

JointModels

May 27, 2023

1 Joint Modelling

In this tutorial you will learn how to set up a joint modelling fit which incorporates the data from multiple images. These use `Group_Model` objects just like in the `GroupModels.ipynb` tutorial, the main difference being how the `Target_Image` object is constructed and that more care must be taken when assigning targets to models.

It is, of course, more work to set up a fit across multiple target images. However, the tradeoff can be well worth it. Perhaps there is space-based data with high resolution, but groundbased data has better S/N. Or perhaps each band individually does not have enough signal for a confident fit, but all three together just might. Perhaps colour information is of paramount importance for a science goal, one would hope that both bands could be treated on equal footing but in a consistent way when extracting profile information. There are a number of reasons why one might wish to try and fit a multi image picture of a galaxy simultaneously.

When fitting multiple bands one often resorts to forced photometry, sometimes also blurring each image to the same approximate PSF. With AutoProf this is entirely unnecessary as one can fit each image in its native PSF simultaneously. The final fits are more meaningful and can incorporate all of the available structure information.

```
[1]: import autoprof as ap
import numpy as np
import torch
from astropy.io import fits
import matplotlib.pyplot as plt
from scipy.stats import iqr

[2]: # First we need some data to work with, let's use LEDA 41136 as our example
    ↪ galaxy

# Our first image is from the DESI Legacy-Survey r-band. This image has a
    ↪ pixelscale of 0.262 arcsec/pixel and is 500 pixels across
target_r = ap.image.Target_Image(
    data = np.array(fits.open("https://www.legacysurvey.org/viewer/fits-cutout?
    ↪ ra=187.3119&dec=12.9783&size=500&layer=ls-dr9&pixscale=0.262&bands=r")[0] .
    ↪ data, dtype = np.float64),
    pixelscale = 0.262,
    zeropoint = 22.5,
```

```

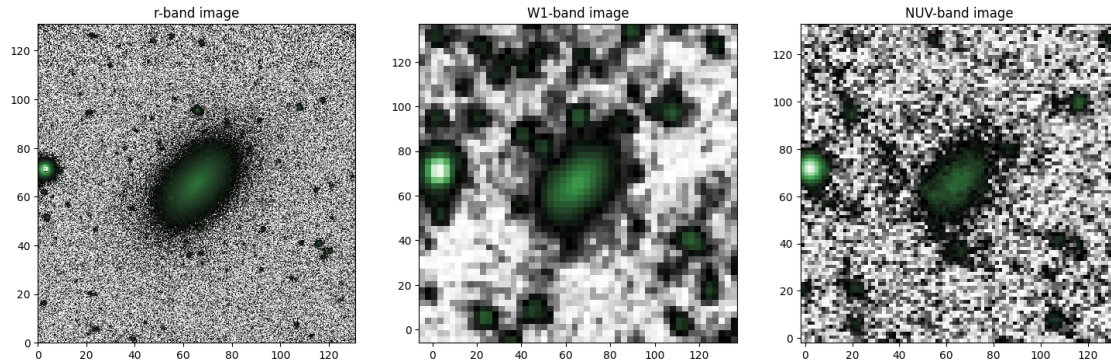
    variance = np.ones((500,500))*0.008**2, # note that the variance is
    ↪important to ensure all images are compared with proper statistical weight.
    ↪Here we just use the  $IQR^2$  of the pixel values as the variance, for science
    ↪data one would use a more accurate variance value
    psf = ap.utils.initialize.gaussian_psf(1.12/2.355, 51, 0.262) # we
    ↪construct a basic gaussian psf for each image by giving the sigma (arcsec),
    ↪image width (pixels), and pixelscale (arcsec/pixel)
)

# The second image is a unWISE W1 band image. This image has a pixelscale of 2.
    ↪75 arcsec/pixel and is 52 pixels across
target_W1 = ap.image.Target_Image(
    data = np.array(fits.open("https://www.legacysurvey.org/viewer/fits-cutout?
    ↪ra=187.3119&dec=12.9783&size=52&layer=unwise-neo7&pixscale=2.75&bands=1")[0].
    ↪data, dtype = np.float64),
    pixelscale = 2.75,
    zeropoint = 25.199,
    variance = np.ones((52,52))*4.9**2,
    psf = ap.utils.initialize.gaussian_psf(6.1/2.355, 21, 2.75),
    origin = (np.array([500,500]))*0.262/2 - (np.array([52,52]))*2.75/2, # here
    ↪we ensure that the images line up by slightly adjusting the origin
)

# The third image is a GALEX NUV band image. This image has a pixelscale of 1.5
    ↪arcsec/pixel and is 90 pixels across
target_NUV = ap.image.Target_Image(
    data = np.array(fits.open("https://www.legacysurvey.org/viewer/fits-cutout?
    ↪ra=187.3119&dec=12.9783&size=90&layer=galex&pixscale=1.5&bands=n")[0].data,
    ↪dtype = np.float64),
    pixelscale = 1.5,
    zeropoint = 20.08,
    variance = np.ones((90,90))*0.0007**2,
    psf = ap.utils.initialize.gaussian_psf(5.4/2.355, 21, 1.5),
    origin = (np.array([500,500]))*0.262/2 - (np.array([90,90]))*1.5/2,
)

fig1, ax1 = plt.subplots(1, 3, figsize = (18,6))
ap.plots.target_image(fig1, ax1[0], target_r)
ax1[0].set_title("r-band image")
ap.plots.target_image(fig1, ax1[1], target_W1)
ax1[1].set_title("W1-band image")
ap.plots.target_image(fig1, ax1[2], target_NUV)
ax1[2].set_title("NUV-band image")
plt.show()

```



```
[3]: # The joint model will need a target to try and fit, but now that we have
      ↪ multiple images the "target" is
      # a Target_Image_List object which points to all three.
      target_full = ap.image.Target_Image_List((target_r, target_W1, target_NUV))
      # It doesn't really need any other information since everything is already
      ↪ available in the individual targets
```

```
[4]: # To make things easy to start, lets just fit a sersic model to all three. In
      ↪ principle one can use arbitrary
      # group models designed for each band individually, but that would be
      ↪ unnecessarily complex for a tutorial
```

```
model_r = ap.models.AutoProf_Model(
    name = "rband model",
    model_type = "sersic galaxy model",
    target = target_r,
    psf_mode = "full",
)
model_W1 = ap.models.AutoProf_Model(
    name = "W1band model",
    model_type = "sersic galaxy model",
    target = target_W1,
    psf_mode = "full",
)
model_NUV = ap.models.AutoProf_Model(
    name = "NUVband model",
    model_type = "sersic galaxy model",
    target = target_NUV,
    psf_mode = "full",
)
```

```
# At this point we would just be fitting three separate models at the same
      ↪ time, not very interesting. Next
```

```
# we add constraints so that some parameters are shared between all the models.
↳ It makes sense to fix
# structure parameters while letting brightness parameters vary between bands
↳ so that's what we do here.
model_W1.add_equality_constraint(model_r, ["center", "q", "PA", "n", "Re"])
model_NUV.add_equality_constraint(model_r, ["center", "q", "PA", "n", "Re"])
# Now every model will have a unique Ie, but every other parameter is shared
↳ for all three
```

```
[5]: # We can now make the joint model object

model_full = ap.models.AutoProf_Model(
    name = "LEDA 41136",
    model_type = "group model",
    models = [model_r, model_W1, model_NUV],
    target = target_full,
)

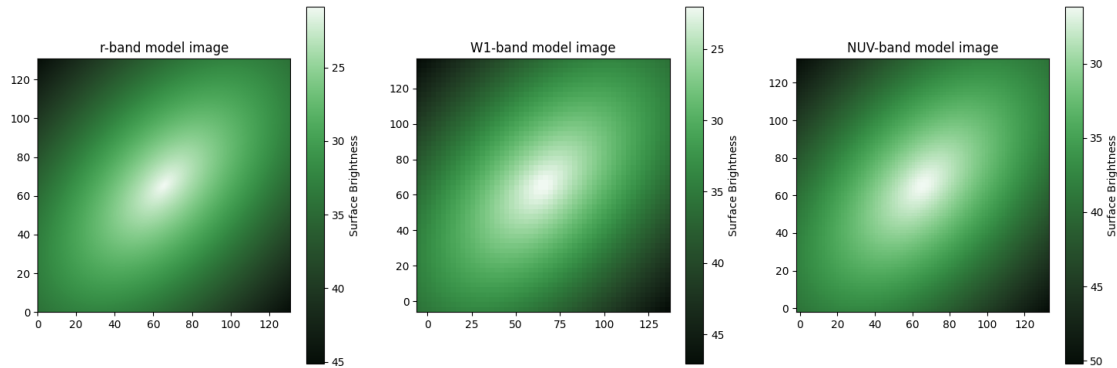
model_full.initialize()
```

```
[6]: result = ap.fit.LM(model_full, verbose = 1).fit()
print(result.message)
```

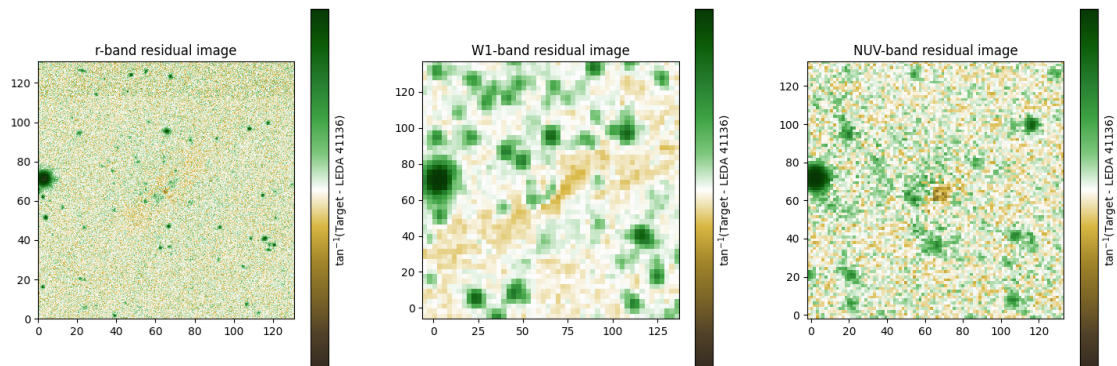
```
L: 1.0
-----init-----
LM loss: 93.27189078643637
L: 1.0
-----iter-----
LM loss: 93.25876606427266
accept
L: 0.1111111111111111
-----iter-----
LM loss: 93.24679451536917
accept
L: 0.012345679012345678
-----iter-----
LM loss: 93.24392242400215
accept
L: 0.0013717421124828531
-----iter-----
LM loss: 93.2437177834453
accept
success
```

```
[7]: # here we plot the results of the fitting, notice that each band has a
↳ different PSF and pixelscale. Also, notice
```

```
# that the colour bars represent significantly different ranges since each
# ↪ model was allowed to fit its own Ie.
# meanwhile the center, PA, q, and Re is the same for every model.
fig1, ax1 = plt.subplots(1, 3, figsize = (18,6))
ap.plots.model_image(fig1, ax1, model_full)
ax1[0].set_title("r-band model image")
ax1[1].set_title("W1-band model image")
ax1[2].set_title("NUV-band model image")
plt.show()
```



```
[8]: # We can also plot the residual images. As can be seen, the galaxy is fit in
# ↪ all three bands simultaneously
# with the majority of the light removed in all bands. A residual can be seen
# ↪ in the r band. This is likely
# due to there being more structure in the r-band than just a sersic. The W1
# ↪ and NUV bands look excellent though
fig1, ax1 = plt.subplots(1, 3, figsize = (18,6))
ap.plots.residual_image(fig1, ax1, model_full)
ax1[0].set_title("r-band residual image")
ax1[1].set_title("W1-band residual image")
ax1[2].set_title("NUV-band residual image")
plt.show()
```



```

[9]: # Save a joint model just like any other model
model_full.save("jointsave.yaml")

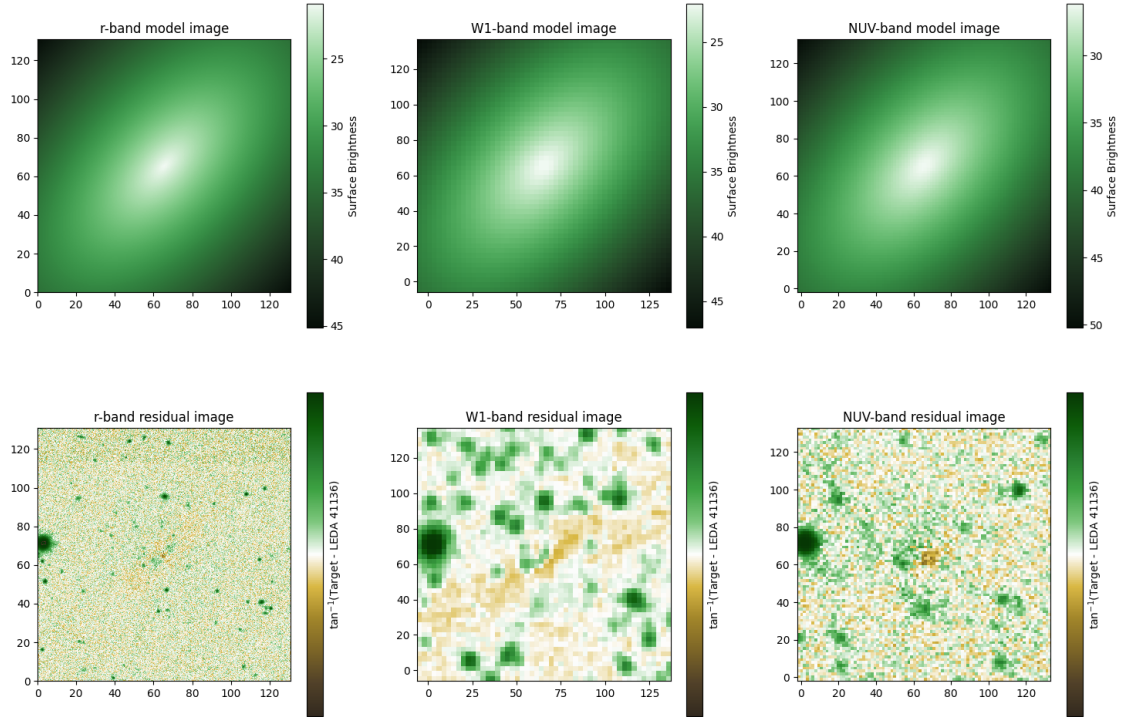
# Load the joint model just like any other
model_reload = ap.models.AutoProf_Model(
    name = "reload LEDA 41136",
    filename = "jointsave.yaml",
)

# However, targets are not saved when saving a model, so those must be
↳re-assigned manually
# Assign the group target
model_reload.target = target_full
# Assign the sub-model targets
model_reload.models["rband model"].target = target_r
model_reload.models["W1band model"].target = target_W1
model_reload.models["NUVband model"].target = target_NUV

# You must also update the full model window before proceeding
model_reload.update_window()

# Plot everything again to check its working
fig1, ax1 = plt.subplots(2, 3, figsize = (18,12))
ap.plots.model_image(fig1, ax1[0], model_reload)
ax1[0][0].set_title("r-band model image")
ax1[0][1].set_title("W1-band model image")
ax1[0][2].set_title("NUV-band model image")
ap.plots.residual_image(fig1, ax1[1], model_reload)
ax1[1][0].set_title("r-band residual image")
ax1[1][1].set_title("W1-band residual image")
ax1[1][2].set_title("NUV-band residual image")
plt.show()

```



1.1 Joint models with multiple models

If you want to analyze more than a single astronomical object, you will need to combine many models for each image in a reasonable structure. There are a number of ways to do this that will work, though may not be as scalable. For small images, just about any arrangement is fine when using the LM optimizer. But as images and number of models scales very large, it may be necessary to sub divide the problem to save memory. To do this you should arrange your models in a hierarchy so that AutoProf has some information about the structure of your problem. There are two ways to do this. First, you can create a group of models where each sub-model is a group which holds all the objects for one image. Second, you can create a group of models where each sub-model is a group which holds all the representations of a single astronomical object across each image. The second method is preferred. See the diagram below to help clarify what this means.

JointGroupModels

Here we will see an example of a multiband fit of an image which has multiple astronomical objects.

```
[10]: # First we need some data to work with, let's use another LEDA object, this
      ↪time a group of galaxies: LEDA 389779, 389797, 389681

RA = 320.5003
DEC = -57.4585
# Our first image is from the DESI Legacy-Survey r-band. This image has a
↪pixelscale of 0.262 arcsec/pixel
rsize = 250
```



```

target_r = ap.image.Target_Image(
    data = np.array(fits.open(f"https://www.legacysurvey.org/viewer/fits-cutout?
    ↪ra={RA}&dec={DEC}&size={rsize}&layer=ls-dr9&pixscale=0.262&bands=r")[0] .
    ↪data, dtype = np.float64),
    pixelscale = 0.262,
    zeropoint = 22.5,
    variance = np.ones((rsize,rsize))*0.008**2, # note that the variance is
    ↪important to ensure all images are compared with proper statistical weight.
    ↪Here we just use the IQR^2 of the pixel values as the variance, for science.
    ↪data one would use a more accurate variance value
    psf = ap.utils.initialize.gaussian_psf(1.12/2.355, 51, 0.262) # we
    ↪construct a basic gaussian psf for each image by giving the sigma (arcsec),
    ↪image width (pixels), and pixelscale (arcsec/pixel)
)

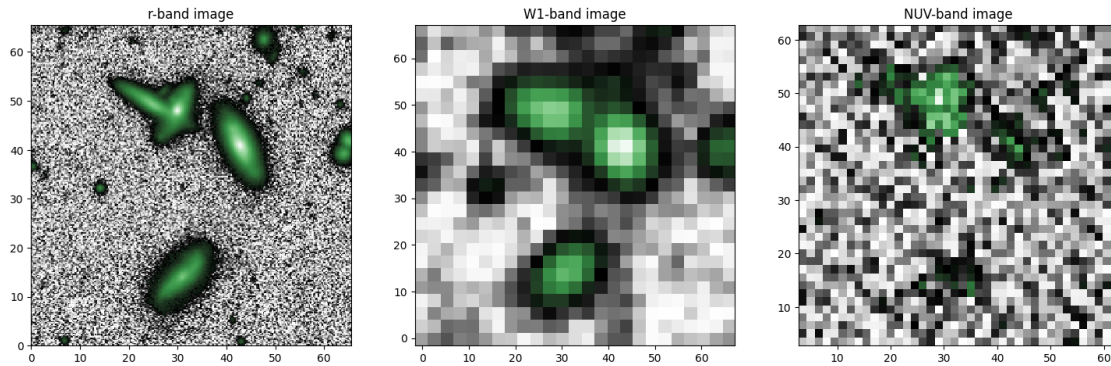
# The second image is a unWISE W1 band image. This image has a pixelscale of 2.
    ↪75 arcsec/pixel
wsize = 25
target_W1 = ap.image.Target_Image(
    data = np.array(fits.open(f"https://www.legacysurvey.org/viewer/fits-cutout?
    ↪ra={RA}&dec={DEC}&size={wsize}&layer=unwise-neo7&pixscale=2.75&bands=1")[0] .
    ↪data, dtype = np.float64),
    pixelscale = 2.75,
    zeropoint = 25.199,
    variance = np.ones((wsize,wsize))*4.9**2,
    psf = ap.utils.initialize.gaussian_psf(6.1/2.355, 21, 2.75),
    origin = (np.array([rsize,rsize]))*0.262/2 - (np.array([wsize,wsize]))*2.75/
    ↪2, # here we ensure that the images line up by slightly adjusting the origin
)

# The third image is a GALEX NUV band image. This image has a pixelscale of 1.5
    ↪arcsec/pixel
gsize = 40
target_NUV = ap.image.Target_Image(
    data = np.array(fits.open(f"https://www.legacysurvey.org/viewer/fits-cutout?
    ↪ra={RA}&dec={DEC}&size={gsize}&layer=galex&pixscale=1.5&bands=n")[0] .data,
    ↪dtype = np.float64),
    pixelscale = 1.5,
    zeropoint = 20.08,
    variance = np.ones((gsize,gsize))*0.0007**2,
    psf = ap.utils.initialize.gaussian_psf(5.4/2.355, 21, 1.5),
    origin = (np.array([rsize,rsize]))*0.262/2 - (np.array([gsize,gsize]))*1.5/
    ↪2,
)
target_full = ap.image.Target_Image_List((target_r, target_W1, target_NUV))

```



```
fig1, ax1 = plt.subplots(1, 3, figsize = (18,6))
ap.plots.target_image(fig1, ax1, target_full)
ax1[0].set_title("r-band image")
ax1[1].set_title("W1-band image")
ax1[2].set_title("NUV-band image")
plt.show()
```



There is barely any signal in the GALEX data and it would be entirely impossible to analyze on its own. With simultaneous multiband fitting it is a breeze to get relatively robust results!

Next we need to construct models for each galaxy. This is understandably more complex than in the single band case, since now we have three times the amount of data to keep track of. Recall that we will create a number of joint models to represent each astronomical object, then put them all together in a larger group model.

```
[11]: # Here we enter the window parameters by hand, in general one would use a
      ↪ segmentation map or some other automated procedure to pick out the area for
      ↪ many objects
windows = [
    {"r": [[72,152],[140,234]], "W1": [[5,16],[13,24]], "NUV": [[8,27],[20,39]]},
    {"r": [[43,155],[138,237]], "W1": [[3,15],[12,25]], "NUV": [[4,22],[19,39]]},
    {"r": [[115,210],[100,228]], "W1": [[10,21],[10,23]], "NUV": 
    ↪ [[17,35],[13,38]]},
    {"r": [[69,170],[10,115]], "W1": [[7,17],[1,13]], "NUV": [[8,30],[1,18]]},
]

model_list = []

for i, window in enumerate(windows):
    # create the submodels for this object
    sub_list = []
    sub_list.append(
        ap.models.AutoProf_Model(
            name = f"rband model {i}",
```

```

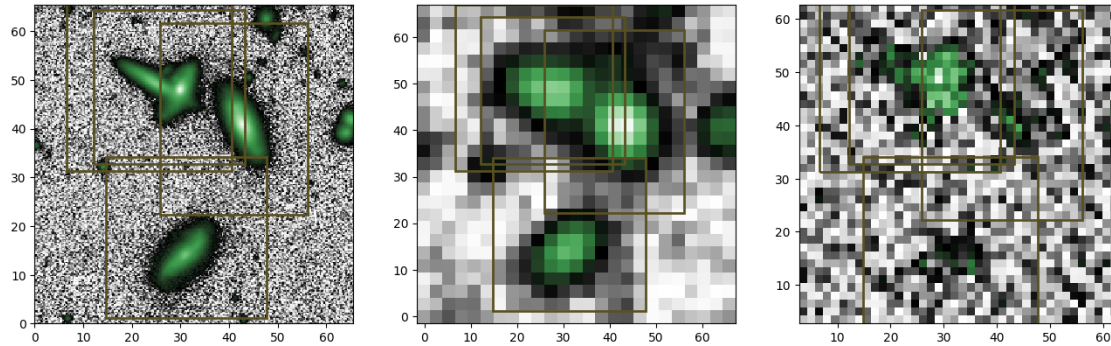
        model_type = "spline galaxy model", # we use spline models for the
        ↪r-band since it is well resolved
        target = target_r,
        window = window["r"],
        psf_mode = "full",
    )
)
sub_list.append(
    ap.models.AutoProf_Model(
        name = f"W1band model {i}",
        model_type = "sersic galaxy model", # we use sersic models for W1
        ↪and NUV since there isn't much visible detail, a simple model is sufficient
        target = target_W1,
        window = window["W1"],
        psf_mode = "full",
    )
)
sub_list.append(
    ap.models.AutoProf_Model(
        name = f"NUVband model {i}",
        model_type = "sersic galaxy model",
        target = target_NUV,
        window = window["NUV"],
        psf_mode = "full",
    )
)
# ensure equality constraints
sub_list[1].add_equality_constraint(sub_list[0], ["center", "q", "PA"])
sub_list[2].add_equality_constraint(sub_list[0], ["center", "q", "PA"])
# Make the multiband model for this object
model_list.append(
    ap.models.AutoProf_Model(
        name = f"model {i}",
        model_type = "group model",
        target = target_full,
        models = sub_list,
    )
)
# Make the full model for this system of objects
MODEL = ap.models.AutoProf_Model(
    name = f"full model",
    model_type = "group model",
    target = target_full,
    models = model_list,
)
fig, ax = plt.subplots(1,3, figsize = (16,7))
ap.plots.target_image(fig, ax, MODEL.target)

```

```

ap.plots.model_window(fig, ax, MODEL)
ax1[0].set_title("r-band image")
ax1[1].set_title("W1-band image")
ax1[2].set_title("NUV-band image")
plt.show()

```



```

[12]: MODEL.initialize()
      result = ap.fit.LM(MODEL, verbose = 1, epsilon4 = 0.05).fit()
      print(result.message)

```

```

L: 1.0
-----init-----
LM loss: 6.61428319445387
L: 1.0
-----iter-----
LM loss: 61974418.77995861
reject
L: 11.0
-----iter-----
LM loss: 5.343013355499518
accept
L: 1.222222222222223
-----iter-----
LM loss: 2228268.716430663
reject
L: 13.444444444444446
-----iter-----
LM loss: 4.71858933625814
accept
L: 1.4938271604938274
-----iter-----
LM loss: 639570.0893393792
reject
L: 16.4320987654321

```

```

-----iter-----
LM loss: 4.286010682555342
accept
L: 1.825788751714678
-----iter-----
LM loss: 2613.5314919854677
reject
L: 20.08367626886146
-----iter-----
LM loss: 3.9402607285792532
accept
L: 2.231519585429051
-----iter-----
LM loss: 2.905211826311042
accept
L: 0.2479466206032279
-----iter-----
LM loss: 8197210.2296158075
reject
L: 2.727412826635507
-----iter-----
LM loss: 2.628484071804751
accept
L: 0.3030458696261674
-----iter-----
LM loss: 8624811.965737557
reject
L: 3.3335045658878415
-----iter-----
LM loss: 2.385697992666576
accept
L: 0.3703893962097602
-----iter-----
LM loss: 8661573.26739865
reject
L: 4.074283358307362
-----iter-----
LM loss: 2.3001561988667447
accept
L: 0.4526981509230402
-----iter-----
LM loss: 8588367.962377366
reject
L: 4.979679660153442
-----iter-----
LM loss: 2.2008950972695205
accept
L: 0.5532977400170491

```

```

-----iter-----
LM loss: 8461299.362177784
reject
L: 6.08627514018754
-----iter-----
LM loss: 2.127286067178282
accept
L: 0.6762527933541711
-----iter-----
LM loss: 8272814.666194783
reject
L: 7.438780726895882
-----iter-----
LM loss: 2.088573032073135
accept
L: 0.8265311918773202
-----iter-----
LM loss: 7830093.0659256065
reject
L: 9.091843110650522
-----iter-----
LM loss: 2.0635863364944993
accept
L: 1.0102047900722804
-----iter-----
LM loss: 6805354.985897078
reject
L: 11.112252690795085
-----iter-----
LM loss: 2.044365149630932
accept
L: 1.2346947434216762
-----iter-----
LM loss: 1807503.4548837973
reject
L: 13.581642177638438
-----iter-----
LM loss: 2.017651625203077
accept
L: 1.5090713530709374
-----iter-----
LM loss: 1.9105798772960185
accept
L: 0.16767459478565971
-----iter-----
LM loss: 1.4690277108093541
accept
L: 0.018630510531739967

```

```
-----iter-----
LM loss: 12.663267144373556
reject
L: 0.20493561584913964
-----iter-----
LM loss: 1.3022199572143198
accept
L: 0.022770623983237738
-----iter-----
LM loss: 53.175384676523784
reject
L: 0.2504768638156151
-----iter-----
LM loss: 1.2222567989533968
accept
L: 0.02783076264617946
-----iter-----
LM loss: 7.095903146417148
reject
L: 0.30613838910797403
-----iter-----
LM loss: 1.1167127843956843
accept
L: 0.03401537656755267
-----iter-----
LM loss: 1.0703422354057703
accept
L: 0.0037794862852836304
-----iter-----
LM loss: 14.937373514157867
reject
L: 0.041574349138119936
-----iter-----
LM loss: 1.0670521260936703
accept
L: 0.0046193721264577705
-----iter-----
LM loss: 1.0863020456443466
reject
L: 0.05081309339103548
-----iter-----
LM loss: 1.0215447651299634
accept
L: 0.005645899265670609
-----iter-----
LM loss: 1.059200167903654
reject
L: 0.0621048919223767
```

```
-----iter-----
LM loss: 1.0153250805637362
accept
L: 0.006900543546930744
-----iter-----
LM loss: 1.0150003219862578
accept
L: 0.0007667270607700827
-----iter-----
LM loss: 129.14706609532365
reject
L: 0.00843399766847091
-----iter-----
LM loss: 1.0929753145825958
reject
L: 0.09277397435318
-----iter-----
LM loss: 1.0017116950722231
accept
L: 0.010308219372575554
-----iter-----
LM loss: 1.0362673404276905
reject
L: 0.11339041309833109
-----iter-----
LM loss: 0.9982185942758852
accept
L: 0.012598934788703454
-----iter-----
LM loss: 0.9975460081374451
accept
L: 0.0013998816431892726
-----iter-----
LM loss: 1.001864022071938
reject
L: 0.015398698075081999
-----iter-----
LM loss: 0.9971755406404218
accept
L: 0.0017109664527868887
-----iter-----
LM loss: 1.0078865096268372
reject
L: 0.018820630980655777
-----iter-----
LM loss: 0.9969449014021601
accept
L: 0.002091181220072864
```



```

-----iter-----
LM loss: 1.0060862139746118
reject
L: 0.023002993420801504
-----iter-----
LM loss: 0.996989057584667
reject
L: 0.2530329276288166
-----iter-----
LM loss: 0.9967624640298572
accept
L: 0.028114769736535174
-----iter-----
LM loss: 0.996844931102197
reject
L: 0.30926246710188693
-----iter-----
LM loss: 0.9967206338369751
accept
L: 0.0343624963446541
-----iter-----
LM loss: 0.9959110825176788
accept
L: 0.0038180551494060113
-----iter-----
LM loss: 0.9960417734949428
reject
L: 0.04199860664346612
-----iter-----
LM loss: 0.995890638440794
accept
L: 0.004666511849274014
-----iter-----
LM loss: 0.9957885837273643
accept
L: 0.0005185013165860015
-----iter-----
LM loss: 1.0272478687047502
reject
L: 0.005703514482446017
-----iter-----
LM loss: 0.9953610663883262
accept
success

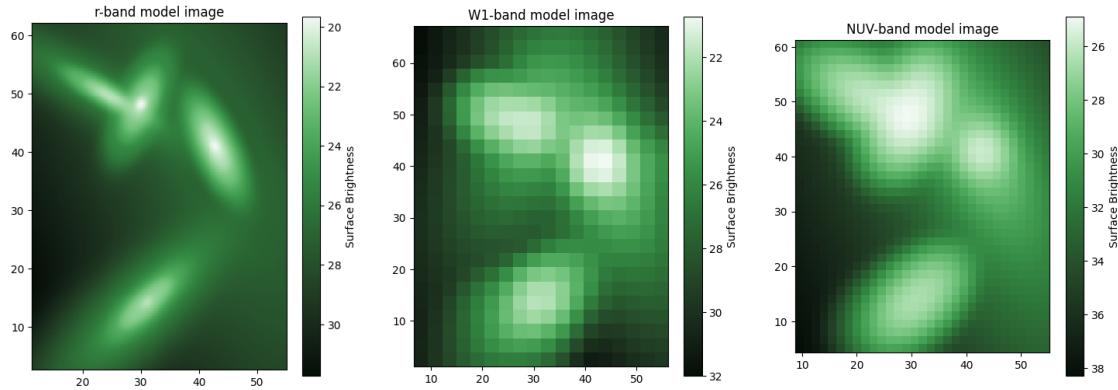
```

```

[13]: fig1, ax1 = plt.subplots(1, 3, figsize = (18,6))
      ap.plots.model_image(fig1, ax1, MODEL)

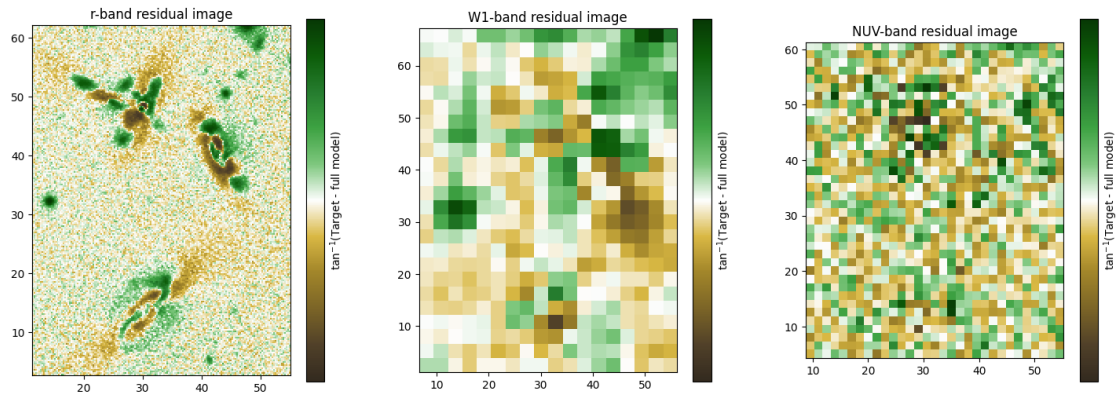
```

```
ax1[0].set_title("r-band model image")
ax1[1].set_title("W1-band model image")
ax1[2].set_title("NUV-band model image")
plt.show()
```



The models look excellent! The power of multiband fitting lets us know that we have extracted all the available information here, no forced photometry required!

```
[14]: fig, ax = plt.subplots(1, 3, figsize = (18,6))
ap.plots.residual_image(fig, ax, MODEL)
ax[0].set_title("r-band residual image")
ax[1].set_title("W1-band residual image")
ax[2].set_title("NUV-band residual image")
plt.show()
```



The residuals look acceptable, but clearly there is more structure to be found in these galaxies, this is especially apparent in the r-band data. At least for the lower galaxy, we can see in the observed image that there are spiral arms, those can easily cause large scale residual patterns.

1.1.1 Dithered images

Note that it is not necessary to use images from different bands. Using dithered images one can effectively achieve higher resolution. It is possible to simultaneously fit dithered images with AutoProf instead of postprocessing the two images together. This will of course be slower, but may be worthwhile for cases where extra care is needed.

1.1.2 Stacked images

Like dithered images, one may wish to combine the statistical power of multiple images but for some reason it is not clear how to add them. In this case one can simply have AutoProf fit the images simultaneously. Again this is slower than if the image could be combined, but should extract all the statistical power from the data.

1.1.3 Time series

Some objects change over time. For example they may get brighter and dimmer, or may have a transient feature appear. However, the structure of an object may remain constant. An example of this is a supernova and its host galaxy. The host galaxy likely doesn't change across images, but the supernova does. It is possible to fit a time series dataset with a shared galaxy model across multiple images, and a shared position for the supernova, but a variable brightness for the supernova over each image.

It is possible to get quite creative with joint models as they allow one to fix selective features of a model over a wide range of data. If you have a situation which may benefit from joint modelling but are having a hard time determining how to format everything, please do contact us!

[]: