Package 'GFLassoInference'

September 21, 2021

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Title Powerful Graph Fused Lasso Inference	
Version 1.0	
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Description An implementation of powerful selective inference for graph fused lasso as described in Chen et al. (2021+)	
License GPL-3	
Depends R (>= 3.5)	
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fusedlasso_inf More powerful test for the graph fused lasso	
Description	

This functions tests the null hypothesis of no difference in means between connected components c1 and c2 of the output of the graph fused lasso solution. The ordering are numbered as per the results of the fusedlasso function in the genlasso package.

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Usage

```
fusedlasso_inf(
   y,
   D,
   c1,
   c2,
   method,
   sigma,
   K = NULL,
   L = NULL,
   early_stop = NULL,
   compute_ci = FALSE,
   alpha_level = 0.05
)
```

Arguments

у	Numeric vector; n dimensional observed data
D	Numeric matrix; m by n penalty matrix, i.e., the oriented incidence matrix over the underlying graph
c1, c2	Integers selecting the two connected components to test, as indexed by the results of genlasso::fusedlasso.
method	One of "K" or "CC", which indicates which conditioning set to use
sigma	Numeric; noise standard deviation for the observed data, a non-negative number.
K	Integer; number of steps to run the dual-path algorithm. It must be specified if method=="K".
L	Integer; the targeted number of connected components. It must be specified if method=="CC".
early_stop	Numeric; specify when the truncation set computation should be terminated. The default is NULL, which indicates infinity.
compute_ci	Logical; the default is False. Specifying whether confidence intervals for $\nu^T \beta$, the difference in means between the two estimated connected components, should be computed.
alpha_level	Numeric; parameter for the 1-alpha_level confidence interval, defeault to 0.05

Details

Currently, we support two different conditioning sets: conditioning set 1 is based on the output after K steps dual-path algorithm; and conditioning set 2 is based on the output of the after the dual-path algorithm yields c connected components in the output.

Input

Consider the generative model $Y_j=\beta_j+\epsilon_j,\epsilon_j\sim N(0,\sigma^2).j=1,...,n$, where the underlying signal β is assumed to be piecewise constant with respect to an underlying graph. The fused lasso estimate minimizes the following objective function

$$minimize_{\beta} \frac{1}{2} \sum_{j=1}^{n} (y_j - \beta_j)^2 + \lambda \sum_{(i,j) \in E} |\beta_i - \beta_j|,$$

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where E is the edge set of the underlying graph. The solution $\hat{\beta}$ can then be segment into connected components; that is, the set of $\hat{\beta}$ that takes on the same value, and are connected in the original graph.

Now suppose we want to test whether the means of two estimated connected components c1 and c2 are equal; or equivalently, the null hypothesis of the form $H_0: \nu^T \beta = 0$ versus $H_1: \nu^T \beta \neq 0$ for suitably chosen ν .

This function computes the following p-value:

$$P(|\nu^T Y| \ge |\nu^T y| \mid \hat{C}_1, \hat{C}_2 \in CC_K(Y), \Pi_{\nu}^{\perp} Y = \Pi_{\nu}^{\perp} y),$$

where $CC_K(Y)$ is the set of estimated connected components from applying K steps of the dual path algorithm on data Y, and Π_{ν}^{\perp} is the orthogonal projection to the orthogonal complement of ν . In particular, the test based on this p-value controls the selective Type I error and has higher power than an existing method by Hyun et al. (2018). Readers can refer to the Section 3 in Chen et al. (2021+) for more details.

Value

Returns a list with elements:

- pval the p-value in Chen et al. (2021+)
- truncation_set the conditioning set of Chen et al. (2021+) stored as Intervals class
- test_stats test statistics: the difference in means of two connected components
- beta_hat Graph fused lasso estimates
- connected_comp Estimated connected component
- Naive the naive p-value using a z-test
- Hyun the p-value proposed in Hyun et al. (2018)
- hyun_set the conditioning set of Hyun et al. (2018) stored as Intervals class
- CI_result confidence interval of level 1-alpha_level if compute_ci=TRUE

References

Chen YT, Jewell SW, Witten DM. (2021+) More powerful selective inference for the graph fused lasso Hyun S, G'Sell M, Tibshirani RJ. (2018) Exact post-selection inference for the generalized lasso path. Electron J Stat.

Examples

```
lev1 <- 0 # mean for group 1
lev2 <- 3 # mean (absolute value) for group 2/3
sigma <- 1 # level of noise
nn <- 8 # grid size
Dmat <- genlasso::getD2d(nn, nn) # generate D matrix for the 2D fused lasso
### Create the underlying signal
A <- matrix(lev1, ncol=nn, nrow = nn)
A[1:round(nn/3),1:round(nn/3)] <- 1*lev2
A[(nn-2):(nn),(nn-2):(nn)] <- -1*lev2
### Visualize the underlying signal
lattice::levelplot(A)
set.seed(2005)
A.noisy <- A + rnorm(nn^2,mean=0,sd=sigma)
y <- c(t(A.noisy))</pre>
```

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```
### Now use the fusedlasso function to obtain estimated connected components after K=13
### steps of the dual path algorithm
K = 13
complete_sol <- genlasso::fusedlasso(y=y,D=Dmat,maxsteps=K)
beta_hat <- complete_sol$beta[,K]
### estimated connected components
estimated_CC <- complete_sol$pathobjs$i
estimated_CC
### Run a test for a difference in means between estimated connected components 1 and 2
result_demo <- fusedlasso_inf(y=y, D=Dmat, c1=1, c2=2, method="K", sigma=sigma, K=K)
summary(result_demo)</pre>
```

GFLassoInference

More powerful test for the graph fused lasso

Description

GFLassoInference is an R package for testing a difference in means between a pair of connected components estimated from the graph fused lasso. Details can be found in our manuscript (Chen et al. 2021+). In addition to the manual in R, a detailed tutorial can be found at https://yiqunchen.github.io/GFLassoInference

Details

Maintainer: Yiqun T. Chen < yiqunc@uw.edu> The main function in the package is fusedlasso_inf. In our tutorials and experiments, we also used functions from the genlasso package and the genlassoinf package.

References

Chen YT, Jewell SW, Witten DM. (2021+) More powerful selective inference for the graph fused lasso

Hyun S, G'Sell M, Tibshirani RJ. (2018) Exact post-selection inference for the generalized lasso path. Electron J Stat.

Tibshirani RJ, Taylor J. The solution path of the generalized lasso. Ann Stat. 2011;39(3):1335-1371. doi:10.1214/11-AOS878

Examples

```
lev1 <- 0 # mean for group 1
lev2 <- 3 # mean (absolute value) for group 2/3
sigma <- 1 # level of noise
nn <- 8 # grid size
Dmat <- genlasso::getD2d(nn, nn) # generate D matrix for the 2D fused lasso
### Create the underlying signal
A <- matrix(lev1, ncol=nn, nrow = nn)
A[1:round(nn/3),1:round(nn/3)] <- 1*lev2
A[(nn-2):(nn),(nn-2):(nn)] <- -1*lev2
### Visualize the underlying signal
lattice::levelplot(A)
set.seed(2005)
A.noisy <- A + rnorm(nn^2,mean=0,sd=sigma)
y <- c(t(A.noisy))</pre>
```

```
### Now use the fusedlasso function to obtain estimated connected components after K=13
### steps of the dual path algorithm
K = 13
complete_sol <- genlasso::fusedlasso(y=y,D=Dmat,maxsteps=K)
beta_hat <- complete_sol$beta[,K]
### estimated connected components
estimated_CC <- complete_sol$pathobjs$i
estimated_CC
### Run a test for a difference in means between estimated connected components 1 and 2
result_demo <- fusedlasso_inf(y=y, D=Dmat, c1=1, c2=2, method="K", sigma=sigma, K=K)
summary(result_demo)</pre>
```

```
summary.fusedlasso_inf
```

Summarize the result for powerful graph fused lasso inference

Description

Summarize the result for powerful graph fused lasso inference

Usage

```
summary.fusedlasso_inf(object, ...)
```

Arguments

```
object output from running spike_estimates
... to be passed to methods
```

Value

A data frame with summarized results

Examples

```
lev1 <- 0 \# mean for group 1
lev2 <- 3 # mean (absolute value) for group 2/3</pre>
sigma <- 1 # level of noise
nn <- 8 # grid size
Dmat <- genlasso::getD2d(nn, nn) # generate D matrix for the 2D fused lasso
### Create the underlying signal
A <- matrix(lev1, ncol=nn, nrow = nn)
A[1:round(nn/3), 1:round(nn/3)] <- 1*lev2
A[(nn-2):(nn),(nn-2):(nn)] <- -1*lev2
### Visualize the underlying signal
lattice::levelplot(A)
set.seed(2005)
A.noisy <- A + rnorm(nn^2,mean=0,sd=sigma)
y \leftarrow c(t(A.noisy))
### Now use the fusedlasso function to obtain estimated connected components after K=13
### steps of the dual path algorithm
complete_sol <- genlasso::fusedlasso(y=y,D=Dmat,maxsteps=K)</pre>
beta_hat <- complete_sol$beta[,K]</pre>
```

```
### estimated connected components
estimated_CC <- complete_sol$pathobjs$i
estimated_CC
### Run a test for a difference in means between estimated connected components 1 and 2
result_demo <- fusedlasso_inf(y=y, D=Dmat, c1=1, c2=2, method="K",
sigma=sigma, K=K, compute_ci=TRUE)
summary(result_demo)</pre>
```

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