Proof-Based Math Readings Session: Linear Algebra

2024 Spring

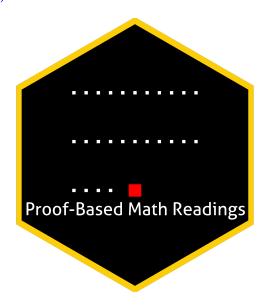
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Version: 07 October 2024, 10:35 AM

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0 Motivation

- Proof-Based Math Readings is a free and independent online reading group where we study mathematics required in economics master's/PhD programs using an intuitive approach.
- This session of the reading group is on Linear Algebra.
- This session is dedicated to Sheldon Axler's lovely cat, Moon, who passed away in August 2023.

1 Prerequisites

- CGPA: 3.00/4.00.
- Proof resources below and Linear Algebra Gilbert Strang (2005) are the prerequisites for this session.
- Please use the Application Form to join our reading group.
- Applicants are informed about their application results within a week via email.

2 Format

- This session takes 12 weeks.
- We discuss the topics/exercises that we struggle with at Proof-Based Math Readings [Discord].
- We do not have face-to-face/online meetings due to the size of the group.
- Members are expected to read the chapters, and watch the chapter videos from the book's playlist.

3 Resources [All are open-access]

3.1 Main Book and Main Book's Playlist

Linear Algebra Done Right - Sheldon Axler (4th Edition, 2024, Errata-free version) is our main book for this session because it is well-written, well-structured, and open-access.

Robert Won's playlist is our main playlist because his narrative is just great.

- Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Errata-free version)
- Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Playlist by Robert Won)
- Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Playlist by Sheldon Axler)
- Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Notes by Robert Won)
- ▶ Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Solutions by MathwithoutCommentary)
- Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Solutions by Oliver Li)
- Linear Algebra Done Right Sheldon Axler (4th Edition, 2024, Solutions by nehc0)
- Linear Algebra Done Right Sheldon Axler (3rd Edition, 2015, Solutions by linearalgebras)
- Linear Algebra Done Right Sheldon Axler (3rd Edition, 2015, Solutions by jubnoske08)
- Linear Algebra Done Right Sheldon Axler (3rd Edition, 2015, Solutions by Solverer)

3.2 Supplementary

3.2.1 Linear Algebra

- Essence of Linear Algebra 3Blue1Brown (2023)
- Linear Algebra Done Right Sheldon Axler (3rd Edition, 2015, Playlist by Jason Morton)
- Down with Determinants! Sheldon Axler (1994)

3.2.2 **Proof**

- Book of Proof Richard Hammack (3.3 Edition, 2022)
- Book of Proof Richard Hammack (3.3 Edition, 2022, Playlist by Jeremy Teitelbaum)
- Book of Proof Richard Hammack (3.3 Edition, 2022, Playlist by Michael Penn)

Reading Schedule 4

• LADR is the abbreviation of Linear Algebra Done Right - Sheldon Axler (4th Edition, 2024).

E LADR, Chapter 1: Vector Spaces

Week 01 #

- $1A R^n$ and C^n
- **1B** Definition of Vector Space
- 1C Subspaces

■ LADR, Chapter 2: Finite-Dimensional Vector Spaces

Week 02-03

- **2A** Span and Linear Independence
- 2B Bases
- 2C Dimension

E LADR, Chapter 3: Linear Maps

Week 04-05-06

- **3A** Vector Space of Linear Maps
- **3B** Null Spaces and Ranges
- **3C** Matrices
- **3D** Invertibility and Isomorphisms

■ LADR, Chapter 5: Eigenvalues and Eigenvectors

Week 07-08

- **5A** Invariant Subspaces
- **5B** The Minimal Polynomial
- **5C** Upper-Triangular Matrices
- **5D** Diagonalizable Operators

■ LADR, Chapter 6: Inner Product Spaces

Week 09-10

- **6A** Inner Products and Norms
- **6B** Orthonormal Bases
- 6C Orthogonal Complements and Minimization Problems

■ LADR, Chapter 7: Operators on Inner Product Spaces

Week 11-12

- 7A Self-Adjoint and Normal Operators
- **7B** Spectral Theorem
- **7C** Positive Operators
- ${\bf 7D}$ Isometries, Unitary Operators, and Matrix Factorization
- **7E** Singular Value Decomposition

Further Readings (Optional) 5

Matrix Analysis - Roger A. Horn, Charles R. Johnson (2nd Edition, 2013)