IS5 in R: The Standard Deviation as a Ruler and the Normal Model (Chapter 5)

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Introduction and background

This document is intended to help describe how to undertake analyses introduced as examples in the Fifth Edition of *Intro Stats* (2018) by De Veaux, Velleman, and Bock. This file as well as the associated R Markdown reproducible analysis source file used to create it can be found at http://nhorton.people.amherst.edu/is5.

This work leverages initiatives undertaken by Project MOSAIC (http://www.mosaic-web.org), an NSF-funded effort to improve the teaching of statistics, calculus, science and computing in the undergraduate curriculum. In particular, we utilize the mosaic package, which was written to simplify the use of R for introductory statistics courses. A short summary of the R needed to teach introductory statistics can be found in the mosaic package vignettes (https://cran.r-project.org/web/packages/mosaic). A paper describing the mosaic approach was published in the R Journal: https://journal.r-project.org/archive/2017/RJ-2017-024.

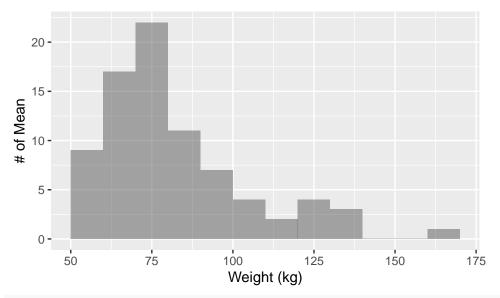
Chapter 5: The Standard Deviation as a Ruler and the Normal Model

```
library(mosaic)
library(readr)
library(janitor)
WomenHeptathlon2016 <-
   read_csv("http://nhorton.people.amherst.edu/is5/data/Womens_Heptathlon_2016.csv") %>%
   janitor::clean_names()
```

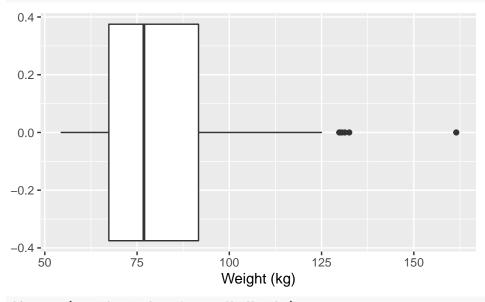
By default, read_csv() prints the variable names. These messages were suppressed using the message = FALSE code chunk option to save space and improve readability. Here we use the clean_names() function from the janitor package to sanitize the names of the columns (which would otherwise contain special characters or whitespace).

```
# page 123
df_stats(~long_jump, data = WomenHeptathlon2016)
                      Q1 median
                                                            sd n missing
##
      response min
                                   Q3 max
                                               mean
                           6.19 6.31 6.58 6.169655 0.2474655 29
## 1 long_jump 5.51 6.08
df_stats(~x200m, data = WomenHeptathlon2016)
##
                                     Q3
     response
                min
                       Q1 median
                                          max
                                                  mean
                                                               sd n missing
                             24.6 24.99 26.32 24.58207 0.6544975 29
        x200m 23.26 24.12
with(WomenHeptathlon2016, stem(x200m))
##
##
     The decimal point is at the |
##
```

```
##
     23 | 3
##
     23 | 589
     24 | 011123334
##
     24 | 5667789
##
##
     25 | 00112444
##
     25 I
     26 I 3
##
with(WomenHeptathlon2016, stem(long jump))
##
##
     The decimal point is 1 digit(s) to the left of the |
##
##
     54 | 1
     56 | 2
##
     58 | 181
##
##
     60 | 0588002569
##
     62 | 023501145
     64 | 38158
Section 5.1: Using the Standard Deviation to Standardize Values
filter(WomenHeptathlon2016, last_name == "Thiam") %>%
 tibble()
## # A tibble: 1 x 9
##
     first_name last_name x200m long_jump x800m high_jump x100m_hurdles javelin
                                     <dbl> <dbl>
                <chr>
                           <dbl>
                                                      <dbl>
                                                                    <dbl>
                            25.1
                                                       1.98
                                                                     13.6
                                                                              53.1
## 1 Nafissatou Thiam
                                      6.58 137.
## # ... with 1 more variable: shot_put <dbl>
# calculate z-score with mean and sd from df_stats
(6.58 - 6.17) / .247 # long jump
## [1] 1.659919
filter(WomenHeptathlon2016, last_name == "Johnson-Thompson") %>%
 tibble()
## # A tibble: 1 x 9
##
     first_name last_name x200m long_jump x800m high_jump x100m_hurdles javelin
                <chr>
                           <dbl>
                                     <dbl> <dbl>
                                                      <dbl>
                                                                    <dbl>
                                                       1.98
                                                                              36.4
## 1 Katarina
                Johnson-~ 23.3
                                      6.51 130.
                                                                     13.5
## # ... with 1 more variable: shot put <dbl>
The tibble() function converts an object into a data frame (you may also see the use of data.frame() for
this purpose.)
Section 5.2: Shifting and Scaling
Shifting to Adjust the Center We begin by reading in the data.
MenWeight <- read_csv("http://nhorton.people.amherst.edu/is5/data/Mens_Weights.csv") %%
  janitor::clean_names()
# Figure 5.2, page 125
gf histogram(~weight in kg, data = MenWeight, binwidth = 10, center = 5) %%
 gf_{labs}(x = "Weight (kg)", y = "# of Mean")
```



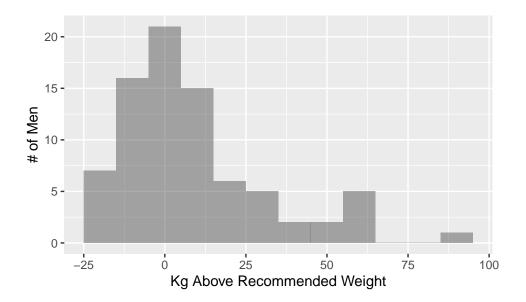
gf_boxplot(~weight_in_kg, data = MenWeight, xlab = "Weight (kg)")



```
df_stats(~weight_in_kg, data = MenWeight)
```

```
## response min Q1 median Q3 max mean sd n missing ## 1 weight_in_kg 54.3 67.35 76.85 91.65 161.5 82.35625 22.26881 80 0
```

```
# Figure 5.3
gf_histogram(~ (weight_in_kg - 74), data = MenWeight, binwidth = 10) %>%
gf_labs(x = "Kg Above Recommended Weight", y = "# of Men")
```



Rescaling to Adjust the Scale Let's review the data from the MenWeight dataset.

```
df_stats(~weight_in_kg, data = MenWeight)
         response min
                          Q1 median
                                        QЗ
                                             max
                                                     mean
                                                                sd n missing
## 1 weight_in_kg 54.3 67.35 76.85 91.65 161.5 82.35625 22.26881 80
df_stats(~weight_in_pounds, data = MenWeight)
##
             response
                         min
                                  Q1 median
                                                QЗ
                                                                         sd n
                                                     max
                                                             mean
## 1 weight_in_pounds 119.46 148.17 169.07 201.63 355.3 181.1838 48.99137 80
     missing
## 1
           0
library(tidyr) # for gather() function
# What does gather() do?
MenWeight %>%
  head() # There are two variables: weight_in_kg and weight_in_pounds.
## # A tibble: 6 x 2
##
     weight_in_kg weight_in_pounds
            <dbl>
##
                              <dbl>
## 1
            107.
                              236.
## 2
             95.7
                              211.
## 3
             68.9
                              152.
## 4
             60.3
                              133.
## 5
             60.4
                              133.
             69.7
                              153.
# Each observation has a value for each.
nrow(MenWeight)
## [1] 80
MenLonger <- MenWeight %>%
  pivot_longer(cols = starts_with("weight"),
               values to = "weight",
```

names_to = "weighttype")

```
MenLonger %>%
```

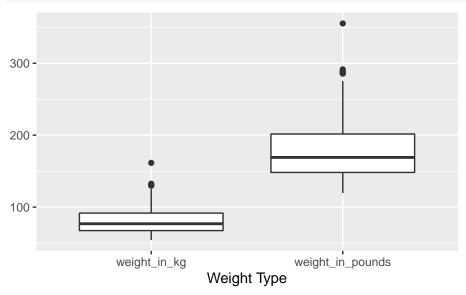
head() # The two variables are weighttype and weight. weighttype is a categorical variable that is ei

```
## # A tibble: 6 x 2
##
     weighttype
                      weight
##
     <chr>
                        <dbl>
## 1 weight_in_kg
                        107.
## 2 weight_in_pounds 236.
## 3 weight_in_kg
                        95.7
## 4 weight_in_pounds
                       211.
## 5 weight_in_kg
                         68.9
## 6 weight_in_pounds
                       152.
nrow(MenLonger) # Each observation from before is now two rows
```

[1] 160

Here we use the tidyr::pivot_wider() function to transform the dataset into the needed format, which can be seen with the head() function.

```
MenLonger %>%
  gf_boxplot(weight ~ weighttype) %>%
  gf_labs(x = "Weight Type", y = "")
```



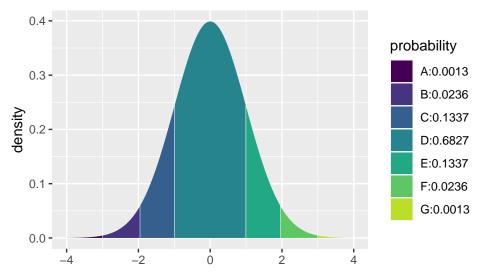
We see the use of goal(Y ~ X) as an example of the general modeling language for two variables in the mosaic package.

Shifting, Scaling, and the z-Scores

Section 5.3: Normal Models

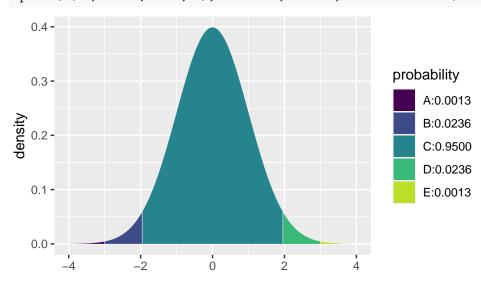
The 68-95-99.7 Rule See display on page 129.

```
# Figure 5.6
# 1, 2 (1.96), and 3 SD's
xpnorm(c(-3, -1.96, -1, 1, 1.96, 3), mean = 0, sd = 1, verbose = FALSE)
```



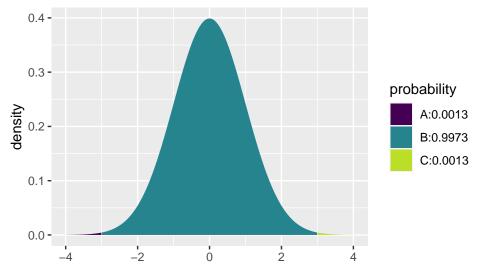
[1] 0.001349898 0.024997895 0.158655254 0.841344746 0.975002105 0.998650102

2 (1.96) and 3 SD's xpnorm(c(-3, -1.96, 1.96, 3), mean = 0, sd = 1, verbose = FALSE)



[1] 0.001349898 0.024997895 0.975002105 0.998650102

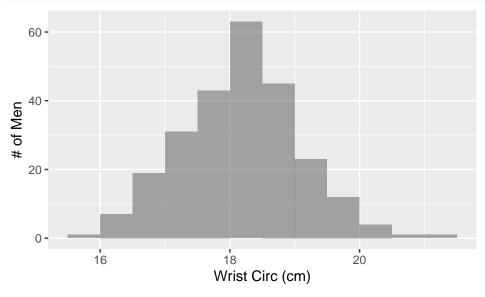
3 SD's xpnorm(c(-3, 3), mean = 0, sd = 1, verbose = FALSE)



[1] 0.001349898 0.998650102

Example 5.4: Using the 68-95-99.7 Rule We begin by reading in the data.

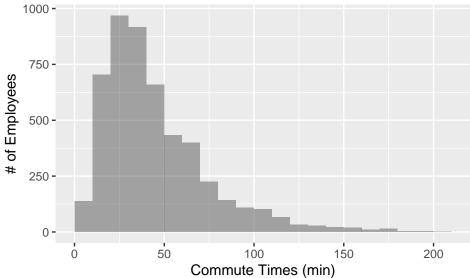
```
BodyFat <- read_csv("http://nhorton.people.amherst.edu/is5/data/Bodyfat.csv")
gf_histogram(~Wrist,
   data = BodyFat, binwidth = .5,
   center = -.25
) %>%
   gf_labs(x = "Wrist Circ (cm)", y = "# of Men")
```



Random Matters Starts on page 133.

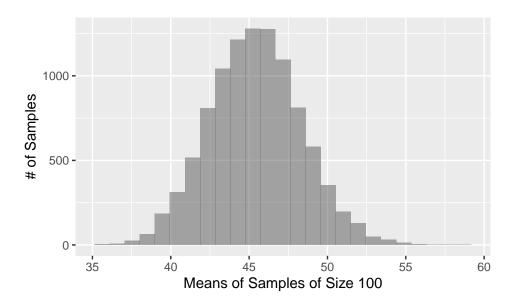
```
Commute <-
    read_csv("http://nhorton.people.amherst.edu/is5/data/Population_Commute_Times.csv") %>%
    janitor::clean_names()

gf_histogram(~commute_time, data = Commute, binwidth = 10, center = 5) %>%
    gf_labs(x = "Commute Times (min)", y = "# of Employees")
```



```
set.seed(2143) # To ensure we get the same values when we run it multiple times
numsim <- 10000 # Number of simulations
mean(~commute_time, data = sample(Commute, size = 100)) # Mean of one random sample
## [1] 45.79
mean(~commute_time, data = sample(Commute, size = 100)) # Mean of another random sample
## [1] 44.7
The mosaic::do() command allows us to run a command multiple times, saving the result as a data frame.
do(2) * mean(~commute_time, data = sample(Commute, size = 100))
##
      mean
## 1 47.43
## 2 45.97
# For the visualization, we use do() 10,000 times
Commute_sample <- do(numsim) * mean(~commute_time, data = sample(Commute, size = 100))</pre>
The do() function generates 10,000 samples of size 100 and for each calculates the sample mean.
```

```
gf_histogram(~mean, data = Commute_sample) %>%
 gf_labs(x = "Means of Samples of Size 100", y = "# of Samples")
```

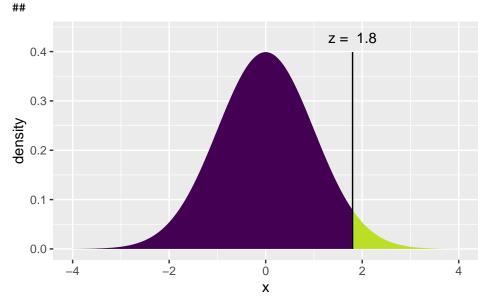


Section 5.4: Working with Normal Percentiles

The pnorm() function calculates normal probabilities. The xpnorm() function from the mosaic package adds a graphical depiction and additional output that may be helpful to new users.

```
xpnorm(1.8, mean = 0, sd = 1)
```

##
If X ~ N(0, 1), then
P(X <= 1.8) = P(Z <= 1.8) = 0.9641
P(X > 1.8) = P(Z > 1.8) = 0.03593
...

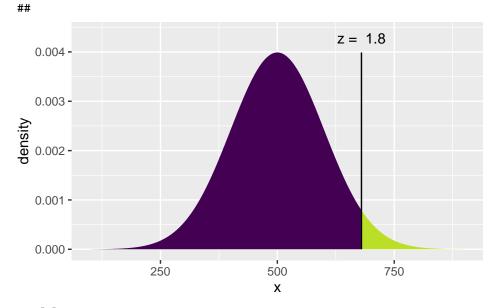


[1] 0.9640697

The qnorm() function finds the inverse of normal probabilities.

```
xqnorm(0.964, mean = 500, sd = 100) # inverse of pnorm()
```

```
##
## If X ~ N(500, 100), then
## P(X <= 679.9118) = 0.964
## P(X > 679.9118) = 0.036
```



```
## [1] 679.9118
qnorm(0.964, mean = 0, sd = 1) # what is the z-score?
```

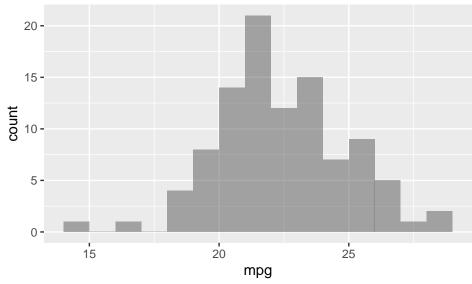
[1] 1.799118

See examples on pages 136-140.

Section 5.5: Normal Probability Plots

We begin by reading in the data.

```
Nissan <- read_csv("http://nhorton.people.amherst.edu/is5/data/Nissan.csv")
# Figure 5.10, page 141
gf_histogram(~mpg, data = Nissan, binwidth = 1, center = .5)</pre>
```



gf_qq(~mpg, data = Nissan, xlab = "Normal Scores") %>%
 gf_qqline(linetype = "solid", color = "red")

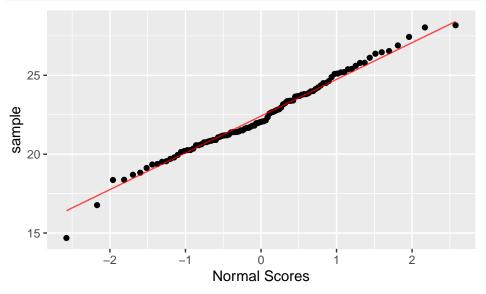


Figure 5.11
gf_histogram(~weight_in_kg, data = MenWeight, xlab = "Weights", binwidth = 10, center = 5)

