SAMB for "ch4"

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• Generation condition

model type: tight_bindingtime-reversal type: electric

- irrep: [A1]
- spinful

• Kets: dimension = 16

Table 1: Hilbert space for full matrix.

No.	ket	No.	ket	No.	ket	No.	ket	No.	ket
1	(s,\uparrow) @C ₁	2	(s,\downarrow) @C ₁	3	(p_x,\uparrow) @C ₁	4	(p_x,\downarrow) @C ₁	5	(p_y,\uparrow) @C ₁
6	(p_y,\downarrow) @C ₁	7	(p_z,\uparrow) @C ₁	8	(p_z,\downarrow) @C ₁	9	(s,\uparrow) @H ₁	10	(s,\downarrow) @H ₁
11	(s,\uparrow) @H ₂	12	(s,\downarrow) @H ₂	13	(s,\uparrow) @H ₃	14	(s,\downarrow) @H ₃	15	(s,\uparrow) @H ₄
 16	(s,\downarrow) @H ₄								

• Sites in (primitive) unit cell:

Table 2: Site-clusters.

site position		mapping
$S_1 [1o: -43m] C_1$	$\begin{pmatrix} 0 & 0 & 0 \end{pmatrix}$	[1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,24]

Table 2

	site	position	mapping
$S_2 [4a: .3m]$	H_1	$\begin{pmatrix} \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \end{pmatrix}$	[1,5,9,16,17,18]
	H_2	$\left(-\frac{1}{3} -\frac{1}{3} \frac{1}{3} \right)$	[2,6,11,13,21,23]
	H_3	$\left(\begin{array}{ccc} \frac{1}{3} & -\frac{1}{3} & -\frac{1}{3} \end{array}\right)$	[3,7,12,15,19,24]
	H_4	$\left(-\frac{1}{3} \frac{1}{3} -\frac{1}{3}\right)$	[4,8,10,14,20,22]

• Bonds in (primitive) unit cell:

Table 3: Bond-clusters.

	bond	tail	head	n	#	b@c	mapping
B ₁ [4a: .3m]	b_1	C_1	H_1	1	1	$\left(\frac{1}{3} \frac{1}{3} \frac{1}{3}\right) @ \left(\frac{1}{6} \frac{1}{6} \frac{1}{6}\right)$	[1,5,9,16,17,18]
	b_2	C_1	H_2	1	1	$\left[\begin{array}{cccc} \left(-\frac{1}{3} & -\frac{1}{3} & \frac{1}{3} \right) @ \left(-\frac{1}{6} & -\frac{1}{6} & \frac{1}{6} \right) \end{array} \right]$	[2,6,11,13,21,23]
	b_3	C_1	H_3	1	1	$\left[\begin{array}{cccc} \left(\frac{1}{3} & -\frac{1}{3} & -\frac{1}{3} \right) @ \left(\frac{1}{6} & -\frac{1}{6} & -\frac{1}{6} \right) \end{array} \right]$	$[3,\!7,\!12,\!15,\!19,\!24]$
	b_4	C_1	H_4	1	1	$\left[\begin{array}{cccc} \left(-\frac{1}{3} & \frac{1}{3} & -\frac{1}{3} \right) @ \left(-\frac{1}{6} & \frac{1}{6} & -\frac{1}{6} \right) \end{array} \right]$	$[4,\!8,\!10,\!14,\!20,\!22]$
B ₂ [6b: 2.mm]	b_5	H_1	H_2	1	1	$ \left(-\frac{2}{3} -\frac{2}{3} 0 \right) @ \left(0 0 \frac{1}{3} \right) $	[1,-2,-13,16]
	b_6	H_3	${\rm H}_4$	1	1	$\left(-\frac{2}{3} \frac{2}{3} 0\right) @ \left(0 0 -\frac{1}{3}\right)$	[3, -4, 19, -22]
	b_7	H_1	H_3	1	1	$\left[\begin{array}{cccc} \left(0 & -\frac{2}{3} & -\frac{2}{3} \right) @ \left(\frac{1}{3} & 0 & 0 \right) \end{array} \right]$	[5, -7, 17, -24]
	b_8	H_2	H_4	1	1	$\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$	[6, -8, -14, 21]
	b_9	H_1	H_4	1	1	$\left(-\frac{2}{3} 0 -\frac{2}{3}\right) @ \left(0 \frac{1}{3} 0\right)$	[9, -10, 18, -20]
	b ₁₀	H_2	H_3	1	1	$ \left(\begin{array}{ccc} \frac{2}{3} & 0 & -\frac{2}{3} \end{array}\right) @ \left(0 & -\frac{1}{3} & 0\right) $	[11,-12,-15,23]

• SAMB:

No. 2
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₃, S₁]

$$\hat{\mathbb{Z}}_2 = \mathbb{X}_{011}[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{U}_{001}[\mathbb{Q}_0^{(s,A_1)}]$$

No. 3
$$\hat{\mathbb{Q}}_0^{(A_1)}(1,1)$$
 [M₃, S₁]

$$\hat{\mathbb{Z}}_3 = \mathbb{X}_{012}[\mathbb{Q}_0^{(a,A_1)}(1,1)] \otimes \mathbb{U}_{001}[\mathbb{Q}_0^{(s,A_1)}]$$

No. 4
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₁, S₂]

$$\hat{\mathbb{Z}}_4 = \mathbb{X}_{001}[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{U}_{002}[\mathbb{Q}_0^{(s,A_1)}]$$

No. 5
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₁, B₁]

$$\hat{\mathbb{Z}}_5 = \mathbb{X}_{001}[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{U}_{003}[\mathbb{Q}_0^{(u,A_1)}]$$

No. 6
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₂, B₁]

$$\hat{\mathbb{Z}}_{6} = \frac{\sqrt{3}\mathbb{X}_{005}[\mathbb{Q}_{1,0}^{(a,T_{2})}] \otimes \mathbb{U}_{004}[\mathbb{Q}_{1,0}^{(u,T_{2})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{006}[\mathbb{Q}_{1,1}^{(a,T_{2})}] \otimes \mathbb{U}_{005}[\mathbb{Q}_{1,1}^{(u,T_{2})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{007}[\mathbb{Q}_{1,2}^{(a,T_{2})}] \otimes \mathbb{U}_{006}[\mathbb{Q}_{1,2}^{(u,T_{2})}]}{3}$$

No. 7
$$\hat{\mathbb{Q}}_0^{(A_1)}(1,0) [M_2, B_1]$$

$$\hat{\mathbb{Z}}_{7} = \frac{\sqrt{3}\mathbb{X}_{008}[\mathbb{Q}_{1,0}^{(a,T_{2})}(1,0)] \otimes \mathbb{U}_{004}[\mathbb{Q}_{1,0}^{(u,T_{2})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{009}[\mathbb{Q}_{1,1}^{(a,T_{2})}(1,0)] \otimes \mathbb{U}_{005}[\mathbb{Q}_{1,1}^{(u,T_{2})}]}{3} + \frac{\sqrt{3}\mathbb{X}_{010}[\mathbb{Q}_{1,2}^{(a,T_{2})}(1,0)] \otimes \mathbb{U}_{006}[\mathbb{Q}_{1,2}^{(u,T_{2})}]}{3}$$

No. 8
$$\hat{\mathbb{Q}}_0^{(A_1)}$$
 [M₁, B₂]

$$\hat{\mathbb{Z}}_8 = \mathbb{X}_{001}[\mathbb{Q}_0^{(a,A_1)}] \otimes \mathbb{U}_{007}[\mathbb{Q}_0^{(u,A_1)}]$$

No. 9
$$\hat{\mathbb{Q}}_3^{(A_1)}(1,-1)$$
 [M₁, B₂]

$$\hat{\mathbb{Z}}_9 = \frac{\sqrt{3}\mathbb{X}_{002}[\mathbb{M}_{1,0}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_{008}[\mathbb{T}_{3,0}^{(u,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{003}[\mathbb{M}_{1,1}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_{009}[\mathbb{T}_{3,1}^{(u,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{004}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{004}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{004}[\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{004}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}]}{3} + \frac{\sqrt{3}\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}]}{3} + \frac{\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}]}{3} + \frac{\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}]}{3} + \frac{\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}]}{3} + \frac{\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}(1,-1)]}{3} + \frac{\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}(1,-1)]}{3} + \frac{\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{U}_{010}[\mathbb{T}_{3,2}^{(u,T_1)}(1,-1)]}{3} + \frac{\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)]}{3} + \frac{\mathbb{X}_{010}[\mathbb{M}_{1,2}^{(u,T_1)}(1,-1)] \otimes \mathbb$$

Table 4: Atomic SAMB group.

group	bra	ket
M_1	$(s,\uparrow),(s,\downarrow)$	$(s,\uparrow),(s,\downarrow)$
M_2	$(s,\uparrow),(s,\downarrow)$	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$
M_3	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$	$(p_x,\uparrow),(p_x,\downarrow),(p_y,\uparrow),(p_y,\downarrow),(p_z,\uparrow),(p_z,\downarrow)$

Table 5: Atomic SAMB.

symbol	type	group	form
\mathbb{X}_1	$\mathbb{Q}_0^{(a,A_1)}$	M_1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & 0\\ 0 & \frac{\sqrt{2}}{2} \end{pmatrix}$
\mathbb{X}_2	$\mathbb{M}_{1,0}^{(a,T_1)}(1,-1)$	M_1	$\begin{pmatrix} 0 & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & 0 \end{pmatrix}$
\mathbb{X}_3	$\mathbb{M}_{1,1}^{(a,T_1)}(1,-1)$	M_1	$\begin{pmatrix} 0 & -rac{\sqrt{2}i}{2} \ rac{\sqrt{2}i}{2} & 0 \end{pmatrix}$
\mathbb{X}_4	$\mathbb{M}_{1,2}^{(a,T_1)}(1,-1)$	M_1	
\mathbb{X}_{5}	$\mathbb{Q}_{1,0}^{(a,T_2)}$	M_2	$\begin{pmatrix} \frac{\sqrt{2}}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{2}}{2} & 0 & 0 & 0 & 0 \end{pmatrix}$
\mathbb{X}_6	$\mathbb{Q}_{1,1}^{(a,T_2)}$	M_2	$\begin{pmatrix} 0 & 0 & \frac{\sqrt{2}}{2} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{2}}{2} & 0 & 0 \end{pmatrix}$
\mathbb{X}_7	$\mathbb{Q}_{1,2}^{(a,T_2)}$	M_2	$\begin{pmatrix} 0 & 0 & \frac{\sqrt{2}}{2} & 0 & 0 & 0\\ 0 & 0 & 0 & \frac{\sqrt{2}}{2} & 0 & 0 \end{pmatrix}$ $\begin{pmatrix} 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{2} & 0\\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{2}}{2} \end{pmatrix}$
\mathbb{X}_8	$\mathbb{Q}_{1,0}^{(a,T_2)}(1,0)$	M_2	$\begin{pmatrix} 0 & 0 & -\frac{i}{2} & 0 & 0 & \frac{1}{2} \\ 0 & 0 & 0 & \frac{i}{2} & -\frac{1}{2} & 0 \end{pmatrix}$
\mathbb{X}_9	$\mathbb{Q}_{1,1}^{(a,T_2)}(1,0)$	M_2	$egin{pmatrix} rac{i}{2} & 0 & 0 & 0 & 0 & -rac{i}{2} \ 0 & -rac{i}{2} & 0 & 0 & -rac{i}{2} & 0 \end{pmatrix}$
\mathbb{X}_{10}	$\mathbb{Q}_{1,2}^{(a,T_2)}(1,0)$	M_2	$\begin{pmatrix} 0 & -\frac{1}{2} & 0 & \frac{i}{2} & 0 & 0 \\ \frac{1}{2} & 0 & \frac{i}{2} & 0 & 0 & 0 \end{pmatrix}$

Table 5

symbol	type	group	form				
X ₁₁	$\mathbb{Q}_0^{(a,A_1)}$	M_3	$\begin{pmatrix} \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{\sqrt{6}}{6} \end{pmatrix}$				
\mathbb{X}_{12}	$\mathbb{Q}_0^{(a,A_1)}(1,1)$	M_3	$ \begin{pmatrix} 0 & 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & \frac{\sqrt{3}}{6} \\ 0 & 0 & 0 & \frac{\sqrt{3}i}{6} & -\frac{\sqrt{3}}{6} & 0 \\ \frac{\sqrt{3}i}{6} & 0 & 0 & 0 & 0 & -\frac{\sqrt{3}i}{6} \\ 0 & -\frac{\sqrt{3}i}{6} & 0 & 0 & -\frac{\sqrt{3}i}{6} & 0 \\ 0 & -\frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 \\ \frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}i}{6} & 0 & 0 & 0 \end{pmatrix} $				

Table 6: Uniform SAMB.

symbol	type	cluster	form
\mathbb{U}_1	$\mathbb{Q}_0^{(s,A_1)}$	S_1	$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 &$
\mathbb{U}_2	$\mathbb{Q}_0^{(s,A_1)}$	S_2	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{2} & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{2} & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{2} & 0 \\ 0 & 0 & 0 & 0 & \frac{1}{2} \end{pmatrix}$

Table 6

symbol	type	cluster	form
\mathbb{U}_3	$\mathbb{Q}_0^{(u,A_1)}$	B ₁	$\begin{pmatrix} 0 & \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} \\ \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \end{pmatrix}$
\mathbb{U}_4	$\mathbb{Q}_{1,0}^{(u,T_2)}$	В1	$ \begin{pmatrix} 0 & \frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} \\ \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \end{pmatrix} $
\mathbb{U}_5	$\mathbb{Q}_{1,1}^{(u,T_2)}$	В1	$ \begin{pmatrix} 0 & \frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{4} \\ \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ -\frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \\ \frac{\sqrt{2}}{4} & 0 & 0 & 0 & 0 \end{pmatrix} $
\mathbb{U}_6	$\mathbb{Q}_{1,2}^{(u,T_2)}$	В1	$ \begin{pmatrix} $
\mathbb{U}_7	$\mathbb{Q}_0^{(u,A_1)}$	B ₂	$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{\sqrt{3}}{6} & \frac{\sqrt{3}}{6} & \frac{\sqrt{3}}{6} \\ 0 & \frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}}{6} & \frac{\sqrt{3}}{6} \\ 0 & \frac{\sqrt{3}}{6} & \frac{\sqrt{3}}{6} & 0 & \frac{\sqrt{3}}{6} \\ 0 & \frac{\sqrt{3}}{6} & \frac{\sqrt{3}}{6} & \frac{\sqrt{3}}{6} & 0 \end{pmatrix}$
\mathbb{U}_8	$\mathbb{T}_{3,0}^{(u,T_1)}$	B_2	$ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{\sqrt{2}i}{4} & 0 & \frac{\sqrt{2}i}{4} \\ 0 & \frac{\sqrt{2}i}{4} & 0 & -\frac{\sqrt{2}i}{4} & 0 \\ 0 & 0 & \frac{\sqrt{2}i}{4} & 0 & -\frac{\sqrt{2}i}{4} \\ 0 & -\frac{\sqrt{2}i}{4} & 0 & \frac{\sqrt{2}i}{4} & 0 \end{pmatrix} $

Table 6

symbol	type	cluster	form					
\mathbb{U}_9	$\mathbb{T}_{3,1}^{(u,T_1)}$	В2	$\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$	0 $-\frac{\sqrt{2}i}{\frac{4}{\sqrt{2}i}}$ 0	0 $\frac{\sqrt{2}i}{4}$ 0 0 $\sqrt{2}i$	0 $-\frac{\sqrt{2}i}{4}$ 0 0 $\frac{\sqrt{2}i}{4}$	$ \begin{pmatrix} 0 \\ 0 \\ \frac{\sqrt{2}i}{4} \\ -\frac{\sqrt{2}i}{4} \\ 0 \end{pmatrix} $	
\mathbb{U}_{10}	$\mathbb{T}_{3,2}^{(u,T_1)}$	B_2	$\begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$	0 0 0 $-\frac{\sqrt{2}i}{\frac{\sqrt{2}i}{4}}$	$ \begin{array}{c} -\frac{4}{4} \\ 0 \\ 0 \\ 0 \\ \frac{\sqrt{2}i}{4} \\ -\frac{\sqrt{2}i}{4} \end{array} $	$ \begin{array}{r} \hline 4 \\ 0 \\ \hline \frac{\sqrt{2}i}{4} \\ -\frac{\sqrt{2}i}{4} \\ 0 \\ 0 \end{array} $	$ \begin{pmatrix} 0 \\ -\frac{\sqrt{2}i}{4} \\ \frac{\sqrt{2}i}{4} \\ 0 \\ 0 \end{pmatrix} $	

Table 7: Polar harmonics.

No.	symbol	rank	irrep.	mul.	comp.	form
1	$\mathbb{Q}_0^{(A_1)}$	0	A_1	_	_	1
2	$\mathbb{Q}_{1,0}^{(T_2)}$	1	T_2	-	0	x
3	$\mathbb{Q}_{1,1}^{(T_2)}$	1	T_2	_	1	y
4	$\mathbb{Q}_{1,2}^{(T_2)}$	1	T_2	_	2	z
5	$\mathbb{Q}_{3,0}^{(T_1)}$	3	T_1	_	0	$\frac{\sqrt{15}x(y-z)(y+z)}{2}$
6	$\mathbb{Q}_{3,1}^{(T_1)}$	3	T_1	_	1	$-\frac{\sqrt{15}y(x-z)(x+z)}{2}$
7	$\mathbb{Q}_{3,2}^{(T_1)}$	3	T_1	_	2	$\frac{\sqrt{15}z(x-y)(x+y)}{2}$

Table 8: Axial harmonics.

No.	symbol	rank	irrep.	mul.	comp.	form
1	$\mathbb{G}_{1,0}^{(T_1)}$	1	T_1	_	0	X
2	$\mathbb{G}_{1,1}^{(T_1)}$	1	T_1	_	1	Y
3	$\mathbb{G}_{1,2}^{(T_1)}$	1	T_1	_	2	Z

 \bullet Group info.: Generator = 2001, 2010, $3^+_{\ 111},\ m_{1-10}$

Table 9: Conjugacy class.

rep. SO	symmetry operations
1	1
2001	$2_{001}, 2_{100}, 2_{010}$
3 ⁺ ₁₁₁	$\begin{vmatrix} 3_{111}^+, \ 3_{1-1-1}^+, \ 3_{-11-1}^+, \ 3_{-1-11}^+, \ 3_{111}^-, \ 3_{1-1-1}^-, \ 3_{-11-1}^-, \ 3_{-1-11}^- \end{vmatrix}$
m_{110}	$m_{110}, m_{101}, m_{011}, m_{1-10}, m_{-101}, m_{01-1}$
-4^{+}_{001}	$-4^{+}_{001}, -4^{+}_{100}, -4^{+}_{010}, -4^{-}_{001}, -4^{-}_{100}, -4^{-}_{010}$

Table 10: Symmetry operations.

No.	SO	No.	SO	No.	SO	No.	SO	No.	SO
 1	1	2	2_{001}	3	2_{100}	4	2_{010}	5	3^{+}_{111}
6	3^{+}_{1-1-1}	7	3^{+}_{-11-1}	8	3^{+}_{-1-11}	9	3^{-}_{111}	10	3^{-}_{1-1-1}
11	3^{-}_{-11-1}	12	3^{-}_{-1-11}	13	m_{110}	14	m_{101}	15	m_{011}
16	m_{1-10}	17	m_{-101}	18	m_{01-1}	19	-4^{+}_{001}	20	-4^{+}_{100}
 21	-4^{+}_{010}	22	-4^{-}_{001}	23	-4^{-}_{100}	24	-4^{-}_{010}		

Table 11: Character table.

	1	2001	3 ⁺ ₁₁₁	m ₁₁₀	-4^{+}_{001}
$\overline{A_1}$	1	1	1	1	1
A_2	1	1	1	-1	-1
E	2	2	-1	0	0
T_1	3	-1	0	-1	1
T_2	3	-1	0	1	-1

Table 12: Parity conversion.

\leftrightarrow	\leftrightarrow	\leftrightarrow	\leftrightarrow	\leftrightarrow
$A_1 (A_2)$	$A_2 (A_1)$	E(E)	T_1 (T_2)	T_2 (T_1)

Table 13: Symmetric product, $[\Gamma \otimes \Gamma']_+$.

	A_1	A_2	E	T_1	T_2
A_1	A_1	A_2	E	T_1	T_2
A_2		A_1	E	T_2	T_1
E			$A_1 + E$	$T_1 + T_2$	$T_1 + T_2$
T_1				$A_1 + E + T_2$	$A_2 + E + T_1 + T_2$
T_2					$A_1 + E + T_2$

Table 14: Anti-symmetric product, $[\Gamma \otimes \Gamma]_-$.

\overline{A}	$A_1 = A_2$	2 E	T_1	T_2
		A_2	T_1	T_1

Table 15: Virtual-cluster sites.

No.	position	No.	position	No.	position	No.	position
1	$\begin{pmatrix} 2 & 1 & 0 \end{pmatrix}$	2	$\begin{pmatrix} -2 & -1 & 0 \end{pmatrix}$	3	$\begin{pmatrix} 2 & -1 & 0 \end{pmatrix}$	4	$\begin{pmatrix} -2 & 1 & 0 \end{pmatrix}$
5	$\begin{pmatrix} 0 & 2 & 1 \end{pmatrix}$	6	$\begin{pmatrix} 0 & -2 & 1 \end{pmatrix}$	7	$\begin{pmatrix} 0 & -2 & -1 \end{pmatrix}$	8	$\begin{pmatrix} 0 & 2 & -1 \end{pmatrix}$
9	$\begin{pmatrix} 1 & 0 & 2 \end{pmatrix}$	10	$\begin{pmatrix} -1 & 0 & -2 \end{pmatrix}$	11	$\begin{pmatrix} -1 & 0 & 2 \end{pmatrix}$	12	$\begin{pmatrix} 1 & 0 & -2 \end{pmatrix}$
13	$\begin{pmatrix} -1 & -2 & 0 \end{pmatrix}$	14	$\begin{pmatrix} 0 & 1 & -2 \end{pmatrix}$	15	$\begin{pmatrix} 2 & 0 & -1 \end{pmatrix}$	16	$\begin{pmatrix} 1 & 2 & 0 \end{pmatrix}$
17	$\begin{pmatrix} 0 & 1 & 2 \end{pmatrix}$	18	$\begin{pmatrix} 2 & 0 & 1 \end{pmatrix}$	19	$\begin{pmatrix} 1 & -2 & 0 \end{pmatrix}$	20	$\begin{pmatrix} -2 & 0 & -1 \end{pmatrix}$
21	$\begin{pmatrix} 0 & -1 & 2 \end{pmatrix}$	22	$\begin{pmatrix} -1 & 2 & 0 \end{pmatrix}$	23	$\begin{pmatrix} -2 & 0 & 1 \end{pmatrix}$	24	$\begin{pmatrix} 0 & -1 & -2 \end{pmatrix}$

Table 16: Virtual-cluster basis.

symbol	1	2	3	4	5	6	7	8	9	10
$\mathbb{Q}_0^{(A_1)}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$
	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$
	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$						
$\mathbb{Q}_{1,0}^{(T_2)}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	0	0	0	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$
	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$
	0	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0						
$\mathbb{Q}_{1,1}^{(T_2)}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	0	0
	0	0	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$	0
	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$						
$\mathbb{Q}_{1,2}^{(T_2)}$	0	0	0	0	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$
	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{20}$
	$\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$						
$\mathbb{Q}_{2,0}^{(E)}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$-\frac{\sqrt{39}}{78}$	$-\frac{\sqrt{39}}{78}$	$-\frac{\sqrt{39}}{78}$	$\frac{7\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$
	$\frac{7\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$-\frac{5\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$
	$\frac{7\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$\frac{7\sqrt{39}}{156}$						
$\mathbb{Q}_{2,1}^{(E)}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$

symbol	1	2	3	4	5	6	7	8	9	10
	$\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$-\frac{3\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{13}$	$-\frac{3\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{13}$	$-\frac{3\sqrt{13}}{52}$	$\frac{\sqrt{13}}{13}$
	$-\frac{\sqrt{13}}{52}$	$-\frac{3\sqrt{13}}{52}$	$\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{52}$						
$\mathbb{Q}_{2,0}^{(T_2)}$	0	0	0	0	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	0
	0	0	0	$-\frac{\sqrt{2}}{4}$	0	0	$\frac{\sqrt{2}}{4}$	0	0	0
	$-\frac{\sqrt{2}}{4}$	0	0	$\frac{\sqrt{2}}{4}$						
$\mathbb{Q}_{2,1}^{(T_2)}$	0	0	0	0	0	0	0	0	$\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$
	$-\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	0	$-\frac{\sqrt{2}}{4}$	0	0	$\frac{\sqrt{2}}{4}$	0	$\frac{\sqrt{2}}{4}$
	0	0	$-\frac{\sqrt{2}}{4}$	0						
$\mathbb{Q}_{2,2}^{(T_2)}$	$\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	0	0	0	0	0
	0	0	$\frac{\sqrt{2}}{4}$	0	0	$\frac{\sqrt{2}}{4}$	0	0	$-\frac{\sqrt{2}}{4}$	0
	0	$-\frac{\sqrt{2}}{4}$	0	0						
$\mathbb{Q}_{3,0}^{(T_1)}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	0	0	0	0	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$
	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$
	0	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0						
$\mathbb{Q}_{3,1}^{(T_1)}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	0	0
	0	0	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$	0
	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$						
$\mathbb{Q}_{3,2}^{(T_1)}$	0	0	0	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$
	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{10}$
	$-\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$						
$\mathbb{Q}_{3,0}^{(T_2)}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	0	0	0	0	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$
	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$	$-rac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$
	0	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0						
$\mathbb{Q}_{3,1}^{(T_2)}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	0	0
	0	0	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$	0
	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$						
$\mathbb{Q}_{3,2}^{(T_2)}$	0	0	0	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$
	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{10}$

Table 16

symbol	1	2	3	4	5	6	7	8	9	10
$\mathbb{Q}_{4,0}^{(E)}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$-\frac{\sqrt{13}}{13}$	$\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$
	$\frac{\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{13}$	$\frac{3\sqrt{13}}{52}$	$\frac{\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{13}$	$\frac{3\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{13}$
	$\frac{\sqrt{13}}{52}$	$\frac{3\sqrt{13}}{52}$	$-\frac{\sqrt{13}}{13}$	$\frac{\sqrt{13}}{52}$						
$\mathbb{Q}_{4,1}^{(E)}$	$\frac{5\sqrt{39}}{156}$	$\frac{5\sqrt{39}}{156}$	$\frac{5\sqrt{39}}{156}$	$\frac{5\sqrt{39}}{156}$	$\frac{\sqrt{39}}{78}$	$\frac{\sqrt{39}}{78}$	$\frac{\sqrt{39}}{78}$	$\frac{\sqrt{39}}{78}$	$-\frac{7\sqrt{39}}{156}$	$-\frac{7\sqrt{39}}{156}$
	$-\frac{7\sqrt{39}}{156}$	$-\frac{7\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$-\frac{5\sqrt{39}}{156}$	$\frac{7\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$
	$\frac{7\sqrt{39}}{156}$	$-\frac{5\sqrt{39}}{156}$	$-\frac{\sqrt{39}}{78}$	$\frac{7\sqrt{39}}{156}$						
$\mathbb{Q}_{4,0}^{(T_1)}$	0	0	0	0	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	0
	0	0	0	$\frac{\sqrt{2}}{4}$	0	0	$-\frac{\sqrt{2}}{4}$	0	0	0
	$\frac{\sqrt{2}}{4}$	0	0	$-\frac{\sqrt{2}}{4}$						
$\mathbb{Q}_{4,1}^{(T_1)}$	0	0	0	0	0	0	0	0	$\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$
	$-\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	0	$\frac{\sqrt{2}}{4}$	0	0	$-\frac{\sqrt{2}}{4}$	0	$-\frac{\sqrt{2}}{4}$
	0	0	$\frac{\sqrt{2}}{4}$	0						
$\mathbb{Q}_{4,2}^{(T_1)}$	$\frac{\sqrt{2}}{4}$	$\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	$-\frac{\sqrt{2}}{4}$	0	0	0	0	0	0
	0	0	$-\frac{\sqrt{2}}{4}$	0	0	$-\frac{\sqrt{2}}{4}$	0	0	$\frac{\sqrt{2}}{4}$	0
	0	$\frac{\sqrt{2}}{4}$	0	0						
$\mathbb{Q}_{5,0}^{(T_1)}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	0	0	0	0	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$
	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$
	0	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	0						
$\mathbb{Q}_{5,1}^{(T_1)}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{10}$	0	0
	0	0	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{10}$	0
	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{20}$						
$\mathbb{Q}_{5,2}^{(T_1)}$	0	0	0	0	$\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$
	$\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{10}$	0	$\frac{\sqrt{10}}{10}$	$\frac{\sqrt{10}}{20}$	0	$-\frac{\sqrt{10}}{10}$	$-\frac{\sqrt{10}}{20}$	0	$\frac{\sqrt{10}}{20}$
	$-\frac{\sqrt{10}}{10}$	0	$-\frac{\sqrt{10}}{20}$	$\frac{\sqrt{10}}{10}$						
$\mathbb{Q}_6^{(A_2)}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$
	$\frac{\sqrt{6}}{12}$	$\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$
	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$	$-\frac{\sqrt{6}}{12}$						