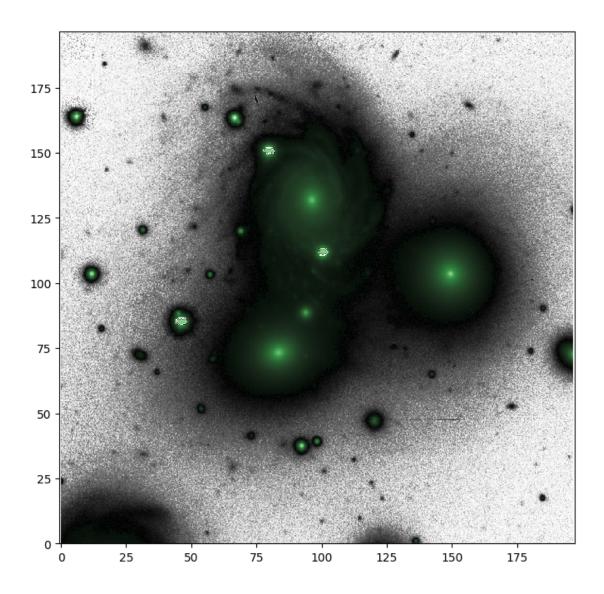
GroupModels

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1 Group Models

Here you will learn how to combine models together into a larger, more complete, model of a given system. This is a powerful and necessary capability when analysing objects in crowded environments. As telescopes achieve ever deeper photometry we have learned that all environments are crowded when projected onto the sky!

```
[1]: import autophot as ap
  import numpy as np
  import torch
  from astropy.io import fits
  import matplotlib.pyplot as plt
  from scipy.stats import iqr
```



```
[3]: # We can see that there are some blown out stars in the image. There isn't muchulathat can be done with them except

# to mask them. A very careful modeller would only mask the blown out pixelsuland then try to fit the rest, but

# today we are not very careful modellers.

mask = np.zeros(target_data.shape, dtype = bool)

mask[410:445,371:402] = True

mask[296:357 ,151:206] = True

mask[558:590,291:322] = True

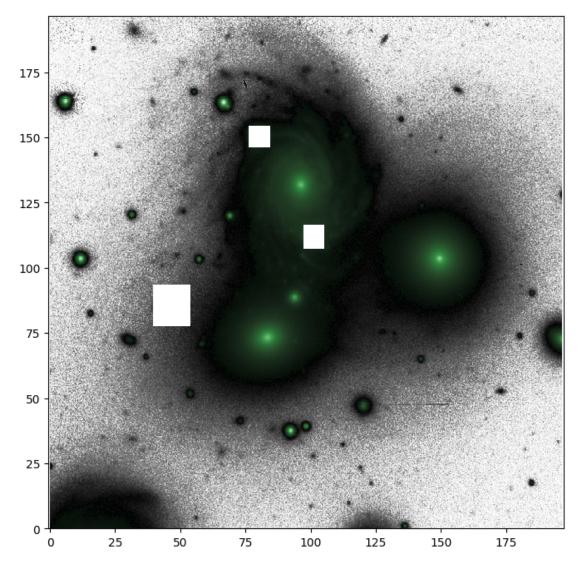
# Note that it is also possible to set a mask just for an individual model.

Simply create a mask in the same way as

# above. Just note that the mask should have the same shape as the model window

instead of the whole image.
```

```
pixelscale = 0.262
target2 = ap.image.Target_Image(
    data = target_data,
    pixelscale = pixelscale,
    zeropoint = 22.5,
    mask = mask, # now the target image has a mask of bad pixels
    variance = 0.001*np.abs(target_data + iqr(target_data,rng=[16,84])/2), # we___
create a variance image, if the image is in counts then variance image =___
image, in this case the sky has been subtracted so we add back in a certain__
amount of variance
)
fig2, ax2 = plt.subplots(figsize = (8,8))
ap.plots.target_image(fig2, ax2, target2)
plt.show()
```

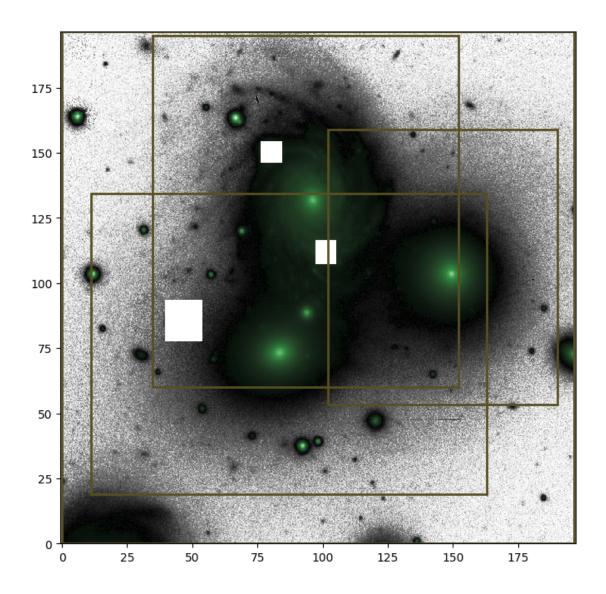


1.1 Group Model

A group model takes a list of other AutoPhot_Model objects and tracks them such that they can be treated as a single larger model. When "initialize" is called on the group model, it simply calls "initialize" on all the individual models. The same is true for a number of other functions like finalize, sample, and so on. For fitting, however, the group model will collect the parameters from all the models together and pass them along as one group to the optimizer. When saving a group model, all the model states will be collected together into one large file.

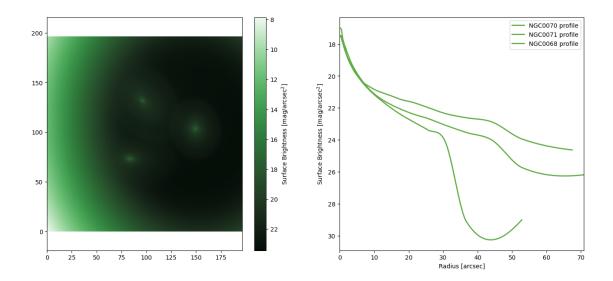
The main difference when constructing a group model is that you must first create all the sub models that will go in it. Once constructed, a group model behaves just like any other model, in fact they are all built from the same base class.

```
[4]: # first we make the list of models to fit
     # Note that we do not assign a target to these models at construction. This is _{\sqcup}
      ⇒ just a choice of style, it is possible
     # to provide the target to each model separately if you wish. Note as well that \Box
      ⇔since a target isn't provided we need
     # to give the windows in arcsec instead of pixels, to do this we provide the
      →window in the format (xmin, xmax, ymin, ymax)
    model kwargs = [
         {"name": "sky", "model_type": "flat sky model", "window": np.
      \rightarrowarray([0,0,750,750])*pixelscale},
         {"name": "NGC0070", "model_type": "spline galaxy model", "window": np.
      →array([133,229,581,744])*pixelscale},
         {"name": "NGC0071", "model_type": "spline galaxy model", "window": np.
      \Rightarrowarray([43,72,622,513])*pixelscale},
         {"name": "NGC0068", "model_type": "spline galaxy model", "window": np.
      →array([390,204,726,607])*pixelscale},
    model_list = []
    for M in model_kwargs:
        model_list.append(ap.models.AutoPhot_Model(target = target2, **M))
    VV166Group = ap.models.AutoPhot_Model(name = "VV166 Group", model_type = "group_
      fig3, ax3 = plt.subplots(figsize = (8,8))
    ap.plots.target_image(fig3, ax3, VV166Group.target)
    ap.plots.model_window(fig3, ax3, VV166Group)
    plt.show()
```



```
[5]: # See if AutoPhot can figure out starting parameters for these galaxies
VV166Group.initialize()

# The results are reasonable starting points, though far from a good model
fig4, ax4 = plt.subplots(1,2,figsize = (16,7))
ap.plots.model_image(fig4, ax4[0], VV166Group)
for M in VV166Group.models.values():
    if M.name == "sky": continue
    ap.plots.galaxy_light_profile(fig4, ax4[1], M)
plt.legend()
plt.show()
```



[6]: # Allow AutoPhot to fit the target image with all 3 models simultaneously. In_
total this is about 80 parameters!

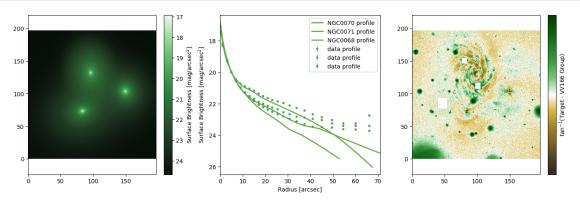
result = ap.fit.LM(VV166Group, verbose = 1).fit()

print(result.message)

-----init-----LM loss: 9.37316066374131 L: 1.0 ----iter----LM loss: 7.843478120691936 accept L: 0.1111111111111111 -----iter----LM loss: 6259.694209844605 reject L: 1.222222222222 -----iter-----LM loss: 7.245507959053041 accept L: 0.13580246913580246 -----iter-----LM loss: 6.732721755632228 accept L: 0.015089163237311385 ----iter----LM loss: 6.5958565919735355 accept L: 0.0016765736930345982 ----iter----

L: 1.0

```
LM loss: 6.58928626136843
accept
L: 0.00018628596589273313
-----iter-----
LM loss: 6.589003442923714
accept
L: 2.0698440654748124e-05
-----iter-----
LM loss: 6.588986850624965
accept
success
```



```
[8]: # To access parameters in a group model you use the same syntax as usual, but with the model name as well:

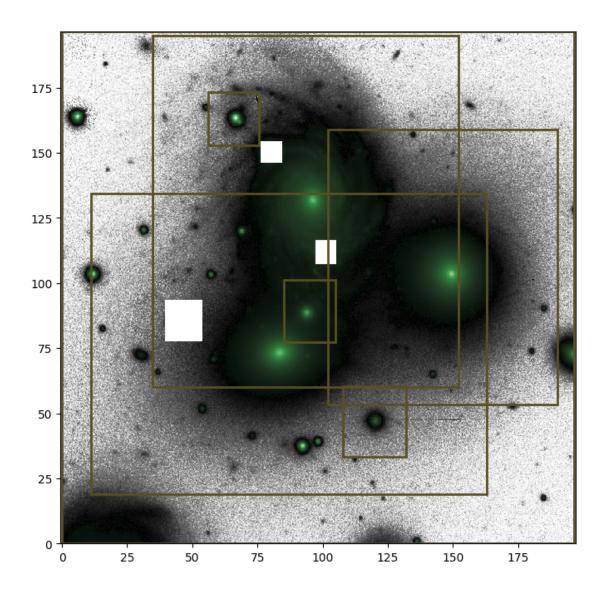
print(VV166Group["NGC0070:PA"])

print(VV166Group["NGC0071:PA"])
```

PA: 0.1127002573243426 +- 0.06 [radians, (tensor(0., dtype=torch.float64),

```
tensor(3.1416, dtype=torch.float64)), cyclic]
PA: 1.9034113106308783 +- 0.06 [radians, (tensor(0., dtype=torch.float64),
tensor(3.1416, dtype=torch.float64)), cyclic]
```

```
[10]: fig6, ax6 = plt.subplots(figsize = (8,8))
ap.plots.target_image(fig6, ax6, VV166Group.target)
ap.plots.model_window(fig6, ax6, VV166Group)
plt.show()
```



```
[11]: # Initialize will only set parameter values for the new models, the old ones_u will just be skipped

VV166Group.initialize()
```

[12]: result = ap.fit.LM(VV166Group, verbose = 1).fit()
print(result.message)

L: 1.0 -----init-----LM loss: 5.228954767072542 L: 1.0 -----iter-----

LM loss: 703301224181332.2

reject

L: 11.0 -----iter-----LM loss: 41.00008011123288 reject L: 121.0 -----iter----LM loss: 5.216126090029055 accept L: 13.4444444444445 -----iter----LM loss: 4.970789869890652 accept L: 1.4938271604938271 ----iter----LM loss: 4.981269419205083 reject L: 16.432098765432098 ----iter----LM loss: 4.960194062478112 accept L: 1.8257887517146776 ----iter----LM loss: 4.91330163701114 accept L: 0.2028654168571864 -----iter----LM loss: 5.1573584362538805 reject L: 2.2315195854290506 ----iter----LM loss: 4.902273373789719 accept L: 0.24794662060322784 -----iter-----LM loss: 5.128945510741161 reject L: 2.727412826635506 -----iter----LM loss: 4.896042583183212 accept L: 0.3030458696261673 ----iter----LM loss: 4.877594397183852 accept L: 0.033671763291796365 -----iter-----

LM loss: 4.849728369132931

accept

L: 0.0037413070324218184 -----iter-----LM loss: 10.484490162426617 reject L: 0.04115437735664 -----iter-----LM loss: 4.8385834738434985 accept L: 0.004572708595182222 -----iter----LM loss: 10.308852753566589 reject L: 0.050299794547004444 ----iter----LM loss: 10.721193995559156 reject L: 0.5532977400170489 -----iter-----LM loss: 4.837191885918613 accept L: 0.06147752666856099 ----iter----LM loss: 10.706775258788106 reject L: 0.6762527933541709 ----iter----LM loss: 4.8359571607650516 accept L: 0.07513919926157454 ----iter----LM loss: 10.39270214935872 reject L: 0.8265311918773199 -----iter-----LM loss: 10.610108663243802 reject L: 9.091843110650519 -----iter-----LM loss: 4.835848508975202 accept L: 1.01020479007228 ----iter----LM loss: 4.826977189150454 accept L: 0.11224497667469777

-----iter-----LM loss: 9.209266405113462

reject

L: 1.2346947434216755

LM loss: 10.355829802248225

reject

L: 13.58164217763843

LM loss: 4.821084380624885

accept

L: 1.5090713530709368

LM loss: 10.178371078386798

reject

L: 16.599784883780305

LM loss: 4.8175543405509185

accept

L: 1.8444205426422562

LM loss: 7.69488160574479

reject

L: 20.288625969064817

LM loss: 4.815038537777016

accept

L: 2.254291774340535

-----iter-----LM loss: 4.785574213655972

accept

L: 0.250476863815615

LM loss: 4.778356369364198

accept

L: 0.027830762646179445

LM loss: 4.77379804808698

accept

L: 0.003092306960686605

LM loss: 4.772033170053745

accept

L: 0.00034358966229851165

-----iter-----

LM loss: 4.771801103557408

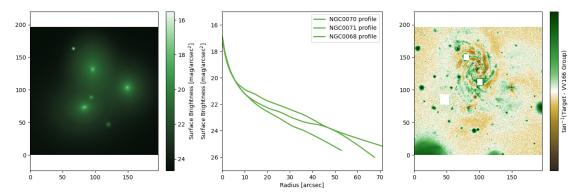
accept

L: 3.8176629144279075e-05

LM loss: 4.771777253437441

accept

```
[13]: # Now we can see what the fitting has produced
fig7, ax7 = plt.subplots(1,3,figsize = (17,5))
ap.plots.model_image(fig7, ax7[0], VV166Group)
# let's just plot the 3 main object profiles
for M in VV166Group.models.values():
    if not "NGC" in M.name: continue
        ap.plots.galaxy_light_profile(fig7, ax7[1], M)
ax7[1].legend()
ax7[1].set_ylim([27,15])
ap.plots.residual_image(fig7, ax7[2], VV166Group)
plt.show()
```

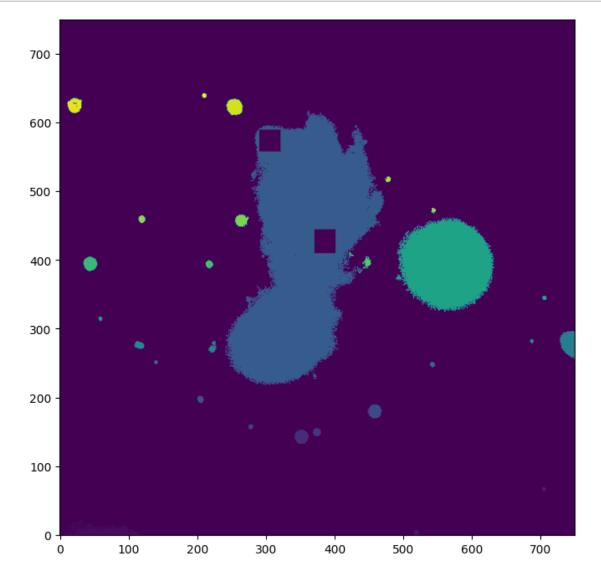


Which is even better than before. As more models are added, the fit should improve. In principle one could model eventually add models for every little smudge in the image. In practice, it is often better to just mask anything below a certain size.

1.2 Working with segmentation maps

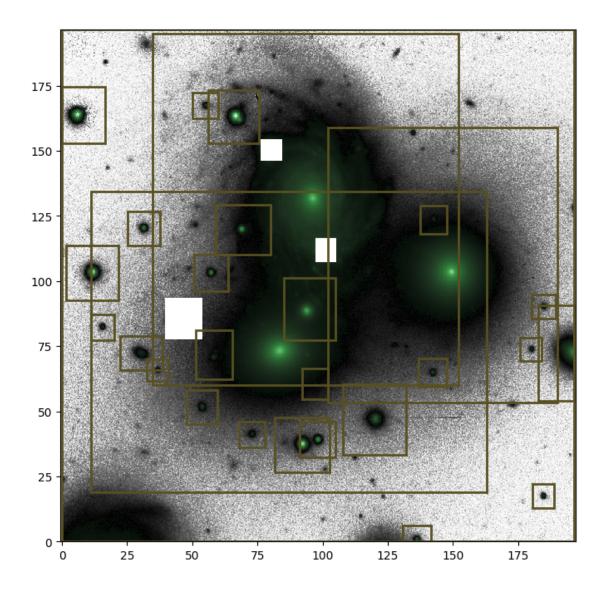
A segmentation map provides information about the contents of an image. It gives the location and shape of any object which the algorithm was able to separate out and identify. This is exactly the information needed to construct the windows for a collection of AutoPhot models.

Photutils provides an easy to use segmentation map implimentation so we use it here for simplicity. In many cases it may be required to use a more detailed segmentation map algorithm such as those implimented in Source Extractor and ProFound (among others), the principle is the same however since the end product for all of them has the same format.



```
[15]: # This will convert the segmentation map into boxes that enclose the identified pixels windows = ap.utils.initialize.windows_from_segmentation_map(segmap.data)
```

```
# Next we filter out any segments which are too big, these are the NGC models ...
              ⇔we already have set up
            windows = ap.utils.initialize.filter_windows(windows, max_size = 100)
            # Next we scale up the windows so that AutoPhot can fit the faint parts of each
              ⇔object as well
            windows = ap.utils.initialize.scale_windows(windows, image_shape = target_data.
              ⇒shape, expand_scale = 3, expand_border = 10)
            del windows[20] # this is a segmented chunk of spiral arm, not a galaxy
            del windows[23] # this is a segmented chunk of spiral arm, not a galaxy
            del windows[24] # this is a segmented chunk of spiral arm, not a galaxy
            del windows[28] # this is a segmented chunk of spiral arm, not a galaxy
            del windows[29] # this is a repeat of little 2
            del windows[7] # this is a repeat of little 3
            print(windows)
          {2: [[499, 540], [0, 24]], 3: [[689, 721], [49, 84]], 4: [[312, 392], [102,
          182]], 5: [[348, 401], [123, 176]], 6: [[259, 297], [138, 176]], 8: [[183, 227],
           [172, 222]], 10: [[352, 390], [209, 253]], 11: [[522, 563], [227, 268]], 12:
           [[124, 156], [235, 267]], 13: [[697, 750], [206, 346]], 14: [[196, 249], [238,
          309]], 15: [[85, 147], [251, 301]], 16: [[671, 703], [264, 299]], 17: [[42, 77],
           [295, 333]], 19: [[688, 723], [327, 362]], 21: [[6, 83], [354, 434]], 22: [[193,
          243], [367, 420]], 25: [[225, 305], [420, 494]], 26: [[96, 143], [434, 484]],
          27: [[525, 563], [451, 492]], 30: [[0, 63], [583, 666]], 31: [[191, 229], [620,
          658]]}
[16]: # Now we use all the windows to add to the list of models
            seg models = []
            for win in windows:
                    seg models.append({"name": f"minor object {win:02d}", "window": | 
              Government of the service of th
            # we make a new set of models for simplicity
            for M in seg_models:
                    VV166Group.add_model(ap.models.AutoPhot_Model(**M))
            VV166Group.initialize()
[17]: fig9, ax9 = plt.subplots(figsize = (8,8))
            ap.plots.target_image(fig9, ax9, VV166Group.target)
            ap.plots.model_window(fig9, ax9, VV166Group)
            plt.show()
```



```
# This is now a very complex model composed of about 30 sub-models! In totaluse253 parameters! While it is

# possible for the AutoPhot Levenberg-Marquardt (LM) algorithm to fullyuseoptimize this model, it is faster in this

# case to apply an iterative fit. AutoPhot will apply LM optimization one modeluse at a time and cycle through all

# the models until the results converge. See the tutorial on AutoPhot fittingusefor more details on the fit methods.

result = ap.fit.Iter(VV166Group, verbose = 1).fit()

print(result.message)

# Other technques that can help for difficult fits:
# - Try running some gradient descent steps (maybe 100) before doing LM
```

```
# - Try changing the initial parameters. AutoPhot seeks a local minimum so make_
sure its the right one!

# - Fit the large models in the frame first, then add in the smaller ones_
(thats what we've done in this tutorial)

# - Fit a simplier model (say a sersic or exponential instead of spline) first,
then use that to initialize the complex model

# - Mix and match optimizers, if one gets stuck another may be better suited_
for that area of parameter space
```

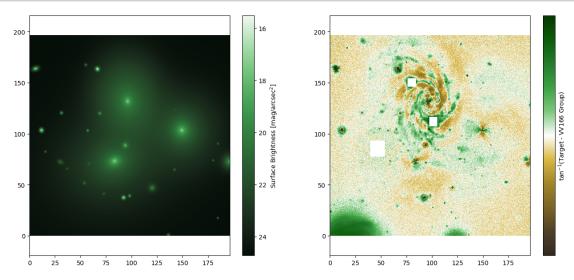
```
-----iter-----
sky
NGC0070
NGC0071
NGC0068
litte 1
litte 2
litte 3
minor object 02
minor object 03
minor object 04
minor object 05
minor object 06
minor object 08
minor object 10
minor object 11
minor object 12
minor object 13
minor object 14
minor object 15
minor object 16
minor object 17
minor object 19
minor object 21
minor object 22
minor object 25
minor object 26
minor object 27
minor object 30
minor object 31
Update Chi^2 with new parameters
Loss: 2.022182609824855
-----iter----
sky
NGC0070
NGC0071
NGC0068
```

litte 1

```
litte 2
litte 3
minor object 02
minor object 03
minor object 04
minor object 05
minor object 06
minor object 08
minor object 10
minor object 11
minor object 12
minor object 13
minor object 14
minor object 15
minor object 16
minor object 17
minor object 19
minor object 21
minor object 22
minor object 25
minor object 26
minor object 27
minor object 30
minor object 31
Update Chi^2 with new parameters
Loss: 2.0208557640251055
-----iter----
sky
NGC0070
NGC0071
NGC0068
litte 1
litte 2
litte 3
minor object 02
minor object 03
minor object 04
minor object 05
minor object 06
minor object 08
minor object 10
minor object 11
minor object 12
minor object 13
minor object 14
minor object 15
minor object 16
minor object 17
```

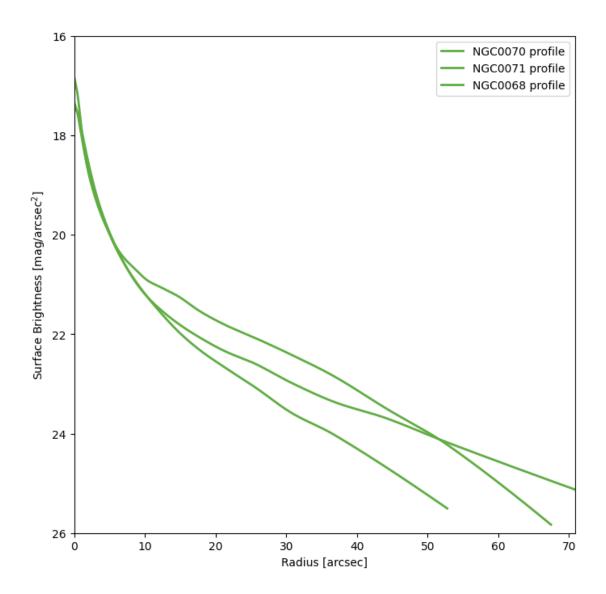
```
minor object 19
     minor object 21
     minor object 22
     minor object 25
     minor object 26
     minor object 27
     minor object 30
     minor object 31
     Update Chi^2 with new parameters
     Loss: 2.0207513909751977
     -----iter----
     sky
     NGC0070
     NGC0071
     NGC0068
     litte 1
     litte 2
     litte 3
     minor object 02
     minor object 03
     minor object 04
     minor object 05
     minor object 06
     minor object 08
     minor object 10
     minor object 11
     minor object 12
     minor object 13
     minor object 14
     minor object 15
     minor object 16
     minor object 17
     minor object 19
     minor object 21
     minor object 22
     minor object 25
     minor object 26
     minor object 27
     minor object 30
     minor object 31
     Update Chi^2 with new parameters
     Loss: 2.020715413118375
     success
[19]: # Indeed the fit converges successfully! These tricks are really useful for
       ⇔complex fits.
```

```
# Now we can see what the fitting has produced
fig10, ax10 = plt.subplots(1,2,figsize = (16,7))
ap.plots.model_image(fig10, ax10[0], VV166Group)
ap.plots.residual_image(fig10, ax10[1], VV166Group)
plt.show()
```



Now that's starting to look like a complete model, and the Chi^2/ndf is much lower! And all for very little effort considering the level of detail. Looking at the residuals there is a clear improvement from the other attempts, that said there is a lot of structure in the residuals around the small objects, suggesting that a sersic alone is not the best model for these galaxies. That's not too surprising, at the very least we should apply PSF convolution to the models to get the proper blurring. PSF convolution is very slow though, so it would be best to do on a GPU, which you can try out if you have access to one! Simply set psf_mode = "full" and run fit again. For now though, we'll forgo the PSF convolution in the interest of time.

```
fig8, ax8 = plt.subplots(figsize = (8,8))
# let's just plot the 3 main object profiles
for M in VV166Group.models.values():
    if not "NGC" in M.name: continue
        ap.plots.galaxy_light_profile(fig8, ax8, M)
ax8.legend()
ax8.set_ylim([26,16])
plt.show()
```



[]: