

Fundamental Haskell

Encyclopedcal handbook for learning and undersatanding fundamentals

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September 14, 2020

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Part I

Introduction

“Employ your time in improving yourself by other men’s writings so that you shall come easily by what others have labored hard for.” (Socrates by Plato)

Important notes on Haskell, [category](#) theory & related fields, terms and recommendations.

Book comes in forms:

- [Web book](#)
- [PDF](#)
- [Open in web PDF viewer](#)
- [L^AT_EX](#)
- [Source code in Org-mode](#)
- [GitHub](#)
- [GitLab](#)

This book is created using complex Org markup file with a lot of L^AT_EX and L^AT_EX formulas. Be aware - GitHub & GitLab only partially parse Org into HTML.

Book becomes too popular (underground scene wibe). To address that - a proper Haskell book would “avoid success at all costs” and go through proper migrations, become free from personal Org-drill metadata, to give clean learning materials for Haskell community.

In work on the book, person basically reinvented the Zettelkasten. Since person arrived at the same design, I would recommend Zettelkasten to anyone.

Current book form also reached the limits of the radio cross-linking scaling of the Emacs Org-mode C-implemented [functions](#). The book would migrate into a most powerful proper Free Software Zettelkasten form there is - [Org-roam](#) - and in that transition book would gain even more versatility and possibilities.

Book also wants to be published in form of the Anki card deck for Anki users. Did you know that Anki is actually former Emacs Org-drill v1?

[So in nearest time book source would go through big structural changes.](#)

To get the full view:

- [Outline navigation](#)
- [L^AT_EX formulas:](#)

$$\left[-\frac{\hbar^2}{2m} \nabla^2 + V(\vec{r}, t) \right] \Psi(\vec{r}, t) = i\hbar \frac{\partial}{\partial t} \Psi(\vec{r}, t), \quad \sum_{k,j} \left[-\frac{\hbar^2}{\sqrt{a}} \frac{\partial}{\partial q^k} \left(\sqrt{a} a^{kj} \frac{\partial}{\partial q^j} \right) + V \right] \Psi + \frac{\hbar}{i} \frac{\partial \Psi}{\partial t} = 0$$

- [Interlinks](#): [Interlinks](#)

, please refer to Web book, PDF, L^AT_EX, or use Org-mode capable viewer/editor.

Note about the markup: <<<This is a radio target>>> - is the anchor for dynamic linking.

Users of Emacs can prettify radio targets to be shown as hyper-links with this Elisp snippet:

```
;;;; 2019-06-12: NOTE:
;;;; Prettify '<<<Radio targets>>>' to be shown as '_Radio_targets_',
;;;; when `org-descriptive-links` set.
;;;; This is improvement of the code from: Tobias&glmorous:
;;;; https://emacs.stackexchange.com/questions/19230/how-to-hide-targets
```

```

;;; There exists library created from the sample:
;;; https://github.com/talwrii/org-hide-targets
(defun org-hidden-links-additional-re "\\(<<<\\)[[:print:]]+?\\(>>>\\)"
  "Regular expression that matches strings where the invisible-property
  of the sub-matches 1 and 2 is set to org-link."
  :type '(choice (const :tag "Off" nil) regexp)
  :group 'org-link)
(make-variable-buffer-local 'org-hidden-links-additional-re)

(defun org-activate-hidden-links-additional (limit)
  "Put invisible-property org-link on strings matching
  `org-hide-links-additional-re'."
  (if org-hidden-links-additional-re
      (re-search-forward org-hidden-links-additional-re limit t)
      (goto-char limit)
      nil))

(defun org-hidden-links-hook-function ()
  "Add rule for `org-activate-hidden-links-additional'
  to `org-font-lock-extra-keywords'.
  You can include this function in `org-font-lock-set-keywords-hook'."
  (add-to-list 'org-font-lock-extra-keywords
    '(org-activate-hidden-links-additional
      (1 '(face org-target invisible org-link))
      (2 '(face org-target invisible org-link)))))

(add-hook 'org-font-lock-set-keywords-hook #'org-hidden-links-hook-function)

```

SCHT: and metadata in :properties: - of my org-drill practices, please just run org-drill-strip-all-data.

Part II

Definitions

Chapter 1

Algebra

↳ *al-jabr* assemble parts

A system of parts based on given axioms ([properties](#)) and operations on them.

====

Additional meanings:

- a. [Algebra](#) - a [set](#) with its [algebraic structure](#).
- b. [Abstract algebra](#) - the study of number systems and operations within them.
- c. [Algebra](#) - vector space over a field with a multiplication.

1.1 *

Algebras

1.2 Algebraic

Composite from simple parts.

Also: [Algebraic data type](#).

1.3 Algebraic structure

* includes axioms that must be satisfied and operations on the underlying (or "carrier") [set](#).

An underlying [set](#) with * on top of it also called "an [algebra](#)".

* include [groups](#), [rings](#), fields, and lattices. More complex [structures](#) can be defined by introducing multiple operations, different underlying [sets](#), or by altering the defining axioms. Examples of more complex * can be many modules, [algebras](#) and other vector spaces, and any variations that the definition includes.

1.3.1 *

Algebraic structures

Table 1.1: Algebraic structures

	Closure	Associativity	Identity	Invertability	Commutativity	Distributive
Semigroupoid		✓				
Small Category		✓	✓			
Groupoid		✓	✓	✓		
Magma	✓					
Quasigroup	✓			✓		
Loop	✓		✓	✓		
Semigroup	✓	✓				
Inverse Semigroup	✓	✓		✓		
Monoid	✓	✓	✓			
Group	✓	✓	✓	✓		
Abelian group	✓	✓	✓	✓	✓	
Non-unital ring (rng)	✓ + ×	✓ + ×	✓ +	✓ +	✓ +	✓
Semiring (rig)	✓ + ×	✓ + ×	✓ + ×	✓ ×	✓ +	✓
Ring	✓ + ×	✓ + ×	✓ + ×	✓ + ×	✓ +	✓

1.3.2 Fundamental theorem of algebra

Any non-constant single-variable polynomial with complex coefficients has at least one complex root.

From this definition follows [property](#) that the field of complex numbers is algebraically [closed](#).

1.3.3 Magma

Set with a [binary operation](#) which form a [closure](#).

1.3.3.1 Semigroup

[Magma](#) with [associative property](#) of [operation](#).

Defined in Haskell as:

```
class Semigroup a where
  (< >) :: a -> a -> a
```

1.3.3.1.1 *

Semigroups

1.3.3.1.2 Monoid

[Semigroup](#) with [identity](#) element.

Ideal ground for any accumulation class.

```
class Semigroup m => Monoid m where
  mempty :: m
  mconcat :: [m] -> m
  mconcat = foldr mappend mempty
```

More generally in [category](#) theory terms:

* - the [object](#) M equipped with two [arrows](#):

$\mu : M \otimes M \rightarrow M$ called multiplication or [product](#), or tensor [product](#). $\eta : I \rightarrow M$ called [unit](#),

so (M, μ, η) . By its definition [category](#) (lets call it C should have \otimes and I . Where $\otimes : C \times C \rightarrow C$ is any [operation](#) that combines [objects](#) and stays ([closed](#)) inside [category](#), so it may be even already [category](#) given [operation](#) of [arrow composition](#). And I is an [identity object](#) of \otimes [operation](#).

[Category](#) that has one [object](#) - always a free [monoid](#) (from definition of "Category" - [composition](#), and there is only one [object](#) so it is always also the [identity object](#)).

For example to represent the whole non-negative integers with the one [object](#) and [morphism](#) "1" is absolutely enough, [composition operation](#) is "+".

```
import Data.Monoid
do
  show (mempty :: Num a => Sum a)
  -- "Sum {getSum = 0}"
  show $ Sum 1
  -- "Sum {getSum = 1}"
  show $ (Sum 1) <> (Sum 1) <> (Sum 1)
  -- "Sum {getSum = 3}"
  -- ...
```

And backwards connection. Any [monoidal category](#) can be isomorphically transformed into one-[object](#) bicategory, thou explaining or proving it is out of the current [scope](#).

Any [monad](#) is [equivalent](#) up to [isomorphism](#) to [monoid](#).

1.3.3.1.2.1 *

Monoidal Monoids

1.3.3.1.2.2 Monoid properties

Monoid left identity property

```
mempty <> x = x
```

Monoid right identity property

```
x <> mempty = x
```

Monoid associativity property

```
x <> mempty = x (y <> z) = (x <> y) <> z
mconcat = foldr (mempty <>)
```

Everything [associative](#) can be mappend.

1.3.3.1.2.3 Commutative monoid

[Operation](#) that forms [structure](#) has [commutativity property](#): $x \circ y = y \circ x$

Opens a big abilities in concurrent and distributed processing.

*

Abelian monoid

1.3.3.1.2.4 Group

[Monoid](#) that has [inverse](#) for every element.

*

Groups

Commutative group [Commutative monoid](#) that is a [group](#).

*

Abelian group

Ring [Commutative group](#) under $+$ & [monoid](#) under \times , $+$ & \times connected by [distributive property](#).

- and \times are generalized [binary](#) operations of addition and multiplication. \times has no requirement for [commutativity](#).

Example: [set](#) of same size square matrices of numbers with matrix operations form a [ring](#).

*

Rings

1.4 Modular arithmetic

System for integers [where](#) numbers wrap around the certain values (single - [modulus](#), plural - [moduli](#)).

Example - 12-hour clock.

1.4.1 *

Clock arithmetic

1.4.2 Modulus

Special numbers [where](#) arithmetic wraps around in [modular arithmetic](#).

1.4.2.1 *

Moduli - plural.

Chapter 2

Category theory

Category \mathcal{C} consists of the basis:

Primitives:

- Objects** - $a^{\mathcal{C}}$. A **node**. **Object** of some **type**. Often **sets**, than it is **Set category**.
- Arrows** - $(a, b)^{\mathcal{C}}$ (AKA **morphisms** mappings).
- Arrow (morphism) composition** - **binary operation**: $(a, b)^{\mathcal{C}} \circ (b, c)^{\mathcal{C}} \equiv (a, c)^{\mathcal{C}} \mid \forall a, b, c \in \mathcal{C}$ AKA principle of **compositionality** for **arrows**.

Properties (or axioms):

- Associativity** of **morphisms**: $h \circ (g \circ f) \equiv (h \circ g) \circ f \mid f_{a \rightarrow b}, g_{b \rightarrow c}, h_{c \rightarrow d}$
- Every **object** has (two-sided) **identity morphism** (& in fact - exactly one): $1_x \circ f_{a \rightarrow x} \equiv f_{a \rightarrow x}, g_{x \rightarrow b} \circ 1_x \equiv g_{x \rightarrow b} \mid \forall x \exists 1_x, \forall f_{a \rightarrow x}, \forall g_{x \rightarrow b}$
- Principle of **compositionality**.

From these axioms, can be proven that there is exactly one **identity morphism** for every **object**.

Object and **morphism** are complete **abstractions** for anything. In majority of cases under **object** is a state and **morphism** is a change.

2.1 *

Category Categories

2.2 Abelian category

Generalised **category** for homological **algebra** (having a possibility of basic constructions and techniques for it).

Category which:

- has a **zero object**,
- has all **binary** biproducts,
- has all **kernel**'s and cokernels,
- (it has all **pullbacks** and pushouts)
- all **monomorphism**'s and **epimorphism**'s are normal.

Abelian category is a stable **structure**; for example it is regular and satisfy the snake lemma. The class of **Abelian categories** is **closed** under several categorical constructions.

There is notion of **Abelian monoid** (AKS **Commutative monoid**) and **Abelian group** (**Commutative group**).

Basic examples of $*$:

- **category** of Abelian **groups**
- **category** of modules over a **ring**.

$*$ are widely used in **algebra**, **algebraic** geometry, and topology.

$*$ has many constructions like in **categories** of modules:

- kernels
- exact **sequences**
- **commutative** diagrams

$*$ has disadvantage over **category** of modules. **Objects** do not necessarily have elements that can be manipulated directly, so traditional definitions do not work. Methods must be supplied that allow definition and manipulation of **objects** without the use of elements.

2.2.1 $*$

Abelian categories

2.3 Composition

Axiom of **Category**.

2.3.1 $*$

Composable Compositions

2.4 Endofunctor category

From the name, in this **Category**:

- **objects** of End are **Endofunctors** $E^{C \rightarrow C}$
- **morphisms** are **natural transformations** between **endofunctors**

2.5 Functor

$*$ full translation (map) of one **category** into another. Translating **objects** and **morphisms** (as input can take **morphism** or **object**).

$*$ - **forgetful** - discards part of the **structure**. $*$ - faithful - fully preserves all **morphisms** - **injective** on **Hom-sets**. $*$ - full - translation of **morphisms** fully covers all the **morphisms** between according objects in the target category.

For **Functor type class** or **fmap** - see **Power set functor**.

Functor properties (axioms):

- $F^{C \rightarrow D}(a) \mid \forall a^C$ - every source **object** is mapped to **object** in target **category**

- $\overline{(F^{C \rightarrow \mathcal{D}}(a), F^{C \rightarrow \mathcal{D}}(b))}^{\mathcal{D}} \mid \forall (a, b)^C$ - every source **morphism** is mapped to target **category morphism** between corresponding **objects**
- $F^{C \rightarrow \mathcal{D}}(\vec{g}^C \circ \vec{f}^C) = F^{C \rightarrow \mathcal{D}}(\vec{g}^C) \circ F^{C \rightarrow \mathcal{D}}(\vec{f}^C) \mid \forall y = \vec{f}^C(x), \forall \vec{g}^C(y)$ - **composition** of **morphisms** translates directly (tautologically goes from other two)

These axioms guarantee that **composition** of **functors** can be fused into one **functor** with **composition** of **morphisms**. This **process** called fusion.

In Haskell this axioms have form:

```
fmap id = id
fmap (f . g) = fmap f . fmap g
```

Since $*$ is 1-1 mapping of initial **objects** - it is a memoizable dictionary with **cardinality** of initial **objects**. Also in **Hask category functors** are obviously **endofunctors** \therefore they are special **kinds** of containers for the parametric values (AKA **product type**). In Haskell **product type** $*$ are **endofunctors** from **polymorphic type** into a **functor** wrapper of a **polymorphic type**.

$*$ translates in one direction, and does not provide algorithm of reversing itself or retrieving the parametric value.

2.5.1 $*$

Functors Functorial - something that has **functor properties**, and so also is a **functor**.

2.5.2 Power set functor

$\mathcal{P}^{\mathcal{S} \rightarrow \mathcal{P}(\mathcal{S})}$

$*$ - **functor** from **set** S to its **power set** $\mathcal{P}(S)$.

Functor type class in Haskell defines a $*$ as **fmap** in a form of **bifunctor**. It allows to do **function application** inside **type structure** layers (denoted f or m). **IO** is also such **structure**. **Power set** is unique to the **set**, $*$ is unique to the **data type** (to the **category** also). Any **endofunctor** embodies into $*$. It is easily seen from Haskell definition - that the $*$ is the **polymorphic** generalization over any **endofunctor** in a **category**.

Application of a **function** to $*$ gives a particular **endofunctor** (see **Hask category**).

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b
```

Functor instance must be of **kind** $(* \rightarrow *)$, so instance for **higher-kinded data type** must be **applied** until this **kind**.

Composed $*$ can **lift functions** through any layers of **structures** that belong to **Functor type class**.

$*$ can be used to filter-out the **structure** through **structure composition**, for example - **composition** with **error** cases (**Nothing** & **Left** cases) in **Maybe**, **Either** and related **types**.

2.5.2.1 $*$

fmap Functor type class

2.5.2.2 Power set functor properties

Type instance of **functor** should abide this **properties**:

2.5.2.2.1 $*$

Functor properties

2.5.2.2.2 Power set functor identity property

Functor translates **object** & its **identity morphism** to target **object** & its **identity morphism**.

```
fmap id == id
```

2.5.2.2.3 Power set functor composition property

Full transparency of **composition** translation. So **order** of **composition** and translation does not matter, the result is always the same.

```
fmap (f . g) == fmap f . fmap g
```

Including cases: a) translate everything one-by-one and assemble at destination **category**. b) assemble everything in source category and translate in one go once.

Composing in source **category** and translating at once - is a much-much more effective computation (known as "**functor fusion**").

2.5.2.3 Lift

```
fmap :: (a -> b) -> (f a -> f b)
```

Functor takes **function** $a \rightarrow b$ and returns a **function** $f\ a \rightarrow f\ b$ this is called **lifting** a **function**. Lift does a **function application** through the **data structure**.

2.5.2.3.1 *

Lifting

2.5.2.4 Power set functor is a free monad

Since:

- $\forall e \in S : \exists \{e\} \in \mathcal{P}(S) \models \forall e \in S : \exists (e \rightarrow \{e\}) \equiv \text{unit}$
- $\forall \mathcal{P}(S) : \mathcal{P}(S) \in \mathcal{P}(S) \models \forall \mathcal{P}(S) : \exists (\mathcal{P}(\mathcal{P}(S)) \rightarrow \mathcal{P}(S)) \equiv \text{join}$

2.5.3 Forgetful functor

Functor that forgets part or all of what defines **structure** in **domain category**. $F^{\text{Grp} \rightarrow \text{Set}}$ that translates **groups** into their underlying **sets**. **Constant functor** is another example.

2.5.3.1 *

Forgetful

2.5.4 Identity functor

Maps all **category** to itself. All **objects** and **morphisms** to themselves.

Denotation: $1^{\mathcal{C} \rightarrow \mathcal{C}}$

2.5.5 Endofunctor

Is a **functor** which source (**domain**) and target (**codomain**) are the same **category**.

$F^{\mathcal{C} \rightarrow \mathcal{C}}, E^{\mathcal{C} \rightarrow \mathcal{C}}$

2.5.5.1 *

Endofunctors

2.5.6 Applicative functor

* - Computer science term. Category theory name - **lax monoidal functor**. And in category *Set*, and so in category *Hask* all **applicatives** and **monads** are strong (have **tensorial strength**).

* - **sequences functorial** computations (plain **functors** can't).

```
(<*>) :: f (a -> b) -> f a -> f b
```

Requires **Functor** to exist. Requires **Monoidal structure**.

Has **monoidal structure** rules, separated from **function application** inside **structure**.

Data type can have several **applicative** implementations.

Standard definition:

```
class Functor f => Applicative f
  where
    (<*>) :: f (a -> b) -> f a -> f b
    pure  :: a -> f a
```

pure - if a **functor**, **identity Kleisli arrow**, **natural transformation**.

Composition of * always produces *, contrary to **monad** (**monads** are not **closed** under **composition**).

`Control.Monad` has an old **function** `ap` that is old implementation of `<*>`:

```
ap :: Monad m => m (a -> b) -> m a -> m b
```

2.5.6.1 *

Applicative Applicatives Applicative functors

2.5.6.2 Applicative property

2.5.6.3 *

Applicative properties

2.5.6.3.1 Applicative identity property

```
pure id <*> v = v
```

2.5.6.3.2 Applicative composition property

Function composition works regularly.

```
pure (.) <*> u <*> v <*> w = u <*> (v <*> w)
```

2.5.6.3.3 Applicative homomorphism property

Internal **function application** doesn't change the **structure** around values.

```
pure f <*> pure x = pure (f x)
```

2.5.6.3.4 Applicative interchange property

On condition that internal **order** of **evaluation** is preserved - **order** of operands is not relevant.

```
u <*> pure y = pure ($ y) <*> u
```

2.5.6.4 Applicative function

2.5.6.4.1 liftA*

2.5.6.4.1.1 liftA

Essentially a `fmap`.

```
:type liftA
liftA :: Applicative f => (a -> b) -> f a -> f b
```

Lifts `function` into `applicative function`.

2.5.6.4.1.2 liftA2

Lifts `binary function` across two `Applicative functors`.

```
liftA2 :: Applicative f => (a -> b -> c) -> f a -> f b -> f c
liftA2 f x y == pure f <*> x <*> y
```

2.5.6.4.1.3 «<liftA2 (<*>)»>

`liftA2 (<*>)` is an `applicative` that lifts a `binary operation` over the two layers (2x2). Pretty useful to remember it.

```
liftA2 :: ( a      -> b -> c ) -> f      a      -> f      b      -> f      c
<*> ::      (f (a -> b) -> f a -> f b)
liftA2 (<*>) ::                                f1 (f2 (a -> b)) -> f1 (f2 a) -> f1 (f2
  ↪      b)
```

2.5.6.4.1.4 liftA2 (liftA2 (<*>))

`liftA2 (<*>)` 3-layer version.

2.5.6.4.1.5 liftA3

`liftA2` 3-parameter version.

```
liftA3 f x y z == pure f <*> x <*> y <*> z
```

2.5.6.4.2 Conditional `applicative` computations

```
when :: Applicative f => Bool -> f () -> f ()
```

Only when `True` - perform an `applicative` computation.

```
unless :: Applicative f => Bool -> f () -> f ()
```

Only when `False` - perform an `applicative` computation.

2.5.6.5 Special applicatives

2.5.6.5.1 Identity applicative

```
-- Applicative f =>
-- f ~ Identity
type Id = Identity
instance Applicative Id
  where
    pure :: a -> Id a
    (<*>) :: Id (a -> b) -> Id a -> Id b
```

```

mkId = Identity
xs = [1, 2, 3]

const <$> mkId xs <*> mkId xs'
-- [1,2,3]

```

2.5.6.5.2 Constant applicative

It holds only to one value. The `function` does not exist and last `parameter` is a phantom.

```

-- Applicative f =>
-- f ~ Constant e
type C = Constant
instance Applicative C
where
  pure :: a -> C e a
  (<*>) :: C e (a -> b) -> C e a -> C e b

```

2.5.6.5.3 Maybe applicative

"There also can be no `function` at all."

If `function` might not exist - embed `f` in `Maybe structure`, and use `Maybe applicative`.

```

-- f ~ Maybe
type M = Maybe
pure :: a -> M a
(<*>) :: M (a -> b) -> M a -> M b

```

2.5.6.5.4 Either applicative

`pure` is `Right`. Defaults to `Left`. And if there is two `Left`'s - to `Left` of the first `argument`.

2.5.6.5.5 Validation applicative

The `Validation data type` isomorphic to `Either`, but has accumulative `Applicative` on the `Left` side. `Validation data type` does not have a `monad` implemented. For `Either monad` `monad` has simple implementation: `Left case` drops computation and returns `Left` value. `Monad` needs to `process` the result of computation - for `Validation` - it requires to be able to `process` all `Left error statement` cases for `Validation`, it is or non-terminating `Monad` or one which is impossible to implement in `polymorphic` way with `Validation`.

2.5.6.6 Monad

μόνος *monos* sole

μονάδα *monáda* unit

In loose terms, `*` - is an ability built over `structures` that allows to `compose functions` that produce that `structures`.

Since it is possible to express unpure `functions` with `equivalent pure functions` that produce a `structure`, `*` become widely used in Haskell for those cases also. `*` with lazy `evaluation` also allows controll over the continuation of calculations by early terminations.

`*` - `lax monoid` in `endofunctor category`, that relies on η (`unit`) and μ (`join`) `natural transformations` to form an `equivalent` of `identity`.

`Monad` on \mathcal{C} is $\{E^{\mathcal{C} \rightarrow \mathcal{C}}, \eta, \mu\}$:

- $E^{\mathcal{C} \rightarrow \mathcal{C}}$ - is an `endofunctor`
- two `natural transformations`, $1^{\mathcal{C}} \rightarrow E$ and $E \circ E \rightarrow E$:

- $\eta^{1^{\mathcal{C}} \rightarrow E} = \text{unit}^{Identity \rightarrow E}(x) = f^{x \rightarrow E(x)}(x)$
- $\mu^{(E \circ E) \rightarrow E} = \text{join}^{(E \circ E) \rightarrow (Identity \circ E)}(x) = |y = E(x)| = f^{E(y) \rightarrow y}(y)$

where:

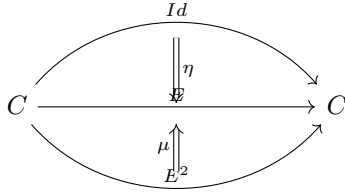
- \mathcal{C} is a **category**
- $1^{\mathcal{C}}$ denotes the \mathcal{C} **identity functor**
- $(E \circ E)$ - **endofunctor** $\mathcal{C} \rightarrow \mathcal{C}$

Definition with $\{E^{\mathcal{C} \rightarrow \mathcal{C}}, \eta, \mu\}$ (in **Hask**: $(\{e :: fa \rightarrow fb, \text{pure}, \text{join}\})$) - is classic categorical, in Haskell minimal complete definition is $\{\text{fmap}, \text{pure}, (\text{«}=\text{«})\}$.

While T is mode classical **Category** theory notation, we used the $E \equiv T$ substitution for purposes of notation being more understandable.

If there is a **structure** S , and a way of taking **object** x into S and a way of collapsing $S \circ S$ - there probably a **monad**.

Monad structure:



Mostly **monads** used for sequencing actions (computations) (that looks like imperative programming), with ability to depend on previous chains. Note if **monad** is **commutative** - it does not **order** actions.

Monad can shorten/terminate **sequence** of computations. It is implemented inside **Monad** instance. For example **Maybe monad** on **Nothing** drops **chain** of computation and returns **Nothing**.

* inherits the **Applicative** instance methods:

```
import Control.Monad (ap)
return == pure
ap == (<*>) -- + Monad requirement
```

Table 2.1: **Monad** in mathematics and Haskell

Math	Meaning	Cat/Fctr	$X \in \mathcal{C}$	Type	Haskell
Id	endofunctor "Id"	$\mathcal{C} \rightarrow \mathcal{C}$	$X \rightarrow Id(X)$	$a \rightarrow a$	id
E	endofunctor "monad"	$\mathcal{C} \rightarrow \mathcal{C}$	$X \rightarrow E(X)$	$m\ a \rightarrow m\ b$	fmap
η	natural transformation "unit"	$Id \rightarrow E$	$Id(X) \rightarrow E(X)$	$a \rightarrow m\ a$	pure
μ	natural transformation "multiplication"	$E \circ E \rightarrow E$	$E(E(X)) \rightarrow E(X)$	$m\ (m\ a) \rightarrow m\ a$	join

Internals of **Monad** are Haskell **data types**, and as such - they can be consumed any number of times.

Composition of **monadic types** does not always results in **monadic type**.

2.5.6.6.1 *

Monads Monadic

2.5.6.6.2 Monad property

Monad corresponds to **functor properties** & **applicative properties** and additionally:

2.5.6.6.2.1 *

Monad properties

2.5.6.6.2.2 Monad left identity property

```
pure x >>= f == f x
```

Explanation:

```
>>= :: Monad f =>    f a  -> (a -> f b) -> f b
                pure x >>=      f          == f x
```

Rule that `>>=` must get first **argument structure** internals and **apply** to the **function** that is the second **argument**.

Diagram on **category** level:

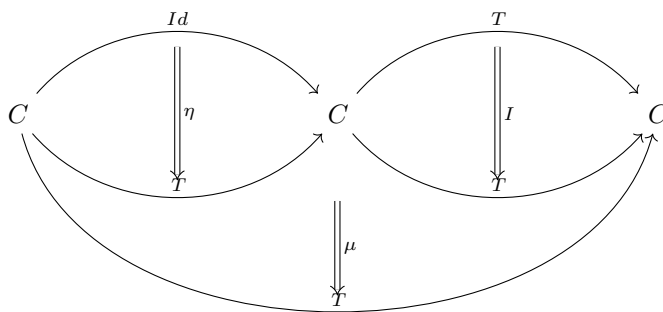
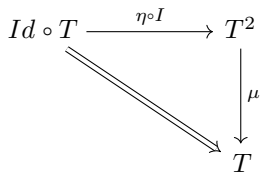


Diagram on **endomorphism** level:



2.5.6.6.2.3 Monad right identity property

```
f >>= pure == f
```

Explanation:

```
>>= :: Monad f => f a  -> (a -> f b) -> f b
                f    >>=      pure      == f
```

AKA it is a **tacit** description of a **monad bind** as **endofunctor**.

Diagram on **category** level:

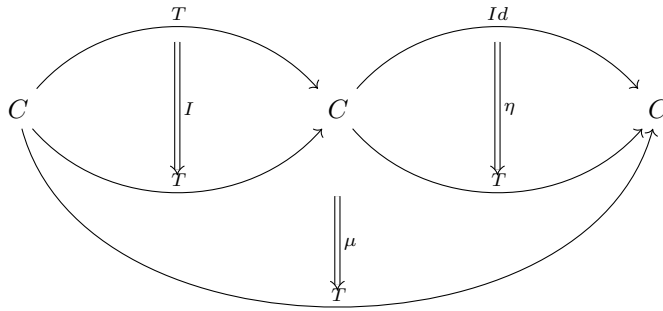
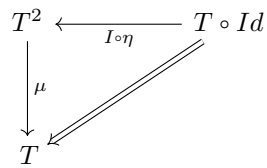


Diagram on endomorphism level:

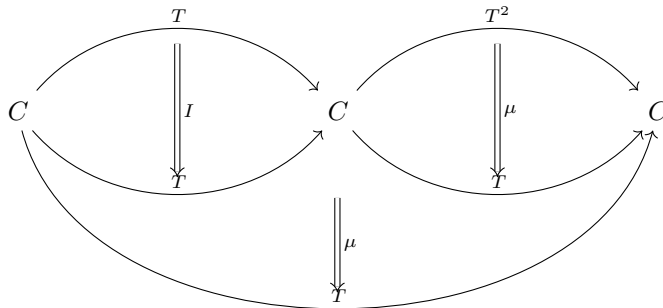


2.5.6.6.2.4 Monad associativity property

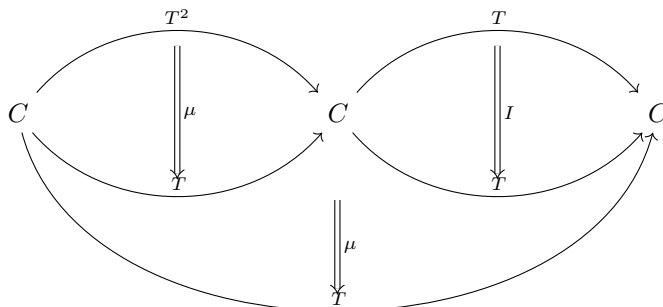
```
join (join (m m) m) == join (m join (m m))
(m >>= f) >>= g == m >>= (\ x -> f x >>= g)
```

In diagram form:

Category level:



is = to:



So, $\mu \circ (\mu \circ I) = \mu \circ (I \circ \mu)$

Endomorphism level:

$$\begin{array}{c}
 T^3 \\
 \begin{array}{c} \curvearrowright \quad \curvearrowleft \\ \mu \circ I \quad I \circ \mu \end{array} \\
 T^2 \\
 \downarrow \mu \\
 T
 \end{array}$$

2.5.6.6.3 Monad type class

```

class Applicative m => Monad m where
  (>>=) :: m a -> (a -> m b) -> m b
  (>>)  :: m a -> m b -> m b
  return :: a -> m a

```

2.5.6.6.3.1 MonadPlus type class

Is a [monoid](#) over [monad](#), with additional rules. The precise [set](#) of rules ([properties](#)) not agreed upon. Class instances obey *monoid* & *left zero* rules, some additionally obey *left catch* and others *left distribution*.

Overall there * currently reforms ([MonadPlus](#) reform proposal) in several smaller nad strictly defined [type classes](#).

Subclass of an [Alternative](#).

*

Monadplus

2.5.6.6.4 Functor -> Applicative -> Monad progression

```

<$> :: Functor    f => (a -> b) -> f a -> f b
<*> :: Applicative f => f (a -> b) -> f a -> f b
=<< :: Monad      f => (a -> f b) -> f a -> f b

```

pure & join are [Natural transformations](#) for the fmap.

2.5.6.6.5 Monad function

2.5.6.6.5.1 Return function

```
return == pure
```

Nonstrict.

2.5.6.6.5.2 Join function

```
join :: Monad m => m (m a) -> m a
```

Generales knowledge of concat.

[Kleisli composition](#) that flattens two layers of [structure](#) into one.

The way to express ordering in [lambda calculus](#) is to nest.

*

join

```
join . fmap == (=«)
```

```
-- b = f b
fmap      :: Monad f => (a -> f b) -> f a -> f (f b)
join      :: Monad f => f (f a) -> f a
join . fmap :: Monad f => (a -> f b) -> f a -> f b
flip      >>= :: Monad f => (a -> f b) -> f a -> f b
```

2.5.6.6.5.3 Bind function

```
>>=      :: Monad f => f a -> (a -> f b) -> f b
join . fmap :: Monad f => (a -> f b) -> f a -> f b
```

Nonstrict.

The most ubiquitous way to `>>=` something is to use [Lambda function](#):

```
getLine >>= \name -> putStrLn "age pls:"
```

Also a neat way is to bundle and handle [Monad](#) - is to bundle it with [bind](#), and leave [applied](#) partially. And use that partial bundle as a [function](#) - every [evaluation](#) of the [function](#) would trigger [evaluation](#) of internal [Monad structure](#). Thumbs up.

```
printOneOf :: Bool -> IO ()
printOneOf False = putStr "1"
printOneOf True  = putStr "2"

quant :: (Bool -> IO b) -> IO b
quant = (>>=) (randomRIO (False, True))

recursePrintOneOf :: Monad m => (t -> m a) -> t -> m b
recursePrintOneOf f x = (f x) >> (recursePrintOneOf f x)

main :: IO ()
main = recursePrintOneOf (quant) $ printOneOf
*
```

Monadic extend Monadic bind Monad bind Binder

```
(>>=)
>>=
(=<<)
=<<
```

2.5.6.6.5.4 Sequencing operator (`>>`) `\equiv` (`*>`):

[Sequencing operator](#), analog to the semicolon (or newline) in imperative languages. Discard value result of the action, sequentially add next ([compose](#) with) next action. [Applicative](#) has a similar [operator](#).

```
(>>) :: m a -> m b -> m b
(*>) :: f a -> f b -> f b
```

2.5.6.6.5.5 Monadic versions of list functions

```
sequence :: (Traversable t, Monad m) => t (m a) -> m (t a)
```

[Sequence](#) gets the traversable of [monadic](#) computations and swaps it into [monad](#) computation of traverse. In the result the collection of [monadic](#) computations turns into one long [monadic](#) computation on traverse of data.

If some step of this long computation fails - [monad](#) fails.

```
mapM :: (Traversable t, Monad m) => (a -> m b) -> t a -> m (t b)
```

mapM gets the AMB function, then takes traversable data. Then applies AMB function to traversable data, and returns converted monadic traversable data.

```
foldM :: (Foldable t, Monad m) => (b -> a -> m b) -> b -> t a -> m b
foldl :: Foldable t           => (b -> a -> b) -> b -> t a -> b
```

* is a monadic foldl.

b is initial cumulative value, m b is a cumulative bank. Right folding achieved by reversing the input list.

```
filterM :: Applicative m => (a -> m Bool) -> [a] -> m [a]
filter :: (a -> Bool) -> [a] -> [a]
```

Take Boolean monadic computation, filter the list by it.

```
zipWithM :: Applicative m => (a -> b -> m c) -> [a] -> [b] -> m [c]
zipWith :: (a -> b -> c) -> [a] -> [b] -> [c]
```

Take monadic combine function and combine two lists with it.

```
msum :: (Foldable t, MonadPlus m) => t (m a) -> m a
sum :: (Foldable t, Num a)         => t a -> a
```

2.5.6.6.5.6 liftM*

liftM Essentially a fmap.

```
liftM :: Monad m => (a -> b) -> m a -> m b
```

Lifts a function into monadic equivalent.

liftM2 Monadic liftA2.

```
liftM2 :: Monad m => (a -> b -> c) -> m a -> m a -> m c
```

Lifts binary function into monadic equivalent.

2.5.6.6.6 Comonad

Category \mathcal{C} comonad is a monad of opposite category \mathcal{C}^{op} .

2.5.6.6.7 Kleisli arrow

Morphism that while doing computation also adds monadic-able structure.

```
a -> m b
```

2.5.6.6.7.1 *

Kleisli arrows Kleisli morphism Kleisli morphisms

2.5.6.6.8 Kleisli composition

Composition of Kleisli arrows.

```
(<=<) :: Monad m => (b -> m c) -> (a -> m b) -> a -> m c infixr 1
;; compare
(.) :: (b -> c) -> (a -> b) -> a -> c
```

Often used left-to-right version:

```
(>=>) :: Monad m => (a -> m b) -> (b -> m c) -> a -> m c
;; compare
(>>=) :: Monad m => m a -> (a -> m b) -> m b
```

Which allows to replace [monadic bind chain](#) with [Kleisli composition](#).

```
f1 arg >>= f2 >>= f3
==
f1 >=> f2 >=> f3 $ arg
==
f3 <=< f2 <=< f1 $ arg
```

2.5.6.6.9 Kleisli category

[Category](#) \mathcal{C} , $\langle E, \vec{\eta}, \vec{\mu} \rangle$ [monad](#) over \mathcal{C} .

[Kleisli category](#) \mathcal{C}_T of \mathcal{C} :

$$\text{Obj}(\mathcal{C}_T) = \text{Obj}(\mathcal{C}) \quad \text{Hom}_{\mathcal{C}_T}(x, y) = \text{Hom}_{\mathcal{C}}(x, E(y))$$

2.5.6.6.10 Special monad

2.5.6.6.10.1 Identity monad

Wraps data in the [Identity constructor](#).

Useful: Creates [monads](#) from [monad transformers](#).

[Bind](#): Applies internal value to the [bound function](#).

Code: (see: [coerce](#))

```
newtype Identity a = Identity { runIdentity :: a }

instance Functor Identity where
    fmap      = coerce

instance Applicative Identity where
    pure      = Identity
    (<*>)     = coerce

instance Monad Identity where
    m >>= k   = k (runIdentity m)
```

Example:

```
-- derive the State monad using the StateT monad transformer
type State s a = StateT s Identity a
```

2.5.6.6.10.2 Maybe monad

Something that may not be or not return a result. Any lookups into the real world, database queries.

[Bind](#): Nothing input gives Nothing output, Just x input uses x as input to the [bound function](#).

When some computation results in [Nothing](#) - drops the [chain](#) of computations and returns [Nothing](#).

[Zero](#): [Nothing](#) Plus: result in first occurrence of Just else [Nothing](#).

Code:

```
data Maybe a = Nothing | Just a

instance Monad Maybe where
    return      = Just
    fail        = Nothing
```

```

Nothing >>= _ = Nothing
(Just x) >>= f = f x

instance MonadPlus Maybe where
  mzero          = Nothing
  Nothing `mplus` x = x
  x `mplus` _     = x

```

Example: Given 3 dictionaries:

- a. Full names to email addresses,
- b. Nicknames to email addresses,
- c. Email addresses to email preferences.

Create a **function** that finds a person's email preferences based on **either** a full name or a nickname.

```

data MailPref = HTML | Plain
data MailSystem = ...

getMailPrefs :: MailSystem -> String -> Maybe MailPref
getMailPrefs sys name =
  do let nameDB = fullNameDB sys
       nickDB = nickNameDB sys
       prefDB = prefsDB sys
     addr <- (lookup name nameDB) `mplus` (lookup name nickDB)
     lookup addr prefDB

```

2.5.6.6.10.3 Either monad

When computation results in **Left** - drops other computations & returns the recieved **Left**.

2.5.6.6.10.4 Error monad

Something that can fail, throw **exceptions**.

The failure **process** records the description of a failure. **Bind function** uses successful values as input to the **bound function**, and passes failure information on without executing the **bound function**.

Useful: Composing **functions** that can fail. Handle **exceptions**, crate **error** handling **structure**.

Zero: empty **error**. Plus: if first **argument** failed then execute second **argument**.

2.5.6.6.10.5 List monad

Computations which may return 0 or more possible results.

Bind: The **bound function** is **applied** to all possible values in the input **list** and the resulting lists are concatenated into **list** of all possible results.

Useful: Building computations from **sequences** of non-deterministic operations.

Zero: [] Plus: (++)

*

[] monad

2.5.6.6.10.6 Reader monad

Creates a read-only shared environment for computations.

The pure `function` ignores the environment, while `>>=` passes the inherited environment to both subcomputations.

Today it is defined though `ReaderT` transformer:

```
type Reader r = ReaderT r Identity -- equivalent to ((->) e), (e ->)
```

Old definition was:

```
newtype Reader e a = Reader { runReader :: (e -> a) }
```

For `(e ->)`:

- `Functor` is `(.)`

```
fmap :: (b -> c) -> (a -> b) -> a -> c
fmap = (.)
```

- `Applicative`:

- `pure` is `const`

```
pure :: a -> b -> a
pure x _ = x
```

- `(<*>)` is:

```
(<*>) :: (a -> b -> c) -> (a -> b) -> a -> c
(<*>) f g = \a -> f a (g a)
```

- `Monad`:

```
(>>=) :: (a -> b) -> (b -> a -> c) -> a -> c
(>>=) m k = Reader $ \r ->
  runReader (k (runReader m r)) r
```

```
join :: (e -> e -> a) -> e -> a
join f x = f x x
```

```
runReader
  :: Reader r a -- the Reader to run
  -> r -- an initial environment
  -> a -- extracted final value
```

Usage:

```
data Env = ...
```

```
createEnv :: IO Env
createEnv = ...
```

```
f :: Reader Env a
f = do
  a <- g
  pure a
```

```
g :: Reader Env a
g = do
  env <- ask -- "Open the environment namespace into env"
  a <- h env -- give env to h
  pure a
```

```
h :: Env -> a
```



```

... -- use env and produce the result

main :: IO ()
main = do
  env <- createEnv
  a = runReader g env
  ...

```

In Haskell under normal circumstances impure [functions](#) should not directly call impure [functions](#). `h` is an impure [function](#), and `createEnv` is impure [function](#), so they should have intermediary.

2.5.6.6.10.7 Writer monad

Computations which accumulate [monoid](#) data to a shared Haskell storage. So `*` is parametrized by [monoidal type](#).

Accumulator is maintained separately from the returned values.

Shared value modified through [Writer monad](#) methods.

`*` frees creator and code from manually keeping the track of accumulation.

Bind: The [bound function](#) is [applied](#) to the input value, [bound function](#) allowed to `<>` to the accumulator.

```
type Writer r = WriterT r Identity
```

Example:

```

f :: Monoid b => a -> (a, b)
f a = if _condition_
      then runWriter $ g a
      else runWriter do
        a1 <- h a
        pure a1

g :: Monoid b => Writer b a
g a = do
  tell _value1_ -- accumulator <> _value1_
  pure a -- observe that accumulator stored inside monad
          -- and only a main value needs to be returned.

h :: Monoid b => Writer b a
h a = do
  tell _value2_ -- accumulator <> _value_
  pure a

runWriter :: Writer w a -> (a, w) -- Unwrap a writer computation
                                   -- as a (result, accumulator) pair.
                                   -- The inverse of writer.

```

`WriterT`, `Writer` unnecessarily keeps the entire logs in the memory. Use `fast-logger` for logging.

2.5.6.6.10.8 State monad

Computations that pass-over a state.

The [bound function](#) is [applied](#) to the input value to produce a state transition [function](#) which is [applied](#) to the input state.

[Pure](#) functional language cannot update values in place because it violates [referential transparency](#).

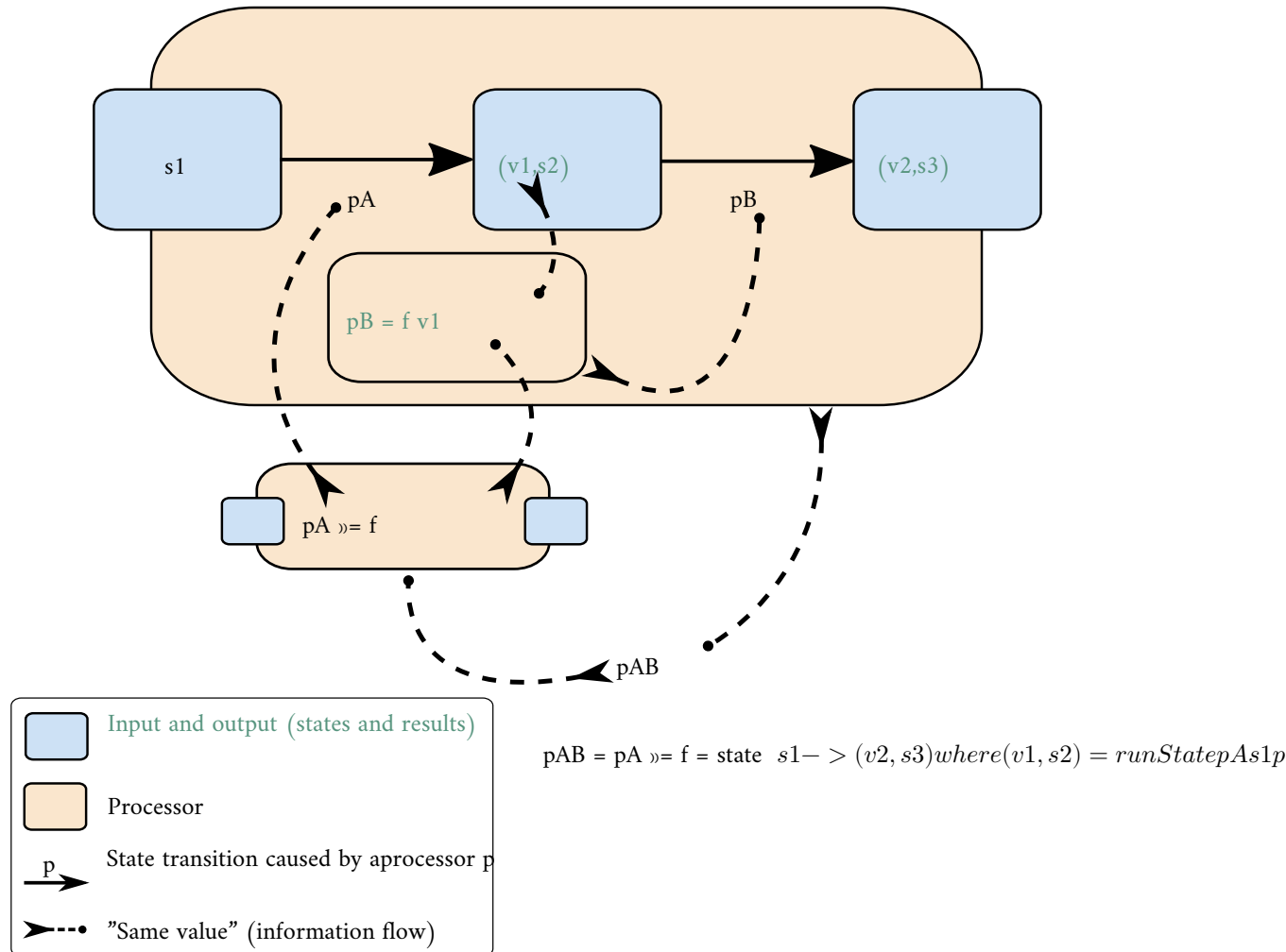
```
type State s = StateT s Identity
```

Binding copies and transforms the state **parameter** through the **sequence** of the **bound functions** so that the same state storage is never used twice. Overall this gives the illusion of in-place update to the programmer and in the code, while in fact the autogenerated transition **functions** handle the state changes.

Example **type**: `State st a`

`State` describes **functions** that consume a state and produce a **tuple** of result and an updated state.

Monad manages the state with the next **process**:



Where:

- `f` - processor making **function**
- `pA`, `pAB`, `pB` - state processors
- `sN` - states
- `vN` - values

Bind with a processor making **function** from state processor (`pA`) creates a new state processor (`pAB`). The wrapping and unwrapping by `State/runState` is implicit.

2.5.6.6.11 Monad transformer

* is a practical solution to the current functional programming situation that generally **monads** do not have **composition** ability. In other words many **monads** can not be **composed**.

* is a **special monad** that extends other **monad** with extra functionality, it is a convenience mechanism, the functionality itself always can be developed in some other way. Sometimes transformers can make things way harder (especially profound for concurrency ([Michael Snoyman - Monad Transformer State](#))) then other ways of implementation, especially when transformers hold some **structure** information (state-like information, in **ExceptT**, **StateT**)

Monad is not **closed** under composition. **Composition** of **monadic types** does not always results in **monadic type**.

Basic **case**: during implementation of **monadic composition**, as a result **type** $m \rightarrow T \rightarrow m \rightarrow a$ arises, which does not allow join transformation for the m **monadic** layers or to have a regular **unit** transformation.

Monads that are * are the **monads** that have own **properties** as also ability to **compose** with any other monad and extend it with own **properties**. * use their implementation to solve the composition **type** layering and allow to attach desirable **property** to result.

* solve **monad composition** and **type** layering by using own **structure** and information about itself. It is often that **process** involves a **catamorphism** of a * **type** layer.

Transformers have a light wrapper around the data that tags the modification with this transformer.

In **type** signatures of transformers $*T \rightarrow m \rightarrow m \rightarrow a$ is already an extended **monad**, so $*T$ is just a wrapper to point that out.

Main **monadic structure** m is wrapped around the internal data (core is a). The **structure** that corresponds to the transformer creation **properties** (if it emitted by η of a transformer), goes into $m \rightarrow$. Open **parameters** go external to the m .

```
newtype ExceptT e m a =
  ExceptT { runExceptT :: m (Either e a) }
```

```
newtype MaybeT m a =
  MaybeT { runMaybeT :: m (Maybe a) }
```

```
newtype ReaderT r m a =
  ReaderT { runReaderT :: r -> m a }
```

This has an **effect** that on stacking **monad** transformers, m becomes **monad stack**, and every next transformer injects the transformer creation-specific properties η inside the **stack**, so out-most transformer has inner-most **structure**. Base **monad** is structurally the outermost.

2.5.6.6.11.1 MaybeT

* extends **monads** by injecting **Maybe** layer underneath **monad**, and processing that **structure**:

```
newtype MaybeT m a = MaybeT { runMaybeT :: m (Maybe a) }
```

2.5.6.6.11.2 EitherT

* extends **monads** by injecting **Either** layer underneath **monad**, and processing that **structure**:

```
newtype EitherT e m a = EitherT { runEitherT :: m (Either e a) }
```

EitherT of either package gets replaced by **ExceptT** of transformers or **mtl** packages.

* **ExceptT**

2.5.6.6.11.3 ReaderT

Definition:

```
newtype ReaderT r m a = ReaderT { runReaderT :: r -> m a }
```

* **functions:** input `monad m a`, out: `m a` wrapped it in a free-variable `r` (**partially applied function**). That allows to use transformed `m a`, now it requires and can use the `r` passed environment.

To create a **Reader monad**:

```
type Reader r = ReaderT r Identity
```

2.5.6.6.11.4 MonadTrans type class

Allows to **lift monadic** actions into a larger **context** in a neutral way.

`pure` takes a parametric **type** and embodies it into constructed **structure** (talking of **monad** transformers - **structure** of the stacked **monads**).

`lift` takes **monad** and extends it with a transformer.

In fact, for **monad** transformers - `lift` is a last stage of the `pure`, it follows from the **lift property**.

Method:

```
lift :: Monad m => m a -> t m a
```

Lift a computation from the **argument monad** to the constructed **monad**.

Neutral means:

```
lift . return = return
```

```
lift (m >>= f) = lift m >>= (lift . f)
```

The general pattern with **MonadTrans** instances is that it usually lifts the **injection** of the known **structure** of transformer over some **Monad**.

`lift` embeds one **monadic** action into **monad transformer**.

The difference between **pure**, **lift** and **MaybeT** constructor becomes clearer if you look at the **types**:

Example, for **MaybeT IO a**:

```
pure      ::      a -> MaybeT IO a
lift      ::      IO a -> MaybeT IO a
MaybeT   :: IO (Maybe a) -> MaybeT IO a
```

```
x = (undefined :: IO a)
```

```
:t (pure x)
(pure x) :: Applicative t => t (IO a)  -- t recieves one argument of product
      ↪ type
:t (pure x :: MaybeT IO a)
-- Expected type: MaybeT IO a1
-- Actual type: MaybeT IO (IO a0)

-- While the real type would be
:t (pure x :: MaybeT IO (IO a))
(pure x :: MaybeT IO (IO a)) :: MaybeT IO (IO a)
-- This goes into a conflict of what type&kind (* -> *) transformer constructor
-- awaits, and `m (m a)` is a layering we not interested in.
```

```

:t (lift x)
(lift x) :: MonadTrans t => t IO a -- result is a proper expected product type

-- To belabour
:t (lift x :: MaybeT IO a)
(lift x) :: MonadTrans t => t IO a -- result is a proper expected product type

lift is a natural transformation  $\eta$  from an Identity monad (functor) with other monad as content into
transformer monad (functor), with the preservation of the contained monad:

-- Abstract monads with content as parameters. Define '~>' as a family of
-- morphisms that translate one functor into another (natural transformation)
type f ~> g = forall x. f x -> g x
-- follows
lift :: m ~> t m

```

MonadIO type class * - allows to lift IO action until reaching the IO monad layer at the top of the Monad stack (which is allways in the Haskell code that does IO).

```

class (Monad m) => MonadIO m where
    liftIO :: IO a -> m a

liftIO properties:
liftIO . pure = pure

liftIO (m >>= f) = liftIO m >>= (liftIO . f)

```

Which is identical properties to MonadTrans lift.

Since lift is one step, and liftIO all steps - all steps defined in terms of one step and all other steps, so the most frequent implementation is self-recursive lift . liftIO:

```
liftIO ioa = lift $ liftIO ioa
```

*

liftIO

2.5.6.7 Alternative type class

Monoid over applicative. Has left catch property.

Allows to run simultaneously several instances of a computation (or computations) and from them yield one result by property from (<|>) :: Type -> Type -> Type.

Minimal complete definition:

```

empty :: f a -- The identity element of <|>
(<|>) :: f a -> f a -> f a -- Associative binary operation

```

Additional functions some and many defined (automatically derived) as the least solutions to the equations:

```

some v = (:) <$> v <*> many v
many v = some v <|> pure []
-- => some v = (:) <$> v <*> $ some v <|> pure []

some :: f a -> f [a] -- One or more. Keep trying applying f to a until it
    => succeeds at least once, and then keep doing it until it fails.
more :: f a -> f [a] -- Zero or more. Apply f to a as many times as you can
    => until failure.

```

So there in the `process` should be found a definitive `case` of failure termination rule or otherwise `process` would never terminate.

To start understand intuitive difference:

```
> some Nothing
Nothing
> many Nothing
Just []
```

Perhaps it helps to see how `some` would be written with `monadic` `do` syntax:

```
some f = do
  x <- f
  xs <- many f
  return (x:xs)
```

So `some f` runs `f` once, then "many" times, and conses the results. `many f` runs `f` "some" times, or "alternative'ly" just returns the empty `list`. The idea is that they both run `f` as often as possible until it "fails", and after that - `compose` the `list` of results. The difference is that `some f` fails if `f` fails immediately, while `many f` will succeed and "return" the empty `list`. But what this all means exactly depends on how `<|>` is defined.

Is it only useful for parsing? Let's see what it does for the instances in base: `Maybe`, `[]` and `STM`.

First `Maybe`. `Nothing` means failure, so `some Nothing` fails as well and evaluates to `Nothing` while `many Nothing` succeeds and evaluates to `Just []`. Both `some (Just ())` and `many (Just ())` never return, because `Just ()` never fails! In a sense they evaluate to `Just (repeat ())`.

For lists, `[]` means failure, so `some []` evaluates to `[]` (no answers) while `many []` evaluates to `[[]]` (there's one answer and it is the empty `list`). Again `some [()]` and `many [()]` don't return. Expanding the instances, `some [()]` means `fmap (():)` (`many [()]`) and `many [()]` means `some [()] ++ [[]]`, so you could say that `many [()]` is the same as `tails (repeat ())`.

For `STM`, failure means that the transaction has to be retried. So `some retry` will retry itself, while `many retry` will simply return the empty `list`. `some f` and `many f` will run `f` repeatedly until it retries. I'm not sure if this is useful thing, but I'm guessing it isn't.

So, for `Maybe`, `[]` and `STM` `many` and `some` don't seem to be that useful. It is only useful if the `applicative` has some `kind` of state that makes failure increasingly likely when running the same thing over and over. For parsers this is the input which is `shrinking` with every successful match.

2.5.6.7.1 *

Alternative

2.5.7 Monoidal functor

`Functors` between `monoidal categories` that preserves `monoidal structure`.

2.5.8 \$>

Get & `set` a value inside `Functor`.

2.5.8.1 *

<\$

2.5.9 Multifunctor

Functor that takes as an **argument** the **product** of **types**.

Or if combine it with **product** - accepts multiple arguments, so from that constructs "source" **product category** (**Cartesian product**) of **categories**, and realizes a **functor** from **product category** to target **category**.

Concept works over N **type** arguments instead of one.

Generalizes the concept of **functor** between **categories**, canonical **morphisms** between multicategories.

Any **product** or sum in a Cartesian **category** is a $*$.

In Haskell there is only one **category**, **Hask**, so in Haskell $*$ is still **endofunctor** $(Hask \times Hask) \rightarrow Hask \Rightarrow |(Hask \times Hask) \equiv Hask| \Rightarrow Hask \rightarrow Hask$.

Code definition:

```
class Bifunctor f
  where
    bimap :: (a -> a') -> (b -> b') -> f a b -> f a' b'
    bimap f g = first f . second g
    first :: (a -> a') -> f a b -> f a' b
    first f = bimap f id
    second :: (b -> b') -> f a b -> f a b'
    second = bimap id
```

2.5.9.1 $*$

Bifunctor

2.6 Hask category

Category of Haskell where **objects** are **types** and **morphisms** are **functions**.

It is a hypothetical **category** at the moment, since **undefined** and **bottom values** break the theory, is not Cartesian **closed**, it does not have sums, **products**, or **initial object**, $()$ is not a **terminal object**, **monad** identities fail for almost all instances of the **Monad** class.

That is why Haskell developers think in subset of Haskell where **types** do not have **bottom values**. This only includes **functions** that terminate, and typically only finite values. The corresponding **category** has the expected initial and terminal **objects**, sums and **products**, and instances of **Functor** and **Monad** really are **endofunctors** and **monads**.

Hask contains subcategories, like **Lst** containing only **list types**.

Haskell and **Category** concepts:

- Things that take a **type** and return another **type** are **type constructors**.
- Things that take a **function** and return another **function** are **higher-order functions**.

2.6.1 $*$

Hask

2.7 Morphism

μορφή *morphe* form

Arrow between two **objects** inside a **category**.

Morphism can be anything.

Morphism is a generalization ($f(x*y) \equiv f(x) \diamond f(y)$) of **homomorphism** ($f(x*y) \equiv f(x)*f(y)$).

Since general **morphisms** not so much often ment and discussed - under **morphism** people almost always really mean the meaning of **homomorphism**-like **properties**, hense they discuss the **algebraic structures (types)** and homomorphisms between them.

In most usage, on a level under the **objects**: * is most often means a map (**relation**) that translates from one mathematical **structure** (that source **object** represents) to another (that target **object** represents) (that is called (somewhat, somehow) "**structure**-preserving", but that **phrase** still means that translation can be lossy and irrevertable, so it is only bear reassemblence of preservation), and in the end the **morphism** can be anything and not hold to this conditions.

Morphism needs to correspond to **function** requirements to be it.

2.7.1 *

Morphisms Arrow Arrows

2.7.2 Homomorphism

ὁμός *homos* same (was chosen because of initial Anglish mistranslation to "similar")

μορφή *morphe* form

similar form

* map between two **algebraic structures** of the same **type** that preserves the operations.

$f(x * y) \equiv f(x) * f(y)$, **where** for $f^{A \rightarrow B}$ - A, B are **sets** with additonal **algebraic structures (algebras)** that include **operation** *; x, y are elements of the **set** B .

* sends **identity morphisms** to **identity morphisms** and inverses to inverses.

The concept of * has been generalized under the name of **morphism** to many **structures** that **either** do not have an underlying **set**, or are not **algebraic**, or do not preserve the **operation**.

2.7.2.1 *

Homomorphic

2.7.3 Identity morphism

Identity morphism - or simply **identity**: $x \in C : id_x = 1_x : x \rightarrow x$ **Composed** with other **morphism** gives same **morphism**.

Corresponds to **Reflexivity** and **Automorphism**.

2.7.3.1 Identity

Identity only possible with **morphism**. See **Identity morphism**.

There is also distinct **Zero** value.

2.7.3.1.1 Two-sided identity of a predicate

$P(e, a) = P(a, e) = a \mid \exists e \in S, \forall a \in S P()$ is **commutative**.

Predicate

2.7.3.1.2 Left identity of a predicate

$$\exists e \in S, \forall a \in S : P(e, a) = a$$

Predicate

2.7.3.1.3 Right identity of a predicate

$$P(a, e) = a \mid \exists e \in S, \forall a \in S$$

Predicate

2.7.3.2 Identity functionReturn itself. $(\backslash x.x)$ `id :: a -> a`**2.7.4 Monomorphism** $\mu\omicron\nu\omicron$ *mono* only $\mu\omicron\rho\phi\eta$ *morphe* form

Maps one to one (uniquely), so invertable (always has [inverse morphism](#)), so preserves the information/structure. [Domain](#) can be equal or less to the [codomain](#).

$f^{X \rightarrow Y}, \forall x \in X \exists! y = f(x) \models f(x) \equiv f_{mono}(x)$ - from [homomorphism context](#) $f_{mono} \circ g1 = f_{mono} \circ g2 \models g1 \equiv g2$ - from general [morphism context](#) Thus * is left cancelable.

If * is a [function](#) - it is [injective](#). Initial [set](#) of f is fully uniquely mapped onto the [image](#) of f .

2.7.4.1 *

Monomorphic Monomorphisms

2.7.5 Epimorphism $\epsilon\pi$ *epi* on, over $\mu\omicron\rho\phi\eta$ *morphe* form

* is end-equating [morphism](#). Since [epimorphism](#) covers target fully - \forall [morphisms](#) [composed](#) to its end (target) are fully active in [composition](#) and so fully comparable between each other.

Term end-equating is more direct, easy and clear then classic [right-cancelable](#). Since "right" is collision between direction of [composition](#) (right to left) (and sometimes [composition](#) gets writted left to right), way it is drawn (left to right), and written $C \rightarrow D$ (left to right).

$f^{X \rightarrow Y}, \forall y \in Y \exists f(x) \models f(x) \equiv f_{epi}(x)$ - from [homomorphism context](#) $g1 \circ f_{epi} = g2 \circ f_{epi} \Rightarrow g1 \equiv g2$ - from general [morphism context](#)

In [Set category](#) if * is a [function](#) - it is [surjective](#) ([image](#) of it fully uses [codomain](#)) [Codomain](#) is a called a projection of the [domain](#).

* fully maps into the target.

2.7.5.1 *

Epimorphic Epimorphisms

2.7.6 Isomorphism

ἴσος *isos* equal

μορφή *morphe* form

Not equal, but equal for current intents and purposes. **Morphism** that has **inverse**. Almost equal, but not quite: (Integer, Bool) & (Bool, Integer) - but can be transformed losslessly into one another.

Bijjective homomorphism is also **isomorphism**.

$$f^{-1, b \rightarrow a} \circ f^{a \rightarrow b} \equiv 1^a, f^{a \rightarrow b} \circ f^{-1, b \rightarrow a} \equiv 1^b$$

2 reasons for non-**isomorphism**:

- **function** at least ones collapses a values of **domain** into one value in **codomain**
- **image** (of a **function** in **codomain**) does not fill-in **codomain**. Then **isomorphism** can exists for **image** but not whole **codomain**.

Categories are **isomorphic** if there $R \circ L = ID$

2.7.6.1 *

Isomorphic Isomorphisms

2.7.6.2 Lax

Holds up to **isomorphism**. (upon the transformation can be used as the same)

2.7.7 Endomorphism

ἐνδο *endo* internal

μορφή *morphe* form

Arrow from **object** to itself. **Endomorphism** forms a **monoid** (**object** exists and **category** requirements already in place).

2.7.7.1 Automorphism

αὐτο *auto* self

μορφή *form* form

Isomorphic endomorphism.

Corresponds to **identity**, **reflexivity**, **permutation**.

2.7.7.1.1 *

Automorphic Automorphisms

2.7.7.2 *

Endomorphic Endomorphisms

2.7.8 Catamorphism

κατά *kata* downward

μορφή *morphe* form

Unique **arrow** from an initial **algebra structure** into different **algebra structure**.

* in FP is a generalization folding, deconstruction of a [data structure](#) into more primitive [data structure](#) using a [functor F-algebra structure](#).

* reduces the [structure](#) to a lower level [structure](#). * creates a projection of a [structure](#) to a lower level [structure](#).

2.7.8.1 *

Catamorphic Catamorphisms

2.7.8.2 Catamorphism property

Table 2.2: [Catamorphism properties](#) in Haskell

Rule name	Haskell
cata-cancel	<code>cata phi . InF = phi . fmap (cata phi)</code>
cata-refl	<code>cata InF = id</code>
cata-fusion	<code>f . phi = phi . fmap f => f . cata phi = cata phi</code>
cata- compose	<code>eps :: f ~> g => cata phi . cata (In . eps) = cata (phi . eps)</code>

2.7.8.2.1 Hylomorphism

[catamorphism](#) \circ [anamorphism](#)

Expanding and collapsing the [structure](#).

2.7.8.2.1.1 *

Hylomorphic Hylomorphisms

2.7.8.3 Anamorphism

Generalizes unfold.

[Dual](#) concept to [catamorphism](#).

Increases the [structure](#).

[Morphism](#) from a [coalgebra](#) to the final [coalgebra](#) for that [endofunctor](#).

Is a [function](#) that generates a [sequence](#) by repeated [application](#) of the [function](#) to its previous result.

2.7.8.3.1 *

Anamorphic Anamorphisms

2.7.9 Kernel

[Kernel](#) of a [homomorphism](#) is a number that measures the [degree homomorphism](#) fails to meet [injectivity](#) (AKA be [monomorphic](#)). It is a number of [domain](#) elements that fail [injectivity](#):

- elements not included into [morphism](#)
- elements that collapse into one element in [codomain](#)

thou [Kernel](#) $[x|x \leftarrow 0||x \geq 2]$.

Denotation: $\ker T = \{\mathbf{v} \in V : T(\mathbf{v}) = \mathbf{0}_W\}$.

2.7.9.1 Kernel homomorphism

Morphism of elements from the **kernel**. Complementary **morphism** of elements that make main **morphism** not **monomorphic**.

2.8 Set category

Category in which **objects** are **sets**, **morphisms** are **functions**.

Denotation: *Set*

2.9 Natural transformation

Roughly $*$ is:

trans :: **F** a -> **G** a

, while **a** is **polymorphic variable**.

Naturality condition: $\forall a \exists (F a \rightarrow G a)$, or, analogous to **parametric polymorphism** in **functions**. Since $*$ in a **category**, stating $\forall (F a \rightarrow G a)$ **Naturality** condition means that all **morphisms** that take part in **homotopy** of source **functor** to target **functor** must exist, and that is the same, diagrams that take part in transformation, should commute, and different paths bring same result: if α - **natural transformation**, α_a **natural transformation component** - $G f \circ \alpha_a = \alpha_b \circ F f$. Since $*$ are just a **type** of parametric **polymorphic function** - they can **compose**.

$*$ ($\vec{\eta}^{\mathcal{D}}$) is transforming: $\vec{\eta}^{\mathcal{D}} \circ F^{\mathcal{C} \rightarrow \mathcal{D}} = G^{\mathcal{C} \rightarrow \mathcal{D}} \circ *$. **abstraction** creates higher-language of **Category** theory, allowing to talk about the **composition** and transformation of complex entities.

It is a **process** of transforming $F^{\mathcal{C} \rightarrow \mathcal{D}}$ into $G^{\mathcal{C} \rightarrow \mathcal{D}}$ using existing **morphisms** in target **category** \mathcal{D} .

Since it uses **morphisms** - it is **structure**-preserving transformation of one **functor** into another. It is mostly a lossy transformation. Only existing **morphisms** can make it exist.

Existence of $*$ between two **functors** can be seen as some **relation**.

Can be observed to be a "**morphism of functors**", especially in **functor category**. $*$ by $\vec{\eta}_{y^e}^{\mathcal{D}}(\overline{(x, y)}^{\mathcal{C}}) \circ F^{\mathcal{C} \rightarrow \mathcal{D}}(\overline{(x, y)}^{\mathcal{C}}) = G^{\mathcal{C} \rightarrow \mathcal{D}}(\overline{(x, y)}^{\mathcal{C}}) \circ \vec{\eta}_{x^e}^{\mathcal{D}}(\overline{(x, y)}^{\mathcal{C}})$, often written short $\vec{\eta}_b \circ F(\vec{f}) = G(\vec{f}) \circ \vec{\eta}_a$. Notice that the $\vec{\eta}_{x^e}^{\mathcal{D}}(\overline{(x, y)}^{\mathcal{C}})$ depends on **objects&morphisms** of \mathcal{C} .

In words: $*$ depends on F and G **functors**, ability of \mathcal{D} **morphisms** to do a **homotopy** of F to G , and $*$:

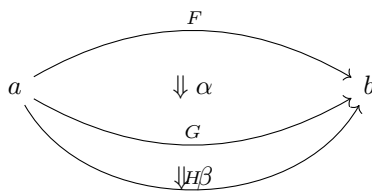
- for every **object** in \mathcal{C} picks **natural transformation component** in \mathcal{D} .
- for every **morphism** in \mathcal{C} picks the **commuting diagram** in \mathcal{D} , called naturality square.

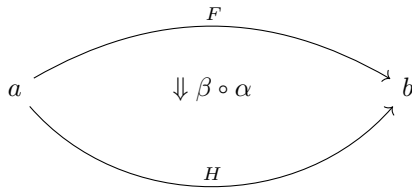
Also see: **Natural transformation in Haskell**

Knowledge of $*$ forms a **2-category**.

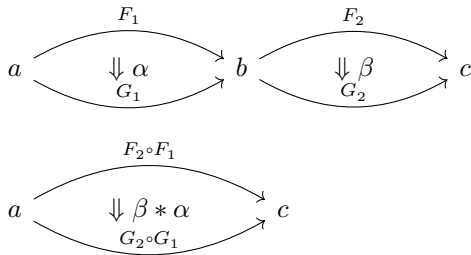
Can be **composed**

- "vertically":





- "horizontally" ("Godement **product**"):



Vertical and horizontal **compositions** can be done in any **order**, they abide the exchange **property**.

2.9.1 *

Natural transformations Naturality condition Naturality

2.9.2 Natural transformation component

$$\vec{\eta}^{\mathcal{D}}(x) = F^{\mathcal{D}}(x) \rightarrow G^{\mathcal{D}}(x) \mid x \in \mathcal{C}$$

2.9.2.1 *

Component of natural transformation

2.9.3 Natural transformation in Haskell

Family of **parametric polymorphism functions** between **endofunctors**.

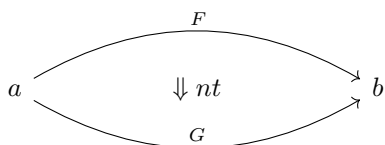
In **Hask** is $F a \rightarrow G a$. Can be analogued to repackaging data into another container, never modifies the **object** content, it only if - can delete it, because **operation** is lossy.

Can be sees as ortogonal to **functors**.

2.9.4 Cat category

Category where:

	Part	Is	#
*	object	category	0-cell
\Rightarrow	morphism	functor	1-cell
\Rightarrow	2-morphism	natural transformation, morphisms homotopy	2-cell



Is Cartesian **closed category**.

2.9.4.1 *

Cat 2-category

2.9.4.2 Bicategory

2-category that is enriched and lax.

For handling relaxed associativity - introduces associator, and for identity 1 - left/right unitor.

Forming from bicategories higher categories by stacking levels of abstraction of such categories - leads to explosion of special cases, differences of every level, and so overall difficulties.

Stacking groupoids (category in which are morphisms are invertable) is much more homogenous up to infinity, and forms base of the homotopy type theory.

2.10 Category dual

Category duality behaves like a logical inverse.

Inverse $\mathcal{C} = \mathcal{C}^{op}$ - inverts the direction of morphisms.

Composition accordingly changes to the morphisms: $(g \circ f)^{op} = f^{op} \circ g^{op}$

Any statement in the terms of \mathcal{C} in \mathcal{C}^{op} has the dual - the logical inverse that is true in \mathcal{C}^{op} terms.

Opposite preserves properties:

- products: $(\mathcal{C} \times \mathcal{D})^{op} \cong \mathcal{C}^{op} \times \mathcal{D}^{op}$
- functors: $(F^{\mathcal{C} \rightarrow \mathcal{D}})^{op} \cong F^{\mathcal{C}^{op} \rightarrow \mathcal{D}^{op}}$
- slices: $(\mathcal{F} \downarrow \mathcal{G})^{op} \cong (\mathcal{G}^{op} \downarrow \mathcal{F}^{op})$

2.10.0.0.1 *

Opposite category Opposite categories Category duality Duality Dual category Dual

2.10.1 Coalgebra

Structures that are dual (in the category-theoretic sense of reversing arrows) to unital associative algebras. Every coalgebra, by vector space duality, reversing arrows - gives rise to an algebra. In finite dimensions, this duality goes in both directions. In infinite - it should be determined.

2.11 Thin category

\forall Hom sets contain zero or one morphism.

$$f \equiv g \mid \forall x, y \forall f, g : x \rightarrow y$$

A proset (preordered set).

2.11.1 *

Proset category Prosetal category Poset category Posetal category

2.12 Commuting diagram

Establishes equality in morphisms that have same source and target.

Draws the morphisms that are: $f = g \Rightarrow \{f, g\} : X \rightarrow Y$

2.12.1 *

Diagram commutes Commutes

2.13 Universal construction

Algorithm of constructing definitions in [Category](#) theory. Specially good to translate [properties](#)/definitions from other theories ([Set theory](#)) to [Categories](#).

Method:

- a. Define a pattern that you defining.
- b. Establish ranking for pattern matches.
- c. The top of ranking, the best match or [set](#) of matches - is the thing you was looking for. Matches are [isomorphic](#) for defined rules.

* uses Yoneda lemma, and as such constructions are defined until [isomorphism](#), and so [isomorphic](#) between each-other.

2.13.1 *

Universal constructions

2.14 Product

[Universal construction](#):

$$\begin{array}{ccccc}
 & & c' & & \\
 & p \swarrow & \downarrow ! & \searrow q & \\
 a & \xleftarrow{\pi_a} & c & \xrightarrow{\pi_b} & b
 \end{array}$$

Pattern: $p : c \rightarrow a$, $q : c \rightarrow b$

Ranking: $\max \sum^{\forall} (! : c' \rightarrow c \mid p' = p \circ !, q' = q \circ !)$

c' is another candidate.

For [sets](#) - [Cartesian product](#).

* is a pair. Corresponds to [product data type](#) in [Hask](#) (inhabited with all elements of the [Cartesian product](#)).

[Dual](#) is [Coproduct](#).

2.14.1 *

Products

2.15 Coproduct

[Universal construction](#):

$$\begin{array}{ccccc}
 & & c' & & \\
 & p \nearrow & \uparrow ! & \nwarrow q & \\
 a & \xrightarrow{\iota_a} & c & \xleftarrow{\iota_b} & b
 \end{array}$$

Pattern: $i : a \rightarrow c$, $j : b \rightarrow c$

Ranking: $\max \sum^{\forall} (! : c \rightarrow c' \mid i' = ! \circ i, j' = ! \circ j)$

c' is another candidate.

For **sets** - Disjoint union.

$*$ is a **set** assembled from other two **sets**, in Haskell it is a tagged **set** (analogous to disjoint union).

Dual is **Product**.

2.15.1 *

Coproducts

2.16 Free object

General particular **structure**. In which **structure**, **properties** autofollows from definition, axioms.

Also uses as a term when surcomstances of **structures**, rules, **properties**, axioms used coincide with the definition of a particular **object** \therefore form **object** of this **type** with the according **properties** and possibilities.

2.17 Internal category

Category which is included into a bigger **category**.

2.18 Hom set

All **morphisms** from source **object** to target **object**.

Denotation: $hom_C(X, Y) = (\forall f : X \rightarrow Y) = hom(X, Y) = C(X, Y)$ Denotation was not standardized.

Hom sets belong to **Set category**.

In **Set category**: $\exists!(a, b) \iff \exists! Hom, \forall Hom \in Set$. **Set category** is special, **Hom sets** are also **objects** of it.

Category can include **Set**, and **hom sets**, or not.

2.18.1 *

Hom-set Hom sets

2.18.2 Hom-functor

$hom : \mathcal{C}^{op} \times \mathcal{C} \rightarrow Set$ **Functor** from the **product** of \mathcal{C} with its **opposite category** to the **category** of **sets**.

Denotation variants: $H_A = Hom(-, A)$ $h_A = \mathcal{C}(-, A)$ $Hom(A, -) : \mathcal{C} \rightarrow Set$

Hom-**bifunctor**: $Hom(-, -) : \mathcal{C}^{op} \times \mathcal{C} \rightarrow Set$

2.18.3 Exponential object

Generalises the notion of **function set** to internal **object**. As also **hom set** to **internal hom objects**.

Cartesian **closed** (**monoidal**) **category** strictly required, as $*$ multiplication holds **composition** requirement:

$$\circ : hom(y, z) \otimes hom(x, y) \rightarrow hom(x, z)$$

Denotation: b^a

Universal construction:

$$\begin{array}{ccccc}
 c & \xleftarrow{\quad} & c \times a & & \\
 \downarrow u & & \downarrow u \times 1^a & \searrow g & \\
 b^a & \xleftarrow{\quad} & b^a \times a & \xrightarrow{\text{eval}} & b
 \end{array}$$

, where in Category: b^a - exponential object, \times - product bifunctor, a - argument of $*$, b - result, c - candidate, $b^a \equiv (a \Rightarrow b) - *$.

$*$ b^a (also as $(a \Rightarrow b)$) represent exponentiation of cardinality of $\forall b^a$ possibilities.

2.18.3.1 *

Function object Internal hom Exponential objects Hom object Hom objects

2.18.3.2 Enriched category

Uses Hom objects (exponential objects), which do not belong into Set category. Category is no longer small, now may be called large.

$$\text{hom}(x, y) \in K.$$

Called: $*$ over K (which holds hom objects).

2.18.3.2.1 *

Enriched Large category

2.19 Mag category

The category of magmas, denoted Mag , has as objects - sets with a binary operation, and morphisms given by homomorphisms of operations (in the universal algebra sense).

2.19.1 *

MAG Magma category Category of magmas

Chapter 3

Data type

Set of values. For [type](#) to have sense the values must share some sense, [properties](#).

3.1 *

Type Types Data types

3.2 Actual type

[Data type](#) recieved by [->inferring->compiling->execution](#).

3.3 Algebraic data type

Composite [type](#) formed by combining other [types](#).

3.3.1 *

AlgDT

3.4 Cardinality

Number of possible implementations for a given [type](#) signature.

[Disjunction](#), sum - adds [cardinalities](#). [Conjunction](#), [product](#) - multiplies [cardinalities](#).

3.4.1 *

Cardinalities

3.5 Data constant

* - [constant](#) value; [nullary data constructor](#).

3.6 Data constructor

One instance that [inhabit data type](#).

3.7 data declaration

Data type declaration is the most general and versatile form to create a new **data type**. Form:

```
data [context =>] type typeVars1..n
  = con1 c1t1..i
  | ...
  | conm cmt1..q
  [deriving]
```

3.8 Dependent type

When **type** and values have **relation** between them. **Type** has restrictions for values, value of a **type variable** has a result on the **type**.

3.8.1 *

Dependent types

3.9 Gen type

Generator. **Gen type** is to generate pseudo-random values for parent **type**. Produces a **list** of values that gets infinitely cycled.

3.10 Higher-kinded data type

Any combination of * and ->

Type that take more **types** as arguments.

*Humbly really a **function***

3.10.1 *

Higher-kinded data types

3.11 newtype declaration

Create a new **type** from old **type** by attaching a new **constructor**, allowing **type class instance declaration**.

```
newtype FirstName = FirstName String
```

Data will have exactly the same representation at runtime, as the **type** that is wrapped.

```
newtype Book = Book (Int, Int)
```

```
    (,)
    /\
Integer Integer
```

3.12 Principal type

The most generic **data type** that still **typechecks**.

3.13 Product data type

Is an [algebraic data type](#) representation of a [product](#) construction. Formed by logical [conjunction](#) (AND, ' * ').

Haskell forms:

```
-- 1. As a tuple (the uncurried & most true-form)
(T1, T2)

-- 2. Curried form, data constructor that takes two types
C T1 T2

-- 3. Using record syntax. =r# <inhabitant>= would return the respective =T#=
C { r1 :: T1
  , r2 :: T2
  }
```

3.13.1 *

Product type

3.13.2 Sequence

Enumerated (ordered) [set](#). [Set](#) with a strict [order property](#).

Denotation:

```
()
( , )
( , , )
( , , ... )
```

More general mathematical denotation was not established, variants: $(n)_{n \in \mathbb{N}} \omega \rightarrow X \{i : Ord \mid i < \alpha\}$

In Haskell: [Data type](#) that stores multiple ordered values withing a single value.

Table 3.1: [Sequence constructor](#) naming by [arity](#)

Name	Arity	Denotation
Unit , empty	0	()
Singleton	1	(_)
Tuple, pair, two-tuple	2	(,)
Triple, three-tuple	3	(, ,)
Sequence	N	(, , ...)

3.13.2.1 *

Sequences Tuples Ordered pair Ordered triple

3.13.2.2 List

[Sequence](#) of one [type](#) objects.

Denotation:

```
[]
[ , ]
[ , , ]
[ , , ... ]
```

Haskell definition:

```
data [] a = [] | a : [a]
```

Definition is self-referential (self-recursive), can be seen as [anamorphism](#) (unfold) of the [] (empty list, memory cell which is container of particular type) and : (cons operation, pointer). As such - can create non-terminating data type (and computation), in other words - infinite.

3.14 Proxy type

[Proxy type](#) holds no data, but has a phantom [parameter](#) of [arbitrary type](#) (or even [kind](#)). Able to provide [type](#) information, even though has no value of that [type](#) (or it can be may too costly to create one).

```
data Proxy a = ProxyValue
```

```
let proxy1 = (ProxyValue :: Proxy Int) -- a has kind `Type`
let proxy2 = (ProxyValue :: Proxy List) -- a has kind `Type -> Type`
```

3.15 Static typing

[Type check](#) takes place at [compile level](#), so compiled program already has expectations of [types](#) it should receive.

3.16 Structural type

Mathematical [type](#). They form into [structural type system](#).

3.16.1 *

Structural

3.17 Structural type system

Strict global hierarchy and relationships of [types](#) and their [properties](#). Haskell [type](#) system is *. In most languages typing is name-based, not [structural](#).

3.17.1 *

Structural typing

3.18 Sum data type

[Algebraic data type](#) formed by logical [disjunction](#) (OR '|').

3.19 Type alias

Create new [type constructor](#), and use all [data structure](#) of the base [type](#).

3.20 Type class

Type system [construct](#) that adds a support of [ad hoc polymorphism](#).

Type class makes a nice way for defining behaviour, [properties](#) over many [types/objects](#) at once.

3.20.1 *

Type classes

3.20.2 Arbitrary type class

Type class of [QuickCheck.Arbitrary](#) (that is reexported by [QuickCheck](#)) for creating a [generator](#)/distribution of values. Useful [function](#) is [arbitrary](#) - that autogenerates values.

3.20.2.1 Arbitrary function

Depends on [type](#) and generates values of that [type](#).

3.20.3 CoArbitrary type class

Pseudogenerates a [function](#) basing on resulting [type](#).

```
coarbitrary :: CoArbitrary a => a -> Gen b -> Gen b
```

3.20.3.1 *

CoArbitrary

3.20.4 Typeable type class

Allows dynamic [type](#) checking in Haskell for a [type](#). Shift a [typechecking](#) of [type](#) from compile time to runtime. * [type](#) gets wrapped in the universal [type](#), that shifts the [type](#) checks to runtime.

Also allows:

- Get the [type](#) of something at runtime (ex. print the [type](#) of something `typeof`).
- Compare the [types](#).
- Reifying [functions](#) from [polymorphic type](#) to concrete (for [functions](#) like `:: Typeable a => a -> String`).

3.20.4.1 *

Typeable

3.20.5 Type class inheritance

Type class has a [superclass](#).

3.20.6 Derived instance

Type class instances sometimes can be automatically [derived](#) from the parent [types](#).

Type classes such as `Eq`, `Enum`, `Ord`, `Show` can have instances generated based on definition of [data type](#).

P.S.

Language options:

- DeriveAnyClass
- DeriveDataTypeable
- DeriveFoldable
- [DeriveFunctor](#)
- DeriveGeneric
- DeriveLift
- DeriveTraversable
- DerivingStrategies
- DerivingVia
- GeneralisedNewtypeDeriving
- StandaloneDeriving

3.20.6.1 *

Derived Deriving

3.21 Type constant

[Nullary type constructor](#).

3.22 Type constructor

Name of the [data type](#).

[Constructor](#) that takes [type](#) as an [argument](#) and produces new [type](#).

3.23 type declaration

Synonym for existing [type](#). Uses the same [data constructor](#).

[type](#) `FirstName = String`

Used to distinct one entities from other entities, while they have the same [type](#). Also main [type functions](#) can operate on a new [type](#).

3.24 Typed hole

* - is a `_` or `_name` in the [expression](#). On [evaluation](#) GHC would show the [derived type](#) information which should be in place of the *. That information helps to fill in the gap.

3.24.1 *

Typed holes

3.25 Type inference

Automatic [data type](#) detection for [expression](#).

3.25.1 *

Inferring Infer Infers Inferred

3.26 Type class instance

Block of implementations of [functions](#), based on unique [type class](#)->[type](#) pairing.

3.27 Type rank

Weak ordering of [types](#).

The rank of [polymorphic type](#) shows at what level of nesting forall [quantifier](#) appears. Count-in only [quantifiers](#) that appear to the left of [arrows](#).

```
f1 :: forall a b. a -> b -> a
-- =
f1 :: a -> b -> c
```

```
g1 :: forall a b. (Ord a, Eq b) => a -> b -> a
-- =
g1 :: (Ord a, Eq b) => a -> b -> a
```

f1, g1 - [rank-1 types](#). Haskell itself implicitly adds universal [quantification](#).

```
f2 :: (forall a. a->a) -> Int -> Int
g2 :: (forall a. Eq a => [a] -> a -> Bool) -> Int -> Int
```

f2, g2 - [rank-2 types](#). Quantifier is on the left side of a \rightarrow . Quantifier shows that [type](#) on the left can be overloaded.

[Type inference](#) in Rank-2 is possible, but not higher.

```
f3 :: ((forall a. a->a) -> Int) -> Bool -> Bool
```

f3 - [rank3-type](#). Has [rank-2 types](#) on the left of a \rightarrow .

```
f :: Int -> (forall a. a -> a)
g :: Int -> Ord a => a -> a
```

f, g are rank 1. [Quantifier](#) appears to the right of an [arrow](#), not to the left. These [types](#) are not [Haskell 98](#). They are supported in [RankNTypes](#).

3.27.1 *

Type ranks Rank type Rank types Rank-1 type Rank-1 types Rank-2 type Rank-2 types Rank-3 type Rank-3 types

3.28 Type variable

Refers to an unspecified parametric [polymorphic type](#) (maybe with [ad-hoc polymorphism constraints](#)) (keeps a [naturality](#) condition) in Haskell [type](#) signature.

In Haskell are always introduced with keyword `forall` explicit or implicit.

3.29 Unlifted type

[Type](#) that directly exist on the hardware. The [type abstraction](#) can be completely removed. With [unlifted types](#) Haskell [type](#) system directly manages data in the hardware.

3.29.1 *

Unlifted types

3.30 Linear type

Type system and algebra that also track the multiplicity of data. There are 3 general linear type groups:

- 0 - exists only at type level and is not allowed to be used at value level. Aka s in ST-Trick.
- 1 - data that is not duplicated
- 1< - all other data, that can be duplicated multiple times.

3.30.1 *

Linear types

3.31 NonEmpty list data type

Data.List.NonEmpty Has a Semigroup instance but can't have a Monoid instance. It never can be an empty list.

```
data NonEmpty a = a :| [a]
    deriving (Eq, Ord, Show)
```

:| - an infix data constructor that takes two (type) arguments. In other words :| returns a product type of left and right

3.32 Session type

* - allows to check that behaviour conforms to the protocol.

So far very complex, not very productive (or well-established) topic.

3.33 Binary tree

Tree where every element is a Leaf (structure stub, Nothing) or a Node (split of branches):

```
data BinaryTree a
    = Leaf
    | Node (BinaryTree a) a (BinaryTree a)
```

3.34 Bottom value

A _ non-value in the type or pattern match expression, placeholder, fits for anything.

Denoted

-

3.34.1 *

Bottom Bottom values

3.35 Bound

Haskell * [type class](#) means to have lowest value & highest value, so a [bounded](#) range of values.

3.35.1 *

Bounded

3.36 Constructor

a. [Type constructor](#)

b. [Data constructor](#)

Also see: [Constant](#)

3.36.1 *

Constructors

3.37 Context

[Type constraints](#) for [polymorphic variables](#). Written before the main [type](#) signature, denoted:

[TypeClass](#) a => ...

3.37.1 *

Contexts

3.38 Inhabit

Values that is a component of [data type set](#).

3.39 Maybe

```
data Maybe
  = Nothing
  | Just a
```

Does not represent the information why Nothing happened. For [error](#) - use [Either](#). Do not propagate *.

Handle * locally to [where](#) it is produced. Nothing does not hold useful info for debugging & short-circuits the processes. Do not expect code [type](#) being bug-free, do not return Maybe to end user since it would be impossible to debug, return something that preserves [error](#) information.

3.39.0.1 *

Nodes

3.40 Expected type

[Data type inferred](#) from the text of the code.

3.41 ADT

- a. Abstract data type
- b. Algebraic data type

3.42 Concrete type

Fully resolved, definitive, non-polymorphic type.

3.43 Type punning

When [type constructor](#) and [data constructor](#) have the same name.

Theoretically if person knows the rules - * can be solved, because in Haskell [type](#) and [data declaration](#) have different places of use.

3.44 Kind

[Kind](#) -> [Type](#) -> Data

3.44.1 *

Kinds

3.45 IO

There is only one way to "perform" an I/O action: [bind](#) it to `Main.main` of the program. For [function](#) I/O it should be in [IO monad](#) and evaluated from `Main.main`.

[Type](#) for values whose evaluations has a possibility to cause side effects or return unpredictable result. Haskell standard uses [monad](#) for constructing and transforming [IO](#) actions. [IO](#) action can be evaluated multiple times.

[IO data type](#) has unpure imperative actions inside. Haskell is [pure Lambda calculus](#), and unpure [IO](#) integrates in the Haskell purely ([type](#) system abstracts [IO](#) un purity inside [IO data type](#)).

[IO sequences effect](#) computation one after another in [order](#) of needed computation, or occurrence:

```
twoBinds :: IO ()
twoBinds =
  putStrLn "First:" >>
  getLine >>=
  \a ->
  putStrLn "Second:" >>
  getLine >>=
  \b ->
  putStrLn ("\nFirst: "
    ++ a ++ ".\nSecond "
    ++ b ++ ".")
main = twoBinds
```

Sequencing is achieved by compilation of effects performing only while they receive the sugared-in & passed around the `RealWorld` fake [type](#) value, that value in the every computation gets the new "value" and then passed to the next requested computation. But special thing is about this [parameter](#), this `RealWorld` [type](#)

value passed, but never looked at. GHC realizes, since value is never used, - it means value and `type` can be equated to `()` and moreover reduced from the code, and sequencing stays.

Chapter 4

Expression

Finite combination of symbols that is well-formed according to [context-free grammar](#).

Generally meaningless. Meaning gets [derived](#) from an * & [context](#) (and/or content words) by congruency with knowledge & experience.

4.1 *

Expressions

4.2 Closed-form expression

* - mathematical [expression](#) that can be evaluated in a finite number of operations.

May contain:

- constants
- [variables](#)
- operations (e.g., $+$ $-$ \times \div)
- [functions](#) (e.g., nth root, exponent, logarithm, trigonometric [functions](#), and [inverse](#) hyperbolic [functions](#)), but usually no limit.

4.3 RHS

Right-hand side of the [expression](#).

4.4 LHS

Left-hand side of the [expression](#).

4.5 Redex

[Reducible expression](#).

4.6 Concatenate

Link together [sequences](#), [expressions](#).

4.7 Alpha equivalence

[Equivalence](#) of a processes in [expressions](#). If [expressions](#) have according [parameters](#) different, but the internal processes are literally the same [process](#).

4.8 Ground expression

[Expression](#) that does not contain any free [variables](#).

4.8.1 *

Ground formula

4.9 Variable

A name for [expression](#).

+===

There fequently can be heard: one of most notable Haskell [properties](#) is Haskell has immutable "variables" (and term here used in the sence that imperative programmers frequently use). Logically we see [statement](#) is contradictory with itself: "[variables](#)" - something that has change as a defining property - are not changing; it is a nonsencical [statement](#). Please, read the saying as: Haskell has immutable values, due to following the value [semantics](#): see "Value". And Haskell [expressions](#) are [functions](#) (that are [referentially transparent](#) - meaning itself immutable) - and they are also values (hense term "functional programming" means - [functions](#) are [first-class](#) values). Since values [bind](#) to [variables](#) - people are wrongly mix-up terms and say their names (according "*) are immutable.

As you see in the code - Haskell [variables](#) (same names) hold different values at different times. [Variables](#) are reused, meaning "names are reused" - binded to different values on [scope](#) changes. But all values that Haskell holds - are, by the design of the language, are treated immutable, any transformations Haskell resolves by creating new values, and frees the space by freeing-up from no longer needed values.

4.9.1 *

Variables

4.10 Phrase

[Composable expression](#).

Chapter 5

Function

Full dependency of one quantity from another quantity.

Denotation: $y = f(x)$ $f : X \rightarrow Y$, where X is domain, Y is codomain.

Directionality and property of invariability emerge from one another.

-- domain func codomain
* -> *

$$y(x) = (zx^2 + bx + 3 \mid b = 5) \wedge \wedge \wedge \wedge \wedge$$

\Var \Constant

\Bound variable

\Free variable

\Parameter

\Name of the function

Lambda abstraction is a function. Function is a mathematical operation.

Function = Total function = Pure function. Function theoretically can be to memoized.

Also see: Partial function Inverse function - often partially exists (partial function).

5.1 *

Functions Bound variable

5.2 Arity

Number of parameters of the function.

- nullary - $f()$
- unary - $f(x)$
- binary - $f(x,y)$
- ternary - $f(x,y,z)$
- n-ary - $f(x,y,z,\dots)$

5.3 Bijection

Function is a complete one-to-one pairing of elements of **domain** and **codomain** (**image**). It means **function** both **surjective** (so **image** == **codomain**) and **injective** (every **domain** element has unique correspondence to the **image** element).

For **bijection inverse** always exists.

Bijection operation holds the **equivalence** of **domain** and **codomain**.

Denotation:

\boxtimes

$\succ \rightarrow \gg$

$f : X \boxtimes Y$

LaTeX needed to combine symbols: $f : X \succ \rightarrow Y$

Corresponds to **isomorphism**.

5.3.1 *

Bijection Bijection function

5.4 Combinator

Function without free **variables**. **Higher-order function** that uses only **function application** and other combinators.

```
\a -> a
\ a b -> a b
\f g x -> f (g x)
\f g x y -> f (g x y)
```

Not combinators:

```
\ xs -> sum xs
```

Informal broad meaning: referring to the style of organizing libraries centered around the idea of combining things.

5.4.1 Ψ -combinator

Transforms two of the same **type**, **applying** same mediate transformation, and then transforming those into the result.

```
import Data.Function (on)
on :: (b -> b -> c) -> (a -> b) -> a -> a -> c

a--\b
   * ---c
a--/b
```

5.4.1.1 *

Psi-combinator On-combinator

5.5 Function application

* - **bind** the **argument** to the **parameter** of a **function**, and do a **beta-reduction**.

5.5.1 *

Apply Applied Applying Application

5.6 Function body

Expression that haracterizes the process.

5.7 Function composition

$(.) :: (b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow c$

$a \rightarrow (a \rightarrow b) \rightarrow (b \rightarrow c) \rightarrow c$

In Haskell inline composition requires:

$h.g.f \$ i$

5.7.1 *

Composition Compose Composed

5.8 Function head

Is a part with name of the function and it's paramenters. AKA: $f(x)$

5.9 Function range

The range of a function refers to either the codomain or the image of the function, depending upon usage. Modern usage almost always uses range to mean image. So, see Function image.

5.10 Higher-order function

Function that has arity > 1.

++++

HOF is:

- function that accepts function as a parameter
- function that has more then one parameter.

Application of an argument to * produces a function that has arity - 1.

5.10.1 *

HOF

5.10.2 Fold

Catamorphism of a structure to a lower type of structure. Often to a single value.

* is a higher-order function that takes a function which operates with both main structure and accumulator structure, * applies units of data structure to a function wich works with accumulator. Upoun traversing the whole structure - the accumulator is returned.

5.11 Injection

Function one-to-one injects from **domain** into **codomain**.

Keeps distinct pairing of elements of **domain** and **image**. Every element in **image** corresponds to one element in **domain**.

$$\forall a, b \in X, f(a) = f(b) \Rightarrow a = b$$

$$\exists(\text{inverse function}) \mid \forall(\text{injective function})$$

Denotation:

\boxtimes

$\succ \rightarrow$

$f : X \boxtimes Y$

$f : X \succ \rightarrow Y$

Corresponds to **Monomorphism**.

5.11.1 *

Injective Injective function Injectivity

5.12 Partial function

One that does not cover all **domain**. **Unsafe** and causes trouble.

5.13 Purity

* means properly abstracted.

If the contrary - **abstraction** is unpure.

Also see: **pure function**.

5.13.1 *

Pure

5.14 Pure function

Function that is **pure** \equiv **referentially transparent function**.

5.15 Sectioning

Writing **function** in a parentheses. Allows to pass around **partially applied functions**.

5.16 Surjection

Function uses **codomain** fully.

$$\forall y \in Y, \exists x \in X$$

Denotation: $f : X \twoheadrightarrow Y$

Corresponds to **Epimorphism**.

5.16.1 *

Surjective Surjective function

5.17 Unsafe function

Function that does not cover at least one edge case.

5.17.1 *

Unsafe

5.18 Variadic

* - having variable arity (often up to indefinite).

5.19 Domain

Source set of a function. X in $X \rightarrow Y$.

5.20 Codomain

Y in $X \rightarrow Y$. Codomain - target set of a function.

5.21 Open formula

Logical function that has arity and produces proposition.

5.22 Recursion

Repeated function application when sometimes the same function gets called.

Allows computations that may require indefinite amount of work.

5.22.1 *

Recursive

5.22.2 Base case

A part of a recursive function that trivially produces result.

5.22.3 Tail recursion

Tail calls are recursive invocations of itself.

5.22.4 Polymorphic recursion

Type of the parameter changes in recursive invocations of function.

Is always a higher-ranked type.

5.22.4.1 *

Milner–Mycroft typability Milner–Mycroft calculus

5.23 Free variable

Variable in the function that is not **bound** by the head. Until there are * - **function** stays **partially applied**.

5.24 Closure

$f(x) = f^{X \rightarrow X} \mid \forall x \in X, X$ is **closed** under f , it is a trivial **case** when **operation** is legitimate for all values of the **domain**.

Operation on members of the **domain** always produces a members of the **domain**. The **domain** is **closed** under the **operation**.

In the **case** when there is a **domain** values for which **operation** is not legitimate/not exists:

$f(x) = f^{V \rightarrow X} \mid V \in X, \forall x \in V, X$ is **closed** under f .

5.24.1 *

Closed

5.25 Parameter

para subsidiary metron measure

Named variable of a **function**.

Argument is a supplied value to a **function parameter**.

Parameter (**formal parameter**) is an **irrefutable** pattern, and implemeted that way in Haskell.

5.25.1 *

Parameters Formal parameter Formal parameters

5.26 Partial application

Part of **function parameters applied**.

5.26.1 *

Partially applied

5.27 Well-formed formula

Expression, logical **function** that is/can produce a **proposition**.

5.27.1 *

Well formed formula WFF wff WFFS wffs

Chapter 6

Homotopy

homotopy homotopy same

One can be "continuously deformed" into the other.

For example - [functions](#), [functors](#). [Natural transformation](#) is a [homotopy](#) of [functors](#).

6.1 *

Homotopies Homotopic

Chapter 7

Lambda calculus

Universal model of computation. Which means * can implement any [Turing machine](#). Based on [function abstraction](#) and [application](#) by substituting [variables](#) and [binding](#) values.

* has [lambda terms](#):

- [variable](#) (x)
- [application](#) ($((ts))$)
- [abstraction](#) ([lambda function](#)) ($((\lambda x.t))$)

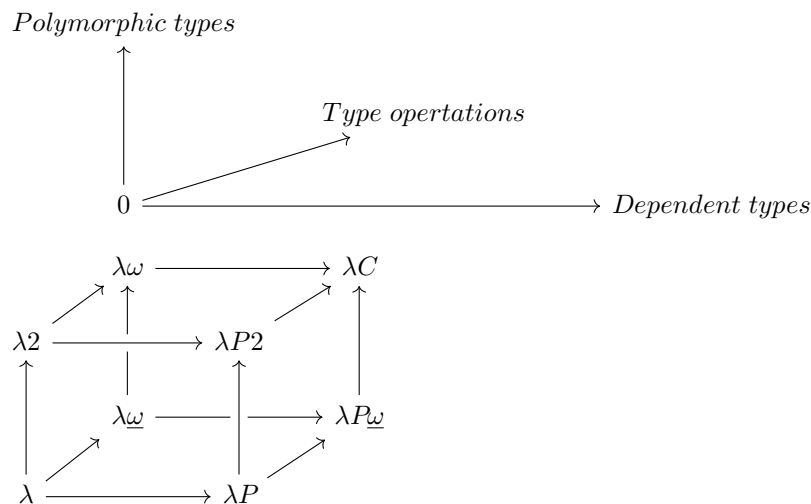
7.1 *

Lambda term Lambda terms

7.2 Lambda cube

[λ-cube](#) shows the 3 dimention of generalizations from simply typed [Lambda calculus](#) to [Calculus of constructions](#).

+===



Each dimension of the cube corresponds to extensions (a new [type](#) of [relation](#) of [objects](#) depending on [objects](#)):

Table 7.1: Three degrees of [type](#) systems generalizations

Denotation	Name	Programming	New type of relations
2	Polymorphic types	First-class polymorphism of types	Terms depending on types
ω	Type operation	Type class, type families	Types depending on types
P	Dependent types	Higher-rank polymorphism , dependent types	Types depending on terms

Table 7.2: [λ-cube](#): Names of the [type](#) systems

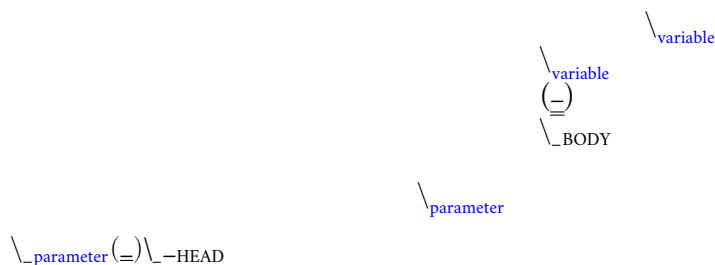
Denotation	Logical system
$\lambda \rightarrow$	(First Order) Propositional Calculus
$\lambda 2$	Second Order Propositional Caculus
$\lambda \omega$	Weakly Higher Order Propositional Calculus
$\lambda \underline{\omega}$	Higher Order Propositional Calculus
λP	(First Order) Predicate Logic
$\lambda P 2$	Second Order Predicate Calculus
$\lambda P \omega$	Weak Higher Order Predicate Calculus
λC	Calculus of Constructions

7.2.1 *

[λ-cube](#) [λ-cube](#)

7.3 Lambda function

[Function](#) of [Lambda calculus](#). $\lambda xy.x^2 + y^3 \wedge \wedge \wedge$



7.3.1 *

[Lambda abstraction](#)

7.3.2 Anonymous lambda function

[Lambda function](#) that is not binded to any name.

7.3.2.1 *

[Anonymous lambda function](#)

7.3.3 Uncurry

Replace sequenced [lambda functions](#) into single [function](#) taking [sequence/product](#) of values as [argument](#).

7.4 β -reduction

Equation of a [parameter](#) to a [bound variable](#), then reducing [parameter](#) from the head.

7.4.1 *

β reduction Beta-reduction Beta reduction

7.4.2 β -normal form

No [beta reduction](#) is possible.

7.4.2.1 *

β normal form Beta normal form Beta-normal form

7.5 Calculus of constructions

Extends the [Curry](#)–Howard correspondence to the proofs in the full intuitionistic [predicate](#) calculus (includes proofs of [quantified statements](#)). [Type](#) theory, typed programming language, and constructivism (philosophy) foundation for mathematics. Directly relates to Coq programming language.

7.5.1 *

«CoC»

7.6 Curry–Howard correspondence

[Equivalence](#) of {[First-order logic](#), computer programming, [Category](#) theory}. They represent each-other, possible in one - possible in the other, so all the definitions and theorems have analogues in other two.

Gives a ground to the [equivalence](#) of computer programs and mathematical proofs.

Lambek added analogue to Cartesian [closed category](#), which can be used to model logic and [type](#) theory.

Table 7.3: Table of basic correspondence

Logic	Type	Category
True	() (any inhabited type)	Terminal
False	Void	Initial
$a \wedge b$	(a, b)	$a \times b$
$a \vee b$	$(a \mid b)$	$a \mid b$
$a \Rightarrow b$	$a \rightarrow b$	b^a

[Algebra](#) correspondence to [types](#):

$$a^b + c \sim (b \mid c \rightarrow a) \quad a^b \times a^c \sim (b \rightarrow a, c \rightarrow a)$$

$$a^{b^c} \sim (c \rightarrow b \rightarrow a) \quad a^{b \times c} \sim ((b, c) \rightarrow a)$$

7.6.1 *

Curry–Howard isomorphism Curry–Howard–Lambek

7.7 Currying

Translating the [evaluation](#) of a multiple [argument function](#) (or a [tuple](#) of arguments) into evaluating a [sequence](#) of [functions](#), each with a single [argument](#).

7.7.1 *

Curry

7.8 Hindley–Milner type system

Classical [type](#) system for the [Lambda calculus](#) with [Parametric polymorphism](#) and [Type inference](#). [Types](#) marked as [polymorphic variables](#), which enables [type inference](#) over the code.

7.8.1 *

Hindley-Milner Damas-Milner Damas-Hindley-Milner

7.9 Reduction

Take out something from a [structure](#), make simpler.

See [Beta reduction](#)

7.9.1 *

Reducible

7.10 β - η normal form

All [\$\beta\$ -reduction](#) and [\$\eta\$ -abstraction](#) are done in the [expression](#).

7.10.1 *

beta-eta normal form beta eta normal form

7.11 η -abstraction

$(\lambda x.Mx) \xleftarrow{\eta} M$

$\backslash x \rightarrow g . f \$ x$
 $\backslash x \rightarrow g . f \quad \text{--eta-abstraction}$

7.11.1 *

η -reduction η -conversion η abstraction η reduction η conversion eta-abstraction eta-reduction eta-conversion eta abstraction eta reduction eta conversion

7.12 Lambda expression

See [Lambda calculus](#) ([Lambda terms](#)) and [Expression](#). In majority cases meaning some [Lambda function](#).

Chapter 8

Operation

Calculation into output value. Can have [zero](#) & more inputs.

8.1 Constant

[Nullary operation](#).

Also see: [Type constant](#).

8.2 Binary operation

$\forall(a, b) \in S, \exists P(a, b) = f(a, b) : S \times S \rightarrow S$

8.2.1 *

Binary operations

8.3 Operator

Denotation symbol/name for the [operation](#).

8.3.1 Shift operator

[Shift operator](#) defined by Lagrange through [Differential operator](#). $T^t = e^{t \frac{d}{dx}}$

8.3.1.1 *

Shift

8.3.2 Differential operator

Denotation. $\frac{d}{dx}$, D , D_x , ∂_x . Last one is partial.

$e^{t \frac{d}{dx}}$ - [Shift operator](#).

8.3.2.1 *

Differential

8.4 Infix

Form of writing of [operator](#) or [function](#) in-between [variables](#) for [application](#).

For priorities see [Fixity](#).

8.5 Fixity

Declares the presedence of action of a [function/operator](#).

Function [application](#) has presedence higher then all [infix](#) operators/[functions](#) (virtually giving it a [priority](#) 10).

Table 8.1: Haskell operators [priority](#) and [fixity](#) association

P	L	Non	R
10			F.A.
9	!!		.
8			^ ^ ^ **
7	*/ div		
6	+-		
5			: , ++
4		<comparison> elem	
3			&&
2			OR
1	» »=		
0			\$ \$! seq

Any [operator](#) lacking a [fixity declaration](#) is assumed to be [infixl](#) 9.

8.5.1 *

Infixl Infixr Priority Precedence

8.6 Zero

* is the value with which [operation](#) always yields [Zero](#) value. $zero, n \in C : \forall n, zero * n = zero$

* is distinct from [Identity](#) value.

8.7 Bind

Establishing equality between two [objects](#).

Most often:

- equating [variable](#) to a value.
- equating [parameter](#) of a [function](#) to an [argument](#) ([variable](#)/value/[function](#)). This term often is equated to [applying argument](#) to a [function](#), which includes [β-reduction](#).

8.7.1 *

Binds Binding Bindings

8.8 Declaration

[Binding](#) name to [expression](#).

8.9 Dispatch

Sort-out & send.

8.10 Evaluation

For FP see [Bind](#).

Chapter 9

Permutation

Bijjective function from domain to itself.

Domain & permutation functions & function composition form a group.

Chapter 10

Point-free

Paradigm [where function](#) only describes the [morphism](#) itself.

[Process](#) of converting [function](#) to [point-free](#). If brackets `()` can be changed to `$` then `$` equal to [composition](#):

```
\ x -> g (f x)
\ x -> g $ f x
\ x -> g . f $ x
\ x -> g . f      --eta-abstraction
```

```
\ x1 x2 -> g (f x1 x2)
\ x1 x2 -> g $ f x1 x2
\ x1 x2 -> g . f x1 $ x2
\ x1      -> g . f x1
```

10.1 *

Pointfree Tacit Tacit programming

10.2 Blackbird

```
(.).(.) :: (b -> c) -> (a1 -> a2 -> b) -> a1 -> a2 -> c
```

[Composition of compositions](#) `(.).(.)`. Allows to [compose](#)-in a [binary function](#) `f1(c) (.).(.) f2(a,b)`.

```
\ f g x y -> f (g x y)
```

10.2.1 *

`.) . (.) . (.)` Composition of compositions

10.3 Swing

```
swing :: ((a -> b) -> b) -> c -> d -> c -> a -> d
swing = flip . (. flip id)
swing f = flip (f . runCont . return)
swing f c a = f ($ a) c
```

10.4 Squish

`f >>= a . b . c =<< g`

Chapter 11

Polymorphism

πολύς *polús* many

At once several forms.

In Haskell - [abstract](#) over [data types](#).

* [types](#):

11.1 *

Polymorphic

11.2 Levity polymorphism

Extending [polymorphism](#) to work with unlifted and lifted [types](#).

11.3 Parametric polymorphism

[Abstracting](#) over [data types](#) by [parameter](#).

In most languages named as 'Generics' (generic programming).

[Types](#):

11.3.1 Rank-1 polymorphism

[Parametric polymorphism](#) by [type variables](#) of [rank-1 types](#).

11.3.1.1 *

Prenex Prenex polymorphism

11.3.2 Let-bound polymorphism

It is [property](#) chosen for Haskell [type](#) system. Haskell is based on [Hindley-Milner type](#) system, it is [let-bound](#). To have strict [type inference](#) with * - if [let](#) and [where](#) declarations are [polymorphic](#) - λ declarations - should be not.

See: [Good](#): In Haskell parameters bound by lambda declaration instantiate to only one concrete type.

11.3.3 Constrained polymorphism

Constrained [Parametric polymorphism](#).

11.3.3.1 Ad hoc polymorphism

Artificial [constrained polymorphism](#) dependent on incoming [data type](#). It is [interface dispatch](#) mechanism of [data types](#). Achieved by creating a [type class instance functions](#).

Commonly known as overloading.

11.3.3.1.0.1 *

Ad-hoc polymorphism Ad hoc polymorphic Ad-hoc polymorphic Constraint Constraints

11.3.4 Impredicative polymorphism

* allows [type](#) λ entities with [polymorphic types](#) that can contain [type](#) λ itself. $T = \forall X. X \rightarrow X : T \in X \models T \in T$

The most powerful form of [parametric polymorphism](#). See: [Impredicative](#).

This approach has Girard's paradox ([type systems](#) [Russell's paradox](#)).

11.3.4.1 *

First-class polymorphism

11.3.5 Higher-rank polymorphism

Means that [polymorphic types](#) can appear within other [types](#) ([types of function](#)). There is a cases [where higher-rank polymorphism](#) than the a Ad hoc - is needed. For example [where ad hoc polymorphism](#) is used in [constraints](#) of several different implementations of [functions](#), and you want to build a [function](#) on top - and use the [abstract interface](#) over these [functions](#).

```
-- ad-hoc polymorphism
f1 :: forall a. MyType Class a => a -> String == f1 :: MyType Class a =>
  a -> String
f1 = -- ...

-- higher-rank polymorphism
f2 :: Int -> (forall a. MyType Class a => a -> String) -> Int
f2 = -- ...
```

By moving forall inside the [function](#) - we can achieve [higher-rank polymorphism](#).

From: <https://news.ycombinator.com/item?id=8130861>

Higher-rank polymorphism is formalized using System F, and there are a few implementations of (incomplete, but decidable) type inference for it - see e.g. Daan Leijen's research page [1] about it, or my experimental implementation [2] of one of his papers. Higher-rank types also have some limited support in OCaml and Haskell.

Useful example also a [ST-Trick monad](#).

11.3.5.1 *

Rank-n polymorphism

11.4 Subtype polymorphism

Allows to declare usage of a [Type](#) and all of its Subtypes. T - [Type](#) S - Subtype of [Type](#) $S <: T$ - subtype of $S <: T = S \leq T$

Subtyping is: If it can be done to T , and there is subtype S - then it also can be done to S . $S <: T : f^{T \rightarrow X} \Rightarrow f^{S \rightarrow X}$

11.5 Row polymorphism

Is a lot like [Subtype polymorphism](#), but aligns itself on allowance (with $| r$) of subtypes and [types](#) with requested [properties](#).

```
printX :: { x :: Int | r } -> String
printX rec = show rec.x

printY :: { y :: Int | r } -> String
printY rec = show rec.y

-- type is inferred as `{x :: Int, y :: Int | r } -> String`
printBoth rec = printX rec ++ printY rec
```

11.6 Kind polymorphism

Achieved using a phantom [type argument](#) in the [data type declaration](#).

```
;;          * -> *
data Proxy a = ProxyValue
```

Then, by default the [data type](#) can be inhabited and fully work being partially defined. But multiple instances of [kind polymorphic type](#) can be distinguished by their particular [type](#).

Example is the [Proxy type](#):

```
data Proxy a = ProxyValue

let proxy1 = (ProxyValue :: Proxy Int) -- * :: Proxy Int
let proxy2 = (ProxyValue :: Proxy a)   -- * -> * :: Proxy a
```

11.7 Linearity polymorphism

Leverages [linear types](#). For example - if [fold](#) over a dynamic array:

- In basic Haskell - array would be copied at every step.
- Use low-level [unsafe functions](#).
- With [Linear type function](#) we guarantee that the array would be used only at one place at a time.

So, if we use a [function](#) $(* -o * -o -o *)$ in [foldr](#) - the [fold](#) will use the initial value only once.

Chapter 12

Compositionality

Complex [expression](#) is determined by the constituent [expressions](#) and the rules used to combine them.

If the meaning fully obtainable from the parts and [composition](#) - it is full, [pure compositionality](#).

If there exists [composed idiomatic expression](#) - it is unfull, unpure [compositionality](#), because meaning leaks-in from the sources that are not in the [composition](#).

12.1 *

Principle of compositionality Composition Compositional

Chapter 13

Referential transparency

Given the same input return the same output. So: * [expression](#) can be replaced with its corresponding resulting value without change for program's behavior. * [functions](#) are [pure](#).

13.1 *

Referentially transparent

Chapter 14

Semantics

Philosophical study of meaning. Meaning of symbols, words.

14.1 Operational semantics

Constructing proofs from [axiomatic semantics](#), verifying procedures and their [properties](#).

Good to solve in-point localized tasks.

[Process](#) of working with [abstractions](#).

14.1.1 Argument

arguere make clearmake known, to prove, to shine

* - evidence, proof, [statement](#) that results systematic changes.

14.1.1.1 Argument of a function

A value binded to the [function parameter](#). Value/topic that the fuction would [process](#)/deal with.

Also see Argument.

14.1.1.1.1 *

Function argument

14.1.1.2 First-class

Means *it*:

- Can be used as value.
- Passed as an [argument](#).

From 1&2 -> *it* can include itself.

14.1.2 Relation

[Relationship](#) between two [objects](#). By default it is not directed and not limited. In [Set theory](#): some subset of a [Cartesian product](#) between [sets](#) of [objects](#).

14.1.2.1 *

Relations Relationship

14.1.3 Context-free grammar

A grammar (set of production rules) that describe all possible properly **composed expressions** in a formal language.

Term is invented by Noam Chomsky.

14.1.3.1 *

CFG

14.1.4 Constructive proof

Method that demonstrates **object** existence by showing the **process** of its creation.

14.2 Denotational semantics

Construction of **objects**, that describe/tag the meanings. In Haskell often **abstractions** that are ment (denotations), implemented directly in the code, sometimes exist over the code - allowing to reason and implement.

* are **composable**.

Good to achive more broad approach/meaning.

Also see **Abstraction**.

14.2.1 Abstraction

abs away from, off (in absentia)

tractus draw, haul, drag

Purified generalization.

Forgetting the details (**axiomatic semantics**). Simplified approach. Out of sight - out of mind.

* creates a new semantic level in which one can be absolutely precise (**operational semantics**).

It is a great did to name an **abstraction** (**denotational semantics**).

The ideal **abstractions** are:

- integrative (global):
 - **nothing**, **void**, emptiness - "none", **initial object**
 - everything - "all", "existence", **terminal object**
- **differential** (**local**):
 - point - "this", "is", "one", stasis
 - chaos - "any", "of", "many", **process**

They are ideal - because they are the **basis**, the beginning. Because you can not express any other obstrac-tions without these.

+===

This is personal idea & the thought of autor of the book regarding basic [abstractions](#) particularly. Other definitions in the book basing on this are the proof that [statement](#) has some ground truth in it. There is ongoing philosophical discussion on the topics like these.

14.2.1.1 *

Abstractions Abstracting Abstract

14.2.1.2 Leaky abstraction

[Abstraction](#) that leaks details that it is supposed to [abstract](#) away.

14.2.1.2.1 *

Leaky abstractions

14.2.1.3 Object

Absolute [abstraction](#).

Point that additionally can have [properties](#).

Often abstracts something, that is why it exposes external [properties](#) on [abstracting](#) something, for example some [structure](#), maybe mathematical. In this book [objects](#) represent [algebraic structures](#), as we are talking about Haskell and [Category](#) theory.

[Objects](#) without [process](#) are in [constant](#) state.

14.2.1.3.1 *

Structure Structures Objects

14.2.1.3.2 Arrow

Second level of absolute [abstraction](#).

[Arrow](#).

Can have target, can have source. Both often are [objects](#).

Often abstracts [process](#).

Can have [properties](#).

Also alias in [Category](#) Theory for "[morphism](#)", thou theory imposes [properties](#).

14.2.1.3.2.1 *

Arrows Process

14.2.1.3.3 Terminal object

One that recieves unique [arrow](#) from every [object](#).

$$\exists! : x \rightarrow 1 \mid \exists 1 \in \mathcal{C}, \forall x \in \mathcal{C}$$

* is an empty [sequence](#) () in Haskell.

Called a [unit](#), so recieves *terminal* or [unit arrow](#).

Dual of [initial object](#).

Denotation:

Category theory 1

Haskell

()

14.2.1.3.4 Initial object

One that emits unique **arrow** into every **object**.

$$\exists ! : \emptyset \rightarrow x \mid \exists \emptyset \in \mathcal{C}, \forall x \in \mathcal{C}$$

If **initial object** is Void (most frequently) - emitted **arrows** called absurd, because they can not be called.

Dual of **terminal object**.

Denotation:

Category theory: \emptyset

Haskell:

Void

14.2.1.3.5 Value

What **object** abstracts. Without any **object** external **structure** (aka **identity** in **Category Theory**). So * is immutable. Such heresy is called "Value **semantics**" and leads such things as **referential transparency**, functional programming and Haskell.

(Except, when you hack Haskell with explicit low-level functions, and start to directly mute values - then you are on your own, Haskell paradigm does not expect that.)

14.2.1.3.5.1 *

Value **semantics** Values

14.2.1.3.6 Tensor

Object existing out of planes, thus it can translate **objects** from one plane into another. * can be tried to be described with knowledge existing inside planes (from projection on the plane), but representation would always be partial.

Tensor of rank 1 is a vector.

Translations with **tensor** can be seen as **functors**.

14.2.1.3.6.1 *

Tensors Tensorial

14.2.2 Ambigram

ambi both

γράμμα *grámma* written character

Object that from different points of view has the same meaning.

While this word has two contradictory diametrically opposite usages, one was chosen (more frequent).

But it has... Both.

TODO: For merit of differentiating the meaning about different meaning referring to *Tensor* as *object* with many meanings.

14.2.3 Binary

Two of something.

14.2.4 Arbitrary

arbitrarius uncertain

Random, any one of.

Used as: Any one with *this* set of properties. (constraints, type, etc.).

When there is a talk about any arbitrary value - in fact it is a talk about the generalization of computations over the set of properties.

14.2.5 Refutable

One that has an option to fail.

14.2.6 Irrefutable

One that can not fail.

14.2.7 Superclass

Broader parent class.

14.2.8 Unit

Represents existence. Denoted as empty sequence.

()

Type () holds only self-representation constructor (), & constructor holds nothing.

Haskell code always should receive something back, hence nothing, emptiness, void can not be theoretically addressed, practically constructed or received - unit in Haskell also has a role of a stub in place of emptiness, like in IO ().

14.2.9 Nullary

Takes no entries (for example has the arity of zero). Has the trivial domain.

14.2.10 Syntax tree

Tree of syntactic elements (each node denotes construct occurring in the language/source code) that represent the full particular composed expression/implementation.

14.2.10.1 Abstract syntax tree

"Abstract" since does not represent every detail of the syntax (ex. parentheses), but rather concentrates on structure and content.

Widely used in compilers to check the code structure for accuracy and coherence.

14.2.10.1.1 *

AST

14.2.10.2 Concrete syntax tree

An ordered, rooted **syntax tree** that represents the syntactic **structure** of a string according to some **context-free grammar**.

"Concrete" since (in contrast to "abstract") - concretely reflects the syntax of the input language.

14.2.10.2.1 *

Parse tree Derivation tree

14.2.11 Stream

* an infinite **sequence** that forgets previous **objects**, and remembers only currently relevant **objects**.

$E \mid X \rightarrow (X \times A + 1)$, the **set** (or **object**) of streams on A (final **coalgebra** A_* of E).

cycle is one of **stream functions**.

a = (cycle [Nothing, Nothing, Just "Fizz"])

b = (cycle [Nothing, Nothing, Nothing, Nothing, Just "Buzz"])

Can be:

- indexed, timeless, with current **object**
- timed:

* [(timescale, event)] * [(realtime, event)]

Has amalgamation with Functional Reactive Programming.

14.2.12 Linear

Values consumed once or not used.

x^2 consumes/uses x two times ($x*x$).

14.2.12.1 *

Linearity

14.2.13 Predicative

Non-self-referencing definition.

+===

Antonym - *Impredicative*.

14.2.14 Quantifier

Specifies the quantity of specimens.

Two most common **quantifiers** \forall (**Forall**) and \exists (**Exists**). $\exists!$ - one and only one (exists only unique).

Turns **predicate** into **statement**.

14.2.14.1 *

Quantification Quantifiers Quantified

14.2.14.2 Forall quantifier

In Haskell [type variables](#) are always introduced with it, explicitly or implicitly.

`forall` means that it will unify/fixed to any [type](#) that consumer may choose.

Permits to not [infer](#) the [type](#), but to use any that fits. The variant depends on the [LANGUAGE option](#) used:

- [ScopedTypeVariables](#)
- [RankNTypes](#)
- [ExistentialQuantification](#)

14.2.14.2.1 *

Forall

14.2.15 Idiom

* - something having a meaning that can not be [derived](#) from the conjoined meanings of * constituents. Meaning can be special for language speakers or human with particular knowledge.

* can also mean [applicative functor](#), people better stop making [idiom](#) from the term "[idiom](#)".

14.2.15.1 *

Idioms Idiomatic

14.2.16 Impredicative

Self-referencing definition.

+===

Antonym - [Predicative](#).

14.3 Axiomatic semantics

Empirical [process](#) of studying something complex by finding and analyzing true [statements](#) about it.

Good for examining interconnections.

14.3.1 Property

Something has a [property](#) in the real world, and [property](#) always yealds an axiom (law) for something.

Meaningful [abstraction](#) denotation always defines through [properties](#) (axioms for that definition).

[Abstraction](#) forms nicely around the boundaries [where](#) the particular [properties](#) spread. [Properties](#) inside [abstraction](#) may have emergence [effect](#) (combination of [properties](#) result into bigger [property](#)), so in that way [abstracting](#) them simplifies outside picture, as [abstraction](#) hides plethora of internal [properties](#) and exposes only emergent [properties](#).

In Haskell under [property/law](#) most often [properties](#) of [algebraic structures](#).

There [property testing](#) wich does what it says.

14.3.1.1 *

Properties

14.3.1.2 Associativity

Joined with a common purpose.

$$P(a, P(b, c)) \equiv P(P(a, b), c) \mid \forall(a, b, c) \in S,$$

* - the **order** (**priority**) of executions of actions can be **arbitrary**, as long as in the end the **chain** is the same - they would produce the same result. Any **priority** of execution of the parts of the **operation chain** would produce the same result, as the **chain** of operations is in fact flat.

Property that determines how operators of the same **precedence** are grouped, (in computer science also in the absence of parentheses).

Etymology: Latin *associatus* past participle of *associare* "join with", from assimilated form of *ad* "to" + *sociare* "unite with", from *socius* "companion, ally" from PIE **sokw-yo-*, suffixed form of root **sekw-* "to follow".

In Haskell * has influence on parsing when compounds have same **fixity**.

14.3.1.2.1 *

Associative Associative property Associativity property

14.3.1.2.2 Left-associativity

* - the operations can be done in **groups** the direction of actions can be from the beginning towards the end.

Example: In lambda **expressions** same level parts follow grouping from left to right. $(\lambda x.x)(\lambda y.y)z \equiv ((\lambda x.x)(\lambda y.y))z$

14.3.1.2.2.1 *

Left-associative

14.3.1.2.3 Right-associativity

* - the operations **groups** the actions from the end towards the beginning.

Example:

$$[1, 2, 3] = 1 : 2 : 3 : [] = 1 : (2 : (3 : []))$$

14.3.1.2.3.1 *

Right-associative

14.3.1.2.4 Non-associativity

Operations can't be chained.

Often is the **case** when the output **type** is incompatible with the input **type**.

14.3.1.2.4.1 *

Non-associative

14.3.1.3 Basis

$\beta\alpha\sigma\iota\varsigma$ - stepping

The initial point, unreducible axioms and terms that spawn a theory. AKA see **Category** theory, or Euclidian geometry **basis**.

14.3.1.3.1 Contravariant

The **property** of **basis**, in which if new **basis** is a **linear** combination of the prior **basis**, and the change of **basis** **inverse**-proportional for the description of a **Tensors** in this basis.

Denotation: Components for **contravariant basis** denoted in the upper indices: $V^i = x$

The **inverse** of a **covariant** transformation is a **contravariant** transformation. Good example of contravariant is: When a vector should stay absolute invariant even when **basis** changes, that is to say it represents the same geometrical or physical **object** having the same magnitude and direction as before - then those absolute invariant components relate to **basis** under the **contravariant** rule.

14.3.1.3.1.1 *

Contravariant cofunctor Contravariant functor - More inline term is **Contravariant cofunctor**

14.3.1.3.2 Covariant

The **property** of **basis**, in which if new **basis** is a **linear** combination of the prior **basis**, and the change of **basis** proportional for a descriptions of **tensors** in basis.

Denotation: Components for **covariant basis** denoted in the upper indices: $V_i = x$

14.3.1.3.2.1 *

Covariant functor Covariant cofunctor

14.3.1.4 Commutativity

$$\forall (a, b) \in S : P(a, b) \equiv P(b, a)$$

All processes that are independent from one-another, but on manifestation of their results - their combination result into something (create circumstances for something) - are **commutative**.

14.3.1.4.1 *

Commutative Commutative property

14.3.1.5 Idempotence

First **application** gives a result. Then same **operation** can be **applied** multiple times without changing the result. Example: Start and Stop buttons on machines.

14.3.1.5.1 *

Idempotent Idempotency

14.3.1.6 Distributivity

In **algebra**:

- **set** S
- two **binary** operators $+$ \times
- $x \times (y + z) = (x \times y) + (x \times z)$ - \times is left-**distributive** over $+$
- $(y + z) \times x = (y \times x) + (z \times x)$ - \times is right-**distributive** over $+$
- left-&right-**distributive** - \times is **distributive** over $+$

If \times has **commutative property** - it is two-side **distributive** over $+$.

14.3.1.6.1 *

Distributive

14.3.2 Effect

Observable action.

14.3.3 Bisimulation

When systems have exact external behaviour so for observer they are the same.

[Binary relation](#) between state transition systems that match each other's moves.

14.3.3.1 *

Bisimilar

14.3.4 Primitive operation

[Operation](#) that is axiomatic (can't be expressed from other given axioms of the system).

In program languages it is most probably implemented by lower-level programming.

In Haskell they are provided by GHC.

More: [GHC Wiki/prim-ops](#).

14.3.4.1 *

PrimOps

14.4 Content word

Words that name [objects](#) of reality and their qualities.

14.5 Ancient Greek and Latin prefixes**14.5.1 ***

Greek prefix Latin prefix

Table 14.1: Ancient Greek and Latin prefixes

Meaning	Greek prefix	Latin prefix
above, excess	hyper-	super-, ultra-
across, beyond, through	dia-	trans-
after		post-
again, back		re-
against	anti-	contra-, (in-, ob-)
all	pan	omni-
around	peri-	circum-
away or from	apo-, ap-	ab- (or de-)
bad, difficult, wrong	dys-	mal-
before	pro-	ante-, pre-
between, among		inter-
both	amphi-	ambi-
completely or very		de-, ob-
down		de-, ob-
four	tetra-	quad-
good	eu-	ben-, bene-
half, partially	hemi-	semi-
in, into	en-	il-, im-, in-, ir-
in front of	pro-	pro-
inside	endo-	intra-
large	macro-	(macro-, from Greek)
many	poly-	multi-
not*	a-, an-	de-, dis-, in-, ob-
on	epi-	
one	mono-	uni-
out of	ek-	ex-, e-
outside	ecto-, exo-	extra-, extro-
over	epi-	ob- (sometimes)
self	auto-, aut-, auth-	ego-
small	micro-	
three	tri-	tri-
through	dia-	trans-
to or toward	epi-	ad-, a-, ac-, as-
two	di-	bi-
under, insufficient	hypo-	sub-
with	sym-, syn-	co-. com-, con-
within, inside	endo-	intra-
without	a-, an-	dis- (sometimes)

Chapter 15

Set

Well-defined collection of distinct **objects**.

15.1 *

Sets Set theory

15.2 Axiom of choice

$$\forall X \left[\emptyset \notin X \implies \exists f: X \rightarrow \bigcup X \quad \forall A \in X (f(A) \in A) \right]$$

Simple version:

For any inhabited **sets**, exists a **set** with exactly one element in common with each of them.

... from more wide-known variant:

Given any **set** X of pairwise disjoint non-empty **sets**, there exists at least one **set** C that contains exactly one element in common with each of the **sets** in X .

Most official formalization:

For any **set** X of nonempty **sets**, there exists a choice **function** f defined on X .

15.3 Closed set

- Set** which complements an open **set**.
- Is form of **Closed-form expression**. **Set** can be **closed** in under a **set** of operations.

15.4 Power set

For some **set** \mathcal{S} , the **power set** $(\mathcal{P}(\mathcal{S}))$ is a **set** of all subsets of \mathcal{S} , including $\{\}$ & \mathcal{S} itself.

Denotation: $\mathcal{P}(\mathcal{S})$

15.5 Singleton

Singleton - **unit set** - **set** with exactly one element. Also 1-**sequence**.

15.6 Russell's paradox

If there exists normal [set](#) of all [sets](#) - it should contain itself, which makes it abnormal.

15.7 Cartesian product

$\mathcal{A} \times \mathcal{B} \equiv \sum^{\forall} (a, b) \mid \forall a \in \mathcal{A}, \forall b \in \mathcal{B}$. [Operation](#), returns a [set](#) of all ordered pairs (a, b)

Any [function](#), [functor](#) is a subset of [Cartesian product](#).

$$\sum (elem \in (\mathcal{A} \times \mathcal{B})) = cardinality^{A \times B}$$

[Properties](#):

- not [associative](#)
- not [commutative](#)

15.7.1 Pullback

Subset of the [cartesian product](#) of two [sets](#).

15.7.1.1 *

Pullbacks

15.8 Zermelo–Fraenkel [set theory](#)

Modern [set theory](#). Axiomatic system free of paradoxes such as [Russell's paradox](#) and at the same time preserves the logical language of scientific works.

15.8.1 *

ZFC

Chapter 16

Testing

16.1 Property testing

Since [property](#) yealds the according [law](#), family of [unit](#) tests for the [property](#) can be abstracted into the [function](#) that test the [law](#).

[Unit](#) test cases come from [generator](#), and test the [law](#) empirically, but repeatedly and automatically.

16.1.1 Function property

[Property](#) corresponds to the according [law](#). In [property testing](#) you need to think additionally about [generator](#) and [shrinking](#).

16.1.2 Property testing type

Table 16.1: [Property testing types](#)

	Exhaustive	Randomized	Unit test
Whole set of values	Exhaustive property test	Randomised property test	One elem
Special subset of values	Exhaustive specialised property test	Randomised specialised property test	One elem

16.1.3 Generator

Seed
|
v
Gen A -> A
^
|
Size

Seed allows reproducibility. There is anyway a need to have some seed. Size allows setting upper [bound](#) on size of generated value. Think about infinity of [list](#).

After failed test - [shrinking](#) tests value parts of contrexample, finds a part that still fails, and recurses [shrinking](#).

16.1.3.1 *

Generators

16.1.3.2 Custom generator

When certain theorem only works for a specific **set** of values - the according **generator** needs to be produced.

```
arbitrary :: Arbitrary a => Gen a
suchThat :: Gen a -> (a -> Bool) -> Gen a
elements :: [a] -> Gen a
```

16.1.4 Reusing test code

Often it is convinient to **abstract testing** of same **function properties**:

It can be done with (aka TestSuite **combinator**):

```
-- Definition
{-# LANGUAGE ScopedTypeVariables #-}
{-# LANGUAGE AllowAmbiguousTypes #-}
eqSpec :: forall a. Arbitrary a => Spec

-- Usage
{-# LANGUAGE TypeApplications #-}
spec :: Spec
spec = do
  eqSpec @Int

Eq Int
  (==) :: Int -> Int -> Bool
    is reflexive
    is symetric
    is transitive
    is equivalent to (\ a b -> not $ a /= b)
  (/=) :: Int -> Int -> Bool
    is antireflexive
    is equivalent to (\ a b -> not $ a == b)
```

16.1.4.1 Test Commutative property

Commutativity

```
:: Arbitrary a => (a -> a -> a) -> Property
```

16.1.4.2 Test Symmetry property

Symmetry

```
:: Arbitrary a => (a -> a -> Bool) -> Property
```

16.1.4.3 Test Equivalence property

Equivalence

```
:: (Arbitrary a, Eq b) => (a -> b) -> (a -> b) -> Property
```

16.1.4.4 Test Inverse property

```
:: (Arbitrary a, Eq b) => (a -> b) -> (b -> a) -> Property
```

16.1.5 QuickCheck

Target is a member of the [Arbitrary type class](#). Target -> Bool is something Testable. This [properties](#) can be complex. [Generator](#) arbitrary gets the seed, and produces values of Target. [Function](#) quickCheck runs the loop and tests that generated Target values always comply the [property](#).

16.1.5.1 Manual automation with QuickCheck properties

```
import Test.QuickCheck
import Test.QuickCheck.Function
import Test.QuickCheck.Property.Common
import Test.QuickCheck.Property.Functor
import Test.QuickCheck.Property.Common.Internal

data Four' a b = Four' a a a b
  deriving (Eq, Show)

instance Functor (Four' a) where
  fmap f (Four' a b c d) = Four' a b c (f d)

instance (Arbitrary a, Arbitrary b) => Arbitrary (Four' a b) where
  arbitrary = do
    a1 <- arbitrary
    a2 <- arbitrary
    a3 <- arbitrary
    b <- arbitrary
    return (Four' a1 a2 a3 b)

-- Wrapper around `prop_FunctorId`
prop_AutoFunctorId :: Functor f => f a -> Equal (f a)
prop_AutoFunctorId = prop_FunctorId T

type Prop_AutoFunctorId f a
  = f a
  -> Equal (f a)

-- Wrapper around `prop_AutoFunctorCompose`
prop_AutoFunctorCompose :: Functor f => Fun a1 a2 -> Fun a2 c -> f a1 -> Equal
  => (f c)
prop_AutoFunctorCompose f1 f2 = prop_FunctorCompose (applyFun f1) (applyFun f2)
  => T

type Prop_AutoFunctorCompose structureType origType midType resultType
  = Fun origType midType
  -> Fun midType resultType
  -> structureType origType
  -> Equal (structureType resultType)

main = do
  quickCheck $ eq $ (prop_AutoFunctorId :: Prop_AutoFunctorId (Four'
    => (Integer)
  quickCheck $ eq $ (prop_AutoFunctorId :: Prop_AutoFunctorId (Four' (
    => (Either Bool String))
  quickCheck $ eq $ (prop_AutoFunctorCompose :: Prop_AutoFunctorCompose (Four'
    => (String Integer String))
```

```
quickCheck $ eq $ (prop_AutoFunctorCompose :: Prop_AutoFunctorCompose (Four'
  ↪ ()) Integer String (Maybe Int))
```

16.2 Write tests algorithm

- a. Pick the right language/[stack](#) to implement features.
- b. How expensive breakage can be.
- c. Pick the right tools to test this.

16.3 Shrinking

[Process](#) of reducing complexity in the test [case](#) - re-run with smaller values and make sure that the test still fails.

Chapter 17

Logic

17.1 Proposition

Purely abstract & theoretical logical **object** (idea) that has a Boolean value.

* is expressed by a **statement**.

17.1.1 *

Propositions

17.1.2 Atomic proposition

Logically undividable **unit**. Does not contain **logical connectives**.

Often abstracts the non-logical ("real") **objects**.

17.1.2.1 *

Atomic propositions

17.1.3 Compound proposition

Formed by connecting **propositions** by **logical connectives**.

17.1.3.1 *

Compound propositions

17.1.4 Propositional logic

Studies **propositions** and **argument** flow.

Distinguishes logically indivisible units (**atomic propositions**) and abstracts them as **variable** and **constant** values of Boolean **type properties**. Studies consequences of those value arguments (**atomic proposition**) on **composed propositions**.

Invented by Aristotle.

Classical system that lead humanity to profound advancement. The classical * language thou is limited and so in modern day extensions (mainly **First-order logic**) are used in the sciences.

Not Turing-complete, for example it is impossible to **construct** an **arbitrary** loop.

17.1.4.1 *

Proposition logic Proposition calculus Propositional calculus Statement logic Sentential logic Sentential calculus Zeroth-order logic

17.1.4.2 First-order logic

Extension of a [propositional logic](#) that adds [quantifiers](#).

Turing-complete.

17.1.4.2.1 *

Predicate logic First-order predicate logic First-order predicate calculus

17.1.4.2.2 Second-order logic

Extension over [first-order logic](#) that quantifies over [relations](#).

17.1.4.2.2.1 Higher-order logic

Extension over [second-order logic](#) that uses additional [quantifiers](#), stronger [semantics](#).

Is more expressive, but model-theoretic [properties](#) are less well-behaved.

17.2 Logical connective

Logical [operation](#).

17.2.1 *

Logical connectives

17.2.2 Conjunction

Logical AND.

Denotation: \wedge

Multiplies [cardinalities](#).

Haskell [kind](#):

[*](#) [*](#)

17.2.3 Disjunction

Logical *OR* Denotation: \vee

Summs [cardinalities](#).

Relates to:

- (in [sets](#)) union
- (in [algebra](#)) addition
- (in [categories](#)) sum

17.3 Predicate

Function with Boolean **codomain**, $P : X \rightarrow \{true, false\}$ - * on X .

Notation: $P(x)$

Im many cases includes **relations**, **quantifiers**.

17.4 Statement

Declarative **expression** that is a bearer of a **proposition**.

When we talk about **expression** or **statement** being true/false - in fact we refer to the **proposition** that they represent.

Difference between **proposition**, **statement**, **expression**:

- a. "2 + 3 = 5"
- b. "two plus three equals five"
 - 1 & 2 are **statements**. Each of them is a collection of transmission symbols (linguistic **objects**) from a symbol systems \equiv **expression**. Each of them is **expression** that bears **proposition** (an idea resulting in a Boolean value) \equiv **statement**.
 - 1 & 2 represent the same **proposition**. **Proposition** from 1 \equiv **proposition** from 2.
 - **Statement** 1 \neq **statement** 2. They are two different **statements**, written in different systems. And **statement** "2 + 3 = 5" \neq **statement** "3 + 2 = 5".

17.4.1 *

Assertion Assertions Statements

17.4.2 Antecedent

The if (requirement) part of the **proposition**.

17.4.3 Consequent

else (consequential) part of the **proposition**.

17.4.4 Vacuous

Nonsensical **proposition** that has {impossible, not full, false} premise and as such - impossible to definitely prove true nor false (under currently given tools inside the particular theory).

Such **proposition** falls into paradox due to **property** of excluded middle in the classical logic.

Requirements of the **proposition** (**antecedent** part) cannot be satisfied.

Therefore "**vacuous** true/false" means: "considered as, but not proven".

Is a good example of why Haskell uses total **functions** even for `if .. then .. else ..` **state-ments**.

There is also vacuous **function** in Haskell, see **Void**.

17.5 Iff

If and only if, exactly when, just. Denotation: \iff

Chapter 18

Haskell structures

18.1 *

Haskell structures

18.2 Pattern match

Are not first-class. It is a set of pattern match semantic notations.

Must be linear.

* precedence (especially with more than one parameter, especially with `_` used) often changes the function.

18.2.1 As-pattern

```
f list@(x, xs) = ...  
f (x:xs)      = x:x:xs -- Can be compiled with reconstruction of x:xs  
f a@(x:_)    = x:a -- Reuses structure without reconstruction
```

18.2.1.1 *

As-patterns As pattern As patterns

18.2.2 Wild-card

Matches anything and can not be binded. For matching something that should pass not checked and is not used.

```
head (x:_)      = x  
tail (_:xs)     = xs
```

18.2.2.1 *

Wild-cards Wildcard Wildcards

18.2.3 Case

```
case x of  
  pattern1 -> ex1
```

```

pattern2 -> ex2
pattern3 -> ex3
otherwise -> exDefault

```

Bolting [guards](#) & [expressions](#) with [syntactic sugar](#) on [case](#):

```

case () of _
| expr1      -> ex1
| expr2      -> ex2
| expr3      -> ex3
| otherwise  -> exDefault

```

Pattern matching in [function](#) definitions is realized with [case expressions](#).

18.2.4 Guard

Check values against the [predicate](#) and use the first match definition:

```

f x
| predicate1 = definition1
| predicate2 = definition2
...
| x < 0      = definitionN
...
| otherwise  = definitionZ

```

18.2.4.1 *

Guards

18.2.5 Pattern guard

Allows check a [list](#) of pattern matches against [functions](#), and then proceed.

```
(patternMatch1) <- (funcCheck1)
```

```
, (patternMatch2) <- (funcCheck2) = RHS
```

```
lookup :: Eq a => a -> [(a, b)] -> Maybe b
```

```

addLookup l a1 a2
| Just b1 <- lookup a1 l
, Just b2 <- lookup a2 l
= b1 + b2
{-...other equations...-}

```

Run [functions](#), they must succeed. Then [pattern match](#) results to b1, b2. Only if successful - execute the equation.

Default in Haskell 2010.

18.2.5.1 *

Pattern guards

18.2.6 Lazy pattern

Defers the [pattern match](#) directly to the last moment of need during execution of the code.

```
f (a, b) = g a b -- It would be checked that the pattern of the pair
    ↪ constructor
-- is present, and that parameters are present in the constructor.
-- Only after that success - work would start on the RHS, aka then construction
-- g would start only then.
```

```
f ~(a, b) = g a b -- Pattern match of (a, b) deferred to the last moment,
-- RHS starts, construction of g starts.
-- For this lazy pattern the equivalent implementation would be:
-- f p = g (fst p) (snd p) -- RHS starts, during construction of g
-- the arguments would be computed and found, or error would be thrown.
```

Due to full laziness deferring everything to the runtime execution - the [lazy pattern](#) is one-size-fits all ([irrefutable](#)), analogous to `_`, and so it does not produce any checks during compilation, and raises [errors](#) during runtime.

`*` is very useful during [recursive](#) construction of [recursive structure/process](#), especially infinite.

18.2.6.1 *

Lazy-pattern Lazy patterns

18.2.7 Pattern binding

Entire [LHS](#) is a pattern, is a [lazy pattern](#).

```
fib@(1:tfib) = 1 : 1 : [ a+b | (a,b) <- zip fib tfib ]
```

18.2.7.1 *

Pattern bindings

18.3 Smart constructor

[Process](#)/code placing extra rules & [constraints](#) on the construction of values.

18.4 Level of code

There are these levels of Haskell code:

18.4.1 *

Code level

18.4.2 Type level

[Level of code](#) that works with [data types](#).

18.4.2.1 Type level declaration

```
type ...
newtype ...
data ...
class ...
instance ...
```

18.4.2.1.1 *

Type level declarations Type-level declaration Type-level declarations

18.4.2.2 Type check

if The [type level](#) information is complete ([strongly connected](#) graph)

then

Generalize the [types](#) and check if [type level](#) consistent to [term level](#).

else

[Infer](#) the missing [type level](#) part from the [term level](#). There are certain situations and [structures where](#) ambiguity arises and is unsolvable from the information of the [term level](#) (most basic example is [polymorphic recursion](#)).

18.4.2.2.1 *

Typecheck Typechecking Typechecks

18.4.2.2.2 Complete user-specific kind signature

[Type level declaration](#) is considered to "have a [CUSK](#)" is it has enough syntatic information to warrant completeness ([strongly connected](#) graph) and start checking [type level](#) correspondence to [term level](#), it is a ad-hock state of [type inferring](#).

In the future GHC would use other algorithm over/instead of [CUSK](#).

18.4.2.2.2.1 *

CUSK CUSKs Complete user-specific kind signatures Complete, user-specific kind signature

18.4.3 Term level

[Level of code](#) that does logical execution.

18.4.4 Compile level

[Level of code](#), about compilation processes/results.

18.4.4.1 *

Compilation level

18.4.5 Runtime level

[Level of code](#) of main program [operation](#), when machine does computations with compiled [binary](#) code.

18.4.6 Kind level

[Level of code where](#) [kinds](#) & [kind](#) declarations are situated, infered and checked.

18.4.6.1 Kind check

Applying the [type check](#) to [kind](#) check:

if The [kind](#) level information is complete ([strongly connected](#) graph)

then

Check if [kind](#) level consistent to [term level](#).

else

[Infer](#) the missing [kind](#) level parts from the [type level](#). There are certain situations and [structures where](#) ambiguity arises and is unsolvable from the information of the [kind](#) level.

With StandaloneKindSignatures [kind](#) completeness happens against found (standalone) [kind](#) signature.

With CUSKs extension kind completeness happens against "[complete user-specific kind signature](#)"

18.4.6.1.1 *

Kindcheck Kind checks

18.5 Orphan instance

Situation when [module](#) provides [type class](#) but does not provide instance for some publically used [type](#).

That allows/pushes to implement own version of instance. If upstream would add instance - now upstream instance and own instance exist. Locally that would create instance clash. Remotely, through modules usage - that should create inconsistency problems in computations, since instances most probably not [bisimilar](#).

If [module](#) has any orphans - then in GHC terms all [module](#) is called an "orphan [module](#)". GHC always visits the [interface](#) file of every orphan [module](#) below the [module](#) being compiled. This is usually a wasted work, but it needs to be done. So do best to have as few orphan modules as possible" ("[GHC User's Guide Documentation, Release 8.8.3](#)"). Orphan prolongs the compilation, and moreover - compilation of all even dependent code on it, because requires [recursive](#) lookups into [module](#) dependencies.

See: [Good: Handling orphan instance](#).

18.6 undefined

Placeholder value that helps to do [typechecking](#).

18.7 Hierarchical module name

Hierarchical naming scheme:

```
Algebra                -- Was this ever used?
  DomainConstructor    -- formerly DoCon
  Geometric             -- formerly BasGeomAlg

Codec                  -- Coders/Decoders for various data formats
  Audio
    Wav
    MP3
    ...
```

```

Compression
  Gzip
  Bzip2
  ...
Encryption
  DES
  RSA
  BlowFish
  ...
Image
  GIF
  PNG
  JPEG
  TIFF
  ...
Text
  UTF8
  UTF16
  ISO8859
  ...
Video
  Mpeg
  QuickTime
  Avi
  ...
Binary                                -- these are for encoding binary data into text
  Base64
  Yenc

Control
  Applicative
  Arrow
  Exception                          -- (opt, inc. error & undefined)
  Concurrent                         -- as hslibs/concurrent
    Chan                            -- these could all be moved under Data
    MVar
    Merge
    QSem
    QSemN
    SampleVar
    Semaphore
  Parallel                           -- as hslibs/concurrent/Parallel
    Strategies
  Monad                             -- Haskell 98 Monad library
    ST                             -- ST defaults to Strict variant?
      Strict                       -- renaming for ST
      Lazy                         -- renaming for LazyST
    State                          -- defaults to Lazy
      Strict
      Lazy
    Error
    Identity
    Monoid
    Reader
    Writer

```

```

    Cont
    Fix          -- to be renamed to Rec?
    List
    RWS

Data
  Binary          -- Binary I/O
  Bits
  Bool            -- &&, ||, not, otherwise
  Tuple          -- fst, snd
  Char            -- H98
  Complex         -- H98
  Dynamic
  Either
  Int
  Maybe           -- H98
  List            -- H98
  PackedString
  Ratio           -- H98
  Word
  IORef
  STRef           -- Same as Data.STRef.Strict
    Strict
    Lazy          -- The lazy version (for Control.Monad.ST.Lazy)
  Binary          -- Haskell binary I/O
  Digest
    MD5
    ...           -- others (CRC ?)
  Array           -- Haskell 98 Array library
    Unboxed
    IArray
    MArray
    IO            -- mutable arrays in the IO/ST monads
    ST
  Trees
    AVL
    RedBlack
    BTree
  Queue
    Bankers
    FIFO
  Collection
  Graph           -- start with GHC's DiGraph?
  FiniteMap
  Set
  Memo            -- (opt)
  Unique

  Edison          -- (opt, uses multi-param type classes)
    Prelude       -- large self-contained packages should have
    Collection    -- their own hierarchy? Like a vendor branch.
    Queue         -- Or should the whole Edison tree be placed

Database
  MySQL

```

```

    PostgreSQL
    ODBC

Dotnet
    ...                -- Mirrors the MS .NET class hierarchy

Debug                -- see also: Test
    Trace
    Observe          -- choose a default amongst the variants
        Textual      -- Andy Gill's release 1
        ToXmlFile    -- Andy Gill's XML browser variant
        GHood        -- Claus Reinke's animated variant

Foreign
    Ptr
    StablePtr
    ForeignPtr      -- rename to FinalisedPtr? to void confusion with Foreign.Ptr
    Storable
    Marshal
        Alloc
        Array
        Errors
        Utils
    C
        Types
        Errors
        Strings

GHC
    Exts            -- hslibs/lang/GlaExts
    ...

Graphics
    HGL
    Rendering
        Direct3D
        FRAN
        Metapost
        Inventor
        Haven
        OpenGL
            GL
            GLU
    Pan
    UI
        FranTk
        Fudgets
        GLUT
        Gtk
        Motif
        ObjectIO
        TkHaskell
    X11
        Xt
        Xlib

```



```

    Xmu
    Xaw

Hugs
...

Language
  Haskell      -- hslibs/hssource
    Syntax
    Lexer
    Parser
    Pretty
  HaskellCore
  Python
  C
  ...

Nhc
...

Numeric      -- exports std. H98 numeric type classes
  Statistics

Network      -- (== hslibs/net/Socket), depends on FFI only
  BER        -- Basic Encoding Rules
  Socket     -- or rename to Posix?
  URI        -- general URI parsing
  CGI        -- one in hslibs is ok?
  Protocol
    HTTP
    FTP
    SMTP

Prelude      -- Haskell98 Prelude (mostly just re-exports
              other parts of the tree).

Sound        -- Sound, Music, Digital Signal Processing
  ALSA
  JACK
  MIDI
  OpenAL
  SC3        -- SuperCollider

System      -- Interaction with the "system"
  Cmd        -- ( system )
  CPUTime    -- H98
  Directory  -- H98
  Exit       -- ( ExitCode(..), exitWith, exitFailure )
  Environment -- ( getArgs, getProgName, getEnv ... )
  Info       -- info about the host system
  IO         -- H98 + IOExts - IOArray - IORef
    Select
    Unsafe   -- unsafePerformIO, unsafeInterleaveIO
  Console
  GetOpt

```

```

    Readline
Locale          -- H98
Posix
    Console
    Directory
    DynamicLinker
        Prim
        Module
    IO
    Process
    Time
Mem             -- rename from cryptic 'GC'
    Weak        -- (opt)
    StableName  -- (opt)
Time           -- H98 + extensions
Win32          -- the full win32 operating system API

Test
    HUnit
    QuickCheck

Text
    Encoding
        QuotedPrintable
        Rot13
    Read
        Lex          -- cut down lexer for "read"
    Show
        Functions    -- optional instance of Show for functions.
Regex          -- previously RegexString
    Posix       -- Posix regular expression interface
PrettyPrint    -- default (HughesPJ?)
    HughesPJ
    Wadler
    Chitil
    ...
HTML           -- HTML combinator lib
XML
    Combinators
    Parse
    Pretty
    Types
ParserCombinators -- no default
    ReadP        -- a more efficient "ReadS"
    Parsec
    Hutton_Meijer
    ...

Training        -- Collect study and learning materials
    <name of the tutor>

```

18.7.1 *

Top-level module name Top-level module names

18.8 Reserved word

Haskell has special meaning for:

case, class, data, deriving, do, else, if, import,
in, infix, infixl, infixr, instance, let,
of, module, newtype, then, type, where

18.8.1 *

Reserved words

18.8.2 import

`import statement` by default imports identifiers from the other [module](#), using [hierarchical module name](#), brings into [scope](#) the identifiers to the global [scope](#) both into unqualified and qualifies by the [hierarchical module name](#) forms.

This possibilities can mix and match:

- `<modName> ()` - [import](#) only instances of [type classes](#).
- `<modName> (x, y)` - [import](#) only declared identifiers.
- `qualified <modName>` - discards unqualified names, force obligatory namespace for the imports.
- `hiding (x, y)` - skip [import](#) of declared identifiers.
- `<modName> as <modName>` - renames [module](#) namespace.
- `<type/class> (..)` - [import](#) class & it's methods, or [type](#), all its data [constructors](#) & field names.

18.8.3 let

* [expression](#) is a [set](#) of cross-[recursive lazy pattern bindings](#).

Declarations permitted:

- [type](#) signatures
- [function bindings](#)
- [pattern bindings](#)

It is an [expression](#) (macro) and that integrates in external [lexical scope expression](#) it [applied](#) in.

Form:

```
let
  b1
  bn
in
  c
```

18.8.3.1 *

Let expression Let expressions

18.8.4 where

Part of the syntax of the whole [function declaration](#), has according [scope](#).

As part of whole [declaration](#) - can extend over definitions of the function (pattern matches, [guards](#)).

Form:

```
f match1 = y
f match2 = y
f x =
  | cond1 x = y
  | cond2 x = y
  | otherwise = y
where
  y = ... x ...
```

18.8.4.1 *

Where clause

18.9 Haskell Language Report

Document that is a standart of language.

18.9.1 *

Report Haskell Report Haskell 98 Language Report Haskell 98 Report Haskell 1998 Language Report Haskell 2010 Language Report Haskell 2010 Report

18.10 Haskell'

Current language development mod.

<https://prime.haskell.org/>

18.10.1 *

Haskell prime

18.11 Lense

Library of combinators to provide Haskell (functional language without mutation) with the emulation of get-ters and set-ters of imperative language.

18.12 Pragma

Pragma - instruction to the compiler that specifies how a compiler should **process** the code. **Pragma** in Haskell have form:

```
{-# PRAGMA options #-}
```

18.12.1 LANGUAGE pragma

Controls what variations of the language are permitted. It has a **set** of allowed options: https://downloads.haskell.org/~ghc/latest/docs/html/users_guide/glasgow_exts.html, which can be supplied.

18.12.1.1 LANGUAGE option**18.12.1.1.1 ***

Language options

18.12.1.1.2 Useful by default

```
import EmptyCase
import FlexibleContexts
import FlexibleInstances
import InstanceSigs
import MultiParamTypeClasses
```

18.12.1.1.3 AllowAmbiguousTypes

Allow [type](#) signatures which appear that they would result in an unusable [binding](#). However GHC will still check and complain about a [functions](#) that can never be called.

18.12.1.1.4 ApplicativeDo

Enables an [alternative](#) in-depth [reduction](#) that translates the do-notation to the operators `<$>`, `<*>`, `join` as far as possible.

For GHC to pickup the patterns, the final [statement](#) must match one of these patterns exactly:

```
pure E
pure $ E
return E
return $ E
```

When the [statements](#) of do [expression](#) have dependencies between them, and [ApplicativeDo](#) cannot [infer](#) an [Applicative type](#) - GHC uses a heuristic $O(n^2)$ algorithm to try to use `<*>` as much as possible. This algorithm usually finds the best solution, but in rare complex cases it might miss an opportunity. There is also $O(n^3)$ algorithm that finds the optimal solution: `-foptimal-applicative-do`.

Requires `ap = <*>`, `return = pure`, which is true for the most [monadic types](#).

- Allows use of do-notation with [types](#) that are an instance of [Applicative](#) and [Functor](#)
- In some [monads](#), using the [applicative](#) operators is more efficient than [monadic bind](#). For example, it may enable more parallelism.

The only way it shows up at the source level is that you can have a do [expression](#) with only [Applicative](#) or [Functor](#) constraint.

It is possible to see the actual translation by using `-ddump-ds`.

18.12.1.1.5 ConstrainedClassMethods

Enable the definition of further [constraints](#) on individual class methods.

18.12.1.1.6 CPP

Enable [C preprocessor](#).

18.12.1.1.7 DeriveFunctor

Automatic [deriving](#) of instances for the [Functor type class](#). For [type power set functor](#) is unique, its derivation implementation can be autochecked.

18.12.1.1.8 ExplicitForAll

Allow explicit `forall` quantificator in places `where` it is implicit by Haskell.

18.12.1.1.9 FlexibleContexts

Ability to use complex `constraints` in class `declaration contexts`. The only restriction on the `context` in a class `declaration` is that the class hierarchy must be acyclic.

```
class C a where
  op :: D b => a -> b -> b
```

```
class C a => D a where ...
```

$C \mathrel{:>} D$, so in `C` we can talk about `D`.

Synergizes with `ConstraintKinds`.

18.12.1.1.10 FlexibleInstances

Allow `type class` instances `types` contain nested `types`.

```
instance C (Maybe Int) where ...
```

Implies `TypeSynonymInstances`.

18.12.1.1.11 GeneralizedNewtypeDeriving

Enable GHC's newtype cunning generalised `deriving` mechanism.

```
newtype Dollars = Dollars Int
  deriving (Eq, Ord, Show, Read, Enum, Num, Real, Bounded, Integral)
```

(In old `Haskell 98` only `Eq`, `Ord`, `Enum` could be inherited.)

18.12.1.1.12 ImplicitParams

Allow definition of `functions` expecting implicit `parameters`. In the Haskell that has static scoping of `variables` allows the dynamic scoping, such as in classic Lisp or ELisp. Sure thing this one can be puzzling as hell inside Haskell.

18.12.1.1.13 LambdaCase

Enables `expressions` of the form:

```
\case { p1 -> e1; ...; pN -> eN }
```

-- OR

```
\case
  p1 -> e1
  ...
  pN -> eN
```

18.12.1.1.14 MultiParamTypeClasses

Implies: `ConstrainedClassMethods` Enable the definitions of typeclasses with more than one `parameter`.

```
class Collection c a where
```

18.12.1.1.15 MultiWayIf

Enable multi-way-if syntax.

```
if | guard1 -> code1
   | ...
   | guardN -> codeN
```

18.12.1.1.16 OverloadedStrings

Enable overloaded string literals (string literals become desugared via the `IsString` class).

With overload, string literals has [type](#):

```
(IsString a) => a
```

The usual string syntax can be used, e.g. `ByteString`, `Text`, and other variations of string-like [types](#). Now they can be used in pattern matches as `char->integer` translations. To [pattern match](#) `Eq` must be [derived](#).

To use class `IsString` - [import](#) it from `GHC.Ext`.

18.12.1.1.17 PartialTypeSignatures

Partial [type](#) signature contains [wildcards](#), placeholders (`_`, `_name`). Allows programmer to which parts of a [type](#) to annotate and which to [infer](#). Also applies to [constraint](#) part.

As untuped [expression](#), partly typed can not polymorphically recurse.

[-Wno-partial-type-signatures](#) suppresses [infer](#) warnings.

18.12.1.1.18 RankNTypes

Enable [types](#) of [arbitrary](#) rank. See [Type rank](#).

Implies [ExplicitForAll](#).

Allows `forall` [quantifier](#):

- Left side of \rightarrow
- Right side of \rightarrow
- as [argument](#) of a [constructor](#)
- as [type](#) of a field
- as [type](#) of an implicit [parameter](#)
- used in pattern [type](#) signature of [lexically scoped type variables](#)

18.12.1.1.19 ScopedTypeVariables

By default [type variables](#) do not have a [scope](#) except inside [type](#) signatures [where](#) they are used.

Extension allows:

- explicitly `forall` [quantified type variables](#) broad the [scope](#) to the internals of implementation.
- pattern [type](#) signatures can use `::` to denote a [type](#) signature within a pattern.

When there are internal [type](#) signatures provided in the code block (`where`, `let`, etc.) they (main [type](#) description of a [function](#) and internal [type](#) descriptions) restrain one-another and become not trully [polymorphic](#), which creates a bounding interdependency of [types](#) that GHC would complain about.

* option provides the [lexical scope](#) inside the code block for [type variables](#) that have `forall` [quantifier](#). Because they are now lexically scoped - those [type variables](#) are used across internal [type](#) signatures.

Implies [ExplicitForAll](#).

See: [GHC documentation](#), [explanation blogpost](#), [typeclasses article](#).

18.12.1.1.20 TupleSections

Allow [tuple](#) section syntax:

```
(, True)
(, "I", , , "Love", , 1337)
```

18.12.1.1.21 TypeApplications

Allow [type application](#) syntax:

```
read @Int 5

:type pure @[]
pure @[] :: a -> [a]

:type (<*>) @[]
(<*>) @[] :: [a -> b] -> [a] -> [b]

--

instance (CoArbitrary a, Arbitrary b) => Arbitrary (a -> b)

λ> ($ 0) <$> generate (arbitrary @(Int -> Int))
```

18.12.1.1.22 TypeSynonymInstances

Now [type](#) synonym can have it's own [type class](#) instances.

18.12.1.1.23 UndecidableInstances

Permit instances which may lead to [type](#)-checker non-termination.

GHC has Instance termination rules regardless of [FlexibleInstances](#) [FlexibleContexts](#).

18.12.1.1.24 ViewPatterns

```
foo (f1 -> Pattern1) = c1
foo (fn -> Pattern2 a b) = g1 a b
```

(*expression* → *pattern*): take what is came to match - [apply](#) the *expression*, then do *pattern*-match, and return what originally came to match.

[Semantics](#):

- *expression* & *pattern* share the [scope](#), so also [variables](#).

expression :: t1 -> t2) && (pattern t2)=) then (ViewPattern (/expression/ -> /pattern/) :: t1) (return what originally was recieved into [pattern match](#)) else skip

* are like [pattern guards](#) that can be nested inside of other patterns. * are a convenient way to pattern-match [algebraic data type](#).

Additional possible usage:

```
foo a (f2 a -> Pattern3 b c) = g2 b c -- only for function definitions
foo ((f,_), f -> Pattern4) = c2 -- variables can be bount to the left in data
  ↳ constructors and tuples
```


18.12.1.1.25 DatatypeContexts

Allow [contexts](#) in [data types](#).

```
data Eq a => Set a = NilSet | ConsSet a (Set a)

-- NilSet :: Set a
-- ConsSet :: Eq a => a -> Set a -> Set a
```

Considered misfeature. Deprecated. Going to be removed.

18.12.1.1.26 StandaloneKindSignatures

Type signatures for [type-level declarations](#).

```
type <name_1> , ... , <name_n> :: <kind>

type MonoTagged :: Type -> Type -> Type
data MonoTagged t x = MonoTagged x

type Id :: forall k. k -> k
type family Id x where
  Id x = x

type C :: (k -> Type) -> k -> Constraint
class C a b where
  f :: a b

type TypeRep :: forall k. k -> Type
data TypeRep a where
  TyInt    :: TypeRep Int
  TyMaybe :: TypeRep Maybe
  TyApp    :: TypeRep a -> TypeRep b -> TypeRep (a b)
```

< GHC 8.10.1 - [type](#) signatures were only for [term level](#) declarations.

Extension makes signatures feature more uniformal.

Allows to [set](#) the [order](#) of [quantification](#), [order](#) of [variables](#) in a [kind](#). For example when using [TypeApplications](#).

Allows to [set](#) full [kind](#) of derivable class, solving situations with [GADT](#) return [kind](#).

18.12.1.1.26.1 *

SAKS Standalone kind signatures

18.12.1.1.27 PartialTypeSignatures

Very helpful. Helps to solve [type level](#), helps to establish [type](#) signatures and [constraints](#). Allow to provide [_](#) in the [type](#) signatures to automatically infer-in the [type](#) information there.

Wild cards:

- [Type](#)
- ```
f :: _ -> _ -> a
```
- [Constraint](#)
- ```
f :: _ => a -> b -> c
```
- [Named](#)

```
f :: _x -> _x -> a
```

allows to identify the same [wildcard](#).

18.12.1.1.28 TypeOperators

Allow [type](#) signature to hold [operator](#) names:

```
data a + b = Plus a b
```

—

Implies [ExplicitNamespaces](#)

18.12.1.2 How to make a GHC LANGUAGE extension

In `libraries/ghc-boot-th/GHC/LanguageExtensions/Type.hs` add new [constructor](#) to the `Extension` type

```
data Extension
  = Cpp
  | OverlappingInstances
  ...
  | Foo
```

`/main/DynFlags.hs` extend `xFlagsDeps`:

```
xFlagsDeps = [
  flagSpec "AllowAmbiguousTypes" LangExt.AllowAmbiguousTypes,
  ...
  flagSpec "Foo" LangExt.Foo
]
```

It is for basic [case](#). For [testing](#), parser see further: <https://blog.shaynefletcher.org/2019/02/adding-ghc-language-extension.html>

Chapter 19

Computer science

19.1 Guerrilla patch

* changing code/[applying](#) patch sneakily - and possibility incompatibility with other at runtime. [Monkey patch](#) is derivative term.

19.1.1 Monkey patch

From [Guerrilla patch](#).

* is a way for program to modify supporting system software affecting only the running instance of the program.

19.2 Interface

Point of mutual meeting. Code behind [interface](#) determines how data is consumed.

19.3 Module

Importable organizational [unit](#).

19.4 Scope

Area [where binds](#) are accessible.

19.4.1 Dynamic scope

The name resolution depends upon the program state when the name is encountered, which is determined by the execution [context](#) or calling [context](#).

19.4.2 Lexical scope

[Scope bound](#) by the [structure](#) of source code [where](#) the named entity is defined.

19.4.2.1 *

Static scope

19.4.3 Local scope

Scope applies only in (current) area.

19.4.3.1 *

Local

19.5 Shadowing

When in the local scope bigger scope variable overridden by same name variable from the local scope.

19.6 Syntactic sugar

Artificial way to make language easier to read and write.

19.7 System F

Is parametric polymorphism in programming.

Extends the Lambda calculus by introducing \forall (universal quantifier) over types.

19.7.1 *

Girard–Reynolds polymorphic lambda calculus Girard–Raynolds

19.8 Tail call

Final evaluation inside the function. Produces the function result.

19.9 Thunk

Not evaluated calculation. Can be dragged around, until be lazily evaluated.

19.10 Application memory

Table 19.1: Application memory structural parts

Storage of	Block name
All not currently processing data	Heap
Function call, local variables	Stack
Static and global variables	Static/Global
Instructions	Binary code

When even Main invoked - it work in Stack, and called Stack frame. Stack frame size for function calculated when it is compiled. When stacked Stack frames exceed the Stack size - stack overflow happens.

19.11 Turing machine

Mathematical model of computation that defines [abstract Turing machine](#). [Abstract](#) machine which manipulates symbols on a strip of tape, according to a table of rules.

19.11.1 Turing complete

[Set](#) of action rules that can simulate any [Turing machine](#).

19.11.1.1 *

Turing incomplete Turing incompleteness Turing completeness Computationally universal

19.12 REPL

Read-eval-print loop, aka interactive shell.

19.13 Domain specific language

Language design/fitted for particular [domain](#) of [application](#). Mainly should be [Turing incomplete](#), since general-purpose language implies [Turing completeness](#).

19.13.1 *

Domain-specific language DSL

19.13.2 Embedded domain specific language

[DSL](#) used inside outer language.

Two levels of embedding:

- Shallow: [DSL](#) translates into Haskell directly
- Deep: Between [DSL](#) and Haskell there is a [data structure](#) that reflects the [expression](#) tree, AKA stores the [syntax tree](#).

19.13.2.1 *

eDSL

19.14 Data structure

19.14.1 Cons cell

Cell that values may [inhabit](#).

19.14.2 Construct

`(:) :: a -> [a] -> [a]`

19.14.2.1 *

Cons

19.14.3 Leaf

-

19.14.4 Node

```

*
/ \

```

19.14.5 Spine

Is a [chain](#) of memory cells, each points to the both value of element and to the next memory cell.

Array:

```

      :
    / \
1     :
    / \
  2     :
    / \
  3     []

```

1:2:3: []

Spine:

```

      :
    / \
-     :
    / \
-     :
    / \
-     []

```

Chapter 20

Graph theory

20.1 Successor

[Object](#) that receives the [arrow](#).

20.1.1 Direct successor

Immediate [successor](#).

20.2 Predecessor

[Object](#) that sends [arrow](#).

20.2.1 Direct predecessor

Immediate [predecessor](#).

20.3 Degree

Number of [arrows](#) of [object](#).

20.3.1 Indegree

Number of ingoing [arrows](#).

20.3.2 Outdegree

Number of outgoing [arrows](#).

20.4 Adjacency matrix

Matrix of connection of objects $\{-1, 0, 1\}$.

20.4.0.1 InstanceSigs

Allow adding [type](#) signatures to [type class function](#) instance [declaration](#).

20.5 Strongly connected

If every vertex in a graph is reachable from every other vertex.

It is possible to find all **strongly connected components** (and that way also test graph for strong connectivity), in **linear** time ($\Theta(V+E)$).

Binary relation of being **strongly connected** is an **equivalence relation**.

20.5.1 *

Strongly-connected

20.5.2 Strongly connected component

Full **strongly connected** subgraph of some graph.

* of a directed graph G is a subgraph that is **strongly connected**, and has **property**: no additional edges or vertices from G can be included in the subgraph without breaking its **property** of being **strongly connected**.

20.5.2.1 *

SCC Strongly connected components Strongly-connected component Strongly-connected components

Chapter 21

Tagless-final

Method of embedding [eDSL](#) in a typed functional host language (Haskell). [Alternative](#) to the embedding as a (generalized) [algebraic data type](#). For parsers of DLS [expressions](#): (1/partial) evaluator, compiler, pretty printer, multi-pass optimizer.

* embedding is writing [denotational semantics](#) for the [DSL](#) in the host language.

Approach can be used [iff eDSL](#) is typed. Only well-typed terms become embeddable, and host language can implemen also a [eDSL type](#) system. Approach that [eDSL](#) code interpretations are [type](#)-preserving.

One of main pros of * - extensibility: implementation of [DSL](#) can be used to analyze/evaluate/transform/pretty-print/compile and interpreters can be extended to more passes, optimizations, and new versions of [DSL](#) while keeping/using/reusing the old versions.

Example fields of [application](#): language-integrated queries, non-deterministic & probabilistic programming, delimiter continuation, computability theory, [stream](#) processing, hardware description languages, generation of specialized numerical kernels, [semantics](#) of natural language.

Chapter 22

Prefix notation

Operators then their operands.

22.1 *

Polish notation PN

22.2 Postfix notation

Operands then their operation.

22.3 *

Reverse Polish notation PRN

Part III

Give definitions

Chapter 23

Identity type

Chapter 24

Constant type

Chapter 25

Gen

Chapter 26

Tensorial strength

Chapter 27

Strong monad

Chapter 28

Weak head normal form

28.1 *

WHNF

Chapter 29

Function image

29.1 *

Image

Chapter 30

Invertible

Chapter 31

Invertibility

Chapter 32

Define LANGUAGE pragma options

32.1 ExistentialQuantification

32.2 GADTs

GADT is a generalization over parametric [algebraic data types](#) which allow explicitly denote the [types](#) ([type](#) matching) of the [constructors](#) and define [data types](#) using pattern matching on the left side of "data" [statements](#).

32.3 *

GADT Generalized algebraic data type First-class phantom data type Guarded recursive data type Equality-qualified data type

32.4 GeneralizedNewTypeClasses

32.5 FuncitonalDependencies

Chapter 33

GHC check keys

33.1 -Wno-partial-type-signatures

Supresses [PartialTypeSignatures wildcard infer](#) warning.

Chapter 34

Generalised algebraic data types

LANGUAGE [GADTs](#)

34.1 *

GADT

Chapter 35

Order theory

Investigates in the depth the intuitive notion of [order](#) using [binary relations](#).

35.1 Domain theory

Formalizes approximation and convergence. Has close [relation](#) to Topology.

35.2 Lattice

[Partially ordered set](#) in which any two elements have unique supremum and infimum.

$$P = (X, \leq), \forall \{x_1, x_2\} \in X : \exists! \{inf, sup\}(\{x_1, x_2\})$$

$$x \vee (y \wedge x) = (x \vee y) \wedge x = x$$

Most of [partially ordered sets](#) are not lattices.

35.3 Order

35.3.1 Preorder

$$R^X \rightarrow X : \text{Reflexive \& Transitive: } aRa, aRb, bRc \Rightarrow aRc$$

Generalization of [equivalence relations](#) [partial orders](#).

* [Antisymmetric](#) \Rightarrow Partial ordering, * [Symmetric](#) \Rightarrow [Equivalence](#).

35.3.1.1 *

Preordered

35.3.1.2 Total preorder

$$\forall a, b : a \leq b \vee b \leq a \Rightarrow \text{Total Preorder.}$$

35.3.2 Partial order

A [binary relation](#) must be [reflexive](#), [antisymmetric](#) and [transitive](#).

Partial - not every elements between them need to be comparable.

Good example of $*$ is a genealogical descendency. Only related people produce [relation](#), not related do not.

35.3.2.1 $*$

Partial orders Partially ordered set Partially ordered sets Poset Posets

35.3.3 Total order

35.3.4 Chain

Totally ordered [set](#), aka [sequence](#).

Chapter 36

Universal algebra

Studies [algebraic structures](#).

Chapter 37

Relation

37.1 Reflexivity

$R^{X \rightarrow X}, \forall x \in X : xRx$ **Order** theory: $a \leq a$

* - each element is comparable to itself.

Corresponds to **Identity** and **Automorphism**.

37.1.1 *

Reflexive Reflexive relation

37.2 Irreflexivity

$R^{X \rightarrow X}, \forall x \in X : \neg R(x, x)$

37.2.1 *

Anti-reflexive Anti-reflexive relation Irreflexive Irreflexive relation

37.3 Transitivity

$\forall a, b, c \in X, \forall R^{X \rightarrow X} : (aRb \wedge bRc) \Rightarrow aRc$

* - the start of a **chain** of **precedence relations** must precede the end of the **chain**.

37.3.1 *

Transitive Transitive relation

37.4 Symmetry

$\forall a, b \in X : (aRb \iff bRa)$

37.4.1 *

Symmetric Symmetric relation

37.5 Equivalence

Reflexive	Symmetric	Transitive
$\forall x \in X, \exists R : xRx$ $a = a$	$\forall a, b \in X : (aRb \iff bRa)$ $a = b \iff b = a$	$\forall a, b, c \in X, \forall R^{X \rightarrow X} : (aRb \wedge bRc) \Rightarrow aRc$ $a = b, b = c \Rightarrow a = c$

37.5.1 *

Equivalent Equivalent relation

37.6 Antisymmetry

$\forall a, b \in X : aRb, bRa \Rightarrow a = b \sim aRb, a \neq b \Rightarrow \nexists bRa$. **Antisymmetry** does not say anything about $R(a, a)$.

* - no two different elements precede each other.

37.6.1 *

Antisymmetric Antisymmetric relation

37.7 Asymmetry

$\forall a, b \in X (aRb \Rightarrow \neg(bRa)) \iff \text{Antisymmetric} \wedge \text{Irreflexive}$. **Asymmetry** \neq "not symmetric"
Symmetric \wedge **Asymmetric** is only empty relation.

37.7.1 *

Asymmetric Asymmetric relation

Chapter 38

Cryptomorphism

[Equivalent](#), interconvertable with no loss of information.

38.1 *

Crypromorphic

Chapter 39

Lexically scoped type variables

Enable [lexical scope](#) for [forall quantifier](#) defined [type variables](#)

Implemented in [ScopedTypeVariables](#)

Chapter 40

Abstract data type

Several definitions here, reduce them.

Data type mathematical model, defined by its **semantics** from the user point of view, listing possible values, operations on the data of the **type**, and behaviour of these operations.

* class of **objects** whose logical behaviour is defined by a **set** of values and **set** of operations (analogue to **algebraic structure** in mathematics).

A specification of a **data type** like a **stack** or queue **where** the specification does not contain any implementation details at all, only the operations for that **data type**. This can be thought of as the contract of the **data type**.

40.1 *

AbsDT

Chapter 41

Functional dependencies

Chapter 42

MonoLocalBinds

Chapter 43

KindSignatures

Chapter 44

ExplicitNamespaces

Chapter 45

Combinator pattern

Chapter 46

Symbolic expression

Nested tree [data structure](#).

Introduced & used in Lisp. Lisp code and data are *.

* in Lisp: Atom or [expression](#) of the form (x . y), x and y are *.

Modern abbreviated notation of *: (x y).

46.1 *

S-expression S-expressions Sexpression Sexpressions Sexp Sexps Sexpr Sexprs

Chapter 47

Polynomial

Expression consisting of:

- **variables**
- coefficients
- addition
- subtraction
- multiplication (including positive integer **variable** exponentiation)

Polynomials form a **ring**. **Polynomial ring**.

47.1 *

Polynomials

Chapter 48

Data family

Indexed form of data and newtype definitions.

Chapter 49

Type synonym family

Indexed form of [type](#) synonyms.

Chapter 50

Indexed type family

* additional structure in language that allows ad-hoc overloading of [data types](#). AKA are to [types](#) as [type class](#) to methods.

Varieties:

- [data family](#)
- [type](#) synonym families

Defined by pattern matching the partial [functions](#) between [types](#). Associates [data types](#) by [type-level function](#) defined by open-ended collection of valid instances of input [types](#) and corresponding output [types](#).

Normal [type classes](#) define partial [functions](#) from [types](#) to a collection of named values by pattern matching on the input [types](#), while [type](#) families define partial [functions](#) from [types](#) to [types](#) by pattern matching on the input [types](#). In fact, in many uses of [type](#) families there is a single [type class](#) which logically contains both values and [types](#) associated with each instance. A [type family](#) declared inside a [type class](#) is called an associated [type](#).

50.1 *

Type family

Chapter 51

TypeFamilies

Allow use and definition of indexed [type](#) families and data families.

* are [type](#)-level programming. * are overload [data types](#) in the same way that [type classes](#) overload [functions](#). * allow handling of [dependent types](#). Before it [Functional dependencies](#) and [GADTs](#) were used to solve that. * useful for generic programming, creating highly parametrised interfaces for libraries, and creating interfaces with enhanced static information (much like [dependent types](#)).

Implies: [MonoLocalBinds](#), [KindSignatures](#), [ExplicitNamespaces](#)

Two [types](#) of * are:

Chapter 52

Error

Mistake in the program that can be resolved only by fixing the program.

`error` is a sugar for `undefined`.

Distinct from [Exception](#).

52.1 *

Errors

Chapter 53

Exception

Expected but irregular situation.

Distinct from [Error](#). Also see [106](#)

53.1 *

Exceptions

Chapter 54

ConstraintKinds

`Constraints` are just handled as `types` of a particular `kind` (`Constraint`). Any `type` of the `kind` `Constraint` can be used as a `constraint`.

- Anything which is already allowed in code as a `constraint` without `*`. Saturated applications to `type` `classes`, implicit `parameter` and equality `constraints`.
- `Tuples`, all of whose component `types` have `kind` `Constraint`.

```
type Some a = (Show a, Ord a, Arbitrary a) -- is of kind Constraint.
```

- Anything form of which is not yet known, but the user has declared for it to have `kind` `Constraint` (for which they need to `import` it from `GHC.Exts`):

```
Foo (f :: Type -> Constraint) = forall b. f b => b -> b -- is allowed
-- as well as examples involving type families:
type family Typ a b :: Constraint
type instance Typ Int b = Show b
type instance Typ Bool b = Num b

func :: Typ a b => a -> b -> b
func = ...
```

Chapter 55

Specialisation

Turns [ad hoc polymorphic function](#) into compiled [type](#)-specific implementations.

55.1 *

Specialise Specialize Specialization

Chapter 56

Diagram

For [categories](#) \mathcal{C} and \mathcal{J} , a [diagram](#) of [type](#) \mathcal{J} in \mathcal{C} is a [covariant functor](#) $D : \mathcal{J} \rightarrow \mathcal{C}$.

Chapter 57

Category theoretical presheaf

For categories C and J , a J -presheaf on C is a contravariant functor $D : C \rightarrow J$.

Chapter 58

Topological presheaf

If X is a topological space, then the open sets in X form a partially ordered set $\text{Open}(X)$ under inclusion. Like every partially ordered set, $\text{Open}(X)$ forms a small category by adding a single arrow $U \rightarrow V$ if and only if $U \subseteq V$. Contravariant functors on $\text{Open}(X)$ are called presheaves on X . For instance, by assigning to every open set U the associative algebra of real-valued continuous functions on U , one obtains a presheaf of algebras on X .

Chapter 59

Diagonal functor

The **diagonal functor** is defined as the **functor** from D to the **functor category** D^C which sends each **object** in D to the **constant functor** at that **object**.

Chapter 60

Limit functor

For a fixed index [category](#) J , if every [functor](#) $J \rightarrow C$ has a limit (for instance if C is complete), then the [limit functor](#) $C^J \rightarrow C$ assigns to each [functor](#) its limit. The existence of this [functor](#) can be proved by realizing that it is the right-adjoint to the [diagonal functor](#) and invoking the Freyd adjoint [functor](#) theorem. This requires a suitable version of the [axiom of choice](#). Similar remarks [apply](#) to the colimit [functor](#) (which is [covariant](#)).

Chapter 61

Dual vector space

The map which assigns to every vector space its [dual](#) space and to every [linear](#) map its [dual](#) or transpose is a [contravariant functor](#) from the [category](#) of all vector spaces over a fixed field to itself.

Chapter 62

Fundamental group

Consider the [category](#) of pointed topological spaces, i.e. topological spaces with distinguished points. The [objects](#) are pairs (X, x_0) , [where](#) X is a topological space and x_0 is a point in X . A [morphism](#) from (X, x_0) to (Y, y_0) is given by a continuous map $f : X \rightarrow Y$ with $f(x_0) = y_0$.

To every topological space X with distinguished point x_0 , one can define the [fundamental group](#) based at x_0 , denoted $\pi_1(X, x_0)$. This is the [group](#) of [homotopy](#) classes of loops based at x_0 . If $f : X \rightarrow Y$ is a [morphism](#) of pointed spaces, then every loop in X with base point x_0 can be [composed](#) with f to yield a loop in Y with base point y_0 . This [operation](#) is compatible with the [homotopy equivalence relation](#) and the [composition](#) of loops, and we get a [group homomorphism](#) from $\pi_1(X, x_0)$ to $\pi_1(Y, y_0)$. We thus obtain a [functor](#) from the [category](#) of pointed topological spaces to the [category](#) of [groups](#).

In the [category](#) of topological spaces (without distinguished point), one considers [homotopy](#) classes of generic curves, but they cannot be [composed](#) unless they share an endpoint. Thus one has the fundamental groupoid instead of the [fundamental group](#), and this construction is [functorial](#).

Chapter 63

Algebra of continuous function

A [contravariant functor](#) from the [category](#) of topological spaces (with continuous maps as [morphisms](#)) to the [category](#) of real [associative algebras](#) is given by assigning to every topological space X the [algebra](#) $C(X)$ of all real-valued continuous [functions](#) on that space. Every continuous map $f : X \rightarrow Y$ induces an [algebra homomorphism](#) $C(f) : C(Y) \rightarrow C(X)$ by the rule $C(f)(\varphi) = \varphi \circ f$ for every φ in $C(Y)$.

Chapter 64

Tangent and cotangent bundle

The map which sends every differentiable manifold to its tangent bundle and every smooth map to its derivative is a [covariant functor](#) from the [category](#) of differentiable manifolds to the [category](#) of vector bundles.

Doing this constructions pointwise gives the tangent space, a [covariant functor](#) from the [category](#) of pointed differentiable manifolds to the [category](#) of real vector spaces. Likewise, cotangent space is a [contravariant functor](#), essentially the [composition](#) of the tangent space with the [dual](#) space above.

Chapter 65

Group action / representation

Every **group** G can be considered as a **category** with a single **object** whose **morphisms** are the elements of G . A **functor** from G to **Set** is then **nothing** but a **group** action of G on a particular **set**, i.e. a **G -set**. Likewise, a **functor** from G to the **category** of vector spaces, Vect_K , is a **linear** representation of G . In general, a **functor** $G \rightarrow C$ can be considered as an "action" of G on an **object** in the **category** C . If C is a **group**, then this action is a **group homomorphism**.

Chapter 66

Lie algebra

Assigning to every real (complex) Lie [group](#) its real (complex) [Lie algebra](#) defines a [functor](#).

Chapter 67

Tensor product

If \mathcal{C} denotes the [category](#) of vector spaces over a fixed field, with [linear](#) maps as [morphisms](#), then the [tensor product](#) $V \otimes W$ defines a [functor](#) $\mathcal{C} \times \mathcal{C} \rightarrow \mathcal{C}$ which is [covariant](#) in both arguments.

Chapter 68

Forgetful functor

The functor $U : \mathbf{Grp} \rightarrow \mathbf{Set}$ which maps a group to its underlying set and a group homomorphism to its underlying function of sets is a functor.^[8] Functors like these, which "forget" some structure, are termed forgetful functors. Another example is the functor $\mathbf{Rng} \rightarrow \mathbf{Ab}$ which maps a ring to its underlying additive abelian group. Morphisms in \mathbf{Rng} (ring homomorphisms) become morphisms in \mathbf{Ab} (abelian group homomorphisms).

Chapter 69

Free functor

Going in the opposite direction of [forgetful functors](#) are free [functors](#). The [free functor](#) $F : \mathbf{Set} \rightarrow \mathbf{Grp}$ sends every [set](#) X to the free [group](#) generated by X . [Functions](#) get mapped to [group](#) homomorphisms between free [groups](#). Free constructions exist for many [categories](#) based on structured [sets](#). See [free object](#).

Chapter 70

Homomorphism group

To every pair A, B of abelian groups one can assign the abelian group $\text{Hom}(A, B)$ consisting of all group homomorphisms from A to B . This is a functor which is contravariant in the first and covariant in the second argument, i.e. it is a functor $\text{Ab}^{\text{op}} \times \text{Ab} \rightarrow \text{Ab}$ (where Ab denotes the category of abelian groups with group homomorphisms). If $f : A_1 \rightarrow A_2$ and $g : B_1 \rightarrow B_2$ are morphisms in Ab , then the group homomorphism $\text{Hom}(f, g) : \text{Hom}(A_2, B_1) \rightarrow \text{Hom}(A_1, B_2)$ is given by $\varphi \mapsto g \circ \varphi \circ f$. See Hom functor.

Chapter 71

Representable functor

We can generalize the previous example to any category C . To every pair X, Y of objects in C one can assign the set $\text{Hom}(X, Y)$ of morphisms from X to Y . This defines a functor to \mathbf{Set} which is contravariant in the first argument and covariant in the second, i.e. it is a functor $C^{\text{op}} \times C \rightarrow \mathbf{Set}$. If $f : X_1 \rightarrow X_2$ and $g : Y_1 \rightarrow Y_2$ are morphisms in C , then the group homomorphism $\text{Hom}(f, g) : \text{Hom}(X_2, Y_1) \rightarrow \text{Hom}(X_1, Y_2)$ is given by $\varphi \mapsto g \circ \varphi \circ f$.

Functors like these are called representable functors. An important goal in many settings is to determine whether a given functor is representable.

Chapter 72

Corecursion

Chapter 73

Coinduction

proper definition

* [dual](#) to induction. Generalises to [corecursion](#).

Chapter 74

Initial algebra of an endofunctor

Chapter 75

Terminal coalgebra for an endofunctor

Chapter 76

Continuation

76.1 Continuation passing style

76.1.1 *

CPS

Chapter 77

Control.Concurrent.Async

Good library for concurrency programming.

Chapter 78

Semilattice

Part IV

Citation

"One of the finer points of the Haskell community has been its propensity for recognizing [abstract](#) patterns in code which have well-defined, lawful representations in mathematics." (Chris Allen, Julie Moronuki - "Haskell Programming from First Principles" (2017))

Part V

Good code

Chapter 79

Good: Type aliasing

Use [data type](#) aliases to deferentiate logic of values.

Chapter 80

Good: Type wideness

Wider the [type](#) the more it is [polymorphic](#), means it has broader [application](#) and fits more [types](#).

The more constrained system has more usefulness.

Unconstrained means most flexible, but also most useless.

Chapter 81

Good: Print

```
print :: Show a => a -> IO ()  
print a = putStrLn (show a)
```

Chapter 82

Good: Fold

`foldr` [spine recursion](#) intermediated by the folding. Can terminate at any point. `foldl` [spine recursion](#) is unconditional, then folding starts. Unconditionally recurses across the whole [spine](#), if it infinite - infinitely.

Chapter 83

Good: Computation model

Model the [domain](#) and [types](#) before thinking about how to write computations.

Chapter 84

**Good: Make bottoms only
local**

Chapter 85

Good: Newtype wrap is ideally transparent for compiler and does not change performance

Chapter 86

Good: Instances of types/type classes must go with code you write

Chapter 87

**Good: Functions can be
abstracted as arguments**

Chapter 88

**Good: Infix operators can be
bind to arguments**

Chapter 89

Good: Arbitrary

Product types can be tested as a product of random generators. Sum types require to implement generators with separate constructors, and picking one of them, use oneof or frequency to pick generators.

Chapter 90

Good: Principle of Separation of concerns

Chapter 91

Good: Function composition

In Haskell inline [composition](#) requires:

```
h.g.f $ i
```

[Function application](#) has a higher [priority](#) than [composition](#). That is why parentheses over [argument](#) are needed. This [precedence](#) allows idiomatically [compose partially applied functions](#).

But it is a way better then:

```
h (g (f i))
```

Chapter 92

Good: Point-free

Use `Tacit` very carefully - it hides `types` and harder to change code `where` it is used. Use just enough `Tacit` to communicate a bit better. Mostly only partial `point-free` communicates better.

92.1 Good: Point-free is great in multi-dimensions

BigData and OLAP analysis.

Chapter 93

Good: Functor application

Function application on n levels beneath:

```
(fmap . fmap) function twoLevelStructure
```

How `fmap . fmap` typechecks:

```
(.)      :: (b -> c) -> (a -> b) -> a -> c
fmap     :: Functor f => (m -> n) -> f m -> f n
fmap     :: Functor g => (x -> y) -> g x -> g y

fmap . fmap :: (Functor f, Functor g)
            => ((g x -> g y) -> f . g x -> f . g y)
            -> (( x -> y) -> g x -> g y)
            -> ( x -> y) -> f . g x -> f . g y
fmap . fmap :: (x -> y) -> f . g x -> f . g y
```

Chapter 94

Good: Parameter order

In [functions parameter order](#) is important. It is best to use first the most reusable [parameters](#). And as last one the one that can be the most [variable](#), that is important to [chain](#).

Chapter 95

Good: Applicative monoid

There can be more than one valid `Monoid` for a `data type`. && There can be more than one valid `Applicative` instance for a `data type`. -> There can be different `Applicatives` with different `Monoid` implementations.

Chapter 96

Good: Creative process

- 96.1 Pick philosophy principles one to three the more - the harder the implementation
- 96.2 Draw the most blurred representation
- 96.3 Deduce **abstractions** and write remotely what they are
- 96.4 Model of computation
 - 96.4.1 Model the **domain**
 - 96.4.2 Model the **types**
 - 96.4.3 Think how to write computations
- 96.5 Create

Chapter 97

Good: About operators ($\langle \$ \rangle$) ($\langle * \rangle$) ($\langle \> \rangle$) ($\langle * \>$) ($\langle * \> \rangle$) ($\langle \> \> \rangle$)

Where character is not present - discard the according processing of a [parameter](#). ($\langle \> \rangle$) is an [exception](#), it does the reverse. ignores the first [parameter](#), in fact $\langle \> \rangle \equiv \langle * \rangle$.

$\langle * \> \equiv$ does the proper action: does calculation, but ignores the value from the first [argument](#).

Chapter 98

**Good: About functions like
{mapM, sequence}_**

Trailing `_` means ignoring the result.

Chapter 99

Good: Guideliles

99.1 Wiki.haskell

99.1.1 Documentation

99.1.1.1 Comments write in **application** terms, not technical.

99.1.1.2 Tell what code needs to do not how it does.

99.1.2 Haddock

99.1.2.1 Put haddock comments to ever exposed **data type** and **function**.

99.1.2.2 Haddock header

```
{- |  
Module      : <File name or $Header$ to be replaced automatically>  
Description : <optional short text displayed on contents page>  
Copyright   : (c) <Authors or Affiliations>  
License     : <license>  
  
Maintainer  : <email>  
Stability   : unstable | experimental | provisional | stable | frozen  
Portability : portable | non-portable (<reason>  
  
<module description starting at first column>  
-}
```

99.1.3 Code

99.1.3.1 Try to stay closer to portable (Haskell98) code

99.1.3.2 Try make lines no longer 80 chars

99.1.3.3 Last char in file should be newline

99.1.3.4 Symbolic **infix** identifiers is only library writer right

99.1.3.5 Every **function** does one thing.

Chapter 100

Good: Use Typed holes to progress the code

[Typed holes](#) help build code in complex situations.

Chapter 101

Good: Haskell allows infinite terms but not infinite types

That is why infinite `types` throw infinite `type error`.

Chapter 102

Good: Use type synonyms to differ the information

Even if there is `types` - define `type` synonyms. They are free. That distinction with synonyms, would allow `TypeSynonymInstances`, which would allow to create a different `type class` instances and behaviour for different information.

Chapter 103

**Good: Use `Control.Monad.Except`
instead of `Control.Monad.Error`**

Chapter 104

Good: Monad OR Applicative

104.0.1 Start writing **monad** using 'return', 'ap', 'liftM', 'liftM2', '»' instead of 'do', '»='

If you wrote code and really needed only those - move that code to **Applicative**.

```
return -> pure
ap -> <*>
liftM -> liftA -> <$>
>> -> *>
```

104.0.2 Basic **case** when **Applicative** can be used

Can be rewritten in **Applicative**:

```
func = do
  a <- f
  b <- g
pure (a, b)
```

Can't be rewritten in **Applicative**:

```
somethingdoSomething' n = do
  a <- f n
  b <- g a
pure (a, b)
```

(f n) creates **monadic structure**, **binds** ot to *a* wich is consumed then by *g*.

104.0.3 **Applicative** block vs **Monad** block

With **Type Applicative** every condition fails/succseeds independently. It needs a boilerplate **data constructor**/value pattern matching code to work. And code you can write only for so many cases and **types**, so boilerplate can not be so flexible as **Monad** that allows **polymorphism**. With **Type Monad** computation can return value that dependent from the previous computation result. So abort or dependent processing can happen.

Chapter 105

Good: Linear type

[Linear types](#) are great to control/minimize resource usage.

Chapter 106

Good: **Exception** vs **Error**

Many languages and Haskell have it all mixup. Here is table showing what belongs to one or other in standard libraries:

Exception	Prelude.catch, Control. Exception .catch, Control. Exception .try, IOError, Control. Monad.Error
Error	error , assert, Control. Exception .catch, Debug.Trace.trace

Chapter 107

Good: Let vs. Where

`let ... in ...` is a separate [expression](#). In contrast, `where` is [bound](#) to a surrounding syntactic [construct](#) (namespace).

Chapter 108

Good: RankNTypes

Can powerfully synergyze with [ScopedTypeVariables](#).

Chapter 109

Good: Handling orphan instance

Practice to address orphan instances:

Does `type class` or `type` defined by you:

Type class	Type	Recommendation
	✓	{ <code>Type</code> , instance} in the same <code>module</code>
✓		{ <code>Type class</code> & instance} in the same <code>module</code> {Define newtype wrap, its instances} in the same <code>module</code>

Chapter 110

Good: Smart constructor

Only proper smart [constructors](#) should be exported. Do not export [data type constructor](#), only a [type](#).

Chapter 111

Good: Thin category

In * all [morphisms](#) are [epimorphisms](#) and [monomorphisms](#).

Chapter 112

Good: Recursion

Writing/thinking about [recursion](#):

- a.* Find the base cases, om input of which the answer can be provided right away. There is mosly one [base case](#), but sometimes there can be several of them. Typical base cases are: [zero](#), the empty [list](#), the empty tree, null, etc.
- b.* Do inductive [case](#). The [recursive](#) invocation. The [argument](#) of a [recursive](#) call needs to be smaller then the current [argument](#). So it would be gradually closer to the [base case](#). The idea is that processes eventually hits the [base case](#).

Simple functional [application](#) is used in the [recursion](#). Assume that the [functions](#) would return the right result.

Chapter 113

Good: Monoid

<>: [Sets](#) - union. Maps - left-biased union. Number - Sum, Product form separate [monoid categories](#).

Chapter 114

Good: Free monad

The main [case](#) of usage of Free [monads](#) in Haskell:

Start implementation of the [monad](#) from a Free [monad](#), drafting the base [monadic](#) operations, then add custom operations.

Gradually build on top of Free [monad](#) and try to find homomorphisms from [monad](#) to [objects](#), and if only [objects](#) are needed - get rid of the free [monad](#).

Chapter 115

Good: Use mostly where clauses

Chapter 116

**Good: Where clause is in a scope
with function parameters**

Chapter 117

Good: Strong preference towards pattern matching over {head, tail, etc.} functions

head and tail and alike [functions](#) are often partial ([unsafe](#)) functions.

Chapter 118

Good: Patternmatching is possible on monadic bind in do

Example:

```
instance (Monad m) => Functor (StateT s m) where
  fmap f m = StateT $ \s -> do
    (x, s') <- runStateT m s  -- Here is a pattern matching bind
    return (f x, s')
```


Chapter 119

Good: Applicative vs Monad

Giving not Monad but Applicative requirement allows parallel computation, but if there should be a chaining of the intermediate state - it must be [monadic](#).

Chapter 120

Good: StateT, ReaderT, WriterT

Reader trait: (r ->).

Writer trait: (a, w).

State trait is combination of both:

```
newtype StateT s m a =  
  StateT { runStateT :: s -> m (a, s) }
```

```
newtype ReaderT r m a =  
  ReaderT { runReaderT :: r -> m a }
```

```
newtype WriterT w m a =  
  WriterT { runWriterT :: m (a, w) }
```

State trait fully replaces writer.

Chapter 121

Good: Working with MonadTrans and lift

From the `lift . pure = pure` follows that `MonadTrans` [type](#) can have a `pure` defined with `lift`.

Stacking of `MonadTrans` [monads](#) can result in a lot of chained `lift` and `unwraps`. There is many ways to cope with that but the most robust and common is to [abstract](#) representation with `newtype` on the `Monad` [stack](#). This can reduce caining or remove the manual [lifting](#) withing the [Monad](#). For perfect combination for contributors to be able to extend the code - keep the `Internal` [module](#) that has a raw representation.

Chapter 122

Good: Don't mix Where and Let

let and where create a [recursive set](#) of definitions with can explode, don't mix them together in code.

Chapter 123

Good: Where vs. Let

Let is self-recursive lazy pattern. It is checked and errors only at execution time. **Binds** only inside expression it is binded to.

Where is a part of definition, scoped over definition implemetations and guards, not self-recursive.

Chapter 124

Good: The proper nature algorithm that models behaviour of many objects is computation heavy

God does not care about our mathematical difficulties. He integrates empirically.

One who is found of mathematical meaning loves to [apply](#) it. But if we implement the "real" algorithms behind nature processes, we face the need to go through the computations of [properties](#) of all particles.

Computation of nature is always a middle way between ideal theory behaviour and computation simplification.

Chapter 125

Good: In Haskell parameters bound by lambda declaration instantiate to only one concrete type

Because of [let-bound polymorphism](#):

This is illegal in Haskell:

```
foo :: (Int, Char)
foo = (\f -> (f 1, f 'a')) id
```

Lambda-bound function (i.e., one passed as [argument](#) to another [function](#)) cannot be instantiated in two different ways, if there is a [let-bound polymorphism](#).

Chapter 126

Good: Instance is a good structure to draw a type line

Instances for data type can differentiate by constraints & types of arguments. So instance can preserve type boundary, and data type declaration can stay very polymorphic. If the need to extend the type boundaries arrives - the instances may extend, or new instances are created, while used data type still the same and unchanged.

Chapter 127

Good: MTL vs. Transformers

Default of mtl.

Transformers is [Haskell 98](#), doesn't have functional dependencies, lacks the [monad](#) classes, has manual [lift](#) of operations to the composite [monad](#).

MTL extends transformers, providing more instances, features and possibilities, may include [alternative](#) packages features as `mtl-tf`.

Part VI

Bad code

Chapter 128

Bad pragma

128.1 Bad: Dangerous **LANGUAGE pragma** option

- [DatatypeContexts](#)
- `OverlappingInstances`
- `IncoherentInstances`
- `ImpredicativeTypes`
- `AllowAmbiguousTypes`
- [UndecidableInstances](#) - often

Part VII

Useful **functions** to remember

Chapter 129

Prelude

```
enumFromTo
enumFromThenTo
reverse
show :: Show a => a -> String
flip
sequence - Evaluate each monadic action in the structure from left to right,
  ↪ and collect the results.
:sprint - show variables to see what has been evaluated already.
minBound - smaller bound
maxBound - larger bound
cycle :: [a] -> [a] - indefinitely cycle s list
repeat - indefinit lis from value
elemIndex e l - return first index, returns Maybe
fromMaybe (default if Nothing) e :: Maybe a -> a
lookup :: Eq a => a -> [(a, b)] -> Maybe b
```

129.1 Ord

compare

129.2 Calc

div - always makes rounding down, to infinity divMod - returns a tuple containing the result of integral division and modulo

129.3 List operations

```
concat - [ [a] ] -> [a]
elem x xs - is element a part of a list
zip :: [a] -> [b] -> [(a, b)] - zips two lists together. Zip stops when one
  ↪ list runs out.
zipWith :: (a -> b -> c) -> [a] -> [b] -> [c] - do the action on corresponding
  ↪ elements of list and store in the new list
```

Chapter 130

Data.List

`intersperse :: a -> [a] -> [a]` - gets the value and inserts it between values
↳ `in` array
`nub` - remove duplicates from the list

Chapter 131

Data.Char

```
ord (Char -> Int)
chr (Int -> Char)
isUpper (Char -> Bool)
toUpper (Char -> Char)
```

Chapter 132

QuickCheck

```
quickCheck :: Testable prop => prop -> IO ()
```

```
quickCheck . verbose - run verbose mode
```


Part VIII

Tool

Chapter 133

ghc-pkg

[List](#) installed packages:

```
ghc-pkg list
```

Chapter 134

Integration of NixOS/Nix with Haskell IDE Engine (HIE) and Emacs (Spacemacs)

134.1 1. Install the Cachix

Upstream doc: <https://github.com/cachix/cachix>

134.2 2. Installation of HIE

Upstream doc: <https://github.com/infinisil/all-hies/#cached-builds>

134.2.1 2.1. Provide cached builds

```
cachix use all-hies
```

134.2.2 2.2.a. Installation on NixOS distribution:

```
{ config, pkgs, ... }:
```

```
let
```

```
    all-hies = import (fetchTarball
    ↪ "https://github.com/infinisil/all-hies/tarball/master") {};
```

```
in {
```

```
    environment.systemPackages = with pkgs; [
```

```
        (all-hies.selection { selector = p: { inherit (p) ghc865 ghc864; }; })
```

```
    ];
```

```
}
```

Insert your GHC versions.

Switch to new configuration:

```
sudo -i nixos-rebuild switch
```

134.2.3 2.2.b. Installation with Nix package manager:

```
nix-env -iA selection --arg selector 'p: { inherit (p) ghc865 ghc864; }' -f  
↪ 'https://github.com/infinisil/all-hies/tarball/master'
```

Insert your GHC versions.

134.3 3. Emacs (Spacemacs) configuration:

```
dotspacemacs-configuration-layers  
'(  
  
  auto-completion  
  
  (lsp :variables  
    default-nix-wrapper (lambda (args)  
                          (append  
                            (append (list "nix-shell" "-I" "." "--command"  
↪ )  
                                (list (mapconcat 'identity args " ")))  
                            )  
                          (list (nix-current-sandbox))  
                          )  
    )  
  
    lsp-haskell-process-wrapper-function default-nix-wrapper  
  )  
  
  (haskell :variables  
    haskell-enable-hindent t  
    haskell-completion-backend 'lsp  
    haskell-process-type 'cabal-new-repl  
  )  
  
)  
  
dotspacemacs-additional-packages '(  
  direnv  
  nix-sandbox  
)  
  
(defun dotspacemacs/user-config ()  
  
  (add-hook 'haskell-mode-hook 'direnv-update-environment) ;; If direnv  
↪ configured  
  
)
```

Where:

auto-completion configures YASnippet.

nix-sandbox (<https://github.com/travisbhartwell/nix-emacs>) has a great helper functions. Using nix-current-sandbox function in default-nix-wrapper that used to properly configure lsp-haskell-process-wrapper-function.

Configuration of the lsp-haskell-process-wrapper-function default-nix-wrapper is a key

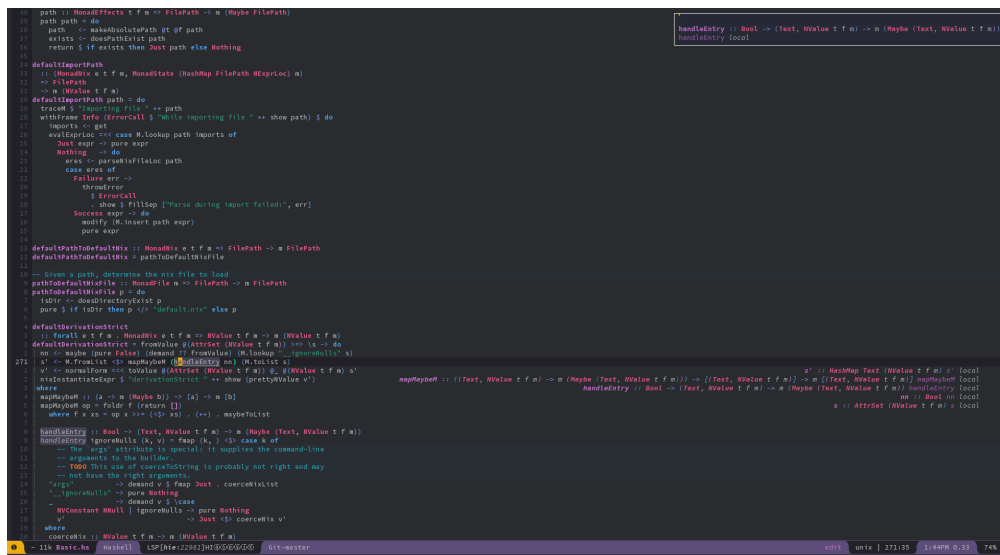
Configuration was reassembled from: <https://github.com/emacs-lsp/lsp-haskell/blob/8f2dbb6e827b1adce6360c56lsp-haskell.el#L57> & its authors config: `[[https://github.com/sevanspowell/dotfiles/blob/master.spacemacs]]/`

Refresh Emasc.

134.4 4. Open the Haskell file from a project

Open system monitor, observe the **process** of environment establishing, packages loading & compiling.

134.5 5. Be pleased writing code



Now, the powers of the Haskell, Nix & Emacs combined. It's fully in your hands now. Be cautious - you can change the world.

134.6 6. (optional) Debugging

- a. If receiving sort-of:

```
readCreateProcess : cabal-helper-wrapper failure
```

HIE tries to run cabal operations like on the non-Nix system. So it is a problem with detection of `nix-shell` environment, running inside it.

- a. If HIE keeps getting ready, failing & restarting - check that the projects `ghc --version` is declared in your `all-hie` NixOS configuration.

Chapter 135

GHC

135.1 GHC code check flags

Additional to default settings it is useful to use `-W`, `-Wcompat`. `-Wall` is for purists and would raise noise. They can be supplied in CLI as also in `.cabal ghc-option`. fr

`-W` turns on additional useful warnings:

- `-Wunused-binds`
- `-Wunused-matches`
- `-Wunused-foralls`
- `-Wunused-imports`
- `-Wincomplete-patterns`
- `-Wdodgy-exports`
- `-Wdodgy-imports`
- `-Wunbanged-strict-patterns`

`-Wall` turns on all warnings that indicate potentially suspicious code.

`-Weverything` turns on all warnings supported by compiler.

`-Wcompat` turns on warnings that will be enabled by default in the future GHC releases, allows library authors make the code compatible in advance for future GHC releases.

`-Werror` promotes warnings into fatal [errors](#), may be useful for CI runs.

`-w` turns off all warnings.

Chapter 136

GHCI

136.1 Debugging in GHCI

Provides:

- [set](#) a breakpoints
- observe step-by-step [evaluation](#)
- tracing mode

Breakpoints

```
:break 2
:show breaks
:delete 0
:continue
```

Step-by-step

```
:step main
```

[List](#) information at the breakpoint

```
:list
```

What been evaluated already

```
:sprint name
```

Chapter 137

GHCID

Commands to run the compile/check loop:

cabal > 3.0 command:

```
ghcid --command='cabal v2-repl --repl-options=-fno-code
↳ --repl-options=-fno-break-on-exception --repl-options=-fno-break-on-error
↳ --repl-options=-v1 --repl-options=-ferror-spans --repl-options=-j'
```

cabal < 3.0 command:

```
ghcid --command='cabal new-repl --ghc-options=-fno-code
↳ --ghc-options=-fno-break-on-exception --ghc-options=-fno-break-on-error
↳ --ghc-options=-v1 --ghc-options=-ferror-spans --ghc-options=-j'
```

nix-shell cabal > 3.0 command:

```
nix-shell --command 'ghcid --command="cabal v2-repl --repl-options=-fno-code
↳ --repl-options=-fno-break-on-exception --repl-options=-fno-break-on-error
↳ --repl-options=-v1 --repl-options=-ferror-spans --repl-options=-j" '
```

nix-shell cabal < 3.0 command:

```
nix-shell --command 'ghcid --command="cabal new-repl --ghc-options=-fno-code
↳ --ghc-options=-fno-break-on-exception --ghc-options=-fno-break-on-error
↳ --ghc-options=-v1 --ghc-options=-ferror-spans --ghc-options=-j" '
```


Chapter 138

runghc

Run Haskell code without first having to compile them.

Official tool in GHC package.

Chapter 139

Packaging

There is a number of good quality projects that export Cabal/Hackage to other packaging systems, big distribution systems and companies rely on them:

139.1 Cabal

- v1 generation of features used/uses own cabal (now legacy) methods of handling packages.
- v2 generation of features (current) uses Nix-like methods internally to handle packages.

Currently Cabal migrated to use of v2 generation by default.

Useful abilities:

`exec` - loads the GHC/GHCI env and launches the passed executable.

`haddock` - builds the documentaiton and places it into `v1 -> dist`, `v2 -> dist-newstyle` directories.

`sdist` - run a thorough [process](#), properly follow `.cabal` instructions, assemble mentioned files and generate a source distribution file `.tar.gz`.

`upload` - upload source distribution file to Hackage.

139.2 Nix

Peter Simmons ([peti](#)) - the main creator maintainer maintainer of the Haskell [stack](#) and packages ("package [set](#)") in [Nixpkgs](#). He is the central person that created most of the tooling and automation of importing Haskell into [Nixpkgs](#).

139.2.1 Nixpkgs

Besides documentation of [Nixpkgs](#) manual there is a [Nixpkgs](#) Haskell lib.

139.3 cabal2nix

Created/maintained by [peti](#).

This tool runs on one compiler version.

139.4 hackage2nix

Allows to clones info from Hackage and convert it into Nix language. Is developed/resides/embedded in cabal2nix project.

139.5 cabal2spec - Cabal to RPM

Also created and maintained by peti, he uses it for OpenSUSE.

139.6 nix-tools

Translates Cabals project description to a Nix [expression](#).

139.7 haskell.nix

Automatically translates Cabal/[Stack](#) project and dependencies into Nix code. Provides IFD ([import](#) from derivation) [functions](#) that minimize the amount of Nix code that is needed to be added. So it autogenerates Nix code hald way for your purposes.

Project of IOHK and has an active big respectable team.

Chapter 140

Emacs/Spacemacs

In Haskell programming spacemacs/jump-to-definition is your friend, `let` yourself - it will guide you.

My (Anton-Latukha's) Spacemacs configuration for Haskell as at: <https://github.com/Anton-Latukha/.spacemacs.d/blob/private/init.el>. Look there for a Haskell keyword, there is layer configuration, and the init boot config inside `(defun dotspacemacs/user-config ())`.

Chapter 141

Continuous integration platrorms (CIs) for Open Source Haskell projects

Since Open Source projects mostly use free tiers of CIs, and different CIs have different features - there is a [constant](#) flux of how to [construct](#) the best possible integration pipeline for Haskell projects.

The current state of affairs is best put in this quote:

Probably the biggest [constraint](#) is whether or not CI needs to test Windows or OS X, since build machines for those are harder to come by. We currently use AppVeyor for Windows builds and Travis for OS X builds since they are free. For Linux you can basically use any CI provider, but in this [case](#) I pay for a Linode VM which I use to host all Dhall-related infrastructure (i.e. all of the *.dhall-lang.org domains), so I reuse that to host Hydra for Nix-related CI so that I can use more parallelism and more efficient caching to test a wider range of GHC versions on a budget.

For [testing](#) OS X and Windows platforms we use [stack](#). The main reason we don't use Nix for [either](#) platform is that Nix only supports building release binaries on Linux (and even then it's still experimental).

So the basic summary I can give is:

For [testing](#) everything other than cross-platform support: Nix + Linux is best in my opinion ... because you get much more control and intelligent build caching, which is usually [where](#) most CI solutions fall short

For cross-platform support: [stack](#) + whatever CI provider provides free builds for that platform

Also, if you ever can pay for your own NixOS VM and you want to reuse the setup I built, you can find the NixOS configuration for dhall-lang.org here:

<https://github.com/dhall-lang/dhall-lang/tree/master/nixops>

Part IX

Library

Chapter 142

Exceptions

- 142.1 **Exceptions** - optionally **pure** extensible **exceptions** that are compatible with the mtl
- 142.2 **Safe-exceptions** - safe, simple API **equivalent** to the underlying implementation in terms of power, encourages best practices minimizing the chances of getting the **exception** handling wrong.
- 142.3 **Enclosed-exceptions** - capture **exceptions** from the enclosed computation, while reacting to asynchronous **exceptions** aimed at the calling thread.

Chapter 143

Memory management

143.1 membrain - [type](#)-safe memory units

Chapter 144

Parsers - megaparsec

Chapter 145

CLIs - optparse-applicative

Builds a shell API and parses those command line options.

Abilities:

- read & validate the arguments passed in any [order](#) to the command;
- handle and [report errors](#);
- generate and have comprehensive docs that help user;
- generate [context](#)-sensitive completions for 'bash', 'zsh', 'fish'.

Introduction (what library is for) Data model ([diagram](#)) – sometimes seeing at once is better than a thousand words of explanation Shortly describe [where](#) is spec'ing happens & belongs, [where](#) is parsing happens & belongs, [where](#) one can custom handle parsed data on top of what is provided in lib. So now readers roughly know the data model and what are [structural](#) parts and [where](#) they are

145.1 Modifiers {Attributes}

Settings that configure the builder.

- long - --key
- short - -k
- help - info that is put into docs. Does not affect the parsing.
- helpDoc - same as help, but with Doc [type](#) support.
- metavar - placeholder for the [argument](#) seen in the docs. Does not affect the parsing.
- value - value by default
- showdefault - in the docs
- hidden - hide from brief info
- internal - hide from descriptions
- style - [function](#) to [apply](#) to descriptions
- command - add command as a subparser option.

```
sample :: Parser Sometype
```

```
sample = subparser $ command "hello" $ info hello $ progDesc "Show greeting"
```

Compose them with `<>`.

Example:

```
( long "example"
<> short 'e'
<> metavar "ARGUMENT_HERE"
<> value "defaultVal"
<> showdefault
<> help "This would produce --example and -e keys for this parser."
      <> "It has defaultVal if key was not used."
      <> "And it would show default value in help message")
```

This `monoid` (`Mod f a`) should be given to according builder that accepts it.

145.2 Builders

Builders are the primitive atomic parsers of the library.

`command` `argument` `--option` `optionArgument`

~`argument` `ReadM a -> Mod ArgumentFields a -> Parser a`~ General implementation that uses given reader to parse direct `argument`.

~`strArgument` `IsString s => Mod ArgumentFields s -> Parser s`~ To consume a string `argument` directly.

~`option` `ReadM a -> Mod OptionFields a -> Parser a`~ General implementation. Allows to use the given reader.

~`flag` `a {default value} -> a {active value} -> Mod FlagFields a {option modifier} -> Parser a`~ `Irrefutable` \Rightarrow no termination for some or many, for them use `flag'`.

~`switch` `Mod FlagFields Bool -> Parser Bool`~ Macro for Boolean flag:

```
switch = flag False True
```

`Irrefutable` \Rightarrow no termination for some or many, for them use `flag'`

~`flag'` `a {active value} -> Mod FlagFields a {option modifier} -> Parser a`~ Flag parser without a default value. Has sence in composite parser, or when requiring `--on` OR `--off` alternatives.

~`infoOption` `String -> Mod OptionFields (a -> a) -> Parser (a -> a)`~ Always stops `binary` and displays a message.

~`strOption` `IsString s => Mod OptionFields s -> Parser s`~ Taking a String `argument`.

~`abortOption` `ParseError -> Mod OptionFields (a -> a) -> Parser (a -> a)`~ Always fails immediately.

~`subparser` `Mod CommandFields a -> Parser a`~ Command parser. The command modifier can be used to specify individual commands.

145.3 Parsers

Definitions (if there are needed) How parsers are `composed` from attributes and builders Examples (if there are needed) Option readers Running a parser

145.4 Composing and more complex parsers

Definitions (if there are needed) `Applicative` on parsers Examples of the use of parsers in the program and how they tie with surrounding `data types Alternative` Then mention `where` and how to customize even

over that and example

145.5 **Error** handling

145.6 Shell expansion

... Rename "How it works" into "How library internally implemented"

Chapter 146

HTML - Lucid

Chapter 147

Web applications - Servant

Chapter 148

IO libraries

148.1 Conduit - practical, monolythic, guarantees termination return

148.2 Pipes + Pipes Parse - modular, more primitive, theoretically driven

Chapter 149

JSON - aeson

Chapter 150

Backpack

On 1-st compilation - * analyzes the [abstract](#) signatures without loading side modules, doing the [type check](#) with assumption that modules provide right [type](#) signatures, the [process](#) does not emit any [binary](#) code and stores the intermediate code in a special form that allows flexibly connect modules provided. Which allows later to compile project with particular instantiations of the modules. Major work of this [process](#) being done by internal Cabal * support and * system that modifies the intermediate code to fit the [module](#).

Chapter 151

DSL

151.1 **"Ivory"** - **eDSL**, safe systems programming, effectively produce C code

Part X

Draft

Chapter 152

Exception handling

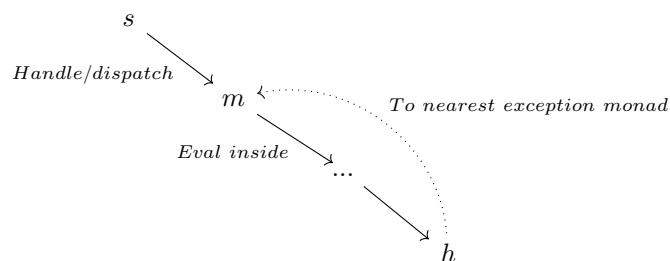
Process of **exception** handling has:

- raising an **exception**
- gathering information and handling an **exception**
- ability to finish important sessions/actions independently of whether **exception** happened or not. That is why it is called guaranteed finalization of important processes.

Exceptions and their handling are for the boundaries that receive external things that are not under Haskell control. It is mainly an **IO** handling. The **exception** mechanism may be used for internal **pure** Haskell part - if it grew too complex to sort-out some situation try/catch mechanism can be used, but then avoid use of runtime system **exceptions** catch and sort programmically and generally avoid it.

It's better to promote **exceptions** to just checking preconditions.

Wrapper with **exception** handler around **function** (**f**) call means that all untreated **exception** of **function** or its subfunctions would be caught by this wrapper into the **scope where** wrapper was used (one syntactic level above **function f**).



Any **monad** that short-circuits after some condition check of first **argument** - has **exception** handling potential.

Laziness as **exceptions** are computations - means that some issues would be skipped altogether, in parts that are/were not used would never throw **exceptions**, but also just as computations - **exceptions** would be raised at different times and states during computations.

Exception throw breaks **purity**, **function** was called but returned a result.

Try to raise and resolve all **exceptions** before acquiring external **IO** resources. And release all resources when or before the exception can happen.

With concurrency thread could be killed by other threads (that is called to raise an asynchronous **exception** in the thread).

152.1 Ideal catching

- Choose what [exceptions](#) to catch. Selection depends on the [type](#).
- No execution of continuation after throw, only handling.
- Handle $\{,a\}$ synchronous [exceptions](#).

152.2 Control.Exception.Safe main sets of functions

- `try*` - allows handle [Either](#) returning [types](#), bridges the [exception](#) handling and basic Haskell computation.
- `handle*` - describes how to handle [exception](#) before the [monadic](#) action itself.
- `catch*` - describes how to handle the [exception](#) after the [monadic](#) action itself.

For asynchronous [exceptions](#) there are special [function](#) to catch them: `catchAsync` and `handleAsync`.

`catch` and `handle` are to catch specific [exception type](#).

`catches`, `catchesDeep` and `catchesAsync` allows to catch matching an elements in the [list](#), and then handle them.

152.3 Clean-up of actions/resources

- `bracket*` - computations to acquire and release resource and computation to run in between.
- `finally` - allows to run declared computations afterward (even if an [exception](#) was raised).
- `onException` - run computations only if [exception](#) happened.

152.4 Ideal model

- ☒ [Exception](#) must include all [context](#) information that may be useful.
- ☒ Store information in a form for further probable deeper automatic diagnostic.
- ☒ Sensitive data/dummies for it - can be useful during development.
- ☒ Sensitive data should be stripped from a program logging & [exceptions](#).
- ☒ [Exception](#) system should be extendable, data storage & representation should be easily extendable.
- ☒ [Exception](#) system should allow easy exhaustive checking of [errors](#), since the different [errors](#) can happen.
- ☒ [Exception](#) system should be automatically well-documented and transparent.
- ☒ [Exception](#) system should have controllable breaking changes downstream.
- ☒ [Exception](#) system should allow complex composite ([sets](#)) [exceptions](#).
- ☒ [Exception](#) system should be lightweight on the [type](#) signatures of other [functions](#).
- ☒ [Exception](#) system should automate the collection of [context](#) for a [exception](#).
- ☒ [Exception](#) system should have [properties](#) and according [functions](#) for particular [types](#) of [errors](#).

`String` is simple and convinient to throw [exception](#), but really a mistake because it the most cumbersome choise:

- ☒ Any [Exception](#) instance can be converted to a `String` with [either](#) `show` or `displayException`.

- ☐ Does not include key debugging information in the **error** message.
- ☐ Does not allow developer to access/manage the **Exception** information.
- ☐ **Exception** messages need to be constructed ahead of time, it can not be internationalized, converted to some data/file format.
- ☐ **Exception** can have a sensitive information that can be useful for developer during work, but should not be logged/shown to end-user. Stripping it from **Strings** in the changing project is a hard task.
- ☐ Impossible to rely on this representation for further/deeper inspection.
- ☐ Impossible to have exhaustive checking - no knowledge no check, no warning if some cases are not handled.

152.5 Universal **exception type**

- ☒ Able to inspect every possible **error case** with **pattern match**.
- ☒ Self-documenting. Shows the hierarchical system of all **exceptions**.
- ☒ Transparent. Ability to discern in current situation what **exceptions** can happen
- ☐ New **exception constructor** causes breaking change to downstream.
- ☐ Wrongly implies completeness. Untreated **Errors** can happen, different **exception** can arrive from the outside code.

Sum **type** must be separate, and **product type structure** over it. Separate **exception type** of

152.6 Individual **exception types**

- ☒ Writing & seing & working with exactly what will go wrong because there is only one possible **error** for this **type of exception**. **Pattern match** happens only onconditions, **constructors** that should happen.
- ☒ Knowledge what exactly goes wrong allows wide usage of **Either**.
- ☐ It is hard to handle complex **exceptions** in the unitary system. Real wrorld can return not a particular **case**, but a **set** of cases {**object** not found, path is unreachable, access is denied}.
- ☐ **Type** signatures grow, and even can become complex, since every **case of exception** has its own **type**.
- ☐ Impure **throw** that users can/should use for your code must account for all your **exception types**.

152.7 **Abstract exception type**

Exception type entirely opaque and inspectable only by accessor **functions**.

- ☒ Updating the internals without breaking the API
- ☒ Semi-automates the **context of exception** with passing it to accessors.
- ☒ Predicates can be **applied** to more than one **constructor**. Which are **properties** that allows to make complex **exceptions** much easier to handle.
- ☐ Not self-documenting.
- ☐ Possible options by design are hidden from the downstream, documentation must be kept.
- ☐ When you change the **exception** handling/throwing **errors** it does not shows to the downstream.

152.8 Composit approach

Provide the [set](#) of [constructors](#) and also a [set](#) of predicates and [set](#) of accessors. Use [pattern synonyms](#) to provide a documented accessor [set](#) without exposing internal [data type](#).

152.9 The changes in GHC 8.8

The fail method of [Monad](#) has been removed in favor of the method of the same name in the MonadFail class.

MonadFail(..) is now exported from the Prelude and Control.[Monad](#) modules. The Monad-FailDesugaring language extension is now deprecated, as its effects are always enabled.

So instead of:

```
import           Control.Monad.Fail
...
class MonadFail m => MonadFile m
...
-- use error instead of fail
Nothing      -> error ("Message " <> show x)
-- if compatibility fith old GHCs needed (ex. library)
#if __GLASGOW_HASKELL__ < 880
import           Control.Monad.Fail
#endif
```

152.10 Diversity in [exceptions](#)

[Exception](#) cause: external or internal.

[Exceptions](#) used by runtime system

```
div 1 0
-- *** Exception: divide by zero
```

[Exceptions](#) used by programmers:

- Language feature
- Programmable (implemented at library level)

152.11 [Exception](#) handling strategies

- Ignore
- Print
- Repeat
- Wait, stop, exit
- Substitute with default
- Throw
- Handle
- Rethrow
- Emergency exit

152.12 Asynchronous exception

Exceptions raised as a result of an "external event", such as signal from another thread.

Are raised by `throwTo`. Are by termin and design should not be caught/handled, by default catching/handling **functions** are not catching them, if someone still wants to catch them - there are special **function**: `catchAsync`.

Further reading: termin and apparatus were introduced by "[Asynchronous Exceptions in Haskell](#)" (Simon Marlow, Simon Peyton Jones, Andrew Moran, John Reppy).

152.13 Monadic Error handling

```
(>>=) :: m a -> (a -> m b) -> m b -- λA.E ⊠ A - computes and drops if error
    ↳ value happens.
catch :: c a -> (e -> c a) -> c a -- λE.E ⊠ A - handles "errors" as "normal"
    ↳ values and stops when an "error" is finally handled.
```


Chapter 153

Constraints

Very strong Haskell [type](#) system makes possible to work with code from the top down, an [axiomatic semantics](#) approach, from [constraints](#) into [types](#).

- Helps to form the [type level](#) code (aka [join](#) points of the code).
- Uses the piling up of [constraints/types](#) information. At some point pick and satisfy [constraints](#), can be done one at a time.
- Provides hints through [type level](#) formulation for [term level](#) calculations, does not formulate the [term level](#).
- Tedious method (a lot of boilerplate and rewriting it) but pretty simple and relaxing.
- [Set](#) of [constraints](#).
- When it is needed or convenient, single [constraint](#) gets a little more realistically concrete/abstracted.

Main [type](#) detail annotation thread can happen in [main](#) or special wrapper [function](#), localization is inside [functions](#).

a. Rest of [constraints set](#) shifts to source [type](#).

3.a. For the class handled or known how to handle - write a [base case](#) instance description.

```
instance (Monad m) => MonadReader r (ReaderT r m)
```

3.b. For others write [recursive](#) instance descriptions:

All other unsolved [constraints](#) move into the source [polymorphic variable](#).

```
instance (MonadError e m) => MonadError e (ReaderT r m)
instance (MonadState s m) => MonadState s (ReaderT r m)
```

a. Repeat from 1 until considered done.

b. Code condensed into terse form.

MonadError [constraints](#) is [IOException](#), not for the [String](#). [IOException](#) vs [String](#).

Reverse pluck MonadReader [constraint](#) with runReader on the [object](#).

MonadState - StateT

Chapter 154

Monad transformers and their type classes

Chapter 155

Layering **monad** transformers

Different layering of the same **monad** transformers is functionality is the same, but the form is different. Surrounding handling **functions** would need to be different.

Chapter 156

Hoogle

156.1 Search

Text search ([case](#) insensitive):

- `a`
- `map`
- `con map`

[Type](#) search:

- `:: a`
- `:: a -> a`

Text & [type](#):

`=id a -> a =`

156.2 Scope

156.2.1 Default

[Scope](#) is [Haskell Platform](#) (and [Haskell keywords](#)).

All [Package](#) packages are available to search with:

156.2.2 [Hierarchical module name](#) system (from big letter):

- `fold +Data.Map` finds results in the `Data.Map` [module](#)
- `file -System` excludes results from modules such as `System.IO`, `System.FilePath.Windows` and `Distribution.System`

156.2.3 Packages (lower [case](#)):

- `mode +platform`
- `mode +cmdargs` (only)
- `mode +platform +cmdargs`
- `file -base` (Haskell Platform, excluding the "base" package)

Chapter 157

ST-Trick monad

ST is like a [lexical scope](#), where all the [variables](#)/state disappear when the [function](#) returns <https://wiki.haskell.org/deamortized-strg/Monad/ST> <https://www.schoolofhaskell.com/school/to-infinity-and-beyond/older-but-still-interesting-polymorphism-nmh>

157.1 *

ST-Trick

Chapter 158

Either

Allows to separate and preserve information about happened, ex. [error](#) handling.

158.1 *

Either data type

Chapter 159

Inverse

- a.* [Inverse function](#)
- b.* In logic: $P \rightarrow Q \Rightarrow \neg P \rightarrow \neg Q$, & same for [category duality](#).
- c.* For [operation](#): element that allows reversing [operation](#), having an element that with the [dual](#) produces the [identity](#) element.
- d.* See [Inversion](#).

Chapter 160

Inversion

- a.* Is a [permutation where](#) two elements are out of [order](#).
- b.* See [Inverse](#)

Chapter 161

Inverse function

$$f_{x \rightarrow y} \circ (f_{x \rightarrow y})^{-1} = 1_x$$

* \iff function is **bijective**. Otherwise - **partial inverse**

Chapter 162

Inverse morphism

For $f : x \rightarrow y$: $\exists g : g \circ f = 1^x$ - g is left [inverse](#) of f , $\exists g : f \circ g = 1^y$ - g is right [inverse](#) of f .

Chapter 163

Partial inverse

* when [function](#) is now [bijective](#). When [bijective](#) see [inverse function](#).

Chapter 164

PatternSynonyms

Enables [pattern synonym declaration](#), which always begins with the `pattern` word. Allows to [abstract](#) away the [structures](#) of pattern matching.

164.1 *

Pattern synonym Pattern synonyms

Chapter 165

GHC debug keys

165.1 -ddump-ds

Dump desugarer output.

165.1.1 *

Desugar GHC desugar

Chapter 166

GHC optimize keys

166.1 -foptimal-applicative-do

$O(n^3)$ Always finds optimal [reduction](#) into `<*>` for [ApplicativeDo](#) do notation.

Chapter 167

Computational trinitarianism

Taken from: <https://ncatlab.org/nlab/show/computational+trinitarianism>

Under the [statements](#):

- [propositions](#) as [types](#)
- programs as proofs
- [relation](#) between [type](#) theory and [category](#) theory

the following notions are [equivalent](#):

== [proposition](#) proof (Logic)

== generalized element of an [object](#) ([Category](#) theory)

== typed program with output ([Type](#) theory & Computer science)

167.1 *

Trinitarism

Table 167.1: Computational trinitarianism

Logic	Category theory	Type theory
true	terminal object / (-2) -truncated object	h-level 0-type/unit type
false	initial object	empty type
proposition	(-1) -truncated object	h-proposition, mere proposition
proof	generalized element	program
cut rule	composition of classifying morphisms / pullback of display maps	substitution
cut elimination for implication	countit for hom-tensor adjunction	beta reduction
introduction rule for implication	unit for hom-tensor adjunction	eta conversion
logical conjunction	product	product type
disjunction	coproduct $((-1)$ -truncation of)	sum type (bracket type of)
implication	internal hom	function type
negation	internal hom into initial object	function type into empty type
universal quantification	dependent product	dependent product type
existential quantification	dependent sum $((-1)$ -truncation of)	dependent sum type (bracket type of)
equivalence	path space object	identity type
equivalence class	quotient	quotient type
induction	colimit	inductive type, W-type, M-type
higher induction	higher colimit	higher inductive type
completely presented set	discrete object/0-truncated object	h-level 2-type/preset/h-set
set	internal 0-groupoid	Bishop set/setoid
universe	object classifier	type of types
modality	closure operator, (idempotent) monad	modal type theory, monad (in computer science)
linear logic	(symmetric, closed) monoidal category	linear type theory/quantum computation
proof net	string diagram	quantum circuit
(absence of) contraction rule	(absence of) diagonal	no-cloning theorem
	synthetic mathematics	domain specific embedded programming language

Chapter 168

Techniques functional programming deals with the state

168.1 Minimizing

Do not rely on state, try not to change the state. Use it only when it is very necessary.

168.2 Concentrating

Concentrate the state in one place.

168.3 Deferring

Defer state to the last step of the program, or to external system.

Chapter 169

Functions

Total **function** uses **domain** fully, but takes only part of the **codomain**. **Function** allows to collapse **domain** values into **codomain** value. Meaning the **function** allows to loose the information. So total **function** is a computation that looses the information or into bigger codomains. That is why the **function** has a directionality, and **inverse** total **process** is partially possible.

Directionality and invertability are terms.

Chapter 170

Void

Emptiness.

Can not be grasped, touched.

A logically uninhabited [data type](#).

(Since [basis](#) of logic is tautologically True and [Void](#) value can not be addressed - there is a logical paradox with the [Void](#)).

Is an [object](#) included into the [Hask category](#), since:

```
:t (id :: Void -> Void)
(id :: Void -> Void) :: Void -> Void
```

id for it exists.

[Type](#) system corresponds to [constructive logic](#) and not to the classical logic. Classical logic answers the question "Is this actually true". Constructive (Intuitionistic) logic answers the question "Is this provable".

Also has [functions](#):

```
-- Represents logical principle of explosion: from falsehood, anything follows.
absurd :: Void -> a
```

```
-- If Functor holds only Void - it holds no values.
vacuous :: Functor f => f Void -> f a
```

```
-- If Monad holds only Void - it holds no values.
vacuousM :: Monad m => m Void -> m a
```

Design pattern: use [polymorphic data types](#) and [Void](#) to get rid of possibilities when you need to.

170.1 *

Nothing, Haskell [expressions](#) can't return [Void](#).

Also see: [Maybe](#).

Chapter 171

Intuitionistic logic

[Proposition](#) considered True due to direct evidence of existence through constructive proof using [Curry-Howard isomorphism](#).

* does not include classic logic fundamental axioms of the excluded middle and double negation elimination. Hence * is weaker than classical logic. Classical logic includes *, all theorems of * are also in classical logic.

171.1 *

Constructive logic

Chapter 172

Principle of explosion

If asserted **statement** contains some **error** or contradiction - anything can be proven through it. The more there is an **error** - the easier logic **chain** arrives at any target.

Ancient principle of logic. Both in classical & intuitionistic logic.

172.1 *

Ex falso quodlibet Ex falso sequitur quodlibet EFG Ex contradictione quodlibet Ex contradictione sequitur quodlibet ECQ Deductive explosion Pseudo-Scotus

Chapter 173

Universal **property**

A **property** of some construction which boils down to (is manifestly **equivalent** to) the **property** that an associated **object** is a universal **initial object** of some (auxiliary) **category**.

Chapter 174

Yoneda lemma

Allows the embedding of any [category](#) into a [category](#) of [functors](#) ([contravariant set-valued functors](#)) defined on that [category](#). It also clarifies how the embedded [category](#), of representable [functors](#) and their [natural transformations](#), relates to the other [objects](#) in the larger [functor category](#).

The Yoneda lemma suggests that instead of studying the (locally small) [category](#) $C \{\{\{C\}\}\}^{\mathcal{C}}$, *one should study the [category](#) of [functors](#)*

Chapter 175

Monoidal category, functoriality of ADTs, Profunctors

Category equipped with [tensor product](#).

<>

wich is a [functor](#) for $*$.

[Set category](#) can be [monoidal](#) under both [product](#) (having [terminal object](#)) or [coproduct](#) (having [initial object](#)) operations, if according [operation](#) exist for all [objects](#).

Any one-object category is $*$.

$(a, ()) \sim a$ up to unique [isomorphism](#), which is called [Lax monoidal functor](#).

[Product](#) and [coproduct](#) are [functorial](#), so, since: [Algebraic data type](#) construction can use:

- [Type constructor](#)
- [Data constructor](#)
- [Const functor](#)
- [Identity functor](#)
- [Product](#)
- [Coproduct](#)

Any [algebraic data type](#) is [functorial](#).

Chapter 176

Const functor

Maps all **objects** of source **category** into one (fixed) **object** of target **category**, and all **morphisms** to **identity morphism** of that fixed **object**.

```
instance Functor (Const c)
  where
    fmap :: (a -> b) -> Const c a -> Const c b
    fmap _ (Const c) = Const c
```

In **Category** theory denoted:

Δ

Last **type parameter** that bears the target **type** of lifted **function** (b) and is a **proxy type**.

Analogy: the container that always has an **object** attached to it, and everything that is put inside - changes the container **type** accordingly, and dissapears.

Chapter 177

Arrow in Haskell

```
(->) a b = a -> b
```

`Functorial` in the last `argument` & called Reader `functor`.

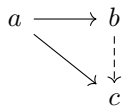
```
newtype Reader c a = Reader (c -> a)
```

```
fmap = ( . )
```

Chapter 178

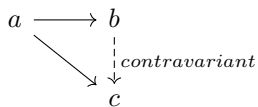
Contravariant functor

```
fmap :: (a -> b) -> Op c a -> Op c b
      (a -> c) -> (b -> c)
```



$$(a \rightarrow b)^C = (a \leftarrow b)^{C^{op}}$$

```
class Contravariant f
where
  contramap :: (b -> a) -> (f a -> f b)
```



If [arrows](#) does not commute Contravariant functor anyway allows to [construct](#) transformation between these such [arrows](#) to other [arrow](#).

Chapter 179

Profunctor

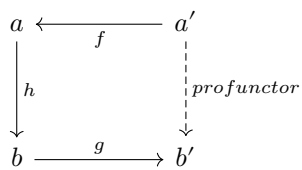
$(\multimap) \text{ a b}$

$C^{op} \times C \rightarrow C$

It is called profunctor.

`dimap :: (a' -> a) -> (b -> b') -> p a b -> p a' b'`

So, profunctor in [case](#) of [arrow](#):



```
dimap :: (a' -> a) -> (b -> b') -> p a b -> p a' b'
dimap ::      f      g      -> (a -> b) -> (a' -> b')
dimap ::      f      g      ->      h      -> (a' -> b')
dimap = g . h . f
```

It is [contravariant functor](#) in the first [argument](#), and [covariant functor](#) in the second [argument](#).

```
dimap id <==> fmap
(flip dimap) id <==> contramap
```

Chapter 180

Coerce

Operates under condition that source and target [types](#) have same representation. Same representation means they are [type](#) aliases, or it the compiler can [infer](#) that they have the same representation. Directly shares the values from the source [type](#) to the target [type](#). Conversion is free, there is no run-time computations.

The [function](#) implementing the transition:

```
coerce :: Coercible a b => a -> b
```

[Type class](#) implementing the instances for transitions:

```
class a ~R# b => Coercible (a :: k0) (b :: k0)
```

When compiler detects [types](#) have same [structure](#), [type class](#) instances coerse implementation for this pairs of [types](#). This [type class](#) does not have regular instances; instead they are created on-the-fly during [type](#)-checking. Trying to manually declare an instance of Coercible is an [error](#).

180.1 *

Coercible

Chapter 181

Universal/Existential quantification

\forall Universal [quantifier](#) - a general [property](#) exists. Global solution. \exists Existential [quantifier](#) - evidence means general [property](#), a [local](#) solution.

\forall and \exists are dualistic. Especially in Haskell universal [type](#) inside [function structure](#) has existential-like [properties](#) and backwards, existential [type](#) has universal-like [properties](#) inside [function](#) implementation.

Haskell [RankNTypes](#) option enables:

`forall ... =>` - universal

If [variable](#) is universally [quantified](#) - the consumer of it can choose the [type](#).

Because the consumer chooses the [type](#) the [variable](#) inside [function body](#) is [quantified](#) existentially.

`=> ... forall` - existential

If [variable](#) is existentially [quantified](#) - the [type](#) of it treated as it is already determined, and consumer can not reify it - consumer must accept and [process](#) the full existential [type](#) as it is.

Since the consumer is not involved into the choosing of the [type](#) - the [variable](#) inside [function body](#) [quantified](#) universally.

181.1 Use of existentials

Haskell existentials are always result in throwing away [type](#) information.

Gives ability to work with data from at external world that we do not know definite [type](#) at compile time.

Some information about existentially [quantified type](#) should be preserved to be able to transform it.

Existential wrappers make possible from a [function](#) to return existentially [quantified](#) data. Wrapper allows to avoid unification with outer [context](#) and "escape" [type variable](#).

There are three general degrees how much [type](#) information for existential to preserve:

- (low) - use existential [variable](#) as is, the use in the code would place it's own constraints (like `[a]`) and so the abilities to do something with that [type variables](#).
- (medium) - provide [type class constraints](#).

- (high) - store existential in parameterized GADT, store type information in GADT constructors, do things and then restore the type information on pattern match on main GADT constructor and get secondary type.

Additional reading: <https://markkarpov.com/post/existential-quantification.html>

Chapter 182

Propagator

Propagator is a monotone **function** between **join**-semilattices.

Where semilattices are amount of information about individual values. As information on input gained - the information on output only grows.

Join-semilattice is a **idempotent commutative monoid**.

If there is a system of **nodes** that each are **join** semilattice, and propagators are transformations that move information between them, and so transmit the information to all of them and bring the system into stable state. Number of times propagator with information fired is not important - because it is **idempotent**. **Order** of propagators in the network firing is not important - it is **commutative**.

Under side-condition for termination (provenance) (information fullness/volume, network becoming stationary or passing some check) - the network terminates and give a deterministic answer.

Provenance - a ad-hoc rules to determine the probability of receiving an close to truth result from number of different approaches and information sources. Also solves the contradictory data and raises the question of deciding between the contradictory world views: what is the least ... to get the most accurate estimates ...

Chapter 183

Code technics

[Dependent types](#) are used in teoretically complex code, in 1-2% of it. [GADTs](#) are fit 5-10% of the code.

Proving the easy targets & most needed ones allows much assurance and makes [testing](#) coverage more sufficient.

Liquid Haskell are useful and its refinement [types](#). [Ideas presentation](#).

There is relatively rough idea that codata should use laziness and data should use strictness, which is not really true because there is a lot of cases [where](#) being lazy on strict data allows to tramendously shorten the computation for data.

You want confluence regardless of totality.

Metaprogramming in Haskell is mainly done through Template Haskell wich is too hard and clunky to work with, due to hard syntax [structure](#).

Unproven Collatz conjecture is a classical computation halting problem. (If x_i is even $\Rightarrow x_{i+1} = 3x_i+1$, if odd $\Rightarrow x_{i+1} = x_i/2$).

Chapter 184

Algorithm of the Hackage package release

184.1 Form `Git{Hub,Lab}` pre-release

Name it `pre-x.x.x.x+1`, so determination of real number happens afterwards.

184.2 Create git branch `release x.x.x.x+1`

184.3 Open-up `git diff <lastVer>..HEAD` on one side of the screen

184.4 Open `CHANGELOG.md` on the other side of the screen

184.5 Walk through diff and populate `CHANGELOG.md`

`CHANGELOG.md` template:

184.5.1 Populate according to PVP

184.5.1.1 Major breaking changes

184.5.1.2 (optional) API additions of functionality

184.5.1.3 (optional) Other changes in the project, news

184.6 Check cabal sdist build passes

184.7 Think what new files can/should be included in .cabal extra-source-files

184.8 Update .cabal version:

184.9 Add a git tag <v>

184.10 git push --tags

184.11 (optional) (Remove git tag)

```
set fork 'f'
set ver '...'
git tag -d $ver
git push --delete $fork $ver
```

184.12 Make a cabal sdist

184.13 Upload package candidate to Hackage

<https://hackage.haskell.org/packages/candidates/upload>

184.14 (careful) Be fully ready when you upload package release to Hackage, since upload is idempotent

<http://hackage.haskell.org/packages/upload>

184.15 (optional) If docs not posted on Hackage

Hackage packaging have internal specifics and can refuse to build docs, to generate docs locally and upload them:

184.15.1 (optional) Nix-shell

```
nix-shell
```

184.15.2 Upload docs

```
set -e
```

184.15. (OPTIONAL) DIST DOCS NOT PROVIDED ON THE PACKAGE RELEASE

```
dir=$(mktemp -d /tmp/dist-docs.XXXXXX)
trap 'rm -r "$dir"' EXIT

# assumes cabal 2.4 or later
cabal v2-haddock --builddir="$dir" --haddock-for-hackage --enable-doc

# (pasting pass does not work) Enter _by hand_: account, password
cabal upload -d --publish $dir/*-docs.tar.gz
```

Chapter 185

Is power set functor is a bifunctor

```
bimap :: (a1 -> a2) -> (b1 -> b2) -> f a1 b1 -> f a2 b2
fmap  :: (a -> b)      -> f a      -> f b
fmap  :: (a -> b)      -> (Id -> Id) -> f a Id -> f b Id
```

Chapter 186

IO

186.1 Base IO Data types

186.1.1 IO a

`data IO a`

Main `data type` of the program run-time execution (`IO`).

All actions should be added to `Main.main IO ()` to be executed.

186.1.2 FilePath

`type FilePath = String`

Contents & Show are OS dependent, hold enough data to debug.

186.1.3 Handle

```
data Handle
  = FileHandle FilePath ... -- for files
  | DuplexHandle FilePath ... -- for streams
```

Handle - a record used by Haskell runtime system to manage I/O external `objects`.

Essential `properties`:

- Direction: In (readable), Out (writable) or both.
- Status: open, semi-closed, closed. A good practice to close handlers with `hClose`, aslo garbage collector at some point most probaly would remove unused handlers.
- Seekable: `True` | `False`.
- Buffering `type` and always a buffer (even if buffer turned off - buffer is 0).
- Position (there are `exceptions`)

186.1.4 HandlePosn

Position in the data `object`.

186.1.5 Standart handlers

- `stdin`
- `stdout`
- `stdin`

For more info - learn this question in POSIX UNIX/Linux.

186.1.6 IOMode

```
data IOMode -- manage
  = ReadMode -- input
  | WriteMode -- output
  | AppendMode -- output
  | ReadWriteMode -- input/output
```

186.1.7 File locking

Implementations should enforce locking as far as possible.

Haskell uses multiple-reader | single-writer locking.

If handle is managing:

- output to a file - no new handles can be allocated for that file.
- input from a file - new non-output handles can be created.

186.1.8 Opening files

```
withFile :: FilePath -> IOMode -> (Handle -> IO r) -> IO r
```

Allows to load the file and run code for it.

```
openFile :: FilePath -> IOMode -> IO Handle
```

Directionality of these functions are determined by IOMode.

186.1.9 hClose

```
hClose :: Handle -> IO ()
```

Close the handle.

186.1.10 Special cases

```
readFile :: FilePath -> IO String
writeFile :: FilePath -> String -> IO ()
appendFile :: FilePath -> String -> IO ()
```

186.1.11 Handle operation

```
hFileSize :: Handle -> IO Integer
hIsEOF :: Handle -> IO Bool
isEOF :: IO Bool -- works only on stdin
hGetPosn :: Handle -> IO HandlePosn
hSetPosn :: HandlePosn -> IO ()
```

186.1.12 BufferMode

```
data BufferMode
= NoBuffering      -- buffering is disabled if possible.
| LineBuffering    -- line-buffering should be enabled if possible.
| BlockBuffering (Maybe Int)
                  -- block-buffering should be enabled if possible.
                  -- Just - the size of the buffer, otherwise
                  --   ↪ implementation-dependent.
```

Styles of buffers supported:

- Block-buffering: the write happens when buffer overflows its size.
- Line-buffering: the write happens when `"` encountered.
- No buffering: everything is passed-through immediately.

Buffer also gets written when `hflush` is used or handle is `closed`.

One should not flush less frequently then specified. One can flush buffers more frequently.

The default buffering mode is implementation-dependent on the file system `object` which is attached to that handle. By default, physical files are block-buffered and terminals are line-buffered.

186.1.13 Buffering operation

```
hSetBuffering :: Handle -> BufferMode -> IO ()
hGetBuffering :: Handle -> IO BufferMode
hFlush :: Handle -> IO ()
```

186.2 Cabal Paths_pkgname

```
version :: Version

getBinDir :: IO FilePath
getLibDir :: IO FilePath
getDynLibDir :: IO FilePath
getDataDir :: IO FilePath
getLibexecDir :: IO FilePath
getSysconfDir :: IO FilePath
```

Cabal automatically generated `module`.

`ghci` would not load the `module`, since it was not generated, use `cabal v2-repl` to load it.

Part XI

Reference

Chapter 187

History

187.1 Functor-Applicative-Monad Proposal

Well known event in Haskell history: https://github.com/quchen/articles/blob/master/applicative_monad.md.

Math justice was restored with a RETroactive CONtinuity. Invented in computer science term [Applicative](#) ([lax monoidal functor](#)) become a [superclass](#) of [Monad](#).

& that is why:

- `return = pure`
- `ap = <*>`
- `>> = *>`
- `liftM = liftA = fmap`
- `liftM* = liftA*`

Also, a side-kick - [Alternative](#) became a [superclass](#) of [MonadPlus](#). Hence:

- `mzero = empty`
- `mplus = (<|>)`

Work of unification continues under: <https://gitlab.haskell.org/ghc/ghc/wikis/proposal/monad-of-no-return>

187.1.1 *

Applicative-Monad proposal AMP

187.2 Haskell 98

In 1998 first solid reference standartization of language was created. Main purpose is that implementors can be committed to rely and support [Haskell 98](#) exactly as it is specified.

In 2002 "[Haskell 98](#)" had a minor revision. Next [Haskell Report](#) is "Haskell 2010".

187.2.1 Old instance termination rules

- a. \forall class [constraint](#) ($C \text{ t1 .. tn}$): 1.1. [type variables](#) have occurrences \leq head 1.2. [constructors+variables](#)+repetitions < head 1.3. \neg [type functions](#) ([type func application](#) can expand to [arbitrary size](#))

- b. \forall functional dependencies, $\llbracket \text{tvs} \rrbracket_{\text{left}} \rightarrow \llbracket \text{tvs} \rrbracket_{\text{right}}$, of the class, every type variable in $S(\llbracket \text{tvs} \rrbracket_{\text{right}})$ must appear in $S(\llbracket \text{tvs} \rrbracket_{\text{left}})$, where S is the substitution mapping each type variable in the class declaration to the corresponding type in the instance head.

187.3 "Great moments in Haskell history" (by Type Classes) - History of Haskell

Chapter 188

Resources

188.1 **"State of the Haskell ecosystem"**

(Gabriel Gonzalez & contributors)

Good per-direction information on state of Haskell ecosystem.

188.2 **"Haskell performance"** tools, processes, comparisons, data, information, guides

(community)

188.3 **data Haskell** - (2017) annotated links to data science & machine learning libraries, overviews and benchmarks of libraries

dataHaskell contributors

Chapter 189

Literature

- "GHC User's Guide Documentation" (GHC Team): [PDF](#)
- "What I Wish I Knew When Learning Haskell" (Stephen Diehl & contributors): [PDF](#)
- "Category Theory for Programmers" (Bartosz Milewski & contributors): [PDF](#)
- Nix manual: [HTML](#)
- Nixpkgs manual: [HTML](#)
- Nixpkgs Haskell lib: [source on the GitHub](#)

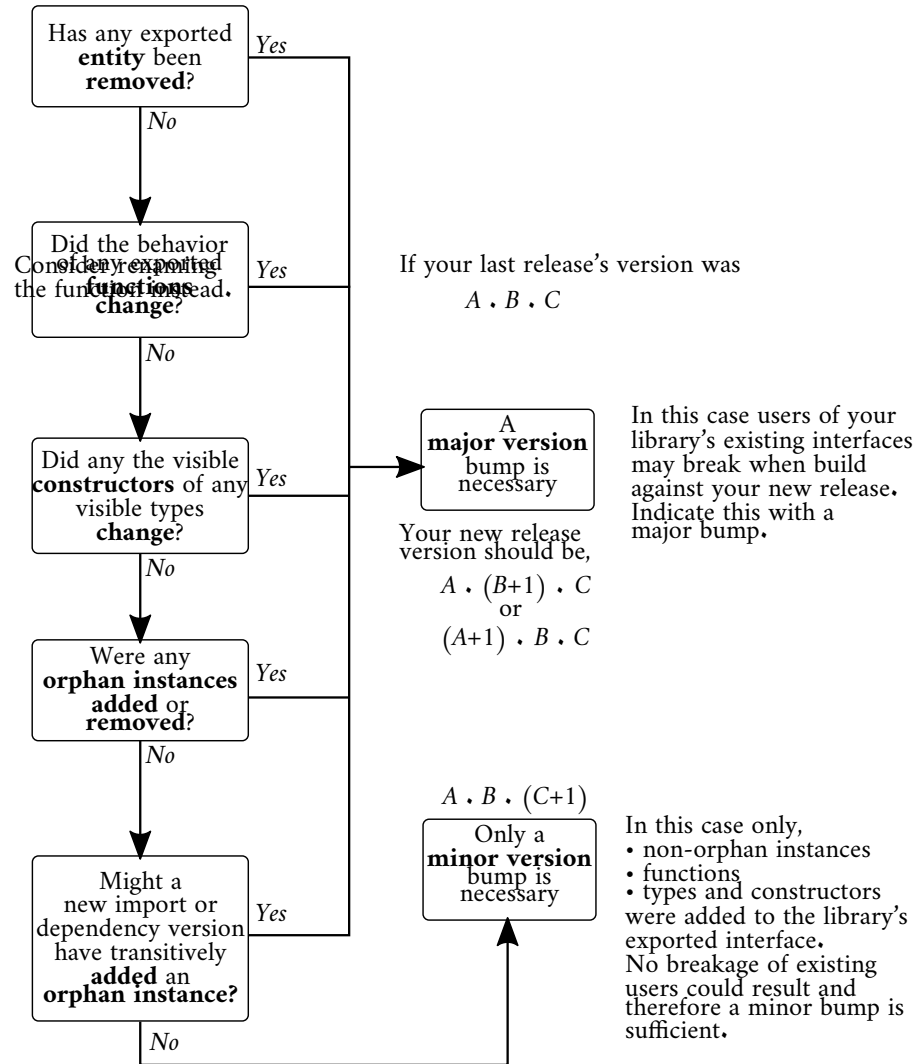
Chapter 190

Haskell Package Versioning Policy

Version policy and dependency management.

So you are releasing a new package version?

Use this decision graph to determine how you should version your new release under Haskell Package Versioning Policy.



```

-- Policy: +----- big breakage of API, big migration
--         / +----- breakage of API
--         / / +----- non-breaking API additions
--         / / / +--- changes that have no API changes
version: 1.2.3.4

```

190.1 *

PVP

Part XII

Giving back

λειτ <- λαός *Laos* the people ουργός <- ἔργο *ergon* work λειτουργία *leitourgia* public work

Moral value of people developed from the community to give back, improving the community.

The life is beautiful. For all humans that make the life have more magic.

This study and work would not be possible without the community: teachers, mathematicians, Haskellers, scientists, creators, contributors. These sides of people are fascinating.

Special accolades for the guys at Serokell. They were the force that got me inspired & gave resources to seriously learn Haskell and create this pocket guide.