

# Lecture 7 - 07-04-2020

Bounding statistical risk of a predictor

Design a learning algorithm that predict with small statistical risk

$$(D, \ell) \quad \ell_d(h) = \mathbb{E}[\ell(y), h(x)]$$

where  $D$  is unknown

$$\ell(y, \hat{y}) \in [0, 1] \quad \forall y, \hat{y} \in Y$$

We cannot compute statistical risk of all predictor.

We assume statistical loss is bounded so between 0 and 1. Not true for all losses (like logarithmic).

Before design a learning algorithm with lowest risk, How can we estimate risk?

We can use test error  $\rightarrow$  way to measure performances of a predictor  $h$ . We want to link test error and risk.

Test set  $S' = \{(x'_1, y'_1) \dots (x'_n, y'_n)\}$  is a random sample from  $D$

How can we use this assumption?

Go back to the definition of test error

Sample mean (IT: Media campionaria)

$$\hat{\ell}_s(h) = \frac{1}{n} \cdot \sum_{t=1}^n \ell(\hat{y}_t, h(x'_t))$$

i can look at this as a random variable  $\ell(y'_t, h(x'_t))$

$$\mathbb{E}[\ell(y'_t, h(x'_t))] = \ell_D(h) \longrightarrow \text{risk}$$