



## 6. Housing

### Adv. Macro: Heterogenous Agent Models

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# Introduction

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# Disclaimer

- Note: The views expressed in this presentation are those of the author and do not represent the views of the Federal Reserve Board or Federal Reserve System.

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  3. Should these tax subsidies be repealed?
- **Plan for today:** Discuss 'Implications of US Tax Policy for House Prices, Rents, and Homeownership' (Sommer & Sullivan, 2018)
  1. Develop a HA model with equilibrium house prices and rents
  2. Calibrate the model to match the US economy
  3. Study the effect of eliminating housing subsidies

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- Depends on equilibrium change in the after-tax cost of homeownership

# Model



- Households
  - get utility from consumption  $c$  and housing services  $s$
  - receive exogenous labor income with wage  $w$
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- Multiple overlapping generations
  - Population grows at constant rate  $n = 0.01$
  - Total population evolves as  $N' = (1 + n)N$

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# Asset structure

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- Households may rent a small unit of shelter,  $\underline{s}$ , smaller than the minimum house size that is available for purchase, so  $\underline{s} < h(1)$ .
- Renters can rent any of the larger shelter sizes on the housing grid. So that for renters,  $s \in \{\underline{s}, h(1), \dots, h(K)\}$ .

- The household's choices about the amount of housing services consumed relative to the housing stock owned determine whether the household is a:
  - renter ( $h' = 0$ )
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- Mortgage debt limited by  $m' \leq (1 - \theta)qh'$

# Household optimization problem

- Households enter each period with a stock of owned housing,  $h \geq 0$ , deposits,  $d \geq 0$ , and mortgage debt,  $m \geq 0$ .

$$v(w, d, m, h) = \max_{c, s, h', d', m'} U(c, s) + \beta \sum_{w' \in \mathcal{W}} \pi(w' | w) v(w', d', m', h')$$

subject to

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- $\phi$  fixed cost incurred by landlords

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$$h' \geq s \text{ if } h' > 0$$

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- $H$  responds not only to increases in population but also to the counterfactual tax reforms studied in this paper.

# Stationary Equilibrium

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- Let  $P(x, x')$  define the transition function, ie the probability that a household with state  $x$  will have state  $x'$  next period



# Stationary Equilibrium

A stationary equilibrium is a collection of

1. value functions  $v(x)$
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3.  $\lambda$  is a stationary distribution:  $\lambda(x) = \int P(x, x') d\lambda$

## Baseline calibration

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- Assume the following utility function:

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- Two stage parameterization
  - Set exogenous parameter values
  - Calibrate remaining parameters to match key moments
    - Homeownership rate
    - Landlord rate
    - Expenditure share on housing
    - Fraction of homeowners with mortgage debt

# Exogenous parameters

TABLE 1—EXOGENOUS PARAMETERS

Parameter	Value
Autocorrelation of labor income shocks ( $\rho_w$ )	0.90
Standard deviation of labor income shocks ( $\sigma_w$ )	0.20
Risk aversion ( $\sigma$ )	2.50
Down payment requirement ( $\theta$ )	0.20
Selling cost ( $\tau^s$ )	0.07
Buying cost ( $\tau^b$ )	0.025
Risk-free interest rate ( $r$ )	0.04
Mortgage interest rate spread ( $\kappa$ )	0.015
Maintenance cost rate ( $\delta^h$ )	0.015
Payroll tax rate ( $\tau^p$ )	0.076
Property tax rate ( $\tau^h$ )	0.01
Mortgage deductibility rate ( $\tau^m$ )	1.00
Deductibility rate for depreciation of rental property ( $\tau^d$ )	0.023
Population growth rate ( $n$ )	0.01

TABLE 2—PROGRESSIVE TAX SYSTEM PARAMETERS

Tax parameter	
<i>Panel A. Marginal rate</i>	Bracket cutoff
$\eta_1 = 10\%$	\$0–\$8,350
$\eta_2 = 15\%$	\$8,350–\$33,950
$\eta_3 = 25\%$	\$33,950–\$82,250
$\eta_4 = 28\%$	\$82,250–\$171,550
$\eta_5 = 33\%$	\$171,550–\$371,950
$\eta_6 = 35\%$	> \$371,950
<i>Panel B. Deduction</i>	Amount
Personal exemption ( $e$ )	\$3,650
Standard deduction ( $\xi$ )	\$5,700

# Internally calibrated Parameters

TABLE 3—PARAMETER VALUES

Parameter	Value
<i>Panel A. Obtained by calibration</i>	
Discount factor ( $\beta$ )	0.985
Consumption share ( $\alpha$ )	0.685
Fixed cost for landlords ( $\phi$ )	0.056
<i>Panel B. Estimated by instrumental variables</i>	
Housing supply elasticity ( $\varepsilon$ )	0.902 (0.171)

*Note:* Standard error in parentheses.

TABLE 4—CALIBRATION TARGETS

Moment	Data	Model
Homeownership rate	0.65	0.65
Landlord rate	0.10	0.10
Expenditure share on housing	0.25	0.25
Fraction of homeowners with gross mortgage debt	0.65	0.65

# Properties of baseline model

TABLE 5—MOMENTS NOT TARGETED IN ESTIMATION

	Waves of the SCF			M
	1998 (1)	2007 (2)	2010 (3)	
Median house value-to-income ratio	2.44	3.32	2.98	
Median loan-to-income ratio	0.58	0.91	0.93	
Median loan-to-value	0.28	0.31	0.37	

*Notes:* Columns 1–3 show statistics from Survey of Consumer Finances. Column 4 shows statistics computed from the model.

# Distribution of shelter consumption

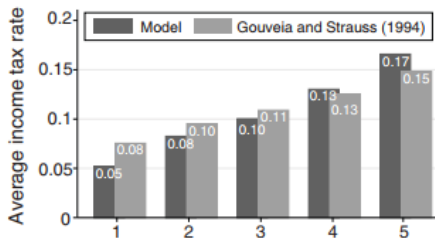
Table 3: The Distribution of Shelter Consumption for Renters and Homeowners

Size	Homeownership Status	
	(1) Renter ( $h' = 0$ )	(2) Owner ( $h' > 0$ )
$\underline{s}$	45.1	0.0
$h(1)$	53.5	17.6
$h(2)$	0.5	54.6
$h(3)$	0.01	13.3
$h(4)$	0.00	5.6
$\geq h(5)$	0.9	8.9

Notes: Entries are percentages (%).

# Properties of baseline model

Panel A. Average income tax rates



Panel B. Share of mortgage interest deduction

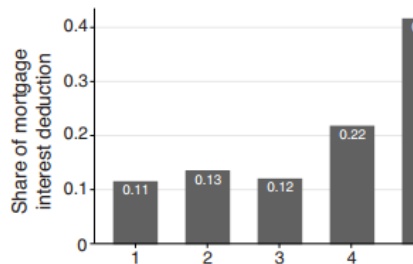


FIGURE 1. TAX RATES AND TAX DEDUCTIONS BY INCOME QUINTILES

- The largest benefits of MITD go to the top quintile

## Counterfactual exercises

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  - Starting from this initial steady state, the mortgage interest deduction is unexpectedly and permanently repealed.
  - Compute the perfect foresight transition path that ends at new s.s.
    - All agents correctly forecast the sequence of house prices and rents, and markets clear in each period.

# Effect of eliminating MITD

TABLE 6—THE EFFECT OF ELIMINATING THE MORTGAGE INTEREST TAX DEDUCTION

	Baseline (1)	Experiment (2)
House price	3.052	2.925
Rent	0.248	0.249
Price-rent ratio	12.320	11.715
Fraction homeowners	0.650	0.702
Fraction renter	0.350	0.297
Fraction owner-occupier	0.549	0.635
Fraction landlord	0.101	0.068
Median $\frac{\text{house value}}{\text{wage}}$	3.815	2.925
Fraction homeowners in debt	0.648	0.634
Average mortgage	2.815	1.931
Consumption equivalent variation ( $cev^*$ )	—	0.757%

Notes: Column 2 is the no-mortgage-deduction economy.  $cev^*$  is the ex ante consumption equivalent variation.

# Eliminating MITD: change in housing by quintile

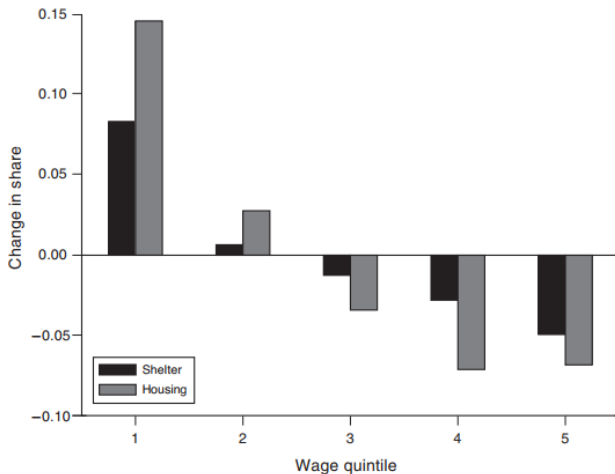


FIGURE 2. PERCENT CHANGE IN THE SHARE OF STEADY-STATE SHELTER CONSUMPTION AND HOUSING OWNERSHIP BY WAGE: ELIMINATION OF MORTGAGE INTEREST DEDUCTION

# Transition dynamics

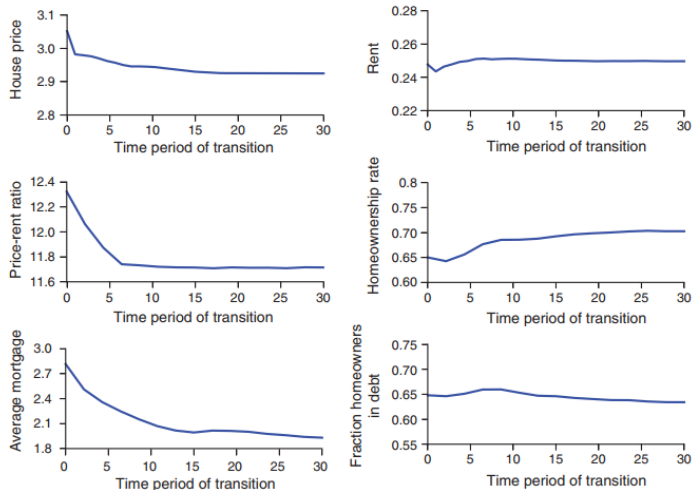


FIGURE 3. TRANSITIONAL DYNAMICS OF THE ECONOMY AFTER UNEXPECTED, PERMANENT ELIMINATION OF THE MORTGAGE INTEREST DEDUCTION AT  $t = 1$



## Welfare effects

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# Heterogeneous welfare effects

- How does the policy change affect household wellbeing?

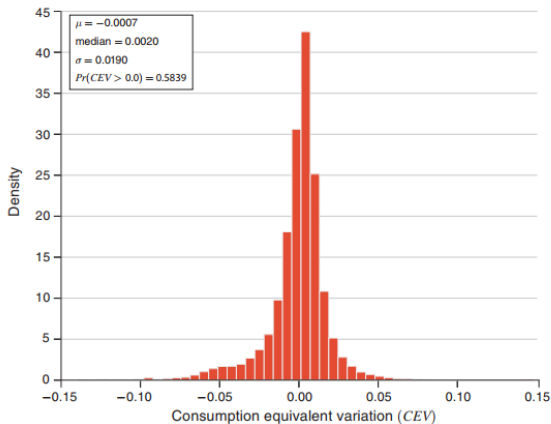


FIGURE 4. HISTOGRAM OF CONSUMPTION EQUIVALENT VARIATION ( $cev_i$ )

# Heterogeneous welfare effects

TABLE 7—SUMMARY STATISTICS: WELFARE OVER THE TRANSITION

	$\mu(cev_i)$	$\sigma(cev_i)$	Fraction $cev_i > 0$
<i>Initial housing tenure</i>			
Renter	0.004	0.015	0.589
Occupier	0.001	0.015	0.655
Landlord	−0.027	0.027	0.184
All	−0.001	0.019	0.584
<i>Initial mortgage</i>			
Have mortgage	−0.005	0.020	0.547
No mortgage	0.002	0.020	0.663
<i>Initial wage</i>			
Wage top 15%	−0.009	0.029	0.539
Wage at median	0.001	0.015	0.639
Wage bottom 15%	0.001	0.014	0.531

Notes:  $cev_i$  refers to the ex post consumption equivalent variation.  $\mu(cev_i)$  and  $\sigma(cev_i)$  represent the mean and standard deviation.

# Heterogeneous welfare effects

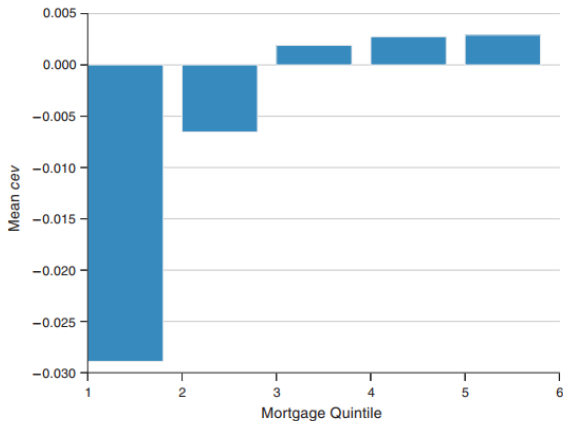


FIGURE 5. MEAN CONSUMPTION EQUIVALENT VARIATION ( $cev_i$ ) BY INITIAL MORTGAGE QUINTILE

*Note:* Quintile 1 represents the largest mortgages.

# Heterogeneous welfare effects

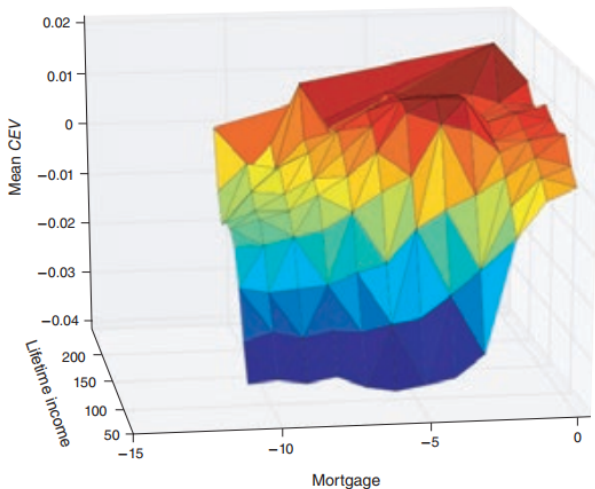


FIGURE 6. MEAN CONSUMPTION EQUIVALENT VARIATION ( $cev_i$ ) BY INITIAL MORTGAGE AND LIFETIME INCOME

TABLE 8—REVENUE NEUTRAL EXPERIMENT: ELIMINATING THE MORTGAGE INTEREST TAX DEDUCTION

	Eliminate MID		
	Baseline (1)	Experiment (2)	Revenue neutral (3)
House price	3.052	2.925	2.931
Rent	0.248	0.249	0.250
Price-rent ratio	12.320	11.715	11.715
Fraction homeowners	0.650	0.702	0.702
Consumption equivalent variation ( $cev^*$ )	—	0.757%	0.786%
% $\Delta$ income tax revenue	0.000	2.596%	1.806%
% $\Delta$ property tax revenue	0.000	−7.798%	−7.614%
% $\Delta$ total tax revenue	0.000	0.598%	0.000%

Notes: Column 2 is the counterfactual no-mortgage-interest deduction economy. Column 3 is the revenue neutral no-mortgage-interest deduction economy.  $cev^*$  is the ex ante consumption equivalent variation. % $\Delta$  indicates percent change relative to baseline model.

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  - decreases housing consumption by the wealthy
  - lowers house prices
  - increases aggregate homeownership
  - improves overall welfare
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# Conclusion

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  - decreases housing consumption by the wealthy
  - lowers house prices
  - increases aggregate homeownership
  - improves overall welfare
  - reduces aggregate mortgage debt
- Equilibrium effects very important
  - In a partial equilibrium model, the MITD would reduce the user cost of owner-occupied housing
  - But in an equilibrium model, the effect on house prices can undo this benefit for most households



# Summary

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