Proof-Based Math Readings Session: Proof Techniques

2023 Summer

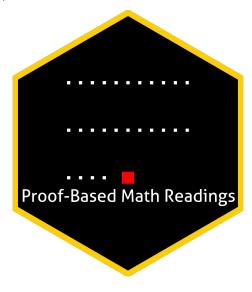
Zeki Akyol*

Department of Economics Istanbul Technical University Click here for the most recent version

Version: 17 February 2025, 06:28 PM $\,$

Table of contents

U	Motivation	2
1	Prerequisites	2
2	Format	2
3	Resources [All are open-access] 3.1 Main Book and Main Book's Playlist 3.2 Supplementary 3.2.1 Proof Techniques 3.2.2 Calculus	$\frac{2}{2}$
4	Reading Schedule	3
5	Further Readings (Optional)	3



^{*}zekiakyol.com

0 Motivation

- Proof-Based Math Readings is a free, independent online reading group where we study the mathematics required for economics master's and PhD programs through an intuitive approach. Active since May 2023.
- This session of the reading group is on *Proof Techniques*.

1 Prerequisites

- Calculus resources below.
- Please use the Application Form to join our reading group; you will receive a response within a week.

2 Format

- This session takes 12 weeks. We do not have face-to-face/online meetings due to the size of the group.
- Members read the main book and discuss the topics/exercises in the Proof-Based Math Readings Discord 🖨.

3 Resources [All are open-access]

3.1 Main Book and Main Book's Playlist

Book of Proof - Richard Hammack (3.4 Edition, 2025) is our main book because it is a well-written and well-structured pedagogical masterpiece. It is also open-access and provides detailed solutions for odd-numbered exercises at the end of the book.

Jeremy Teitelbaum's playlist on Book of Proof is our main playlist because his narrative is great.

- Book of Proof Richard Hammack (3.4 Edition, 2025)
- Book of Proof Richard Hammack (3.4 Edition, 2025, Playlist by Jeremy Teitelbaum, Chapters 1-12)

3.2 Supplementary

3.2.1 Proof Techniques

Because our main playlist does not cover Chapters 13-14, we cover these chapters from Michael Penn's playlist.

- Book of Proof Richard Hammack (3.4 Edition, 2025, Playlist by Michael Penn, Chapters 1-14)
- Book of Proof Richard Hammack (3.4 Edition, 2025, Playlist by Valerie Hower, Chapters 1-12)
- Book of Proof Richard Hammack (3.4 Edition, 2025, Workbook by Justin Wright)
- Appendix A: Elements of Style for Proofs Dana C. Ernst (2025)

3.2.2 Calculus

- Essence of Calculus 3Blue1Brown (2023)
- Single Variable Calculus David Jerison (2006)
- Multivariable Calculus Denis Auroux (2007)
 - 🖬 Sequences and Series Calculator Geogebra
 - Function Graph Geogebra

Reading Schedule 4

I recommend the following study routine below:

- 1) First read a chapter from the book, then watch the playlist of the chapter.
- 2) Solve odd-numbered exercises and check their solutions at the end of the book.
- 3) Solve even-numbered exercises and check their solutions from our unofficial solutions manual.
- 4) If you cannot solve/understand an exercise, discuss the exercise in our Discord.
- 5) Move on to the next chapter of the book.

Book of Proof

Week 01 #

Chapter 1: Sets Chapter 2: Logic Chapter 3: Counting

Book of Proof

Week 02-03 🛱

Chapter 4: Direct Proof

Chapter 5: Contrapositive Proof Chapter 6: Proof by Contradiction

Book of Proof

Week 04-05

Chapter 7: Proving Non-Conditional Statements

Chapter 8: Proofs Involving Sets

Chapter 9: Disproof

Book of Proof

Week 06

Chapter 10: Mathematical Induction

Book of Proof

Week 07-08

Chapter 11: Relations Chapter 12: Functions

Book of Proof

Week 09-10 #

Chapter 14: Cardinality of Sets

(This chapter requires a solid understanding of Chapter 12)

Book of Proof

Week 11-12 🛱

Chapter 13: Proofs in Calculus

(This chapter is denser than the previous ones)

5 Further Readings (Optional)

- Mathematical Proofs A Transition to Advanced Mathematics G. Chartrand, A. Polimeni, P. Zhang (Chapters 0-14, 4th Edition, 2018)
- Mathematical Proofs A Transition to Advanced Mathematics G. Chartrand, A. Polimeni, P. Zhang (Chapters 0-14, 4th Edition, 2018, Slides)