

# Your Paper

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## Abstract

We studied signals.

## 1 Introduction and Background

### 1.1 The Fourier Transform

### 1.2 Nyquist's Theorem

### 1.3 The Convolution and Correlation Theorems

### 1.4 Sideband Theory

## 2 Methods

This is the equipment I used. These are the libraries and functions I used. Uncertainty? Technical errors?

### 2.1 Sideband

We used one signal generator (N9310A) with a wide range of allowed frequencies, while the other (83712B) with a lower frequency limit of 10 MHz.

We set the 83712B to run at 11 MHz and 1.5 dBm (justify??). This gave  $\Delta\nu = .05 \times \nu_{LO} \approx .55$  MHz. We set the N9310A to run at 1.5 dBm as well and, depending on the trial, either  $\nu_{RF} = \nu_{LO} + \Delta\nu = 11.55$  MHz or  $\nu_{RF} = \nu_{LO} - \Delta\nu = 10.45$  MHz.

When collecting data, we sampled at 32.5 MHz, which is more than double the Nyquist frequency. ?? why is this important and give a calculation of how far above the Nyquist this is

?? I didn't identify the sum and difference frequencies from observation!!

$$\sin(\nu_{LO} + \Delta\nu) = \sin \nu_{LO} \cos \Delta\nu + \cos \nu_{LO} \sin \Delta\nu$$

$$\sin(\nu_{LO} - \Delta\nu) = \sin \nu_{LO} \cos \Delta\nu - \cos \nu_{LO} \sin \Delta\nu$$

But these are not relevant, we want

$$\sin(a) + \sin(a+b) = ?, \text{ right?}$$

$$\sin(\nu_{LO}) \sin(\nu_{LO} + \Delta\nu) = \frac{1}{2}(\cos \Delta\nu - \cos(2\nu_{LO} + \Delta\nu)) \text{ by evenness of the cosine function}$$

and

$$\sin(\nu_{LO}) \sin(\nu_{LO} - \Delta\nu) = \frac{1}{2}(\cos \Delta\nu - \cos(2\nu_{LO} - \Delta\nu))$$

Why do the power spectra look the way they do. Upper sideband and lower sideband.

For the upper sideband, we can see spikes at almost the difference frequency (.575 MHz  $\approx$  .55 MHz). The other spikes are at 10.2 MHz? Why?

For the lower sideband, we see outer spikes at 9 MHz. The inner spikes are still at roughly the difference frequency...

### 3 Outline and To-Do

What am I doing? Not ACF (5.3, 5.7) and procrastinating on 5.5 so that I can get some writing done.

I did ACF analysis for neither 5.3 nor 5.7

Major logic error: side-by-side captions are mutilated!

Idea: put signal and power spectrum plots side by side, not signals with signals

Rough outline:

argue what the Nyquist criterion is, based on results.

Observations and Data

- \* Include make and model of all equipment used.

- \* "Don't quote a number without the uncertainty and units."

- \* Introduce a hypothesis before each result, and justify each hypothesis with theory

Discussion on results for week 2, section 1

I need to include details about the equipment used, but how in-depth do I need to go? Current plan

- \* For most things, use model number and manufacturer

- \* When data analysis depends on a spec sheet, offer a brief summary of the specs to which you are referring to fine-tune your analysis

I need uncertainties on results but I do not yet know how to get these.

### 4 Results

#### 4.1 5.2

Without taking the spectrum, we want to perform visual analysis of the plots and find periods

Motivation

- \* Pico sampler model, what sampling rate we used

- \* We're using the ugradio pico sampler code

- \* We're using the \_\_\_\_ signal generator

- \* Define terms  $\nu_0$  = input frequency.  $\nu_s$  = sampling frequency.

Finally, we took the default 16000 samples for each signal. However, for the data analysis, we will be excluding the first 100 samples due to a peculiarity of the pico sampler which distorted these (1).

We may begin inspection of the samples with a qualitative approach. Figure 2 shows a signal which repeats about five times in the span of about 4 microseconds. This gives us 1.25 cycles per microsecond, or 1.25 MHz, as expected. Figure 5 is not as obviously derived from a sine wave (the shape is distorted by the shrinking gap between  $\nu_0$  and  $\nu_s$ ), but we may still say that there is a repeating signal with slightly under five repetitions in a span of 4 microseconds. This would give us slightly under 1.25 MHz, which is incorrect; thus we have qualitatively demonstrated an aliasing effect.

#### 4.2 5.3

"What does it mean, that the voltage spectra are complex? What do the real and imaginary parts represent? Is the imaginary part less 'real' than the real part? What does it mean, for frequencies to be negative versus positive?"

"Why might we use power spectra instead of voltage spectra, and vice versa?"

"According to the correlation theorem, the Fourier transform of the power spectrum should equal the ACF. Does it? Explain any differences."

"you need to make sure `dft.idft` correctly infers the frequencies corresponding to each bins in your power spectrum array"

"When calculating a digital version of the correlation function, you have to worry about end effects. Suppose you are calculating an ACF for N samples with delays  $\Delta N$  ranging up to  $N/2$ .

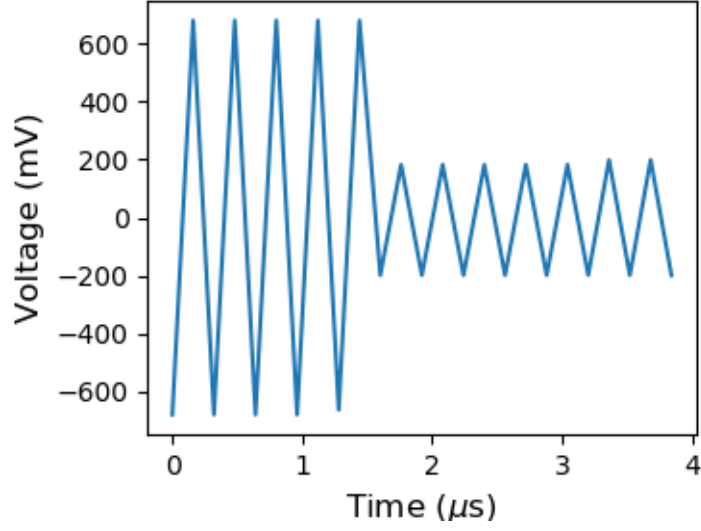


Figure 1: The oscilloscope displayed a constant signal throughout the period of data-taking. The data sampled from the pico sampler, however, reconstructs a signal with large aberrations in the first few microseconds.

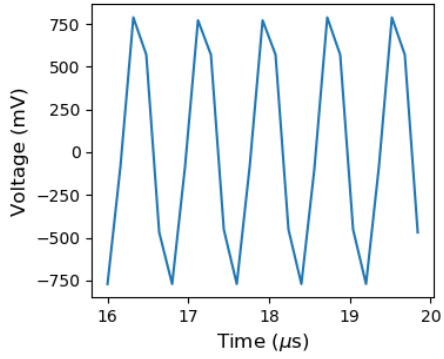


Figure 2:  $\nu_0 = .2\nu_s = 1.25$  MHz.

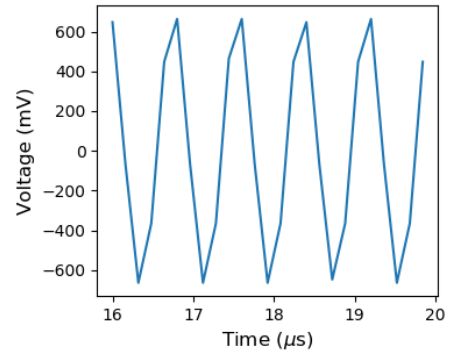


Figure 3:  $\nu_0 = .8\nu_s = 5$  MHz.

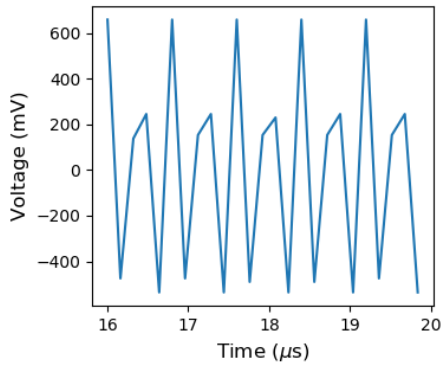


Figure 4:  $\nu_0 = .4\nu_s = 2.5$  MHz.

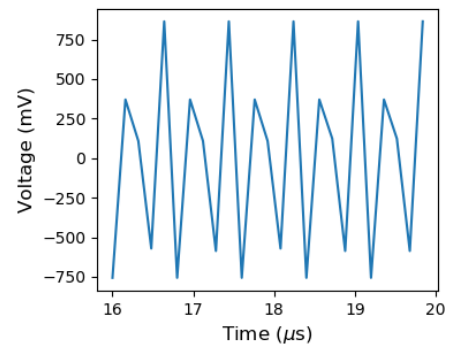


Figure 5:  $\nu_0 = .6\nu_s = 3.75$  MHz.

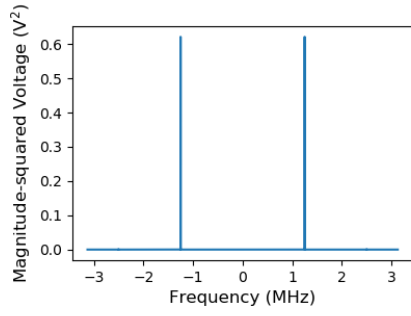


Figure 6:  $\nu_0 = .2\nu_s = 1.25$  MHz. Peak amplitudes at  $\pm 1.25$  MHz

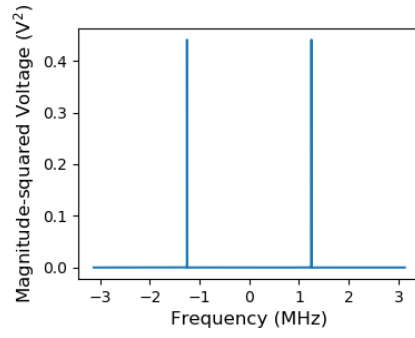


Figure 7:  $\nu_0 = .8\nu_s = 5$  MHz. Peak amplitudes at  $\pm 1.25$  MHz

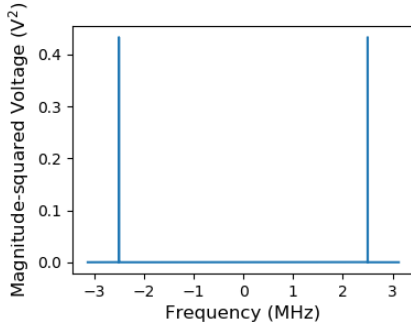


Figure 8:  $\nu_0 = .4\nu_s = 2.5$  MHz. Peak amplitudes at  $\pm 2.5$  MHz

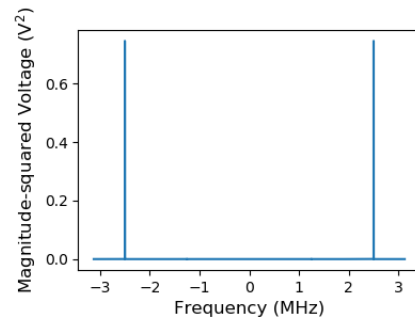


Figure 9:  $\nu_0 = .6\nu_s = 3.75$  MHz. Peak amplitudes at  $\pm 2.5$  MHz

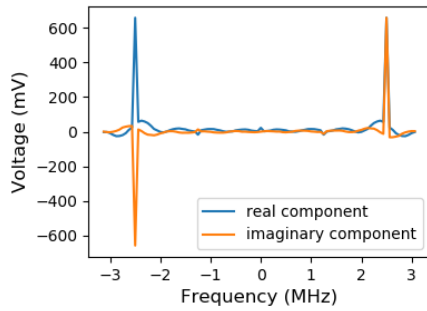


Figure 10: Voltage

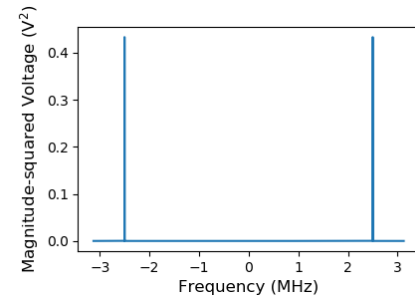


Figure 11: Powerish

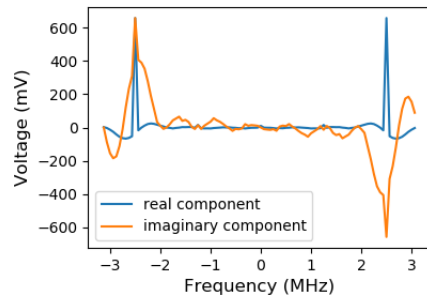


Figure 12: Voltage

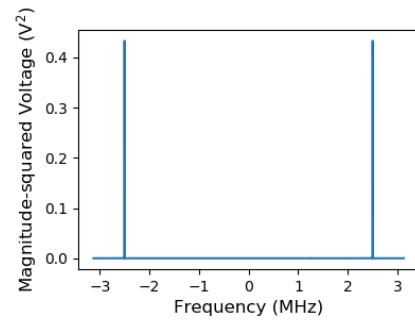


Figure 13: Powerish

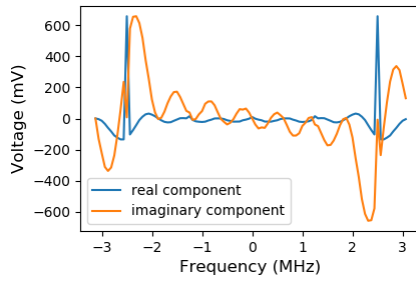


Figure 14: Voltage

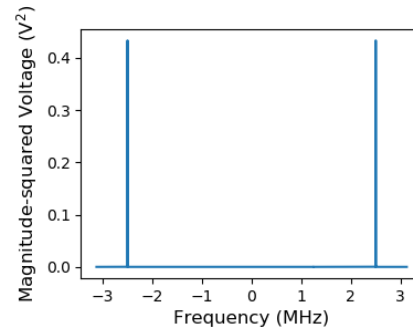


Figure 15: Powerish

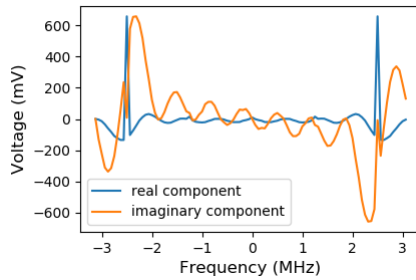


Figure 16: Voltage

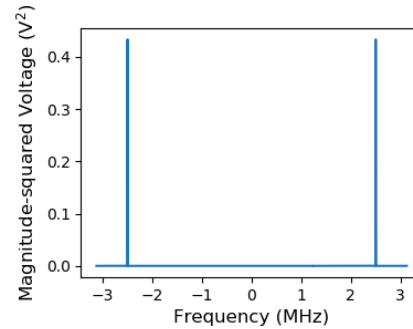


Figure 17: Powerish

Then the number of terms in the sum is always smaller than  $N$  because the delays spill over the edge of the available samples.”

How am I supposed to account for this?

Differences? Probably because I did not zero out the middle

### 4.3 5.4

The y-axis is labeled incorrectly. We want log of square of voltage.

Recall that spectral leakage is introduced by the finite bounds on our Fourier transforms. Why does that math correspond to these results?

### 4.4 5.5

The separation looks pretty good so far.

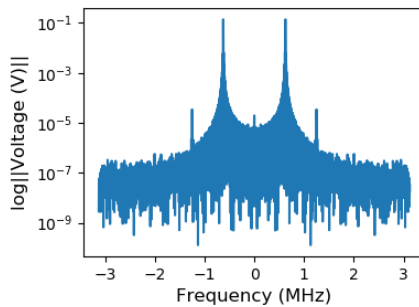


Figure 18:  $\nu_0 = .1\nu_s = .625$  MHz

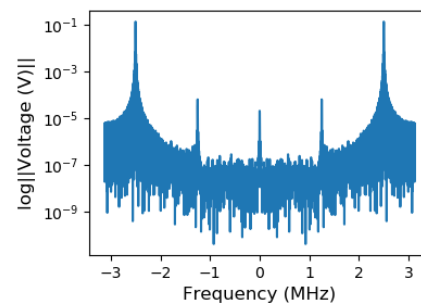


Figure 19:  $\nu_0 = .4\nu_s = 2.5$  MHz

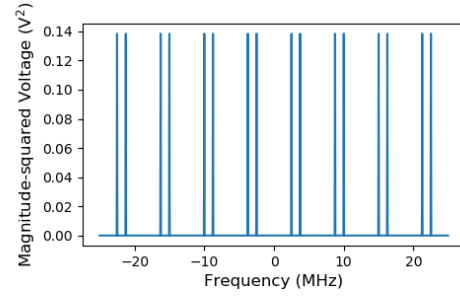
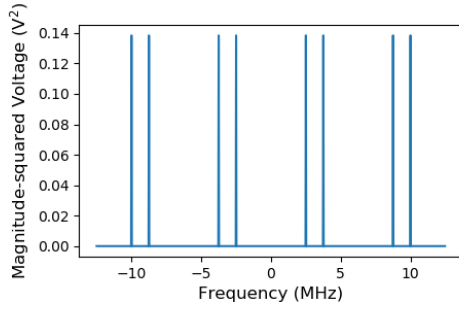


Figure 20:  $\nu_0 = .4\nu_s = 2.5$  MHz. Fourth window. Figure 21: Same frequency. Eighth window.

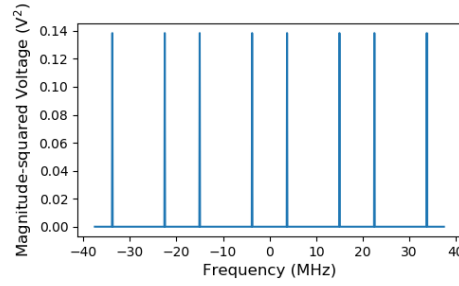


Figure 22: Same frequency. Twelfth window.

4.5 5.6

4.6 5.7

First sample:

Mean = 3.899292452830189 mV Standard deviation = 20.079642416978363 mV Variance = 403.19203959371663 (mV)<sup>2</sup>

I am allowing the first 100 samples to contaminate. I do not know how much I should trod outside the 16000 recommendation.

4.7 7.1

These figures are missing captions!

4.8 7.2

4.9 7.3

Single side band mixer is more difficult to perform.

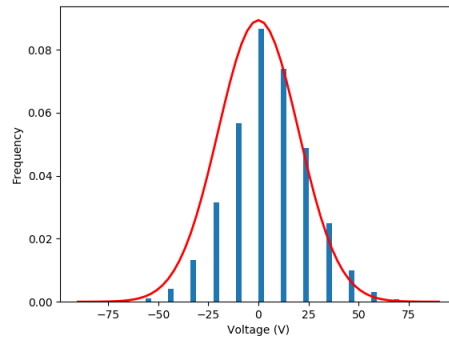


Figure 23

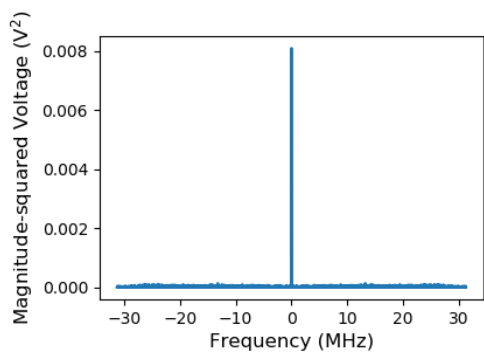


Figure 24

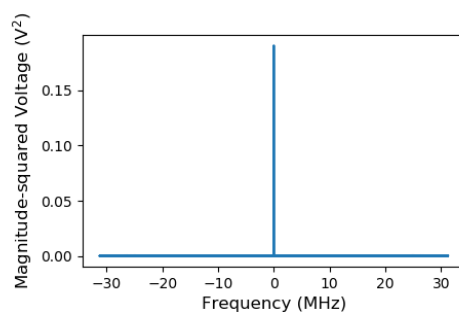


Figure 25

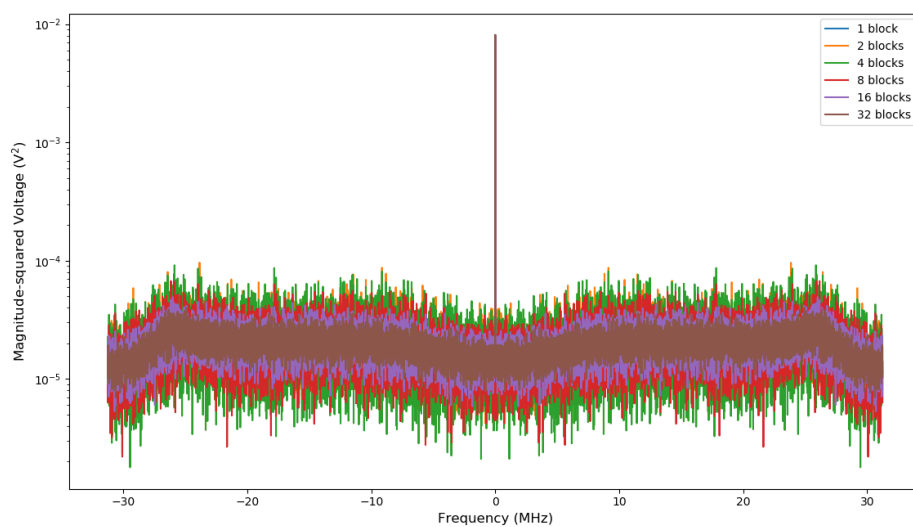


Figure 26

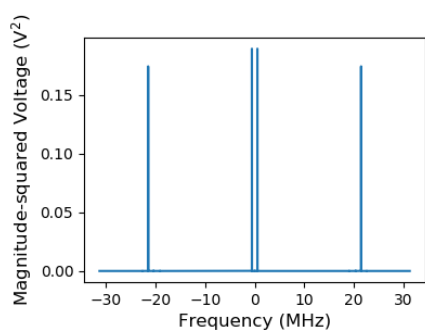


Figure 27

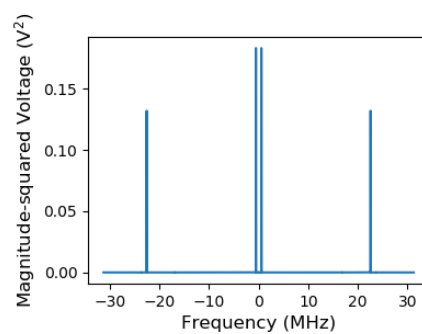


Figure 28

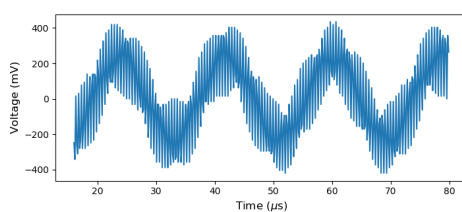


Figure 29

## References

- [Gre93] George D. Greenwade. The Comprehensive Tex Archive Network (CTAN). *TUGBoat*, 14(3):342–351, 1993.