

RISC-V XBitmanip Extension

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Chapter 1

Introduction

This is the RISC-V XBitmanip Extension draft spec. Originally it was the B-Extension draft spec, but the work group got dissolved for bureaucratic reasons in November 2017.

It is currently an independently maintained document. We'd happily donate it to the RISC-V foundation as starting point for a new B-Extension work group, if there will be one.

1.1 ISA Extension Proposal Design Criteria

Any proposed changes to the ISA should be evaluated according to the following criteria.

- **Architecture Consistency:** Decisions must be consistent with RISC-V philosophy. ISA changes should deviate as little as possible from existing RISC-V standards (such as instruction encodings), and should not re-implement features that are already found in the base specification or other extensions.
- **Threshold Metric:** The proposal should provide a *significant* savings in terms of clocks or instructions. As a heuristic, any proposal should replace at least four instructions. An instruction that only replaces three may be considered, but only if the frequency of use is very high and/or the implementation very cheap.
- **Data-Driven Value:** Usage in real world applications, and corresponding benchmarks showing a performance increase, will contribute to the score of a proposal. A proposal will not be accepted on the merits of its *theoretical* value alone, unless it is used in the real world.
- **Hardware Simplicity:** Though instructions saved is the primary benefit, proposals that dramatically increase the hardware complexity and area, or are difficult to implement, should be penalized and given extra scrutiny. The final proposals should only be made if a test implementation can be produced.
- **Compiler Support:** ISA changes that can be natively detected by the compiler, or are already used as intrinsics, will score higher than instructions which do not fit that criteria.

1.2 B Extension Adoption Strategy

The overall goal of this extension is pervasive adoption by minimizing potential barriers and ensuring the instructions can be mapped to the largest number of ops, either direct or pseudo, that are supported by the most popular processors and compilers. By adding generic instructions and taking advantage of the RISC-V base instructions that already operate on bits, the minimal set of instructions need to be added while at the same time enabling a rich of operations.

The instructions cover the four major categories of bit manipulation: Count, Extract, Insert, Swap. The spec supports RV32, RV64, and RV128. “Clever” obscure and/or overly specific instructions are avoided in favor of more straightforward, fast, generic ones. Coordination with other emerging RISC-V ISA extensions groups is required to ensure our instruction sets are architecturally consistent.

1.3 Next steps

- Assign concrete instruction encodings so that we can start implementing the extension in processor cores and compilers.
- Add support for this extension to processor cores and compilers so we can run quantitative evaluations on the instructions.
- Create assembler snippets for common operations that do not map 1:1 to any instruction in this spec, but can be implemented easily using clever combinations of the instructions. Add support for those snippets to compilers.

Chapter 2

RISC-V XBitmanip Extension

In the proposals provided in this section, the C code examples are for illustration purposes. They are not optimal implementations, but are intended to specify the desired functionality. See Chapter 6 for fast C code for use in emulators.

The sections on encodings are mere placeholders.

2.1 Count Leading/Trailing Zeros (`clz`, `ctz`)

The `clz` operation counts the number of 0 bits at the MSB end of the argument. That is, the number of 0 bits before the first 1 bit counting from the most significant bit. If the input is 0, the output is XLEN. If the input is -1, the output is 0.

The `ctz` operation counts the number of 0 bits at the LSB end of the argument. If the input is 0, the output is XLEN. If the input is -1, the output is 0.

```
uint_xlen_t clz(uint_xlen_t rs1)
{
    for (int count = 0; count < XLEN; count++)
        if ((rs1 << count) >> (XLEN - 1))
            return count;
    return XLEN;
}

uint_xlen_t ctz(uint_xlen_t rs1)
{
    for (int count = 0; count < XLEN; count++)
        if ((rs1 >> count) & 1)
            return count;
    return XLEN;
}
```

31	20 19	15 14	12 11	7 6	0
imm[11:0]	rs1	funct3	rd	opcode	
12	5	3	5	7	
???????????	src	CLZ	dest	OP-IMM	
???????????	src	CTZ	dest	OP-IMM	
???????????	src	CLZW	dest	OP-IMM-32	
???????????	src	CTZW	dest	OP-IMM-32	

One possible encoding for `clz` and `ctz` is as standard I-type opcodes somewhere in the brownfield surrounding the shift-immediate instructions.

2.2 Count Bits Set (pcnt)

This instruction counts the number of 1 bits in a register. This operations is known as population count, popcount, sideways sum, bit summation, or Hamming weight. [5, 4]

```
uint_xlen_t pcnt(uint_xlen_t rs1)
{
    int count = 0;
    for (int index = 0; index < XLEN; index++)
        count += (rs1 >> index) & 1;
    return count;
}
```

31	20 19	15 14	12 11	7 6	0
imm[11:0]	rs1	funct3	rd	opcode	
12	5	3	5	7	
???????????	src	PCNT	dest	OP-IMM	
???????????	src	PCNTW	dest	OP-IMM-32	

One possible encoding for `pcnt` is as a standard I-type opcode somewhere in the brownfield surrounding the shift-immediate instructions.

2.3 And-with-complement (andc)

This instruction implements the and-with-complement operation.

```
uint_xlen_t andc(uint_xlen_t rs1, uint_xlen_t rs2)
{
    return rs1 & ~rs2;
}
```


Other with-complement operations (`orc`, `nand`, `nor`, etc) can be implemented by combining `not` (`c.not`) with the base ALU operation. (Which can fit in 32 bit when using two compressed instructions.) Only and-with-complement occurs frequently enough to warrant a dedicated instruction.

31	25 24	20 19	15 14	12 11	7 6	0
funct7	rs2	rs1	funct3	rd	opcode	
7	5	5	3	5	7	
???????	src2	src1	ANDC	dest	OP	

2.4 Shift Ones (Left/Right) (`slo`, `sloi`, `sro`, `sroi`)

These instructions are similar to shift-logical operations from the base spec, except instead of shifting in zeros, they shifts in ones.

```
uint_xlen_t slo(uint_xlen_t rs1, uint_xlen_t rs2)
{
    int shamt = rs2 & (XLEN - 1);
    return ~(~rs1 << shamt);
}

uint_xlen_t sro(uint_xlen_t rs1, uint_xlen_t rs2)
{
    int shamt = rs2 & (XLEN - 1);
    return ~(~rs1 >> shamt);
}
```

31	25 24	20 19	15 14	12 11	7 6	0
funct7	rs2	rs1	funct3	rd	opcode	
7	5	5	3	5	7	
10?????	src2	src1	SRO	dest	OP	
10?????	src2	src1	SLO	dest	OP	
10?????	src2	src1	SROW	dest	OP-32	
10?????	src2	src1	SLOW	dest	OP-32	

31	27 26	20 19	15 14	12 11	7 6	0
imm[11:7]	imm[6:0]	rs1	funct3	rd	opcode	
5	7	5	3	5	7	
10???	shamt	src	SLOI	dest	OP-IMM	
10???	shamt	src	SROI	dest	OP-IMM	

31	25 24	20 19	15 14	12 11	7 6	0
imm[11:5]	imm[4:0]	rs1	funct3	rd	opcode	
7	5	5	3	5	7	
10?????	shamt	src	SLOIW	dest	OP-IMM-32	
10?????	shamt	src	SROIW	dest	OP-IMM-32	

`s(l/r)o(i)` is encoded similarly to the logical shifts in the base spec. However, the spec of the entire family of instructions is changed so that the high bit of the instruction indicates the value to be inserted during a shift. This means that a `sloi` instruction can be encoded similarly to an `slli` instruction, but with a 1 in the highest bit of the encoded instruction. This encoding is backwards compatible with the definition for the shifts in the base spec, but allows for simple addition of a ones-insert.

When implementing this circuit, the only change in the ALU over a standard logical shift is that the value shifted in is not zero, but is a 1-bit register value that has been forwarded from the high bit of the instruction decode. This creates the desired behavior on both logical zero-shifts and logical ones-shifts.

2.5 Rotate (Left/Right) (`rol`, `ror`, `rori`)

These instructions are similar to shift-logical operations from the base spec, except they shift in the values from the opposite side of the register, in order. This is also called ‘circular shift’.

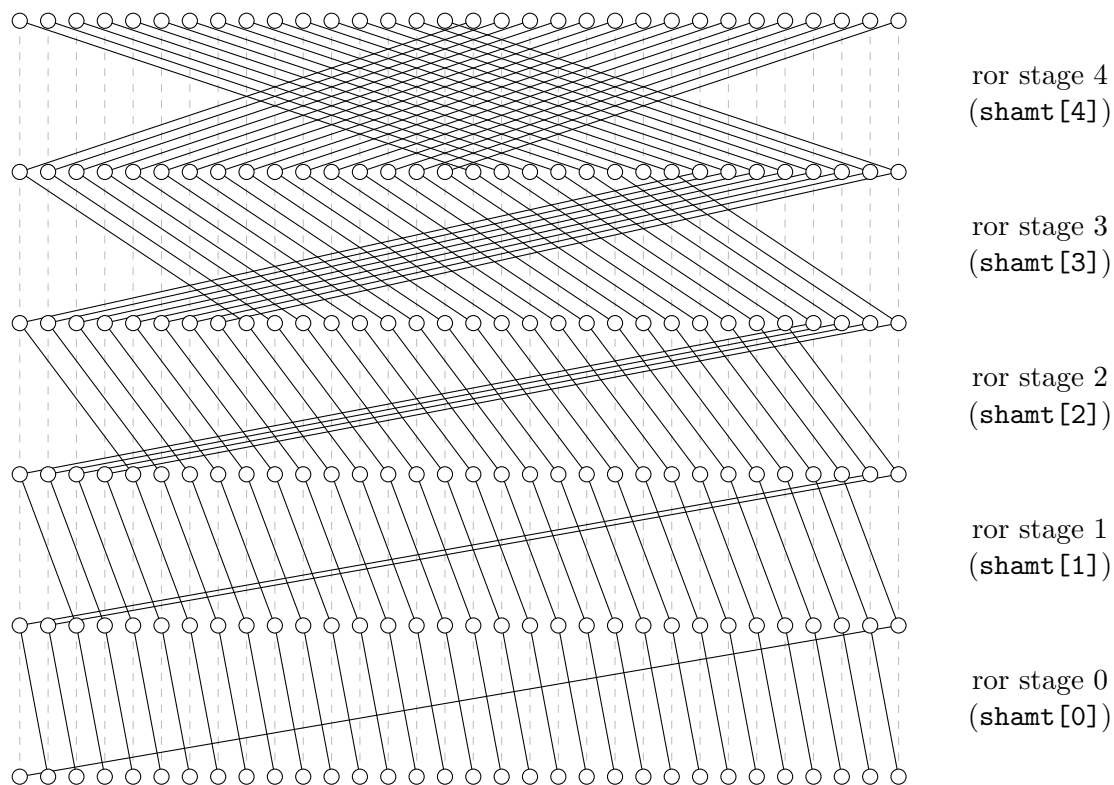
```
uint_xlen_t rol(uint_xlen_t rs1, uint_xlen_t rs2)
{
    int shamt = rs2 & (XLEN - 1);
    return (rs1 << shamt) | (rs1 >> (XLEN - shamt));
}

uint_xlen_t ror(uint_xlen_t rs1, uint_xlen_t rs2)
{
    int shamt = rs2 & (XLEN - 1);
    return (rs1 >> shamt) | (rs1 << (XLEN - shamt));
}
```

31	25 24	20 19	15 14	12 11	7 6	0
funct7	rs2	rs1	funct3	rd	opcode	
7	5	5	3	5	7	
11?????	src2	src1	ROR	dest	OP	
11?????	src2	src1	ROL	dest	OP	
11?????	src2	src1	RORW	dest	OP-32	
11?????	src2	src1	ROLW	dest	OP-32	

31	27 26	20 19	15 14	12 11	7 6	0
imm[11:7]	imm[6:0]	rs1	funct3	rd	opcode	
5	7	5	3	5	7	
11???	shamt	src	RORI	dest	OP-IMM	

31	25 24	20 19	15 14	12 11	7 6	0
imm[11:5]	imm[4:0]	rs1	funct3	rd	opcode	
7	5	5	3	5	7	
11?????	shamt	src	RORIW	dest	OP-IMM-32	

Figure 2.1: **ror** permutation network

Rotate shift is implemented very similarly to the other shift instructions. One possible way to encode it is to re-use the way that bit 30 in the instruction encoding selects ‘arithmetic shift’ when bit 31 is zero (signalling a logical-zero shift). We can re-use this so that when bit 31 is set (signalling a logical-ones shift), if bit 31 is also set, then we are doing a rotate. The following table summarizes the behavior. The generalized reverse instructions can be encoded using the bit pattern that would otherwise encode an “Arithmetic Left Shift” (which is an operation that does not exist). Likewise, the generalized zip instruction can be encoded using the bit pattern that would otherwise encode an “Rotate left immediate”.

Bit 31	Bit 30	Meaning
0	0	Logical Shift-Zeros
0	1	Arithmetic Shift
1	0	Logical Shift-Ones
1	1	Rotate

2.6 Generalized Reverse (**grev**, **grevi**)

This instruction provides a single hardware instruction that can implement all of byte-order swap, bitwise reversal, short-order-swap, word-order-swap (RV64), nibble-order swap, bitwise reversal in a



Figure 2.2: grev permutation network

byte, etc, all from a single hardware instruction. It takes in a single register value and an immediate that controls which function occurs, through controlling the levels in the recursive tree at which reversals occur.

This operation iteratively checks each bit i in rs2 from $i = 0$ to $XLEN - 1$, and if the corresponding bit is set, swaps each adjacent pair of 2^i bits.

```
uint32_t grev32(uint32_t rs1, uint32_t rs2)
{
    uint32_t x = rs1;
    int shamt = rs2 & 31;
    if (shamt & 1) x = ((x & 0x55555555) << 1) | ((x & 0xAAAAAAAA) >> 1);
    if (shamt & 2) x = ((x & 0x33333333) << 2) | ((x & 0xCCCCCCCC) >> 2);
    if (shamt & 4) x = ((x & 0x0F0F0F0F) << 4) | ((x & 0xF0F0F0F0) >> 4);
    if (shamt & 8) x = ((x & 0x00FF00FF) << 8) | ((x & 0xFF00FF00) >> 8);
    if (shamt & 16) x = ((x & 0x0000FFFF) << 16) | ((x & 0xFFFF0000) >> 16);
    return x;
}
```

```

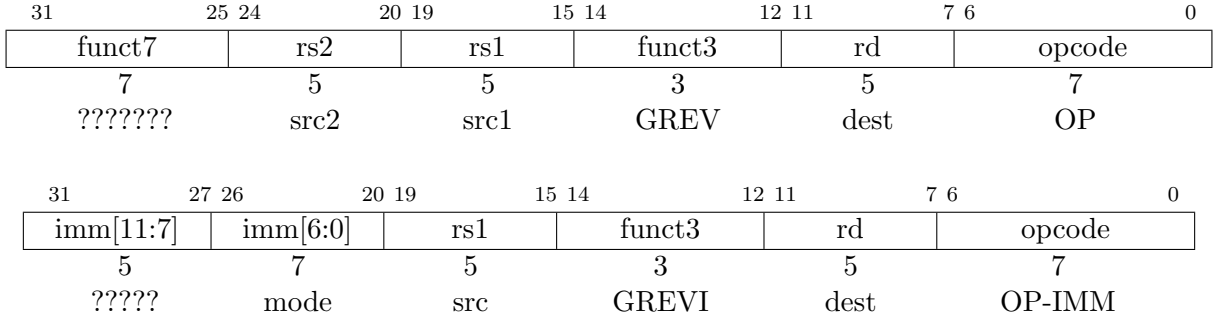
uint64_t grev64(uint64_t rs1, uint64_t rs2)
{
    uint64_t x = rs1;
    int shamt = rs2 & 63;
    if (shamt & 1) x = ((x & 0x5555555555555555LL) << 1) |
                      ((x & 0xAAAAAAAAAAAAAAAAALL) >> 1);
    if (shamt & 2) x = ((x & 0x3333333333333333LL) << 2) |
                      ((x & 0xCCCCCCCCCCCCCCCCLL) >> 2);
    if (shamt & 4) x = ((x & 0x0F0F0F0F0F0F0F0FLL) << 4) |
                      ((x & 0xF0F0F0F0F0F0F0F0LL) >> 4);
    if (shamt & 8) x = ((x & 0x00FF00FF00FF00FFLL) << 8) |
                      ((x & 0xFF00FF00FF00FF00LL) >> 8);
    if (shamt & 16) x = ((x & 0x0000FFFF0000FFFFLL) << 16) |
                      ((x & 0xFFFF0000FFFF0000LL) >> 16);
    if (shamt & 32) x = ((x & 0x00000000FFFFFFFFLL) << 32) |
                      ((x & 0xFFFFFFFF00000000LL) >> 32);

    return x;
}

```

The above pattern should be intuitive to understand in order to extend this definition in an obvious manner for RV128.

The **grev** operation can easily be implemented using a permutation network with $\log_2(\text{XLEN})$ stages. Figure 2.1 shows the permutation network for **ror** for reference. Figure 2.2 shows the permutation network for **grev**.



grev is encoded as standard R-type opcode and **grevi** is encoded as standard I-type opcode. **grev** and **grevi** can use the instruction encoding for “arithmetic shift left”.

2.7 Generalized zip/unzip (gzip)

gzip is the third bit permutation instruction in XBitmanip, after **rori** and **grevi**. It implements a generalization of the operation commonly known as perfect outer shuffle and its inverse (shuffle/unshuffle), also known as zip/unzip or interlace/uninterlace.

This set of operation is best understood as operation on the bit indices. For reference, rotate shift adds **shamt** to the bit index (modulo XLEN), and generalized reversed performs an XOR between

RV32		RV64	
shamt	Instruction	shamt	Instruction
0: 00000	—	0: 000000	—
1: 00001	brev.p	1: 000001	brev.p
2: 00010	pswap.n	2: 000010	pswap.n
3: 00011	brev.n	3: 000011	brev.n
4: 00100	nswap.b	4: 000100	nswap.b
5: 00101	—	5: 000101	—
6: 00110	pswap.b	6: 000110	pswap.b
7: 00111	brev.b	7: 000111	brev.b
8: 01000	bswap.h	8: 001000	bswap.h
9: 01001	—	9: 001001	—
10: 01010	—	10: 001010	—
11: 01011	—	11: 001011	—
12: 01100	nswap.h	12: 001100	nswap.h
13: 01101	—	13: 001101	—
14: 01110	pswap.h	14: 001110	pswap.h
15: 01111	brev.h	15: 001111	brev.h
16: 10000	hswap	16: 010000	hswap.w
17: 10001	—	17: 010001	—
18: 10010	—	18: 010010	—
19: 10011	—	19: 010011	—
20: 10100	—	20: 010100	—
21: 10101	—	21: 010101	—
22: 10110	—	22: 010110	—
23: 10111	—	23: 010111	—
24: 11000	bswap	24: 011000	bswap.w
25: 11001	—	25: 011001	—
26: 11010	—	26: 011010	—
27: 11011	—	27: 011011	—
28: 11100	nswap	28: 011100	nswap.w
29: 11101	—	29: 011101	—
30: 11110	pswap	30: 011110	pswap.w
31: 11111	brev	31: 011111	brev.w
		32: 100000	wswap
		33: 100001	—
		34: 100010	—
		35: 100011	—
		36: 100100	—
		37: 100101	—
		38: 100110	—
		39: 100111	—
		40: 101000	—
		41: 101001	—
		42: 101010	—
		43: 101011	—
		44: 101100	—
		45: 101101	—
		46: 101110	—
		47: 101111	—
		48: 110000	hswap
		49: 110001	—
		50: 110010	—
		51: 110011	—
		52: 110100	—
		53: 110101	—
		54: 110110	—
		55: 110111	—
		56: 111000	bswap
		57: 111001	—
		58: 111010	—
		59: 111011	—
		60: 111100	nswap
		61: 111101	—
		62: 111110	pswap
		63: 111111	brev

Table 2.1: Pseudo-instructions for **grevi** instruction

the bit index and **shamt**. Generalized zip/unzip performs a rotate left shift (zip) or rotate right shift (unzip) on a continuous range of bits in the bit index. Every arbitrary permutation of the bit index bits can be achieved by applying **gzip** repeatedly.

The **gzip** instruction uses an I-type encoding similar to **grevi**. There are XLEN different generalized zip operations, some of which are reserved because they are no-ops, or equivalent to other modes, or encode for obscure combinations of other modes. The bit pattern for the non-reserved modes match the regular expression `/^0*(10+|11+0*[01])$/`, or in words: Bits `mode[LOG2.XLEN-1:1]` must only contain one continuous range of 1 bits, and if only one bit in `mode[LOG2.XLEN-1:1]` is set then `mode[0]` must be cleared. See Tables 2.2 and 2.3.

Reserving modes that encode for “obscure combinations of other modes” can help implementations that use different base permutations (or completely different mechanisms) to implement the **gzip** instruction. The reserved modes can be used to encode unary functions such as **ctz**, **clz**, and **pcnt**.

mode	Bit index rotations	Pseudo-Instruction
0: 0000 0	no-op	<i>reserved</i>
1: 0000 1	no-op	<i>reserved</i>
2: 0001 0	i[1] -> i[0]	zip.n, unzip.n
3: 0001 1	<i>equivalent to 0001 0</i>	<i>reserved</i>
4: 0010 0	i[2] -> i[1]	zip2.b, unzip2.b
5: 0010 1	<i>equivalent to 0010 0</i>	<i>reserved</i>
6: 0011 0	i[2] -> i[0]	zip.b
7: 0011 1	i[2] <- i[0]	unzip.b
8: 0100 0	i[3] -> i[2]	zip4.h, unzip4.h
9: 0100 1	<i>equivalent to 0100 0</i>	<i>reserved</i>
10: 0101 0	i[3] -> i[2], i[1] -> i[0]	<i>reserved</i>
11: 0101 1	<i>equivalent to 0101 0</i>	<i>reserved</i>
12: 0110 0	i[3] -> i[1]	zip2.h
13: 0110 1	i[3] <- i[1]	unzip2.h
14: 0111 0	i[3] -> i[0]	zip.h
15: 0111 1	i[3] <- i[0]	unzip.h
16: 1000 0	i[4] -> i[3]	zip8, unzip8
17: 1000 1	<i>equivalent to 1000 0</i>	<i>reserved</i>
18: 1001 0	i[4] -> i[3], i[1] -> i[0]	<i>reserved</i>
19: 1001 1	<i>equivalent to 1001 0</i>	<i>reserved</i>
20: 1010 0	i[4] -> i[3], i[2] -> i[1]	<i>reserved</i>
21: 1010 1	<i>equivalent to 1010 0</i>	<i>reserved</i>
22: 1011 0	i[4] -> i[3], i[2] -> i[0]	<i>reserved</i>
23: 1011 1	i[4] <- i[3], i[2] <- i[0]	<i>reserved</i>
24: 1100 0	i[4] -> i[2]	zip4
25: 1100 1	i[4] <- i[2]	unzip4
26: 1101 0	i[4] -> i[2], i[1] -> i[0]	<i>reserved</i>
27: 1101 1	i[4] <- i[2], i[1] <- i[0]	<i>reserved</i>
28: 1110 0	i[4] -> i[1]	zip2
29: 1110 1	i[4] <- i[1]	unzip2
30: 1111 0	i[4] -> i[0]	zip
31: 1111 1	i[4] <- i[0]	unzip

Table 2.2: RV32 modes and pseudo-instructions for **gzip** instruction

Like GREV and rotate shift, the **gzip** instruction can be implemented using a short sequence of atomic permutations, that are enabled or disabled by the mode (shamt) bits. But zip has one stage fewer than GREV and the LSB bit of mode controls the order in which the stages are applied:

```
uint32_t gzip32_stage(uint32_t src, uint32_t maskL, uint32_t maskR, int N)
{
    uint32_t x = src & ~(maskL | maskR);
    x |= ((src << N) & maskL) | ((src >> N) & maskR);
    return x;
}
```

mode	Pseudo-Instruction	mode	Pseudo-Instruction
0: 00000 0	reserved	32: 10000 0	zip16, unzip16
1: 00000 1	reserved	33: 10000 1	reserved
2: 00001 0	zip.n, unzip.n	34: 10001 0	reserved
3: 00001 1	reserved	35: 10001 1	reserved
4: 00010 0	zip2.b, unzip2.b	36: 10010 0	reserved
5: 00010 1	reserved	37: 10010 1	reserved
6: 00011 0	zip.b	38: 10011 0	reserved
7: 00011 1	unzip.b	39: 10011 1	reserved
8: 00100 0	zip4.h, unzip4.h	40: 10100 0	reserved
9: 00100 1	reserved	41: 10100 1	reserved
10: 00101 0	reserved	42: 10101 0	reserved
11: 00101 1	reserved	43: 10101 1	reserved
12: 00110 0	zip2.h	44: 10110 0	reserved
13: 00110 1	unzip2.h	45: 10110 1	reserved
14: 00111 0	zip.h	46: 10111 0	reserved
15: 00111 1	unzip.h	47: 10111 1	reserved
16: 01000 0	zip8.w, unzip8.w	48: 11000 0	zip8, unzip8
17: 01000 1	reserved	49: 11000 1	reserved
18: 01001 0	reserved	50: 11001 0	reserved
19: 01001 1	reserved	51: 11001 1	reserved
20: 01010 0	reserved	52: 11010 0	reserved
21: 01010 1	reserved	53: 11010 1	reserved
22: 01011 0	reserved	54: 11011 0	reserved
23: 01011 1	reserved	55: 11011 1	reserved
24: 01100 0	zip4.w	56: 11100 0	zip4
25: 01100 1	unzip4.w	57: 11100 1	unzip4
26: 01101 0	reserved	58: 11101 0	reserved
27: 01101 1	reserved	59: 11101 1	reserved
28: 01110 0	zip2.w	60: 11110 0	zip2
29: 01110 1	unzip2.w	61: 11110 1	unzip2
30: 01111 0	zip.w	62: 11111 0	zip
31: 01111 1	unzip.w	63: 11111 1	unzip

Table 2.3: RV64 modes and pseudo-instructions for gzip instruction

```

uint32_t gzip32(uint32_t rs1, uint32_t rs2)
{
    uint32_t x = rs1;
    int mode = rs2 & 31;

    if (mode & 1) {
        if (mode & 2) x = gzip32_stage(x, 0x44444444, 0x22222222, 1);
        if (mode & 4) x = gzip32_stage(x, 0x30303030, 0x0c0c0c0c, 2);
        if (mode & 8) x = gzip32_stage(x, 0x0f000f00, 0x00f000f0, 4);
        if (mode & 16) x = gzip32_stage(x, 0x00ff0000, 0x0000ff00, 8);
    } else {
        if (mode & 16) x = gzip32_stage(x, 0x00ff0000, 0x0000ff00, 8);
        if (mode & 8) x = gzip32_stage(x, 0x0f000f00, 0x00f000f0, 4);
        if (mode & 4) x = gzip32_stage(x, 0x30303030, 0x0c0c0c0c, 2);
        if (mode & 2) x = gzip32_stage(x, 0x44444444, 0x22222222, 1);
    }

    return x;
}

```

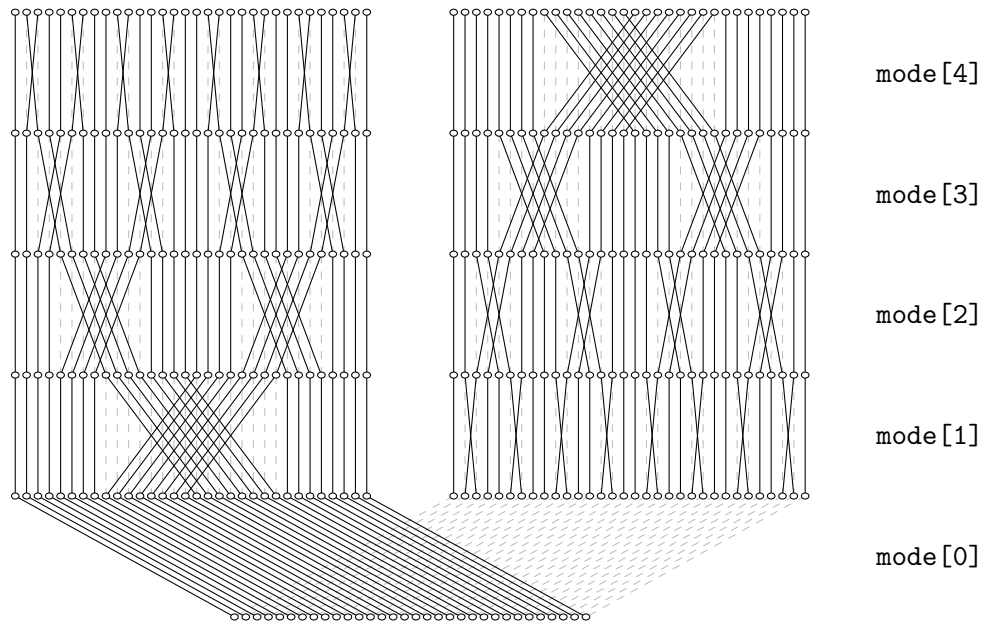



Figure 2.3: gzip permutation network without “flip” stages

Or for RV64:

```
uint64_t gzip64_stage(uint64_t src, uint64_t maskL, uint64_t maskR, int N)
{
    uint64_t x = src & ~(maskL | maskR);
    x |= ((src << N) & maskL) | ((src >> N) & maskR);
    return x;
}
```

```

uint64_t gzip64(uint64_t rs1, uint64_t rs2)
{
    uint64_t x = rs1;
    int mode = rs2 & 63;

    if (mode & 1) {
        if (mode & 2) x = gzip64_stage(x, 0x4444444444444444LL,
                                         0x2222222222222222LL, 1);
        if (mode & 4) x = gzip64_stage(x, 0x3030303030303030LL,
                                         0x0c0c0c0c0c0c0c0cLL, 2);
        if (mode & 8) x = gzip64_stage(x, 0x0f000f000f000f00LL,
                                         0x00f000f000f000f0LL, 4);
        if (mode & 16) x = gzip64_stage(x, 0x00ff000000ff0000LL,
                                         0x0000ff000000ff00LL, 8);
        if (mode & 32) x = gzip64_stage(x, 0x0000ffff00000000LL,
                                         0x00000000ffff0000LL, 16);
    } else {
        if (mode & 32) x = gzip64_stage(x, 0x0000ffff00000000LL,
                                         0x00000000ffff0000LL, 16);
        if (mode & 16) x = gzip64_stage(x, 0x00ff000000ff0000LL,
                                         0x0000ff000000ff00LL, 8);
        if (mode & 8) x = gzip64_stage(x, 0x0f000f000f000f00LL,
                                         0x00f000f000f000f0LL, 4);
        if (mode & 4) x = gzip64_stage(x, 0x3030303030303030LL,
                                         0x0c0c0c0c0c0c0c0cLL, 2);
        if (mode & 2) x = gzip64_stage(x, 0x4444444444444444LL,
                                         0x2222222222222222LL, 1);
    }

    return x;
}

```

The above pattern should be intuitive to understand in order to extend this definition in an obvious manner for RV128.

Alternatively **gzip** can be implemented in a single network with one more stage than GREV, with the additional first and last stage executing a permutation that effectively reverses the order of the inner stages. However, since the inner stages only mux half of the bits in the word each, a hardware implementation using this additional “flip” stages might actually be more expensive than simply creating two networks.

```

uint32_t gzip32_flip(uint32_t src)
{
    uint32_t x = src & 0x88224411;
    x |= ((src << 6) & 0x22001100) | ((src >> 6) & 0x00880044);
    x |= ((src << 9) & 0x00440000) | ((src >> 9) & 0x00002200);
    x |= ((src << 15) & 0x44110000) | ((src >> 15) & 0x00008822);
    x |= ((src << 21) & 0x11000000) | ((src >> 21) & 0x00000088);
    return x;
}

uint32_t gzip32alt(uint32_t rs1, uint32_t rs2)
{
    uint32_t x = rs1;
    int mode = rs2 & 31;

    if (mode & 1)
        x = gzip32_flip(x);

    if ((mode & 17) == 16 || (mode & 3) == 3)
        x = gzip32_stage(x, 0x00ff0000, 0x0000ff00, 8);

    if ((mode & 9) == 8 || (mode & 5) == 5)
        x = gzip32_stage(x, 0x0f000f00, 0x00f000f0, 4);

    if ((mode & 5) == 4 || (mode & 9) == 9)
        x = gzip32_stage(x, 0x30303030, 0x0c0c0c0c, 2);

    if ((mode & 3) == 2 || (mode & 17) == 17)
        x = gzip32_stage(x, 0x44444444, 0x22222222, 1);

    if (mode & 1)
        x = gzip32_flip(x);

    return x;
}

```

Figure 2.4 shows the `gzip` permutation network with “flip” stages and Figure 2.3 shows the `gzip` permutation network without “flip” stages.

The `zip` instruction with the upper half of its input cleared performs the commonly needed “fan-out” operation. (Equivalent to `bdep` with a `0x55555555` mask.) The `zip` instruction applied twice fans out the bits in the lower quarter of the input word by a spacing of 4 bits.

For example, the following code calculates the bitwise prefix sum of the bits in the lower byte of a 32 bit word on RV32:

```

andi a0, a0, 0xff
zip a0, a0
zip a0, a0

```

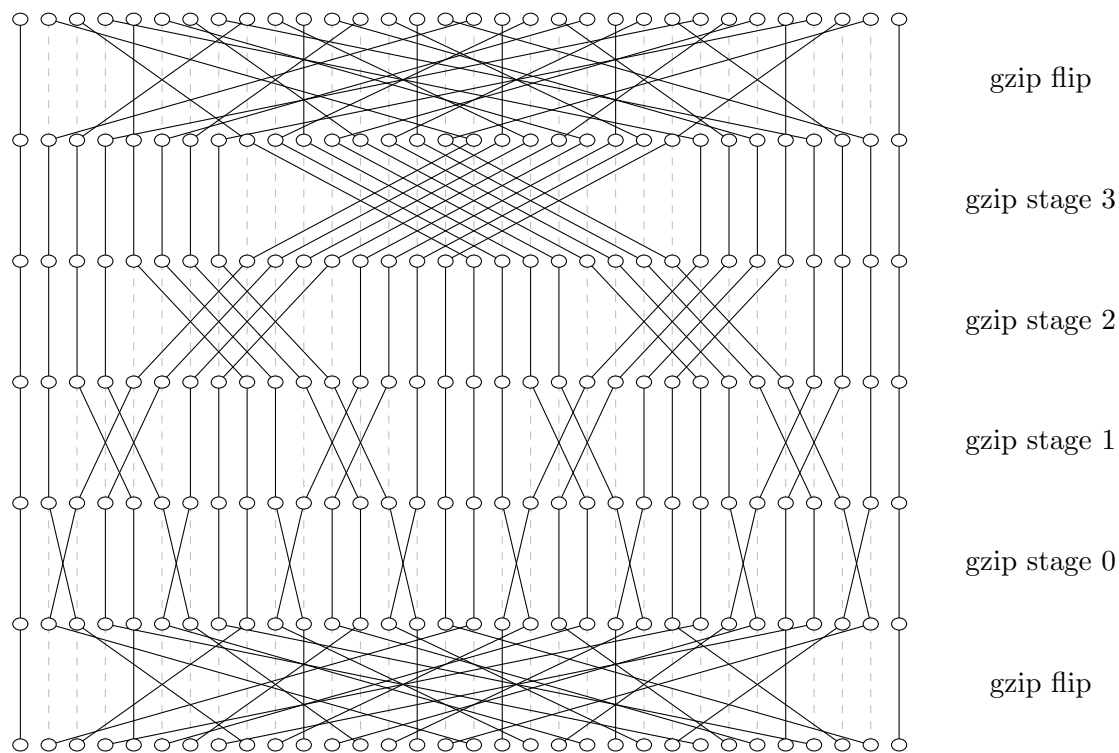


Figure 2.4: gzip permutation network with “flip” stages

```

slli a1, a0, 4
c.add a0, a1
slli a1, a0, 8
c.add a0, a1
slli a1, a0, 16
c.add a0, a1

```

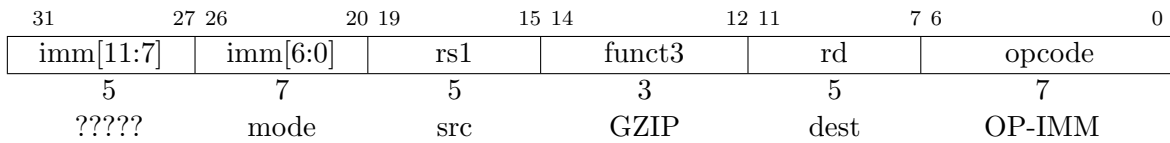
The final prefix sum is stored in the 8 nibbles of the a0 output word.

Other gzip modes can be used to “fan-out” in blocks of 2, 4, 8, or 16 bit. gzip can be combined with grevi to perform inner shuffles. For example on RV64:

```

li a0, 0x0000000012345678
zip4 t0, a0 ; <- 0x0102030405060708
nswap.b t1, t0 ; <- 0x1020304050607080
zip8 t2, a0 ; <- 0x0012003400560078
bswap.h t3, t2 ; <- 0x1200340056007800
zip16 t4, a0 ; <- 0x0000123400005678
hswap.w t5, t4 ; <- 0x1234000056780000

```



There is no R-type instruction for `gzip`. It is an I-type only instruction. `gzip` can use the instruction encoding for “rotate left immediate”.

2.8 Bit Extract/Deposit (`bext`, `bdep`)

This instructions implement the generic bit extract and bit deposit functions. This operation is also referred to as bit gather/scatter, bit pack/unpack, parallel extract/deposit, compress/expand, or `right_compress/right_expand`.

`bext` collects LSB justified bits to `rd` from `rs1` using extract mask in `rs2`.

`bdep` writes LSB justified bits from `rs1` to `rd` using deposit mask in `rs2`.

```
uint_xlen_t bext(uint_xlen_t rs1, uint_xlen_t rs2)
{
    uint_xlen_t r = 0;
    for (int i = 0, j = 0; i < XLEN; i++)
        if ((rs2 >> i) & 1) {
            if ((rs1 >> i) & 1)
                r |= uint_xlen_t(1) << j;
            j++;
        }
    return r;
}

uint_xlen_t bdep(uint_xlen_t rs1, uint_xlen_t rs2)
{
    uint_xlen_t r = 0;
    for (int i = 0, j = 0; i < XLEN; i++)
        if ((rs2 >> i) & 1) {
            if ((rs1 >> j) & 1)
                r |= uint_xlen_t(1) << i;
            j++;
        }
    return r;
}
```

Implementations may choose to use smaller multi-cycle implementations of `bext` and `bdep`, or even emulate the instructions in software.

Even though multi-cycle `bext` and `bdep` often are not fast enough to outperform algorithms that use sequences of shifts and bit masks, dedicated instructions for those operations can still be of

great advantage in cases where the mask argument is not constant.

For example, the following code efficiently calculates the index of the tenth set bit in `a0` using `bdep`:

```
li a1, 0x00000200
bdep a0, a1, a0
ctz a0, a0
```

For cases with a constant mask an optimizing compiler would decide when to use `bext` or `bdep` based on the optimization profile for the concrete processor it is optimizing for. This is similar to the decision whether to use `MUL` or `DIV` with a constant, or to perform the same operation using a longer sequence of much simpler operations.

31	25 24	20 19	15 14	12 11	7 6	0
funct7	rs2	rs1	funct3	rd	opcode	
7	5	5	3	5	7	
???????	src2	src1	BEXT	dest	OP	
???????	src2	src1	BDEP	dest	OP	
???????	src2	src1	BEXTW	dest	OP-32	
???????	src2	src1	BDEPW	dest	OP-32	

2.9 Compressed instructions (`c.not`, `c.neg`, `c.brev`)

The RISC-V ISA has no dedicated instructions for bitwise inverse (`not`) and arithmetic inverse (`neg`). Instead `not` is implemented as `xori rd, rs, -1` and `neg` is implemented as `sub rd, x0, rs`.

In bitmanipulation code `not` and `neg` are very common operations. But there are no compressed encodings for those operations because there is no `c.xori` instruction and `c.sub` can not operate on `x0`.

Many bit manipulation operations that have dedicated opcodes in other ISAs must be constructed from smaller atoms in RISC-V XBitmanip code. But implementations might choose to implement them in a single micro-op using macro-op-fusion. For this it can be helpful when the fused sequences are short. `not` and `neg` are good candidates for macro-op-fusion, so it can be helpful to have compressed opcodes for them.

Likewise `brev` (an alias for `grevi rd, rs, -1`, i.e. bitwise reversal) is also a very common atom for building bit manipulation operations. So it is helpful to have a compressed opcode for this instruction as well.

The compressed instructions `c.not`, `c.neg`, `c.brev` must be supported by all implementations that support the `C` extension and XBitmanip.

These three instructions fit nicely in the reserved space in `C.LUI/C.ADDI16SP`. They only occupy 0.1% of the ≈ 15.6 bits wide RVC encoding space.

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	
011	nzimm[9]			2				nzimm[4 6 8:7 5]				01			C.ADDI16SP <small>(<i>RES</i>, <i>nzimm</i>=0)</small>	
011	nzimm[17]			rd≠{0, 2}				nzimm[16:12]				01			C.LUI <small>(<i>RES</i>, <i>nzimm</i>=0; <i>HINT</i>, <i>rd</i>=0)</small>	
011	0			00	rs2'/rd'			0				01			C.NEG	
011	0			01	rs1'/rd'			0				01			C.NOT	
011	0			10	rs1'/rd'			0				01			C.BREV	
011	0			11	—			0				01			Reserved	

2.10 Bit-field extract pseudo instruction (bfext)

Extract the continuous bit field starting at `pos` with length `len` from `rs` (with `pos > 0`, `len > 0`, and `pos + len ≤ XLEN`).

```
bfext rd, rs, pos, len    ->    slli rd, rs, (XLEN-pos-len)
                               srlr rd, rd, (XLEN-len)
```

If possible, an implementation should fuse this two shift operations into a single macro-op. (Some implementors have raised concerns about the lack of a dedicated bit field extract instruction with large immediate, especially for implementations that can not fuse instructions into macro-ops and/or implementations that do not support compressed instructions. See Chapter 5 for a brief discussion of why no such instruction is part of XBitmanip, and a short separate extension proposal that adds such an instruction.)

Chapter 3

Discussion

3.1 Frequently Asked Questions

grev seems to be overly complicated? Do we really need it?

The **grev** instruction can be used to build a wide range of common bit permutation instructions, such as endianness conversion or bit reversal.

If **grev** were removed from this spec we would need to add a few new instructions in its place for those operations.

Do we really need all the *W opcodes for 32 bit ops on RV64?

I don't know. I think nobody does know at the moment. But they add very little complexity to the core. So the only question is if it is worth the encoding space. We need to run proper experiments with compilers that support those instructions. So they are in for now and if future evaluations show that they are not worth the encoding space then we can still throw them out.

Why only andc and not any other complement operators?

Early versions of this spec also included other *c operators. But experiments have shown that **andc** is much more common in bit manipulation code than any other operators. [7] Especially because it is commonly used in **mix** and **mux** operations.

Why andc? It can easily be emulated using and and not.

Yes, and we did not include any other ALU+complement operators. But **andc** is so common (mostly because of the **mix** and **mux** patterns), and its implementation is so cheap, that we decided to dedicate an R-type instruction to the operation.

The shift-ones instructions can be emulated using not and logical shift? Do we really need it?

Yes, a shift-ones instruction can easily be implemented using the logical shift instructions, with a bitwise invert before and after it. (This is literally the code we are using in the reference C implementation of shift-ones.)

We have decided to include it for now so that we can collect benchmark data before making a final decision on the inclusion or exclusion of those instructions. The main objection here is instruction encoding space. The hardware overhead of adding this functionality to a shifter is relatively low.

BEXT/BDEP look like really expensive operations. Do we really need them?

Yes, they are expensive, but not as expensive as one might expect. A single-cycle 32 bit BEXT+BDEP+GREV core can be implemented in less space than a single-cycle 16x16 bit multiplier with 32 bit output. [6]

It is also important to keep in mind that implementing those operations in software is very expensive. Hacker’s Delight contains a highly optimized software implementation of 32-bit BEXT that requires > 120 instructions. Their BDEP software implementation requires > 160 instructions. (Please disregard the “hardware-oriented algorithm” described in Hacker’s Delight. It is extremely expensive compared to other implementations. [6])

But do we really need 64-bit BEXT/BDEP?

Good question. A 64-bit BEXT/BDEP unit certainly is more than 2x the size of a 32-bit unit and in most cases 32-bit would be sufficient. It is also not very difficult to emulate 64-bit BEXT/BDEP using 32-bit BEXT/BDEP. On RV64 (with data in a0 and mask in a1):

<pre> bext64: pcntw a2, a1 bextw a3, a0, a1 c.srli a0, 32 c.srli a1, 32 bextw a0, a0, a1 sloi a1, zero, 32 c.and a3, a1 c.and a0, a1 sll a0, a2 c.or a0, a3 ret </pre>	<pre> bdep64: pcntw a2, a1 bdepw a3, a0, a1 srl a0, a0, a2 c.srli a1, 32 bdepw a0, a0, a1 c.slli a0, 32 c.slli a3, 32 c.srli a3, 32 c.or a0, a3 ret </pre>
--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------

However, one solution here would be to still reserve the opcode for 64-bit BEXT/BDEP and leave it to the implementation to decide whether to implement the function in hardware or emulating it using a software trap.

RV32		RV64		Instruction
3x	0	6x	0	CLZ, CLZW, CTZ, CTZW, PCNT, PCNTW
1x	15	1x	15	GREV
2x	15	2x	16	GREVI, ZIP
2x	15	6x	15	SLO, SRO, SLOW, SROW, SLOIW, SROIW
2x	15	2x	16	SLOI, SROI
2x	15	5x	15	ROR, ROL, RORW, ROLW, RORIW
1x	15	1x	16	RORI
3x	15	3x	15	ANDC, BEXT, BDEP
		2x	15	BEXTW, BDEPW
3x	4	3x	4	C.NEG, C.NOT, C.BREV

Table 3.1: XBitmanip encoding space (\log_2 , i.e. in equivalent number of bits)

3.2 Analysis of used encoding space

So how much encoding space is used by the XBitmanip extension?

We do not count any encoding space for the unary instructions `clz`, `clzw`, `ctz`, `ctzw`, `pcnt`, and `pcntw` because they can be implemented in the reserved modes in `zip`.

The compressed encoding space is ≈ 15.6 bits wide.

$$\log_2(3 \cdot 2^{14}) \approx 15.585$$

The compressed XBitmanip instructions need the equivalent of a 5.6 bit encoding space, or $\approx 0.1\%$ of the total ≈ 15.6 bits available.

$$\begin{aligned} \log_2(3 \cdot 2^4) &\approx 5.585 \\ 100/(2^{15.585-5.585}) &\approx 0.098 \end{aligned}$$

The reserved “C” encoding space as of Version 2.2 of the RISC-V User-Level ISA is summarized in Table 3.2. According to this information the reserved space is ≈ 11.2 bits wide. Therefore the compressed XBitmanip instructions would use $\approx 2.1\%$ of the remaining reserved “C” encoding space.

$$\begin{aligned} \log_2(2^3 - 1 + 2^{11} + 2^5 + 2^7 + 2^6 + 1) &\approx 11.155 \\ 100/(2^{11.155-5.585}) &\approx 2.105 \end{aligned}$$

On RV32, XBitmanip requires the equivalent of a ≈ 18.7 bit encoding space in the uncompressed encoding space. For comparison: A single standard I-type instruction (such as `ADDI` or `SLTIU`) requires a 22 bit encoding space. I.e. the entire RV32 XBitmanip extension needs less than one-eighth of the encoding space of the `SLTIU` instruction.

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0			
000			0									nz			00		$2^3 - 1$	
100			—												00		2^{11}	
011			0	—					0					01			2^5	
100			111			—			1	—					01			2^7
010			—	0					—					10			2^6	
100			0	0					0					10			1	

Table 3.2: Reserved “C” encoding space as of Version 2.2 of the RISC-V User-Level ISA

$$\log_2(13 \cdot 2^{15}) \approx 18.700$$

On RV64, XBitmanip requires the equivalent of a ≈ 19.8 bit encoding space in the uncompressed encoding space. I.e. the entire RV64 XBitmanip extension needs about one-quarter of the encoding space of the SLTIU instruction.

$$\log_2(17 \cdot 2^{15} + 5 \cdot 2^{16}) \approx 19.755$$

3.3 Area usage of reference implementations

We created RV32 implementations for the different compute cores necessary to implement XBitmanip (and XBitfield): <https://github.com/cliffordwolf/xbitmanip/tree/master/verilog>

We are comparing the area of those cores with the following two references:

1. A very basic right-rotate shift core (**ror**):

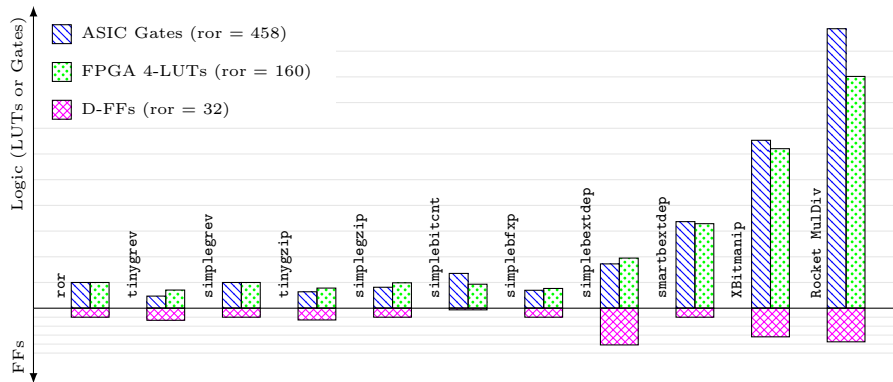


Figure 3.1: Relative area of XBitmanip reference cores compared to simple 32-bit rotate shift and Rocket MulDiv. The height of 1 LUT $\hat{=}$ 2.86 Gates, 1 FF $\hat{=}$ 5.00 Gates.

```

module reference_ror (
    input clock,
    input [31:0] din,
    input [4:0] shamt,
    output reg [31:0] dout
);
    always @(posedge clock)
        dout <= {din, din} >> shamt;
endmodule

```

2. A version of the Rocket RV32 MulDiv core that performs multiplication in 5 cycles and division/modulo in 32+ cycles. This is the MulDiv default configuration used in Rocket for small cores.

The implementations of cores performing XBitmanip (and XBitfield) operations are:

- **tinygrev** — A small multi-cycle implementation of **grev/grevi**. It takes 6 cycles for one operation.
- **tinygzip** — A small multi-cycle implementation of **gzip**. It takes 5 cycles for one operation.
- **simplegrev** — A simple single-cycle implementation of **grev/grevi**.
- **simplegzip** — A simple single-cycle implementation of **gzip**.
- **simplebitcnt** — A simple single-cycle implementation of **clz**, **ctz**, and **pcnt**.
- **simplebfxp** — A simple single-cycle implementation of the XBitfield **bfxp** instruction (see Chapter 5). It requires an external rotate-shift implementation.
- **simplebextdep** — A straight-forward multi-cycle implementation of **bext/bdep**. It takes up to 32 cycles for one operation (number of set mask bits).
- **smartbextdep** — A single-cycle implementation of **bext/bdep** using the method described in [3].

We implemented those cores with an ASIC cell library containing NOT, NAND, NOR, AOI3, OAI3, AOI4, and OAI4 gates. For the gate counts below we count NAND and NOR as 1 gate, NOT as 0.5 gates, AOI3 and OAI3 as 1.5 gates, and AOI4 and OAI4 as 2 gates.

We also implemented the cores using a simple FPGA architecture with 4-LUTs (and no dedicated CARRY or MUX resources).

Table 3.3 and Figure 3.1 show the area and logic depth of our reference cores (and the simple 32-bit rotate shift and Rocket MulDiv for comparison).

smartbextdep could share resources with **simplegrev** (it contains two butterfly circuits) and **simplebitcnt** (it contains a prefix adder network). We have not explored those resource sharing options in our reference cores.

Module	Gates	Depth	4-LUTs	Depth	FFs
<code>ror</code>	458	7	160	5	32
<code>tinygrev</code>	215	5	113	3	43
<code>simplegrev</code>	458	7	160	5	32
<code>tinygzip</code>	292	6	125	4	42
<code>simplegzip</code>	373	6	158	4	32
<code>simplebitcnt</code>	619	42	149	13	6
<code>simplebfxp</code>	319	13	123	6	32
<code>simplebextdep</code>	790	35	312	13	131
<code>smartbextdep</code>	1542	28	526	10	32
<code>XBitmanip</code>	2992	42	993	13	102
<code>Rocket MulDiv</code>	4980	53	1443	24	120

Table 3.3: Area and logic depth of XBitmanip reference cores compared to simple 32-bit rotate shift and Rocket MulDiv. The entry `XBitmanip` is just the total of `simplegrev` + `simplegzip` + `simplebitcnt` + `smartbextdep`. Not included in `XBitmanip` is the cost for adding shift-ones and rotate-shift support to the existing ALU shifter and the cost for additional decode and control logic.

Chapter 4

Evaluation

This chapter contains a collection of short code snippets and algorithms using the XBitmanip extension for evaluation purposes. For the sake of simplicity we assume RV32 for most examples in this chapter.

Most assembler routines in this chapter are written as if they were ABI functions, i.e. arguments are passed in `a0`, `a1`, ... and results are returned in `a0`. Registers `t0`, `t1`, ... and `a0`, `a1`, ... are used for spilling.

Some of the assembler routines below can not or should not overwrite their first argument. In those cases the arguments are passed in `a1`, `a2`, ... and results are returned in `a0`.

4.1 MIX/MUX pattern

A MIX pattern selects bits from `a0` and `a1` based on the bits in the control word `a2`.

```
c.and a0, a2
andc a1, a1, a2
c.or a0, a1
```

A MUX operation selects word `a0` or `a1` based on if the control word `a2` is zero or nonzero, without branching.

```
snez a2, a2
c.neg a2
c.and a0, a2
andc a1, a1, a2
c.or a0, a1
```

Or when `a2` is already either 0 or 1:

```

c.neg a2
c.and a0, a2
andc a1, a1, a2
c.or a0, a1

```

Alternatively, a core might fuse a conditional branch that just skips one instruction with that instruction to form a fused conditional macro-op.

4.2 Bit scanning and counting

Counting leading ones:

```

c.not a0
clz a0, a0

```

Counting trailing ones:

```

c.not a0
ctz a0, a0

```

Counting bits cleared:

```

c.not a0
pcnt a0, a0

```

(This is better than XLEN-pcnt because RISC-V has no “reverse-subtract-immediate” operation.)

Odd parity:

```

pcnt a0, a0
c.andi a0, 1

```

Even parity:

```

pcnt a0, a0
c.addi a0, 1
c.andi a0, 1

```

(Using `addi` here is better than using `xori`, because there is a compressed opcode for `addi` but none for `xori`.)

4.3 Arbitrary bit permutations

This section lists code snippets for computing arbitrary bit permutations that are defined by data (as opposed to bit permutations that are known at compile time and can likely be compiled into shift-and-mask operations and/or a few instances of bext/bdep).

4.3.1 Using butterfly operations

The following macro performs a stage-N butterfly operation on the word in **a0** using the mask in **a1**.

```
grevi a2, a0, (1 << N)
c.and a2, a1
andc a0, a0, a1
c.or a0, a2
```

The bitmask in **a1** must be preformatted correctly for the selected butterfly stage. A butterfly operation only has a $XLEN/2$ wide control word. The following macros format the mask assuming those $XLEN/2$ bits in the lower half of **a1** on entry (preformatted mask in **a1** on exit):

```
bfly_msk_0:
    zip a1, a1
    slli a2, a1, 1
    c.or a1, a2
```

```
bfly_msk_1:
    zip2 a1, a1
    slli a2, a1, 2
    c.or a1, a2
```

```
bfly_msk_2:
    zip4 a1, a1
    slli a2, a1, 4
    c.or a1, a2
```

...

A sequence of $2 \cdot \log_2(XLEN) - 1$ butterfly operations can perform any arbitrary bit permutation (Beneš network):

```
butterfly(LOG2_XLEN-1)
butterfly(LOG2_XLEN-2)
...
```

```

butterfly(0)
...
butterfly(LOG2_XLEN-2)
butterfly(LOG2_XLEN-1)

```

Many permutations arising from real-world applications can be implemented using shorter sequences. For example, any sheep-and-goats operation with either the sheep or the goats bit reversed can be implemented in $\log_2(\text{XLEN})$ butterfly operations.

Reversing a permutation implemented using butterfly operations is as simple as reversing the order of butterfly operations.

4.3.2 Using omega-flip networks

The omega operation is a stage-0 butterfly preceded by a zip operation:

```

zip a0, a0
grevi a2, a0, 1
c.and a2, a1
andc a0, a0, a1
c.or a0, a2

```

The flip operation is a stage-0 butterfly followed by an unzip operation:

```

grevi a2, a0, 1
c.and a2, a1
andc a0, a0, a1
c.or a0, a2
unzip a0, a0

```

A sequence of $\log_2(\text{XLEN})$ omega operations followed by $\log_2(\text{XLEN})$ flip operations can implement any arbitrary 32 bit permutation.

As for butterfly networks, permutations arising from real-world applications can often be implemented using a shorter sequence.

4.3.3 Using baseline networks

Another way of implementing arbitrary 32 bit permutations is using a baseline network followed by an inverse baseline network.

A baseline network is a sequence of $\log_2(\text{XLEN})$ butterfly(0) operations interleaved with unzip operations. For example, a 32-bit baseline network:

```

butterfly(0)
unzip
butterfly(0)
unzip.h
butterfly(0)
unzip.b
butterfly(0)
unzip.n
butterfly(0)

```

An inverse baseline network is a sequence of $\log_2(\text{XLEN})$ butterfly(0) operations interleaved with zip operations. The order is opposite to the order in a baseline network. For example, a 32-bit inverse baseline network:

```

butterfly(0)
zip.n
butterfly(0)
zip.b
butterfly(0)
zip.h
butterfly(0)
zip
butterfly(0)

```

A baseline network followed by an inverse baseline network can implement any arbitrary bit permutation.

4.3.4 Using sheep-and-goats

The Sheep-and-goats (SAG) operation is a common operation for bit permutations. It moves all the bits selected by a mask (goats) to the LSB end of the word and all the remaining bits (sheep) to the MSB end of the word, without changing the order of sheep or goats.

The SAG operation can easily be performed using `bext` (data in `a0` and mask in `a1`):

```

bext a2, a0, a1
c.not a1
bext a0, a0, a1
pcnt a1, a1
ror a0, a0, a1
c.or a0, a2

```

Any arbitrary bit permutation can be implemented in $\log_2(\text{XLEN})$ SAG operations.

The Hacker's Delight describes an optimized standard C implementation of the SAG operation. Their algorithm takes 254 instructions (for 32 bit) or 340 instructions (for 64 bit) on their reference RISC instruction set. [1, p. 152f, 162f]

4.4 Comparison with x86 Bit Manipulation ISAs

The following code snippets implement all instructions from the x86 bit manipulation ISA extensions ABM, BMI1, BMI2, and TBM using RISC-V code that does not spill any registers and thus could easily be implemented in a single instruction using macro-op fusion. (Some of them simply map directly to instructions in this spec and so no macro-op fusion is needed.) Note that shorter RISC-V code sequences are sometimes possible if we allow spilling to temporary registers.

ABM added x86 encodings for POPCNT, LZCNT, and TZCNT.¹ The difference between LZCNT and the 80386 instruction BSR, and between TZCNT and the 80386 instruction BSF, is that the new instructions return the operand size when the input operand is zero, while BSR and BSF were undefined in that case. The ABM instructions map 1:1 to XBitmanip instructions. See Table 4.1.

x86 Instruction	Bytes		RISC-V Code
	x86	RV	
POPCNT	5	4	<code>pcnt a0, a0</code>
LZCNT	5	4	<code>clz a0, a0</code>
TZCNT	5	4	<code>ctz a0, a0</code>

Table 4.1: Comparison of x86 ABM with XBitmanip

BMI1 adds some instructions for trailing bit manipulations, an add-complement instruction, and a bit field extract instruction that expects the length and start position packed in one register operand. Our version expects the length in a0, start position in a1, and source value in a2. See Table 4.2.

x86 Instruction	Bytes		RISC-V Code
	x86	RV	
ANDN	5	4	<code>andc a0, a2, a1</code>
BEXTR (regs)	5	12	<code>c.add a0, a1</code> <code>slo a0, zero, a0</code> <code>c.and a0, a2</code> <code>srl a0, a0, a1</code>
BLSI	5	6	<code>neg a0, a1</code> <code>c.and a0, a1</code>
BLSMSK	5	6	<code>addi a0, a1, -1</code> <code>c.xor a0, a1</code>
BLSR	5	6	<code>addi a0, a1, -1</code> <code>c.and a0, a1</code>

Table 4.2: Comparison of x86 BMI1 with XBitmanip

¹Depending on if you ask Intel or AMD you will get different opinion regarding whether LZCNT and/or TZCNT are part of ABM or BMI1.

BMI2 adds a few **X* instructions that just perform the indicated operation without changing any flags. RISC-V does not use flags, so these instructions trivially just map to their regular RISC-V counterparts. In addition to those instructions, BMI2 adds bit extract and deposit instructions and an instruction to clear high bits above a given bit index. See Table 4.3.

x86 Instruction	Bytes		RISC-V Code
	x86	RV	
BZHI	5	6	<code>slo a0, zero, a2</code> <code>c.and a0, a1</code>
PDEP	5	4	<code>bdep</code>
PEXT	5	4	<code>bext</code>
MULX	5	4	<code>mul</code>
RORX	6	4	<code>rori</code>
SARX	5	4	<code>sra</code>
SHRX	5	4	<code>srl</code>
SHLX	5	4	<code>sll</code>

Table 4.3: Comparison of x86 BMI2 with XBitmanip

Finally, TBM was a short-lived x86 ISA extension introduced by AMD in Piledriver processors, complementing the trailing bit manipulation instructions from BMI1. See Table 4.4.

There will be a separate RISC-V standard for recommended sequences for macro-op fusion. The macros listed here are merely for demonstrating that suitable sequences exist. We do not advocate for any of those sequences to become “standard sequences” for macro-op fusion.

4.5 Comparison with RI5CY Bit Manipulation ISA

The following section compares XBitmanip with the RI5CY bit manipulation instructions as documented in [2]. All RI5CY bit manipulation instructions can be emulated with XBitmanip using 3 instructions or less.

RI5CY Instructions `p.extract`, `p.extractu`, `p.extractr`, and `p.extractur`

These four RI5CY instructions extract bit-fields. The non-*u*-versions sign-extend the extracted bit-field. This operations can be performed with two shift-immediate operations. It even fits in a 32-bit word when using compressed instructions (requires `rd = rs`).

```
p.extract rd, rs, len, pos:
    slli rd, rs, (XLEN-pos-len)
    srai rd, rd, (XLEN-len)
```

```
p.extractu rd, rs, len, pos:
    slli rd, rs, (XLEN-pos-len)
    srli rd, rd, (XLEN-len)
```

x86 Instruction	Bytes		RISC-V Code
	x86	RV	
BEXTR (imm)	7	4	c.slli a0, (32-START-LEN) c.srli a0, (32-LEN)
BLCFILL	5	6	addi a0, a1, 1 c.and a0, a1
BLCI	5	8	addi a0, a1, 1 c.not a0 c.or a0, a1
BLCIC	5	10	addi a0, a1, 1 andc a0, a1, a0 c.not a0
BLCMSK	5	6	addi a0, a1, 1 c.xor a0, a1
BLCS	5	6	addi a0, a1, 1 c.or a0, a1
BLSFILL	5	6	addi a0, a1, -1 c.or a0, a1
BLSIC	5	10	addi a0, a1, -1 andc a0, a1, a0 c.not a0
T1MSKC	5	10	addi a0, a1, +1 andc a0, a1, a0 c.not a0
T1MSK	5	8	addi a0, a1, -1 andc a0, a0, a1

Table 4.4: Comparison of x86 TBM with XBitmanip

The **r**-versions expect the bit-field size in bits 9:5 of the second source register and the bit-field start in bits 4:0. Instead we use two registers, **rx** = $XLEN - pos - len$ and **ry** = $XLEN - len$.

```
p.extractr:
    sll rd, rs, rx
    sra rd, rd, ry
```

```
p.extractu:
    sll rd, rs, rx
    srl rd, rd, ry
```

RI5CY Instructions **p.insert** and **p.insertr**

These instructions OR the destination register with the **len** LSB bits from the source register, shifted up by **pos** bits. This can easily be achieved using three instructions and a temporary register **rt**:

```

p.insert rd, rs, len, pos, rt:
    slli rt, rs, (XLEN-len)
    srli rt, rt, (XLEN-len-pos)
    or rd, rd, rt

```

The **r**-version of the instruction expects **len** in bits 9:5 of the second source register and **pos** in bits 4:0. Instead we use two registers, **rx** = $XLEN - pos - len$ and **ry** = $XLEN - len$.

```

p.insertr:
    slli rt, rs, ry
    srli rt, rt, rx
    or rd, rd, rt

```

RI5CY Instructions **p.bclr** and **p.bclrr**

These instructions clear **len** bits starting with bit **pos**. Using a temporary register **rt**:

```

p.bclr rd, rs, len, pos, rt:
    sloi rt, zero, len
    slli rt, rt, pos
    andc rd, rs, rt

```

Or using two registers **rLen** and **rPos**:

```

p.bclr rd, rs, rLen, rPos, rt:
    slo rt, zero, rLen
    sll rt, rt, rPos
    andc rd, rs, rt

```

RI5CY Instructions **p.bset** and **p.bsetr**

These instructions set **len** bits starting with bit **pos**. They can be implemented similar to **p.bclr** and **p.bclrr** by replacing **andc** with **or**:

```

p.bset rd, rs, len, pos, rt:
    sloi rt, zero, len
    slli rt, rt, pos
    or rd, rs, rt

```

```

p.bset rd, rs, rLen, rPos, rt:
    slo rt, zero, rLen
    sll rt, rt, rPos
    or rd, rs, rt

```

RI5CY Instructions p.ff1, p.cnt, and p.ror

These instructions map directly to the XBitmanip instructions `ctz`, `pcnt`, and `ror`.

RI5CY Instructions p.fl1

This instruction returns the index of the last set bit in `rs`.

```
p.fl1 rd, rs:
    clz rd, rs
    neg rd, rd
    addi rd, rd, 31
```

RI5CY Instructions p.clb

This instruction counts the number of consecutive 1s or 0s from MSB. If `rs1` is 0, `rd` will be 0.

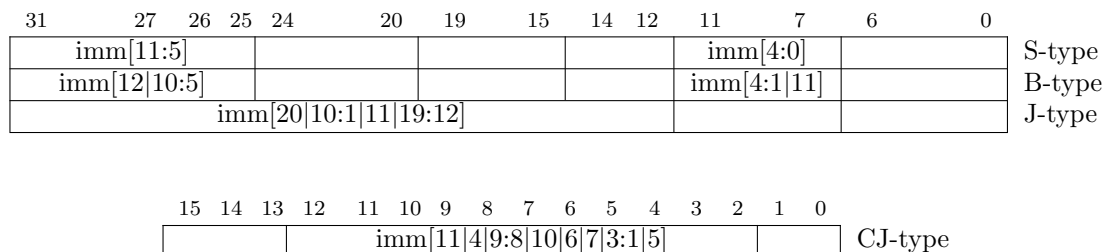
Using the arguably more consistent definition that the instruction should return `XLEN` when `rs1` is 0, and assuming `rd` \neq `rs1`:

```
p.clb:
    srai rd, rs1, XLEN-1
    xor rd, rd, rs1
    clz rd, rd
```

Simply add `andi rd, rd, XLEN-1` if `rd` should be zero when `rs1` is 0.

4.6 Decoding RISC-V Immediates

The following code snippets decode and sign-extend the immediate from RISC-V S-type, B-type, J-type, and CJ-type instructions. They are nice “nothing up my sleeve”-examples for real-world bit permutations.




```

decode_s:
    li t0, 0xfe000f80
    bext a0, a0, t0
    c.slli a0, 20
    c.srai a0, 20
    ret

decode_b:
    li t0, 0xea800aa
    rori a0, a0, 8
    grevi a0, a0, 8
    gzip a0, a0, 14
    bext a0, a0, t0
    c.slli a0, 20
    c.srai a0, 19
    ret

decode_j:
    li t0, 0x800003ff
    li t1, 0x800ff000
    bext a1, a0, t1
    c.slli a1, 23
    rori a0, a0, 21
    bext a0, a0, t0
    c.slli a0, 12
    c.or a0, a1
    c.srai a0, 11
    ret

// variant 1 (with XBitmanip)
decode_cj:
    li t0, 0x28800001
    li t1, 0x000016b8
    li t2, 0xb4e00000
    li t3, 0x4b000000
    bext a1, a0, t1

    bdep a1, a1, t2
    rori a0, a0, 11
    bext a0, a0, t0
    bdep a0, a0, t3
    c.or a0, a1
    c.srai a0, 20
    ret

// variant 2 (without XBitmanip)
decode_cj:
    srli a5, a0, 2
    srli a4, a0, 7
    c.andi a4, 16
    slli a3, a0, 3
    c.andi a5, 14
    c.add a5, a4
    andi a3, a3, 32
    srli a4, a0, 1
    c.add a5, a3
    andi a4, a4, 64
    slli a2, a0, 1
    c.add a5, a4
    andi a2, a2, 128
    srli a3, a0, 1
    slli a4, a0, 19
    c.add a5, a2
    andi a3, a3, 768
    c.slli a0, 2
    c.add a5, a3
    andi a0, a0, 1024
    c.srai a4, 31
    c.add a5, a0
    slli a0, a4, 11
    c.add a0, a5
    ret

```


Chapter 5

XBitfield Extension

The most asked-for feature in XBitmanip is an instruction for bit field extract. XBitmanip recommends the usage of `slli` followed by `slri` for this operation and asks implementors to fuse this sequence into a single macro-op. However, there are valid concerns regarding this approach:

- Not all processors that might want to implement a fast bitfield extract can fuse macro-ops.
- In some architectures it might be hard to fuse the two shift instructions if one of them is using a 32-bit instruction encoding. Therefore the instruction can not be fused if `rd` \neq `rs1`.
- `bext` and `bdep` can do a lot of the heavy lifting in applications that would otherwise require many individual bitfield-extract operations. But smaller cores might not provide a fast `bext`/`bdep` unit, or provide no hardware support for those instructions at all.

Therefore this chapter proposes the RISC-V XBitfield extension. Note that, unlike XBitmanip, **we do not propose XBitfield for adoption as official RISC-V ISA extension.**

The encoding for a proper 32-bit bitfield extract instruction, if encoded in a clean and future-safe way that scales all the way to RV128, would require a 14 bit immediate (7 bits for start and 7 bits for length), or the equivalent of 4 I-type instructions with full immediate length, or half of a major opcode, way too wasteful for an official RISC-V ISA extension, especially for something that can be encoded in the same space with two compressed instructions.

However, there is a tendency for implementors to fill the unused instruction encoding space with a myriad of complex instructions with large immediates. [2]

So might as well propose XBitfield, a custom, non-standard extension that uses almost the entire major opcode 1111011 (*custom-3*) for a single bit-field extract and place (`bfxp`) instruction, effectively packing 3 shift-immediate operations and one OR in one single instruction.

The main goal here is that individual implementors can use the same patches for compiler toolchains. By standardising one powerful but easy to implement instruction instead of a whole range of simpler instructions we keep the complexity of the extension low and ease adoption.

5.1 Bit-field extract and place (bfxp)

The bit-field extract and place instruction extracts a bitfield of length `len` starting at bit position `start`, creates a new value with the extraced bitfield at offset `dest`, and OR's that with `rs2`.

The immediate argument `start` is a 5 bit unsigned immediate on RV32 and a 6 bit unsigned immediate on RV64.

The immediate arguments `len` and `dest` are unsigned 5 bit immediates. On RV64 `len = 0` encodes for `len = 32`. On RV32 `len = 0` is reserved for other instructions.

Instruction words with `start + len > XLEN` or `dest + len > XLEN` are reserved for other instructions.

```
uint_xlen_t bfxp(uint_xlen_t rs1, uint_xlen_t rs2,
                 unsigned start, unsigned len, unsigned dest)
{
    assert(start < XLEN && len < 32 && dest < 32);

    if (XLEN > 32 && len == 0)
        len = 32;

    assert(start + len <= XLEN);
    assert(dest + len <= XLEN);
    assert(len != 0);

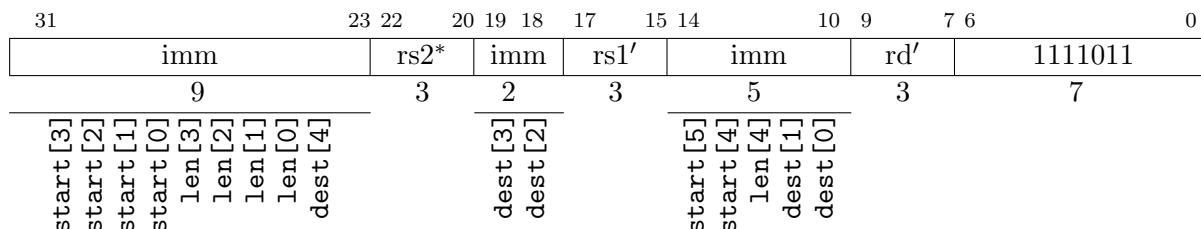
    uint_xlen_t x = rs1;
    x <<= XLEN-start-len;
    x >>= XLEN-len;
    x <<= dest;

    return x | rs2;
}
```

The assembler mnemonic for `bfxp` is as follows.

```
bfxp rd, rs1, rs2, start, len, dest
```

`bfxp` occupies the *custom-3* major opcode:



With $rs1'$ and rd' interpreted as in “C” opcodes ($rs1 = rs1' + 8$, $rd = rd' + 8$), and $rs2^*$ being interpreted the same way, except that $rs2 = 0$ when $rs2^* = 0$.

The bits from **start**, **len**, and **dest** are placed in the three immediate fields in a manner that aims at maximizing the usefulness of the remaining brownfield in the *custom-3* opcode: On RV64, if instruction bits 14:12 are all set ($funct3 = 111$), then the instruction is reserved if any of the bits 31:24 are set.

5.2 Evaluation: Decoding RISC-V immediates

The following code snippets decode and sign-extend the immediate from RISC-V S-type, B-type, J-type, and CJ-type instructions. They are nice “nothing up my sleeve”-examples for real-world bit permutations.

31	27	26	25	24	20	19	15	14	12	11	7	6	0	
imm[11:5]										imm[4:0]				S-type
imm[12 10:5]										imm[4:1 11]				B-type
imm[20 10:1 11 19:12]														J-type

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	
				imm[11 4 9:8 10 6 7 3:1 5]												CJ-type

```

decode_s:
    bfxp a1, a0, zero, 7, 5, 20
    bfxp a0, a0, a1, 25, 7, 25
    c.srai a0, 20
    ret

decode_b:
    bfxp a1, a0, zero, 7, 1, 30
    bfxp a1, a0, a1, 25, 6, 24
    bfxp a1, a0, a1, 8, 4, 20
    bfxp a0, a0, a1, 31, 1, 31
    c.srai a0, 19
    ret

decode_j:
    bfxp a1, a0, zero, 21, 10, 12
    bfxp a1, a0, a1, 20, 1, 22

    bfxp a1, a0, a1, 12, 8, 23
    bfxp a0, a0, a1, 31, 1, 31
    c.srai a0, 11
    ret

decode_cj:
    bfxp a1, a0, zero, 11, 1, 24
    bfxp a1, a0, a1, 9, 2, 28
    bfxp a1, a0, a1, 8, 1, 30
    bfxp a1, a0, a1, 7, 1, 26
    bfxp a1, a0, a1, 6, 1, 27
    bfxp a1, a0, a1, 3, 3, 21
    bfxp a1, a0, a1, 2, 1, 25
    bfxp a0, a0, a1, 12, 1, 31
    c.srai a0, 20
    ret

```


Chapter 6

Fast C reference implementations

GCC has intrinsics for the bit counting instructions `clz`, `ctz`, and `pcnt`. So a performance-sensitive application (such as an emulator) should probably just use those:

```
uint32_t fast_clz32(uint32_t rs1)
{
    if (rs1 == 0)
        return XLEN;
    assert(sizeof(int) == 4);
    return __builtin_clz(rs1);
}

uint64_t fast_clz64(uint64_t rs1)
{
    if (rs1 == 0)
        return XLEN;
    assert(sizeof(long long) == 8);
    return __builtin_clzll(rs1);
}

uint32_t fast_ctz32(uint32_t rs1)
{
    if (rs1 == 0)
        return XLEN;
    assert(sizeof(int) == 4);
    return __builtin_ctz(rs1);
}

uint64_t fast_ctz64(uint64_t rs1)
{
    if (rs1 == 0)
        return XLEN;
    assert(sizeof(long long) == 8);
    return __builtin_ctzll(rs1);
}
```

```

uint32_t fast_pcmt32(uint32_t rs1)
{
    assert(sizeof(int) == 4);
    return __builtin_popcount(rs1);
}

uint64_t fast_pcmt64(uint64_t rs1)
{
    assert(sizeof(long long) == 8);
    return __builtin_popcountll(rs1);
}

```

For processors with BMI2 support GCC has intrinsics for bit extract and bit deposit instructions (compile with `-mbmi2`):

```

uint32_t fast_bext32(uint32_t rs1, uint32_t rs2)
{
    return _pext_u32(rs1, rs2);
}

uint64_t fast_bext64(uint64_t rs1, uint64_t rs2)
{
    return _pext_u64(rs1, rs2);
}

uint32_t fast_bdep32(uint32_t rs1, uint32_t rs2)
{
    return _pdep_u32(rs1, rs2);
}

uint64_t fast_bdep64(uint64_t rs1, uint64_t rs2)
{
    return _pdep_u64(rs1, rs2);
}

```

For other processors we need to provide our own implementations. The following implementation is a good compromise between code complexity and runtime:

```

uint_xlen_t fast_bext(uint_xlen_t rs1, uint_xlen_t rs2)
{
    uint_xlen_t c = 0, i = 0, mask = rs2;
    while (mask) {
        uint_xlen_t b = mask & ~((mask | (mask-1)) + 1);
        c |= (rs1 & b) >> (fast_ctz(b) - i);
        i += fast_pcmt(b);
        mask -= b;
    }
    return c;
}

```



```
uint_xlen_t fast_bdep(uint_xlen_t rs1, uint_xlen_t rs2)
{
    uint_xlen_t c = 0, i = 0, mask = rs2;
    while (mask) {
        uint_xlen_t b = mask & ~((mask | (mask-1)) + 1);
        c |= (rs1 << (fast_ctz(b) - i)) & b;
        i += fast_pcnt(b);
        mask -= b;
    }
    return c;
}
```

For the other XBitmanip instructions the C reference functions given in Chapter 2 are already reasonably efficient.

Change History

Date	Rev	Changes
2017-07-17	0.10	Initial Draft
2017-11-02	0.11	Removed roli, assembler can convert it to use a rori Removed bitwise subset and replaced with andc Doc source text same base for study and spec. Fixed typos
2017-11-30	0.32	Jump rev number to be on par with associated Study Moved pdep/pext into spec draft and called it scattergather
2018-04-07	0.33	Move to github, throw out study, convert from .md to .tex Fixed typos and fixed some reference C implementations Rename bgat/bsca to bext/bdep Remove post-add immediate from clz Clean up encoding tables and code sections
2018-04-20	0.34	Add GREV, CTZ, and compressed instructions Restructure document: Move discussions to extra sections Add FAQ, add analysis of used encoding space Add Pseudo-Ops, Macros, Algorithms Add Generalized Bit Permutations (shuffle)
????-??-??	0.35	Replace shuffle with generalized zip (gzip) Add additional XBitfield ISA Extension Add figures and tables, Clean up document Add Verilog reference implementations Add fast C reference implementations

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