Proof-Based Math Readings Session: Measure Theoretic Probability

2024 Fall

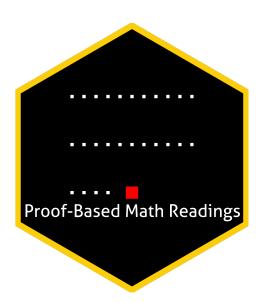
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0 Motivation

- Proof-Based Math Readings is a free and independent online reading group where we study mathematics required in economics master's/PhD programs using an intuitive approach.
- This session of the reading group is on Measure Theoretic Probability.

1 Prerequisites

- CGPA: 3.00/4.00.
- Proof and Real Analysis resources below are the prerequisites for this session.
- Please use the **O** Application Form to join our reading group anytime.
- Applicants are informed about their application results within a week via email.

2 Format

- This session takes 12 weeks.
- We discuss the topics/exercises that we struggle with at Proof-Based Math Readings [Discord].
- We do not have face-to-face/online meetings due to the size of the group.
- Members are expected to read the chapters, and watch the chapter videos from the book's playlist.

3 Resources

3.1 Main Book and Main Book's Playlist

A First Look at Rigorous Probability Theory - Jeffrey S. Rosenthal (2nd Edition, 2006) is our main book for this session because it is well-written and well-structured.

Jem Corcoran's playlist is our main playlist because his narrative is just great.

- A First Look at Rigorous Probability Theory Jeffrey S. Rosenthal (2nd Edition, 2006)
- A First Look at Rigorous Probability Theory Jeffrey S. Rosenthal (2nd Edition, 2006, Errata)
- A First Look at Rigorous Probability Theory Jeffrey S. Rosenthal (2nd Edition, 2006, Solutions)
- ▶ Measure Theoretic Probability Jem Corcoran (Companion playlist, 2024)

3.2 Supplementary

3.2.1 **Proof**

- Book of Proof Richard Hammack (3.3 Edition, 2022)
- Book of Proof Richard Hammack (3.3 Edition, 2022, Companion playlist by Jeremy Teitelbaum)
- Book of Proof Richard Hammack (3.3 Edition, 2022, Companion playlist by Michael Penn)

3.2.2 Real Analysis

- Basic Analysis I: Introduction to Real Analysis [Volume I] Jiri Lebl (Version 6.0, 2023)
- ▶ Real Analysis Casey Rodriguez (2020, Companion playlist to Basic Analysis I)
- Introduction To Metric Spaces Paige Bright (2023)

3.2.3 Measure Theoretic Probability

- Probability: Theory and Examples Rick Durrett (5th Edition, 2019)
- Probability: Theory and Examples Rick Durrett (5th Edition, 2019, Solutions by Hoil Lee, Wonjun Seo)
- Probability: Theory and Examples Rick Durrett (5th Edition, 2019, Solutions by Luke Andrejek)
- ► Measure Theoretic Probability-I Supriyo Bhar (2021)
- Probability Foundations Krishna Jagannathan (2020)

4 Reading Schedule

RPT is the abbreviation of A First Look at Rigorous Probability Theory - Jeffrey S. Rosenthal (2nd Edition, 2006).

■ RPT Week 01-02 A: Mathematical Background Chapter 1: The need for measure theory Chapter 2: Probability triples **■** RPT Week 03-04 Chapter 3: Further probabilistic foundations Chapter 4: Expected values **■** RPT Week 05-06 Chapter 5: Inequality and convergence Chapter 6: Distributions of random variables **■** RPT Week 07-08 Chapter 9: More probability theorems Chapter 10: Weak convergence **RPT** Week 09-10 Chapter 11: Characteristic functions **■** RPT Week 11-12 Chapter 12: Decomposition of probability laws Chapter 13: Conditional probability and expectation