Searching and Sorting

December 1, 2021

Administrative Notes

Searching and sorting

Why do we care about them so much?

- They're common problems that happen a lot when you're dealing with giant data sets - which is happening more and more
- They've been studied a lot, for decades, and we now know that there are good solutions and not-so-good solutions
-

Now, let's talk about sorting lists of elements

All of our examples tonight use integers, but it all works the same way. As long as all elements in the list are of the same type, you can sort them into an order.

An easy one to understand - **bubble sort.**

Suppose you have a list of integers:

[4, -2, 19, 944, 27, 3]

You can go through the list and compare each pair of numbers. If the first one is larger than the second one, swap them.

When you have gone through the list one time, you will have "bubbled" the largest

Element up to the end of the list.

An example - first, on the slide; then some coding

Original list :[4, -2, 19, 944, 27, 3]

Bubble sort - "bubble" the largest number left each time to the end of the list

-2, 4, 19, 944, 27, 3

-2, 4, 19, 27, 944, 3

-2, 4, 19, 27, 3, 944

_____

-2, 4, 19, 3, 27, 944

We can write bubble sort as an iterative function, or as a recursive one

```python
if (numbers[j]>numbers[j+1]):
        #swap the numbers - we'll use a temp

        temp = numbers[j]
        numbers[j] = numbers [j+1]
        numbers[j+1] = temp
    return(numbers)
```

```python
def iterative_bubble_sort (numbers):
# go through the entire list of numbers
    for i in range(len(numbers)-1,0, -1):
        for j in range(i):
```

Recursive Bubble Sort

```python
def recursive_bubble_sort (numbers):
    if len(numbers) <= 1:
        return(numbers)
    else:
        #bubble the largest number to the end
        for j in range(len(numbers)-1):
            if numbers[j] > numbers[j+1]:
                temp = numbers[j]
                numbers[j] = numbers[j+1]
                numbers[j+1] = temp
        #then recursively call the function with
        #all but the last element of the list
        new_nums = recursive_bubble_sort(numbers[:-1])
        #add the last element back on
        sorted_list = new_nums + numbers[-1:]
        return(sorted_list)
```

Stopping the sort

The list is sorted if there are no swaps made during a pass through the list

- Think about why

The previous code continues through even after the list is sorted.

We can be more efficient by converting the outer "for" loop into a "while" loop and using a boolean flag

- Let's look at the code

[4, -2, 5, 19, 27, 944]

[-2, 4, 5, 19, 27, 944]

Selection Sort

Now, a different type of sorting.

This time, we're going to search through the entire list to find the smallest element, and then swap it with the first element in the list.

We then go through the rest of the list and select the smallest remaining element. We put this into the next available slot, and repeat until the list is sorted

We "select" the smallest element from the list, and thus this called a

...selection sort

[4, -2, 5, 944, 27, 3]

Swap -2 with the first element

[-2, 4, 5, 944, 27, 3]

[-2, 3, 5, 944, 27, 4]

[-2, 3, 4, 944, 27, 5]

[-2, 3, 4, 5, 27, 944]

Selection sort, on paper and as an iterative function

Original list :[4, -2, 19, 944, 27, 3]

-2, 4, 19, 944, 27, 3

-2, 3, 19, 944, 27, 4

-2, 3, 4, 944, 27, 19

-2, 3, 4, 19, 27, 944

```python
def iterative_selection_sort(numbers):
    for i in range(len(numbers)):

        #find the smallest element remaining in the
        #unsorted list. Start by presuming it's the
        #first element
        smallest = i
        for j in range(i + 1, len(numbers)):
            if numbers[smallest] > numbers[j]:
                smallest = j

        # When the loop is done, we know that smallest is
        # the index of the smallest value. Swap it
        # with the first element
        temp = numbers[smallest]
        numbers[smallest] = numbers[i]
        numbers[i] = temp
```

Can we implement *this* as a recursive function?

```python
def recursive_selection_sort (nums):
    #The base case is: a list of length 0 or 1 is sorted
    if len(nums) <= 1:
        return nums
    else:
        #the core of the algorithm is the same
        #as the iterative routine
        index_of_smallest = 0
        for j in range(1, len(nums)):
            if nums[j] < nums[index_of_smallest]:
                index_of_smallest = j
```

```python
        # now swap the smallest element found with the first
        temp = nums[0]
        nums[0] = nums[index_of_smallest]
        nums[index_of_smallest] = temp
        #now make the recursive call with the first
        #element stripped out
        r = recursive_selection_sort(nums[1:])
        results = nums[:1] + r
        return results
```

You cannot stop selection sort early

You can stop bubble sort early BECAUSE you can keep track of how many swaps you've made each time through and you KNOW that if go through without making any swaps, you're done.

Not true for selection sort. All you can do is go through the list, and know that the first value is the smallest. You don't know anything about any other values in the list.

One more sorting algorithm: QuickSort

The idea here: pick an element in the list. Call this the "pivot"

Sort the list so that every item less than the pivot is before the pivot - "to the left of" the pivot, if you will

Every item greater than the pivot will be to the right - after the pivot in the list.

Note that there is no guarantee the items to the left and to the right of the pivot will be in any order at all.

So you have to recursively call the quicksort routine on the left side of the pivot, and then on the right.

Spoiler alert: this is called quicksort because it works faster than the other algorithms

A paper example before the code

Original list :[4, -2, 19, 944, 27, 3]

Less: -2, 3

Equal: 4

Greater: 19, 944, 27

Recursive call: Less; Greater

Quicksort code - this works best as a recursive function

```
def quicksort(list_of_nums):                #define three empty lists, for elements
    #base case - a list of length one is  greater than the pivot, less than the pivot,
sorted                                      and equal to the pivot
    if len(list_of_nums) <= 1:                  less = []
        return(list_of_nums)                    equal = []
    #recursive case                             greater =[]
    else:
        #pick a pivot - the first element
        pivot = list_of_nums[0]
```

Quicksort (continued)

```python
# go through the list and put each
element in the proper list
    for i in range(len(list_of_nums)):
        if list_of_nums[i] > pivot:

greater.append(list_of_nums[i])
```

```python
        elif list_of_nums[i] == pivot:

equal.append(list_of_nums[i])
        else:
            less.append(list_of_nums[i])
        results = quicksort(less) +
equal + quicksort(greater)
        return(results)
```

Searching - linear and binary

Linear search is what python uses as a default

Go through the list, one item at a time, in order from first element to last

Stop when you find the right element, or return failure if you never find it

It works, but it's not efficient

Binary Search

If the list is already sorted, we can search much more efficiently.

Go to the middle element of the list. List [len(list)//2]

Is this greater than the element we're searching for? If it is, just look at the first half of the original list. If not, just look at the right half. If this element is exactly what we're looking for, stop.

So now we have a recursive call to a list half the size of the original list

We'll look at the code in a minute, but we'll find the element we're looking for, or find it isn't there, in log(base2) of the length of the original list operations.

Code for binary search

```python
def binary_search (numbers, target):
    if len(numbers)//2 == 0:
        return -1
    if numbers[len(numbers)//2] == target:
        return len(numbers)//2
    elif numbers[len(numbers)//2] > target:
        return binary_search(numbers[:len(numbers)//2], target)
    else:
        return binary_search(numbers[len(numbers)//2:], target)
```