Faster generic IND-CCA2 secure KEM using "encrypt-then-MAC"

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Abstract. The modular Fujisaki-Okamoto (FO) transformation takes public-key encryption with weaker security and constructs a key encapsulation mechanism (KEM) with indistinguishability under adaptive chosen ciphertext attacks. While the modular FO transform enjoys tight security bound and quantum resistance, it also suffers from computational inefficiency and vulnerabilities to side-channel attacks due to using de-randomization and re-encryption for providing ciphertext integrity. In this work, we propose an alternative KEM construction that achieves ciphertext integrity using a message authentication code (MAC) and instantiate a concrete instance using Kyber. Our experimental results showed that where the encryption routine incurs heavy computational cost, replacing re-encryption with MAC provides substantial performance improvements at comparable security level.

Keywords: Key encapsulation mechanism, post-quantum cryptography, lattice cryptography, Fujisaki-Okamoto transformation

1 Introduction

Key encapsulation mechanism (KEM) is a cryptographic primitive that allows two parties to establish a shared secret over an insecure channel. The combination of KEM and some data encapsulation mechanism (DEM), such as AES-GCM and ChaCha20-Poly1305, is the foundation of many of today's most popular secure communication protocols such as Transport Layer Security (TLS) and Secure Shell (SSH). The commonly accepted security standard of a KEM is *Indistinguishability under adaptive chosen-ciphertext attack* (IND-CCA2): no efficient adversary can distinguish a shared secret obtained by running the encapsulation routine from random noise, even with access to a decapsulation oracle throughout the attack. KEM is related to another important cryptographic primitive called public-key encryption (PKE), and their security standards are similar. The desired security standard for PKE, also called IND-CCA2, requires that no efficient adversary can distinguish the encryption of two adversarially chosen messages even with access to decryption oracle.

It is difficult to build a provably IND-CCA2 secure KEM from scratch. Instead, secure KEMs are usually built on top of a PKE with weaker security property (e.g. being only OW-CPA or IND-CPA secure, not IND-CCA2). One such construction is the Fujisaki-Okamoto transformation, proposed in 1999 by Fujisaki Eiichiro and Okamoto Tetsuyaki in their seminal paper [FO99][FO13]. The first Fujisaki-Okamoto transformation combines an OW-CPA secure PKE with an IND-CPA secure symmetric cipher into a hybrid PKE (HPKE) with proven IND-CCA2 security under the random oracle model. Subsequent works [OP01b][CHJ⁺02][Den03] improved on the original proposal and adapted it to build KEM instead of HPKE. This line of work culminated in a landmark publication in 2017 by Hofhein, Hovelmann, and Kiltz [HHK17][HHM22], where the authors provided a versatile variety of modular KEM constructions with tight security reduction in the random oracle model and non-tight security reduction in the quantum random oracle model.

The modular Fujisaki-Okamoto KEM transformation is remarkably successful. It was adopted by many submissions to NIST's post-quantum cryptography competition,

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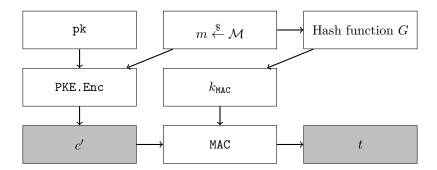


Figure 1: Combining PKE with MAC using "encrypt-then-MAC" to encapsulate a shared secret. The returned values are colored grey

including Kyber [BDK⁺18], Saber [DKRV18], FrodoKEM [BCD⁺16], and classic McEliece [ABC⁺20] among others. When Kyber was standardized by NIST in FIPS 203 "Module-lattice key-encapsulation mechanism" (ML-KEM) [oST24], it kept the Fujisaki-Okamoto transformation in its KEM construction. However, the Fujisaki-Okamoto transformation is not perfect. It uses *de-randomization* and *re-encryption* to achieve *rigidity* [BP18] which then ensures ciphertext integrity. This brings two problems:

- computational inefficiency: where the PKE's encryption routine is substantially more expensive than the decryption routine, using re-encryption causes the decapsulation routine in the output KEM to become computationally expensive
- side-channel vulnerability: running the input PKE's encryption routine in the output KEM's decapsulation routine introduces risk of side-channel vulnerabilities not found in the input PKE's decryption routine alone. In fact, many practical attacks [UXT⁺22][RRCB19] exploit re-encryption to decrypt ciphertext or recover secret keys. Countermeasures such as masking have been proposed to address these side channels, but they inevitably carry substantial performance penalty.

1.1 Our contributions

Our main contribution is a novel generic KEM construction that combines a PKE with weak security and a message authentication code (MAC). We were inspired by the strategy used in symmetric cyrptography for achieving IND-CCA2 security: combining a symmetric 63 cipher with a MAC in a pattern called "encrypt-then-MAC". In the encapsulation routine of the "encrypt-then-MAC" KEM construction, a random PKE plaintext m is sampled and encrypted into some PKE ciphertext c'; a symmetric key k, derived from hashing the plaintext, is used to compute a message authenticator t on the PKE ciphertext c'. 67 The KEM ciphertext c = (c', t) contains both the PKE ciphertext and the message authenticator. At decapsulation, the PKE ciphertext c' is decrypted into \hat{m} first, then a symmetric key \hat{k} is derived from hashing the decryption \hat{m} . The symmetric key is used to 70 verify the authenticator against the PKE ciphertext. A illustration of the data flow in the 71 "encrypt-then-MAC" KEM construction can be found in figure 1. A detailed description of the individual routines can be found in figure 5.

1.1.1 Security reduction

By authenticating the PKE ciphertext using a symmetric key derived from its decryption, the "encrypt-then-MAC" construction greatly limits the amount of information an adversary can learn from a chosen-ciphertext attack. For an adversary to produce a valid

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KEM ciphertext, it must produce a valid message authenticator for the PKE ciphertext under the correct symmetric key. Under the random oracle model, the symmetric key is indistinguishable from uniformly random unless the adversary also knows the corresponding plaintext completely, thus rendering the output of the decasulation oracle redundant. Furthermore, because each encapsulation will pick a random message, within a reasonable lifetime of the KEM keypair, each KEM ciphertext will be authenticated using a distinct symmetric key, so the choice of MAC is only required to be one-time secure, affording us additional performance gains by choosing more efficient MAC instances. In section 3, we prove that the IND-CCA2 security of the "encrypt-then-MAC" KEM reduces tightly to the OW-PCA security of the input PKE and the one-time existential unforgeability of the input MAC under the random oracle model.

One-wayness under plaintext-checking attack (OW-PCA)[OP01b] requires that no efficient adversary can recover some random encryption even with access to a plaintext-checking oracle, who accepts a plaintext-ciphertext pair (m,c) and returns whether the queried ciphertext decrypts to the queried plaintext. While it is not a standard security notion, it is useful when reducing the security of the "encrypt-then-MAC" KEM to the security of the PKE, and there are many well studied cryptosystems that are known to be OW-PCA: the RSA cryptosystem [RSA78] is known to be a trapdoor permutation and thus trivially OW-PCA secure; the ElGamal cryptosystem [Gam85] is conjectured to be OW-PCA secure under the Gap Diffie-Hellman assumption [OP01a].

1.1.2 Performance improvements

The main advantage of our KEM construction over the Fujisaki-Okamoto transformation is the performance gains: our construction replaces re-encryption with computing a message authenticator, which is significantly faster. When instantiated with the underlying PKE routines of ML-KEM and the Poly1305 message authenticator, our construction ML-KEM⁺ achieves on average 72%-80% reduction of CPU cycles needed for decapsulation while only incurring 2%-7% increase of CPU cycles for encapsulation when compared to ML-KEM.

	Table 1: ML-KEM is instantiated with Poly1305						
	ML-KEM	ML-KEM ⁺	ML-KEM	ML-KEM ⁺	ML-KEM	ML-KEM ⁺	
	512	512	768	768	1024	1024	
Encap	91467	93157	136405	146405	199185	205763	
(ccl/tick)		(+1.8%)		(+7.3%)		(+3.3%)	
Decap	121185	33733	186445	43315	246245	51375	
(ccl/tick)		(-72.2%)		(-76.8%)		(-79.1%)	
CT size	768	784	1088	1104	1568	1584	
(bytes)		(+2.1%)		(+1.5%)		(+1.0%)	

Table 1: ML-KEM⁺ is instantiated with Poly1305

We also implemented and measured the round trip time of key exchange protocols with various modes of authentication. When compared to ML-KEM, ML-KEM $^+$ achieves 24%-28% reduction of round trip time in unauthenticated key exchange (KE), 29%-35% reduction in unilaterally authenticated key exchange (UAKE), and 35%-48% reduction in mutually authenticated key exchange (AKE).

Table 2: Key exchange round-trip times

	ML-KEM	ML-KEM ⁺	ML-KEM	ML-KEM ⁺	ML-KEM	ML-KEM ⁺
	512	512	768	768	1024	1024
KE RTT	92	70	135	99	193	138
(μs)		(-23.9%)		(-26.7%)		(-28.5%)
UAKE RTT	145	103	215	144	310	202
(μs)		(-29.0%)		(-33.0%)		(-34.8%)
AKE RTT	220	133	294	190	512	266
(μs)		(-39.5%)		(-35.4%)		(-48.0%)

1.2 Related works

As mentioned at the beginning of section 1, there is a large volume of previous proposals that combine cryptographic primitives with weak security properties into cryptographic primitives with strong security properties. Besides the Fujisaki-Okamoto transformation, another transformation that sees substantial adoption is *Optimal Asymmetric Encryption Padding (OAEP)* [BR94]. Unfortunately, OAEP can only be applied to one-way trapdoor permutation, a rare occurrence. To this day, RSA remains the only viable candidate [FOPS01], though RSA-OAEP has been widely adopted after its standardization in PKCS#1 v2.2 [MKJR16].

Securing an encryption scheme against chosen-ciphertext attack was a well-studied problem in the context of symmetric cryptography. Among the three generic patterns "encrypt-then-MAC", "encrypt-and-MAC", "MAC-then-encrypt", only the first one is formally analyzed and proved to be secure with any combination of symmetric cipher and MAC [Kra01][CK01]. "MAC-then-encrypt" is only secure with specific choices of symmetric cipher and MAC, and "encrypt-and-MAC" is generally not semantically secure since most MAC will leak information about the message it authenticates. Today's most well-established symmetric encryption schemes, including AES-GCM and ChaCha20-Poly1305, largely follow the pattern of "encrypt-then-MAC".

The idea of using a message authenticator to ensure ciphertext integrity was instantiated with ElGamal cryptosystem by Bellare and Rogaway in 1997 [BR97], and its security was later reduced to the Gap Diffie-Hellman assumption by Abdulla, Bellare, and Rogaway in [ABR01] in 2001. Our work can be seen as generalizing Bellare and Rogaway's scheme from ElGamal cryptosystem to all PKE with OW-PCA security.

2 Preliminaries and previous results

2.1 Public-key encryption scheme

Syntax. A public-key encryption scheme PKE(KeyGen, Enc, Dec) is a collection of three routines defined over some plaintext space \mathcal{M} and some ciphertext space \mathcal{C} . (pk, sk) $\overset{\$}{\leftarrow}$ KeyGen() is a randomized routine that returns a keypair. The encryption routine Enc: (pk, m) $\mapsto c$ encrypts the input plaintext under the input public key. The decryption routine Dec: (sk, c) $\mapsto m$ decrypts the input ciphertext under the input secret key. Where the encryption routine is randomized, we denote the randomness by $r \in \mathcal{R}$, where \mathcal{R} is called the coin space. The decryption routine is assumed to always be deterministic. Some decryption routines can detect malformed ciphertext and output the rejection symbol \bot accordingly.

Correctness. Following the definition in [DNR04] and [HHK17], a PKE is δ -correct if:

$$E\left[\max_{m \in \mathcal{M}} P\left[\mathtt{Dec}(\mathtt{sk}, c) \neq m \mid c \overset{\$}{\leftarrow} \mathtt{Enc}(\mathtt{pk}, m)\right]\right] \leq \delta$$

Where the expectation is taken with respect to the probability distribution of all possible keypairs (pk, sk) $\stackrel{\$}{\leftarrow}$ PKE.KeyGen(). For many lattice-based cryptosystems, including ML-KEM, decryption failures could leak information about the secret key, although the probability of a decryption failure is low enough that classical adversaries cannot exploit decryption failure more than they can defeat the underlying lattice problem. On the other hand, a quantum adversary may be able to exploit decryption failure in reasonable runtime by efficiently searching through all possible inputs using Grover's search algorithm. For that, ML-KEM made slight modifications in its KEM construction to prevent quantum adversary from precomputing large lookup table. We refer readers to [ABD+19] and [BDK+18] for the details.

Security. We discuss the security of a PKE using the sequence of games described in [Sho04]. Specifically, we first define the OW-ATK as they pertain to a public key encryption scheme. In later section we will define the IND-CCA game as it pertains to a key encapsulation mechanism.

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 \begin{array}{c} \overline{\text{The OW-ATK game}} \\ 1: \ (\text{pk}, \text{sk}) \xleftarrow{\$} \text{KeyGen}(1^{\lambda}) \\ 2: \ m^* \xleftarrow{\$} \mathcal{M} \\ 3: \ c^* \xleftarrow{\$} \text{Enc}(\text{pk}, m^*) \\ 4: \ \hat{m} \xleftarrow{\$} \mathcal{A}^{\mathcal{O}_{\text{ATK}}}(1^{\lambda}, \text{pk}, c^*) \\ 5: \ \mathbf{return} \ \llbracket m^* = \hat{m} \rrbracket \end{array} \qquad \begin{array}{c} \overline{\text{PCO}(m \in \mathcal{M}, c \in \mathcal{C})} \\ 1: \ \mathbf{return} \ \llbracket \text{Dec}(\text{sk}, c) = m \rrbracket \end{array}
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Figure 2: One-way security game of PKE (left) and plaintext-checking oracle (right)

In the OW-ATK game (see figure 2), an adversary's goal is to recover the decryption of a randomly generated ciphertext. A challenger randomly samples a keypair and a challenge plaintext m^* , encrypts the challenge plaintext $c^* \stackrel{\$}{\leftarrow} \operatorname{Enc}(\operatorname{pk}, m^*)$, then gives pk and c^* to the adversary A. The adversary A, with access to some oracle $\mathcal{O}_{\operatorname{ATK}}$, outputs a guess decryption \hat{m} . A wins the game if its guess \hat{m} is equal to the challenge plaintext m^* . The advantage $\operatorname{Adv}_{\operatorname{OW-ATK}}$ of an adversary in this game is the probability that it wins the game:

$$\mathtt{Adv}_{\mathtt{OW-ATK}}(A) = P\left[A(\mathtt{pk}, c^*) = m^* | (\mathtt{pk}, \mathtt{sk}) \xleftarrow{\$} \mathtt{KeyGen}(); m^* \xleftarrow{\$} \mathcal{M}; c^* \xleftarrow{\$} \mathtt{Enc}(\mathtt{pk}, m^*)\right]$$

The capabilities of the oracle $\mathcal{O}_{\mathtt{ATK}}$ depends on the choice of security goal ATK. Particularly relevant to our result is security against plaintext-checking attack (PCA), for which the adversary has access to a plaintext-checking oracle (PCO) (see figure 2). A PCO takes as input a plaintext-ciphertext pair (m,c) and returns True if m is the decryption of c or False otherwise.

2.2 Key encapsulation mechanism (KEM)

A key encapsulation mechanism is a collection of three routines (KeyGen, Encap, Decap) defined over some ciphertext space $\mathcal C$ and some key space $\mathcal K$. The key generation routine takes the security parameter 1^λ and outputs a keypair (pk, sk) $\stackrel{\$}{\leftarrow}$ KeyGen(1^λ). Encap(pk) is a probabilistic routine that takes a public key pk and outputs a pair of values (c,K) where $c \in \mathcal C$ is the ciphertext (also called encapsulation) and $K \in \mathcal K$ is the shared secret (also called session key). Decap(sk, c) is a deterministic routine that takes the secret key sk and the encapsulation c and returns the shared secret K if the ciphertext is valid. Some KEM constructions use explicit rejection, where if c is invalid then Decap will return a rejection symbol \bot ; other KEM constructions use implicit rejection, where if c is invalid then Decap will return a fake session key that depends on the ciphertext and some other secret values.

The IND-CCA security of a KEM is defined by an adversarial game in which an adversary's goal is to distinguish pseudorandom shared secret (generated by running the Encap routine) and a truly random value.

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 \begin{array}{c} \underline{\text{KEM-IND-CCA2 game}} \\ 1: \; (\text{pk}, \text{sk}) \xleftarrow{\$} \text{KeyGen}(1^{\lambda}) \\ 2: \; (c^*, K_0) \xleftarrow{\$} \text{Encap}(\text{pk}) \\ 3: \; K_1 \xleftarrow{\$} \mathcal{K} \\ 4: \; b \xleftarrow{\$} \{0, 1\} \\ 5: \; \hat{b} \xleftarrow{\$} A^{\mathcal{O}_{\text{Decap}}}(1^{\lambda}, \text{pk}, c^*, K_b) \\ 6: \; \mathbf{return} \; [\hat{b} = b] & \underline{\mathcal{O}_{\text{Decap}}(c)} \\ 1: \; \mathbf{return} \; \mathbf{Decap}(\text{sk}, c) \\ \end{array}
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Figure 3: IND-CCA2 game for KEM (left) and decapsulation oracle (right)

The decapsulation oracle $\mathcal{O}^{\text{Decap}}$ takes a ciphertext c and returns the output of the Decap routine using the secret key. The advantage $\epsilon_{\text{IND-CCA}}$ of an IND-CCA adversary $\mathcal{A}_{\text{IND-CCA}}$ is defined by

$$\mathtt{Adv}_{\mathtt{IND-CCA}}(A) = \left| P[A^{\mathcal{O}_{\mathtt{Decap}}}(a^{\lambda}, \mathtt{pk}, c^*, K_b) = b] - \frac{1}{2} \right|$$

2.3 Message authentication code (MAC)

A message authentication code MAC is a collection of routines (Sign, Verify) defined over some key space \mathcal{K} , some message space \mathcal{M} , and some tag space \mathcal{T} . The signing routine Sign(k,m) takes the secret key $k \in \mathcal{K}$ and some message, and outputs a tag t. The verification routine Verify(k,m,t) takes the triplet of secret key, message, and tag, and outputs 1 if the message-tag pair is valid under the secret key, or 0 otherwise. Many MAC constructions are deterministic. For these constructions it is simpler to denote the signing routine by $t \leftarrow \text{MAC}(k,m)$ and perform verification using a simple comparison.

The security of a MAC is defined in an adversarial game in which an adversary, with access to some signing oracle $\mathcal{O}_{\mathtt{Sign}}(m)$, tries to forge a new valid message-tag pair that has never been queried before. The existential unforgeability under chosen message attack (EUF-CMA) game is shown below:

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EUF-CMA game

1: k^* \stackrel{\$}{\leftarrow} \mathcal{K}
2: (\hat{m}, \hat{t}) \stackrel{\$}{\leftarrow} \mathcal{A}^{\mathcal{O}_{\operatorname{Sign}}}()
3: return [Verify(k^*, \hat{m}, \hat{t}) \wedge (\hat{m}, \hat{t}) \not\in \mathcal{O}_{\operatorname{Sign}}]
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Figure 4: The existential forgery game

The advantage $Adv_{EUF-CMA}$ of the existential forgery adversary is the probability that it wins the EUF-CMA game.

3 The "encrypt-then-MAC" transformation

Let \mathcal{B}^* denote the set of finite bit strings. Let PKE(KeyGen, Enc, Dec) be a public-key encryption scheme defined over message space \mathcal{M} and ciphertext space \mathcal{C} . Let MAC: $\mathcal{K}_{MAC} \times \mathcal{B}^* \to \mathcal{T}$ be a deterministic message authentication code that takes a key $k \in \mathcal{K}_{MAC}$, some message $m \in \mathcal{B}^*$, and outputs a digest $t \in \mathcal{T}$. Let $G: \mathcal{M} \to \mathcal{K}_{MAC}$ be a hash

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function that maps from PKE's plaintext space to MAC's key space. Let $H: \mathcal{B}^* \to \mathcal{K}_{\texttt{KEM}}$ be a hash function that maps bit strings into the set of possible shared secrets. The "encrypt-then-MAC" transformation EtM[PKE,MAC,G,H] constructs a key encapsulation mechanism $\texttt{KEM}_{\texttt{EtM}}(\texttt{KeyGen}_{\texttt{KEM}},\texttt{Encap},\texttt{Decap})$, whose routines are described in figure 5.

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KEM_{EtM}.KeyGen()
                                                                                 KEM_{EtM}.Decap(sk, c)
                                                                                   1: (c',t) \leftarrow c
  1: (pk, sk') \stackrel{\$}{\leftarrow} PKE.KeyGen()
                                                                                  2: (sk', z) \leftarrow sk
  2: z \stackrel{\$}{\leftarrow} \mathcal{M}
                                                                                  3: \hat{m} \leftarrow \texttt{PKE.Dec}(\texttt{sk}', c')
  3: sk \leftarrow sk' ||z|
                                                                                   4: \hat{k} \leftarrow G(\hat{m})
  4: return (pk, sk)
                                                                                       if MAC(k, c') \neq t then
                                                                                             K \leftarrow H(z,c')
                                                                                  6:
                                                                                  7: else
KEM_{EtM}.Encap(pk)
                                                                                             K \leftarrow H(\hat{m}, c')
                                                                                  8:
                                                                                  9: end if
  1: m \stackrel{\$}{\leftarrow} \mathcal{M}
                                                                                 10: \mathbf{return}\ K
  2: k \leftarrow G(m)
  3: c' \stackrel{\$}{\leftarrow} \texttt{PKE.Enc}(\texttt{pk}, m)
  4: t \leftarrow \text{MAC}(k, c')
  5: K \leftarrow H(m, c')
  6: c \leftarrow c' || t
  7: return (c, K)
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Figure 5: KEM_{EtM} routines

The key generation routine of $\mathtt{KEM}_{\mathtt{EtM}}$ is largely identical to that of the PKE, only a secret value z is sampled as the implicit rejection symbol. In the encapsulation routine, a MAC key is derived from the randomly sampled plaintext $k \leftarrow G(m)$, then used to sign the unauthenticated ciphertext c'. Because the encryption routine might be randomized, the session key is derived from both the message and the ciphertext. Finally, the unauthenticated ciphertext c' and the tag t combine into the authenticated ciphertext c that would be transmitted to the peer. In the decapsulation routine, the decryption \hat{m} of the unauthenticated ciphertext is used to re-derive the MAC key \hat{k} , which is then used to re-compute the tag \hat{t} . The ciphertext is considered valid if and only if the recomputed tag is identical to the input tag.

For an adversary A to produce a valid tag t for some unauthenticated ciphertext c' under the symmetric key $k \leftarrow G(\mathtt{Dec}(\mathtt{sk'},c'))$ implies that A must either know the symmetric key k or produce a forgery. Under the random oracle model, A also cannot know k without knowing its preimage $\mathtt{Dec}(\mathtt{sk'},c')$, so A must either have produced c' honestly, or have broken the one-way security of PKE. This means that the decapsulation oracle will not give out information on decryptions that the adversary does not already know.

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\begin{split} & \frac{\texttt{PCO}(m,c)}{1: \ k \leftarrow G(m)} \\ & 2: \ t \leftarrow \texttt{MAC}(k,c) \\ & 3: \ \mathbf{return} \ \llbracket \mathcal{O}^{\texttt{Decap}}((c,t)) = H(m,c) \rrbracket \end{split}
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Figure 6: Every decapsulation oracle can be converted into a plaintext-checking oracle

However, a decapsulation oracle can still give out some information: for a known plaintext m, all possible encryptions $c' \stackrel{\$}{\leftarrow} \operatorname{Enc}(\operatorname{pk}, m)$ can be correctly signed, while ciphertexts that don't decrypt back to m cannot be correctly signed. This means that a decapsulation oracle can be converted into a plaintext-checking oracle (see figure 6), so every chosen-ciphertext attack against the KEM can be converted into a plaintext-checking attack against the underlying PKE.

On the other hand, if the underlying PKE is one-way secure against plaintext-checking attack that makes q plaintext-checking queries, then "encrypt-then-MAC" KEM is semantically secure under chosen ciphertext attacks making the same number of decapsulation queries:

Theorem 1. For every IND-CCA2 adversary A against KEM_{EtM} that makes q decapsulation queries, there exists an OW-PCA adversary B who makes at least q plaintext-checking queries against the underlying PKE, and an one-time existential forgery adversary C against the underlying MAC such that

$$\mathit{Adv}_{\mathit{IND-CCA2}}(A) \leq q \cdot \mathit{Adv}_{\mathit{OT-MAC}}(C) + 2 \cdot \mathit{Adv}_{\mathit{OW-PCA}}(B)$$

Theorem 1 naturally flows into an equivalence relationship between the security of the KEM and the security of the PKE:

Lemma 1. KEM_{EtM} is IND-CCA2 secure if and only if the input PKE is OW-PCA secure

3.1 Proof of theorem 1

We will prove theorem 1 using a sequence of game. A summary of the the sequence of games can be found in figure 7 and 8. From a high level we made three incremental modifications to the IND-CCA2 game for KEM_{EtM} : replace true decapsulation with simulated decapsulation, replace the pseudorandom MAC key $k^* \leftarrow G(m^*)$ with a truly random MAC key $k^* \leftarrow \mathcal{K}_{MAC}$, and finally replace pseudorandom shared secret $K_0 \leftarrow H(m^*, c')$ with a truly random shared secret $K_0 \leftarrow \mathcal{K}_{KEM}$. A OW-PCA adversary can then simulate the modified IND-CCA2 game for the KEM adversary, and the advantage of the OW-PCA adversary is associated with the probability of certain behaviors of the KEM adversary.

Proof. Game 0 is the standard IND-CCA2 game for KEMs. The decapsulation oracle $\mathcal{O}^{\mathsf{Decap}}$ executes the decapsulation routine using the challenge keypair and return the results faithfully. The queries made to the hash oracles $\mathcal{O}^G, \mathcal{O}^H$ are recorded to their respective tapes $\mathcal{L}^G, \mathcal{L}^H$.

Game 1 is identical to game 0 except that the true decapsulation oracle $\mathcal{O}^{\mathsf{Decap}}$ is replaced with a simulated oracle $\mathcal{O}^{\mathsf{Decap}}_1$. Instead of directly decrypting c' as in the decapsulation routine, the simulated oracle searches through the tape \mathcal{L}^G to find a matching query (\tilde{m}, \tilde{k}) such that \tilde{m} is the decryption of c'. The simulated oracle then uses \tilde{k} to validate the tag t against c'.

If the simulated oracle accepts the queried ciphertext as valid, then there is a matching query that also validates the tag, which means that the queried ciphertext is honestly generated. Therefore, the true oracle must also accept the queried ciphertext. On the other hand, if the true oracle rejects the queried ciphertext (and output the implicit rejection H(z,c')), then the tag is simply invalid under the MAC key k=G(Dec(sk',c')). Therefore, there could not have been a matching query that also validates the tag, and the simulated oracle must also rejects the queried ciphertext.

This means that from the adversary A's perspective, game 1 and game 0 differ only when the true oracle accepts while the simulated oracle rejects, which means that t is a valid tag for c' under $k = G(\mathtt{Dec}(\mathtt{sk}', c'))$, but k has never been queried. Under the random

IND-CCA2 game for KEM _{EtM}		$\mathcal{O}^{ extsf{Decap}}(c)$
1: $(pk, sk) \stackrel{\$}{\leftarrow} KEM_{EtM}$. $KeyGen()$ 2: $m^* \stackrel{\$}{\leftarrow} \mathcal{M}$ 3: $c' \stackrel{\$}{\leftarrow} PKE$. $Enc(pk, m^*)$ 4: $k^* \leftarrow G(m^*)$ 5: $k^* \stackrel{\$}{\leftarrow} \mathcal{K}_{MAC}$ 6: $t \leftarrow MAC(k^*, c')$ 7: $c^* \leftarrow c' t$ 8: $K_0 \leftarrow H(m^*, c')$ 9: $K_0 \stackrel{\$}{\leftarrow} \mathcal{K}_{KEM}$	 ▷ Game 0-1 ▷ Game 2-3 ▷ Game 0-2 ▷ Game 3 	1: $(c',t) \leftarrow c$ 2: $\hat{m} = \text{Dec}(sk',c')$ 3: $\hat{k} \leftarrow G(\hat{m})$ 4: if $\text{MAC}(\hat{k},c') = t$ then 5: $K \leftarrow H(\hat{m},c')$ 6: else 7: $K \leftarrow H(z,c')$ 8: end if 9: return K
10: $K_1 \stackrel{\$}{\leftarrow} \mathcal{K}_{\text{KEM}}$ 11: $b \stackrel{\$}{\leftarrow} \{0, 1\}$ 12: $\hat{b} \leftarrow A^{\mathcal{O}^{\text{Decap}}}(\text{pk}, c^*, K_b)$ 13: $\hat{b} \leftarrow A^{\mathcal{O}^{\text{Decap}}}(\text{pk}, c^*, K_b)$ 14: $\mathbf{return} \ [\![\hat{b} = b]\!]$	 ⊳ Game 0 ⊳ Game 1-3 	$\begin{array}{l} \overline{\mathcal{O}_{1}^{Decap}(c)} \\ \hline 1: \ (c',t) \leftarrow c \\ 2: \ \mathbf{if} \ \exists (\tilde{m},\tilde{k}) \in \mathcal{L}^G : \ \tilde{m} = Dec(sk',c') \land \\ MAC(\tilde{k},c') = t \ \mathbf{then} \\ 3: \ K \leftarrow H(\tilde{m},c') \\ 4: \ \mathbf{else} \\ 5: \ K \leftarrow H(z,c') \\ 6: \ \mathbf{end} \ \mathbf{if} \\ 7: \ \mathbf{return} \ K \end{array}$
1: if $\exists (\tilde{m}, \tilde{k}) \in \mathcal{L}^{G} : \tilde{m} = m$ th 2: return \tilde{k} 3: end if 4: $k \stackrel{\$}{\leftarrow} \mathcal{K}_{\texttt{MAC}}$ 5: $\mathcal{L}^{G} \leftarrow \mathcal{L}^{G} \cup \{(m, k)\}$ 6: return k	en	$\begin{array}{c} \overline{\mathcal{O}^{H}(m,c)} \\ 1: \ \mathbf{if} \ \exists (\tilde{m},\tilde{c},\tilde{K}) \in \mathcal{L}^{H} : \tilde{m} = m \wedge \tilde{c} = c \\ \mathbf{then} \\ 2: \ \mathbf{return} \ \tilde{K} \\ 3: \ \mathbf{end} \ \mathbf{if} \\ 4: \ K \overset{\$}{\leftarrow} \mathcal{K}_{\mathtt{KEM}} \\ 5: \ \mathcal{L}^{H} \leftarrow \mathcal{L}^{H} \cup \{(m,c,K)\} \\ 6: \ \mathbf{return} \ K \end{array}$

Figure 7: Sequence of games

oracle model, such k is a uniformly random sample of \mathcal{K}_{MAC} that the adversary does not know, so for A to produce a valid tag is to produce a forgery against the MAC under an unknown and uniformly random key. Furthermore, the security game does not include a signing oracle, so this is a zero-time forgery. While zero-time forgery is not a standard security definition for a MAC, we can bound it by the advantage of a one-time forgery adversary C:

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$$P\left[\mathcal{O}^{\mathtt{Decap}}(c) \neq \mathcal{O}^{\mathtt{Decap}}_1(c)\right] \leq \mathtt{Adv}_{\mathtt{OT-MAC}}(C)$$

Across all q decapsulation queries, the probability that at least one query is a forgery is thus at most $q \cdot P \left[\mathcal{O}^{\mathsf{Decap}}(c) \neq \mathcal{O}^{\mathsf{Decap}}_1(c) \right]$. By the difference lemma:

$$Adv_{G_0}(A) - Adv_{G_1}(A) \le q \cdot Adv_{OT-MAC}(C)$$

Game 2 is identical to game 1, except that the challenger samples a uniformly random MAC key $k^* \stackrel{\$}{\leftarrow} \mathcal{K}_{\texttt{MAC}}$ instead of deriving it from m^* . From A's perspective the two games are indistinguishable, unless A queries G with the value of m^* . Denote the probability that A queries G with m^* by P[QUERY G], then:

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Adv_{G_1}(A) - Adv_{G_2}(A) \leq P[QUERY G]
```

Game 3 is identical to game 2, except that the challenger samples a uniformly random shared secret $K_0 \stackrel{\$}{\leftarrow} \mathcal{K}_{\texttt{KEM}}$ instead of deriving it from m^* and c'. From A's perspective the two games are indistinguishable, unless A queries H with (m^*, \cdot) . Denote the probability that A queries H with (m^*, \cdot) by P[QUERY H], then:

$$\mathrm{Adv}_{G_2}(A)-\mathrm{Adv}_{G_3}(A)\leq P\left[\mathrm{QUERY}\ \mathrm{H}\right]$$

Since in game 3, both K_0 and K_1 are uniformly random and independent of all other variables, no adversary can have any advantage: $Adv_{G_3}(A) = 0$.

```
\mathcal{O}_B^{\mathtt{Decap}}(c)
B(pk, c'^*)
  1: z \overset{\$}{\leftarrow} \mathcal{M}
2: k \overset{\$}{\leftarrow} \mathcal{K}_{\text{MAC}}
                                                                                                       1: (c',t) \leftarrow c
                                                                                                       2: if \exists (\tilde{m}, \tilde{k}) \in \mathcal{L}^G : PCO(c', \tilde{m}) = 1 \land
                                                                                                             MAC(\tilde{k}, c') = t then
  3: t \leftarrow \text{MAC}(k, c'^*)
                                                                                                                     K \leftarrow H(\tilde{m}, c')
                                                                                                       3:
  4: c^* \leftarrow (c'^*, t)
                                                                                                       4: else
  5: K \stackrel{\$}{\leftarrow} \mathcal{K}_{\mathtt{KEM}}
6: \hat{b} \leftarrow A^{\mathcal{O}_{B}^{\mathtt{Decap}}, \mathcal{O}_{B}^{G}, \mathcal{O}_{B}^{H}}(\mathtt{pk}, c^{*}, K)
                                                                                                                     K \leftarrow H(z, c')
                                                                                                       6: end if
  7: if ABORT(m) then
                                                                                                       7: return K
                return m
  9: end if
                                                                                                     \mathcal{O}_B^G(m)
                                                                                                       1: if PCO(m, c'^*) = 1 then
\mathcal{O}_B^H(m,c)
                                                                                                                     ABORT(m)
    if PCO(m, c'^*) = 1 then
                                                                                                       3: end if
            ABORT(m)
                                                                                                       4: if \exists (\tilde{m}, \tilde{k}) \in \mathcal{L}^G : \tilde{m} = m then
                                                                                                                     return k
    if \exists (\tilde{m}, \tilde{c}, \tilde{K}) \in \mathcal{L}^H : \tilde{m} = m \land \tilde{c} = c then
                                                                                                       6: end if
            return \tilde{K}
                                                                                                       7: k \stackrel{\$}{\leftarrow} \mathcal{K}_{\text{MAC}}
    end if
                                                                                                       8: \mathcal{L}^G \leftarrow \mathcal{L}^G \cup \{(m,k)\}
    K \overset{\$}{\leftarrow} \mathcal{K}_{\text{KEM}} \mathcal{L}^H \leftarrow \mathcal{L}^H \cup \{(m, c, K)\}
                                                                                                       9: \mathbf{return} \ k
    \mathbf{return}\ K
```

Figure 8: OW-PCA adversary B simulates game 3 for IND-CCA2 adversary A

We will bound $P[\mathtt{QUERY}\ \mathtt{G}]$ and $P[\mathtt{QUERY}\ \mathtt{H}]$ by constructing a OW-PCA adversary B against the underlying PKE that uses A as a sub-routine. B's behaviors are summarized in figure 8.

B simulates game 3 for A: receiving the public key pk and challenge encryption c'^* , B samples random MAC key and session key to produce the challenge encapsulation, then feeds it to A. When simulating the decapsulation oracle, B uses the plaintext-checking oracle to look for matching queries in \mathcal{L}^G . When simulating the hash oracles, B uses the plaintext-checking oracle to detect when $m^* = \text{Dec}(sk', c'^*)$ has been queried. When m^* is queried, B terminates A and returns m^* to win the OW-PCA game. In other words:

```
P[QUERY G] \le Adv_{OW-PCA}(B)

P[QUERY H] \le Adv_{OW-PCA}(B)
```

Combining all equations above produce the desired security bound.

4 Implementation

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ML-KEM is an IND-CCA2 secure key encapsulation mechanism standardized by NIST in FIPS 203. The IND-CCA2 security of ML-KEM is achieved in two steps. First, ML-KEM constructs an IND-CPA secure public key encryption scheme K-PKE(KeyGen, Enc, Dec) whose security is based on the conjectured intractability of the module learning with error (MLWE) problems against both classical and quantum adversaries. Then, the U_m^{\perp} variant of the Fujisaki-Okamoto transformation [HHK17] is used to construct the KEM MLKEM(KeyGen, Encap, Decap) by calling K-PKE(KeyGen, Enc, Dec) as sub-routines. Because K-PKE.Enc includes substantially more arithmetics than K-PKE.Dec, by using re-encryption and de-randomization, ML-KEM's decapsulation routine incurs significant computational cost.

We implemented the "encrypt-then-MAC" KEM construction using K-PKE as the input PKE and compared its performance against ML-KEM under a variety of scenarios. The experimental data showed that while the "encrypt-then-MAC" construction adds a small amount of computational overhead to the encapsulation routine and a small increase in ciphertext size when compared with ML-KEM, it boasts enormous runtime savings in the decapsulation routine, which makes it particularly suitable for deployment in constrained environment. See appendix 6.1 for comparison with Kyber's third round submission to NIST's PQC competition.

We refer readers to [oST24] for the details of the K-PKE routines. The "encrypt-then-MAC" KEM routines are described in figure 9 below.

```
ML-KEM+.KeyGen()
                                                                            ML-KEM<sup>+</sup>.Decap(sk, c)
                                                                            Require: Secret key sk = (sk'||pk||h||z)
  1: z \stackrel{\$}{\leftarrow} \{0,1\}^{256}
                                                                            Require: Ciphertext c = (c'||t)
  2: (pk, sk') \stackrel{\$}{\leftarrow} K-PKE.KeyGen()
                                                                              1: (sk', pk, h, z) \leftarrow sk
  3: h \leftarrow H(pk)
                                                                              2: (c',t) \leftarrow c
  4: sk \leftarrow (sk'||pk||h||z)
                                                                              3: \hat{m} \leftarrow \text{K-PKE.Dec}(\text{sk}', c')
  5: return (pk, sk)
                                                                                   (\overline{K}, \hat{r}, \hat{k}) \leftarrow \mathtt{XOF}(\hat{m} || h)
                                                                              5: \hat{t} \leftarrow \text{MAC}(\hat{k}, c')
ML-KEM<sup>+</sup>.Encap(pk)
                                                                              6: if \hat{t} = t then
                                                                                        K \leftarrow \mathtt{KDF}(\overline{K}||t)
Require: Public key pk
                                                                              7:
                                                                                  else
                                                                              8:
  1: m \leftarrow \{0,1\}^{256}
                                                                                        K \leftarrow \texttt{KDF}(z||t)
                                                                              9:
  2: (\overline{K}, r, k) \leftarrow \texttt{XOF}(m || H(\texttt{pk}))
                                                                             10: end if
  3: c' \leftarrow \text{K-PKE.Enc}(\text{pk}, m, r)
                                                                             11: return K
  4: t \leftarrow \text{MAC}(k, c')
  5: K \leftarrow \text{KDF}(\overline{K} || c')
  6: c \leftarrow (c', t)
  7: return (c, K)
```

Figure 9: ML-KEM⁺ routines

Our implementation extended from the reference implementation by the PQCrystals team (https://github.com/pq-crystals/kyber). All C code is compiled with GCC 11.4.1 and OpenSSL 3.0.8. All binaries are executed on an AWS c7a.medium instance with an AMD EPYC 9R14 CPU at 3.7 GHz and 1 GB of RAM.

4.1 Choosing a message authenticator

For the ML-KEM⁺ implementation, we instantiated MAC with a selection that covered a wide range of MAC designs, including Poly1305 [Ber05], GMAC [MV04], CMAC [IK03][BR05], and KMAC [Gro13].

Poly1305 and GMAC are both Carter-Wegman style authenticators [WC81] that compute the tag using finite field arithmetic. Generically speaking, Carter-Wegman MAC is parameterized by some finite field \mathbb{F} and the maximal message length L>0. Each symmetric key $k=(k_1,k_2)$ $\stackrel{\$}{\leftarrow} \mathbb{F}^2$ is a pair of uniformly ranodm field elements, and the message is parsed into tuples of field elements up to length L: $m=(m_1,m_2,\ldots,m_l) \in \mathbb{F}^{\leq L}$. The tag t is computed by evaluating a polynomial whose coefficients the message blocks and whose indeterminate is the key:

$$MAC((k_1, k_2), m) = H_{xpoly}(k_1, m) + k_2$$
(1)

Where H_{xpoly} is given by:

$$H_{\text{xpoly}}(k_1, m) = k_1^{l+1} + k_1^l \cdot m_1 + k_1^{l-1} \cdot m_2 + \dots + k_1 \cdot m_l$$

The authenticator formulated in equation 1 is a one-time MAC. To make the construction many-time secure, a non-repeating nonce r and a PRF is needed:

$$\texttt{MAC}((k_1,k_2),m,r) = H_{\texttt{xpoly}}(k_1,m) \oplus \texttt{PRF}(k_2,r)$$

Specifically, Poly1035 operates in the prime field \mathbb{F}_q where $q=2^{130}-5$ whereas GMAC operates in the binary field $\mathbb{F}_{2^{128}}$. In OpenSSL's implementation, standalone Poly1305 is a one-time secure MAC, whereas GMAC uses a nonce and AES as the PRF and is thus many-time secure (in OpenSSL GMAC is AES-256-GCM except all data is fed into the "associated data" section and thus not encrypted).

CMAC is based on the CBC-MAC with the block cipher instantiated from AES-256. To compute a CMAC tag, the message is first broke into 128-bit blocks with appropriate padding. Each block is first XOR'd with the previous block's output, then encrypted under AES using the symmetric key. The final output is XOR'd with a sub key derived from the symmetric key, before being encrypted for one last time.

KMAC is defined in [Gro13] to be based on the family of sponge functions with Keccak permutaiton as the underlying function. We chose KMAC-256, which uses Shake256 as the underlying extendable output functions. KMAC allows variable-length key and tag, but we chose the 256 bits for key length and 128 bits for tag size for consistency with other authenticators.

To isolate the performance characteristics of each authenticator in our instantiation of ML-KEM⁺, we measured the CPU cycles needed for each authenticator to compute a tag on random inputs whose sizes correspond to the ciphertext sizes of ML-KEM. The measurements are summarized in table 3.

From our testing, we found Poly1305 to exhibit the best performance characteristics. However, there are additional security considerations that may require the use of other less efficient MAC instances. For example, it is possible for an adversary with large computing infrastructure or quantum computers to pre-compute a large lookup table mapping symmetric key to the source plaintext. Upon receiving a ciphertext, the adversary can then search through the lookup table for a matching key, which would've revealed the corresponding decryption. We partially mitigated such attack by deriving the symmetric key from both the public key and the plaintext, but in case of a long-term keypair, the adversary might still be able to compute a large lookup table AFTER obtaining the long-term public key. Further mitigation could include using larger-size keys, which can be accomplished either by using a Carter-Wegman MAC that operates on a larger finite field or using a MAC with a variable key-length such as KMAC.

	rable of the cycles include to compare tag on various input sizes							
Input size: 768 bytes			Input size: 1088 bytes			Input size: 1568 bytes		
MAC	Median	Average	MAC	Median	Average	MAC	Median	Average
Poly1305	909	2823	Poly1305	961	2704	Poly1305	1065	1809
GMAC	3899	4859	GMAC	3899	4827	GMAC	4055	5026
CMAC	6291	6373	CMAC	7305	7588	CMAC	8735	8772
KMAC	6373	7791	KMAC	9697	9928	KMAC	11647	12186

Table 3: CPU cycles needed to compute tag on various input sizes

4.2 KEM performance

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Compared to the $U_m^{\not\perp}$ variant of Fujisaki-Okamoto transformed used in ML-KEM, the "encrypt-then-MAC" transformation the following trade-off when given the same input sub-routines:

- 1. Both encapsulation and decap sulation add a small amount of overhead for needing to hash both the PKE plain text and the PKE ciphertext when deriving the shared secret, where as the $U_m^{\not\perp}$ transformation only needs to hash the PKE plain text.
- 2. The encapsulation routine adds a small amount of run-time overhead for computing the authenticator
- 3. The decapsulation routine enjoys substantial runtime speedup because *re-encryption* is replaced with computing an authenticator
- 4. Ciphertext size increases by the size of an authenticator

Since K-PKE.Enc carries significantly more computational complexity than K-PKE.Dec or any MAC we chose, the performance advantage of the "encrypt-then-MAC" transformation over the $U_m^{\not\perp}$ transformation is dominated by the runtime saving gained from replacing re-encryption with MAC. A comparison between ML-KEM and variations of the ML-KEM⁺ can be found in table 4

Table 4: CPU cycles of each KEM routine

Table 4. Of C cycles of each KEM fourthe						
128-bit security	KEM variant	Encap cycles/tick		Decap cycles/tick		
size parameters (bytes)	KEW Variant	Median	Average	Median	Average	
pk size 800	ML-KEM-512	91467	92065	121185	121650	
sk size 1632	Kyber512	97811	98090	119937	120299	
ct size 768	ML-KEM ⁺ -512 w/ Poly1305	93157	93626	33733	33908	
KeyGen cycles/tick	ML-KEM ⁺ -512 w/ GMAC	97369	97766	37725	37831	
Median 75945	ML-KEM ⁺ -512 w/ CMAC	99739	99959	40117	39943	
Average 76171	ML-KEM ⁺ -512 w/ KMAC	101009	101313	40741	40916	

192-bit security size parameters (bytes)		KEM variant	Encap cycles/tick		Decap cycles/tick	
		KEW Variant	Median	Average	Median	Average
pk size	1184	ML-KEM-768	136405	147400	186445	187529
sk size	2400	Kyber768	153061	153670	182129	182755
ct size	1088	ML-KEM ⁺ -768 w/ Poly1305	146405	146860	43315	43463
KeyGen cycles/tick		ML-KEM ⁺ -768 w/ GMAC	149525	150128	46513	46706
Median	129895	ML-KEM ⁺ -768 w/ CMAC	153139	153735	49841	50074
Average	130650	ML-KEM ⁺ -768 w/ KMAC	155219	155848	52415	52611

256-bit security		KEM variant	Encap cy	cles/tick	Decap cycles/tick	
size parameters (bytes)		KEW Variant	Median	Average	Median	Average
pk size	1568	ML-KEM-1024	199185	199903	246245	247320
sk size	3168	Kyber1024	222351	223260	258231	259067
ct size	1568	ML-KEM ⁺ -1024 w/ Poly1305	205763	206499	51375	51562
1 *	cycles/tick	ML-KEM ⁺ -1024 w/ GMAC	208805	209681	54573	54780
Median	194921	ML-KEM ⁺ -1024 w/ CMAC	213667	214483	59175	59408
Average	195465	ML-KEM ⁺ -1024 w/ KMAC	216761	217468	62269	62516

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4.3 Key exchange protocols

A common application of key encapsulation mechanism is key exchange protocols, where two parties establish a shared secret using a public channel. [BDK+18] described three key exchange protocols: unauthenticated key exchange (KE), unilaterally authenticated key exchange (UAKE), and mutually authenticated key exchange (AKE). We instantiated an implementation for each of the three key exchange protocols using different variations of the "encrypt-then-MAC" KEM and compared round trip time with implementations instantiated using ML-KEM.

For clarity, we denote the party who sends the first message to be the client and the other party to be the server. Round trip time (RTT) is defined to be the time interval between the moment before the client starts generating ephemeral keypairs and the moment after the client derives the final session key. All experiements are run on a pair of AWS c7a.medium instances both located in the us-west-2 region. For each experiment, a total of 10,000 rounds of key exchange are performed, with the median and average round trip time (measured in microsecond) recorded.

4.3.1 Unauthenticated key exchange (KE)

In unauthenticated key exchange, a single pair of ephemeral keypair $(pk_e, sk_e) \stackrel{\$}{\leftarrow} KeyGen()$ is generated by the client. The client transmits the ephemeral public key pk_e to the server, who runs the encapsulation routine $(c_e, K_e) \stackrel{\$}{\leftarrow} Encap(pk_e)$ and transmits the ciphertext c_e back to the client. The client finally decapsulates the ciphertext to recover the shared secret $K_e \leftarrow Decap(sk_e, c_e)$. The key exchange routines are summarized in figure 10.

Note that in our implementation, a key derivation function (KDF) is applied to the ephemeral shared secret to derive the final session key. This step is added to maintain consistency with other authenticated key exchange protocols, where the final session key is derived from multiple shared secrets. The key derivation function is instantiated using Shake256, and the final session key is 256 bits in length.

```
\begin{array}{c|c} \hline {\sf KE_C()} \\ \hline \\ 1: \ ({\sf pk}_e, {\sf sk}_e) \overset{\$}{\leftarrow} {\sf KeyGen()} \\ 2: \ {\sf send(pk}_e) \\ 3: \ c_e \leftarrow {\sf read()} \\ 4: \ K_e \leftarrow {\sf Decap(sk}_e, c_e) \\ 5: \ K \leftarrow {\sf KDF}(K) \\ 6: \ {\sf return} \ K \\ \hline \end{array} \begin{array}{c} \hline {\sf KE_S()} \\ \hline \\ 1: \ {\sf pk}_e \leftarrow {\sf read()} \\ 2: \ (c_e, K_e) \overset{\$}{\leftarrow} {\sf Encap(pk}_e) \\ 3: \ {\sf send(c_e)} \\ 4: \ K \leftarrow {\sf KDF}(K_e) \\ 5: \ {\sf return} \ K \\ \hline \end{array}
```

Figure 10: Unauthenticated key exchange (KE) routines

RTT time (μs) KEM variant Client TX bytes Server TX bytes $\overline{\text{Median}}$ Average ML-KEM-512 ML-KEM-512⁺ w/ Poly1305 ML-KEM-512⁺ w/ GMAC $ML-KEM-512^+$ w/ CMAC ML-KEM-512⁺ w/ KMAC

Table 5: KE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT time (μs)		
KEWI Variant	Cheff IX bytes	Derver 1A bytes	Median	Average	
ML-KEM-768	1184	1088	135	140	
ML-KEM-768 ⁺ w/ Poly1305	1184	1104	99	104	
ML-KEM-768 ⁺ w/ GMAC	1184	1104	101	105	
ML-KEM-768 ⁺ w/ CMAC	1184	1104	103	109	
ML-KEM-768 ⁺ w/ KMAC	1184	1104	103	107	

KEM variant	Client TX bytes	Server TX bytes	RTT time (μs)		
KEW Variant	Cheff 1A bytes	Derver 1A bytes	Median	Average	
ML-KEM-1024	1568	1568	193	199	
ML-KEM-1024 ⁺ w/ Poly1305	1568	1584	138	141	
ML -KEM-1024 $^+$ w/ $GMAC$	1568	1584	140	145	
ML-KEM-1024 ⁺ w/ CMAC	1568	1584	143	148	
ML-KEM-1024 ⁺ w/ KMAC	1568	1584	144	149	

4.3.2 Unilaterally authenticated key exchange (UAKE)

In unilaterally authenticated key exchange, the authenticating party proves its identity to the other party by demonstrating possession of a secret key that corresponds to a published long-term public key. In this implementation, the client possesses the long-term public key pk_S of the server, and the server authenticates itself by demonstrating possession of the corresponding long-term secret key sk_S . UAKE routines are summarized in figure 11.

In addition to the long-term key, the client will also generate an ephemeral keypair as it does in an unauthenticated key exchange, and the session key is derived by applying the KDF to the concatenation of both the ephemeral shared secret and the shared secret encapsulated under server's long-term key. This helps the key exchange to achieve weak forward secrecy (citation needed).

Using KEM for authentication is especially interesting within the context of post-quantum cryptography: post-quantum KEM schemes usually enjoy better performance characteristics than post-quantum signature schemes with faster runtime, smaller memory footprint, and smaller communication sizes. KEMTLS was proposed in 2020 as an alternative to existing TLS handshake protocols, and many experimental implementations have demonstrated the performance advantage. (citation needed).

$\overline{\mathtt{UAKE}_\mathtt{C}(\mathtt{pk}_S)}$	<u>—</u>
Require: Server's long-term pk_S	$\overline{{ t UAKE_S(sk_S)}}$
$1: \ (\mathtt{pk}_e, \mathtt{sk}_e) \overset{\$}{\leftarrow} \mathtt{KeyGen}()$	Require: Server's long-term sk_S
$2: (c_S, K_S) \stackrel{\$}{\leftarrow} \mathtt{Encap}(\mathtt{pk}_S)$	1: $(\mathtt{pk}_e, c_S) \leftarrow \mathtt{read}()$
$3: \mathtt{send}(\mathtt{pk}_e, c_S)$	2: $K_S \leftarrow exttt{Decap}(exttt{sk}_S, c_S)$
$c_e \leftarrow \mathtt{read}()$	$\text{3: } (c_e, K_e) \xleftarrow{\$} \mathtt{Encap}(\mathtt{pk}_e)$
5: $K_e \leftarrow \mathtt{Decap}(\mathtt{sk}_e, c_e)$	4: $\mathtt{send}(c_e)$
6: $K \leftarrow \texttt{KDF}(K_e K_S)$	5: $K \leftarrow \mathtt{KDF}(K_e \ K_S)$
7: $\mathbf{return}\ K$	6: $\mathbf{return}\ K$

Figure 11: Unilaterally authenticated key exchange (UAKE) routines

Table 6: UAKE RTT comparison

KEM variant	Client TX bytes	Server TX bytes	RTT time (μs)		
TYPINI Variant	Cheff 1A bytes	Derver 1 A bytes	Median	Average	
ML-KEM-512	1568	768	145	151	
ML-KEM-512 ⁺ w/ Poly1305	1584	784	103	106	
ML-KEM-512 ⁺ w/ GMAC	1584	784	106	110	
ML-KEM-512 ⁺ w/ CMAC	1584	784	108	112	
ML-KEM-512 ⁺ w/ KMAC	1584	784	109	113	

KEM variant	Client TX bytes	Server TX bytes	RTT time (μs)		
KEW Variant	Cheff 1A bytes	Server 1 A bytes	Median	Average	
ML-KEM-768	2272	1088	215	222	
ML-KEM-768 ⁺ w/ Poly1305	2288	1104	144	150	
ML-KEM-768 ⁺ w/ GMAC	2288	1104	149	156	
ML-KEM-768 ⁺ w/ CMAC	2288	1104	153	160	
ML-KEM-768 ⁺ w/ KMAC	2288	1104	154	159	

KEM variant	Client TX bytes	Server TX bytes	RTT time (μs)	
			Median	Average
ML-KEM-1024	3136	1568	310	318
ML-KEM-1024 ⁺ w/ Poly1305	3152	1584	202	209
ML-KEM-1024 ⁺ w/ GMAC	3152	1584	212	228
ML-KEM-1024 ⁺ w/ CMAC	3152	1584	212	218
ML-KEM-1024 ⁺ w/ KMAC	3152	1584	213	220

4.3.3 Mutually authenticated key exchange (AKE)

Mutually authenticated key exchange is largely identical to unilaterally authenticated key exchange, except for that client authentication is required. This means that client possesses server's long-term public key and its own long-term secret key, while the server possesses client's long-term public key and its own long-term secret key. The session key is derived by applying KDF onto the concatenation of shared secrets produced under the ephemeral keypair, server's long-term keypair, and client's long-term keypair, in this order.

$\overline{\mathtt{AKE}_\mathtt{C}(\mathtt{pk}_S,\mathtt{sk}_C)}$	
	$= = \frac{1}{AKE_S(sk_S, pk_C)}$
Require: Server's long-term pk_S	
Require: Client's long-term \mathfrak{sk}_C	Require: Server's long-term sk_S
$1: \ (\mathtt{pk}_e, \mathtt{sk}_e) \xleftarrow{\$} \mathtt{KeyGen}()$	Require: Client's long-term pk_C
$2: (c_S, K_S) \stackrel{\$}{\leftarrow} \texttt{Encap}(\texttt{pk}_S)$	$1: \ (\mathtt{pk}_e, c_S) \leftarrow \mathtt{read}()$
	2: $K_S \leftarrow exttt{Decap}(exttt{sk}_S, c_S)$
$3: \mathtt{send}(\mathtt{pk}_e, c_S)$	$3: (c_e, K_e) \stackrel{\$}{\leftarrow} \mathtt{Encap}(\mathtt{pk}_e)$
$4: (c_e, c_C) \leftarrow \mathtt{read}()$	- 12 6/
5: $K_e \leftarrow \mathtt{Decap}(\mathtt{sk}_e, c_e)$	$4 \colon \left(c_C, K_C \right) \overset{\$}{\leftarrow} \texttt{Encap}(\texttt{pk}_C)$
6: $K_C \leftarrow \mathtt{Decap}(\mathtt{sk}_e, c_C)$	5: $\mathtt{send}(c_e, c_C)$
7: $K \leftarrow \texttt{KDF}(K_e K_S K_C)$	6: $K \leftarrow \texttt{KDF}(K_e K_S K_C)$
8: $\mathbf{return}\ K$	7: return K

Figure 12: Mutually authenticated key exchange (AKE) routines

KEM variant	Client TX bytes S	Server TX bytes	RTT time (μs)	
			Median	Average
ML-KEM-512	1568	1536	220	213
ML-KEM-512 ⁺ w/ Poly1305	1584	1568	133	138
ML-KEM-512 ⁺ w/ GMAC	1584	1568	139	143
MI -KEM-512+ w/ CMAC	1584	1568	143	1/18

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Table 7: AKE RTT comparison

KEM variant	Client TX bytes Server TX bytes	Correr TV bytes	RTT time (μs)	
		Median	Average	
ML-KEM-768	2272	2176	294	301
ML-KEM-768 ⁺ w/ Poly1305	2288	2208	190	196
ML-KEM-768 ⁺ w/ GMAC	2288	2208	197	210
ML-KEM-768 ⁺ w/ CMAC	2288	2208	202	208
ML-KEM-768 ⁺ w/ KMAC	2288	2208	204	210

KEM variant	Client TV bytes	ient TX bytes Server TX bytes	RTT time (μs)	
	Cheft 1A bytes		Median	Average
ML-KEM-1024	3136	3136	512	511
ML-KEM-1024 ⁺ w/ Poly1305	3152	3168	266	273
ML -KEM-1024 $^+$ w/ $GMAC$	3152	3168	273	282
ML-KEM-1024 ⁺ w/ CMAC	3152	3168	280	287
ML-KEM-1024 ⁺ w/ KMAC	3152	3168	282	288

5 Conclusions and future works

w/ KMAC

ML-KEM-512⁺

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The "encrypt-then-MAC" transformation is a generic KEM construction that achieves IND-CCA2 security under the random oracle model if the input PKE is OW-PCA secure. Compared to the Fujisaki-Okamoto transformation, our construction replaced de-randomization and re-encryption with a message authenticator. At the cost of some minimal increase in communication size and encapsulation runtime, our construction achieves significant efficiency gains in the decapsulation routine. In practical key exchange protocols, our construction saves between 35-45% in round trip time.

Other suitable post-quantum instantiation. In section 4, we instantiated the "encrypt-then-MAC" KEM transformation with the PKE subroutines of ML-KEM. Unfortunately, ML-KEM is vulnerable to plaintext checking attacks that can recover complete

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secret key if the keypair is reused [BDH⁺19]. In fact, as Chris Peikert pointed out, because
of the search-decision equivalence of LWE problems, almost all LWE-based cryptosystems
will be vulerable to plaintext-checking attacks [Pei14]. This naturally raises the question
of finding other post-quantum primitives to instantiate "encrypt-then-MAC" with, such
as other lattice-based cryptosystems not based on LWE, code-based cryptosystems and
isogeny-based cryptosystems.

References

- [ABC⁺20] Martin R. Albrecht, Daniel J. Bernstein, Tung Chou, Carlos Cid, Jan Gilcher,
 Tanja Lange, Varun Maram, Ingo von Maurich, Rafael Misoczki, RubenNiederhagen, Kenneth G. Paterson, Edoardo Persichetti, Christiane Peters, Peter
 Schwabe, Nicolas Sendrier, Jakub Szefer, Cen Jung Tjhai, Martin Tomlinson,
 and Wen Wang. Classic mceliece. Technical report, National Institute of
 Standards and Technology, 2020.
- [ABD+19] Roberto Avanzi, Joppe Bos, Léo Ducas, Eike Kiltz, Tancrède Lepoint, Vadim
 Lyubashevsky, John M Schanck, Peter Schwabe, Gregor Seiler, and Damien
 Stehlé. Crystals-kyber algorithm specifications and supporting documentation.
 NIST PQC Round, 2(4):1-43, 2019.
- [ABR01] Michel Abdalla, Mihir Bellare, and Phillip Rogaway. The oracle diffie-hellman assumptions and an analysis of DHIES. In David Naccache, editor, Topics in Cryptology CT-RSA 2001, The Cryptographer's Track at RSA Conference 2001, San Francisco, CA, USA, April 8-12, 2001, Proceedings, volume 2020 of Lecture Notes in Computer Science, pages 143-158. Springer, 2001.
- [BCD⁺16] Joppe W. Bos, Craig Costello, Léo Ducas, Ilya Mironov, Michael Naehrig,
 Valeria Nikolaenko, Ananth Raghunathan, and Douglas Stebila. Frodo: Take
 off the ring! practical, quantum-secure key exchange from LWE. In Edgar R.
 Weippl, Stefan Katzenbeisser, Christopher Kruegel, Andrew C. Myers, and
 Shai Halevi, editors, Proceedings of the 2016 ACM SIGSAC Conference on
 Computer and Communications Security, Vienna, Austria, October 24-28, 2016,
 pages 1006–1018. ACM, 2016.
- [BDH⁺19] Ciprian Baetu, F. Betül Durak, Loïs Huguenin-Dumittan, Abdullah Talayhan, and Serge Vaudenay. Misuse attacks on post-quantum cryptosystems. In Yuval Ishai and Vincent Rijmen, editors, Advances in Cryptology - EUROCRYPT 2019 - 38th Annual International Conference on the Theory and Applications of Cryptographic Techniques, Darmstadt, Germany, May 19-23, 2019, Proceedings, Part II, volume 11477 of Lecture Notes in Computer Science, pages 747–776. Springer, 2019.
 - [BDK⁺18] Joppe W. Bos, Léo Ducas, Eike Kiltz, Tancrède Lepoint, Vadim Lyubashevsky, John M. Schanck, Peter Schwabe, Gregor Seiler, and Damien Stehlé. CRYS-TALS kyber: A cca-secure module-lattice-based KEM. In 2018 IEEE European Symposium on Security and Privacy, EuroS&P 2018, London, United Kingdom, April 24-26, 2018, pages 353–367. IEEE, 2018.
- Daniel J. Bernstein. The poly1305-aes message-authentication code. In Henri Gilbert and Helena Handschuh, editors, Fast Software Encryption: 12th International Workshop, FSE 2005, Paris, France, February 21-23, 2005, Revised Selected Papers, volume 3557 of Lecture Notes in Computer Science, pages 32-49. Springer, 2005.

515

516

517

- Daniel J. Bernstein and Edoardo Persichetti. Towards KEM unification. *IACR Cryptol. ePrint Arch.*, page 526, 2018.
- Mihir Bellare and Phillip Rogaway. Optimal asymmetric encryption. In Alfredo De Santis, editor, Advances in Cryptology EUROCRYPT '94, Workshop on the Theory and Application of Cryptographic Techniques, Perugia, Italy,
 May 9-12, 1994, Proceedings, volume 950 of Lecture Notes in Computer Science,
 pages 92–111. Springer, 1994.
- Mihir Bellare and Phillip Rogaway. Minimizing the use of random oracles in authenticated encryption schemes. In Yongfei Han, Tatsuaki Okamoto, and Sihan Qing, editors, Information and Communication Security, First International Conference, ICICS'97, Beijing, China, November 11-14, 1997, Proceedings, volume 1334 of Lecture Notes in Computer Science, pages 1–16.

 Springer, 1997.
- John Black and Phillip Rogaway. CBC macs for arbitrary-length messages: The three-key constructions. *J. Cryptol.*, 18(2):111–131, 2005.
 - [CHJ⁺02] Jean-Sébastien Coron, Helena Handschuh, Marc Joye, Pascal Paillier, David Pointcheval, and Christophe Tymen. GEM: A generic chosen-ciphertext secure encryption method. In Bart Preneel, editor, Topics in Cryptology CT-RSA 2002, The Cryptographer's Track at the RSA Conference, 2002, San Jose, CA, USA, February 18-22, 2002, Proceedings, volume 2271 of Lecture Notes in Computer Science, pages 263–276. Springer, 2002.
- [CK01] Ran Canetti and Hugo Krawczyk. Analysis of key-exchange protocols and their use for building secure channels. In Birgit Pfitzmann, editor, Advances in Cryptology EUROCRYPT 2001, International Conference on the Theory and Application of Cryptographic Techniques, Innsbruck, Austria, May 6-10, 2001, Proceeding, volume 2045 of Lecture Notes in Computer Science, pages 453–474. Springer, 2001.
- [Den03] Alexander W. Dent. A designer's guide to kems. In Kenneth G. Paterson, editor,

 Cryptography and Coding, 9th IMA International Conference, Cirencester, UK,

 December 16-18, 2003, Proceedings, volume 2898 of Lecture Notes in Computer

 Science, pages 133-151. Springer, 2003.
- [DKRV18] Jan-Pieter D'Anvers, Angshuman Karmakar, Sujoy Sinha Roy, and Frederik
 Vercauteren. Saber: Module-lwr based key exchange, cpa-secure encryption
 and cca-secure KEM. In Antoine Joux, Abderrahmane Nitaj, and Tajjeeddine
 Rachidi, editors, Progress in Cryptology AFRICACRYPT 2018 10th International Conference on Cryptology in Africa, Marrakesh, Morocco, May 7-9,
 2018, Proceedings, volume 10831 of Lecture Notes in Computer Science, pages
 282–305. Springer, 2018.
- [DNR04] Cynthia Dwork, Moni Naor, and Omer Reingold. Immunizing encryption schemes from decryption errors. In Christian Cachin and Jan Camenisch, editors, Advances in Cryptology EUROCRYPT 2004, International Conference on the Theory and Applications of Cryptographic Techniques, Interlaken, Switzerland, May 2-6, 2004, Proceedings, volume 3027 of Lecture Notes in Computer Science, pages 342–360. Springer, 2004.
- [FO99] Eiichiro Fujisaki and Tatsuaki Okamoto. Secure integration of asymmetric and symmetric encryption schemes. In Michael J. Wiener, editor, Advances in Cryptology CRYPTO '99, 19th Annual International Cryptology Conference,

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583

- Santa Barbara, California, USA, August 15-19, 1999, Proceedings, volume 1666 of Lecture Notes in Computer Science, pages 537–554. Springer, 1999.
- ⁵⁴⁶ [FO13] Eiichiro Fujisaki and Tatsuaki Okamoto. Secure integration of asymmetric and symmetric encryption schemes. *J. Cryptol.*, 26(1):80–101, 2013.
- [FOPS01] Eiichiro Fujisaki, Tatsuaki Okamoto, David Pointcheval, and Jacques Stern.

 RSA-OAEP is secure under the RSA assumption. In Joe Kilian, editor, Advances in Cryptology CRYPTO 2001, 21st Annual International Cryptology
 Conference, Santa Barbara, California, USA, August 19-23, 2001, Proceedings,
 volume 2139 of Lecture Notes in Computer Science, pages 260–274. Springer,
 2001.
 - [Gam85] Taher El Gamal. A public key cryptosystem and a signature scheme based on discrete logarithms. *IEEE Trans. Inf. Theory*, 31(4):469–472, 1985.
 - [Gro13] Joint Task Force Transformation Initiative Interagency Working Group. Security and privacy controls for federal information systems and organizations. Technical Report NIST Special Publication (SP) 800-53, Rev. 4, Includes updates as of January 22, 2015, National Institute of Standards and Technology, Gaithersburg, MD, 2013.
- [HHK17] Dennis Hofheinz, Kathrin Hövelmanns, and Eike Kiltz. A modular analysis of the fujisaki-okamoto transformation. In Yael Kalai and Leonid Reyzin, editors,
 Theory of Cryptography 15th International Conference, TCC 2017, Baltimore,
 MD, USA, November 12-15, 2017, Proceedings, Part I, volume 10677 of Lecture
 Notes in Computer Science, pages 341–371. Springer, 2017.
- Kathrin Hövelmanns, Andreas Hülsing, and Christian Majenz. Failing gracefully: Decryption failures and the fujisaki-okamoto transform. In Shweta
 Agrawal and Dongdai Lin, editors, Advances in Cryptology ASIACRYPT
 2022 28th International Conference on the Theory and Application of Cryptology and Information Security, Taipei, Taiwan, December 5-9, 2022, Proceedings,
 Part IV, volume 13794 of Lecture Notes in Computer Science, pages 414–443.
 Springer, 2022.
 - [IK03] Tetsu Iwata and Kaoru Kurosawa. OMAC: one-key CBC MAC. In Thomas Johansson, editor, Fast Software Encryption, 10th International Workshop, FSE 2003, Lund, Sweden, February 24-26, 2003, Revised Papers, volume 2887 of Lecture Notes in Computer Science, pages 129–153. Springer, 2003.
- Kra01] Hugo Krawczyk. The order of encryption and authentication for protecting communications (or: How secure is ssl?). In Joe Kilian, editor, Advances in Cryptology CRYPTO 2001, 21st Annual International Cryptology Conference, Santa Barbara, California, USA, August 19-23, 2001, Proceedings, volume 2139 of Lecture Notes in Computer Science, pages 310-331. Springer, 2001.
 - [MKJR16] Kathleen Moriarty, Burt Kaliski, Jakob Jonsson, and Andreas Rusch. PKCS#1: RSA Cryptography Specifications Version 2.2. RFC 8017, November 2016.
- David A. McGrew and John Viega. The security and performance of the galois/counter mode (GCM) of operation. In Anne Canteaut and Kapalee Viswanathan, editors, Progress in Cryptology INDOCRYPT 2004, 5th International Conference on Cryptology in India, Chennai, India, December 20-22, 2004, Proceedings, volume 3348 of Lecture Notes in Computer Science, pages 343–355. Springer, 2004.

- Tatsuaki Okamoto and David Pointcheval. The gap-problems: A new class of problems for the security of cryptographic schemes. In Kwangjo Kim, editor,

 Public Key Cryptography, 4th International Workshop on Practice and Theory
 in Public Key Cryptography, PKC 2001, Cheju Island, Korea, February 13-15,
 2001, Proceedings, volume 1992 of Lecture Notes in Computer Science, pages
 104–118. Springer, 2001.
- Tatsuaki Okamoto and David Pointcheval. REACT: rapid enhanced-security asymmetric cryptosystem transform. In David Naccache, editor, Topics in Cryptology CT-RSA 2001, The Cryptographer's Track at RSA Conference 2001, San Francisco, CA, USA, April 8-12, 2001, Proceedings, volume 2020 of Lecture Notes in Computer Science, pages 159–175. Springer, 2001.
- [oST24] National Institute of Standards and Technology. Module-lattice-based keyencapsulation mechanism standard. Technical Report Federal Information Processing Standards Publication (FIPS) NIST FIPS 203, U.S. Department of Commerce, Washington, D.C., 2024.
- Chris Peikert. Lattice cryptography for the internet. In Michele Mosca, editor,

 Post-Quantum Cryptography 6th International Workshop, PQCrypto 2014,

 Waterloo, ON, Canada, October 1-3, 2014. Proceedings, volume 8772 of Lecture

 Notes in Computer Science, pages 197–219. Springer, 2014.
- [RRCB19] Prasanna Ravi, Sujoy Sinha Roy, Anupam Chattopadhyay, and Shivam Bhasin.

 Generic side-channel attacks on cca-secure lattice-based PKE and KEM schemes.

 IACR Cryptol. ePrint Arch., page 948, 2019.
- Ronald L. Rivest, Adi Shamir, and Leonard M. Adleman. A method for obtaining digital signatures and public-key cryptosystems. *Commun. ACM*, 21(2):120–126, 1978.
- [Sho04] Victor Shoup. Sequences of games: a tool for taming complexity in security proofs. IACR Cryptol. ePrint Arch., page 332, 2004.
- [UXT⁺22] Rei Ueno, Keita Xagawa, Yutaro Tanaka, Akira Ito, Junko Takahashi, and
 Naofumi Homma. Curse of re-encryption: A generic power/em analysis on postquantum kems. IACR Trans. Cryptogr. Hardw. Embed. Syst., 2022(1):296–322,
 2022.
- [WC81] Mark N. Wegman and Larry Carter. New hash functions and their use in authentication and set equality. *J. Comput. Syst. Sci.*, 22(3):265–279, 1981.

6 Appendix

$_{\scriptscriptstyle 44}$ 6.1 Performance comparison between <code>ML-KEM+</code> and <code>Kyber</code>

ML-KEM directly evolved from CRYSTALS-Kyber's third round submission to NIST's post quantum cryptography competition. While their IND-CPA subroutines (see figure 13) are identical, ML-KEM deviated from Kyber by choosing a different variant of the Fujisaki-Okamoto transformation.

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K-PKE.KeyGen()	K-PKE.Enc(pk, m)	K-PKE.Dec(sk, c)
1: $A \stackrel{\$}{\leftarrow} R_q^{k \times k}$ 2: $\mathbf{s} \stackrel{\$}{\leftarrow} \mathcal{X}_{\eta_1}^k$ 3: $\mathbf{e} \stackrel{\$}{\leftarrow} \mathcal{X}_{\eta_1}^k$ 4: $\mathbf{t} \leftarrow A\mathbf{s} + \mathbf{e}$ 5: $\mathbf{pk} \leftarrow (A, \mathbf{t})$	Ensure: $pk = (A, \mathbf{t})$ Ensure: $m \in R_2$ 1: $\mathbf{r} \stackrel{\$}{\leftarrow} \mathcal{X}_{\eta_1}^k$ 2: $\mathbf{e}_1 \stackrel{\$}{\leftarrow} \mathcal{X}_{\eta_2}^k$ 3: $e_2 \stackrel{\$}{\leftarrow} \mathcal{X}_{\eta_2}$	Ensure: $c = (\mathbf{c}_1, c_2)$ Ensure: $\mathbf{sk} = \mathbf{s}$ 1: $\hat{m} \leftarrow c_2 - \mathbf{c}_1^{T} \cdot \mathbf{s}$ 2: $\hat{m} \leftarrow Round(\hat{m})$ 3: $\mathbf{return} \ \hat{m}$
6: $sk \leftarrow s$ 7: $return (pk, sk)$	4: $\mathbf{c}_1 \leftarrow A\mathbf{r} + \mathbf{e}_1$ 5: $c_2 \leftarrow \mathbf{t}^{\intercal}\mathbf{r} + e_2 + m \cdot \lfloor \frac{q}{2} \rceil$ 6: $\mathbf{return} \ (\mathbf{c}_1, c_2)$	_

Figure 13: K-PKE routines are identical between Kyber and ML-KEM

CRYSTALS-Kyber uses the $U^{\not\perp}$ variant, where the shared secret is derived from both the plaintext and the ciphertext. On the other hand, because by using *re-encryption* and *de-randomization*, the PKE is already made *rigid*, the CRYSTALS-Kyber team decided to use the $U_m^{\not\perp}$ variant, where the shared secret is derived from the plaintext alone.

KEM.KeyGen()		KEM.Decap(sk, c)	
1: $z \stackrel{\$}{\leftarrow} \{0,1\}^{256}$ 2: $(\mathtt{pk},\mathtt{sk}') \stackrel{\$}{\leftarrow} \mathtt{PKE.KeyGen}()$ 3: $\mathtt{sk} \leftarrow (\mathtt{sk}' \ \mathtt{pk} \ H(\mathtt{pk}) \ z)$ 4: $\mathtt{return} \ (\mathtt{pk},\mathtt{sk})$		Ensure: $\mathtt{sk} = (\mathtt{sk'} \ \mathtt{pk} \ H(\mathtt{pk}) \ z)$ 1: $\hat{m} \leftarrow \mathtt{PKE.Dec}(\mathtt{sk'}, c)$ 2: $(\overline{K}, \hat{r}) \leftarrow G(\hat{m} \ H(\mathtt{pk}))$ 3: if $\mathtt{PKE.Enc}(\mathtt{pk}, \hat{m}, \hat{r}) = c$ then 4: $K \leftarrow \mathtt{KDF}(\overline{K}, H(c))$ 5: $K \leftarrow \overline{K}$ 6: else	$\triangleright U^{\cancel{\perp}}$ $\triangleright U_m^{\cancel{\perp}}$
KEM. Encap(pk) 1: $m \stackrel{\$}{\leftarrow} \{0, 1\}^{256}$		7: $K \leftarrow \mathtt{KDF}(z \ H(c))$ 8: end if 9: return K	
2: $(\overline{K}, r) \leftarrow G(m H(\texttt{pk}))$ 3: $c \leftarrow \texttt{PKE.Enc}(\texttt{pk}, m, r)$ 4: $K \leftarrow \texttt{KDF}(\overline{K} H(c))$ 5: $K \leftarrow \overline{K}$ 6: $\mathbf{return}(c, K)$	$\triangleright U^{\cancel{\bot}}$ $\triangleright U_m^{\cancel{\bot}}$		

Figure 14: Kyber uses $U^{\not\perp}$ variant. ML-KEM uses $U_m^{\not\perp}$ variant.

The reason for ML-KEM to use a different variant of the Fujisaki-Okamoto transformation is two-fold. The first reason is performance: using the U_m^{χ} transformation saves the need to hash the ciphertext, and since Kyber/ML-KEM's performance is mainly bottlenecked by the symmetric components, omitting the hash leads to significant runtime savings (up to 17% in AVX-2 optimized implementations). The second reason is the simplified security proof and tighter security bounds of the U_m^{χ} variant compared to the U_m^{χ} variant. We will omit the details of the security proof and refer readers to [HHK17].

In section 4, we mainly compared $\mathtt{ML}\text{-}\mathtt{KEM}^+$ with $\mathtt{ML}\text{-}\mathtt{KEM}$, but the we would like to point out that, because Kyber uses the $U^{\not\perp}$ variant and needs to hash the ciphertext for deriving the shared secret, the performance advantage of $\mathtt{ML}\text{-}\mathtt{KEM}^+$ over Kyber will be even greater.