

Algorithms

Algorithm 1. Hierarchical arc-merging (HAM) Algorithm.

Input: network G .

Output: network list L .

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1:   $NetLevel \leftarrow 0$ 
2:   $L \leftarrow []$ 
3:  For  $v_i$  in  $V$ :
4:      create neighbor set  $\Gamma(i)$  of  $v_i$ 
5:      calculate node degree  $k_i$  of  $v_i$ 
6:  For  $e_{ij} = (v_i, v_j)$  in  $E$ :
7:      calculate similarity  $w_{ij}$  of  $e_{ij}$ 
8:  append  $G$  to network list  $L$ :  $L \leftarrow L + [G]$ 
9:   $NetLevel \leftarrow NetLevel + 1$ 
10: While true:
11:     create an empty super-node network  $H$ 
12:     If  $NetLevel == 1$ :
13:         /* Original HAM network phase */
14:         create  $H$  initial member-node information
15:         classify  $E$  into three edge classes:  $E^W$ ,  $E^B$  and  $E^S$ 
16:         If  $E^W$  is empty:
17:             break
18:         process weighted-edge  $E^W$  to construct  $H$  using S1-1
19:         process bridge-edge  $E^B$  to construct  $H$  using S1-2
20:         process sink-edge  $E^S$  to construct  $H$  using S1-3
21:     Else:
22:         /* Super-node HAM network phase */
23:         create previous level network  $G$  member node information
24:         classify  $E$  into two edge classes:  $E^{\Delta Q}$  and  $E^P$ 
25:         If  $E^{\Delta Q}$  is empty:
26:             break
27:         process deltaQ-edge  $E^{\Delta Q}$  to construct  $H$  using S1-4
28:         process passed-edge  $E^P$  to construct  $H$  using S1-5
29:         refine  $H$  member node information
30:         calculate  $H$  modularity using member-node information
31:         If  $NetLevel > 1$ :
32:              $\Delta Q = Q^H - Q^G$ 
33:             If  $\Delta Q$  is less than threshold:
34:                 break
35:         copy  $H$  as  $G$ :  $H \leftarrow G$ 
36:         append  $G$  to network list  $L$ :  $L \leftarrow L + [G]$ 
37:          $NetLevel \leftarrow NetLevel + 1$ 
38: Return  $L$ 
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