Proof-Based Math Readings Session: Proof Techniques

2023 Summer

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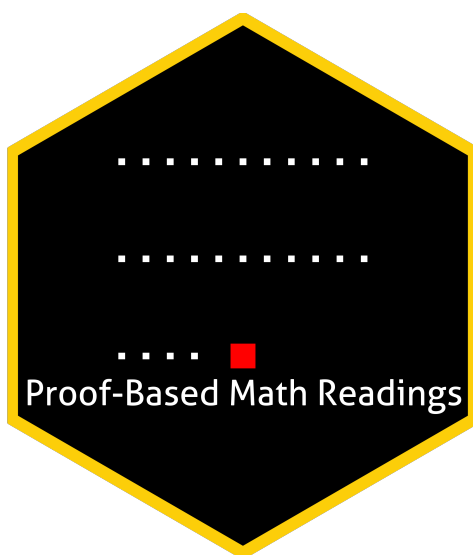Department of Economics
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Proof-Based Math Readings

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0   Motivation

- *Proof-Based Math Readings* is an independent online reading group where we study mathematics required in economics master's/PhD programs using an intuitive approach.
- This first session of the reading group is on *Proof Techniques*.

1   Prerequisites

- CGPA: 3.00/4.00
- Please apply by uploading your CV and transcript to this 🔗 Google Form until 23:59, 04 June 2023.
  Please upload your CV and transcript as **NameSurname.pdf**, not **CV.pdf**.
  Students who applied will be informed about their application results via email at 10:00, 06 June 2023.

2   Format

- This session will last 5 weeks from 12 June 2023 to 16 July 2023.
- We will discuss the topics/exercises that we struggle with at 😀 Proof-Based Math Readings [Discord].
- We will not have face-to-face/online meetings due to size of the group.
- Members are expected to read the chapters, and watch the chapter videos from the book's playlist.

3   Resources [All are open-access]

3.1   Main Book and Main Book's Playlist

Book of Proof by Richard Hammack is our main book because it is a well-written and well-structured pedagogical masterpiece. It is also open-access and provides detailed solutions for odd-numbered exercises at the end of the book.

Jeremy Teitelbaum's playlist on Book of Proof is our main playlist because his narrative is just great.

📖 Book of Proof - Richard Hammack (3.3 Edition, 2022)

▶️ Book of Proof - Richard Hammack (3.3 Edition, 2022, Companion playlist by Jeremy Teitelbaum, Chapter 1-12)

3.2   Supplementary

3.2.1   Proof

In case we need to watch a proof topic from another instructor, we have 2 additional companion playlists.
Because our main playlist does not cover Chapter 13-14, we will cover theese chapters from Penn's playlist.

▶️ Book of Proof - Richard Hammack (3.3 Edition, 2022, Companion playlist by Michael Penn, Chapter 1-14)

▶️ Book of Proof - Richard Hammack (3.3 Edition, 2022, Companion playlist by Valerie Hower, Chapter 1-12)

📖 Book of Proof - Richard Hammack (3.3 Edition, 2022, Companion workbook by Justin Wright)

3.2.2   Calculus

In case we need to remember a topic from calculus, we can use these playlists.

▶️ Essence of Calculus - 3Blue1Brown (2023)

📖 ▶️ Single Variable Calculus - David Jerison (2006)

📖 ▶️ Multi Variable Calculus - Denis Auroux (2007)

4   Reading Schedule

I recommend this study routine:

1) We read the chapter from the main book.
2) We watch the main playlist of the chapter.
3) We solve odd-numbered exercises and check their solutions at the end of the main book.
4) We solve even-numbered exercises.
5) If we cannot solve/understand an exercise, we can discuss the exercise in our Discord server.
6) We move on to the next chapter of the book.

Week 01　　　　　　　　　　　　　　　　　　　　　📅 **12 June - 18 June**

- 📘 Book of Proof, Chapter 1: Sets
- 📘 Book of Proof, Chapter 2: Logic
- 📘 Book of Proof, Chapter 3: Counting

Week 02　　　　　　　　　　　　　　　　　　　　　📅 **19 June - 25 June**

- 📘 Book of Proof, Chapter 4: Direct Proof
- 📘 Book of Proof, Chapter 5: Contrapositive Proof
- 📘 Book of Proof, Chapter 6: Proof by Contradiction

Week 03　　　　　　　　　　　　　　　　　　　　　📅 **26 June - 02 July**

- 📘 Book of Proof, Chapter 7: Proving Non-Conditional Statements
- 📘 Book of Proof, Chapter 8: Proofs Involving Sets
- 📘 Book of Proof, Chapter 9: Disproof
- 📘 Book of Proof, Chapter 10: Mathematical Induction

Week 04　　　　　　　　　　　　　　　　　　　　　📅 **03 July - 09 July**

- 📘 Book of Proof, Chapter 11: Relations
- 📘 Book of Proof, Chapter 12: Functions

Week 05　　　　　　　　　　　　　　　　　　　　　📅 **10 July - 16 July**

- 📘 Book of Proof, Chapter 14: Cardinality of Sets
- 📘 Book of Proof, Chapter 13: Proofs in Calculus

5   The Next Session After This One

Real Analysis: [**Application Deadline 23:59, 28 July 2023 via** 🔗 **Google Form**]

- 📘 Basic Analysis I: Introduction to Real Analysis [Volume I] - Jiri Lebl (Version 6.0, 2023)
- ▶️ Real Analysis - Casey Rodriguez (2020, Companion playlist to the main real analysis book)

If you are admitted to *Proof Techniques* session, you do not have to apply for *Real Analysis* session again. In other words, you can directly join *Real Analysis* session if you wish.