# ModelZoo

April 1, 2023

# 1 Model Zoo

In this notebook you will see every kind of model in AutoProf. Printed in each cell will also be the list of parameters which the model looks for while fitting. Many models have unique capabilities and features, this will be introduced here, though fully taking advantage of them will be dependent on your science case.

For a family tree of all the AutoProf models see this link

Note, we will not be covering Group\_Model here as that requires a dedicated discussion. See the dedicated notebook for that.

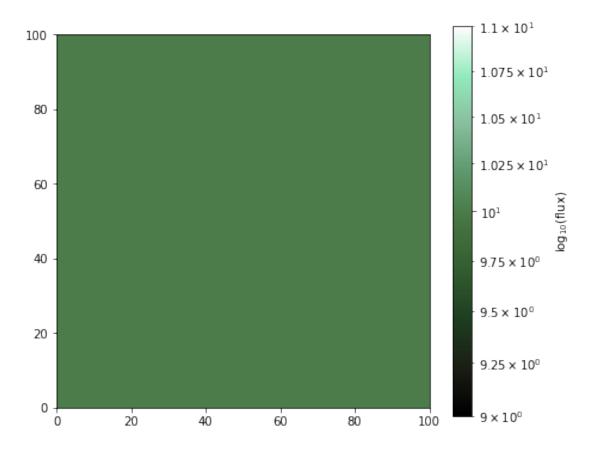
```
[1]: import autoprof as ap
  import numpy as np
  import torch
  import matplotlib.pyplot as plt
  %matplotlib inline
  basic_target = ap.image.Target_Image(np.zeros((100,100)), pixelscale = 1)
```

# 1.1 Sky Models

#### 1.1.1 Flat Sky Model

('log10(flux/arcsec^2)',)

```
1
```



# 1.1.2 Plane Sky Model

('flux/arcsec^2', 'sky/arcsec')

```
[3]: M = ap.models.AutoProf_Model(name = "plane sky", model_type = "plane sky"

→model", parameters = {"center":[50,50], "sky": 10, "delta": [1e-2,2e-2]},

→target = basic_target)

print(M.parameter_order())

print(tuple(M.parameters[P].units for P in M.parameter_order()))

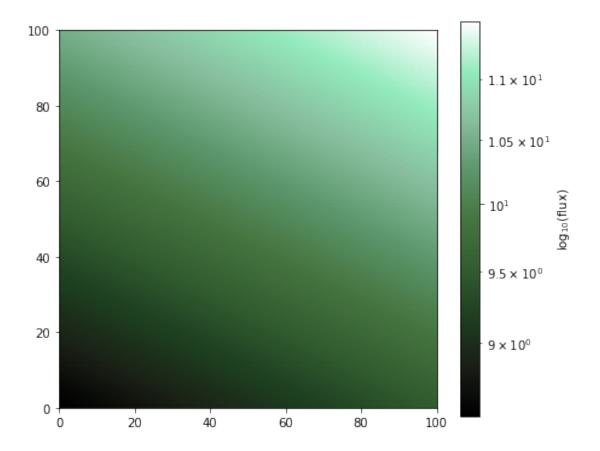
M.initialize()

fig, ax = plt.subplots(figsize = (7,6))

ap.plots.model_image(fig, ax, M)

plt.show()

('sky', 'delta')
```



# 1.2 Star Models

#### 1.2.1 PSF Star

```
from scipy.special import jv

xx, yy = np.meshgrid(np.linspace(-49,49,99), np.linspace(-49,49,99))

x = np.sqrt(xx**2 + yy**2)/5 +1e-6

PSF = (2*jv(1, x)/x)**2 + 1e-4 # the PSF can be any image, here we construct and airy disk

target = ap.image.Target_Image(data = np.zeros((100,100)), pixelscale = 1, psfu = PSF) # the target image holds the PSF for itself

M = ap.models.AutoProf_Model(name = "psf star", model_type = "psf star model",u target = target, parameters = {"center": [49.5,49.5], "flux": 1})

print(M.parameter_order())

print(tuple(M.parameters[P].units for P in M.parameter_order()))

M.initialize()

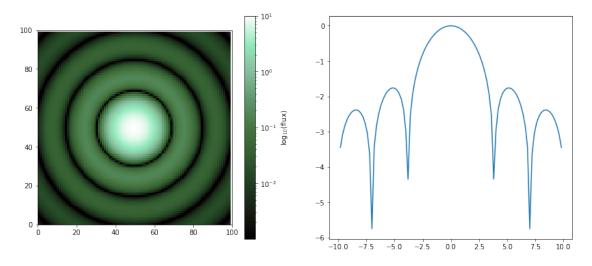
fig, ax = plt.subplots(1,2, figsize = (14,6))

ap.plots.model_image(fig, ax[0], M)

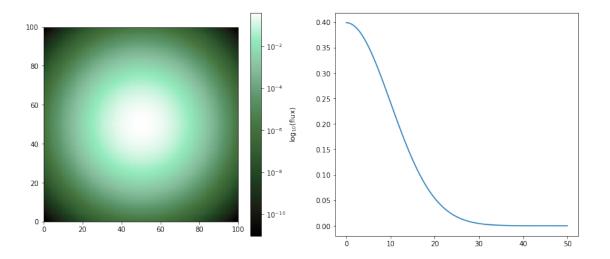
x = np.linspace(-49,49,99)/5 + 1e-6
```

```
ax[1].plot(x, np.log10((2*jv(1, x)/x)**2))
plt.show()
```

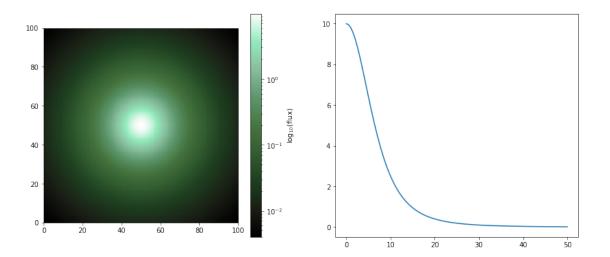
```
('center', 'flux')
('arcsec', 'log10(flux/arcsec^2)')
```



#### 1.2.2 Gaussian Star



# 1.2.3 Moffat Star

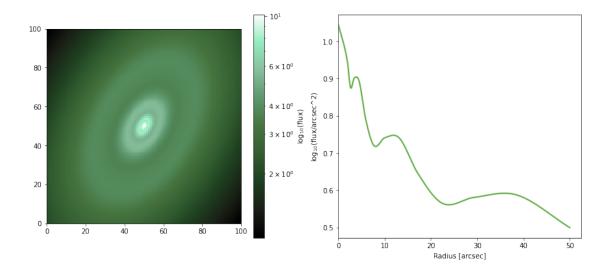


# 2 Galaxy Models

#### 2.0.1 Spline Galaxy Model

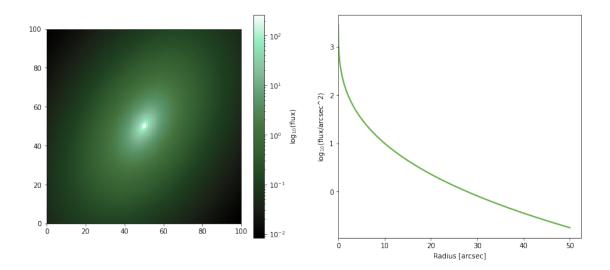
```
[7]: # Here we make an arbitrary spline profile out of a sine wave and a line
     x = np.linspace(0,10,14)
     spline_profile = np.sin(x*2+2)/20 + 1 - x/20
     # Here we write down some corresponding radii for the points in the
     →non-parametric profile. AutoProf will make
     # radii to match an input profile, but it is generally better to manually ...
     →provide values so you have some control
     # over their placement. Just note that it is assumed the first point will be at |
     \hookrightarrow R = 0.
     NP_prof = [0] + list(np.logspace(np.log10(2),np.log10(50),13))
     M = ap.models.AutoProf Model(name = "spline galaxy", model type = "spline"
     →galaxy model", parameters = {"center": [50,50], "q": 0.6, "PA": 60*np.pi/
     →180, "I(R)": {"value": spline_profile, "prof": NP_prof}}, target =
     →basic_target)
     print(M.parameter_order())
     print(tuple(M.parameters[P].units for P in M.parameter_order()))
     M.initialize()
     fig, ax = plt.subplots(1,2, figsize = (14,6))
     ap.plots.model_image(fig, ax[0], M)
     ap.plots.galaxy_light_profile(fig,ax[1],M)
     plt.show()
    ('center', 'q', 'PA', 'I(R)')
```

('arcsec', 'b/a', 'radians', 'log10(flux/arcsec^2)')



# 2.0.2 Sersic Galaxy Model

```
('center', 'q', 'PA', 'n', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'none', 'arcsec', 'log10(flux/arcsec^2)')
```

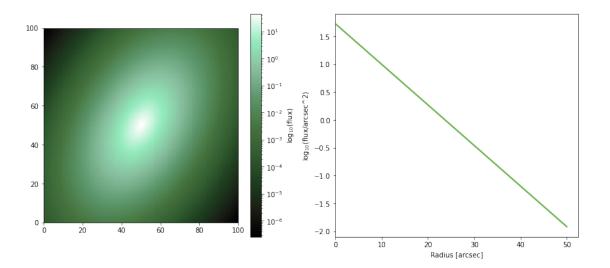


# 2.0.3 Exponential Galaxy Model

```
[9]: M = ap.models.AutoProf_Model(name = "exponential galaxy", model_type =

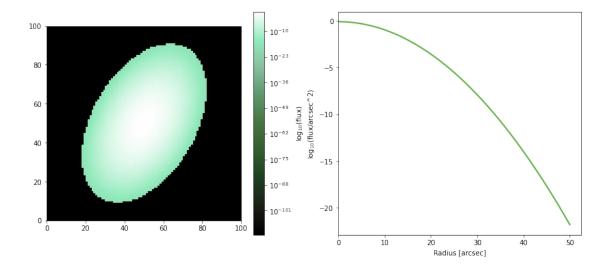
→ "exponential galaxy model", parameters = {"center": [50,50], "q": 0.6, "PA":
□
     →60*np.pi/180, "Re": 10, "Ie": 1}, target = basic_target)
     print(M.parameter_order())
     print(tuple(M.parameters[P].units for P in M.parameter_order()))
     M.initialize()
     fig, ax = plt.subplots(1,2, figsize = (14,6))
     ap.plots.model_image(fig, ax[0], M)
     ap.plots.galaxy_light_profile(fig,ax[1],M)
     plt.show()
    ('center', 'q', 'PA', 'Re', 'Ie')
```

```
('arcsec', 'b/a', 'radians', 'arcsec', 'log10(flux/arcsec^2)')
```



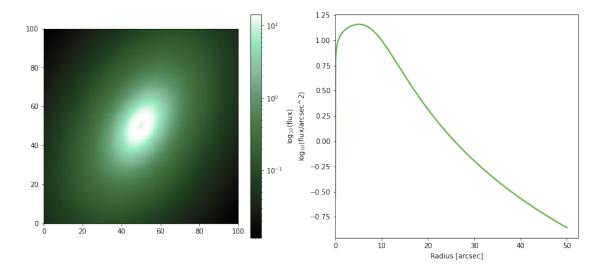
# 2.0.4 Gaussian Galaxy Model

```
('center', 'q', 'PA', 'sigma', 'flux')
('arcsec', 'b/a', 'radians', 'arcsec', 'log10(flux)')
```



# 2.0.5 Nuker Galaxy Model

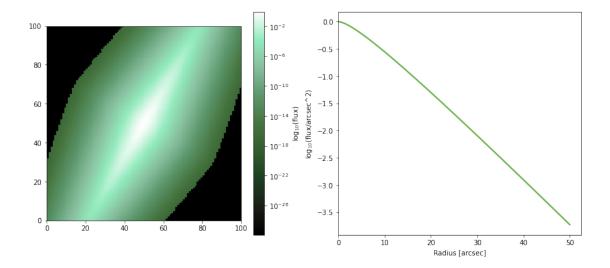
'none')



# 2.1 Edge on model

Currently there is only one dedicared edge on model, the self gravitating isothermal disk from van der Kruit & Searle 1981. If you know of another common edge on model, feel free to let us know and we can add it in!

```
('center', 'PA', 'I0', 'hs', 'rs')
('arcsec', 'rad', 'log10(flux/arcsec^2)', 'arcsec', 'arcsec')
```

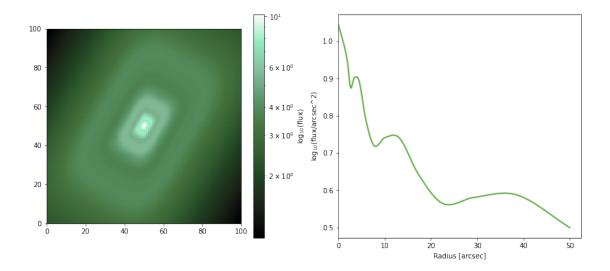


# 2.2 Super Ellipse Models

A super ellipse is a regular ellipse, except the radius metric changes from  $R = \operatorname{sqrt}(x^2 + y^2)$  to the more general:  $R = (x^C + y^C)1/C$ . The parameter C = 2 for a regular ellipse, for 0 < C < 2 the shape becomes more "disky" and for C > 2 the shape becomes more "boxy." In AutoProf we use the parameter C0 = C-2 for simplicity.

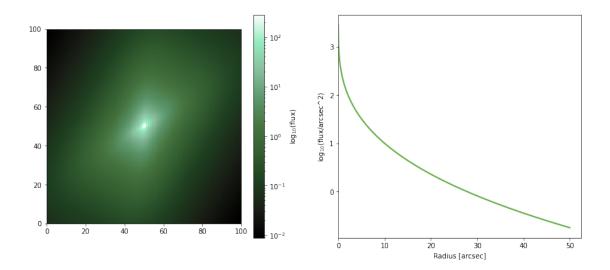
# 2.2.1 Spline SuperEllipse

('arcsec', 'b/a', 'radians', 'C-2', 'log10(flux/arcsec^2)')



# 2.2.2 Sersic SuperEllipse

```
('center', 'q', 'PA', 'CO', 'n', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'C-2', 'none', 'arcsec', 'log10(flux/arcsec^2)')
```

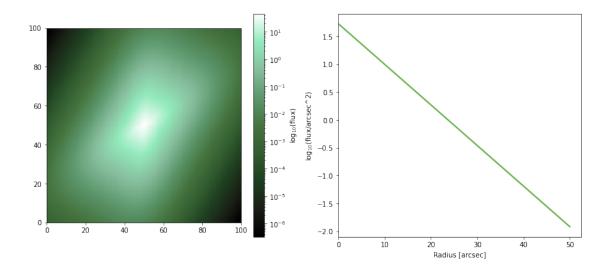


# 2.2.3 Exponential SuperEllipse

```
[15]: M = ap.models.AutoProf_Model(name = "exponential superellipse", model_type = ""exponential superellipse galaxy model", parameters = {"center": [50,50], ""q": 0.6, "PA": 60*np.pi/180, "CO": 2, "Re": 10, "Ie": 1}, target = ""obasic_target)
print(M.parameter_order())
print(tuple(M.parameters[P].units for P in M.parameter_order()))
M.initialize()

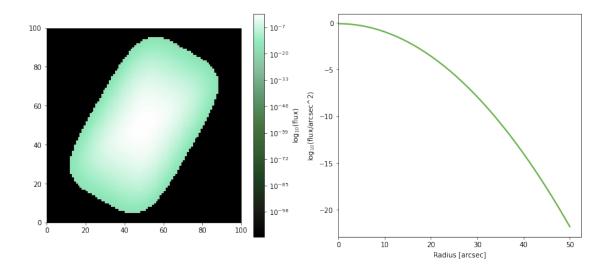
fig, ax = plt.subplots(1,2, figsize = (14,6))
ap.plots.model_image(fig, ax[0], M)
ap.plots.galaxy_light_profile(fig,ax[1],M)
plt.show()
```

```
('center', 'q', 'PA', 'CO', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'C-2', 'arcsec', 'log10(flux/arcsec^2)')
```



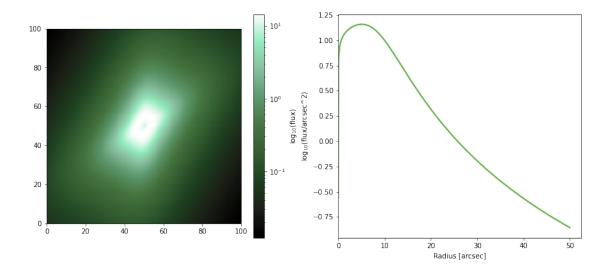
# 2.2.4 Gaussian SuperEllipse

('arcsec', 'b/a', 'radians', 'C-2', 'arcsec', 'log10(flux)')



# 2.2.5 Nuker SuperEllipse

```
('center', 'q', 'PA', 'CO', 'Rb', 'Ib', 'alpha', 'beta', 'gamma')
('arcsec', 'b/a', 'radians', 'C-2', 'arcsec', 'log10(flux/arcsec^2)', 'none',
'none', 'none')
```

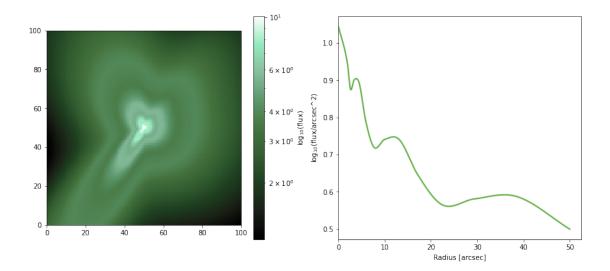


#### 2.3 Fourier Ellipse Models

A Fourier ellipse is a scaling on the radius values as a function of theta. It takes the form:  $R' = R * exp(\sum_m am * cos(m * theta + phim))$ , where am and phim are the parameters which describe the Fourier perturbations. Using the "modes" argument as a tuple, users can select which Fourier modes are used. As a rough intuition: mode 1 acts like a shift of the model; mode 2 acts like ellipticity; mode 3 makes a lopsided model (triangular in the extreme); and mode 4 makes peanut/diamond perturbations.

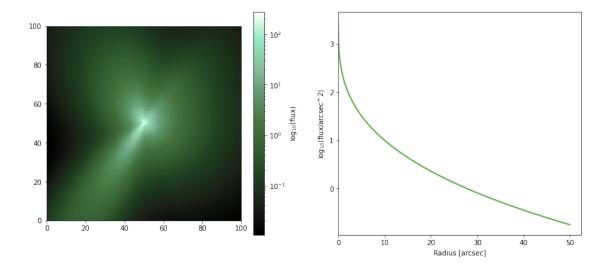
# 2.3.1 Spline Fourier

```
('center', 'q', 'PA', 'am', 'phim', 'I(R)')
('arcsec', 'b/a', 'radians', 'none', 'radians', 'log10(flux/arcsec^2)')
```

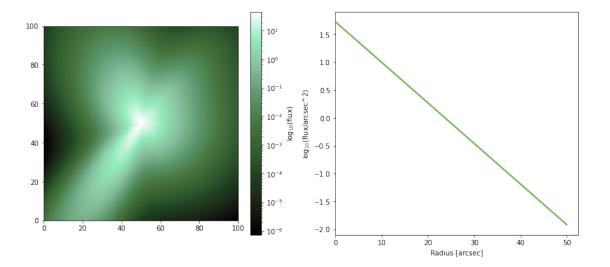


#### 2.3.2 Sersic Fourier

'log10(flux/arcsec^2)')

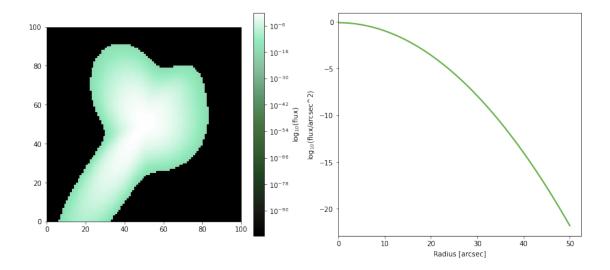


# 2.3.3 Exponential Fourier



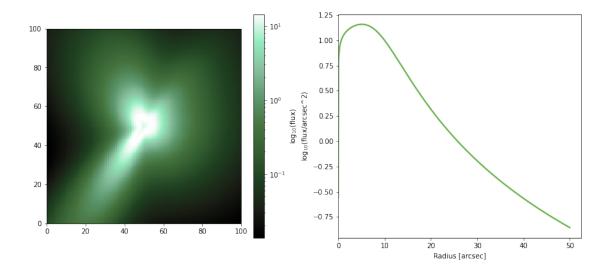
#### 2.3.4 Gaussian Fourier

```
('center', 'q', 'PA', 'am', 'phim', 'sigma', 'flux')
('arcsec', 'b/a', 'radians', 'none', 'radians', 'arcsec', 'log10(flux)')
```



# 2.3.5 Nuker Fourier

```
('center', 'q', 'PA', 'am', 'phim', 'Rb', 'Ib', 'alpha', 'beta', 'gamma')
('arcsec', 'b/a', 'radians', 'none', 'radians', 'arcsec',
'log10(flux/arcsec^2)', 'none', 'none')
```



# 2.4 Warp Model

A warp model performs a radially varying coordinate transform. Essentially instead of applying a rotation matrix **Rot** on all coordinates X,Y we instead construct a unique rotation matrix for each coordinate pair  $\mathbf{Rot}(\mathbf{R})$  where  $R = \sqrt{(X^2 + Y^2)}$ . We also apply a radially dependent axis ratio  $\mathbf{q}(\mathbf{R})$  to all the coordinates:

$$R = \sqrt{(X^2 + Y^2)}$$
 
$$X, Y = Rotate(X, Y, PA(R))$$
 
$$Y = Y/q(R)$$

The net effect is a radially varying PA and axis ratio which allows the model to represent spiral arms, bulges, or other features that change the apparent shape of a galaxy in a radially varying way.

# 2.4.1 Spline Warp

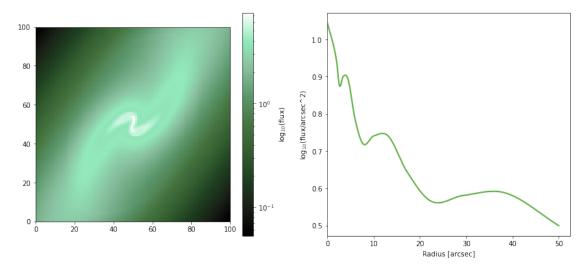
```
[23]: warp_q = np.linspace(0.1,0.4,14)
  warp_pa = np.linspace(0,np.pi-0.2,14)

M = ap.models.AutoProf_Model(name = "spline warp", model_type = "spline warp_\top \top \text{galaxy model", parameters = {"center": [50,50], "q": 0.6, "PA": 60*np.pi/\top 180, "q(R)": warp_q, "PA(R)": warp_pa, "I(R)": {"value": spline_profile,\top \top "prof": NP_prof}}, target = basic_target)
  print(M.parameter_order())
  print(tuple(M.parameters[P].units for P in M.parameter_order()))
  M.initialize()

fig, ax = plt.subplots(1,2, figsize = (14,6))
  ap.plots.model_image(fig, ax[0], M)
  ap.plots.galaxy_light_profile(fig,ax[1],M)
```

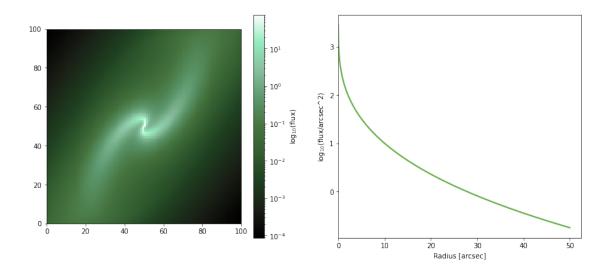
# plt.show()

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'I(R)')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'log10(flux/arcsec^2)')
```



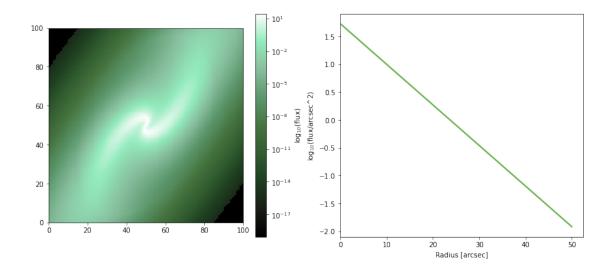
# 2.4.2 Sersic Warp

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'n', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'none', 'arcsec',
'log10(flux/arcsec^2)')
```



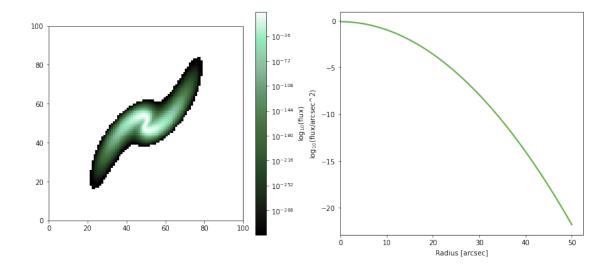
# 2.4.3 Exponential Warp

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'arcsec', 'log10(flux/arcsec^2)')
```



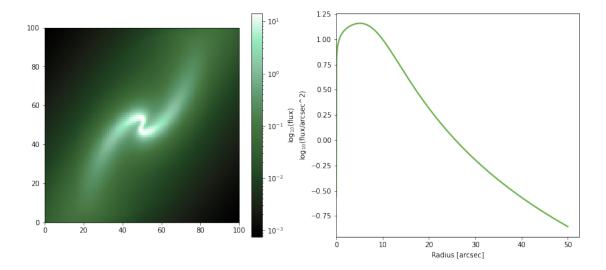
# 2.4.4 Gaussian Warp

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'sigma', 'flux')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'arcsec', 'log10(flux)')
```



# 2.4.5 Nuker Warp

('center', 'q', 'PA', 'q(R)', 'PA(R)', 'Rb', 'Ib', 'alpha', 'beta', 'gamma')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'arcsec', 'log10(flux/arcsec^2)',
'none', 'none', 'none')



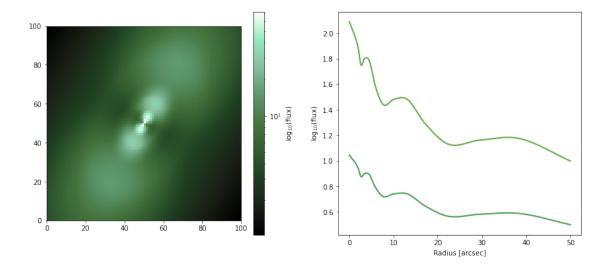
# 2.5 Ray Model

A ray model allows the user to break the galaxy up into regions that can be fit separately. There are two basic kinds of ray model: symmetric and asymetric. A symmetric ray model (symmetric\_rays = True) assumes 180 degree symmetry of the galaxy and so each ray is reflected through the center. This means that essentially the major axes and the minor axes are being fit separately. For an asymmetric ray model (symmetric\_rays = False) each ray is it's own profile to be fit separately.

In a ray model there is a smooth boundary between the rays. This smoothness is acomplished by applying a  $(\cos(r*theta)+1)/2$  weight to each profile, where r is dependent on the number of rays and theta is shifted to center on each ray in turn. The exact cosine weighting is dependent on if the rays are symmetric and if there is an even or odd number of rays.

#### 2.5.1 Spline Ray

```
('center', 'q', 'PA', 'I(R)')
('arcsec', 'b/a', 'radians', 'log10(flux/arcsec^2)')
```



# 2.5.2 Sersic Ray

```
[29]: M = ap.models.AutoProf_Model(name = "sersic ray", model_type = "sersic ray"

→galaxy model", symmetric_rays = True, rays = 2, parameters = {"center":

→[50,50], "q": 0.6, "PA": 60*np.pi/180, "n": [1,3], "Re": [10,5],"Ie": [1,0.

→5]}, target = basic_target)

print(M.parameter_order())

print(tuple(M.parameters[P].units for P in M.parameter_order()))

M.initialize()

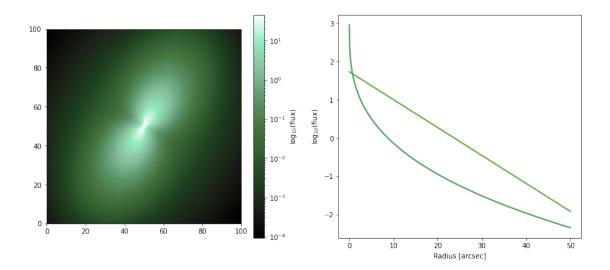
fig, ax = plt.subplots(1,2, figsize = (14,6))

ap.plots.model_image(fig, ax[0], M)

ap.plots.ray_light_profile(fig,ax[1],M)

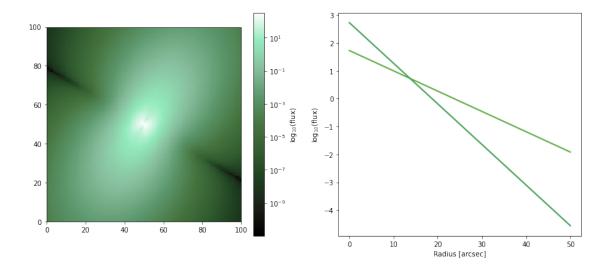
plt.show()
```

```
('center', 'q', 'PA', 'n', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'none', 'arcsec', 'log10(flux/arcsec^2)')
```



# 2.5.3 Exponential Ray

```
('center', 'q', 'PA', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'arcsec', 'log10(flux/arcsec^2)')
```



# 2.5.4 Gaussian Ray

```
[31]: M = ap.models.AutoProf_Model(name = "gaussian ray", model_type = "gaussian ray"

→ galaxy model", symmetric_rays = True, rays = 2, parameters = {"center":

→ [50,50], "q": 0.6, "PA": 60*np.pi/180, "sigma": [5,8], "flux": [1.5,1.]},

→ target = basic_target)

print(M.parameter_order())

print(tuple(M.parameters[P].units for P in M.parameter_order()))

M.initialize()

fig, ax = plt.subplots(1,2, figsize = (14,6))

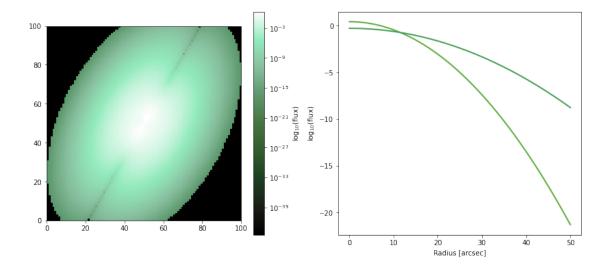
ap.plots.model_image(fig, ax[0], M)

ap.plots.ray_light_profile(fig,ax[1],M)

plt.show()

('center', 'q', 'PA', 'sigma', 'flux')

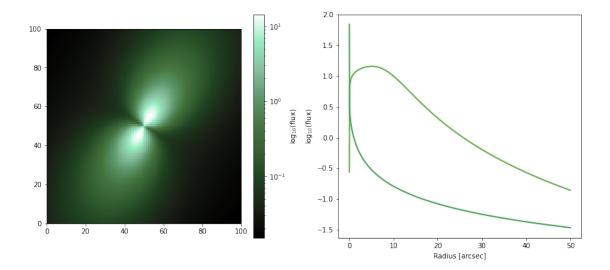
('arcsec', 'b/a', 'radians', 'arcsec', 'log10(flux)')
```



# 2.5.5 Nuker Ray

'none')

('arcsec', 'b/a', 'radians', 'arcsec', 'log10(flux/arcsec^2)', 'none', 'none',

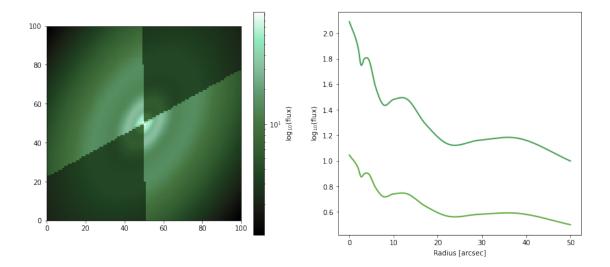


# 2.6 Wedge Model

A wedge model behaves just like a ray model, except the boundaries are sharp. This has the advantage that the wedges can be very different in brightness without the "smoothing" from the ray model washing out the dimmer one. It also has the advantage of less "mixing" of information between the rays, each one can be counted on to have fit only the pixels in it's wedge without any influence from a neighbor. However, it has the disadvantage that the discontinuity at the boundary makes fitting behave strangely when a bright spot lays near the boundary.

# 2.6.1 Spline Wedge

```
('center', 'q', 'PA', 'I(R)')
('arcsec', 'b/a', 'radians', 'log10(flux/arcsec^2)')
```



# 3 High Order Warp Models

The models below combine the Warp coordinate transform with radial behaviour transforms: SuperEllipse and Fourier. These higher order models can create highly complex shapes, though their scientific use-case is less clear. They are included for completeness as they may be useful in some specific instances. These models are also included to demonstrate the flexibility in making AutoProf models, in a future tutorial we will discuss how to make your own model types.

# 3.0.1 Spline SuperEllipse Warp

```
[34]: M = ap.models.AutoProf_Model(name = "spline super warp", model_type = "spline_\cup superellipse warp galaxy model", parameters = {"center": [50,50], "q": 0.6,\cup \to "PA": 60*np.pi/180, "q(R)": warp_q, "PA(R)": warp_pa, "CO": 2, "I(R)":\cup \to {"value": spline_profile, "prof": NP_prof}}, target = basic_target)

print(M.parameter_order())

print(tuple(M.parameters[P].units for P in M.parameter_order()))

M.initialize()

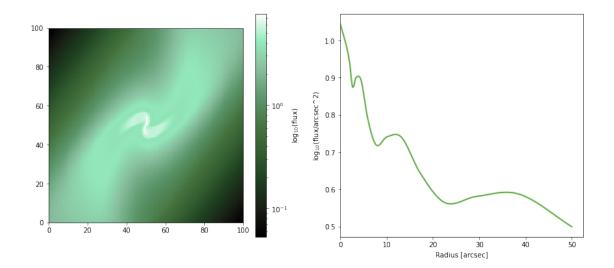
fig, ax = plt.subplots(1,2, figsize = (14,6))

ap.plots.model_image(fig, ax[0], M)

ap.plots.galaxy_light_profile(fig,ax[1],M)

plt.show()
```

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'CO', 'I(R)')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'C-2', 'log10(flux/arcsec^2)')
```

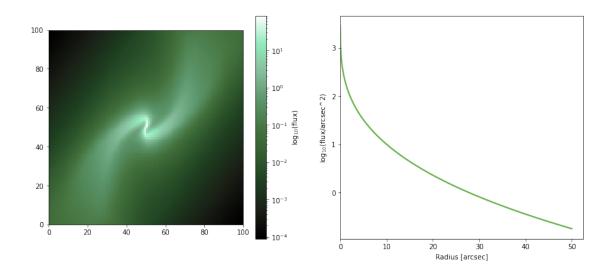


# 3.0.2 Sersic SuperEllipse Warp

```
[35]: M = ap.models.AutoProf_Model(name = "sersic super warp", model_type = "sersic_\[ \infty \superset \text{superellipse warp galaxy model", parameters = {"center": [50,50], "q": 0.6,\[ \infty \text{"PA": 60*np.pi/180, "q(R)": warp_q, "PA(R)": warp_pa, "CO": 2, "n": 3, "Re":\[ \infty \text{10, "Ie": 1}, target = basic_target) \]
print(M.parameter_order())
print(tuple(M.parameters[P].units for P in M.parameter_order()))
M.initialize()

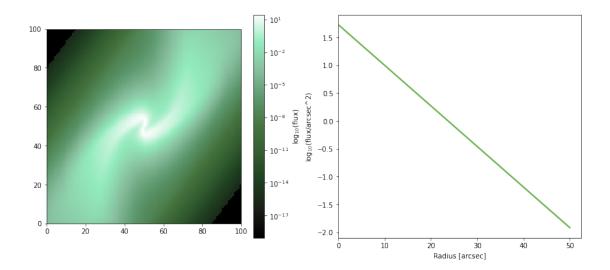
fig, ax = plt.subplots(1,2, figsize = (14,6))
ap.plots.model_image(fig, ax[0], M)
ap.plots.galaxy_light_profile(fig,ax[1],M)
plt.show()
```

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'CO', 'n', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'C-2', 'none', 'arcsec',
'log10(flux/arcsec^2)')
```



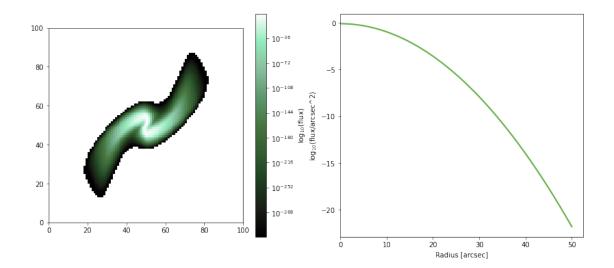
# 3.0.3 Exponential SuperEllipse Warp

'log10(flux/arcsec^2)')



# 3.0.4 Gaussian SuperEllipse Warp

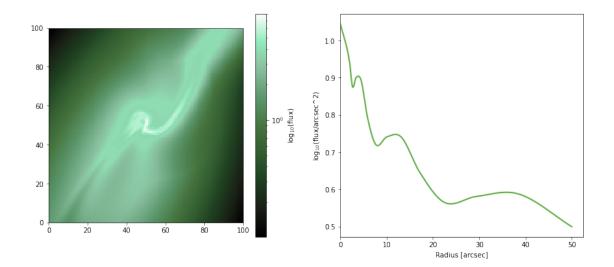
```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'CO', 'sigma', 'flux')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'C-2', 'arcsec', 'log10(flux)')
```



# 3.0.5 Spline Fourier Warp

'log10(flux/arcsec^2)')

not sure how this abomination would fit a galaxy, but you are welcome to try

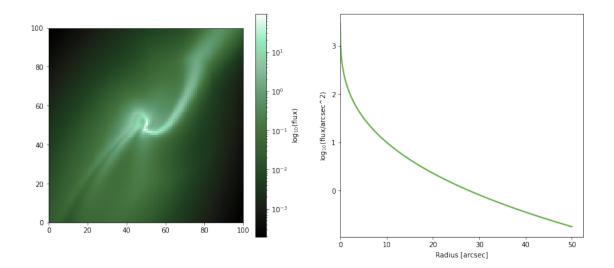


# 3.0.6 Sersic Fourier Warp

```
[39]: M = ap.models.AutoProf_Model(name = "sersic fourier warp", model_type = "sersic_\[ \sigma fourier warp galaxy model", parameters = {"center": [50,50], "q": 0.6, "PA":\[ \sigma 60*np.pi/180, "q(R)": warp_q, "PA(R)": warp_pa, "am": fourier_am, "phim":\[ \sigma fourier_phim, "n": 3, "Re": 10, "Ie": 1}, target = basic_target)
    print(M.parameter_order())
    print(tuple(M.parameters[P].units for P in M.parameter_order()))
    M.initialize()

fig, ax = plt.subplots(1,2, figsize = (14,6))
    ap.plots.model_image(fig, ax[0], M)
    ap.plots.galaxy_light_profile(fig,ax[1],M)
    plt.show()
```

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'am', 'phim', 'n', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'none', 'radians', 'none', 'arcsec',
'log10(flux/arcsec^2)')
```

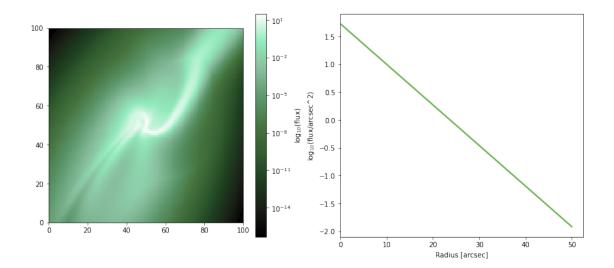


# 3.0.7 Exponential Fourier Warp

```
[40]: M = ap.models.AutoProf_Model(name = "exp fourier warp", model_type = ""exponential fourier warp galaxy model", parameters = {"center": [50,50], ""o"q": 0.6, "PA": 60*np.pi/180, "q(R)": warp_q, "PA(R)": warp_pa, "am": "ofourier_am, "phim": fourier_phim, "Re": 10, "Ie": 1}, target = basic_target) print(M.parameter_order()) print(tuple(M.parameters[P].units for P in M.parameter_order())) M.initialize()

fig, ax = plt.subplots(1,2, figsize = (14,6)) ap.plots.model_image(fig, ax[0], M) ap.plots.galaxy_light_profile(fig,ax[1],M) plt.show()
```

```
('center', 'q', 'PA', 'q(R)', 'PA(R)', 'am', 'phim', 'Re', 'Ie')
('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'none', 'radians', 'arcsec',
'log10(flux/arcsec^2)')
```



# 3.0.8 Gassian Fourier Warp

```
[41]: M = ap.models.AutoProf_Model(name = "gaussian fourier warp", model_type = U → "gaussian fourier warp galaxy model", parameters = {"center": [50,50], "q": U → 0.6, "PA": 60*np.pi/180, "q(R)": warp_q, "PA(R)": warp_pa, "am": fourier_am, U → "phim": fourier_phim, "sigma": 5, "flux": 1}, target = basic_target)

print(M.parameter_order())

print(tuple(M.parameters[P].units for P in M.parameter_order()))

M.initialize()

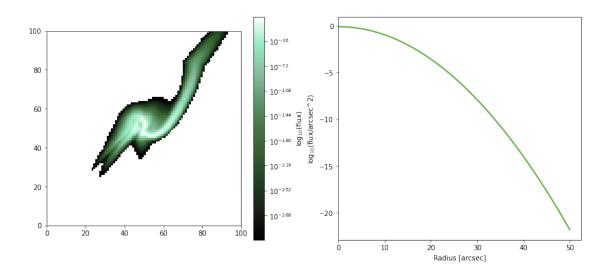
fig, ax = plt.subplots(1,2, figsize = (14,6))

ap.plots.model_image(fig, ax[0], M)

ap.plots.galaxy_light_profile(fig,ax[1],M)

plt.show()
```

('center', 'q', 'PA', 'q(R)', 'PA(R)', 'am', 'phim', 'sigma', 'flux') ('arcsec', 'b/a', 'radians', 'b/a', 'rad', 'none', 'radians', 'arcsec', 'log10(flux)')



[]: