

1 Assumed Knowledge

1.1 Algebra

1.1.1 Completing the Square

$$x^2 + bx + c = \left(x + \frac{b}{2}\right)^2 + c - \left(\frac{b}{2}\right)^2$$

1.1.2 Polynomial Expansions

$$(a \pm b)^2 = a^2 \pm 2ab + b^2$$

$$a^2 - b^2 = (a + b)(a - b)$$

$$a^3 \pm b^3 = (a \pm b)(a^2 \mp 2ab + b^2)$$

1.1.3 Partial Fractions

$$\begin{aligned} & \frac{f(x)}{(ax+b)(cx+d)} \\ &= g(x) + \frac{A}{ax+b} + \frac{B}{cx+d} \\ & \frac{f(x)}{(ax+b)(cx+d)^2} \\ &= g(x) + \frac{A}{ax+b} + \frac{B}{cx+d} + \frac{C}{(cx+d)^2} \\ & \frac{f(x)}{(ax+b)(x^2+c)} \\ &= g(x) + \frac{A}{ax+b} + \frac{Bx+C}{x^2+c} \end{aligned}$$

1.1.4 Exponent and Logarithm

$$e^n = \underbrace{e \times e \times e \times \dots \times e}_{n \text{ times}}$$

$$e^{\frac{1}{2}} = \sqrt{e}$$

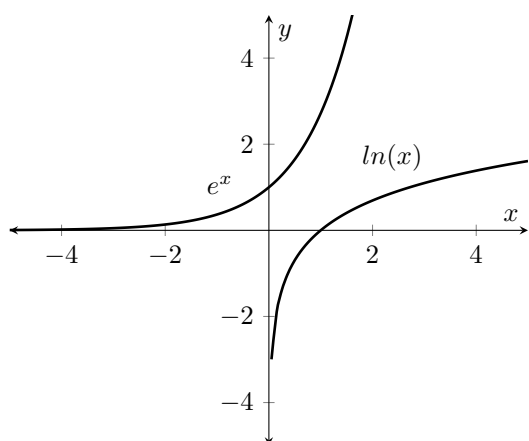
$$\log_e(x) = \ln(x)$$

= how many times e is multiplied by itself to get x

$$\log_{10}(x) = \lg(x)$$

$$x = e^{\ln(x)}$$

$$\log_x(y) = \frac{\log_{base}(y)}{\log_{base}(x)}$$



1.2 Trigonometry

1.2.1 Sine and Cosine Rule

For any triangle with length of sides a , b and c and with opposite angles A , B and C :

$$\frac{a}{\sin(A)} = \frac{b}{\sin(B)} = \frac{c}{\sin(C)}$$

$$a^2 = b^2 + c^2 - 2bc\cos(A)$$

$$\cos(A) = \frac{b^2 + c^2 - a^2}{2bc}$$

1.2.2 Sum of Angles

$$\sin(A \pm B) = \sin(A)\cos(B) \pm \cos(A)\sin(B)$$

$$\sin(2A) = 2\sin(A)\cos(A)$$

$$\cos(A \pm B) = \cos(A)\cos(B) \mp \sin(A)\sin(B)$$

$$\cos(2A) = \cos^2(A) - \sin^2(A)$$

$$= 2\cos^2(A) - 1$$

$$= 1 - 2\sin^2(A)$$

$$\tan(A \pm B) = \frac{\tan(A) \pm \tan(B)}{1 \mp \tan(A)\tan(B)}$$

$$\tan(2A) = \frac{2\tan(A)}{1 - \tan^2(A)}$$

$$\text{Area of Triangle} = \frac{1}{2}ab\sin(C)$$

1.2.3 Factor and Reverse Factor Formula

$$\sin(A) + \sin(B) = 2\sin\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right)$$

$$\sin(A) - \sin(B) = 2\cos\left(\frac{A+B}{2}\right)\sin\left(\frac{A-B}{2}\right)$$

$$\cos(A) + \cos(B) = 2\cos\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right)$$

$$\cos(A) - \cos(B) = -2\sin\left(\frac{A+B}{2}\right)\sin\left(\frac{A-B}{2}\right)$$

$$\sin(A)\cos(B) = \frac{1}{2}[\sin(A+B) - \sin(A-B)]$$