

Proof-Based Math Readings

Session: Real Analysis

2023 Summer

Zeki Akyol*

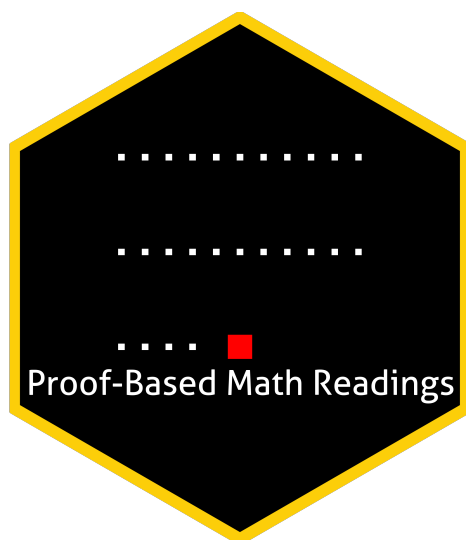
Department of Economics
Istanbul Technical University

[Click here for the most recent versions of the syllabuses](#)

Version: 02 November 2024, 06:28 PM

Table of contents

0 Motivation	2
1 Prerequisites	2
2 Format	2
3 Resources [All are open-access]	2
3.1 Main Book and Main Book's Playlist	2
3.2 Supplementary	2
3.2.1 Real Analysis	2
3.2.2 Calculus	2
3.2.3 Proof Techniques	2
4 Reading Schedule	3
5 Further Readings (Optional)	3




*zekiakyol.com


0 Motivation

- *Proof-Based Math Readings* is a free, independent online reading group where we study the mathematics required for economics master's and PhD programs through an intuitive approach. Active since May 2023.
- This session of the reading group is on *Real Analysis*.

1 Prerequisites

- CGPA: 3.00/4.00. Proof Techniques resources below.
- Please use the  **Application Form** to join our reading group; you will receive a response within a week.

2 Format

- This session takes 12 weeks. We do not have face-to-face/online meetings due to the size of the group.
- Members read the main book and discuss the topics/exercises in the Proof-Based Math Readings Discord .

3 Resources [All are open-access]

3.1 Main Book and Main Book's Playlist





Basic Analysis I: Introduction to Real Analysis - Jiri Lebl (Version 6.1, 2024) is our main book for this session because it is well-written, well-structured, and open-access.

Casey Rodriguez's playlist is our main playlist because his narrative is just great.






-  **Basic Analysis I: Introduction to Real Analysis - Jiri Lebl (Version 6.1, 2024)**
-  **Basic Analysis I: Introduction to Real Analysis - Jiri Lebl (Version 6.1, 2024, Playlist by Casey Rodriguez)**
-  **Basic Analysis I: Introduction to Real Analysis - Jiri Lebl (Version 6.1, 2024, Notes by Casey Rodriguez)**

3.2 Supplementary

3.2.1 Real Analysis

-  **Real Analysis - Wrath of Math (2024)** → Start with this playlist if you find the main book challenging
-  **Real Analysis - Michael Penn (2021)**
-  **Understanding Analysis - Stephen Abbott (2nd Edition 2016, Playlist by Marc Renault)**
-  **Understanding Analysis - Stephen Abbott (2nd Edition 2016, Solutions by Ulisse Mini, Jesse Liby)**

3.2.2 Calculus

-  **Essence of Calculus - 3Blue1Brown (2023)**
-   **Single Variable Calculus - David Jerison (2006) and Multivariable Calculus - Denis Auroux (2007)**
-  **Sequences and Series Calculator - Geogebra**
-  **Function Graph - Geogebra**

3.2.3 Proof Techniques

-  **Book of Proof - Richard Hammack (3.3 Edition, 2022)**
-  **Book of Proof - Richard Hammack (3.3 Edition, 2022, Playlist by Jeremy Teitelbaum, Chapters 1-12)**
-  **Book of Proof - Richard Hammack (3.3 Edition, 2022, Playlist by Michael Penn, Chapters 1-14)**

4 Reading Schedule

- **BAI** is the abbreviation of Basic Analysis I: Introduction to Real Analysis - Jiri Lebl (Version 6.1, 2024).
- We use [Understanding Analysis - Stephen Abbott \(2nd Edition 2016, Solutions by Ulisse Mini, Jesse Liby\)](#) for exercises.

BAI, Chapter 0: Introduction

Week 01 

List of Notation (Page 309-312)

0.1 About this book

0.2 About analysis

0.3 Basic set theory

BAI, Chapter 1: Real Numbers

Week 02 


1.1 Basic properties

1.2 The set of real numbers

1.3 Absolute value and bounded functions

1.4 Intervals and the size of \mathbb{R}

BAI, Chapter 2: Sequence and Series

Week 03-04-05 

2.1 Sequences and limits


2.2 Facts about limits of sequences

2.3 Limit superior, limit inferior, and Bolzano-Weierstrass

2.4 Cauchy sequences

2.5 Series

BAI, Chapter 3: Continuous Functions

Week 06-07-08 


3.1 Limits of functions

3.2 Continuous functions

3.3 Extreme and intermediate value theorems

3.4 Uniform continuity

BAI, Chapter 4: The Derivative


Week 09-10 

4.1 The derivative

4.2 Mean value theorem

4.3 Taylor's theorem

BAI, Chapter 5: The Riemann Integral

Week 11-12 

5.1 The Riemann integral

5.2 Properties of the integral

5.3 Fundamental theorem of calculus

5 Further Readings (Optional)

 [Introduction To Metric Spaces - Paige Bright \(2023\)](#)