Reference Manual

Generated by Doxygen 1.8.11

Contents

1	Mod	lular art	oitrary-ord	der ocean-atmosphere model: MAOOAM Fortran implementation	1
2	Mod	lular art	oitrary-ord	der ocean-atmosphere model: The Tangent Linear and Adjoint model	5
3	Mod	lules Inc	dex		7
	3.1	Modul	es List		7
4	Data	a Type I	ndex		9
	4.1	Data T	ypes List		9
5	File	Index			11
	5.1	File Lis	st		11
6	Mod	lule Doc	cumentati	on Control of the Con	13
	6.1	aotens	sor_def Mo	odule Reference	13
		6.1.1	Detailed	Description	14
		6.1.2	Function	n/Subroutine Documentation	14
			6.1.2.1	a(i)	14
			6.1.2.2	add_count(i, j, k, v)	14
			6.1.2.3	$coeff(i,j,k,v) \ldots \ldots$	14
			6.1.2.4	compute_aotensor(func)	15
			6.1.2.5	init_aotensor	15
			6.1.2.6	kdelta(i, j)	16
			6.1.2.7	psi(i)	16
			6.1.2.8	t(i)	16
			6.1.2.9	theta(i)	16

iv CONTENTS

	6.1.3	Variable	Documentation	. 17
		6.1.3.1	aotensor	. 17
		6.1.3.2	count_elems	. 17
		6.1.3.3	real_eps	. 17
6.2	ic_def	Module Re	eference	. 17
	6.2.1	Detailed	Description	. 18
	6.2.2	Function	/Subroutine Documentation	. 18
		6.2.2.1	load_ic	. 18
	6.2.3	Variable	Documentation	. 19
		6.2.3.1	exists	. 19
		6.2.3.2	ic	. 19
6.3	icdelta	_def Modu	ule Reference	. 20
	6.3.1	Detailed	Description	. 20
	6.3.2	Function	/Subroutine Documentation	. 20
		6.3.2.1	load_icdelta	. 20
	6.3.3	Variable	Documentation	. 21
		6.3.3.1	exists	. 21
		6.3.3.2	icdelta	. 22
6.4	inprod_	_analytic N	Module Reference	. 22
	6.4.1	Detailed	Description	. 23
	6.4.2	Function	/Subroutine Documentation	. 24
		6.4.2.1	b1(Pi, Pj, Pk)	. 24
		6.4.2.2	b2(Pi, Pj, Pk)	. 24
		6.4.2.3	calculate_a(i, j)	. 24
		6.4.2.4	$calculate_b(i,j,k) \dots \dots \dots \dots \dots \dots \dots \dots \dots $. 24
		6.4.2.5	calculate_c_atm(i, j)	. 25
		6.4.2.6	$calculate_c_oc(i,j,k) \ldots \ldots \ldots \ldots \ldots \ldots$. 25
		6.4.2.7	$calculate_d(i,j) \ . \ . \ . \ . \ . \ . \ . \ . \ . \ $. 25
		6.4.2.8	$calculate_g(i,j,k) \dots \dots \dots \dots \dots \dots \dots \dots \dots$. 26
		6.4.2.9	$calculate_k(i,j) \ . \ . \ . \ . \ . \ . \ . \ . \ . \ $. 27

CONTENTS

		6.4.2.10	calculate_m(i, j)	27
		6.4.2.11	calculate_n(i, j)	27
		6.4.2.12	calculate_o(i, j, k)	28
		6.4.2.13	calculate_s(i, j)	28
		6.4.2.14	$calculate_w(i,j) \dots $	29
		6.4.2.15	delta(r)	29
		6.4.2.16	flambda(r)	29
		6.4.2.17	init_inprod	29
		6.4.2.18	s1(Pj, Pk, Mj, Hk)	31
		6.4.2.19	s2(Pj, Pk, Mj, Hk)	31
		6.4.2.20	s3(Pj, Pk, Hj, Hk)	31
		6.4.2.21	s4(Pj, Pk, Hj, Hk)	31
	6.4.3	Variable	Documentation	31
		6.4.3.1	atmos	31
		6.4.3.2	awavenum	32
		6.4.3.3	ocean	32
		6.4.3.4	owavenum	32
6.5	integra	itor Module	e Reference	32
	6.5.1	Detailed	Description	33
	6.5.2	Function	/Subroutine Documentation	33
		6.5.2.1	init_integrator	33
		6.5.2.2	step(y, t, dt, res)	33
		6.5.2.3	tendencies(t, y, res)	34
	6.5.3	Variable	Documentation	34
		6.5.3.1	buf_f0	34
		6.5.3.2	buf_f1	34
		6.5.3.3	buf_ka	35
		6.5.3.4	buf_kb	35
		6.5.3.5	buf_y1	35
6.6	lyap_s	tat Module	Reference	35

vi

	6.6.1	Detailed	Description	36
	6.6.2	Function	/Subroutine Documentation	36
		6.6.2.1	lyap_acc(x)	36
		6.6.2.2	lyap_init_stat	36
		6.6.2.3	lyap_iter()	37
		6.6.2.4	lyap_mean()	37
		6.6.2.5	lyap_reset	37
		6.6.2.6	lyap_var()	37
	6.6.3	Variable	Documentation	37
		6.6.3.1	i	37
		6.6.3.2	m	38
		6.6.3.3	mprev	38
		6.6.3.4	mtmp	38
		6.6.3.5	v	38
6.7	lyap_ve	ectors Mod	dule Reference	38
	6.7.1	Detailed	Description	39
	6.7.2	Function	Subroutine Documentation	39
		6.7.2.1	benettin_step	39
		6.7.2.2	get_lyap_state(prop_ret, ensemble_ret)	40
		6.7.2.3	init_lyap	40
		6.7.2.4	multiply_prop(prop_mul)	40
	6.7.3	Variable	Documentation	41
		6.7.3.1	ensemble	41
		6.7.3.2	loclyap	41
		6.7.3.3	lwork	41
		6.7.3.4	lyapunov	41
		6.7.3.5	prop	42
		6.7.3.6	prop_buf	42
		6.7.3.7	tau	42
		6.7.3.8	work	42

CONTENTS vii

		6.7.3.9	work2	42
6.8	params	s Module F	Reference	42
	6.8.1	Detailed	Description	45
	6.8.2	Function	/Subroutine Documentation	45
		6.8.2.1	init_nml	45
		6.8.2.2	init_params	46
	6.8.3	Variable	Documentation	47
		6.8.3.1	ams	47
		6.8.3.2	betp	47
		6.8.3.3	ca	47
		6.8.3.4	co	48
		6.8.3.5	cpa	48
		6.8.3.6	сро	48
		6.8.3.7	d	48
		6.8.3.8	dp	48
		6.8.3.9	dt	49
		6.8.3.10	epsa	49
		6.8.3.11	f0	49
		6.8.3.12	g	49
		6.8.3.13	ga	49
		6.8.3.14	go	50
		6.8.3.15	gp	50
		6.8.3.16	h	50
		6.8.3.17	k	50
		6.8.3.18	kd	50
		6.8.3.19	kdp	51
		6.8.3.20	kp	51
		6.8.3.21	1	51
		6.8.3.22	lambda	51
		6.8.3.23	lpa	51

viii CONTENTS

6.8.3.24	lpo	52
6.8.3.25	Ir	52
6.8.3.26	Isbpa	52
6.8.3.27	Isbpo	52
6.8.3.28	$n \ldots \ldots \ldots \ldots \ldots$	52
6.8.3.29	natm	53
6.8.3.30	nbatm	53
6.8.3.31	nboc	53
6.8.3.32	ndim	53
6.8.3.33	noc	53
6.8.3.34	nua	54
6.8.3.35	nuap	54
6.8.3.36	nuo	54
6.8.3.37	nuop	54
6.8.3.38	oms	54
6.8.3.39	phi0	55
6.8.3.40	phi0_npi	55
6.8.3.41	pi	55
6.8.3.42	$r \ldots \ldots \ldots \ldots \ldots$	55
6.8.3.43	rescaling_time	55
6.8.3.44	rp	56
6.8.3.45	rr	56
6.8.3.46	rra	56
6.8.3.47	sb	56
6.8.3.48	sbpa	56
6.8.3.49	sbpo	57
6.8.3.50	sc	57
6.8.3.51	scale	57
6.8.3.52	sig0	57
6.8.3.53	t_run	57

CONTENTS

		6.8.3.54	t_trans	. 58
		6.8.3.55	ta0	. 58
		6.8.3.56	to0	. 58
		6.8.3.57	tw	. 58
		6.8.3.58	writeout	. 58
6.9	stat Mo	dule Refe	rence	. 58
	6.9.1	Detailed	Description	. 59
	6.9.2	Function/	/Subroutine Documentation	. 59
		6.9.2.1	acc(x)	. 59
		6.9.2.2	init_stat	. 60
		6.9.2.3	iter()	. 60
		6.9.2.4	mean()	. 60
		6.9.2.5	reset	. 60
		6.9.2.6	var()	. 60
	6.9.3	Variable I	Documentation	. 61
		6.9.3.1	i	. 61
		6.9.3.2	m	. 61
		6.9.3.3	mprev	. 61
		6.9.3.4	mtmp	. 61
		6.9.3.5	v	. 61
6.10	tensor	Module Re	eference	. 61
	6.10.1	Detailed	Description	. 63
	6.10.2	Function/	/Subroutine Documentation	. 63
		6.10.2.1	add_check(t, i, j, k, v, dst)	. 63
		6.10.2.2	$add_elem(t,i,j,k,v) \ \ldots \ldots$. 63
		6.10.2.3	add_to_tensor(src, dst)	. 64
		6.10.2.4	copy_coo(src, dst)	. 65
		6.10.2.5	jsparse_mul(coolist_ijk, arr_j, jcoo_ij)	. 65
		6.10.2.6	jsparse_mul_mat(coolist_ijk, arr_j, jcoo_ij)	. 66
		6.10.2.7	load_tensor_from_file(s, t)	. 67

CONTENTS

		6.10.2.8 mat	_to_coo(src, dst)	67
		6.10.2.9 print	t_tensor(t, s)	68
		6.10.2.10 simp	olify(tensor)	69
		6.10.2.11 spar	rse_mul2(coolist_ij, arr_j, res)	70
		6.10.2.12 spar	rse_mul3(coolist_ijk, arr_j, arr_k, res)	70
		6.10.2.13 write	e_tensor_to_file(s, t)	71
	6.10.3	Variable Docu	mentation	71
		6.10.3.1 real	_eps	71
6.11	tl_ad_ir	ntegrator Modul	e Reference	71
	6.11.1	Detailed Descri	ription	73
	6.11.2	Function/Subro	outine Documentation	73
		6.11.2.1 ad_s	step(y, ystar, t, dt, res)	73
		6.11.2.2 evol	ve_ad_step(y, deltay, t, dt, ynew, deltaynew)	74
		6.11.2.3 evol	ve_tl_step(y, deltay, t, dt, ynew, deltaynew)	75
		6.11.2.4 init_	tl_ad_integrator	75
		6.11.2.5 prop	o_step(y, propagator, t, dt, ynew, adjoint)	76
		6.11.2.6 tend	lencies(t, y, res)	76
		6.11.2.7 tl_st	ep(y, ystar, t, dt, res)	77
	6.11.3	Variable Docu	mentation	77
		6.11.3.1 buf_	f0	77
		6.11.3.2 buf_	f00	78
		6.11.3.3 buf_	f1	78
		6.11.3.4 buf_	f11	78
		6.11.3.5 buf_	j1	78
		6.11.3.6 buf_	j1h	78
		6.11.3.7 buf_	j2	79
		6.11.3.8 buf_	j2h	79
		6.11.3.9 buf_	j3	79
		6.11.3.10 buf_	j3h	79
		6.11.3.11 buf_	j4	79

CONTENTS xi

	6.11.3.12	2 buf_j4h	. 80
	6.11.3.13	3 buf_ka	. 80
	6.11.3.14	4 buf_kaa	. 80
	6.11.3.15	5 buf_kb	. 80
	6.11.3.16	6 buf_kbb	. 80
	6.11.3.17	7 buf_kc	. 81
	6.11.3.18	8 buf_kd	. 81
	6.11.3.19	9 buf_y1	. 81
	6.11.3.20	0 buf_y11	. 81
	6.11.3.21	1 one	. 81
6.12 tl_ad_	tensor Mod	dule Reference	. 82
6.12.1	Detailed	Description	. 83
6.12.2	Function	/Subroutine Documentation	. 83
	6.12.2.1	ad(t, ystar, deltay, buf)	. 83
	6.12.2.2	$ad_add_count(i,j,k,v) \dots \dots$. 83
	6.12.2.3	ad_add_count_ref(i, j, k, v)	. 84
	6.12.2.4	$ad_coeff(i,j,k,v) \ldots \ldots \ldots \ldots \ldots \ldots \ldots$. 84
	6.12.2.5	$ad_coeff_ref(i,j,k,v) \ldots \ldots \ldots \ldots \ldots \ldots$. 85
	6.12.2.6	compute_adtensor(func)	. 85
	6.12.2.7	compute_adtensor_ref(func)	. 85
	6.12.2.8	compute_tltensor(func)	. 86
	6.12.2.9	init_adtensor	. 86
	6.12.2.10	0 init_adtensor_ref	. 86
	6.12.2.11	1 init_tltensor	. 87
	6.12.2.12	2 jacobian(ystar)	. 87
	6.12.2.13	3 jacobian_mat(ystar)	. 87
	6.12.2.14	4 tl(t, ystar, deltay, buf)	. 88
	6.12.2.15	5 tl_add_count(i, j, k, v)	. 88
	6.12.2.16	6 tl_coeff(i, j, k, v)	. 89
6.12.3	Variable	Documentation	. 89
	6.12.3.1	adtensor	. 89
	6.12.3.2	count_elems	. 89
	6.12.3.3	real_eps	. 90
	6.12.3.4	tltensor	. 90
6.13 util Mo	dule Refer	rence	. 90
6.13.1	Detailed	Description	. 90
6.13.2	Function	/Subroutine Documentation	. 91
	6.13.2.1	init_one(A)	. 91
	6.13.2.2	init_random_seed()	. 91
	6.13.2.3	isin(c, s)	. 91
	6.13.2.4	piksrt(k, arr, par)	. 91
	6.13.2.5	rstr(x, fm)	. 92
	6.13.2.6	str(k)	. 92

xii CONTENTS

7	Data	Type D	Pocumentation	93
	7.1	inprod_	_analytic::atm_tensors Type Reference	93
		7.1.1	Detailed Description	93
		7.1.2	Member Data Documentation	93
			7.1.2.1 a	93
			7.1.2.2 b	93
			7.1.2.3 c	94
			7.1.2.4 d	94
			7.1.2.5 g	94
			7.1.2.6 s	94
	7.2	inprod	_analytic::atm_wavenum Type Reference	94
		7.2.1	Detailed Description	95
		7.2.2	Member Data Documentation	95
			7.2.2.1 h	95
			7.2.2.2 m	95
			7.2.2.3 nx	95
			7.2.2.4 ny	95
			7.2.2.5 p	95
			7.2.2.6 typ	95
	7.3	tensor	::coolist Type Reference	96
		7.3.1	Detailed Description	96
		7.3.2	Member Data Documentation	96
			7.3.2.1 elems	96
			7.3.2.2 nelems	96
	7.4	tensor	::coolist_elem Type Reference	96
		7.4.1	Detailed Description	97
		7.4.2	Member Data Documentation	97
			7.4.2.1 j	97
			7.4.2.2 k	97
			7.4.2.3 v	97

CONTENTS xiii

	7.5	inprod	_analytic::ocean_tensors Type Reference	98
		7.5.1	Detailed Description	98
		7.5.2	Member Data Documentation	98
			7.5.2.1 c	98
			7.5.2.2 k	98
			7.5.2.3 m	98
			7.5.2.4 n	98
			7.5.2.5 0	99
			7.5.2.6 w	99
	7.6	inprod	_analytic::ocean_wavenum Type Reference	99
		7.6.1	Detailed Description	99
		7.6.2	Member Data Documentation	99
			7.6.2.1 h	99
			7.6.2.2 nx	99
			7.6.2.3 ny	100
			7.6.2.4 p	100
8	File	Docum		
8			entation	101
8	8.1	aotens	entation cor_def.f90 File Reference	101 101
8	8.1 8.2	aotens doc/ge	entation cor_def.f90 File Reference	101 101 102
8	8.1 8.2 8.3	aotens doc/ge doc/tl_	entation sor_def.f90 File Reference en_doc.md File Reference ad_doc.md File Reference	101 101 102 102
8	8.1 8.2 8.3 8.4	aotens doc/ge doc/tl_ ic_def.	entation for_def.f90 File Reference en_doc.md File Reference ad_doc.md File Reference f90 File Reference	101 101 102 102
8	8.1 8.2 8.3 8.4 8.5	aotens doc/ge doc/tl_ ic_def. icdelta	entation for_def.f90 File Reference en_doc.md File Reference ad_doc.md File Reference f90 File Reference _def.f90 File Reference	101 101 102 102 102
8	8.1 8.2 8.3 8.4 8.5 8.6	aotens doc/ge doc/tl_ ic_def. icdelta	entation for_def.f90 File Reference en_doc.md File Reference ad_doc.md File Reference f90 File Reference _def.f90 File Reference _analytic.f90 File Reference	101 101 102 102 102 103
8	8.1 8.2 8.3 8.4 8.5	aotens doc/ge doc/tl_ ic_def. icdelta inprod_	entation cor_def.f90 File Reference cn_doc.md File Reference ad_doc.md File Reference f90 File Reference _def.f90 File Reference _analytic.f90 File Reference SE.txt File Reference	101 101 102 102 102 103 104
8	8.1 8.2 8.3 8.4 8.5 8.6	aotens doc/ge doc/tl_ ic_def. icdelta	entation sor_def.f90 File Reference en_doc.md File Reference ad_doc.md File Reference f90 File Reference _def.f90 File Reference _analytic.f90 File Reference SE.txt File Reference Function Documentation	101 101 102 102 102 103 104
8	8.1 8.2 8.3 8.4 8.5 8.6	aotens doc/ge doc/tl_ ic_def. icdelta inprod_	entation for_def.f90 File Reference ad_doc.md File Reference ad_doc.md File Reference f90 File Reference _def.f90 File Reference _analytic.f90 File Reference SE.txt File Reference Function Documentation 8.7.1.1 files(the""Software"")	101 101 102 102 102 103 104 106
8	8.1 8.2 8.3 8.4 8.5 8.6	aotens doc/ge doc/tl_ ic_def. icdelta inprod_ LICEN 8.7.1	entation for_def.f90 File Reference fin_doc.md File Reference ad_doc.md File Reference f90 File Reference _def.f90 File Reference _analytic.f90 File Reference SE.txt File Reference Function Documentation 8.7.1.1 files(the""Software"") 8.7.1.2 License(MIT) Copyright(c) 2015-2016 Lesley De Cruz	101 101 102 102 102 103 104 106 106
8	8.1 8.2 8.3 8.4 8.5 8.6	aotens doc/ge doc/tl_ ic_def. icdelta inprod_	entation for_def.f90 File Reference en_doc.md File Reference ad_doc.md File Reference f90 File Reference _def.f90 File Reference _analytic.f90 File Reference SE.txt File Reference Function Documentation 8.7.1.1 files(the""Software"") 8.7.1.2 License(MIT) Copyright(c) 2015-2016 Lesley De Cruz Variable Documentation	101 101 102 102 102 103 104 106 106
8	8.1 8.2 8.3 8.4 8.5 8.6	aotens doc/ge doc/tl_ ic_def. icdelta inprod_ LICEN 8.7.1	entation for_def.f90 File Reference fin_doc.md File Reference ad_doc.md File Reference f90 File Reference _def.f90 File Reference _analytic.f90 File Reference SE.txt File Reference Function Documentation 8.7.1.1 files(the""Software"") 8.7.1.2 License(MIT) Copyright(c) 2015-2016 Lesley De Cruz Variable Documentation 8.7.2.1 charge	101 101 102 102 102 103 104 106 106

xiv CONTENTS

		8.7.2.3	conditions	 	107
		8.7.2.4	CONTRACT	 	107
		8.7.2.5	copy	 	107
		8.7.2.6	distribute	 	107
		8.7.2.7	FROM	 	107
		8.7.2.8	granted	 	107
		8.7.2.9	IMPLIED	 	107
		8.7.2.10	KIND	 	108
		8.7.2.11	LIABILITY	 	108
		8.7.2.12	MERCHANTABILITY	 	108
		8.7.2.13	merge	 	108
		8.7.2.14	modify	 	108
		8.7.2.15	OTHERWISE	 	108
		8.7.2.16	publish	 	109
		8.7.2.17	restriction	 	109
		8.7.2.18	so	 	109
		8.7.2.19	Software	 	109
		8.7.2.20	sublicense	 	109
		8.7.2.21	use	 	109
8.8	lyap_st	tat.f90 File	e Reference	 	109
8.9	lyap_ve	ectors.f90	File Reference	 	110
8.10) maooa	m.f90 File	e Reference	 	111
	8.10.1	Function/	n/Subroutine Documentation	 	111
		8.10.1.1	maooam	 	111
8.1	1 maooa	m_lyap.f90	90 File Reference	 	111
	8.11.1	Function/	n/Subroutine Documentation	 	112
		8.11.1.1	maooam_lyap	 	112
8.12	2 maooa	.m_lyap_di	div.f90 File Reference	 	112
	8.12.1	Function/	n/Subroutine Documentation	 	112
		8.12.1.1	maooam_lyap_div	 	112

CONTENTS xv

8.13	params	s.f90 File F	Reference .			 	 	 	 	 	 112
8.14	rk2_int	egrator.f90	File Refere	nce		 	 	 	 	 	 115
8.15	rk2_tl_	ad_integra	tor.f90 File F	Reference		 	 	 	 	 	 115
8.16	rk4_int	egrator.f90	File Refere	nce		 	 	 	 	 	 116
8.17	rk4_tl_	ad_integra	tor.f90 File F	Reference		 	 	 	 	 	 117
8.18	stat.f90	File Refe	rence			 	 	 	 	 	 118
8.19	tensor.	f90 File Re	eference			 	 	 	 	 	 119
8.20	test_ac	tensor.f90	File Refere	nce		 	 	 	 	 	 120
	8.20.1	Function/	Subroutine I	Document	ation .	 	 	 	 	 	 120
		8.20.1.1	test_aotens	sor		 	 	 	 	 	 120
8.21	test_in	orod_analy	rtic.f90 File I	Reference		 	 	 	 	 	 121
	8.21.1	Function/	Subroutine I	Document	ation .	 	 	 	 	 	 121
		8.21.1.1	inprod_ana	ılytic_test		 	 	 	 	 	 121
8.22	test_tl_	ad.f90 File	Reference			 	 	 	 	 	 121
	8.22.1	Function/	Subroutine I	Document	ation .	 	 	 	 	 	 121
		8.22.1.1	gasdev(idu	m)		 	 	 	 	 	 121
		8.22.1.2	ran2(idum)			 	 	 	 	 	 122
		8.22.1.3	test_tl_ad .			 	 	 	 	 	 122
8.23	tl_ad_t	ensor.f90 l	File Reference	ce		 	 	 	 	 	 122
8.24	tr_jacol	b_mat.f90	File Referer	ice		 	 	 	 	 	 123
	8.24.1	Function/	Subroutine I	Document	ation .	 	 	 	 	 	 124
		8.24.1.1	tr_jacob_m	at		 	 	 	 	 	 124
8.25	util.f90	File Refer	ence			 	 	 	 	 	 124
	8.25.1	Function/	Subroutine I	Document	ation .	 	 	 	 	 	 124
		8.25.1.1	lcg(s)			 	 	 	 	 	 124
Index											125

Chapter 1

Modular arbitrary-order ocean-atmosphere model: MAOOAM -- Fortran implementation

About

(c) 2013-2016 Lesley De Cruz and Jonathan Demaeyer

See LICENSE.txt for license information.

This software is provided as supplementary material with:

• De Cruz, L., Demaeyer, J. and Vannitsem, S.: The Modular Arbitrary-Order Ocean-Atmosphere Model: M → AOOAM v1.0, Geosci. Model Dev., 9, 2793-2808, doi:10.5194/gmd-9-2793-2016, 2016.

Please cite this article if you use (a part of) this software for a publication.

The authors would appreciate it if you could also send a reprint of your paper to lesley.decruz@meteo.be, jonathan.demaeyer@meteo.be and svn@meteo.be.

Consult the MAOOAM code repository for updates, and our website for additional resources.

A pdf version of this manual is available here.

Installation

The program can be installed with Makefile. We provide configuration files for two compilers : gfortran and ifort.

By default, gfortran is selected. To select one or the other, simply modify the Makefile accordingly or pass the CO← MPILER flag to make. If gfortran is selected, the code should be compiled with gfortran 4.7+ (allows for allocatable arrays in namelists). If ifort is selected, the code has been tested with the version 14.0.2 and we do not guarantee compatibility with older compiler version.

To install, unpack the archive in a folder or clone with git:

¹ git clone https://github.com/Climdyn/MAOOAM.git

² cd MAOOAM

and run:

1 make

By default, the inner products of the basis functions, used to compute the coefficients of the ODEs, are not stored in memory. If you want to enable the storage in memory of these inner products, run make with the following flag:

```
1 make RES=store
```

Depending on the chosen resolution, storing the inner products may result in a huge memory usage and is not recommended unless you need them for a specific purpose.

Remark: The command "make clean" removes the compiled files.

For Windows users, a minimalistic GNU development environment (including gfortran and make) is available at www.mingw.org.

Description of the files

The model tendencies are represented through a tensor called aotensor which includes all the coefficients. This tensor is computed once at the program initialization.

- maooam.f90 : Main program.
- aotensor_def.f90 : Tensor aotensor computation module.
- IC def.f90: A module which loads the user specified initial condition.
- inprod analytic.f90: Inner products computation module.
- rk2_integrator.f90 : A module which contains the Heun integrator for the model equations.
- rk4_integrator.f90 : A module which contains the RK4 integrator for the model equations.
- · Makefile: The Makefile.
- params.f90 : The model parameters module.
- tl ad tensor.f90: Tangent Linear (TL) and Adjoint (AD) model tensors definition module
- rk2_tl_ad_integrator.f90: Heun Tangent Linear (TL) and Adjoint (AD) model integrators module
- rk4_tl_ad_integrator.f90: RK4 Tangent Linear (TL) and Adjoint (AD) model integrators module
- test_tl_ad.f90 : Tests for the Tangent Linear (TL) and Adjoint (AD) model versions
- · README.md : A read me file.
- LICENSE.txt: The license text of the program.
- util.f90 : A module with various useful functions.
- tensor.f90 : Tensor utility module.
- stat.f90 : A module for statistic accumulation.
- params.nml : A namelist to specify the model parameters.
- int_params.nml : A namelist to specify the integration parameters.
- modeselection.nml: A namelist to specify which spectral decomposition will be used.

Usage

The user first has to fill the params.nml and int_params.nml namelist files according to their needs. Indeed, model and integration parameters can be specified respectively in the params.nml and int_params.nml namelist files. Some examples related to already published article are available in the params folder.

The modeselection.nml namelist can then be filled:

- NBOC and NBATM specify the number of blocks that will be used in respectively the ocean and the atmosphere. Each block corresponds to a given x and y wavenumber.
- The OMS and AMS arrays are integer arrays which specify which wavenumbers of the spectral decomposition
 will be used in respectively the ocean and the atmosphere. Their shapes are OMS(NBOC,2) and AMS(NB

 ATM,2).
- The first dimension specifies the number attributed by the user to the block and the second dimension specifies the x and the y wavenumbers.
- The VDDG model, described in Vannitsem et al. (2015) is given as an example in the archive.
- Note that the variables of the model are numbered according to the chosen order of the blocks.

The Makefile allows to change the integrator being used for the time evolution. The user should modify it according to its need. By default a RK2 scheme is selected.

Finally, the IC.nml file specifying the initial condition should be defined. To obtain an example of this configuration file corresponding to the model you have previously defined, simply delete the current IC.nml file (if it exists) and run the program :

./maooam

It will generate a new one and start with the 0 initial condition. If you want another initial condition, stop the program, fill the newly generated file and restart:

./maooam

It will generate two files:

- · evol_field.dat : the recorded time evolution of the variables.
- · mean_field.dat : the mean field (the climatology)

The tangent linear and adjoint models of MAOOAM are provided in the tl_ad_tensor, rk2_tl_ad_integrator and rk4_tl_ad_integrator modules. It is documented here.

Implementation notes

As the system of differential equations is at most bilinear in y_j (j = 1..n), y being the array of variables, it can be expressed as a tensor contraction :

$$\frac{dy_i}{dt} = \sum_{i,k=0}^{ndim} \mathcal{T}_{i,j,k} \, y_k \, y_j$$

with $y_0 = 1$.

The tensor aotensor_def::aotensor is the tensor \mathcal{T} that encodes the differential equations is composed so that:

- $\mathcal{T}_{i,j,k}$ contains the contribution of dy_i/dt proportional to $y_j y_k$.
- Furthermore, y_0 is always equal to 1, so that $\mathcal{T}_{i,0,0}$ is the constant contribution to dy_i/dt
- $\mathcal{T}_{i,j,0} + \mathcal{T}_{i,0,j}$ is the contribution to dy_i/dt which is linear in y_i .

Ideally, the tensor aotensor_def::aotensor is composed as an upper triangular matrix (in the last two coordinates).

The tensor for this model is composed in the aotensor_def module and uses the inner products defined in the inprod analytic module.

Final Remarks

The authors would like to thank Kris for help with the lua2fortran project. It has greatly reduced the amount of (error-prone) work.

No animals were harmed during the coding process.

Chapter 2

Modular arbitrary-order ocean-atmosphere model: The Tangent Linear and Adjoint model

Description:

The Tangent Linear and Adjoint model model are implemented in the same way as the nonlinear model, with a tensor storing the different terms. The Tangent Linear (TL) tensor $\mathcal{T}_{i,j,k}^{TD}$ is defined as:

$$\mathcal{T}_{i,j,k}^{TL} = \mathcal{T}_{i,k,j} + \mathcal{T}_{i,j,k}$$

while the Adjoint (AD) tensor $\mathcal{T}_{i,j,k}^{AD}$ is defined as:

$$\mathcal{T}_{i,j,k}^{AD} = \mathcal{T}_{j,k,i} + \mathcal{T}_{j,i,k}.$$

where $\mathcal{T}_{i,j,k}$ is the tensor of the nonlinear model.

These two tensors are used to compute the trajectories of the models, with the equations

$$\frac{d\delta y_i}{dt} = \sum_{i=1}^{ndim} \sum_{k=0}^{ndim} \mathcal{T}_{i,j,k}^{TL} y_k^* \, \delta y_j.$$

$$-\frac{d\delta y_i}{dt} = \sum_{i=1}^{ndim} \sum_{k=0}^{ndim} \mathcal{T}_{i,j,k}^{AD} y_k^* \, \delta y_j.$$

where \boldsymbol{y}^* is the point where the Tangent model is defined (with $y_0^*=1$).

Implementation:

The two tensors are implemented in the module tl_ad_tensor and must be initialized (after calling params::init_\top params and aotensor_def::aotensor) by calling tl_ad_tensor::init_tltensor() and tl_ad_tensor::init_adtensor(). The tendencies are then given by the routine tl(t,ystar,deltay,buf) and ad(t,ystar,deltay,buf). An integrator with the Heun method is available in the module rk2_tl_ad_integrator and a fourth-order Runge-Kutta integrator in rk4_tl_ad_\top integrator. An example on how to use it can be found in the test file test_tl_ad_f90

6	Modular arbitrary-order ocean-atmosphere model: The Tangent Linear and Adjoint model

Chapter 3

Modules Index

3.1 Modules List

Here is a list of all modules with brief descriptions:

aotensor_def	
The equation tensor for the coupled ocean-atmosphere model with temperature which allows for an extensible set of modes in the ocean and in the atmosphere	13
ic def	
Module to load the initial condition	17
icdelta def	
Module to load the perturbation initial condition	20
inprod_analytic	
Inner products between the truncated set of basis functions for the ocean and atmosphere streamfunction fields. These are partly calculated using the analytical expressions from Cehelsky, P., & Tung, K. K.: Theories of multiple equilibria and weather regimes-A critical reexamination. Part II: Baroclinic two-layer models. Journal of the atmospheric sciences, 44(21), 3282-3303, 1987	22
integrator	
Module with the integration routines	32
lyap_stat	
Statistics accumulators for the Lyapunov exponents	35
lyap_vectors	
Module for computation of Lyapunov exponents and vectors	38
params	
The model parameters module	42
stat	
Statistics accumulators	58
Tanaar utilitu madula	61
Tensor utility module	01
Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Integrators module	71
tl ad tensor	
Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Tensors definition module .	82
util	-
Utility module	90

8 Modules Index

Chapter 4

Data Type Index

4.1 Data Types List

Here are the data types with brief descriptions:

inprod_analytic::atm_tensors
Type holding the atmospheric inner products tensors
inprod_analytic::atm_wavenum
Atmospheric bloc specification type
tensor::coolist
Coordinate list. Type used to represent the sparse tensor
tensor::coolist_elem
Coordinate list element type. Elementary elements of the sparse tensors
inprod_analytic::ocean_tensors
Type holding the oceanic inner products tensors
inprod_analytic::ocean_wavenum
Oceanic bloc specification type

10 Data Type Index

Chapter 5

File Index

5.1 File List

Here is a list of all files with brief descriptions:

aotensor_def.f90	J 1
ic_def.f90	ე2
icdelta_def.f90	02
inprod_analytic.f90	03
lyap_stat.f90	09
lyap_vectors.f90	10
maooam.f90	11
maooam_lyap.f90	11
maooam_lyap_div.f90	12
params.f90	12
rk2_integrator.f90	15
rk2_tl_ad_integrator.f90	15
rk4_integrator.f90	16
rk4_tl_ad_integrator.f90	17
stat.f90	18
tensor.f90	19
test_aotensor.f90	20
test_inprod_analytic.f90	21
test_tl_ad.f90	21
tl_ad_tensor.f90	22
tr_jacob_mat.f90	23
util f90	24

12 File Index

Chapter 6

Module Documentation

6.1 aotensor_def Module Reference

The equation tensor for the coupled ocean-atmosphere model with temperature which allows for an extensible set of modes in the ocean and in the atmosphere.

Functions/Subroutines

integer function psi (i)

Translate the $\psi_{a,i}$ coefficients into effective coordinates.

• integer function theta (i)

Translate the $\theta_{a,i}$ coefficients into effective coordinates.

• integer function a (i)

Translate the $\psi_{o,i}$ coefficients into effective coordinates.

• integer function t (i)

Translate the $\delta T_{o,i}$ coefficients into effective coordinates.

• integer function kdelta (i, j)

Kronecker delta function.

• subroutine coeff (i, j, k, v)

Subroutine to add element in the aotensor $\mathcal{T}_{i,j,k}$ structure.

subroutine add_count (i, j, k, v)

Subroutine to count the elements of the aotensor $\mathcal{T}_{i,j,k}$. Add +1 to count_elems(i) for each value that is added to the tensor i-th component.

• subroutine compute_aotensor (func)

Subroutine to compute the tensor aotensor.

• subroutine, public init_aotensor

Subroutine to initialise the aotensor tensor.

Variables

• integer, dimension(:), allocatable count elems

Vector used to count the tensor elements.

real(kind=8), parameter real_eps = 2.2204460492503131e-16

Epsilon to test equality with 0.

• type(coolist), dimension(:), allocatable, public aotensor

 $\mathcal{T}_{i,j,k}$ - Tensor representation of the tendencies.

14 Module Documentation

6.1.1 Detailed Description

The equation tensor for the coupled ocean-atmosphere model with temperature which allows for an extensible set of modes in the ocean and in the atmosphere.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Remarks

Generated Fortran90/95 code from aotensor.lua

6.1.2 Function/Subroutine Documentation

```
6.1.2.1 integer function aotensor_def::a ( integer i ) [private]
```

Translate the $\psi_{o,i}$ coefficients into effective coordinates.

Definition at line 76 of file aotensor_def.f90.

```
76 INTEGER :: i,a
77 a = i + 2 * natm
```

6.1.2.2 subroutine aotensor_def::add_count (integer, intent(in) *i*, integer, intent(in) *j*, integer, intent(in) *k*, real(kind=8), intent(in) *v*) [private]

Subroutine to count the elements of the aotensor $\mathcal{T}_{i,j,k}$. Add +1 to count_elems(i) for each value that is added to the tensor i-th component.

Parameters

i	tensor i index
j	tensor j index
k	tensor k index
V	value that will be added

Definition at line 124 of file aotensor_def.f90.

```
124 INTEGER, INTENT(IN) :: i,j,k
125 REAL(KIND=8), INTENT(IN) :: v
126 IF (abs(v) .ge. real_eps) count_elems(i)=count_elems(i)+1
```

6.1.2.3 subroutine aotensor_def::coeff (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) ν) [private]

Subroutine to add element in the aotensor $\mathcal{T}_{i,j,k}$ structure.

Parameters

i	tensor i index
j	$tensor\ j \ index$
k	tensor \boldsymbol{k} index
V	value to add

Definition at line 99 of file aotensor def.f90.

```
99
         INTEGER, INTENT(IN) :: i,j,k
100
          REAL(KIND=8), INTENT(IN) :: v
          INTEGER :: n
101
          IF (.NOT. ALLOCATED(actensor)) stop "*** coeff routine : tensor not yet allocated ***"

IF (.NOT. ALLOCATED(actensor(i)%elems)) stop "*** coeff routine : tensor not yet allocated ***"
102
103
104
          IF (abs(v) .ge. real_eps) THEN
105
              n=(aotensor(i)%nelems)+1
              IF (j .LE. k) THEN
  aotensor(i)%elems(n)%j=j
106
107
108
                  aotensor(i)%elems(n)%k=k
110
                 aotensor(i)%elems(n)%j=k
111
                  aotensor(i)%elems(n)%k=j
112
             aotensor(i)%elems(n)%v=v
aotensor(i)%nelems=n
113
114
115
          END IF
```

6.1.2.4 subroutine aotensor_def::compute_aotensor(external func) [private]

Subroutine to compute the tensor aotensor.

Parameters

func	External function to be used
------	------------------------------

Definition at line 132 of file aotensor def.f90.

6.1.2.5 subroutine, public aotensor_def::init_aotensor()

Subroutine to initialise the aotensor tensor.

Remarks

This procedure will also call params::init_params() and inprod_analytic::init_inprod(). It will finally call inprod
_analytic::deallocate_inprod() to remove the inner products, which are not needed anymore at this point.

Definition at line 203 of file aotensor def.f90.

```
203 INTEGER :: i
204 INTEGER :: allocstat
205
206 CALL init_params ! Iniatialise the parameter
207
208 CALL init_inprod ! Initialise the inner product tensors
209
210 ALLOCATE(aotensor(ndim), count_elems(ndim), stat=allocstat)
211 IF (allocstat /= 0) stop "*** Not enough memory! ***"
```

16 Module Documentation

```
212
           count_elems=0
213
214
           CALL compute_aotensor(add_count)
215
216
217
           DO i=1, ndim
              ALLOCATE(aotensor(i) %elems(count_elems(i)), stat=allocstat)

IF (allocstat /= 0) stop "*** Not enough memory ! ***"
218
219
220
           DEALLOCATE(count_elems, stat=allocstat)
IF (allocstat /= 0) stop "*** Deallocation problem ! ***"
221
222
223
224
           CALL compute aotensor(coeff)
225
226
           CALL simplify(aotensor)
227
```

6.1.2.6 integer function aotensor_def::kdelta (integer i, integer j) [private]

Kronecker delta function.

Definition at line 88 of file aotensor_def.f90.

6.1.2.7 integer function aotensor_def::psi(integer i) [private]

Translate the $\psi_{a,i}$ coefficients into effective coordinates.

Definition at line 64 of file aotensor_def.f90.

```
64 INTEGER :: i,psi
65 psi = i
```

6.1.2.8 integer function aotensor_def::t(integer i) [private]

Translate the $\delta T_{o,i}$ coefficients into effective coordinates.

Definition at line 82 of file aotensor_def.f90.

6.1.2.9 integer function aotensor_def::theta (integer *i*) [private]

Translate the $\theta_{a,i}$ coefficients into effective coordinates.

Definition at line 70 of file aotensor_def.f90.

```
70 INTEGER :: i,theta
71 theta = i + natm
```

6.1.3 Variable Documentation

6.1.3.1 type(coolist), dimension(:), allocatable, public aotensor_def::aotensor

 $\mathcal{T}_{i,j,k}$ - Tensor representation of the tendencies.

Definition at line 45 of file aotensor_def.f90.

```
45 TYPE(coolist), DIMENSION(:), ALLOCATABLE, PUBLIC :: aotensor
```

6.1.3.2 integer, dimension(:), allocatable aotensor_def::count_elems [private]

Vector used to count the tensor elements.

Definition at line 37 of file aotensor_def.f90.

```
37 INTEGER, DIMENSION(:), ALLOCATABLE :: count_elems
```

6.1.3.3 real(kind=8), parameter aotensor_def::real_eps = 2.2204460492503131e-16 [private]

Epsilon to test equality with 0.

Definition at line 40 of file aotensor_def.f90.

```
40 REAL(KIND=8), PARAMETER :: real_eps = 2.2204460492503131e-16
```

6.2 ic_def Module Reference

Module to load the initial condition.

Functions/Subroutines

• subroutine, public load_ic

Subroutine to load the initial condition if IC.nml exists. If it does not, then write IC.nml with 0 as initial condition.

Variables

· logical exists

Boolean to test for file existence.

 real(kind=8), dimension(:), allocatable, public ic Initial condition vector. 18 Module Documentation

6.2.1 Detailed Description

Module to load the initial condition.

Copyright

2016 Lesley De Cruz, Jonathan Demaeyer & Sebastian Schubert See LICENSE.txt for license information.

6.2.2 Function/Subroutine Documentation

```
6.2.2.1 subroutine, public ic_def::load_ic ( )
```

Subroutine to load the initial condition if IC.nml exists. If it does not, then write IC.nml with 0 as initial condition.

Definition at line 32 of file ic def.f90.

```
32
        INTEGER :: i,allocstat,j
33
        CHARACTER(len=20) :: fm
34
        REAL(KIND=8) :: size_of_random_noise
35
        INTEGER, DIMENSION(:), ALLOCATABLE :: seed
        CHARACTER(LEN=4) :: init_type
namelist /iclist/ ic
36
37
        namelist /rand/ init_type, size_of_random_noise, seed
38
40
41
        fm(1:6) = '(F3.1)'
42
        CALL random seed(size=j)
4.3
44
        IF (ndim == 0) stop "*** Number of dimensions is 0! ***"
45
        ALLOCATE(ic(0:ndim), seed(j), stat=allocstat)

IF (allocstat /= 0) stop "*** Not enough memory! ***"
47
48
        INOUIRE(file='./IC.nml',exist=exists)
49
50
51
        IF (exists) THEN
            OPEN(8, file="IC.nml", status='OLD', recl=80, delim='APOSTROPHE')
53
           READ(8, nml=iclist)
54
           READ(8, nml=rand)
55
           CLOSE (8)
           SELECT CASE (init_type)
56
              CASE ('seed')
57
                 CALL random_seed(put=seed)
59
                 CALL random_number(ic)
60
                 ic=2*(ic-0.5)
61
                ic=ic*size_of_random_noise*10.d0
                 ic(0)=1.0d0
62
63
                 WRITE(6,*) "*** IC.nml namelist written. Starting with 'seeded' random initial condition !***"
              CASE ('rand')
                 CALL init_random_seed()
66
                CALL random_seed(get=seed)
67
                CALL random_number(ic)
68
                 ic=2*(ic-0.5)
                ic=ic*size_of_random_noise*10.d0
69
70
                 ic(0) = 1.0d0
                 WRITE((6,*) "*** IC.nml namelist written. Starting with random initial condition !***"
71
72
              CASE ('zero')
73
                 CALL init_random_seed()
74
                 CALL random_seed(get=seed)
75
                 ic=0
76
                 ic(0) = 1.0d0
                  \texttt{WRITE} \ (\textbf{6}, \star) \quad \texttt{"} \star \star \star \quad \texttt{IC.nml} \ \ \texttt{namelist} \ \ \texttt{written}. \ \ \texttt{Starting} \ \ \texttt{with} \ \ \texttt{initial} \ \ \texttt{condition} \ \ \texttt{in} \ \ \texttt{IC.nml} \ \ ! \star \star \star \star "
78
              CASE ('read')
79
                 CALL init_random_seed()
80
                 CALL random_seed(get=seed)
                 ic(0) = 1.0d0
81
                   except IC(0), nothing has to be done IC has already the right values
                  \text{WRITE} \left( 6, \star \right) \text{ "*** IC.nml namelist written. Starting with initial condition in IC.nml !***"} 
           END SELEC
85
        ELSE
86
           CALL init_random_seed()
           CALL random_seed(get=seed)
            ic=0
88
            ic(0) = 1.0d0
```

```
90
         init_type="zero"
         size_of_random_noise=0.d0
92
         WRITE(6,*) "*** IC.nml namelist written. Starting with 0 as initial condition !***"
      END IF
93
94
      OPEN(8, file="IC.nml", status='REPLACE')
      WRITE(8,'(a)')
95
      WRITE(8,'(a)') "! Namelist file :
96
      WRITE(8,'(a)') "! Initial condition.
      98
99
100
       WRITE(8,*) " ! psi variables"
101
102
       DO i=1, natm
          103
104
105
106
       WRITE(8,*) " ! theta variables"
107
108
       DO i=1, natm
       ! typ= "&
109
               &//awavenum(i)&typ/", Nx= "//trim(rstr(awavenum(i)&&%Nx,fm))//", Ny= "//trim(rstr(awavenum(i)%Ny,fm))
110
111
112
113
       WRITE(8,*) " ! A variables"
114
115
       DO i=1, noc
          WRITE(8,*) " IC("//trim(str(i+2*natm))//") = ",ic(i+2*natm)," ! Nx&
116
117
               &= "//trim(rstr(owavenum(i)%Nx,fm))//", Ny= "&
118
               &//trim(rstr(owavenum(i)%Ny,fm))
119
120
       WRITE(8,*) " ! T variables"
121
       DO i=1, noc
          122
123
124
               &//trim(rstr(owavenum(i)%Ny,fm))
125
126
127
       WRITE(8,'(a)') "&END"
128
       WRITE(8,*) ""
129
       WRITE(8,'(a)') "!-----
       WRITE(8,'(a)') "! Initialisation type.
WRITE(8,'(a)') "!-----
130
131
       WRITE(8,'(a)') "! type = 'read': use IC above (will generate a new seed);"
132
       WRITE(8,'(a)') "!
133
                              'rand': random state (will generate a new seed);"
       WRITE(8,'(a)') "!
                               'zero': zero IC (will generate a new seed);"
134
135
       WRITE(8,'(a)') "!
                               'seed': use the seed below (generate the same IC)"
136
       WRITE(8,*) ""
       WRITE(8,'(a)') "&RAND"
WRITE(8,'(a)') " init_
137
       WRITE(8,'(a)') " init_type='"//init_type//"'"
WRITE(8,'(a)') " size_of_random_noise = ",size_of_random_noise
138
139
140
       DO i=1, j
141
          WRITE(8,*) " seed("//trim(str(i))//") = ",seed(i)
142
       WRITE(8,'(a)') "&END" WRITE(8,*) ""
143
144
145
       CLOSE (8)
```

6.2.3 Variable Documentation

6.2.3.1 logicalic_def::exists [private]

Boolean to test for file existence.

Definition at line 21 of file ic_def.f90.

```
21 LOGICAL :: exists !< Boolean to test for file existence.
```

6.2.3.2 real(kind=8), dimension(:), allocatable, public ic_def::ic

Initial condition vector.

Definition at line 23 of file ic_def.f90.

```
23 REAL(KIND=8), DIMENSION(:), ALLOCATABLE, PUBLIC :: ic !< Initial condition vector
```

20 Module Documentation

6.3 icdelta_def Module Reference

Module to load the perturbation initial condition.

Functions/Subroutines

· subroutine, public load icdelta

Subroutine to load the initial condition if ICdelta.nml exists. If it does not, then write ICdelta.nml with random initial condition.

Variables

· logical exists

Boolean to test for file existence.

• real(kind=8), dimension(:), allocatable, public icdelta

Initial condition vector.

6.3.1 Detailed Description

Module to load the perturbation initial condition.

Copyright

2016 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

6.3.2 Function/Subroutine Documentation

6.3.2.1 subroutine, public icdelta_def::load_icdelta ()

Subroutine to load the initial condition if ICdelta.nml exists. If it does not, then write ICdelta.nml with random initial condition.

Definition at line 32 of file icdelta_def.f90.

```
32
       INTEGER :: i,allocstat
       CHARACTER(len=20) :: fm
33
       REAL(KIND=8) :: size_of_random_noise
       CHARACTER(LEN=4) :: init_type namelist /iclist/ icdelta
35
36
37
       namelist /rand/ init_type,size_of_random_noise
38
39
40
       fm(1:6)='(F3.1)'
42
       IF (ndim == 0) stop "*** Number of dimensions is 0! ***"
43
       ALLOCATE (icdelta(0:ndim), stat=allocstat)

IF (allocstat /= 0) stop "*** Not enough memory ! ***"
44
45
       INQUIRE(file='./ICdelta.nml',exist=exists)
48
49
       IF (exists) THEN
           OPEN(8, file="ICdelta.nml", status='OLD', recl=80, delim='APOSTROPHE')
50
51
           READ(8, nml=iclist)
52
           READ(8, nml=rand)
           SELECT CASE (init_type)
```

```
54
           CASE ('rand')
            CALL random_number(icdelta)
56
             icdelta=2 * (icdelta-0.5)
57
             icdelta=icdelta*size_of_random_noise*10.d0
58
             icdelta(0)=1.0d0
             WRITE (6,\star) "*** ICdelta.nml namelist written. Starting with random initial condition !***"
59
           CASE ('zero')
60
             icdelta=0
             icdelta(0)=1.0d0
62
63
             WRITE(6,*) "*** ICdelta.nml namelist written. Starting with initial condition in ICdelta.nml
      ! * * * "
64
           CASE ('read')
             !nothing has to be done ICdelta has already the right values
65
             WRITE(6,*) "*** ICdelta.nml namelist written. Starting with initial condition in ICdelta.nml
67
68
         CLOSE(8)
      ELSE
69
        CALL random_number(icdelta)
70
         icdelta=2*(icdelta-0.5)
         size_of_random_noise=1.d-3
72
73
         icdelta=icdelta*size_of_random_noise*10.d0
74
         icdelta(0)=1.0d0
         init_type="rand"
7.5
         WRITE(6,*) "*** ICdelta.nml namelist written. Starting with 0 as initial condition !***"
76
78
79
      OPEN(8, file="ICdelta.nml", status='REPLACE')
      80
81
      WRITE(8,'(a)') "! Initial condition.
82
      WRITE(8,'(a)') "!-
83
      WRITE(8,*) ""
84
8.5
      WRITE(8,'(a)') "&ICLIST"
      WRITE(8,*) " ! psi variables"
86
87
      DO i=1.natm
         WRITE(8,*) " ICdelta("//trim(str(i))//") = ",icdelta(i+natm)," ! typ= "&
88
              &//awavenum(i)%typ//", Nx= "//trim(rstr(awavenum(i)&
89
              &%Nx,fm))//", Ny= "//trim(rstr(awavenum(i)%Ny,fm))
      END DO
91
92
      WRITE(8,*) " ! theta variables"
9.3
      DO i=1, natm
        94
95
              &%Nx,fm))//", Ny= "//trim(rstr(awavenum(i)%Ny,fm))
96
97
98
      WRITE(8,*) " ! A variables"
99
100
       DO i=1.noc
          WRITE(8,*) " ICdelta("//trim(str(i+2*natm))//") = ",icdelta(i+2*natm)," ! Nx&
101
               &= "//trim(rstr(owavenum(i)%Nx,fm))//", Ny= "&
102
103
               &//trim(rstr(owavenum(i)%Ny,fm))
104
105
       WRITE(8,*) " ! T variables"
106
       DO i=1.noc
          107
108
109
               &//trim(rstr(owavenum(i)%Ny,fm))
110
111
       WRITE(8.'(a)') "&END"
112
       WRITE(8,*) ""
113
114
       WRITE(8,'(a)') "!-
       WRITE(8,'(a)') "! Initialisation type.
115
       WRITE(8,'(a)') "!--
116
       WRITE(8,'(a)') "! type = 'read': use ICdelta; 'rand': random state; 'zero': zero condition "
117
       WRITE(8, '(a)') "! The seed is specified in IC.nml" WRITE(8,*) ""
118
       WRITE (8, *)
119
       WRITE(8,'(a)') "&RAND"
120
       WRITE(8,'(a)') " init_type= '"//init_type//"'
WRITE(8,'(a,d15.7)') " size_of_random_noise = ",size_of_random_noise
WRITE(8,'(a)') "&END"
WRITE(8,*) ""
121
122
123
124
125
       CLOSE (8)
```

6.3.3 Variable Documentation

6.3.3.1 logical icdelta_def::exists [private]

Boolean to test for file existence.

Definition at line 21 of file icdelta def.f90.

```
21 LOGICAL :: exists !< Boolean to test for file existence.
```

6.3.3.2 real(kind=8), dimension(:), allocatable, public icdelta_def::icdelta

Initial condition vector.

Definition at line 23 of file icdelta def.f90.

```
23 REAL(KIND=8), DIMENSION(:), ALLOCATABLE, PUBLIC :: icdelta !< Initial condition vector
```

6.4 inprod_analytic Module Reference

Inner products between the truncated set of basis functions for the ocean and atmosphere streamfunction fields. These are partly calculated using the analytical expressions from Cehelsky, P., & Tung, K. K.: Theories of multiple equilibria and weather regimes-A critical reexamination. Part II: Baroclinic two-layer models. Journal of the atmospheric sciences, 44(21), 3282-3303, 1987.

Data Types

· type atm_tensors

Type holding the atmospheric inner products tensors.

· type atm wavenum

Atmospheric bloc specification type.

type ocean_tensors

Type holding the oceanic inner products tensors.

· type ocean wavenum

Oceanic bloc specification type.

Functions/Subroutines

```
    real(kind=8) function b1 (Pi, Pj, Pk)
```

Cehelsky & Tung Helper functions.

• real(kind=8) function b2 (Pi, Pj, Pk)

Cehelsky & Tung Helper functions.

• real(kind=8) function delta (r)

Integer Dirac delta function.

• real(kind=8) function flambda (r)

"Odd or even" function

• real(kind=8) function s1 (Pj, Pk, Mj, Hk)

Cehelsky & Tung Helper functions.

• real(kind=8) function s2 (Pj, Pk, Mj, Hk)

Cehelsky & Tung Helper functions.

real(kind=8) function s3 (Pj, Pk, Hj, Hk)

Cehelsky & Tung Helper functions.

• real(kind=8) function s4 (Pj, Pk, Hj, Hk)

Cehelsky & Tung Helper functions.

real(kind=8) function calculate_a (i, j)

Eigenvalues of the Laplacian (atmospheric)

• real(kind=8) function calculate_b (i, j, k)

Streamfunction advection terms (atmospheric)

real(kind=8) function calculate_c_atm (i, j)

Beta term for the atmosphere.

real(kind=8) function calculate_d (i, j)

Forcing of the ocean on the atmosphere.

real(kind=8) function calculate_g (i, j, k)

Temperature advection terms (atmospheric)

real(kind=8) function calculate_s (i, j)

Forcing (thermal) of the ocean on the atmosphere.

• real(kind=8) function calculate_k (i, j)

Forcing of the atmosphere on the ocean.

real(kind=8) function calculate_m (i, j)

Forcing of the ocean fields on the ocean.

• real(kind=8) function calculate_n (i, j)

Beta term for the ocean.

• real(kind=8) function calculate_o (i, j, k)

Temperature advection term (passive scalar)

real(kind=8) function calculate_c_oc (i, j, k)

Streamfunction advection terms (oceanic)

real(kind=8) function calculate_w (i, j)

Short-wave radiative forcing of the ocean.

· subroutine, public init inprod

Initialisation of the inner product.

Variables

- type(atm_wavenum), dimension(:), allocatable, public awavenum Atmospheric blocs specification.
- type(ocean_wavenum), dimension(:), allocatable, public owavenum

Oceanic blocs specification.

• type(atm_tensors), public atmos

Atmospheric tensors.

• type(ocean tensors), public ocean

Oceanic tensors.

6.4.1 Detailed Description

Inner products between the truncated set of basis functions for the ocean and atmosphere streamfunction fields. These are partly calculated using the analytical expressions from Cehelsky, P., & Tung, K. K.: Theories of multiple equilibria and weather regimes-A critical reexamination. Part II: Baroclinic two-layer models. Journal of the atmospheric sciences, 44(21), 3282-3303, 1987.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Remarks

Generated Fortran90/95 code from inprod_analytic.lua

6.4.2 Function/Subroutine Documentation

6.4.2.1 real(kind=8) function inprod_analytic::b1 (integer Pi, integer Pj, integer Pk) [private]

Cehelsky & Tung Helper functions.

Definition at line 100 of file inprod_analytic.f90.

```
100 INTEGER :: pi,pj,pk
101 b1 = (pk + pj) / REAL(pi)
```

6.4.2.2 real(kind=8) function inprod_analytic::b2 (integer Pi, integer Pi, integer Pi) [private]

Cehelsky & Tung Helper functions.

Definition at line 106 of file inprod analytic.f90.

```
106 INTEGER :: pi,pj,pk
107 b2 = (pk - pj) / REAL(pi)
```

6.4.2.3 real(kind=8) function inprod_analytic::calculate_a (integer, intent(in) i, integer, intent(in) j) [private]

Eigenvalues of the Laplacian (atmospheric)

```
a_{i,j} = (F_i, \nabla^2 F_j).
```

Definition at line 164 of file inprod_analytic.f90.

```
164 INTEGER, INTENT(IN) :: i, j
165 TYPE(atm_wavenum) :: ti
166
167 calculate_a = 0.d0
168 IF (i==j) THEN
169 ti = awavenum(i)
170 calculate_a = -(n**2) * ti*Nx**2 - ti*Ny**2
```

6.4.2.4 real(kind=8) function inprod_analytic::calculate_b (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k)

[private]

Streamfunction advection terms (atmospheric)

```
b_{i,j,k} = (F_i, J(F_j, \nabla^2 F_k)) .
```

Definition at line 178 of file inprod_analytic.f90.

6.4.2.5 real(kind=8) function inprod_analytic::calculate_c_atm (integer, intent(in) i, integer, intent(in) j) [private]

Beta term for the atmosphere.

```
c_{i,j} = (F_i, \partial_x F_j).
```

Definition at line 188 of file inprod_analytic.f90.

```
INTEGER, INTENT(IN) :: i,j
188
189
           TYPE(atm_wavenum) :: ti, tj
190
191
           ti = awavenum(i)
192
           tj = awavenum(j)
          c] = awavenum(j)
calculate_c_atm = 0.d0
IF ((ti%typ == "K") .AND. (tj%typ == "L")) THEN
    calculate_c_atm = n * ti%M * delta(ti%M - tj%H) * delta(ti%P - tj%P)
ELSE IF ((ti%typ == "L") .AND. (tj%typ == "K")) THEN
193
194
195
196
197
198
                tj = awavenum(i)
199
               calculate_c_atm = - n * ti%M * delta(ti%M - tj%H) * delta(ti%P - tj%P)
           END IF
200
```

6.4.2.6 real(kind=8) function inprod_analytic::calculate_c_oc (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k)

[private]

Streamfunction advection terms (oceanic)

$$C_{i,j,k} = (\eta_i, J(\eta_j, \nabla^2 \eta_k))$$
.

Definition at line 412 of file inprod_analytic.f90.

6.4.2.7 real(kind=8) function inprod_analytic::calculate_d (integer, intent(in) *i*, integer, intent(in) *j*) [private]

Forcing of the ocean on the atmosphere.

$$d_{i,j} = (F_i, \nabla^2 \eta_j)$$
.

Definition at line 208 of file inprod analytic.f90.

```
208 INTEGER, INTENT(IN) :: i,j
209
210 calculate_d=calculate_s(i,j) * calculate_m(j,j)
211
```

6.4.2.8 real(kind=8) function inprod_analytic::calculate_g (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k)

[private]

Temperature advection terms (atmospheric)

```
g_{i,j,k} = (F_i, J(F_j, F_k)).
```

Definition at line 218 of file inprod analytic.f90.

```
218
         INTEGER, INTENT(IN) :: i, j, k
          TYPE(atm_wavenum) :: ti,tj,tk
219
         REAL(KIND=8) :: val, vb1, vb2, vs1, vs2, vs3, vs4
221
         INTEGER, DIMENSION(3) :: a,b
222
         INTEGER, DIMENSION(3,3) :: w
223
         CHARACTER, DIMENSION(3) :: s
224
         INTEGER :: par
225
226
         ti = awavenum(i)
         tj = awavenum(j)
         tk = awavenum(k)
228
229
230
         a(1) = i
231
         a(2) = i
232
         a(3) = k
233
234
         val=0.d0
235
         IF ((ti%typ == "L") .AND. (tj%typ == "L") .AND. (tk%typ == "L")) THEN
236
237
238
            CALL piksrt(3,a,par)
239
240
            ti = awavenum(a(1))
241
             tj = awavenum(a(2))
242
             tk = awavenum(a(3))
243
244
             vs3 = s3(tj%P,tk%P,tj%H,tk%H)
             vs4 = s4(tj%P,tk%P,tj%H,tk%H)
             val = vs3 * ((delta(tk%H - tj%H - ti%H) - delta(tk%H &
                   = VSS * ((delta(tk%n - tj%n - ti%n) - delta(tk%n + tj%H)) * delta(tk%P + tj%P - ti%P) + & & delta(tk%H + tj%H - ti%H) * (delta(tk%P - tj%P& & + ti%P) - delta(tk%P - tj%P - ti%P))) + vs4 *& & ((delta(tk%H + tj%H - ti%H) * delta(tk%P - tj&
247
248
249
250
                   &%P - ti%P)) + (delta(tk%H - tj%H + ti%H) - & & delta(tk%H - tj%H - ti%H)) * (delta(tk%P - tj&
251
252
253
                   &%P - ti%P) - delta(tk%P - tj%P + ti%P)))
2.54
         ELSE
255
256
            s(1)=ti%tvp
257
            s(2)=tj%typ
258
            s(3)=tk%typ
259
260
             w(1,:) = i sin("A",s)
             w(2,:)=isin("K",s)
261
             w(3,:) = isin("L",s)
262
263
             IF (any(w(1,:)/=0) .AND. any(w(2,:)/=0) .AND. any(w(3,:)/=0)) THEN
265
266
                 ti = awavenum(a(b(1)))
2.67
                 ti = awavenum(a(b(2)))
                tk = awavenum(a(b(3)))
268
269
                call piksrt(3,b,par)
                vb1 = b1(ti%P,tj%P,tk%P)
271
                 vb2 = b2(ti%P,tj%P,tk%P)
             272
273
274
                ti = awavenum(a(w(2,1)))
275
                tj = awavenum(a(w(2,2)))
276
277
                 tk = awavenum(a(w(3,1)))
278
                b(1) = w(2, 1)
279
                b(2) = w(2, 2)
280
                b(3) = w(3,1)
                call piksrt(3,b,par)
281
282
                 vs1 = s1(tj%P,tk%P,tj%M,tk%H)
                 vs2 = s2(tj%P,tk%P,tj%M,tk%H)
283
284
                 val = vs1 * (delta(ti%M - tk%H - tj%M) * delta(ti%P -&
                      & tk%P + tj%P) - delta(ti%M- tk%H - tj%M) *& & delta(ti%P + tk%P - tj%P) + (delta(tk%H - tj%M& + ti%M) + delta(tk%H - tj%M - ti%M)) *& & delta(tk%P + tj%P - ti%P)) + vs2 * (delta(ti%M&
285
286
287
288
                       & - tk%H - tj%M) * delta(ti%P - tk%P - tj%P) +&
```

6.4.2.9 real(kind=8) function inprod_analytic::calculate_k (integer, intent(in) i, integer, intent(in) j) [private]

Forcing of the atmosphere on the ocean.

$$K_{i,j} = (\eta_i, \nabla^2 F_j)$$
.

Definition at line 336 of file inprod_analytic.f90.

```
336     INTEGER, INTENT(IN) :: i,j
337
338     calculate_k = calculate_s(j,i) * calculate_a(j,j)
```

6.4.2.10 real(kind=8) function inprod_analytic::calculate_m (integer, intent(in) i, integer, intent(in) j) [private]

Forcing of the ocean fields on the ocean.

$$M_{i,j} = (eta_i, \nabla^2 \eta_j)$$
.

Definition at line 345 of file inprod_analytic.f90.

6.4.2.11 real(kind=8) function inprod_analytic::calculate_n (integer, intent(in) i, integer, intent(in) j) [private]

Beta term for the ocean.

$$N_{i,j} = (\eta_i, \partial_x \eta_j).$$

Definition at line 359 of file inprod_analytic.f90.

```
INTEGER, INTENT(IN) :: i, j
359
          TYPE(ocean_wavenum) :: di,dj
360
361
          REAL(KIND=8) :: val
362
363
          di = owavenum(i)
364
          dj = owavenum(j)
          calculate_n = 0.d0
IF (dj%H/=di%H) THEN
365
366
             val = delta(di%P - dj%P) * flambda(di%H + dj%H) calculate_n = val * (-2) * dj%H * di%H * n / ((dj%H**2 - di%H**2) * pi)
367
368
369
370
```

6.4.2.12 real(kind=8) function inprod_analytic::calculate_o (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k)

[private]

Temperature advection term (passive scalar)

```
O_{i,j,k} = (\eta_i, J(\eta_j, \eta_k)).
```

Definition at line 377 of file inprod_analytic.f90.

```
377
       INTEGER, INTENT(IN) :: i,j,k
378
       TYPE(ocean_wavenum) :: di,dj,dk
REAL(KIND=8) :: vs3,vs4,val
379
380
       INTEGER, DIMENSION(3) :: a
       INTEGER :: par
381
382
383
       val=0.d0
384
385
       a(1) = i
386
       a(2) = i
387
       a(3) = k
388
389
       CALL piksrt(3,a,par)
390
391
       di = owavenum(a(1))
392
       di = owavenum(a(2))
       dk = owavenum(a(3))
393
394
395
       vs3 = s3(dj%P,dk%P,dj%H,dk%H)
396
       vs4 = s4(dj%P,dk%P,dj%H,dk%H)
       val = vs3*((delta(dk%H - dj%H - di%H) - delta(dk%H - dj%H))
397
            &%H + di%H)) * delta(dk%P + dj%P - di%P) + delta(dk&
398
       399
400
401
402
403
404
405
```

6.4.2.13 real(kind=8) function inprod_analytic::calculate_s (integer, intent(in) i, integer, intent(in) j) [private]

Forcing (thermal) of the ocean on the atmosphere.

$$s_{i,j} = (F_i, \eta_j)$$
.

Definition at line 303 of file inprod analytic.f90.

```
INTEGER, INTENT(IN) :: i,j
304
         TYPE(atm_wavenum) :: ti
305
         TYPE(ocean_wavenum) :: dj
306
         REAL(KIND=8) :: val
307
308
         ti = awavenum(i)
         dj = owavenum(j)
309
310
         val=0.d0
311
         IF (ti%typ == "A") THEN
             val = flambda(dj%H) * flambda(dj%P + ti%P)
312
            IF (val /= 0.d0) THEN
  val = val*8*sqrt(2.)*dj%P/(pi**2 * (dj%P**2 - ti%P**2) * dj%H)
313
314
315
316
         ELSEIF (ti%typ == "K") THEN
            val = flambda(2 * ti%M + dj%H) * delta(dj%P - ti%P)
IF (val /= 0.d0) THEN
val = val*4*dj%H/(pi * (-4 * ti%M**2 + dj%H**2))
317
318
319
320
321
         ELSEIF (ti%typ == "L") THEN
             val = delta(dj%P - ti%P) * delta(2 * ti%H - dj%H)
323
324
         calculate_s=val
325
```

6.4.2.14 real(kind=8) function inprod_analytic::calculate_w(integer, intent(in) i, integer, intent(in) j) [private]

Short-wave radiative forcing of the ocean.

```
W_{i,j} = (\eta_i, F_j) .
```

Definition at line 422 of file inprod_analytic.f90.

```
422 INTEGER, INTENT(IN) :: i,j
423
424 calculate_w = calculate_s(j,i)
425
```

6.4.2.15 real(kind=8) function inprod_analytic::delta (integer *r*) [private]

Integer Dirac delta function.

Definition at line 112 of file inprod_analytic.f90.

```
112 INTEGER :: r

113 IF (r==0) THEN

114 delta = 1.d0

115 ELSE

116 delta = 0.d0

117 ENDIF
```

6.4.2.16 real(kind=8) function inprod_analytic::flambda (integer *r*) [private]

"Odd or even" function

Definition at line 122 of file inprod_analytic.f90.

```
122 INTEGER :: r

123 IF (mod(r,2)==0) THEN

124 flambda = 0.d0

125 ELSE

126 flambda = 1.d0
```

6.4.2.17 subroutine, public inprod_analytic::init_inprod ()

Initialisation of the inner product.

Definition at line 436 of file inprod_analytic.f90.

```
436
         INTEGER :: i,j
437
         INTEGER :: allocstat
438
439
        IF (natm == 0 ) THEN
        stop "*** Problem : natm==0 ! ***"

ELSEIF (noc == 0) then
440
441
           stop "*** Problem : noc==0 ! ***"
442
443
444
445
446
        ! Definition of the types and wave numbers tables
447
448
        ALLOCATE (owavenum (noc), awavenum (natm), stat=allocstat)
449
        IF (allocstat /= 0) stop "*** Not enough memory ! ***"
450
451
        DO i=1.nbatm
452
453
           IF (ams(i,1)==1) THEN
               awavenum(j+1)%typ='A'
454
455
               awavenum(j+2)%typ='K'
456
               awavenum(j+3)%typ='L'
457
458
               awavenum(j+1)%P=ams(i,2)
               awavenum(j+2)%M=ams(i,1)
459
460
               awavenum (j+2) %P=ams (i,2)
               awavenum(j+3)%H=ams(i,1)
461
462
               awavenum (j+3) %P=ams (i,2)
463
464
               awavenum(j+1)%Ny=REAL(ams(i,2))
               awavenum(j+2)%Nx=REAL(ams(i,1))
awavenum(j+2)%Ny=REAL(ams(i,2))
465
466
467
               awavenum(j+3)%Nx=REAL(ams(i,1))
468
               awavenum(j+3)%Ny=REAL(ams(i,2))
469
           j=j+3
ELSE
470
471
               awavenum(j+1)%typ='K'
472
473
               awavenum(j+2)%typ='L'
474
475
               awavenum(j+1)%M=ams(i,1)
               awavenum(j+1)%P=ams(i,2)awavenum(j+2)%H=ams(i,1)
476
477
478
               \texttt{awavenum(j+2)} \ \$\texttt{P} \texttt{=} \texttt{ams(i,2)}
479
480
               awavenum(j+1)%Nx=REAL(ams(i,1))
481
               awavenum(j+1)%Ny=REAL(ams(i,2))
482
               awavenum(j+2)%Nx=REAL(ams(i,1))
483
               \texttt{awavenum(j+2) \%Ny=REAL(ams(i,2))}
484
485
               i=i+2
486
487
            ENDIF
488
489
490
        DO i=1.noc
491
           owavenum(i)%H=oms(i,1)
492
            owavenum(i)%P=oms(i,2)
493
494
            owavenum(i)%Nx=oms(i,1)/2.d0
495
            owavenum(i)%Ny=oms(i,2)
496
497
498
499
        ! Pointing to the atmospheric inner products functions
500
501
        atmos%a => calculate_a
502
        atmos %g => calculate\_g
503
        atmos%s => calculate s
504
        atmos%b => calculate_b
        atmos%d => calculate_d
505
506
        atmos%c => calculate_c_atm
507
508
        ! Pointing to the oceanic inner products functions
509
        ocean%M => calculate_m
510
511
        ocean%N => calculate_n
512
        ocean%O => calculate_o
513
         ocean%C => calculate_c_oc
        ocean%W => calculate_w
514
        ocean%K => calculate_k
515
516
```

6.4.2.18 real(kind=8) function inprod_analytic::s1 (integer Pj, integer Pk, integer Mj, integer Hk) [private]

Cehelsky & Tung Helper functions.

Definition at line 132 of file inprod_analytic.f90.

```
132 INTEGER :: pk, pj, mj, hk
133 s1 = -((pk * mj + pj * hk)) / 2.d0
```

6.4.2.19 real(kind=8) function inprod_analytic::s2 (integer Pj, integer Pk, integer Mj, integer Hk) [private]

Cehelsky & Tung Helper functions.

Definition at line 138 of file inprod_analytic.f90.

```
138 INTEGER :: pk,pj,mj,hk
139 s2 = (pk * mj - pj * hk) / 2.d0
```

6.4.2.20 real(kind=8) function inprod_analytic::s3 (integer Pj, integer Pk, integer Hj, integer Hk) [private]

Cehelsky & Tung Helper functions.

Definition at line 144 of file inprod_analytic.f90.

```
144 INTEGER :: pj,pk,hj,hk
145 s3 = (pk * hj + pj * hk) / 2.d0
```

6.4.2.21 real(kind=8) function inprod_analytic::s4 (integer Pj, integer Pk, integer Hj, integer Hk) [private]

Cehelsky & Tung Helper functions.

Definition at line 150 of file inprod_analytic.f90.

```
150 INTEGER :: pj,pk,hj,hk
151 s4 = (pk * hj - pj * hk) / 2.d0
```

6.4.3 Variable Documentation

6.4.3.1 type(atm_tensors), public inprod_analytic::atmos

Atmospheric tensors.

Definition at line 78 of file inprod_analytic.f90.

```
78 TYPE(atm_tensors), PUBLIC :: atmos
```

6.4.3.2 type(atm_wavenum), dimension(:), allocatable, public inprod_analytic::awavenum

Atmospheric blocs specification.

Definition at line 73 of file inprod_analytic.f90.

```
73 TYPE(atm_wavenum), DIMENSION(:), ALLOCATABLE, PUBLIC :: awavenum
```

6.4.3.3 type(ocean_tensors), public inprod_analytic::ocean

Oceanic tensors.

Definition at line 80 of file inprod_analytic.f90.

```
TYPE(ocean_tensors), PUBLIC :: ocean
```

6.4.3.4 type(ocean_wavenum), dimension(:), allocatable, public inprod_analytic::owavenum

Oceanic blocs specification.

Definition at line 75 of file inprod_analytic.f90.

```
75 TYPE(ocean_wavenum), DIMENSION(:), ALLOCATABLE, PUBLIC :: owavenum
```

6.5 integrator Module Reference

Module with the integration routines.

Functions/Subroutines

- subroutine, public init_integrator
 - Routine to initialise the integration buffers.
- subroutine tendencies (t, y, res)

Routine computing the tendencies of the model.

• subroutine, public step (y, t, dt, res)

Routine to perform an integration step (Heun algorithm). The incremented time is returned.

Variables

- real(kind=8), dimension(:), allocatable buf_y1
 - Buffer to hold the intermediate position (Heun algorithm)
- real(kind=8), dimension(:), allocatable buf_f0
 - Buffer to hold tendencies at the initial position.
- real(kind=8), dimension(:), allocatable buf_f1
 - Buffer to hold tendencies at the intermediate position.
- real(kind=8), dimension(:), allocatable buf_ka
 - Buffer A to hold tendencies.
- real(kind=8), dimension(:), allocatable buf_kb

Buffer B to hold tendencies.

6.5.1 Detailed Description

Module with the integration routines.

Module with the RK4 integration routines.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Remarks

This module actually contains the Heun algorithm routines. The user can modify it according to its preferred integration scheme. For higher-order schemes, additional buffers will probably have to be defined.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Remarks

This module actually contains the RK4 algorithm routines. The user can modify it according to its preferred integration scheme. For higher-order schemes, additional buffers will probably have to be defined.

6.5.2 Function/Subroutine Documentation

6.5.2.1 subroutine public integrator::init_integrator ()

Routine to initialise the integration buffers.

Definition at line 37 of file rk2_integrator.f90.

```
37     INTEGER :: allocstat
38     ALLOCATE(buf_y1(0:ndim), buf_f0(0:ndim), buf_f1(0:ndim) , stat=allocstat)
39     IF (allocstat /= 0) stop "*** Not enough memory ! ***"
```

6.5.2.2 subroutine public integrator::step (real(kind=8), dimension(0:ndim), intent(in) *y,* real(kind=8), intent(inout) *t,* real(kind=8), intent(in) *dt,* real(kind=8), dimension(0:ndim), intent(out) *res*)

Routine to perform an integration step (Heun algorithm). The incremented time is returned.

Routine to perform an integration step (RK4 algorithm). The incremented time is returned.

Parameters

	У	Initial point.
	t	Actual integration time
	dt	Integration timestep.
	res	Final point after the step.

Definition at line 61 of file rk2_integrator.f90.

```
61 REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: y
62 REAL(KIND=8), INTENT(INOUT) :: t
63 REAL(KIND=8), INTENT(IN) :: dt
64 REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: res
65
66 CALL tendencies(t,y,buf_f0)
67 buf_y1 = y+dt*buf_f0
68 CALL tendencies(t+dt,buf_y1,buf_f1)
69 res=y+0.5*(buf_f0+buf_f1)*dt
70 t=t+dt
```

6.5.2.3 subroutine integrator::tendencies (real(kind=8), intent(in) t, real(kind=8), dimension(0:ndim), intent(in) y, real(kind=8), dimension(0:ndim), intent(out) res) [private]

Routine computing the tendencies of the model.

Parameters

t	Time at which the tendencies have to be computed. Actually not needed for autonomous systems.	
У	Point at which the tendencies have to be computed.	
res	vector to store the result.	

Remarks

Note that it is NOT safe to pass y as a result buffer, as this operation does multiple passes.

Definition at line 49 of file rk2 integrator.f90.

```
49 REAL(KIND=8), INTENT(IN) :: t
50 REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: y
51 REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: res
52 CALL sparse_mul3(aotensor, y, y, res)
```

6.5.3 Variable Documentation

6.5.3.1 real(kind=8), dimension(:), allocatable integrator::buf_f0 [private]

Buffer to hold tendencies at the initial position.

Definition at line 28 of file rk2_integrator.f90.

```
28 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_f0 !< Buffer to hold tendencies at the initial position
```

6.5.3.2 real(kind=8), dimension(:), allocatable integrator::buf_f1 [private]

Buffer to hold tendencies at the intermediate position.

Definition at line 29 of file rk2_integrator.f90.

```
29 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_f1 !< Buffer to hold tendencies at the intermediate
position
```

```
6.5.3.3 real(kind=8), dimension(:), allocatable integrator::buf_ka [private]
```

Buffer A to hold tendencies.

Definition at line 28 of file rk4_integrator.f90.

```
28 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_ka !< Buffer A to hold tendencies
```

```
6.5.3.4 real(kind=8), dimension(:), allocatable integrator::buf_kb [private]
```

Buffer B to hold tendencies.

Definition at line 29 of file rk4_integrator.f90.

```
29 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_kb !< Buffer B to hold tendencies
```

```
6.5.3.5 real(kind=8), dimension(:), allocatable integrator::buf_y1 [private]
```

Buffer to hold the intermediate position (Heun algorithm)

Definition at line 27 of file rk2_integrator.f90.

```
27 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_y1 !< Buffer to hold the intermediate position (Heun algorithm)
```

6.6 lyap_stat Module Reference

Statistics accumulators for the Lyapunov exponents.

Functions/Subroutines

• subroutine, public lyap_init_stat

Initialise the accumulators.

• subroutine, public lyap_acc (x)

Accumulate one state.

• real(kind=8) function, dimension(0:ndim), public lyap_mean ()

Function returning the mean.

real(kind=8) function, dimension(0:ndim), public lyap_var ()

Function returning the variance.

• integer function, public lyap_iter ()

Function returning the number of data accumulated.

• subroutine, public lyap_reset

Routine resetting the accumulators.

Variables

• integer i =0

Number of stats accumulated.

• real(kind=8), dimension(:), allocatable m

Vector storing the inline mean.

• real(kind=8), dimension(:), allocatable mprev

Previous mean vector.

• real(kind=8), dimension(:), allocatable v

Vector storing the inline variance.

• real(kind=8), dimension(:), allocatable mtmp

6.6.1 Detailed Description

Statistics accumulators for the Lyapunov exponents.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

6.6.2 Function/Subroutine Documentation

6.6.2.1 subroutine, public lyap_stat::lyap_acc (real(kind=8), dimension(0:ndim), intent(in) x)

Accumulate one state.

Definition at line 48 of file lyap_stat.f90.

6.6.2.2 subroutine, public lyap_stat::lyap_init_stat()

Initialise the accumulators.

Definition at line 35 of file lyap_stat.f90.

```
35 INTEGER :: allocstat
36
37 ALLOCATE(m(0:ndim),mprev(0:ndim),v(0:ndim),mtmp(0:ndim), stat=allocstat)
38 IF (allocstat /= 0) stop '*** Not enough memory ***'
39 m=0.d0
40 mprev=0.d0
41 v=0.d0
42 mtmp=0.d0
43
```

```
6.6.2.3 integer function, public lyap_stat::lyap_iter ( )
```

Function returning the number of data accumulated.

Definition at line 72 of file lyap_stat.f90.

```
72 INTEGER :: lyap_iter
73 lyap_iter=i
```

6.6.2.4 real(kind=8) function, dimension(0:ndim), public lyap_stat::lyap_mean ()

Function returning the mean.

Definition at line 60 of file lyap_stat.f90.

```
60 REAL(KIND=8), DIMENSION(0:ndim) :: lyap_mean 61 lyap_mean=m
```

6.6.2.5 subroutine, public lyap_stat::lyap_reset ()

Routine resetting the accumulators.

Definition at line 78 of file lyap_stat.f90.

6.6.2.6 real(kind=8) function, dimension(0:ndim), public lyap_stat::lyap_var ()

Function returning the variance.

Definition at line 66 of file lyap_stat.f90.

```
66 REAL(KIND=8), DIMENSION(0:ndim) :: lyap_var
67 lyap_var=v/(i-1)
```

6.6.3 Variable Documentation

```
6.6.3.1 integer lyap_stat::i = 0 [private]
```

Number of stats accumulated.

Definition at line 20 of file lyap_stat.f90.

```
20 INTEGER :: i=0 !< Number of stats accumulated
```

```
6.6.3.2 real(kind=8), dimension(:), allocatable lyap_stat::m [private]
```

Vector storing the inline mean.

Definition at line 23 of file lyap stat.f90.

```
23 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: m !< Vector storing the inline mean
```

6.6.3.3 real(kind=8), dimension(:), allocatable lyap_stat::mprev [private]

Previous mean vector.

Definition at line 24 of file lyap stat.f90.

```
24 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: mprev    !< Previous mean vector
```

6.6.3.4 real(kind=8), dimension(:), allocatable lyap_stat::mtmp [private]

Definition at line 26 of file lyap stat.f90.

```
26 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: mtmp
```

6.6.3.5 real(kind=8), dimension(:), allocatable lyap_stat::v [private]

Vector storing the inline variance.

Definition at line 25 of file lyap_stat.f90.

6.7 lyap_vectors Module Reference

Module for computation of Lyapunov exponents and vectors.

Functions/Subroutines

• subroutine, public init_lyap

Initialize Lyapunov computation (possibly also vectors in later version) and initializes also a random orthogonal matrix for the matrix ensemble.

subroutine, public multiply_prop (prop_mul)

Multiplies prop_mul from the left with the prop matrix defined in this module and saves the result to prop_mul.

• subroutine, public benettin_step

Performs the benettin step in integration. Multiplies the aggregated propagators in prop with ensemble and performs QR decomposition (Gram-Schmidt orthogonalization gives Q and upper triangular matrix R). Computes also the Lyapunov exponents via the diagonal of R. WATCH OUT: prop is changed during the subroutine and restored to a unit matrix.

subroutine, public get_lyap_state (prop_ret, ensemble_ret)

Routine that returns the current global propagator and ensemble of lyapunov vectors.

Variables

- real(kind=8), dimension(:), allocatable, public loclyap

 Buffer containing the local Lyapunov exponent.
- real(kind=8), dimension(:), allocatable, public lyapunov
 Buffer containing the averaged Lyapunov exponent.
- real(kind=8), dimension(:,:), allocatable, public ensemble

 Buffer containing the QR decompsoition of the ensemble.
- real(kind=8), dimension(:,:), allocatable prop
 Buffer holding the propagator matrix.
- · integer lwork
- real(kind=8), dimension(:), allocatable work
 Temporary buffer for QR decomposition.
- real(kind=8), dimension(:), allocatable work2
 Temporary buffer for QR decomposition.
- real(kind=8), dimension(:), allocatable tau
 Temporary buffer for QR decomposition.
- real(kind=8), dimension(:,:), allocatable prop_buf
 Buffer holding the local propagator matrix.

6.7.1 Detailed Description

Module for computation of Lyapunov exponents and vectors.

Copyright

2016 Sebastian Schubert. See LICENSE.txt for license information.

Remarks

This module contains the necessary tools to perform the Benettin steps to compute the lyapunov exponents. (Ginelli for CLV will be added later)

References: Benettin, G., Galgani, L., Giorgilli, A., & Strelcyn, J. M. (1980). Lyapunov characteristic exponents for smooth dynamical systems; a method for computing all of them. Part 2: Numerical application. *Meccanica*, 15, 21-30.

6.7.2 Function/Subroutine Documentation

6.7.2.1 subroutine, public lyap_vectors::benettin_step ()

Performs the benettin step in integration. Multiplies the aggregated propagators in prop with ensemble and performs QR decomposition (Gram-Schmidt orthogonalization gives Q and upper triangular matrix R). Computes also the Lyapunov exponents via the diagonal of R. WATCH OUT: prop is changed during the subroutine and restored to a unit matrix.

Definition at line 99 of file lyap_vectors.f90.

```
99
        INTEGER :: info,k
100
101
         ! Multiply the Propagator prop from the right side with the non transposed q matrix
         ! from the qr decomposition which is stored in ensemble.
CALL dorm2r("r", "n", ndim, ndim, ndim, ensemble, ndim, tau, prop, ndim, work2, info)
102
103
         ! prop contains prop*ensemble but QR decomposed(tau is needed for that as ! well !) => copy to ensemble
104
105
106
         ensemble=prop
107
108
         ! From here on ensemble contains the new information prop*ensemble
109
         CALL dgeqrf(ndim, ndim, ensemble, ndim, tau, work, lwork, info) ! qr decomposition
110
111
         DO k=1, ndim
112
           loclyap(k) = log(abs(ensemble(k,k)))/rescaling_time
113
114
115
116
         ! Add here save for
117
118
119
         ! Initialise prop again with unit matrix
120
         CALL init_one(prop)
121
```

6.7.2.2 subroutine, public lyap_vectors::get_lyap_state (real(kind=8), dimension(ndim,ndim), intent(out) prop_ret, real(kind=8), dimension(ndim,ndim), intent(out) ensemble_ret)

Routine that returns the current global propagator and ensemble of lyapunov vectors.

Definition at line 127 of file lyap_vectors.f90.

```
127 REAL(KIND=8), DIMENSION(ndim,ndim),INTENT(OUT) :: prop_ret,ensemble_ret
128 prop_ret=prop
129 ensemble_ret=ensemble
```

6.7.2.3 subroutine, public lyap_vectors::init_lyap ()

Initialize Lyapunov computation (possibly also vectors in later version) and initializes also a random orthogonal matrix for the matrix ensemble.

Definition at line 69 of file lyap_vectors.f90.

```
69
        INTEGER :: allocstat,ilaenv,info
        {\tt lwork=ilaenv}\,({\tt l,"dgeqrf","}\,\,{\tt ",ndim,ndim,ndim,-l})
70
        lwork=ndim*lwork
71
72
       ALLOCATE (prop_buf (ndim, ndim), lyapunov(ndim), loclyap(ndim), ensemble (ndim, ndim), tau(ndim), prop(ndim, ndim)
       & work2(ndim),work(lwork),stat=allocstat)

IF (allocstat /= 0) stop "*** Not enough memory ! ***"
73
75
76
       lyapunov=0.0d0
        loclyap=0.0d0
77
        CALL init_one (prop)
        CALL random_number(ensemble)
80
        ensemble=2*(ensemble-0.5)
        CALL dgeqrf(ndim,ndim,ensemble,ndim,tau,work,lwork, info) ! qr decomposition
```

6.7.2.4 subroutine, public lyap_vectors::multiply_prop (real(kind=8), dimension(ndim,ndim), intent(in) prop_mul)

Multiplies prop_mul from the left with the prop matrix defined in this module and saves the result to prop_mul.

Parameters

propagator to multiply with the globa	local propagator to multiply with the global one
---------------------------------------	--

Definition at line 88 of file lyap_vectors.f90.

```
REAL(KIND=8), DIMENSION(ndim,ndim),INTENT(IN) :: prop_mul
prop_buf=prop
CALL dgemm ('n', 'n', ndim, ndim, ndim, 1.0d0, prop_mul, ndim,prop_buf, ndim,0.0d0, prop, ndim)
```

6.7.3 Variable Documentation

6.7.3.1 real(kind=8), dimension(:,:), allocatable, public lyap_vectors::ensemble

Buffer containing the QR decompsoition of the ensemble.

Definition at line 42 of file lyap_vectors.f90.

```
42 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: ensemble !< Buffer containing the QR decompsoition of the ensemble
```

6.7.3.2 real(kind=8), dimension(:), allocatable, public lyap_vectors::loclyap

Buffer containing the local Lyapunov exponent.

Definition at line 40 of file lyap vectors.f90.

```
40 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: loclyap   !< Buffer containing the local Lyapunov exponent
```

6.7.3.3 integer lyap_vectors::lwork [private]

Definition at line 45 of file lyap vectors.f90.

```
45 INTEGER :: lwork
```

6.7.3.4 real(kind=8), dimension(:), allocatable, public lyap_vectors::lyapunov

Buffer containing the averaged Lyapunov exponent.

Definition at line 41 of file lyap_vectors.f90.

```
41 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: lyapunov   !< Buffer containing the averaged Lyapunov exponent
```

6.7.3.5 real(kind=8), dimension(:,:), allocatable lyap_vectors::prop [private]

Buffer holding the propagator matrix.

Definition at line 43 of file lyap_vectors.f90.

```
43 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: prop !< Buffer holding the propagator matrix
```

6.7.3.6 real(kind=8), dimension(:,:), allocatable lyap_vectors::prop_buf [private]

Buffer holding the local propagator matrix.

Definition at line 49 of file lyap_vectors.f90.

```
49 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: prop_buf !< Buffer holding the local propagator matrix
```

6.7.3.7 real(kind=8), dimension(:), allocatable lyap_vectors::tau [private]

Temporary buffer for QR decomposition.

Definition at line 48 of file lyap_vectors.f90.

```
48 REAL(kind=8), DIMENSION(:), ALLOCATABLE :: tau !< Temporary buffer for QR decomposition
```

6.7.3.8 real(kind=8), dimension(:), allocatable lyap_vectors::work [private]

Temporary buffer for QR decomposition.

Definition at line 46 of file lyap_vectors.f90.

```
46 REAL(kind=8), DIMENSION(:), ALLOCATABLE :: work !< Temporary buffer for QR decomposition
```

6.7.3.9 real(kind=8), dimension(:), allocatable lyap_vectors::work2 [private]

Temporary buffer for QR decomposition.

Definition at line 47 of file lyap_vectors.f90.

```
47 REAL(kind=8), DIMENSION(:), ALLOCATABLE :: work2 !< Temporary buffer for QR decomposition
```

6.8 params Module Reference

The model parameters module.

Functions/Subroutines

subroutine, private init_nml

Read the basic parameters and mode selection from the namelist.

• subroutine init_params

Parameters initialisation routine.

Variables

```
• real(kind=8) n n=2L_y/L_x \text{ - Aspect ratio} • real(kind=8) phi0  \text{Latitude in radian.}
```

• real(kind=8) rra

Earth radius.

• real(kind=8) sig0

 σ_0 - Non-dimensional static stability of the atmosphere.

real(kind=8) k

Bottom atmospheric friction coefficient.

real(kind=8) kp

 k^{\prime} - Internal atmospheric friction coefficient.

real(kind=8) r

Frictional coefficient at the bottom of the ocean.

real(kind=8) d

Merchanical coupling parameter between the ocean and the atmosphere.

• real(kind=8) f0

 f_0 - Coriolis parameter

• real(kind=8) gp

g' Reduced gravity

• real(kind=8) h

Depth of the active water layer of the ocean.

• real(kind=8) phi0_npi

Latitude exprimed in fraction of pi.

• real(kind=8) lambda

 λ - Sensible + turbulent heat exchange between the ocean and the atmosphere.

• real(kind=8) co

 ${\it C_a}$ - Constant short-wave radiation of the ocean.

• real(kind=8) go

 γ_o - Specific heat capacity of the ocean.

• real(kind=8) ca

 ${\it C_a}$ - Constant short-wave radiation of the atmosphere.

• real(kind=8) to0

 T_o^0 - Stationary solution for the 0-th order ocean temperature.

real(kind=8) ta0

 T_a^0 - Stationary solution for the 0-th order atmospheric temperature.

real(kind=8) epsa

 ϵ_a - Emissivity coefficient for the grey-body atmosphere.

• real(kind=8) ga

 γ_a - Specific heat capacity of the atmosphere.

• real(kind=8) rr

```
R - Gas constant of dry air
• real(kind=8) scale
      L_y = L \pi - The characteristic space scale.

 real(kind=8) pi

 real(kind=8) lr

      \mathcal{L}_R - Rossby deformation radius

 real(kind=8) g

 real(kind=8) rp

      r' - Frictional coefficient at the bottom of the ocean.

 real(kind=8) dp

      d^\prime - Non-dimensional mechanical coupling parameter between the ocean and the atmosphere.

 real(kind=8) kd

      k_d - Non-dimensional bottom atmospheric friction coefficient.

 real(kind=8) kdp

      k_d' - Non-dimensional internal atmospheric friction coefficient.
• real(kind=8) cpo
      C_a^\prime - Non-dimensional constant short-wave radiation of the ocean.

 real(kind=8) lpo

      \lambda_o' - Non-dimensional sensible + turbulent heat exchange from ocean to atmosphere.
• real(kind=8) cpa
      C_a' - Non-dimensional constant short-wave radiation of the atmosphere.
• real(kind=8) lpa
      \lambda_a' - Non-dimensional sensible + turbulent heat exchange from atmosphere to ocean.
· real(kind=8) sbpo
      \sigma'_{B,o} - Long wave radiation lost by ocean to atmosphere & space.

    real(kind=8) sbpa

      \sigma_{B,a}' - Long wave radiation from atmosphere absorbed by ocean.

    real(kind=8) Isbpo

      S_{B,o}' - Long wave radiation from ocean absorbed by atmosphere.

    real(kind=8) lsbpa

      S_{B,a}^{\prime} - Long wave radiation lost by atmosphere to space & ocean.
real(kind=8)
      L - Domain length scale
• real(kind=8) sc
      Ratio of surface to atmosphere temperature.
• real(kind=8) sb
      Stefan-Boltzmann constant.

    real(kind=8) betp

      \beta' - Non-dimensional beta parameter
• real(kind=8) nua =0.D0
      Dissipation in the atmosphere.
• real(kind=8) nuo =0.D0
      Dissipation in the ocean.
• real(kind=8) nuap
      Non-dimensional dissipation in the atmosphere.
• real(kind=8) nuop
      Non-dimensional dissipation in the ocean.
• real(kind=8) t_trans
      Transient time period.
```

real(kind=8) t_run

Effective intergration time (length of the generated trajectory)

• real(kind=8) dt

Integration time step.

• real(kind=8) tw

Write all variables every tw time units.

· logical writeout

Write to file boolean.

• real(kind=8) rescaling_time

Rescaling time for the Lyapunov computation.

• integer nboc

Number of atmospheric blocks.

integer nbatm

Number of oceanic blocks.

• integer natm =0

Number of atmospheric basis functions.

• integer noc =0

Number of oceanic basis functions.

· integer ndim

Number of variables (dimension of the model)

• integer, dimension(:,:), allocatable oms

Ocean mode selection array.

• integer, dimension(:,:), allocatable ams

Atmospheric mode selection array.

6.8.1 Detailed Description

The model parameters module.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Remarks

Once the init_params() subroutine is called, the parameters are loaded globally in the main program and its subroutines and function

6.8.2 Function/Subroutine Documentation

6.8.2.1 subroutine, private params::init_nml() [private]

Read the basic parameters and mode selection from the namelist.

Definition at line 99 of file params.f90.

```
99
       INTEGER :: allocstat
100
101
        namelist /aoscale/ scale,f0,n,rra,phi0_npi
        namelist /oparams/ gp,r,h,d,nuo
namelist /aparams/ k,kp,sig0,nua
namelist /toparams/ go,co,to0
102
103
104
105
        namelist /taparams/ ga,ca,epsa,ta0
106
        namelist /otparams/ sc,lambda,rr,sb
107
108
        namelist /modeselection/ oms,ams
109
        namelist /numblocs/ nboc, nbatm
110
        namelist /int_params/ t_trans,t_run,dt,tw,writeout
111
112
        namelist /lyap_params/ rescaling_time
113
114
        OPEN(8, file="params.nml", status='OLD', recl=80, delim='APOSTROPHE')
115
        READ(8, nml=aoscale)
116
117
        READ(8, nml=oparams)
118
        READ(8, nml=aparams)
119
        READ(8, nml=toparams)
120
        READ(8, nml=taparams)
121
        READ(8, nml=otparams)
122
123
        CLOSE (8)
124
125
        OPEN(8, file="modeselection.nml", status='OLD', recl=80, delim='APOSTROPHE')
126
        READ(8, nml=numblocs)
127
128
        ALLOCATE(oms(nboc,2),ams(nbatm,2), stat=allocstat)
        IF (allocstat /= 0) stop "*** Not enough memory ! ***"
129
130
131
132
        CLOSE (8)
133
        OPEN(8, file="int_params.nml", status='OLD', recl=80, delim='APOSTROPHE')
134
        READ(8, nml=int_params)
135
136
        READ (8, nml=lyap_params)
137
```

6.8.2.2 subroutine params::init_params ()

Parameters initialisation routine.

Definition at line 142 of file params.f90.

```
INTEGER, DIMENSION(2) :: s
142
        INTEGER :: i
143
144
        CALL init_nml
145
146
147
148
        ! Computation of the dimension of the atmospheric
149
        ! and oceanic components
150
151
152
153
        natm=0
154
        DO i=1, nbatm
         IF (ams(i,1)==1) THEN
155
156
              natm=natm+3
157
158
              natm=natm+2
159
160
161
        s=shape(oms)
162
        noc=s(1)
163
164
        ndim=2*natm+2*noc
165
166
167
168
        ! Some general parameters (Domain, beta, gamma, coupling)
169
170
171
172
        pi=dacos(-1.d0)
173
        l=scale/pi
174
        phi0=phi0_npi*pi
```

```
lr=sqrt(gp*h)/f0
176
177
                                          betp=1/rra*cos(phi0)/sin(phi0)
178
                                          rp=r/f0
179
                                           dp=d/f0
180
                                           kd=k*2
181
                                          kdp=kp
182
183
184
                                          ! DERIVED QUANTITIES
185
186
187
188
189
                                           \texttt{cpo=co/(go*f0)} \;\; \star \;\; \texttt{rr/(f0**2*1**2)}
190
                                          lpo=lambda/(go*f0)
                                           cpa=ca/(ga*f0) * rr/(f0**2*1**2)/2 ! Cpa acts on psi1-psi3, not on theta
191
                                           lpa=lambda/(ga*f0)
192
193
                                          sbpo=4*sb*to0**3/(go*f0) ! long wave radiation lost by ocean to atmosphere space
                                          \begin{array}{l} \text{Sppa-8*epsa*sb*ta0**3/(go*f0)} \text{ ! long wave radiation from atmosphere absorbed by ocean} \\ \text{lsbpa-2*epsa*sb*to0**3/(ga*f0)} \text{ ! long wave radiation from ocean absorbed by atmosphere} \\ \text{lsbpa-8*epsa*sb*ta0**3/(ga*f0)} \text{ ! long wave radiation lost by atmosphere to space \& ocean} \\ \text{lspa-8*epsa*sb*ta0**3/(ga*f0)} \text{ ! long wave radiation lost by atmosphere} \\ \text{lspa-8*epsa*sb*ta0**3/(ga*f0)} \text{ ! long wave radiation lost by atmosphere} \\ \text{lspa-8*epsa*sb*ta0**3/(ga*f0)} \\ \text{lspa-8*epsa*sb*ta0**3/(ga*f0)} \text{ ! long wave radiation lost by atmosphere} \\ \text{lspa-8*epsa*sb*ta0**3/(ga*f0)} \\ \text{lspa-9*epsa*sb*ta0**3/(ga*f0)} \\ \text{lsp
194
195
196
197
                                          nuap=nua/(f0*1**2)
198
                                          nuop=nuo/(f0*1**2)
199
```

6.8.3 Variable Documentation

6.8.3.1 integer, dimension(:,:), allocatable params::ams

Atmospheric mode selection array.

Definition at line 89 of file params.f90.

```
89 INTEGER, DIMENSION(:,:), ALLOCATABLE :: ams !< Atmospheric mode selection array
```

6.8.3.2 real(kind=8) params::betp

 β' - Non-dimensional beta parameter

Definition at line 67 of file params.f90.

```
67 REAL(KIND=8) :: betp !< \f$\beta'\f$ - Non-dimensional beta parameter
```

6.8.3.3 real(kind=8) params::ca

 ${\cal C}_a$ - Constant short-wave radiation of the atmosphere.

Definition at line 40 of file params.f90.

```
40 REAL(KIND=8) :: ca !< f^c_a/f^s - Constant short-wave radiation of the atmosphere.
```

6.8.3.4 real(kind=8) params::co

 C_a - Constant short-wave radiation of the ocean.

Definition at line 38 of file params.f90.

6.8.3.5 real(kind=8) params::cpa

 C_a^\prime - Non-dimensional constant short-wave radiation of the atmosphere.

Remarks

Cpa acts on psi1-psi3, not on theta.

Definition at line 58 of file params.f90.

6.8.3.6 real(kind=8) params::cpo

 C_a' - Non-dimensional constant short-wave radiation of the ocean.

Definition at line 56 of file params.f90.

6.8.3.7 real(kind=8) params::d

Merchanical coupling parameter between the ocean and the atmosphere.

Definition at line 31 of file params.f90.

```
31 REAL(KIND=8) :: d !< Merchanical coupling parameter between the ocean and the atmosphere.
```

6.8.3.8 real(kind=8) params::dp

d' - Non-dimensional mechanical coupling parameter between the ocean and the atmosphere.

Definition at line 52 of file params.f90.

6.8.3.9 real(kind=8) params::dt

Integration time step.

Definition at line 77 of file params.f90.

```
77 REAL(KIND=8) :: dt !< Integration time step
```

6.8.3.10 real(kind=8) params::epsa

 ϵ_a - Emissivity coefficient for the grey-body atmosphere.

Definition at line 43 of file params.f90.

```
43 REAL(KIND=8) :: epsa !< f=sion_a\f$ - Emissivity coefficient for the grey-body atmosphere.
```

6.8.3.11 real(kind=8) params::f0

 f_0 - Coriolis parameter

Definition at line 32 of file params.f90.

6.8.3.12 real(kind=8) params::g

 γ

Definition at line 50 of file params.f90.

```
50 REAL(KIND=8) :: g !< f^{\gamma}f
```

6.8.3.13 real(kind=8) params::ga

 γ_a - Specific heat capacity of the atmosphere.

Definition at line 44 of file params.f90.

```
6.8.3.14 real(kind=8) params::go
```

 γ_o - Specific heat capacity of the ocean.

Definition at line 39 of file params.f90.

6.8.3.15 real(kind=8) params::gp

g'Reduced gravity

Definition at line 33 of file params.f90.

```
33 REAL(KIND=8) :: gp !< \f$g'\f$Reduced gravity
```

6.8.3.16 real(kind=8) params::h

Depth of the active water layer of the ocean.

Definition at line 34 of file params.f90.

```
34 REAL(KIND=8) :: h !< Depth of the active water layer of the ocean.
```

6.8.3.17 real(kind=8) params::k

Bottom atmospheric friction coefficient.

Definition at line 28 of file params.f90.

```
28 REAL(KIND=8) :: k !< Bottom atmospheric friction coefficient.
```

6.8.3.18 real(kind=8) params::kd

 $\ensuremath{k_{d}}$ - Non-dimensional bottom atmospheric friction coefficient.

Definition at line 53 of file params.f90.

```
53 REAL(KIND=8) :: kd !< \f$k_d\f$ - Non-dimensional bottom atmospheric friction coefficient.
```

6.8.3.19 real(kind=8) params::kdp

 k_d' - Non-dimensional internal atmospheric friction coefficient.

Definition at line 54 of file params.f90.

```
54 REAL(KIND=8) :: kdp !< f$k'_df$ - Non-dimensional internal atmospheric friction coefficient.
```

6.8.3.20 real(kind=8) params::kp

k' - Internal atmospheric friction coefficient.

Definition at line 29 of file params.f90.

6.8.3.21 real(kind=8) params::I

${\cal L}$ - Domain length scale

Definition at line 64 of file params.f90.

```
64 REAL(KIND=8) :: 1 !< \f$L\f$ - Domain length scale
```

6.8.3.22 real(kind=8) params::lambda

 λ - Sensible + turbulent heat exchange between the ocean and the atmosphere.

Definition at line 37 of file params.f90.

```
37 REAL(KIND=8) :: lambda !< f - Sensible + turbulent heat exchange between the ocean and the atmosphere.
```

6.8.3.23 real(kind=8) params::lpa

 λ_a' - Non-dimensional sensible + turbulent heat exchange from atmosphere to ocean.

Definition at line 59 of file params.f90.

```
6.8.3.24 real(kind=8) params::lpo
```

 λ_o' - Non-dimensional sensible + turbulent heat exchange from ocean to atmosphere.

Definition at line 57 of file params.f90.

6.8.3.25 real(kind=8) params::Ir

 \mathcal{L}_{R} - Rossby deformation radius

Definition at line 49 of file params.f90.

```
49 REAL(KIND=8) :: lr !< \f$L_R\f$ - Rossby deformation radius
```

6.8.3.26 real(kind=8) params::lsbpa

 $S_{B,a}^{\prime}$ - Long wave radiation lost by atmosphere to space & ocean.

Definition at line 63 of file params.f90.

```
63 REAL(KIND=8) :: lsbpa !< fs'_{B,a}f - Long wave radiation lost by atmosphere to space & ocean.
```

6.8.3.27 real(kind=8) params::lsbpo

 $S_{B,o}^{\prime}$ - Long wave radiation from ocean absorbed by atmosphere.

Definition at line 62 of file params.f90.

```
62 REAL(KIND=8) :: lsbpo !< fs'_{B,o}f - Long wave radiation from ocean absorbed by atmosphere.
```

6.8.3.28 real(kind=8) params::n

```
n=2L_y/L_x - Aspect ratio
```

Definition at line 24 of file params.f90.

```
24 REAL(KIND=8) :: n !< \f$n = 2 L_y / L_x\f$ - Aspect ratio
```

6.8.3.29 integer params::natm =0

Number of atmospheric basis functions.

Definition at line 85 of file params.f90.

```
85 INTEGER :: natm=0 !< Number of atmospheric basis functions
```

6.8.3.30 integer params::nbatm

Number of oceanic blocks.

Definition at line 84 of file params.f90.

```
84 INTEGER :: nbatm !< Number of oceanic blocks
```

6.8.3.31 integer params::nboc

Number of atmospheric blocks.

Definition at line 83 of file params.f90.

```
83 INTEGER :: nboc   !< Number of atmospheric blocks
```

6.8.3.32 integer params::ndim

Number of variables (dimension of the model)

Definition at line 87 of file params.f90.

```
87 INTEGER :: ndim   !< Number of variables (dimension of the model)
```

6.8.3.33 integer params::noc =0

Number of oceanic basis functions.

Definition at line 86 of file params.f90.

```
86 INTEGER :: noc=0 !< Number of oceanic basis functions
```

```
6.8.3.34 real(kind=8) params::nua =0.D0
```

Dissipation in the atmosphere.

Definition at line 69 of file params.f90.

```
69 REAL(KIND=8) :: nua=0.d0 !< Dissipation in the atmosphere
```

6.8.3.35 real(kind=8) params::nuap

Non-dimensional dissipation in the atmosphere.

Definition at line 72 of file params.f90.

```
72 REAL(KIND=8) :: nuap !< Non-dimensional dissipation in the atmosphere
```

6.8.3.36 real(kind=8) params::nuo =0.D0

Dissipation in the ocean.

Definition at line 70 of file params.f90.

```
70 REAL(KIND=8) :: nuo=0.d0 !< Dissipation in the ocean
```

6.8.3.37 real(kind=8) params::nuop

Non-dimensional dissipation in the ocean.

Definition at line 73 of file params.f90.

```
73 REAL(KIND=8) :: nuop !< Non-dimensional dissipation in the ocean
```

6.8.3.38 integer, dimension(:,:), allocatable params::oms

Ocean mode selection array.

Definition at line 88 of file params.f90.

```
88 INTEGER, DIMENSION(:,:), ALLOCATABLE :: oms   !< Ocean mode selection array
```

6.8.3.39 real(kind=8) params::phi0

Latitude in radian.

Definition at line 25 of file params.f90.

```
25 REAL(KIND=8) :: phi0 !< Latitude in radian
```

6.8.3.40 real(kind=8) params::phi0_npi

Latitude exprimed in fraction of pi.

Definition at line 35 of file params.f90.

```
35 REAL(KIND=8) :: phi0_npi !< Latitude exprimed in fraction of pi.
```

6.8.3.41 real(kind=8) params::pi

 π

Definition at line 48 of file params.f90.

6.8.3.42 real(kind=8) params::r

Frictional coefficient at the bottom of the ocean.

Definition at line 30 of file params.f90.

```
30 REAL(KIND=8) :: r !< Frictional coefficient at the bottom of the ocean.
```

6.8.3.43 real(kind=8) params::rescaling_time

Rescaling time for the Lyapunov computation.

Definition at line 81 of file params.f90.

```
81 REAL(KIND=8) :: rescaling_time !< Rescaling time for the Lyapunov computation
```

```
6.8.3.44 real(kind=8) params::rp
```

 r^{\prime} - Frictional coefficient at the bottom of the ocean.

Definition at line 51 of file params.f90.

```
51 REAL(KIND=8) :: rp !< fr'\f - Frictional coefficient at the bottom of the ocean.
```

6.8.3.45 real(kind=8) params::rr

 ${\cal R}$ - Gas constant of dry air

Definition at line 45 of file params.f90.

```
45 REAL(KIND=8) :: rr !< fR\f - Gas constant of dry air
```

6.8.3.46 real(kind=8) params::rra

Earth radius.

Definition at line 26 of file params.f90.

```
26 REAL(KIND=8) :: rra !< Earth radius
```

6.8.3.47 real(kind=8) params::sb

Stefan-Boltzmann constant.

Definition at line 66 of file params.f90.

```
66 REAL(KIND=8) :: sb !< Stefan-Boltzmann constant
```

6.8.3.48 real(kind=8) params::sbpa

 $\sigma_{B,a}^{\prime}$ - Long wave radiation from atmosphere absorbed by ocean.

Definition at line 61 of file params.f90.

```
61 REAL(KIND=8) :: sbpa !< f^{a}_{a}^{f} - Long wave radiation from atmosphere absorbed by ocean.
```

6.8.3.49 real(kind=8) params::sbpo

 $\sigma_{B,o}'$ - Long wave radiation lost by ocean to atmosphere & space.

Definition at line 60 of file params.f90.

6.8.3.50 real(kind=8) params::sc

Ratio of surface to atmosphere temperature.

Definition at line 65 of file params.f90.

```
65 REAL(KIND=8) :: sc !< Ratio of surface to atmosphere temperature.
```

6.8.3.51 real(kind=8) params::scale

 $L_y = L\,\pi$ - The characteristic space scale.

Definition at line 47 of file params.f90.

```
47 REAL(KIND=8) :: scale !< fL_y = L \ , \phi f - The characteristic space scale.
```

6.8.3.52 real(kind=8) params::sig0

 σ_0 - Non-dimensional static stability of the atmosphere.

Definition at line 27 of file params.f90.

```
27 REAL(KIND=8) :: sig0    !< \f$\sigma_0\f$ - Non-dimensional static stability of the atmosphere.
```

6.8.3.53 real(kind=8) params::t_run

Effective intergration time (length of the generated trajectory)

Definition at line 76 of file params.f90.

```
76 REAL(KIND=8) :: t_run    !< Effective intergration time (length of the generated trajectory)
```

6.8.3.54 real(kind=8) params::t_trans

Transient time period.

Definition at line 75 of file params.f90.

```
75 REAL(KIND=8) :: t_trans !< Transient time period
```

6.8.3.55 real(kind=8) params::ta0

 T_a^0 - Stationary solution for the 0-th order atmospheric temperature.

Definition at line 42 of file params.f90.

6.8.3.56 real(kind=8) params::to0

 T_o^0 - Stationary solution for the 0-th order ocean temperature.

Definition at line 41 of file params.f90.

6.8.3.57 real(kind=8) params::tw

Write all variables every tw time units.

Definition at line 78 of file params.f90.

```
78 REAL(KIND=8) :: tw !< Write all variables every tw time units
```

6.8.3.58 logical params::writeout

Write to file boolean.

Definition at line 79 of file params.f90.

```
79 LOGICAL :: writeout !< Write to file boolean
```

6.9 stat Module Reference

Statistics accumulators.

6.9 stat Module Reference 59

Functions/Subroutines

• subroutine, public init_stat

Initialise the accumulators.

• subroutine, public acc (x)

Accumulate one state.

• real(kind=8) function, dimension(0:ndim), public mean ()

Function returning the mean.

• real(kind=8) function, dimension(0:ndim), public var ()

Function returning the variance.

• integer function, public iter ()

Function returning the number of data accumulated.

· subroutine, public reset

Routine resetting the accumulators.

Variables

• integer i =0

Number of stats accumulated.

• real(kind=8), dimension(:), allocatable m

Vector storing the inline mean.

• real(kind=8), dimension(:), allocatable mprev

Previous mean vector.

real(kind=8), dimension(:), allocatable v

Vector storing the inline variance.

• real(kind=8), dimension(:), allocatable mtmp

6.9.1 Detailed Description

Statistics accumulators.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

6.9.2 Function/Subroutine Documentation

6.9.2.1 subroutine, public stat::acc (real(kind=8), dimension(0:ndim), intent(in) x)

Accumulate one state.

Definition at line 48 of file stat.f90.

```
6.9.2.2 subroutine, public stat::init_stat ( )
```

Initialise the accumulators.

Definition at line 35 of file stat.f90.

```
35 INTEGER :: allocstat
36
37 ALLOCATE(m(0:ndim),mprev(0:ndim),v(0:ndim),mtmp(0:ndim), stat=allocstat)
38 IF (allocstat /= 0) stop '*** Not enough memory ***'
39 m=0.d0
40 mprev=0.d0
41 v=0.d0
42 mtmp=0.d0
43
```

6.9.2.3 integer function, public stat::iter ()

Function returning the number of data accumulated.

Definition at line 72 of file stat.f90.

```
72 INTEGER :: iter
73 iter=i
```

6.9.2.4 real(kind=8) function, dimension(0:ndim), public stat::mean ()

Function returning the mean.

Definition at line 60 of file stat.f90.

```
60 REAL(KIND=8), DIMENSION(0:ndim) :: mean 61 mean=m
```

6.9.2.5 subroutine, public stat::reset ()

Routine resetting the accumulators.

Definition at line 78 of file stat.f90.

6.9.2.6 real(kind=8) function, dimension(0:ndim), public stat::var ()

Function returning the variance.

Definition at line 66 of file stat.f90.

```
66 REAL(KIND=8), DIMENSION(0:ndim) :: var 67 var=v/(i-1)
```

6.9.3 Variable Documentation

```
6.9.3.1 integer stat::i=0 [private]
```

Number of stats accumulated.

Definition at line 20 of file stat.f90.

```
20 INTEGER :: i=0 !< Number of stats accumulated
```

6.9.3.2 real(kind=8), dimension(:), allocatable stat::m [private]

Vector storing the inline mean.

Definition at line 23 of file stat.f90.

```
23 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: m !< Vector storing the inline mean
```

6.9.3.3 real(kind=8), dimension(:), allocatable stat::mprev [private]

Previous mean vector.

Definition at line 24 of file stat.f90.

```
24 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: mprev !< Previous mean vector
```

6.9.3.4 real(kind=8), dimension(:), allocatable stat::mtmp [private]

Definition at line 26 of file stat.f90.

```
26 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: mtmp
```

6.9.3.5 real(kind=8), dimension(:), allocatable stat::v [private]

Vector storing the inline variance.

Definition at line 25 of file stat.f90.

```
25 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: v !< Vector storing the inline variance
```

6.10 tensor Module Reference

Tensor utility module.

Data Types

type coolist

Coordinate list. Type used to represent the sparse tensor.

type coolist_elem

Coordinate list element type. Elementary elements of the sparse tensors.

Functions/Subroutines

• subroutine, public copy coo (src, dst)

Routine to copy a coolist.

• subroutine, public mat to coo (src, dst)

Routine to convert a matrix to a tensor.

• subroutine, public sparse_mul3 (coolist_ijk, arr_j, arr_k, res)

Sparse multiplication of a tensor with two vectors: $\sum_{j,k=0}^{ndim} \mathcal{T}_{i,j,k} \ a_j \ b_k$.

• subroutine, public jsparse_mul (coolist_ijk, arr_j, jcoo_ij)

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} \left(\mathcal{T}_{i,j,k} + \mathcal{T}_{i,k,j} \right) a_k.$$

It's implemented slightly differently: for every $\mathcal{T}_{i,j,k}$, we add to $J_{i,j}$ as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a coolist (sparse tensor).

subroutine, public jsparse_mul_mat (coolist_ijk, arr_j, jcoo_ij)

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} \left(\mathcal{T}_{i,j,k} + \mathcal{T}_{i,k,j} \right) a_k.$$

It's implemented slightly differently: for every $\mathcal{T}_{i,j,k}$, we add to $J_{i,j}$ as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a matrix.

• subroutine, public sparse_mul2 (coolist_ij, arr_j, res)

Sparse multiplication of a 2d sparse tensor with a vector: $\sum_{i=0}^{ndim} \mathcal{T}_{i,j,k} a_j$.

• subroutine, public simplify (tensor)

Routine to simplify a coolist (sparse tensor). For each index i, it upper triangularize the matrix

$$\mathcal{T}_{i,j,k}$$
 $0 \le j, k \le ndim.$

• subroutine, public add_elem (t, i, j, k, v)

Subroutine to add element to a coolist.

subroutine, public add_check (t, i, j, k, v, dst)

Subroutine to add element to a coolist and check for overflow. Once the t buffer tensor is full, add it to the destination buffer.

• subroutine, public add_to_tensor (src, dst)

Routine to add a rank-3 tensor to another one.

• subroutine, public print_tensor (t, s)

Routine to print a rank 3 tensor coolist.

• subroutine, public write_tensor_to_file (s, t)

Load a rank-4 tensor coolist from a file definition.

• subroutine, public load_tensor_from_file (s, t)

Load a rank-4 tensor coolist from a file definition.

Variables

• real(kind=8), parameter real_eps = 2.2204460492503131e-16

Parameter to test the equality with zero.

6.10.1 Detailed Description

Tensor utility module.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

6.10.2 Function/Subroutine Documentation

6.10.2.1 subroutine, public tensor::add_check (type(coolist), dimension(ndim), intent(inout) t, integer, intent(in) i, integer, intent(in) k, real(kind=8), intent(in) v, type(coolist), dimension(ndim), intent(inout) dst)

Subroutine to add element to a coolist and check for overflow. Once the t buffer tensor is full, add it to the destination buffer.

Parameters

t	temporary buffer tensor for the destination tensor
i	tensor i index
j	tensor j index
k	tensor k index
V	value to add
dst	destination tensor

Definition at line 303 of file tensor.f90.

```
303
          \texttt{TYPE}\,(\texttt{coolist})\,,\,\,\texttt{DIMENSION}\,(\texttt{ndim})\,,\,\,\texttt{INTENT}\,(\texttt{INOUT})\,\,::\,\,\mathsf{t}
          TYPE (coolist), DIMENSION(ndim), INTENT(INOUT) :: dst INTEGER, INTENT(IN) :: i,j,k
304
305
          REAL(KIND=8), INTENT(IN) :: v
306
307
          INTEGER :: n
308
          CALL add_elem(t,i,j,k,v)
309
          IF (t(i)%nelems==size(t(i)%elems)) THEN
310
             CALL add_to_tensor(t,dst)
311
            DO n=1, ndim
                   t(n)%nelems=0
312
            ENDDO
313
          ENDIF
```

6.10.2.2 subroutine, public tensor::add_elem (type(coolist), dimension(ndim), intent(inout) t, integer, intent(in) i, integer, intent(in) k, real(kind=8), intent(in) v)

Subroutine to add element to a coolist.

Parameters

t	destination tensor
i	tensor i index
j	tensor j index
k	tensor k index
V	value to add

Definition at line 281 of file tensor.f90.

```
281
        TYPE(coolist), DIMENSION(ndim), INTENT(INOUT) :: t
        INTEGER, INTENT(IN) :: i,j,k
REAL(KIND=8), INTENT(IN) :: v
282
283
        INTEGER :: n
284
285
        IF (abs(v) .ge. real_eps) THEN
286
           n=(t(i)%nelems)+1
287
           t(i)%elems(n)%i=i
           t(i)%elems(n)%k=k
288
289
            t(i)%elems(n)%v=v
290
            t(i)%nelems=n
291
        END IF
```

6.10.2.3 subroutine, public tensor::add_to_tensor (type(coolist), dimension(ndim), intent(in) *src*, type(coolist), dimension(ndim), intent(inout) *dst*)

Routine to add a rank-3 tensor to another one.

Parameters

src	Tensor to add
dst	Destination tensor

Definition at line 321 of file tensor.f90.

```
TYPE(coolist), DIMENSION(ndim), INTENT(IN) :: src TYPE(coolist), DIMENSION(ndim), INTENT(INOUT) :: dst
322
323
         TYPE(coolist_elem), DIMENSION(:), ALLOCATABLE :: celems
324
         INTEGER :: i,j,n,allocstat
325
326
         DO i=1, ndim
327
            IF (src(i)%nelems/=0) THEN
                IF (dst(i)%nelems==0) THEN
328
                   IF (ALLOCATED(dst(i)%elems)) THEN
329
                      DEALLOCATE(dst(i)%elems, stat=allocstat)

IF (allocstat /= 0) stop "*** Deallocation problem ! ***"
330
331
332
333
                   ALLOCATE(dst(i)%elems(src(i)%nelems), stat=allocstat)
                   IF (allocstat /= 0) stop "*** Not enough memory ! ***"
334
                   n=0
335
                ELSE
336
337
                   n=dst(i)%nelems
338
                   ALLOCATE (celems(n), stat=allocstat)
                   DO j=1,n
339
340
                       celems(j)%j=dst(i)%elems(j)%j
341
                       celems(j)%k=dst(i)%elems(j)%k
342
                       celems(j)%v=dst(i)%elems(j)%v
343
                   DEALLOCATE(dst(i)%elems, stat=allocstat)

IF (allocstat /= 0) stop "*** Deallocation problem ! ***"
344
345
346
                   ALLOCATE(dst(i)%elems(src(i)%nelems+n), stat=allocstat)
347
                    IF (allocstat /= 0) stop "*** Not enough memory ! ***"
348
                   DO j=1, n
349
                       dst(i)%elems(j)%j=celems(j)%j
350
                       dst(i)%elems(j)%k=celems(j)%k
351
                       dst(i)%elems(j)%v=celems(j)%v
```

```
353
                   DEALLOCATE(celems, stat=allocstat)
354
                    IF (allocstat /= 0) stop "*** Deallocation problem ! ***"
                ENDIF
355
356
                DO j=1, src(i) %nelems
                   dst(i)%elems(n+j)%j=src(i)%elems(j)%j
dst(i)%elems(n+j)%k=src(i)%elems(j)%k
357
359
                   dst(i) %elems(n+j)%v=src(i)%elems(j)%v
360
361
                dst(i)%nelems=src(i)%nelems+n
362
363
364
```

6.10.2.4 subroutine, public tensor::copy_coo (type(coolist), dimension(ndim), intent(in) *src*, type(coolist), dimension(ndim), intent(out) *dst*)

Routine to copy a coolist.

Parameters

src	Source coolist
dst	Destination coolist

Remarks

The destination tensor have to be an empty tensor, i.e. with unallocated list of elements and nelems set to 0.

Definition at line 45 of file tensor.f90.

```
45
         {\tt TYPE} \, ({\tt coolist}) \, , \, \, {\tt DIMENSION} \, ({\tt ndim}) \, , \, \, {\tt INTENT} \, ({\tt IN}) \, \, :: \, \, {\tt src} \,
46
          TYPE(coolist), DIMENSION(ndim), INTENT(OUT) :: dst
47
         INTEGER :: i,j,allocstat
48
49
         DO i=1, ndim
                 (dst(i)%nelems/=0) stop "*** copy_coo : Destination coolist not empty ! ***"
              ALLOCATE(dst(i)%elems(src(i)%nelems), stat=allocstat)

IF (allocstat /= 0) stop "*** Not enough memory! ***"
52
53
              DO j=1, src(i) %nelems
                 dst(i)%elems(j)%j=src(i)%elems(j)%j
dst(i)%elems(j)%k=src(i)%elems(j)%k
54
55
                  dst(i)%elems(j)%v=src(i)%elems(j)%v
58
             dst(i)%nelems=src(i)%nelems
         ENDDO
59
```

6.10.2.5 subroutine, public tensor::jsparse_mul (type(coolist), dimension(ndim), intent(in) coolist_ijk, real(kind=8), dimension(0:ndim), intent(in) arr_j, type(coolist), dimension(ndim), intent(out) jcoo_ij)

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} \left(\mathcal{T}_{i,j,k} + \mathcal{T}_{i,k,j} \right) a_k.$$

It's implemented slightly differently: for every $\mathcal{T}_{i,j,k}$, we add to $J_{i,j}$ as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a coolist (sparse tensor).

Parameters

coolist← _ijk	a coordinate list (sparse tensor) of which index 2 or 3 will be contracted.
arr_j	the vector to be contracted with index 2 and then index 3 of ffi_coo_ijk
jcoo_ij	a coolist (sparse tensor) to store the result of the contraction

Definition at line 124 of file tensor.f90.

```
124
          TYPE(coolist), DIMENSION(ndim), INTENT(IN):: coolist_ijk
         TYPE (coolist), DIMENSION(ndim), INTENT(N):: coolist_
TYPE(coolist), DIMENSION(ndim), INTENT(OUT):: jcoo_ij
REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: arr_j
REAL(KIND=8) :: v
INTEGER :: i,j,k,n,nj,allocstat
125
126
127
128
129
         DO i=1, ndim
              IF (jcoo_ij(i)%nelems/=0) stop "*** jsparse_mul : Destination coolist not empty ! ***"
131
              nj=2*coolist_ijk(i)%nelems
132
             ALLOCATE(jcoo_ij(i)%elems(nj), stat=allocstat)
133
             IF (allocstat /= 0) stop "*** Not enough memory ! ***"
134
             n i = 0
135
             DO n=1, coolist_ijk(i) %nelems
136
                 j=coolist_ijk(i)%elems(n)%j
137
                 k=coolist_ijk(i)%elems(n)%k
138
                 v=coolist_ijk(i)%elems(n)%v
                 IF (j /=0) THEN
139
140
                     nj=nj+1
                     jcoo_ij(i)%elems(nj)%j=j
jcoo_ij(i)%elems(nj)%k=0
141
143
                     jcoo_ij(i)%elems(nj)%v=v*arr_j(k)
144
145
                 IF (k /=0) THEN
146
147
                     n j = n j + 1
148
                     jcoo_ij(i)%elems(nj)%j=k
                      jcoo_ij(i)%elems(nj)%k=0
150
                     jcoo_ij(i)%elems(nj)%v=v*arr_j(j)
151
152
              jcoo_ij(i)%nelems=nj
153
         END DO
154
```

6.10.2.6 subroutine, public tensor::jsparse_mul_mat (type(coolist), dimension(ndim), intent(in) coolist_ijk, real(kind=8), dimension(0:ndim), intent(in) arr_j, real(kind=8), dimension(ndim,ndim), intent(out) jcoo_ij)

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} \left(\mathcal{T}_{i,j,k} + \mathcal{T}_{i,k,j} \right) a_k.$$

It's implemented slightly differently: for every $\mathcal{T}_{i,j,k}$, we add to $J_{i,j}$ as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a matrix.

Parameters

coolist←	a coordinate list (sparse tensor) of which index 2 or 3 will be contracted.
_ijk	
arr_j	the vector to be contracted with index 2 and then index 3 of ffi_coo_ijk
jcoo_ij	a matrix to store the result of the contraction

Definition at line 167 of file tensor.f90.

```
TYPE(coolist), DIMENSION(ndim), INTENT(IN):: coolist_ijk
168
         REAL(KIND=8), DIMENSION(ndim, ndim), INTENT(OUT):: jcoo_ij
        REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: arr_j
169
170
        REAL(KIND=8) :: v
        INTEGER :: i,j,k,n
jcoo_ij=0.d0
171
172
173
        DO i=1, ndim
174
           DO n=1,coolist_ijk(i)%nelems
175
               j=coolist_ijk(i)%elems(n)%j
176
               k=coolist_ijk(i)%elems(n)%k
177
               v=coolist_ijk(i)%elems(n)%v
              IF (j /=0) jcoo_ij(i,j)=jcoo_ij(i,j)+v*arr_j(k)
IF (k /=0) jcoo_ij(i,k)=jcoo_ij(i,k)+v*arr_j(j)
178
179
           END DO
181
      END DO
```

6.10.2.7 subroutine, public tensor::load_tensor_from_file (character (len=*), intent(in) s, type(coolist), dimension(ndim), intent(out) t)

Load a rank-4 tensor coolist from a file definition.

Parameters

s	Filename of the tensor definition file
t	The loaded coolist

Remarks

The destination tensor have to be an empty tensor, i.e. with unallocated list of elements and nelems set to 0.

Definition at line 416 of file tensor.f90.

```
416
       CHARACTER (LEN=*), INTENT(IN) :: s
        TYPE (coolist), DIMENSION (ndim), INTENT (OUT) :: t
417
        INTEGER :: i,ir,j,k,n,allocstat
418
419
        REAL(KIND=8) :: v
420
       OPEN(30, file=s, status='old')
421
       DO i=1, ndim
422
          READ(30,*) ir,n
          IF (n /= 0) THEN
423
424
             ALLOCATE(t(i)%elems(n), stat=allocstat)
425
             IF (allocstat /= 0) stop "*** Not enough memory ! ***"
426
             t(i)%nelems=n
427
          DO n=1,t(i)%nelems
428
             READ(30,*) ir,j,k,v
429
430
             t(i)%elems(n)%j=j
             t(i)%elems(n)%k=k
432
             t(i)%elems(n)%v=v
433
434
       CLOSE (30)
435
```

6.10.2.8 subroutine, public tensor::mat_to_coo (real(kind=8), dimension(0:ndim,0:ndim), intent(in) *src*, type(coolist), dimension(ndim), intent(out) *dst*)

Routine to convert a matrix to a tensor.

Parameters

src	Source matrix
dst	Destination tensor

Remarks

The destination tensor have to be an empty tensor, i.e. with unallocated list of elements and nelems set to 0.

Definition at line 67 of file tensor.f90.

```
REAL(KIND=8), DIMENSION(0:ndim,0:ndim), INTENT(IN) :: src
       TYPE (coolist), DIMENSION (ndim), INTENT (OUT) :: dst
68
69
       INTEGER :: i,j,n,allocstat
70
       DO i=1, ndim
71
          n=0
72
          DO j=1, ndim
              IF (abs(src(i,j))>real_eps) n=n+1
73
74
           IF (dst(i)%nelems/=0) stop "*** mat_to_coo : Destination coolist not empty ! ***"
          ALLOCATE(dst(i)%elems(n), stat=allocstat)

IF (allocstat /= 0) stop "*** Not enough memory ! ***"
76
77
78
          n=0
79
          DO j=1, ndim
              IF (abs(src(i,j))>real_eps) THEN
80
81
                 n=n+1
                 dst(i)%elems(n)%j=j
83
                 dst(i)%elems(n)%k=0
84
                 dst(i)%elems(n)%v=src(i,j)
85
          ENDDO
86
          dst(i)%nelems=n
```

6.10.2.9 subroutine, public tensor::print_tensor (type(coolist), dimension(ndim), intent(in) t, character, intent(in), optional s)

Routine to print a rank 3 tensor coolist.

Parameters

```
t coolist to print
```

Definition at line 370 of file tensor.f90.

```
370
       USE util, only: str
       TYPE(coolist), DIMENSION(ndim), INTENT(IN) :: t CHARACTER, INTENT(IN), OPTIONAL :: s
371
372
       CHARACTER :: r
INTEGER :: i,n,j,k
373
374
375
       IF (PRESENT(s)) THEN
376
377
       ELSE
       r="t"
378
379
380
       DO i=1, ndim
          DO n=1,t(i)%nelems
381
382
             j=t(i)%elems(n)%j
383
             k=t (i) elems (n) k
             384
385
386
387
             END IF
388
389
       END DO
```

6.10.2.10 subroutine, public tensor::simplify (type(coolist), dimension(ndim), intent(inout) tensor)

Routine to simplify a coolist (sparse tensor). For each index i, it upper triangularize the matrix

$$\mathcal{T}_{i,j,k}$$
 $0 \leq j,k \leq ndim.$

•

Parameters

tensor a coordinate list (sparse tensor) which will be simplified.

Definition at line 209 of file tensor.f90.

```
209
      TYPE(coolist), DIMENSION(ndim), INTENT(INOUT):: tensor
210
      INTEGER :: i,j,k
      INTEGER :: li,lii,liii,n
211
212
      DO i= 1, ndim
213
         n=tensor(i)%nelems
         DO li=n,2,-1
214
215
             j=tensor(i)%elems(li)%j
216
             k=tensor(i)%elems(li)%k
217
            DO lii=li-1,1,-1
218
               IF (((j==tensor(i)%elems(lii)%j).AND.(k==tensor(i)&
219
                    &%elems(lii)%k)).OR.((j==tensor(i)%elems(lii)%k).AND.(k==
     tensor(i)%elems(lii)%j))) THEN
220
                   ! Found another entry with the same i,j,k: merge both into
                   ! the one listed first (of those two).
221
222
                   tensor(i)%elems(lii)%v=tensor(i)%elems(lii)%v+tensor(i)%elems(lii)%v
223
                   IF (i>k) THEN
224
                     tensor(i)%elems(lii)%j=tensor(i)%elems(li)%k
                      tensor(i)%elems(lii)%k=tensor(i)%elems(lii)%j
225
226
                   ENDIF
227
228
                   ! Shift the rest of the items one place down.
229
                  DO liii=li+1.n
230
                      tensor(i)%elems(liii-1)%j=tensor(i)%elems(liii)%j
231
                      tensor(i)%elems(liii-1)%k=tensor(i)%elems(liii)%k
232
                      tensor(i)%elems(liii-1)%v=tensor(i)%elems(liii)%v
233
234
                   tensor(i)%nelems=tensor(i)%nelems-1
                   235
236
237
                  EXIT
239
240
241
         n=tensor(i)%nelems
242
         DO li=1.n
243
             ! Clear new "almost" zero entries and shift rest of the items one place down.
             ! Make sure not to skip any entries while shifting!
244
245
             DO WHILE (abs(tensor(i)%elems(li)%v) < real_eps)
246
               DO liii=li+1, n
                   tensor(i)%elems(liii-1)%j=tensor(i)%elems(liii)%j
247
                   tensor(i)%elems(liii-1)%k=tensor(i)%elems(liii)%k
248
                   tensor(i)%elems(liii-1)%v=tensor(i)%elems(liii)%v
249
251
               tensor(i) %nelems=tensor(i) %nelems-1
252
               if (li > tensor(i)%nelems) THEN
253
254
            ENDDO
255
256
258
          n=tensor(i)%nelems
259
         DO li=1, n
2.60
             ! Upper triangularize
261
             i=tensor(i)%elems(li)%i
262
             k=tensor(i)%elems(li)%k
            IF (j>k) THEN
263
264
               tensor(i)%elems(li)%j=k
265
               tensor(i)%elems(li)%k=j
266
267
268
270
```

6.10.2.11 subroutine, public tensor::sparse_mul2 (type(coolist), dimension(ndim), intent(in) coolist_ij, real(kind=8), dimension(0:ndim), intent(in) arr_j, real(kind=8), dimension(0:ndim), intent(out) res

Sparse multiplication of a 2d sparse tensor with a vector: $\sum_{j=0}^{ndim} \mathcal{T}_{i,j,k} \, a_j.$

Parameters

coolist←	a coordinate list (sparse tensor) of which index 2 will be contracted.
_ij	
arr_j	the vector to be contracted with index 2 of coolist_ijk
res	vector (buffer) to store the result of the contraction

Remarks

Note that it is NOT safe to pass arr_j as a result buffer, as this operation does multiple passes.

Definition at line 192 of file tensor.f90.

```
TYPE(coolist), DIMENSION(ndim), INTENT(IN):: coolist_ij
REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: arr_j
REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: res
192
193
194
195
              INTEGER :: i,j,n
196
197
              res=0.d0
             DO i=1, ndim
               DO n=1,coolist_ij(i)%nelems

j=coolist_ij(i)%elems(n)%j

res(i) = res(i) + coolist_ij(i)%elems(n)%v * arr_j(j)
198
199
201
              END DO
202
           END DO
```

6.10.2.12 subroutine, public tensor::sparse_mul3 (type(coolist), dimension(ndim), intent(in) coolist_ijk, real(kind=8), dimension(0:ndim), intent(in) arr_k, real(kind=8), dimension(0:ndim), intent(in) arr_k, real(kind=8), dimension(0:ndim), intent(out) res)

Sparse multiplication of a tensor with two vectors: $\sum_{j,k=0}^{ndim} \mathcal{T}_{i,j,k} \, a_j \, b_k.$

Parameters

coolist←	a coordinate list (sparse tensor) of which index 2 and 3 will be contracted.
_ijk	
arr_j	the vector to be contracted with index 2 of coolist_ijk
arr_k	the vector to be contracted with index 3 of coolist_ijk
res	vector (buffer) to store the result of the contraction

Remarks

Note that it is NOT safe to pass arr_j/arr_k as a result buffer, as this operation does multiple passes.

Definition at line 100 of file tensor.f90.

```
TYPE(coolist), DIMENSION(ndim), INTENT(IN):: coolist_ijk
        REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: arr_j, arr_k
REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: res
101
102
103
        INTEGER :: i,j,k,n
104
        res=0.d0
105
        DO i=1.ndim
          DO n=1, coolist_ijk(i)%nelems
106
107
              j=coolist_ijk(i)%elems(n)%j
108
              k=coolist_ijk(i)%elems(n)%k
109
              res(i) = res(i) + coolist_ijk(i) elems(n) v * arr_j(j) * arr_k(k)
110
111
```

6.10.2.13 subroutine, public tensor::write_tensor_to_file (character (len=*), intent(in) s, type(coolist), dimension(ndim), intent(in) t)

Load a rank-4 tensor coolist from a file definition.

Parameters

s	Destination filename
t	The coolist to write

Definition at line 396 of file tensor.f90.

```
CHARACTER (LEN=*), INTENT(IN) :: s
TYPE(coolist), DIMENSION(ndim), INTENT(IN) :: t
396
397
          INTEGER :: i,j,k,n
OPEN(30,file=s)
398
399
          DO i=1, ndim
400
           WRITE(30,*) i,t(i)%nelems
DO n=1,t(i)%nelems
401
402
                j=t(i)%elems(n)%j
k=t(i)%elems(n)%k
403
404
405
                   WRITE(30, \star) i, j, k, t(i)%elems(n)%v
406
        END DO
END DO
407
408
         CLOSE (30)
```

6.10.3 Variable Documentation

6.10.3.1 real(kind=8), parameter tensor::real_eps = 2.2204460492503131e-16

Parameter to test the equality with zero.

Definition at line 33 of file tensor.f90.

```
33 REAL(KIND=8), PARAMETER :: real_eps = 2.2204460492503131e-16
```

6.11 tl_ad_integrator Module Reference

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Integrators module.

Functions/Subroutines

subroutine tendencies (t, y, res)

Routine computing the tendencies of the nonlinear model.

subroutine, public init_tl_ad_integrator

Routine to initialise the integration buffers.

• subroutine, public ad_step (y, ystar, t, dt, res)

Routine to perform an integration step (Heun algorithm) of the adjoint model. The incremented time is returned.

• subroutine, public evolve ad step (y, deltay, t, dt, ynew, deltaynew)

Routine to perform a simultaneous integration step (RK4 algorithm) of the nonlinear and adjoint together. The incremented time is returned.

• subroutine, public tl_step (y, ystar, t, dt, res)

Routine to perform an integration step (Heun algorithm) of the tangent linear model. The incremented time is returned.

• subroutine, public evolve_tl_step (y, deltay, t, dt, ynew, deltaynew)

Routine to perform a simultaneous integration step (RK4 algorithm) of the nonlinear and the tangent linear model together. The incremented time is returned.

• subroutine, public prop_step (y, propagator, t, dt, ynew, adjoint)

Routine to perform a simultaneously an integration step (Heun algorithm) of the nonlinear and computes the Heun tangent linear propagator. The boolean variable adjoint allows for an adjoint forward integration. The incremented time is returned.

Variables

real(kind=8), dimension(:), allocatable buf_y1

Buffer to hold the intermediate position (Heun algorithm) of the tangent linear model.

real(kind=8), dimension(:), allocatable buf_f0

Buffer to hold tendencies at the initial position of the tangent linear model.

• real(kind=8), dimension(:), allocatable buf_f1

Buffer to hold tendencies at the intermediate position of the tangent linear model.

real(kind=8), dimension(:), allocatable buf_y11

Buffer to hold the intermediate position (Heun algorithm) of the tangent linear model.

• real(kind=8), dimension(:), allocatable buf_f00

Buffer to hold tendencies at the initial position of the tangent linear model.

• real(kind=8), dimension(:), allocatable buf_f11

Buffer to hold tendencies at the intermediate position of the tangent linear model.

real(kind=8), dimension(:,:), allocatable buf_j1

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

real(kind=8), dimension(:,:), allocatable buf_j2

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

• real(kind=8), dimension(:,:), allocatable buf_j1h

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

• real(kind=8), dimension(:,:), allocatable buf_j2h

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

• real(kind=8), dimension(:,:), allocatable one

unit matrix

• real(kind=8), dimension(:), allocatable buf ka

Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

real(kind=8), dimension(:), allocatable buf kb

Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

real(kind=8), dimension(:), allocatable buf_kc

Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

- real(kind=8), dimension(:), allocatable buf_kd
 - Buffer to hold tendencies in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:,:), allocatable buf_j3
 - Buffer to hold jacobians in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:,:), allocatable buf_j4
 - Buffer to hold jacobians in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:,:), allocatable buf j3h
 - Buffer to hold jacobians in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:,:), allocatable buf_j4h
 - Buffer to hold jacobians in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:), allocatable buf_kaa
 - Buffer to hold tendencies in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:), allocatable buf_kbb
 - Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

6.11.1 Detailed Description

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Integrators module.

Copyright

2016 Lesley De Cruz, Jonathan Demaeyer & Sebastian Schubert. See LICENSE.txt for license information.

Remarks

This module actually contains the Heun algorithm routines. The user can modify it according to its preferred integration scheme. For higher-order schemes, additional buffers will probably have to be defined.

Copyright

2016 Lesley De Cruz, Jonathan Demaeyer & Sebastian Schubert. See LICENSE.txt for license information.

Remarks

This module actually contains the RK4 algorithm routines. The user can modify it according to its preferred integration scheme. For higher-order schemes, additional bufers will probably have to be defined.

6.11.2 Function/Subroutine Documentation

6.11.2.1 subroutine public tl_ad_integrator::ad_step (real(kind=8), dimension(0:ndim), intent(in) y, real(kind=8), dimension(0:ndim), intent(in) ystar, real(kind=8), intent(inout) t, real(kind=8), intent(in) dt, real(kind=8), dimension(0:ndim), intent(out) res)

Routine to perform an integration step (Heun algorithm) of the adjoint model. The incremented time is returned.

Routine to perform an integration step (RK4 algorithm) of the adjoint model. The incremented time is returned.

Parameters

У	Initial point.
ystar	Adjoint model at the point ystar.
t	Actual integration time
dt	Integration timestep.
res	Final point after the step.

Definition at line 92 of file rk2_tl_ad_integrator.f90.

```
92
        REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: y,ystar
93
        REAL(KIND=8), INTENT(INOUT) :: t
        REAL(KIND=8), INTENT(IN) :: dt
REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: res
94
95
97
        CALL ad(t,ystar,y,buf_f0)
        buf_y1 = y+dt*buf_f0
CALL ad(t+dt,ystar,buf_y1,buf_f1)
98
99
100
         res=y+0.5*(buf_f0+buf_f1)*dt
         t = t + dt
101
```

6.11.2.2 subroutine public tl_ad_integrator::evolve_ad_step (real(kind=8), dimension(0:ndim), intent(in) y, real(kind=8), dimension(0:ndim), intent(in) deltay, real(kind=8), intent(inout) t, real(kind=8), intent(in) dt, real(kind=8), dimension(0:ndim), intent(out) ynew, real(kind=8), dimension(0:ndim), intent(out) deltaynew)

Routine to perform a simultaneous integration step (RK4 algorithm) of the nonlinear and adjoint together. The incremented time is returned.

Routine to perform a simultaneous integration step (RK4 algorithm) of the nonlinear and adjoint model together. The incremented time is returned.

Parameters

У	Model variable at time t	
deltay	Perturbation at time t	
t	Actual integration time	
dt Integration timestep.		
ynew Model variable at time t-		
deltaynew	Perturbation at time t+dt	

Definition at line 112 of file rk2 tl ad integrator.f90.

```
112
         {\tt REAL\,(KIND=8)\,,\;\;DIMENSION\,(0:ndim)\,,\;\;INTENT\,(IN)\;\;::\;\;y,deltay}
         REAL(KIND=8), INTENT(INOUT) :: t
REAL(KIND=8), INTENT(IN) :: dt
113
114
         REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: ynew,deltaynew
115
116
117
         CALL tendencies(t,y,buf_f0)
118
         CALL ad(t,y,deltay,buf_f00)
119
         buf_y1 = y + dt*buf_f0
buf_y11 = deltay + dt*buf_f00
120
121
122
123
         CALL tendencies(t+dt,buf_y1,buf_f1)
124
         CALL ad(t+dt,buf_y1,buf_y11,buf_f11)
125
126
127
         ynew=y+0.5*(buf_f0+buf_f1)*dt
128
         deltaynew=deltay+0.5*(buf_f00+buf_f11)*dt
```

6.11.2.3 subroutine public tl_ad_integrator::evolve_tl_step (real(kind=8), dimension(0:ndim), intent(in) *y,* real(kind=8), dimension(0:ndim), intent(in) *deltay,* real(kind=8), intent(inout) *t,* real(kind=8), intent(in) *dt,* real(kind=8), dimension(0:ndim), intent(out) *ynew,* real(kind=8), dimension(0:ndim), intent(out) *deltaynew*)

Routine to perform a simultaneous integration step (RK4 algorithm) of the nonlinear and the tangent linear model together. The incremented time is returned.

Routine to perform a simultaneous integration step (RK4 algorithm) of the nonlinear and tangent linear model togheter. The incremented time is returned.

Parameters

у	Model variable at time t
deltay	Perturbation at time t
t	Actual integration time
dt	Integration timestep.
ynew	Model variable at time t+dt
deltaynew	Perturbation at time t+dt

Definition at line 165 of file rk2_tl_ad_integrator.f90.

```
REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: y, deltay
165
        REAL(KIND=8), INTENT(INOUT) :: t
REAL(KIND=8), INTENT(IN) :: dt
166
167
168
        REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: ynew,deltaynew
169
170
171
        CALL tendencies (t,y,buf_f0)
        CALL ad(t,y,deltay,buf_f00)
172
        buf_y1 = y + dt*buf_f0
173
        buf_y11 = deltay + dt*buf_f00
175
        CALL tendencies(t+dt,buf_y1,buf_f1)
176
177
        CALL ad(t+dt,buf_y1,buf_y11,buf_f11)
178
179
        ynew=y+0.5*(buf_f0+buf_f1)*dt
180
        deltaynew=deltay+0.5*(buf_f00+buf_f11)*dt
```

6.11.2.4 subroutine public tl_ad_integrator::init_tl_ad_integrator()

Routine to initialise the integration buffers.

Routine to initialise the TL-AD integration bufers.

Definition at line 68 of file rk2_tl_ad_integrator.f90.

6.11.2.5 subroutine public tl_ad_integrator::prop_step (real(kind=8), dimension(0:ndim), intent(in) y, real(kind=8), dimension(ndim,ndim), intent(out) propagator, real(kind=8), intent(inout) t, real(kind=8), intent(in) dt, real(kind=8), dimension(0:ndim), intent(out) ynew, logical, intent(in) adjoint)

Routine to perform a simultaneously an integration step (Heun algorithm) of the nonlinear and computes the Heun tangent linear propagator. The boolean variable adjoint allows for an adjoint forward integration. The incremented time is returned.

Routine to perform a simultaneously an integration step (RK4 algorithm) of the nonlinear and computes the RK4 tangent linear propagator. The boolean variable adjoint allows for an adjoint forward integration. The incremented time is returned.

Parameters

У	Model variable at time t
propagator	Propagator at time t
t	Actual integration time
dt	Integration timestep.
ynew	Model variable at time t+dt
adjoint	If true, compute the propagator of the adjoint model (AD) instead of the tangent one (TL)
У	Model variable at time t
propagator	Propagator at time t
t	Actual integration time
dt	Integration timestep
ynew	Model variable at time t+dt
adjoint	If true, compute the propagator of the adjoint model (AD) instead of the tangent one (TL)

Definition at line 193 of file rk2_tl_ad_integrator.f90.

```
193
        REAL(KIND=8), INTENT(INOUT) :: t
194
        REAL(KIND=8), INTENT(IN) :: dt
195
        REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: y
196
        LOGICAL, INTENT(IN) :: adjoint
197
       REAL(KIND=8), DIMENSION(ndim,ndim), INTENT(OUT) :: propagator
198
       REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: ynew
199
200
        CALL tendencies (t,y,buf_f0)
201
       buf_j1=jacobian_mat(y)
202
203
       buf_y1 = y + dt*buf_f0
204
       CALL tendencies(t+dt,buf_y1,buf_f1)
205
206
       buf_j2=jacobian_mat(buf_y1)
207
208
       buf_j1h=buf_j1
209
       buf_j2h=buf_j2
210
       CALL dgemm ('n', 'n', ndim, ndim, ndim, dt, buf_j2, ndim,buf_j1h, ndim,1.0d0, buf_j2h, ndim)
211
212
       ynew=y + dt/2.0d0*(buf_f0 + buf_f1)
213
        IF (adjoint) THEN
214
               propagator=one - dt/2.0d0*(buf_j1h + buf_j2h)
215
       ELSE
                propagator=one + dt/2.0d0*(buf_j1h + buf_j2h)
216
217
       END IF
       t=t+dt
218
```

6.11.2.6 subroutine tl_ad_integrator::tendencies (real(kind=8), intent(in) t, real(kind=8), dimension(0:ndim), intent(in) y, real(kind=8), dimension(0:ndim), intent(out) res) [private]

Routine computing the tendencies of the nonlinear model.

Parameters

t	Time at which the tendencies have to be computed. Actually not needed for autonomous systems.	
У	y Point at which the tendencies have to be computed.	
res	res vector to store the result.	

Remarks

Note that it is NOT safe to pass y as a result bufer, as this operation does multiple passes.

Definition at line 60 of file rk2_tl_ad_integrator.f90.

```
60 REAL(KIND=8), INTENT(IN) :: t
61 REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: y
62 REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: res
63 CALL sparse_mul3(aotensor, y, y, res)
```

6.11.2.7 subroutine public tl_ad_integrator::tl_step (real(kind=8), dimension(0:ndim), intent(in) y, real(kind=8), dimension(0:ndim), intent(in) ystar, real(kind=8), intent(inout) t, real(kind=8), intent(in) dt, real(kind=8), dimension(0:ndim), intent(out) res)

Routine to perform an integration step (Heun algorithm) of the tangent linear model. The incremented time is returned.

Routine to perform an integration step (RK4 algorithm) of the tangent linear model. The incremented time is returned.

Parameters

У	Initial point.
ystar	Adjoint model at the point ystar.
t	Actual integration time
dt	Integration timestep.
res	Final point after the step.

Definition at line 145 of file rk2_tl_ad_integrator.f90.

6.11.3 Variable Documentation

6.11.3.1 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_f0 [private]

Buffer to hold tendencies at the initial position of the tangent linear model.

Definition at line 35 of file rk2_tl_ad_integrator.f90.

```
35 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_f0 !< Buffer to hold tendencies at the initial position of the tangent linear model
```

```
6.11.3.2 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_f00 [private]
```

Buffer to hold tendencies at the initial position of the tangent linear model.

Definition at line 39 of file rk2 tl ad integrator.f90.

```
39 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_f00 !< Buffer to hold tendencies at the initial position of the tangent linear model
```

```
6.11.3.3 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_f1 [private]
```

Buffer to hold tendencies at the intermediate position of the tangent linear model.

Definition at line 36 of file rk2_tl_ad_integrator.f90.

```
36 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_f1 !< Buffer to hold tendencies at the intermediate position of the tangent linear model
```

```
6.11.3.4 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_f11 [private]
```

Buffer to hold tendencies at the intermediate position of the tangent linear model.

Definition at line 40 of file rk2_tl_ad_integrator.f90.

```
40 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_f11 !< Buffer to hold tendencies at the intermediate position of the tangent linear model
```

```
6.11.3.5 real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j1 [private]
```

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

Definition at line 42 of file rk2_tl_ad_integrator.f90.

```
42 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: buf_j1 !< Buffer to hold jacobians in the RK4 scheme for the tangent linear model
```

```
6.11.3.6 real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j1h [private]
```

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

Definition at line 44 of file rk2_tl_ad_integrator.f90.

```
44 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: buf_j1h !< Buffer to hold jacobians in the RK4 scheme for the tangent linear model
```

```
6.11.3.7 real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j2 [private]
```

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

Definition at line 43 of file rk2 tl ad integrator.f90.

```
43 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: buf_j2 !< Buffer to hold jacobians in the RK4 scheme for the tangent linear model
```

```
6.11.3.8 real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j2h [private]
```

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

Definition at line 45 of file rk2 tl ad integrator.f90.

```
45 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: buf_j2h !< Buffer to hold jacobians in the RK4 scheme for the tangent linear model
```

```
6.11.3.9 real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j3 [private]
```

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

Definition at line 42 of file rk4_tl_ad_integrator.f90.

```
42 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: buf_j3 !< Buffer to hold jacobians in the RK4 scheme for the tangent linear model
```

```
6.11.3.10 real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j3h [private]
```

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

Definition at line 46 of file rk4 tl ad integrator.f90.

```
46 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: buf_j3h !< Buffer to hold jacobians in the RK4 scheme for the tangent linear model
```

```
6.11.3.11 real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_i4 [private]
```

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

Definition at line 43 of file rk4 tl ad integrator.f90.

```
43 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: buf_j4 !< Buffer to hold jacobians in the RK4 scheme for the tangent linear model
```

```
6.11.3.12 real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_i4h [private]
```

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

Definition at line 47 of file rk4 tl ad integrator.f90.

```
47 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: buf_j4h !< Buffer to hold jacobians in the RK4 scheme for the tangent linear model
```

```
6.11.3.13 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_ka [private]
```

Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

Definition at line 35 of file rk4 tl ad integrator.f90.

```
35 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_ka !< Buffer to hold tendencies in the RK4 scheme for the tangent linear model
```

```
6.11.3.14 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_kaa [private]
```

Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

Definition at line 48 of file rk4_tl_ad_integrator.f90.

```
48 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_kaa !< Buffer to hold tendencies in the RK4 scheme for the tangent linear model
```

```
6.11.3.15 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_kb [private]
```

Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

Definition at line 36 of file rk4 tl ad integrator.f90.

```
36 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_kb !< Buffer to hold tendencies in the RK4 scheme for the tangent linear model
```

```
6.11.3.16 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_kbb [private]
```

Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

Definition at line 49 of file rk4 tl ad integrator.f90.

```
49 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_kbb !< Buffer to hold tendencies in the RK4 scheme for the tangent linear model
```

```
6.11.3.17 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_kc [private]
```

Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

Definition at line 38 of file rk4_tl_ad_integrator.f90.

```
38 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_kc !< Buffer to hold tendencies in the RK4 scheme for the tangent linear model
```

```
6.11.3.18 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_kd [private]
```

Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

Definition at line 39 of file rk4 tl ad integrator.f90.

```
39 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_kd !< Buffer to hold tendencies in the RK4 scheme for the tangent linear model
```

```
6.11.3.19 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_y1 [private]
```

Buffer to hold the intermediate position (Heun algorithm) of the tangent linear model.

Buffer to hold the intermediate position of the tangent linear model.

Definition at line 34 of file rk2_tl_ad_integrator.f90.

```
34 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_y1 !< Buffer to hold the intermediate position (Heun algorithm) of the tangent linear model
```

```
6.11.3.20 real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_y11 [private]
```

Buffer to hold the intermediate position (Heun algorithm) of the tangent linear model.

Buffer to hold the intermediate position of the tangent linear model.

Definition at line 38 of file rk2_tl_ad_integrator.f90.

```
38 REAL(KIND=8), DIMENSION(:), ALLOCATABLE :: buf_y11 !< Buffer to hold the intermediate position (Heun algorithm) of the tangent linear model
```

```
6.11.3.21 real(kind=8), dimension(:,:), allocatable tl_ad_integrator::one [private]
```

unit matrix

Definition at line 46 of file rk2_tl_ad_integrator.f90.

```
46 REAL(KIND=8), DIMENSION(:,:), ALLOCATABLE :: one !< unit matrix
```

6.12 tl_ad_tensor Module Reference

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Tensors definition module.

Functions/Subroutines

type(coolist) function, dimension(ndim) jacobian (ystar)

Compute the Jacobian of MAOOAM in point ystar.

real(kind=8) function, dimension(ndim, ndim), public jacobian_mat (ystar)

Compute the Jacobian of MAOOAM in point ystar.

· subroutine, public init tltensor

Routine to initialize the TL tensor.

subroutine compute_tltensor (func)

Routine to compute the TL tensor from the original MAOOAM one.

• subroutine tl_add_count (i, j, k, v)

Subroutine used to count the number of TL tensor entries.

subroutine tl_coeff (i, j, k, v)

Subroutine used to compute the TL tensor entries.

· subroutine, public init_adtensor

Routine to initialize the AD tensor.

• subroutine compute_adtensor (func)

Subroutine to compute the AD tensor from the original MAOOAM one.

subroutine ad_add_count (i, j, k, v)

Subroutine used to count the number of AD tensor entries.

- subroutine ad_coeff (i, j, k, v)
- subroutine, public init_adtensor_ref

Alternate method to initialize the AD tensor from the TL tensor.

• subroutine compute_adtensor_ref (func)

Alternate subroutine to compute the AD tensor from the TL one.

• subroutine ad_add_count_ref (i, j, k, v)

Alternate subroutine used to count the number of AD tensor entries from the TL tensor.

• subroutine ad_coeff_ref (i, j, k, v)

Alternate subroutine used to compute the AD tensor entries from the TL tensor.

subroutine, public ad (t, ystar, deltay, buf)

Tendencies for the AD of MAOOAM in point ystar for perturbation deltay.

• subroutine, public tl (t, ystar, deltay, buf)

Tendencies for the TL of MAOOAM in point ystar for perturbation deltay.

Variables

• real(kind=8), parameter real_eps = 2.2204460492503131e-16

Epsilon to test equality with 0.

• integer, dimension(:), allocatable count_elems

Vector used to count the tensor elements.

• type(coolist), dimension(:), allocatable, public tltensor

Tensor representation of the Tangent Linear tendencies.

type(coolist), dimension(:), allocatable, public adtensor

Tensor representation of the Adjoint tendencies.

6.12.1 Detailed Description

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Tensors definition module.

Copyright

2016 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Remarks

The routines of this module should be called only after params::init_params() and aotensor_def::init_ aotensor() have been called !

6.12.2 Function/Subroutine Documentation

6.12.2.1 subroutine, public tl_ad_tensor::ad (real(kind=8), intent(in) t, real(kind=8), dimension(0:ndim), intent(in) ystar, real(kind=8), dimension(0:ndim), intent(in) deltay, real(kind=8), dimension(0:ndim), intent(out) buf)

Tendencies for the AD of MAOOAM in point ystar for perturbation deltay.

Parameters

t	time
ystar	vector with the variables (current point in trajectory)
deltay	vector with the perturbation of the variables at time t
buf	vector (buffer) to store derivatives.

Definition at line 384 of file tl_ad_tensor.f90.

```
REAL(KIND=8), INTENT(IN) :: t
REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: ystar,deltay
REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: buf
CALL sparse_mul3(adtensor,deltay,ystar,buf)
```

6.12.2.2 subroutine tl_ad_tensor::ad_add_count (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v) [private]

Subroutine used to count the number of AD tensor entries.

Parameters

i	tensor i index
j	tensor j index
k	tensor k index
V	value that will be added

Definition at line 243 of file tl_ad_tensor.f90.

```
243 INTEGER, INTENT(IN) :: i,j,k
244 REAL(KIND=8), INTENT(IN) :: v
245 IF ((abs(v) .ge. real_eps).AND.(i /= 0)) THEN
246 IF (k /= 0) count_elems(k) = count_elems(k) + 1
247 IF (j /= 0) count_elems(j) = count_elems(j) + 1
248 ENDIF
```

6.12.2.3 subroutine tl_ad_tensor::ad_add_count_ref (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v) [private]

Alternate subroutine used to count the number of AD tensor entries from the TL tensor.

Parameters

i	tensor i index
j	tensor j index
k	tensor k index
V	value that will be added

Definition at line 346 of file tl_ad_tensor.f90.

6.12.2.4 subroutine tl_ad_tensor::ad_coeff (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v) [private]

Parameters

i	tensor i index
j	$tensor\ j \ index$
k	tensor k index
V	value to add

Definition at line 257 of file tl_ad_tensor.f90.

```
INTEGER, INTENT(IN) :: i,j,k
258
         REAL(KIND=8), INTENT(IN) :: v
259
         INTEGER :: n
        IF (.NOT. ALLOCATED(adtensor)) stop "*** ad_coeff routine : tensor not yet allocated ***" IF ((abs(v) .ge. real_eps).AND.(i /=0)) THEN IF (k /=0) THEN
260
261
262
263
               IF (.NOT. ALLOCATED(adtensor(k)%elems)) stop "*** ad_coeff routine : tensor not yet allocated
264
               n=(adtensor(k)%nelems)+1
265
               adtensor(k)%elems(n)%j=i
               adtensor(k)%elems(n)%k=i
266
267
               adtensor(k)%elems(n)%v=v
268
               adtensor(k)%nelems=n
269
            END IF
270
            IF (j /=0) THEN
271
               IF (.NOT. ALLOCATED(adtensor(j)%elems)) stop "*** ad_coeff routine : tensor not yet allocated
272
               n=(adtensor(i)%nelems)+1
273
               adtensor(j)%elems(n)%j=i
               adtensor(j)%elems(n)%k=k
```

```
275 adtensor(j)%elems(n)%v=v
276 adtensor(j)%nelems=n
277 END IF
278 END IF
```

6.12.2.5 subroutine tl_ad_tensor::ad_coeff_ref (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v) [private]

Alternate subroutine used to compute the AD tensor entries from the TL tensor.

Parameters

i	tensor i index
j	$tensor\ j \ index$
k	tensor k index
V	value to add

Definition at line 358 of file tl_ad_tensor.f90.

```
INTEGER, INTENT(IN) :: i,j,k
359
     REAL(KIND=8), INTENT(IN) :: v
360
     INTEGER :: n
    361
362
363
364
       n=(adtensor(j)%nelems)+1
365
       adtensor(j)%elems(n)%j=i
366
       \texttt{adtensor(j)\$elems(n)\$k=k}
367
       adtensor(j)%elems(n)%v=v
368
       adtensor(j)%nelems=n
369
```

6.12.2.6 subroutine tl_ad_tensor::compute_adtensor(external *func*) [private]

Subroutine to compute the AD tensor from the original MAOOAM one.

Parameters

func | subroutine used to do the computation

Definition at line 217 of file tl_ad_tensor.f90.

6.12.2.7 subroutine tl_ad_tensor::compute_adtensor_ref(external *func*) [private]

Alternate subroutine to compute the AD tensor from the TL one.

Parameters

func subroutine used to do the computation

Definition at line 318 of file tl_ad_tensor.f90.

```
6.12.2.8 subroutine tl_ad_tensor::compute_tltensor( external func ) [private]
```

Routine to compute the TL tensor from the original MAOOAM one.

Parameters

```
func subroutine used to do the computation
```

Definition at line 121 of file tl_ad_tensor.f90.

```
6.12.2.9 subroutine, public tl_ad_tensor::init_adtensor()
```

Routine to initialize the AD tensor.

Definition at line 193 of file tl_ad_tensor.f90.

```
193
          INTEGER :: i
194
          INTEGER :: allocstat
         ALLOCATE(adtensor(ndim),count_elems(ndim), stat=allocstat)

IF (allocstat /= 0) stop "*** Not enough memory! ***"
195
196
197
         count_elems=0
198
         CALL compute_adtensor(ad_add_count)
199
200
         DO i=1, ndim
            ALLOCATE(adtensor(i)%elems(count_elems(i)), stat=allocstat)
201
             IF (allocstat /= 0) stop "*** Not enough memory! ***
202
203
204
         DEALLOCATE(count_elems, stat=allocstat)
IF (allocstat /= 0) stop "*** Deallocation problem ! ***"
205
206
207
208
         CALL compute adtensor (ad coeff)
209
210
         CALL simplify(adtensor)
```

6.12.2.10 subroutine, public tl_ad_tensor::init_adtensor_ref()

Alternate method to initialize the AD tensor from the TL tensor.

Remarks

The tltensor must be initialised before using this method.

Definition at line 294 of file tl_ad_tensor.f90.

```
294
         INTEGER :: i
295
          INTEGER :: allocstat
         ALLOCATE(adtensor(ndim),count_elems(ndim), stat=allocstat)

IF (allocstat /= 0) stop "*** Not enough memory! ***"
296
297
298
         count_elems=0
299
         CALL compute_adtensor_ref(ad_add_count_ref)
300
         DO i=1,ndim
301
302
            ALLOCATE(adtensor(i)%elems(count_elems(i)), stat=allocstat)
303
             IF (allocstat /= 0) stop "*** Not enough memory ! ***"
304
305
         DEALLOCATE(count_elems, stat=allocstat)
IF (allocstat /= 0) stop "*** Deallocation problem ! ***"
306
307
308
309
         CALL compute_adtensor_ref(ad_coeff_ref)
310
311
         CALL simplify(adtensor)
312
```

6.12.2.11 subroutine, public tl_ad_tensor::init_tltensor()

Routine to initialize the TL tensor.

Definition at line 97 of file tl ad tensor.f90.

```
INTEGER :: i
98
       INTEGER :: allocstat
99
       ALLOCATE(tltensor(ndim),count_elems(ndim), stat=allocstat)
100
       IF (allocstat /= 0) stop "*** Not enough memory ! ***
101
       count_elems=0
       CALL compute_tltensor(tl_add_count)
102
103
104
105
          ALLOCATE(tltensor(i)%elems(count_elems(i)), stat=allocstat)
106
          IF (allocstat /= 0) stop "*** Not enough memory ! ***"
107
108
109
       DEALLOCATE(count_elems, stat=allocstat)
110
       IF (allocstat /= 0) stop "*** Deallocation problem ! ***"
111
112
       CALL compute_tltensor(tl_coeff)
113
       CALL simplify(tltensor)
114
115
```

6.12.2.12 type(coolist) function, dimension(ndim) tl_ad_tensor::jacobian (real(kind=8), dimension(0:ndim), intent(in) ystar)

[private]

Compute the Jacobian of MAOOAM in point ystar.

Parameters

ystar array with variables in which the jacobian should be evaluated.

Returns

Jacobian in coolist-form (table of tuples {i,j,0,value})

Definition at line 75 of file tl_ad_tensor.f90.

```
75 REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: ystar
76 TYPE(coolist), DIMENSION(ndim) :: jacobian
77 CALL jsparse_mul(aotensor,ystar,jacobian)
```

6.12.2.13 real(kind=8) function, dimension(ndim,ndim), public tl_ad_tensor::jacobian_mat (real(kind=8), dimension(0:ndim), intent(in) ystar)

Compute the Jacobian of MAOOAM in point ystar.

Parameters

ystar array with variables in which the jacobian should be evaluated.

Returns

Jacobian in matrix form

Definition at line 84 of file tl ad tensor.f90.

```
REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: ystar
REAL(KIND=8), DIMENSION(ndim,ndim) :: jacobian_mat
CALL jsparse_mul_mat(aotensor,ystar,jacobian_mat)
```

6.12.2.14 subroutine, public tl_ad_tensor::tl (real(kind=8), intent(in) t, real(kind=8), dimension(0:ndim), intent(in) ystar, real(kind=8), dimension(0:ndim), intent(out) buf)

Tendencies for the TL of MAOOAM in point ystar for perturbation deltay.

Parameters

t	time
ystar	vector with the variables (current point in trajectory)
deltay	vector with the perturbation of the variables at time t
buf	vector (buffer) to store derivatives.

Definition at line 396 of file tl_ad_tensor.f90.

```
396 REAL(KIND=8), INTENT(IN) :: t
397 REAL(KIND=8), DIMENSION(0:ndim), INTENT(IN) :: ystar,deltay
398 REAL(KIND=8), DIMENSION(0:ndim), INTENT(OUT) :: buf
399 CALL sparse_mul3(tltensor,deltay,ystar,buf)
```

6.12.2.15 subroutine tl_ad_tensor::tl_add_count (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v) [private]

Subroutine used to count the number of TL tensor entries.

Parameters

i	tensor i index
j	tensor j index
k	tensor k index
V	value that will be added

Definition at line 147 of file tl_ad_tensor.f90.

6.12.2.16 subroutine tl_ad_tensor::tl_coeff (integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v) [private]

Subroutine used to compute the TL tensor entries.

Parameters

i	tensor i index
j	$tensor\ j \ index$
k	tensor k index
V	value to add

Definition at line 161 of file tl_ad_tensor.f90.

```
INTEGER, INTENT(IN) :: i,j,k
162
       REAL(KIND=8), INTENT(IN) :: v
163
        INTEGER :: n
        IF (.NOT. ALLOCATED(tltensor)) stop "*** tl_coeff routine : tensor not yet allocated ***"
164
       IF (.NOT. ALLOCATED(tltensor(i)%elems)) stop "*** tl_coeff routine : tensor not yet allocated ***"
165
       IF (abs(v) .ge. real_eps) THEN
IF (j /=0) THEN
166
167
168
             n=(tltensor(i)%nelems)+1
169
             tltensor(i)%elems(n)%j=j
170
             tltensor(i)%elems(n)%k=k
171
             tltensor(i)%elems(n)%v=v
172
             tltensor(i)%nelems=n
173
174
         IF (k /=0) THEN
175
             n=(tltensor(i)%nelems)+1
176
             tltensor(i)%elems(n)%j=k
177
             tltensor(i)%elems(n)%k=i
178
             tltensor(i)%elems(n)%v=v
179
             tltensor(i)%nelems=n
       END IF
181
```

6.12.3 Variable Documentation

6.12.3.1 type(coolist), dimension(:), allocatable, public tl_ad_tensor::adtensor

Tensor representation of the Adjoint tendencies.

Definition at line 44 of file tl ad tensor.f90.

```
44 TYPE(coolist), DIMENSION(:), ALLOCATABLE, PUBLIC :: adtensor
```

6.12.3.2 integer, dimension(:), allocatable tl_ad_tensor::count_elems [private]

Vector used to count the tensor elements.

Definition at line 38 of file tl_ad_tensor.f90.

```
38 INTEGER, DIMENSION(:), ALLOCATABLE :: count_elems
```

6.12.3.3 real(kind=8), parameter tl_ad_tensor::real_eps = 2.2204460492503131e-16 [private]

Epsilon to test equality with 0.

Definition at line 35 of file tl ad tensor.f90.

```
REAL(KIND=8), PARAMETER :: real_eps = 2.2204460492503131e-16
```

6.12.3.4 type(coolist), dimension(:), allocatable, public tl_ad_tensor::tltensor

Tensor representation of the Tangent Linear tendencies.

Definition at line 41 of file tl_ad_tensor.f90.

```
TYPE(coolist), DIMENSION(:), ALLOCATABLE, PUBLIC :: tltensor
```

6.13 util Module Reference

Utility module.

Functions/Subroutines

• character(len=20) function, public str (k)

Convert an integer to string.

• character(len=40) function, public rstr (x, fm)

Convert a real to string with a given format.

• integer function, dimension(size(s)), public isin (c, s)

Determine if a character is in a string and where.

• subroutine, public init_random_seed ()

Random generator initialization routine.

• subroutine, public piksrt (k, arr, par)

Simple card player sorting function.

• subroutine, public init_one (A)

Initialize a square matrix A as a unit matrix.

6.13.1 Detailed Description

Utility module.

Copyright

2018 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

6.13 util Module Reference 91

6.13.2 Function/Subroutine Documentation

6.13.2.1 subroutine, public util::init_one (real(kind=8), dimension(:,:), intent(inout) \emph{A})

Initialize a square matrix A as a unit matrix.

Definition at line 137 of file util.f90.

```
137 REAL(KIND=8), DIMENSION(:,:),INTENT(INOUT) :: a
138 INTEGER :: i,n
139 n=size(a,1)
140 a=0.0d0
141 DO i=1,n
142 a(i,i)=1.0d0
143 END DO
144
```

6.13.2.2 subroutine, public util::init_random_seed ()

Random generator initialization routine.

Definition at line 62 of file util.f90.

6.13.2.3 integer function, dimension(size(s)), public util::isin (character, intent(in) c, character, dimension(:), intent(in) s)

Determine if a character is in a string and where.

Remarks

: return positions in a vector if found and 0 vector if not found

Definition at line 45 of file util.f90.

```
45
       CHARACTER, INTENT(IN) :: c
46
       CHARACTER, DIMENSION(:), INTENT(IN) :: s
47
       INTEGER, DIMENSION(size(s)) :: isin
48
       INTEGER :: i,j
49
       isin=0
52
       DO i=size(s),1,-1
          IF (c==s(i)) THEN
    j=j+1
    isin(j)=i
53
54
55
          END IF
       END DO
```

6.13.2.4 subroutine, public util::piksrt (integer, intent(in) k, integer, dimension(k), intent(inout) arr, integer, intent(out) par)

Simple card player sorting function.

Definition at line 116 of file util.f90.

```
INTEGER, INTENT(IN) :: k
INTEGER, DIMENSION(k), INTENT(INOUT) :: arr
116
117
         INTEGER, INTENT(OUT) :: par
118
        INTEGER :: i,j,a,b
119
120
121
        par=1
122
        DO i=2.k
123
124
           a=arr(j)
125
            DO i=j-1,1,-1
126
               if(arr(i).le.a) EXIT
127
                arr(i+1) = arr(i)
            par=-par
END DO
128
129
            arr(i+1)=a
130
131
132
        RETURN
```

6.13.2.5 character(len=40) function, public util::rstr (real(kind=8), intent(in) x, character(len=20), intent(in) fm)

Convert a real to string with a given format.

Definition at line 36 of file util.f90.

```
36 REAL(KIND=8), INTENT(IN) :: x
37 CHARACTER(len=20), INTENT(IN) :: fm
38 WRITE (rstr, trim(adjustl(fm))) x
39 rstr = adjustl(rstr)
```

6.13.2.6 character(len=20) function, public util::str (integer, intent(in) k)

Convert an integer to string.

Definition at line 29 of file util.f90.

```
29 INTEGER, INTENT(IN) :: k
30 WRITE (str, *) k
31 str = adjust1(str)
```

Chapter 7

Data Type Documentation

7.1 inprod_analytic::atm_tensors Type Reference

Type holding the atmospheric inner products tensors.

Private Attributes

- procedure(calculate_a), pointer, nopass a
- procedure(calculate_b), pointer, nopass b
- procedure(calculate_c_atm), pointer, nopass c
- procedure(calculate_d), pointer, nopass d
- procedure(calculate_g), pointer, nopass g
- procedure(calculate_s), pointer, nopass s

7.1.1 Detailed Description

Type holding the atmospheric inner products tensors.

Definition at line 53 of file inprod_analytic.f90.

7.1.2 Member Data Documentation

7.1.2.1 procedure(calculate_a), pointer, nopass inprod_analytic::atm_tensors::a [private]

Definition at line 54 of file inprod_analytic.f90.

```
PROCEDURE (calculate_a), POINTER, NOPASS :: a
```

7.1.2.2 procedure(calculate_b), pointer, nopass inprod_analytic::atm_tensors::b [private]

Definition at line 55 of file inprod_analytic.f90.

```
55 PROCEDURE(calculate_b), POINTER, NOPASS :: b
```

7.1.2.3 procedure(calculate_c_atm), pointer, nopass inprod_analytic::atm_tensors::c [private]

Definition at line 56 of file inprod_analytic.f90.

```
PROCEDURE (calculate_c_atm), POINTER, NOPASS :: c
```

7.1.2.4 procedure(calculate_d), pointer, nopass inprod_analytic::atm_tensors::d [private]

Definition at line 57 of file inprod_analytic.f90.

```
57 PROCEDURE (calculate_d), POINTER, NOPASS :: d
```

7.1.2.5 procedure(calculate_g), pointer, nopass inprod_analytic::atm_tensors::g [private]

Definition at line 58 of file inprod_analytic.f90.

```
58 PROCEDURE(calculate_g), POINTER, NOPASS :: g
```

7.1.2.6 procedure(calculate_s), pointer, nopass inprod_analytic::atm_tensors::s [private]

Definition at line 59 of file inprod_analytic.f90.

```
59 PROCEDURE (calculate_s), POINTER, NOPASS :: s
```

The documentation for this type was generated from the following file:

• inprod_analytic.f90

7.2 inprod_analytic::atm_wavenum Type Reference

Atmospheric bloc specification type.

Private Attributes

- character typ
- integer m =0
- integer p =0
- integer h =0
- real(kind=8) nx =0.
- real(kind=8) ny =0.

7.2.1 Detailed Description

Atmospheric bloc specification type.

Definition at line 40 of file inprod_analytic.f90.

7.2.2 Member Data Documentation

7.2.2.1 integer inprod_analytic::atm_wavenum::h =0 [private]

Definition at line 42 of file inprod_analytic.f90.

7.2.2.2 integer inprod_analytic::atm_wavenum::m =0 [private]

Definition at line 42 of file inprod_analytic.f90.

```
42 INTEGER :: m=0, p=0, h=0
```

7.2.2.3 real(kind=8) inprod_analytic::atm_wavenum::nx =0. [private]

Definition at line 43 of file inprod_analytic.f90.

```
43 REAL(KIND=8) :: nx=0., ny=0.
```

7.2.2.4 real(kind=8) inprod_analytic::atm_wavenum::ny =0. [private]

Definition at line 43 of file inprod_analytic.f90.

7.2.2.5 integer inprod_analytic::atm_wavenum::p = 0 [private]

Definition at line 42 of file inprod_analytic.f90.

7.2.2.6 character inprod_analytic::atm_wavenum::typ [private]

Definition at line 41 of file inprod_analytic.f90.

```
41 CHARACTER :: typ
```

The documentation for this type was generated from the following file:

inprod_analytic.f90

7.3 tensor::coolist Type Reference

Coordinate list. Type used to represent the sparse tensor.

Public Attributes

- type(coolist_elem), dimension(:), allocatable elems
 Lists of elements tensor::coolist_elem.
- integer nelems = 0

Number of elements in the list.

7.3.1 Detailed Description

Coordinate list. Type used to represent the sparse tensor.

Definition at line 27 of file tensor.f90.

7.3.2 Member Data Documentation

7.3.2.1 type(coolist_elem), dimension(:), allocatable tensor::coolist::elems

Lists of elements tensor::coolist_elem.

Definition at line 28 of file tensor.f90.

```
TYPE(coolist_elem), DIMENSION(:), ALLOCATABLE :: elems !< Lists of elements tensor::coolist_elem
```

7.3.2.2 integer tensor::coolist::nelems = 0

Number of elements in the list.

Definition at line 29 of file tensor.f90.

```
29 INTEGER :: nelems = 0 !< Number of elements in the list.
```

The documentation for this type was generated from the following file:

• tensor.f90

7.4 tensor::coolist_elem Type Reference

Coordinate list element type. Elementary elements of the sparse tensors.

Private Attributes

integer j

Index j of the element.

integer k

Index k of the element.

• real(kind=8) v

Value of the element.

7.4.1 Detailed Description

Coordinate list element type. Elementary elements of the sparse tensors.

Definition at line 20 of file tensor.f90.

7.4.2 Member Data Documentation

```
7.4.2.1 integer tensor::coolist_elem::j [private]
```

Index j of the element.

Definition at line 21 of file tensor.f90.

```
21 INTEGER :: j !< Index f of the element
```

7.4.2.2 integer tensor::coolist_elem::k [private]

Index k of the element.

Definition at line 22 of file tensor.f90.

```
22 INTEGER :: k < Index f of the element
```

7.4.2.3 real(kind=8) tensor::coolist_elem::v [private]

Value of the element.

Definition at line 23 of file tensor.f90.

```
23 REAL(KIND=8) :: v !< Value of the element
```

The documentation for this type was generated from the following file:

• tensor.f90

7.5 inprod_analytic::ocean_tensors Type Reference

Type holding the oceanic inner products tensors.

Private Attributes

- procedure(calculate_k), pointer, nopass k
- procedure(calculate_m), pointer, nopass m
- procedure(calculate_c_oc), pointer, nopass c
- procedure(calculate_n), pointer, nopass n
- procedure(calculate_o), pointer, nopass o
- procedure(calculate_w), pointer, nopass w

7.5.1 Detailed Description

Type holding the oceanic inner products tensors.

Definition at line 63 of file inprod_analytic.f90.

7.5.2 Member Data Documentation

7.5.2.1 procedure(calculate_c_oc), pointer, nopass inprod_analytic::ocean_tensors::c [private]

Definition at line 66 of file inprod_analytic.f90.

```
PROCEDURE (calculate_c_oc), POINTER, NOPASS :: c
```

7.5.2.2 procedure(calculate_k), pointer, nopass inprod_analytic::ocean_tensors::k [private]

Definition at line 64 of file inprod analytic.f90.

```
PROCEDURE(calculate_k), POINTER, NOPASS :: k
```

7.5.2.3 procedure(calculate_m), pointer, nopass inprod_analytic::ocean_tensors::m [private]

Definition at line 65 of file inprod analytic.f90.

```
PROCEDURE (calculate_m), POINTER, NOPASS :: m
```

7.5.2.4 procedure(calculate_n), pointer, nopass inprod_analytic::ocean_tensors::n [private]

Definition at line 67 of file inprod_analytic.f90.

```
PROCEDURE (calculate_n), POINTER, NOPASS :: n
```

7.5.2.5 procedure(calculate_o), pointer, nopass inprod_analytic::ocean_tensors::o [private]

Definition at line 68 of file inprod_analytic.f90.

```
68 PROCEDURE (calculate_o), POINTER, NOPASS :: o
```

7.5.2.6 procedure(calculate_w), pointer, nopass inprod_analytic::ocean_tensors::w [private]

Definition at line 69 of file inprod_analytic.f90.

```
69 PROCEDURE (calculate_w), POINTER, NOPASS :: w
```

The documentation for this type was generated from the following file:

• inprod_analytic.f90

7.6 inprod_analytic::ocean_wavenum Type Reference

Oceanic bloc specification type.

Private Attributes

- integer p
- integer h
- real(kind=8) nx
- real(kind=8) ny

7.6.1 Detailed Description

Oceanic bloc specification type.

Definition at line 47 of file inprod_analytic.f90.

7.6.2 Member Data Documentation

```
7.6.2.1 integer inprod_analytic::ocean_wavenum::h [private]
```

Definition at line 48 of file inprod analytic.f90.

```
7.6.2.2 real(kind=8) inprod_analytic::ocean_wavenum::nx [private]
```

Definition at line 49 of file inprod_analytic.f90.

```
49 REAL(KIND=8) :: nx,ny
```

```
7.6.2.3 real(kind=8) inprod_analytic::ocean_wavenum::ny [private]
```

Definition at line 49 of file inprod_analytic.f90.

```
7.6.2.4 integer inprod_analytic::ocean_wavenum::p [private]
```

Definition at line 48 of file inprod_analytic.f90.

```
48 INTEGER :: p,h
```

The documentation for this type was generated from the following file:

• inprod_analytic.f90

Chapter 8

File Documentation

8.1 aotensor_def.f90 File Reference

Modules

· module aotensor_def

The equation tensor for the coupled ocean-atmosphere model with temperature which allows for an extensible set of modes in the ocean and in the atmosphere.

Functions/Subroutines

• integer function aotensor_def::psi (i)

Translate the $\psi_{a,i}$ coefficients into effective coordinates.

• integer function aotensor_def::theta (i)

Translate the $\theta_{a,i}$ coefficients into effective coordinates.

• integer function aotensor_def::a (i)

Translate the $\psi_{o,i}$ coefficients into effective coordinates.

• integer function aotensor_def::t (i)

Translate the $\delta T_{o,i}$ coefficients into effective coordinates.

• integer function aotensor_def::kdelta (i, j)

Kronecker delta function.

• subroutine $aotensor_def::coeff(i, j, k, v)$

Subroutine to add element in the aotensor $\mathcal{T}_{i,j,k}$ structure.

• subroutine aotensor_def::add_count (i, j, k, v)

Subroutine to count the elements of the aotensor $\mathcal{T}_{i,j,k}$. Add +1 to count_elems(i) for each value that is added to the tensor i-th component.

subroutine aotensor_def::compute_aotensor (func)

Subroutine to compute the tensor aotensor.

• subroutine, public aotensor def::init aotensor

Subroutine to initialise the aotensor tensor.

Variables

• integer, dimension(:), allocatable aotensor_def::count_elems

Vector used to count the tensor elements.

real(kind=8), parameter aotensor_def::real_eps = 2.2204460492503131e-16
 Epsilon to test equality with 0.

• type(coolist), dimension(:), allocatable, public aotensor_def::aotensor

 $\mathcal{T}_{i,j,k}$ - Tensor representation of the tendencies.

8.2 doc/gen_doc.md File Reference

8.3 doc/tl_ad_doc.md File Reference

8.4 ic_def.f90 File Reference

Modules

• module ic_def

Module to load the initial condition.

Functions/Subroutines

• subroutine, public ic_def::load_ic

Subroutine to load the initial condition if IC.nml exists. If it does not, then write IC.nml with 0 as initial condition.

Variables

logical ic_def::exists

Boolean to test for file existence.

• real(kind=8), dimension(:), allocatable, public ic_def::ic

Initial condition vector.

8.5 icdelta_def.f90 File Reference

Modules

• module icdelta_def

Module to load the perturbation initial condition.

Functions/Subroutines

• subroutine, public icdelta_def::load_icdelta

Subroutine to load the initial condition if ICdelta.nml exists. If it does not, then write ICdelta.nml with random initial condition.

Variables

· logical icdelta_def::exists

Boolean to test for file existence.

• real(kind=8), dimension(:), allocatable, public icdelta_def::icdelta

Initial condition vector.

8.6 inprod_analytic.f90 File Reference

Data Types

· type inprod analytic::atm wavenum

Atmospheric bloc specification type.

· type inprod analytic::ocean wavenum

Oceanic bloc specification type.

type inprod_analytic::atm_tensors

Type holding the atmospheric inner products tensors.

type inprod_analytic::ocean_tensors

Type holding the oceanic inner products tensors.

Modules

• module inprod_analytic

Inner products between the truncated set of basis functions for the ocean and atmosphere streamfunction fields. These are partly calculated using the analytical expressions from Cehelsky, P., & Tung, K. K.: Theories of multiple equilibria and weather regimes-A critical reexamination. Part II: Baroclinic two-layer models. Journal of the atmospheric sciences, 44(21), 3282-3303, 1987.

Functions/Subroutines

real(kind=8) function inprod_analytic::b1 (Pi, Pj, Pk)

Cehelsky & Tung Helper functions.

• real(kind=8) function inprod_analytic::b2 (Pi, Pj, Pk)

Cehelsky & Tung Helper functions.

• real(kind=8) function inprod_analytic::delta (r)

Integer Dirac delta function.

• real(kind=8) function inprod_analytic::flambda (r)

"Odd or even" function

• real(kind=8) function inprod_analytic::s1 (Pj, Pk, Mj, Hk)

Cehelsky & Tung Helper functions.

real(kind=8) function inprod_analytic::s2 (Pj, Pk, Mj, Hk)

Cehelsky & Tung Helper functions.

real(kind=8) function inprod analytic::s3 (Pj, Pk, Hj, Hk)

Cehelsky & Tung Helper functions.

real(kind=8) function inprod_analytic::s4 (Pj, Pk, Hj, Hk)

Cehelsky & Tung Helper functions.

• real(kind=8) function inprod_analytic::calculate_a (i, j)

Eigenvalues of the Laplacian (atmospheric)

- real(kind=8) function inprod_analytic::calculate_b (i, j, k)
 Streamfunction advection terms (atmospheric)

 real(kind=8) function inprod_analytic::calculate_c_atm (i, j)
- Beta term for the atmosphere.

• real(kind=8) function inprod_analytic::calculate_d (i, j)

Forcing of the ocean on the atmosphere.

• real(kind=8) function inprod_analytic::calculate_g (i, j, k)

Temperature advection terms (atmospheric)

real(kind=8) function inprod analytic::calculate s (i, j)

Forcing (thermal) of the ocean on the atmosphere.

• real(kind=8) function inprod_analytic::calculate_k (i, j)

Forcing of the atmosphere on the ocean.

• real(kind=8) function inprod_analytic::calculate_m (i, j)

Forcing of the ocean fields on the ocean.

 $\bullet \ \ real(kind=8) \ function \ inprod_analytic::calculate_n \ (i, j) \\$

Beta term for the ocean.

• real(kind=8) function inprod_analytic::calculate_o (i, j, k)

Temperature advection term (passive scalar)

real(kind=8) function inprod_analytic::calculate_c_oc (i, j, k)

Streamfunction advection terms (oceanic)

• real(kind=8) function inprod analytic::calculate w (i, j)

Short-wave radiative forcing of the ocean.

· subroutine, public inprod_analytic::init_inprod

Initialisation of the inner product.

Variables

- type(atm_wavenum), dimension(:), allocatable, public inprod_analytic::awavenum
 Atmospheric blocs specification.
- type(ocean_wavenum), dimension(:), allocatable, public inprod_analytic::owavenum
 Oceanic blocs specification.
- type(atm_tensors), public inprod_analytic::atmos

Atmospheric tensors.

• type(ocean_tensors), public inprod_analytic::ocean

Oceanic tensors.

8.7 LICENSE.txt File Reference

Functions

- The MIT License (MIT) Copyright(c) 2015-2016 Lesley De Cruz
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation files (the "Software")

Variables

- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby granted
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of charge
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without restriction
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to use
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to copy
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to modify
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to merge
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to publish
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to distribute
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to sublicense
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the Software
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do so
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a
 copy of this software and associated documentation to deal in the Software without including without limitation
 the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject
 to the following conditions
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a
 copy of this software and associated documentation to deal in the Software without including without limitation
 the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject
 to the following WITHOUT WARRANTY OF ANY KIND
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a
 copy of this software and associated documentation to deal in the Software without including without limitation
 the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject
 to the following WITHOUT WARRANTY OF ANY EXPRESS OR IMPLIED
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a
 copy of this software and associated documentation to deal in the Software without including without limitation
 the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject
 to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE
 WARRANTIES OF MERCHANTABILITY
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a
 copy of this software and associated documentation to deal in the Software without including without limitation
 the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject
 to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE
 WARRANTIES OF FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT IN NO EVENT
 SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY CLAIM

The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a
copy of this software and associated documentation to deal in the Software without including without limitation
the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject
to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE
WARRANTIES OF FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT IN NO EVE

NT SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY DAMAGES OR OTHER
LIABILITY

- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a
 copy of this software and associated documentation to deal in the Software without including without limitation
 the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject
 to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE
 WARRANTIES OF FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT IN NO EVE

 NT SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY DAMAGES OR OTHER
 WHETHER IN AN ACTION OF CONTRACT
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a
 copy of this software and associated documentation to deal in the Software without including without limitation
 the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject
 to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE
 WARRANTIES OF FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT IN NO EVE
 NT SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY DAMAGES OR OTHER
 WHETHER IN AN ACTION OF TORT OR OTHERWISE
- The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a
 copy of this software and associated documentation to deal in the Software without including without limitation
 the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject
 to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE
 WARRANTIES OF FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT IN NO EVE

 NT SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY DAMAGES OR OTHER
 WHETHER IN AN ACTION OF TORT OR ARISING FROM

8.7.1 Function Documentation

- 8.7.1.1 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation files (the "Software")
- 8.7.1.2 The MIT License (MIT)
- 8.7.2 Variable Documentation
- 8.7.2.1 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of charge

Definition at line 6 of file LICENSE.txt.

8.7.2.2 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE WARRANTIES OF FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT IN NO EVENT SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY CLAIM

Definition at line 8 of file LICENSE.txt.

8.7.2.3 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject to the following conditions

Definition at line 8 of file LICENSE.txt.

8.7.2.4 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE WARRANTIES OF FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT IN NO EVENT SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY DAMAGES OR OTHER WHETHER IN AN ACTION OF CONTRACT

Definition at line 8 of file LICENSE.txt.

8.7.2.5 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to copy

Definition at line 8 of file LICENSE.txt.

8.7.2.6 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to distribute

Definition at line 8 of file LICENSE.txt.

8.7.2.7 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE WARRANTIES OF FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT IN NO EVENT SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY DAMAGES OR OTHER WHETHER IN AN ACTION OF TORT OR ARISING FROM

Definition at line 8 of file LICENSE.txt.

8.7.2.8 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby granted

Definition at line 6 of file LICENSE.txt.

8.7.2.9 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject to the following WITHOUT WARRANTY OF ANY EXPRESS OR IMPLIED

Definition at line 8 of file LICENSE.txt.

8.7.2.10 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject to the following WITHOUT WARRANTY OF ANY KIND

Definition at line 8 of file LICENSE.txt.

8.7.2.11 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE WARRANTIES OF FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT IN NO EVENT SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY DAMAGES OR OTHER LIABILITY

Definition at line 8 of file LICENSE.txt.

8.7.2.12 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE WARRANTIES OF MERCHANTABILITY

Definition at line 8 of file LICENSE.txt.

8.7.2.13 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to merge

Definition at line 8 of file LICENSE.txt.

8.7.2.14 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to modify

Definition at line 8 of file LICENSE.txt.

8.7.2.15 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do subject to the following WITHOUT WARRANTY OF ANY EXPRESS OR INCLUDING BUT NOT LIMITED TO THE WARRANTIES OF FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT IN NO EVENT SHALL THE AUTHORS OR COPYRIGHT HOLDERS BE LIABLE FOR ANY DAMAGES OR OTHER WHETHER IN AN ACTION OF TORT OR OTHERWISE

Definition at line 8 of file LICENSE.txt.

8.7.2.16 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to publish

Definition at line 8 of file LICENSE.txt.

8.7.2.17 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without restriction

Definition at line 8 of file LICENSE.txt.

8.7.2.18 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the and to permit persons to whom the Software is furnished to do so

Definition at line 8 of file LICENSE.txt.

8.7.2.19 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to and or sell copies of the Software

Definition at line 8 of file LICENSE.txt.

8.7.2.20 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to sublicense

Definition at line 8 of file LICENSE.txt.

8.7.2.21 The MIT Jonathan Demaeyer and Sebastian Schubert Permission is hereby free of to any person obtaining a copy of this software and associated documentation to deal in the Software without including without limitation the rights to use

Definition at line 8 of file LICENSE.txt.

8.8 lyap stat.f90 File Reference

Modules

· module lyap_stat

Statistics accumulators for the Lyapunov exponents.

Functions/Subroutines

• subroutine, public lyap_stat::lyap_init_stat

Initialise the accumulators.

subroutine, public lyap_stat::lyap_acc (x)

Accumulate one state.

• real(kind=8) function, dimension(0:ndim), public lyap_stat::lyap_mean ()

Function returning the mean.

• real(kind=8) function, dimension(0:ndim), public lyap_stat::lyap_var ()

Function returning the variance.

• integer function, public lyap_stat::lyap_iter ()

Function returning the number of data accumulated.

subroutine, public lyap_stat::lyap_reset

Routine resetting the accumulators.

Variables

• integer lyap stat::i =0

Number of stats accumulated.

real(kind=8), dimension(:), allocatable lyap_stat::m

Vector storing the inline mean.

• real(kind=8), dimension(:), allocatable lyap stat::mprev

Previous mean vector.

real(kind=8), dimension(:), allocatable lyap_stat::v

Vector storing the inline variance.

real(kind=8), dimension(:), allocatable lyap_stat::mtmp

8.9 lyap_vectors.f90 File Reference

Modules

module lyap vectors

Module for computation of Lyapunov exponents and vectors.

Functions/Subroutines

• subroutine, public lyap vectors::init lyap

Initialize Lyapunov computation (possibly also vectors in later version) and initializes also a random orthogonal matrix for the matrix ensemble.

subroutine, public lyap vectors::multiply prop (prop mul)

Multiplies prop_mul from the left with the prop matrix defined in this module and saves the result to prop_mul.

• subroutine, public lyap_vectors::benettin_step

Performs the benettin step in integration. Multiplies the aggregated propagators in prop with ensemble and performs QR decomposition (Gram-Schmidt orthogonalization gives Q and upper triangular matrix R). Computes also the Lyapunov exponents via the diagonal of R. WATCH OUT: prop is changed during the subroutine and restored to a unit matrix.

subroutine, public lyap_vectors::get_lyap_state (prop_ret, ensemble_ret)

Routine that returns the current global propagator and ensemble of lyapunov vectors.

Variables

- real(kind=8), dimension(:), allocatable, public lyap_vectors::loclyap Buffer containing the local Lyapunov exponent.
- real(kind=8), dimension(:), allocatable, public lyap_vectors::lyapunov

 Buffer containing the averaged Lyapunov exponent.
- real(kind=8), dimension(:,:), allocatable, public lyap_vectors::ensemble
 Buffer containing the QR decompsoition of the ensemble.
- real(kind=8), dimension(:,:), allocatable lyap_vectors::prop
 Buffer holding the propagator matrix.
- · integer lyap_vectors::lwork
- real(kind=8), dimension(:), allocatable lyap_vectors::work

Temporary buffer for QR decomposition.

- real(kind=8), dimension(:), allocatable lyap_vectors::work2
 Temporary buffer for QR decomposition.
- real(kind=8), dimension(:), allocatable lyap_vectors::tau

 Temporary buffer for QR decomposition.
- real(kind=8), dimension(:,:), allocatable lyap_vectors::prop_buf

 Buffer holding the local propagator matrix.

8.10 maooam.f90 File Reference

Functions/Subroutines

· program maooam

Fortran 90 implementation of the modular arbitrary-order ocean-atmosphere model MAOOAM.

8.10.1 Function/Subroutine Documentation

```
8.10.1.1 program maooam ( )
```

Fortran 90 implementation of the modular arbitrary-order ocean-atmosphere model MAOOAM.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Definition at line 13 of file maooam.f90.

8.11 maooam_lyap.f90 File Reference

Functions/Subroutines

program maooam_lyap

Fortran 90 implementation of the modular arbitrary-order ocean-atmosphere model MAOOAM computing the Lyapunov spectrum.

8.11.1 Function/Subroutine Documentation

8.11.1.1 program maooam_lyap ()

Fortran 90 implementation of the modular arbitrary-order ocean-atmosphere model MAOOAM computing the Lyapunov spectrum.

Copyright

2016 Lesley De Cruz, Sebastian Schubert & Jonathan Demaeyer. See LICENSE.txt for license information.

Definition at line 13 of file maooam_lyap.f90.

8.12 maooam_lyap_div.f90 File Reference

Functions/Subroutines

· program maooam lyap div

Fortran 90 implementation of the modular arbitrary-order ocean-atmosphere model MAOOAM computing the first Lyapunov exponent with the divergence method.

8.12.1 Function/Subroutine Documentation

```
8.12.1.1 program maooam_lyap_div ( )
```

Fortran 90 implementation of the modular arbitrary-order ocean-atmosphere model MAOOAM computing the first Lyapunov exponent with the divergence method.

Copyright

2016 Lesley De Cruz, Sebastian Schubert & Jonathan Demaeyer. See LICENSE.txt for license information.

Definition at line 14 of file maooam lyap div.f90.

8.13 params.f90 File Reference

Modules

module params

The model parameters module.

Functions/Subroutines

• subroutine, private params::init_nml

Read the basic parameters and mode selection from the namelist.

• subroutine params::init_params

Parameters initialisation routine.

Variables

```
• real(kind=8) params::n
     n=2L_y/L_x - Aspect ratio
• real(kind=8) params::phi0
     Latitude in radian.
• real(kind=8) params::rra
     Earth radius.
• real(kind=8) params::sig0
     \sigma_0 - Non-dimensional static stability of the atmosphere.
real(kind=8) params::k
     Bottom atmospheric friction coefficient.
real(kind=8) params::kp
     k^{\prime} - Internal atmospheric friction coefficient.
real(kind=8) params::r
      Frictional coefficient at the bottom of the ocean.
real(kind=8) params::d
     Merchanical coupling parameter between the ocean and the atmosphere.
• real(kind=8) params::f0
      f_0 - Coriolis parameter
• real(kind=8) params::gp
     g' Reduced gravity
• real(kind=8) params::h
     Depth of the active water layer of the ocean.
real(kind=8) params::phi0_npi
     Latitude exprimed in fraction of pi.
• real(kind=8) params::lambda
      \lambda - Sensible + turbulent heat exchange between the ocean and the atmosphere.
real(kind=8) params::co
     C_a - Constant short-wave radiation of the ocean.
real(kind=8) params::go
     \gamma_o - Specific heat capacity of the ocean.
• real(kind=8) params::ca
     C_a - Constant short-wave radiation of the atmosphere.
real(kind=8) params::to0
     T_o^0 - Stationary solution for the 0-th order ocean temperature.
• real(kind=8) params::ta0
     T_a^0 - Stationary solution for the 0-th order atmospheric temperature.
• real(kind=8) params::epsa
     \epsilon_a - Emissivity coefficient for the grey-body atmosphere.
• real(kind=8) params::ga
     \gamma_a - Specific heat capacity of the atmosphere.
real(kind=8) params::rr
     R - Gas constant of dry air
• real(kind=8) params::scale
      L_y = L \pi - The characteristic space scale.
real(kind=8) params::pi
real(kind=8) params::lr
      L_R - Rossby deformation radius
```

real(kind=8) params::g

γ real(kind=8) params::rp

 r' - Frictional coefficient at the bottom of the ocean.

 real(kind=8) params::dp

 d' - Non-dimensional mechanical coupling parameter

 d^\prime - Non-dimensional mechanical coupling parameter between the ocean and the atmosphere.

real(kind=8) params::kd

 k_d - Non-dimensional bottom atmospheric friction coefficient.

real(kind=8) params::kdp

 k_d' - Non-dimensional internal atmospheric friction coefficient.

• real(kind=8) params::cpo

 C_a' - Non-dimensional constant short-wave radiation of the ocean.

real(kind=8) params::lpo

 λ_o' - Non-dimensional sensible + turbulent heat exchange from ocean to atmosphere.

• real(kind=8) params::cpa

 C_a' - Non-dimensional constant short-wave radiation of the atmosphere.

• real(kind=8) params::lpa

 λ_a' - Non-dimensional sensible + turbulent heat exchange from atmosphere to ocean.

• real(kind=8) params::sbpo

 $\sigma_{B,o}^{\prime}$ - Long wave radiation lost by ocean to atmosphere & space.

real(kind=8) params::sbpa

 $\sigma_{B,a}^{\prime}$ - Long wave radiation from atmosphere absorbed by ocean.

• real(kind=8) params::lsbpo

 $S'_{B,o}$ - Long wave radiation from ocean absorbed by atmosphere.

• real(kind=8) params::lsbpa

 $S_{B,a}'$ - Long wave radiation lost by atmosphere to space & ocean.

• real(kind=8) params::I

 ${\cal L}$ - Domain length scale

real(kind=8) params::sc

Ratio of surface to atmosphere temperature.

• real(kind=8) params::sb

Stefan-Boltzmann constant.

real(kind=8) params::betp

 β' - Non-dimensional beta parameter

• real(kind=8) params::nua =0.D0

Dissipation in the atmosphere.

real(kind=8) params::nuo =0.D0

Dissipation in the ocean.
• real(kind=8) params::nuap

Non-dimensional dissipation in the atmosphere.

real(kind=8) params::nuop

Non-dimensional dissipation in the ocean.

• real(kind=8) params::t trans

Transient time period.

real(kind=8) params::t_run

Effective intergration time (length of the generated trajectory)

• real(kind=8) params::dt

Integration time step.

• real(kind=8) params::tw

Write all variables every tw time units.

logical params::writeout

Write to file boolean.

real(kind=8) params::rescaling_time

Rescaling time for the Lyapunov computation.

• integer params::nboc

Number of atmospheric blocks.

• integer params::nbatm

Number of oceanic blocks.

• integer params::natm =0

Number of atmospheric basis functions.

• integer params::noc =0

Number of oceanic basis functions.

• integer params::ndim

Number of variables (dimension of the model)

• integer, dimension(:,:), allocatable params::oms

Ocean mode selection array.

• integer, dimension(:,:), allocatable params::ams

Atmospheric mode selection array.

8.14 rk2_integrator.f90 File Reference

Modules

· module integrator

Module with the integration routines.

Functions/Subroutines

• subroutine, public integrator::init_integrator

Routine to initialise the integration buffers.

• subroutine integrator::tendencies (t, y, res)

Routine computing the tendencies of the model.

• subroutine, public integrator::step (y, t, dt, res)

Routine to perform an integration step (Heun algorithm). The incremented time is returned.

Variables

• real(kind=8), dimension(:), allocatable integrator::buf_y1

Buffer to hold the intermediate position (Heun algorithm)

real(kind=8), dimension(:), allocatable integrator::buf_f0

Buffer to hold tendencies at the initial position.

• real(kind=8), dimension(:), allocatable integrator::buf_f1

Buffer to hold tendencies at the intermediate position.

8.15 rk2_tl_ad_integrator.f90 File Reference

Modules

· module tl_ad_integrator

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Integrators module.

Functions/Subroutines

• subroutine tl ad integrator::tendencies (t, y, res)

Routine computing the tendencies of the nonlinear model.

• subroutine, public tl_ad_integrator::init_tl_ad_integrator

Routine to initialise the integration buffers.

• subroutine, public tl ad integrator::ad step (y, ystar, t, dt, res)

Routine to perform an integration step (Heun algorithm) of the adjoint model. The incremented time is returned.

• subroutine, public tl_ad_integrator::evolve_ad_step (y, deltay, t, dt, ynew, deltaynew)

Routine to perform a simultaneous integration step (RK4 algorithm) of the nonlinear and adjoint together. The incremented time is returned.

• subroutine, public tl_ad_integrator::tl_step (y, ystar, t, dt, res)

Routine to perform an integration step (Heun algorithm) of the tangent linear model. The incremented time is returned.

subroutine, public tl_ad_integrator::evolve_tl_step (y, deltay, t, dt, ynew, deltaynew)

Routine to perform a simultaneous integration step (RK4 algorithm) of the nonlinear and the tangent linear model together. The incremented time is returned.

• subroutine, public tl_ad_integrator::prop_step (y, propagator, t, dt, ynew, adjoint)

Routine to perform a simultaneously an integration step (Heun algorithm) of the nonlinear and computes the Heun tangent linear propagator. The boolean variable adjoint allows for an adjoint forward integration. The incremented time is returned.

Variables

real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_y1

Buffer to hold the intermediate position (Heun algorithm) of the tangent linear model.

• real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_f0

Buffer to hold tendencies at the initial position of the tangent linear model.

• real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_f1

Buffer to hold tendencies at the intermediate position of the tangent linear model.

• real(kind=8), dimension(:), allocatable tl ad integrator::buf y11

Buffer to hold the intermediate position (Heun algorithm) of the tangent linear model.

real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_f00

Buffer to hold tendencies at the initial position of the tangent linear model.

real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_f11

Buffer to hold tendencies at the intermediate position of the tangent linear model.

real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j1

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j2

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

• real(kind=8), dimension(:,:), allocatable tl ad integrator::buf j1h

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j2h

Buffer to hold jacobians in the RK4 scheme for the tangent linear model.

real(kind=8), dimension(:,:), allocatable tl_ad_integrator::one
 unit matrix

8.16 rk4_integrator.f90 File Reference

Modules

· module integrator

Module with the integration routines.

Functions/Subroutines

· subroutine, public integrator::init integrator

Routine to initialise the integration buffers.

• subroutine integrator::tendencies (t, y, res)

Routine computing the tendencies of the model.

subroutine, public integrator::step (y, t, dt, res)

Routine to perform an integration step (Heun algorithm). The incremented time is returned.

Variables

• real(kind=8), dimension(:), allocatable integrator::buf_ka

Buffer A to hold tendencies.

real(kind=8), dimension(:), allocatable integrator::buf kb

Buffer B to hold tendencies.

8.17 rk4_tl_ad_integrator.f90 File Reference

Modules

• module tl_ad_integrator

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Integrators module.

Functions/Subroutines

subroutine tl_ad_integrator::tendencies (t, y, res)

Routine computing the tendencies of the nonlinear model.

subroutine, public tl_ad_integrator::init_tl_ad_integrator

Routine to initialise the integration buffers.

subroutine, public tl_ad_integrator::ad_step (y, ystar, t, dt, res)

Routine to perform an integration step (Heun algorithm) of the adjoint model. The incremented time is returned.

• subroutine, public tl_ad_integrator::evolve_ad_step (y, deltay, t, dt, ynew, deltaynew)

Routine to perform a simultaneous integration step (RK4 algorithm) of the nonlinear and adjoint together. The incremented time is returned.

• subroutine, public tl_ad_integrator::tl_step (y, ystar, t, dt, res)

Routine to perform an integration step (Heun algorithm) of the tangent linear model. The incremented time is returned.

• subroutine, public tl_ad_integrator::evolve_tl_step (y, deltay, t, dt, ynew, deltaynew)

Routine to perform a simultaneous integration step (RK4 algorithm) of the nonlinear and the tangent linear model together. The incremented time is returned.

• subroutine, public tl_ad_integrator::prop_step (y, propagator, t, dt, ynew, adjoint)

Routine to perform a simultaneously an integration step (Heun algorithm) of the nonlinear and computes the Heun tangent linear propagator. The boolean variable adjoint allows for an adjoint forward integration. The incremented time is returned.

Variables

- real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_ka
 Buffer to hold tendencies in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_kb
 Buffer to hold tendencies in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_kc
 Buffer to hold tendencies in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_kd
 Buffer to hold tendencies in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j3
 Buffer to hold jacobians in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j4
 Buffer to hold jacobians in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j3h
 Buffer to hold jacobians in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:,:), allocatable tl_ad_integrator::buf_j4h
 Buffer to hold jacobians in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_kaa
 Buffer to hold tendencies in the RK4 scheme for the tangent linear model.
- real(kind=8), dimension(:), allocatable tl_ad_integrator::buf_kbb
 Buffer to hold tendencies in the RK4 scheme for the tangent linear model.

8.18 stat.f90 File Reference

Modules

module stat

Statistics accumulators.

Functions/Subroutines

- subroutine, public stat::init_stat
 - Initialise the accumulators.
- subroutine, public stat::acc (x)

Accumulate one state.

- real(kind=8) function, dimension(0:ndim), public stat::mean ()
 Function returning the mean.
- real(kind=8) function, dimension(0:ndim), public stat::var ()
- integer function, public stat::iter ()

Function returning the variance.

Function returning the number of data accumulated.

• subroutine, public stat::reset

Routine resetting the accumulators.

Variables

• integer stat::i =0

Number of stats accumulated.

• real(kind=8), dimension(:), allocatable stat::m

Vector storing the inline mean.

real(kind=8), dimension(:), allocatable stat::mprev

Previous mean vector.

• real(kind=8), dimension(:), allocatable stat::v

Vector storing the inline variance.

• real(kind=8), dimension(:), allocatable stat::mtmp

8.19 tensor.f90 File Reference

Data Types

· type tensor::coolist_elem

Coordinate list element type. Elementary elements of the sparse tensors.

· type tensor::coolist

Coordinate list. Type used to represent the sparse tensor.

Modules

module tensor

Tensor utility module.

Functions/Subroutines

• subroutine, public tensor::copy_coo (src, dst)

Routine to copy a coolist.

subroutine, public tensor::mat_to_coo (src, dst)

Routine to convert a matrix to a tensor.

• subroutine, public tensor::sparse_mul3 (coolist_ijk, arr_j, arr_k, res)

Sparse multiplication of a tensor with two vectors: $\sum_{j,k=0}^{ndim} \mathcal{T}_{i,j,k} \, a_j \, b_k$.

• subroutine, public tensor::jsparse_mul (coolist_ijk, arr_j, jcoo_ij)

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} \left(\mathcal{T}_{i,j,k} + \mathcal{T}_{i,k,j} \right) a_k.$$

It's implemented slightly differently: for every $\mathcal{T}_{i,j,k}$, we add to $J_{i,j}$ as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a coolist (sparse tensor).

• subroutine, public tensor::jsparse_mul_mat (coolist_ijk, arr_j, jcoo_ij)

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} (\mathcal{T}_{i,j,k} + \mathcal{T}_{i,k,j}) \ a_k.$$

It's implemented slightly differently: for every $\mathcal{T}_{i,j,k}$, we add to $J_{i,j}$ as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a matrix.

• subroutine, public tensor::sparse_mul2 (coolist_ij, arr_j, res)

Sparse multiplication of a 2d sparse tensor with a vector: $\sum_{j=0}^{ndim} \mathcal{T}_{i,j,k} a_j$.

• subroutine, public tensor::simplify (tensor)

Routine to simplify a coolist (sparse tensor). For each index i, it upper triangularize the matrix

$$\mathcal{T}_{i,j,k}$$
 $0 \le j, k \le ndim$.

• subroutine, public tensor::add_elem (t, i, j, k, v)

Subroutine to add element to a coolist.

• subroutine, public tensor::add_check (t, i, j, k, v, dst)

Subroutine to add element to a coolist and check for overflow. Once the t buffer tensor is full, add it to the destination buffer.

• subroutine, public tensor::add_to_tensor (src, dst)

Routine to add a rank-3 tensor to another one.

• subroutine, public tensor::print tensor (t, s)

Routine to print a rank 3 tensor coolist.

subroutine, public tensor::write_tensor_to_file (s, t)

Load a rank-4 tensor coolist from a file definition.

• subroutine, public tensor::load_tensor_from_file (s, t)

Load a rank-4 tensor coolist from a file definition.

Variables

real(kind=8), parameter tensor::real_eps = 2.2204460492503131e-16
 Parameter to test the equality with zero.

8.20 test aotensor.f90 File Reference

Functions/Subroutines

• program test_aotensor

Small program to print the inner products.

8.20.1 Function/Subroutine Documentation

8.20.1.1 program test_aotensor ()

Small program to print the inner products.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Definition at line 13 of file test_aotensor.f90.

8.21 test_inprod_analytic.f90 File Reference

Functions/Subroutines

program inprod_analytic_test
 Small program to print the inner products.

8.21.1 Function/Subroutine Documentation

```
8.21.1.1 program inprod_analytic_test ( )
```

Small program to print the inner products.

Copyright

2015 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Remarks

Print in the same order as test_inprod.lua

Definition at line 18 of file test_inprod_analytic.f90.

8.22 test_tl_ad.f90 File Reference

Functions/Subroutines

· program test_tl_ad

Tests for the Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM.

- real(kind=8) function gasdev (idum)
- real(kind=8) function ran2 (idum)

8.22.1 Function/Subroutine Documentation

8.22.1.1 real(kind=8) function gasdev (integer idum)

Definition at line 149 of file test_tl_ad.f90.

```
INTEGER :: idum
150
      REAL(KIND=8) :: gasdev,ran2
           USES ran2
151
      INTEGER :: iset
152
      REAL(KIND=8) :: fac,gset,rsq,v1,v2
153
      SAVE iset, gset
155 DATA iset/0/
156 if (idum.lt.0) iset=0
157 if (iset.eq.0) then
158 1 v1=2.d0*ran2(idum)-1.
         v2=2.d0*ran2(idum)-1.
159
160
        rsq=v1**2+v2**2
          if (rsq.ge.1.d0.or.rsq.eq.0.d0) goto 1
        fac=sqrt(-2.*log(rsq)/rsq)
162
163
         gset=v1*fac
164
          gasdev=v2*fac
          iset=1
165
166
      else
167
        gasdev=gset
168
          iset=0
169
      endif
170
```

8.22.1.2 real(kind=8) function ran2 (integer idum)

Definition at line 174 of file test_tl_ad.f90.

```
INTEGER :: idum,im1,im2,imm1,ia1,ia2,iq1,iq2,ir1,ir2,ntab,ndiv
     REAL(KIND=8) :: ran2,am,eps,rnmx
parameter(im1=2147483563,im2=2147483399,am=1.d0/im1,imm1=im1-1&
176
177
            &,ia1=40014,ia2=40692,iq1=53668,iq2=52774,ir1=12211,ir2&
178
           &=3791,ntab=32,ndiv=1+imm1/ntab,eps=1.2d-7,rnmx=1.d0-eps)
      INTEGER :: idum2, j, k, iv(ntab), iy
179
180
      SAVE iv,iy,idum2
DATA idum2/123456789/, iv/ntab*0/, iy/0/
181
182
      if (idum.le.0) then
183
         idum=max(-idum,1)
       idum2=idum
184
185
       do j=ntab+8,1,-1
           k=idum/iq1
idum=ia1*(idum-k*iq1)-k*ir1
186
187
            if (idum.lt.0) idum=idum+im1
189
            if (j.le.ntab) iv(j)=idum
190
        enddo
191
        iy=iv(1)
192
      endi f
193
      k=idum/iq1
      idum=ia1*(idum-k*iq1)-k*ir1
194
195
      if (idum.lt.0) idum=idum+im1
196
      k=idum2/iq2
      idum2=ia2*(idum2-k*iq2)-k*ir2
197
198
      if (idum2.lt.0) idum2=idum2+im2
199
      j=1+iy/ndiv
200
      iy=iv(j)-idum2
      iv(j)=idum
202
      if (iy.lt.1) iy=iy+imm1
203
      ran2=min(am*iy,rnmx)
204
      return
```

8.22.1.3 program test_tl_ad ()

Tests for the Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM.

Copyright

2016 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Definition at line 14 of file test_tl_ad.f90.

8.23 tl_ad_tensor.f90 File Reference

Modules

module tl_ad_tensor

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Tensors definition module.

Functions/Subroutines

type(coolist) function, dimension(ndim) tl_ad_tensor::jacobian (ystar)

Compute the Jacobian of MAOOAM in point ystar.

real(kind=8) function, dimension(ndim, ndim), public tl_ad_tensor::jacobian_mat (ystar)

Compute the Jacobian of MAOOAM in point ystar.

subroutine, public tl_ad_tensor::init_tltensor

Routine to initialize the TL tensor.

• subroutine tl ad tensor::compute tltensor (func)

Routine to compute the TL tensor from the original MAOOAM one.

subroutine tl ad tensor::tl add count (i, j, k, v)

Subroutine used to count the number of TL tensor entries.

subroutine tl_ad_tensor::tl_coeff (i, j, k, v)

Subroutine used to compute the TL tensor entries.

subroutine, public tl_ad_tensor::init_adtensor

Routine to initialize the AD tensor.

subroutine tl_ad_tensor::compute_adtensor (func)

Subroutine to compute the AD tensor from the original MAOOAM one.

subroutine tl ad tensor::ad add count (i, j, k, v)

Subroutine used to count the number of AD tensor entries.

- subroutine tl_ad_tensor::ad_coeff (i, j, k, v)
- · subroutine, public tl ad tensor::init adtensor ref

Alternate method to initialize the AD tensor from the TL tensor.

subroutine tl ad tensor::compute adtensor ref (func)

Alternate subroutine to compute the AD tensor from the TL one.

subroutine tl_ad_tensor::ad_add_count_ref (i, j, k, v)

Alternate subroutine used to count the number of AD tensor entries from the TL tensor.

subroutine tl_ad_tensor::ad_coeff_ref (i, j, k, v)

Alternate subroutine used to compute the AD tensor entries from the TL tensor.

subroutine, public tl_ad_tensor::ad (t, ystar, deltay, buf)

Tendencies for the AD of MAOOAM in point ystar for perturbation deltay.

subroutine, public tl_ad_tensor::tl (t, ystar, deltay, buf)

Tendencies for the TL of MAOOAM in point ystar for perturbation deltay.

Variables

- real(kind=8), parameter tl_ad_tensor::real_eps = 2.2204460492503131e-16
 Epsilon to test equality with 0.
- integer, dimension(:), allocatable tl_ad_tensor::count_elems

Vector used to count the tensor elements.

type(coolist), dimension(:), allocatable, public tl_ad_tensor::tltensor

Tensor representation of the Tangent Linear tendencies.

• type(coolist), dimension(:), allocatable, public tl ad tensor::adtensor

Tensor representation of the Adjoint tendencies.

8.24 tr_jacob_mat.f90 File Reference

Functions/Subroutines

program tr_jacob_mat

Tests to obtain the trace of the Jacobian matrix.

8.24.1 Function/Subroutine Documentation

```
8.24.1.1 program tr_jacob_mat()
```

Tests to obtain the trace of the Jacobian matrix.

Copyright

2016 Lesley De Cruz & Jonathan Demaeyer. See LICENSE.txt for license information.

Definition at line 13 of file tr jacob mat.f90.

8.25 util.f90 File Reference

Modules

module util

Utility module.

Functions/Subroutines

• character(len=20) function, public util::str (k)

Convert an integer to string.

• character(len=40) function, public util::rstr (x, fm)

Convert a real to string with a given format.

• integer function, dimension(size(s)), public util::isin (c, s)

Determine if a character is in a string and where.

• subroutine, public util::init_random_seed ()

Random generator initialization routine.

- integer function lcg (s)
- subroutine, public util::piksrt (k, arr, par)

Simple card player sorting function.

• subroutine, public util::init_one (A)

Initialize a square matrix A as a unit matrix.

8.25.1 Function/Subroutine Documentation

8.25.1.1 integer function init_random_seed::lcg (integer(int64) s)

Definition at line 102 of file util.f90.

```
integer :: lcg
103
          integer(int64) :: s
104
          IF (s == 0) THEN s = 104729
105
          ELSE
106
107
             s = mod(s, 4294967296_int64)
109
          s = mod(s * 279470273_int64, 4294967291_int64)
110
          lcg = int(mod(s, int(huge(0), int64)), kind(0))
        END FUNCTION lcg
111
```

Index

a	b
aotensor_def, 14	inprod_analytic::atm_tensors, 93
inprod_analytic::atm_tensors, 93	b1
acc	inprod_analytic, 24
stat, 59	b2
ad	inprod_analytic, 24
tl_ad_tensor, 83	benettin_step
ad_add_count	lyap_vectors, 39
tl_ad_tensor, 83	betp
ad_add_count_ref	params, 47
tl_ad_tensor, 84	buf_f0
ad_coeff	integrator, 34
tl_ad_tensor, 84	tl_ad_integrator, 77
ad_coeff_ref	buf_f00
tl_ad_tensor, 85	tl_ad_integrator, 78
ad_step	buf_f1
tl_ad_integrator, 73	integrator, 34
add_check	tl_ad_integrator, 78
tensor, 63	buf_f11
add_count	tl_ad_integrator, 78
aotensor_def, 14	buf_j1
add_elem	tl_ad_integrator, 78
tensor, 63	buf_j1h
add_to_tensor	tl_ad_integrator, 78
tensor, 64	buf_j2
adtensor	tl_ad_integrator, 78
tl ad tensor, 89	buf_j2h
ams	tl_ad_integrator, 79
params, 47	buf_j3
aotensor	tl_ad_integrator, 79
aotensor def, 17	buf_j3h
aotensor_def, 13	tl_ad_integrator, 79
a, 14	buf j4
add_count, 14	tl_ad_integrator, 79
aotensor, 17	buf_j4h
coeff, 14	tl_ad_integrator, 79
compute aotensor, 15	buf_ka
count elems, 17	integrator, 34
init aotensor, 15	tl ad integrator, 80
kdelta, 16	buf_kaa
psi, 16	tl ad integrator, 80
real eps, 17	buf kb
t, 16	integrator, 35
theta, 16	tl ad integrator, 80
aotensor_def.f90, 101	buf_kbb
atmos	tl_ad_integrator, 80
inprod_analytic, 31	buf_kc
awavenum	tl_ad_integrator, 80
inprod analytic, 31	buf kd

tl_ad_integrator, 81	tensor, 65
buf_y1	count_elems
— -	
integrator, 35	aotensor_def, 17
tl_ad_integrator, 81	tl_ad_tensor, 89
buf_y11	сра
tl_ad_integrator, 81	params, 48
2	сро
C	params, 48
inprod_analytic::atm_tensors, 93	
inprod_analytic::ocean_tensors, 98	d
CLAIM	inprod_analytic::atm_tensors, 94
LICENSE.txt, 106	params, 48
CONTRACT	delta
LICENSE.txt, 107	inprod_analytic, 29
ca	distribute
params, 47	LICENSE.txt, 107
calculate_a	doc/gen_doc.md, 102
inprod_analytic, 24	doc/tl_ad_doc.md, 102
calculate_b	dp
inprod_analytic, 24	
calculate c atm	params, 48
inprod_analytic, 24	dt
calculate_c_oc	params, 48
inprod_analytic, 25	elems
calculate_d	tensor::coolist, 96
inprod_analytic, 25	ensemble
calculate_g	lyap_vectors, 41
inprod_analytic, 25	epsa
calculate_k	params, 49
inprod_analytic, 27	evolve_ad_step
calculate_m	tl_ad_integrator, 74
inprod_analytic, 27	evolve_tl_step
calculate_n	tl ad integrator, 74
inprod_analytic, 27	exists
calculate_o	ic_def, 19
inprod_analytic, 27	icdelta_def, 21
calculate_s	iodolia_doi, Zi
inprod_analytic, 28	fO
calculate_w	params, 49
inprod_analytic, 28	FROM
charge	LICENSE.txt, 107
LICENSE.txt, 106	files
CO 47	LICENSE.txt, 106
params, 47	flambda
coeff	inprod_analytic, 29
aotensor_def, 14	
compute_adtensor	g
tl_ad_tensor, 85	inprod_analytic::atm_tensors, 94
compute_adtensor_ref	params, 49
tl_ad_tensor, 85	ga
compute_aotensor	params, 49
aotensor_def, 15	gasdev
compute_tltensor	test_tl_ad.f90, 121
tl_ad_tensor, 86	get_lyap_state
conditions	lyap_vectors, 40
	• • -
LICENSE.txt, 106	go
COPY LICENSE had 107	params, 49
LICENSE.txt, 107	gp
copy_coo	params, 50

granted	calculate_b, 24
LICENSE.txt, 107	calculate_c_atm, 24
	calculate_c_oc, 25
h	calculate_d, 25
inprod_analytic::atm_wavenum, 95	calculate_g, 25
inprod_analytic::ocean_wavenum, 99	calculate_k, 27
params, 50	calculate_m, 27
	calculate_n, 27
i	calculate_o, 27
lyap_stat, 37	calculate_s, 28
stat, 61	calculate w, 28
IMPLIED	delta, 29
LICENSE.txt, 107	flambda, 29
ic	
ic_def, 19	init_inprod, 29
ic_def, 17	ocean, 32
exists, 19	owavenum, 32
ic, 19	s1, 30
load_ic, 18	s2, 31
ic_def.f90, 102	s3, <mark>3</mark> 1
icdelta	s4, <mark>3</mark> 1
icdelta_def, 22	inprod_analytic.f90, 103
icdelta_def, 20	inprod_analytic::atm_tensors, 93
	a, 93
exists, 21	b, 93
icdelta, 22	c, 93
load_icdelta, 20	d, 94
icdelta_def.f90, 102	g, 94
init_adtensor	s, 94
tl_ad_tensor, 86	inprod_analytic::atm_wavenum, 94
init_adtensor_ref	h, 95
tl_ad_tensor, 86	
init_aotensor	m, 95
aotensor_def, 15	nx, 95
init_inprod	ny, 95
inprod_analytic, 29	p, 95
init_integrator	typ, 95
integrator, 33	inprod_analytic::ocean_tensors, 98
init_lyap	c, 98
lyap_vectors, 40	k, 98
init nml	m, 98
params, 45	n, 98
init one	o, 98
util, 91	w, 99
init params	inprod_analytic::ocean_wavenum, 99
params, 46	h, 99
init_random_seed	nx, 99
util, 91	ny, 99
init stat	p, 100
_	inprod_analytic_test
stat, 59	test_inprod_analytic.f90, 121
init_tl_ad_integrator	— · — ·
tl_ad_integrator, 75	integrator, 32
init_tltensor	buf_f0, 34
tl_ad_tensor, 86	buf_f1, 34
inprod_analytic, 22	buf_ka, 34
atmos, 31	buf_kb, 35
awavenum, 31	buf_y1, 35
b1, 24	init_integrator, 33
b2, 24	step, 33
calculate_a, 24	tendencies, 34

isin		laml	oda
	util, 91		params, 51
iter		lcg	
	stat, 60		util.f90, 124
		Lice	nse
j			LICENSE.txt, 106
•	tensor::coolist_elem, 97	load	
iaco	bian	iuau	_
jaco	tl_ad_tensor, 87		ic_def, 18
iooo		load	_icdelta
jaco	bian_mat		icdelta_def, 20
	tl_ad_tensor, 87	load	_tensor_from_file
Jspa	rse_mul		tensor, 67
	tensor, 65	locly	ap
jspa	rse_mul_mat		lyap vectors, 41
	tensor, 66	lpa	, , _ ,
			params, 51
k		lpo	paramo, or
	inprod_analytic::ocean_tensors, 98	ipo	noromo E1
	params, 50		params, 51
	tensor::coolist_elem, 97	lr	
KIN			params, 52
1 (11 (LICENSE.txt, 107	Isbp	a
kd	LIGENGE: IXI, 107		params, 52
κu	70. FO	Isbp	0
	params, 50		params, 52
kdel		lwor	
	aotensor_def, 16		lyap_vectors, 41
kdp		lvan	
	params, 50	iyap	_acc
kp		l	lyap_stat, 36
	params, 51	iyap	_init_stat
			lyap_stat, 36
1		lyap	_iter
	params, 51		lyap_stat, 36
ΙΙΔΕ	BILITY	lyap	_mean
L", \L	LICENSE.txt, 108		lyap_stat, 37
LICI	ENSE.txt, 104	lvap	_reset
LICI		.,	lyap_stat, 37
	CLAIM, 106	lvan	_stat, 35
	CONTRACT, 107	iyap	
	charge, 106		i, 37
	conditions, 106		lyap_acc, 36
	copy, 107		lyap_init_stat, 36
	distribute, 107		lyap_iter, 36
	FROM, 107		lyap_mean, 37
	files, 106		lyap_reset, 37
	granted, 107		lyap_var, 37
	IMPLIED, 107		m, 37
	KIND, 107		mprev, 38
	LIABILITY, 108		mtmp, 38
	License, 106		v, 38
		lvan	_stat.f90, 109
	MERCHANTABILITY, 108		
	merge, 108	iyap	_var
	modify, 108		lyap_stat, 37
	OTHERWISE, 108	lyap	_vectors, 38
	publish, 108		benettin_step, 39
	restriction, 109		ensemble, 41
	so, 109		get_lyap_state, 40
	Software, 109		init_lyap, 40
	sublicense, 109		loclyap, 41
	use, 109		lwork, 41
	400, 700		

lyapunov, 41	tensor::coolist, 96
multiply_prop, 40	noc
prop, 41	params, 53
prop_buf, 42	nua
tau, 42	params, 53
work, 42	nuap
work2, 42	params, 54
lyap_vectors.f90, 110	nuo
lyapunov	params, 54
lyap_vectors, 41	nuop
• 1 = - /	params, 54
m	nx
inprod_analytic::atm_wavenum, 95	inprod_analytic::atm_wavenum, 95
inprod_analytic::ocean_tensors, 98	inprod_analytic::ocean_wavenum, 99
lyap_stat, 37	ny
stat, 61	inprod_analytic::atm_wavenum, 95
MERCHANTABILITY	inprod analytic::ocean wavenum, 99
LICENSE.txt, 108	mprod_ariary tronoccan_waveriam, co
maooam	0
maooam.f90, 111	inprod analytic::ocean tensors, 98
maooam.f90, 111	OTHERWISE
maooam, 111	LICENSE.txt, 108
maooam_lyap	ocean
maooam_lyap.f90, 112	inprod_analytic, 32
maooam_lyap.f90, 111	. — .
	oms
maooam_lyap, 112	params, 54
maooam_lyap_div	One
maooam_lyap_div.f90, 112	tl_ad_integrator, 81
maooam_lyap_div.f90, 112	owavenum
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
maooam_lyap_div, 112	inprod_analytic, 32
mat_to_coo	. – ,
_,	р
mat_to_coo tensor, 67 mean	p inprod_analytic::atm_wavenum, 95
mat_to_coo tensor, 67 mean stat, 60	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100
mat_to_coo tensor, 67 mean stat, 60 merge	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 co, 47 cpa, 48 cpo, 48 d, 48
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 co, 47 cpa, 48 cpo, 48 d, 48
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 dt, 48
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dp, 48 dt, 48 epsa, 49
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49 ga, 49
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40 n inprod_analytic::ocean_tensors, 98	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49 ga, 49 go, 49
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40 n inprod_analytic::ocean_tensors, 98 params, 52	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49 ga, 49 go, 49 gp, 50
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40 n inprod_analytic::ocean_tensors, 98 params, 52 natm	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49 ga, 49 go, 49 gp, 50 h, 50
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40 n inprod_analytic::ocean_tensors, 98 params, 52 natm params, 52	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49 ga, 49 go, 49 gp, 50 h, 50 init_nml, 45
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40 n inprod_analytic::ocean_tensors, 98 params, 52 natm params, 52 nbatm	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49 ga, 49 go, 49 go, 49 gp, 50 h, 50 init_nml, 45 init_params, 46
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40 n inprod_analytic::ocean_tensors, 98 params, 52 natm params, 52 nbatm params, 53 nboc	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49 ga, 49 go, 49 gp, 50 h, 50 init_nml, 45 init_params, 46 k, 50 kd, 50
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40 n inprod_analytic::ocean_tensors, 98 params, 52 natm params, 52 nbatm params, 53	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49 ga, 49 go, 49 gp, 50 h, 50 init_nml, 45 init_params, 46 k, 50 kd, 50 kdp, 50
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40 n inprod_analytic::ocean_tensors, 98 params, 52 natm params, 52 nbatm params, 53 nboc params, 53 ndim	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49 ga, 49 go, 49 gp, 50 h, 50 init_nml, 45 init_params, 46 k, 50 kd, 50 kdp, 50 kp, 51
mat_to_coo tensor, 67 mean stat, 60 merge LICENSE.txt, 108 modify LICENSE.txt, 108 mprev lyap_stat, 38 stat, 61 mtmp lyap_stat, 38 stat, 61 multiply_prop lyap_vectors, 40 n inprod_analytic::ocean_tensors, 98 params, 52 natm params, 52 nbatm params, 53 nboc params, 53	p inprod_analytic::atm_wavenum, 95 inprod_analytic::ocean_wavenum, 100 params, 42 ams, 47 betp, 47 ca, 47 co, 47 cpa, 48 cpo, 48 d, 48 dp, 48 dt, 48 epsa, 49 f0, 49 g, 49 ga, 49 go, 49 gp, 50 h, 50 init_nml, 45 init_params, 46 k, 50 kd, 50 kdp, 50

lpa, 51	params, 55
lpo, 51	ran2
lr, 52	test_tl_ad.f90, 121
Isbpa, 52	real_eps
Isbpo, 52	aotensor_def, 17
n, 52	tensor, 71
natm, 52	tl_ad_tensor, 89
nbatm, 53	rescaling_time
nboc, 53	params, 55
ndim, 53	reset
noc, 53	stat, 60
nua, 53	restriction
nuap, 54	LICENSE.txt, 109
nuo, 54	rk2_integrator.f90, 115
nuop, 54	rk2_tl_ad_integrator.f90, 115
oms, 54	rk4_integrator.f90, 116
phi0, 54	rk4_tl_ad_integrator.f90, 117
•	
phi0_npi, 55	rp
pi, 55	params, 55
r, 55	rr
rescaling_time, 55	params, 56
rp, 55	rra
rr, 56	params, 56
rra, <mark>56</mark>	rstr
sb, 56	util, 91
sbpa, 56	
sbpo, 56	s
sc, 57	inprod_analytic::atm_tensors, 94
scale, 57	s1
sig0, 57	inprod_analytic, 30
t_run, 57	s2
t_trans, 57	inprod_analytic, 31
ta0, 58	s3
to0, 58	inprod_analytic, 31
tw, 58	s4
writeout, 58	inprod_analytic, 31
params.f90, 112	sb
phi0	params, 56
params, 54	sbpa
•	params, 56
phi0_npi	sbpo
params, 55	params, 56
pi	SC
params, 55	params, 57
piksrt	scale
util, 91	
print_tensor	params, 57
tensor, 68	sig0
prop	params, 57
lyap_vectors, 41	simplify
prop_buf	tensor, 68
lyap_vectors, 42	SO
prop_step	LICENSE.txt, 109
tl_ad_integrator, 75	Software
psi	LICENSE.txt, 109
aotensor_def, 16	sparse_mul2
publish	tensor, 69
LICENSE.txt, 108	sparse_mul3
2.02.102.00, 100	tensor, 70
r	stat, 58
	,

acc, 59	test_inprod_analytic.f90, 121
i, 61	inprod_analytic_test, 121
init_stat, 59	test_tl_ad
iter, 60	 test_tl_ad.f90, 122
m, <mark>61</mark>	test_tl_ad.f90, 121
mean, 60	gasdev, 121
mprev, 61	ran2, 121
mtmp, 61	
•	test_tl_ad, 122
reset, 60	theta
v, 61	aotensor_def, 16
var, 60	tl
stat.f90, 118	tl_ad_tensor, 88
step	tl_ad_integrator, 71
integrator, 33	ad_step, 73
str	buf_f0, 77
util, 92	buf_f00, 78
sublicense	buf_f1, 78
LICENSE.txt, 109	buf_f11, 78
	buf_j1, <mark>78</mark>
t	buf_j1h, 78
aotensor_def, 16	buf_j2, 78
t_run	buf_j2h, 79
params, 57	_ -
t_trans	buf_j3, 79
params, 57	buf_j3h, 79
ta0	buf_j4, 79
params, 58	buf_j4h, 79
tau	buf_ka, 80
lyap_vectors, 42	buf_kaa, <mark>80</mark>
tendencies	buf_kb, 80
integrator, 34	buf_kbb, 80
	buf kc, 80
tl_ad_integrator, 76	buf_kd, 81
tensor, 61	buf_y1, <mark>81</mark>
add_check, 63	buf_y11, 81
add_elem, 63	evolve_ad_step, 74
add_to_tensor, 64	evolve_tl_step, 74
copy_coo, 65	
jsparse_mul, 65	init_tl_ad_integrator, 75
jsparse_mul_mat, 66	one, 81
load_tensor_from_file, 67	prop_step, 75
mat_to_coo, 67	tendencies, 76
print_tensor, 68	tl_step, 77
real_eps, 71	tl_ad_tensor, 82
simplify, 68	ad, <mark>83</mark>
sparse_mul2, 69	ad_add_count, 83
sparse_mul3, 70	ad_add_count_ref, 84
write_tensor_to_file, 71	ad coeff, 84
tensor.f90, 119	ad_coeff_ref, 85
tensor::coolist, 96	adtensor, 89
elems, 96	compute_adtensor, 85
nelems, 96	compute_adtensor_ref, 85
	compute_tltensor, 86
tensor::coolist_elem, 96	
j, 97	count_elems, 89
k, 97	init_adtensor, 86
v, 97	init_adtensor_ref, 86
test_aotensor	init_tltensor, 86
test_aotensor.f90, 120	jacobian, <mark>87</mark>
test_aotensor.f90, 120	jacobian_mat, 87
test_aotensor, 120	real_eps, 89

```
tl, 88
     tl_add_count, 88
     tl_coeff, 88
     tltensor, 90
tl_ad_tensor.f90, 122
tl_add_count
     tl_ad_tensor, 88
tl_coeff
     tl_ad_tensor, 88
tl_step
     tl_ad_integrator, 77
tltensor
     tl_ad_tensor, 90
to0
     params, 58
tr_jacob_mat
     tr_jacob_mat.f90, 124
tr_jacob_mat.f90, 123
     tr_jacob_mat, 124
tw
     params, 58
typ
     inprod_analytic::atm_wavenum, 95
use
     LICENSE.txt, 109
util, 90
     init_one, 91
     init_random_seed, 91
     isin, 91
     piksrt, 91
     rstr, 91
     str, 92
util.f90, 124
     lcg, 124
٧
     lyap_stat, 38
     stat, 61
     tensor::coolist_elem, 97
var
     stat, 60
W
     inprod_analytic::ocean_tensors, 99
work
     lyap_vectors, 42
work2
     lyap_vectors, 42
write_tensor_to_file
    tensor, 71
writeout
     params, 58
```