HW #1 Due Feb. 2

Discrete Grading Policy. 5 points for each: 2 points for trying, 3 points if partial answer, 5 point if correct.

- 1. Consider the following sequence of rotations:
 - 1) Rotate by α_1 about the current x-axis.
 - 2) Rotate by α_2 about the world *y*-axis.
 - 3) Rotate by α_3 about the current z-axis.
 - 4) Rotate by α_4 about the world x-axis.

Write the matrix product that will give the resulting rotation matrix (do not perform the matrix multiplication). Use the composition rule to derive each step.

2. Verify Equation (2-11) for similarity transformations, namely

$$B = (R_1^0)^{-1} A R_1^0$$
.

(If A is the matrix representation of a given linear transformation in $o_0x_0y_0z_0$ and B is the representation of the same linear transformation in $o_1x_1y_1z_1$ then A and B are related as (2-11))

3. Suppose that three coordinate frames $o_1x_1y_1z_1$, $o_2x_2y_2z_2$, and $o_3x_3y_3z_3$ are given, and suppose

$$R_3^2 = \begin{bmatrix} c_{\theta} & 0 & s_{\theta} \\ 0 & 1 & 0 \\ -s_{\theta} & 0 & c_{\theta} \end{bmatrix}, R_3^1 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{\phi} - s_{\phi} \\ 0 & s_{\phi} & c_{\phi} \end{bmatrix}$$

Find the matrix R_2^1 .

4. Given a rotation matrix $R \in SO(3)$

$$R = \begin{bmatrix} 0.0802 & -0.3801 & 0.2644 \\ 2.1764 & 1.0114 & -0.5641 \\ 0.2724 & 0.3050 & 0.9084 \end{bmatrix}$$

Let V be a set of vectors, and $V \subset \mathbb{R}$, $V = \left\{ v \in V \mid \frac{Rv \cdot v}{\left\|v\right\|^2} = \frac{1}{2} \right\}$. You may use MATLAB, etc.

- 1) Use two-argument arctangent function to specify the Euler angles (ϕ, θ, φ) of the rotation transformation R
- 2) Give a physical interpretation of the set V.

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- 5. Let $k = \begin{bmatrix} 0.5378, \ 0.2534, \ 0.8041 \end{bmatrix}^T$, $\theta = 30^{\circ}$. Find $R_{k,\theta}$.
- 6. Consider the diagram of a rotary inverted pendulum in Figure 1. The center of a rotary wheel is set up at the origin of a fixed frame oxyz. A frame $o_1x_1y_1z_1$ is fixed to the edge of the first arm, and another frame $o_2x_2y_2z_2$ is fixed to the edge of the second arm. Lengths and angles are specified in Fig.1. Find the homogeneous transformations relating each of these frames the world frame oxyz. Find the homogeneous transformations relating $o_1x_1y_1z_1$ and $o_2x_2y_2z_2$.

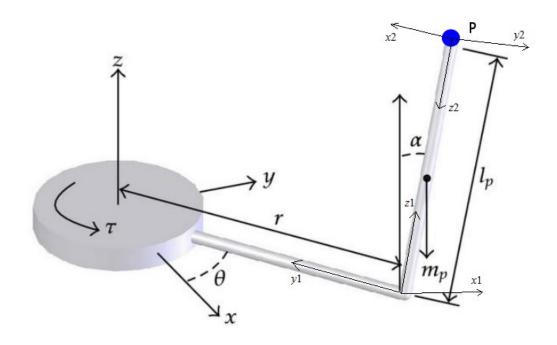


Figure 1. A rotary inverted pendulum