

## Exercise sheet 2: Edit operations and alignments

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### Exercise sheet 2 - Levenshtein Distance

Compute the minimal Levenshtein edit distance for the following pairs of sequences.

#### Question 1A

$$S_1 = A \tag{1}$$

$$S_2 = T \tag{2}$$

**Hint**  $A \rightarrow T$

**Correct Answer**  $A \rightarrow T = 1$

#### Question 1B

$$S_1 = AGATATA \tag{3}$$

$$S_2 = TATATATA \tag{4}$$

**Hint**  $AGATATA \rightarrow ATATATA \rightarrow \dots$

**Correct Answer**  $AGATATA \rightarrow ATATATA \rightarrow TATATATA = 3$

#### Question 1C

$$S_1 = AGTCCT \tag{5}$$

$$S_2 = CGCTCA \tag{6}$$

**Hint**  $AGTCCT \rightarrow AGCTCA \rightarrow \dots$

**Correct Answer**  $AGTCCT \rightarrow CGTCCT \rightarrow CGCCCT \rightarrow CGCTCA = 4$

### Question 1D

$$S_1 = TGCATAT \quad (7)$$

$$S_2 = ATCCGAT \quad (8)$$

**Hint**  $TGCATAT \rightarrow AGCATAT \rightarrow \dots$

**Correct Answer**  $TGCATAT \rightarrow AGCATAT \rightarrow ATCATAT \rightarrow ATCCGAT = 4$

### Question 1E

$$S_1 = ACGTATATAGCCCCGCG \quad (9)$$

$$S_2 = ACGTTATATAGCCGCGC \quad (10)$$

**Hint** You need to use all the possible operations

$ACGTATATAGCCCCGCG \rightarrow ACGTTATATAGCCCCGCG \rightarrow \dots$

**Correct Answer**  $ACGTATATAGCCCCGCG \rightarrow ACGTTATATAGCCCCGCG \rightarrow ACGTTATATAGCCGCGC \rightarrow ACGTTATATAGCCGCGC = 4$

## Exercise 2 - Metric function

Check if the corresponding functions are metric.

### Question 2A

$$w(x, y) = x - y \quad (11)$$

**Hint** What if  $x = -5$  and  $y = -5$ ?

**Correct Answer** Not metric

### Question 2B

$$w(x, y) = |x - y| \quad (12)$$

**Hint** You need to check all the properties.

**Correct Answer** Metric

**Question 2C**

$$w(x, y) = x + y \quad (13)$$

**Hint** What if  $x = -5$  and  $y = -5$ ?

**Correct Answer** Not metric

**Question 2D**

$$w(x, y) = \begin{cases} 1 & \text{if } x \neq y \\ 0 & \text{else} \end{cases} \quad (14)$$

**Hint** You need to check all the properties.

**Correct Answer** Metric

## Exercise 3 - DNA and RNA