

## Algorithm 1: The training process of Preferential Labeling

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**Data:**  $D$ : the training dataset;  $E$  the maximum training epochs;  $K$  the sampling times;  
GNN the GNN model

```
1 epoch = 0
2 while epoch < E do
3     epoch += 1
4     for each batch  $B \in D$  do
5         dataList = []
6         for each graph  $G$  and its ground truth  $Y$  in  $B$  do
7             lowestLoss = inf
8             candidateG = None
9              $i = 0$ 
10            while  $i < K$  do
11                 $i += 1$ 
12                // randomly permute  $G$ 
13                PG = randomPermute( $G$ )
14                // feed the permuted graph to GNN and compute the loss
15                 $y = \text{GNN}(PG)$ 
16                loss = computeLoss( $y, Y$ )
17                if loss < lowestLoss then
18                    lowestLoss = loss
19                    candidateG = PG
20                end
21            end
22            // select the permutation that has the lowest loss
23            data = (candidateG,  $Y$ )
24            dataList.append(data)
25        end
26        // use the permutation that has the lowest loss to optimize GNN
27        GNN.optimize(dataList)
28    end
29 end
```

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