# COMPARISON OF CURRENT ONLINE STOCK PORTFOLIO SELECTION METHODS

Tayisiya Chernenko, Travis Dula, Abby East, Sayyant Rath, Dr. Gopal Gupta



### **Abstract**

With the recent controversy and excitement over \$GME and \$AMC, the stock market has piqued the interest of many students. Online portfolio selection aims to determine the best way to allocate wealth across several assets to maximize return with no prior knowledge or market conditions. Because this is such a broad and expansive problem, there exist numerous approaches to solving it. We aim to compare some of the current approaches in a variety of trading scenarios, portfolio compositions, and trading frequencies to determine how well they performed in different situations. We did this by implementing and benchmarking baseline strategies as well as a variety of modern approaches discussed in current scientific literature.

# **Problem Setting & Approach**

We define a *portfolio* b as an *m*-dimensional vector of weights, the components of which add up to 1. Each weight represents the proportion of the initial capital invested in an asset. Investors distribute the amount they choose to allocate among multiple stocks in hopes of maximizing expected profits while minimizing losses due to assets performing poorly.

The unit of change within an equities market is called a *tick*, which represents a singular change in an asset's ask or bid price (quantized down to some base unit, usually the thousandth of a dollar).

As the market experiences changes, the portfolio wealth distribution may change based on the *update rules* of various trading strategies (see Fig. 1), which utilize different methods for re-balancing the distribution of a portfolio. If a stock generates profit, then it will generate more cumulative wealth than a stock that lost a portion of its value.

As an online optimization problem, the strategies have no initial knowledge about prices and market conditions and are expected to react to net price changes. Our key goal within this project was to determine which update scheme is the best when maximizing return and how these methods handle a variety of trading situations and portfolio compositions.

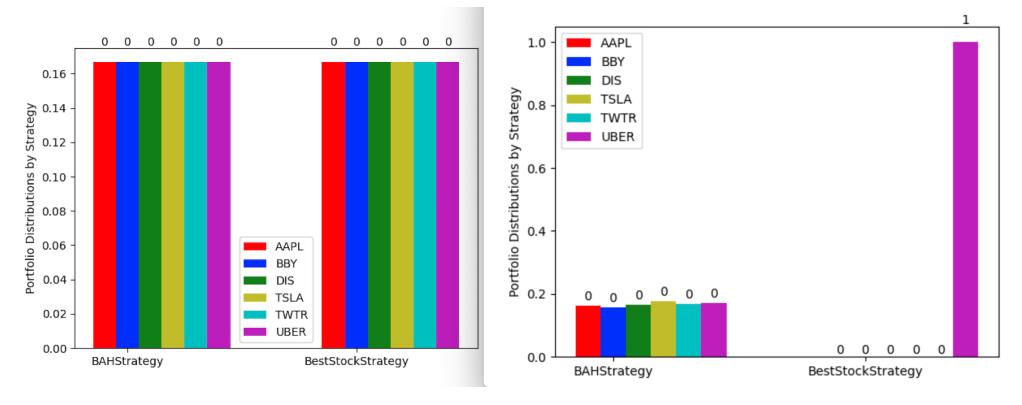


Fig. 1: Portfolio update for two strategies

Careful portfolio design and data selection was critical to the success of this project. When selecting data, we considered two main variations:

- Stock Diversity Picking stocks from numerous industries assures that the trends for their growth will be distinct.
- Time Tracking stocks over multiple days and sometimes through extraordinary trading scenarios allows for enough changes to see how algorithms uniquely handle the situation.

We began by implementing strategies as discussed in [Li and Hoi 2014]. We then developed a backtesting framework to allow us to run such strategies at arbitrary frequencies. We located tick-level and lower-resolution (5-minute and intraday) historical data both on the NASDAQ and NYSE exchanges. These tests were run on market windows consisting from just a few hours to about a year's worth of historical data.

# Strategies

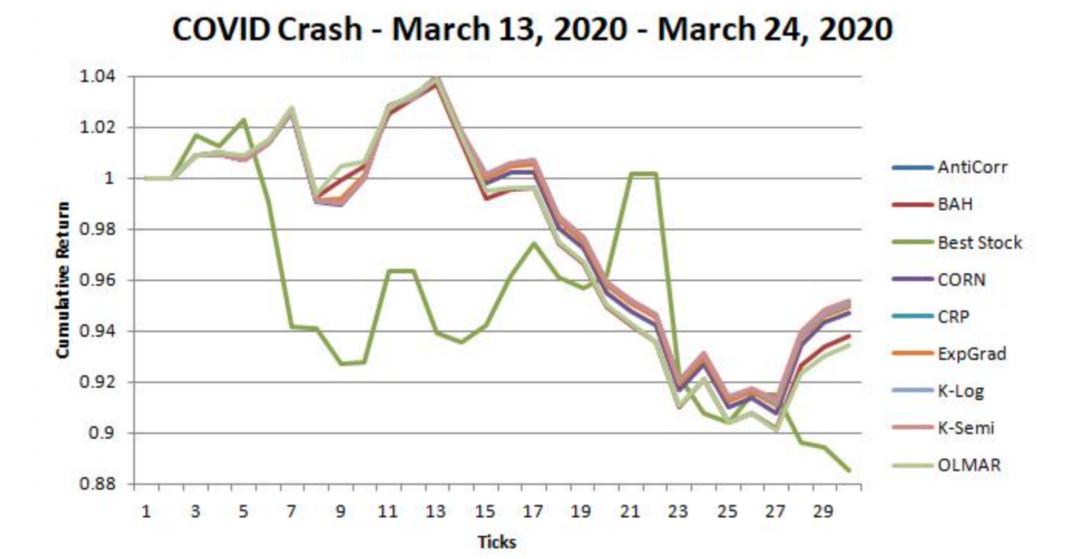


Fig. 2: The compared cumulative return of multiple strategies over an adverse trading event

There exist four main categories of strategies that reallocate wealth based on historical data. All portfolios begin with an even wealth distribution, and as the market changes the strategies determine through various methods as rooted in economic and optimization theory.

#### **Baseline Strategies**

Such strategies are fairly simple and are used as a comparison standard when comparing the performance of more complex strategies. One such strategy is called Buy And Hold, in which the initial portfolio is never modified. Another baseline strategy, Constant Rebalanced Portfolios, aims to reinvest gains back into each asset equally.

#### **Follow the Winner**

This intuitive approach invests more of the total into the stock that performs the best. The percentage that constitutes "more" can be as simple as putting 100 percent, as is performed by the Best Stock strategy (pictured in Fig. 1), or may take a more complex approach.

#### Follow the Loser

This category is developed on the foundation of the Mean Reversion Principle, the theory that market changes will return towards some equilibrium. Thus, these strategies invest more of the total into the stock that performs the worst in anticipation of a rise back to the mean.

### Pattern-Matching

Pattern-matching strategies take a two-part approach to selecting optimal portfolio weights. First, *sample selection* analyzes subsets of historical market changes called windows and utilizes various metrics for determining the most similar windows to the previous trading period (given in the form of probabilities). Then, *portfolio optimization* aims to utilize those predictions to handle the next period's price changes. All of the selected indices from the last step are used to construct a potential portfolio distribution, and then one is selected. Being selective on when to update reduces transaction costs, and this method provides adjustable parameters for doing so.

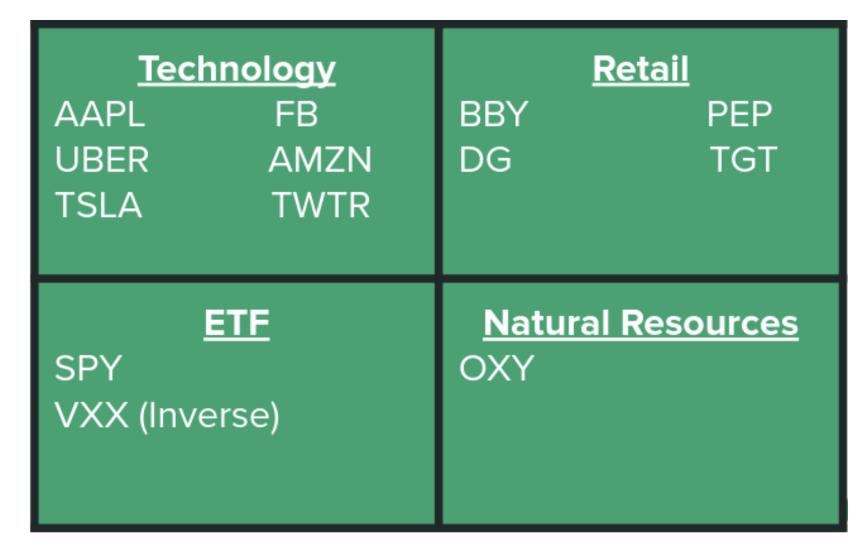


Fig. 3: Examples of how a portfolio can be diversified

### Results

Through analyzing a wide variety of portfolios in combinations of stable vs. volatile stocks in short and long-term time frames, we have been able to understand the cumulative return of these strategies in various scenarios.

The Benchmark and the Follow the Winner strategies tend to generate large return for short periods of time if the market is following an upward trend. However, they react poorly to market volatility and can lose most of the profit rapidly in such situations. As a result, these approaches produce significantly lower reward over time in comparison to steadier strategies. For small trading period, utilizing these can be rewarding, but comes with high risk.

On the other hand, Follow the Loser strategies fared better in more volatile environments, seeing as the principle behind this approach is the market will return to an equilibrium. By betting on the worst performing stock, these strategies produced periods of return where it outperformed other strategies as the market shifted. However, for long periods of steady growth, this strategy was ill-equipped to compete with the rest.

Pattern Matching Strategies proved to be the most stable. They analyzed the history of the market to make predictions, making smaller adjustments in comparison to strategies that went all in on a chosen stock. This produced less sudden spikes of wealth, but also reduced the loss rate during periods of market instability. Over time, these strategies overtook the previous categories, indicating a slow and steady approach is favorable for predictable long-term return.

The final consideration for any potential trader in deciding upon which of these approaches to utilize is the transaction costs in trading. While our project did not consider transaction costs, the strategies which drastically reallocate their wealth and do so often will often be penalized and perform worse than demonstrated within our research. These strategies are Constant Rebalanced Portfolio and Best Stock.

Our data preprocessing module, strategy implementations, backtesting infrastructure, and visualization code have been condensed into an extensible code architecture/ Python package which functions much like an equities market. This implementation is able to simulate the market and the prices fed in through market data CSVs, backtest the strategies in that time frame, and then visualize the final results.

#### **Future Goals**

The heavily extensible, object-oriented approach lends the package well to future work within this field. Due to its potential to streamline many actions into just a few lines of code, one of our future goals aims to make our package downloadable. We would also like to explore adding features to handle other market events such as after-hours trading, stock splits, and dividend reinvestment. Lastly, the architecture of the package lends itself well to developers by allowing them to develop and backtest their own trading strategies. The possibilities are limitless and we are excited to continue work on this project.

#### References

Bin Li and Steven C. H. Hoi. 2014. Online portfolio selection: A survey. ACM Comput. Surv. 46, 3, Article 35 (January 2014), 36 pages. DOI: http://dx.doi.org/10.1145/2512962

# Acknowledgements

The Online Portfolio Selection team would like to extend our gratitude to Aditya Rathod and Dr. Gopal Gupta for their guidance and contributions.