IS5 in R: Multiple Regression (Chapter 9)

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Introduction and background

This document is intended to help describe how to undertake analyses introduced as examples in the Fifth Edition of *Intro Stats* (2018) by De Veaux, Velleman, and Bock. More information about the book can be found at http://wps.aw.com/aw_deveaux_stats_series. This file as well as the associated R Markdown reproducible analysis source file used to create it can be found at http://nhorton.people.amherst.edu/is5.

This work leverages initiatives undertaken by Project MOSAIC (http://www.mosaic-web.org), an NSF-funded effort to improve the teaching of statistics, calculus, science and computing in the undergraduate curriculum. In particular, we utilize the mosaic package, which was written to simplify the use of R for introductory statistics courses. A short summary of the R needed to teach introductory statistics can be found in the mosaic package vignettes (http://cran.r-project.org/web/packages/mosaic). A paper describing the mosaic approach was published in the R Journal: https://journal.r-project.org/archive/2017/RJ-2017-024.

Chapter 9: Multiple Regression

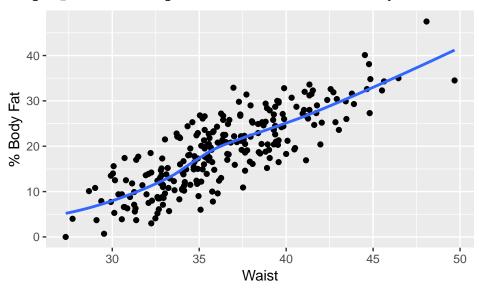
```
library(mosaic)
library(readr)
library(janitor)
BodyFat <- read_csv("http://nhorton.people.amherst.edu/is5/data/Bodyfat.csv") %>%
  clean_names()
## Parsed with column specification:
## cols(
##
     Density = col_double(),
##
     Pct.BF = col_double(),
##
     Age = col_integer(),
##
     Weight = col_double(),
     Height = col_double(),
##
##
     Neck = col double(),
##
     Chest = col_double(),
##
     Abdomen = col double(),
##
     Waist = col_double(),
##
     Hip = col double(),
     Thigh = col double(),
##
     Knee = col_double(),
##
##
     Ankle = col_double(),
##
     Bicep = col_double(),
##
     Forearm = col_double(),
##
     Wrist = col_double()
## )
```

By default, read_csv() prints the variable names. These messages can be suppressed using the message=FALSE code chunk option to save space and improve readability.

Here we use the clean_names() function from the janitor package to sanitize the names of the columns (which would otherwise contain special characters or whitespace).

```
# Figure 9.1, page 276
gf_point(pct_bf ~ waist, data = BodyFat) %>%
gf_labs(x = "Waist", y = "% Body Fat") %>%
gf_smooth()
```

`geom_smooth()` using method = 'loess' and formula 'y ~ x'



We've added gf_smooth() to demonstrate how to add a smoother.

Section 9.1: What is Multiple Regression?

XX Generate number table on page 277

Example 9.1: Modeling Home Prices

```
RealEstate <- read_csv("http://nhorton.people.amherst.edu/is5/data/Real_Estate.csv") %>%
    clean_names()
```

```
## Parsed with column specification:
## cols(
##
    Price = col_integer(),
##
     `Living area` = col_integer(),
##
     bedrooms = col_integer(),
##
     bathrooms = col_double(),
##
    year = col_integer(),
##
     garage = col_integer(),
     `date collected` = col_character(),
##
##
     `location type` = col_character(),
##
     Urban = col_integer(),
##
     Suburb = col_integer(),
     Rural = col_integer()
##
msummary(lm(price ~ living_area + bedrooms, data = RealEstate)) # save this as an object for a make fun
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 308100.44
                          41147.84
                                     7.488 1.69e-13 ***
```

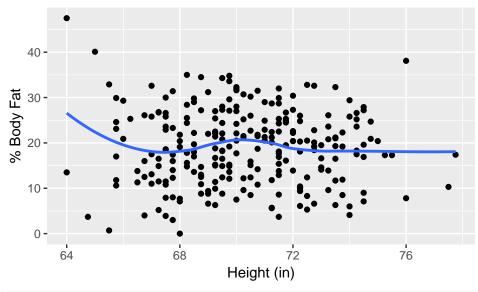
```
## living_area 135.09 11.48 11.771 < 2e-16 ***
## bedrooms -43346.81 12844.14 -3.375 0.000771 ***
##
## Residual standard error: 266900 on 891 degrees of freedom
## Multiple R-squared: 0.1463, Adjusted R-squared: 0.1444
## F-statistic: 76.34 on 2 and 891 DF, p-value: < 2.2e-16</pre>
```

The coefficients for the model can be seen in the Estimate column.

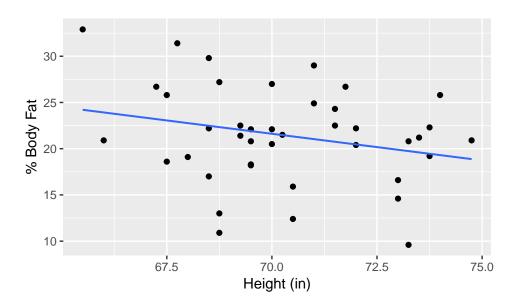
Section 9.2: Interpreting Multiple Regression Coefficients

```
# Figure 9.2, page 279
gf_point(pct_bf ~ height, data = BodyFat) %>%
  gf_smooth() %>% # Added a smoother to assess linearity
  gf_labs(x = "Height (in)", y = "% Body Fat")
```

$geom_smooth()$ using method = 'loess' and formula 'y ~ x'



```
# Figure 9.3
BodyFat %>%
filter(waist >= 36 & waist <= 38) %>% # Just plotting waist sizes between 36 and 38 inches
gf_point(pct_bf ~ height) %>%
gf_labs(x = "Height (in)", y = "% Body Fat") %>%
gf_lm()
```



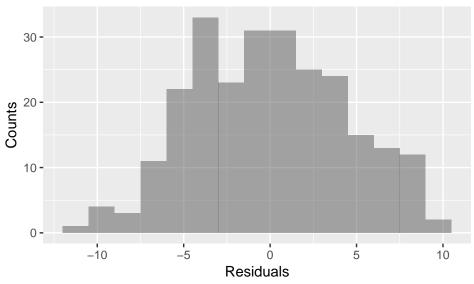
Section 9.3: The Multiple Regression Model–Assumptions and Conditions

Linearity Assumption

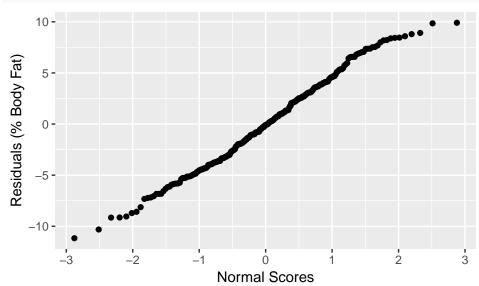
Equal Variance Assumption

Check the Residuals

```
# Figure 9.5
gf_histogram(~ resid(bodyfatlm), binwidth = 1.5, center = 0.75) %>%
gf_labs(x = "Residuals", y = "Counts")
```



```
gf_qq(~ resid(bodyfatlm)) %>%
gf_labs(x = "Normal Scores", y = "Residuals (% Body Fat)")
```



Step-By-Step Example: Multiple Regression

HousingPrices <- read_csv("http://nhorton.people.amherst.edu/is5/data/Housing_prices.csv") %>%
 clean_names()

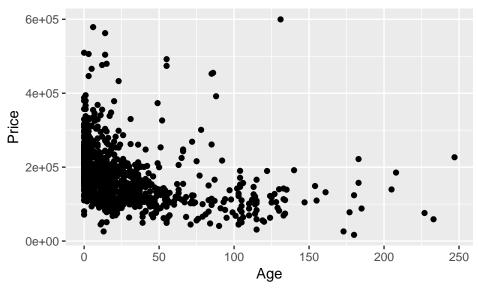
```
## Parsed with column specification:
## cols(
## Price = col_integer(),
## Living.Area = col_integer(),
## Bedrooms = col_integer(),
## Bathrooms = col_double(),
## Fireplaces = col_integer(),
## Age = col_integer()
## )
```

```
gf_point(price ~ living_area, data = HousingPrices) %>%
  gf_labs(x = "Living Area", y = "Price")
   6e+05 -
   4e+05 -
Price
   2e+05 -
   0e+00 -
                          2000
                                       3000
                                                   4000
                                                                5000
              1000
                                  Living Area
gf_boxplot(price ~ as.factor(bedrooms), data = HousingPrices) %>%
  gf_labs(x = "Bedrooms", y = "Price")
   6e+05 -
   4e+05 -
   2e+05 -
   0e+00 -
                                                                5
                                                    4
```

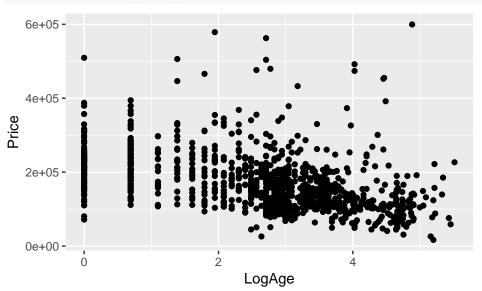
Bedrooms

gf_point(price ~ age, data = HousingPrices) %>%

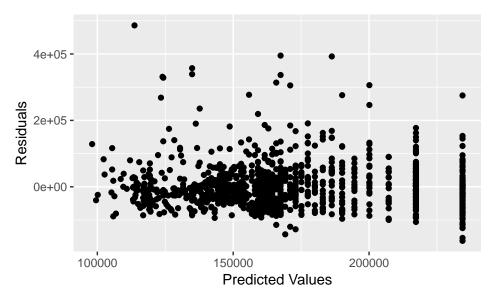
gf_labs(x = "Age", y = "Price")



```
gf_point(price ~ log(age + 1), data = HousingPrices) %>%
gf_labs(x = "LogAge", y = "Price")
```



housinglm <- lm(price ~ log(age + 1), data = HousingPrices)
gf_point(resid(housinglm) ~ fitted(housinglm)) %>%
 gf_labs(x = "Predicted Values", y = "Residuals")

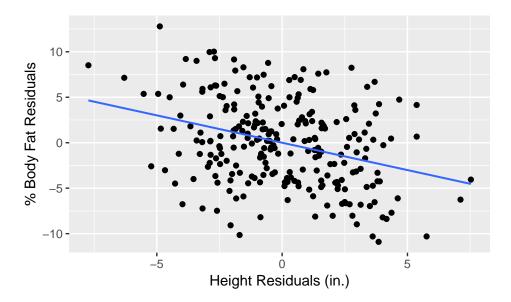


```
housinglm2 <- lm(price ~ living_area + log(age + 1) + bedrooms, data = HousingPrices)
msummary(housinglm2)</pre>
```

```
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 44797.165
                           8356.609 5.361 1.02e-07 ***
## living_area
                  87.260
                              3.365 25.928 < 2e-16 ***
## log(age + 1) -6270.813
                           1299.133 -4.827 1.59e-06 ***
## bedrooms
               -5902.756
                           2773.934 -2.128
                                              0.0336 *
##
## Residual standard error: 49620 on 1053 degrees of freedom
## Multiple R-squared: 0.5876, Adjusted R-squared: 0.5864
## F-statistic: 500.1 on 3 and 1053 DF, p-value: < 2.2e-16
```

Section 9.4: Partial Regression Plots

```
# Figure 9.6 (instructions on 287)
# Step 1
otherthanheightlm <- lm(pct_bf ~ waist, data = BodyFat)
# Step 2
residualsoflm <- resid(otherthanheightlm)
# Step 3
yheightlm <- lm(height ~ waist, data = BodyFat)
# Step 4
residualsoflm2 <- resid(yheightlm)
# Step 5
gf_point(residualsoflm ~ residualsoflm2) %>%
    gf_lm() %>%
    gf_labs(x = "Height Residuals (in.)", y = "% Body Fat Residuals")
```



Just Checking

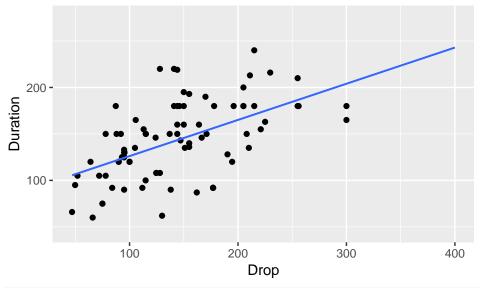
```
Hurricanes <- read_csv("http://nhorton.people.amherst.edu/is5/data/Hurricanes_2015.csv") %>%
  clean_names()
## Parsed with column specification:
     Name = col_character(),
##
##
     Year = col_integer(),
     `Max.Wind.Speed(kts)` = col_integer(),
##
     `Central.Pressure(mb)` = col_integer(),
##
##
     Category = col_integer()
## )
hurricanelm <- lm(max_wind_speed_kts ~ year + central_pressure_mb, data = Hurricanes)
msummary(hurricanelm)
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        1.032e+03 3.852e+01 26.789
                                                       <2e-16 ***
## year
                       -3.132e-04 9.075e-03 -0.035
                                                        0.973
## central_pressure_mb -9.750e-01 3.287e-02 -29.666
                                                       <2e-16 ***
## Residual standard error: 8.199 on 217 degrees of freedom
     (7 observations deleted due to missingness)
## Multiple R-squared: 0.8056, Adjusted R-squared: 0.8038
## F-statistic: 449.6 on 2 and 217 DF, p-value: < 2.2e-16
```

Section 9.5: Indicator Variables

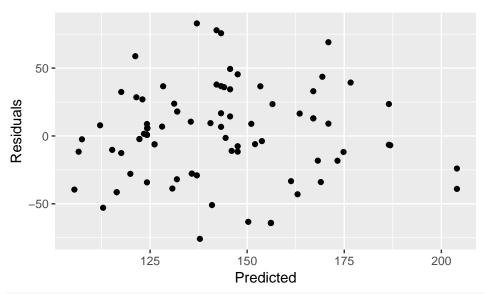
```
library(broom) # We'll use this for augment() later
Coasters <- read_csv("http://nhorton.people.amherst.edu/is5/data/Coasters_2015.csv")
## Parsed with column specification:
## cols(
## Name = col_character(),</pre>
```

```
##
     Park = col_character(),
##
     Track = col_character(),
##
     Speed = col_double(),
     Height = col_double(),
##
##
     Drop = col_double(),
     Length = col_double(),
##
##
     Duration = col integer(),
     Inversions = col_integer()
##
## )
# Table 9.2, page 288
head(Coasters)
## # A tibble: 6 x 9
                           Track Speed Height Drop Length Duration Inversions
##
     Name
               Park
##
     <chr>
               <chr>
                           <chr> <dbl>
                                        <dbl> <dbl>
                                                      <dbl>
                                                               <int>
                                                                           <int>
## 1 Top Thri~ Cedar Poi~ Steel
                                          420
                                                400
                                                       2800
                                                                               0
                                   120
                                                                  NA
                                                                               0
## 2 Superman~ Six Flags~ Steel
                                   100
                                          415
                                                328.
                                                       1235
                                                                  NA
## 3 Millenni~ Cedar Poi~ Steel
                                                                               0
                                    93
                                          310
                                                300
                                                       6595
                                                                  165
## 4 Goliath
               Six Flags~ Steel
                                    85
                                          235
                                                255
                                                       4500
                                                                  180
                                                                               0
## 5 Titan
               Six Flags~ Steel
                                    85
                                          245
                                                255
                                                       5312
                                                                  210
                                                                               0
## 6 Phantom'~ Kennywood~ Steel
                                    82
                                          160
                                                228
                                                       3200
                                                                               0
                                                                  NA
# Figure 9.7
# Coasters[72, ], Tower of Terror isn't included by the book
Coasters <- Coasters %>%
  filter(Name != "Tower of Terror") %>%
  mutate(Inversions = as.factor(Inversions))
gf_point(Duration ~ Drop, data = Coasters) %>%
  gf_lm()
## Warning: Removed 150 rows containing non-finite values (stat_lm).
```

Warning: Removed 150 rows containing missing values (geom_point).



```
coasterlm <- lm(Duration ~ Drop, data = Coasters)</pre>
gf_point(resid(coasterlm) ~ fitted(coasterlm)) %>%
  gf_labs(x = "Predicted", y = "Residuals")
```

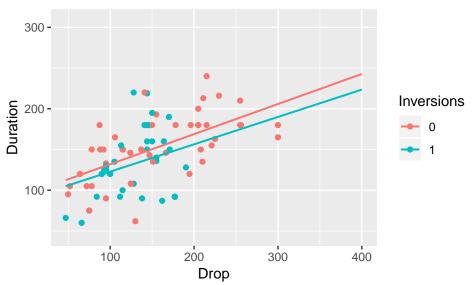


msummary(coasterlm)

```
Estimate Std. Error t value Pr(>|t|)
## (Intercept) 87.22005
                           9.73524
                                     8.959 4.98e-14 ***
## Drop
                0.38928
                           0.06428
                                     6.056 3.36e-08 ***
##
## Residual standard error: 34.06 on 88 degrees of freedom
     (150 observations deleted due to missingness)
## Multiple R-squared: 0.2942, Adjusted R-squared: 0.2862
## F-statistic: 36.68 on 1 and 88 DF, p-value: 3.356e-08
# Figure 9.8
gf_point(Duration ~ Drop, color = ~ Inversions, data = Coasters) %>%
  gf_lm() %>%
  gf_labs(color = "Inversions")
```

Warning: Removed 150 rows containing non-finite values (stat_lm).

Warning: Removed 150 rows containing missing values (geom_point).



```
coasterlm2 <- lm(Duration ~ Drop + Inversions, data = Coasters)</pre>
msummary(coasterlm2)
                Estimate Std. Error t value Pr(>|t|)
##
                            11.69140
## (Intercept)
                96.14026
                                       8.223 1.74e-12 ***
## Drop
                  0.36215
                             0.06699
                                       5.406 5.58e-07 ***
## Inversions1 -10.20093
                             7.48401
                                      -1.363
                                                 0.176
##
## Residual standard error: 33.9 on 87 degrees of freedom
     (150 observations deleted due to missingness)
## Multiple R-squared: 0.3089, Adjusted R-squared: 0.293
## F-statistic: 19.45 on 2 and 87 DF, p-value: 1.045e-07
coasterlm2asdata <- augment(coasterlm2) %>%
  clean_names()
names(coasterlm2asdata)
    [1] "rownames"
                      "duration"
                                   "drop"
                                                 "inversions" "fitted"
   [6] "se fit"
                      "resid"
                                                 "sigma"
                                    "hat"
                                                               "cooksd"
## [11] "std_resid"
glance(coasterlm2asdata)
     nrow ncol complete.obs na.fraction
## 1
       90
                          90
            11
gf_point(resid ~ fitted, color = ~ inversions, data = coasterlm2asdata)
   50 -
                                                           inversions
esid
    0 -
   -50
      100
                 125
                            150
                                       175
                                                  200
                             fitted
```

The augment() function creates a data frame from a linear model that includes a column for residuals, fitted values, etc. Here we use names() to check out the column names and glance() to view the structure of the data set.

Example 9.3: Using Indicator Variables

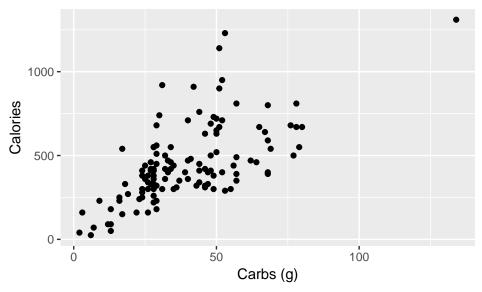
```
DirtBikes <- read_csv("http://nhorton.people.amherst.edu/is5/data/Dirt_bikes_2014.csv")
## Parsed with column specification:
## cols(</pre>
```

```
##
     .default = col_character(),
##
     Year = col_integer(),
##
     MSRP = col_integer(),
     Displacement = col_double(),
##
##
     `Wheel Base` = col_double(),
     Bore = col_double(),
##
##
     Stroke = col double(),
     Ratio = col_double(),
##
##
     Weight = col_double(),
     Rake = col_double(),
##
##
     Trail = col_double(),
     Tank = col_double(),
##
     `Engine cooling` = col_integer()
##
## )
## See spec(...) for full column specifications.
DirtBikes <- DirtBikes %>%
  filter(Cooling != "NA") %>%
  mutate(Cooling = ifelse(Cooling == "Air-Cooled", "Air-Cooled", "LiquidCooled"))
gf_point(MSRP ~ (Displacement)^(1/3), color = ~ Cooling, data = DirtBikes) %>%
  gf_lm()
   10000 -
    7500 -
                                                      Cooling
MSRP
                                                          Air-Cooled
    5000
                                                          LiquidCooled
    2500
                              6
                   (Displacement)^(1/3)
bikeslm <- lm(MSRP ~ I(Displacement^(1/3)) + Cooling, data = DirtBikes)</pre>
msummary(bikeslm)
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                           -3814.9
                                         278.0 -13.72
                                                         <2e-16 ***
## I(Displacement^(1/3))
                            1341.4
                                          50.4
                                                 26.61
                                                         <2e-16 ***
## CoolingLiquidCooled
                            2908.1
                                         154.0
                                                 18.88
                                                         <2e-16 ***
##
## Residual standard error: 602.7 on 106 degrees of freedom
## Multiple R-squared: 0.9423, Adjusted R-squared: 0.9413
## F-statistic: 866.3 on 2 and 106 DF, p-value: < 2.2e-16
```

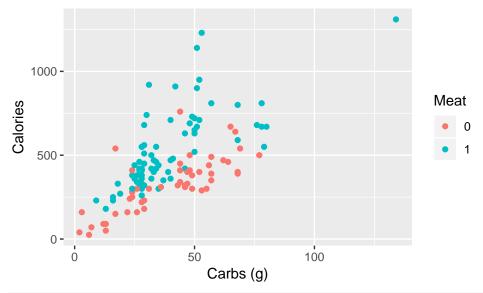
The I() function is used to keep the class of an object the same. Here we use it to keep the variable Displacement "as is" to prevent an error.

Adjusting for Different Slopes

```
BurgerKing <- read_csv("http://nhorton.people.amherst.edu/is5/data/Burger_King_items.csv") %%
  clean_names()
## Parsed with column specification:
## cols(
##
     Item = col_character(),
##
     Serving.size = col_integer(),
##
     Calories = col_integer(),
     Fat.Cal = col_integer(),
##
##
     `Protein(g)` = col_integer(),
##
     `Fat(g)` = col_double(),
##
     `Sat.Fat(g)` = col_double(),
     `Trans.fat(g)` = col_double(),
##
     `Chol(mg)` = col_integer(),
##
     `Sodium(mg)` = col integer(),
##
##
     `Carbs(g)` = col_integer(),
     `Fiber(g)` = col_integer(),
##
##
     `Sugar(g)` = col_integer(),
##
     Meat = col_integer(),
##
     Breakfast = col_integer(),
     `Not Breakfast` = col_integer(),
##
##
     CarbsxMeat = col_integer()
## )
# Figure 9.9, page 292
gf_point(calories ~ carbs_g, data = BurgerKing) %>%
 gf_labs(x = "Carbs (g)", y = "Calories")
```



```
# Figure 9.10
gf_point(calories ~ carbs_g, color = ~ as.factor(meat), data = BurgerKing) %>%
gf_labs(x = "Carbs (g)", y = "Calories", color = "Meat")
```



```
msummary(lm(calories ~ carbs_g * as.factor(meat), data = BurgerKing))
```

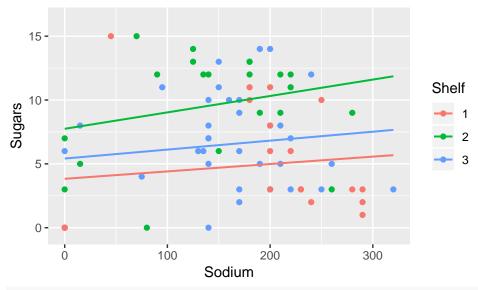
```
##
                            Estimate Std. Error t value Pr(>|t|)
                              83.533
                                                  1.779
## (Intercept)
                                         46.955
                                                          0.0778 .
                               6.255
                                          1.063
                                                  5.885 3.81e-08 ***
## carbs_g
## as.factor(meat)1
                             120.220
                                         60.694
                                                  1.981
                                                           0.0499 *
## carbs_g:as.factor(meat)1
                                          1.378
                               2.145
                                                  1.557
                                                           0.1222
## Residual standard error: 146.5 on 118 degrees of freedom
## Multiple R-squared: 0.6072, Adjusted R-squared: 0.5972
## F-statistic: 60.8 on 3 and 118 DF, p-value: < 2.2e-16
```

One, Two, Many

Cereal <- read_csv("http://nhorton.people.amherst.edu/is5/data/Cereals.csv")</pre>

```
## Parsed with column specification:
## cols(
##
     name = col_character(),
##
     mfr = col_character(),
##
     calories = col_integer(),
     sugars = col integer(),
##
##
     carbo = col_double(),
     protein = col_integer(),
##
##
     fat = col_integer(),
##
     sodium = col_integer(),
##
     fiber = col_double(),
##
     potass = col_integer(),
##
     shelf = col_integer(),
##
     Middle = col_character(),
##
     shelf_1 = col_integer(),
##
     shelf_2 = col_integer(),
##
     shelf_3 = col_integer()
cereallm <- lm(sugars ~ sodium + as.factor(shelf), data = Cereal)</pre>
gf_point(sugars ~ sodium, color = ~ as.factor(shelf), data = Cereal) %>%
```

```
gf_lm() %>%
gf_labs(x = "Sodium", y = "Sugars", color = "Shelf")
```



msummary(cereallm)

carat_size

colorE

61.2491

-2.1027

```
Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                    3.446740
                               1.345111
                                          2.562 0.012457 *
                                          1.417 0.160818
                    0.007962
                               0.005620
## sodium
                                          3.906 0.000207 ***
## as.factor(shelf)2 5.012166
                              1.283154
## as.factor(shelf)3 1.818214
                              1.139384
                                         1.596 0.114857
## Residual standard error: 4.07 on 73 degrees of freedom
## Multiple R-squared: 0.1866, Adjusted R-squared: 0.1532
## F-statistic: 5.583 on 3 and 73 DF, p-value: 0.001669
```

Example 9.4: Indicators for Variables with Several Levels

```
Diamonds <- read_csv("http://nhorton.people.amherst.edu/is5/data/Diamonds.csv") %>%
  clean_names()
```

```
## Parsed with column specification:
## cols(
##
     Price = col_integer(),
     `Carat Size` = col_double(),
##
##
     Color = col_character(),
##
     Clarity = col_character(),
     Cut = col_character()
## )
# Parallel Slopes
diamondlm <- lm(sqrt(price) ~ carat_size + color, data = Diamonds)</pre>
msummary(diamondlm)
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 13.1946
```

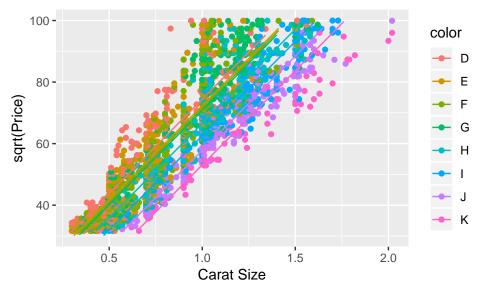
0.5488 24.043 < 2e-16 ***

0.5032 121.722 < 2e-16 ***

0.5399 -3.895 0.000101 ***

```
0.5576 -5.136 3.00e-07 ***
## colorF
               -2.8640
## colorG
               -3.6320
                           0.5769 -6.296 3.57e-10 ***
## colorH
               -7.8948
                           0.5858 -13.477 < 2e-16 ***
                           0.6261 -18.932 < 2e-16 ***
## colorI
              -11.8542
## colorJ
               -16.6404
                           0.6637 -25.071 < 2e-16 ***
## colorK
               -21.3577
                           0.8282 -25.787 < 2e-16 ***
## Residual standard error: 7.218 on 2681 degrees of freedom
## Multiple R-squared: 0.8583, Adjusted R-squared: 0.8579
## F-statistic: 2030 on 8 and 2681 DF, p-value: < 2.2e-16
diamondpredict <- makeFun(diamondlm)</pre>
diamonddata <- augment(diamondlm) %>% # To get fitted values
  clean names()
str(diamonddata)
## 'data.frame':
                   2690 obs. of 10 variables:
                      31.6 31.6 31.6 31.6 31.6 ...
   $ sqrt_price: num
   $ carat_size: num
                      0.3 0.44 0.31 0.66 0.47 0.4 0.36 0.52 0.53 0.43 ...
                      "E" "E" "E" "K" ...
## $ color
               : chr
                      29.5 38 30.1 32.3 34.1 ...
## $ fitted
               : num
   $ se_fit
                      0.374 0.344 0.372 0.707 0.442 ...
##
               : num
               : num 2.156 -6.419 1.544 -0.639 -2.464 ...
##
   $ resid
## $ hat
               : num 0.00269 0.00226 0.00265 0.00959 0.00375 ...
## $ sigma
               : num 7.22 7.22 7.22 7.22 ...
                : num 2.68e-05 2.00e-04 1.35e-05 8.51e-06 4.89e-05 ...
   $ cooksd
## $ std_resid : num 0.2991 -0.8902 0.2141 -0.0889 -0.342 ...
gf_point(sqrt_price ~ carat_size, color = ~ color, data = diamonddata) %>%
 gf line(fitted ~ carat size) %>%
  gf_labs(x = "Carat Size", y = "sqrt(Price)") +
 ylim(30, 100)
```

Warning: Removed 79 rows containing missing values (geom_path).



```
# With interaction
diamondlm2 <- lm(sqrt(price) ~ carat_size * color, data = Diamonds)</pre>
```

msummary(diamondlm2)

```
Estimate Std. Error t value Pr(>|t|)
##
                                 1.2142
                                          7.679 2.23e-14 ***
## (Intercept)
                      9.3239
## carat size
                     67.0408
                                 1.7025 39.379 < 2e-16 ***
## colorE
                      -0.5392
                                 1.5075
                                         -0.358 0.72063
## colorF
                     -2.3716
                                 1.5627
                                         -1.518 0.12922
## colorG
                     -2.6709
                                 1.6643
                                        -1.605 0.10867
## colorH
                      -3.9177
                                 1.8248
                                         -2.147 0.03189 *
                                         -1.320 0.18689
## colorI
                      -2.5481
                                 1.9301
## colorJ
                     -5.4176
                                 2.0716 -2.615 0.00897 **
## colorK
                      0.5976
                                 2.7815
                                          0.215 0.82991
## carat_size:colorE -2.4007
                                 2.0999
                                        -1.143 0.25305
## carat_size:colorF
                     -1.3211
                                 2.0954
                                         -0.630 0.52843
## carat_size:colorG -2.5457
                                        -1.220 0.22260
                                 2.0868
## carat_size:colorH -5.9017
                                 2.1774 -2.710 0.00676 **
## carat_size:colorI -10.9139
                                 2.1812 -5.004 5.99e-07 ***
## carat_size:colorJ -12.4948
                                 2.2531
                                         -5.546 3.22e-08 ***
                                 2.6978 -7.950 2.72e-15 ***
## carat_size:colorK -21.4477
## Residual standard error: 7.058 on 2674 degrees of freedom
## Multiple R-squared: 0.8649, Adjusted R-squared: 0.8641
## F-statistic: 1141 on 15 and 2674 DF, p-value: < 2.2e-16
gf_point(sqrt(price) ~ carat_size, color = ~ color, data = Diamonds) %>%
  gf_lm() %>%
  gf_labs(x = "Carat Size", y = "sqrt(Price)") +
 ylim(30, 100)
```

Warning: Removed 204 rows containing missing values (geom_lm).

