CS 525 Homework 2

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February 12, 2014

1 Computing the Pagerank vector

1. Write down the global-address space parallel algorithm for computing the Pagerank vector using the algorithmic notation we have used in class.

Function Pagerank

```
Input: n, rbegin, colindex, value, threshold, a
Output: x
while (max_error > threshold) do {
        max_error = 0;
#pragma omp parallel shared(a,n) reduction(max:max_error)
        int k,k1,k2,j;
                                              //counter, index
        double prev,temp,error;
#pragma omp for
        for row i = 0 to n-1 do
                temp = 0;
                k1 = rbegin[i];
                k2 = rbegin[i+1] - 1;
                if k2 < k1 then continue; end if
                for k = k1 to k2 do
                        j = coloindex[k];
                        temp += value[k]*x[j];
                end for
                temp = a*temp + (1-a)/n; //a is the alpha
                                          // prev is used to store the previous x_i
                prev = x[i];
                y[i] = temp;
                                        // y is a vector to store the updated x_i
                error = fabs(temp - prev);
```

2. Analyze the parallel time complexity of one iteration of the PageRank computation with the two different schedules as described above.

There are two *for* loops in the algorithm. One is for sparse matrix multiplication; another is for updating the pagerank vector. The first loop ends with an implicit synchronization. So there are actually two parallel regions. Here, we only use dynamic scheduling for the first region since the second one is for updating the vector.

Static

```
\lceil n/p \rceil (2\Delta + 6)
```

Dynamic

$$2 \lceil nnz(A)/p \rceil + 6 \lceil n/p \rceil$$

2 Implementation

1. Run your code on 1, 2, 4, and 8 threads on the mc machines. Report the run times and speed-ups for the three data matrices provided.

Dynamic scheduling

```
Dataset 1
# of iterations = 12
chunksize: 10

Dataset 2
# of iterations = 42
chunksize: 1000
```

| Thread | Time | Speedup |
|--------|---------|--------------|
| 1 | 0.02725 | 1 |
| 2 | 0.01616 | 1.6862623762 |
| 4 | 0.00892 | 3.0549327354 |
| 8 | 0.00522 | 5.2203065134 |

| Thread | Time | Speedup |
|--------|---------|--------------|
| 1 | 1.7758 | 1 |
| 2 | 0.94625 | 1.87667107 |
| 4 | 0.54996 | 3.2289621063 |
| 8 | 0.40544 | 4.3799329124 |

Dataset 3

of iterations = 38 chunksize: 10000

| Thread | Time | Speedup |
|--------|---------|--------------|
| 1 | 4.93079 | 1 |
| 2 | 2.5236 | 1.9538714535 |
| 4 | 1.39284 | 3.5400979294 |
| 8 | 1.13423 | 4.3472576109 |

2. Experiment with the scheduling options (dynamic and static), choosing a chunk size to get fast run times.

All on 8 threads

Dataset 1

| | Static | | Dynamic | |
|-----------|---------|--------------|---------|--------------|
| Chunksize | Time | Speedup | Time | Speedup |
| 1 | 0.00559 | 4.5706618962 | 0.00731 | 3.4952120383 |
| 10 | 0.00455 | 5.6153846154 | 0.00431 | 5.9280742459 |
| 100 | 0.00455 | 5.6153846154 | 0.00415 | 6.156626506 |
| 1000 | 0.01001 | 2.5524475524 | 0.0097 | 2.6340206186 |
| 10000 | 0.02658 | 0.9612490594 | 0.02658 | 0.9612490594 |
| 100000 | 0.02652 | 0.9634238311 | 0.02645 | 0.965973535 |

Dataset 2

| | Static | | Dynamic | |
|-----------|---------|--------------|---------|--------------|
| Chunksize | Time | Speedup | Time | |
| 1 | 1.04673 | 1.6924135164 | 1.55299 | 1.1407027734 |
| 10 | 0.67653 | 2.618509157 | 0.68959 | 2.5689177627 |
| 100 | 0.4532 | 3.908870256 | 0.44105 | 4.0165514114 |
| 1000 | 0.403 | 4.3957816377 | 0.40368 | 4.3883769322 |
| 10000 | 0.44204 | 4.0075558773 | 0.44473 | 3.9833157197 |
| 100000 | 0.75676 | 2.3409006819 | 0.78691 | 2.2512104307 |

Dataset 3

| | Static | | Dynamic | |
|-----------|---------|--------------|---------|--------------|
| Chunksize | Time | Speedup | Time | Speedup |
| 1 | 2.69868 | 1.8246179614 | 3.15172 | 1.5623405632 |
| 10 | 1.632 | 3.0171936275 | 1.56002 | 3.1564082512 |
| 100 | 1.26771 | 3.8842164217 | 1.20288 | 4.0935587922 |
| 1000 | 1.19526 | 4.1196559744 | 1.13779 | 4.32774062 |
| 10000 | 1.17125 | 4.2041067236 | 1.13275 | 4.3469962481 |
| 100000 | 1.68652 | 2.9196570453 | 1.66451 | 2.9582639936 |

3 Pagerank with dangling nodes

1. Write down the corresponding algorithm.

Function Pagerank_with_dangling

Input: n, rbegin, colindex, value, threshold, a

Output: x

Global variables: total, max_error, gamma, y[]

```
while (max_error > threshold) {    //termination condition
                max_error = 0;
                total = 0;
#pragma omp parallel shared(n,a) reduction(+:total)
                                                //counteer
                int k;
                int k1,k2,j;
                                      //index
                double tmp;
                                   // updated x[i]
#pragma omp for
          for (i = 0; i < n; i++){
                          tmp = 0;
                          k1 = rbegin[i];
                          k2 = rbegin[i+1]-1;
                          if (k2 < k1){
                                   continue;
                          }
                          for (k = k1; k \le k2; k++){
                                   j = colind[k];
                                   tmp += value[k]*x[j];
                          }
                          y[i] = a*tmp;
                          total += a*tmp;
                }
}// end parallel
        gamma = 1 - total;
#pragma omp parallel shared(n,gamma) reduction(max:maxerr)
{
        double error, tmp, prev;
#pragma omp for
                for (i = 0; i < n; i++){
                          tmp = y[i];
                          prev = x[i];
                          tmp = tmp + gamma/n;
                          error = fabs(tmp - prev);
                          if(error > max_error){
                                  max_error = error;
                          x[i] = tmp;
                }// end for loop
```

}// end parallel
}// end while loop

return x;

2. Time Complexity

There are two parallel region. One is for sparse matrix multiplication; another is for updating the pagerank vector. For the first one, the time complexity for each thread is $\lceil n/p \rceil$ ($2\Delta + 4$). For the second parallel region, the time complexity for each thread is $2 \lceil n/p \rceil$. Therefore, for one iteration, the time complexity is $\lceil n/p \rceil$ ($2\Delta + 6$). Hence, when dynamic scheduling is used (only for the first region), the time complexity becomes $2 \lceil nnz(A)/p \rceil + 6 \lceil n/p \rceil$.

Performance (default scheduling)

All on 1 thread

| | Time |
|-------|---------|
| Data1 | 0.02616 |
| Data2 | 1.96057 |
| Data3 | 5.13793 |

All on 8 thread

| | Time | Speedup |
|-------|---------|--------------|
| Data1 | 0.00652 | 4.0122699387 |
| Data2 | 0.47 | 4.1714255319 |
| Data3 | 1.28149 | 4.0093406894 |