

1



# An Introduction to Convolutional Neural Networks

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# Summary

- ▶ We had covered so far
  - ▶ Linear models (linear and logistic regression) – always a good start, simple yet powerful
  - ▶ Model Assessment and Selection – basics for all methods
  - ▶ Trees, Random Forests, and Boosting – good for high dim mixed-type heterogeneous features
  - ▶ Support Vector Machines – good for small amount of data but high dim geometric features
- ▶ Next, neural networks for unstructured data (image, language etc.):
  - ▶ **Convolutional Neural Networks** – image data
  - ▶ Generative models and GANs – new unsupervised learning for image, etc.
  - ▶ Recurrent Neural Networks, LSTM – sequence data
  - ▶ Transformer, BERT – machine translation etc.
  - ▶ Reinforcement Learning – Markov decision process, playing games, etc.

# Kaggle survey: Top ML Methods

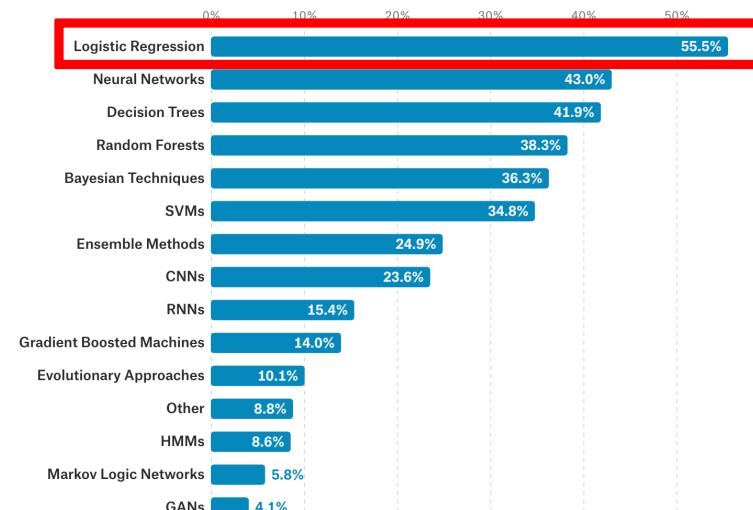
<https://www.kaggle.com/surveys/2017>

## Academic

### What data science methods are used at work?

Logistic regression is the most commonly reported data science method used at work for all industries except [Military and Security](#) where Neural Networks are used slightly more frequently.

Company Size ▾ Academic ▾ Job Title ▾



1,201 responses

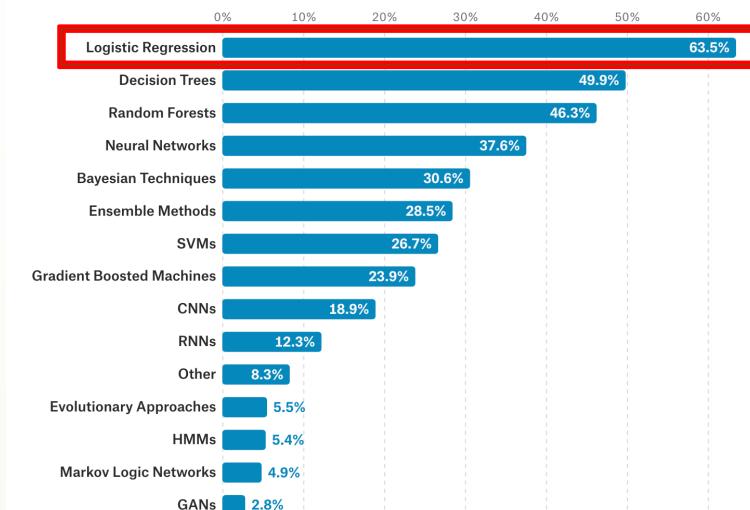
View code in Kaggle Kernels

## Industry

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Company Size ▾ Industry ▾ Job Title ▾



7,301 responses

View code in Kaggle Kernels

# What type of data is used at work?

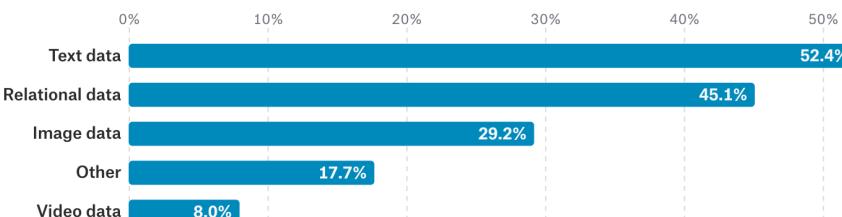
<https://www.kaggle.com/surveys/2017>

## Academic

### What type of data is used at work?

Relational data is the most commonly reported type of data used at work for all industries except for **Academia** and the **Military and Security** industry where text data's used more.

Company Size ▾ Academic ▾ Job Title ▾



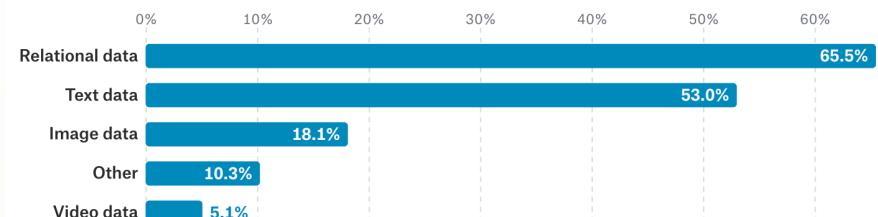
1,277 responses

## Industry

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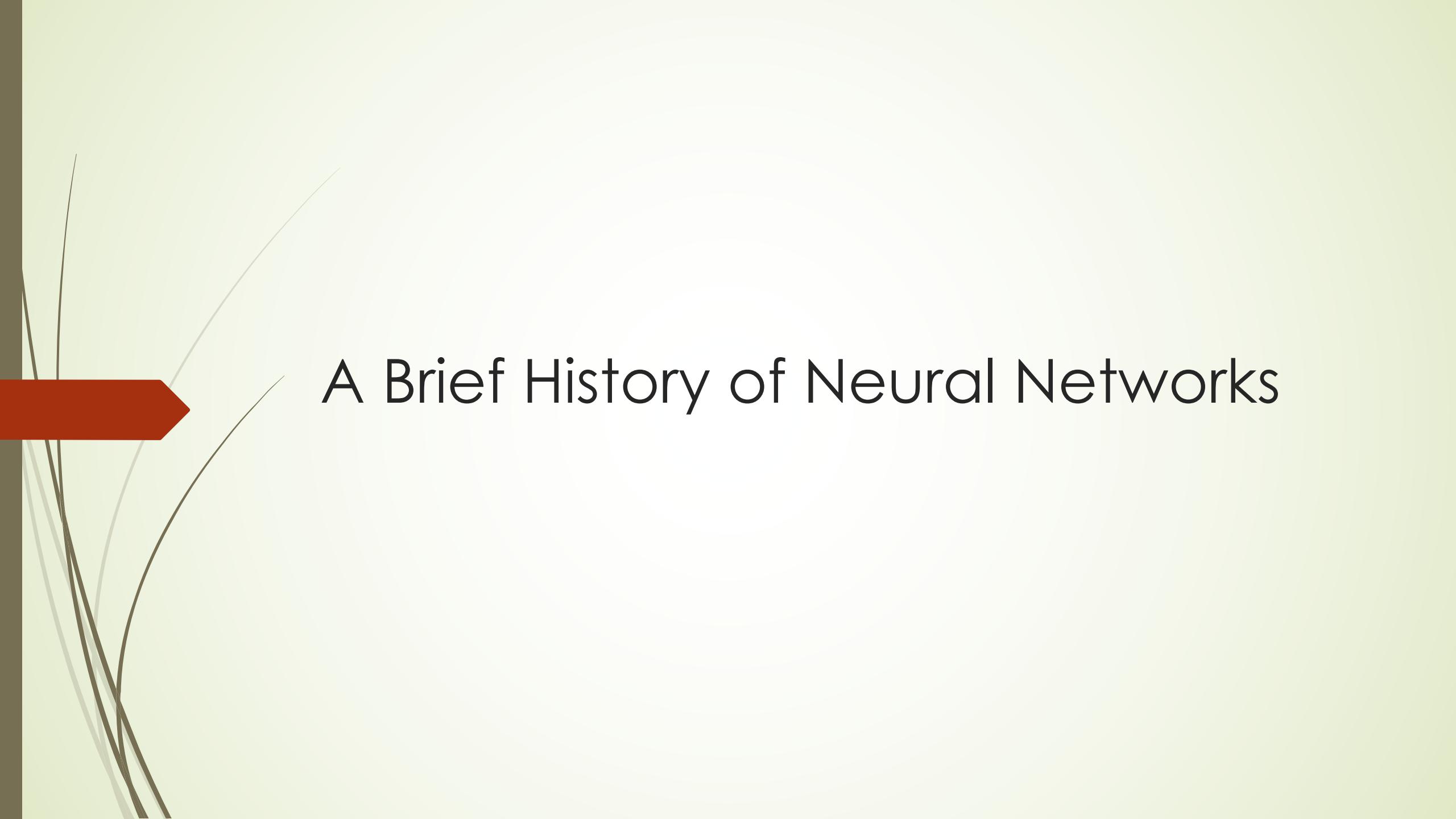
Company Size ▾ Industry ▾ Job Title ▾



8,024 responses

# Some reference books on Deep Learning

- ▶ Deep Learning with Python, Manning Publications 2017
  - ▶ by François Chollet
  - ▶ [https://www.manning.com/books/deep-learning-with-python?a\\_aid=keras&a\\_bid=76564dff](https://www.manning.com/books/deep-learning-with-python?a_aid=keras&a_bid=76564dff)
- ▶ Deep Learning, MIT Press 2016
  - ▶ By Ian Goodfellow, Yoshua Bengio, and Aaron Courville,
  - ▶ <http://www.deeplearningbook.org/>
- ▶ Many other public resources

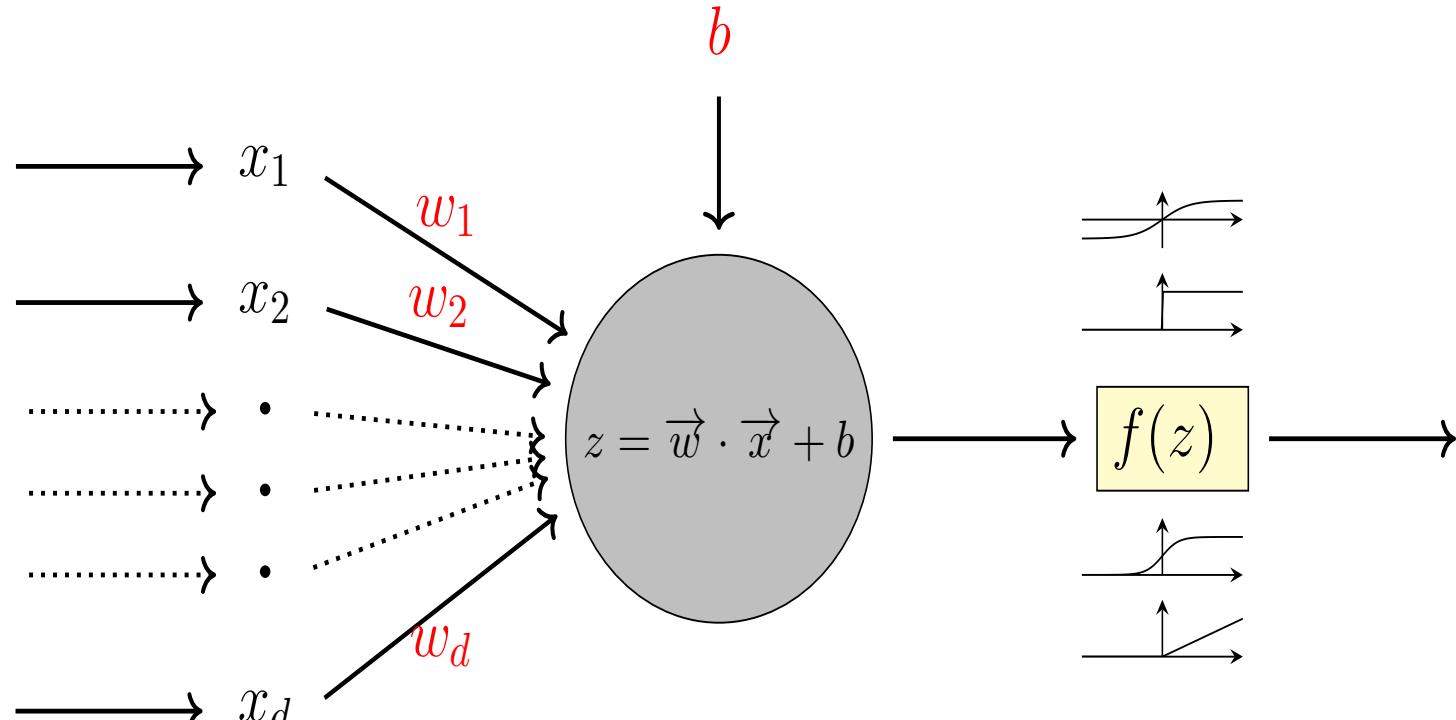


# A Brief History of Neural Networks

# Perceptron: single-layer



- Invented by Frank Rosenblatt (1957)



# The Perceptron Algorithm

$$\ell(w) = - \sum_{i \in \mathcal{M}_w} y_i \langle w, \mathbf{x}_i \rangle, \quad \mathcal{M}_w = \{i : y_i \langle \mathbf{x}_i, w \rangle < 0, y_i \in \{-1, 1\}\}.$$

The Perceptron Algorithm is a *Stochastic Gradient Descent* method  
([Robbins–Monro 1950](#); [Kiefer–Wolfowitz 1951](#)) :

$$\begin{aligned} w_{t+1} &= w_t - \eta_t \nabla_i \ell(w_t) \\ &= \begin{cases} w_t - \eta_t y_i \mathbf{x}_i, & \text{if } y_i w_t^T \mathbf{x}_i < 0, \\ w_t, & \text{otherwise .} \end{cases} \end{aligned}$$

# Separable Data with Margin: Stopping of Perceptron after Finite Steps

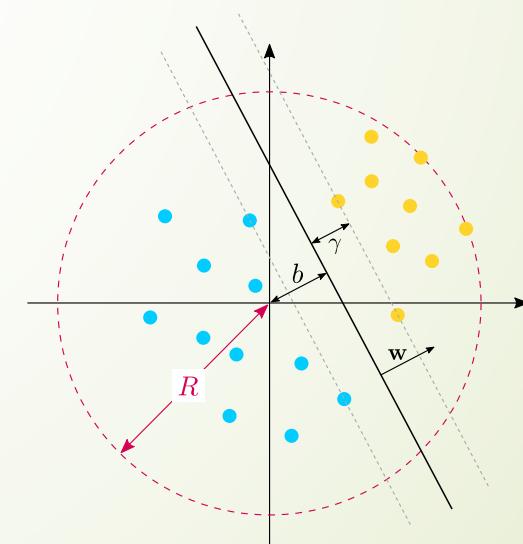
The perceptron convergence theorem was proved by [Block \(1962\)](#) and [Novikoff \(1962\)](#). The following version is based on that in [Cristianini and Shawe-Taylor \(2000\)](#).

**Theorem 1** (Block, Novikoff). *Let the training set  $S = \{(\mathbf{x}_1, t_1), \dots, (\mathbf{x}_n, t_n)\}$  be contained in a sphere of radius  $R$  about the origin. Assume the dataset to be linearly separable, and let  $\mathbf{w}_{\text{opt}}$ ,  $\|\mathbf{w}_{\text{opt}}\| = 1$ , define the hyperplane separating the samples, having functional margin  $\gamma > 0$ . We initialise the normal vector as  $\mathbf{w}_0 = \mathbf{0}$ . The number of updates,  $k$ , of the perceptron algorithms is then bounded by*

$$k \leq \left( \frac{2R}{\gamma} \right)^2. \quad (10)$$

Input ball:  $R = \max_i \|\mathbf{x}_i\|$ .

Margin:  $\gamma := \min_i y_i f(\mathbf{x}_i)$



# Proof.

- ▶ For convenience, denote
  - $\hat{\mathbf{w}} = (\mathbf{w}^T, b/R)^T = (w_1, \dots, w_D, b/R)^T$
  - $\hat{\mathbf{x}} = (\mathbf{x}^T, R)^T = (x_1, \dots, x_D, R)^T$

- ▶ The perceptron algorithm:

$$\hat{\mathbf{w}}_{t+1} = \begin{cases} \hat{\mathbf{w}}_t - \eta_t y_i \mathbf{x}_i, & \text{if } y_i \hat{\mathbf{w}}_t^T \hat{\mathbf{x}}_i < 0, \\ \hat{\mathbf{w}}_t, & \text{otherwise .} \end{cases}$$

where we set  $\eta_t = 1$  as the hyperplane is unchanged if we multiply the normal vector  $\hat{\mathbf{w}}$  by a constant.

# Proof (continued, growth of $\|\hat{\mathbf{w}}_k\|^2$ )

- ▶ We first derive an upper bound on how fast  $\|\hat{\mathbf{w}}\|^2$  grows.

$$\begin{aligned}\|\hat{\mathbf{w}}_{k+1}\|^2 &= (\hat{\mathbf{w}}_k + y_i \hat{\mathbf{x}}_i)^\top (\hat{\mathbf{w}}_k + y_i \hat{\mathbf{x}}_i) \\&= \hat{\mathbf{w}}_k^\top \hat{\mathbf{w}}_k + \hat{\mathbf{x}}_i^\top \hat{\mathbf{x}}_i + 2y_i \hat{\mathbf{w}}_k^\top \hat{\mathbf{x}}_i \\&= \|\hat{\mathbf{w}}_k\|^2 + \|\hat{\mathbf{x}}_i\|^2 + 2y_i \hat{\mathbf{w}}_k^\top \hat{\mathbf{x}}_i \\&\leq \|\hat{\mathbf{w}}_k\|^2 + \|\hat{\mathbf{x}}_i\|^2, \text{ by } y_i \hat{\mathbf{w}}_k^\top \hat{\mathbf{x}}_i < 0, \\&= \|\hat{\mathbf{w}}_k\|^2 + (\|\mathbf{x}_i\|^2 + R^2) \\&\leq \|\hat{\mathbf{w}}_k\|^2 + 2R^2, \text{ by } \|\mathbf{x}_i\|^2 \leq R^2\end{aligned}$$

which implies  $\|\hat{\mathbf{w}}_k\|^2 \leq 2kR^2$ .

# Proof (lower bound, projection on $\hat{\mathbf{w}}_{\text{opt}}$ )

- ▶ We then proceed to show how the inner product between an update of the normal vector and  $\hat{\mathbf{w}}_{\text{opt}}$  increases with each update

$$\begin{aligned}\hat{\mathbf{w}}_{\text{opt}}^T \hat{\mathbf{w}}_{k+1} &= \hat{\mathbf{w}}_{\text{opt}}^T \hat{\mathbf{w}}_k + y_i \hat{\mathbf{w}}_{\text{opt}}^T \hat{\mathbf{x}}_i \\ &\geq \hat{\mathbf{w}}_{\text{opt}}^T \hat{\mathbf{w}}_k + \gamma, \text{ by } y_i \hat{\mathbf{w}}_k^T \hat{\mathbf{x}}_i > \gamma \\ &\geq (k+1)\gamma\end{aligned}$$

i.e.  $\hat{\mathbf{w}}_{\text{opt}}^T \hat{\mathbf{w}}_k \geq k\gamma$ .

- ▶ Then by the Cauchy-Schwartz inequality

$$\begin{aligned}k^2\gamma^2 &\leq (\hat{\mathbf{w}}_{\text{opt}}^T \hat{\mathbf{w}}_k)^2 \leq \|\hat{\mathbf{w}}_{\text{opt}}\|^2 \|\hat{\mathbf{w}}_k\|^2 \leq 2kR^2 \|\hat{\mathbf{w}}_{\text{opt}}\|^2 \\ &\Rightarrow k \leq 2 \|\hat{\mathbf{w}}_{\text{opt}}\|^2 \frac{R^2}{\gamma^2} \quad (1)\end{aligned}$$

## Proof (continued)

- ▶ As  $b < R$ , we can rewrite the norm of the normal vector:

$$\|\hat{\mathbf{w}}_{\text{opt}}\|^2 = \|\mathbf{w}_{\text{opt}}\|^2 + \frac{b^2}{R^2} \leq \|\mathbf{w}_{\text{opt}}\|^2 + 1 = 2$$

- ▶ Therefore, the number of mistake updates can be bounded by

$$k \leq 4 \frac{R^2}{\gamma^2} = \left( \frac{2R}{\gamma} \right)^2.$$

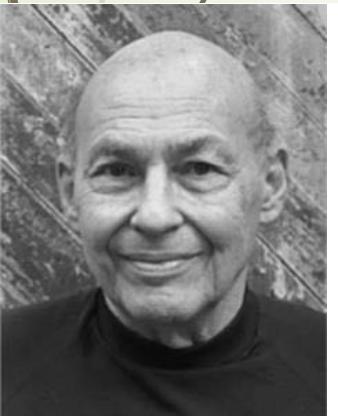
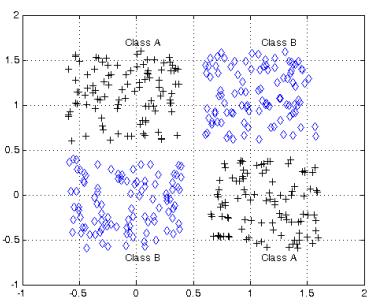
This completes the proof. □

# Locality or Sparsity of Computation

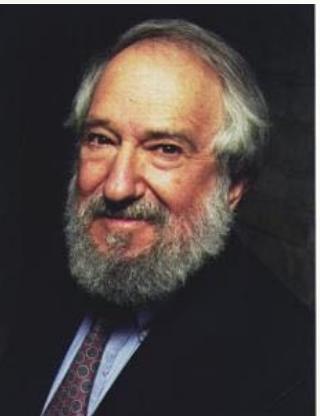
Minsky and Papert, 1969

Perceptron can't do **XOR** classification

Perceptron needs infinite global  
information to compute **connectivity**



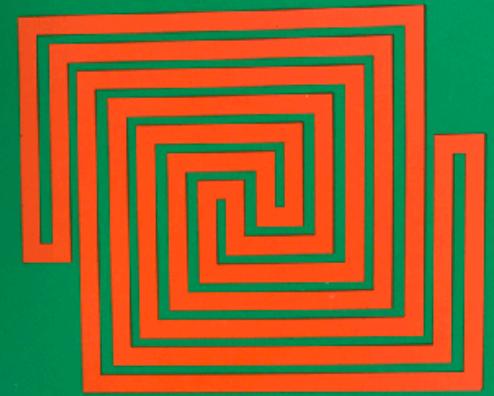
Marvin Minsky



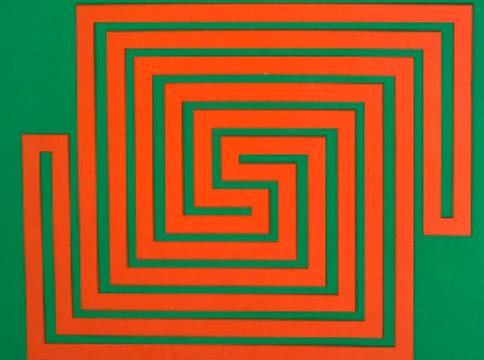
Seymour Papert

**Locality** or **Sparsity** is important:  
Locality in time?  
Locality in space?

Expanded Edition



Perceptrons



Marvin L. Minsky  
Seymour A. Papert

# Locality or Sparsity is a fundamental limitation

Definition (Minsky-Papert'1969)

The decision function that  $f(X) \in \{1, -1\}$  for  $X \subseteq \mathbb{R}^p$  has **order**  $k$ , if it can be represented by a superposition of functions whose supports are at most  $k$ , i.e. there exists a (possibly of infinite members) family of  $\{\phi_\alpha(X) : \text{supp}(\phi_\alpha) \leq k\}$  such that

$$f(X) = \sum_{\alpha} \phi_{\alpha}(X)$$

- Minsky-Papert model admits **infinitely many neurons** (wide network) in parallel processing, yet only **sparse** or **local inputs**. Note that it is not a Turing model.

# Examples of Finite Orders

- $f(X) = [X \text{ is nonempty}]$  has order 1, as  $\phi_a(X) = [a \in X]$  and  $f(X) = \sum_a \phi_a(X)$ .
- $f(X) = [X \text{ is convex}]$  has order 3, as

$$f(X) = - \sum_{a,b \in X} [\text{midpoint } ([a, b]) \text{ not in } X]$$

- The only topologically invariant predicates of finite order are functions of the Euler number  $E(X)$ , which for simplicial complex  $X \subseteq \mathbb{R}^2$  is defined as

$$\begin{aligned} E(X) &:= \#(\text{faces } (X)) - \#(\text{edges } (X)) + \#(\text{vertices } (X)) \\ &= \beta_0 - \beta_1 \end{aligned}$$

# Connectivity is of infinite order

- Which one of these two figures is connected?



Figure 5.1

Theorem (Minsky-Papert'1969)

*The decision function that  $f(X) = [X \text{ is connected}]$  for  $X \subseteq \mathbb{R}^p$  is **not of any finite order**, i.e. for any  $k < \infty$ , there does not exist a (possibly of infinite members) family of  $\{\phi_\alpha(X) : \text{supp}(\phi_\alpha) \leq k\}$  whose supports are at most  $k$ , such that*

$$f(X) = \left[ \sum_{\alpha} \phi_{\alpha}(X) \geq 0 \right] \quad (21)$$

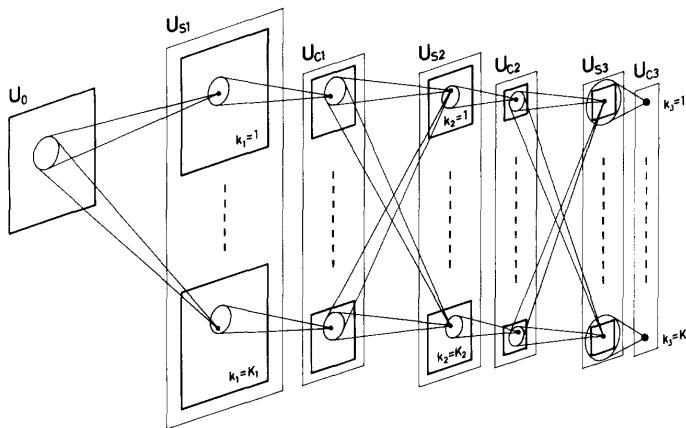
# Convolutional Neural Networks: local receptive field and shift invariance

Biol. Cybernetics 36, 193–202 (1980)

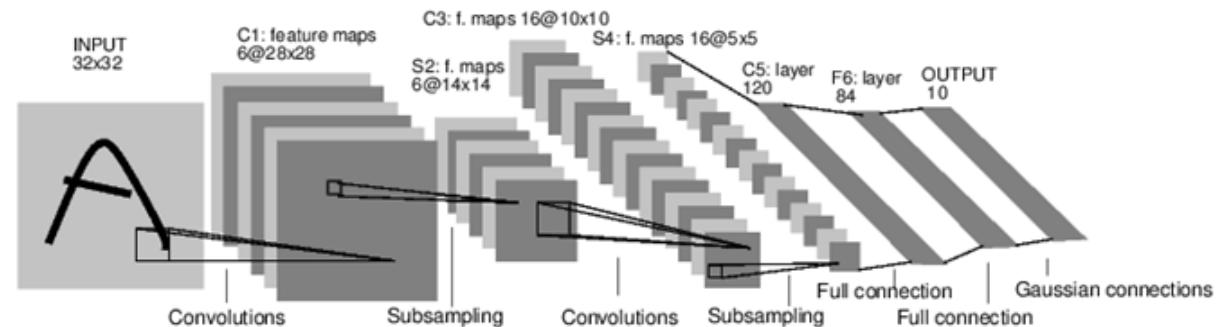
**Neocognitron: A Self-organizing Neural Network Model for a Mechanism of Pattern Recognition Unaffected by Shift in Position**

Kunihiko Fukushima

NHK Broadcasting Science Research Laboratories, Kinuta, Setagaya, Tokyo, Japan



- Can be traced to *Neocognitron* of Kunihiko Fukushima (1979)
- Yann LeCun combined convolutional neural networks with back propagation (1989)
- Imposes **shift invariance** and **locality** on the weights
- Forward pass remains similar
- Backpropagation slightly changes – need to sum over the gradients from all spatial positions



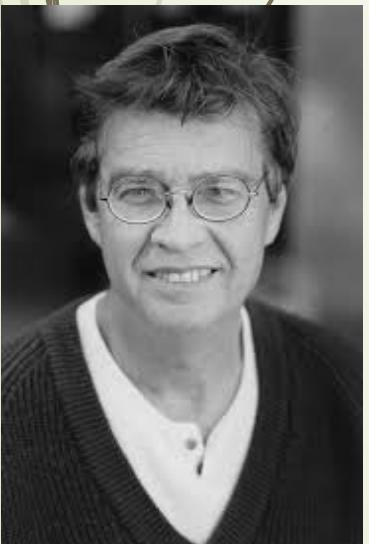
# Multilayer Perceptrons (MLP) and Back-Propagation (BP) Algorithms

Rumelhart, Hinton, Williams (1986)

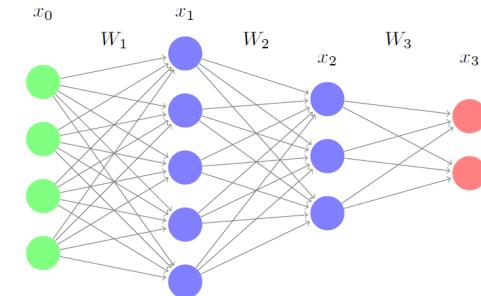
Learning representations by back-propagating errors, Nature, 323(9): 533-536

BP algorithms as **stochastic gradient descent** algorithms (**Robbins–Monro 1950; Kiefer–Wolfowitz 1951**) with Chain rules of Gradient maps

MLP classifies **XOR**, but the global hurdle on topology (connectivity) computation still exists



NATURE VOL. 323 9 OCTOBER 1986 LETTERS TO NATURE 533



## Learning representations by back-propagating errors

David E. Rumelhart\*, Geoffrey E. Hinton† & Ronald J. Williams\*

\* Institute for Cognitive Science, C-015, University of California, San Diego, La Jolla, California 92093, USA  
† Department of Computer Science, Carnegie-Mellon University, Pittsburgh, Philadelphia 15213, USA

We describe a new learning procedure, back-propagation, for networks of neuron-like units. The procedure repeatedly adjusts the weights of the connections in the network so as to minimize a measure of the difference between the actual output vector of the net and the desired output vector. As a result of the weight adjustments, internal 'hidden' units which are not part of the input or output code to represent important features of the task domain, and the regularities in the task are captured by the interactions of these units. The ability to create useful new features distinguishes back-propagation from earlier, simpler methods such as the perceptron-error minimization procedure.

There have been many attempts to design self-organizing neural networks. The aim is to find a powerful synaptic modification rule that will allow an arbitrarily connected neural network to develop an internal structure that is appropriate for a particular task domain. The task is specified by giving the desired state vector of the output units for each state vector of the input units. If the input units are directly connected to the output units it is relatively easy to find learning rules that iteratively adjust the relative strengths of the connections so as to progressively reduce the difference between the actual and desired output vectors\*. Learning becomes more interesting but

more difficult when we introduce hidden units whose actual or desired states are not specified by the task. (In perceptrons, there are 'feature analysers' between the input and output that are not true hidden units because their input connections are fixed by hand, so their states are completely determined by the input vector: they do not learn representations.) The learning procedure must decide under what circumstances the hidden units should be active in order to help achieve the desired input-output behaviour. This amounts to deciding what these units should represent. We demonstrate that a general purpose and relatively simple procedure is powerful enough to construct appropriate learned representations.

The simplest form of the learning procedure is for layered networks which have a layer of input units at the bottom, any number of intermediate layers, and a layer of output units at the top. Connections within a layer or from higher to lower layers are forbidden, but connections can skip intermediate layers. An input vector is presented to the network by setting the states of the input units. Then the states of the units in each layer are determined by applying equations (1) and (2) to the connections coming from lower layers. All units within a layer have their states set in parallel, but different layers have their states set sequentially, starting at the bottom and working upwards until the states of the output units are determined.

The total input,  $x_j$ , to unit  $j$  is a linear function of the outputs,  $y_i$ , of the units that are connected to  $j$  and of the weights,  $w_{ij}$ , on these connections

$$x_j = \sum_i y_i w_{ij} \quad (1)$$

Units can be given biases by introducing an extra input to each unit which always has a value of 1. The weight on this extra input is called the bias and is equivalent to a threshold of the opposite sign. It can be treated just like the other weights.

A unit has a real-valued output,  $y_j$ , which is a non-linear function of its total input

$$y_j = \frac{1}{1 + e^{-x_j}} \quad (2)$$

\* To whom correspondence should be addressed

# BP Algorithm: Forward Pass

- Cascade of repeated [linear operation followed by coordinatewise nonlinearity]'s
- Nonlinearities: sigmoid, hyperbolic tangent, (recently) ReLU.

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## Algorithm 1 Forward pass

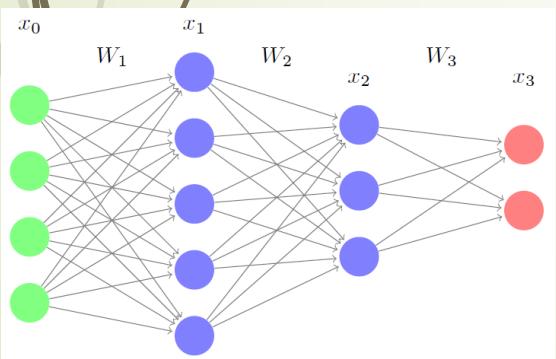
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**Input:**  $x_0$

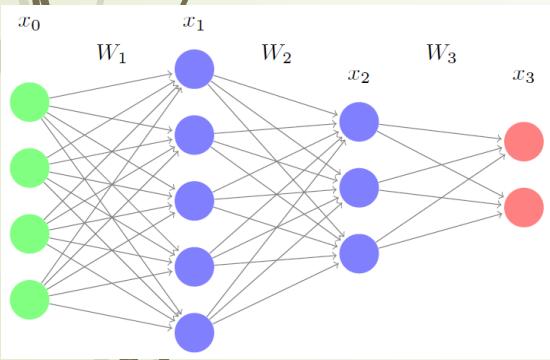
**Output:**  $x_L$

```
1: for  $\ell = 1$  to  $L$  do
2:    $x_\ell = f_\ell(W_\ell x_{\ell-1} + b_\ell)$ 
3: end for
```

---



# BP algorithm = Gradient Descent Method



- Training examples  $\{x_0^i\}_{i=1}^n$  and labels  $\{y^i\}_{i=1}^n$
- Output of the network  $\{x_L^i\}_{i=1}^m$
- Objective

$$J(\{W_l\}, \{b_l\}) = \frac{1}{n} \sum_{i=1}^n \frac{1}{2} \|y^i - x_L^i\|_2^2 \quad (1)$$

Other losses include cross-entropy, logistic loss, exponential loss, etc.

- Gradient descent

$$W_l = W_l - \eta \frac{\partial J}{\partial W_l}$$

$$b_l = b_l - \eta \frac{\partial J}{\partial b_l}$$

In practice: use Stochastic Gradient Descent (SGD)

# Derivation of BP: Lagrangian Multiplier

LeCun et al. 1988

Given  $n$  training examples  $(I_i, y_i) \equiv (\text{input}, \text{target})$  and  $L$  layers

- Constrained optimization

$$\min_{W,x} \quad \sum_{i=1}^n \|x_i(L) - y_i\|_2$$

$$\text{subject to} \quad x_i(\ell) = f_\ell \left[ W_\ell x_i(\ell-1) \right], \\ i = 1, \dots, n, \quad \ell = 1, \dots, L, \quad x_i(0) = I_i$$

- Lagrangian formulation (Unconstrained)

$$\min_{W,x,B} \mathcal{L}(W, x, B)$$

$$\mathcal{L}(W, x, B) = \sum_{i=1}^n \left\{ \|x_i(L) - y_i\|_2^2 + \sum_{\ell=1}^L B_i(\ell)^T \left( x_i(\ell) - f_\ell \left[ W_\ell x_i(\ell-1) \right] \right) \right\}$$

# back-propagation – derivation

- $\frac{\partial \mathcal{L}}{\partial B}$

## Forward pass

$$x_i(\ell) = f_\ell \left[ \underbrace{W_\ell x_i(\ell-1)}_{A_i(\ell)} \right] \quad \ell = 1, \dots, L, \quad i = 1, \dots, n$$

- $\frac{\partial \mathcal{L}}{\partial x}, z_\ell = [\nabla f_\ell] B(\ell)$

## Backward (adjoint) pass

$$z(L) = 2\nabla f_L \left[ A_i(L) \right] (y_i - x_i(L))$$

$$z_i(\ell) = \nabla f_\ell \left[ A_i(\ell) \right] W_{\ell+1}^T z_i(\ell+1) \quad \ell = 0, \dots, L-1$$

- $W \leftarrow W + \lambda \frac{\partial \mathcal{L}}{\partial W}$

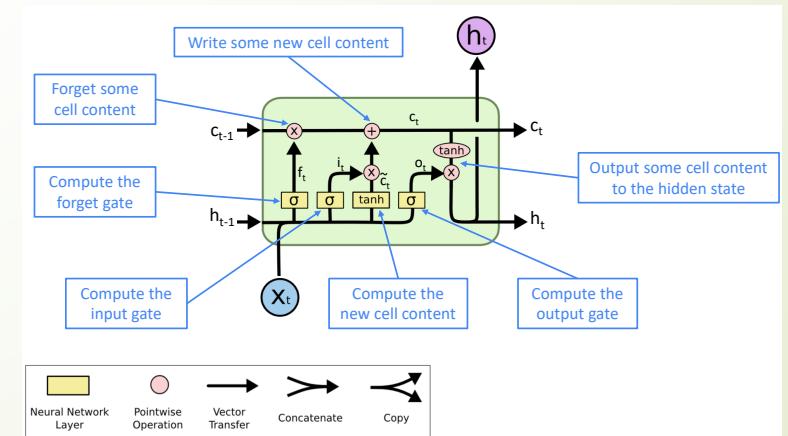
## Weight update

$$W_\ell \leftarrow W_\ell + \lambda \sum_{i=1}^n z_i(\ell) x_i^T(\ell-1)$$

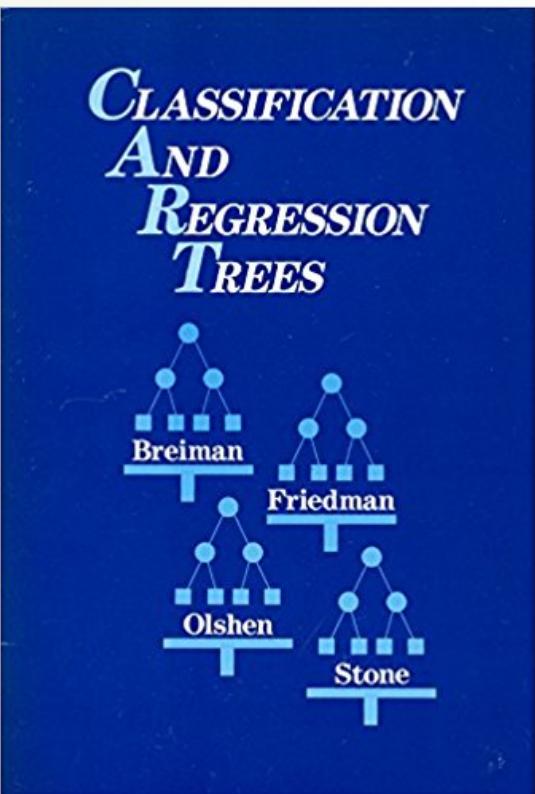
# Long-Short-Term-Memory (LSTM, 1997)



- ▶ Sepp Hochreiter; Jürgen Schmidhuber (1997). "Long short-term memory". *Neural Computation*. 9 (8): 1735–1780. (<https://www.bioinf.jku.at/publications/older/2604.pdf>)
- ▶ BP can not train deep networks due to gradient vanishing problem etc.
- ▶ Introduction of short path to train deep networks without vanishing gradient problem.
- ▶ This idea will return to Convolutional Networks as **ResNet** in 2015.



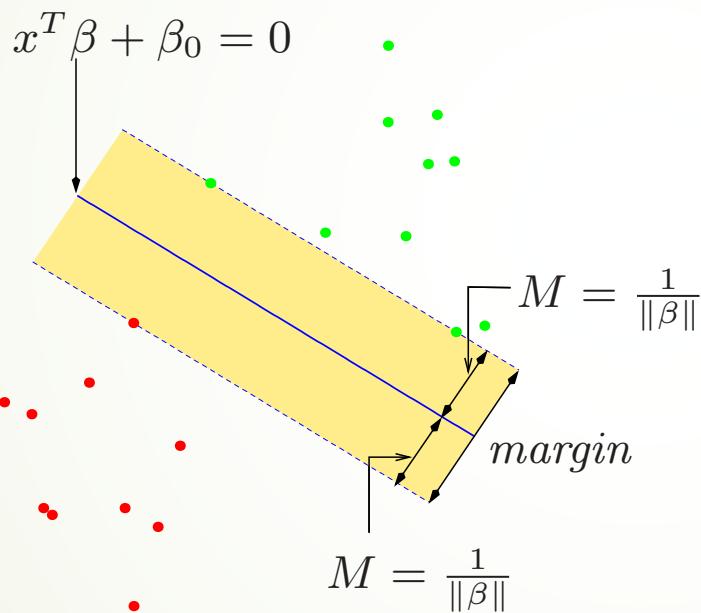
# Decision Trees and Boosting



- ▶ Breiman, Friedman, Olshen, Stone, (1983): CART
- ▶ ``The Boosting problem'' (M. Kearns & L. Valiant):  
**Can a set of weak learners create a single strong learner?** (三个臭皮匠顶个诸葛亮?)
- ▶ Breiman (1996): Bagging
- ▶ Freund, Schapire (1997): AdaBoost
- ▶ Breiman (2001): Random Forests



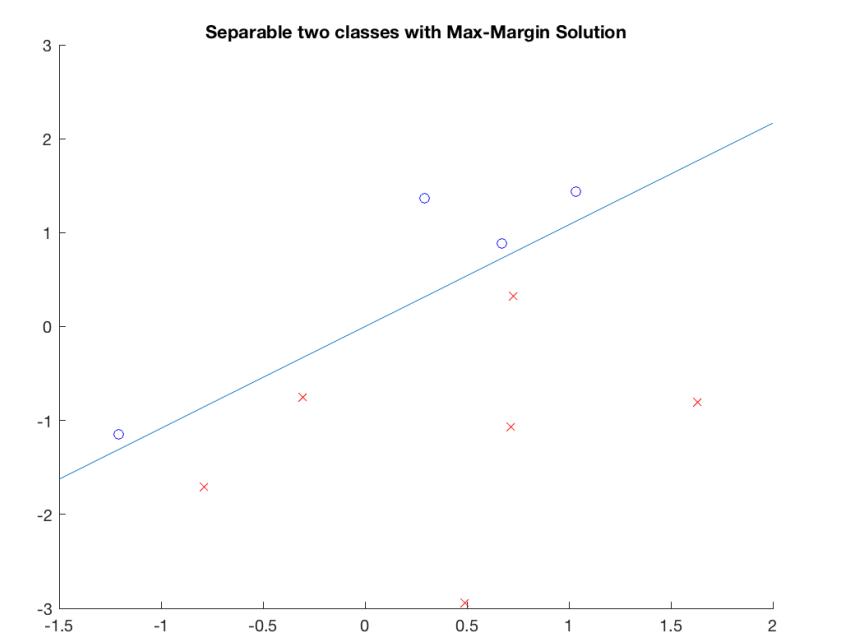
# Support Vector Machine (Max-Margin Classifier)



Vladimir Vapnik, 1994

$$\text{minimize}_{\beta_0, \beta_1, \dots, \beta_p} \|\beta\|^2 := \sum_j \beta_j^2$$

subject to  $y_i(\beta_0 + \beta_1 x_{i1} + \dots + \beta_p x_{ip}) \geq 1$  for all  $i$



Convex optimization + Reproducing Kernel Hilbert Spaces (Grace Wahba etc.)

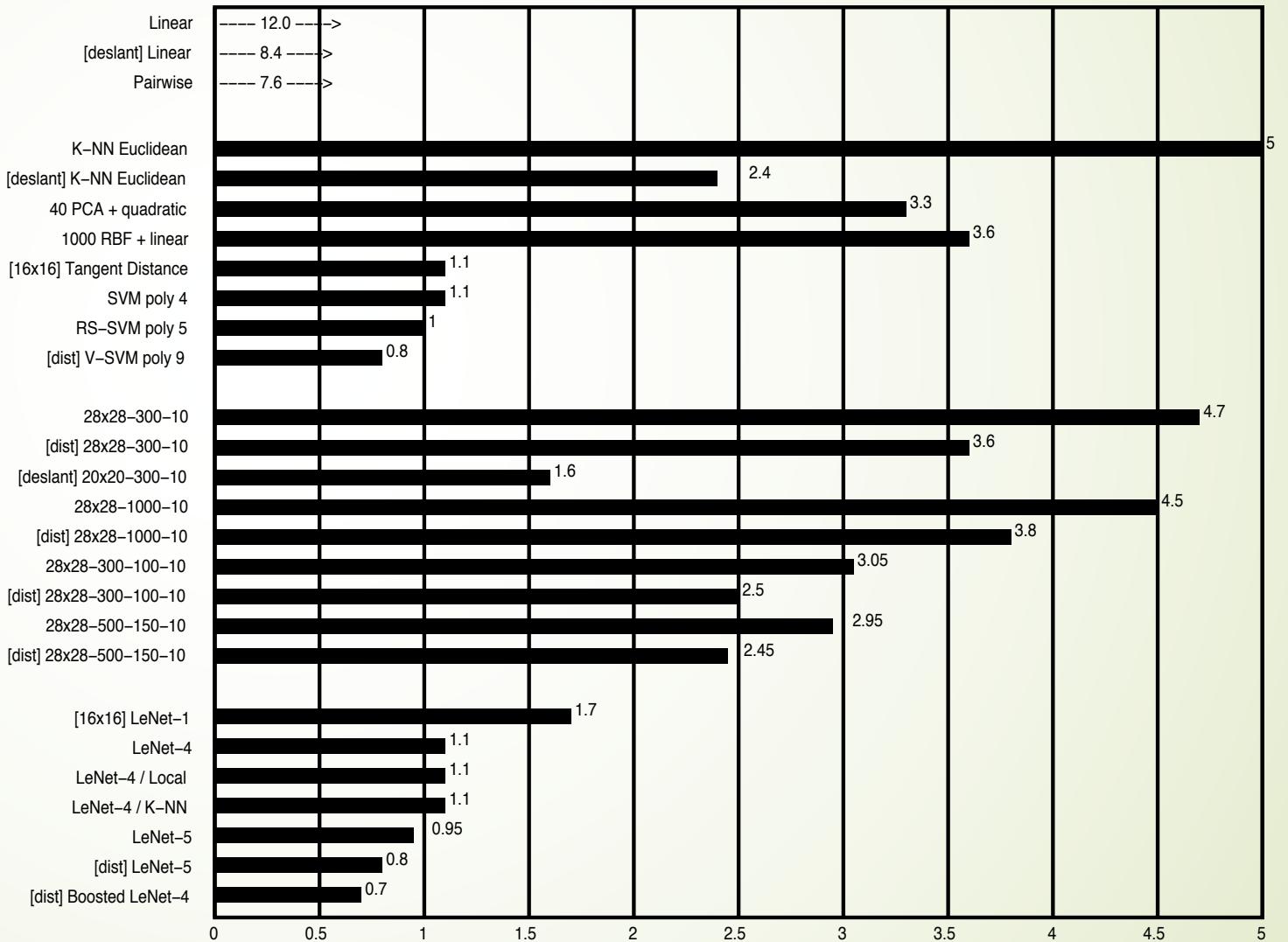
# MNIST Challenge Test Error: SVM vs. CNN

## LeCun et al. 1998



Simple SVM performs as well as Multilayer Convolutional Neural Networks which need careful tuning (LeNets)

Second dark era for NN:  
2000s



# LeNet

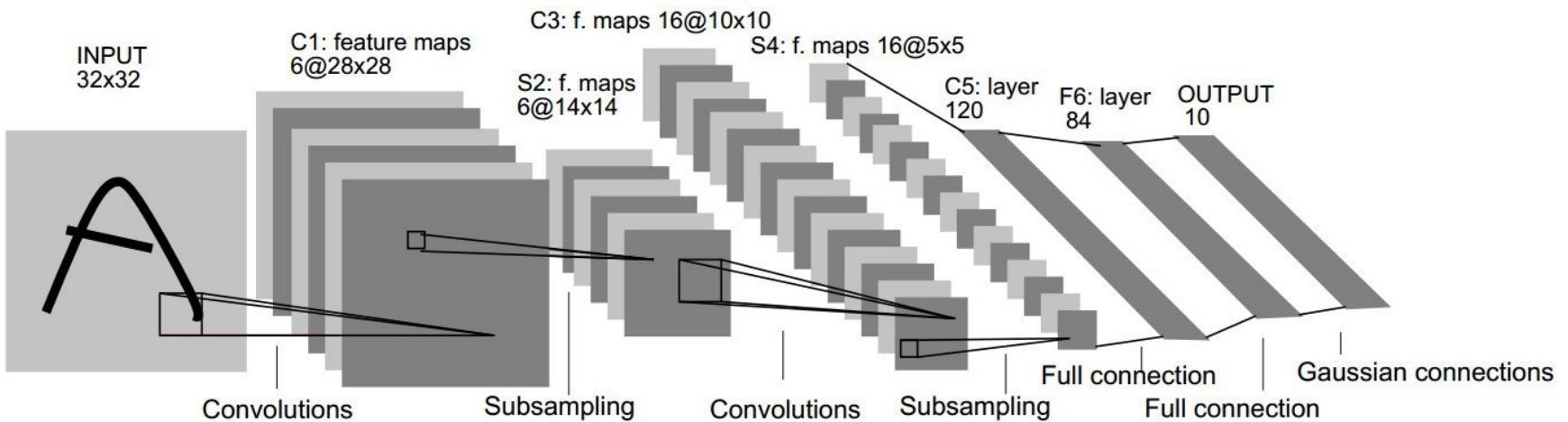


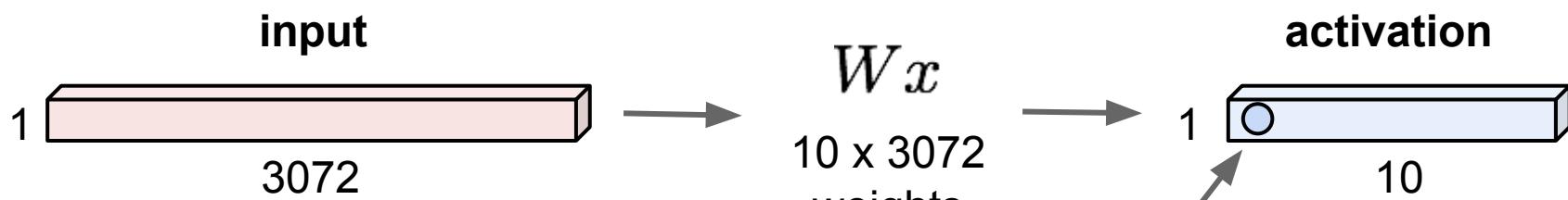
Fig. 2. Architecture of LeNet-5, a Convolutional Neural Network, here for digits recognition. Each plane is a feature map, i.e. a set of units whose weights are constrained to be identical.

<http://blog.csdn.net/Chenyukuai6625>

- **Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner.** Gradient-based learning applied to document recognition. *Proceedings of the IEEE*, november 1998.

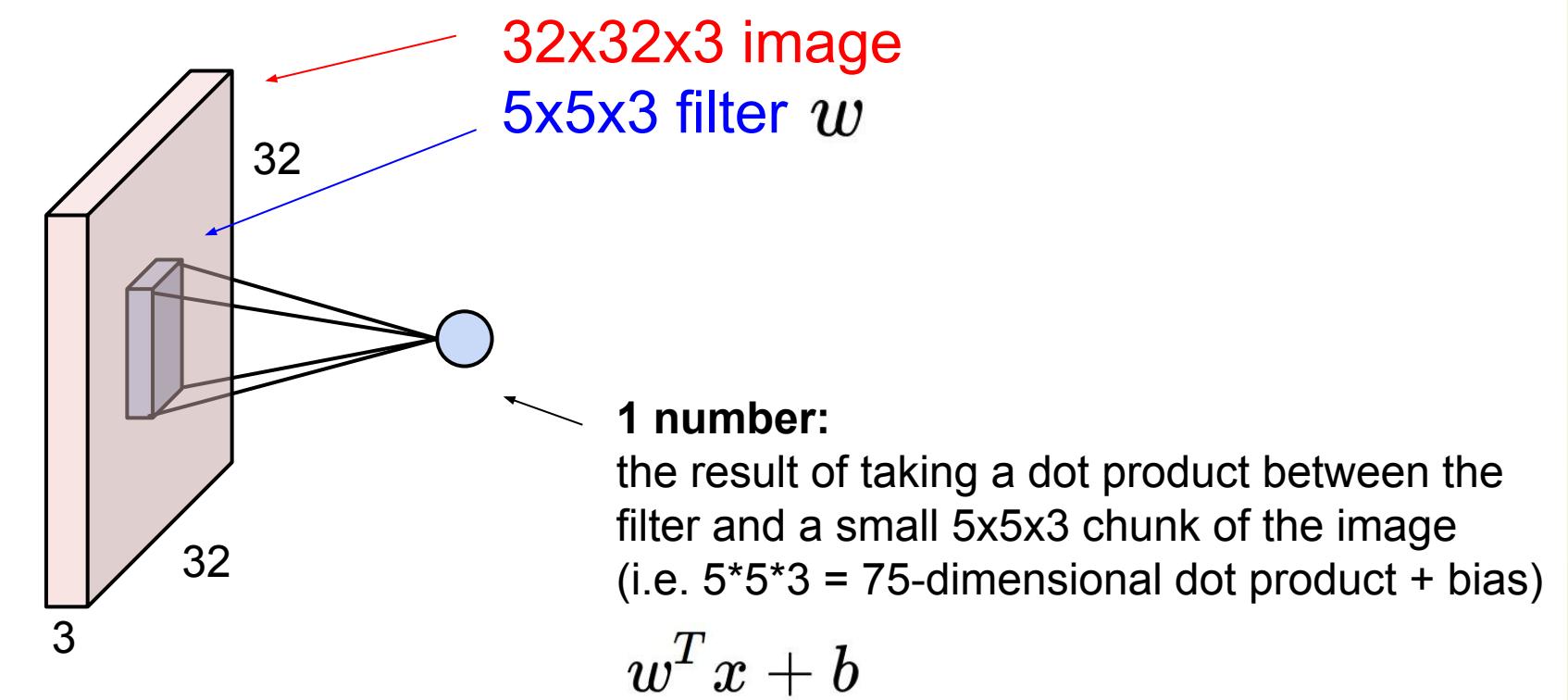
# Fully Connected Layer

32x32x3 image -> stretch to 3072 x 1

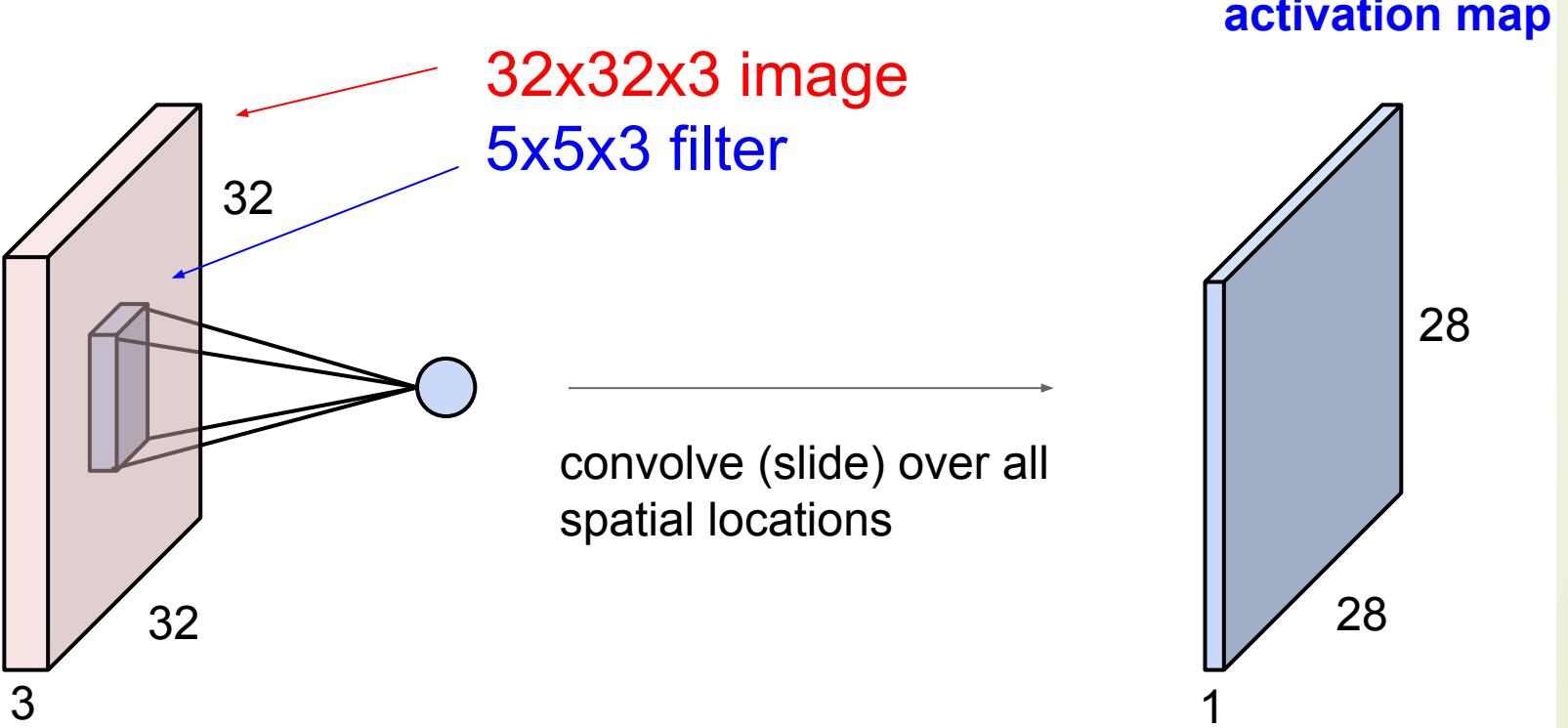


**1 number:**  
the result of taking a dot product  
between a row of  $W$  and the input  
(a 3072-dimensional dot product)

# Convolution



# Convolution Layer: a first (blue) filter

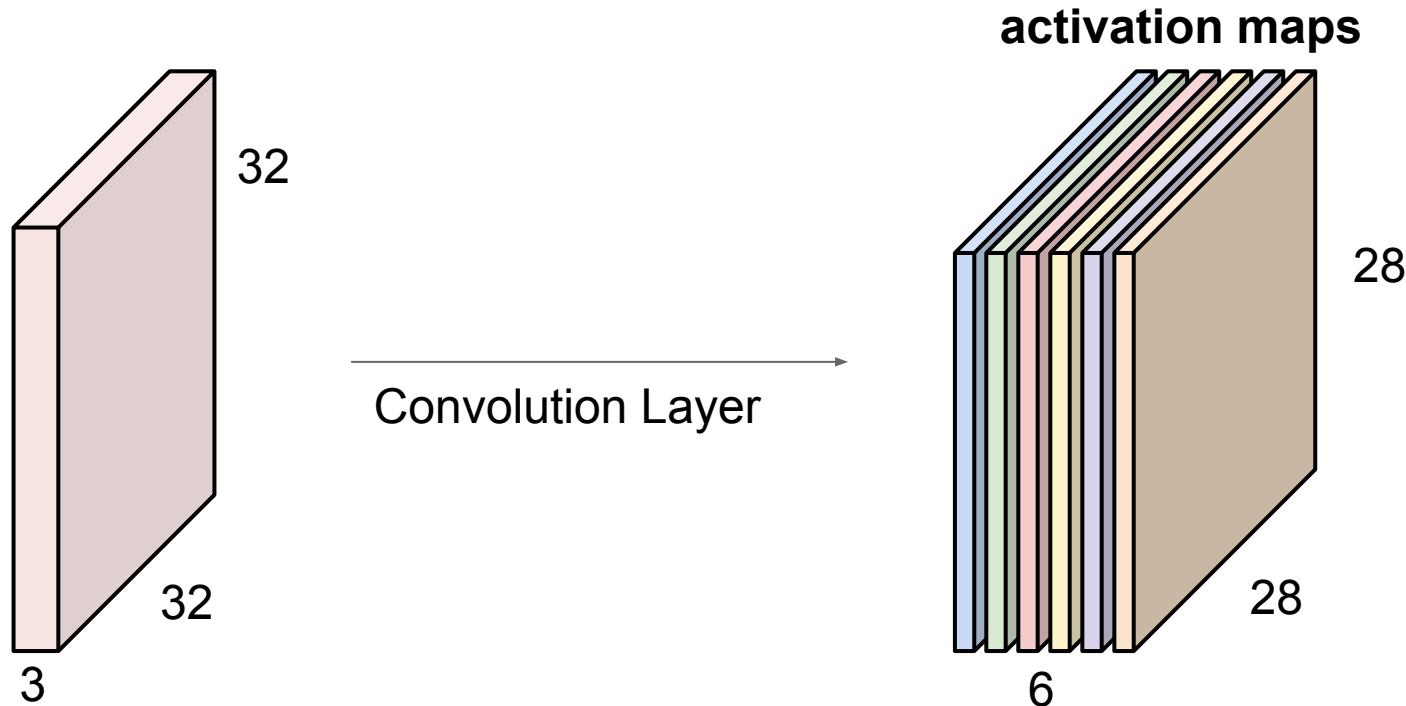


# Convolution Layer: a second (green) filter



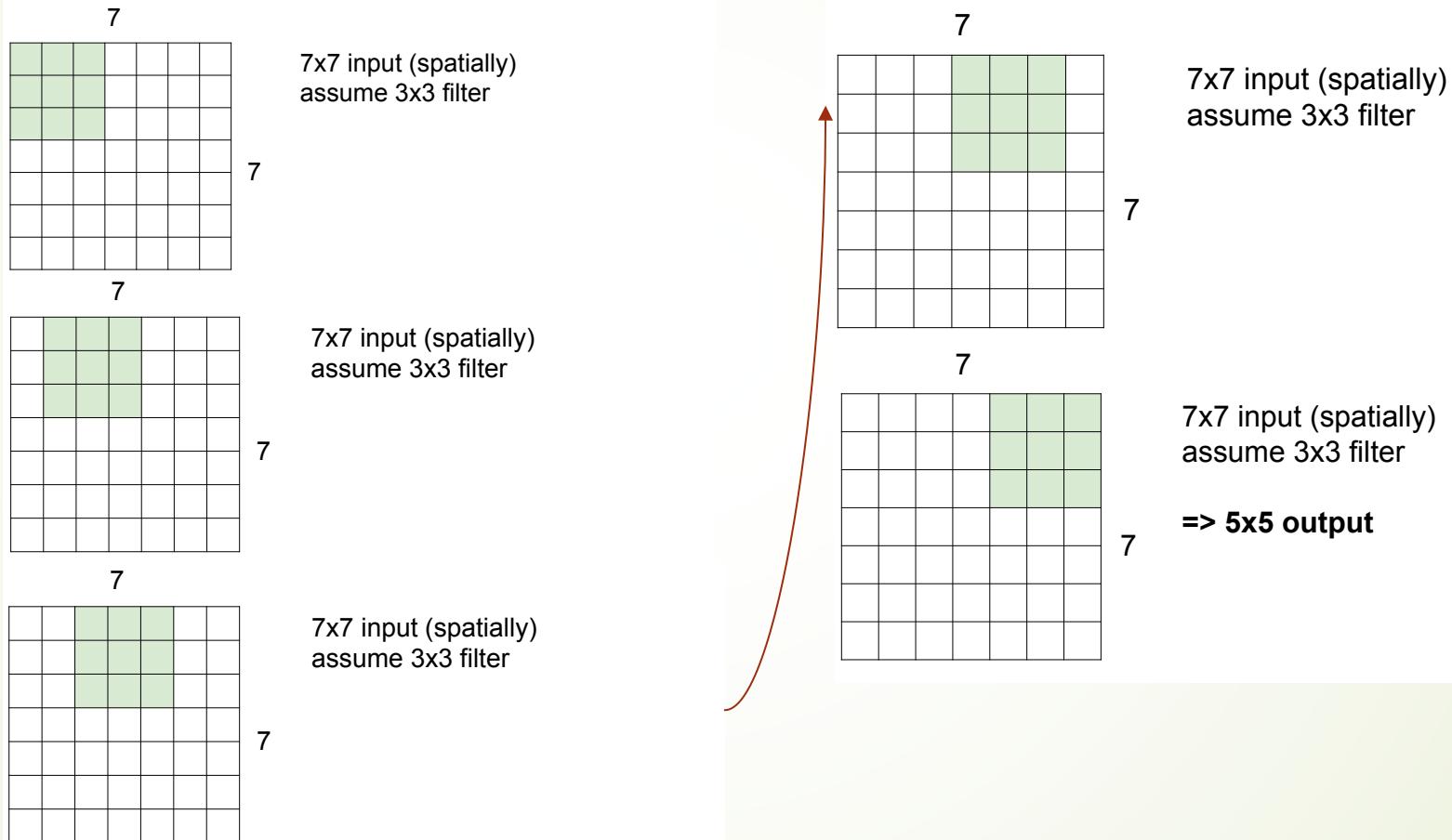
# Convolution Layer

For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:

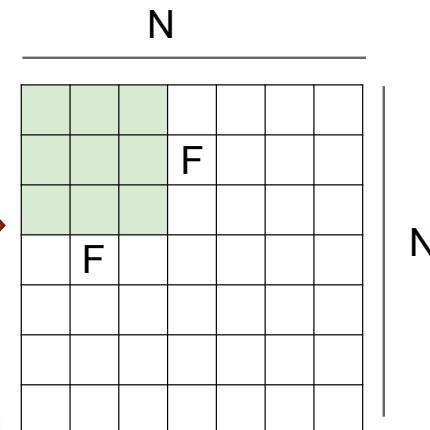
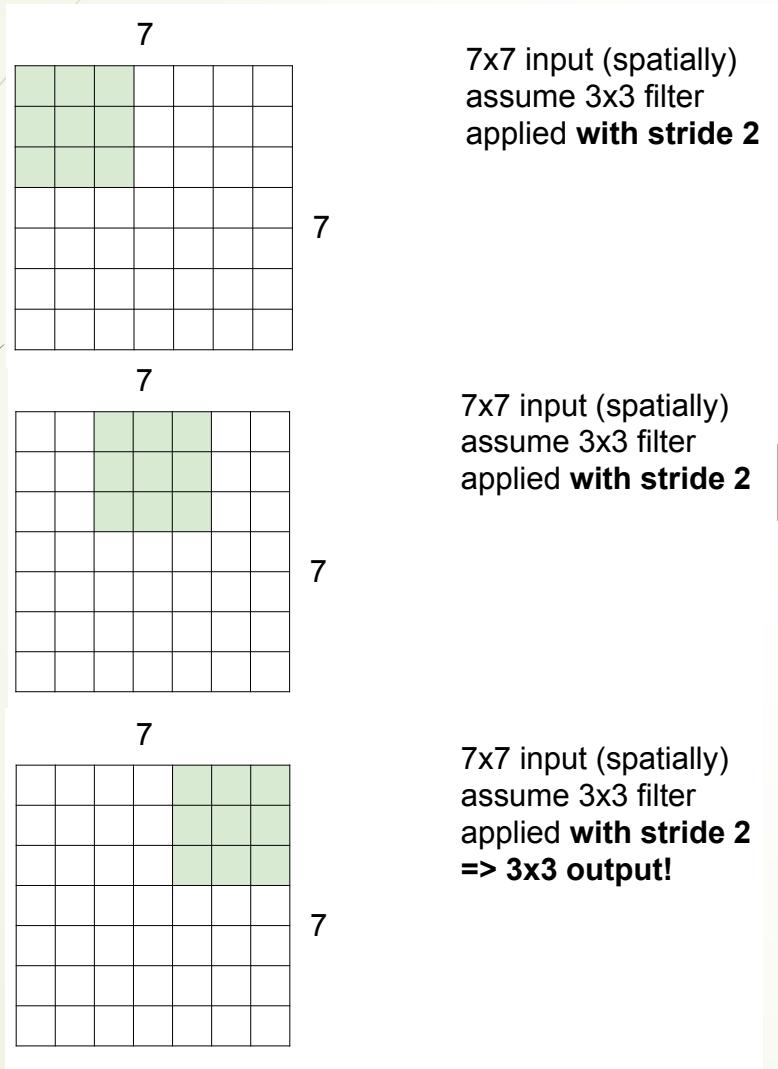


We stack these up to get a “new image” of size  $28 \times 28 \times 6$ !

# A Closer Look at Convolution: stride=1



# A Closer Look at Convolution: stride=2



Output size:  
**(N - F) / stride + 1**

e.g. N = 7, F = 3:  
stride 1 =>  $(7 - 3)/1 + 1 = 5$   
stride 2 =>  $(7 - 3)/2 + 1 = 3$   
stride 3 =>  $(7 - 3)/3 + 1 = 2.33 \vdots$

# A Closer Look at Convolution: Padding

0	0	0	0	0	0			
0								
0								
0								
0								

e.g. input 7x7

**3x3 filter, applied with stride 1**

**pad with 1 pixel border => what is the output?**

**7x7 output!**

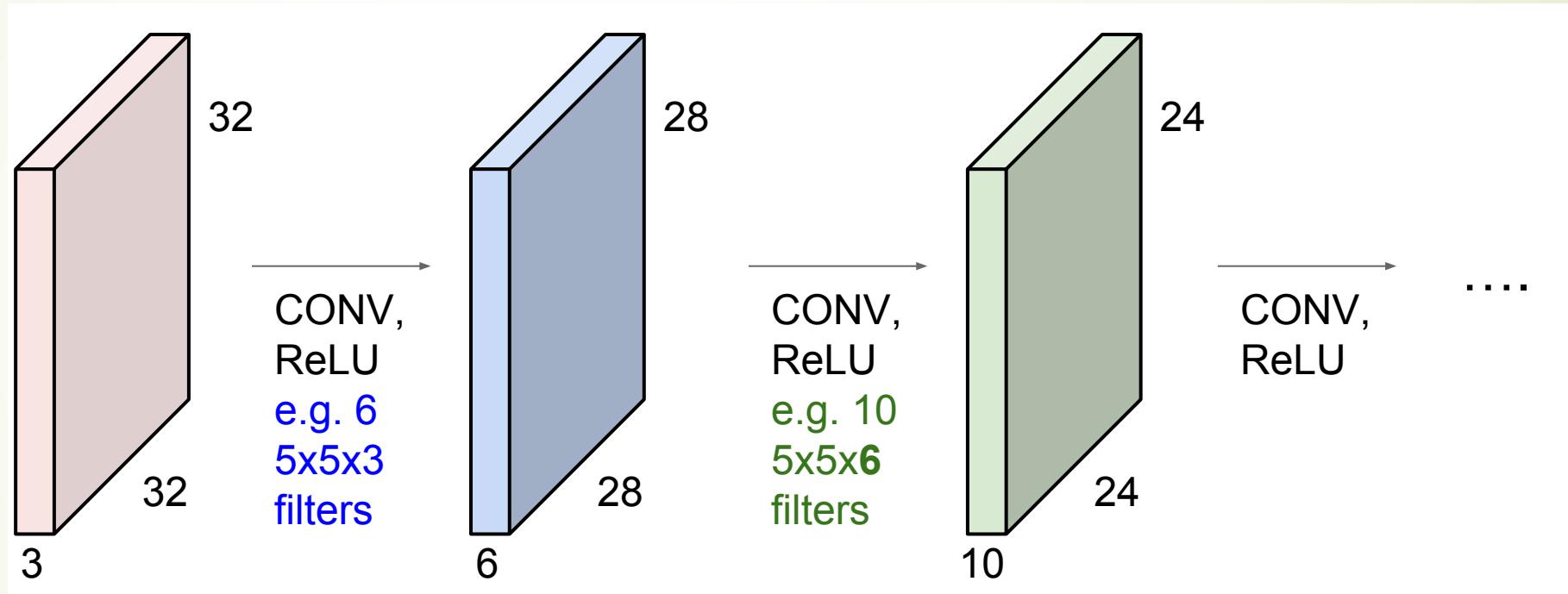
in general, common to see CONV layers with stride 1, filters of size FxF, and zero-padding with  $(F-1)/2$ . (will preserve size spatially)

e.g.  $F = 3 \Rightarrow$  zero pad with 1

$F = 5 \Rightarrow$  zero pad with 2

$F = 7 \Rightarrow$  zero pad with 3

# ConvNet:



Stride = 1  
Padding = 0

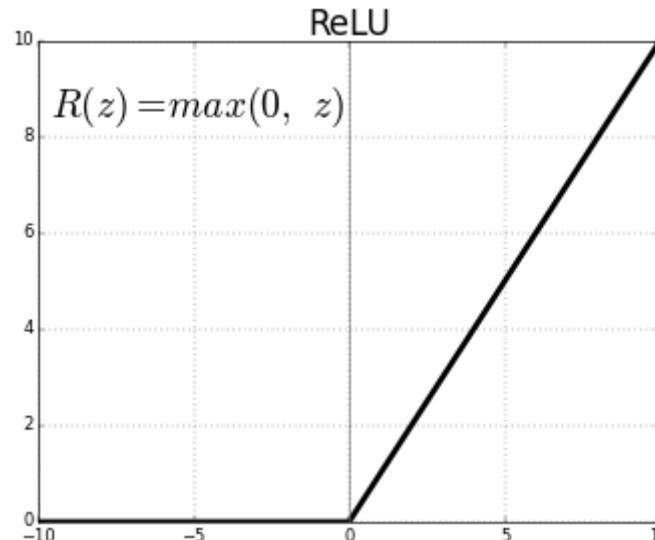
# Formula: `NewImageSize = floor((ImageSize - Filter + 2*Padding)/Stride + 1)`

**Summary.** To summarize, the Conv Layer:

- Accepts a volume of size  $W_1 \times H_1 \times D_1$
- Requires four hyperparameters:
  - Number of filters  $K$ ,
  - their spatial extent  $F$ ,
  - the stride  $S$ ,
  - the amount of zero padding  $P$ .
- Produces a volume of size  $W_2 \times H_2 \times D_2$  where:
  - $W_2 = (W_1 - F + 2P)/S + 1$
  - $H_2 = (H_1 - F + 2P)/S + 1$  (i.e. width and height are computed equally by symmetry)
  - $D_2 = K$
- With parameter sharing, it introduces  $F \cdot F \cdot D_1$  weights per filter, for a total of  $(F \cdot F \cdot D_1) \cdot K$  weights and  $K$  biases.
- In the output volume, the  $d$ -th depth slice (of size  $W_2 \times H_2$ ) is the result of performing a valid convolution of the  $d$ -th filter over the input volume with a stride of  $S$ , and then offset by  $d$ -th bias.

# ReLU

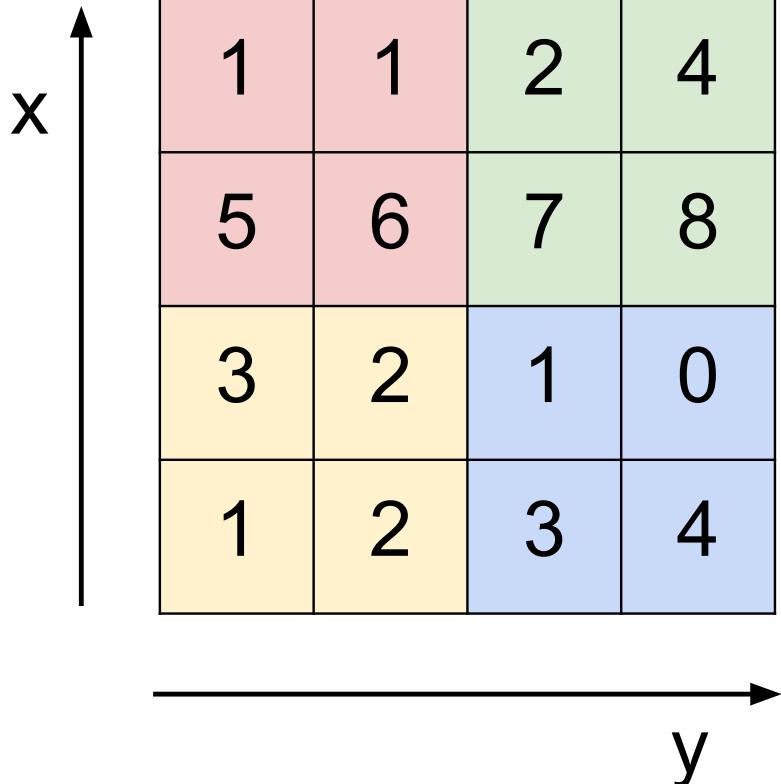
- Non-saturating function and therefore faster convergence when compared to other nonlinearities
- Problem of dying neurons



Source: [https://ml4a.github.io/ml4a/neural\\_networks/](https://ml4a.github.io/ml4a/neural_networks/)

# Max Pooling

Single depth slice



max pool with 2x2 filters  
and stride 2

The result of the max pooling operation is a 2x2 output tensor:

6	8
3	4

# 2000-2010: The Era of SVM, Boosting, ... as nights of Neural Networks



# Restricted Boltzman Machine (Deep Learning)

- ▶ Hinton and Salakhutdinov,  
Reducing the Dimensionality of  
Data with Neural Networks,  
**Science**, 2006
- ▶ Reinvigorating research in Deep  
Learning
- ▶ Shows importance of pretraining

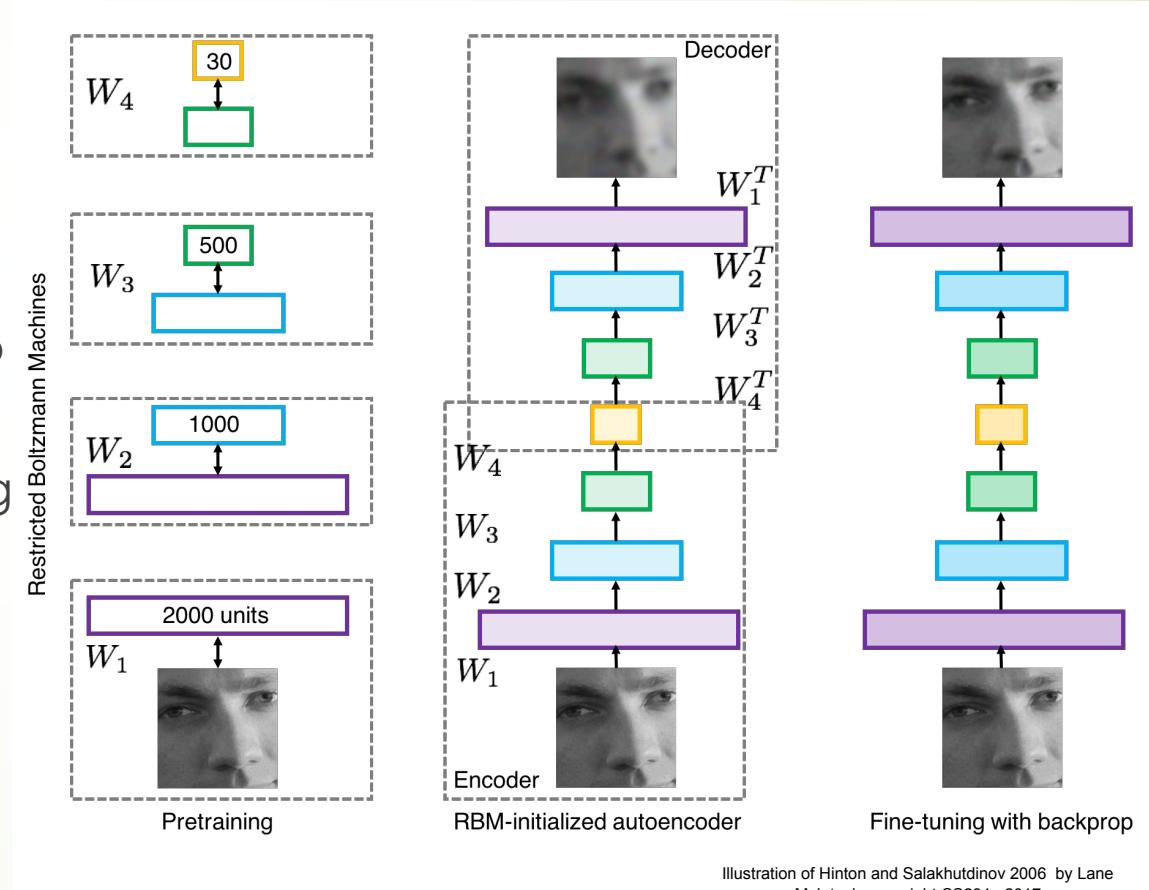
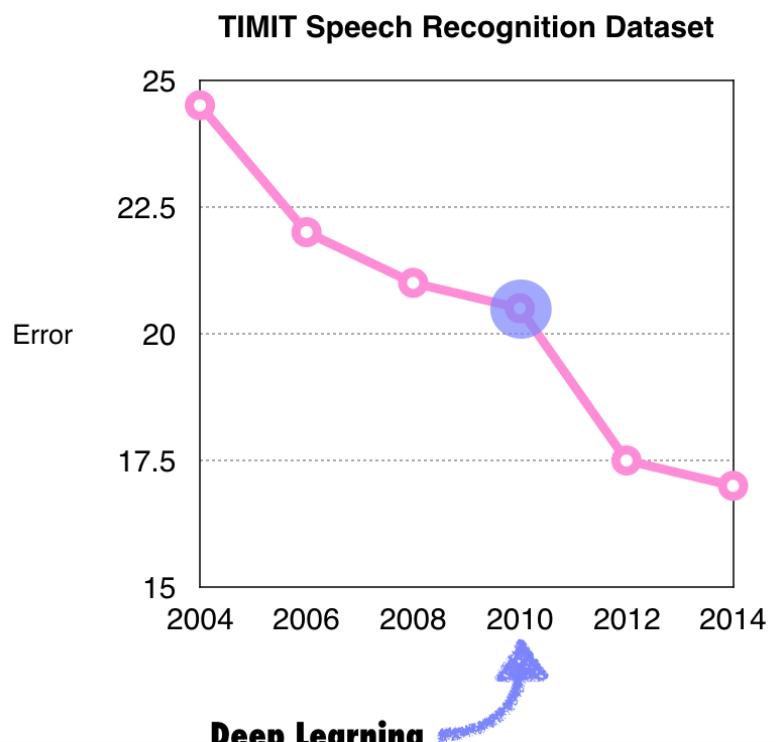


Illustration of Hinton and Salakhutdinov 2006 by Lane  
McIntosh, copyright CS231n 2017

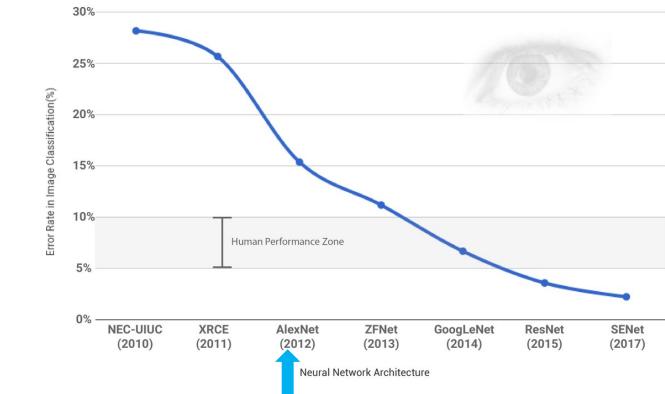
# Around the year of 2012...

## Speech Recognition: TIMIT



## Computer Vision: ImageNet

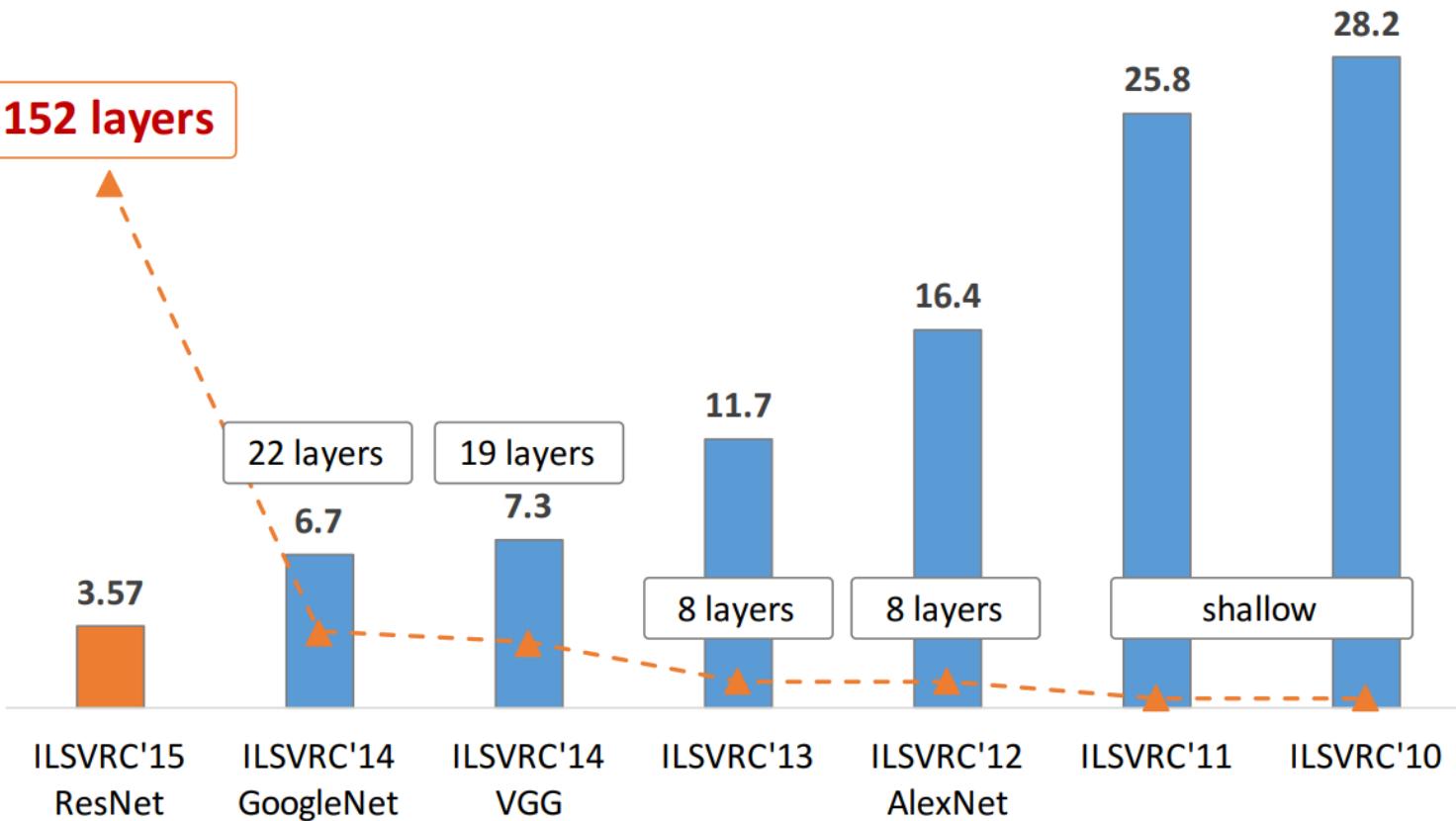
- ImageNet (subset):
  - 1.2 million training images
  - 100,000 test images
  - 1000 classes
- ImageNet large-scale visual recognition Challenge



source: <https://www.linkedin.com/pulse/must-read-path-breaking-papers-image-classification-muktabh-mayank>

Deep Learning

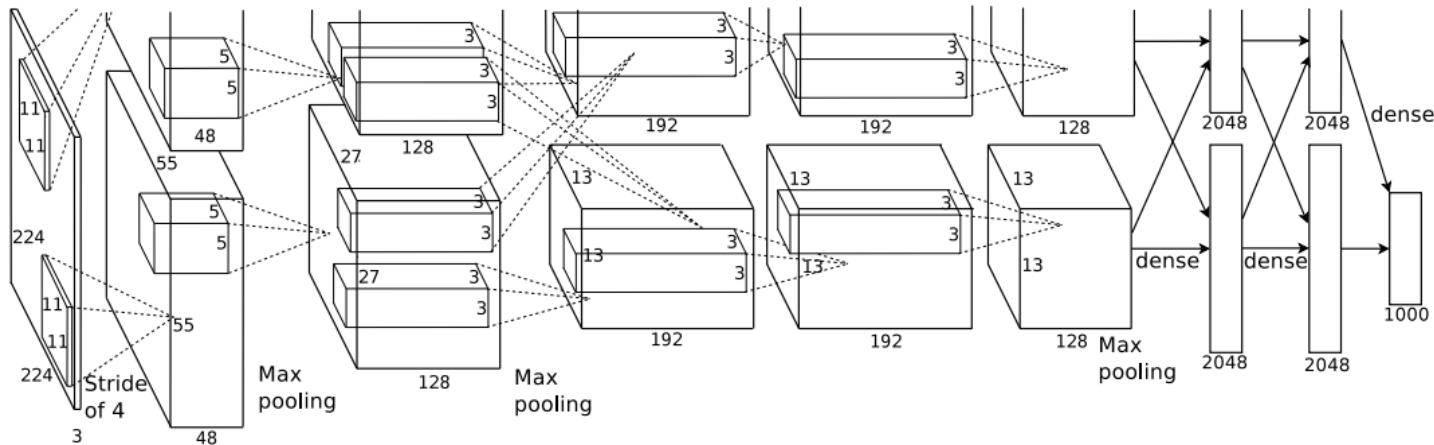
# Depth as function of year



[He et al., 2016]

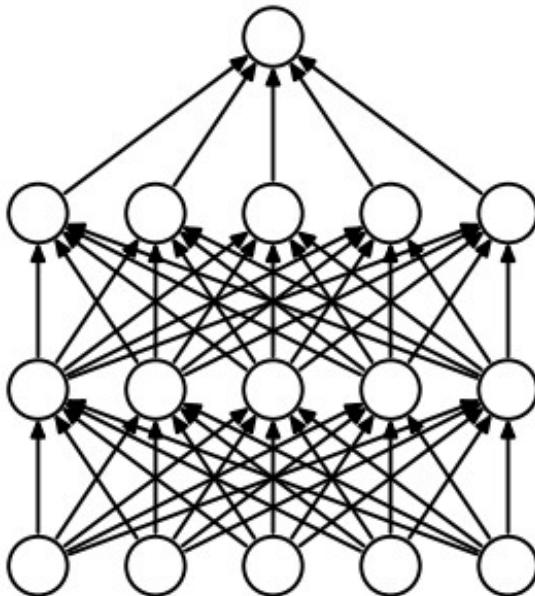
# AlexNet (2012): Architecture

- 8 layers: first 5 convolutional, rest fully connected
- ReLU nonlinearity
- Local response normalization
- Max-pooling
- Dropout

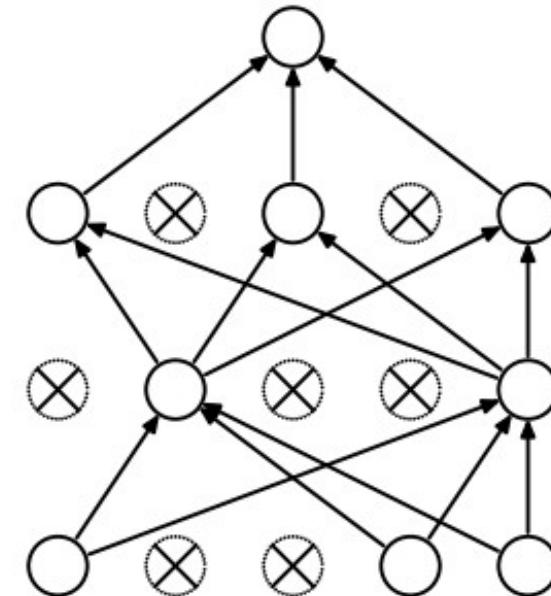


Source: [Krizhevsky et al., 2012]

# AlexNet (2012): Dropout



(a) Standard Neural Net



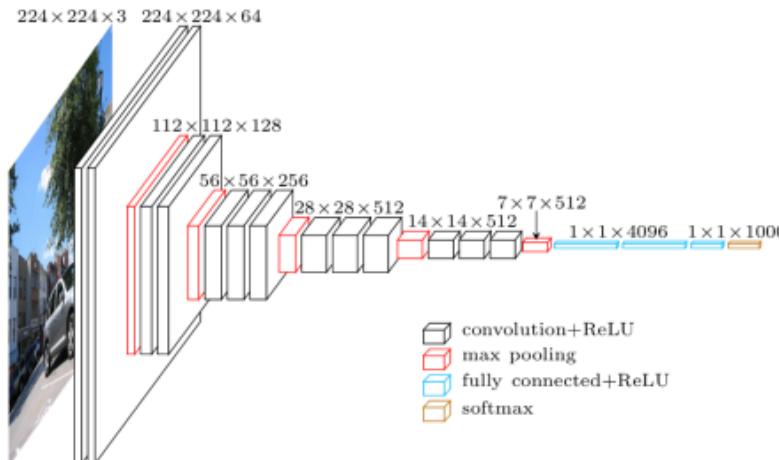
(b) After applying dropout.

Source: [Srivastava et al., 2014]

- Zero every neuron with probability  $1 - p$
- At test time, multiply every neuron by  $p$

# VGG (2014) [Simonyan-Zisserman'14]

- Deeper than AlexNet: 11-19 layers versus 8
- No local response normalization
- Number of filters multiplied by two every few layers
- Spatial extent of filters  $3 \times 3$  in all layers
- Instead of  $7 \times 7$  filters, use three layers of  $3 \times 3$  filters
  - Gain intermediate nonlinearity
  - Impose a regularization on the  $7 \times 7$  filters

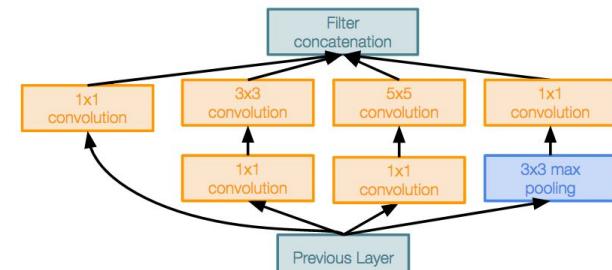


Stanford University

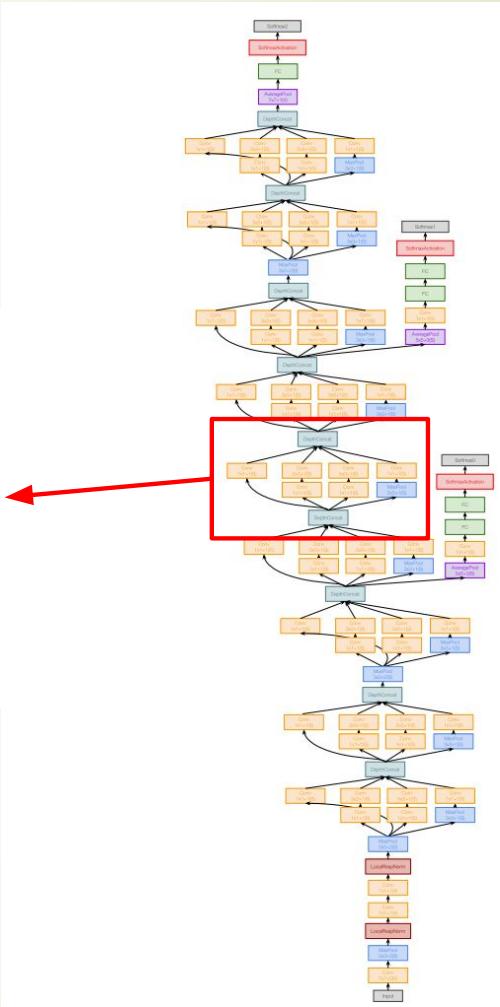
Source: <https://blog.heuritech.com/2016/02/29/>

# GoogLeNet [Szegedy et al., 2014]

- ▶ 22 layers
- ▶ Efficient “Inception” module
- ▶ No FC layers
- ▶ Only 5 million parameters!
- ▶ 12x less than AlexNet
- ▶ ILSVRC’14 classification winner  
(6.7% top 5 error)

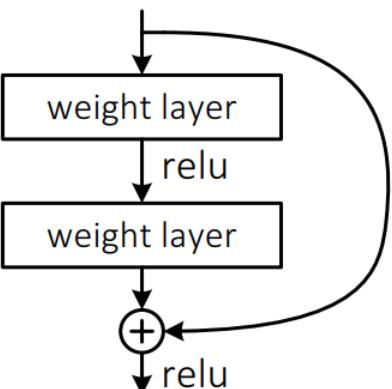


Inception module

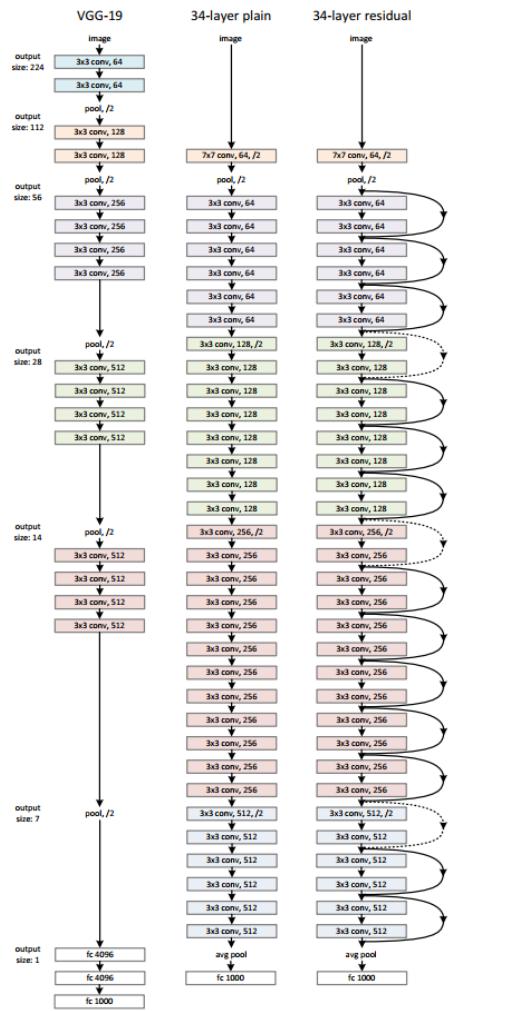


# ResNet (2015) [HGRS-15]

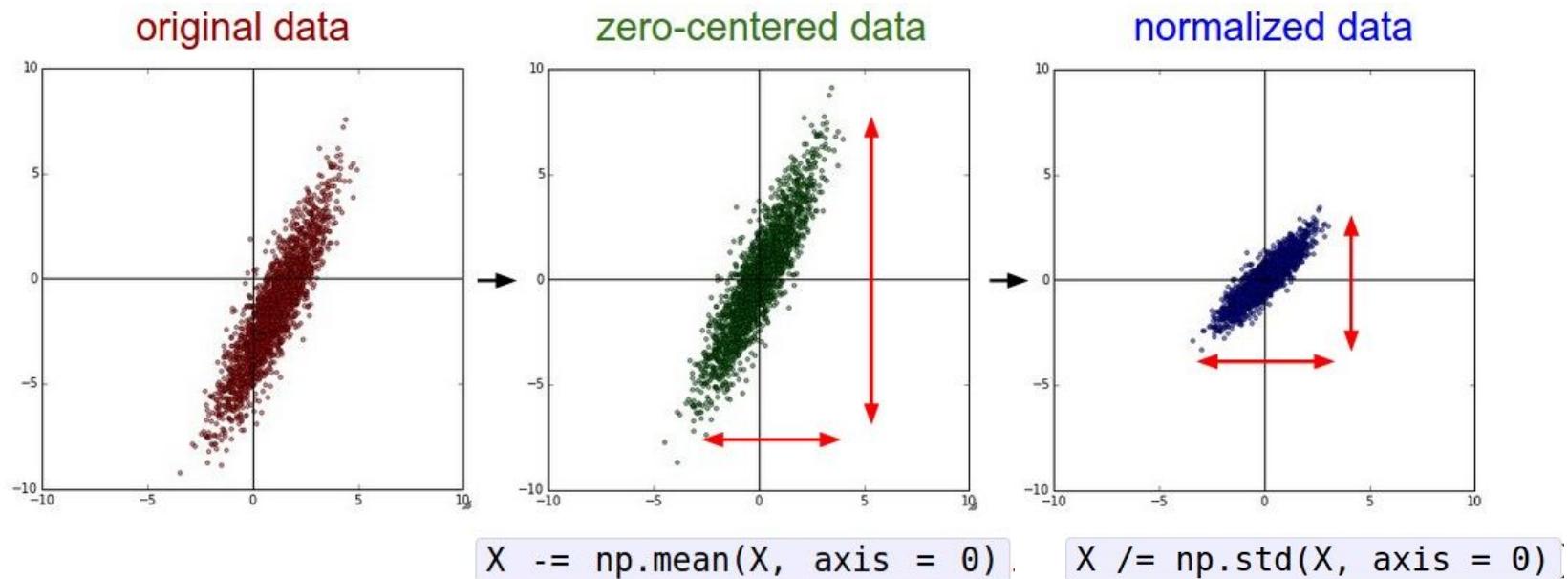
- Solves problem by adding skip connections
  - Very deep: 152 layers
  - No dropout
  - Stride
  - Batch normalization



Source: Deep Residual Learning for Image Recognition



# Batch Normalization



(Assume  $X$  [NxD] is data matrix,  
each example in a row)

# Batch Normalization

---

**Algorithm 2** Batch normalization [Ioffe and Szegedy, 2015]

**Input:** Values of  $x$  over minibatch  $x_1 \dots x_B$ , where  $x$  is a certain channel in a certain feature vector

**Output:** Normalized, scaled and shifted values  $y_1 \dots y_B$

$$1: \mu = \frac{1}{B} \sum_{b=1}^B x_b$$

$$2: \sigma^2 = \frac{1}{B} \sum_{b=1}^B (x_b - \mu)^2$$

$$3: \hat{x}_b = \frac{x_b - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

$$4: y_b = \gamma \hat{x}_b + \beta$$

---

- Accelerates training and makes initialization less sensitive
- Zero mean and unit variance feature vectors

# BatchNorm at Test

**Input:** Values of  $x$  over a mini-batch:  $\mathcal{B} = \{x_1 \dots m\}$ ;  
Parameters to be learned:  $\gamma, \beta$

**Output:**  $\{y_i = \text{BN}_{\gamma, \beta}(x_i)\}$

$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^m x_i \quad // \text{mini-batch mean}$$

$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2 \quad // \text{mini-batch variance}$$

$$\hat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}} \quad // \text{normalize}$$

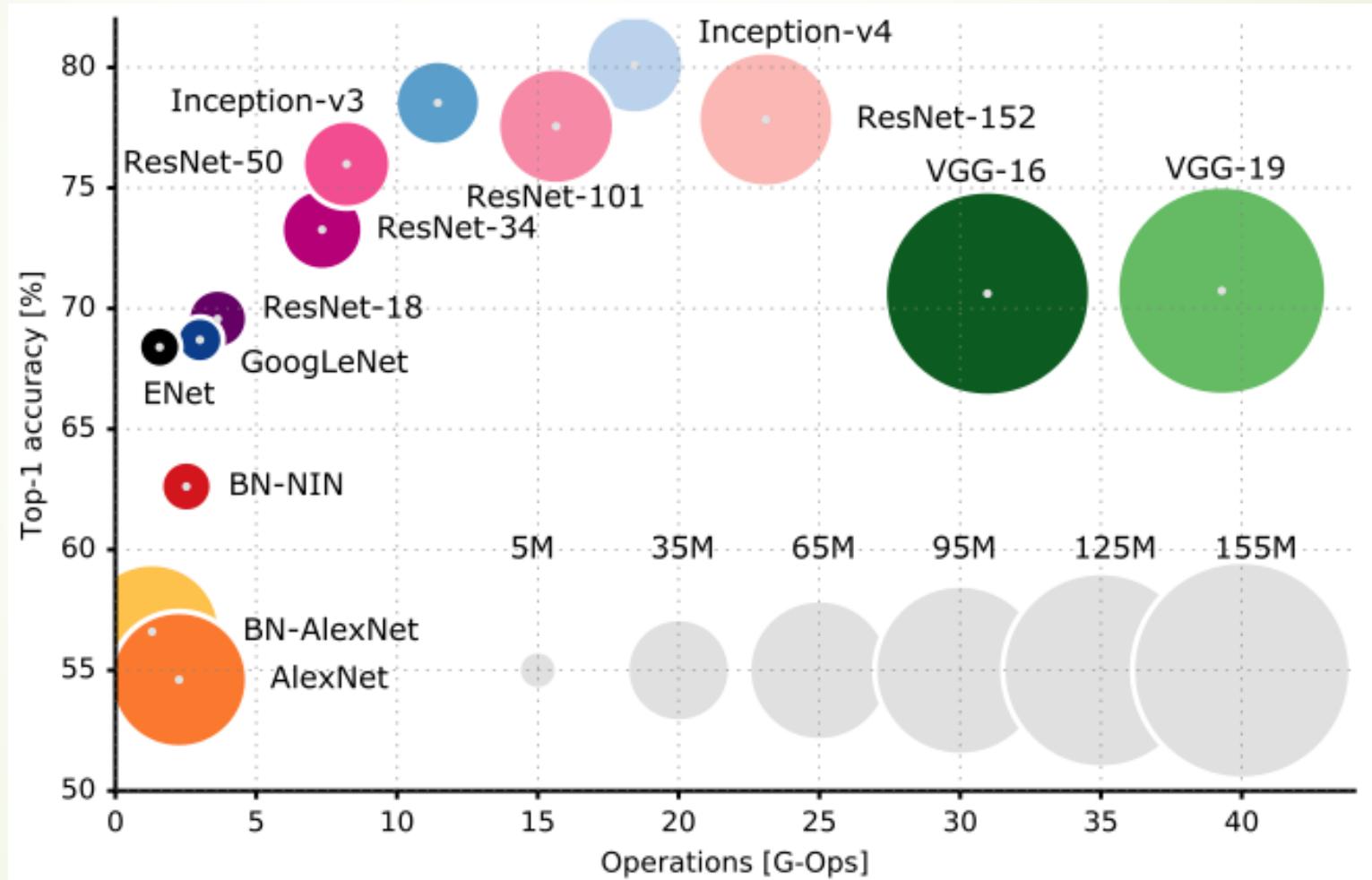
$$y_i \leftarrow \gamma \hat{x}_i + \beta \equiv \text{BN}_{\gamma, \beta}(x_i) \quad // \text{scale and shift}$$

**Note: at test time BatchNorm layer functions differently:**

The mean/std are not computed based on the batch. Instead, a single fixed empirical mean of activations during training is used.

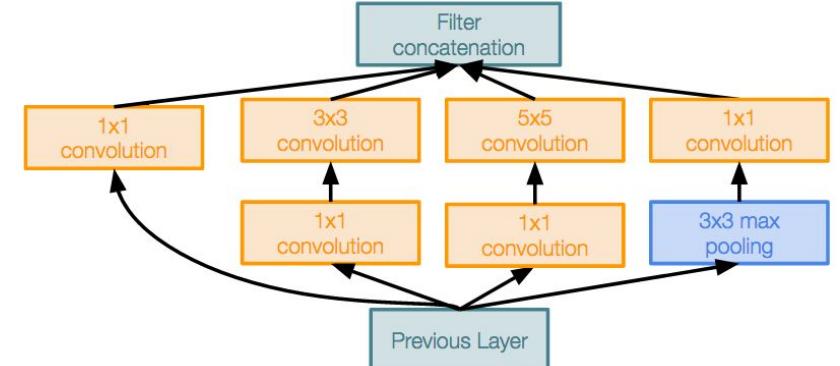
(e.g. can be estimated during training with running averages)

# Complexity vs. Accuracy of Different Networks

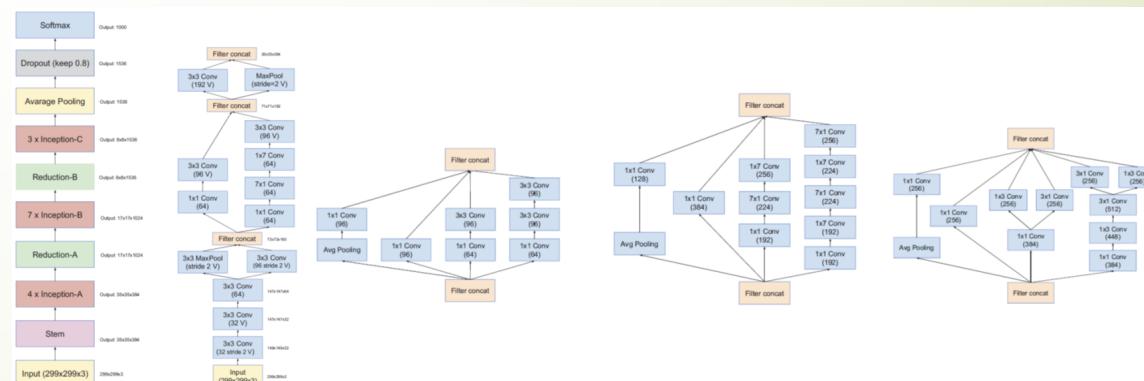


# Inception-v4 = ResNet + Inception

- ▶ “Inception” module:
  - ▶ Introduced by Szegedy et al., 2014 in **GoogLeNet**
  - ▶ ILSVRC’14 classification winner (6.7% top 5 error)
- ▶ Apply parallel filter operations on the input from previous layer:
  - ▶ Dimensionality reduction ( $1 \times 1$  conv)
  - ▶ Multiple receptive field sizes for convolution ( $1 \times 1$ ,  $3 \times 3$ ,  $5 \times 5$ )
  - ▶ Pooling operation ( $3 \times 3$ )
- ▶ Concatenate all filter outputs together depth-wise



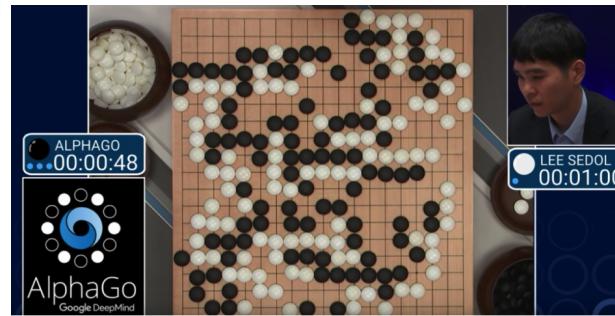
Inception module



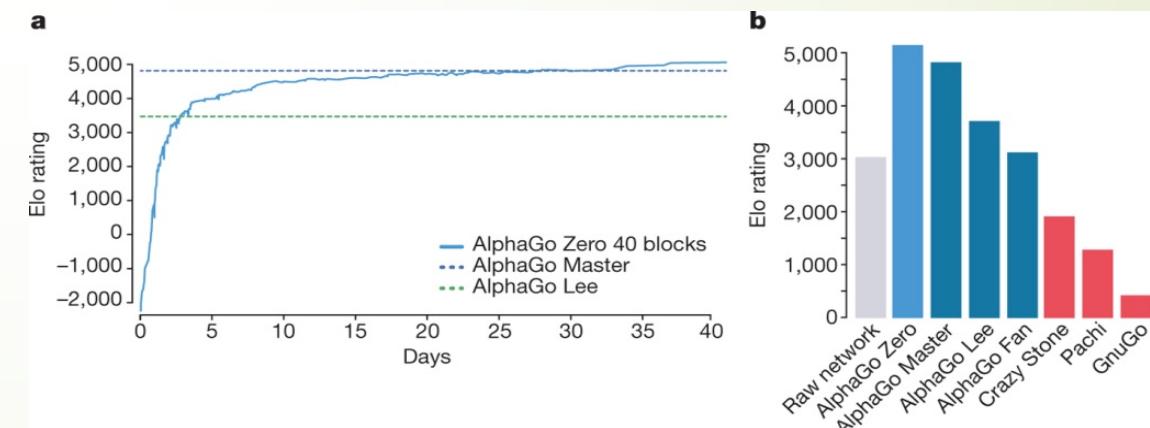
# Reaching Human Performance Level in Games



Deep Blue in 1997

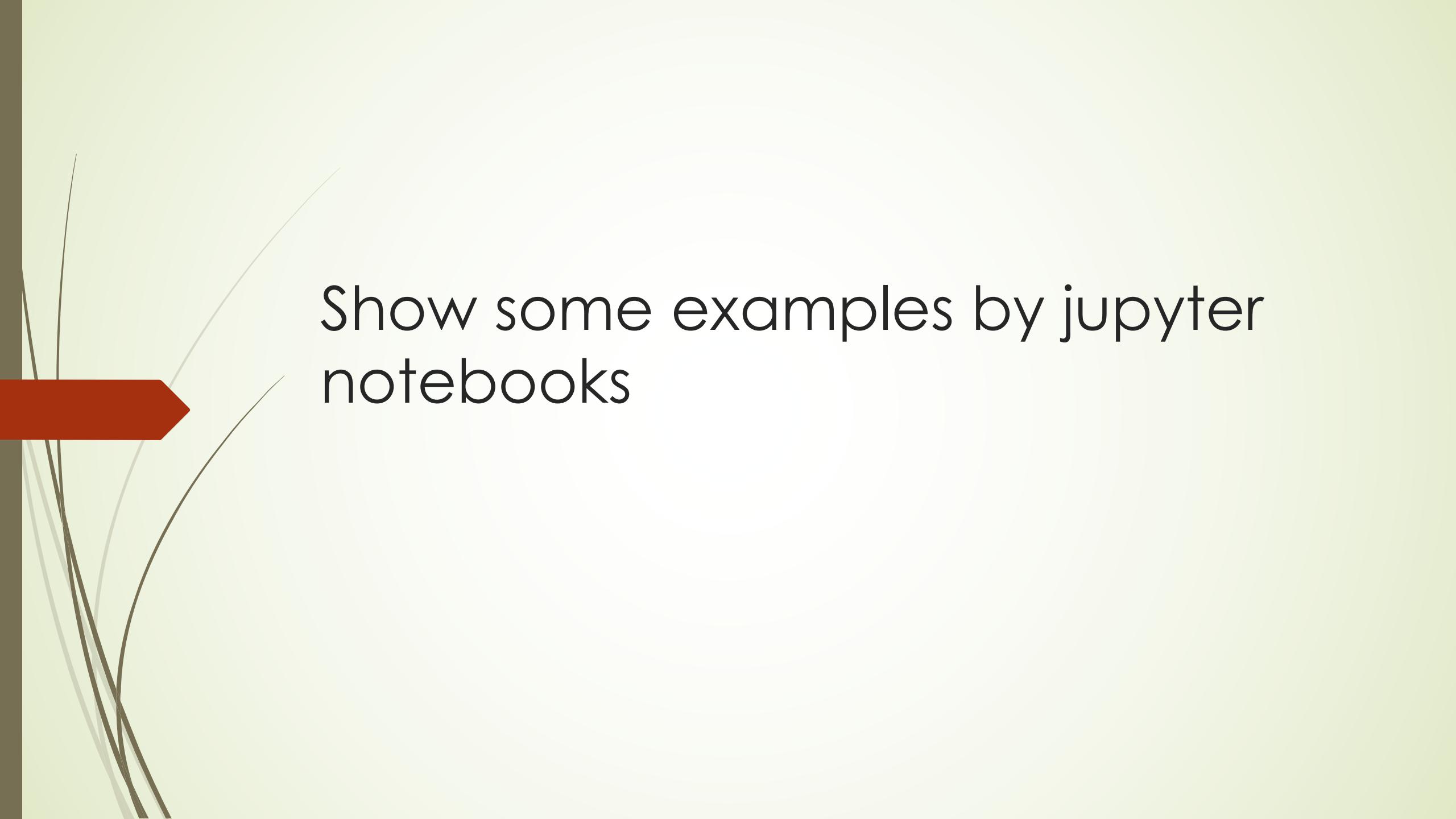


AlphaGo “LEE” 2016: Monte-Carlo Tree Pruning Search+CNN



# Deep Learning Softwares

- ▶ **Pytorch** (developed by Yann LeCun and Facebook):
  - ▶ <http://pytorch.org/tutorials/>
- ▶ Tensorflow (developed by Google based on Caffe)
  - ▶ <https://www.tensorflow.org/tutorials/>
- ▶ Theano (developed by Yoshua Bengio)
  - ▶ <http://deeplearning.net/software/theano/tutorial/>
- ▶ **Keras (based on Tensorflow or Pytorch)**
  - ▶ [https://www.manning.com/books/deep-learning-with-python?a\\_aid=keras&a\\_bid=76564dff](https://www.manning.com/books/deep-learning-with-python?a_aid=keras&a_bid=76564dff)



Show some examples by jupyter  
notebooks

Thank you!

