# imputeR Documentation

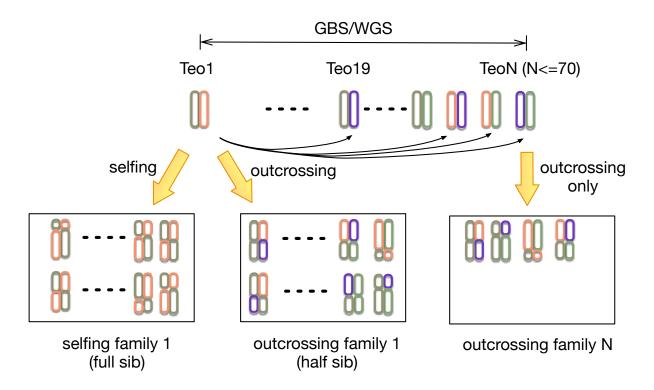
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### 1 Introduction

#### 1.1 Crossing Scheme and Experimental Design



In this experiment, we selfed and outcrossed a set of  $\sim 70$  teosinte landraces to get a progeny array composed of 4,875 individuals. The  $\sim 70$  founders and all the progeny were genotyped using GBS. We also re-sequenced 20/70 founder lines (the others will be re-sequenced soon). Because of the high error rate of the GBS data, especially problematic for calling heterozygous sites, we employed a phasing and imputation strategy to infer the expected genotypes by combining parentage and GBS information.

This file is to document the R package we developed to solve the problems step by step.

#### 1.2 Install and Usage

Install devtools first, and then use devtools to install impute from github.

```
# install and load devtools
devtools::install_github("hadley/devtools")
library(devtools)
# install and load imputeR
install_github("yangjl/imputeR")
library(imputeR)
```

#### 1.3 How to find help.

Within "R" console, type "?impute\_mom" or "help(impute\_mom)" to find help information about the function.

```
library(imputeR)
?impute_mom
```

### 2 Infer mom's genotype from GBS data

If we got mom's WGS data, this step can be skipped.

We have observed mom and observed (selfed) kids. We want to know  $P(G|\theta)$ , or the probability of mom's genotype given observed data  $\theta$ . And according to Bayes' theorem,

$$P(G|\theta) \propto P(\theta|G) \times P(G)$$
,

where P(G) is the probability of the genotype according to the Hardy-Weinberg equilibrium estimated from the population. This consists of observed genotypes (G') of both mom and kids. So:

$$P(G|\theta) \propto \left(\prod_{i=1}^{k} P(G'_{k}|G)\right) \times P(G'_{mom}|G) \times P(G),$$

where  $P(G'_{mom}|G)$  is the probability of mom's observed genotype given a true genotype G by considering error rates, i.e. GBS homozygote error = 0.02 and heterozygote error = 0.8.

And  $P(G'_k|G)$  is the probability of the k th kid's observed genotype given genotype G by considering error rates and Mendelian segregation rate.

```
# set the path
setwd("../")
# loading all the R functions from folder "lib"
f <- sapply(list.files(pattern="[.]R$", path="lib", full.names=TRUE), source)

set.seed(123456)
sim <- SimSelfer(size.array=10, het.error=0.7, hom.error=0.002, numloci=100, rec=1.2, imiss=0.3)
plotselfer(sim, kids=6:10, snps=40:100, cols=c("green", "blue"))

#install.packages(c("devtools", "roxygen2", "testthat", "knitr"))</pre>
```

This function is to impute mom's genotype from a progeny array of k kids at a single locus. inferred\_mom=1 -> 00, 2->01, 3->11

### 3 Imputing Founder Genotypes

$$P(G|\theta) \propto P(\theta|G) \times P(G)$$

$$P(G|\theta) \propto \left(\prod_{i=1}^{k} P(G'_{i}|G)\right) \times \left(\sum_{n=1}^{mom} P(G'_{mom}|G)\right) \times P(G)$$

This function is to impute mom's genotype by finding the maximum likelihood of  $P(G|\theta)$  from a progeny array of k kids at a single locus. - Where  $\theta$  denotes observed data. It consists of observed genotypes (G') of both mom and kids

- P(G) is the probability of a genotype given Hardy-Weinberg frequencies estimated from the observed data.
- $P(G'_{mom}|G)$  is the error matrix estimated from the data, i.e. homozygote error = 0.02 and heterozygote error = 0.6.
- $P(G'_{i}|G)$  is the error matrix times Mendelian segregation rate.

### 4 Phasing Founder Genotypes

$$\begin{split} &P(H|\theta) \propto P(\theta|H) \times P(H) \\ &P(H|\theta) \propto \left(\prod_{i=1}^k P(H_k'|H)\right) \times P(H) \\ &P(H|\theta) \propto \left(\prod_{i=1}^k \prod_{l=1}^n P(G_{i,l}'|H)\right) \times P(H) \end{split}$$

- Where  $\theta$  denotes observed data.
- P(H) is the probability of the haplotype for a given window size of n.
- $P(G'_{i,l}|H)$  is the probability of kid i at locus l for a given haplotype H.
- The prior P(H) is that all possible haplotypes of a given window size are equally likely.

### 5 Imputing and Phasing Kids

$$\begin{split} &P(H_k|\theta) \propto P(\theta|H_k) \times P(H_k) \\ &P(H_k|\theta) \propto \left(\prod_{i=k} P(H_k'|H_k)\right) \times P(H_k) \\ &P(H_k|\theta) \propto \left(\prod_{i=k} \prod_{l=1}^{n} P(G_{i,l}'|H_k)\right) \times P(H_k) \end{split}$$

- Where  $\theta$  denotes observed data.
- P(H) is the probability of the haplotype for a given window size of n.
- $P(G'_{i,l}|H)$  is the probability of kid i at locus l for a given haplotype H.
- The prior P(H) is that all possible haplotypes of a given window size are equally likely.

```
phase <- read.csv("../data/sim_phasing_res.csv")
hist(phase\u00eder, breaks=30, main="Simulation (N=100)",col="#faebd7", xlab="Phasing Error Rate")
abline(v=mean(phase\u00eder), col="red", lwd=2)
abline(v=median(phase\u00eder), col="darkblue", lwd=2)</pre>
```

### 6 Phasing Dad of outcrossing progeny array

$$P(H_d|\theta) \propto P(\theta|H_d) \times P(H_d)$$

$$P(H_d|\theta) \propto \left(\prod_{i=1}^k P(H'_k|H_d, H_m)\right) \times P(H_m) \times P(H_d)$$

$$P(H|\theta) \propto \left(\prod_{i=1}^k \prod_{l=1}^n P(G'_{i,l}|H)\right) \times P(H)$$

- Where  $\theta$  denotes observed data.
- $P(H_d)$  is the probability of the dad's haplotype for a given window size of n.
- $P(G'_{i,l}|H)$  is the probability of kid i at locus l for a given haplotype H.
- The prior P(H) is that all possible haplotypes of a given window size are equally likely.