#### Introduction to PETSc

Victor Eijkhout



#### **Outline**

- Introduction
- An example program
- Vec datatype: vectors
- Mat Datatype: matrix
- KSP & PC: Iterative solvers
- Making and running PETSc programs
- Profiling, debugging
- Remaining topics



#### Introduction



# What is PETSc? Why should you use PETSc?

Portable Extendable Toolkit for Scientific Computations

- Scientific Computations: parallel linear algebra, in particular linear and nonlinear solvers
- Toolkit: Contains high level solvers, but also the low level tools to roll your own.
- Portable: Available on many platforms, basically anything that has MPI

Why use it? It's big, powerful, well supported.



#### What is in PETSc?

- Linear system solvers (sparse/dense, iterative/direct)
- Nonlinear system solvers
- Tools for distributed matrices
- Support for profiling, debugging, graphical output



#### An example program



#### Include files

Multiple include files; in C only the highest level

```
#include "petscksp.h"
```

In Fortran sequence of include files in the subprogram

```
#include "include/finclude/petsc.h"
#include "include/finclude/petscvec.h"
#include "include/finclude/petscmat.h"
#include "include/finclude/petscksp.h"
#include "include/finclude/petscpc.h"
```



# Program/subprogram heading

CPP definition of (sub)program name: will be used in traceback

```
#undef __FUNCT__
#define __FUNCT__ "main"
int main(int argc,char **args)
{
   PetscFunctionBegin;
   ...
   PetscFunctionReturn(0);
}
```

Use this for every subprogram.

Not available in Fortran



# Petsc initialize / finalize

One-time initialization, includes MPI if not already initialized:

```
ierr = PetscInitialize(&argc,&args,0,0);
....
ierr = PetscFinalize();
```

#### Fortran:

```
call PetscInitialize(PETSC_NULL_CHARACTER,ierr)
....
call PetscFinalize(ierr)
```



#### Petsc function return values

```
Every PETSc function returns an error code, zero is success.
C:
ierr = SomePetscFunction(....); CHKERRQ(ierr);
Fortran:
call SomePetscFunction(...., ierr )
CHKERRQ(ierr);
```



#### Variable declarations

Everything is an object

```
MPI_Comm comm;
PetscErrorCode ierr; PetscTruth flag;
KSP Solver; Mat A; Vec Rhs, Sol;
PetscScalar one; PetscInt its; PetscReal norm;
PetscErrorCode ierr
PetscTruth flag
KSP Solver
PC Prec
Mat. A
PetscInt its
```



(note scalar vs real)

#### Read input parameter

Read user commandline argument (a.out -n 55)

```
ierr = PetscOptionsGetInt
  (PETSC_NULL, "-n", &dom_size, &flag); CHKERRQ(ierr);
if (!flag) dom_size = 10;
matrix_size = dom_size*dom_size;
call PetscOptionsGetInt(PETSC_NULL_CHARACTER,
     "-n",dom_size,flag,ierr)
CHKERRQ(ierr)
if (flag==0) dom_size = 10
matrix_size = dom_size*dom_size;
```



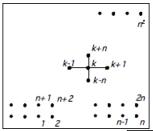
#### Create matrix

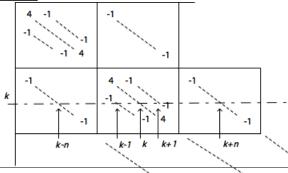
Create distributed matrix on communicator, set local and global size.

```
ierr = MatCreate(comm,&A); CHKERRQ(ierr);
ierr = MatSetSizes(A,PETSC_DECIDE,PETSC_DECIDE,
 matrix_size,matrix_size); CHKERRQ(ierr);
ierr = MatSetType(A,MATMPIAIJ); CHKERRQ(ierr);
call MatCreate(comm, A, ierr)
CHKERRQ(ierr)
call MatSetSizes(A,PETSC_DECIDE,PETSC_DECIDE,
     matrix size.matrix size.ierr)
CHKERRQ(ierr)
call MatSetType(A,MATMPIAIJ,ierr)
CHKERRQ(ierr)
```



# **Five-point Laplacian**





# Fill in matrix elements (C)

```
ierr = MatGetOwnershipRange(A,&low,&high); CHKERRQ(ierr)
for ( i=0; i<m; i++ ) {
  for (j=0; j< n; j++) {
    I = j + n*i;
    if (I>=low && I<high) {
      J = I-1: v = -1.0:
      ierr = MatSetValues
          (mat,1,&I,1,&J,&v,INSERT_VALUES); CHKERRQ(ierr)
ierr = MatAssemblyBegin(mat,MAT_FINAL_ASSEMBLY); CHKERRQ
ierr = MatAssemblyEnd(mat,MAT_FINAL_ASSEMBLY); CHKERRQ(ie)
```



# Fill in matrix elements (F)

```
call MatGetOwnershipRange(A,low,high,ierr)
do i=0,m-1
   do j=0,n-1
      ii = j + n*i
      if (ii>=low .and. ii<high) then
         jj = ii - n
         call MatSetValues(mat,1,ii,1,jj,v,INSERT_VALUES
         CHKERRQ(ierr)
         . . .
call MatAssemblyBegin(mat,MAT_FINAL_ASSEMBLY,ierr)
CHKERRQ(ierr)
call MatAssemblyEnd(mat,MAT_FINAL_ASSEMBLY,ierr)
CHKERRQ(ierr)
```



#### Create solver

```
ierr = KSPCreate(comm,&Solver);
ierr = KSPSetOperators(Solver,A,A,O); CHKERRQ(ierr);
ierr = KSPSetType(Solver,KSPCGS); CHKERRQ(ierr);

call KSPCreate(comm,Solve,ierr)
call KSPSetOperators(Solve,A,A,O,ierr)
CHKERRQ(ierr)
call KSPSetType(Solve,KSPCGS,ierr)
CHKERRQ(ierr)
```



#### Create preconditioner

```
PC Prec:
  ierr = KSPGetPC(Solver,&Prec); CHKERRQ(ierr);
 ierr = PCSetType(Prec,PCJACOBI); CHKERRQ(ierr);
call KSPGetPC(Solve, Prec, ierr)
CHKERRQ(ierr)
call PCSetType(Prec,PCJACOBI,ierr)
CHKERRQ(ierr)
```



#### Input and output vectors

```
ierr = VecCreateMPI(comm,PETSC_DECIDE,matrix_size,&Rhs);
ierr = VecDuplicate(Rhs,&Sol); CHKERRQ(ierr);
ierr = VecSet(Rhs,one); CHKERRQ(ierr);

call VecCreateMPI(comm,PETSC_DECIDE,matrix_size,Rhs,ierr);
CHKERRQ(ierr)
call VecDuplicate(Rhs,Sol,ierr)
CHKERRQ(ierr)
call VecSet(Rhs,one,ierr)
CHKERRQ(ierr)
```



# Solve! (C)

```
ierr = KSPSolve(Solver,Rhs,Sol); CHKERRQ(ierr);
 PetscInt its; KSPConvergedReason reason;
 Vec Res: PetscReal norm:
  ierr = KSPGetConvergedReason(Solver,&reason);
  if (reason<0) {
   PetscPrintf(comm, "Failure to converge\n");
  } else {
    ierr = KSPGetIterationNumber(Solver,&its); CHKERRQ(ie)
    PetscPrintf(comm, "Number of iterations: %d\n",its);
```



# Solve! (F)

```
call KSPSolve(Solve, Rhs, Sol, ierr)
  CHKERRQ(ierr)
  call KSPGetConvergedReason(Solve, reason, ierr)
  if (reason<0) then
     call PetscPrintf(comm, "Failure to converge\n")
  else
     call KSPGetIterationNumber(Solve, its, ierr)
     CHKERRQ(ierr)
     write(msg,10) its
10 format('Number of iterations: i4")
     call PetscPrintf(comm,msg,ierr)
  end if
```



#### Residual calculation

```
ierr = VecDuplicate(Rhs,&Res); CHKERRQ(ierr);
ierr = MatMult(A,Sol,Res); CHKERRQ(ierr);
ierr = VecAXPY(Res,-1,Rhs); CHKERRQ(ierr);
ierr = VecNorm(Res,NORM_2,&norm); CHKERRQ(ierr);
ierr = PetscPrintf(MPI_COMM_WORLD, "residual norm: %e\n",;
call VecDuplicate(Rhs,Res,ierr)
CHKERRQ(ierr)
call MatMult(A,Sol,Res,ierr)
CHKERRQ(ierr)
call VecAXPY(Res,mone,Rhs,ierr)
CHKERRQ(ierr)
call VecNorm(Res,NORM_2,norm,ierr)
CHKERRQ(ierr)
if (mytid==0) print *, "residual norm: ", norm
```



#### Clean up

```
ierr = VecDestroy(Res); CHKERRQ(ierr);
ierr = KSPDestroy(Solver); CHKERRQ(ierr);
ierr = VecDestroy(Rhs); CHKERRQ(ierr);
ierr = VecDestroy(Sol); CHKERRQ(ierr);
call MatDestroy(A,ierr)
CHKERRQ(ierr)
call KSPDestroy(Solve, ierr)
CHKERRQ(ierr)
call VecDestroy(Rhs,ierr)
CHKERRQ(ierr)
call VecDestroy(Sol,ierr)
CHKERRQ(ierr)
call VecDestroy(Res,ierr)
CHKERRQ(ierr)
```



Vec datatype: vectors



#### Create calls

Everything in PETSc is an object, with create and destroy calls:

```
VecCreate(MPI Comm comm, Vec *v);
VecDestroy(Vec v);
/* C */
Vec V:
ierr = VecCreate(MPI_COMM_SELF,&V); CHKERRQ(ierr);
ierr = VecDestroy(V); CHKERRQ(ierr);
! Fortran
Vec V
call VecCreate(MPI_COMM_SELF,V)
CHKERRQ(ierr)
call VecDestroy(V)
CHKERRQ(ierr);
```

Note: in Fortran there are no "star" arguments



#### More about vectors

A vector is a vectors of PetscScalars: there are no vectors of integers (see the IS datatype later)

The vector object is not completely created in one call:

```
VecSetSizes(Vec v, int m, int M);
```

Other ways of creating: make more vectors like this one:

```
VecDuplicate(Vec v,Vec *w);
```

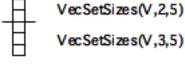


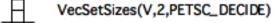
## Parallel layout

Local or global size in

VecSetSizes(Vec v, int m, int M);

Global size can be specified as PETSC\_DECIDE.





VecSetSizes(V,3,PETSC\_DECIDE)



# Parallel layout up to PETSc

```
VecSetSizes(Vec v, int m, int M);
```

Local size can be specified as PETSC\_DECIDE.

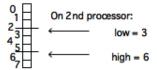




# Query parallel layout

Query vector layout:

VecGetOwnershipRange(Vec x,PetscInt \*low,PetscInt \*high)



Query general layout:

PetscSplitOwnership(MPI\_Comm comm,PetscInt \*n,PetscInt \*N)

(get local/global given the other)



# **Setting values**

Set vector to constant value:

```
VecSet(Vec x.PetscScalar value):
Set individual elements (global indexing!):
VecSetValues(Vec x,int n,int *indices,PetscScalar *values,
    INSERT VALUES): /* or ADD VALUES */
i = 1; v = 3.14;
VecSetValues(x,1,&i,&v,INSERT_VALUES);
ii[0] = 1: ii[1] = 2; vv[0] = 2.7; vv[1] = 3.1;
VecSetValues(x,2,ii,vv,INSERT_VALUES);
call VecSetValues(x,1,i,v,INSERT_VALUES,ierr)
call VecSetValues(x,2,ii,vv,INSERT_VALUES,ierr)
```



## Setting values'

```
No restrictions on parallelism; after setting, move values to appropriate processor:
```

```
VecAssemblyBegin(Vec x);
VecAssemblyEnd(Vec x);
```



#### **Getting values**

Setting values is done without user access to the stored data Getting values is often not necessary: many operations provided. what if you do want access to the data?

Create vector from user provided array:

```
VecCreateSeqWithArray(MPI_Comm comm,
  PetscInt n,const PetscScalar array[],Vec *V)
VecCreateMPIWithArray(MPI_Comm comm,
  PetscInt n,PetscInt N,const PetscScalar array[],Vec *vv)
```

 Get the internal array (local only; see VecScatter for more general mechanism):

```
VecGetArray(Vec x,PetscScalar *a[])
/* do something with the array */
VecRestoreArray(Vec x,PetscScalar *a[])
```



#### **Getting values example**

```
int localsize,first,i;
PetscScalar *a;
VecGetLocalSize(x,&localsize);
VecGetOwnershipRange(x,&first,PETSC_NULL);
VecGetArray(x,&a);
for (i=0; i<localsize; i++)
    printf("Vector element %d : %e\n",first+i,a[i]);
VecRestoreArray(x,&a);</pre>
```



# Array handling in F90

```
PetscScalar, pointer :: xx_v(:)
....
call VecGetArrayF90(x,xx_v,ierr)
a = xx_v(3)
call VecRestoreArrayF90(x,xx_v,ierr)
```

More seperate F90 versions for 'Get' routines



### **Basic operations**

```
VecAXPY(Vec y,PetscScalar a,Vec x); /* y <- y + a x */</pre>
VecAYPX(Vec y,PetscScalar a,Vec x); /* y <- a y + x */</pre>
VecScale(Vec x, PetscScalar a);
VecDot(Vec x, Vec y, PetscScalar *r); /* several variants */
VecMDot(Vec x,int n,Vec y[],PetscScalar *r);
VecNorm(Vec x,NormType type, double *r);
VecSum(Vec x, PetscScalar *r);
VecCopy(Vec x, Vec y);
VecSwap(Vec x, Vec y);
VecPointwiseMult(Vec w, Vec x, Vec y);
VecPointwiseDivide(Vec w, Vec x, Vec y);
VecMAXPY(Vec y,int n, PetscScalar *a, Vec x[]);
VecMax(Vec x, int *idx, double *r);
VecMin(Vec x, int *idx, double *r);
VecAbs(Vec x):
VecReciprocal(Vec x);
VecShift(Vec x,PetscScalar s);
```



Mat Datatype: matrix



## **Matrix creation**

The usual create/destroy calls:

```
MatCreate(MPI Comm comm, Mat *A)
MatDestroy(Mat A)
```

Several more aspects to creation:

```
MatSetType(A,MATSEQAIJ) /* or MATMPIAIJ */
MatSetSizes(Mat A,int m,int n,int M,int N)
MatSeqAIJSetPreallocation /* more about this later*/
   (Mat B,PetscInt nz,const PetscInt nnz[])
```

Local or global size can be PETSC\_DECIDE (as in the vector case)



## Matrix creation all in one

```
MatCreateSeqAIJ(MPI_Comm comm,PetscInt m,PetscInt n,
   PetscInt nz,const PetscInt nnz[],Mat *A)
MatCreateMPIAIJ(MPI_Comm comm,
   PetscInt m,PetscInt n,PetscInt M,PetscInt N,
   PetscInt d_nz,const PetscInt d_nnz[],
   PetscInt o_nz,const PetscInt o_nnz[],
   Mat *A)
```



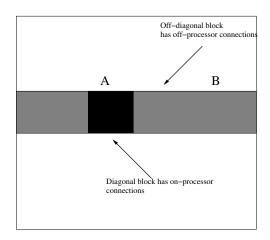
# Sequential matrix structure

```
MatCreateSeqAIJ(comm,int m,int n,
        int nz,int *nnz,Mat *A);
/* or */
MatSeqAIJSetPreallocation
      (Mat B,PetscInt nz,const PetscInt nnz[])
```

- nz number of nonzeros per row (or slight overestimate)
- nnz array of row lengths (or overestimate)
- considerable savings over dynamic allocation!



## Parallel matrix structure





# Parallel matrix structure description

- d\_nz: number of nonzeros per row in diagonal part
- o\_nz: number of nonzeros per row in off-diagonal part
- d\_nnz: array of numbers of nonzeros per row in diagonal part
- o\_nnz: array of numbers of nonzeros per row in off-diagonal part

```
MatCreateMPIAIJ(MPI Comm comm,int m,int n,int M,int N,
    int d_nz,int *d_nnz, int o_nz,int *o_nnz,Mat *A);
```

In Fortran use PETSC\_NULL\_INTEGER if not specifying arrays



# Querying parallel structure

Matrix partitioned by block rows:

```
MatGetSize(Mat mat,PetscInt *m,PetscInt* n);
MatGetLocalSize(Mat mat,PetscInt *m,PetscInt* n);
MatGetOwnershipRange(Mat A,int *first row,int *last row);
```



# **Setting values**

Setting is independent of parallelism

Set block of values:

```
MatSetValues(Mat A,int m,const int idxm[],
    int n,const int idxn[],const PetscScalar values[],
    INSERT VALUES); /* or ADD_VALUES */
MatAssemblyBegin(Mat A,MAT_FINAL_ASSEMBLY);
MatAssemblyEnd(Mat A,MAT_FINAL_ASSEMBLY);
(v is row-oriented)
Common case:
```

MatSetValues(A,1,&i,1,&j,&v,INSERT\_VALUES);



# **Getting values**

- Values are often not needed: many matrix operations supported
- Matrix elements can only be obtained locally.
- Getting globally: submatrix extraction.

```
PetscErrorCode MatGetRow(Mat mat,
  PetscInt row,PetscInt *ncols,const PetscInt *cols[],
  const PetscScalar *vals[])
PetscErrorCode MatRestoreRow(/* same parameters */
```

Note: for inspection only; possibly expensive.



# Other matrix types

```
MATBAIJ: blocked matrices (dof per node)

MATAIJMUMPS: for the Mumps solver (explained later)

(see PETSC_DIR/include/petscmat.h)

Dense:
```

```
MatCreateSeqDense(PETSC COMM SELF,int m,int n,
  PetscScalar *data,Mat *A);
MatCreateMPIDense(MPI Comm comm,int m,int n,int M,int N,
  PetscScalar *data,Mat *A)
```

Data argument optional



# Matrix operations

Main operations are matrix-vector:

```
MatMult(Mat A,Vec in,Vec out);
MatMultAdd
MatMultTranspose
MatMultTransposeAdd
```

Simple operations on matrices:

MatNorm

MatScale MatDiagonalScale



## Matrix viewers

```
MatView(A,0);
row 0: (0, 1) (2, 0.333333) (3, 0.25) (4, 0.2)
row 1: (0, 0.5) (1, 0.333333) (2, 0.25) (3, 0.2)
....
```

- Shorthand for MatView(A,PETSC\_VIEWER\_STDOUT\_WORLD);
   or even MatView(A,0)
- also invoked by -mat\_view
- Sparse: only allocated positions listed
- other viewers: for instance -mat\_view\_draw (X terminal)



# More matrix topics

- Viewers are also for binary dump, plotting with X
- Shell matrices: matrix-free operation
- Submatrix extraction
- Matrix partitioning for load balancing



KSP & PC: Iterative solvers



# **Basic concepts**

- All linear solvers in PETSc are iterative (see below)
- Object oriented: solvers only need matrix action, so can handle shell matrices
- Preconditioners
- Fargoing control through commandline options
- Tolerances, convergence and divergence reason
- Custom monitors and convergence tests



**KSP: Krylov Space objects** 



## **Iterative solver basics**

```
KSPCreate(comm,&solver); KSPDestroy(solver);
KSPSetOperators(solver,A,B,MAT_SAME_STRUCTURE);
/* optional */ KSPSetup(solver);
KSPSolve(solver,rhs,sol);
```



# Settings in general

- Other settings, both as command and runtime option
- option -ksp\_view
- (preconditioners discussed below)



# Solver type and tolerances

```
KSPSetType(solver, KSPGMRES);
KSPSetTolerances(solver,rtol,atol,dtol,maxit);
KSP can be controlled from the commandline.
KSPSetFromOptions(solver);
/* right before KSPSolve or KSPSetUp */
then options -ksp.... are parsed.
  • type: -ksp_type gmres -ksp_gmres_restart 20
  • tolerances: -ksp_max_it 50
```



# Convergence

#### Iterative solvers can fail

- Solve call itself gives no feedback: solution may be completely wrong
- KSPGetConvergedReason(solver,&reason): positive is convergence, negative divergence (PETSC\_DIR/include/petscksp.h for list)
- KSPGetIterationNumber(solver,&nits): after how many iterations did the method stop?



```
KSPSolve(solver,B,X);
KSPGetConvergedReason(solver,&reason);
if (reason<0) {
    printf("Divergence.\n");
} else {
    KSPGetIterationNumber(solver,&its);
    printf("Convergence in %d iterations.\n",(int)its);
}</pre>
```



# More KSP topics

- Custom monitors and convergence tests
- Method-specific options (especially GMRES)
- Null spaces



**PC: Preconditioner objects** 



## PC basics

 PC usually created as part of KSP: separate create and destroy calls exist, but are (almost) never needed

```
KSP solver; PC precon;
KSPCreate(comm,&solver);
KSPGetPC(solver,&precon);
PCSetType(precon,PCJACOBI);
```

- PCJACOBI, PCILU (only sequential), PCASM, PCBJACOBI, PCMG, et cetera
- Controllable through commandline options:
   -pc\_type ilu -pc\_factor\_levels 3



#### **Direct methods**

- Iterative method with direct solver as preconditioner would converge in one step
- Direct methods in PETSc implemented as special iterative method: KSPPREONLY only apply preconditioner
- All direct methods are preconditioner type PCLU:
- different solvers triggered by matrix type, for instance MATAIJMUMPS

myprog -mat\_type aijmumps -ksp\_type preonly -pc\_type lu



# Making and running PETSc programs



## Installation

```
cd petsc-2.3.3
python config/configure.py
make ; make install
```

configure.py --help gives

#### PETSc:

- --prefix=<path> --with-sudo=sudo
- --with-default-arch=<bool>
- --PETSC ARCH
- --with-petsc-arch
- --PETSC DIR
- --with-installation-method=<method>

- : Specifiv location to install PETSc (eg. /usr/local)
- : Use sudo when installing packages
- : Allow using the last configured arch without setting PETSC\_A : The configuration name
- : The configuration name
- : The root directory of the PETSc installation
- : Method of installation, e.g. tarball, clone, etc.



# Compiling

Petsc compile and link lines are very long!
Use PETSc include file with variables and rules:

#### My preference:



#### **Environment variables**

- PETSC\_DIR : different for different version numbers
- PETSC\_ARCH: for one version, this controls real/complex or opt/debug variants

#### Versions available at TACC

```
petsc/2.3.2petsc/2.3.2-debugpetsc/2.3.2-cxxpetsc/2.3.2-cxxdebugpetsc/2.3.3(default)petsc/2.3.3-debugpetsc/2.3.3-complexpetsc/2.3.3-complexdebugpetsc/2.3.3-cxxpetsc/2.3.3-cxxdebug
```

```
%% module load petsc/2.3.3-cxx
%% echo $PETSC_DIR
/opt/apps/petsc-intel9-2.3.3/2.3.3
%% echo $PETSC_ARCH
em64t-cxx
***
```



# Running

mpirun -np 3 petscprog <bunch of runtime options>
(or ibrun on Lonestar)

- -log\_summary : give runtime statistics
- -malloc\_dump -memory\_info : memory statistics
- -start\_in\_debugger : parallel debugging
- -options\_left : check for mistyped options
- -ksp\_type gmres (et cetera) : program control

more later



# **Documentation and examples**

- Manual in pdf form
- All man pages online

```
http://www-unix.mcs.anl.gov/petsc/petsc-as/snapshots/petsc-2.3.3/docs/manualpages/singleindex.html
```

start at http://www.mcs.anl.gov/petsc/

- Example codes, found online, and in \$PETSC\_DIR/src/mat/examples et cetera
- Sometimes consult include files, for instance \$PETSC\_DIR/include/petscmat.h



#### **Fortran**

Include files:

```
#include "include/finclude/petsc.h"
#include "include/finclude/petscmat.h"
#include "include/finclude/petscksp.h"
```

- Separate F90 version of various 'Get' routines
- Null pointers: C is tolerant for 0 or PETSC\_NULL, Fortran use PETSC\_NULL\_CHARACTER, PETSC\_NULL\_INTEGER et cetera. Example:

```
call PetscOptionsGetInt(PETSC_NULL_CHARACTER,"-name",
    N,flg,ierr)
```



Profiling, debugging



# Basic profiling

- -log\_summary flop counts and timings of all PETSc events
- -info all sorts of information, in particular

```
%% mpiexec yourprogram -info | grep malloc
```

- [0] MatAssemblyEnd\_SeqAIJ():
  - Number of mallocs during MatSetValues() is 0
- -log\_trace start and end of all events: good for hanging code



# Log summary: overall

	Max	Max/Min	Avg	Total
Time (sec):	5.493e-01	1.00006	5.493e-01	
Objects:	2.900e+01	1.00000	2.900e+01	
Flops:	1.373e+07	1.00000	1.373e+07	2.746e+07
Flops/sec:	2.499e+07	1.00006	2.499e+07	4.998e+07
Memory:	1.936e+06	1.00000		3.871e+06
MPI Messages:	1.040e+02	1.00000	1.040e+02	2.080e+02
MPI Msg Lengths:	4.772e+05	1.00000	4.588e+03	9.544e+05
MPI Reductions:	1.450e+02	1.00000		



# Log summary: details

	Max Ratio	Max R	atio	Max 1	Ratio	Avg len	%Т	%F	%M	%L	%R	%Т	%F	%M	%L	%R	Mflop/s
MatMult	100 1.0	3.4934e-02	1.0	1.28e+0	8 1.0	8.0e+02	6	32	96	17	0	6	32	96	17	0	255
MatSolve	101 1.0	2.9381e-02	1.0	1.53e+0	8 1.0	0.0e+00	5	33	0	0	0	5	33	0	0	0	305
MatLUFactorNum	1 1.0	2.0621e-03	1.0	2.18e+0	7 1.0	0.0e+00	0	0	0	0	0	0	0	0	0	0	43
MatAssemblyBegin	1 1.0	2.8350e-03	1.1	0.00e+0	0.0	1.3e+05	0	0	3	83	1	0	0	3	83	1	0
MatAssemblyEnd	1 1.0	8.8258e-03	1.0	0.00e+0	0.0	4.0e+02	2	0	1	0	3	2	0	1	0	3	0
VecDot	101 1.0	8.3244e-03	1.2	1.43e+0	8 1.2	0.0e+00	1	7	0	0	35	1	7	0	0	35	243
KSPSetup	2 1.0	1.9123e-02	1.0	0.00e+0	0.0	0.0e+00	3	0	0	0	2	3	0	0	0	2	0
KSPSolve	1 1.0	1.4158e-01	1.0	9.70e+0	7 1.0	8.0e+02	261	00	96	17	92	261	.00	96	17	92	194



# Debugging

- Use of CHKERRQ and SETERRQ for catching and generating error
- Use of PetscMalloc and PetscFree to catch memory problems;
   CHKMEMQ for instantaneous memory test (debug mode only)

