

Faster generic IND-CCA secure KEM using encrypt-then-MAC

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Abstract. ML-KEM is a lattice-based IND-CCA secure key encapsulation mechanism (KEM) standardized by NIST in FIPS 203. ML-KEM achieves chosen-ciphertext security by applying the Fujisaki-Okamoto transformation to an IND-CPA secure public-key encryption (PKE) scheme. The Fujisaki-Okamoto transformation uses de-randomization and re-encryption to ensure ciphertext non-malleability, but because ML-KEM’s underlying PKE encryption is significantly slower than the underlying PKE decryption, ML-KEM’s decapsulation performance is dominated by re-encryption. In this paper, we propose an alternative generic IND-CCA secure KEM transformation that applies the encrypt-then-MAC pattern to an OW-PCA secure PKE and an existentially unforgeable MAC. Compared to the Fujisaki-Okamoto transformation, our encrypt-then-MAC transformation replaces de-randomization and re-encryption with computing a MAC tag. We then implemented ML-KEM⁺ by applying the encrypt-then-MAC transformation to the PKE sub-routines of ML-KEM and a wide selection of MACs including Poly1305, GMAC, CMAC, and KMAC. At the cost of minimal increase in encapsulation CPU cycles (+1.8%) and ciphertext size (+2.1%), ML-KEM⁺ achieves massive reduction of decapsulation CPU cycles (-72.2%) compared to ML-KEM. We also implemented key exchange protocols and measured realistic network round trip time (RTT), where ML-KEM⁺ reduces RTT by 23.9%-39.5% compared to ML-KEM.

Keywords: Key encapsulation mechanism, message authentication code, post-quantum cryptography, lattice cryptography, Fujisaki-Okamoto transformation

1 Introduction

A key encapsulation mechanism (KEM) [Sho01] is a cryptographic primitive that allows two parties to establish a shared secret over an insecure channel. The desired security standard for a KEM is called indistinguishability under chosen-ciphertext attack (IND-CCA). Intuitively speaking, IND-CCA security requires that no efficient adversary can distinguish a pseudorandom shared secret from a uniformly random bit string of equal length, even with access to a decapsulation oracle throughout the attack. However, building a provably IND-CCA secure KEM is tremendously difficult. Early attempts without formal proofs, such as RSA encryption defined in PKCS#1 v1.5 [Kal98], were later shown to be vulnerable to practical chosen-ciphertext attacks [Ble98]. In recent decades, the most viable approach has been to start with cryptographic primitives possessing weaker security properties, such as a public-key encryption (PKE) scheme with one-way security under chosen-plaintext attack (OW-CPA), then add steps to achieve *ciphertext non-malleability* [BN00]. Some of the earliest proposals for generic IND-CCA secure constructions include OAEP [BR94], Fujisaki-Okamoto transformation [FO99][FO13], REACT [OP01b], and GEM [CHJ⁺02].

On the other hand, chosen-ciphertext security is a solved problem in symmetric cryptography. It is well understood that, by combining an IND-CPA secure symmetric encryption scheme with an existentially unforgeable message authentication code (MAC) in a pattern called encrypt-then-MAC [Kra01], one can build an authenticated encryption

scheme [BN00] that achieves IND-CCA security. While this technique cannot be directly applied in the context of public-key cryptography due to the lack of a shared symmetric key between the two communicating parties, the concept of authenticating ciphertext using a MAC still has strong merits. Abdalla, Rogaway, and Bellare proposed DHIES (also known as “Hashed ElGamal”)[ABR99][ABR01], a hybrid public-key encryption (HPKE) scheme whose IND-CCA security reduces to the Gap Diffie-Hellman assumption [OP01a] under the random oracle model. The technique behind DHIES is to derive both the shared secret and a symmetric MAC key by hashing a random PKE plaintext, encrypting the PKE plaintext, then authenticating the PKE ciphertext using the previously derived MAC key. When the Gap Diffie-Hellman assumption holds and the MAC is existentially unforgeable, no efficient adversary can recover the decryption of an unknown ciphertext even with access to a decryption oracle because it cannot produce a valid tag for such unknown ciphertext.

1.1 Our contribution

Encrypt-then-MAC: a generic IND-CCA secure KEM transformation In this paper, we propose a generic IND-CCA secure KEM using techniques adapted from DHIES. We call our proposed scheme the encrypt-then-MAC transformation due to the conceptual similarity to the namesake symmetric encryption technique for achieving authenticated encryption. We prove that the IND-CCA security of the encrypt-then-MAC transformation reduces tightly to the OW-PCA security of the underlying PKE and the existential unforgeability of the underlying MAC. In addition, we argue that the encrypt-then-MAC transformation can be instantiated with one-time MAC for further performance improvements.

ML-KEM⁺: an instantiation of encrypt-then-MAC transformation with ML-KEM’s PKE sub-routines. We implemented ML-KEM⁺ by applying our encrypt-then-MAC transformation to ML-KEM’s PKE sub-routines. Compared with ML-KEM, which is based on the U^\perp variant (implicit rejection with rigidity) of the modular Fujisaki-Okamoto KEM transformation, ML-KEM⁺ demonstrates massive performance improvements in decapsulation while only incurring minimal performance penalty in encapsulation runtime and ciphertext size. On an AMD EPYC 9R14 CPU, ML-KEM⁺ with Poly1305 achieves between 72%-80% reduction of CPU cycles needed for decapsulation while only incurring 2%-7% increase of CPU cycles needed for encapsulation (see Table 1).

C implementation and performance comparison To observe the real-world performance of our encrypt-then-MAC transformation, we implemented ML-KEM⁺ in C and measured the CPU cycle count for encapsulation and decapsulation routines. Compared to ML-KEM, ML-KEM⁺ with Poly1305 achieves 72%-80% reduction of CPU cycle count for decapsulation while only increasing encapsulation CPU cycle count by 2%-7% (See Table 1). We also implemented the Kyber key exchange protocols (described in [BDK⁺18]) using ML-KEM⁺. Compared to ML-KEM, ML-KEM⁺ achieves 24%-28% reduction of round trip time in unauthenticated key exchange (KE), 29%-35% in unilaterally authenticated key exchange (UAKE), and 35%-48% reduction in mutually authenticated key exchange (AKE). See Table 2 for a summary of round trip times.

1.2 Related works

Optimal Asymmetric Encryption Padding (OAEP) [BR94][BDPR98] is a generic chosen-ciphertext secure PKE. Under the random oracle model, the chosen-ciphertext security of the OAEP encryption scheme reduces to the one-wayness of the input trapdoor permutation. Although it was discovered that there exist trapdoor permutations with which the OAEP encryption scheme does not achieve full IND-CCA security [Sho02], Fujisaki et al. later proved that the OAEP is IND-CCA secure when combined with the

Table 1: ML-KEM⁺ achieves large performance improvements in decapsulation at the cost of minimal penalty in encapsulation performance and ciphertext size

	Encap (ccl/tick)	Decap (ccl/tick)	CT size (bytes)
ML-KEM ⁺ -512 (Poly1305)	93157 (+1.8%)	33733 (-72.2%)	784 (+2.1%)
ML-KEM ⁺ -512 (GMAC)	97369 (+6.5%)	37725 (-68.9%)	784 (+2.1%)
ML-KEM ⁺ -512 (CMAC)	99739 (+9.0%)	40117 (-66.9%)	784 (+2.1%)
ML-KEM ⁺ -512 (KMAC-256)	101009 (+10.4%)	40741 (-66.4%)	784 (+2.1%)

Table 2: ML-KEM⁺ achieves substantial RTT savings despite increased encapsulation cost and ciphertext size

	KE RTT (μs)	UAKE RTT (μs)	AKE RTT (μs)
ML-KEM ⁺ -512 (Poly1305)	70 (-23.9%)	103 (-29.0%)	133 (-39.5%)
ML-KEM ⁺ -512 (GMAC)	73 (-20.7%)	106 (-26.9%)	139 (-36.8%)
ML-KEM ⁺ -512 (CMAC)	75 (-18.5%)	108 (-25.5%)	143 (-35.0%)
ML-KEM ⁺ -512 (KMAC-256)	76 (-17.4%)	109 (-24.8%)	145 (-34.1%)

92 RSA trapdoor permutation [FOPS01][RSA78]. RSA-OAEP was standardized in PKCS#1
 93 v2 [MKJR16] and is currently the most recommended of all RSA-based encryption schemes.
 94 Unfortunately, OAEP’s requirement for a trapdoor permutation is immensely difficult to
 95 satisfy, and no other practical instantiation saw widespread adoption to this day.

96 The **Fujisaki-Okamoto transformation** [FO99][FO13] is another generic chosen-
 97 ciphertext secure transformation. While Fujisaki and Okamoto originally proposed a
 98 hybrid public-key encryption scheme whose IND-CCA security reduces non-tightly to the
 99 OW-CPA security of the underlying PKE and the IND-CPA security of the symmetric
 100 encryption scheme. Later works [Den03][HHK17][DNR04][HHM22][BP18] tightened the
 101 security reduction, accounted for imperfect correctness, adapted the original proposal to
 102 build a KEM, and proved its security in the quantum random oracle model (QROM).

$\text{KEM}_m^\chi.\text{KeyGen}()$	$\text{KEM}_m^\chi.\text{Encap}(\text{pk})$	$\text{KEM}_m^\chi.\text{Decap}(\text{sk}, c)$
1: $(\text{pk}, \text{sk}') \xleftarrow{\$} \text{PKE}.\text{KeyGen}()$ 2: $z \xleftarrow{\$} \mathcal{M}$ 3: $\text{sk} \leftarrow (\text{sk}', \text{pk}, z)$ 4: return (pk, sk)	1: $m \xleftarrow{\$} \mathcal{M}$ 2: $r \leftarrow G(m)$ 3: $c \leftarrow \text{PKE}.\text{Enc}(\text{pk}, m, r)$ 4: $K \leftarrow H(m)$ 5: return (c, K)	1: $\hat{m} \leftarrow \text{PKE}.\text{Dec}(\text{sk}', c)$ 2: $\hat{r} \leftarrow G(\hat{m})$ 3: $\hat{c} \leftarrow \text{PKE}.\text{Enc}(\text{pk}, \hat{m}, \hat{r})$ 4: if $\hat{c} = c$ then 5: $K \leftarrow H(\hat{m})$ 6: else 7: $K \leftarrow H(z, c)$ 8: end if 9: return K

Figure 1: The U_m^χ variant of Fujisaki-Okamoto transformation is used in ML-KEM

103 The modular Fujisaki-Okamoto KEM transformation is remarkably successful because of

the simplicity of its construction, the tightness of the security bound, and the proven (though non-tight) security against quantum adversaries. It was adopted by many submissions to NIST’s post-quantum cryptography competition, including Kyber [BDK⁺18], Saber [DKRV18], FrodoKEM [BCD⁺16], and classic McEliece [ABC⁺20] among others. The U_m^\perp variant of the Fujisaki-Okamoto transformation (see Figure 1) is adopted in ML-KEM.

However, the Fujisaki-Okamoto transformation is not perfect. Because it uses de-randomization and re-encryption for achieving ciphertext non-malleability, the Fujisaki-Okamoto transformation suffers from the following two problems:

- **Computational inefficiency.** The decapsulation routine needs to re-encrypt the decryption to ensure ciphertext has not been tempered with. For input PKE whose encryption routine carries substantial computational cost, such as most lattice-based cryptosystems, re-encryption slows down decapsulation significantly.
- **Side-channel vulnerability.** Re-encryption also introduces side-channels that can leak information about the decrypted PKE plaintext. As demonstrated in [UXT⁺22][RRCB19][TUX⁺23], these side-channels can be converted into efficient plaintext-checking attacks that can fully recover the secret key.

The rest of the paper is organized as follows. In Section 2, we define and discuss the preliminary concepts and theorems. In Section 3, we present our encrypt-then-MAC transformation in details, prove its security results, and discusses its relationship to the ElGamal cryptosystem. In Section 4, we present ML-KEM⁺, an instantiation of the encrypt-then-MAC transformation using ML-KEM’s PKE sub-routines, then discuss some implementation rationales. In Section 5, we benchmark and compare the performance of individual KEM routines and key exchange round trip times between ML-KEM⁺ and ML-KEM.

2 Preliminaries

2.1 Public-key encryption scheme

Syntax. A public-key encryption scheme $\text{PKE}(\text{KeyGen}, \text{Enc}, \text{Dec})$ is a collection of three routines defined over some plaintext space \mathcal{M} and some ciphertext space \mathcal{C} . Key generation $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{KeyGen}()$ is a randomized routine that returns a keypair. The encryption routine $\text{Enc} : (\text{pk}, m) \mapsto c$ encrypts the input plaintext under the input public key. The decryption routine $\text{Dec} : (\text{sk}, c) \mapsto m$ decrypts the input ciphertext under the input secret key. Where the encryption routine is randomized, we denote the randomness by a coin $r \in \mathcal{R}$, where \mathcal{R} is called the coin space. The decryption routine is assumed to always be deterministic. Some decryption routines can detect malformed ciphertext and output the rejection symbol \perp accordingly.

Correctness. Following the definition in [DNR04], a PKE is δ -correct if:

$$E \left[\max_{m \in \mathcal{M}} P \left[\text{Dec}(\text{sk}, c) \neq m \mid c \xleftarrow{\$} \text{Enc}(\text{pk}, m) \right] \right] \leq \delta$$

Where the expectation is taken with respect to the probability distribution of all possible keypairs $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{PKE}.\text{KeyGen}()$. For many lattice-based cryptosystems, including ML-KEM, decryption failures could leak information about the secret key, although the probability of a decryption failure is low enough that classical adversaries cannot exploit decryption failure more than they can defeat the underlying lattice problem.

Security. The security of public-key encryption is conventionally discussed within the context of adversarial games played between a challenger and an adversary [GM82]. There are two main types of games: in the one-wayness game, the adversary is given a random

148 encryption, then asked to produce the correct decryption; in the indistinguishability game,
 149 the adversary is given the encryption of one of two adversary-chosen plaintexts, then asked
 150 to decide which of the plaintexts corresponds with the given encryption. Depending on
 151 the attack model, the adversary may have access to various oracles. Within the context of
 152 public-key cryptography, adversaries are always assumed to have the public key with which
 153 they can mount chosen-plaintext attack (CPA). If the adversary has access to a plaintext-
 154 checking oracle (PCO) [OP01b] then it can mount plaintext-checking attack (PCA). Where
 155 the adversary has access to a decryption oracle, it can mount chosen-ciphertext attacks
 156 (CCA).

OW-ATK Game	IND-ATK Game	$\mathcal{O}_{\text{PCO}}(m, c)$
1: $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{KeyGen}(1^\lambda)$	1: $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{KeyGen}(1^\lambda)$	1: return $\llbracket m = \text{Dec}(\text{sk}, c) \rrbracket$
2: $m^* \xleftarrow{\$} \mathcal{M}$	2: $(m_0, m_1) \xleftarrow{\$} A^{\mathcal{O}_{\text{ATK}}}(1^\lambda, \text{pk})$	
3: $c^* \xleftarrow{\$} \text{Enc}(\text{pk}, m^*)$	3: $b \xleftarrow{\$} \{0, 1\}$	
4: $\hat{m} \xleftarrow{\$} A^{\mathcal{O}_{\text{ATK}}}(1^\lambda, \text{pk}, c^*)$	4: $c^* \xleftarrow{\$} \text{Enc}(\text{pk}, m_b)$	$\mathcal{O}_{\text{Dec}}(c)$
5: return $\llbracket \hat{m} = m^* \rrbracket$	5: $\hat{b} \xleftarrow{\$} A^{\mathcal{O}_{\text{ATK}}}(1^\lambda, \text{pk}, c^*)$	1: return $\text{Dec}(\text{sk}, c)$
	6: return $\llbracket \hat{b} = b \rrbracket$	

Figure 2: The one-way game, indistinguishability game, plaintext-checking oracle (PCO), and decryption oracle. $\text{ATK} \in \{\text{CPA}, \text{PCA}, \text{CCA}\}$

157 The advantage of an adversary in the OW-ATK game is the probability that it outputs the
 158 correct decryption. The advantage of an adversary in the IND-ATK game is defined below.
 159 A PKE is OW-ATK/IND-ATK secure if no efficient adversary has non-negligible advantage in
 160 the corresponding security game.

$$\text{Adv}_{\text{IND-ATK}}(A) = \left| P[\hat{b} = b] - \frac{1}{2} \right|$$

161 2.2 Key encapsulation mechanism (KEM)

162 **Syntax** A key encapsulation mechanism $\text{KEM}(\text{KeyGen}, \text{Encap}, \text{Decap})$ is a collection of three
 163 routines defined over some ciphertext space \mathcal{C} and some key space \mathcal{K} . The key generation
 164 routine takes the security parameter 1^λ and outputs a keypair $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{KeyGen}(1^\lambda)$.
 165 $\text{Encap}(\text{pk})$ is a probabilistic routine that takes a public key pk and outputs a pair of values
 166 (c, K) where $c \in \mathcal{C}$ is the ciphertext (also called encapsulation) and $K \in \mathcal{K}$ is the shared
 167 secret (also called session key). $\text{Decap}(\text{sk}, c)$ is a deterministic routine that takes the secret
 168 key sk and the encapsulation c and returns the shared secret K if the ciphertext is valid.
 169 Some KEM constructions use explicit rejection, where if c is invalid then Decap will return
 170 a rejection symbol \perp ; other KEM constructions use implicit rejection, where if c is invalid
 171 then Decap will return a fake session key that depends on the ciphertext and some other
 172 secret values.

173 **Security** The security of KEMs is similarly discussed in adversarial games (Figure 3),
 174 although the win conditions differ slightly from the win conditions of a PKE's indistin-
 175 guishability game. In a KEM's indistinguishability game, an adversary is given the public
 176 key and a challenge ciphertext, then asked to distinguish a pseudorandom shared secret
 177 K_0 associated with the challenge ciphertext from a truly random bit string of equal length.

178 The decapsulation oracle $\mathcal{O}^{\text{Decap}}$ takes a ciphertext c and returns the output of the
 179 Decap routine using the secret key. The advantage $\epsilon_{\text{IND-CCA}}$ of an IND-CCA adversary

IND-ATK game	$\mathcal{O}_{\text{Decap}}(c)$
1: $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{KeyGen}(1^\lambda)$	1: return $\text{Decap}(\text{sk}, c)$
2: $(c^*, K_0) \xleftarrow{\$} \text{Encap}(\text{pk})$	
3: $K_1 \xleftarrow{\$} \mathcal{K}$	
4: $b \xleftarrow{\$} \{0, 1\}$	
5: $\hat{b} \xleftarrow{\$} A^{\mathcal{O}_{\text{ATK}}}(1^\lambda, \text{pk}, c^*, K_b)$	
6: return $\llbracket \hat{b} = b \rrbracket$	

Figure 3: IND-ATK game for KEM and decapsulation oracle $\mathcal{O}_{\text{Decap}}$

180 $\mathcal{A}_{\text{IND-CCA}}$ is defined by the adversary's ability to correctly distinguish the two cases beyond
 181 blind guess:

$$\text{Adv}_{\text{IND-CCA}}(A) = \left| P[A^{\mathcal{O}_{\text{Decap}}}(a^\lambda, \text{pk}, c^*, K_b) = b] - \frac{1}{2} \right|$$

182 A KEM is IND-ATK secure if no efficient adversary has non-negligible advantage in the
 183 corresponding security game.

184 2.3 Message authentication code (MAC)

185 A message authentication code $\text{MAC}(\text{KeyGen}, \text{Sign}, \text{Verify})$ is a collection of routines defined
 186 over some key space \mathcal{K} , some message space \mathcal{M} , and some tag space \mathcal{T} . The signing
 187 routine $\text{Sign}(k, m)$ authenticates the message m under the secret key k by producing a tag
 188 t (also called digest). The verification routine $\text{Verify}(k, m, t)$ takes the triplet of secret
 189 key, message, and tag, and outputs 1 if the message-tag pair is valid under the secret key,
 190 or 0 otherwise. Many MAC constructions are deterministic. For these constructions it is
 191 simpler to denote the signing routine by $t \leftarrow \text{MAC}(k, m)$ and perform verification using a
 192 simple comparison.

193 The security of a MAC is defined in an adversarial game in which an adversary, with
 194 access to some signing oracle $\mathcal{O}_{\text{Sign}}(m)$, tries to forge a new valid message-tag pair that
 195 has never been queried before. The existential unforgeability under chosen message attack
 196 (EUF-CMA) game is shown below:

EUF-CMA game
1: $k^* \xleftarrow{\$} \mathcal{K}$
2: $(\hat{m}, \hat{t}) \xleftarrow{\$} \mathcal{A}^{\mathcal{O}_{\text{Sign}}}()$
3: return $\llbracket \text{Verify}(k^*, \hat{m}, \hat{t}) \wedge (\hat{m}, \hat{t}) \notin \mathcal{O}_{\text{Sign}} \rrbracket$

Figure 4: The existential forgery game

197 The advantage $\text{Adv}_{\text{EUF-CMA}}$ of the existential forgery adversary is the probability that it
 198 wins the EUF-CMA game. Some MACs are one-time existentially unforgeable, meaning
 199 that each secret key can be used to authenticate only a single message. The corresponding
 200 security game is modified such that the signing oracle will only answer a single signing
 201 query.

3 The encrypt-then-MAC transformation

In this section we introduce the encrypt-then-MAC transformation that transforms an OW-PCA secure PKE and an one-time existentially unforgeable MAC into an IND-CCA secure KEM. Our scheme mainly differs from DHIES in its versatility and input requirement. Whereas the IND-CCA security of DHIES reduces specifically to the Gap Diffie-Hellman assumption, the chosen-ciphertext security of the encrypt-then-MAC KEM reduces more generally to the OW-PCA security [OP01b] of the input scheme (we will show in Section 3.2 that the Gap Diffie-Hellman assumption implies OW-PCA security). In addition, we propose that because each call to encapsulation samples a fresh PKE plaintext, the encrypt-then-MAC KEM can be instantiated with one-time secure MAC such as Poly1305 (M. Abdalla et al. originally proposed to use HMAC and CBC-MAC, which are many-time secure MAC but less efficient than one-time MAC, see Section 4.1), which greatly improves the computational efficiency of the scheme. A summary of encapsulation data flow is illustrated in Figure 5.

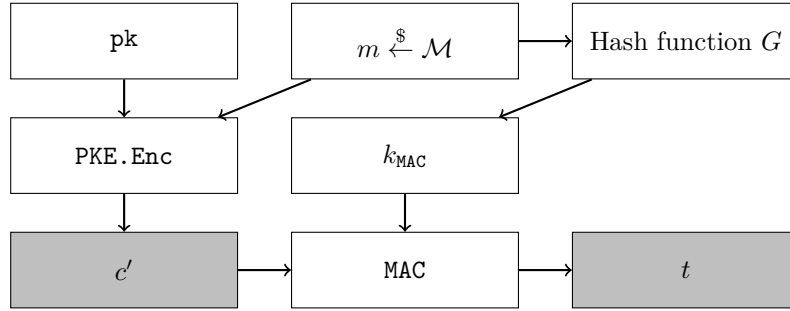


Figure 5: Combining PKE with MAC using encrypt-then-MAC to ensure ciphertext integrity

In Section 3.1 we reduce the IND-CCA security of the KEM tightly to the OW-PCA security of the underlying PKE, and non-tightly to the unforgeability of the MAC. In Section 3.2, we show that the “Hashed ElGamal” cryptosystem in [ABR01] is a special case of the encrypt-then-MAC transformation by reducing the OW-PCA security of the ElGamal cryptosystem to the Gap Diffie-Hellman assumption.

Let \mathcal{B}^* denote the set of finite bit strings. Let $\text{PKE}(\text{KeyGen}, \text{Enc}, \text{Dec})$ be a public-key encryption scheme defined over message space \mathcal{M} and ciphertext space \mathcal{C} . Let $\text{MAC} : \mathcal{K}_{\text{MAC}} \times \mathcal{B}^* \rightarrow \mathcal{T}$ be a deterministic message authentication code that takes a key $k \in \mathcal{K}_{\text{MAC}}$, some message $m \in \mathcal{B}^*$, and outputs a digest $t \in \mathcal{T}$. Let $G : \mathcal{M} \rightarrow \mathcal{K}_{\text{MAC}}$ be a hash function that maps from PKE’s plaintext space to MAC’s key space. Let $H : \mathcal{B}^* \rightarrow \mathcal{K}_{\text{KEM}}$ be a hash function that maps bit strings into the set of possible shared secrets. The encrypt-then-MAC transformation $\text{EtM}[\text{PKE}, \text{MAC}, G, H]$ constructs a key encapsulation mechanism $\text{KEM}_{\text{EtM}}(\text{KeyGen}, \text{Encap}, \text{Decap})$, whose routines are described in Figure 6.

The key generation routine of KEM_{EtM} is largely identical to that of the PKE, only a secret value z is sampled as the implicit rejection symbol. In the encapsulation routine, a MAC key is derived from the randomly sampled plaintext $k \leftarrow G(m)$, then used to sign the unauthenticated ciphertext c' . Finally, the unauthenticated ciphertext c' and the tag t combine into the authenticated ciphertext c that would be transmitted to the peer. In the decapsulation routine, the decryption \hat{m} of the unauthenticated ciphertext is used to re-derive the MAC key \hat{k} , which is then used to re-compute the tag \hat{t} . The ciphertext is considered valid if and only if the recomputed tag is identical to the input tag.

Since the encrypt-then-MAC transformation removes re-encryption in decapsulation, there is no longer the need for fixing the pseudorandom coin r in the PKE’s encryption

$\text{KEM}_{\text{EtM}}.\text{KeyGen}()$	$\text{KEM}_{\text{EtM}}.\text{Decap}(\text{sk}, c)$
1: $(\text{pk}, \text{sk}') \xleftarrow{\$} \text{PKE}.\text{KeyGen}()$ 2: $z \xleftarrow{\$} \mathcal{M}$ 3: $\text{sk} \leftarrow (\text{sk}', z)$ 4: return (pk, sk)	1: $(c', t) \leftarrow c$ 2: $(\text{sk}', z) \leftarrow \text{sk}$ 3: $\hat{m} \leftarrow \text{PKE}.\text{Dec}(\text{sk}', c')$ 4: $\hat{k} \leftarrow G(\hat{m})$ 5: if $\text{MAC}(\hat{k}, c') \neq t$ then 6: $K \leftarrow H(z, c')$ 7: else 8: $K \leftarrow H(\hat{m}, c')$ 9: end if 10: return K
$\text{KEM}_{\text{EtM}}.\text{Encap}(\text{pk})$	
1: $m \xleftarrow{\$} \mathcal{M}$ 2: $k \leftarrow G(m)$ 3: $c' \xleftarrow{\$} \text{PKE}.\text{Enc}(\text{pk}, m)$ 4: $t \leftarrow \text{MAC}(k, c')$ 5: $K \leftarrow H(m, c')$ 6: $c \leftarrow (c', t)$ 7: return (c, K)	

Figure 6: The encrypt-then-MAC transformation builds a KEM KEM_{EtM} using a $\text{PKE}(\text{KeyGen}, \text{Enc}, \text{Dec})$, a MAC, and two hash functions G, H

239 routine. If the input PKE is already rigid, then the shared secret may be derived from
240 hashing the PKE plaintext alone. However, if the input PKE is not rigid, then the shared
241 secret must be derived from hashing both the PKE plaintext and the PKE ciphertext.

242 The chosen-ciphertext security of the encrypt-then-MAC scheme can be intuitively
243 argued through an adversary's inability to learn additional information from the decap-
244 sulation oracle. For an adversary A to produce a valid tag t for some unauthenticated
245 ciphertext c' under the symmetric key $k \leftarrow G(\text{Dec}(\text{sk}', c'))$ implies that A must either
246 know the symmetric key k or produce a forgery. Under the random oracle model, A also
247 cannot know k without knowing its preimage $\text{Dec}(\text{sk}', c')$, so A must either have produced
248 c' honestly, or have broken the one-way security of PKE. This means that the decapsulation
249 oracle will not give out information on decryptions that the adversary does not already
250 know.

251 However, a decapsulation oracle can still give out some information: for a known
252 plaintext m , all possible encryptions $c' \xleftarrow{\$} \text{Enc}(\text{pk}, m)$ can be correctly signed, while
253 ciphertexts that don't decrypt back to m cannot be correctly signed. This means that a
254 decapsulation oracle can be converted into a plaintext-checking oracle (see Figure 7), so
255 every chosen-ciphertext attack against the KEM can be converted into a plaintext-checking
256 attack against the underlying PKE.

$\text{PCO}(m, c)$
1: $k \leftarrow G(m)$ 2: $t \leftarrow \text{MAC}(k, c)$ 3: return $\llbracket \mathcal{O}^{\text{Decap}}((c, t)) = H(m, c) \rrbracket$

Figure 7: With the encrypt-then-MAC transformation, every chosen-ciphertext attack against the KEM implies a plaintext-checking attack against the underlying PKE

On the other hand, if the underlying PKE is OW-PCA secure and the underlying MAC is one-time existentially unforgeable, then the encrypt-then-MAC KEM is IND-CCA secure:

Theorem 1. *For every IND-CCA adversary A against KEM_{EtM} that makes q decapsulation queries, there exists an OW-PCA adversary B who makes at least q plaintext-checking queries against the underlying PKE, and an one-time existential forgery adversary C against the underlying MAC such that*

$$\text{Adv}_{\text{IND-CCA}}(A) \leq q \cdot \text{Adv}_{\text{OT-MAC}}(C) + 2 \cdot \text{Adv}_{\text{OW-PCA}}(B)$$

Theorem 1 naturally flows into an equivalence relationship between the security of the KEM and the security of the PKE:

Lemma 1. *KEM_{EtM} is IND-CCA secure if and only if the input PKE is OW-PCA secure*

3.1 Proof of theorem 1

We will prove Theorem 1 using a sequence of game. A summary of the the sequence of games can be found in Figure 8 and 9. From a high level we made three incremental modifications to the IND-CCA game for KEM_{EtM} : replace true decapsulation with simulated decapsulation, replace the pseudorandom MAC key $k^* \leftarrow G(m^*)$ with a truly random MAC key $k^* \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$, and finally replace pseudorandom shared secret $K_0 \leftarrow H(m^*, c')$ with a truly random shared secret $K_0 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$. A OW-PCA adversary can then simulate the modified IND-CCA game for the KEM adversary, and the advantage of the OW-PCA adversary is associated with the probability of certain behaviors of the KEM adversary.

Proof. *Game 0* is the standard IND-CCA game for KEMs. The decapsulation oracle $\mathcal{O}^{\text{Decap}}$ executes the decapsulation routine using the challenge keypair and return the results faithfully. The queries made to the hash oracles $\mathcal{O}^G, \mathcal{O}^H$ are recorded to their respective tapes $\mathcal{L}^G, \mathcal{L}^H$.

Game 1 is identical to game 0 except that the true decapsulation oracle $\mathcal{O}^{\text{Decap}}$ is replaced with a simulated oracle $\mathcal{O}_1^{\text{Decap}}$. Instead of directly decrypting c' as in the decapsulation routine, the simulated oracle searches through the tape \mathcal{L}^G to find a matching query (\tilde{m}, \tilde{k}) such that \tilde{m} is the decryption of c' . The simulated oracle then uses \tilde{k} to validate the tag t against c' .

If the simulated oracle accepts the queried ciphertext as valid, then there is a matching query that also validates the tag, which means that the queried ciphertext is honestly generated. Therefore, the true oracle must also accept the queried ciphertext. On the other hand, if the true oracle rejects the queried ciphertext (and output the implicit rejection $H(z, c')$), then the tag is simply invalid under the MAC key $k = G(\text{Dec}(\text{sk}', c'))$. Therefore, there could not have been a matching query that also validates the tag, and the simulated oracle must also rejects the queried ciphertext.

This means that from the adversary A 's perspective, game 1 and game 0 differ only when the true oracle accepts while the simulated oracle rejects, which means that t is a valid tag for c' under $k = G(\text{Dec}(\text{sk}', c'))$, but k has never been queried. Under the random oracle model, such k is a uniformly random sample of \mathcal{K}_{MAC} that the adversary does not know, so for A to produce a valid tag is to produce a forgery against the MAC under an unknown and uniformly random key. Furthermore, the security game does not include a signing oracle, so this is a zero-time forgery. While zero-time forgery is not a standard security definition for a MAC, we can bound it by the advantage of a one-time forgery adversary C :

$$P \left[\mathcal{O}^{\text{Decap}}(c) \neq \mathcal{O}_1^{\text{Decap}}(c) \right] \leq \text{Adv}_{\text{OT-MAC}}(C)$$

IND-CCA game for KEM_{EtM}	$\mathcal{O}^{\text{Decap}}(c)$
1: $(\text{pk}, \text{sk}) \xleftarrow{\$} \text{KEM}_{\text{EtM}}.\text{KeyGen}()$ 2: $m^* \xleftarrow{\$} \mathcal{M}$ 3: $c' \xleftarrow{\$} \text{PKE}.\text{Enc}(\text{pk}, m^*)$ 4: $k^* \leftarrow G(m^*)$ \triangleright Game 0-1 5: $k^* \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ \triangleright Game 2-3 6: $t \leftarrow \text{MAC}(k^*, c')$ 7: $c^* \leftarrow c' t$ 8: $K_0 \leftarrow H(m^*, c')$ \triangleright Game 0-2 9: $K_0 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ \triangleright Game 3 10: $K_1 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ 11: $b \xleftarrow{\$} \{0, 1\}$ 12: $\hat{b} \leftarrow A^{\mathcal{O}^{\text{Decap}}}(\text{pk}, c^*, K_b)$ \triangleright Game 0 13: $\hat{b} \leftarrow A^{\mathcal{O}_1^{\text{Decap}}}(\text{pk}, c^*, K_b)$ \triangleright Game 1-3 14: return $[\hat{b} = b]$	1: $(c', t) \leftarrow c$ 2: $\hat{m} = \text{Dec}(\text{sk}', c')$ 3: $\hat{k} \leftarrow G(\hat{m})$ 4: if $\text{MAC}(\hat{k}, c') = t$ then 5: $K \leftarrow H(\hat{m}, c')$ 6: else 7: $K \leftarrow H(z, c')$ 8: end if 9: return K
	$\mathcal{O}_1^{\text{Decap}}(c)$ 1: $(c', t) \leftarrow c$ 2: if $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = \text{Dec}(\text{sk}', c') \wedge \text{MAC}(\tilde{k}, c') = t$ then 3: $K \leftarrow H(\tilde{m}, c')$ 4: else 5: $K \leftarrow H(z, c')$ 6: end if 7: return K
$\mathcal{O}^G(m)$ 1: if $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = m$ then 2: return \tilde{k} 3: end if 4: $k \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ 5: $\mathcal{L}^G \leftarrow \mathcal{L}^G \cup \{(m, k)\}$ 6: return k	$\mathcal{O}^H(m, c)$ 1: if $\exists(\tilde{m}, \tilde{c}, \tilde{K}) \in \mathcal{L}^H : \tilde{m} = m \wedge \tilde{c} = c$ then 2: return \tilde{K} 3: end if 4: $K \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ 5: $\mathcal{L}^H \leftarrow \mathcal{L}^H \cup \{(m, c, K)\}$ 6: return K

Figure 8: Sequence of games

301 Across all q decapsulation queries, the probability that at least one query is a forgery
302 is thus at most $q \cdot P \left[\mathcal{O}^{\text{Decap}}(c) \neq \mathcal{O}_1^{\text{Decap}}(c) \right]$. By the difference lemma:

$$\text{Adv}_{G_0}(A) - \text{Adv}_{G_1}(A) \leq q \cdot \text{Adv}_{\text{OT-MAC}}(C)$$

303 *Game 2* is identical to game 1, except that the challenger samples a uniformly random
304 MAC key $k^* \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ instead of deriving it from m^* . From A 's perspective the two games
305 are indistinguishable, unless A queries G with the value of m^* . Denote the probability
306 that A queries G with m^* by $P[\text{QUERY } G]$, then:

$$\text{Adv}_{G_1}(A) - \text{Adv}_{G_2}(A) \leq P[\text{QUERY } G]$$

307 *Game 3* is identical to game 2, except that the challenger samples a uniformly random
308 shared secret $K_0 \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ instead of deriving it from m^* and c' . From A 's perspective the
309 two games are indistinguishable, unless A queries H with (m^*, \cdot) . Denote the probability
310 that A queries H with (m^*, \cdot) by $P[\text{QUERY } H]$, then:

$$\text{Adv}_{G_2}(A) - \text{Adv}_{G_3}(A) \leq P[\text{QUERY } H]$$

Since in game 3, both K_0 and K_1 are uniformly random and independent of all other variables, no adversary can have any advantage: $\text{Adv}_{G_3}(A) = 0$.

$B(\text{pk}, c'^*)$	$\mathcal{O}_B^{\text{Decap}}(c)$
1: $z \xleftarrow{\$} \mathcal{M}$ 2: $k \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ 3: $t \leftarrow \text{MAC}(k, c'^*)$ 4: $c^* \leftarrow (c'^*, t)$ 5: $K \xleftarrow{\$} \mathcal{K}_{\text{KEM}}^{\text{cap}}$ 6: $\tilde{b} \leftarrow A^{\mathcal{O}_B^{\text{Decap}}, \mathcal{O}_B^G, \mathcal{O}_B^H}(\text{pk}, c^*, K)$ 7: if $\text{ABORT}(m)$ then 8: return m 9: end if	1: $(c', t) \leftarrow c$ 2: if $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \text{PCO}(c', \tilde{m}) = 1 \wedge \text{MAC}(\tilde{k}, c') = t$ then 3: $K \leftarrow H(\tilde{m}, c')$ 4: else 5: $K \leftarrow H(z, c')$ 6: end if 7: return K
$\mathcal{O}_B^H(m, c)$	$\mathcal{O}_B^G(m)$
if $\text{PCO}(m, c'^*) = 1$ then $\text{ABORT}(m)$ end if if $\exists(\tilde{m}, \tilde{c}, \tilde{K}) \in \mathcal{L}^H : \tilde{m} = m \wedge \tilde{c} = c$ then return \tilde{K} end if $K \xleftarrow{\$} \mathcal{K}_{\text{KEM}}$ $\mathcal{L}^H \leftarrow \mathcal{L}^H \cup \{(m, c, K)\}$ return K	1: if $\text{PCO}(m, c'^*) = 1$ then 2: $\text{ABORT}(m)$ 3: end if 4: if $\exists(\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = m$ then 5: return \tilde{k} 6: end if 7: $k \xleftarrow{\$} \mathcal{K}_{\text{MAC}}$ 8: $\mathcal{L}^G \leftarrow \mathcal{L}^G \cup \{(m, k)\}$ 9: return k

Figure 9: OW-PCA adversary B simulates game 3 for IND-CCA adversary A

We will bound $P[\text{QUERY G}]$ and $P[\text{QUERY H}]$ by constructing a OW-PCA adversary B against the underlying PKE that uses A as a sub-routine. B 's behaviors are summarized in Figure 9.

B simulates game 3 for A : receiving the public key pk and challenge encryption c'^* , B samples random MAC key and session key to produce the challenge encapsulation, then feeds it to A . When simulating the decapsulation oracle, B uses the plaintext-checking oracle to look for matching queries in \mathcal{L}^G . When simulating the hash oracles, B uses the plaintext-checking oracle to detect when $m^* = \text{Dec}(\text{sk}', c'^*)$ has been queried. When m^* is queried, B terminates A and returns m^* to win the OW-PCA game. In other words:

$$P[\text{QUERY G}] \leq \text{Adv}_{\text{OW-PCA}}(B)$$

$$P[\text{QUERY H}] \leq \text{Adv}_{\text{OW-PCA}}(B)$$

Combining all equations above produce the desired security bound. \square

3.2 ElGamal is OW-PCA secure

We show that the DHAES/DHIES hybrid encryption scheme is a special case of the encrypt-then-MAC transformation. Specifically, we will sketch a proof of the following lemma:

Lemma 2. *For every OW-PCA adversary A against the ElGamal cryptosystem, there exists a Gap Diffie-Hellman problem solver B such that:*

$$Adv_{GapDH}(B) = Adv_{OW-PCA}(A)$$

329 *In other words, ElGamal is OW-PCA secure under the Gap Diffie-Hellman assumption.*

330 Each ElGamal cryptosystem [Gam85] is parameterized by a cyclic group $G = \langle g \rangle$ of
331 prime order $q > 2$. A summary of the routine is shown in Figure 10:

KeyGen()	Enc(pk = $g^x, m \in G$)	Dec(sk = $x, c = (w, v) \in G^2$)
1: $x \xleftarrow{\$} \mathbb{Z}_q$	Require: $m \in G$	1: $\hat{m} \leftarrow (w^x)^{-1} \cdot v$
2: $sk \leftarrow x$	1: $y \xleftarrow{\$} \mathbb{Z}_q$	2: return \hat{m}
3: $pk \leftarrow g^x$	2: $w \leftarrow g^y$	
4: return (pk, sk)	3: $v \leftarrow m \cdot (g^x)^y$	
	4: return $c = (w, v)$	

Figure 10: ElGamal cryptosystem

332 The security of ElGamal cryptosystem reduces to the conjectured intractability of the
333 computational Diffie-Hellman problem and the decisional Diffie-Hellman problem:

334 **Definition 1 (computational Diffie-Hellman problem (CDH)).** Let $x, y \xleftarrow{\$} \mathbb{Z}_q$ be
335 uniformly random samples. Given (g, g^x, g^y) , compute g^{xy} .

336 **Definition 2 (decisional Diffie-Hellman problem (DDH)).** Let $x, y, z \xleftarrow{\$} \mathbb{Z}_q$ be
337 uniformly random samples. Let $h \xleftarrow{\$} \{g^z, g^{xy}\}$ be randomly chosen between g^z and g^{xy} .
338 Given (g, g^x, g^y, h) , determine whether h is g^{xy} or g^z .

339 It is also conjectured in [ABR01] that for certain choice of cyclic group G , the com-
340 putational Diffie-Hellman problem remains intractable even if the adversary has access to
341 a restricted decisional Diffie-Hellman oracle. This assumption is captured in the Gap
342 Diffie-Hellman problem:

343 **Definition 3 (Gap Diffie-Hellman problem).** Let $G = \langle g \rangle$ be a cyclic group of prime
344 order $q > 2$. Let $x, y \xleftarrow{\$} \mathbb{Z}_q$ be uniformly random samples. Given (g, g^x, g^y) and a restricted
345 DDH oracle $\mathcal{O}^{DDH} : (u, v) \mapsto \llbracket u^x = v \rrbracket$, compute g^{xy} .

346 We now present the proof for Lemma 2

347 *Proof.* We will prove by sequence of game. A summary can be found in Figure 11

348 *Game 0* is the OW-PCA game. Adversary A has access to the plaintext-checking oracle
349 PCO and wins the game if it can correctly recover the challenge plaintext m^* .

350 *Game 1* is identical to game 0, except that the formulation of the PCO is changed.
351 When servicing the plaintext-checking query $(m, c = (w, v))$, PCO₁ checks whether w^x is
352 equal to $m^{-1} \cdot v$. Observe that in the cyclic group G , the algebraic expressions in PCO and
353 PCO₁ are equivalent, which means that PCO₁ behaves identically to PCO.

354 *Game 2* is identical to game 1 except for two modifications: first, when computing
355 the challenge ciphertext, v is no longer computed from m^* but is randomly sampled;
356 second, the win condition changed from $\hat{m} = m^*$ to $\hat{m} = w^{-x} \cdot v$. Notice that in game 0-1,
357 $v \xleftarrow{\$} m^* \cdot (g^x)^y$ follows uniform random distribution on the cyclic group G because m^* is
358 uniformly random in the cyclic group, so adversary A retains its advantage in “recovering
359 the decryption” when v becomes truly uniformly random in the cyclic group. It is easy to
360 verify that the two win conditions are equivalent. Up to this point, we have simply moved
361 things around, and game 0 through game 2 are algebraically equivalent:

$G_0 - G_2$	$\text{PCO}(m, c = (w, v))$
1: $x \xleftarrow{\$} \mathbb{Z}_q$	1: return $\llbracket m = (w^x)^{-1} \cdot v \rrbracket$
2: $m^* \xleftarrow{\$} G$	
3: $y \xleftarrow{\$} \mathbb{Z}_q, w \leftarrow g^y$	
4: $v \leftarrow m^* \cdot (g^x)^y$ $\triangleright G_0 - G_1$	$\text{PCO}_1(m, c = (w, v))$
5: $v \xleftarrow{\$} G$ $\triangleright G_2$	1: return $\llbracket (w^x) = m^{-1} \cdot v \rrbracket$
6: $c^* \leftarrow (w, v)$	
7: $\hat{m} \xleftarrow{\$} A^{\text{PCO}}(g^x, c^*)$ $\triangleright G_0$	
8: $\hat{m} \xleftarrow{\$} A^{\text{PCO}_1}(g^x, c^*)$ $\triangleright G_1 - G_2$	
9: return $\llbracket \hat{m} = m^* \rrbracket$ $\triangleright G_0 - G_1$	
10: return $\llbracket \hat{m} = w^{-x} \cdot v \rrbracket$ $\triangleright G_2$	

Figure 11: Lemma 2 sequence of games

$$\text{Adv}_0(A) = \text{Adv}_1(A) = \text{Adv}_2(A)$$

362 The Gap Diffie-Hellman adversary B can perfectly simulate game 2 for A (see Figure
 363 12): B receives as the Gap Diffie-Hellman problem inputs g^x and g^y . g^x simulates an
 364 ElGamal public key, where as g^y simulates the first component of the challenge ciphertext.
 365 As in game 2, the second component of the challenge ciphertext can be randomly sampled.
 366 Finally, the PCO_1 from game 2 can be perfectly simulated using the restricted DDH oracle
 367 \mathcal{O}^{DDH} .

$B^{\mathcal{O}^{\text{DDH}}}(g, g^x, g^y)$	$\mathcal{O}^{\text{DDH}}(u, v)$
1: $w \leftarrow g^y$	1: return $\llbracket u^x = v \rrbracket$
2: $v \xleftarrow{\$} G$	
3: $c^* \leftarrow (w, v)$	
4: $\hat{m} \xleftarrow{\$} A^{\text{PCO}_2}(g^x, c^*)$	$\text{PCO}_2(m, c = (w, v))$
5: return $\hat{m}^{-1} \cdot v$	1: return $\mathcal{O}^{\text{DDH}}(w, m^{-1} \cdot v)$

Figure 12: Gap Diffie-Hellman adversary B simulates game 2 for A

368 If A wins game 2, then its output is $\hat{m} = w^{-x} \cdot v = g^{-xy} \cdot v$, so $m^{-1} \cdot v$ is g^{xy} , the
 369 correct answer to the Gap Diffie-Hellman problem. In other words, B solves its Gap
 370 Diffie-Hellman problem if and only if A wins the simulated game 2.

$$\text{Adv}_2(A) = \text{Adv}_{\text{GapDH}}(B)$$

371

□

372 4 Practical instantiation with ML-KEM

373 ML-KEM is an IND-CCA secure key encapsulation mechanism standardized by NIST in
 374 FIPS 203 [oST24]. The chosen-ciphertext security of ML-KEM is achieved in two steps.
 375 First, ML-KEM constructs a PKE (called K-PKE, see Figure 13) whose IND-CPA security
 376 reduces to the conjectured intractability of the decisional Module Learning with Error

377 (MLWE) problem. Then, the $U_m^\mathcal{L}$ variant of the Fujisaki-Okamoto transformation is applied
 378 to convert the IND-CPA secure PKE into an IND-CCA secure KEM (see Figure 14).

K-PKE.KeyGen()	K-PKE.Enc(pk, m)	K-PKE.Dec(sk, c)
1: $A \xleftarrow{\$} R_q^{k \times k}$	Ensure: $\text{pk} = (A, \mathbf{t})$	Ensure: $c = (c_1, c_2)$
2: $\mathbf{s} \xleftarrow{\$} \mathcal{X}_{\eta_1}^k$	Ensure: $m \in R_2$	Ensure: $\text{sk} = \mathbf{s}$
3: $\mathbf{e} \xleftarrow{\$} \mathcal{X}_{\eta_1}^k$	1: $\mathbf{r} \xleftarrow{\$} \mathcal{X}_{\eta_1}^k$	1: $\hat{m} \leftarrow c_2 - \mathbf{c}_1^\top \cdot \mathbf{s}$
4: $\mathbf{t} \leftarrow A\mathbf{s} + \mathbf{e}$	2: $\mathbf{e}_1 \xleftarrow{\$} \mathcal{X}_{\eta_2}^k$	2: $\hat{m} \leftarrow \text{Round}(\hat{m})$
5: $\text{pk} \leftarrow (A, \mathbf{t})$	3: $e_2 \xleftarrow{\$} \mathcal{X}_{\eta_2}$	3: return \hat{m}
6: $\text{sk} \leftarrow \mathbf{s}$	4: $\mathbf{c}_1 \leftarrow A\mathbf{r} + \mathbf{e}_1$	
7: return (pk, sk)	5: $c_2 \leftarrow \mathbf{t}^\top \mathbf{r} + e_2 + m \cdot \lfloor \frac{q}{2} \rfloor$	
	6: return (\mathbf{c}_1, c_2)	

Figure 13: K-PKE is an IND-CPA secure PKE based on the conjectured intractability of the Module Learning with Error (MWLE) problem

ML-KEM.KeyGen()	ML-KEM.Decap(sk, c)
1: $(\text{pk}, \text{sk}') \xleftarrow{\$} \text{K-PKE.KeyGen}()$	1: $\hat{m} \leftarrow \text{K-PKE.Dec}(\text{sk}', c)$
2: $h \leftarrow \text{SHA3-256}(\text{pk})$	2: $(\bar{K}, \hat{r}) \leftarrow \text{SHA3-512}(\hat{m}, h)$
3: $z \xleftarrow{\$} \mathcal{M}$	3: $\hat{c} \leftarrow \text{K-PKE.Enc}(\text{pk}, m, \hat{r})$
4: $\text{sk} \leftarrow (\text{sk}', \text{pk}, h, z)$	4: if $\hat{c} = c$ then
5: return (pk, sk)	5: $K \leftarrow \bar{K}$
	6: else
	7: $K \leftarrow \text{SHA3-256}(c, z)$
	8: end if
	9: return K
ML-KEM.Encap(pk)	
1: $m \xleftarrow{\$} \mathcal{M}$	
2: $h \leftarrow \text{SHA3-256}(\text{pk})$	
3: $(K, r) \leftarrow \text{SHA3-512}(m, h)$	
4: $c \leftarrow \text{K-PKE.Enc}(\text{pk}, m, r)$	
5: return (c, K)	

Figure 14: ML-KEM uses the $U_m^\mathcal{L}$ variant of the modular Fujisaki-Okamoto KEM transformation

379 We applied the encrypt-then-MAC transformation to the K-PKE routines of ML-KEM.
 380 The resulting KEM is called ML-KEM⁺ (See Figure 15).

381 When applying our encrypt-then-MAC transformation to K-PKE, we modified the
 382 routines described in Figure 6 such that the public key is added into the derivation of the
 383 MAC key and the shared secret. There are two main reasons behind this modification.
 384 First, in a realistic key exchange scenario, the public key will be generated by one party
 385 while the random PKE plaintext is sampled by the other party. Hashing both the public
 386 key and the plaintext ensures that both parties in a key exchange have inputs into deriving
 387 the shared secret. The second reason is to prevent a dictionary attack on the MAC key. If
 388 the MAC key is derived on plaintext alone, then an adversary can pre-compute a large
 389 dictionary mapping MAC keys to the corresponding PKE plaintext. Upon receiving the
 390 ciphertext, the adversary can search through the MAC keys and recover the PKE plaintext.

ML-KEM ⁺ .KeyGen()	ML-KEM ⁺ .Decap(sk, c)
1: $z \xleftarrow{\$} \{0, 1\}^{256}$ 2: $(pk, sk') \xleftarrow{\$} \text{K-PKE.KeyGen}()$ 3: $h \leftarrow H(pk)$ 4: $sk \leftarrow (sk' pk h z)$ 5: return (pk, sk)	Require: Secret key $sk = (sk' pk h z)$ Require: Ciphertext $c = (c' t)$ 1: $(sk', pk, h, z) \leftarrow sk$ 2: $(c', t) \leftarrow c$ 3: $\hat{m} \leftarrow \text{K-PKE.Dec}(sk', c')$ 4: $(\bar{K}, \hat{k}) \leftarrow G(\hat{m} h)$ 5: $\hat{t} \leftarrow \text{MAC}(\hat{k}, c')$ 6: if $\hat{t} = t$ then 7: $K \leftarrow \text{KDF}(\bar{K} t)$ 8: else 9: $K \leftarrow \text{KDF}(z t)$ 10: end if 11: return K
ML-KEM ⁺ .Encap(pk)	
1: $m \xleftarrow{\$} \{0, 1\}^{256}$ 2: $(\bar{K}, k) \leftarrow G(m H(pk))$ 3: $c' \xleftarrow{\$} \text{K-PKE.Enc}(pk, m)$ 4: $t \leftarrow \text{MAC}(k, c')$ 5: $K \leftarrow \text{KDF}(\bar{K} t)$ 6: $c \leftarrow (c', t)$ 7: return (c, K)	

Figure 15: ML-KEM⁺ applies our encrypt-then-MAC transformation to K-PKE. G is SHA3-512, H is SHA3-256, KDF is Shake256

Adding the public key into the derivation of the MAC key will dramatically increase the space requirement and render such dictionary attack infeasible in practice.

We also modified how the shared secret is derived: instead of hashing the entire ciphertext, we hashed the MAC tag, which essentially functions as a hash of the ciphertext and thus serves the same purpose. On the other hand, because ML-KEM ciphertext sizes range from 768 bytes to 1568 bytes while the tag size is fixed at 16 bytes, applying the KDF to the tag instead of the entire ciphertext further yields meaningful performance improvements.

4.1 Choosing a message authenticator

For implementation, we instantiated the MAC with a selection that covered a wide range of MAC designs, including Poly1305 [Ber05], GMAC [MV04], CMAC [IK03][BR05], and KMAC [Gro13].

Poly1305 and GMAC are both Carter-Wegman style authenticators [WC81] that compute the tag using finite field arithmetic. Generically speaking, Carter-Wegman MAC operates by breaking the message into message blocks that can then be parsed into finite field elements. The tag is computed by evaluating a polynomial whose coefficients are the message blocks and whose interderminate is the secret key.

Specifically, Poly1305 operates in the prime field \mathbb{F}_q where $q = 2^{130} - 5$ whereas GMAC operates in the binary field $\mathbb{F}_{2^{128}}$. In OpenSSL's implementation, standalone Poly1305 is a one-time secure MAC, whereas GMAC uses a nonce and AES as the PRF and is thus many-time secure (in OpenSSL GMAC is AES-256-GCM except all data is fed into the "associated data" section and thus not encrypted).

CMAC is based on the CBC-MAC with the block cipher instantiated from AES-256. To compute a CMAC tag, the message is first broke into 128-bit blocks with appropriate padding. Each block is first XOR'd with the previous block's output, then encrypted under AES using the symmetric key. The final output is XOR'd with a sub key derived from the symmetric key, before being encrypted for one last time.

KMAC is based on the SHA-3 family of sponge functions [oST15]. We chose KMAC-256, which uses Shake256 as the underlying extendable output functions. KMAC allows variable-length key and tag, but we chose the 256 bits for key length and 128 bits for tag size for consistency with other authenticators.

Remark. Unfortunately Poly1305, GMAC, and CMAC all use tag size of 128 bits with no straightforward ways to increase the tag size. We suspect this small tag size to be unsuitable for instantiation with ML-KEM-768 and ML-KEM-1024 due to their higher security target (192-bit and 256-bit security respectively). Consequently, we only instantiate with ML-KEM-512, with a target 128-bit security level.

5 Performance comparison

We measured the real-world performance of the individual routines of our ML-KEM⁺ construction, as well as the round trip time of performing key exchange over a network in a variety of authentication modes. Our implementation extended from the reference implementation by the PQCrystals team [BDK⁺24]. All C code is compiled with GCC 11.4.1 and OpenSSL 3.0.8. All binaries are executed on an AWS c7a.medium instance (AMD EPYC 9R14 CPU at 3.7 GHz and 1 GB of RAM) in the `us-west-2` region.

5.1 MAC performance

To isolate the performance characteristics of each authenticator in our instantiation of ML-KEM⁺ we measured the CPU cycles needed for each authenticator to compute a tag on random inputs whose sizes correspond to the ciphertext sizes of ML-KEM. The measurements are summarized in Table 3.

Table 3: CPU cycles needed to compute tag on various input sizes

Input size: 768 bytes		
MAC	Median (ccl/tick)	Average (ccl/tick)
Poly1305	909	2823
GMAC	3899	4859
CMAC	6291	6373
KMAC	6373	7791

5.2 Individual routine performance

Compared to the U_m^X variant of Fujisaki-Okamoto transformed used in ML-KEM, the encrypt-then-MAC transformation achieves massive CPU cycle count reduction in decapsulation while incurring only a minimal increase of encapsulation cycle count and ciphertext size. Since `K-PKE.Enc` carries significantly more computational complexity than `K-PKE.Dec` or any MAC we chose, the performance advantage of the encrypt-then-MAC transformation over the U_m^X transformation is dominated by the runtime saving gained from replacing *re-encryption* with MAC. A comparison between ML-KEM and variations of the ML-KEM⁺ can be found in Table 4.

Remark. We also included the performance of Kyber as it is submitted to the third round of the NIST PQC standardization project, which differs from ML-KEM by deriving the shared secret from hashing the public key, the PKE plaintext, and the PKE ciphertext, while ML-KEM derives its shared secret by hashing only the public key and the PKE plaintext. This results in ML-KEM having meaningful performance improvement in encapsulation over Kyber, though the performance difference in decapsulation is negligible.

Table 4: CPU cycles of each KEM routine

128-bit security		KEM variant		Encap cycles/tick		Decap cycles/tick	
size parameters (bytes)				Median	Average	Median	Average
pk size	800	ML-KEM-512		91467	92065	121185	121650
sk size	1632	Kyber512		97811	98090	119937	120299
ct size	768	ML-KEM ⁺ -512 w/ Poly1305		93157	93626	33733	33908
KeyGen cycles/tick		ML-KEM ⁺ -512 w/ GMAC		97369	97766	37725	37831
Median		ML-KEM ⁺ -512 w/ CMAC		99739	99959	40117	39943
Average		ML-KEM ⁺ -512 w/ KMAC		101009	101313	40741	40916

5.3 Key exchange protocols

The CRYSTALS-Kyber team [BDK⁺18] proposed three key exchange protocols: **Kyber**.KE for a passively secure ephemeral key exchange, **Kyber**.UAKE for unilaterally authenticated key exchange, and **Kyber**.AKE for mutually authenticated key exchange. First formally proposed in [BCK98] and later analyzed in [CK01], these key exchange protocols all achieve weak forward secrecy, and the authenticated key exchange protocols are resistant to certain categories of active adversaries (e.g. Man-in-the-Middle attacks).

We implemented each of the three Kyber key exchange protocols using ML-KEM⁺ and ML-KEM, then measured the round trip time of each handshake. We denote the party who sends the first message to be the client and the other party to be the server. Round trip time (RTT) is defined to be the time interval between the moment before the client starts generating ephemeral keypairs and the moment after the client derives the final session key. All experiments are run on a pair of AWS c7a.medium instances both located in the **us-west-2** region. For each experiment, a total of 10,000 rounds of key exchange are performed, with the median and average round trip time (measured in microsecond) recorded.

Remark. Using KEM for authentication is especially interesting within the context of post-quantum cryptography: post-quantum KEM schemes usually enjoy better performance characteristics than post-quantum signature schemes with faster runtime, smaller memory footprint, and smaller communication sizes. KEMTLS [SSW20] was proposed in 2020 as an alternative to existing TLS handshake protocols, and many experimental implementations have demonstrated the performance advantage.

5.3.1 Unauthenticated key exchange

In unauthenticated key exchange (KE), a single pair of ephemeral keypair $(\mathbf{pk}_e, \mathbf{sk}_e) \xleftarrow{\$} \text{KeyGen}()$ is generated by the client. The client transmits the ephemeral public key \mathbf{pk}_e to the server, who runs the encapsulation routine $(c_e, K_e) \xleftarrow{\$} \text{Encap}(\mathbf{pk}_e)$ and transmits the ciphertext c_e back to the client. The client finally decapsulates the ciphertext to recover the shared secret $K_e \leftarrow \text{Decap}(\mathbf{sk}_e, c_e)$. The key exchange routines are summarized in Figure 16. The key derivation function is instantiated using Shake256, and the final session key is 256 bits in length. The RTT comparison is summarized in Table 5

Table 5: KE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT (μs)	
			Median	Average
ML-KEM-512	800	768	92	97
ML-KEM ⁺ -512 w/ Poly1305	800	784	70	72
ML-KEM ⁺ -512 w/ GMAC	800	784	73	76
ML-KEM ⁺ -512 w/ CMAC	800	784	75	79
ML-KEM ⁺ -512 w/ KMAC	800	784	76	78

$\text{KE}_c()$	$\text{KE}_s()$
1: $(\text{pk}_e, \text{sk}_e) \xleftarrow{\$} \text{KeyGen}()$ 2: send (pk_e) 3: $c_e \leftarrow \text{read}()$ 4: $K_e \leftarrow \text{Decap}(\text{sk}_e, c_e)$ 5: $K \leftarrow \text{KDF}(K_e)$ 6: return K	1: $\text{pk}_e \leftarrow \text{read}()$ 2: $(c_e, K_e) \xleftarrow{\$} \text{Encap}(\text{pk}_e)$ 3: send (c_e) 4: $K \leftarrow \text{KDF}(K_e)$ 5: return K

Figure 16: Unauthenticated key exchange (KE) routines

5.3.2 Unilaterally authenticated key exchange

In unilaterally authenticated key exchange (UAKE), the authenticating party proves its identity to the other party by demonstrating possession of a secret key that corresponds to a published long-term public key. In this implementation, the client possesses the long-term public key pk_S of the server, and the server authenticates itself by correctly decrypting the challenge encryption sent by the client. UAKE routines are summarized in Figure 17.

$\text{UAKE}_c(\text{pk}_S)$	$\text{UAKE}_s(\text{sk}_S)$
Require: Server's long-term pk_S 1: $(\text{pk}_e, \text{sk}_e) \xleftarrow{\$} \text{KeyGen}()$ 2: $(c_S, K_S) \xleftarrow{\$} \text{Encap}(\text{pk}_S)$ 3: send (pk_e, c_S) 4: $c_e \leftarrow \text{read}()$ 5: $K_e \leftarrow \text{Decap}(\text{sk}_e, c_e)$ 6: $K \leftarrow \text{KDF}(K_e \ K_S)$ 7: return K	Require: Server's long-term sk_S 1: $(\text{pk}_e, c_S) \leftarrow \text{read}()$ 2: $K_S \leftarrow \text{Decap}(\text{sk}_S, c_S)$ 3: $(c_e, K_e) \xleftarrow{\$} \text{Encap}(\text{pk}_e)$ 4: send (c_e) 5: $K \leftarrow \text{KDF}(K_e \ K_S)$ 6: return K

Figure 17: Unilaterally authenticated key exchange (UAKE) routines

In addition to the long-term key, the client will also generate an ephemeral keypair as it does in an unauthenticated key exchange, and the session key is derived by applying the KDF to the concatenation of both the ephemeral shared secret and the shared secret encapsulated under server's long-term key. This helps the key exchange to achieve weak forward secrecy [CK01]. Performance data is summarized in Table 6.

Table 6: UAKE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT (μs)	
			Median	Average
ML-KEM-512	1568	768	145	151
ML-KEM ⁺ -512 w/ Poly1305	1584	784	103	106
ML-KEM ⁺ -512 w/ GMAC	1584	784	106	110
ML-KEM ⁺ -512 w/ CMAC	1584	784	108	112
ML-KEM ⁺ -512 w/ KMAC	1584	784	109	113

5.3.3 Mutually authenticated key exchange (AKE)

Mutually authenticated key exchange is largely identical to unilaterally authenticated key exchange, except for that client authentication is required. This means that client possesses server's long-term public key and its own long-term secret key, while the server possesses client's long-term public key and its own long-term secret key. The session key is derived by applying KDF onto the concatenation of shared secrets produced under the ephemeral keypair, server's long-term keypair, and client's long-term keypair, in this order. the key exchange routines are described in Figure 18 and the performance data summarized in Table 7.

$\text{AKE}_c(\text{pk}_S, \text{sk}_C)$	$\text{AKE}_s(\text{sk}_S, \text{pk}_C)$
Require: Server's long-term pk_S	Require: Server's long-term sk_S
Require: Client's long-term sk_C	Require: Client's long-term pk_C
1: $(\text{pk}_e, \text{sk}_e) \xleftarrow{\$} \text{KeyGen}()$	1: $(\text{pk}_e, c_S) \leftarrow \text{read}()$
2: $(c_S, K_S) \xleftarrow{\$} \text{Encap}(\text{pk}_S)$	2: $K_S \leftarrow \text{Decap}(\text{sk}_S, c_S)$
3: send (pk_e, c_S)	3: $(c_e, K_e) \xleftarrow{\$} \text{Encap}(\text{pk}_e)$
4: $(c_e, c_C) \leftarrow \text{read}()$	4: $(c_C, K_C) \xleftarrow{\$} \text{Encap}(\text{pk}_C)$
5: $K_e \leftarrow \text{Decap}(\text{sk}_e, c_e)$	5: send (c_e, c_C)
6: $K_C \leftarrow \text{Decap}(\text{sk}_e, c_C)$	6: $K \leftarrow \text{KDF}(K_e \ K_S \ K_C)$
7: $K \leftarrow \text{KDF}(K_e \ K_S \ K_C)$	7: return K
8: return K	

Figure 18: Mutually authenticated key exchange (AKE) routines

Table 7: AKE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT (μs)	
			Median	Average
ML-KEM-512	1568	1536	220	213
ML-KEM ⁺ -512 w/ Poly1305	1584	1568	133	138
ML-KEM ⁺ -512 w/ GMAC	1584	1568	139	143
ML-KEM ⁺ -512 w/ CMAC	1584	1568	143	148
ML-KEM ⁺ -512 w/ KMAC	1584	1568	145	151

6 Conclusions and future works

The encrypt-then-MAC transformation is a generic KEM construction whose IND-CCA security reduces to the OW-PCA security of the input PKE and the one-time existential unforgeability of the input MAC in the random oracle model. Compared to the Fujisaki-Okamoto transformation, the encrypt-then-MAC replaces the computationally expensive re-encryption with computing a MAC tag. At the cost of minimal increase in encapsulation cost and ciphertext size, the encrypt-then-MAC substantially improves the efficiency of the decapsulation routine. Where the input PKE's encryption is slower than decryption, the encrypt-then-MAC KEM achieves meaningful time savings in practical key exchange protocols.

In our future work, we would like to look at applying encryption-then-MAC transformation to other post-quantum cryptosystems for improving their practical implementation efficiency.

Code-based cryptosystems. Because the general problem of decoding a linear code is proven NP hard [BMvT78], code-based cryptosystems does not suffer from the inherent search-decision equivalence of lattice problems and thus be viable candidates with OW-PCA security. Unfortunately, among the code-based submissions to NIST PQC, HQC [MAB⁺18] and BIKE [ABB⁺22] are known to be vulnerable to key-recovery plaintext-checking attacks (KR-PCA) [TUX⁺23]. On the other hand, classic McEliece [ABC⁺20] seems to be PCA secure and thus a viable candidate, although in classic McEliece, the decoding routine is more expensive than the encryption routine, so applying encrypt-then-MAC may yield less impressive performance gains.

Isogeny-based cryptosystems. The intractability assumptions of isogeny-based cryptography resemble the classical Diffie-Hellman assumptions, and it seems possible to formulate a “Gap Diffie-Hellman assumption” in supersingular isogeny [FTTY18]. In fact, SIKE [ACC⁺17] also uses the Fujisaki-Okamoto transformation, and given the heavy computational cost of isogeny computation, replacing re-encryption with MAC will result in substantial performance improvements. While SIKE and SIDH were found to be insecure [CD23], other isogeny-based cryptosystem such as CSIDH [CLM⁺18] remains unaffected by the aforementioned attack and might be suitable candidates.

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