

I) Fprop \rightarrow

for layer L ,

$$\textcircled{1} \quad z^L = w^L \times a^{L-1} + b^L$$

$(n^L, m) \quad (n^L, n^{L-1}) \quad (n^{L-1}, m) \quad (n^L, m)$

$$\textcircled{2} \quad a^L = g^L(z^L), \quad g^L() \text{ is some nonlinearity.}$$

$(n^L, m) \quad (n^L, m)$

③) Save (a^L, z^L, w^L, b^L) to dictionary.
 if return (a^L)

if layer L is the last layer,

i) compute cost (scalar) J

ii) Save $(a^L, z^L, w^L, b^L), (J)$ to dictionary.

iii) return (a^L, J)

II) Back Prop \rightarrow

for Layer L ,

① If L is the last layer,

$$a) \quad \Delta a^L = d^T J$$

$(\text{scalar}) \quad (\text{scalar})$

$$b) \quad \Delta z^L = \Delta a^L \cdot a^{L'} \quad , \quad a^{L'} = g^{L'}(z) = \frac{\partial}{\partial z} (\text{non linearity})$$

$(n^L, m) \quad (\text{scalar}) \quad (n^L, m)$

$$c) \quad \Delta a^{L-1} = w^{L^T} \times \Delta z^L$$

$(n^{L-1}, m) \quad (n^{L-1}, n^L) \quad (n^L, m)$

$$d) \quad \Delta b^L = \Delta z^L \rightarrow (n^L, m)$$

$$\Delta w^L = \Delta z^L \times a^{L-1^T}$$

$(n^L, n^{L-1}) \quad (n^L, m) \quad (m, n^{L-1})$

② If L is not last layer,

$$a) \quad \Delta a^L = \Delta a^L \text{ from previous iteration.}$$

...

same as before.

III) Grad. dec. \rightarrow

for any layer L ,

$$w^L = w^L - \eta \Delta w^L$$

$$b^L = b^L - \eta \Delta b^L$$

where η is the learning rate.

IV) Loop \rightarrow

Loop over I \rightarrow II \rightarrow III till specified epochs.