Mixed-effects models

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1. Take a look

```
ggplot(dfinal, aes(app.mthd, e.rel, colour = institute)) +
  geom_jitter(height = 0) +
  theme(legend.position = 'top')
## Warning: Removed 33 rows containing missing values (`geom_point()`).
                       AAFC
                                     ΑU
                                                   IGER
                                                                 MU
                                                                               USDA
                       ADAS
                                                                 NMI-WUR
                                                                               WUR
                                     CAU-LU
                                                   IMAG
           institute
                       ADAS-RR
                                     CRPA
                                                   INH-HAFL
                                                                 TEAGASC
                       ARDC
                                     DIAS
                                                   INRA
                                                                 UNIMI
                                                                 UNINA
                                      DiSAA-IT
                                                   IUL/FAT
  3 -
  2 -
e.rel
  1
  0 -
                                   bsth
                                                         os
                                           app.mthd
ggplot(dfinal, aes(app.mthd, err2, colour = institute)) +
  geom_jitter(height = 0) +
  theme(legend.position = 'top')
```

Warning: Removed 33 rows containing missing values (`geom_point()`).





Drop values > 100% applied TAN.

```
dim(dfinal)
```

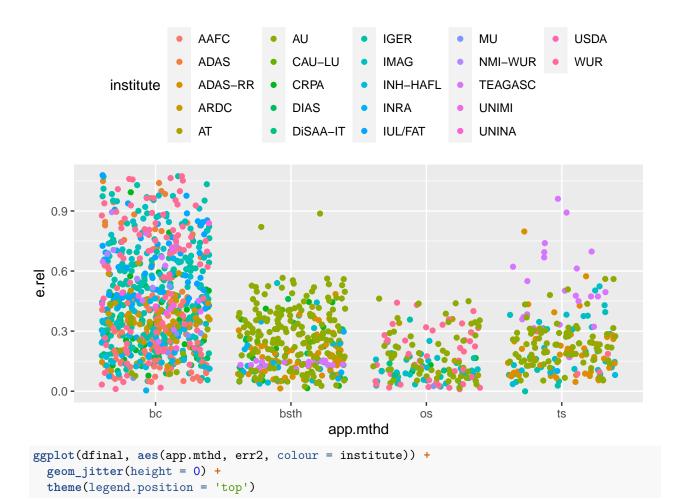
```
## [1] 1487 279
```

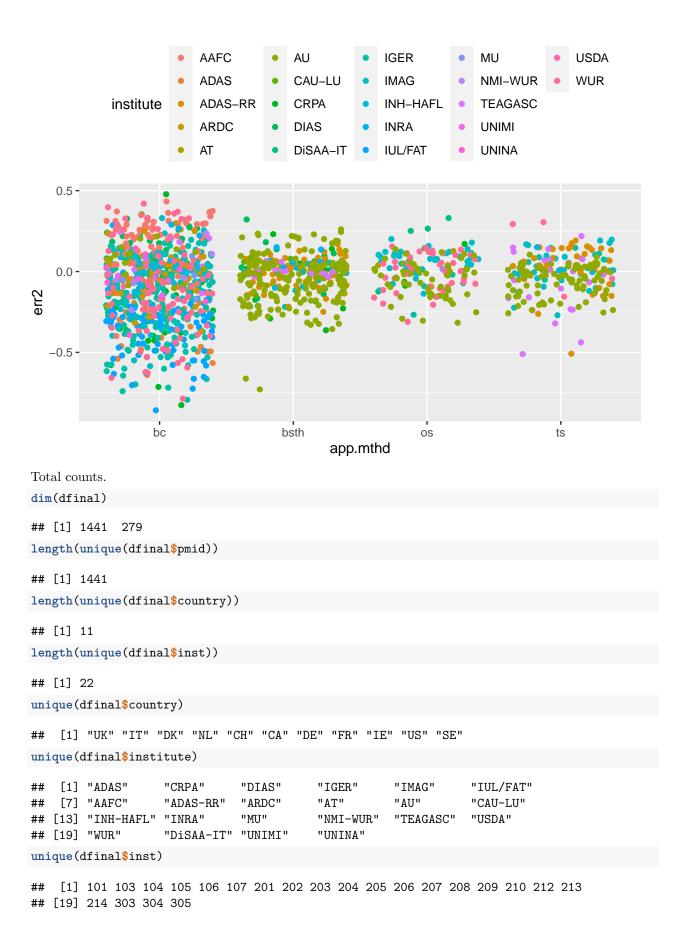
```
length(unique(dfinal$pmid))
```

```
## [1] 1487
```

```
dfinal <- dfinal[e.rel < 1.1, ]</pre>
```

```
ggplot(dfinal, aes(app.mthd, e.rel, colour = institute)) +
  geom_jitter(height = 0) +
  theme(legend.position = 'top')
```





2. Data prep

```
dfinal <- droplevels(dfinal[!is.na(e.rel), ])
dfinal$inst <- factor(dfinal$inst)
dfinal$inst.meas.tech <- interaction(dfinal$institute, dfinal$meas.tech)
dfinal$app.mthd <- factor(dfinal$app.mthd)

Get subset without crazy broadcast
dfinalb <- dfinal[app.mthd != 'bc', ]

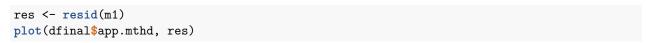
Subset without outliers.
dfinal[, z := abs(scale(e.rel)), by = c('inst', 'app.mthd')]
dfinalo <- dfinal[z < 2, ]
dfinalbo <- dfinal[app.mthd != 'bc' & z < 2, ]</pre>
```

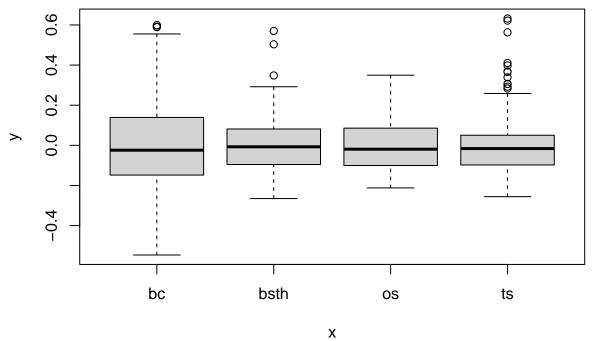
3. Basic variability and comparison of simplest predictors

```
m0 <- lmer(e.rel ~ (1|inst.meas.tech), data = dfinal)</pre>
m1 <- lmer(e.rel ~ app.mthd + (1|inst.meas.tech), data = dfinal)
m2 <- lm(e.rel ~ app.mthd, data = dfinal)
AIC(m0, m1, m2)
     df
               AIC
## m0 3 -421.8459
## m1 6 -678.7292
## m2 5 -438.8121
summary(m0)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ (1 | inst.meas.tech)
     Data: dfinal
##
##
## REML criterion at convergence: -427.8
## Scaled residuals:
      Min 1Q Median
                                3Q
                                       Max
## -2.1406 -0.6467 -0.1080 0.5530 3.3263
##
## Random effects:
## Groups
                  Name
                              Variance Std.Dev.
## inst.meas.tech (Intercept) 0.01762 0.1327
## Residual
                              0.04119 0.2030
## Number of obs: 1441, groups: inst.meas.tech, 37
##
## Fixed effects:
              Estimate Std. Error t value
## (Intercept) 0.32878
                           0.02539
summary(m1)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ app.mthd + (1 | inst.meas.tech)
     Data: dfinal
##
##
## REML criterion at convergence: -690.7
##
## Scaled residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
## -2.9593 -0.6684 -0.0838 0.5823 3.4226
##
## Random effects:
## Groups
                               Variance Std.Dev.
                   Name
## inst.meas.tech (Intercept) 0.01128 0.1062
## Residual
                               0.03410 0.1847
## Number of obs: 1441, groups: inst.meas.tech, 37
##
## Fixed effects:
##
                Estimate Std. Error t value
## (Intercept)
                0.43034
                            0.02195
                                      19.60
                                     -10.21
## app.mthdbsth -0.19508
                            0.01911
## app.mthdos
               -0.33559
                            0.01954
                                    -17.17
## app.mthdts
               -0.21475
                            0.02057 -10.44
##
## Correlation of Fixed Effects:
##
               (Intr) app.mthdb app.mthds
## app.mthdbst -0.291
## app.mthdos -0.227
                       0.436
## app.mthdts -0.236 0.616
                                 0.401
summary(m2)
##
## Call:
## lm(formula = e.rel ~ app.mthd, data = dfinal)
##
## Residuals:
##
                  1Q
        Min
                       Median
                                    3Q
                                            Max
## -0.44340 -0.13681 -0.03545 0.12378 0.71341
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 0.447225
                            0.007547
                                       59.26
                                               <2e-16 ***
## app.mthdbsth -0.212243
                            0.013699 - 15.49
                                               <2e-16 ***
## app.mthdos
                -0.284969
                            0.018189 -15.67
                                               <2e-16 ***
                            0.016491 -12.11
## app.mthdts
                -0.199741
                                               <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2074 on 1437 degrees of freedom
## Multiple R-squared: 0.235, Adjusted R-squared: 0.2334
## F-statistic: 147.1 on 3 and 1437 DF, p-value: < 2.2e-16
So, institute x measurement technique effect is around 11% of applied TAN (from model m1). Residuals are
```

So, institute x measurement technique effect is around 11% of applied TAN (from model m1). Residuals are large, around 18% of applied TAN. Presumably residuals are smaller for injection.





Perhaps, but could be worse (even more different).

Repeat without outliers.

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ (1 | inst.meas.tech)
      Data: dfinalo
##
##
## REML criterion at convergence: -561.6
##
## Scaled residuals:
                1Q Median
##
       Min
                                3Q
                                       Max
## -2.2634 -0.6354 -0.0813 0.5481
                                   3.2783
##
## Random effects:
## Groups
                   Name
                               Variance Std.Dev.
## inst.meas.tech (Intercept) 0.01756 0.1325
```

```
0.03685 0.1920
## Residual
## Number of obs: 1386, groups: inst.meas.tech, 37
## Fixed effects:
              Estimate Std. Error t value
## (Intercept) 0.31626
                         0.02528
                                  12.51
summary(m1o)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ app.mthd + (1 | inst.meas.tech)
##
     Data: dfinalo
## REML criterion at convergence: -868.9
##
## Scaled residuals:
      Min
           10 Median
                              3Q
                                     Max
## -3.2059 -0.6708 -0.0570 0.5943 3.3765
## Random effects:
## Groups
                             Variance Std.Dev.
                  Name
## inst.meas.tech (Intercept) 0.01173 0.1083
                             0.02927 0.1711
## Number of obs: 1386, groups: inst.meas.tech, 37
## Fixed effects:
              Estimate Std. Error t value
## (Intercept) 0.41738 0.02197
## app.mthdbsth -0.19011
                          0.01802 -10.55
## app.mthdos
             -0.34559
                          0.01856 -18.62
## app.mthdts -0.22455
                          0.01952 -11.51
## Correlation of Fixed Effects:
              (Intr) app.mthdb app.mthds
## app.mthdbst -0.271
## app.mthdos -0.211 0.432
## app.mthdts -0.217 0.616
                               0.394
summary(m2o)
##
## Call:
## lm(formula = e.rel ~ app.mthd, data = dfinalo)
## Residuals:
                 1Q Median
## -0.43103 -0.12915 -0.03158 0.11553 0.65919
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.434855 0.007289 59.66 <2e-16 ***
## app.mthdbsth -0.206815 0.013184 -15.69
                                            <2e-16 ***
## app.mthdos -0.282355 0.017672 -15.98 <2e-16 ***
## app.mthdts -0.202053 0.016012 -12.62 <2e-16 ***
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1965 on 1382 degrees of freedom
## Multiple R-squared: 0.2502, Adjusted R-squared: 0.2486
## F-statistic: 153.7 on 3 and 1382 DF, p-value: < 2.2e-16
Repeat without broadcast
m0b <- lmer(e.rel ~ (1 inst.meas.tech), data = dfinalb)</pre>
m1b <- lmer(e.rel ~ app.mthd + (1|inst.meas.tech), data = dfinalb)</pre>
m2b <- lm(e.rel ~ app.mthd, data = dfinalb)</pre>
AIC(mOb, m1b, m2b)
      df
## m0b 3 -722.8347
## m1b 5 -733.1104
## m2b 4 -702.5938
summary(m0b)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ (1 | inst.meas.tech)
##
     Data: dfinalb
##
## REML criterion at convergence: -728.8
## Scaled residuals:
               1Q Median
                                3Q
                                       Max
## -1.7406 -0.7082 -0.1489 0.5329 4.5316
## Random effects:
## Groups
                               Variance Std.Dev.
                  Name
## inst.meas.tech (Intercept) 0.003508 0.05922
## Residual
                               0.019267 0.13881
## Number of obs: 686, groups: inst.meas.tech, 19
## Fixed effects:
              Estimate Std. Error t value
## (Intercept) 0.19900
                          0.01659
summary(m1b)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ app.mthd + (1 | inst.meas.tech)
     Data: dfinalb
##
## REML criterion at convergence: -743.1
## Scaled residuals:
      Min
               1Q Median
                                3Q
                                       Max
## -1.8037 -0.7134 -0.1433 0.5686 4.5847
## Random effects:
## Groups
                             Variance Std.Dev.
                  Name
```

```
## inst.meas.tech (Intercept) 0.003163 0.05624
                               0.018580 0.13631
## Residual
## Number of obs: 686, groups: inst.meas.tech, 19
##
## Fixed effects:
##
               Estimate Std. Error t value
## (Intercept) 0.221512
                          0.016987 13.040
## app.mthdos -0.077669
                          0.016031 - 4.845
## app.mthdts
               0.004581
                          0.013043 0.351
##
## Correlation of Fixed Effects:
##
              (Intr) app.mthds
## app.mthdos -0.330
## app.mthdts -0.240 0.347
summary(m2b)
##
## Call:
## lm(formula = e.rel ~ app.mthd, data = dfinalb)
## Residuals:
       Min
                  1Q
                      Median
                                    30
## -0.24808 -0.10570 -0.03087 0.07986 0.71341
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.234982 0.007965 29.502 < 2e-16 ***
## app.mthdos -0.072725
                          0.014014 -5.190 2.78e-07 ***
## app.mthdts
              0.012503 0.012954 0.965
                                              0.335
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1445 on 683 degrees of freedom
## Multiple R-squared: 0.04971,
                                   Adjusted R-squared: 0.04693
## F-statistic: 17.86 on 2 and 683 DF, p-value: 2.741e-08
Less variability without broadcast.
Repeat without broadcast and without outliers.
m0bo <- lmer(e.rel ~ (1 inst.meas.tech), data = dfinalbo)
m1bo <- lmer(e.rel ~ app.mthd + (1|inst.meas.tech), data = dfinalbo)
m2bo <- lm(e.rel ~ app.mthd, data = dfinalbo)</pre>
AIC(mObo, m1bo, m2bo)
##
        df
                AIC
## m0bo 3 -820.8819
## m1bo 5 -839.2062
## m2bo 4 -794.6552
summary(m0bo)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ (1 | inst.meas.tech)
```

```
##
     Data: dfinalbo
##
## REML criterion at convergence: -826.9
## Scaled residuals:
##
      Min
           1Q Median
                               3Q
                                      Max
## -1.8556 -0.7180 -0.1071 0.5527 4.5344
##
## Random effects:
## Groups
                              Variance Std.Dev.
                  Name
## inst.meas.tech (Intercept) 0.002702 0.05198
## Residual
                              0.015898 0.12609
## Number of obs: 659, groups: inst.meas.tech, 18
##
## Fixed effects:
##
              Estimate Std. Error t value
## (Intercept) 0.18845
                          0.01485
                                    12.69
summary(m1bo)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ app.mthd + (1 | inst.meas.tech)
     Data: dfinalbo
##
## REML criterion at convergence: -849.2
## Scaled residuals:
##
      Min
           1Q Median
                               30
## -1.9745 -0.7268 -0.1155 0.5459 4.6448
##
## Random effects:
## Groups
                  Name
                              Variance Std.Dev.
## inst.meas.tech (Intercept) 0.002793 0.05285
## Residual
                              0.015074 0.12278
## Number of obs: 659, groups: inst.meas.tech, 18
##
## Fixed effects:
               Estimate Std. Error t value
## (Intercept) 0.214914 0.015932 13.490
## app.mthdos -0.087243
                          0.014847 -5.876
## app.mthdts -0.006317
                          0.012008 -0.526
## Correlation of Fixed Effects:
             (Intr) app.mthds
## app.mthdos -0.320
## app.mthdts -0.229 0.339
summary(m2bo)
##
## Call:
## lm(formula = e.rel ~ app.mthd, data = dfinalbo)
## Residuals:
##
                 1Q Median
       Min
                                   3Q
                                           Max
```

```
## -0.23339 -0.09825 -0.02822 0.07978 0.65919
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.228040
                        0.007374 30.925 < 2e-16 ***
## app.mthdos -0.075540
                        0.013082 -5.774 1.19e-08 ***
              0.004763
                          0.012081
                                   0.394
## app.mthdts
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1319 on 656 degrees of freedom
## Multiple R-squared: 0.05716,
                                  Adjusted R-squared: 0.05428
## F-statistic: 19.88 on 2 and 656 DF, p-value: 4.129e-09
4. ALFAM2 model residuals
m3 <- lmer(err2 ~ (1|inst.meas.tech), data = dfinal)
m4 <- lmer(err2 ~ app.mthd + (1 inst.meas.tech), data = dfinal)
summary(m0)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ (1 | inst.meas.tech)
     Data: dfinal
##
## REML criterion at convergence: -427.8
##
## Scaled residuals:
      Min
           1Q Median
                               ЗQ
                                      Max
## -2.1406 -0.6467 -0.1080 0.5530 3.3263
##
## Random effects:
## Groups
                              Variance Std.Dev.
                  Name
## inst.meas.tech (Intercept) 0.01762 0.1327
## Residual
                              0.04119 0.2030
## Number of obs: 1441, groups: inst.meas.tech, 37
##
## Fixed effects:
              Estimate Std. Error t value
## (Intercept) 0.32878
                          0.02539
                                    12.95
summary(m1)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ app.mthd + (1 | inst.meas.tech)
     Data: dfinal
##
## REML criterion at convergence: -690.7
## Scaled residuals:
```

Max

##

##

Min

1Q Median

-2.9593 -0.6684 -0.0838 0.5823 3.4226

3Q

```
## Random effects:
## Groups
                  Name
                              Variance Std.Dev.
## inst.meas.tech (Intercept) 0.01128 0.1062
## Residual
                              0.03410 0.1847
## Number of obs: 1441, groups: inst.meas.tech, 37
##
## Fixed effects:
##
               Estimate Std. Error t value
## (Intercept) 0.43034
                          0.02195 19.60
## app.mthdbsth -0.19508
                           0.01911 -10.21
## app.mthdos
              -0.33559
                           0.01954 -17.17
## app.mthdts
              -0.21475
                           0.02057 - 10.44
## Correlation of Fixed Effects:
##
              (Intr) app.mthdb app.mthds
## app.mthdbst -0.291
## app.mthdos -0.227 0.436
## app.mthdts -0.236 0.616
                                0.401
summary(m3)
## Linear mixed model fit by REML ['lmerMod']
## Formula: err2 ~ (1 | inst.meas.tech)
     Data: dfinal
##
## REML criterion at convergence: -902.5
## Scaled residuals:
            1Q Median
      Min
                               3Q
                                      Max
## -4.1054 -0.5388 0.1000 0.6074 3.5407
##
## Random effects:
## Groups
                              Variance Std.Dev.
                  Name
## inst.meas.tech (Intercept) 0.01207 0.1098
## Residual
                              0.02965 0.1722
## Number of obs: 1441, groups: inst.meas.tech, 37
##
## Fixed effects:
##
              Estimate Std. Error t value
## (Intercept) -0.03566
                        0.02111 -1.689
summary(m4)
## Linear mixed model fit by REML ['lmerMod']
## Formula: err2 ~ app.mthd + (1 | inst.meas.tech)
     Data: dfinal
## REML criterion at convergence: -904.7
##
## Scaled residuals:
               1Q Median
      Min
                               3Q
                                      Max
## -3.9679 -0.5474 0.0938 0.5880 3.6548
##
## Random effects:
## Groups
                              Variance Std.Dev.
                  Name
```

```
## inst.meas.tech (Intercept) 0.01161 0.1077
                               0.02929 0.1711
## Residual
## Number of obs: 1441, groups: inst.meas.tech, 37
##
## Fixed effects:
##
                Estimate Std. Error t value
## (Intercept) -0.05802
                            0.02173 - 2.670
## app.mthdbsth 0.03633
                            0.01783
                                      2.037
## app.mthdos
                 0.08261
                            0.01818
                                      4.544
                                      2.592
## app.mthdts
                 0.04962
                            0.01915
## Correlation of Fixed Effects:
               (Intr) app.mthdb app.mthds
## app.mthdbst -0.272
## app.mthdos -0.214 0.439
## app.mthdts -0.220 0.619
                                 0.404
AIC(m3, m4)
##
               AIC
      df
## m3 3 -896.5180
## m4 6 -892.7441
Reassuring that m3 is actually a better model than m4, meaning adding application method on top of ALFAM2
predictions doesn't help.
Again, exclude broadcast.
m3b <- lmer(err2 ~ (1|inst.meas.tech), data = dfinalb)
m4b <- lmer(err2 ~ app.mthd + (1 inst.meas.tech), data = dfinalb)
summary(m0b)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ (1 | inst.meas.tech)
##
      Data: dfinalb
##
## REML criterion at convergence: -728.8
##
## Scaled residuals:
##
       Min
                1Q Median
                                ЗQ
                                        Max
## -1.7406 -0.7082 -0.1489 0.5329 4.5316
##
## Random effects:
## Groups
                   Name
                               Variance Std.Dev.
## inst.meas.tech (Intercept) 0.003508 0.05922
                               0.019267 0.13881
## Number of obs: 686, groups: inst.meas.tech, 19
##
## Fixed effects:
               Estimate Std. Error t value
## (Intercept) 0.19900
                           0.01659
summary(m1b)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ app.mthd + (1 | inst.meas.tech)
```

```
##
     Data: dfinalb
##
## REML criterion at convergence: -743.1
## Scaled residuals:
##
      Min
           1Q Median
                            3Q
                                      Max
## -1.8037 -0.7134 -0.1433 0.5686 4.5847
##
## Random effects:
## Groups
                              Variance Std.Dev.
                  Name
## inst.meas.tech (Intercept) 0.003163 0.05624
## Residual
                              0.018580 0.13631
## Number of obs: 686, groups: inst.meas.tech, 19
##
## Fixed effects:
##
               Estimate Std. Error t value
## (Intercept) 0.221512 0.016987 13.040
## app.mthdos -0.077669 0.016031 -4.845
                                   0.351
## app.mthdts
              0.004581 0.013043
## Correlation of Fixed Effects:
             (Intr) app.mthds
## app.mthdos -0.330
## app.mthdts -0.240 0.347
summary(m3b)
## Linear mixed model fit by REML ['lmerMod']
## Formula: err2 ~ (1 | inst.meas.tech)
     Data: dfinalb
##
##
## REML criterion at convergence: -900.2
## Scaled residuals:
##
      Min
             1Q Median
                               3Q
                                      Max
## -4.8657 -0.5597 0.1550 0.6170 2.5881
##
## Random effects:
## Groups
                  Name
                              Variance Std.Dev.
## inst.meas.tech (Intercept) 0.00298 0.05459
                              0.01498 0.12239
## Residual
## Number of obs: 686, groups: inst.meas.tech, 19
##
## Fixed effects:
               Estimate Std. Error t value
##
## (Intercept) -0.008732 0.015141 -0.577
summary(m4b)
## Linear mixed model fit by REML ['lmerMod']
## Formula: err2 ~ app.mthd + (1 | inst.meas.tech)
##
     Data: dfinalb
##
## REML criterion at convergence: -886.8
##
```

```
## Scaled residuals:
##
      Min 1Q Median
                             3Q
                                      Max
## -4.8666 -0.5765 0.1516 0.6033 2.6082
## Random effects:
## Groups
                              Variance Std.Dev.
                  Name
## inst.meas.tech (Intercept) 0.002823 0.05313
## Residual
                              0.015029 0.12259
## Number of obs: 686, groups: inst.meas.tech, 19
##
## Fixed effects:
               Estimate Std. Error t value
## (Intercept) -0.012550 0.015805 -0.794
## app.mthdos 0.009106
                          0.014461 0.630
## app.mthdts
              0.005060
                        0.011744 0.431
##
## Correlation of Fixed Effects:
             (Intr) app.mthds
## app.mthdos -0.321
## app.mthdts -0.232 0.348
AIC(m3b, m4b)
##
      df
               ATC
## m3b 3 -894.2066
## m4b 5 -876.8290
Here too, m3b is better.
Exlude outliers
m3o <- lmer(err2 ~ (1|inst.meas.tech), data = dfinalo)
m4o <- lmer(err2 ~ app.mthd + (1|inst.meas.tech), data = dfinalo)
summary(m0o)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ (1 | inst.meas.tech)
##
     Data: dfinalo
##
## REML criterion at convergence: -561.6
## Scaled residuals:
      Min 1Q Median
                               3Q
                                      Max
## -2.2634 -0.6354 -0.0813 0.5481 3.2783
##
## Random effects:
## Groups
                  Name
                              Variance Std.Dev.
## inst.meas.tech (Intercept) 0.01756 0.1325
## Residual
                              0.03685 0.1920
## Number of obs: 1386, groups: inst.meas.tech, 37
## Fixed effects:
              Estimate Std. Error t value
## (Intercept) 0.31626 0.02528 12.51
```

```
summary(m1o)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ app.mthd + (1 | inst.meas.tech)
     Data: dfinalo
##
## REML criterion at convergence: -868.9
##
## Scaled residuals:
      Min
              1Q Median
                              3Q
## -3.2059 -0.6708 -0.0570 0.5943 3.3765
##
## Random effects:
## Groups
                  Name
                              Variance Std.Dev.
## inst.meas.tech (Intercept) 0.01173 0.1083
## Residual
                             0.02927 0.1711
## Number of obs: 1386, groups: inst.meas.tech, 37
## Fixed effects:
               Estimate Std. Error t value
## (Intercept) 0.41738
                          0.02197
                                   19.00
## app.mthdbsth -0.19011
                          0.01802 -10.55
## app.mthdos -0.34559
                          0.01856 -18.62
## app.mthdts -0.22455
                          0.01952 -11.51
##
## Correlation of Fixed Effects:
              (Intr) app.mthdb app.mthds
## app.mthdbst -0.271
## app.mthdos -0.211 0.432
                               0.394
## app.mthdts -0.217 0.616
summary(m3o)
## Linear mixed model fit by REML ['lmerMod']
## Formula: err2 ~ (1 | inst.meas.tech)
##
     Data: dfinalo
##
## REML criterion at convergence: -1053.7
##
## Scaled residuals:
      Min 1Q Median
                               3Q
                                     Max
## -4.4031 -0.5537 0.0885 0.6163 3.6573
##
## Random effects:
## Groups
           Name
                             Variance Std.Dev.
## inst.meas.tech (Intercept) 0.01171 0.1082
## Residual
                              0.02586 0.1608
## Number of obs: 1386, groups: inst.meas.tech, 37
## Fixed effects:
              Estimate Std. Error t value
## (Intercept) -0.02301
                          0.02074 - 1.109
```

summary(m4o)

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: err2 ~ app.mthd + (1 | inst.meas.tech)
     Data: dfinalo
##
## REML criterion at convergence: -1065.7
##
## Scaled residuals:
##
      Min
              1Q Median
                                3Q
                                       Max
## -4.2529 -0.5617 0.0782 0.6054 3.7979
##
## Random effects:
## Groups
                               Variance Std.Dev.
                   Name
## inst.meas.tech (Intercept) 0.01136 0.1066
                               0.02533 0.1592
## Number of obs: 1386, groups: inst.meas.tech, 37
##
## Fixed effects:
##
               Estimate Std. Error t value
## (Intercept) -0.04595
                            0.02130 -2.157
## app.mthdbsth 0.03249
                            0.01683
                                     1.930
## app.mthdos
                0.09350
                            0.01730
                                    5.405
## app.mthdts
                 0.05660
                            0.01820
                                     3.110
##
## Correlation of Fixed Effects:
##
               (Intr) app.mthdb app.mthds
## app.mthdbst -0.259
## app.mthdos -0.203 0.434
## app.mthdts -0.208 0.618
                                 0.396
AIC(m3o, m4o)
##
      df
                AIC
## m3o 3 -1047.673
## m4o 6 -1053.700
Here too, m3o is better.
Exclude broadcast and outliers.
m3bo <- lmer(err2 ~ (1|inst.meas.tech), data = dfinalbo)
m4bo <- lmer(err2 ~ app.mthd + (1 inst.meas.tech), data = dfinalbo)
summary(m0bo)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ (1 | inst.meas.tech)
##
     Data: dfinalbo
##
## REML criterion at convergence: -826.9
##
## Scaled residuals:
##
      Min
               1Q Median
                                3Q
                                       Max
## -1.8556 -0.7180 -0.1071 0.5527 4.5344
##
## Random effects:
## Groups
                   Name
                               Variance Std.Dev.
```

```
## inst.meas.tech (Intercept) 0.002702 0.05198
## Residual
                            0.015898 0.12609
## Number of obs: 659, groups: inst.meas.tech, 18
## Fixed effects:
##
             Estimate Std. Error t value
## (Intercept) 0.18845 0.01485 12.69
summary(m1bo)
## Linear mixed model fit by REML ['lmerMod']
## Formula: e.rel ~ app.mthd + (1 | inst.meas.tech)
     Data: dfinalbo
##
## REML criterion at convergence: -849.2
##
## Scaled residuals:
      Min 1Q Median
                            3Q
                                    Max
## -1.9745 -0.7268 -0.1155 0.5459 4.6448
##
## Random effects:
## Groups Name
                       Variance Std.Dev.
## inst.meas.tech (Intercept) 0.002793 0.05285
## Residual
                            0.015074 0.12278
## Number of obs: 659, groups: inst.meas.tech, 18
## Fixed effects:
              Estimate Std. Error t value
## (Intercept) 0.214914 0.015932 13.490
## app.mthdos -0.087243 0.014847 -5.876
## app.mthdts -0.006317 0.012008 -0.526
## Correlation of Fixed Effects:
            (Intr) app.mthds
## app.mthdos -0.320
## app.mthdts -0.229 0.339
summary(m3bo)
## Linear mixed model fit by REML ['lmerMod']
## Formula: err2 ~ (1 | inst.meas.tech)
    Data: dfinalbo
##
##
## REML criterion at convergence: -986.8
##
## Scaled residuals:
      Min 1Q Median
                            3Q
                                    Max
## -3.6817 -0.6016 0.1141 0.6133 2.7596
##
## Random effects:
## Groups Name Variance Std.Dev.
## inst.meas.tech (Intercept) 0.001377 0.03711
## Residual
                            0.012559 0.11207
## Number of obs: 659, groups: inst.meas.tech, 18
##
```

```
## Fixed effects:
##
                Estimate Std. Error t value
## (Intercept) -0.000692
                           0.011226 -0.062
summary(m4bo)
## Linear mixed model fit by REML ['lmerMod']
## Formula: err2 ~ app.mthd + (1 | inst.meas.tech)
      Data: dfinalbo
##
##
## REML criterion at convergence: -975.6
##
## Scaled residuals:
##
       Min
                1Q Median
                                ЗQ
                                       Max
## -3.7334 -0.6029 0.1017 0.5962
                                   2.8218
##
## Random effects:
##
  Groups
                   Name
                               Variance Std.Dev.
   inst.meas.tech (Intercept) 0.001244 0.03528
## Residual
                               0.012560 0.11207
## Number of obs: 659, groups: inst.meas.tech, 18
##
## Fixed effects:
##
                Estimate Std. Error t value
## (Intercept) -0.009483
                           0.011899
                                     -0.797
## app.mthdos
               0.021102
                           0.013250
                                      1.593
## app.mthdts
                0.012920
                           0.010865
                                      1.189
##
## Correlation of Fixed Effects:
##
              (Intr) app.mthds
## app.mthdos -0.379
## app.mthdts -0.285 0.337
AIC(m3bo, m4bo)
##
        df
                 AIC
## m3bo 3 -980.7708
## m4bo 5 -965.6264
Here too, m3bo is boetter.
```

5. "Institution effect"

Our best estimate of an "institution effect" is from m3, where we have corrected for different application methods, manure DM, pH, and weather using the ALFAM2 model.

With no outlier removal:

```
VarCorr(m1)

## Groups Name Std.Dev.
## inst.meas.tech (Intercept) 0.10621
## Residual 0.18467

VarCorr(m1b)

## Groups Name Std.Dev.
## inst.meas.tech (Intercept) 0.056243
```

```
## Residual
                               0.136309
VarCorr(m3)
## Groups
                   Name
                               Std.Dev.
## inst.meas.tech (Intercept) 0.10984
## Residual
                               0.17220
VarCorr(m3b)
## Groups
                   Name
                               Std.Dev.
## inst.meas.tech (Intercept) 0.054594
## Residual
                               0.122390
Excluding outliers:
VarCorr(m1o)
## Groups
                   Name
                               Std.Dev.
## inst.meas.tech (Intercept) 0.10829
## Residual
                               0.17109
VarCorr(m1bo)
## Groups
                   Name
                               Std.Dev.
## inst.meas.tech (Intercept) 0.052848
## Residual
                               0.122775
VarCorr(m3o)
## Groups
                   Name
                               Std.Dev.
## inst.meas.tech (Intercept) 0.10822
## Residual
                               0.16080
VarCorr(m3bo)
## Groups
                   Name
                               Std.Dev.
## inst.meas.tech (Intercept) 0.037109
```

0.112067

Residual