Econ720 - TA Session 1

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UNC-Chapel Hill

2020. 8. 21

0. Macro is saying hi to you!

Office Hour:

Thursday, 1:00 - 2:00, Zoom

Link:

https://us02web.zoom.us/j/5736769300 pwd=VmRvMOt1dVB5RTF5c3FoZ0hFVGxJQT09

• ID: 5736769300

Passcode: 0EGbBi

Appointment by email: yanran@ad.unc.edu

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Recitation:

Friday, 8:00 - 8:50, Zoom

• Link:

https://us02web.zoom.us/j/5736769300 pwd=VmRvMOt1dVB5RTF5c3FoZ0hFVGxJQT09

• ID: 5736769300

Passcode: 0EGbBi

 I will record class meetings via zoom and send recordings by email.

0. Macro is saying hi to you!

Today's Task:

- How to define competitive equilibrium (On the Next: a detailed OLG example)
- Walras Law
- Arrow-Debreu and Sequential Trading

- Describe the economy (Find how many sectors there are)
- Solve each sector's problem (e.g. Household, Firm) endogenous/ choice variables price variables

Example

$$max \ u(c_1, c_2)$$

s.t. $p_1c_1 + p_2c_2 = p_1e_1 + p_2e_2$

Choice variables?

Written in real terms: $c_1 + pc_2 = e_1 + pe_2$, where $p = \frac{p_2}{p_1}$

Solve each sector's problem (e.g. Household, Firm)

$$max ln(c_1) + \beta ln(c_2)$$

 $s.t. c_1 + pc_2 = e_1 + pe_2$

- Set up Lagrangean
- Get FOCs by taking derivative with respect all choice variables in the Lagrangean.

Solve each sector's problem (e.g. Household, Firm)

max
$$ln(c_1) + \beta ln(c_2)$$

s.t. $c_1 + pc_2 = e_1 + pe_2$

- Set up Lagrangean
- Get FOCs by taking derivative with respect all choice variables in the Lagrangean.

$$\mathcal{L} = In(c_1) + \beta In(c_2) + \lambda (e_1 + pe_2 - c_1 - pc_2)$$

Solve each sector's problem (e.g. Household, Firm)

$$max ln(c_1) + \beta ln(c_2)$$

 $s.t. c_1 + pc_2 = e_1 + pe_2$

- Set up Lagrangean
- Get FOCs by taking derivative with respect all choice variables in the Lagrangean.

$$\mathcal{L} = \ln(\mathbf{c_1}) + \beta \ln(\mathbf{c_2}) + \lambda (e_1 + pe_2 - \mathbf{c_1} - p\mathbf{c_2})$$

- State the market clearing condition
 - How to find markets?
 - → Start with choice variables
 - How to write market clearing conditions?
 - → Aggregate supply = Aggregate demand
- Define the equilibrium Allocations { ... } and prices { ... } that satisfy

Optimality conditions for each sector $\left\{ egin{array}{ll} \mbox{Household problem} \mbox{ Firm problem} \end{array} \right.$

Market clearing condition Accounting identity

N objects, N+1 equations (Walras' Law)

2. Walras' Law

Define the equilibrium

Allocations $\{c_1, c_2\}$ and prices $\{p\}$ that satisfy

- Optimality conditions for household
 - **1** FOC: $\beta \frac{c_1}{c_2} = p$
 - ② BC: $c_1 + pc_2 = e_1 + pe_2$
- Market clearing condition
 - $c_1 = e_1$
 - $c_2 = e_2$

3 objects, 4 equations (Walras' Law)

Linear combination exists in these 4 equations: equation 2 is a linear combination of equation 3 and 4

Two-period Example

Demographics: N identical household live for 2 periods, t = 1, 2

Commodities: c_1 , c_2

Preference: $u(c_1, c_2)$

Endowments: e_1 , e_2

Two-period t = 1, 2

- c_1 : consumption in period 1
- c_2 : consumption in period 2

Goods in different periods can be considered different goods

- \circ c_1 : apple
- c₂: pineapple

(1). Arrow-Debreu Trading

All trades take place at t = 1



(1). Arrow-Debreu Trading

```
All trades take place at t=1\Rightarrow Only one BC!!
BC: p_1c_1+p_2c_2=p_1e_1+p_2e_2

max\ u(c_1,c_2)
s.t.\ c_1+pc_2=e_1+pe_2 (BC here is written in real terms.)
\mathscr{L}=u(c_1,c_2)+\lambda(e_1+pe_2-c_1-pc_2)
\therefore \frac{u_1}{u_2}=\frac{1}{p}
```

Competitive Equilibrium

Allocations { } and price { } that satisfy Household problem solution:

Goods market clearing conditions:

(1). Arrow-Debreu Trading

```
All trades take place at t=1\Rightarrow Only one BC!!
BC: p_1c_1+p_2c_2=p_1e_1+p_2e_2

max\ u(c_1,c_2)
s.t.\ c_1+pc_2=e_1+pe_2 (BC here is written in real terms.)
\mathscr{L}=u(c_1,c_2)+\lambda(e_1+pe_2-c_1-pc_2)
\therefore \frac{u_1}{u_2}=\frac{1}{p}
```

Competitive Equilibrium

Allocations $\{c_1, c_2\}$ and price $\{p\}$ that satisfy Household problem solution: F.O.C., BC Goods market clearing conditions: $c_1 = e_1, c_2 = e_2$

(2). Sequential Trading

Markets open at each date ⇒ For each period,there is a BC!! Budget Constraint:

$$p_1c_1 + () = p_1e_1$$

 $p_2c_2 = p_2e_2 + ()$

⇒ We need assets to transfer resources between periods!

$$p_1c_1 + Qb = p_1e_1$$

 $p_2c_2 = p_2e_2 + p_2b$

Choose one price to normalize in one BC.

Normalize the price of good 1 in the first BC: $c_1 + qb = e_1$ where $q = \frac{Q}{p_1}$ Normalize the price of good 2 in the second BC: $c_2 = e_2 + b_1$

(2). Sequential Trading

$$max \ u(c_1, c_2)$$
 $s.t. \ c_1 + qb = e_1$
 $c_2 = e_2 + b$
 $\mathscr{L} = u(c_1, c_2) + \lambda(e_1 + qe_2 - c_1 - qc_2)$
 $\therefore \frac{u_1}{u_2} = \frac{1}{q}$

Competitive Equilibrium

Allocations { } and price { } that satisfy Household problem solution: Market clearing conditions:

(2). Sequential Trading

$$egin{aligned} \max & u(c_1,c_2) \ s.t. & c_1+qb=e_1 \ & c_2=e_2+b \ \mathscr{L} &= u(c_1,c_2) + \lambda(e_1+qe_2-c_1-qc_2) \ dots & \dfrac{u_1}{u_2} &= \dfrac{1}{q} \end{aligned}$$

Competitive Equilibrium

Allocations $\{c_1, c_2, b\}$ and price $\{q\}$ that satisfy

Household problem solution: F.O.C., BC

Market clearing conditions:

Goods market: $c_1 = e_1$, $c_2 = e_2$

Bonds market: b = 0



4. Why $b_t = 0$?

In equilibrium, the bond market clearing condition is $b_t = 0$

Recall the fundamental rule for market clearing condition:

 $\mathsf{Aggregate}\ \mathsf{supply} = \mathsf{Aggregate}\ \mathsf{demand}$

- → Who supplies bonds? Household!
 Who demands bonds? Household!
- ightarrow The model setup assumes **Representative Agent**, indicating that we can consider the model as if there was only **A SINGLE HOUSE-HOLD** in this economy.

4. Why $b_t = 0$?

Could there be cases where $b_t \neq 0$ in equilibrium?

Yes!

e.g. Government issuing bonds

Heterogeneous agents (See PS1-Question 2)