

Autonomous Vehicle Simulation (AVS) Laboratory, University of Colorado

Basilisk Technical Memorandum

Document ID: Basilisk-imu

INERTIAL MEASUREMENT UNIT C++ MODEL

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Status: Tested

Scope/Contents

The Basilisk IMU module is responsible for producing sensed body rates and acceleration from calculated values. The IMU module applies Gauss-Markov process noise to the true body rates and acceleration. A unit test has been written which validates MRP switching, static bias, process noise, discretization, saturation, spacecraft center of mass (CoM) offset, sensor misalignment, and bias walk bounds for both the gyroscope and accelerometer.

Rev	Change Description	Ву	Date
1.0	First draft	J. Alcorn	20170713
1.1	Added Math Documentation and User Guide. Implemented AutoTeX	S. Carnahan	20170713

Doc. ID: Basilisk-imu Page 1 of 8

Contents

1	Model Description	1
	1.1 Mathematical Model	1
	1.1.1 Error Modeling	
	1.1.2 Data Discretization	1
	1.1.3 Saturation	2
2	Model Functions	2
3	Model Assumptions and Limitations	1 2 2 2 2 3 4 7
4	Test Description and Success Criteria	3
5	Test Parameters	
	5.1 Test Results	4
6	User Guide	
	6.1 Code Diagram	7
	6.2 Variable Definitions	7

1 Model Description

The Basilisk IMU module imu_sensor.cpp is responsible for producing sensed body rates and acceleration from simulation truth values. Each check within test_imu_sensor.py sets initial attitude MRP, body rates, and accumulated Delta V and validates output for a range of time.

1.1 Mathematical Model

1.1.1 Error Modeling

The state which the simulation records for the spacecraft prior to sending that state to the IMU module is considered to be "truth". So, to simulate the errors found in real instrumentation, errors are added to the "truth" values for any measurement, $\mathbf{m}_{\mathrm{truth}}$, that the IMU deals with.

$$\mathbf{m}_{\text{measured}} = \mathbf{m}_{\text{truth}} + \mathbf{e}_{\text{noise}} + \mathbf{e}_{\text{bias}}$$
 (1)

1.1.2 Data Discretization

Because sensors record data digitally, that data can only be recorded in discrete chunks, rather than the (relatively) continuous values that the computer calculates at each time steps. In order to simulation real IMU behavior in this way, a least significant bit (LSB) value is accepted for both the gyro and the accelerometer. This LSB is applied as follows to any 3-dimensional measurement \mathbf{m} :

$$\mathbf{m}_{\text{discretized}} = (\text{LSB}) \left| \left| \frac{\mathbf{m}_{\text{measured}}}{(\text{LSB})} \right| \right|$$
 (2)

Where [] indicate the **floor()** function and LSB can be either the accelerometer or gyro least significant bit.

Doc. ID: Basilisk-imu Page 2 of 8

1.1.3 Saturation

Real sensors can also become saturated. This is modeled simply by comparing $\mathbf{m}_{discretized}$ to the high and low saturation values for the sensor:

$$\mathbf{m}_{\text{saturated}} = max \Big(\mathbf{m}_{\text{sat,min}}, \big(min(\mathbf{m}_{\text{discretized}}, \mathbf{m}_{\text{sat,max}}) \big) \Big)$$
 (3)

Note that this is actually only computed if $\mathbf{m}_{discretized}$ proves to be outside of its saturation bounds.

2 Model Functions

The mathematical description of the IMU are implemented in imu_sensor.cpp. This code performs the following primary functions

- **Spacecraft State Measurement**: The code provides measurements of the spacecraft state (angular and linear).
- Bias Modeling: The code adds instrument bias and bias random walk to the signals.
- **Noise Modeling**: The code calculates noise according to the Gauss Markov model if the user asks for it and provides a perturbation matrix.
- **Discretization**: The code discretizes the signal to emulate real digital instrumentation. The least significant bit (LSB) can be set by the user.
- **Saturation**: The code bounds the output signal according to user-specified maximum and minimum saturation values.
- Accelerometer Center of Mass Offset: The code can handle accelerometer placement other than the center of mass of the spacecraft.
- **IMU Misalignment**: The code can handle IMU placement in a frame with constant rotational offset from assumed IMU orientation.
- Bias Random Walk Bounds: The code bounds bias random walk per user-specified bounds.
- Interface: Spacecraft States: The code sends and receives spacecraft state information via the Basilisk messaging system.
- Interface: Spacecraft Mass: The code receives spacecraft mass information via the Basilisk messaging system.

3 Model Assumptions and Limitations

This code makes assumptions which are common to IMU modeling.

• Error Inputs: Because the error models rely on user inputs, these inputs are the most likely source of error in IMU output. Instrument bias would have to be measured experimentally or an educated guess would have to be made. The Guass-Markov noise model has a well-known assumptions and is generally accepted to be a good model for this application.

Doc. ID: Basilisk-imu Page 3 of 8

4 Test Description and Success Criteria

This test is located at SimCode/sensors/imu_sensor/_UnitTest/test_imu_sensor.py. In order to get good coverage of all the aspects of the module, the test is broken up into several parts:

- Gyro/Accelerometer I/O The check verifies basic I/O of body rates and acceleration. Initial attitude MRP, body rates, and Delta V are propagated and corresponding body rates, acceleration, DR, and DV are compared to module output.
- 2. MRP Switch The check validates that the module accounts for attitude MRP switching in calculation of body rates. Initial attitude MRP and body rates are propagated for a sufficient amount of time for the MRP to switch to the shadow set. The test verifies that the module sets the MRP switch flag to TRUE.
- 3. <u>Static Bias</u> The check validates static bias in gyro/accel measurements. Gyro and accelerometer static bias are set to nonzero values. Initial MRP, body rates, and DV are propagated. Module output is verified to contain data with static bias.
- 4. <u>Process Noise</u> The check verifies that the Gauss-Markov model applies noise of appropriate mean and standard deviation to the attitude coordinate output. This check does not consider bias random walk. Accelerometer and gyro noise standard deviations are set to nonzero values for each axis. Module output is verified by taking the standard deviation of output data and comparing to specified values.
- 5. <u>Discretization</u> The check verifies that the module correctly discretizes the gyro/accel data according to the specified least significant bit (LSB). LSB of gyro and accelerometer are set to nonzero values. Output is verifed to round input to nearest multiple of LSB.
- 6. <u>Saturation</u> The check verifies that the module saturates the output according to specified values. Gyro and accelerometer maximum output are set to nonzero values. Output is verified to not exceed specified saturation values for both negative and positive cases.
- 7. <u>Accelerometer Center of Mass Offset</u> The check validates that the accelerometer will give appropriate output based on an offset in center of mass from accelerometer. Sensed acceleration is given by the equation

$$\ddot{r}_{\text{sensed}} = \boldsymbol{\omega} \times (\boldsymbol{\omega} \times \boldsymbol{r}_{\text{SC}}) + \dot{\boldsymbol{\omega}} \times \boldsymbol{r}_{\text{SC}} + \ddot{r}_{B/N} \tag{4}$$

where ω is the spacecraft angular velocity vector, $r_{\rm SC}$ is the position vector of the IMU with respect to the spacecraft center of mass, and $\ddot{r}_{B/N}$ is the actual inertial acceleration of the spacecraft.

- 8. <u>IMU Misalignment</u> The check validates measurements taken when the IMU is not correctly aligned (i.e. the IMU measurements are taken in a frame with constant rotational offset from assumed IMU orientation).
- 9. <u>Bias Random Walk Bounds</u> The check verifies that the Gauss-Markov model correctly applies bias random walk to the gyro and accelerometer output. Specified walk bounds are validated.

5 Test Parameters

This section summarizes the specific error tolerances for each test. Error tolerances are determined based on whether the test results comparison should be exact or approximate due to integration or other reasons. Error tolerances for each test are summarized in table 4.

Doc. ID: Basilisk-imu Page 4 of 8

Table 2: Error tolerance for each test.

Test	Tolerated Error
Gyro/Accelerometer I/O	1.0e-06
MRP Switching	-
Static Bias	1.0e-03
Process Noise	1.0e-03
Discretization	1.0e-05
Saturation	1.0e-03
Accelerometer Center of Mass Offset	1.0e-05
IMU Misalignment	1.0e-04
Bias Walk Bounds	-

5.1 Test Results

All checks within test_imu_sensor.py passed as expected. Table 3 shows the test results. Figures 5.1 and 5.1 show the module output for the process noise and walk bounds checks, respectively.

Table 3: Test results

Test	Pass/Fail	Notes
Gyro/Accelerometer I/O	Passed	
MRP Switching	Passed	
Static Bias	Passed	
Process Noise	Passed	
Discretization	Passed	
Saturation	Passed	
Accelerometer Center of Mass Offset	Passed	
IMU Misalignment	Passed	
Bias Walk Bounds	Passed	

Doc. ID: Basilisk-imu Page 5 of 8

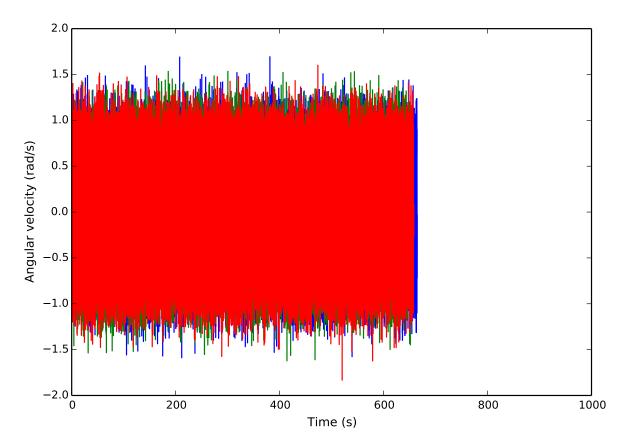


Fig. 1: Module output of noise standard deviation check

Doc. ID: Basilisk-imu Page 6 of 8

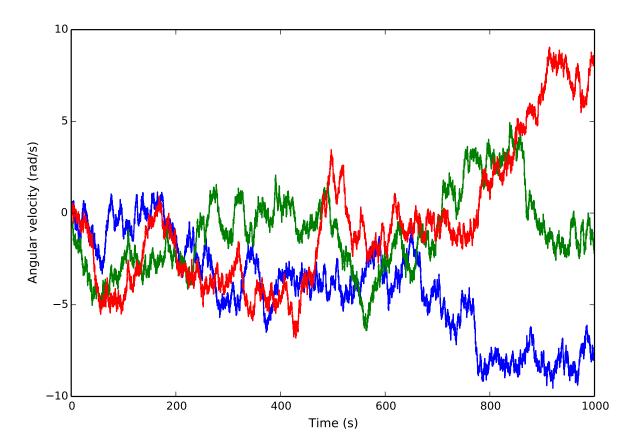


Fig. 2: Module output for random walk bounds check

Doc. ID: Basilisk-imu Page 7 of 8

6 User Guide

This section contains conceptual overviews of the code and clear examples for the prospective user.

6.1 Code Diagram

The diagram in Fig. 3 demonstrates the basic logic of the IMU module. There is additional code that deals with auxiliary functions. An example of IMU use is given in test_imu_sensor.py in the imu_sensor_UnitTest folder. Application of each IMU function follows a simple, linear progression until realistic IMU outputs are achieved and sent out via the messaging system.

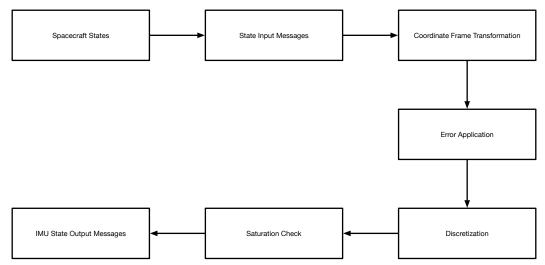


Fig. 3: A pseudo-code diagram demonstrating the flow of inputs and outputs in the IMU module.

6.2 Variable Definitions

The variables in Table 4 are available for user input. Variables used by the module but not available to the user are not mentioned here. Variables with default settings do not necessarily need to be changed by the user, but may be.

Doc. ID: Basilisk-imu Page 8 of 8

Table 4: Definition and Explanation of Variables Used.

Variable	LaTeX Equivalent	Variable Type	Notes
InputStateMsg	N/A	string	Default setting: "inertial_state_output". This is the message from which the IMU receives spacecraft inertial data.
OutputDataMsg	N/A	string	Default setting: "imu_meas_data". This message contains the information output by the IMU.
InputMassMsg	N/A	string	Default setting: "spacecraft_mass_props". This is the message from which the IMU received spacecraft mass data.
SensorPos_B	N/A	double [3]	[m] Required input - no default. This is the sensor position in the body frame relative to the body frame.
roll, pitch, yaw	N/A	double, double, dou- ble	Default setting: (0,0,0). To set non-zero initial angles between imu and spacecraft body, call setBodyToPlatformDCM(roll, pitch, yaw)
dcm_PB	N/A	double [3][3]	Default setting: Identity. Setting dcm_PB is equivalent to calling setBody-ToPlatformDCM(roll, pitch yaw) above. Use one method or the other.
senRotBias	$\mathbf{e}_{ ext{bias}}$	double [3]	[r/s] Default setting: zeros. This is the rotational sensor bias value for each axis.
senTransBias	$\mathbf{e}_{ ext{bias}}$	double [3]	[m/s2] Default setting: zeros. This is the translational sensor bias value for each axis
senRotMax	$\mathbf{m}_{\mathrm{sat,max}}$	double	[r/s] Required input - no default. This is the gyro saturation value.
senTransMax	$\mathbf{m}_{\mathrm{sat,max}}$	double	[m/s2] Required input - no default. This is the accelerometer saturation value.
PMatrixAccel	N/A yet	double [3][3]	Default: zeros. This is the covariance matrix used to perturb the state.
PMatrixGyro	N/A yet	double [3][3]	Default: zeros. This is the covariance matrix used to perturb the state.
walkBoundsGyro	N/A yet	double [3]	Default: zeros. This is the "3-sigma" errors to permit for gyro states
walkBoundsAccel	N/A yet	double [3]	Default: zeros. This is the "3-sigma errors ot permit for acceleration states.
accelLSB	(LSB)	double	Default: 0.0. This is the discretization value (least significant bit) for acceleration. Zero indicates no discretization.
gyroLSB	(LSB)	double	Default: 0.0. This is the discretization value (least significant bit) for acceleration. Zero indicates no discretization.