Proof-Based Math Readings Session: Linear Algebra

2024 Spring

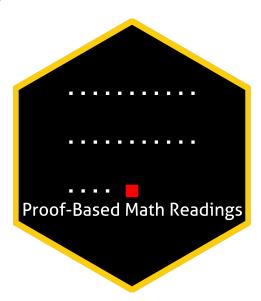
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0 Motivation

- Proof-Based Math Readings is a free and independent online reading group where we study mathematics required in economics master's/PhD programs using an intuitive approach.
- This session of the reading group is on *Linear Algebra*.
- This session is dedicated to Sheldon Axler's lovely cat, Moon, who passed away in August 2023.

1 Prerequisites

- CGPA: 3.00/4.00.
- Proof resources below and Linear Algebra Gilbert Strang (2005) are the prerequisites for this session.
- Please use the **O** Application Form to join our reading group.
- Applicants are informed about their application results within a week via email.

2 Format

- This session takes 12 weeks.
- We discuss the topics/exercises that we struggle with at Proof-Based Math Readings [Discord].
- We do not have face-to-face/online meetings due to the size of the group.
- Members are expected to read the chapters, and watch the chapter videos from the book's playlist.

3 Resources [All are open-access]

3.1 Main Book and Main Book's Playlist

Linear Algebra Done Right (4th Edition, 2024) by Sheldon Axler is our main book for this session because it is well-written, well-structured, and open-access.

Robert Won's playlist is our main playlist because his narrative is just great.

- Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Errata-free version)
- ▶ Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Playlist by Robert Won)
- ▶ Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Playlist by Sheldon Axler)
- Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Solutions by MathwithoutCommentary)
- Linear Algebra Done Right Sheldon Axler (3rd Edition, 2015, Solutions by linearalgebras)
- Linear Algebra Done Right Sheldon Axler (3rd Edition, 2015, Solutions by jubnoske08)
- Linear Algebra Done Right Sheldon Axler (3rd Edition, 2015, Solutions by solverer.com)

3.2 Supplementary

3.2.1 Linear Algebra

- Essence of Linear Algebra 3Blue1Brown (2023)
- Linear Algebra Done Right Sheldon Axler (3rd Edition, 2015, Playlist by Jason Morton)
- Linear Algebra Done Right Sheldon Axler (3rd Edition, 2015, Playlist by Felix Leditzky)

3.2.2 Proof

- Book of Proof Richard Hammack (3.3 Edition, 2022)
- Book of Proof Richard Hammack (3.3 Edition, 2022, Playlist by Jeremy Teitelbaum)
- Book of Proof Richard Hammack (3.3 Edition, 2022, Playlist by Michael Penn)

4 Reading Schedule

• LADR is the abbreviation of Linear Algebra Done Right - Sheldon Axler (4th Edition, 2024).

■ LADR, Chapter 1: Vector Spaces 1A Rⁿ and Cⁿ 1B Definition of Vector Space 1C Subspaces ■ LADR, Chapter 2: Finite-Dimensional Vector Spaces 2A Span and Linear Independence

2B Bases

2C Dimension

E LADR, Chapter 3: Linear Maps 3A Vector Space of Linear Maps 3B Null Spaces and Ranges 3C Matrices 3D Invertibility and Isomorphisms

E LADR, Chapter 5: Eigenvalues and Eigenvectors 5A Invariant Subspaces 5B The Minimal Polynomial 5C Upper-Triangular Matrices 5D Diagonalizable Operators

E LADR, Chapter 6: Inner Product Spaces 6A Inner Products and Norms 6B Orthonormal Bases 6C Orthogonal Complements and Minimization Problems

TA Self-Adjoint and Normal Operators 7A Self-Adjoint and Normal Operators 7B Spectral Theorem 7C Positive Operators 7D Isometries, Unitary Operators, and Matrix Factorization 7E Singular Value Decomposition Week 11-12

5 Further Readings (Optional)

You can check out our Matrix Algebra syllabus at quithub.com/zekiakyol/proof-based-math-readings