ModelZoo

August 10, 2023

1 Model Zoo

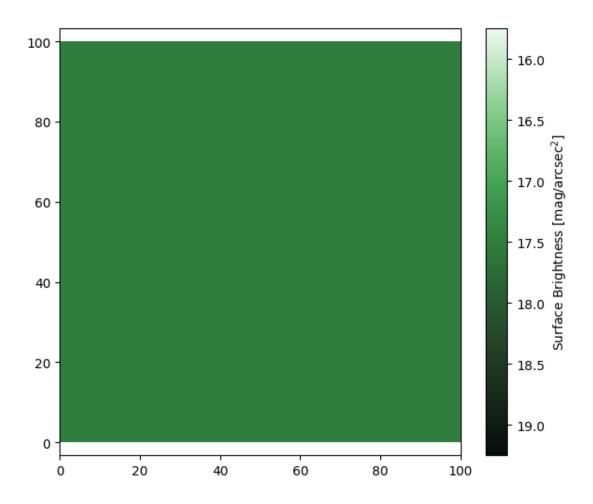
In this notebook you will see every kind of model in AstroPhot. Printed in each cell will also be the list of parameters which the model looks for while fitting. Many models have unique capabilities and features, this will be introduced here, though fully taking advantage of them will be dependent on your science case.

For a family tree of all the AstroPhot models see this link

Note, we will not be covering Group_Model here as that requires a dedicated discussion. See the dedicated notebook for that.

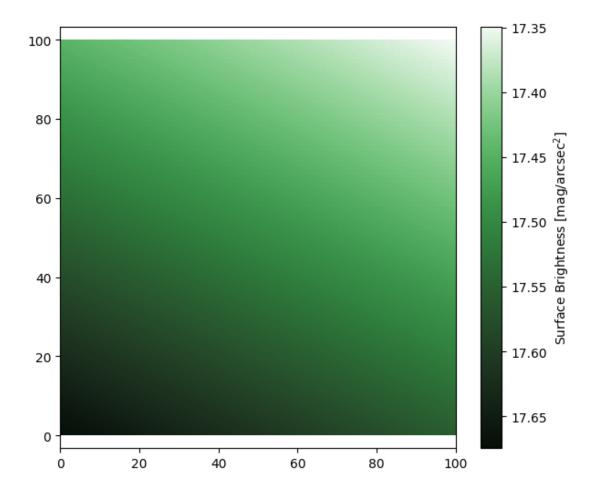
1.1 Sky Models

1.1.1 Flat Sky Model



1.1.2 Plane Sky Model

('flux/arcsec^2', 'flux/arcsec')



1.2 Star Models

1.2.1 PSF Star

Note that in this model you can define an arbitrary pixel map, for the sake of demonstration we build an Airy disk but you can assign whatever you like to the pixels.

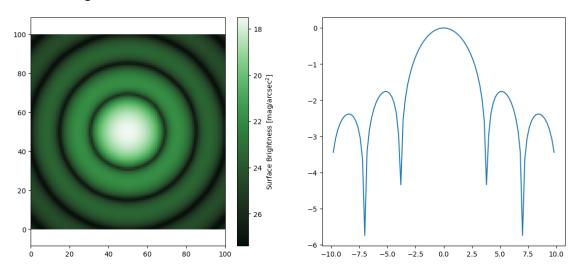
```
[4]: from scipy.special import jv
xx, yy = np.meshgrid(np.linspace(-50,50,101), np.linspace(-50,50,101))
x = np.sqrt(xx**2 + yy**2)/5 +1e-6
PSF = (2*jv(1, x)/x)**2 + 1e-4 # the PSF can be any image, here we construct anuairy disk
target = ap.image.Target_Image(data = np.zeros((100,100)), pixelscale = 1,uazeropoint = 20, psf = PSF) # the target image holds the PSF for itself

M = ap.models.AstroPhot_Model(name = "psf star", model_type = "psf star model",uarget = target, parameters = {"center": [50,50], "flux": 1})
print(M.parameter_order)
print(tuple(P.units for P in M.parameters))
```

```
M.initialize()

fig, ax = plt.subplots(1,2, figsize = (14,6))
ap.plots.model_image(fig, ax[0], M)
x = np.linspace(-49,49,99)/5 + 1e-6
ax[1].plot(x, np.log10((2*jv(1, x)/x)**2))
plt.show()
```

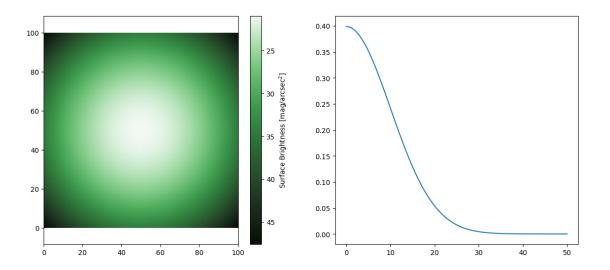
```
('center', 'flux')
('arcsec', 'log10(flux/arcsec^2)')
```



1.2.2 Gaussian Star

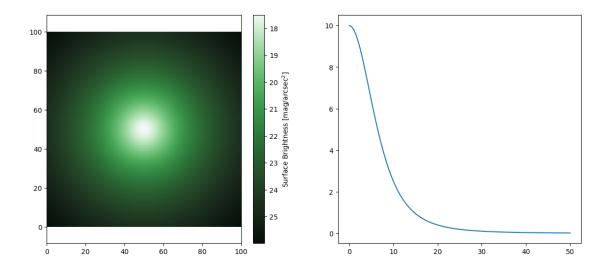
Never a great PSF model, but the Gaussian is simple. This makes it a good starting choice to get results before stepping up the complexity level.

```
('center', 'sigma', 'flux')
('arcsec', 'arcsec', 'log10(flux)')
```



1.2.3 Moffat Star

('center', 'n', 'Rd', 'I0')
('arcsec', 'none', 'arcsec', 'log10(flux/arcsec^2)')



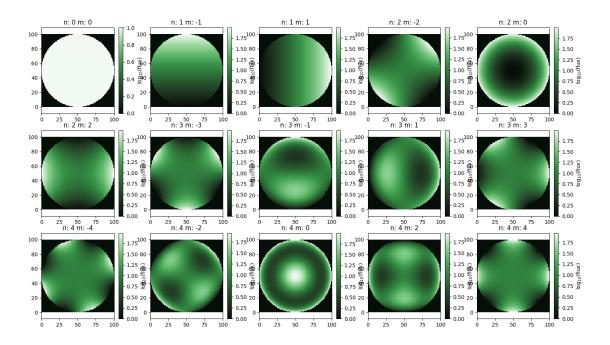
1.2.4 Zernike Polynomial star

```
[7]: super_basic_target = ap.image.Target_Image(np.zeros((100,100)), pixelscale = 1)
     M = ap.models.AstroPhot_Model(name = "zernike star", model_type = "zernike star"

_model", parameters = {"center":[50,50]}, order_n = 4, integrate_mode =
__

¬"none", target = super_basic_target)

     print(M.parameter_order)
     print(tuple(P.units for P in M.parameters))
     M.initialize()
     fig, axarr = plt.subplots(3,5, figsize = (18, 10))
     for i, ax in enumerate(axarr.flatten()):
         Anm = torch.zeros_like(M["Anm"].value)
         Anm[0] = 1.
         Anm[i] = 1.
         M["Anm"].value = Anm
         ax.set_title(f"n: {M.nm_list[i][0]} m: {M.nm_list[i][1]}")
         ap.plots.model_image(fig, ax, M, norm = None)
     plt.show()
    ('center', 'Anm')
    ('arcsec', 'flux/arcsec^2')
```



2 Galaxy Models

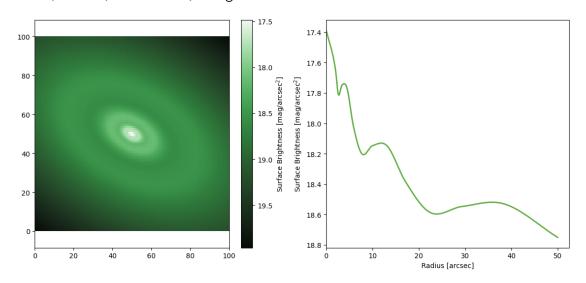
2.0.1 Spline Galaxy Model

This model has a radial surface brightness profile which can take on any function (that can be represented as a spline). This is somewhat like elliptical isophote fitting, though it is more precise in its definition of the SB model.

```
[8]: # Here we make an arbitrary spline profile out of a sine wave and a line
     x = np.linspace(0,10,14)
     spline_profile = np.sin(x*2+2)/20 + 1 - x/20
     # Here we write down some corresponding radii for the points in the
      ⇔non-parametric profile. AstroPhot will make
     # radii to match an input profile, but it is generally better to manually_
      ⇒provide values so you have some control
     # over their placement. Just note that it is assumed the first point will be at ...
      \hookrightarrow R = 0.
     NP prof = [0] + list(np.logspace(np.log10(2),np.log10(50),13))
     M = ap.models.AstroPhot Model(name = "spline galaxy", model type = "spline"
      ⇒galaxy model", parameters = {"center": [50,50], "q": 0.6, "PA": 60*np.pi/
      4180, "I(R)": {"value": spline_profile, "prof": NP_prof}}, target = 180, "I(R)": {"value": spline_profile, "prof": NP_prof}},
      ⇒basic_target)
     print(M.parameter_order)
     print(tuple(P.units for P in M.parameters))
     M.initialize()
```

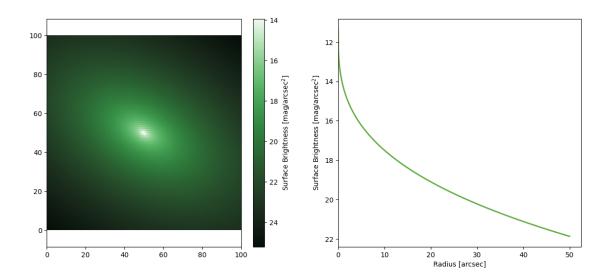
```
fig, ax = plt.subplots(1,2, figsize = (14,6))
ap.plots.model_image(fig, ax[0], M)
ap.plots.galaxy_light_profile(fig,ax[1],M)
plt.show()
```

```
('center', 'q', 'PA', 'I(R)')
('arcsec', 'b/a', 'radians', 'log10(flux/arcsec^2)')
```

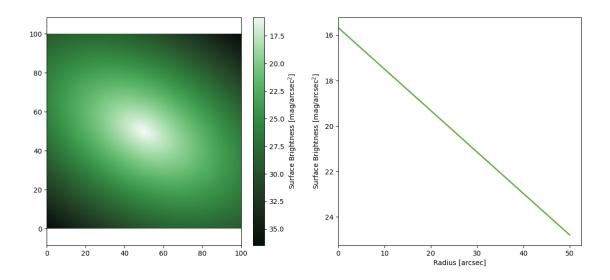


2.0.2 Sersic Galaxy Model

```
('center', 'q', 'PA', 'n', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'none', 'arcsec', 'log10(flux/arcsec^2)')
```



2.0.3 Exponential Galaxy Model

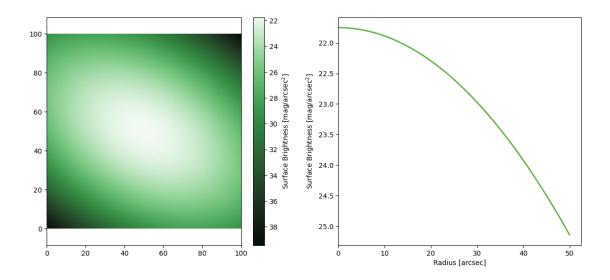


2.0.4 Gaussian Galaxy Model

```
[11]: M = ap.models.AstroPhot_Model(name = "Gaussian", model_type = "gaussian galaxy"
       →model", parameters = {"center": [50,50], "q": 0.6, "PA": 60*np.pi/180, □

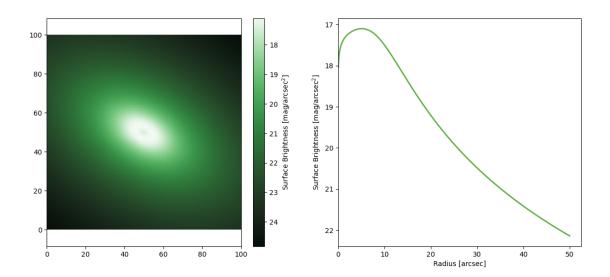
¬"sigma": 20, "flux": 1}, target = basic_target)
      print(M.parameter_order)
      print(tuple(P.units for P in M.parameters))
      M.initialize()
      fig, ax = plt.subplots(1,2, figsize = (14,6))
      ap.plots.model_image(fig, ax[0], M)
      ap.plots.galaxy_light_profile(fig,ax[1],M)
      plt.show()
     ('center', 'q', 'PA', 'sigma', 'flux')
```

```
('arcsec', 'b/a', 'radians', 'arcsec', 'log10(flux)')
```



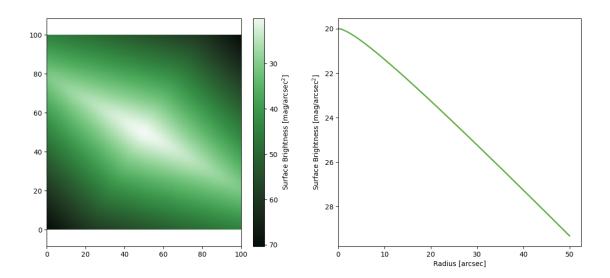
2.0.5 Nuker Galaxy Model

```
[12]: M = ap.models.AstroPhot_Model(name = "Nuker", model_type = "nuker galaxy_
       model", parameters = {"center": [50,50], "q": 0.6, "PA": 60*np.pi/180, "Rb":
       410., "Ib": 1., "alpha": 4., "beta": 3., "gamma": -0.2}, target = 10.
       ⇔basic_target)
      print(M.parameter order)
      print(tuple(P.units for P in M.parameters))
      M.initialize()
      fig, ax = plt.subplots(1,2, figsize = (14,6))
      ap.plots.model_image(fig, ax[0], M)
      ap.plots.galaxy_light_profile(fig,ax[1],M)
      plt.show()
     ('center', 'q', 'PA', 'Rb', 'Ib', 'alpha', 'beta', 'gamma')
     ('arcsec', 'b/a', 'radians', 'arcsec', 'log10(flux/arcsec^2)', 'none', 'none',
     'none')
     /home/connor/Programming/AstroPhot/astrophot/utils/conversions/units.py:9:
     RuntimeWarning: divide by zero encountered in log10
       return -2.5 * np.log10(flux) + zeropoint + 2.5 * np.log10(pixel_area)
```



2.1 Edge on model

Currently there is only one dedicared edge on model, the self gravitating isothermal disk from van der Kruit & Searle 1981. If you know of another common edge on model, feel free to let us know and we can add it in!



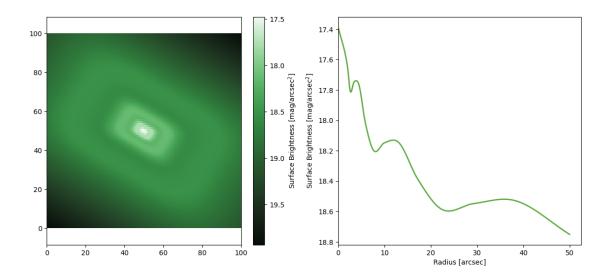
2.2 Super Ellipse Models

A super ellipse is a regular ellipse, except the radius metric changes from $R = \operatorname{sqrt}(x^2 + y^2)$ to the more general: $R = (x^C + y^C)1/C$. The parameter C = 2 for a regular ellipse, for 0 < C < 2 the shape becomes more "disky" and for C > 2 the shape becomes more "boxy." In AstroPhot we use the parameter C0 = C-2 for simplicity.

2.2.1 Spline SuperEllipse

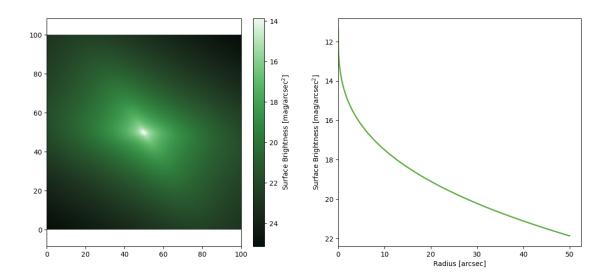
('center', 'q', 'PA', 'CO', 'I(R)')

('arcsec', 'b/a', 'radians', 'C-2', 'log10(flux/arcsec^2)')

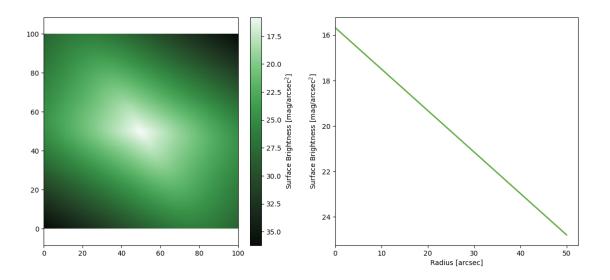


2.2.2 Sersic SuperEllipse

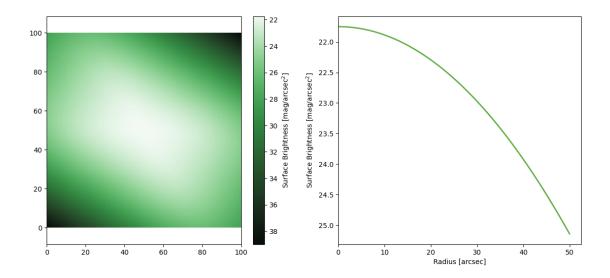
('arcsec', 'b/a', 'radians', 'C-2', 'none', 'arcsec', 'log10(flux/arcsec^2)')



2.2.3 Exponential SuperEllipse

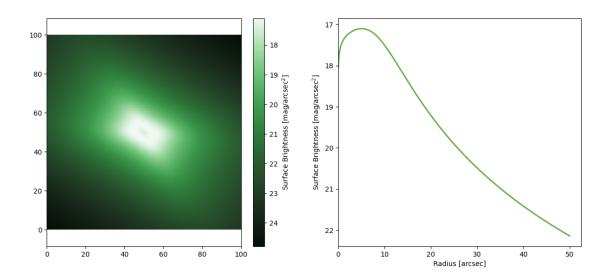


2.2.4 Gaussian SuperEllipse



2.2.5 Nuker SuperEllipse

```
[18]: M = ap.models.AstroPhot_Model(name = "nuker superellipse", model_type = "nuker_
       ⇒superellipse galaxy model", parameters = {"center": [50,50], "q": 0.6, "PA":⊔
       →60*np.pi/180, "CO": 2, "Rb": 10., "Ib": 1., "alpha": 4., "beta": 3., "gamma":
       → -0.2}, target = basic_target)
      print(M.parameter order)
      print(tuple(P.units for P in M.parameters))
      M.initialize()
      fig, ax = plt.subplots(1,2, figsize = (14,6))
      ap.plots.model_image(fig, ax[0], M)
      ap.plots.galaxy_light_profile(fig,ax[1],M)
      plt.show()
     ('center', 'q', 'PA', 'CO', 'Rb', 'Ib', 'alpha', 'beta', 'gamma')
     ('arcsec', 'b/a', 'radians', 'C-2', 'arcsec', 'log10(flux/arcsec^2)', 'none',
     'none', 'none')
     /home/connor/Programming/AstroPhot/astrophot/utils/conversions/units.py:9:
     RuntimeWarning: divide by zero encountered in log10
       return -2.5 * np.log10(flux) + zeropoint + 2.5 * np.log10(pixel_area)
```

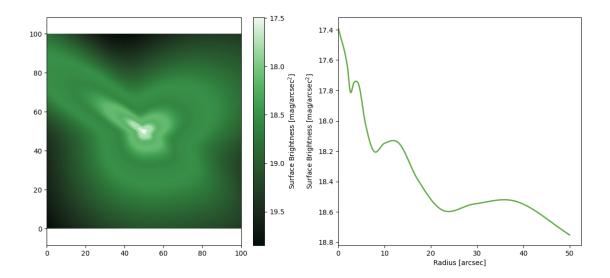


2.3 Fourier Ellipse Models

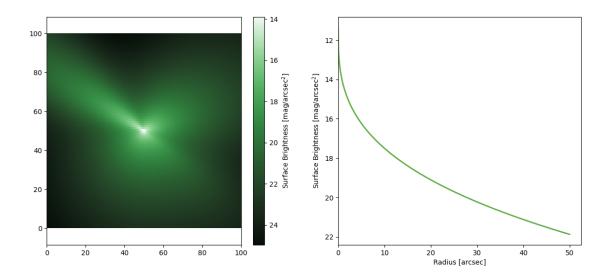
A Fourier ellipse is a scaling on the radius values as a function of theta. It takes the form: $R' = R * exp(\sum_m am * cos(m*theta + phim))$, where am and phim are the parameters which describe the Fourier perturbations. Using the "modes" argument as a tuple, users can select which Fourier modes are used. As a rough intuition: mode 1 acts like a shift of the model; mode 2 acts like ellipticity; mode 3 makes a lopsided model (triangular in the extreme); and mode 4 makes peanut/diamond perturbations.

2.3.1 Spline Fourier

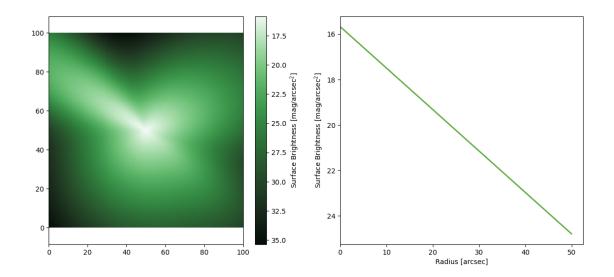
```
('center', 'q', 'PA', 'am', 'phim', 'I(R)')
('arcsec', 'b/a', 'radians', 'none', 'radians', 'log10(flux/arcsec^2)')
```



2.3.2 Sersic Fourier



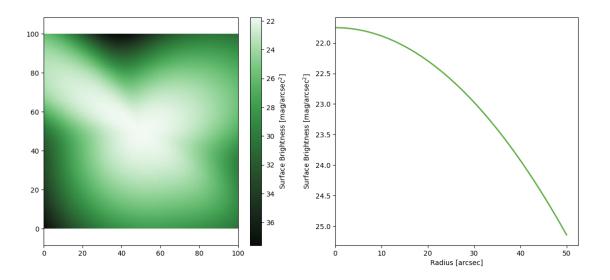
2.3.3 Exponential Fourier



2.3.4 Gaussian Fourier

```
[22]: M = ap.models.AstroPhot_Model(name = "gaussian fourier", model_type = "gaussian_"
       ofourier galaxy model", parameters = {"center": [50,50], "q": 0.6, "PA":⊔
       →60*np.pi/180, "am": fourier_am, "phim": fourier_phim, "sigma": 20, "flux":⊔
      →1}, target = basic_target)
      print(M.parameter_order)
      print(tuple(P.units for P in M.parameters))
      M.initialize()
      fig, ax = plt.subplots(1,2, figsize = (14,6))
      ap.plots.model_image(fig, ax[0], M)
      ap.plots.galaxy_light_profile(fig,ax[1],M)
      plt.show()
     ('center', 'q', 'PA', 'am', 'phim', 'sigma', 'flux')
```

```
('arcsec', 'b/a', 'radians', 'none', 'radians', 'arcsec', 'log10(flux)')
```

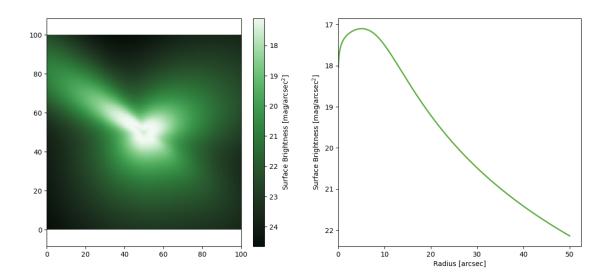


2.3.5 Nuker Fourier

```
[23]: M = ap.models.AstroPhot_Model(name = "nuker fourier", model_type = "nuker_
       ofourier galaxy model", parameters = {"center": [50,50], "q": 0.6, "PA":⊔
       →60*np.pi/180, "am": fourier_am, "phim": fourier_phim, "Rb": 10., "Ib": 1., "

¬"alpha": 4., "beta": 3., "gamma": -0.2}, target = basic_target)

      print(M.parameter_order)
      print(tuple(P.units for P in M.parameters))
      M.initialize()
      fig, ax = plt.subplots(1,2, figsize = (14,6))
      ap.plots.model_image(fig, ax[0], M)
      ap.plots.galaxy_light_profile(fig,ax[1],M)
      plt.show()
     ('center', 'q', 'PA', 'am', 'phim', 'Rb', 'Ib', 'alpha', 'beta', 'gamma')
     ('arcsec', 'b/a', 'radians', 'none', 'radians', 'arcsec',
     'log10(flux/arcsec^2)', 'none', 'none', 'none')
     /home/connor/Programming/AstroPhot/astrophot/utils/conversions/units.py:9:
     RuntimeWarning: divide by zero encountered in log10
       return -2.5 * np.log10(flux) + zeropoint + 2.5 * np.log10(pixel_area)
```



2.4 Warp Model

A warp model performs a radially varying coordinate transform. Essentially instead of applying a rotation matrix **Rot** on all coordinates X,Y we instead construct a unique rotation matrix for each coordinate pair $\mathbf{Rot}(\mathbf{R})$ where $R = \sqrt{(X^2 + Y^2)}$. We also apply a radially dependent axis ratio $\mathbf{q}(\mathbf{R})$ to all the coordinates:

$$R = \sqrt(X^2 + Y^2)$$

$$X, Y = Rotate(X, Y, PA(R))$$

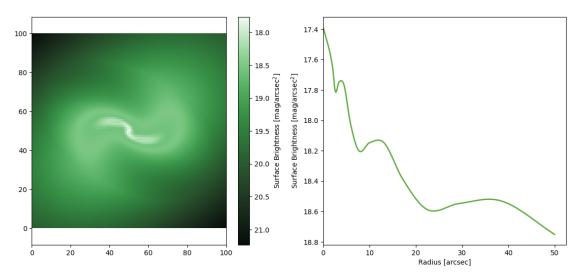
$$Y = Y/q(R)$$

The net effect is a radially varying PA and axis ratio which allows the model to represent spiral arms, bulges, or other features that change the apparent shape of a galaxy in a radially varying way.

2.4.1 Spline Warp

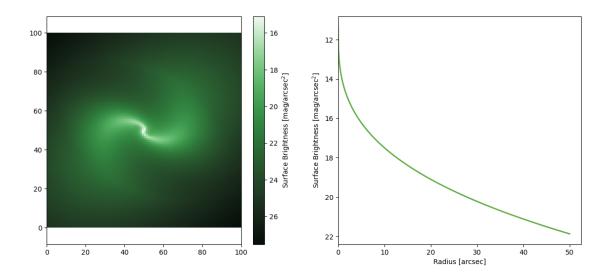
```
plt.show()
```

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'I(R)')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'log10(flux/arcsec^2)')
```



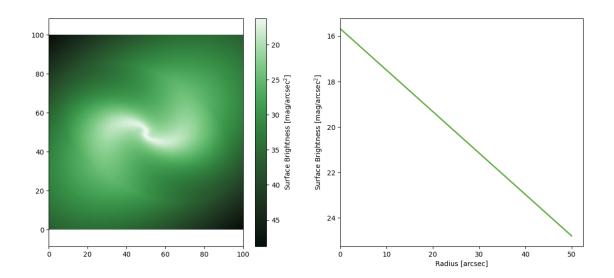
2.4.2 Sersic Warp

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'n', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'none', 'arcsec',
'log10(flux/arcsec^2)')
```



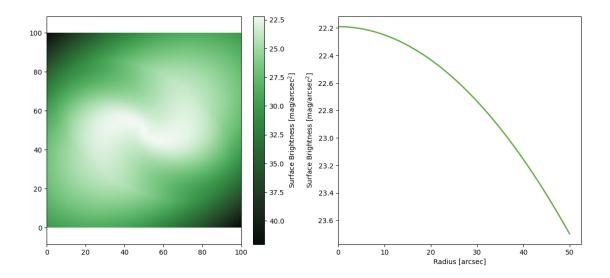
2.4.3 Exponential Warp

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'arcsec', 'log10(flux/arcsec^2)')
```



2.4.4 Gaussian Warp

('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'arcsec', 'log10(flux)')



2.4.5 Nuker Warp

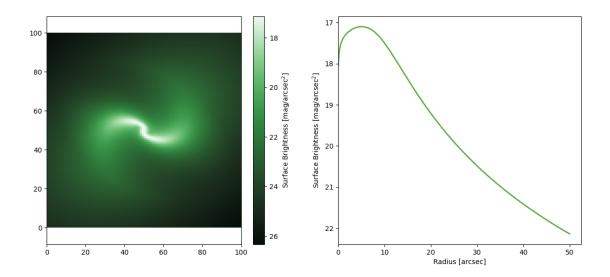
```
[28]: M = ap.models.AstroPhot_Model(name = "nuker warp", model_type = "nuker warp"

¬galaxy model", parameters = {"center": [50,50], "q": 0.6, "PA": 60*np.pi/
       4180, "q(R)": warp_q, "PA(R)": warp_pa, "Rb": 10., "Ib": 1., "alpha": 4.,⊔

¬"beta": 3., "gamma": -0.2}, target = basic_target)

      print(M.parameter order)
      print(tuple(P.units for P in M.parameters))
      M.initialize()
      fig, ax = plt.subplots(1,2, figsize = (14,6))
      ap.plots.model_image(fig, ax[0], M)
      ap.plots.galaxy_light_profile(fig,ax[1],M)
      plt.show()
     ('center', 'q', 'PA', 'q(R)', 'PA(R)', 'Rb', 'Ib', 'alpha', 'beta', 'gamma')
     ('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'arcsec', 'log10(flux/arcsec^2)',
     'none', 'none', 'none')
     /home/connor/Programming/AstroPhot/astrophot/utils/conversions/units.py:9:
     RuntimeWarning: divide by zero encountered in log10
```

return -2.5 * np.log10(flux) + zeropoint + 2.5 * np.log10(pixel_area)



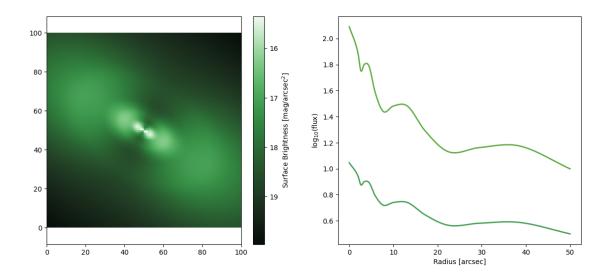
2.5 Ray Model

A ray model allows the user to break the galaxy up into regions that can be fit separately. There are two basic kinds of ray model: symmetric and asymetric. A symmetric ray model (symmetric_rays = True) assumes 180 degree symmetry of the galaxy and so each ray is reflected through the center. This means that essentially the major axes and the minor axes are being fit separately. For an asymmetric ray model (symmetric_rays = False) each ray is it's own profile to be fit separately.

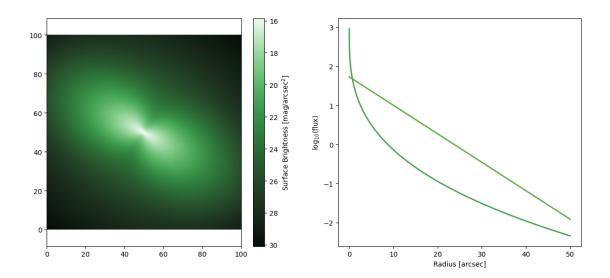
In a ray model there is a smooth boundary between the rays. This smoothness is acomplished by applying a $(\cos(r*theta)+1)/2$ weight to each profile, where r is dependent on the number of rays and theta is shifted to center on each ray in turn. The exact cosine weighting is dependent on if the rays are symmetric and if there is an even or odd number of rays.

2.5.1 Spline Ray

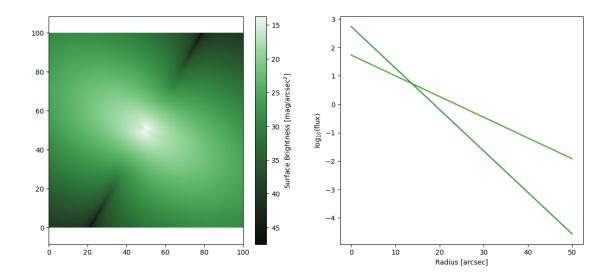
```
('center', 'q', 'PA', 'I(R)')
('arcsec', 'b/a', 'radians', 'log10(flux/arcsec^2)')
```



2.5.2 Sersic Ray



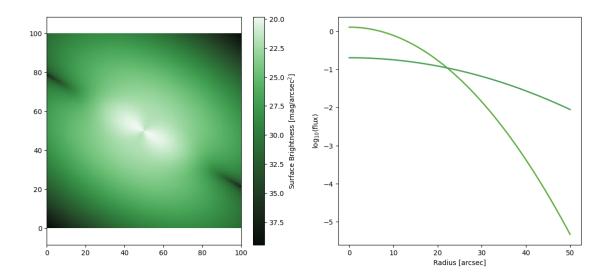
2.5.3 Exponential Ray



2.5.4 Gaussian Ray

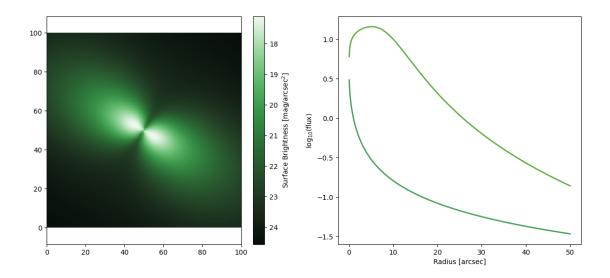
```
[32]: M = ap.models.AstroPhot_Model(name = "gaussian ray", model_type = "gaussian ray"
       ⇒galaxy model", symmetric_rays = True, rays = 2, parameters = {"center":⊔
       →[50,50], "q": 0.6, "PA": 60*np.pi/180, "sigma": [10,20], "flux": [1.5,1.]}, __
       starget = basic_target)
      print(M.parameter_order)
      print(tuple(P.units for P in M.parameters))
      M.initialize()
      fig, ax = plt.subplots(1,2, figsize = (14,6))
      ap.plots.model_image(fig, ax[0], M)
      ap.plots.ray_light_profile(fig,ax[1],M)
      plt.show()
     ('center', 'q', 'PA', 'sigma', 'flux')
```

```
('arcsec', 'b/a', 'radians', 'arcsec', 'log10(flux)')
```



2.5.5 Nuker Ray

```
[33]: M = ap.models.AstroPhot_Model(name = "nuker ray", model_type = "nuker ray"
       ⇒galaxy model", symmetric_rays = True, rays = 2, parameters = {"center":⊔
       ↔[50,50], "q": 0.6, "PA": 60*np.pi/180, "Rb": [10.,1.], "Ib": [1.,0.], "
       o"alpha": [4.,1.], "beta": [3.,1.], "gamma": [-0.2,0.2]}, target = □
       →basic_target)
      print(M.parameter_order)
      print(tuple(P.units for P in M.parameters))
      M.initialize()
      fig, ax = plt.subplots(1,2, figsize = (14,6))
      ap.plots.model image(fig, ax[0], M)
      ap.plots.ray_light_profile(fig,ax[1],M)
      plt.show()
     ('center', 'q', 'PA', 'Rb', 'Ib', 'alpha', 'beta', 'gamma')
     ('arcsec', 'b/a', 'radians', 'arcsec', 'log10(flux/arcsec^2)', 'none', 'none',
     'none')
     /home/connor/Programming/AstroPhot/astrophot/plots/profile.py:196:
     RuntimeWarning: divide by zero encountered in log10
       np.log10(model.iradial_model(r, xx).detach().cpu().numpy()),
```

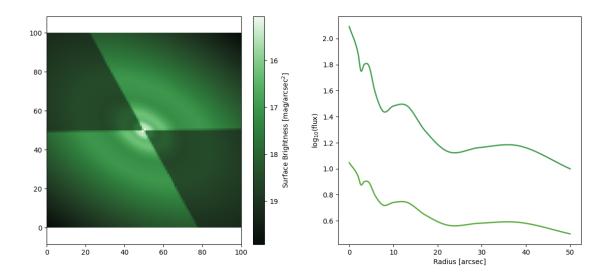


2.6 Wedge Model

A wedge model behaves just like a ray model, except the boundaries are sharp. This has the advantage that the wedges can be very different in brightness without the "smoothing" from the ray model washing out the dimmer one. It also has the advantage of less "mixing" of information between the rays, each one can be counted on to have fit only the pixels in it's wedge without any influence from a neighbor. However, it has the disadvantage that the discontinuity at the boundary makes fitting behave strangely when a bright spot lays near the boundary.

2.6.1 Spline Wedge

```
('center', 'q', 'PA', 'I(R)')
('arcsec', 'b/a', 'radians', 'log10(flux/arcsec^2)')
```

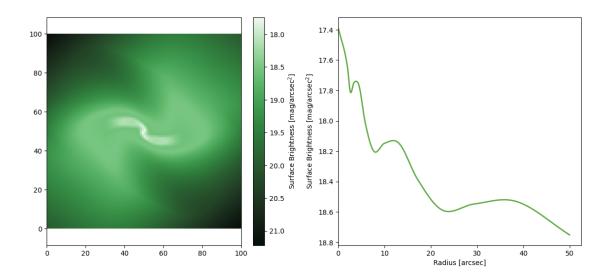


3 High Order Warp Models

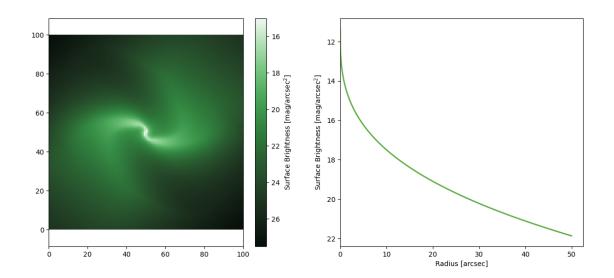
The models below combine the Warp coordinate transform with radial behaviour transforms: SuperEllipse and Fourier. These higher order models can create highly complex shapes, though their scientific use-case is less clear. They are included for completeness as they may be useful in some specific instances. These models are also included to demonstrate the flexibility in making AstroPhot models, in a future tutorial we will discuss how to make your own model types.

3.0.1 Spline SuperEllipse Warp

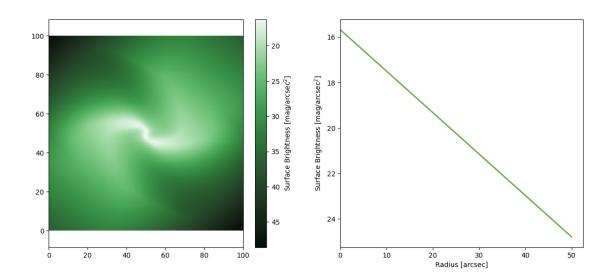
```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'CO', 'I(R)')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'C-2', 'log10(flux/arcsec^2)')
```



3.0.2 Sersic SuperEllipse Warp



3.0.3 Exponential SuperEllipse Warp

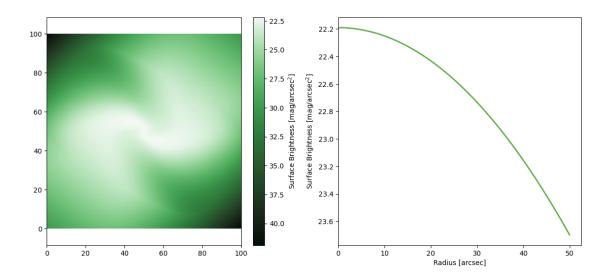


3.0.4 Gaussian SuperEllipse Warp

```
[38]: M = ap.models.AstroPhot_Model(name = "gauss super warp", model_type = "gaussian_"
       ⇒superellipse warp galaxy model", parameters = {"center": [50,50], "q": 0.6,⊔
       →"PA": 60*np.pi/180, "q(R)": warp_q, "PA(R)": warp_pa, "C0": 2, "sigma": 30, ⊔

¬"flux": 1}, target = basic_target)
      print(M.parameter order)
      print(tuple(P.units for P in M.parameters))
      M.initialize()
      fig, ax = plt.subplots(1,2, figsize = (14,6))
      ap.plots.model_image(fig, ax[0], M)
      ap.plots.galaxy_light_profile(fig,ax[1],M)
      plt.show()
     ('center', 'q', 'PA', 'q(R)', 'PA(R)', 'CO', 'sigma', 'flux')
```

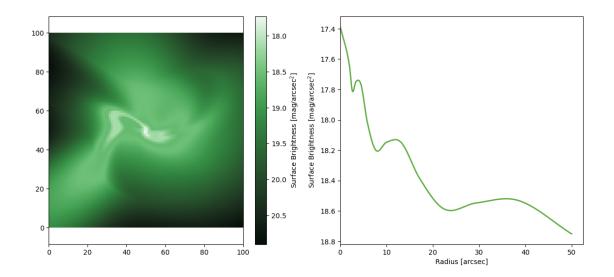
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'C-2', 'arcsec', 'log10(flux)')



3.0.5 Spline Fourier Warp

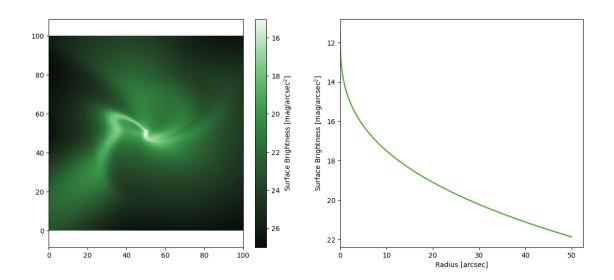
not sure how this abomination would fit a galaxy, but you are welcome to try

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'am', 'phim', 'I(R)')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'none', 'radians',
'log10(flux/arcsec^2)')
```



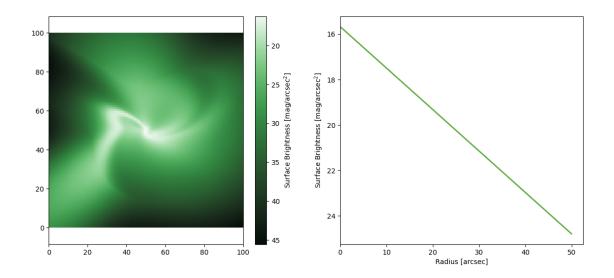
3.0.6 Sersic Fourier Warp

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'am', 'phim', 'n', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'none', 'radians', 'none', 'arcsec',
'log10(flux/arcsec^2)')
```



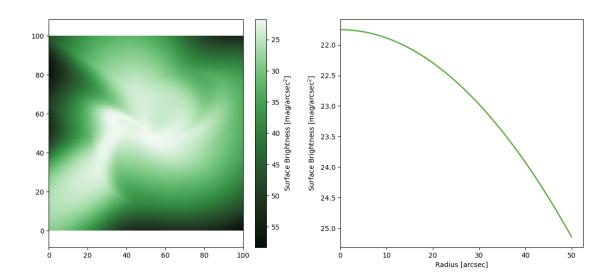
3.0.7 Exponential Fourier Warp

'log10(flux/arcsec^2)')



3.0.8 Gassian Fourier Warp

('center', 'q', 'PA', 'q(R)', 'PA(R)', 'am', 'phim', 'sigma', 'flux')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'none', 'radians', 'arcsec',
'log10(flux)')



[]: