

# HOTT EXERCISES IN AGDA

ERIC BAILEY

## CONTENTS

1. Chapter 1	2
1.1. Exercise 1	2

## 1. CHAPTER 1

## 1.1. Exercise 1.

Use the same options as HoTT-Agda.

```
{-# OPTIONS --without-K --rewriting #-}
```

Declare the module.

```
module HoTT.Chapter1.Ex1 where
```

Import the propositional equality module for  $\equiv$ .

```
open import Relation.Binary.PropositionalEquality
```

Given functions  $f : A \rightarrow B$  and  $g : B \rightarrow C$ , define their **composite**  $g \circ f : A \rightarrow C$ .

```
_o_ :  $\forall \{A B C : \text{Set}\} \rightarrow (B \rightarrow C) \rightarrow (A \rightarrow B) \rightarrow A \rightarrow C$ 
```

```
 $g \circ f = \lambda x \rightarrow g (f x)$ 
```

Prove that function composition is associative, i.e.

$$h \circ (g \circ f) \equiv (h \circ g) \circ f$$

```
o-assoc :  $\forall \{A B C D : \text{Set}\} \{f : A \rightarrow B\} \{g : B \rightarrow C\} \{h : C \rightarrow D\} \rightarrow$   

 $h \circ (g \circ f) \equiv (h \circ g) \circ f$ 
```

```
o-assoc = refl
```