# IS5 in R: Relationships Between Categorical Variables—Contingency Tables (Chapter 3)

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# Introduction and background

This document is intended to help describe how to undertake analyses introduced as examples in the Fifth Edition of *Intro Stats* (2018) by De Veaux, Velleman, and Bock. More information about the book can be found at http://wps.aw.com/aw\_deveaux\_stats\_series. This file as well as the associated R Markdown reproducible analysis source file used to create it can be found at http://nhorton.people.amherst.edu/is5.

This work leverages initiatives undertaken by Project MOSAIC (http://www.mosaic-web.org), an NSF-funded effort to improve the teaching of statistics, calculus, science and computing in the undergraduate curriculum. In particular, we utilize the mosaic package, which was written to simplify the use of R for introductory statistics courses. A short summary of the R needed to teach introductory statistics can be found in the mosaic package vignettes (http://cran.r-project.org/web/packages/mosaic). A paper describing the mosaic approach was published in the R Journal: https://journal.r-project.org/archive/2017/RJ-2017-024.

## Chapter 3: Relationships Between Categorical Variables-Contingency Tables

#### Section 3.1: Contingency Tables

```
library(mosaic)
library(readr)
library(janitor)
OKCupid <- read csv("http://nhorton.people.amherst.edu/is5/data/OKCupid CatsDogs.csv", skip = 1) %>%
  clean names()
## Parsed with column specification:
## cols(
##
     CatsDogsBoth = col_character(),
##
     Gender = col_character(),
     `drugsY/N` = col character(),
##
     `smokesY/N` = col_character()
##
## )
# If you look at the data set, you'll see that the first line is "Col1", "Col2", etc
tally(~ cats dogs both + gender, margin = TRUE, data = OKCupid)
##
                 gender
## cats_dogs_both
                      F
                            M Total
                          577
##
         Has Both
                    897
                               1474
##
         Has cats 3412
                         2388
                               5800
##
         Has dogs 3431 3587 7018
                  16377 29274 45651
##
         <NA>
```

24117 35826 59943

##

Total

```
tally(~ cats_dogs_both + gender, format = "percent", margin = TRUE, data = OKCupid)
##
                 gender
## cats_dogs_both
                            F
                                                Total
                                        Μ
##
         Has Both
                    1.4964216
                                0.9625811
                                            2.4590027
##
         Has cats
                    5.6920741
                                3.9837846
                                            9.6758587
##
         Has dogs
                    5.7237709
                                5.9840182
                                           11.7077891
##
         <NA>
                   27.3209549 48.8363946 76.1573495
                   40.2332216 59.7667784 100.0000000
##
         Total
tally(~ cats_dogs_both | gender, format = "percent", margin = TRUE, data = OKCupid)
##
                 gender
## cats_dogs_both
                                      М
                           F
##
         Has Both
                               1.610562
                    3.719368
##
         Has cats 14.147697
                               6.665550
##
         Has dogs 14.226479
                              10.012282
##
         <NA>
                   67.906456 81.711606
##
         Total
                  100.000000 100.000000
tally(~ gender | cats_dogs_both, format = "percent", margin = TRUE, data = OKCupid)
##
          cats_dogs_both
## gender
           Has Both Has cats Has dogs
                                              <NA>
##
            60.85482 58.82759 48.88857
                                          35.87435
    F
##
            39.14518 41.17241 51.11143 64.12565
    Total 100.00000 100.00000 100.00000 100.00000
Example 3.1: Exploring Marginal Distributions
SuperBowl <- read_csv("http://nhorton.people.amherst.edu/is5/data/Watch_the_Super_bowl.csv", skip = 1)
## Parsed with column specification:
## cols(
    Plan = col_character(),
##
    Sex = col_character()
## )
tally(~ Plan + Sex, data = SuperBowl)
##
                Sex
## Plan
                 Female Male
##
     Commercials
                    156
                          81
                    200
                         279
##
     Game
##
     Wont Watch
                    160 132
```

Example 3.2: Exploring Percentages: Children and First-Class Ticket Holders First?

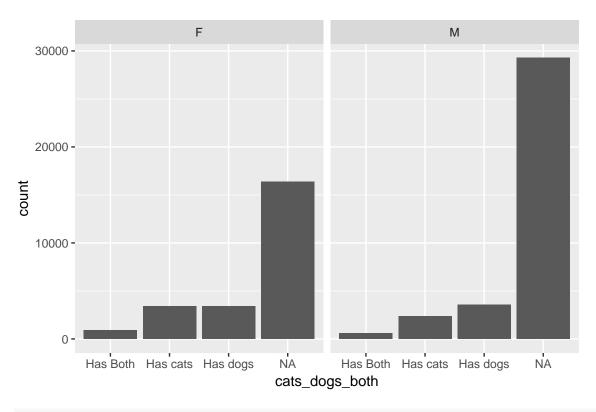
```
## Parsed with column specification:
## cols(
    Name = col_character(),
##
##
     Survived = col_character(),
    Boarded = col_character(),
##
    Class = col_character(),
##
    MWC = col_character(),
##
##
    Age = col_double(),
##
     Adut_or_Chld = col_character(),
##
    Sex = col_character(),
    Paid = col_double(),
##
##
    Ticket_No = col_character(),
##
    Boat_or_Body = col_character(),
##
     Job = col_character(),
##
    Class_Dept = col_character(),
    Class_Full = col_character()
##
## )
tally(~ Class + Survived, format = "percent", margin = TRUE, data = Titanic)
          Survived
##
## Class
                Alive
                            Dead
                                      Total
                        5.570652 14.673913
##
             9.103261
     1
##
             5.389493
                       7.518116 12.907609
##
    3
             8.152174 24.003623 32.155797
##
             9.601449 30.661232 40.262681
    Crew
    Total 32.246377 67.753623 100.000000
##
tally(~ Survived | Class, format = "percent", margin = TRUE, data = Titanic)
##
           Class
## Survived
                              2
      Alive 62.03704 41.75439 25.35211
                                           23.84702
##
##
             37.96296 58.24561 74.64789
##
      Total 100.00000 100.00000 100.00000 100.00000
tally(~ Class | Survived, format = "percent", margin = TRUE, data = Titanic)
##
          Survived
## Class
                Alive
                            Dead
##
     1
            28.230337
                        8.221925
##
     2
            16.713483 11.096257
##
     3
            25.280899 35.427807
            29.775281 45.254011
##
     Crew
     Total 100.000000 100.000000
```

Titanic <- read\_csv("http://nhorton.people.amherst.edu/is5/data/Titanic.csv")</pre>

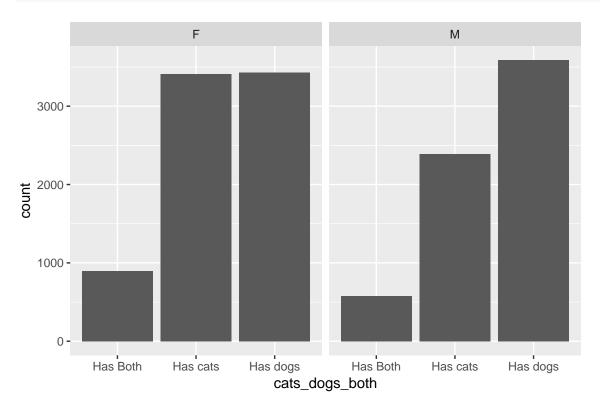
#### Section 3.2: Conditional Distributions

See displays on 68-69.

gf\_bar(~ cats\_dogs\_both | gender, data = OKCupid)



#There are many who don't own either
gf\_bar(~ cats\_dogs\_both | gender, data = filter(OKCupid, cats\_dogs\_both != "NA"))

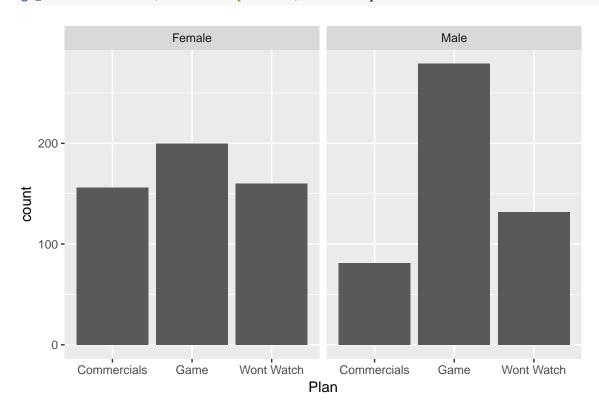


Example 3.3: Finding Conditional Distributions: Watching the Super Bowl

```
tally(~ Plan + Sex, margin = TRUE, data = SuperBowl)
##
                Sex
## Plan
                 Female Male Total
##
     Commercials
                     156
                           81
                                237
                          279
                                479
##
     Game
                     200
##
     Wont Watch
                     160
                          132
                                292
##
     Total
                     516
                          492
                               1008
tally(~ Plan | Sex, format = "percent", data = SuperBowl)
##
                Sex
## Plan
                    Female
                               Male
##
     Commercials 30.23256 16.46341
##
                  38.75969 56.70732
##
     Wont Watch 31.00775 26.82927
```

Example 3.4: Looking for Associations Between Variables: Still Watching the Super Bowl





### **Examining Contingency Tables**

See displays on page 72.

```
FishDiet <- read_csv("http://nhorton.people.amherst.edu/is5/data/Fish_diet.csv", skip = 1) %>%
clean_names()
## Parsed with column specification:
## cols(
    `Diet:Counts` = col_character(),
   `Cancer:Counts` = col_character()
## )
tally(~ diet_counts + cancer_counts, data = FishDiet)
##
              cancer_counts
## diet_counts No Yes
##
      Large
                507
                     42
##
      Moderate 2769 209
##
      Never
               110
                     14
      Small
               2420 201
##
Random Matters
Seee display on page 74.
Nightmares <- read_csv("http://nhorton.people.amherst.edu/is5/data/Nightmares.csv", skip = 1)
## Parsed with column specification:
    Side = col_character(),
    Dream = col_character()
## )
Nightmares <- Nightmares %>%
  mutate(Dream = ifelse(Dream == "N", "Nightmare", "SweetDreams"))
tally(~ Side + Dream, data = Nightmares)
##
       Dream
## Side Nightmare SweetDreams
     L
                9
##
      R.
                           35
                6
Section 3.3: Displaying Contingency Tables
tally(~ Class + Survived, format = "count", data = Titanic)
##
         Survived
## Class Alive Dead
##
     1
           201 123
##
    2
            119 166
            180 530
##
    3
```

##

Crew

212 677

```
tally(~ Class + Survived, format = "percent", data = Titanic)
```

```
## Survived

## Class Alive Dead

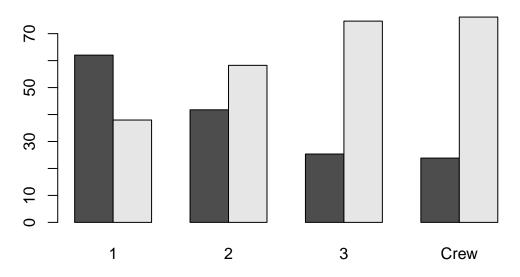
## 1 9.103261 5.570652

## 2 5.389493 7.518116

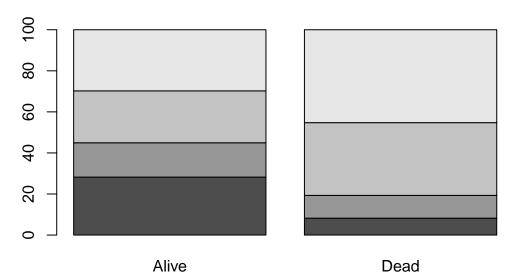
## 3 8.152174 24.003623

## Crew 9.601449 30.661232
```

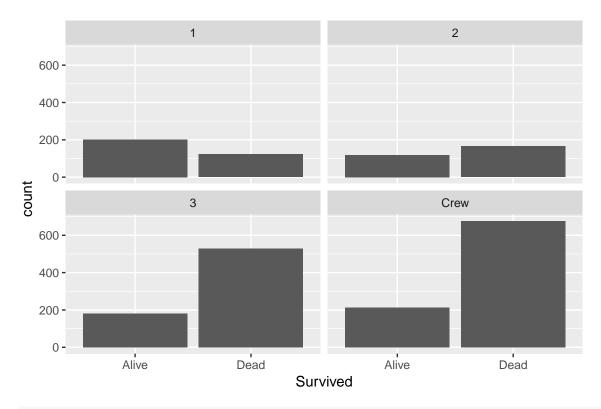
barplot(tally(~ Survived | Class, format = "percent", data = Titanic), beside = TRUE)



barplot(tally(~ Class | Survived, format = "percent", data = Titanic))



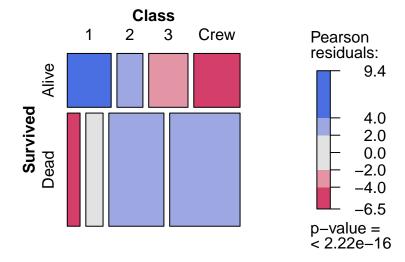
gf\_bar(~ Survived | Class, format = "percent", data = Titanic)



 $\#gf\_bar$  automatically facets

```
vcd::mosaic(tally(~ Survived + Class, data = Titanic),
    main = "Mosaic plot of Class by Survival",
    shade = TRUE)
```

# Mosaic plot of Class by Survival



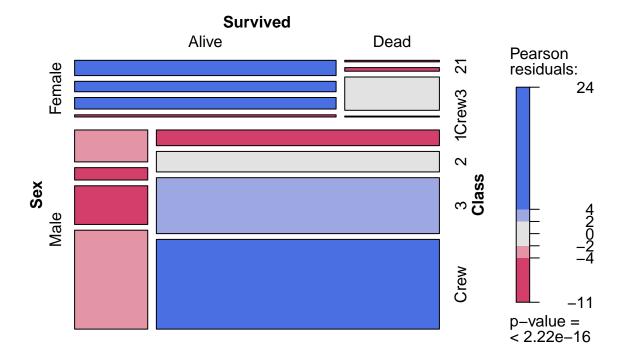
See the mosaic plots on page 77.

#### Section 3.4: Three Categorical Variables

```
tally(~ gender + cats_dogs_both + drugs_y_n, format = "percent", data = OKCupid)
## , , drugs_y_n = No
##
##
        cats_dogs_both
           Has Both
                                 Has dogs
                                                <NA>
## gender
                      Has cats
       F 1.0243064 3.4199156 3.9437466 18.0187845
##
       M 0.5922293 2.0819779 3.7769214 30.0719016
##
##
##
   , , drugs_y_n = Yes
##
##
        cats_dogs_both
           Has Both
## gender
                     Has cats
                                 Has dogs
                                                <NA>
##
       F 0.2085314 0.8941828 0.6272626 2.9794972
       M 0.1901807 0.8658225 0.9041923 6.9132342
##
##
##
   , , drugs_y_n = NA
##
##
        cats_dogs_both
           Has Both
## gender
                      Has cats
                                 Has dogs
##
       F 0.2635837 1.3779757 1.1527618 6.3226732
##
       M 0.1801712 1.0359842 1.3029044 11.8512587
```

Example 3.7: Looking for Associations Among Three Variables at Once

```
vcd::mosaic(tally(~ Sex + Survived + Class, data = Titanic), shade = TRUE)
```



#### Example 3.8: Simpson's Paradox: Gender Discrimination?

See tables on page 80.

```
# Two ways to create a data frame
Berk 2 <- rbind(</pre>
  do(512) * data.frame(admit = TRUE, sex = "M", school = "A"),
  do(313) * data.frame(admit = TRUE, sex = "M", school = "B"),
  do(120) * data.frame(admit = TRUE, sex = "M", school = "C"),
  do(138) * data.frame(admit = TRUE, sex = "M", school = "D"),
  do(53) * data.frame(admit = TRUE, sex = "M", school = "E"),
  do(22) * data.frame(admit = TRUE, sex = "M", school = "F"),
  do(316) * data.frame(admit = FALSE, sex = "M", school = "A"),
  do(206) * data.frame(admit = FALSE, sex = "M", school = "B"),
  do(205) * data.frame(admit = FALSE, sex = "M", school = "C"),
  do(278) * data.frame(admit = FALSE, sex = "M", school = "D"),
  do(138) * data.frame(admit = FALSE, sex = "M", school = "E"),
  do(350) * data.frame(admit = FALSE, sex = "M", school = "F"),
  do(89) * data.frame(admit = TRUE, sex = "F", school = "A"),
  do(17) * data.frame(admit = TRUE, sex = "F", school = "B"),
  do(202) * data.frame(admit = TRUE, sex = "F", school = "C"),
  do(131) * data.frame(admit = TRUE, sex = "F", school = "D"),
  do(94) * data.frame(admit = TRUE, sex = "F", school = "E"),
  do(24) * data.frame(admit = TRUE, sex = "F", school = "F"),
  do(16) * data.frame(admit = FALSE, sex = "F", school = "A"),
  do(8) * data.frame(admit = FALSE, sex = "F", school = "B"),
  do(391) * data.frame(admit = FALSE, sex = "F", school = "C"),
  do(245) * data.frame(admit = FALSE, sex = "F", school = "D"),
  do(300) * data.frame(admit = FALSE, sex = "F", school = "E"),
  do(318) * data.frame(admit = FALSE, sex = "F", school = "F")
) # some numbers are off but it's really annoying to fix
tally(~ sex + admit, data = Berk_2)
##
      admit
## sex TRUE FALSE
    M 1158 1493
##
##
    F 557 1278
tally(~ sex + school + admit, data = Berk_2)
## , , admit = TRUE
##
##
      school
       Α
            В
                 C
    M 512 313 120 138
                        53 22
##
##
    F 89 17 202 131
##
## , , admit = FALSE
##
##
      school
## sex
        Α
                 C
                     D
            В
    M 316 206 205 278 138 350
##
    F 16
           8 391 245 300 318
```

```
admit <- c(rep("TRUE", 1158), rep("FALSE", 1493), rep("TRUE", 557), rep("FALSE", 1278))
sex \leftarrow c(rep("M", 1158 + 1493), rep("F", 557 + 1278))
school \leftarrow c(rep("A", 512), rep("B", 313), rep("C", 120),
            rep("D", 138), rep("E", 53), rep("F", 22),
            rep("A", 512/.621 - 512), rep("B", 313/.602 - 313),
            rep("C", 120/.369 - 120), rep("D", 138/.331 - 138),
            rep("E", 53/.277 - 53), rep("F", 22/.059 - 22),
           rep("A", 89), rep("B", 17), rep("C", 202),
            rep("D", 131), rep("E", 94), rep("F", 24),
            rep("A", 89/.824 - 89 + 1), rep("B", 17/.68 - 17 + 1),
            rep("C", 202/.341 - 202 + 1), rep("D", 131/.349 - 131 + 1),
            rep("E", 94/.239 - 94 + 1), rep("F", 24/.07 - 24)) # + 1 because the rows weren't matching
Berk <- data.frame(sex, admit, school)</pre>
tally(~ sex + admit, data = Berk)
##
      admit
## sex FALSE TRUE
##
    F 1278 557
   M 1493 1158
tally(~ sex + school + admit, data = Berk)
## , , admit = FALSE
##
     school
## sex A B
                C D
                        F.
   F 16 8 391 245 300 318
##
   M 316 206 205 278 138 350
## , , admit = TRUE
##
##
     school
## sex A
           В
                C D
                            F
   F 89 17 202 131 94 24
##
   M 512 313 120 138 53 22
```