

# Biomedical Signal Processing

## Lecture 6

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# ECG 量測範例

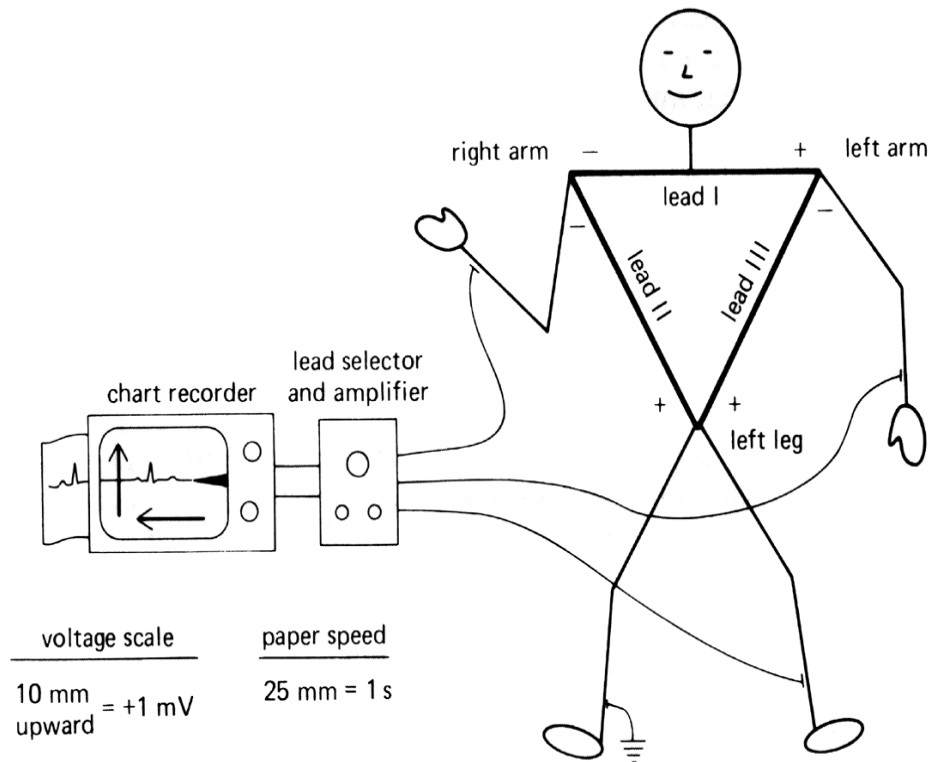


Figure 5-2 Einthoven's electrocardiographic conventions.



# ECG 量測範例

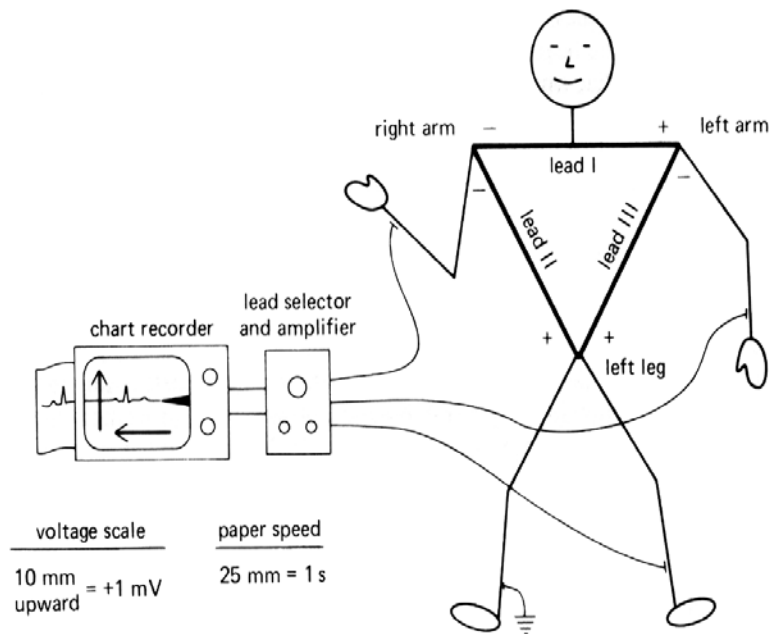
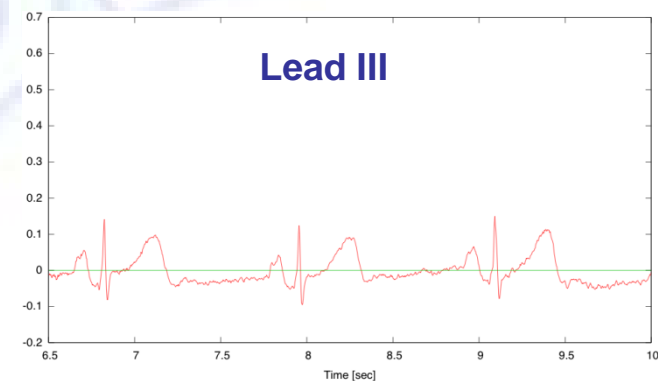
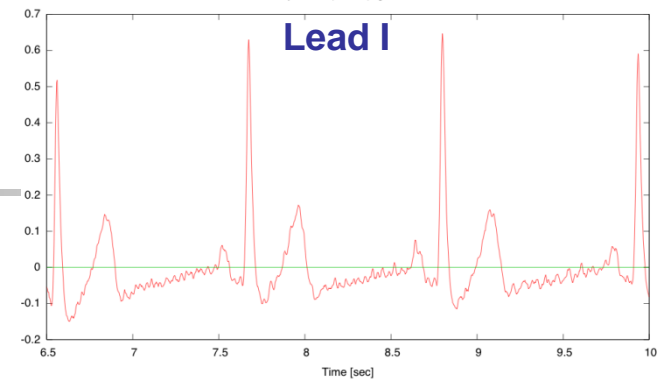
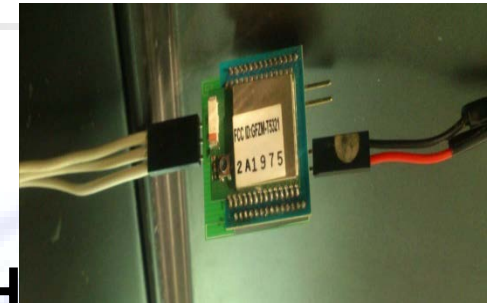


Figure 5-2 Einthoven's electrocardiographic conventions.

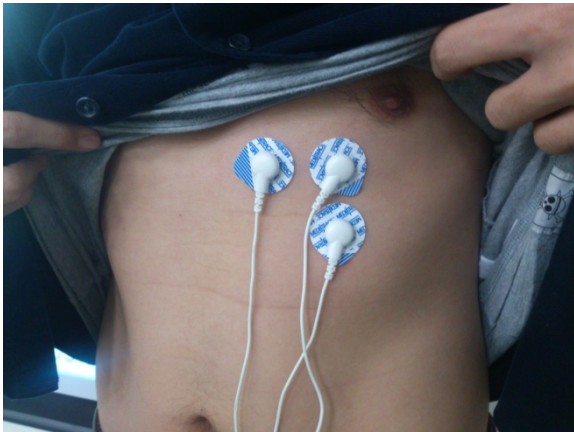


# The Recording System

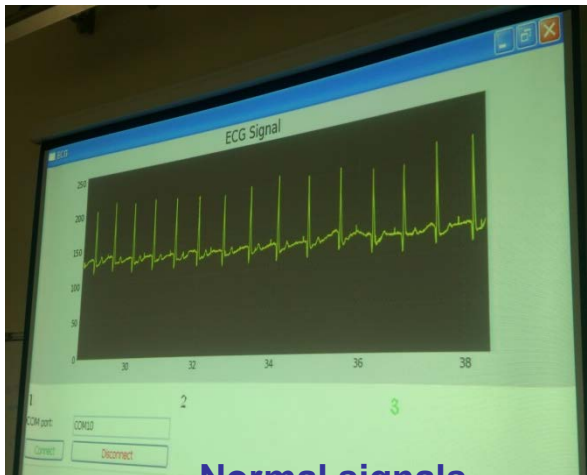
- **Amplifier & Analog Filter**
  - Gain: 1000 times
  - Cut-off frequency: 0.8 ~ 80 (Hz)
- **ADC:**
  - cc2530 ( 8051 base )
  - wireless transmission ( Zigbee )
- **GUI & DSP:**
  - Python implementation
  - Cross platform
  - Real-time system



# Artifacts



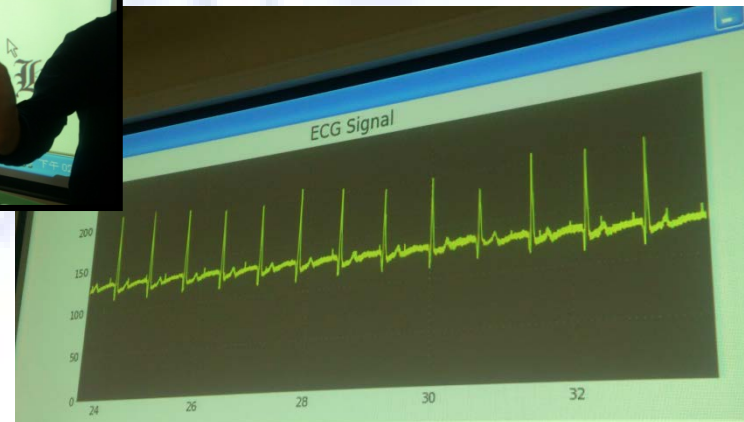
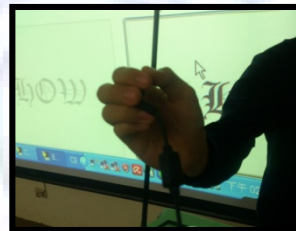
Electrode placement



Normal signals

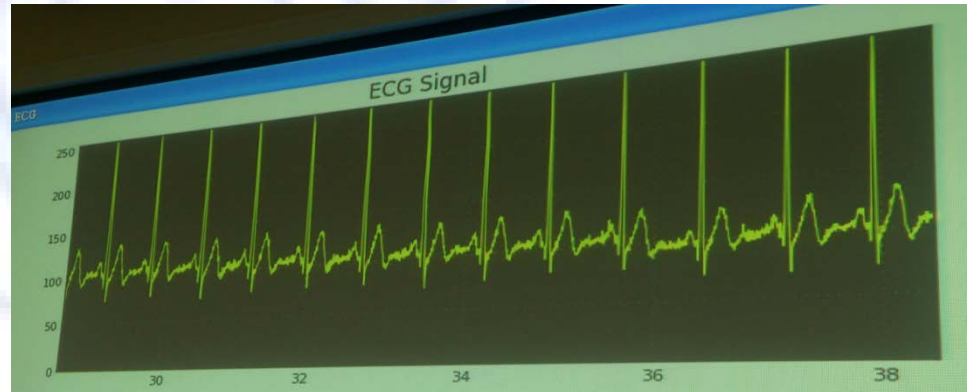


Movement artifacts



60Hz artifacts

# 電極擺放差異





# The Pan-Tompkins Algorithm for QRS Detection

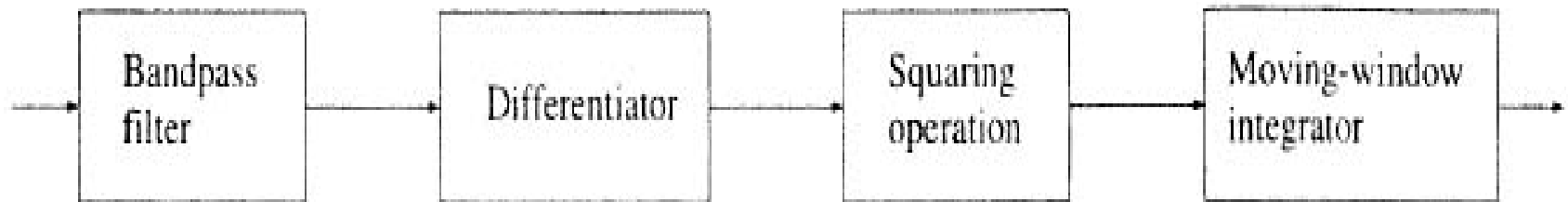
- An Algorithm to detect QRS complexes in an ongoing ECG signal.
- Ref
  - 4.3.2 of Biomedical Signal Analysis, Rangaraj M. Rangayyan, Wiley.
  - Pan, J. and Tompkins, W.J., “A real-time QRS detection algorithm,” IEEE Tans. On Biomedical Engineering, vol. 32, pp. 230-236, 1985.
  - Tompkins WJ, Biomedical Digital Signal Processing. Prentice-Hall, 1995.

# The Pan-Tompkins Algorithm for QRS Detection

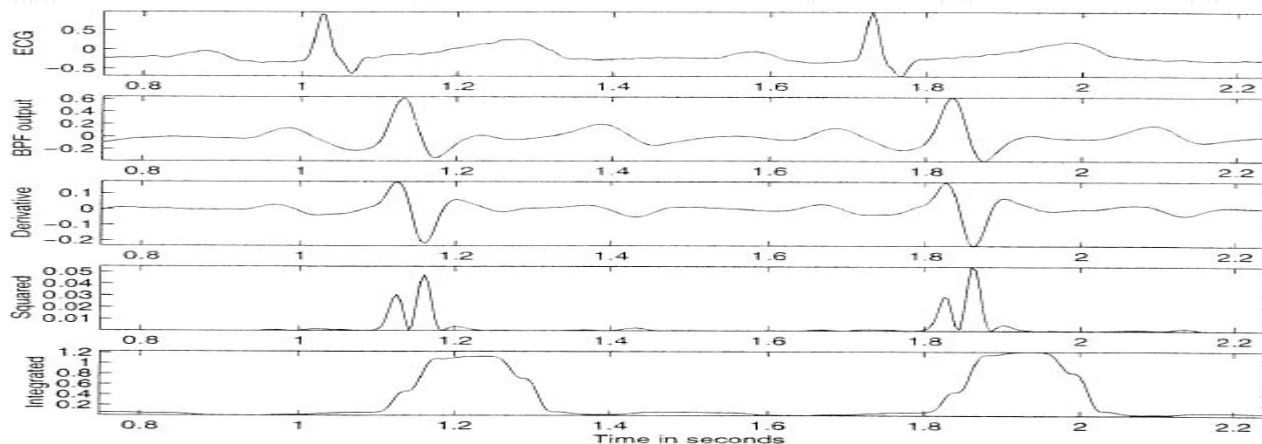
- Pan-Tomplins algorithm is based on analysis of the slope, amplitude, and width of QRS complexes.
- It includes a series of
  - bandpass (lowpass+high pass)
  - derivative,
  - squaring,
  - integration,
  - adaptive thresholding & search procedures.



# The Pan-Tompkins Algorithm for QRS Detection



**Figure 4.4** Block diagram of the Pan-Tompkins algorithm for QRS detection.



**Figure 4.6** Results of the Pan-Tompkins algorithm. From top to bottom: two cycles of a filtered version of the ECG signal shown in Figure 3.5 (the same as that in Figure 4.2); output of the bandpass filter (BPF, a combination of lowpass and highpass filters); output of the derivative-based operator; the result of squaring; and  $100 \times$  the result of the final integrator.

## Lowpass Filter

- **Integer coefficients** were used to reduce computational complexity.

$$H(z) = \frac{1}{32} \frac{(1 - z^{-6})^2}{(1 - z^{-1})^2}.$$

- The output  $y(n)$  related to the input  $x(n)$  is

$$y(n) = 2y(n-1) - y(n-2) + \frac{1}{32} [x(n) - 2x(n-6) + x(n-12)].$$

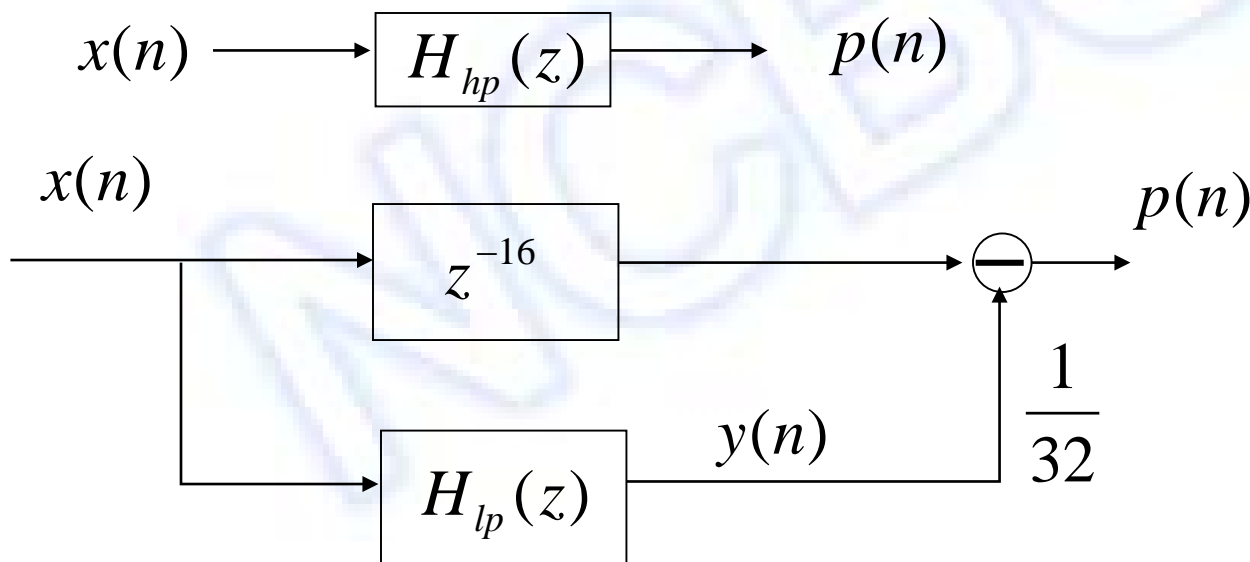
# Lowpass Filter

- It introduces a **delay** of 5 samples or **25 ms** with the sampling rate being 200 Hz.
- The cutoff frequency is **11 Hz** and it provides an attenuation greater than **35 dB at 60 Hz**.
- It effectively suppresses **power-line** interference, if present.

# Highpass Filter

- The highpass is implemented as an allpass filter minus a lowpass filter.

$$H_{hp}(z) = z^{-16} - \frac{1}{32} H_{lp}(z)$$



# Highpass Filter

- The lowpass  $H_{lp}(z)$  is

$$H_{lp}(z) = \frac{(1 - z^{-32})}{(1 - z^{-1})};$$

- The input-output relationship of  $H_{lp}(z)$  is

$$y(n) = y(n - 1) + x(n) - x(n - 32).$$

# Highpass Filter

$$\frac{P(z)}{X(z)} = H_{hp}(z) = z^{-16} - \frac{1}{32} H_{lp}(z) = z^{-16} - \frac{1}{32} \frac{Y(z)}{X(z)}$$

$$P(z) = X(z)z^{-16} - \frac{1}{32} Y(z)$$

- The output  $p(n)$  of the highpass is

$$p(n) = x(n - 16) - \frac{1}{32} [y(n - 1) + x(n) - x(n - 32)],$$

- The highpass filter has a **cutoff** frequency of **5 Hz** and introduces a **delay** of **80 ms**.

# Derivative Operator

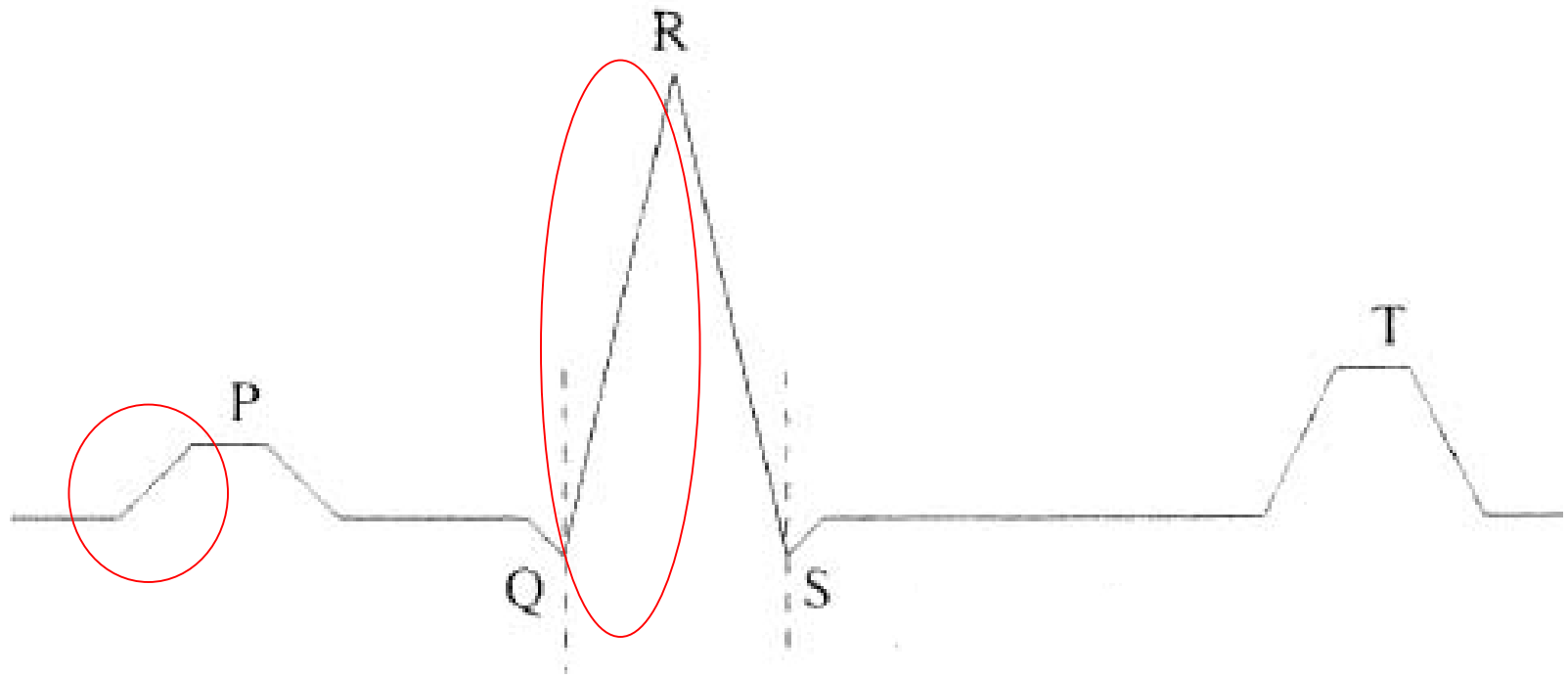
- The derivative operation is

$$y(n) = \frac{1}{8} [2x(n) + x(n-1) - x(n-3) - 2x(n-4)],$$

- It approximates the ideal  $d/dt$  up to 30Hz.
- The derivative procedure **suppresses** the low-frequency components of P and T.
- It provides a **large gain** to the high-frequency components arising from the high slopes of the **QRS**.



# Derivative Operator



# Squaring

- The squaring operation

$$y(n) = x^2(n)$$

will

- make the result positive
- **emphasize large differences** from QRS complexes
- **suppress small difference** arising from P and T.
- The high-frequency components related to the QRS are further enhanced.

# Integration

- A **derivative** based operation will exhibit **multiple peaks** in the duration of a single QRS complex.
- A moving-window **integration** is performed to **smooth** the output of the preceding operations in Pan-Tompkins algorithm.

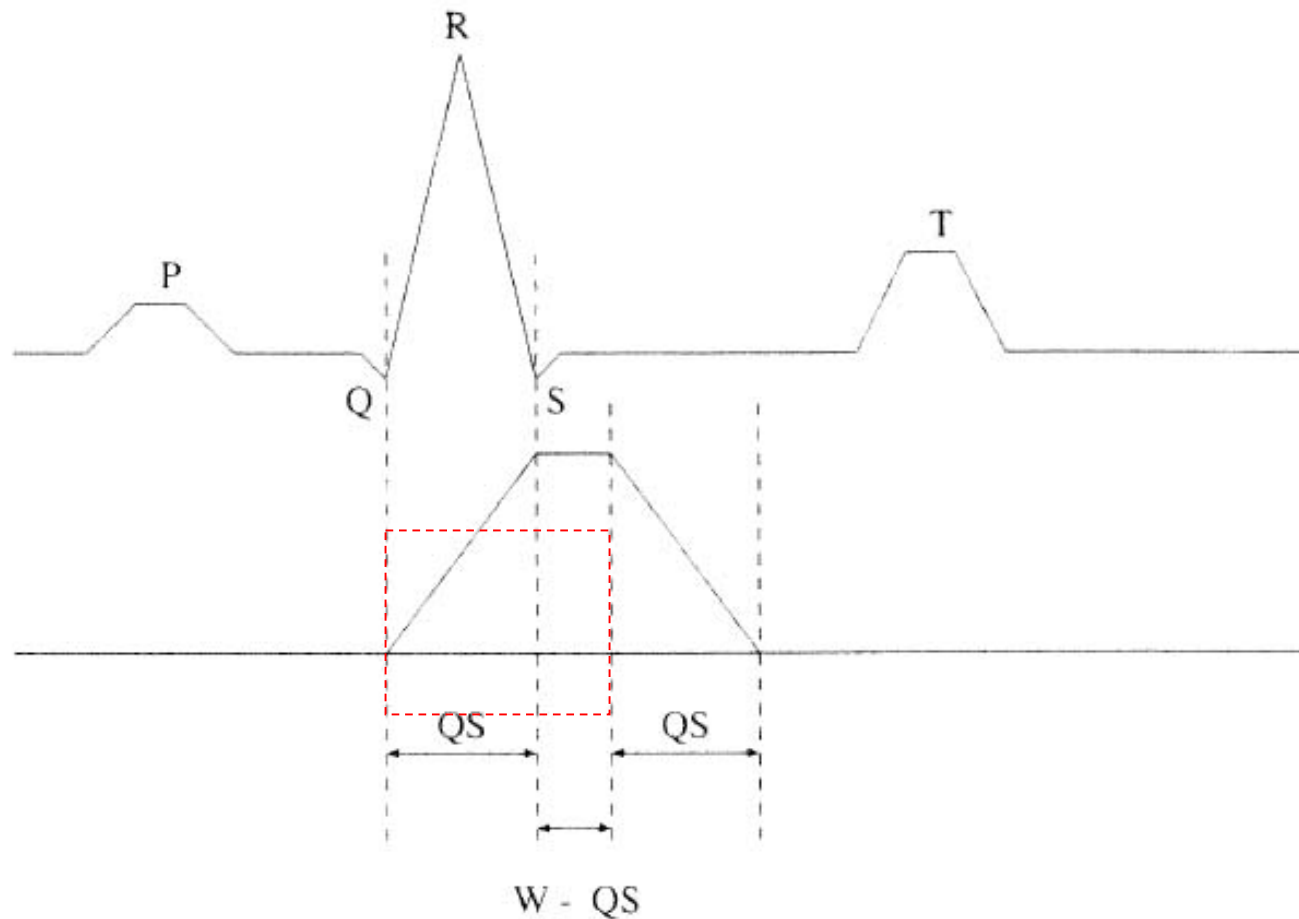
# Integration

- The moving-window integration filter

$$y(n) = \frac{1}{N} [x(n - (N - 1)) + x(n - (N - 2)) + \cdots + x(n)].$$

is used to smooth multiple peaks in a single QRS complex.

- large window will result large values since QRS and T are merged.
- small window will yield several peaks for a single QRS.
- **N=30** is suitable for **fs=200 Hz**.



**Figure 4.5** The relationship of a QRS complex to the moving-window integrator output. Upper plot: Schematic ECG signal. Lower plot: Output of the moving-window integrator. QS: QRS complex width. W: width of the integrator window, given as  $N/f_s$  s. Adapted from Tompkins [27].

# Adaptive Thresholding

- If a peak **exceeds a threshold** called THRESHOLD I1, it is classified as a QRS peak.
- THRESHOLD I1 should be updated according the **QRS peaks** and **noise peaks**.
- How to do it?

# Adaptive Thresholding

- Definition
  - $PEAKI$ : the detected new peak
  - $SPKI$ : peak level of QRS peaks.
  - $NPKI$ : peak level of non-QRS peaks.

$$SPKI = 0.125 PEAKI + 0.875 SPKI \quad \text{if } PEAKI \text{ is a signal peak; (4.15)}$$

$$NPKI = 0.125 PEAKI + 0.875 NPKI \quad \text{if } PEAKI \text{ is a noise peak;}$$

$$THRESHOLD I1 = NPKI + 0.25(SPKI - NPKI); \quad (4.16)$$

$$THRESHOLD I2 = 0.5 THRESHOLD I1.$$



## Searchback Procedure

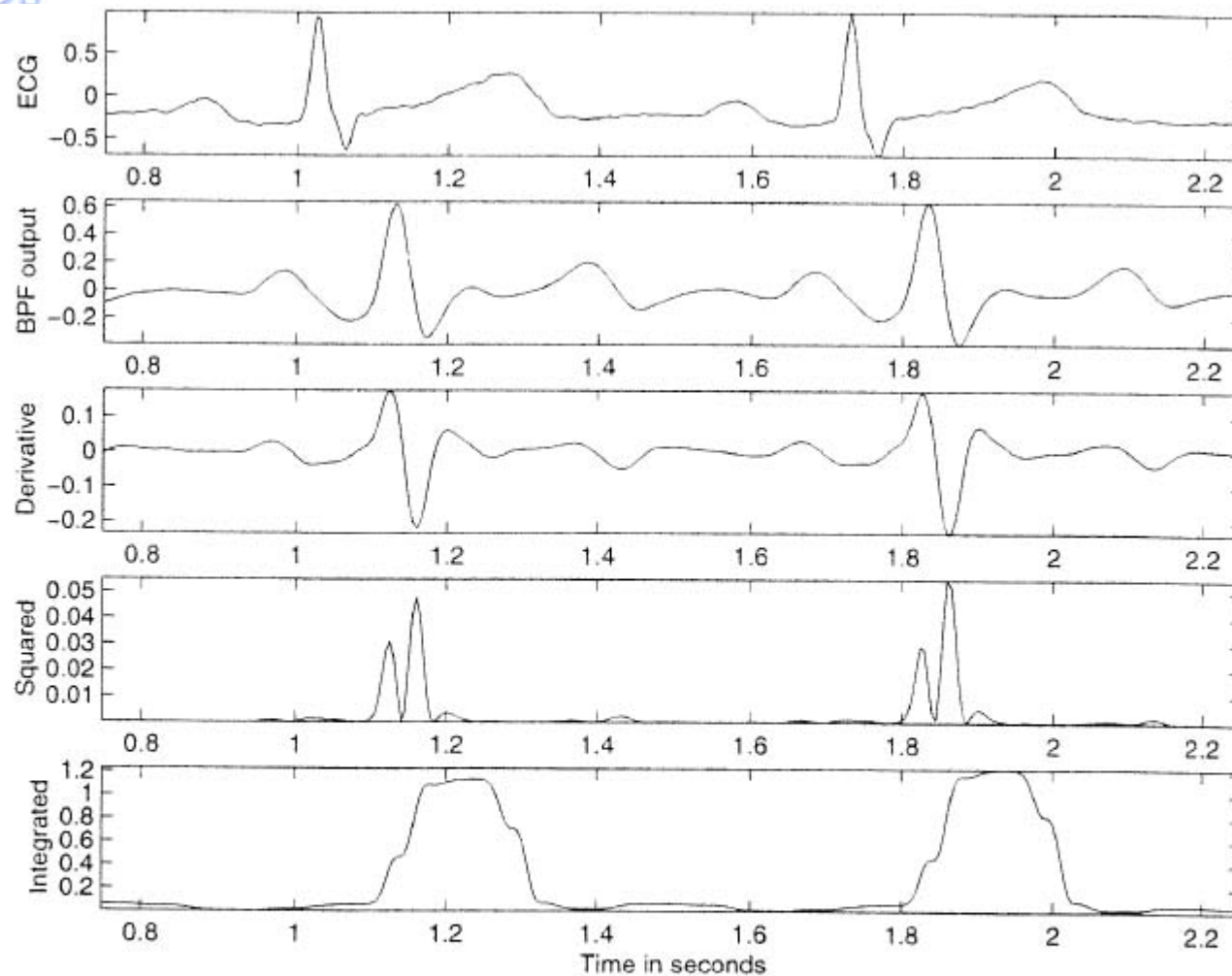
- Some QRS may be missed by the hard-thresholding forward searching.
- Ex. THRESHOLD I1 = 0.5, a peak is 0.48, it is a noise peak or a QRS?
- A searchback procedure is used to reconfirm the peaks.
- The averaged **RR-duration** is used to detect if it misses a QRS for a long period (ex. 1.66 RR-duration)

## Searchback Procedure

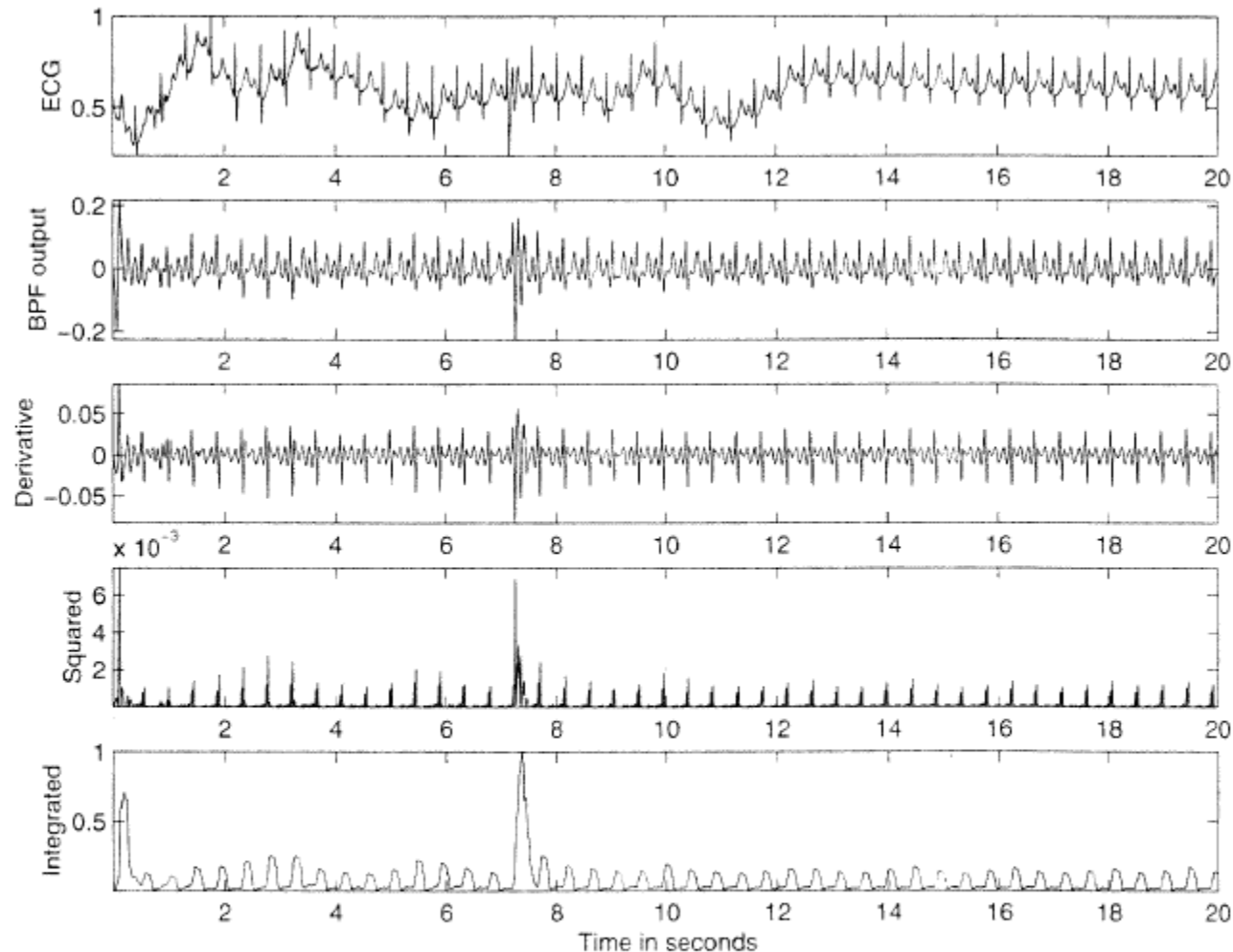
- If there is no QRS is detected for a predefined period, (ex. 1.66 averaged RR-duration), we may miss a QRS.
- Searchback to detect the peak by a **lower threshold** called THRESHOLD I2 that is 0.5 THRESHOLD I1.
- This concept has also been used for **sleep scoring**.

# Searchback Procedure

**Searchback procedure:** The Pan-Tompkins algorithm maintains two *RR*-interval averages: *RR AVERAGE1* is the average of the eight most-recent beats, and *RR AVERAGE2* is the average of the eight most-recent beats having *RR* intervals within the range specified by *RR LOW LIMIT*  $= 0.92 \times RR AVERAGE2$  and *RR HIGH LIMIT*  $= 1.16 \times RR AVERAGE2$ . Whenever a QRS is not detected for a certain interval specified as *RR MISSED LIMIT*  $= 1.66 \times RR AVERAGE2$ , the QRS is taken to be the peak between the established thresholds applied in the searchback procedure.



**Figure 4.6** Results of the Pan-Tompkins algorithm. From top to bottom: two cycles of a filtered version of the ECG signal shown in Figure 3.5 (the same as that in Figure 4.2); output of the bandpass filter (BPF, a combination of lowpass and highpass filters); output of the derivative-based operator; the result of squaring; and  $100 \times$  the result of the final integrator.



**Figure 4.26** Results of the Pan-Tompkins algorithm with a noisy ECG signal. From top to bottom: ECG signal sampled at 200  $Hz$ ; output of the bandpass filter (BPF); output of the derivative-based operator; the result of squaring; and normalized result of the final integrator.