

Localization of Heterogeneous Disease Features in Neuroimage: A Differential Inclusion Approach

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1 Alzheimer's Detection

- Heterogeneity of features
- Summary

2 Other works

- Robust Estimates via Generative Adversarial Networks
- Decentralized and Parsimonious Training of Neural Networks

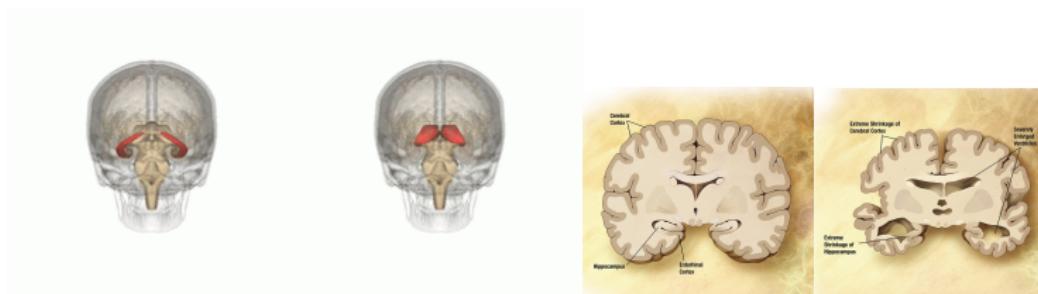
What is Alzheimer's Disease (AD)

- A complex chronically progressive neurodegenerative disease and the most common form of dementia in elderly people worldwide.
- In 2015, about **29.8 million AD** people worldwide and dementia resulted in **1.9 million deaths**.
- In Hong Kong alone, dementia was estimated to affect approximately 103,433 people over the age of 60 years in 2009 and is expected to increase 222% by 2039.
- The patient with AD is transitioned from Normal Control (NC), to Mild Cognitive Impairment (MCI) then to AD.
- There are no clear rules to define status of the diseases.
- However, the brain structure changes a lot during the process before functional changes detected.

Heterogeneity of features

Biomarkers from sMRI

- Biomarkers processed by structural Magnetic Resonance Imaging (sMRI) (PET etc.) as predictors used to classify NC, MCI, and AD, e.g. atrophy of Hippocampus and Thalamus.
- Symptoms can be alleviated or inhibited by drugs, it's hard to say whether it has structurally improvement.



Heterogeneity of features

Heterogeneity of Voxel-based Features

The preprocessed features on structural Magnetic Resonance Imaging (sMRI) images contain the following voxel-wise features:

- **Lesion features** that are contributed to the disease
- **Procedural bias** introduced during the preprocessing steps and shown to be helpful in classification
- **Irrelevant or null features** that are not due to disease status

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Our two goals in voxel-based neuroimage analysis for disease prediction:

- **Accurate Classification:** NC, MCI, AD
- **Stable feature selection** of lesion features and procedural bias, with high recall and low false discovery rate (FDR).

Heterogeneity of features

Lesion Features

- Have been the main focus in disease prediction.
- Only a few number of gray matter voxels are correlated with the disease.
- Geometrically clustered in atrophied regions in dementia disease such as Alzheimer's Disease (AD).



Heterogeneity of features

Procedural Bias

- Introduced during the preprocessing steps, are found to be helpful for disease prediction.
- Refer to the mistakenly enlarged Gray Matter (GM) voxels surrounding locations with cerebral spinal fluid (CSF) spaces enlarged, e.g. lateral ventricle in AD. [Sun et al. MICCAI 2017]

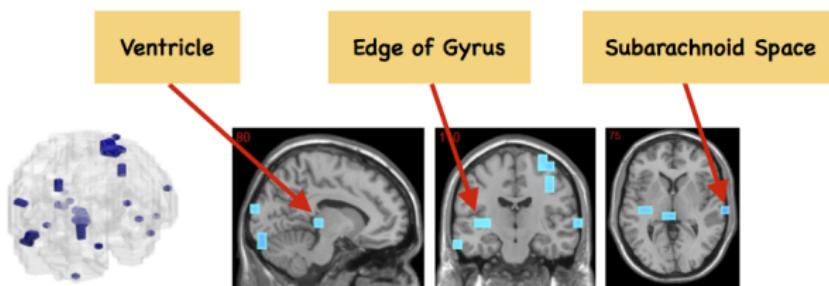


Fig. 1. The overlapped voxels among top 150 negative value voxels in each fold of β_{pre} at the time corresponding to the best average prediction result in the path of GSsplit LBI using 10-fold cross-validation. For subjects with AD, they represent enlarged GM voxels surrounding lateral ventricle, subarachnoid space, edge of gyrus, etc.

Heterogeneity of features

Limitation of Existing Models

- The lesion features have been the only focus of existing models for their medical interpretability.
- In VBM analysis, procedure biases are introduced on some features during the commonly used preprocessing procedure of T_1 weighted image (e.g. DARTEL [[Ashburner 2007, Neuroimage](#)])
- Procedure bias can be helpful for classification, however they are ignored in the literature.

Heterogeneity of features

ADNI Dataset

- Consider AD/NC classification (namely ADNC) and MCI (Mild Cognitive Impairment)/NC (namely MCINC) classification
- The data are obtained from ADNI¹ database, which is split into 1.5T and 3.0T (namely 15 and 30) MRI scan magnetic field strength datasets.
- DARTEL VBM pipeline [[Ashburner \(2007\) Neuroimage](#)] is implemented to preprocess the data.
- The input features consist of 2,527 $8 \times 8 \times 8$ mm³ size voxels with average values in GM population template greater than 0.1.
- Experiments are designed on 15ADNC, 30ADNC and 15MCINC tasks.

¹<http://adni.loni.ucla.edu>

Heterogeneity of features

The efficacy of Procedural bias in prediction

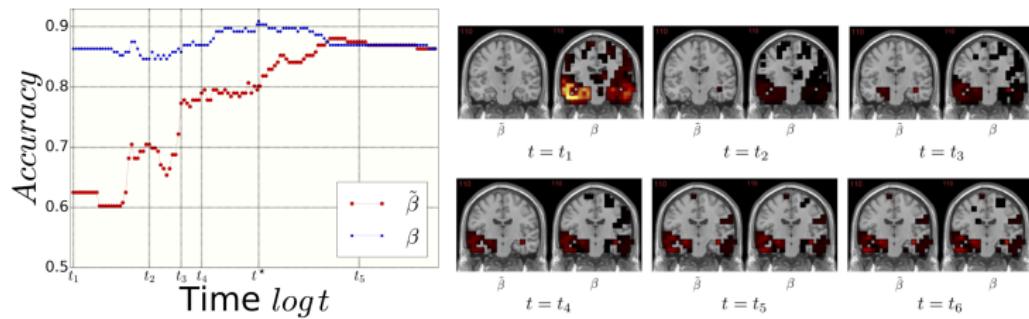


Figure: Exploitation of both lesion features and procedure bias (blue) improves prediction accuracy by dominating the curve merely by lesion features (red). $\tilde{\beta}$ corresponds to the lesion features interpretable for AD, while β additionally leverages the procedure bias to improve the prediction.

Heterogeneity of features

Lesion Features vs. Procedure Bias

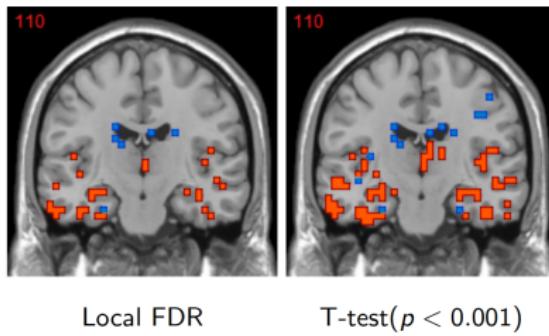


Figure: Lesion features (**red**) as degenerate GM voxels, while Procedure Bias (**blue**) contains 'enlarging' GM voxels in preprocessing due to the enlarging cerebral spinal fluid (CSF), surrounding lateral ventricle and subarachnoid space etc.

Heterogeneity of features

Results of Prediction

Exploiting both the procedure bias and lesion features, our method (GSplitLBI [Sun-Hu-Y.-Wang 2017]) achieves the state-of-the-art performance in the 10-fold cross-validation error:

Table 1. Comparison of GSplit LBI with other models

	MLDA	SVM	Lasso	Graphnet	Elastic Net	TV + l_1	n^2 GFL	GSplit LBI (β_{pre})
15ADNC	85.06%	83.12%	87.01%	86.36%	88.31%	83.77%	86.36%	88.96%
30ADNC	86.93%	87.50%	87.50%	88.64%	89.20%	87.50%	87.50%	90.91%
15MCINC	61.41%	70.13%	69.80%	72.15%	70.13%	73.83%	69.80%	75.17%

Heterogeneity of features

Stability of Feature Selection

Our method (GSplitLBI [[Sun-Hu-Y.-Wang](#) 2017]) also champions in stability of heterogeneous feature selection:

Table 2. mDC comparison between GSplit LBI and other models

	Lasso	Elastic Net	Graphnet	TV + l_1	n^2 GFL	GSplit LBI (β_{les})
Accuracy	87.50%	89.20%	88.64%	87.50%	87.50%	88.64%
mDC	0.1992	0.5631	0.6005	0.5824	0.5362	0.7805
$\sum_{k=1}^{10} S(k) /10$	50.2	777.8	832.6	712.6	443.9	129.4

Where

$$mDC := \frac{10 |\cap_{k=1}^{10} S(k)|}{\sum_{k=1}^{10} |S(k)|}$$

with $S(k)$ denoting the support set of β_{les} in k -th fold.

How do we reach this?

Below we are going to introduce a new methodology:

- **Boosting with Structural Sparsity**
- mathematically, a differential inclusion method as restricted gradient flows, whose discretization meets the sparse mirror descent algorithm
- variable splitting enables us to exploit both lesion features and procedure bias effectively
- it can be generalized to FDR heterogeneous smoothing for new algorithms in Empirical Bayes

Some Reference

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- **R** package:
 - <http://cran.r-project.org/web/packages/Libra/index.html>
- **Matlab** package:
 - <https://github.com/yuany-pku/split-lbi>
- **Python** package to appear

Summary: A Renaissance of Boosting?

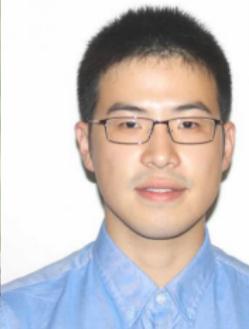
- Boosting as gradient descent is arguably the **best off-the-shelf machine learning algorithm** ([Leo Breiman](#)): **AdaBoost** ([Freund-Schapire](#)), **L2Boost** ([Buhlman-Yu](#)), **LogitBoost** ([Friedman](#))
- The (sparsity) restricted gradient descent dynamics: **differential inclusions**
 - has a simple discretized algorithm to follow the regularization path (LBI), amiable for parallel realizations in **big data analytics**
 - improves model selection or prediction, **better than generalized LASSO**
 - is widely adapted to **various sparsity** constraints
- This is a gift of **Applied Mathematics** to High Dimensional **Statistics**



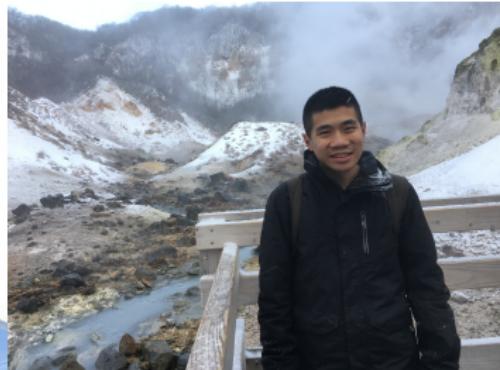
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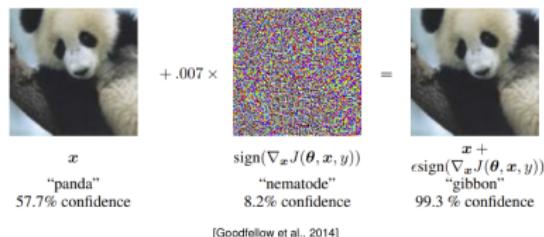
Jiyu Liu (Yale)



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Robustness?

- How can one achieve robustness against adversarial?
- Robust statistics: for Huber's ϵ -contamination model, Generative Adversarial Networks (GANs) provably achieve **statistically optimal robust estimates**
- Reference
 - Gao, Liu, Yao, and Zhu, “[Robust Estimation and Generative Adversarial Networks](#)”, ICLR 2019, [arXiv:1810.02030](#).
 - Gao, Yao, and Zhu, “[Generative Adversarial Nets for Robust Scatter Estimation: A Proper Scoring Rule Perspective.](#)”, [arXiv:1903.01944](#).



Decentralized Training of Neural Networks

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- Global Convergence of Block Coordinate Descent in Deep Learning Jinshan Zeng, Tim Tsz-Kit Lau, Shaobo Lin, Yuan Yao. ICML.
- A Convergence Analysis of Nonlinearly Constrained ADMM in Deep Learning. Jinshan Zeng, Shao-Bo Lin, Yuan Yao.

The END

