Exercise sheet 5: Local Sequence Alignment

Exercise 1 - Smith-Waterman

Consider the following sequences S1 and S2, a similarity scoring via s(x, y) and a gap cost function g(k).

$$S1 = TCCGA \tag{1}$$

$$S2 = TACGCAGA \tag{2}$$

$$s(x,y) = \begin{cases} +1 & if \ x = y \\ 0 & else \end{cases}$$
 (3)

$$g(k) = -k \tag{4}$$

1a)

Compute the local alignment matrix $S_{i,j}$ for the given sequence.

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Matrix

Hint: Formulae

$$H_{0,0} = 0 (5)$$

$$H_{i,0} = 0 (6)$$

$$H_{0,j} = 0 (7)$$

$$H_{i,j} = \max \begin{cases} H_{i-1,j-1} + s(a_i, b_j) \\ H_{i-1,j} + s(a_i, -) \\ H_{i,j-1} + s(-, b_j) \\ 0 \end{cases}$$
(8)

Solution

1b)

Give all optimal local alignments and the according score.

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Solution score: 3

TCCG	TCCGA	TCCG-A	CCGA
1:11	1:11:	1:11 1	1:11
TACG	TACGC	TACGCA	CAGA

Exercise 2 - Affine gap costs

2a)

Which of these statements are correct?

Statements

Distance and similarity scores are equally useful for local alignment scoring
Similarity scores are not suited for local alignment scoring
Distance scores are not suited for local alignment scoring

Solution

Distance and similarity scores are equally useful for local alignment s	scoring
Similarity scores are not suited for local alignment scoring	

☐ Distance scores are not suited for local alignment scoring

2b)

You want to extend the Smith-Waterman algorithm for local alignment to more general gap scoring functions g(k) (where k denotes the gap length).

The following recursions were created analogously to the Waterman-Smith-Beyer algorithm. Which of these (if any) represents a variant of the Smith-Waterman algorithm that allows for an arbitrary gap scoring function?

$$D_{0,0} = 0, \ D_{i,0} = 0, \ D_{0,j} = 0$$

$$D_{i,j} \stackrel{(i)}{=} max \begin{cases} Di - 1, j - 1 + s(a_i, b_j) \\ max_{1 \le k \le j} D_{i,j-k} + g(1) \\ max_{1 \le k \le i} D_{i-k,j} + g(1) \\ 0 \end{cases} \qquad D_{i,j} \stackrel{(ii)}{=} max \begin{cases} Di - 1, j - 1 + s(a_i, b_j) \\ max_{1 \le k \le j} D_{i,j-k} + g(k) \\ max_{1 \le k \le i} D_{i-k,j} + g(k) \\ 0 \end{cases}$$
(9)

(10)

(12)

$$D_{i,j} \stackrel{(iii)}{=} min \begin{cases} Di - 1, j - 1 + s(a_i, b_j) \\ max_{1 \le k \le j} D_{i,j-k} + g(k) \\ max_{1 \le k \le i} D_{i-k,j} + g(k) \\ 0 \end{cases} \qquad D_{i,j} \stackrel{(iv)}{=} min \begin{cases} Di - 1, j - 1 + s(a_i, b_j) \\ max_{1 \le k \le j} D_{i,j-k} + g(1) \\ max_{1 \le k \le i} D_{i-k,j} + g(1) \\ 0 \end{cases}$$
(11)

$$D_{i,j} \stackrel{(v)}{=} max \begin{cases} Di - 1, j - 1 + s(a_i, b_j) \\ max_{1 \le k \le j} D_{i,j-k} + g(1) \\ max_{1 \le k \le i} D_{i-k,j} + g(1) \\ -1 \end{cases}$$

$$(13)$$

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Solution Only Formula *ii* allows for an arbitrary gap scoring.

Note

Distance scores are not suited for local alignment scoring, thus all minimization approaches are not suitable. Further g(1) does not represent an affine scoring.

2c)

The following recursions were created analogously to the Gotoh algorithm. Which of these (if any) represents a variant of the Smith-Waterman algorithm that allows for an affine gap scoring function?

$$D_{0,0} = 0, \ D_{i,0} = 0, \ D_{0,j} = 0$$

$$D_{i,j} \stackrel{(i)}{=} max \begin{cases} D_{i-1,j-1} + s(a_i, b_j) & P_{i,j} = max \begin{cases} D_{i-1,j} + g(1) \\ P_{i-1,j} + \beta \end{cases} \\ Q_{i,j} & Q_{i,j} = max \begin{cases} D_{i,j-1} + g(1) \\ Q_{i,j-1} + \beta \end{cases} \end{cases}$$

$$(14)$$

$$D_{i,j} \stackrel{(ii)}{=} max \begin{cases} D_{i-1,j-1} + s(a_i, b_j) & P_{i,j} = max \begin{cases} D_{i-1,j} + g(k) \\ P_{i-1,j} + \beta \end{cases} \\ Q_{i,j} & Q_{i,j} = max \begin{cases} D_{i,j-1} + g(k) \\ Q_{i,j-1} + \beta \end{cases} \end{cases}$$
(16)

(15)

(17)

(19)

$$D_{i,j} \stackrel{(iii)}{=} min \begin{cases} D_{i-1,j-1} + s(a_i, b_j) & P_{i,j} = min \begin{cases} D_{i-1,j} + g(k) \\ P_{i-1,j} + \beta \end{cases} \\ Q_{i,j} & Q_{i,j} = min \begin{cases} D_{i,j-1} + g(k) \\ Q_{i,j-1} + \beta \end{cases} \end{cases}$$
(18)

$$D_{i,j} \stackrel{(iv)}{=} min \begin{cases} D_{i-1,j-1} + s(a_i, b_j) & P_{i,j} = min \begin{cases} D_{i-1,j} + g(1) \\ P_{i-1,j} + \beta \end{cases} \\ Q_{i,j} & Q_{i,j} = min \begin{cases} D_{i,j-1} + g(1) \\ Q_{i,j-1} + \beta \end{cases} \end{cases}$$
(20)

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Solution Only Formula i allows for an affine gap scoring.

Note

Distance scores are not suited for local alignment scoring, thus all minimization approaches are not suitable. Further g(1) does not represent an affine scoring.

Exercise 3 - Programming assignment

Programming assignments are available via Github Classroom and contain automatic tests.

We recommend doing these assignments since they will help you to further understand this topic.

Access the Github Classroom link: Programming Assignment: Sheet 05.