fujisaki-Okamoto transformation is the performance gains: our construction replaces re-encryption with computing a symmetric message authenticator, which is significantly faster, especially for one-time MAC. At the cost of computing an authenticator in encapsulation and increasing the ciphertext size by a message authenticator, our construction speeds up decapsulation by 10x.

When instantiated with the underlying PKE routines of ML-KEM and the Poly1305 message authenticator, our construction ML-KEM<sup>+</sup> achieves on average 72%-80% reduction

of CPU cycles needed for decapsulation while only incurring 2%-7% increase of CPU cycles for encapsulation when compared to ML-KEM.

We also implemented and measured the round trip time of key exchange protocols with various modes of authentication. When compared to ML-KEM, ML-KEM<sup>+</sup> achieves 24%-28% reduction of round trip time in unauthenticated key exchange, 29%-35% reduction in unilaterally authenticated key exchange, and 35%-48% reduction in mutually authenticated key exchange.

## 1.2 Related works

A similar construction was proposed by Abdulla et al [ABR01], though our construction builds a KEM instead of a HPKE, and our construction is generic over all OW-PCA secure PKE.

## 2 Preliminaries and previous results

### 2.1 Public-key encryption scheme

**Syntax.** A public-key encryption scheme  $\text{PKE}(\text{KeyGen}, \text{Enc}, \text{Dec})$  is a collection of three routines defined over some plaintext space  $\mathcal{M}$  and some ciphertext space  $\mathcal{C}$ .  $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{KeyGen}()$  is a randomized routine that returns a keypair. The encryption routine  $\text{Enc} : (\text{pk}, m) \mapsto c$  encrypts the input plaintext under the input public key. The decryption routine  $\text{Dec} : (\text{sk}, c) \mapsto m$  decrypts the input ciphertext under the input secret key. Where the encryption routine is randomized, we denote the randomness by  $r \in \mathcal{R}$ , where  $\mathcal{R}$  is called the coin space. The decryption routine is assumed to always be deterministic. Some decryption routines can detect malformed ciphertext and output the rejection symbol  $\perp$  accordingly.

**Correctness.** Following the definition in [DNR04] and [HHK17b], a PKE is  $\delta$ -correct if:

$$E \left[ \max_{m \in \mathcal{M}} P \left[ \text{Dec}(\text{sk}, c) \neq m \mid c \xleftarrow{\$} \text{Enc}(\text{pk}, m) \right] \right] \leq \delta$$

Where the expectation is taken with respect to the probability distribution of all possible keypairs  $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{PKE}.\text{KeyGen}()$ . For many lattice-based cryptosystems, including ML-KEM, decryption failures could leak information about the secret key, although the probability of a decryption failure is low enough that classical adversaries cannot exploit decryption failure more than they can defeat the underlying lattice problem (see table 1).

Table 1: Estimated probability of decryption failure in ML-KEM

	ML-KEM-512	ML-KEM-768	ML-KEM-1024
$\delta$	???	???	???

On the other hand, a quantum adversary may be able to exploit decryption failure in reasonable runtime by efficiently searching through all possible inputs using Grover's search algorithm. For that, ML-KEM made slight modifications in its KEM construction to prevent quantum adversary from precomputing large lookup table. We refer readers to [ABD<sup>+</sup>19] and [BDK<sup>+</sup>18b] for the details.

**Security.** We discuss the security of a PKE using the sequence of games described in [Sho04]. Specifically, we first define the OW-ATK as they pertain to a public key encryption scheme. In later section we will define the IND-CCA game as it pertains to a key encapsulation mechanism.

The OW-ATK game	
1: $(\mathbf{pk}, \mathbf{sk}) \xleftarrow{\$} \text{KeyGen}(1^\lambda)$	
2: $m^* \xleftarrow{\$} \mathcal{M}$	
3: $c^* \xleftarrow{\$} \text{Enc}(\mathbf{pk}, m^*)$	
4: $\hat{m} \xleftarrow{\$} \mathcal{A}^{\mathcal{O}_{\text{ATK}}}(1^\lambda, \mathbf{pk}, c^*)$	$\text{PCO}(m \in \mathcal{M}, c \in \mathcal{C})$
5: <b>return</b> $\llbracket m^* = \hat{m} \rrbracket$	1: <b>return</b> $\llbracket \text{Dec}(\mathbf{sk}, c) = m \rrbracket$

Figure 1: One-way security game of PKE (left) and plaintext-checking oracle (right)

130 In the OW-ATK game (see figure 1), an adversary’s goal is to recover the decryption of a  
 131 randomly generated ciphertext. A challenger randomly samples a keypair and a challenge  
 132 plaintext  $m^*$ , encrypts the challenge plaintext  $c^* \xleftarrow{\$} \text{Enc}(\mathbf{pk}, m^*)$ , then gives  $\mathbf{pk}$  and  $c^*$   
 133 to the adversary  $A$ . The adversary  $A$ , with access to some oracle  $\mathcal{O}_{\text{ATK}}$ , outputs a guess  
 134 decryption  $\hat{m}$ .  $A$  wins the game if its guess  $\hat{m}$  is equal to the challenge plaintext  $m^*$ . The  
 135 *advantage*  $\text{Adv}_{\text{OW-ATK}}$  of an adversary in this game is the probability that it wins the game:

$$\text{Adv}_{\text{OW-ATK}}(A) = P \left[ A(\mathbf{pk}, c^*) = m^* \mid (\mathbf{pk}, \mathbf{sk}) \xleftarrow{\$} \text{KeyGen}(); m^* \xleftarrow{\$} \mathcal{M}; c^* \xleftarrow{\$} \text{Enc}(\mathbf{pk}, m^*) \right]$$

136 The capabilities of the oracle  $\mathcal{O}_{\text{ATK}}$  depends on the choice of security goal ATK. Particu-  
 137 larly relevant to our result is security against plaintext-checking attack (PCA), for which  
 138 the adversary has access to a plaintext-checking oracle (PCO) (see figure 1). A PCO takes  
 139 as input a plaintext-ciphertext pair  $(m, c)$  and returns **True** if  $m$  is the decryption of  $c$  or  
 140 **False** otherwise.

## 141 2.2 Key encapsulation mechanism (KEM)

142 A key encapsulation mechanism is a collection of three routines (**KeyGen**, **Encap**, **Decap**)  
 143 defined over some ciphertext space  $\mathcal{C}$  and some key space  $\mathcal{K}$ . The key generation routine  
 144 takes the security parameter  $1^\lambda$  and outputs a keypair  $(\mathbf{pk}, \mathbf{sk}) \xleftarrow{\$} \text{KeyGen}(1^\lambda)$ . **Encap**( $\mathbf{pk}$ )  
 145 is a probabilistic routine that takes a public key  $\mathbf{pk}$  and outputs a pair of values  $(c, K)$   
 146 where  $c \in \mathcal{C}$  is the ciphertext (also called encapsulation) and  $K \in \mathcal{K}$  is the shared secret  
 147 (also called session key). **Decap**( $\mathbf{sk}, c$ ) is a deterministic routine that takes the secret key  
 148  $\mathbf{sk}$  and the encapsulation  $c$  and returns the shared secret  $K$  if the ciphertext is valid. Some  
 149 KEM constructions use explicit rejection, where if  $c$  is invalid then **Decap** will return a  
 150 rejection symbol  $\perp$ ; other KEM constructions use implicit rejection, where if  $c$  is invalid  
 151 then **Decap** will return a fake session key that depends on the ciphertext and some other  
 152 secret values.

153 The IND-CCA security of a KEM is defined by an adversarial game in which an  
 154 adversary’s goal is to distinguish pseudorandom shared secret (generated by running the  
 155 **Encap** routine) and a truly random value.

KEM-IND-CCA2 game	
1: $(\mathbf{pk}, \mathbf{sk}) \xleftarrow{\$} \text{KeyGen}(1^\lambda)$	
2: $(c^*, K_0) \xleftarrow{\$} \text{Encap}(\mathbf{pk})$	
3: $K_1 \xleftarrow{\$} \mathcal{K}$	
4: $b \xleftarrow{\$} \{0, 1\}$	
5: $\hat{b} \xleftarrow{\$} A^{\mathcal{O}_{\text{Decap}}}(1^\lambda, \mathbf{pk}, c^*, K_b)$	$\mathcal{O}_{\text{Decap}}(c)$
6: <b>return</b> $\llbracket \hat{b} = b \rrbracket$	1: <b>return</b> $\text{Decap}(\mathbf{sk}, c)$

Figure 2: IND-CCA2 game for KEM (left) and decapsulation oracle (right)

156 The decapsulation oracle  $\mathcal{O}^{\text{Decap}}$  takes a ciphertext  $c$  and returns the output of the  
 157 **Decap** routine using the secret key. The advantage  $\epsilon_{\text{IND-CCA}}$  of an IND-CCA adversary  
 158  $\mathcal{A}_{\text{IND-CCA}}$  is defined by

$$\text{Adv}_{\text{IND-CCA}}(A) = \left| P[A^{\mathcal{O}_{\text{Decap}}}(a^\lambda, \mathbf{pk}, c^*, K_b) = b] - \frac{1}{2} \right|$$

## 159 2.3 Message authentication code (MAC)

160 A message authentication code **MAC** is a collection of routines (**Sign**, **Verify**) defined over  
 161 some key space  $\mathcal{K}$ , some message space  $\mathcal{M}$ , and some tag space  $\mathcal{T}$ . The signing routine  
 162 **Sign**( $k, m$ ) takes the secret key  $k \in \mathcal{K}$  and some message, and outputs a tag  $t$ . The  
 163 verification routine **Verify**( $k, m, t$ ) takes the triplet of secret key, message, and tag, and  
 164 outputs 1 if the message-tag pair is valid under the secret key, or 0 otherwise. Many MAC  
 165 constructions are deterministic. For these constructions it is simpler to denote the signing  
 166 routine by  $t \leftarrow \text{MAC}(k, m)$  and perform verification using a simple comparison.

167 The security of a MAC is defined in an adversarial game in which an adversary, with  
 168 access to some signing oracle  $\mathcal{O}_{\text{Sign}}(m)$ , tries to forge a new valid message-tag pair that  
 169 has never been queried before. The existential unforgeability under chosen message attack  
 170 (EUF-CMA) game is shown below:

EUF-CMA game	
1: $k^* \xleftarrow{\$} \mathcal{K}$	
2: $(\hat{m}, \hat{t}) \xleftarrow{\$} \mathcal{A}^{\mathcal{O}_{\text{Sign}}}()$	
3: <b>return</b> $\llbracket \text{Verify}(k^*, \hat{m}, \hat{t}) \wedge (\hat{m}, \hat{t}) \notin \mathcal{O}_{\text{Sign}} \rrbracket$	

Figure 3: The existential forgery game

171 The advantage  $\text{Adv}_{\text{EUF-CMA}}$  of the existential forgery adversary is the probability that it  
 172 wins the EUF-CMA game.

## 173 3 The “encrypt-then-MAC” transformation

174 Let  $\mathcal{B}^*$  denote the set of finite bit strings. Let  $\text{PKE}(\text{KeyGen}, \text{Enc}, \text{Dec})$  be a public-key  
 175 encryption scheme defined over message space  $\mathcal{M}$  and ciphertext space  $\mathcal{C}$ . Let  $\text{MAC} : \mathcal{K}_{\text{MAC}} \times \mathcal{B}^* \rightarrow \mathcal{T}$   
 176 be a deterministic message authentication code that takes a key  $k \in \mathcal{K}_{\text{MAC}}$ ,  
 177 some message  $m \in \mathcal{B}^*$ , and outputs a digest  $t \in \mathcal{T}$ . Let  $G : \mathcal{M} \rightarrow \mathcal{K}_{\text{MAC}}$  be a hash

178 function that maps from PKE’s plaintext space to MAC’s key space. Let  $H : \mathcal{B}^* \rightarrow \mathcal{K}_{\text{KEM}}$   
 179 be a hash function that maps bit strings into the set of possible shared secrets. The  
 180 “encrypt-then-MAC” transformation  $\text{EtM}[\text{PKE}, \text{MAC}, G, H]$  constructs a key encapsulation  
 181 mechanism  $\text{KEM}_{\text{EtM}}(\text{KeyGen}_{\text{KEM}}, \text{Encap}, \text{Decap})$ , whose routines are described in figure 4.

$\text{KEM}_{\text{EtM}}.\text{KeyGen}()$	$\text{KEM}_{\text{EtM}}.\text{Decap}(\text{sk}, c)$
1: $(\text{pk}, \text{sk}') \xleftarrow{\$} \text{PKE}.\text{KeyGen}()$ 2: $z \xleftarrow{\$} \mathcal{M}$ 3: $\text{sk} \leftarrow \text{sk}' \  z$ 4: <b>return</b> $(\text{pk}, \text{sk})$	<b>Require:</b> $c = c' \  t, \text{sk} = \text{sk}' \  z$ <b>Ensure:</b> $c'$ is some PKE ciphertext <b>Ensure:</b> $t$ is some MAC tag <b>Ensure:</b> $\text{sk}'$ is some PKE secret key <b>Ensure:</b> $z$ is some PKE plaintext 1: $(c', t) \leftarrow c$ 2: $(\text{sk}', z) \leftarrow \text{sk}$ 3: $\hat{m} \leftarrow \text{PKE}.\text{Dec}(\text{sk}', c')$ 4: $\hat{k} \leftarrow G(\hat{m})$ 5: <b>if</b> $\text{MAC}(\hat{k}, c') \neq t$ <b>then</b> 6: $K \leftarrow H(z, c')$ 7: <b>else</b> 8: $K \leftarrow H(\hat{m}, c')$ 9: <b>end if</b> 10: <b>return</b> $K$
$\text{KEM}_{\text{EtM}}.\text{Encap}(\text{pk})$	
<b>Ensure:</b> $\text{pk}$ is some PKE public key 1: $m \xleftarrow{\$} \mathcal{M}$ 2: $k \leftarrow G(m)$ 3: $c' \xleftarrow{\$} \text{PKE}.\text{Enc}(\text{pk}, m)$ 4: $t \leftarrow \text{MAC}(k, c')$ 5: $K \leftarrow H(m, c')$ 6: $c \leftarrow c' \  t$ 7: <b>return</b> $(c, K)$	

Figure 4:  $\text{KEM}_{\text{EtM}}$  routines

182 The key generation routine of  $\text{KEM}_{\text{EtM}}$  is largely identical to that of the PKE, only a  
 183 secret value  $z$  is sampled as the implicit rejection symbol. In the encapsulation routine,  
 184 a MAC key is derived from the randomly sampled plaintext  $k \leftarrow G(m)$ , then used  
 185 to sign the unauthenticated ciphertext  $c'$ . Because the encryption routine might be  
 186 randomized, the session key is derived from both the message and the ciphertext. Finally,  
 187 the unauthenticated ciphertext  $c'$  and the tag  $t$  combine into the authenticated ciphertext  
 188  $c$  that would be transmitted to the peer. In the decapsulation routine, the decryption  $\hat{m}$   
 189 of the unauthenticated ciphertext is used to re-derive the MAC key  $\hat{k}$ , which is then used  
 190 to re-compute the tag  $\hat{t}$ . The ciphertext is considered valid if and only if the recomputed  
 191 tag is identical to the input tag.

192 For an adversary  $A$  to produce a valid tag  $t$  for some unauthenticated ciphertext  
 193  $c'$  under the symmetric key  $k \leftarrow G(\text{Dec}(\text{sk}', c'))$  implies that  $A$  must either know the  
 194 symmetric key  $k$  or produce a forgery. Under the random oracle model,  $A$  also cannot  
 195 know  $k$  without knowing its preimage  $\text{Dec}(\text{sk}', c')$ , so  $A$  must either have produced  $c'$   
 196 honestly, or have broken the one-way security of PKE. This means that the decapsulation  
 197 oracle will not give out information on decryptions that the adversary does not already  
 198 know.

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PCO( $m, c$ )

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1:  $k \leftarrow G(m)$ 
2:  $t \leftarrow \text{MAC}(k, c)$ 
3: return  $\llbracket \mathcal{O}^{\text{Decap}}((c, t)) = H(m, c) \rrbracket$ 

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Figure 5: Every decapsulation oracle can be converted into a plaintext-checking oracle

199 However, a decapsulation oracle can still give out some information: for a known  
200 plaintext  $m$ , all possible encryptions  $c' \xleftarrow{\$} \text{Enc}(\text{pk}, m)$  can be correctly signed, while  
201 ciphertexts that don't decrypt back to  $m$  cannot be correctly signed. This means that a  
202 decapsulation oracle can be converted into a plaintext-checking oracle (see figure 5), so  
203 every chosen-ciphertext attack against the KEM can be converted into a plaintext-checking  
204 attack against the underlying PKE.

205 On the other hand, if the underlying PKE is one-way secure against plaintext-checking  
206 attack that makes  $q$  plaintext-checking queries, then “encrypt-then-MAC” KEM is seman-  
207 tically secure under chosen ciphertext attacks making the same number of decapsulation  
208 queries:

209 **Theorem 1.** *For every IND-CCA2 adversary  $A$  against  $\text{KEM}_{\text{ETM}}$  that makes  $q$  decapsulation*  
210 *queries, there exists an OW-PCA adversary  $B$  who makes at least  $q$  plaintext-checking queries*  
211 *against the underlying PKE, and an one-time existential forgery adversary  $C$  against the*  
212 *underlying MAC such that*

$$\text{Adv}_{\text{IND-CCA2}}(A) \leq q \cdot \text{Adv}_{\text{OT-MAC}}(C) + 2 \cdot \text{Adv}_{\text{OW-PCA}}(B)$$

213 Theorem 1 naturally flows into an equivalence relationship between the security of the  
214 KEM and the security of the PKE:

215 **Lemma 1.**  *$\text{KEM}_{\text{ETM}}$  is IND-CCA2 secure if and only if the input PKE is OW-PCA secure*

### 216 3.1 Proof of theorem 1

217 We will prove theorem 1 using a sequence of game. A summary of the the sequence  
218 of games can be found in figure 6 and 7. From a high level we made three incremental  
219 modifications to the IND-CCA2 game for  $\text{KEM}_{\text{ETM}}$ : replace true decapsulation with simulated  
220 decapsulation, replace the pseudorandom MAC key  $k^* \leftarrow G(m^*)$  with a truly random  
221 MAC key  $k^* \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ , and finally replace pseudorandom shared secret  $K_0 \leftarrow H(m^*, c')$   
222 with a truly random shared secret  $K_0 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ . A OW-PCA adversary can then simulate  
223 the modified IND-CCA2 game for the KEM adversary, and the advantage of the OW-PCA  
224 adversary is associated with the probability of certain behaviors of the KEM adversary.

225 *Proof.* *Game 0* is the standard IND-CCA2 game for KEMs. The decapsulation oracle  
226  $\mathcal{O}^{\text{Decap}}$  executes the decapsulation routine using the challenge keypair and return the results  
227 faithfully. The queries made to the hash oracles  $\mathcal{O}^G, \mathcal{O}^H$  are recorded to their respective  
228 tapes  $\mathcal{L}^G, \mathcal{L}^H$ .

229 *Game 1* is identical to game 0 except that the true decapsulation oracle  $\mathcal{O}^{\text{Decap}}$  is replaced  
230 with a simulated oracle  $\mathcal{O}_1^{\text{Decap}}$ . Instead of directly decrypting  $c'$  as in the decapsulation  
231 routine, the simulated oracle searches through the tape  $\mathcal{L}^G$  to find a matching query  $(\tilde{m}, \tilde{k})$   
232 such that  $\tilde{m}$  is the decryption of  $c'$ . The simulated oracle then uses  $\tilde{k}$  to validate the tag  $t$   
233 against  $c'$ .

234 If the simulated oracle accepts the queried ciphertext as valid, then there is a matching  
235 query that also validates the tag, which means that the queried ciphertext is honestly

IND-CCA2 game for $\text{KEM}_{\text{EtM}}$	$\mathcal{O}^{\text{Decap}}(c)$
1: $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{KEM}_{\text{EtM}}.\text{KeyGen}()$ 2: $m^* \xleftarrow{\$} \mathcal{M}$ 3: $c' \xleftarrow{\$} \text{PKE}.\text{Enc}(\text{pk}, m^*)$ 4: $k^* \leftarrow G(m^*)$ $\triangleright$ Game 0-1 5: $k^* \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ $\triangleright$ Game 2-3 6: $t \leftarrow \text{MAC}(k^*, c')$ 7: $c^* \leftarrow c'    t$ 8: $K_0 \leftarrow H(m^*, c')$ $\triangleright$ Game 0-2 9: $K_0 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ $\triangleright$ Game 3 10: $K_1 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ 11: $b \xleftarrow{\$} \{0, 1\}$ 12: $\hat{b} \leftarrow A^{\mathcal{O}^{\text{Decap}}}(\text{pk}, c^*, K_b)$ $\triangleright$ Game 0 13: $\hat{b} \leftarrow A^{\mathcal{O}_1^{\text{Decap}}}(\text{pk}, c^*, K_b)$ $\triangleright$ Game 1-3 14: <b>return</b> $\llbracket \hat{b} = b \rrbracket$	1: $(c', t) \leftarrow c$ 2: $\hat{m} = \text{Dec}(\text{sk}', c')$ 3: $\hat{k} \leftarrow G(\hat{m})$ 4: <b>if</b> $\text{MAC}(\hat{k}, c') = t$ <b>then</b> 5: $K \leftarrow H(\hat{m}, c')$ 6: <b>else</b> 7: $K \leftarrow H(z, c')$ 8: <b>end if</b> 9: <b>return</b> $K$
$\mathcal{O}^G(m)$	$\mathcal{O}_1^{\text{Decap}}(c)$
1: <b>if</b> $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = m$ <b>then</b> 2: <b>return</b> $\tilde{k}$ 3: <b>end if</b> 4: $k \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ 5: $\mathcal{L}^G \leftarrow \mathcal{L}^G \cup \{(m, k)\}$ 6: <b>return</b> $k$	1: $(c', t) \leftarrow c$ 2: <b>if</b> $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = \text{Dec}(\text{sk}', c') \wedge \text{MAC}(\tilde{k}, c') = t$ <b>then</b> 3: $K \leftarrow H(\tilde{m}, c')$ 4: <b>else</b> 5: $K \leftarrow H(z, c')$ 6: <b>end if</b> 7: <b>return</b> $K$
$\mathcal{O}^H(m, c)$	$\mathcal{O}^H(m, c)$
	1: <b>if</b> $\exists(\tilde{m}, \tilde{c}, \tilde{K}) \in \mathcal{L}^H : \tilde{m} = m \wedge \tilde{c} = c$ <b>then</b> 2: <b>return</b> $\tilde{K}$ 3: <b>end if</b> 4: $K \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ 5: $\mathcal{L}^H \leftarrow \mathcal{L}^H \cup \{(m, c, K)\}$ 6: <b>return</b> $K$

Figure 6: Sequence of games

generated. Therefore, the true oracle must also accept the queried ciphertext. On the other hand, if the true oracle rejects the queried ciphertext (and output the implicit rejection  $H(z, c')$ ), then the tag is simply invalid under the MAC key  $k = G(\text{Dec}(\text{sk}', c'))$ . Therefore, there could not have been a matching query that also validates the tag, and the simulated oracle must also reject the queried ciphertext.

This means that from the adversary  $A$ 's perspective, game 1 and game 0 differ only when the true oracle accepts while the simulated oracle rejects, which means that  $t$  is a valid tag for  $c'$  under  $k = G(\text{Dec}(\text{sk}', c'))$ , but  $k$  has never been queried. Under the random oracle model, such  $k$  is a uniformly random sample of  $\mathcal{K}_{\text{MAC}}$  that the adversary does not know, so for  $A$  to produce a valid tag is to produce a forgery against the MAC under an unknown and uniformly random key. Furthermore, the security game does not include a signing oracle, so this is a zero-time forgery. While zero-time forgery is not a standard security definition for a MAC, we can bound it by the advantage of a one-time forgery adversary  $C$ :

$$P \left[ \mathcal{O}^{\text{Decap}}(c) \neq \mathcal{O}_1^{\text{Decap}}(c) \right] \leq \text{Adv}_{\text{OT-MAC}}(C)$$



250 Across all  $q$  decapsulation queries, the probability that at least one query is a forgery  
 251 is thus at most  $q \cdot P \left[ \mathcal{O}^{\text{Decap}}(c) \neq \mathcal{O}_1^{\text{Decap}}(c) \right]$ . By the difference lemma:

$$\text{Adv}_{G_0}(A) - \text{Adv}_{G_1}(A) \leq q \cdot \text{Adv}_{\text{OT-MAC}}(C)$$

252 *Game 2* is identical to game 1, except that the challenger samples a uniformly random  
 253 MAC key  $k^* \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$  instead of deriving it from  $m^*$ . From  $A$ 's perspective the two games  
 254 are indistinguishable, unless  $A$  queries  $G$  with the value of  $m^*$ . Denote the probability  
 255 that  $A$  queries  $G$  with  $m^*$  by  $P[\text{QUERY } G]$ , then:

$$\text{Adv}_{G_1}(A) - \text{Adv}_{G_2}(A) \leq P[\text{QUERY } G]$$

256 *Game 3* is identical to game 2, except that the challenger samples a uniformly random  
 257 shared secret  $K_0 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$  instead of deriving it from  $m^*$  and  $c'$ . From  $A$ 's perspective the  
 258 two games are indistinguishable, unless  $A$  queries  $H$  with  $(m^*, \cdot)$ . Denote the probability  
 259 that  $A$  queries  $H$  with  $(m^*, \cdot)$  by  $P[\text{QUERY } H]$ , then:

$$\text{Adv}_{G_2}(A) - \text{Adv}_{G_3}(A) \leq P[\text{QUERY } H]$$

260 Since in game 3, both  $K_0$  and  $K_1$  are uniformly random and independent of all other  
 261 variables, no adversary can have any advantage:  $\text{Adv}_{G_3}(A) = 0$ .

$B(\text{pk}, c'^*)$	$\mathcal{O}_B^{\text{Decap}}(c)$
1: $z \xleftarrow{\$} \mathcal{M}$ 2: $k \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ 3: $t \leftarrow \text{MAC}(k, c'^*)$ 4: $c^* \leftarrow (c'^*, t)$ 5: $K \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ 6: $\hat{b} \leftarrow A^{\mathcal{O}_B^{\text{Decap}}, \mathcal{O}_B^G, \mathcal{O}_B^H}(\text{pk}, c^*, K)$ 7: <b>if</b> $\text{ABORT}(m)$ <b>then</b> 8: <b>return</b> $m$ 9: <b>end if</b>	1: $(c', t) \leftarrow c$ 2: <b>if</b> $\exists (\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \text{PCO}(c', \tilde{m}) = 1 \wedge \text{MAC}(k, c') = t$ <b>then</b> 3: $K \leftarrow H(\tilde{m}, c')$ 4: <b>else</b> 5: $K \leftarrow H(z, c')$ 6: <b>end if</b> 7: <b>return</b> $K$
$\mathcal{O}_B^H(m, c)$	$\mathcal{O}_B^G(m)$
<b>if</b> $\text{PCO}(m, c'^*) = 1$ <b>then</b> $\text{ABORT}(m)$ <b>end if</b> <b>if</b> $\exists (\tilde{m}, \tilde{c}, \tilde{K}) \in \mathcal{L}^H : \tilde{m} = m \wedge \tilde{c} = c$ <b>then</b> <b>return</b> $\tilde{K}$ <b>end if</b> $K \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ $\mathcal{L}^H \leftarrow \mathcal{L}^H \cup \{(m, c, K)\}$ <b>return</b> $K$	1: <b>if</b> $\text{PCO}(m, c'^*) = 1$ <b>then</b> 2: $\text{ABORT}(m)$ 3: <b>end if</b> 4: <b>if</b> $\exists (\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = m$ <b>then</b> 5: <b>return</b> $\tilde{k}$ 6: <b>end if</b> 7: $k \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ 8: $\mathcal{L}^G \leftarrow \mathcal{L}^G \cup \{(m, k)\}$ 9: <b>return</b> $k$

Figure 7: OW-PCA adversary  $B$  simulates game 3 for IND-CCA2 adversary  $A$

262 We will bound  $P[\text{QUERY } G]$  and  $P[\text{QUERY } H]$  by constructing a OW-PCA adversary  $B$   
 263 against the underlying PKE that uses  $A$  as a sub-routine.  $B$ 's behaviors are summarized  
 264 in figure 7.

265  $B$  simulates game 3 for  $A$ : receiving the public key  $\text{pk}$  and challenge encryption  $c'^*$ ,  $B$   
 266 samples random MAC key and session key to produce the challenge encapsulation, then  
 267 feeds it to  $A$ . When simulating the decapsulation oracle,  $B$  uses the plaintext-checking  
 268 oracle to look for matching queries in  $\mathcal{L}^G$ . When simulating the hash oracles,  $B$  uses the  
 269 plaintext-checking oracle to detect when  $m^* = \text{Dec}(\text{sk}', c'^*)$  has been queried. When  $m^*$   
 270 is queried,  $B$  terminates  $A$  and returns  $m^*$  to win the OW-PCA game. In other words:

$$P[\text{QUERY } G] \leq \text{Adv}_{\text{OW-PCA}}(B)$$

$$P[\text{QUERY } H] \leq \text{Adv}_{\text{OW-PCA}}(B)$$

271 Combining all equations above produce the desired security bound.  $\square$

## 272 4 Implementation

273 ML-KEM is an IND-CCA2 secure key encapsulation mechanism standardized by NIST  
 274 in FIPS 203. The IND-CCA2 security of ML-KEM is achieved in two steps. First, ML-  
 275 KEM constructs an IND-CPA secure public key encryption scheme  $\text{K-PKE}(\text{KeyGen}, \text{Enc}, \text{Dec})$   
 276 whose security is based on the conjectured intractability of the module learning with  
 277 error (MLWE) problems against both classical and quantum adversaries. Then, the  $U_m^{\mathcal{L}}$   
 278 variant of the Fujisaki-Okamoto transformation [HHK17b] is used to construct the KEM  
 279  $\text{MLKEM}(\text{KeyGen}, \text{Encap}, \text{Decap})$  by calling  $\text{K-PKE}(\text{KeyGen}, \text{Enc}, \text{Dec})$  as sub-routines. Because  
 280  $\text{K-PKE.Enc}$  includes substantially more arithmetics than  $\text{K-PKE.Dec}$ , by using *re-encryption*  
 281 and *de-randomization*, ML-KEM’s decapsulation routine incurs significant computational  
 282 cost.

283 We implemented the “encrypt-then-MAC” KEM construction using  $\text{K-PKE}$  as the input  
 284 PKE and compared its performance against ML-KEM under a variety of scenarios. The  
 285 experimental data showed that while the “encrypt-then-MAC” construction adds a small  
 286 amount of computational overhead to the encapsulation routine and a small increase in  
 287 ciphertext size when compared with ML-KEM, it boasts enormous runtime savings in the  
 288 decapsulation routine, which makes it particularly suitable for deployment in constrained  
 289 environment. See appendix 6.1 for comparison with Kyber’s third round submission to  
 290 NIST’s PQC competition.

291 A detailed description of  $\text{K-PKE}$ ’s routines can be found in FIPS 203 (TODO: citation).  
 292 The “encrypt-then-MAC” routines are described in figure 8.

ML-KEM <sup>+</sup> .KeyGen()	ML-KEM <sup>+</sup> .Decap(sk, c)
1: $z \xleftarrow{\$} \{0, 1\}^{256}$ 2: $(pk, sk') \xleftarrow{\$} \text{K-PKE.KeyGen}()$ 3: $h \leftarrow H(pk)$ 4: $sk \leftarrow (sk'    pk    h    z)$ 5: <b>return</b> (pk, sk)	<b>Require:</b> Secret key $sk = (sk'    pk    h    z)$ <b>Require:</b> Ciphertext $c = (c'    t)$ 1: $(sk', pk, h, z) \leftarrow sk$ 2: $(c', t) \leftarrow c$ 3: $\hat{m} \leftarrow \text{K-PKE.Dec}(sk', c')$ 4: $(\bar{K}, \hat{r}, \hat{k}) \leftarrow \text{XOF}(\hat{m}    h)$ 5: $\hat{t} \leftarrow \text{MAC}(\hat{k}, c')$ 6: <b>if</b> $\hat{t} = t$ <b>then</b> 7: $K \leftarrow \text{KDF}(\bar{K}    t)$ 8: <b>else</b> 9: $K \leftarrow \text{KDF}(z    t)$ 10: <b>end if</b> 11: <b>return</b> K
ML-KEM <sup>+</sup> .Encap(pk)	
<b>Require:</b> Public key pk 1: $m \xleftarrow{\$} \{0, 1\}^{256}$ 2: $(\bar{K}, r, k) \leftarrow \text{XOF}(m    H(pk))$ 3: $c' \leftarrow \text{K-PKE.Enc}(pk, m, r)$ 4: $t \leftarrow \text{MAC}(k, c')$ 5: $K \leftarrow \text{KDF}(\bar{K}    c')$ 6: $c \leftarrow (c', t)$ 7: <b>return</b> (c, K)	

Figure 8: ML-KEM<sup>+</sup> routines

Our implementation extended from the reference implementation by the PQCrystals team (<https://github.com/pq-crystals/kyber>). All C code is compiled with GCC 11.4.1 and OpenSSL 3.0.8. All binaries are executed on an AWS c7a.medium instance with an AMD EPYC 9R14 CPU at 3.7 GHz and 1 GB of RAM.

## 4.1 Choosing a message authenticator

For the ML-KEM<sup>+</sup> implementation, we instantiated MAC with a selection that covered a wide range of MAC designs, including Poly1305 [Ber05], GMAC [MV04], CMAC [IK03][BR05], and KMAC [KCP16].

Poly1305 and GMAC are both Carter-Wegman style authenticators that compute the tag using finite field arithmetic. Generically speaking, Carter-Wegman MAC is parameterized by some finite field  $\mathbb{F}$  and the maximal message length  $L > 0$ . Each symmetric key  $k = (k_1, k_2) \xleftarrow{\$} \mathbb{F}^2$  is a pair of uniformly random field elements, and the message is parsed into tuples of field elements up to length  $L$ :  $m = (m_1, m_2, \dots, m_l) \in \mathbb{F}^{\leq L}$ . The tag  $t$  is computed by evaluating a polynomial whose coefficients are the message blocks and whose indeterminate is the key:

$$\text{MAC}((k_1, k_2), m) = H_{\text{xpoly}}(k_1, m) + k_2 \quad (1)$$

Where  $H_{\text{xpoly}}$  is given by:

$$H_{\text{xpoly}}(k_1, m) = k_1^{l+1} + k_1^l \cdot m_1 + k_1^{l-1} \cdot m_2 + \dots + k_1 \cdot m_l$$

The authenticator formulated in equation 1 is a one-time MAC. To make the construction many-time secure, a non-repeating nonce  $r$  and a PRF is needed:

$$\text{MAC}((k_1, k_2), m, r) = H_{\text{xpoly}}(k_1, m) \oplus \text{PRF}(k_2, r)$$

Specifically, Poly1305 operates in the prime field  $\mathbb{F}_q$  where  $q = 2^{130} - 5$  whereas GMAC operates in the binary field  $\mathbb{F}_{2^{128}}$ . In OpenSSL's implementation, standalone Poly1305 is a one-time secure MAC, whereas GMAC uses a nonce and AES as the PRF and is thus

many-time secure (in OpenSSL GMAC is AES-256-GCM except all data is fed into the “associated data” section and thus not encrypted).

CMAC is based on the CBC-MAC with the block cipher instantiated from AES-256. To compute a CMAC tag, the message is first broke into 128-bit blocks with appropriate padding. Each block is first XOR’d with the previous block’s output, then encrypted under AES using the symmetric key. The final output is XOR’d with a sub key derived from the symmetric key, before being encrypted for one last time. A summary of the computation can be found in figure 9

Sub-key derivation	CMAC(k, m)
<b>Require:</b> 256-bit key $k$ <b>Require:</b> $\text{const\_Rb} = 0x87$ 1: $l \leftarrow \text{AES-256}(k, 0^{128})$ 2: <b>if</b> MostSignificantBit( $l$ ) = 0 <b>then</b> 3: $k_1 \leftarrow l \ll 1$ 4: <b>else</b> 5: $k_1 \leftarrow l \ll 1 \oplus \text{const\_Rb}$ 6: <b>end if</b> 7: <b>if</b> MostSignificantBit( $k_1$ ) = 0 <b>then</b> 8: $k_2 \leftarrow k_1 \ll 1$ 9: <b>else</b> 10: $k_2 \leftarrow k_1 \ll 1 \oplus \text{const\_Rb}$ 11: <b>end if</b> 12: <b>return</b> $k_1, k_2$	<b>Require:</b> 256-bit symmetric key $k$ 1: $(k_1, k_2) \leftarrow \text{deriveSubKey}(k)$ 2: $n \leftarrow \lceil \text{bytesLen}(m)/16 \rceil$ 3: <b>if</b> $n = 0$ <b>then</b> 4: $n \leftarrow 1$ 5: $m_{\text{last}} \leftarrow m_n \oplus k_2$ 6: <b>else if</b> $\text{bytesLen}(m) \bmod 16 = 0$ <b>then</b> 7: $m_{\text{last}} \leftarrow m_n \oplus k_1$ 8: <b>else</b> 9: $m_{\text{last}} \leftarrow m_n \oplus k_2$ 10: <b>end if</b> 11: $x = 0^{128}$ 12: <b>for</b> $i \in \{1, 2, \dots, n-1\}$ <b>do</b> 13: $y \leftarrow x \oplus m_i$ 14: $x \leftarrow \text{AES-256}(k, y)$ 15: <b>end for</b> 16: $y \leftarrow m_{\text{last}} \oplus x$ 17: $t \leftarrow \text{AES-256}(k, y)$ 18: <b>return</b> $t$

Figure 9: AES-256 CMAC

KMAC is defined in NIST SP 800-185 to be based on the family of sponge functions with Keccak permutaiton as the underlying function. We chose KMAC-256, which uses Shake256 as the underlying extendable output functions. KMAC allows variable-length key and tag, but we chose the 256 bits for key length and 128 bits for tag size for consistency with other authenticators.

To isolate the performance characteristics of each authenticator in our instantiation of ML-KEM<sup>+</sup>, we measured the CPU cycles needed for each authenticator to compute a tag on random inputs whose sizes correspond to the ciphertext sizes of ML-KEM. The measurements are summarized in table 2.

Table 2: CPU cycles needed to compute tag on various input sizes

Input size: 768 bytes			Input size: 1088 bytes			Input size: 1568 bytes		
MAC	Median	Average	MAC	Median	Average	MAC	Median	Average
Poly1305	909	2823	Poly1305	961	2704	Poly1305	1065	1809
GMAC	3899	4859	GMAC	3899	4827	GMAC	4055	5026
CMAC	6291	6373	CMAC	7305	7588	CMAC	8735	8772
KMAC	6373	7791	KMAC	9697	9928	KMAC	11647	12186

## 4.2 KEM performance

Compared to the  $U_m^{\mathcal{K}}$  variant of Fujisaki-Okamoto transformed used in ML-KEM, the “encrypt-then-MAC” transformation the following trade-off when given the same input sub-routines:

1. Both encapsulation and decapsulation add a small amount of overhead for needing to hash both the PKE plaintext and the PKE ciphertext when deriving the shared secret, where as the  $U_m^{\mathcal{K}}$  transformation only needs to hash the PKE plaintext.
2. The encapsulation routine adds a small amount of run-time overhead for computing the authenticator
3. The decapsulation routine enjoys substantial runtime speedup because *re-encryption* is replaced with computing an authenticator
4. Ciphertext size increases by the size of an authenticator

Since `K-PKE.Enc` carries significantly more computational complexity than `K-PKE.Dec` or any MAC we chose, the performance advantage of the “encrypt-then-MAC” transformation over the  $U_m^{\mathcal{K}}$  transformation is dominated by the runtime saving gained from replacing *re-encryption* with MAC. A comparison between ML-KEM and variations of the ML-KEM-ETM can be found in table 3

Table 3: CPU cycles of each KEM routine

128-bit security		KEM variant	Encap cycles/tick		Decap cycles/tick	
size parameters (bytes)			Median	Average	Median	Average
pk size	800	ML-KEM-512	91467	92065	121185	121650
sk size	1632	Kyber512	97811	98090	119937	120299
ct size	768	ML-KEM-512 <sup>+</sup> w/ Poly1305	93157	93626	33733	33908
KeyGen cycles/tick		ML-KEM-512 <sup>+</sup> w/ GMAC	97369	97766	37725	37831
Median	75945	ML-KEM-512 <sup>+</sup> w/ CMAC	99739	99959	40117	39943
Average	76171	ML-KEM-512 <sup>+</sup> w/ KMAC	101009	101313	40741	40916

  

192-bit security		KEM variant	Encap cycles/tick		Decap cycles/tick	
size parameters (bytes)			Median	Average	Median	Average
pk size	1184	ML-KEM-768	136405	147400	186445	187529
sk size	2400	Kyber768	153061	153670	182129	182755
ct size	1088	ML-KEM-768 <sup>+</sup> w/ Poly1305	146405	146860	43315	43463
KeyGen cycles/tick		ML-KEM-768 <sup>+</sup> w/ GMAC	149525	150128	46513	46706
Median	129895	ML-KEM-768 <sup>+</sup> w/ CMAC	153139	153735	49841	50074
Average	130650	ML-KEM-768 <sup>+</sup> w/ KMAC	155219	155848	52415	52611

  

256-bit security		KEM variant	Encap cycles/tick		Decap cycles/tick	
size parameters (bytes)			Median	Average	Median	Average
pk size	1568	ML-KEM-1024	199185	199903	246245	247320
sk size	3168	Kyber1024	222351	223260	258231	259067
ct size	1568	ML-KEM-1024 <sup>+</sup> w/ Poly1305	205763	206499	51375	51562
KeyGen cycles/tick		ML-KEM-1024 <sup>+</sup> w/ GMAC	208805	209681	54573	54780
Median	194921	ML-KEM-1024 <sup>+</sup> w/ CMAC	213667	214483	59175	59408
Average	195465	ML-KEM-1024 <sup>+</sup> w/ KMAC	216761	217468	62269	62516

## 4.3 Key exchange protocols

A common application of key encapsulation mechanism is key exchange protocols, where two parties establish a shared secret using a public channel. [BDK<sup>+</sup>18b] described three key exchange protocols: unauthenticated key exchange (KE), unilaterally authenticated key exchange (UAKE), and mutually authenticated key exchange (AKE). We instantiated an implementation for each of the three key exchange protocols using different variations

of the “encrypt-then-MAC” KEM and compared round trip time with implementations instantiated using ML-KEM.

For clarity, we denote the party who sends the first message to be the client and the other party to be the server. Round trip time (RTT) is defined to be the time interval between the moment before the client starts generating ephemeral keypairs and the moment after the client derives the final session key. All experiments are run on a pair of AWS c7a.medium instances both located in the **us-west-2** region. For each experiment, a total of 10,000 rounds of key exchange are performed, with the median and average round trip time (measured in microsecond) recorded.

#### 4.3.1 Unauthenticated key exchange (KE)

In unauthenticated key exchange, a single pair of ephemeral keypair  $(\mathbf{pk}_e, \mathbf{sk}_e) \xleftarrow{\$} \text{KeyGen}()$  is generated by the client. The client transmits the ephemeral public key  $\mathbf{pk}_e$  to the server, who runs the encapsulation routine  $(c_e, K_e) \xleftarrow{\$} \text{Encap}(\mathbf{pk}_e)$  and transmits the ciphertext  $c_e$  back to the client. The client finally decapsulates the ciphertext to recover the shared secret  $K_e \leftarrow \text{Decap}(\mathbf{sk}_e, c_e)$ . The key exchange routines are summarized in figure 10.

Note that in our implementation, a key derivation function (KDF) is applied to the ephemeral shared secret to derive the final session key. This step is added to maintain consistency with other authenticated key exchange protocols, where the final session key is derived from multiple shared secrets. The key derivation function is instantiated using Shake256, and the final session key is 256 bits in length.

$\text{KE}_C()$	$\text{KE}_S()$
1: $(\mathbf{pk}_e, \mathbf{sk}_e) \xleftarrow{\$} \text{KeyGen}()$	1: $\mathbf{pk}_e \leftarrow \text{read}()$
2: <b>send</b> ( $\mathbf{pk}_e$ )	2: $(c_e, K_e) \xleftarrow{\$} \text{Encap}(\mathbf{pk}_e)$
3: $c_e \leftarrow \text{read}()$	3: <b>send</b> ( $c_e$ )
4: $K_e \leftarrow \text{Decap}(\mathbf{sk}_e, c_e)$	4: $K \leftarrow \text{KDF}(K_e)$
5: $K \leftarrow \text{KDF}(K)$	5: <b>return</b> $K$
6: <b>return</b> $K$	

Figure 10: Unauthenticated key exchange (KE) routines

The RTT comparison is summarized in table 4

Table 4: KE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-512	800	768	92	97
ML-KEM-512 <sup>+</sup> w/ Poly1305	800	784	70	72
ML-KEM-512 <sup>+</sup> w/ GMAC	800	784	73	76
ML-KEM-512 <sup>+</sup> w/ CMAC	800	784	75	79
ML-KEM-512 <sup>+</sup> w/ KMAC	800	784	76	78

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-768	1184	1088	135	140
ML-KEM-768 <sup>+</sup> w/ Poly1305	1184	1104	99	104
ML-KEM-768 <sup>+</sup> w/ GMAC	1184	1104	101	105
ML-KEM-768 <sup>+</sup> w/ CMAC	1184	1104	103	109
ML-KEM-768 <sup>+</sup> w/ KMAC	1184	1104	103	107

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-1024	1568	1568	193	199
ML-KEM-1024 <sup>+</sup> w/ Poly1305	1568	1584	138	141
ML-KEM-1024 <sup>+</sup> w/ GMAC	1568	1584	140	145
ML-KEM-1024 <sup>+</sup> w/ CMAC	1568	1584	143	148
ML-KEM-1024 <sup>+</sup> w/ KMAC	1568	1584	144	149

### 4.3.2 Unilaterally authenticated key exchange (UAKE)

In unilaterally authenticated key exchange, the authenticating party proves its identity to the other party by demonstrating possession of a secret key that corresponds to a published long-term public key. In this implementation, the client possesses the long-term public key  $\text{pk}_S$  of the server, and the server authenticates itself by demonstrating possession of the corresponding long-term secret key  $\text{sk}_S$ . UAKE routines are summarized in figure 11.

In addition to the long-term key, the client will also generate an ephemeral keypair as it does in an unauthenticated key exchange, and the session key is derived by applying the KDF to the concatenation of both the ephemeral shared secret and the shared secret encapsulated under server’s long-term key. This helps the key exchange to achieve weak forward secrecy (citation needed).

Using KEM for authentication is especially interesting within the context of post-quantum cryptography: post-quantum KEM schemes usually enjoy better performance characteristics than post-quantum signature schemes with faster runtime, smaller memory footprint, and smaller communication sizes. KEMTLS was proposed in 2020 as an alternative to existing TLS handshake protocols, and many experimental implementations have demonstrated the performance advantage. (citation needed).

$\text{UAKE}_c(\text{pk}_S)$	$\text{UAKE}_s(\text{sk}_S)$
<b>Require:</b> Server's long-term $\text{pk}_S$	<b>Require:</b> Server's long-term $\text{sk}_S$
1: $(\text{pk}_e, \text{sk}_e) \xleftarrow{\$} \text{KeyGen}()$	1: $(\text{pk}_e, c_S) \leftarrow \text{read}()$
2: $(c_S, K_S) \xleftarrow{\$} \text{Encap}(\text{pk}_S)$	2: $K_S \leftarrow \text{Decap}(\text{sk}_S, c_S)$
3: <b>send</b> $(\text{pk}_e, c_S)$	3: $(c_e, K_e) \xleftarrow{\$} \text{Encap}(\text{pk}_e)$
4: $c_e \leftarrow \text{read}()$	4: <b>send</b> $(c_e)$
5: $K_e \leftarrow \text{Decap}(\text{sk}_e, c_e)$	5: $K \leftarrow \text{KDF}(K_e \  K_S)$
6: $K \leftarrow \text{KDF}(K_e \  K_S)$	6: <b>return</b> $K$
7: <b>return</b> $K$	

Figure 11: Unilaterally authenticated key exchange (UAKE) routines

Table 5: UAKE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-512	1568	768	145	151
ML-KEM-512 <sup>+</sup> w/ Poly1305	1584	784	103	106
ML-KEM-512 <sup>+</sup> w/ GMAC	1584	784	106	110
ML-KEM-512 <sup>+</sup> w/ CMAC	1584	784	108	112
ML-KEM-512 <sup>+</sup> w/ KMAC	1584	784	109	113

  

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-768	2272	1088	215	222
ML-KEM-768 <sup>+</sup> w/ Poly1305	2288	1104	144	150
ML-KEM-768 <sup>+</sup> w/ GMAC	2288	1104	149	156
ML-KEM-768 <sup>+</sup> w/ CMAC	2288	1104	153	160
ML-KEM-768 <sup>+</sup> w/ KMAC	2288	1104	154	159

  

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-1024	3136	1568	310	318
ML-KEM-1024 <sup>+</sup> w/ Poly1305	3152	1584	202	209
ML-KEM-1024 <sup>+</sup> w/ GMAC	3152	1584	212	228
ML-KEM-1024 <sup>+</sup> w/ CMAC	3152	1584	212	218
ML-KEM-1024 <sup>+</sup> w/ KMAC	3152	1584	213	220

### 4.3.3 Mutually authenticated key exchange (AKE)

Mutually authenticated key exchange is largely identical to unilaterally authenticated key exchange, except for that client authentication is required. This means that client possesses server's long-term public key and its own long-term secret key, while the server possesses client's long-term public key and its own long-term secret key. The session key is derived by applying KDF onto the concatenation of shared secrets produced under the ephemeral keypair, server's long-term keypair, and client's long-term keypair, in this order.



$\text{AKE}_C(\text{pk}_S, \text{sk}_C)$	$\text{AKE}_S(\text{sk}_S, \text{pk}_C)$
<b>Require:</b> Server's long-term $\text{pk}_S$	<b>Require:</b> Server's long-term $\text{sk}_S$
<b>Require:</b> Client's long-term $\text{sk}_C$	<b>Require:</b> Client's long-term $\text{pk}_C$
1: $(\text{pk}_e, \text{sk}_e) \xleftarrow{\$} \text{KeyGen}()$	1: $(\text{pk}_e, c_S) \leftarrow \text{read}()$
2: $(c_S, K_S) \xleftarrow{\$} \text{Encap}(\text{pk}_S)$	2: $K_S \leftarrow \text{Decap}(\text{sk}_S, c_S)$
3: <b>send</b> ( $\text{pk}_e, c_S$ )	3: $(c_e, K_e) \xleftarrow{\$} \text{Encap}(\text{pk}_e)$
4: $(c_e, c_C) \leftarrow \text{read}()$	4: $(c_C, K_C) \xleftarrow{\$} \text{Encap}(\text{pk}_C)$
5: $K_e \leftarrow \text{Decap}(\text{sk}_e, c_e)$	5: <b>send</b> ( $c_e, c_C$ )
6: $K_C \leftarrow \text{Decap}(\text{sk}_e, c_C)$	6: $K \leftarrow \text{KDF}(K_e \  K_S \  K_C)$
7: $K \leftarrow \text{KDF}(K_e \  K_S \  K_C)$	7: <b>return</b> $K$
8: <b>return</b> $K$	

Figure 12: Mutually authenticated key exchange (AKE) routines

Table 6: AKE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-512	1568	1536	220	213
ML-KEM-512 <sup>+</sup> w/ Poly1305	1584	1568	133	138
ML-KEM-512 <sup>+</sup> w/ GMAC	1584	1568	139	143
ML-KEM-512 <sup>+</sup> w/ CMAC	1584	1568	143	148
ML-KEM-512 <sup>+</sup> w/ KMAC	1584	1568	145	151

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-768	2272	2176	294	301
ML-KEM-768 <sup>+</sup> w/ Poly1305	2288	2208	190	196
ML-KEM-768 <sup>+</sup> w/ GMAC	2288	2208	197	210
ML-KEM-768 <sup>+</sup> w/ CMAC	2288	2208	202	208
ML-KEM-768 <sup>+</sup> w/ KMAC	2288	2208	204	210

KEM variant	Client TX bytes	Server TX bytes	RTT time ( $\mu s$ )	
			Median	Average
ML-KEM-1024	3136	3136	512	511
ML-KEM-1024 <sup>+</sup> w/ Poly1305	3152	3168	266	273
ML-KEM-1024 <sup>+</sup> w/ GMAC	3152	3168	273	282
ML-KEM-1024 <sup>+</sup> w/ CMAC	3152	3168	280	287
ML-KEM-1024 <sup>+</sup> w/ KMAC	3152	3168	282	288

## 5 Conclusions and future works

The “encrypt-then-MAC” transformation is a generic KEM construction that achieves IND-CCA2 security under the random oracle model if the input PKE is OW-PCA secure. Compared to the Fujisaki-Okamoto transformation, our construction replaced *de-randomization* and *re-encryption* with a message authenticator. At the cost of some minimal increase in communication size and encapsulation runtime, our construction achieves significant efficiency gains in the decapsulation routine. In practical key exchange protocols, our construction saves between 35-45% in round trip time.

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## 6 Appendix

### 6.1 Performance comparison between ML-KEM<sup>+</sup> and Kyber

ML-KEM directly evolved from CRYSTALS-Kyber’s third round submission to NIST’s post quantum cryptography competition. While their IND-CPA subroutines (see figure 13) are identical, ML-KEM deviated from Kyber by choosing a different variant of the Fujisaki-Okamoto transformation.

K-PKE.KeyGen()	K-PKE.Enc(pk, m)	K-PKE.Dec(sk, c)
1: $A \xleftarrow{\$} R_q^{k \times k}$ 2: $\mathbf{s} \xleftarrow{\$} \mathcal{X}_{\eta_1}^k$ 3: $\mathbf{e} \xleftarrow{\$} \mathcal{X}_{\eta_1}^k$ 4: $\mathbf{t} \leftarrow A\mathbf{s} + \mathbf{e}$ 5: $\mathbf{pk} \leftarrow (A, \mathbf{t})$ 6: $\mathbf{sk} \leftarrow \mathbf{s}$ 7: <b>return</b> (pk, sk)	<b>Ensure:</b> $\mathbf{pk} = (A, \mathbf{t})$ <b>Ensure:</b> $m \in R_2$ 1: $\mathbf{r} \xleftarrow{\$} \mathcal{X}_{\eta_1}^k$ 2: $\mathbf{e}_1 \xleftarrow{\$} \mathcal{X}_{\eta_2}^k$ 3: $e_2 \xleftarrow{\$} \mathcal{X}_{\eta_2}$ 4: $\mathbf{c}_1 \leftarrow A\mathbf{r} + \mathbf{e}_1$ 5: $c_2 \leftarrow \mathbf{t}^\top \mathbf{r} + e_2 + m \cdot \lfloor \frac{q}{2} \rfloor$ 6: <b>return</b> ( $\mathbf{c}_1, c_2$ )	<b>Ensure:</b> $c = (c_1, c_2)$ <b>Ensure:</b> $\mathbf{sk} = \mathbf{s}$ 1: $\hat{m} \leftarrow c_2 - \mathbf{c}_1^\top \cdot \mathbf{s}$ 2: $\hat{m} \leftarrow \text{Round}(\hat{m})$ 3: <b>return</b> $\hat{m}$

Figure 13: K-PKE routines are identical between Kyber and ML-KEM

CRYSTALS-Kyber uses the  $U^\mathcal{L}$  variant, where the shared secret is derived from both the plaintext and the ciphertext. On the other hand, because by using *re-encryption* and *de-randomization*, the PKE is already made *rigid*, the CRYSTALS-Kyber team decided to use the  $U_m^\mathcal{L}$  variant, where the shared secret is derived from the plaintext alone.

KEM.KeyGen()	KEM.Decap(sk, c)
1: $z \xleftarrow{\$} \{0, 1\}^{256}$ 2: $(\mathbf{pk}, \mathbf{sk}') \xleftarrow{\$} \text{PKE.KeyGen}()$ 3: $\mathbf{sk} \leftarrow (\mathbf{sk}' \parallel \mathbf{pk} \parallel H(\mathbf{pk}) \parallel z)$ 4: <b>return</b> (pk, sk)	<b>Ensure:</b> $\mathbf{sk} = (\mathbf{sk}' \parallel \mathbf{pk} \parallel H(\mathbf{pk}) \parallel z)$ 1: $\hat{m} \leftarrow \text{PKE.Dec}(\mathbf{sk}', c)$ 2: $(\bar{K}, \hat{r}) \leftarrow G(\hat{m} \parallel H(\mathbf{pk}))$ 3: <b>if</b> $\text{PKE.Enc}(\mathbf{pk}, \hat{m}, \hat{r}) = c$ <b>then</b> 4: $K \leftarrow \text{KDF}(\bar{K}, H(c))$ <span style="float: right;"><math>\triangleright U^\mathcal{L}</math></span> 5: $K \leftarrow \bar{K}$ <span style="float: right;"><math>\triangleright U_m^\mathcal{L}</math></span> 6: <b>else</b> 7: $K \leftarrow \text{KDF}(z \parallel H(c))$ 8: <b>end if</b> 9: <b>return</b> $K$
KEM.Encap(pk)	
1: $m \xleftarrow{\$} \{0, 1\}^{256}$ 2: $(\bar{K}, r) \leftarrow G(m \parallel H(\mathbf{pk}))$ 3: $c \leftarrow \text{PKE.Enc}(\mathbf{pk}, m, r)$ 4: $K \leftarrow \text{KDF}(\bar{K} \parallel H(c))$ <span style="float: right;"><math>\triangleright U^\mathcal{L}</math></span> 5: $K \leftarrow \bar{K}$ <span style="float: right;"><math>\triangleright U_m^\mathcal{L}</math></span> 6: <b>return</b> (c, K)	

Figure 14: Kyber uses  $U^\mathcal{L}$  variant. ML-KEM uses  $U_m^\mathcal{L}$  variant.

The reason for ML-KEM to use a different variant of the Fujisaki-Okamoto transformation is two-fold. The first reason is performance: using the  $U_m^\mathcal{L}$  transformation saves the need to hash the ciphertext, and since Kyber/ML-KEM's performance is mainly bottlenecked by the symmetric components, omitting the hash leads to significant runtime savings (up to 17% in AVX-2 optimized implementations). The second reason is the simplified security proof and tighter security bounds of the  $U_m^\mathcal{L}$  variant compared to the  $U^\mathcal{L}$  variant. We will omit the details of the security proof and refer readers to [HHK17b].

In section 4, we mainly compared ML-KEM<sup>+</sup> with ML-KEM, but we would like to point out that, because Kyber uses the  $U^\mathcal{L}$  variant and needs to hash the ciphertext for deriving the shared secret, the performance advantage of ML-KEM<sup>+</sup> over Kyber will be even greater.