

Reference Manual

Generated by Doxygen 1.8.13

Contents

1	Modular arbitrary-order ocean-atmosphere model: MAOOAM -- Fortran implementation	1
2	Modular arbitrary-order ocean-atmosphere model: The Tangent Linear and Adjoint model	5
3	Modules Index	7
3.1	Modules List	7
4	Data Type Index	9
4.1	Class Hierarchy	9
5	Data Type Index	11
5.1	Data Types List	11
6	Module Documentation	13
6.1	aotensor_def Module Reference	13
6.1.1	Detailed Description	13
6.1.2	Function/Subroutine Documentation	13
6.1.2.1	delete_aotensor()	13
6.1.2.2	init_aotensor()	14
6.2	inprod_analytic Module Reference	15
6.2.1	Detailed Description	16
6.2.2	Function/Subroutine Documentation	16
6.2.2.1	calculate_a()	16
6.2.2.2	calculate_b()	17
6.2.2.3	calculate_c_atm()	17
6.2.2.4	calculate_c_oc()	18

6.2.2.5	<code>calculate_d()</code>	18
6.2.2.6	<code>calculate_g()</code>	19
6.2.2.7	<code>calculate_k()</code>	20
6.2.2.8	<code>calculate_m()</code>	20
6.2.2.9	<code>calculate_n()</code>	21
6.2.2.10	<code>calculate_o()</code>	21
6.2.2.11	<code>calculate_s()</code>	22
6.2.2.12	<code>calculate_w()</code>	22
6.2.2.13	<code>delete_inner_products()</code>	22
6.2.2.14	<code>init_inner_products()</code>	23
6.3	<code>integrator_def</code> Module Reference	24
6.3.1	Detailed Description	25
6.4	<code>model_def</code> Module Reference	25
6.4.1	Detailed Description	25
6.4.2	Function/Subroutine Documentation	26
6.4.2.1	<code>ad_tendencies()</code>	26
6.4.2.2	<code>delete_model()</code>	26
6.4.2.3	<code>init_ad_model()</code>	27
6.4.2.4	<code>init_model()</code>	27
6.4.2.5	<code>init_tl_model()</code>	28
6.4.2.6	<code>jacobian()</code>	28
6.4.2.7	<code>jacobian_mat()</code>	30
6.4.2.8	<code>load_ic()</code>	30
6.4.2.9	<code>tendencies()</code>	33
6.4.2.10	<code>tl_tendencies()</code>	33
6.5	<code>params</code> Module Reference	34
6.5.1	Detailed Description	34
6.5.2	Function/Subroutine Documentation	34
6.5.2.1	<code>clean_model_config()</code>	34
6.5.2.2	<code>init_model_config()</code>	35

6.6	rk2_ad_integrator Module Reference	36
6.6.1	Detailed Description	36
6.6.2	Function/Subroutine Documentation	36
6.6.2.1	ad_step()	36
6.7	rk2_integrator Module Reference	37
6.7.1	Detailed Description	37
6.7.2	Function/Subroutine Documentation	38
6.7.2.1	clean()	38
6.7.2.2	init()	38
6.7.2.3	step()	39
6.8	rk2_tl_integrator Module Reference	39
6.8.1	Detailed Description	40
6.8.2	Function/Subroutine Documentation	40
6.8.2.1	tl_step()	40
6.9	rk4_ad_integrator Module Reference	41
6.9.1	Detailed Description	41
6.9.2	Function/Subroutine Documentation	41
6.9.2.1	ad_step()	41
6.10	rk4_integrator Module Reference	42
6.10.1	Detailed Description	42
6.10.2	Function/Subroutine Documentation	42
6.10.2.1	clean()	42
6.10.2.2	init()	43
6.10.2.3	step()	44
6.11	rk4_tl_integrator Module Reference	44
6.11.1	Detailed Description	45
6.11.2	Function/Subroutine Documentation	45
6.11.2.1	tl_step()	45
6.12	stat Module Reference	45
6.12.1	Detailed Description	46

6.12.2	Function/Subroutine Documentation	46
6.12.2.1	acc()	46
6.12.2.2	clean()	47
6.12.2.3	init_stat()	47
6.12.2.4	iter()	48
6.12.2.5	mean()	48
6.12.2.6	reset()	49
6.12.2.7	var()	49
6.13	tensor_def Module Reference	50
6.13.1	Detailed Description	51
6.13.2	Function/Subroutine Documentation	51
6.13.2.1	add_elem()	51
6.13.2.2	add_from_tensor()	52
6.13.2.3	clean()	53
6.13.2.4	copy()	53
6.13.2.5	empty()	54
6.13.2.6	from_mat()	54
6.13.2.7	init()	55
6.13.2.8	jsparse_mul()	56
6.13.2.9	jsparse_mul_mat()	57
6.13.2.10	load_tensor_from_file()	58
6.13.2.11	print_tensor()	58
6.13.2.12	simplify()	59
6.13.2.13	sparse_mul2()	60
6.13.2.14	sparse_mul3()	61
6.13.2.15	tensor_size()	61
6.13.2.16	test_alloc()	62
6.13.2.17	write_tensor_to_file()	62
6.14	tl_ad_tensor Module Reference	63
6.14.1	Detailed Description	63
6.14.2	Function/Subroutine Documentation	64
6.14.2.1	delete_tensor()	64
6.14.2.2	init_adtensor()	65
6.14.2.3	init_tltensor()	66
6.15	util Module Reference	67
6.15.1	Detailed Description	67
6.15.2	Function/Subroutine Documentation	67
6.15.2.1	isin()	67

7 Data Type Documentation	69
7.1 <code>tl_ad_tensor::adtensor</code> Type Reference	69
7.1.1 Detailed Description	70
7.2 <code>aotensor_def::atmoctensor</code> Type Reference	70
7.2.1 Detailed Description	71
7.3 <code>inprod_analytic::atmosphereinnerproducts</code> Type Reference	71
7.3.1 Detailed Description	72
7.4 <code>inprod_analytic::atmosphericwavenumber</code> Type Reference	72
7.4.1 Detailed Description	72
7.5 <code>integrator_def::clean_int</code> Interface Reference	72
7.5.1 Detailed Description	72
7.6 <code>tensor_def::coolist</code> Type Reference	73
7.6.1 Detailed Description	73
7.7 <code>tensor_def::coolistelem</code> Type Reference	73
7.7.1 Detailed Description	74
7.8 <code>integrator_def::init_int</code> Interface Reference	74
7.8.1 Detailed Description	74
7.9 <code>inprod_analytic::innerproducts</code> Type Reference	74
7.9.1 Detailed Description	75
7.10 <code>params::integrationparameters</code> Type Reference	75
7.10.1 Detailed Description	75
7.11 <code>integrator_def::integrator</code> Type Reference	76
7.11.1 Detailed Description	76
7.12 <code>model_def::model</code> Type Reference	76
7.12.1 Detailed Description	77
7.13 <code>params::modelconfiguration</code> Type Reference	77
7.13.1 Detailed Description	77
7.14 <code>params::modesconfiguration</code> Type Reference	78
7.14.1 Detailed Description	78
7.15 <code>inprod_analytic::oceanicwavenumber</code> Type Reference	78

7.15.1 Detailed Description	78
7.16 inprod_analytic::oceaninnerproducts Type Reference	79
7.16.1 Detailed Description	79
7.17 params::physicsconfiguration Type Reference	79
7.17.1 Detailed Description	81
7.17.2 Member Data Documentation	82
7.17.2.1 cpa	82
7.18 rk2_ad_integrator::rk2adintegrator Type Reference	82
7.18.1 Detailed Description	83
7.19 rk2_integrator::rk2integrator Type Reference	83
7.19.1 Detailed Description	84
7.20 rk2_tl_integrator::rk2tlintegrator Type Reference	84
7.20.1 Detailed Description	85
7.21 rk4_ad_integrator::rk4adintegrator Type Reference	85
7.21.1 Detailed Description	86
7.22 rk4_integrator::rk4integrator Type Reference	86
7.22.1 Detailed Description	87
7.23 rk4_tl_integrator::rk4tlintegrator Type Reference	87
7.23.1 Detailed Description	88
7.24 stat::stataccumulator Type Reference	88
7.24.1 Detailed Description	88
7.25 integrator_def::step_int Interface Reference	89
7.25.1 Detailed Description	89
7.26 tensor_def::tensor Type Reference	89
7.26.1 Detailed Description	90
7.27 tl_ad_tensor::tltensor Type Reference	90
7.27.1 Detailed Description	91

Chapter 1

Modular arbitrary-order ocean-atmosphere model: MAOOAM -- Fortran implementation

About

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This software is provided as supplementary material with:

- De Cruz, L., Demaeyer, J. and Vannitsem, S.: The Modular Arbitrary-Order Ocean-Atmosphere Model: MAOOAM v1.0, Geosci. Model Dev., 9, 2793-2808, [doi:10.5194/gmd-9-2793-2016](https://doi.org/10.5194/gmd-9-2793-2016), 2016.

Please cite this article if you use (a part of) this software for a publication.

The authors would appreciate it if you could also send a reprint of your paper to lesley.decruz@meteo.be, jonathan.demaeyer@meteo.be and svn@meteo.be.

Consult the MAOOAM [code repository](#) for updates, and [our website](#) for additional resources.

A pdf version of this manual is available [here](#).

Installation

The program can be installed with Makefile. We provide configuration files for two compilers : gfortran and ifort.

By default, gfortran is selected. To select one or the other, simply modify the Makefile accordingly or pass the COMPILER flag to make.

To install, unpack the archive in a folder or clone with git:

```
git clone https://github.com/Climdyn/MAOOAM.git
cd MAOOAM/fortran
```

and run:

```
make
```

The command

```
make clean
```

removes the compiled files.

For Windows users, a minimalistic GNU development environment (including gfortran and make) is available at www.mingw.org.

Description of the files

The model tendencies are represented through a tensor class called `AtmOcTensor` (`aotensor_def::atmootensor`) which includes all the coefficients. In the standard implementation using `maooam.f90`, this tensor is computed once at the program initialization.

- `maooam.f90` : Main program.
- `model_def.f90` : Main model class module.
- `aotensor_def.f90` : Tensor class `AtmOcTensor` module.
- `inprod_analytic.f90` : Inner products class module.
- `integrator_def.f90` : A module holding the model's integrator base class definition.
- `rk2_integrator.f90` : A module which contains the Heun integrator class for the model equations.
- `rk2_tl_integrator.f90` : Heun Tangent Linear (TL) model integrator class module.
- `rk2_ad_integrator.f90` : Heun Adjoint (AD) model integrator class module.
- `rk4_integrator.f90` : A module which contains the RK4 integrator class for the model equations.
- `rk4_tl_integrator.f90` : RK4 Tangent Linear (TL) model integrators module.
- `rk4_ad_integrator.f90` : Adjoint (AD) model integrators module.
- `Makefile` : The Makefile.
- `params.f90` : The model parameters classes module.
- `tl_ad_tensor.f90` : Tangent Linear (TL) and Adjoint (AD) model tensors class definition module.
- `test_tl_ad.f90` : Tests for the Tangent Linear (TL) and Adjoint (AD) model versions.
- `README.md` : A read me file.
- `LICENSE.txt` : The license text of the program.
- `util.f90` : A module with various useful functions.
- `tensor_def.f90` : Main tensor class utility module.
- `stat.f90` : A module implementing a statistics accumulator class.
- `params.nml` : A namelist to specify the model parameters.
- `int_params.nml` : A namelist to specify the integration parameters.
- `modeselection.nml` : A namelist to specify which spectral decomposition will be used.

Usage

The user first has to fill the `params.nml` and `int_params.nml` namelist files according to their needs. Indeed, model and integration parameters can be specified respectively in the `params.nml` and `int_params.nml` namelist files. Some examples related to already published article are available in the `params` folder.

The `modeselection.nml` namelist can then be filled :

- `NBOC` and `NBATM` specify the number of blocks that will be used in respectively the ocean and the atmosphere. Each block corresponds to a given x and y wavenumber.

- The OMS and AMS arrays are integer arrays which specify which wavenumbers of the spectral decomposition will be used in respectively the ocean and the atmosphere. Their shapes are OMS(NBOC,2) and AMS(NBOC,2).
- The first dimension specifies the number attributed by the user to the block and the second dimension specifies the x and the y wavenumbers.
- The VDDG model is given as a default example. It is described in:
 - Vannitsem, S., Demaeyer, J., De Cruz, L., and Ghil, M.: Low-frequency variability and heat transport in a low-order nonlinear coupled ocean-atmosphere model, *Physica D: Nonlinear Phenomena*, 309, 71-85, doi:10.1016/j.physd.2015.07.006, 2015.
- Note that the variables of the model are numbered according to the chosen order of the blocks.

Finally, the IC.nml file specifying the initial condition should be defined. To obtain an example of this configuration file corresponding to the model you have previously defined, simply delete the current IC.nml file (if it exists) and run the program :

```
./maooam
```

It will generate a new one and start with the 0 initial condition. If you want another initial condition, stop the program, fill the newly generated file and restart :

```
./maooam
```

It will generate two files :

- evol_field.dat : the recorded time evolution of the variables.
- mean_field.dat : the mean field (the climatology)

By default, the code uses the `rk2_integrator` class of integrator, which integrates the model with the `Heun algorithm`. However, by modifying the file `maooam.f90`, it is possible to use the `rk4_integrator` class which integrates the model with the `fourth-order Runge-Kutta algorithm (RK4)`. It is also possible to write an user-defined integrator by subclassing the base class `integrator_def::integrator`.

The tangent linear and adjoint models of MAOOAM are provided in the `tl_ad_tensor`, with integrators provided in the `rk2_tl_integrator`, `rk2_ad_integrator`, `rk4_tl_integrator` and `rk4_ad_integrator` modules. It is documented [here](#).

Implementation notes

As the system of differential equations is at most bilinear in y_j ($j = 1..n$), \mathbf{y} being the array of variables, it can be expressed as a tensor contraction :

$$\frac{dy_i}{dt} = \sum_{j,k=0}^{ndim} \mathcal{T}_{i,j,k} y_k y_j$$

with $y_0 = 1$.

The tensor `aotensor_def::aotensor` is the tensor \mathcal{T} that encodes the differential equations is composed so that:

- $\mathcal{T}_{i,j,k}$ contains the contribution of dy_i/dt proportional to $y_j y_k$.
- Furthermore, y_0 is always equal to 1, so that $\mathcal{T}_{i,0,0}$ is the constant contribution to dy_i/dt
- $\mathcal{T}_{i,j,0} + \mathcal{T}_{i,0,j}$ is the contribution to dy_i/dt which is linear in y_j .

The tensor `aotensor_def::atmooctensor` is composed as an upper triangular matrix (in the last two coordinates), and its computation uses the inner products defined in a `inprod_analytic::innerproducts` class.

The implementation is made using Fortran classes that are linked together. It turns the model into an instantiated object that can be reused, allowing the usage of several different model versions in the same program. See the page `model_def::model` for a sketch of how the various classes are linked together.

Final Remarks

The authors would like to thank Kris for help with the lua2fortran project. It has greatly reduced the amount of (error-prone) work.

No animals were harmed during the coding process.

Chapter 2

Modular arbitrary-order ocean-atmosphere model: The Tangent Linear and Adjoint model

Description :

The Tangent Linear and Adjoint model are implemented in the same way as the nonlinear model, with a tensor storing the different terms. The Tangent Linear (TL) tensor $\mathcal{T}_{i,j,k}^{TL}$ is defined as:

$$\mathcal{T}_{i,j,k}^{TL} = \mathcal{T}_{i,k,j} + \mathcal{T}_{i,j,k}$$

while the Adjoint (AD) tensor $\mathcal{T}_{i,j,k}^{AD}$ is defined as:

$$\mathcal{T}_{i,j,k}^{AD} = \mathcal{T}_{j,k,i} + \mathcal{T}_{j,i,k}.$$

where $\mathcal{T}_{i,j,k}$ is the tensor of the nonlinear model.

These two tensors are used to compute the trajectories of the models, with the equations

$$\frac{d\delta y_i}{dt} = \sum_{j=1}^{ndim} \sum_{k=0}^{ndim} \mathcal{T}_{i,j,k}^{TL} y_k^* \delta y_j.$$

$$-\frac{d\delta y_i}{dt} = \sum_{j=1}^{ndim} \sum_{k=0}^{ndim} \mathcal{T}_{i,j,k}^{AD} y_k^* \delta y_j.$$

where y^* is the point where the Tangent model is defined (with $y_0^* = 1$).

Implementation :

The two tensors are implemented in the module `tl_ad_tensor` and must be initialized inside a given `model_def::model` object with the method `model_def::init_tl_model` and `model_def::init_ad_model`. The tendencies are then given by the routine `model_def::tl_tendencies` and `model_def::ad_tendencies`. Integrators with the Heun method (RK2) or the 4th-order Runge-Kutta method are available with the classes `rk2_tl_integrator`, `rk2_ad_integrator`, `rk4_tl_integrator` and `rk4_ad_integrator`. An example on how to use it can be found in the test file `test_tl_ad.f90`

Chapter 3

Modules Index

3.1 Modules List

Here is a list of all documented modules with brief descriptions:

aotensor_def	The equation tensor $\mathcal{T}_{i,j,k}$ for the coupled ocean-atmosphere model with temperature which allows for an extensible set of modes in the ocean and in the atmosphere	13
inprod_analytic	Inner products between the truncated set of basis functions for the ocean and atmosphere streamfunction fields	15
integrator_def	Base class definition for the model's integrators	24
model_def	Module to articulate the model classes and define a model version	25
params	The model parameters module	34
rk2_ad_integrator	Adjoint (AD) model versions of MAOOAM. Second-order Runge-Kutta (RK2) integrators module	36
rk2_integrator	Module containing the second-order Runge-Kutta (RK2) integration routines	37
rk2_tl_integrator	Tangent Linear (TL) model versions of MAOOAM. Second-order Runge-Kutta (RK2) integrators module	39
rk4_ad_integrator	Adjoint (AD) model versions of MAOOAM. Fourth-order Runge-Kutta (RK4) integrators module	41
rk4_integrator	Module containing the fourth-order Runge-Kutta (RK4) integration routines	42
rk4_tl_integrator	Tangent Linear (TL) model versions of MAOOAM. Fourth-order Runge-Kutta (RK4) integrators module	44
stat	Statistics accumulators	45
tensor_def	Tensor utility module. Contains class to represent sparse tensors	50
tl_ad_tensor	Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Tensors definition module	63
util	Utility module	67

Chapter 4

Data Type Index

4.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

aotensor_def::atmoctensor	70
inprod_analytic::atmosphereinnerproducts	71
inprod_analytic::atmosphericwavenumber	72
integrator_def::clean_int	72
tensor_def::coolist	73
tensor_def::coolistelem	73
integrator_def::init_int	74
inprod_analytic::innerproducts	74
params::integrationparameters	75
integrator_def::integrator	76
Integrator	
rk2_integrator::rk2integrator	83
rk4_integrator::rk4integrator	86
model_def::model	76
params::modelconfiguration	77
params::modesconfiguration	78
inprod_analytic::oceanicwavenumber	78
inprod_analytic::oceaninnerproducts	79
params::physicsconfiguration	79
RK2Integrator	
rk2_ad_integrator::rk2adintegrator	82
rk2_tl_integrator::rk2tlintegrator	84
RK4Integrator	
rk4_ad_integrator::rk4adintegrator	85
rk4_tl_integrator::rk4tlintegrator	87
stat::stataccumulator	88
integrator_def::step_int	89
tensor_def::tensor	89
TITensor	
tl_ad_tensor::adtensor	69
tl_ad_tensor::tltensor	90

Chapter 5

Data Type Index

5.1 Data Types List

Here are the data types with brief descriptions:

tl_ad_tensor::adtensor	Tensor representation of the Adjoint tendencies	69
aotensor_def::atmoctensor	Class to hold the tensor $\mathcal{T}_{i,j,k}$ representation of the tendencies	70
inprod_analytic::atmosphereinnerproducts	Class holding the atmospheric inner products functions	71
inprod_analytic::atmosphericwavenumber	Atmospheric bloc specification object	72
integrator_def::clean_int	Abstract interface for the procedure to clean the integrator objects	72
tensor_def::coolist	Coordinate list. Type used to represent the sparse tensor	73
tensor_def::coolistelem	Coordinate list element type. Elementary elements of the sparse tensors	73
integrator_def::init_int	Abstract interface for the procedures initializing the integrator objects	74
inprod_analytic::innerproducts	Global class for the inner products. Contains also the modes informations	74
params::integrationparameters	The subclass containing the integration parameters	75
integrator_def::integrator	Base class to be subclassed to create a new integrator	76
model_def::model	Class to hold the components of a model version	76
params::modelconfiguration	The general class holding the model configuration	77
params::modesconfiguration	The subclass containing the modes parameters	78
inprod_analytic::oceanicwavenumber	Oceanic bloc specification object	78
inprod_analytic::oceaninnerproducts	Class holding the oceanic inner products functions	79
params::physicsconfiguration	The subclass containing the physical parameters of the model	79
rk2_ad_integrator::rk2adintegrator	Class for the Heun (RK2) AD integrator object	82

rk2_integrator::rk2integrator	
Class for the Heun (RK2) integrator object	83
rk2_tl_integrator::rk2tlintegrator	
Class for the Heun (RK2) TL integrator object	84
rk4_ad_integrator::rk4adintegrator	
Class for the fourth-order Runge-Kutta (RK4) AD integrator object	85
rk4_integrator::rk4integrator	
Class for the fourth-order Runge-Kutta (RK4) integrator object	86
rk4_tl_integrator::rk4tlintegrator	
Class for the fourth-order Runge-Kutta (RK4) TL integrator object	87
stat::stataccumulator	
Statistics accumulator objects class	88
integrator_def::step_int	
Abstract interface for the procedure to make the integrator compute a model's time step	89
tensor_def::tensor	
General class to represent a sparse tensor	89
tl_ad_tensor::tltensor	
Tensor representation of the Tangent Linear tendencies	90

Chapter 6

Module Documentation

6.1 aotensor_def Module Reference

The equation tensor $\mathcal{T}_{i,j,k}$ for the coupled ocean-atmosphere model with temperature which allows for an extensible set of modes in the ocean and in the atmosphere.

Data Types

- type [atmoctensor](#)
Class to hold the tensor $\mathcal{T}_{i,j,k}$ representation of the tendencies.

Functions/Subroutines

- subroutine [init_aotensor](#) (aot, model_configuration, inprods)
Subroutine to initialise the AtmOcTensor tensor.
- subroutine [delete_aotensor](#) (aot)
Subroutine to clean a AtmOcTensor tensor.

6.1.1 Detailed Description

The equation tensor $\mathcal{T}_{i,j,k}$ for the coupled ocean-atmosphere model with temperature which allows for an extensible set of modes in the ocean and in the atmosphere.

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6.1.2 Function/Subroutine Documentation

6.1.2.1 delete_aotensor()

```
subroutine aotensor_def::delete_aotensor (  
    class(atmoctensor), intent(inout) aot ) [private]
```

Subroutine to clean a AtmOcTensor tensor.

Parameters

in, out	<i>aot</i>	The AtmOcTensor tensor object to initialize.
---------	------------	--

Definition at line 277 of file aotensor_def.f90.

```

277     CLASS(atmoctensor), INTENT(INOUT) :: aot
278
279     IF (allocated(aot%count_elems)) DEALLOCATE(aot%count_elems)
280
281     CALL aot%tensor%clean
282     NULLIFY(aot%ndim)
283     NULLIFY(aot%natm)
284     NULLIFY(aot%noc)
285
286     aot%initialized = .false.
287

```

6.1.2.2 init_aotensor()

```

subroutine aotensor_def::init_aotensor (
    class(atmoctensor), intent(inout) aot,
    class(modelconfiguration), intent(in), target model_configuration,
    class(innerproducts), intent(in), target inprods ) [private]

```

Subroutine to initialise the AtmOcTensor tensor.

Parameters

in, out	<i>aot</i>	The AO tensor object to initialize.
in	<i>model_configuration</i>	A model configuration object to initialize the model tensor with.
in	<i>inprods</i>	A model inner products object to initialize the model with.

Definition at line 221 of file aotensor_def.f90.

```

221     CLASS(atmoctensor), INTENT(INOUT) :: aot
222     CLASS(modelconfiguration), INTENT(IN), TARGET :: model_configuration
223     CLASS(innerproducts), INTENT(IN), TARGET :: inprods
224
225     INTEGER :: i
226     INTEGER :: allocstat
227
228     IF (.NOT.model_configuration%initialized) THEN
229         print*, "Warning: Model configuration not initialized."
230         print*, "Aborting aotensor initialization."
231         RETURN
232     END IF
233
234     IF (.NOT.inprods%initialized) THEN
235         print*, "Warning: Inner products not initialized."
236         print*, "Aborting aotensor initialization."
237         RETURN
238     END IF
239
240     aot%ndim => model_configuration%modes%ndim
241     aot%natm => model_configuration%modes%natm
242     aot%noc => model_configuration%modes%noc
243
244     ALLOCATE(aot%count_elems(aot%ndim), stat=allocstat)
245     IF (allocstat /= 0) THEN
246         print*, "*** init_aotensor: Problem with allocation! ***"

```

```

247     stop "Exiting ..."
248 END IF
249 aot%count_elems=0
250
251 CALL aot%tensor%init(aot%ndim)
252
253 aot%operation => ao_add_count
254 CALL aot%compute_tensor(model_configuration, inprods)
255
256 DO i=1,aot%ndim
257     ALLOCATE(aot%tensor%t(i)%elems(aot%count_elems(i)), stat=allocstat)
258     IF (allocstat /= 0) THEN
259         print*, "*** init_aotensor: Problem with allocation! ***"
260         stop "Exiting ..."
261     END IF
262
263 END DO
264
265 aot%operation => ao_coeff
266 CALL aot%compute_tensor(model_configuration, inprods)
267
268 CALL aot%tensor%simplify
269
270 aot%initialized = .true.
271

```

6.2 inprod_analytic Module Reference

Inner products between the truncated set of basis functions for the ocean and atmosphere streamfunction fields.

Data Types

- type [atmosphereinnerproducts](#)
Class holding the atmospheric inner products functions.
- type [atmosphericwavenumber](#)
Atmospheric bloc specification object.
- type [innerproducts](#)
Global class for the inner products. Contains also the modes informations.
- type [oceanicwavenumber](#)
Oceanic bloc specification object.
- type [oceaninnerproducts](#)
Class holding the oceanic inner products functions.

Functions/Subroutines

- real(kind=8) function [calculate_a](#) (self, i, j)
Eigenvalues of the Laplacian (atmospheric)
- real(kind=8) function [calculate_b](#) (self, i, j, k)
Streamfunction advection terms (atmospheric)
- real(kind=8) function [calculate_c_atm](#) (self, i, j)
Beta term for the atmosphere.
- real(kind=8) function [calculate_d](#) (self, i, j)
Forcing of the ocean on the atmosphere.
- real(kind=8) function [calculate_g](#) (self, i, j, k)
Temperature advection terms (atmospheric)
- real(kind=8) function [calculate_s](#) (self, i, j)
Forcing (thermal) of the ocean on the atmosphere.
- real(kind=8) function [calculate_k](#) (self, i, j)

- *Forcing of the atmosphere on the ocean.*
real(kind=8) function [calculate_m](#) (self, i, j)
- *Forcing of the ocean fields on the ocean.*
real(kind=8) function [calculate_n](#) (self, i, j)
- *Beta term for the ocean.*
real(kind=8) function [calculate_o](#) (self, i, j, k)
- *Temperature advection term (passive scalar)*
real(kind=8) function [calculate_c_oc](#) (self, i, j, k)
- *Streamfunction advection terms (oceanic)*
real(kind=8) function [calculate_w](#) (self, i, j)
- *Short-wave radiative forcing of the ocean.*
subroutine [init_inner_products](#) (inner_products, model_config)
- *Initialization routine for the inner products functions.*
subroutine [delete_inner_products](#) (inner_products)
- *Routine to clean a inner products global object.*

6.2.1 Detailed Description

Inner products between the truncated set of basis functions for the ocean and atmosphere streamfunction fields.

Remarks

These are partly calculated using the analytical expressions from Cehelsky, P., & Tung, K. K. : Theories of multiple equilibria and weather regimes-A critical reexamination. Part II: Baroclinic two-layer models. Journal of the atmospheric sciences, 44(21), 3282-3303, 1987.

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6.2.2 Function/Subroutine Documentation

6.2.2.1 [calculate_a\(\)](#)

```
real(kind=8) function inprod_analytic::calculate_a (
    class(atmosphereinnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j ) [private]
```

Eigenvalues of the Laplacian (atmospheric)

$$a_{i,j} = (F_i, \nabla^2 F_j).$$

Definition at line 179 of file inprod_analytic.f90.

```
179    CLASS(atmosphereinnerproducts), INTENT(IN) :: self
180    INTEGER, INTENT(IN) :: i,j
181    TYPE(atmosphericwavenumber) :: ti
182
183    calculate_a = 0.d0
184    IF (i==j) THEN
185        ti = self%inner_products%awavenum(i)
186        calculate_a = -(self%inner_products%model_config%physics%n**2) * ti%Nx**2 - ti%Ny**2
187    END IF
```


6.2.2.2 calculate_b()

```
real(kind=8) function inprod_analytic::calculate_b (
    class(atmosphereinnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j,
    integer, intent(in) k ) [private]
```

Streamfunction advection terms (atmospheric)

$$b_{i,j,k} = (F_i, J(F_j, \nabla^2 F_k)) .$$

Definition at line 194 of file inprod_analytic.f90.

```
194     CLASS(atmosphereinnerproducts), INTENT(IN) :: self
195     INTEGER, INTENT(IN) :: i,j,k
196
197     calculate_b = self%a(k,k) * self%g(i,j,k)
198
```

6.2.2.3 calculate_c_atm()

```
real(kind=8) function inprod_analytic::calculate_c_atm (
    class(atmosphereinnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j ) [private]
```

Beta term for the atmosphere.

$$c_{i,j} = (F_i, \partial_x F_j) .$$

Definition at line 205 of file inprod_analytic.f90.

```
205     CLASS(atmosphereinnerproducts), INTENT(IN) :: self
206     INTEGER, INTENT(IN) :: i,j
207     TYPE(atmosphericwavenumber) :: ti, tj
208
209     ti = self%inner_products%awavenum(i)
210     tj = self%inner_products%awavenum(j)
211     calculate_c_atm = 0.d0
212     IF ((ti%typ == "K") .AND. (tj%typ == "L")) THEN
213         calculate_c_atm = ti%M * delta(ti%M - tj%H) * delta(ti%P - tj%P)
214     ELSE IF ((ti%typ == "L") .AND. (tj%typ == "K")) THEN
215         ti = self%inner_products%awavenum(j)
216         tj = self%inner_products%awavenum(i)
217         calculate_c_atm = - ti%M * delta(ti%M - tj%H) * delta(ti%P - tj%P)
218     END IF
219     calculate_c_atm = self%inner_products%model_config%physics%n * calculate_c_atm
```

6.2.2.4 calculate_c_oc()

```
real(kind=8) function inprod_analytic::calculate_c_oc (
    class(oceaninnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j,
    integer, intent(in) k ) [private]
```

Streamfunction advection terms (oceanic)

$$C_{i,j,k} = (\eta_i, J(\eta_j, \nabla^2 \eta_k)) .$$

Definition at line 438 of file inprod_analytic.f90.

```
438     CLASS(oceaninnerproducts), INTENT(IN) :: self
439     INTEGER, INTENT(IN) :: i,j,k
440
441     calculate_c_oc = self%M(k,k) * self%O(i,j,k)
442
```

6.2.2.5 calculate_d()

```
real(kind=8) function inprod_analytic::calculate_d (
    class(atmosphereinnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j ) [private]
```

Forcing of the ocean on the atmosphere.

$$d_{i,j} = (F_i, \nabla^2 \eta_j) .$$

Definition at line 226 of file inprod_analytic.f90.

```
226     CLASS(atmosphereinnerproducts), INTENT(IN) :: self
227     INTEGER, INTENT(IN) :: i,j
228
229     calculate_d=self%s(i,j) * self%inner_products%ocean%M(j,j)
230
```

6.2.2.6 calculate_g()

```

real(kind=8) function inprod_analytic::calculate_g (
    class(atmosphereinnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j,
    integer, intent(in) k ) [private]

```

Temperature advection terms (atmospheric)

$$g_{i,j,k} = (F_i, J(F_j, F_k)).$$

Definition at line 237 of file inprod_analytic.f90.

```

237  CLASS(atmosphereinnerproducts), INTENT(IN) :: self
238  INTEGER, INTENT(IN) :: i,j,k
239  TYPE(atmosphericwavenumber) :: ti,tj,tk
240  REAL(KIND=8) :: val,vb1, vb2, vs1, vs2, vs3, vs4
241  INTEGER, DIMENSION(3) :: a,b
242  INTEGER, DIMENSION(3,3) :: w
243  CHARACTER, DIMENSION(3) :: s
244  INTEGER :: par
245
246  ti = self%inner_products%awavenum(i)
247  tj = self%inner_products%awavenum(j)
248  tk = self%inner_products%awavenum(k)
249
250  a(1)=i
251  a(2)=j
252  a(3)=k
253
254  val=0.d0
255
256  IF ((ti%typ == "L") .AND. (tj%typ == "L") .AND. (tk%typ == "L")) THEN
257
258      CALL piksrt(3,a,par)
259
260      ti = self%inner_products%awavenum(a(1))
261      tj = self%inner_products%awavenum(a(2))
262      tk = self%inner_products%awavenum(a(3))
263
264      vs3 = s3(tj%P,tk%P,tj%H,tk%H)
265      vs4 = s4(tj%P,tk%P,tj%H,tk%H)
266      val = vs3 * ((delta(tk%H - tj%H - ti%H) - delta(tk%H &
267          &- tj%H + ti%H)) * delta(tk%P + tj%P - ti%P) + &
268          & delta(tk%H + tj%H - ti%H) * (delta(tk%P - tj%P &
269          & + ti%P) - delta(tk%P - tj%P - ti%P))) + vs4 * &
270          & ((delta(tk%H + tj%H - ti%H) * delta(tk%P - tj%
271          &%P - ti%P)) + (delta(tk%H - tj%H + ti%H) - &
272          & delta(tk%H - tj%H - ti%H)) * (delta(tk%P - tj%
273          &%P - ti%P) - delta(tk%P - tj%P + ti%P)))
274  ELSE
275
276      s(1)=ti%typ
277      s(2)=tj%typ
278      s(3)=tk%typ
279
280      w(1,:)=isin("A",s)
281      w(2,:)=isin("K",s)
282      w(3,:)=isin("L",s)
283
284      IF (any(w(1,:)/=0) .AND. any(w(2,:)/=0) .AND. any(w(3,:)/=0)) THEN
285          b=w(:,1)
286          ti = self%inner_products%awavenum(a(b(1)))
287          tj = self%inner_products%awavenum(a(b(2)))
288          tk = self%inner_products%awavenum(a(b(3)))
289          call piksrt(3,b,par)
290          vb1 = b1(ti%P,tj%P,tk%P)
291          vb2 = b2(ti%P,tj%P,tk%P)
292          val = -2 * sqrt(2.) / self%inner_products%model_config%physics%pi * tj%M * delta(tj%M - tk%H) *
293          flambda(ti%P + tj%P + tk%P)
294          IF (val /= 0.d0) val = val * (vb1**2 / (vb1**2 - 1) - vb2**2 / (vb2**2 - 1))
295      ELSEIF ((w(2,2)/=0) .AND. (w(2,3)=0) .AND. any(w(3,:)/=0)) THEN
296          ti = self%inner_products%awavenum(a(w(2,1)))
297          tj = self%inner_products%awavenum(a(w(2,2)))
298          tk = self%inner_products%awavenum(a(w(3,1)))
299          b(1)=w(2,1)
300          b(2)=w(2,2)
301          b(3)=w(3,1)

```

```

301      call piksrt(3,b,par)
302      vs1 = s1(tj%P,tk%P,tj%M,tk%H)
303      vs2 = s2(tj%P,tk%P,tj%M,tk%H)
304      val = vs1 * (delta(ti%M - tk%H - tj%M) * delta(ti%P - &
305        & tk%P + tj%P) - delta(ti%M- tk%H - tj%M) * &
306        & delta(ti%P + tk%P - tj%P) + (delta(tk%H - tj%M&
307        & + ti%M) + delta(tk%H - tj%M - ti%M)) * &
308        & delta(tk%P + tj%P - ti%P)) + vs2 * (delta(ti%M&
309        & - tk%H - tj%M) * delta(ti%P - tk%P - tj%P) + &
310        & (delta(tk%H - tj%M - ti%M) + delta(ti%M + tk%H&
311        & - tj%M)) * (delta(ti%P - tk%P + tj%P) - &
312        & delta(tk%P - tj%P + ti%P)))
313      ENDIF
314    ENDIF
315    calculate_g=par*val*self%inner_products%model_config%physics%n
316

```

6.2.2.7 calculate_k()

```

real(kind=8) function inprod_analytic::calculate_k (
    class(oceaninnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j ) [private]

```

Forcing of the atmosphere on the ocean.

$$K_{i,j} = (\eta_i, \nabla^2 F_j) .$$

Definition at line 357 of file inprod_analytic.f90.

```

357      CLASS(oceaninnerproducts), INTENT(IN) :: self
358      INTEGER, INTENT(IN) :: i,j
359
360      calculate_k = self%inner_products%atmos%(j,i) * self%inner_products%atmos%(j,j)

```

6.2.2.8 calculate_m()

```

real(kind=8) function inprod_analytic::calculate_m (
    class(oceaninnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j ) [private]

```

Forcing of the ocean fields on the ocean.

$$M_{i,j} = (\eta_i, \nabla^2 \eta_j) .$$

Definition at line 367 of file inprod_analytic.f90.

```

367      CLASS(oceaninnerproducts), INTENT(IN) :: self
368      INTEGER, INTENT(IN) :: i,j
369      TYPE(oceanicwavenumber) :: di
370
371      calculate_m=0.d0
372      IF (i==j) THEN
373          di = self%inner_products%owavenum(i)
374          calculate_m = -(self%inner_products%model_config%physics%n**2) * di%Nx**2 - di%Ny**2
375      END IF

```

6.2.2.9 calculate_n()

```
real(kind=8) function inprod_analytic::calculate_n (
    class(oceaninnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j ) [private]
```

Beta term for the ocean.

$$N_{i,j} = (\eta_i, \partial_x \eta_j).$$

Definition at line 382 of file inprod_analytic.f90.

```
382 CLASS(oceaninnerproducts), INTENT(IN) :: self
383 INTEGER, INTENT(IN) :: i,j
384 TYPE(oceanicwavenumber) :: di,dj
385 REAL(KIND=8) :: val
386
387 di = self%inner_products%owavenum(i)
388 dj = self%inner_products%owavenum(j)
389 calculate_n = 0.d0
390 IF (dj%H/=di%H) THEN
391     val = delta(di%P - dj%P) * flambda(di%H + dj%H)
392     calculate_n = val * (-2) * dj%H * di%H * self%inner_products%model_config%physics%n
393     calculate_n = calculate_n / ((dj%H**2 - di%H**2) * self%inner_products%model_config%physics%pi)
394 ENDIF
395
```

6.2.2.10 calculate_o()

```
real(kind=8) function inprod_analytic::calculate_o (
    class(oceaninnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j,
    integer, intent(in) k ) [private]
```

Temperature advection term (passive scalar)

$$O_{i,j,k} = (\eta_i, J(\eta_j, \eta_k)).$$

Definition at line 402 of file inprod_analytic.f90.

```
402 CLASS(oceaninnerproducts), INTENT(IN) :: self
403 INTEGER, INTENT(IN) :: i,j,k
404 TYPE(oceanicwavenumber) :: di,dj,dk
405 REAL(KIND=8) :: vs3,vs4,val
406 INTEGER, DIMENSION(3) :: a
407 INTEGER :: par
408
409 val=0.d0
410
411 a(1)=i
412 a(2)=j
413 a(3)=k
414
415 CALL piksrt(3,a,par)
416
417 di = self%inner_products%owavenum(a(1))
418 dj = self%inner_products%owavenum(a(2))
419 dk = self%inner_products%owavenum(a(3))
420
421 vs3 = s3(dj%P,dk%P,dj%H,dk%H)
422 vs4 = s4(dj%P,dk%P,dj%H,dk%H)
423 val = vs3*((delta(dk%H - dj%H - di%H) - delta(dk%H - dj%
424 &H + di%H)) * delta(dk%P + dj%P - di%P) + delta(dk%
425 &H + dj%H - di%H) * (delta(dk%P - dj%P + di%P) -&
426 & delta(dk%P - dj%P - di%P))) + vs4 * ((delta(dk%H &
427 & + dj%H - di%H) * delta(dk%P - dj%P - di%P)) +&
428 & (delta(dk%H - dj%H + di%H) - delta(dk%H - dj%H -&
429 & di%H)) * (delta(dk%P - dj%P - di%P) - delta(dk%P &
430 & - dj%P + di%P)))
431 calculate_o = par * val * self%inner_products%model_config%physics%n / 2
```

6.2.2.11 calculate_s()

```
real(kind=8) function inprod_analytic::calculate_s (
    class(atmosphereinnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j ) [private]
```

Forcing (thermal) of the ocean on the atmosphere.

$$s_{i,j} = (F_i, \eta_j).$$

Definition at line 323 of file inprod_analytic.f90.

```
323  CLASS(atmosphereinnerproducts), INTENT(IN) :: self
324  INTEGER, INTENT(IN) :: i,j
325  TYPE(atmosphericwavenumber) :: ti
326  TYPE(oceanicwavenumber) :: dj
327  REAL(KIND=8) :: val
328
329  ti = self%inner_products%awavenum(i)
330  dj = self%inner_products%owavenum(j)
331  val=0.d0
332  IF (ti%typ == "A") THEN
333      val = flambda(dj%H) * flambda(dj%P + ti%P)
334      IF (val /= 0.d0) THEN
335          val = val*8*sqrt(2.)*dj%P/(self%inner_products%model_config%physics%pi**2 * (dj%P**2 - ti%P**2) *
          dj%H)
336      END IF
337  ELSEIF (ti%typ == "K") THEN
338      val = flambda(2 * ti%M + dj%H) * delta(dj%P - ti%P)
339      IF (val /= 0.d0) THEN
340          val = val*4*dj%H/(self%inner_products%model_config%physics%pi * (-4 * ti%M**2 + dj%H**2))
341      END IF
342  ELSEIF (ti%typ == "L") THEN
343      val = delta(dj%P - ti%P) * delta(2 * ti%H - dj%H)
344  END IF
345  calculate_s=val
346
```

6.2.2.12 calculate_w()

```
real(kind=8) function inprod_analytic::calculate_w (
    class(oceaninnerproducts), intent(in) self,
    integer, intent(in) i,
    integer, intent(in) j ) [private]
```

Short-wave radiative forcing of the ocean.

$$W_{i,j} = (\eta_i, F_j).$$

Definition at line 449 of file inprod_analytic.f90.

```
449  CLASS(oceaninnerproducts), INTENT(IN) :: self
450  INTEGER, INTENT(IN) :: i,j
451
452  calculate_w = self%inner_products%atmos%(j,i)
453
```

6.2.2.13 delete_inner_products()

```
subroutine inprod_analytic::delete_inner_products (
    class(innerproducts), intent(inout), target inner_products ) [private]
```

Routine to clean a inner products global object.

Parameters

in, out	<i>inner_products</i>	Inner products global object to initialize
---------	-----------------------	--

Definition at line 558 of file inprod_analytic.f90.

```

558     CLASS(innerproducts), INTENT(INOUT), TARGET :: inner_products
559
560     IF (allocated(inner_products%owavenum)) DEALLOCATE(inner_products%owavenum)
561     IF (allocated(inner_products%awavenum)) DEALLOCATE(inner_products%awavenum)
562
563     inner_products%initialized = .false.
564
```

6.2.2.14 init_inner_products()

```

subroutine inprod_analytic::init_inner_products (
    class(innerproducts), intent(inout), target inner_products,
    class(modelconfiguration), intent(in), target model_config ) [private]
```

Initialization routine for the inner products functions.

Parameters

in, out	<i>inner_products</i>	Inner products global object to initialize
in	<i>model_config</i>	Global model configuration object to initialize the inner products with

Definition at line 466 of file inprod_analytic.f90.

```

466     CLASS(innerproducts), INTENT(INOUT), TARGET :: inner_products
467     CLASS(modelconfiguration), INTENT(IN), TARGET :: model_config
468
469     TYPE(innerproducts), POINTER :: ips
470
471     INTEGER :: i,j
472     INTEGER :: allocstat
473
474     ips => inner_products
475
476     IF (.NOT.model_config%initialized) THEN
477         print*, "Warning: Model configuration not initialized."
478         print*, "Aborting inner products initialization."
479         RETURN
480     END IF
481
482     ! Definition of the types and wave numbers tables
483
484     IF (allocated(ips%owavenum)) DEALLOCATE(ips%owavenum)
485     ALLOCATE(ips%owavenum(model_config%modes%noc), stat=allocstat)
486     IF (allocstat /= 0) THEN
487         print*, "*** init_inner_products: Problem with allocation! ***"
488         stop "Exiting ..."
489     END IF
490
491
492     IF (allocated(ips%awavenum)) DEALLOCATE(ips%awavenum)
493     ALLOCATE(ips%awavenum(model_config%modes%natm), stat=allocstat)
494     IF (allocstat /= 0) THEN
495         print*, "*** init_inner_products: Problem with allocation! ***"
496         stop "Exiting ..."
497     END IF
498
```

```

499     j=0
500     DO i=1,model_config%modes%nbatm
501         IF (model_config%modes%ams(i,1)==1) THEN
502             ips%awavenum(j+1)%typ='A'
503             ips%awavenum(j+2)%typ='K'
504             ips%awavenum(j+3)%typ='L'
505
506             ips%awavenum(j+1)%P=model_config%modes%ams(i,2)
507             ips%awavenum(j+2)%M=model_config%modes%ams(i,1)
508             ips%awavenum(j+2)%P=model_config%modes%ams(i,2)
509             ips%awavenum(j+3)%H=model_config%modes%ams(i,1)
510             ips%awavenum(j+3)%P=model_config%modes%ams(i,2)
511
512             ips%awavenum(j+1)%Ny=REAL(model_config%modes%ams(i,2))
513             ips%awavenum(j+2)%Nx=REAL(model_config%modes%ams(i,1))
514             ips%awavenum(j+2)%Ny=REAL(model_config%modes%ams(i,2))
515             ips%awavenum(j+3)%Nx=REAL(model_config%modes%ams(i,1))
516             ips%awavenum(j+3)%Ny=REAL(model_config%modes%ams(i,2))
517
518             j=j+3
519         ELSE
520             ips%awavenum(j+1)%typ='K'
521             ips%awavenum(j+2)%typ='L'
522
523             ips%awavenum(j+1)%M=model_config%modes%ams(i,1)
524             ips%awavenum(j+1)%P=model_config%modes%ams(i,2)
525             ips%awavenum(j+2)%H=model_config%modes%ams(i,1)
526             ips%awavenum(j+2)%P=model_config%modes%ams(i,2)
527
528             ips%awavenum(j+1)%Nx=REAL(model_config%modes%ams(i,1))
529             ips%awavenum(j+1)%Ny=REAL(model_config%modes%ams(i,2))
530             ips%awavenum(j+2)%Nx=REAL(model_config%modes%ams(i,1))
531             ips%awavenum(j+2)%Ny=REAL(model_config%modes%ams(i,2))
532
533             j=j+2
534
535         END IF
536     ENDDO
537
538     DO i=1,model_config%modes%noc
539         ips%owavenum(i)%H=model_config%modes%oms(i,1)
540         ips%owavenum(i)%P=model_config%modes%oms(i,2)
541
542         ips%owavenum(i)%Nx=model_config%modes%oms(i,1)/2.d0
543         ips%owavenum(i)%Ny=model_config%modes%oms(i,2)
544
545     ENDDO
546
547     inner_products%model_config => model_config
548     inner_products%atmos%inner_products => inner_products
549     inner_products%ocean%inner_products => inner_products
550
551     inner_products%initialized = .true.
552

```

6.3 integrator_def Module Reference

Base class definition for the model's integrators.

Data Types

- interface [clean_int](#)
Abstract interface for the procedure to clean the integrator objects.
- interface [init_int](#)
Abstract interface for the procedures initializing the integrator objects.
- type [integrator](#)
Base class to be subclassed to create a new integrator.
- interface [step_int](#)
Abstract interface for the procedure to make the integrator compute a model's time step.

6.3.1 Detailed Description

Base class definition for the model's integrators.

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6.4 model_def Module Reference

Module to articulate the model classes and define a model version.

Data Types

- type `model`
Class to hold the components of a model version.

Functions/Subroutines

- type(`tensor`) function `jacobian` (imodel, ystar)
Compute the Jacobian of MAOOAM in point y^ and return a tensor object.*
- real(kind=8) function, dimension(imodel%ndim, imodel%ndim) `jacobian_mat` (imodel, ystar)
Compute the Jacobian of MAOOAM in point y^ and return a tensor object.*
- subroutine `tendencies` (imodel, t, y, res)
Routine computing the tendencies of the model.
- subroutine `ad_tendencies` (imodel, t, ystar, deltat, res)
Tendencies for the AD model of MAOOAM in point y^ for a perturbation δy .*
- subroutine `tl_tendencies` (imodel, t, ystar, deltat, res)
Tendencies for the TL model of MAOOAM in point y^ for a perturbation δy .*
- subroutine `init_model` (imodel, physics_nml, mode_nml, int_nml)
Subroutine to initialize the model object from NML files.
- subroutine `delete_model` (imodel)
Subroutine to clean a model object.
- subroutine `init_tl_model` (imodel)
Subroutine to initialize the TL tendencies tensor of a model.
- subroutine `init_ad_model` (imodel)
Subroutine to initialize the AD tendencies tensor of a model.
- real(kind=8) function, dimension(0:imodel%ndim) `load_ic` (imodel, filename)
Subroutine to initialize the AD tendencies tensor of a model.

6.4.1 Detailed Description

Module to articulate the model classes and define a model version.

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6.4.2 Function/Subroutine Documentation

6.4.2.1 `ad_tendencies()`

```
subroutine model_def::ad_tendencies (
    class(model), intent(in) imodel,
    real(kind=8), intent(in) t,
    real(kind=8), dimension(0:imodel%ndim), intent(in) ystar,
    real(kind=8), dimension(0:imodel%ndim), intent(in) deltay,
    real(kind=8), dimension(0:imodel%ndim), intent(out) res ) [private]
```

Tendencies for the AD model of MAOOAM in point y^* for a perturbation δy .

Parameters

in	<i>imodel</i>	Model to compute the AD tendencies of.
in	<i>t</i>	time
in	<i>ystar</i>	Vector y^* (current point in model's trajectory).
in	<i>deltay</i>	Vector δy , i.e. the perturbation of the variables at time <i>t</i> .
out	<i>res</i>	Vector to store the tendencies.

Definition at line 99 of file `model_def.f90`.

```
99      CLASS(model), INTENT(IN) :: imodel
100     REAL(KIND=8), INTENT(IN) :: t
101     REAL(KIND=8), DIMENSION(0:imodel%ndim), INTENT(IN) :: ystar,deltay
102     REAL(KIND=8), DIMENSION(0:imodel%ndim), INTENT(OUT) :: res
103     CALL imodel%adtensor%tensor%sparse_mul3(deltay, ystar, res)
```

6.4.2.2 `delete_model()`

```
subroutine model_def::delete_model (
    class(model), intent(inout) imodel ) [private]
```

Subroutine to clean a model object.

Parameters

in, out	<i>imodel</i>	Model object to clean.
---------	---------------	------------------------

Definition at line 152 of file `model_def.f90`.

```
152     CLASS(model), INTENT(INOUT) :: imodel
153
154     NULLIFY(imodel%ndim)
155
156     CALL imodel%model_configuration%clean
```

```

157     CALL imodel%inner_products%clean
158     CALL imodel%aotensor%clean
159
160     CALL imodel%tltensor%clean
161     CALL imodel%adtensor%clean
162
163     imodel%initialized = .false.
164

```

6.4.2.3 init_ad_model()

```

subroutine model_def::init_ad_model (
    class(model), intent(inout), target imodel ) [private]

```

Subroutine to initialize the AD tendencies tensor of a model.

Parameters

in, out	<i>imodel</i>	Model object to initialize.
---------	---------------	-----------------------------

Definition at line 186 of file model_def.f90.

```

186     CLASS(model), INTENT(INOUT), TARGET :: imodel
187
188     CALL imodel%adtensor%clean
189
190     IF (.NOT.imodel%initialized) THEN
191         print*, "*** init_ad_model: Trying to initialize AD model of an uninitialized model ! ***"
192         print*, "Please first initialize the model before trying to initialize the AD model."
193         print*, "Aborting operation."
194         RETURN
195     END IF
196     CALL imodel%adtensor%init(imodel%aotensor)

```

6.4.2.4 init_model()

```

subroutine model_def::init_model (
    class(model), intent(inout), target imodel,
    character(len=*), intent(in), optional physics_nml,
    character(len=*), intent(in), optional mode_nml,
    character(len=*), intent(in), optional int_nml ) [private]

```

Subroutine to initialize the model object from NML files.

Parameters

in, out	<i>imodel</i>	Model object to initialize.
in	<i>physics_nml</i>	Physical parameters namelist filename
in	<i>mode_nml</i>	Modes configuration namelist filename
in	<i>int_nml</i>	Numerical integration parameters namelist filename

Remarks

If no NML filenames are provided, it will assume that the standard filenames of the model NML have to be used (e.g. "params.nml", "modeselection.nml" and "int_params.nml").

Definition at line 127 of file model_def.f90.

```

127     CLASS(model), INTENT(INOUT), TARGET :: imodel
128     CHARACTER(LEN=*), INTENT(IN), OPTIONAL :: physics_nml
129     CHARACTER(LEN=*), INTENT(IN), OPTIONAL :: mode_nml
130     CHARACTER(LEN=*), INTENT(IN), OPTIONAL :: int_nml
131     LOGICAL :: ok
132
133     CALL imodel%model_configuration%clean
134     CALL imodel%inner_products%clean
135     CALL imodel%aotensor%clean
136
137     CALL imodel%model_configuration%init(physics_nml=physics_nml, mode_nml=mode_nml, int_nml=int_nml)
138     CALL imodel%inner_products%init(imodel%model_configuration)
139     CALL imodel%aotensor%init(imodel%model_configuration, imodel%inner_products)
140
141     imodel%ndim => imodel%model_configuration%modes%ndim
142
143     ok = imodel%model_configuration%initialized .AND. imodel%inner_products%initialized .AND. imodel%
%aotensor%initialized
144
145     if (ok) imodel%initialized = .true.
146

```

6.4.2.5 init_tl_model()

```

subroutine model_def::init_tl_model (
    class(model), intent(inout), target imodel ) [private]

```

Subroutine to initialize the TL tendencies tensor of a model.

Parameters

in, out	<i>imodel</i>	Model object to initialize.
---------	---------------	-----------------------------

Definition at line 170 of file model_def.f90.

```

170     CLASS(model), INTENT(INOUT), TARGET :: imodel
171
172     CALL imodel%tltensor%clean
173
174     IF (.NOT.imodel%initialized) THEN
175         print*, "*** init_tl_model: Trying to initialize TL model of an uninitialized model ! ***"
176         print*, "Please first initialize the model before trying to initialize the TL model."
177         print*, "Aborting operation."
178         RETURN
179     END IF
180     CALL imodel%tltensor%init(imodel%aotensor)

```

6.4.2.6 jacobian()

```

type(tensor) function model_def::jacobian (
    class(model), intent(in) imodel,
    real(kind=8), dimension(0:imodel%ndim), intent(in) ystar )

```

Compute the Jacobian of MAOOAM in point \mathbf{y}^* and return a tensor object.

Parameters

in	<i>imodel</i>	Model to return the Jacobian of.
in	<i>ystar</i>	Vector y^* at which the jacobian should be evaluated.

Returns

Jacobian in tensor form (table of tuples {i,j,0,value}).

Definition at line 59 of file model_def.f90.

```

59     CLASS(model), INTENT(IN) :: imodel
60     REAL(KIND=8), DIMENSION(0:imodel%ndim), INTENT(IN) :: ystar
61     TYPE(tensor) :: jacobian
62     CALL jacobian%init(imodel%ndim)
63     CALL imodel%aotensor%tensor%jsparse_mul(ystar, jacobian)

```

6.4.2.7 jacobian_mat()

```

real(kind=8) function, dimension(imodel%ndim,imodel%ndim) model_def::jacobian_mat (
    class(model), intent(in) imodel,
    real(kind=8), dimension(0:imodel%ndim), intent(in) ystar ) [private]

```

Compute the Jacobian of MAOOAM in point y^* and return a tensor object.

Parameters

in	<i>imodel</i>	Model to return the Jacobian of.
in	<i>ystar</i>	Vector y^* at which the jacobian should be evaluated.

Returns

Jacobian in matrix form.

Definition at line 71 of file model_def.f90.

```

71     CLASS(model), INTENT(IN) :: imodel
72     REAL(KIND=8), DIMENSION(0:imodel%ndim), INTENT(IN) :: ystar
73     REAL(KIND=8), DIMENSION(imodel%ndim,imodel%ndim) :: jacobian_mat
74     CALL imodel%aotensor%tensor%jsparse_mul_mat(ystar, jacobian_mat)

```

6.4.2.8 load_ic()

```

real(kind=8) function, dimension(0:imodel%ndim) model_def::load_ic (
    class(model), intent(in), target imodel,
    character(len=*), intent(in), optional filename ) [private]

```

Subroutine to initialize the AD tendencies tensor of a model.

Parameters

in	<i>imodel</i>	Model object for wich to load the initial condition.
in	<i>filename</i>	Filename of the initial condition NML file.

Returns

A vector with the initial condition.

Definition at line 204 of file model_def.f90.

```

204  CLASS(model), INTENT(IN), TARGET :: imodel
205  CHARACTER(LEN=*) , INTENT(IN), OPTIONAL :: filename
206  REAL(KIND=8), DIMENSION(0:imodel%ndim) :: ic
207
208  INTEGER :: i,allocstat,j
209  INTEGER, POINTER :: ndim, natm, noc
210  CHARACTER(len=20) :: fm
211  REAL(KIND=8) :: size_of_random_noise
212  INTEGER, DIMENSION(:), ALLOCATABLE :: seed
213  CHARACTER(LEN=4) :: init_type
214  LOGICAL :: exists, std
215  namelist /iclist/ ic
216  namelist /rand/ init_type,size_of_random_noise,seed
217
218  fm(1:6)='(F3.1)'
219
220  IF (.NOT.imodel%initialized) THEN
221    print*, 'Model not yet initialized, impossible to load any initial condition!'
222    RETURN
223  END IF
224
225  CALL random_seed(size=j)
226
227  ndim => imodel%model_configuration%modes%ndim
228  natm => imodel%model_configuration%modes%natm
229  noc => imodel%model_configuration%modes%noc
230
231  ALLOCATE(seed(j), stat=allocstat)
232  IF (allocstat /= 0) THEN
233    print*, "*** load_ic: Problem with allocation! ***"
234    stop "Exiting ..."
235  END IF
236
237
238  IF (present(filename)) THEN
239    INQUIRE(file=filename,exist=exists)
240    std = .false.
241  ELSE
242    print*, "Warning: IC filename not provided."
243    print*, "Trying to load the standard file IC.nml instead ..."
244    INQUIRE(file='./IC.nml',exist=exists)
245    std = .true.
246  END IF
247
248  IF (exists) THEN
249    IF (std) THEN
250      OPEN(8, file="IC.nml", status='OLD', recl=80, delim='APOSTROPHE')
251    ELSE
252      OPEN(8, file=filename, status='OLD', recl=80, delim='APOSTROPHE')
253    END IF
254    READ(8,nml=iclist)
255    READ(8,nml=rand)
256    CLOSE(8)
257    SELECT CASE (init_type)
258    CASE ('seed')
259      CALL random_seed(put=seed)
260      CALL random_number(ic)
261      ic=2*(ic-0.5)
262      ic=ic*size_of_random_noise*10.d0
263      ic(0)=1.0d0
264      WRITE(6,*) "*** Namelist file written. Starting with 'seeded' random initial condition !***"
265    CASE ('rand')
266      CALL init_random_seed()
267      CALL random_seed(get=seed)
268      CALL random_number(ic)
269      ic=2*(ic-0.5)
270      ic=ic*size_of_random_noise*10.d0

```

```

271         ic(0)=1.0d0
272         WRITE(6,*) "*** Namelist file written. Starting with random initial condition !***"
273     CASE ('zero')
274         CALL init_random_seed()
275         CALL random_seed(get=seed)
276         ic=0
277         ic(0)=1.0d0
278         WRITE(6,*) "*** Namelist file written. Starting with initial condition in IC.nml !***"
279     CASE ('read')
280         CALL init_random_seed()
281         CALL random_seed(get=seed)
282         ic(0)=1.0d0
283         ! except IC(0), nothing has to be done IC has already the right values
284         WRITE(6,*) "*** Namelist file written. Starting with initial condition in IC.nml !***"
285     END SELECT
286 ELSE
287     CALL init_random_seed()
288     CALL random_seed(get=seed)
289     ic=0
290     ic(0)=1.0d0
291     init_type="zero"
292     size_of_random_noise=0.d0
293     WRITE(6,*) "*** Namelist file written. Starting with 0 as initial condition !***"
294 END IF
295 IF (std) THEN
296     OPEN(8, file="IC.nml", status='REPLACE')
297 ELSE
298     OPEN(8, file=filename, status='REPLACE')
299 END IF
300 WRITE(8,'(a)') "!-----!"
301 WRITE(8,'(a)') "! Namelist file : !"
302 WRITE(8,'(a)') "! Initial condition. !"
303 WRITE(8,'(a)') "!-----!"
304 WRITE(8,*) ""
305 WRITE(8,'(a)') "&ICLIST"
306 WRITE(8,*) " ! psi variables"
307 DO i=1,natm
308     WRITE(8,*) " IC("//trim(str(i))//") = ",ic(i)," ! typ= "&
309     &//imodel%inner_products%awavenum(i)%typ//", Nx= "//trim(rstr(imodel%inner_products%awavenum(i)&
310     &%Nx,fm))//", Ny= "//trim(rstr(imodel%inner_products%awavenum(i)%Ny,fm))
311 END DO
312 WRITE(8,*) " ! theta variables"
313 DO i=1,natm
314     WRITE(8,*) " IC("//trim(str(i+natm))//") = ",ic(i+natm)," ! typ= "&
315     &//imodel%inner_products%awavenum(i)%typ//", Nx= "//trim(rstr(imodel%inner_products%awavenum(i)&
316     &%Nx,fm))//", Ny= "//trim(rstr(imodel%inner_products%awavenum(i)%Ny,fm))
317 END DO
318
319 WRITE(8,*) " ! A variables"
320 DO i=1,noc
321     WRITE(8,*) " IC("//trim(str(i+2*natm))//") = ",ic(i+2*natm)," ! Nx&
322     &= " //trim(rstr(imodel%inner_products%owavenum(i)%Nx,fm))//", Ny= "&
323     &//trim(rstr(imodel%inner_products%owavenum(i)%Ny,fm))
324 END DO
325 WRITE(8,*) " ! T variables"
326 DO i=1,noc
327     WRITE(8,*) " IC("//trim(str(i+noc+2*natm))//") = ",ic(i+2*natm+noc)," &
328     &! Nx= " //trim(rstr(imodel%inner_products%owavenum(i)%Nx,fm))//", Ny= "&
329     &//trim(rstr(imodel%inner_products%owavenum(i)%Ny,fm))
330 END DO
331
332 WRITE(8,'(a)') "&END"
333 WRITE(8,*) ""
334 WRITE(8,'(a)') "!-----!"
335 WRITE(8,'(a)') "! Initialisation type. !"
336 WRITE(8,'(a)') "!-----!"
337 WRITE(8,'(a)') "! type = 'read': use IC above (will generate a new seed);"
338 WRITE(8,'(a)') "! 'rand': random state (will generate a new seed);"
339 WRITE(8,'(a)') "! 'zero': zero IC (will generate a new seed);"
340 WRITE(8,'(a)') "! 'seed': use the seed below (generate the same IC)"
341 WRITE(8,*) ""
342 WRITE(8,'(a)') "&RAND"
343 WRITE(8,'(a)') " init_type= '//init_type//'"
344 WRITE(8,'(a,d15.7)') " size_of_random_noise = ",size_of_random_noise
345 DO i=1,j
346     WRITE(8,*) " seed("//trim(str(i))//") = ",seed(i)
347 END DO
348 WRITE(8,'(a)') "&END"
349 WRITE(8,*) ""
350 CLOSE(8)
351

```


6.4.2.9 tendencies()

```

subroutine model_def::tendencies (
    class(model), intent(in) imodel,
    real(kind=8), intent(in) t,
    real(kind=8), dimension(0:imodel%ndim), intent(in) y,
    real(kind=8), dimension(0:imodel%ndim), intent(out) res ) [private]

```

Routine computing the tendencies of the model.

Parameters

in	<i>imodel</i>	Model to compute the tendencies of.
in	<i>t</i>	Time at which the tendencies have to be computed. Actually not needed for autonomous systems.
in	<i>y</i>	Point at which the tendencies have to be computed.
out	<i>res</i>	Vector to store the tendencies.

Remarks

Note that it is NOT safe to pass *y* as a result buffer, as this operation does multiple passes.

Definition at line 85 of file model_def.f90.

```

85     CLASS(model), INTENT(IN) :: imodel
86     REAL(KIND=8), INTENT(IN) :: t
87     REAL(KIND=8), DIMENSION(0:imodel%ndim), INTENT(IN) :: y
88     REAL(KIND=8), DIMENSION(0:imodel%ndim), INTENT(OUT) :: res
89     CALL imodel%aotensor%tensor%sparse_mul3(y, y, res)

```

6.4.2.10 tl_tendencies()

```

subroutine model_def::tl_tendencies (
    class(model), intent(in) imodel,
    real(kind=8), intent(in) t,
    real(kind=8), dimension(0:imodel%ndim), intent(in) ystar,
    real(kind=8), dimension(0:imodel%ndim), intent(in) deltay,
    real(kind=8), dimension(0:imodel%ndim), intent(out) res ) [private]

```

Tendencies for the TL model of MAOOAM in point \mathbf{y}^* for a perturbation $\delta\mathbf{y}$.

Parameters

in	<i>imodel</i>	Model to compute the TL tendencies of.
in	<i>t</i>	time
in	<i>ystar</i>	Vector \mathbf{y}^* (current point in model's trajectory).
in	<i>deltay</i>	Vector $\delta\mathbf{y}$, i.e. the perturbation of the variables at time <i>t</i> .
out	<i>res</i>	Vector to store the tendencies.

Definition at line 113 of file model_def.f90.

```

113     CLASS(model), INTENT(IN) :: imodel
114     REAL(KIND=8), INTENT(IN) :: t
115     REAL(KIND=8), DIMENSION(0:imodel%ndim), INTENT(IN) :: ystar,deltay
116     REAL(KIND=8), DIMENSION(0:imodel%ndim), INTENT(OUT) :: res
117     CALL imodel%tltensor%tensor%sparse_mul3(deltay,ystar,res)

```

6.5 params Module Reference

The model parameters module.

Data Types

- type [integrationparameters](#)
The subclass containing the integration parameters.
- type [modelconfiguration](#)
The general class holding the model configuration.
- type [modesconfiguration](#)
The subclass containing the modes parameters.
- type [physicsconfiguration](#)
The subclass containing the physical parameters of the model.

Functions/Subroutines

- subroutine [init_model_config](#) (model_config, physics_nml, mode_nml, int_nml)
Subroutine to initialize the model configuration with NML files. Reads the physical parameters and mode selection from the namelist.
- subroutine [clean_model_config](#) (model_config)
Subroutine to clean the model configuraion object.

6.5.1 Detailed Description

The model parameters module.

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6.5.2 Function/Subroutine Documentation

6.5.2.1 clean_model_config()

```

subroutine params::clean_model_config (
    class(modelconfiguration), intent(inout) model_config )

```

Subroutine to clean the model configuraion object.

Parameters

in, out	<i>model_config</i>	Model configuration object
---------	---------------------	----------------------------

Definition at line 159 of file params.f90.

```

159     CLASS(modelconfiguration), INTENT(INOUT) :: model_config
160
161     CALL model_config%modes%clean
162     model_config%initialized = .false.
163     model_config%integration%initialized = .false.
164     model_config%physics%initialized = .false.
165
```

6.5.2.2 init_model_config()

```

subroutine params::init_model_config (
    class(modelconfiguration), intent(inout) model_config,
    character(len=*), intent(in), optional physics_nml,
    character(len=*), intent(in), optional mode_nml,
    character(len=*), intent(in), optional int_nml )

```

Subroutine to initialize the model configuration with NML files. Reads the physical parameters and mode selection from the namelist.

Parameters

in, out	<i>model_config</i>	Model configuration object
in	<i>physics_nml</i>	Physical parameters namelist filename
in	<i>mode_nml</i>	Modes configuration namelist filename
in	<i>int_nml</i>	Numerical integration parameters namelist filename

Remarks

If no NML filenames are provided, it will assume that the standard filenames of the model NML have to be used (e.g. "params.nml", "modeselection.nml" and "int_params.nml").

Definition at line 127 of file params.f90.

```

127     CLASS(modelconfiguration), INTENT(INOUT) :: model_config
128     CHARACTER(LEN=*), INTENT(IN), OPTIONAL :: physics_nml
129     CHARACTER(LEN=*), INTENT(IN), OPTIONAL :: mode_nml
130     CHARACTER(LEN=*), INTENT(IN), OPTIONAL :: int_nml
131
132     IF (present(physics_nml)) THEN
133         CALL model_config%physics%init(physics_nml)
134     ELSE
135         CALL model_config%physics%init
136     END IF
137
138     IF (present(mode_nml)) THEN
139         CALL model_config%modes%init(mode_nml)
140     ELSE
141         CALL model_config%modes%init
142     END IF
143
```

```

144     IF (present(int_nml)) THEN
145         CALL model_config%integration%init(int_nml)
146     ELSE
147         CALL model_config%integration%init
148     END IF
149
150     IF ((model_config%physics%initialized).AND.(model_config%modes%initialized).AND.(model_config
%integration%initialized)) THEN
151         model_config%initialized = .true.
152     END IF
153

```

6.6 rk2_ad_integrator Module Reference

Adjoint (AD) model versions of MAOOAM. Second-order Runge-Kutta (RK2) integrators module.

Data Types

- type [rk2adintegrator](#)
Class for the Heun (RK2) AD integrator object.

Functions/Subroutines

- subroutine [ad_step](#) (integr, y, ystar, t, res)
Routine to perform an integration step (Heun algorithm) of the adjoint model. The incremented time is returned.

6.6.1 Detailed Description

Adjoint (AD) model versions of MAOOAM. Second-order Runge-Kutta (RK2) integrators module.

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Remarks

This module actually contains the Heun algorithm routines.

6.6.2 Function/Subroutine Documentation

6.6.2.1 ad_step()

```

subroutine rk2_ad_integrator::ad_step (
    class(rk2adintegrator), intent(inout) integr,
    real(kind=8), dimension(0:integr%ndim), intent(in) y,
    real(kind=8), dimension(0:integr%ndim), intent(in) ystar,
    real(kind=8), intent(inout) t,
    real(kind=8), dimension(0:integr%ndim), intent(out) res )

```

Routine to perform an integration step (Heun algorithm) of the adjoint model. The incremented time is returned.

Parameters

in, out	<i>integr</i>	Integrator object to perform the step with.
in	<i>y</i>	Initial point.
in	<i>ystar</i>	Evaluating the adjoint model at the point y^* .
in	<i>t</i>	Actual integration time
out	<i>res</i>	Final point after the step.

Definition at line 49 of file rk2_ad_integrator.f90.

```

49      CLASS(rk2adintegrator), INTENT(INOUT) :: integr
50      REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(IN) :: y, ystar
51      REAL(KIND=8), INTENT(INOUT) :: t
52      REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(OUT) :: res
53
54      CALL integr%model%ad_tendencies(t, ystar, y, integr%buf_f0)
55      integr%buf_y1 = y + integr%dt * integr%buf_f0
56      CALL integr%model%ad_tendencies(t + integr%dt, ystar, integr%buf_y1, integr%buf_f1)
57      res = y + 0.5 * (integr%buf_f0 + integr%buf_f1) * integr%dt
58      t = t + integr%dt

```

6.7 rk2_integrator Module Reference

Module containing the second-order Runge-Kutta (RK2) integration routines.

Data Types

- type [rk2integrator](#)
Class for the Heun (RK2) integrator object.

Functions/Subroutines

- subroutine [init](#) (integr, imodel)
Routine to initialise the integration buffers.
- subroutine [step](#) (integr, y, t, res)
Routine to perform an integration step (Heun algorithm). The incremented time is returned.
- subroutine [clean](#) (integr)
Routine to clean the integrator.

6.7.1 Detailed Description

Module containing the second-order Runge-Kutta (RK2) integration routines.

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Remarks

This module actually contains the Heun algorithm routines.

6.7.2 Function/Subroutine Documentation

6.7.2.1 clean()

```
subroutine rk2_integrator::clean (
    class(rk2integrator), intent(inout) integr ) [private]
```

Routine to clean the integrator.

Parameters

in, out	<i>integr</i>	Integrator object to clean.
---------	---------------	-----------------------------

Definition at line 92 of file rk2_integrator.f90.

```
92      CLASS(rk2integrator), INTENT(INOUT) :: integr
93
94      IF (allocated(integr%buf_y1)) DEALLOCATE(integr%buf_y1)
95      IF (allocated(integr%buf_f1)) DEALLOCATE(integr%buf_f1)
96      IF (allocated(integr%buf_f0)) DEALLOCATE(integr%buf_f0)
97
```

6.7.2.2 init()

```
subroutine rk2_integrator::init (
    class(rk2integrator), intent(inout) integr,
    class(model), intent(in), target imodel )
```

Routine to initialise the integration buffers.

Parameters

in, out	<i>integr</i>	Integrator object to initialize.
in	<i>imodel</i>	Model object to initialize the integrator with.

Definition at line 41 of file rk2_integrator.f90.

```
41      CLASS(rk2integrator), INTENT(INOUT) :: integr
42      CLASS(model), INTENT(IN), TARGET :: imodel
43      INTEGER :: allocstat
44      IF (.NOT.imodel%initialized) THEN
45          print*, 'Model not yet initialized, impossible to associate an integrator to an empty model!'
46          RETURN
47      END IF
48
49      integr%pmodel => imodel
50      integr%dt => imodel%model_configuration%integration%dt
51      integr%ndim => imodel%model_configuration%modes%ndim
52
53      ALLOCATE(integr%buf_y1(0:integr%ndim) ,stat=allocstat)
54      IF (allocstat /= 0) THEN
```

```

55     print*, "*** rk2integrator%init: Problem with allocation! ***"
56     stop "Exiting ..."
57   END IF
58   ALLOCATE(integr%buf_f0(0:integr%ndim) ,stat=allocstat)
59   IF (allocstat /= 0) THEN
60     print*, "*** rk2integrator%init: Problem with allocation! ***"
61     stop "Exiting ..."
62   END IF
63   ALLOCATE(integr%buf_f1(0:integr%ndim) ,stat=allocstat)
64   IF (allocstat /= 0) THEN
65     print*, "*** rk2integrator%init: Problem with allocation! ***"
66     stop "Exiting ..."
67   END IF
68

```

6.7.2.3 step()

```

subroutine rk2_integrator::step (
    class(rk2integrator), intent(inout) integr,
    real(kind=8), dimension(0:integr%ndim), intent(in) y,
    real(kind=8), intent(inout) t,
    real(kind=8), dimension(0:integr%ndim), intent(out) res ) [private]

```

Routine to perform an integration step (Heun algorithm). The incremented time is returned.

Parameters

in, out	<i>integr</i>	Integrator object to perform the step with.
in	<i>y</i>	Initial point.
in	<i>t</i>	Actual integration time
out	<i>res</i>	Final point after the step.

Definition at line 77 of file rk2_integrator.f90.

```

77   CLASS(rk2integrator), INTENT(INOUT) :: integr
78   REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(IN) :: y
79   REAL(KIND=8), INTENT(INOUT) :: t
80   REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(OUT) :: res
81
82   CALL integr%model%tendencies(t,y,integr%buf_f0)
83   integr%buf_y1 = y+integr%dt*integr%buf_f0
84   CALL integr%model%tendencies(t+integr%dt,integr%buf_y1,integr%buf_f1)
85   res=y+0.5*(integr%buf_f0+integr%buf_f1)*integr%dt
86   t=t+integr%dt

```

6.8 rk2_tl_integrator Module Reference

Tangent Linear (TL) model versions of MAOOAM. Second-order Runge-Kutta (RK2) integrators module.

Data Types

- type `rk2tlintegrator`

Class for the Heun (RK2) TL integrator object.

Functions/Subroutines

- subroutine [tl_step](#) (integr, y, ystar, t, res)

Routine to perform an integration step (Heun algorithm) of the tangent linear model. The incremented time is returned.

6.8.1 Detailed Description

Tangent Linear (TL) model versions of MAOOAM. Second-order Runge-Kutta (RK2) integrators module.

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Remarks

This module actually contains the Heun algorithm routines.

6.8.2 Function/Subroutine Documentation

6.8.2.1 tl_step()

```
subroutine rk2_tl_integrator::tl_step (
    class(rk2tlintegrator), intent(inout) integr,
    real(kind=8), dimension(0:integr%ndim), intent(in) y,
    real(kind=8), dimension(0:integr%ndim), intent(in) ystar,
    real(kind=8), intent(inout) t,
    real(kind=8), dimension(0:integr%ndim), intent(out) res )
```

Routine to perform an integration step (Heun algorithm) of the tangent linear model. The incremented time is returned.

Parameters

in, out	<i>integr</i>	Integrator object to perform the step with.
in	<i>y</i>	Initial point.
in	<i>ystar</i>	Evaluating the adjoint model at the point y^* .
in	<i>t</i>	Actual integration time
out	<i>res</i>	Final point after the step.

Definition at line 49 of file rk2_tl_integrator.f90.

```
49     CLASS(rk2tlintegrator), INTENT(INOUT) :: integr
50     REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(IN) :: y, ystar
51     REAL(KIND=8), INTENT(INOUT) :: t
52     REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(OUT) :: res
53
54     CALL integr%pmode%tl_tendencies(t, ystar, y, integr%buf_f0)
55     integr%buf_y1 = y + integr%dt * integr%buf_f0
```



```

56      CALL integr%model%tl_tendencies (t+integr%dt, ystar, integr%buf_y1, integr%buf_f1)
57      res=y+0.5*(integr%buf_f0+integr%buf_f1)*integr%dt
58      t=t+integr%dt

```

6.9 rk4_ad_integrator Module Reference

Adjoint (AD) model versions of MAOOAM. Fourth-order Runge-Kutta (RK4) integrators module.

Data Types

- type [rk4adintegrator](#)
Class for the fourth-order Runge-Kutta (RK4) AD integrator object.

Functions/Subroutines

- subroutine [ad_step](#) (integr, y, ystar, t, res)
Routine to perform an integration step (RK4 algorithm) of the adjoint model. The incremented time is returned.

6.9.1 Detailed Description

Adjoint (AD) model versions of MAOOAM. Fourth-order Runge-Kutta (RK4) integrators module.

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6.9.2 Function/Subroutine Documentation

6.9.2.1 ad_step()

```

subroutine rk4_ad_integrator::ad_step (
    class(rk4adintegrator), intent(inout) integr,
    real(kind=8), dimension(0:integr%ndim), intent(in) y,
    real(kind=8), dimension(0:integr%ndim), intent(in) ystar,
    real(kind=8), intent(inout) t,
    real(kind=8), dimension(0:integr%ndim), intent(out) res )

```

Routine to perform an integration step (RK4 algorithm) of the adjoint model. The incremented time is returned.

Parameters

in, out	<i>integr</i>	Integrator object to perform the step with.
in	<i>y</i>	Initial point.
in	<i>ystar</i>	Evaluating the adjoint model at the point y^* .
in	<i>t</i>	Actual integration time
Generated by Doxygen out	<i>res</i>	Final point after the step.

Definition at line 47 of file rk4_ad_integrator.f90.

```

47      CLASS(rk4adintegrator), INTENT(INOUT) :: integr
48      REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(IN) :: y,ystar
49      REAL(KIND=8), INTENT(INOUT) :: t
50      REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(OUT) :: res
51
52      CALL integr%model%ad_tendencies(t,ystar,y,integr%buf_kA)
53      integr%buf_y1 = y+0.5*integr%dt*integr%buf_kA
54      CALL integr%model%ad_tendencies(t+0.5*integr%dt,ystar,integr%buf_y1,integr%buf_kB)
55      integr%buf_y1 = y+0.5*integr%dt*integr%buf_kB
56      integr%buf_kA = integr%buf_kA+2*integr%buf_kB
57      CALL integr%model%ad_tendencies(t+0.5*integr%dt,ystar,integr%buf_y1,integr%buf_kB)
58      integr%buf_y1 = y+0.5*integr%dt*integr%buf_kB
59      integr%buf_kA = integr%buf_kA+2*integr%buf_kB
60      CALL integr%model%ad_tendencies(t+integr%dt,ystar,integr%buf_y1,integr%buf_kB)
61      integr%buf_kA = integr%buf_kA+integr%buf_kB
62      res=y+integr%buf_kA*integr%dt/6
63      t=t+integr%dt

```

6.10 rk4_integrator Module Reference

Module containing the fourth-order Runge-Kutta (RK4) integration routines.

Data Types

- type [rk4integrator](#)
Class for the fourth-order Runge-Kutta (RK4) integrator object.

Functions/Subroutines

- subroutine [init](#) (integr, imodel)
Routine to initialise the integration buffers.
- subroutine [step](#) (integr, y, t, res)
Routine to perform an integration step (RK4 algorithm). The incremented time is returned.
- subroutine [clean](#) (integr)
Routine to clean the integrator.

6.10.1 Detailed Description

Module containing the fourth-order Runge-Kutta (RK4) integration routines.

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6.10.2 Function/Subroutine Documentation

6.10.2.1 [clean\(\)](#)

```

subroutine rk4_integrator::clean (
    class(rk4integrator), intent(inout) integr ) [private]

```

Routine to clean the integrator.

Parameters

in, out	<i>integr</i>	Integrator object to clean.
---------	---------------	-----------------------------

Definition at line 101 of file rk4_integrator.f90.

```

101      CLASS(rk4integrator), INTENT(INOUT) :: integr
102
103      IF (allocated(integr%buf_y1)) DEALLOCATE(integr%buf_y1)
104      IF (allocated(integr%buf_kA)) DEALLOCATE(integr%buf_kA)
105      IF (allocated(integr%buf_kB)) DEALLOCATE(integr%buf_kB)
106

```

6.10.2.2 init()

```

subroutine rk4_integrator::init (
    class(rk4integrator), intent(inout) integr,
    class(model), intent(in), target imodel )

```

Routine to initialise the integration buffers.

Parameters

in, out	<i>integr</i>	Integrator object to initialize.
in	<i>imodel</i>	Model object to initialize the integrator with.

Definition at line 39 of file rk4_integrator.f90.

```

39      CLASS(rk4integrator), INTENT(INOUT) :: integr
40      CLASS(model), INTENT(IN), TARGET :: imodel
41      INTEGER :: allocstat
42      IF (.NOT.imodel%initialized) THEN
43          print*, 'Model not yet initialized, impossible to associate an integrator to an empty model!'
44          RETURN
45      END IF
46
47      integr%pmodel => imodel
48      integr%dt => imodel%model_configuration%integration%dt
49      integr%ndim => imodel%model_configuration%modes%ndim
50
51      ALLOCATE(integr%buf_y1(0:integr%ndim) ,stat=allocstat)
52      IF (allocstat /= 0) THEN
53          print*, "*** rk4integrator%init: Problem with allocation! ***"
54          stop "Exiting ..."
55      END IF
56      ALLOCATE(integr%buf_kA(0:integr%ndim) ,stat=allocstat)
57      IF (allocstat /= 0) THEN
58          print*, "*** rk4integrator%init: Problem with allocation! ***"
59          stop "Exiting ..."
60      END IF
61      ALLOCATE(integr%buf_kB(0:integr%ndim) ,stat=allocstat)
62      IF (allocstat /= 0) THEN
63          print*, "*** rk4integrator%init: Problem with allocation! ***"
64          stop "Exiting ..."
65      END IF
66

```

6.10.2.3 step()

```
subroutine rk4_integrator::step (
    class(rk4integrator), intent(inout) integr,
    real(kind=8), dimension(0:integr%ndim), intent(in) y,
    real(kind=8), intent(inout) t,
    real(kind=8), dimension(0:integr%ndim), intent(out) res ) [private]
```

Routine to perform an integration step (RK4 algorithm). The incremented time is returned.

Parameters

in, out	<i>integr</i>	Integrator object to perform the step with.
in	<i>y</i>	Initial point.
in	<i>t</i>	Actual integration time
out	<i>res</i>	Final point after the step.

Definition at line 75 of file rk4_integrator.f90.

```
75     CLASS(rk4integrator), INTENT(INOUT) :: integr
76     REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(IN) :: y
77     REAL(KIND=8), INTENT(INOUT) :: t
78     REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(OUT) :: res
79
80     CALL integr%model%tendencies(t,y,integr%buf_kA)
81     integr%buf_y1 = y + 0.5*integr%dt*integr%buf_kA
82
83     CALL integr%model%tendencies(t+0.5*integr%dt,integr%buf_y1,integr%buf_kB)
84     integr%buf_y1 = y + 0.5*integr%dt*integr%buf_kB
85     integr%buf_kA = integr%buf_kA + 2*integr%buf_kB
86
87     CALL integr%model%tendencies(t+0.5*integr%dt,integr%buf_y1,integr%buf_kB)
88     integr%buf_y1 = y + integr%dt*integr%buf_kB
89     integr%buf_kA = integr%buf_kA + 2*integr%buf_kB
90
91     CALL integr%model%tendencies(t+integr%dt,integr%buf_y1,integr%buf_kB)
92     integr%buf_kA = integr%buf_kA + integr%buf_kB
93
94     t=t+integr%dt
95     res=y+integr%buf_kA*integr%dt/6
```

6.11 rk4_tl_integrator Module Reference

Tangent Linear (TL) model versions of MAOOAM. Fourth-order Runge-Kutta (RK4) integrators module.

Data Types

- type [rk4tlintegrator](#)

Class for the fourth-order Runge-Kutta (RK4) TL integrator object.

Functions/Subroutines

- subroutine [tl_step](#) (integr, y, ystar, t, res)

Routine to perform an integration step (RK4 algorithm) of the tangent linear model. The incremented time is returned.

6.11.1 Detailed Description

Tangent Linear (TL) model versions of MAOOAM. Fourth-order Runge-Kutta (RK4) integrators module.

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6.11.2 Function/Subroutine Documentation

6.11.2.1 tl_step()

```
subroutine rk4_tl_integrator::tl_step (
    class(rk4tlintegrator), intent(inout) integr,
    real(kind=8), dimension(0:integr%ndim), intent(in) y,
    real(kind=8), dimension(0:integr%ndim), intent(in) ystar,
    real(kind=8), intent(inout) t,
    real(kind=8), dimension(0:integr%ndim), intent(out) res )
```

Routine to perform an integration step (RK4 algorithm) of the tangent linear model. The incremented time is returned.

Parameters

in, out	<i>integr</i>	Integrator object to perform the step with.
in	<i>y</i>	Initial point.
in	<i>ystar</i>	Evaluating the adjoint model at the point y^* .
in	<i>t</i>	Actual integration time
out	<i>res</i>	Final point after the step.

Definition at line 47 of file rk4_tl_integrator.f90.

```
47      CLASS(rk4tlintegrator), INTENT(INOUT) :: integr
48      REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(IN) :: y, ystar
49      REAL(KIND=8), INTENT(INOUT) :: t
50      REAL(KIND=8), DIMENSION(0:integr%ndim), INTENT(OUT) :: res
51
52      CALL integr%model%tl_tendencies(t, ystar, y, integr%buf_kA)
53      integr%buf_y1 = y+0.5*integr%dt*integr%buf_kA
54      CALL integr%model%tl_tendencies(t+0.5*integr%dt, ystar, integr%buf_y1, integr%buf_kB)
55      integr%buf_y1 = y+0.5*integr%dt*integr%buf_kB
56      integr%buf_kA = integr%buf_kA+2*integr%buf_kB
57      CALL integr%model%tl_tendencies(t+0.5*integr%dt, ystar, integr%buf_y1, integr%buf_kB)
58      integr%buf_y1 = y+0.5*integr%dt*integr%buf_kB
59      integr%buf_kA = integr%buf_kA+2*integr%buf_kB
60      CALL integr%model%tl_tendencies(t+integr%dt, ystar, integr%buf_y1, integr%buf_kB)
61      integr%buf_kA = integr%buf_kA+integr%buf_kB
62      res=y+integr%buf_kA*integr%dt/6
63      t=t+integr%dt
```

6.12 stat Module Reference

Statistics accumulators.

Data Types

- type `stataaccumulator`
Statistics accumulator objects class.

Functions/Subroutines

- subroutine `init_stat` (istat, ndim)
Initialize the accumulators.
- subroutine `acc` (istat, x)
Accumulate one state.
- real(kind=8) function, dimension(size(istat%m)) `mean` (istat)
Function returning the mean.
- real(kind=8) function, dimension(size(istat%m)) `var` (istat)
Function returning the variance.
- integer function `iter` (istat)
Function returning the number of data accumulated.
- subroutine `reset` (istat)
Routine resetting the accumulator.
- subroutine `clean` (istat)
Routine to clean the accumulator.

6.12.1 Detailed Description

Statistics accumulators.

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6.12.2 Function/Subroutine Documentation

6.12.2.1 `acc()`

```
subroutine stat::acc (
    class(stataaccumulator), intent(inout) istat,
    real(kind=8), dimension(:), intent(in) x ) [private]
```

Accumulate one state.

Parameters

in, out	<i>istat</i>	Statistical accumulator to initialize
in	<i>x</i>	State to accumulate

Definition at line 69 of file stat.f90.

```

69      CLASS(stataccumulator), INTENT(INOUT) :: istat
70      REAL(KIND=8), DIMENSION(:), INTENT(IN) :: x
71      istat%i=istat%i+1
72      istat%mprev=istat%m+(x-istat%m)/istat%i
73      istat%mtmp=istat%mprev
74      istat%mprev=istat%m
75      istat%m=istat%mtmp
76      istat%v=istat%v+(x-istat%mprev)*(x-istat%m)

```

6.12.2.2 clean()

```

subroutine stat::clean (
    class(stataccumulator), intent(inout) istat ) [private]

```

Routine to clean the accumulator.

Parameters

in, out	<i>istat</i>	Statistical accumulator to clean
---------	--------------	----------------------------------

Definition at line 119 of file stat.f90.

```

119      CLASS(stataccumulator), INTENT(INOUT) :: istat
120
121      IF (allocated(istat%m)) DEALLOCATE(istat%m)
122      IF (allocated(istat%mprev)) DEALLOCATE(istat%mprev)
123      IF (allocated(istat%v)) DEALLOCATE(istat%v)
124      IF (allocated(istat%mtmp)) DEALLOCATE(istat%mtmp)
125

```

6.12.2.3 init_stat()

```

subroutine stat::init_stat (
    class(stataccumulator), intent(inout) istat,
    integer, intent(in) ndim )

```

Initialize the accumulators.

Parameters

in, out	<i>istat</i>	Statistical accumulator to initialize
in	<i>ndim</i>	Dimension of the state space to accumulate statistics for.

Definition at line 44 of file stat.f90.

```

44      CLASS(stataccumulator), INTENT(INOUT) :: istat
45      INTEGER, INTENT(in) :: ndim

```

```

46     INTEGER :: allocstat
47
48     ALLOCATE(istat%m(ndim), istat%mprev(ndim), stat=allocstat)
49     IF (allocstat /= 0) THEN
50         print*, "*** init_stat: Problem with allocation! ***"
51         stop "Exiting ..."
52     END IF
53     ALLOCATE(istat%v(ndim), istat%mtmp(ndim), stat=allocstat)
54     IF (allocstat /= 0) THEN
55         print*, "*** init_stat: Problem with allocation! ***"
56         stop "Exiting ..."
57     END IF
58     istat%m=0.d0
59     istat%mprev=0.d0
60     istat%v=0.d0
61     istat%mtmp=0.d0
62

```

6.12.2.4 iter()

```

integer function stat::iter (
    class(stataccumulator), intent(in) istat ) [private]

```

Function returning the number of data accumulated.

Parameters

in, out	<i>istat</i>	Statistical accumulator to initialize
---------	--------------	---------------------------------------

Returns

The number of the accumulated states

Definition at line 101 of file stat.f90.

```

101     CLASS(stataccumulator), INTENT(IN) :: istat
102     INTEGER :: iter
103     iter=istat%i

```

6.12.2.5 mean()

```

real(kind=8) function, dimension(size(istat%m)) stat::mean (
    class(stataccumulator), intent(in) istat ) [private]

```

Function returning the mean.

Parameters

in, out	<i>istat</i>	Statistical accumulator to initialize
---------	--------------	---------------------------------------

Returns

The mean of the accumulated states

Definition at line 83 of file stat.f90.

```
83      CLASS(stataccumulator), INTENT(IN) :: istat
84      REAL(KIND=8), DIMENSION(size(istat%m)) :: mean
85      mean=istat%m
```

6.12.2.6 reset()

```
subroutine stat::reset (
    class(stataccumulator), intent(inout) istat ) [private]
```

Routine resetting the accumulator.

Parameters

<i>in, out</i>	<i>istat</i>	Statistical accumulator to initialize
----------------	--------------	---------------------------------------

Definition at line 109 of file stat.f90.

```
109      CLASS(stataccumulator), INTENT(INOUT) :: istat
110      istat%m=0.d0
111      istat%mprev=0.d0
112      istat%v=0.d0
113      istat%i=0
```

6.12.2.7 var()

```
real(kind=8) function, dimension(size(istat%m)) stat::var (
    class(stataccumulator), intent(in) istat ) [private]
```

Function returning the variance.

Parameters

<i>in, out</i>	<i>istat</i>	Statistical accumulator to initialize
----------------	--------------	---------------------------------------

Returns

The variance of the accumulated states

Definition at line 92 of file stat.f90.

```
92      CLASS(stataccumulator), INTENT(IN) :: istat
93      REAL(KIND=8), DIMENSION(size(istat%m)) :: var
94      var=istat%v/(istat%i-1)
```

6.13 tensor_def Module Reference

Tensor utility module. Contains class to represent sparse tensors.

Data Types

- type `coolist`
Coordinate list. Type used to represent the sparse tensor.
- type `coolistelem`
Coordinate list element type. Elementary elements of the sparse tensors.
- type `tensor`
General class to represent a sparse tensor.

Functions/Subroutines

- logical function `test_alloc` (mtensor)
Function to test if the tensor is allocated.
- logical function `empty` (mtensor)
Function to test if the tensor is empty.
- subroutine `clean` (mtensor)
Routine to clean (deallocate) a tensor.
- subroutine `init` (mtensor, ndim)
Routine to initialize a tensor.
- integer function `tensor_size` (mtensor)
- subroutine `copy` (src, dst)
Routine to copy a tensor into another one.
- subroutine `from_mat` (src, dst)
Routine to convert a matrix to a tensor, using only the first two indices of the rank-3 tensor.
- subroutine `sparse_mul3` (mtensor, arr_j, arr_k, res)
Sparse multiplication of a tensor with two vectors: $\sum_{j,k=0}^{ndim} \mathcal{T}_{i,j,k} a_j b_k$.
- subroutine `simplify` (mtensor)
Routine to simplify a coolist (sparse tensor). For each index i , it upper triangularize the matrix

$$\mathcal{T}_{i,j,k} \quad 0 \leq j, k \leq ndim.$$

- subroutine `jsparse_mul` (mtensor, arr_j, jtensor)
Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} (\mathcal{T}_{i,j,k} + \mathcal{T}_{i,k,j}) a_k.$$

It's implemented slightly differently: for every $\mathcal{T}_{i,j,k}$, we add to $J_{i,j}$ as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k \quad J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a sparse tensor.

- subroutine `jsparse_mul_mat` (mtensor, arr_j, jmatrix)

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} (\mathcal{T}_{i,j,k} + \mathcal{T}_{i,k,j}) a_k.$$

It's implemented slightly differently: for every $\mathcal{T}_{i,j,k}$, we add to $J_{i,j}$ as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a matrix.

- subroutine `sparse_mul2` (mtensor, arr_j, res)

Sparse multiplication of a 2d sparse tensor with a vector: $\sum_{j=0}^{ndim} \mathcal{T}_{i,j,k} a_j$.

- subroutine `add_elem` (mtensor, i, j, k, v)

Subroutine to add element to a coolist.

- subroutine `add_from_tensor` (src, dst)

Routine to add the entries of a rank-3 tensor to another one.

- subroutine `print_tensor` (mtensor, s)

Routine to print a rank-3 tensor.

- subroutine `write_tensor_to_file` (mtensor, s)

Write a rank-3 tensor coolist to a file.

- subroutine `load_tensor_from_file` (mtensor, s)

Load a rank-3 tensor coolist from a file definition.

6.13.1 Detailed Description

Tensor utility module. Contains class to represent sparse tensors.

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6.13.2 Function/Subroutine Documentation

6.13.2.1 add_elem()

```
subroutine tensor_def::add_elem (
    class(tensor), intent(inout) mtensor,
    integer, intent(in) i,
    integer, intent(in) j,
    integer, intent(in) k,
    real(kind=8), intent(in) v ) [private]
```

Subroutine to add element to a coolist.

Parameters

in, out	<i>mtensor</i>	A tensor to add the element to.
in	<i>i</i>	tensor <i>i</i> index
in	<i>j</i>	tensor <i>j</i> index
Generated by Doxygen		tensor <i>k</i> index
in	<i>v</i>	value to add

Definition at line 377 of file tensor_def.f90.

```

377  CLASS(tensor), INTENT(INOUT) :: mtensor
378  INTEGER, INTENT(IN) :: i,j,k
379  REAL(KIND=8), INTENT(IN) :: v
380  INTEGER :: n
381  IF (abs(v) .ge. real_eps) THEN
382      n=(mtensor%t(i)%elems)+1
383      mtensor%t(i)%elems(n)%j=j
384      mtensor%t(i)%elems(n)%k=k
385      mtensor%t(i)%elems(n)%v=v
386      mtensor%t(i)%elems=n
387  END IF

```

6.13.2.2 add_from_tensor()

```

subroutine tensor_def::add_from_tensor (
    class(tensor), intent(in) src,
    class(tensor), intent(inout) dst ) [private]

```

Routine to add the entries of a rank-3 tensor to another one.

Parameters

in	src	Tensor to add
in, out	dst	Destination tensor

Definition at line 417 of file tensor_def.f90.

```

417  CLASS(tensor), INTENT(IN) :: src
418  CLASS(tensor), INTENT(INOUT) :: dst
419  TYPE(coolistelem), DIMENSION(:), ALLOCATABLE :: celems
420  INTEGER :: i,j,n,allocstat
421
422  DO i=1,dst%ndim()
423      IF (src%t(i)%elems/=0) THEN
424          IF (dst%t(i)%elems==0) THEN
425              IF (allocated(dst%t(i)%elems)) THEN
426                  DEALLOCATE(dst%t(i)%elems, stat=allocstat)
427                  IF (allocstat /= 0) THEN
428                      print*, "*** tensor%add_from_tensor: Problem with allocation! ***"
429                      stop "Exiting ..."
430                  END IF
431              END IF
432              ALLOCATE(dst%t(i)%elems(src%t(i)%elems), stat=allocstat)
433              IF (allocstat /= 0) THEN
434                  print*, "*** tensor%add_from_tensor: Problem with allocation! ***"
435                  stop "Exiting ..."
436              END IF
437              n=0
438          ELSE
439              n=dst%t(i)%elems
440              ALLOCATE(celems(n), stat=allocstat)
441              DO j=1,n
442                  celems(j)%j=dst%t(i)%elems(j)%j
443                  celems(j)%k=dst%t(i)%elems(j)%k
444                  celems(j)%v=dst%t(i)%elems(j)%v
445              ENDDO
446              IF (allocated(dst%t(i)%elems)) DEALLOCATE(dst%t(i)%elems, stat=allocstat)
447              ALLOCATE(dst%t(i)%elems(src%t(i)%elems+n), stat=allocstat)
448              IF (allocstat /= 0) THEN
449                  print*, "*** tensor%add_from_tensor: Problem with allocation! ***"
450                  stop "Exiting ..."
451              END IF
452              DO j=1,n
453                  dst%t(i)%elems(j)%j=celems(j)%j
454                  dst%t(i)%elems(j)%k=celems(j)%k

```

```

455         dst%t(i)%elems(j)%v=celems(j)%v
456     ENDDO
457     IF (allocated(celems)) DEALLOCATE(celems, stat=allocstat)
458 ENDIF
459 DO j=1,src%t(i)%nelems
460     dst%t(i)%elems(n+j)%j=src%t(i)%elems(j)%j
461     dst%t(i)%elems(n+j)%k=src%t(i)%elems(j)%k
462     dst%t(i)%elems(n+j)%v=src%t(i)%elems(j)%v
463 ENDDO
464 dst%t(i)%nelems=src%t(i)%nelems+n
465 ENDDIF
466 ENDDO
467

```

6.13.2.3 clean()

```

subroutine tensor_def::clean (
    class(tensor), intent(inout) mtensor ) [private]

```

Routine to clean (deallocate) a tensor.

Parameters

in, out	<i>mtensor</i>	The tensor to clean.
---------	----------------	----------------------

Definition at line 92 of file tensor_def.f90.

```

92     CLASS(tensor), INTENT(INOUT) :: mtensor
93
94     IF (mtensor%allocated()) DEALLOCATE(mtensor%t)
95

```

6.13.2.4 copy()

```

subroutine tensor_def::copy (
    class(tensor), intent(in) src,
    class(tensor), intent(out) dst ) [private]

```

Routine to copy a tensor into another one.

Parameters

in	<i>src</i>	Source tensor.
out	<i>dst</i>	Destination tensor.

Warning

The destination tensor will be reinitialized, erasing all previous content! Use with care...

Definition at line 130 of file tensor_def.f90.

```

130  CLASS(tensor), INTENT(IN) :: src
131  CLASS(tensor), INTENT(OUT) :: dst
132  INTEGER :: i,j,allocstat
133
134  CALL dst%init(src%ndim())
135  DO i=1,src%ndim()
136      ALLOCATE(dst%t(i)%elems(src%t(i)%elems), stat=allocstat)
137      IF (allocstat /= 0) THEN
138          print*, "*** tensor%copy: Problem with allocation! ***"
139          stop "Exiting ..."
140      END IF
141      DO j=1,src%t(i)%elems
142          dst%t(i)%elems(j)%j=src%t(i)%elems(j)%j
143          dst%t(i)%elems(j)%k=src%t(i)%elems(j)%k
144          dst%t(i)%elems(j)%v=src%t(i)%elems(j)%v
145      ENDDO
146      dst%t(i)%nelems=src%t(i)%nelems
147  ENDDO

```

6.13.2.5 empty()

```

logical function tensor_def::empty (
    class(tensor) mtensor ) [private]

```

Function to test if the tensor is empty.

Parameters

<i>mtensor</i>	The tensor to test.
----------------	---------------------

Returns

A boolean indicating if the tensor is empty.

Definition at line 75 of file tensor_def.f90.

```

75  CLASS(tensor) :: mtensor
76  LOGICAL :: empty
77  INTEGER :: i
78
79  empty = .true.
80
81  IF (.NOT. mtensor%allocated()) RETURN
82
83  DO i=1,mtensor%ndim()
84      IF (mtensor%t(i)%nelems/=0) empty = .false.
85  END DO
86

```

6.13.2.6 from_mat()

```

subroutine tensor_def::from_mat (
    real(kind=8), dimension(:,,:), intent(in) src,
    class(tensor), intent(inout) dst ) [private]

```

Routine to convert a matrix to a tensor, using only the fist two indices of the rank-3 tensor.

Parameters

in	src	Source matrix
out	dst	Destination tensor.

Warning

The destination tensor will be reinitialized, erasing all previous content! Use with care...

Definition at line 155 of file tensor_def.f90.

```

155     CLASS(tensor), INTENT(INOUT) :: dst
156     REAL(KIND=8), DIMENSION(:, :), INTENT(IN) :: src
157     INTEGER :: i, j, n, allocstat
158     INTEGER :: ndim
159     INTEGER, DIMENSION(2) :: sh
160
161     sh = shape(src)
162     ndim = sh(1)
163     CALL dst%init(ndim)
164
165     DO i=1, ndim
166         n=0
167         DO j=1, ndim
168             IF (abs(src(i, j)) > real_eps) n=n+1
169         ENDDO
170         ALLOCATE(dst%t(i)%elems(n), stat=allocstat)
171         IF (allocstat /= 0) THEN
172             print*, "*** tensor%from_mat: Problem with allocation! ***"
173             stop "Exiting ..."
174         END IF
175         n=0
176         DO j=1, ndim
177             IF (abs(src(i, j)) > real_eps) THEN
178                 n=n+1
179                 dst%t(i)%elems(n)%j=j
180                 dst%t(i)%elems(n)%k=0
181                 dst%t(i)%elems(n)%v=src(i, j)
182             END IF
183         ENDDO
184         dst%t(i)%elems=n
185     ENDDO

```

6.13.2.7 init()

```

subroutine tensor_def::init (
    class(tensor), intent(inout) mtensor,
    integer, intent(in) ndim ) [private]

```

Routine to initialize a tensor.

Parameters

in, out	mtensor	The tensor to clean.
in	ndim	The first dimension of the tensor.

Definition at line 102 of file tensor_def.f90.

```

102     CLASS(tensor), INTENT(INOUT) :: mtensor

```

```

103     INTEGER, INTENT(IN) :: ndim
104     INTEGER :: allocstat
105
106     CALL mtensor%clean
107     ALLOCATE(mtensor%t(ndim), stat=allocstat)
108     IF (allocstat /= 0) THEN
109         print*, "*** tensor%init: Problem with allocation! ***"
110         stop "Exiting ..."
111     END IF
112

```

6.13.2.8 jsparse_mul()

```

subroutine tensor_def::jsparse_mul (
    class(tensor), intent(in) mtensor,
    real(kind=8), dimension(0:size(mtensor%t)), intent(in) arr_j,
    type(tensor), intent(inout) jtensor ) [private]

```

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} (\mathcal{T}_{i,j,k} + \mathcal{T}_{i,k,j}) a_k.$$

It's implemented slightly differently: for every $\mathcal{T}_{i,j,k}$, we add to $J_{i,j}$ as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a sparse tensor.

Parameters

in	<i>mtensor</i>	A sparse tensor of which index 2 or 3 will be contracted.
in	<i>arr_j</i>	The vector a to be contracted with.
out	<i>jtensor</i>	A sparse tensor to store the result of the contraction

Warning

The output jtensor will be reinitialized, erasing all previous content! Use with care...

Definition at line 288 of file tensor_def.f90.

```

288     CLASS(tensor), INTENT(IN) :: mtensor
289     TYPE(tensor), INTENT(INOUT):: jtensor
290     REAL(KIND=8), DIMENSION(0:size(mtensor%t)), INTENT(IN) :: arr_j
291     REAL(KIND=8) :: v
292     INTEGER :: i,j,k,n,nj,allocstat
293     CALL jtensor%init(mtensor%ndim())
294     DO i=1,mtensor%ndim()
295         nj=2*jtensor%t(i)%elems
296         ALLOCATE(jtensor%t(i)%elems(nj), stat=allocstat)
297         IF (allocstat /= 0) THEN
298             print*, "*** tensor%jsparse_mul: Problem with allocation! ***"
299             stop "Exiting ..."
300         END IF
301         nj=0
302         DO n=1,mtensor%t(i)%elems
303             j=mtensor%t(i)%elems(n)%j
304             k=mtensor%t(i)%elems(n)%k
305             v=mtensor%t(i)%elems(n)%v
306             IF (j /=0) THEN

```



```

307         nj=nj+1
308         jtensor%t(i)%elems(nj)%j=j
309         jtensor%t(i)%elems(nj)%k=0
310         jtensor%t(i)%elems(nj)%v=v*arr_j(k)
311     END IF
312
313     IF (k /=0) THEN
314         nj=nj+1
315         jtensor%t(i)%elems(nj)%j=k
316         jtensor%t(i)%elems(nj)%k=0
317         jtensor%t(i)%elems(nj)%v=v*arr_j(j)
318     END IF
319 END DO
320 jtensor%t(i)%elems=nj
321 END DO

```

6.13.2.9 jsparse_mul_mat()

```

subroutine tensor_def::jsparse_mul_mat (
    class(tensor), intent(in) mtensor,
    real(kind=8), dimension(0:size(mtensor%t)), intent(in) arr_j,
    real(kind=8), dimension(size(mtensor%t),size(mtensor%t)), intent(out) jmatrix )
[private]

```

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} (\mathcal{T}_{i,j,k} + \mathcal{T}_{i,k,j}) a_k.$$

It's implemented slightly differently: for every $\mathcal{T}_{i,j,k}$, we add to $J_{i,j}$ as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a matrix.

Parameters

in	<i>mtensor</i>	A sparse tensor of which index 2 or 3 will be contracted.
in	<i>arr_j</i>	The vector <i>a</i> to be contracted with.
out	<i>jmatrix</i>	A matrix to store the result of the contraction.

Definition at line 333 of file tensor_def.f90.

```

333 CLASS(tensor), INTENT(IN) :: mtensor
334 REAL(KIND=8), DIMENSION(size(mtensor%t),size(mtensor%t)), INTENT(OUT):: jmatrix
335 REAL(KIND=8), DIMENSION(0:size(mtensor%t)), INTENT(IN) :: arr_j
336 REAL(KIND=8) :: v
337 INTEGER :: i,j,k,n
338 jmatrix=0.d0
339 DO i=1,mtensor%ndim()
340     DO n=1,mtensor%t(i)%elems
341         j=mtensor%t(i)%elems(n)%j
342         k=mtensor%t(i)%elems(n)%k
343         v=mtensor%t(i)%elems(n)%v
344         IF (j /=0) jmatrix(i,j)=jmatrix(i,j)+v*arr_j(k)
345         IF (k /=0) jmatrix(i,k)=jmatrix(i,k)+v*arr_j(j)
346     END DO
347 END DO

```

6.13.2.10 load_tensor_from_file()

```
subroutine tensor_def::load_tensor_from_file (
    class(tensor), intent(inout) mtensor,
    character (len=*), intent(in) s ) [private]
```

Load a rank-3 tensor coolist from a file definition.

Parameters

in, out	<i>mtensor</i>	The tensor to load to.
in	<i>s</i>	Filename of the tensor definition file.

Remarks

The destination tensor have to be an empty tensor, i.e. with unallocated list of elements and nelems set to 0.

Definition at line 522 of file tensor_def.f90.

```
522 CLASS(tensor), INTENT(INOUT) :: mtensor
523 CHARACTER (LEN=*), INTENT(IN) :: s
524 INTEGER :: i,ir,j,k,n,allocstat, ndim
525 REAL(KIND=8) :: v
526 OPEN(30,file=s,status='old')
527 READ(30, *) ndim
528 ALLOCATE(mtensor%t(ndim), stat=allocstat)
529 IF (allocstat /= 0) THEN
530     print*, "*** tensor%load_tensor_from_file: Problem with allocation! ***"
531     stop "Exiting ..."
532 END IF
533 DO i=1,ndim
534     READ(30,*) ir,n
535     IF (n /= 0) THEN
536         ALLOCATE(mtensor%t(i)%elems(n), stat=allocstat)
537         IF (allocstat /= 0) THEN
538             print*, "*** tensor%load_tensor_from_file: Problem with allocation! ***"
539             stop "Exiting ..."
540         END IF
541         mtensor%t(i)%nelems=n
542     ENDIF
543     DO n=1,mtensor%t(i)%nelems
544         READ(30,*) ir,j,k,v
545         mtensor%t(i)%elems(n)%j=j
546         mtensor%t(i)%elems(n)%k=k
547         mtensor%t(i)%elems(n)%v=v
548     ENDDO
549 END DO
550 CLOSE(30)
```

6.13.2.11 print_tensor()

```
subroutine tensor_def::print_tensor (
    class(tensor), intent(in) mtensor,
    character(len=*), intent(in), optional, target s ) [private]
```

Routine to print a rank-3 tensor.

Parameters

in	<i>mtensor</i>	Tensor to print.
in	<i>s</i>	String to put before tensor entries. Default to "t".

Definition at line 474 of file tensor_def.f90.

```

474  CLASS(tensor), INTENT(IN) :: mtensor
475  CHARACTER(LEN=*), INTENT(IN), TARGET, OPTIONAL :: s
476
477  CHARACTER, TARGET :: sr = "t"
478  CHARACTER, POINTER :: r
479  INTEGER :: i,n,j,k
480  IF (present(s)) THEN
481    r => s
482  ELSE
483    r => sr
484  END IF
485  DO i=1,mtensor%ndim()
486    DO n=1,mtensor%t(i)%elems
487      j=mtensor%t(i)%elems(n)%j
488      k=mtensor%t(i)%elems(n)%k
489      IF (abs(mtensor%t(i)%elems(n)%v) .GE. real_eps) THEN
490        write(*,"(A,ES12.5)") r//"[//trim(str(i))//"] [//trim(str(j)) &
491          & //"] [//trim(str(k))//"] = ",mtensor%t(i)%elems(n)%v
492      END IF
493    END DO
494  END DO

```

6.13.2.12 simplify()

```

subroutine tensor_def::simplify (
  class(tensor), intent(inout) mtensor ) [private]

```

Routine to simplify a coolist (sparse tensor). For each index i , it upper triangularize the matrix

$$\mathcal{T}_{i,j,k} \quad 0 \leq j, k \leq ndim.$$

.

Parameters

in, out	mtensor	A sparse tensor which will be simplified.
---------	---------	---

Definition at line 214 of file tensor_def.f90.

```

214  CLASS(tensor), INTENT(INOUT) :: mtensor
215  INTEGER :: i,j,k
216  INTEGER :: li,lii,liii,n
217  DO i= 1,mtensor%ndim()
218    n=mtensor%t(i)%elems
219    DO li=n,2,-1
220      j=mtensor%t(i)%elems(li)%j
221      k=mtensor%t(i)%elems(li)%k
222      DO lii=li-1,1,-1
223        IF ((j==mtensor%t(i)%elems(lii)%j).AND.(k==mtensor%t(i)%&
224          &%elems(lii)%k)).OR.((j==mtensor%t(i)%elems(lii)%k).AND.(k==mtensor%t(i)%elems(lii)%j))) THEN
225          ! Found another entry with the same i,j,k: merge both into
226          ! the one listed first (of those two).
227          mtensor%t(i)%elems(lii)%v=mtensor%t(i)%elems(lii)%v+mtensor%t(i)%elems(li)%v
228          IF (j>k) THEN
229            mtensor%t(i)%elems(lii)%j=mtensor%t(i)%elems(li)%k
230            mtensor%t(i)%elems(lii)%k=mtensor%t(i)%elems(li)%j
231          ENDIF
232
233          ! Shift the rest of the items one place down.
234          DO liii=li+1,n
235            mtensor%t(i)%elems(liii-1)%j=mtensor%t(i)%elems(liii)%j
236            mtensor%t(i)%elems(liii-1)%k=mtensor%t(i)%elems(liii)%k
237            mtensor%t(i)%elems(liii-1)%v=mtensor%t(i)%elems(liii)%v
238          END DO
239          mtensor%t(i)%elems=mtensor%t(i)%elems-1

```

```

240         ! Here we should stop because the li no longer points to the
241         ! original i,j,k element
242         EXIT
243     ENDIF
244 ENDDO
245 ENDDO
246 n=mtensor%t(i)%nelems
247 li=1
248 DO WHILE (li<=mtensor%t(i)%nelems)
249     ! Clear new "almost" zero entries and shift rest of the items one place down.
250     ! Make sure not to skip any entries while shifting!
251     DO WHILE (abs(mtensor%t(i)%elems(li)%v) < real_eps)
252         DO liii=li+1,n
253             mtensor%t(i)%elems(liii-1)%j=mtensor%t(i)%elems(liii)%j
254             mtensor%t(i)%elems(liii-1)%k=mtensor%t(i)%elems(liii)%k
255             mtensor%t(i)%elems(liii-1)%v=mtensor%t(i)%elems(liii)%v
256         ENDDO
257         mtensor%t(i)%nelems=mtensor%t(i)%nelems-1
258         if (li > mtensor%t(i)%nelems) THEN
259             EXIT
260         ENDIF
261     ENDDO
262     li=li+1
263 ENDDO
264
265 n=mtensor%t(i)%nelems
266 DO li=1,n
267     ! Upper triangularize
268     j=mtensor%t(i)%elems(li)%j
269     k=mtensor%t(i)%elems(li)%k
270     IF (j>k) THEN
271         mtensor%t(i)%elems(li)%j=k
272         mtensor%t(i)%elems(li)%k=j
273     ENDIF
274 ENDDO
275 ENDDO

```

6.13.2.13 sparse_mul2()

```

subroutine tensor_def::sparse_mul2 (
    class(tensor), intent(in) mtensor,
    real(kind=8), dimension(0:size(mtensor%t)), intent(in) arr_j,
    real(kind=8), dimension(0:size(mtensor%t)), intent(out) res ) [private]

```

Sparse multiplication of a 2d sparse tensor with a vector: $\sum_{j=0}^{ndim} \mathcal{T}_{i,j,k} a_j$.

Parameters

in	<i>mtensor</i>	A sparse tensor of which index 2 will be contracted.
in	<i>arr_j</i>	The vector <i>a</i> to be contracted with.
out	<i>res</i>	vector (buffer) to store the result of the contraction

Remarks

Note that it is NOT safe to pass `arr_j` as a result buffer, as this operation does multiple passes.

Definition at line 357 of file `tensor_def.f90`.

```

357 CLASS(tensor), INTENT(IN) :: mtensor
358 REAL(KIND=8), DIMENSION(0:size(mtensor%t)), INTENT(IN) :: arr_j
359 REAL(KIND=8), DIMENSION(0:size(mtensor%t)), INTENT(OUT) :: res

```

```

360     INTEGER :: i,j,n
361     res=0.d0
362     DO i=1,mtensor%ndim()
363         DO n=1,mtensor%(i)%elems
364             j=mtensor%(i)%elems(n)%j
365             res(i) = res(i) + mtensor%(i)%elems(n)%v * arr_j(j)
366         END DO
367     END DO

```

6.13.2.14 sparse_mul3()

```

subroutine tensor_def::sparse_mul3 (
    class(tensor), intent(in) mtensor,
    real(kind=8), dimension(0:size(mtensor%t)), intent(in) arr_j,
    real(kind=8), dimension(0:size(mtensor%t)), intent(in) arr_k,
    real(kind=8), dimension(0:size(mtensor%t)), intent(out) res ) [private]

```

Sparse multiplication of a tensor with two vectors: $\sum_{j,k=0}^{ndim} T_{i,j,k} a_j b_k$.

Parameters

in	<i>mtensor</i>	A sparse tensor of which index 2 and 3 will be contracted.
in	<i>arr_j</i>	The vector <i>a</i> to be contracted with index 2 of the tensor.
in	<i>arr_k</i>	The vector <i>b</i> to be contracted with index 3 of the tensor.
out	<i>res</i>	Vector to store the result of the contraction.

Remarks

Note that it is NOT safe to pass *arr_j* or *arr_k* as a result buffer, as this operation does multiple passes. However, passing the same vector as *arr_j* and *arr_k* is safe.

Definition at line 196 of file tensor_def.f90.

```

196     CLASS(tensor), INTENT(IN) :: mtensor
197     REAL(KIND=8), DIMENSION(0:size(mtensor%t)), INTENT(IN) :: arr_j, arr_k
198     REAL(KIND=8), DIMENSION(0:size(mtensor%t)), INTENT(OUT) :: res
199     INTEGER :: i,j,k,n
200     res=0.d0
201     DO i=1,mtensor%ndim()
202         DO n=1,mtensor%(i)%elems
203             j=mtensor%(i)%elems(n)%j
204             k=mtensor%(i)%elems(n)%k
205             res(i) = res(i) + mtensor%(i)%elems(n)%v * arr_j(j)*arr_k(k)
206         END DO
207     END DO

```

6.13.2.15 tensor_size()

```

integer function tensor_def::tensor_size (
    class(tensor) mtensor ) [private]

```

Parameters

<i>mtensor</i>	The tensor to return the size of.
----------------	-----------------------------------

Returns

The size of the tensor

Definition at line 119 of file tensor_def.f90.

```
119    CLASS(tensor) :: mtensor
120    INTEGER :: ndim
121    ndim = size(mtensor%t)
```

6.13.2.16 test_alloc()

```
logical function tensor_def::test_alloc (
    class(tensor) mtensor )
```

Function to test if the tensor is allocated.

Parameters

<i>mtensor</i>	The tensor to test.
----------------	---------------------

Returns

A boolean indicating if the tensor is allocated.

Definition at line 64 of file tensor_def.f90.

```
64    CLASS(tensor) :: mtensor
65    LOGICAL :: test_alloc
66
67    test_alloc = allocated(mtensor%t)
68
```

6.13.2.17 write_tensor_to_file()

```
subroutine tensor_def::write_tensor_to_file (
    class(tensor), intent(in) mtensor,
    character (len=*), intent(in) s ) [private]
```

Write a rank-3 tensor coolist to a file.

Parameters

	<i>mtensor</i>	The tensor to write
in	<i>s</i>	Filename

Definition at line 501 of file tensor_def.f90.

```

501  CLASS(tensor), INTENT(IN) :: mtensor
502  CHARACTER (LEN=*) , INTENT(IN) :: s
503  INTEGER :: i, j, k, n
504  OPEN(30, file=s)
505  WRITE(30, *) mtensor%ndim()
506  DO i=1,mtensor%ndim()
507      WRITE(30, *) i,mtensor%t(i)%elems
508      DO n=1,mtensor%t(i)%elems
509          j=mtensor%t(i)%elems(n)%j
510          k=mtensor%t(i)%elems(n)%k
511          WRITE(30, *) i, j, k, mtensor%t(i)%elems(n)%v
512      END DO
513  END DO
514  CLOSE(30)

```

6.14 tl_ad_tensor Module Reference

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Tensors definition module.

Data Types

- type [adtensor](#)
Tensor representation of the Adjoint tendencies.
- type [tltensor](#)
Tensor representation of the Tangent Linear tendencies.

Functions/Subroutines

- subroutine [delete_tensor](#) (tens)
Subroutine to clean a TL tensor.
- subroutine [init_tltensor](#) (tens, aot)
Subroutine to initialise the TL tensor.
- subroutine [init_adtensor](#) (tens, aot)
Subroutine to initialise the AD tensor.

6.14.1 Detailed Description

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Tensors definition module.

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6.14.2 Function/Subroutine Documentation

6.14.2.1 delete_tensor()

```
subroutine tl_ad_tensor::delete_tensor (  
    class(tltensor), intent(inout) tens )
```

Subroutine to clean a TL tensor.

Parameters

in, out	<i>tens</i>	The tensor to clean.
---------	-------------	----------------------

Definition at line 64 of file tl_ad_tensor.f90.

```

64      CLASS(tltensor), INTENT(INOUT) :: tens
65
66      IF (allocated(tens%count_elems)) DEALLOCATE(tens%count_elems)
67
68      CALL tens%tensor%clean
69
70      tens%initialized = .false.
71

```

6.14.2.2 init_adtensor()

```

subroutine tl_ad_tensor::init_adtensor (
    class(adtensor), intent(inout) tens,
    class(atmoctensor), intent(in), target aot ) [private]

```

Subroutine to initialise the AD tensor.

Parameters

in, out	<i>tens</i>	The tensor to clean.
in	<i>aot</i>	A Atmosphere-Ocean tensor to initialize the AD tensor with.

Definition at line 204 of file tl_ad_tensor.f90.

```

204      CLASS(adtensor), INTENT(INOUT) :: tens
205      CLASS(atmoctensor), INTENT(IN), TARGET :: aot
206
207      INTEGER :: i
208      INTEGER, POINTER :: ndim
209      INTEGER :: allocstat
210
211      IF (.NOT.aot%initialized) THEN
212          print*, 'Provided AO tensor not yet initialized, impossible to initialize AD tensor!'
213          RETURN
214      END IF
215
216      ndim => aot%ndim
217
218      ALLOCATE(tens%count_elems(ndim), stat=allocstat)
219      IF (allocstat /= 0) THEN
220          print*, "*** init_adtensor: Problem with allocation! ***"
221          stop "Exiting ..."
222      END IF
223      tens%count_elems=0
224
225      CALL tens%tensor%init(ndim)
226
227      tens%ad_operation => ad_add_count
228      CALL tens%compute_tensor(aot)
229
230      DO i=1,ndim
231          ALLOCATE(tens%tensor%i%elems(tens%count_elems(i)), stat=allocstat)
232          IF (allocstat /= 0) THEN
233              print*, "*** init_adtensor: Problem with allocation! ***"
234              stop "Exiting ..."
235          END IF
236      END DO

```

```

237
238     tens%ad_operation => ad_coeff
239     CALL tens%compute_tensor(aot)
240
241     CALL tens%tensor%simplify
242
243     tens%initialized = .true.
244

```

6.14.2.3 init_tltensor()

```

subroutine tl_ad_tensor::init_tltensor (
    class(tltensor), intent(inout) tens,
    class(atmoctensor), intent(in), target aot ) [private]

```

Subroutine to initialise the TL tensor.

Parameters

in, out	<i>tens</i>	The tensor to clean.
in	<i>aot</i>	A Atmosphere-Ocean tensor to initialize the TL tensor with.

Definition at line 85 of file tl_ad_tensor.f90.

```

85     CLASS(tltensor), INTENT(INOUT) :: tens
86     CLASS(atmoctensor), INTENT(IN), TARGET :: aot
87
88     INTEGER :: i
89     INTEGER, POINTER :: ndim
90     INTEGER :: allocstat
91
92     IF (.NOT.aot%initialized) THEN
93         print*, 'Provided AO tensor not yet initialized, impossible to initialize TL tensor!'
94         RETURN
95     END IF
96
97     ndim => aot%ndim
98
99     ALLOCATE(tens%count_elems(ndim), stat=allocstat)
100     IF (allocstat /= 0) THEN
101         print*, "*** init_tltensor: Problem with allocation! ***"
102         stop "Exiting ..."
103     END IF
104     tens%count_elems=0
105
106     CALL tens%tensor%init(ndim)
107
108     tens%tl_operation => tl_add_count
109     CALL tens%compute_tensor(aot)
110
111     DO i=1,ndim
112         ALLOCATE(tens%tensor%i%elems(tens%count_elems(i)), stat=allocstat)
113         IF (allocstat /= 0) THEN
114             print*, "*** init_tltensor: Problem with allocation! ***"
115             stop "Exiting ..."
116         END IF
117     END DO
118
119     tens%tl_operation => tl_coeff
120     CALL tens%compute_tensor(aot)
121
122     CALL tens%tensor%simplify
123
124     tens%initialized = .true.
125

```

6.15 util Module Reference

Utility module.

Functions/Subroutines

- character(len=20) function, public `str` (k)
Convert an integer to string.
- character(len=40) function, public `rstr` (x, fm)
Convert a real to string with a given format.
- integer function, dimension(size(s)), public `isin` (c, s)
Determine if a character is in a string and where.
- subroutine, public `init_random_seed` ()
Random generator initialization routine.
- subroutine, public `piksort` (k, arr, par)
Simple card player sorting function.
- subroutine, public `init_one` (A)
Initialize a square matrix A as a unit matrix.

6.15.1 Detailed Description

Utility module.

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6.15.2 Function/Subroutine Documentation

6.15.2.1 `isin()`

```
integer function, dimension(size(s)), public util::isin (
    character, intent(in) c,
    character, dimension(:), intent(in) s )
```

Determine if a character is in a string and where.

Remarks

: return positions in a vector if found and 0 vector if not found

Definition at line 45 of file util.f90.

```
45     CHARACTER, INTENT(IN) :: c
46     CHARACTER, DIMENSION(:), INTENT(IN) :: s
47     INTEGER, DIMENSION(size(s)) :: isin
48     INTEGER :: i, j
49
50     isin=0
51     j=0
52     DO i=size(s),1,-1
53         IF (c==s(i)) THEN
54             j=j+1
55             isin(j)=i
56         END IF
57     END DO
```

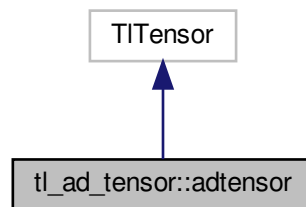

Chapter 7

Data Type Documentation

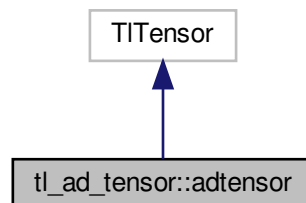
7.1 tl_ad_tensor::adtensor Type Reference

Tensor representation of the Adjoint tendencies.

Inheritance diagram for tl_ad_tensor::adtensor:



Collaboration diagram for tl_ad_tensor::adtensor:



7.1.1 Detailed Description

Tensor representation of the Adjoint tendencies.

Definition at line 46 of file `tl_ad_tensor.f90`.

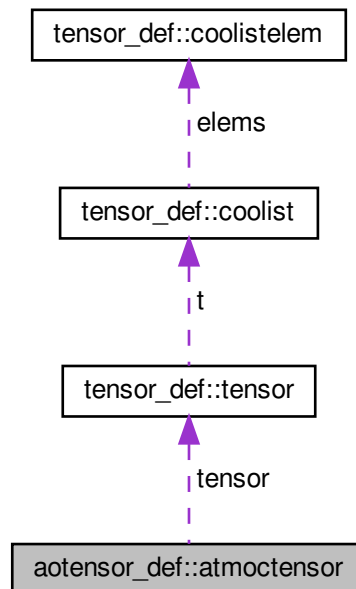
The documentation for this type was generated from the following file:

- `tl_ad_tensor.f90`

7.2 `aotensor_def::atmoctensor` Type Reference

Class to hold the tensor $\mathcal{T}_{i,j,k}$ representation of the tendencies.

Collaboration diagram for `aotensor_def::atmoctensor`:



Public Attributes

- `type(tensor) tensor`
The tensor object.
- `integer, dimension(:), allocatable count_elems`
A list of the number of non-zero entries of the tensor component along i .

7.3.1 Detailed Description

Class holding the atmospheric inner products functions.

Definition at line 51 of file inprod_analytic.f90.

The documentation for this type was generated from the following file:

- inprod_analytic.f90

7.4 inprod_analytic::atmosphericwavenumber Type Reference

Atmospheric bloc specification object.

7.4.1 Detailed Description

Atmospheric bloc specification object.

Definition at line 38 of file inprod_analytic.f90.

The documentation for this type was generated from the following file:

- inprod_analytic.f90

7.5 integrator_def::clean_int Interface Reference

Abstract interface for the procedure to clean the integrator objects.

7.5.1 Detailed Description

Abstract interface for the procedure to clean the integrator objects.

Parameters

<i>in, out</i>	<i>integr</i>	Integrator object to clean.
----------------	---------------	-----------------------------

Definition at line 62 of file integrator_def.f90.

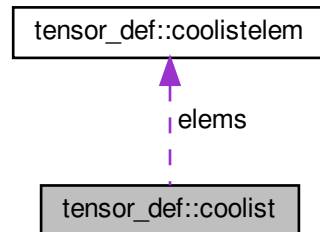
The documentation for this interface was generated from the following file:

- integrator_def.f90

7.6 tensor_def::coolist Type Reference

Coordinate list. Type used to represent the sparse tensor.

Collaboration diagram for tensor_def::coolist:



Private Attributes

- type([coolistelem](#)), dimension(:), allocatable [elems](#)
Lists of elements tensor_def::coolist_elem.
- integer [nelems](#) = 0
Number of elements in the list.

7.6.1 Detailed Description

Coordinate list. Type used to represent the sparse tensor.

Definition at line 30 of file tensor_def.f90.

The documentation for this type was generated from the following file:

- tensor_def.f90

7.7 tensor_def::coolistelem Type Reference

Coordinate list element type. Elementary elements of the sparse tensors.

Private Attributes

- integer [j](#)
Index j of the element.
- integer [k](#)
Index k of the element.
- real(kind=8) [v](#)
Value of the element.

7.7.1 Detailed Description

Coordinate list element type. Elementary elements of the sparse tensors.

Definition at line 23 of file tensor_def.f90.

The documentation for this type was generated from the following file:

- tensor_def.f90

7.8 integrator_def::init_int Interface Reference

Abstract interface for the procedures initializing the integrator objects.

7.8.1 Detailed Description

Abstract interface for the procedures initializing the integrator objects.

Parameters

in, out	<i>integr</i>	Integrator object to initialize.
in	<i>imodel</i>	Model object to initialize the integrator with.

Definition at line 37 of file integrator_def.f90.

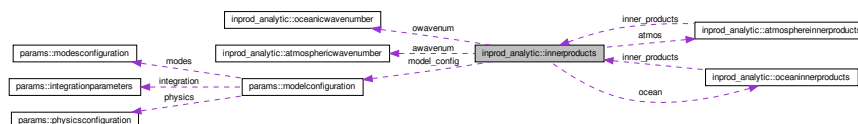
The documentation for this interface was generated from the following file:

- integrator_def.f90

7.9 inprod_analytic::innerproducts Type Reference

Global class for the inner products. Contains also the modes informations.

Collaboration diagram for inprod_analytic::innerproducts:



Public Member Functions

- PROCEDURE `init` => `init_inner_products`
Procedure to initialize the inner products functions based on the modes configuration.
- PROCEDURE `clean` => `delete_inner_products`
Procedure to clean the inner products object.

Public Attributes

- type(modelconfiguration), pointer model_config
Pointer to a model configuration object.
- type(atmosphericwavenumber), dimension(:), allocatable, public awavenum
Atmospheric blocs specification.
- type(oceanicwavenumber), dimension(:), allocatable, public owavenum
Oceanic blocs specification.
- type(atmosphereinnerproducts), public atmos
Atmospheric tensors.
- type(oceaninnerproducts), public ocean
Oceanic tensors.

7.9.1 Detailed Description

Global class for the inner products. Contains also the modes informations.

Definition at line 75 of file inprod_analytic.f90.

The documentation for this type was generated from the following file:

- inprod_analytic.f90

7.10 params::integrationparameters Type Reference

The subclass containing the integration parameters.

Public Attributes

- real(kind=8) t_trans
Transient time period.
- real(kind=8) t_run
Effective intergration time (length of the generated trajectory)
- real(kind=8) dt
Integration time step.
- real(kind=8) tw
Write all variables every tw time units.
- real(kind=8) tw_snap
Write a snapshot every tw_snap time units.
- logical writeout
Write to file boolean.

7.10.1 Detailed Description

The subclass containing the integration parameters.

Definition at line 79 of file params.f90.

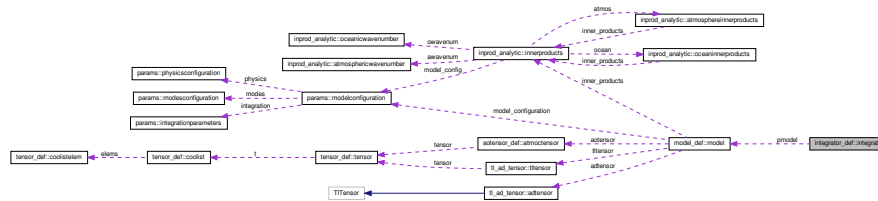
The documentation for this type was generated from the following file:

- params.f90

7.11 integrator_def::integrator Type Reference

Base class to be subclassed to create a new integrator.

Collaboration diagram for integrator_def::integrator:



Public Attributes

- type([model](#)), pointer [pmodel](#)
A pointer to the model to integrate.
- real(kind=8), pointer [dt](#)
Time step of the integrator.
- integer, pointer [ndim](#)
Dimension of the phase space of the model to integrate.

7.11.1 Detailed Description

Base class to be subclassed to create a new integrator.

Definition at line 23 of file integrator_def.f90.

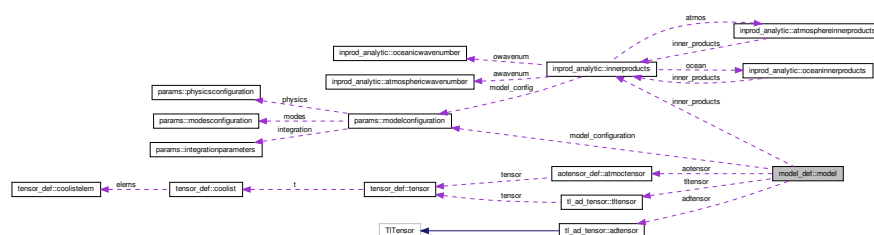
The documentation for this type was generated from the following file:

- integrator_def.f90

7.12 model_def::model Type Reference

Class to hold the components of a model version.

Collaboration diagram for model_def::model:



Public Attributes

- type(modelconfiguration) `model_configuration`
Model configuration object of the model.
- type(innerproducts) `inner_products`
Inner products object of the model.
- type(atmoctensor) `aotensor`
Atmosphere-Ocean tendencies tensor of the model.
- type(tltensor) `tltensor`
Tangent linear model tendencies.
- type(adtensor) `adtensor`
Adjoint model tendencies.
- integer, pointer `ndim`
Dimension of the phase space of the model to integrate.

7.12.1 Detailed Description

Class to hold the components of a model version.

Definition at line 25 of file `model_def.f90`.

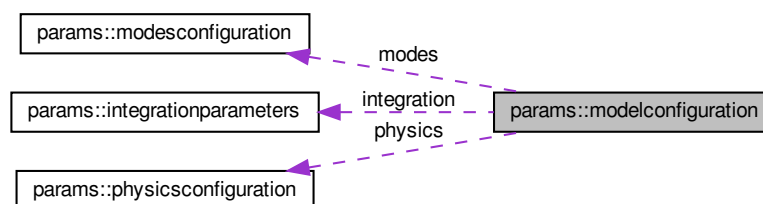
The documentation for this type was generated from the following file:

- `model_def.f90`

7.13 params::modelconfiguration Type Reference

The general class holding the model configuration.

Collaboration diagram for `params::modelconfiguration`:



7.13.1 Detailed Description

The general class holding the model configuration.

Definition at line 107 of file `params.f90`.

The documentation for this type was generated from the following file:

- `params.f90`

7.14 params::modesconfiguration Type Reference

The subclass containing the modes parameters.

Public Attributes

- integer `nboc`
Number of atmospheric blocks.
- integer `nbatm`
Number of oceanic blocks.
- integer, dimension(:,:), allocatable `oms`
Ocean mode selection array.
- integer, dimension(:,:), allocatable `ams`
Atmospheric mode selection array.
- integer `natm` =0
Number of atmospheric basis functions.
- integer `noc` =0
Number of oceanic basis functions.
- integer `ndim`
Number of variables (dimension of the model)

7.14.1 Detailed Description

The subclass containing the modes parameters.

Definition at line 92 of file `params.f90`.

The documentation for this type was generated from the following file:

- `params.f90`

7.15 inprod_analytic::oceanicwavenumber Type Reference

Oceanic bloc specification object.

7.15.1 Detailed Description

Oceanic bloc specification object.

Definition at line 45 of file `inprod_analytic.f90`.

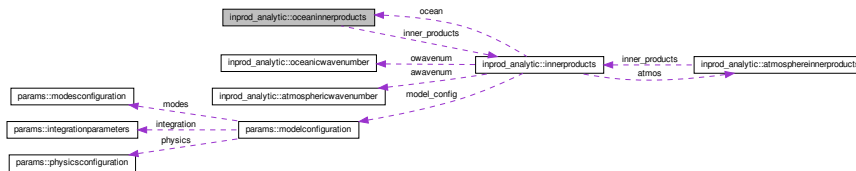
The documentation for this type was generated from the following file:

- `inprod_analytic.f90`

7.16 inprod_analytic::oceaninnerproducts Type Reference

Class holding the oceanic inner products functions.

Collaboration diagram for inprod_analytic::oceaninnerproducts:



Private Member Functions

- PROCEDURE **k** => calculate_K
Forcing of the atmosphere on the ocean.
- PROCEDURE **m** => calculate_M
Forcing of the ocean fields on the ocean.
- PROCEDURE **c** => calculate_C_oc
Streamfunction advection terms (oceanic)
- PROCEDURE **n** => calculate_N
Beta term for the ocean.
- PROCEDURE **o** => calculate_O
Temperature advection term (passive scalar)
- PROCEDURE **w** => calculate_W
Short-wave radiative forcing of the ocean.

Private Attributes

- type(**innerproducts**), pointer **inner_products**
Pointer to a global inner products object.

7.16.1 Detailed Description

Class holding the oceanic inner products functions.

Definition at line 63 of file inprod_analytic.f90.

The documentation for this type was generated from the following file:

- inprod_analytic.f90

7.17 params::physicsconfiguration Type Reference

The subclass containing the physical parameters of the model.

Public Attributes

- real(kind=8) **n**
 $n = 2L_y/L_x$ - Aspect ratio
- real(kind=8) **phi0**
Latitude in radian.
- real(kind=8) **rra**
Earth radius.
- real(kind=8) **sig0**
 σ_0 - Non-dimensional static stability of the atmosphere.
- real(kind=8) **k**
Bottom atmospheric friction coefficient.
- real(kind=8) **kp**
 k' - Internal atmospheric friction coefficient.
- real(kind=8) **r**
Frictional coefficient at the bottom of the ocean.
- real(kind=8) **d**
Merchanical coupling parameter between the ocean and the atmosphere.
- real(kind=8) **f0**
 f_0 - Coriolis parameter
- real(kind=8) **gp**
 g' Reduced gravity
- real(kind=8) **h**
Depth of the active water layer of the ocean.
- real(kind=8) **phi0_npi**
Latitude exprimed in fraction of pi.
- real(kind=8) **lambda**
 λ - Sensible + turbulent heat exchange between the ocean and the atmosphere.
- real(kind=8) **co**
 C_a - Constant short-wave radiation of the ocean.
- real(kind=8) **go**
 γ_o - Specific heat capacity of the ocean.
- real(kind=8) **ca**
 C_a - Constant short-wave radiation of the atmosphere.
- real(kind=8) **to0**
 T_o^0 - Stationary solution for the 0-th order ocean temperature.
- real(kind=8) **ta0**
 T_a^0 - Stationary solution for the 0-th order atmospheric temperature.
- real(kind=8) **epsa**
 ϵ_a - Emissivity coefficient for the grey-body atmosphere.
- real(kind=8) **ga**
 γ_a - Specific heat capacity of the atmosphere.
- real(kind=8) **rr**
 R - Gas constant of dry air
- real(kind=8) **scale**
 $L_y = L \pi$ - The characteristic space scale.
- real(kind=8) **pi**
 π
- real(kind=8) **lr**
 L_R - Rossby deformation radius
- real(kind=8) **g**

- γ
 - real(kind=8) [rp](#)
r' - Frictional coefficient at the bottom of the ocean.
 - real(kind=8) [dp](#)
d' - Non-dimensional mechanical coupling parameter between the ocean and the atmosphere.
 - real(kind=8) [kd](#)
k_d - Non-dimensional bottom atmospheric friction coefficient.
 - real(kind=8) [kdp](#)
k'_d - Non-dimensional internal atmospheric friction coefficient.
 - real(kind=8) [cpo](#)
C'_a - Non-dimensional constant short-wave radiation of the ocean.
 - real(kind=8) [lpo](#)
λ'_o - Non-dimensional sensible + turbulent heat exchange from ocean to atmosphere.
 - real(kind=8) [cpa](#)
C'_a - Non-dimensional constant short-wave radiation of the atmosphere.
 - real(kind=8) [lpa](#)
λ'_a - Non-dimensional sensible + turbulent heat exchange from atmosphere to ocean.
 - real(kind=8) [sbpo](#)
σ'_{B,o} - Long wave radiation lost by ocean to atmosphere & space.
 - real(kind=8) [sbpa](#)
σ'_{B,a} - Long wave radiation from atmosphere absorbed by ocean.
 - real(kind=8) [lsbpo](#)
S'_{B,o} - Long wave radiation from ocean absorbed by atmosphere.
 - real(kind=8) [lsbpa](#)
S'_{B,a} - Long wave radiation lost by atmosphere to space & ocean.
 - real(kind=8) [l](#)
L - Domain length scale
 - real(kind=8) [sc](#)
Ratio of surface to atmosphere temperature.
 - real(kind=8) [sb](#)
Stefan–Boltzmann constant.
 - real(kind=8) [betp](#)
β' - Non-dimensional beta parameter
 - real(kind=8) [nua](#) = 0.D0
Dissipation in the atmosphere.
 - real(kind=8) [nuo](#) = 0.D0
Dissipation in the ocean.
 - real(kind=8) [nuap](#)
Non-dimensional dissipation in the atmosphere.
 - real(kind=8) [nuop](#)
Non-dimensional dissipation in the ocean.

7.17.1 Detailed Description

The subclass containing the physical parameters of the model.

Definition at line 22 of file params.f90.

7.17.2 Member Data Documentation

7.17.2.1 cpa

```
real(kind=8) params::physicsconfiguration::cpa
```

C'_a - Non-dimensional constant short-wave radiation of the atmosphere.

Remarks

Cpa acts on psi1-psi3, not on theta.

Definition at line 57 of file params.f90.

```
57      REAL(KIND=8) :: cpa          !< \f$C'_a\f$ - Non-dimensional constant short-wave radiation of the
      atmosphere. @remark Cpa acts on psi1-psi3, not on theta.
```

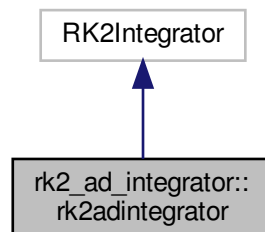
The documentation for this type was generated from the following file:

- params.f90

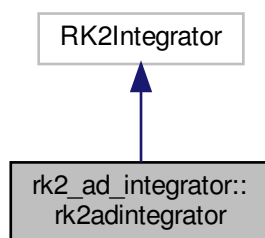
7.18 rk2_ad_integrator::rk2adintegrator Type Reference

Class for the Heun (RK2) AD integrator object.

Inheritance diagram for rk2_ad_integrator::rk2adintegrator:



Collaboration diagram for rk2_ad_integrator::rk2adintegrator:



7.18.1 Detailed Description

Class for the Heun (RK2) AD integrator object.

Definition at line 29 of file `rk2_ad_integrator.f90`.

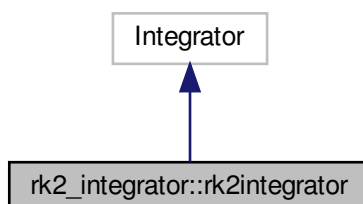
The documentation for this type was generated from the following file:

- `rk2_ad_integrator.f90`

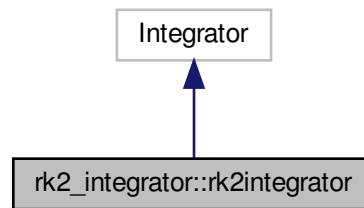
7.19 rk2_integrator::rk2integrator Type Reference

Class for the Heun (RK2) integrator object.

Inheritance diagram for `rk2_integrator::rk2integrator`:



Collaboration diagram for `rk2_integrator::rk2integrator`:



Public Attributes

- `real(kind=8), dimension(:), allocatable buf_y1`
Buffer to hold the intermediate position (Heun algorithm)
- `real(kind=8), dimension(:), allocatable buf_f0`
Buffer to hold tendencies at the initial position.
- `real(kind=8), dimension(:), allocatable buf_f1`
Buffer to hold tendencies at the intermediate position.

7.19.1 Detailed Description

Class for the Heun (RK2) integrator object.

Definition at line 25 of file `rk2_integrator.f90`.

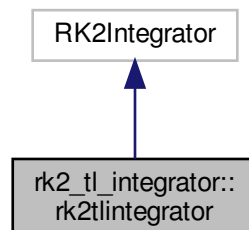
The documentation for this type was generated from the following file:

- `rk2_integrator.f90`

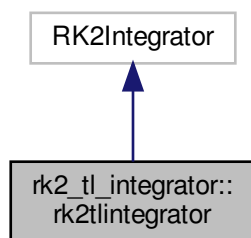
7.20 `rk2_tl_integrator::rk2tlintegrator` Type Reference

Class for the Heun (RK2) TL integrator object.

Inheritance diagram for `rk2_tl_integrator::rk2tlintegrator`:



Collaboration diagram for rk2_tl_integrator::rk2tlinTEGRATOR:



7.20.1 Detailed Description

Class for the Heun (RK2) TL integrator object.

Definition at line 29 of file rk2_tl_integrator.f90.

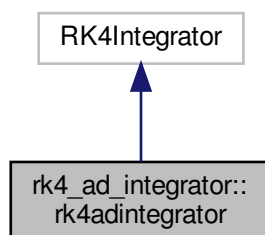
The documentation for this type was generated from the following file:

- rk2_tl_integrator.f90

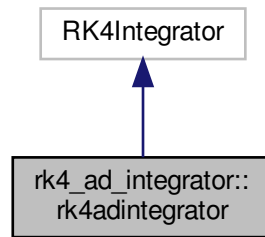
7.21 rk4_ad_integrator::rk4adintegrator Type Reference

Class for the fourth-order Runge-Kutta (RK4) AD integrator object.

Inheritance diagram for rk4_ad_integrator::rk4adintegrator:



Collaboration diagram for `rk4_ad_integrator::rk4adintegrator`:



7.21.1 Detailed Description

Class for the fourth-order Runge-Kutta (RK4) AD integrator object.

Definition at line 27 of file `rk4_ad_integrator.f90`.

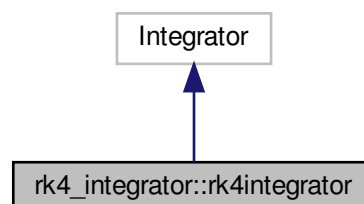
The documentation for this type was generated from the following file:

- `rk4_ad_integrator.f90`

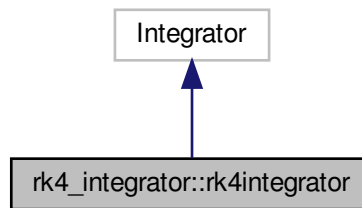
7.22 `rk4_integrator::rk4integrator` Type Reference

Class for the fourth-order Runge-Kutta (RK4) integrator object.

Inheritance diagram for `rk4_integrator::rk4integrator`:



Collaboration diagram for rk4_integrator::rk4integrator:



Public Attributes

- real(kind=8), dimension(:), allocatable [buf_y1](#)
Buffer to hold the intermediate position.
- real(kind=8), dimension(:), allocatable [buf_ka](#)
Buffer to hold tendencies at the initial position.
- real(kind=8), dimension(:), allocatable [buf_kb](#)
Buffer to hold tendencies at the intermediate position.

7.22.1 Detailed Description

Class for the fourth-order Runge-Kutta (RK4) integrator object.

Definition at line 23 of file rk4_integrator.f90.

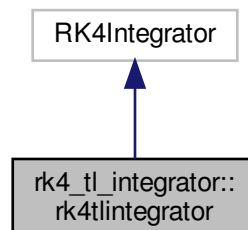
The documentation for this type was generated from the following file:

- rk4_integrator.f90

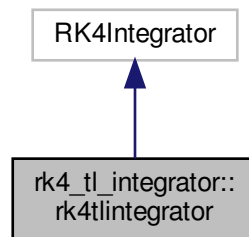
7.23 rk4_tl_integrator::rk4tlintegrator Type Reference

Class for the fourth-order Runge-Kutta (RK4) TL integrator object.

Inheritance diagram for rk4_tl_integrator::rk4tlintegrator:



Collaboration diagram for `rk4_tl_integrator::rk4tlintegrator`:



7.23.1 Detailed Description

Class for the fourth-order Runge-Kutta (RK4) TL integrator object.

Definition at line 27 of file `rk4_tl_integrator.f90`.

The documentation for this type was generated from the following file:

- `rk4_tl_integrator.f90`

7.24 `stat::stataccumulator` Type Reference

Statistics accumulator objects class.

Public Attributes

- integer `i` = 0
Number of stats accumulated.
- `real(kind=8), dimension(:), allocatable` `m`
Vector storing the inline mean.
- `real(kind=8), dimension(:), allocatable` `mprev`
Previous mean vector.
- `real(kind=8), dimension(:), allocatable` `v`
Vector storing the inline variance.

7.24.1 Detailed Description

Statistics accumulator objects class.

Definition at line 20 of file `stat.f90`.

The documentation for this type was generated from the following file:

- `stat.f90`

7.25 integrator_def::step_int Interface Reference

Abstract interface for the procedure to make the integrator compute a model's time step.

7.25.1 Detailed Description

Abstract interface for the procedure to make the integrator compute a model's time step.

Parameters

in, out	<i>integr</i>	Integrator object to perform the step with.
in	<i>y</i>	Initial point.
in	<i>t</i>	Actual integration time
out	<i>res</i>	Final point after the step.

Definition at line 50 of file integrator_def.f90.

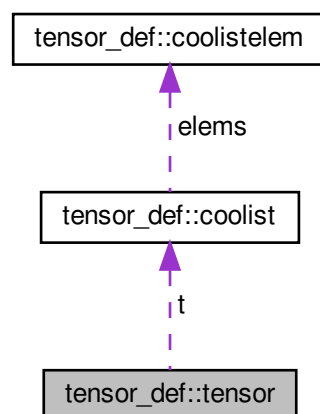
The documentation for this interface was generated from the following file:

- integrator_def.f90

7.26 tensor_def::tensor Type Reference

General class to represent a sparse tensor.

Collaboration diagram for tensor_def::tensor:



Public Attributes

- `type(colist)`, `dimension(:)`, allocatable `t`
Sparse representation of the tensor as a `tensor_def::colist`.

7.26.1 Detailed Description

General class to represent a sparse tensor.

Definition at line 36 of file `tensor_def.f90`.

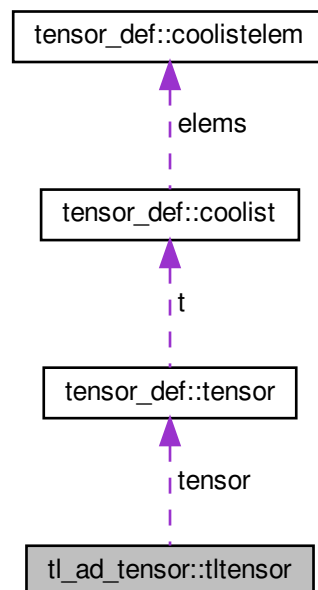
The documentation for this type was generated from the following file:

- `tensor_def.f90`

7.27 `tl_ad_tensor::tltensor` Type Reference

Tensor representation of the Tangent Linear tendencies.

Collaboration diagram for `tl_ad_tensor::tltensor`:



Public Attributes

- `type(tensor)` `tensor`
The TL tensor object.
- `integer`, `dimension(:)`, allocatable `count_elems`
A list of the number of non-zero entries of the tensor component along the first index.

7.27.1 Detailed Description

Tensor representation of the Tangent Linear tendencies.

Definition at line 34 of file `tl_ad_tensor.f90`.

The documentation for this type was generated from the following file:

- `tl_ad_tensor.f90`

Index

acc
 stat, [46](#)

ad_step
 rk2_ad_integrator, [36](#)
 rk4_ad_integrator, [41](#)

ad_tendencies
 model_def, [26](#)

add_elem
 tensor_def, [51](#)

add_from_tensor
 tensor_def, [52](#)

aotensor_def, [13](#)
 delete_aotensor, [13](#)
 init_aotensor, [14](#)

aotensor_def::atmactensor, [70](#)

calculate_a
 inprod_analytic, [16](#)

calculate_b
 inprod_analytic, [16](#)

calculate_c_atm
 inprod_analytic, [17](#)

calculate_c_oc
 inprod_analytic, [17](#)

calculate_d
 inprod_analytic, [18](#)

calculate_g
 inprod_analytic, [18](#)

calculate_k
 inprod_analytic, [20](#)

calculate_m
 inprod_analytic, [20](#)

calculate_n
 inprod_analytic, [20](#)

calculate_o
 inprod_analytic, [21](#)

calculate_s
 inprod_analytic, [21](#)

calculate_w
 inprod_analytic, [22](#)

clean
 rk2_integrator, [38](#)
 rk4_integrator, [42](#)
 stat, [47](#)
 tensor_def, [53](#)

clean_model_config
 params, [34](#)

copy
 tensor_def, [53](#)

cpa
 params::physicsconfiguration, [82](#)

delete_aotensor
 aotensor_def, [13](#)

delete_inner_products
 inprod_analytic, [22](#)

delete_model
 model_def, [26](#)

delete_tensor
 tl_ad_tensor, [64](#)

empty
 tensor_def, [54](#)

from_mat
 tensor_def, [54](#)

init
 rk2_integrator, [38](#)
 rk4_integrator, [43](#)
 tensor_def, [55](#)

init_ad_model
 model_def, [27](#)

init_adtensor
 tl_ad_tensor, [65](#)

init_aotensor
 aotensor_def, [14](#)

init_inner_products
 inprod_analytic, [23](#)

init_model
 model_def, [27](#)

init_model_config
 params, [35](#)

init_stat
 stat, [47](#)

init_tl_model
 model_def, [28](#)

init_tltensor
 tl_ad_tensor, [66](#)

inprod_analytic, [15](#)
 calculate_a, [16](#)
 calculate_b, [16](#)
 calculate_c_atm, [17](#)
 calculate_c_oc, [17](#)
 calculate_d, [18](#)
 calculate_g, [18](#)
 calculate_k, [20](#)
 calculate_m, [20](#)
 calculate_n, [20](#)
 calculate_o, [21](#)

- calculate_s, 21
 - calculate_w, 22
 - delete_inner_products, 22
 - init_inner_products, 23
- inprod_analytic::atmosphereinnerproducts, 71
- inprod_analytic::atmosphericwavenumber, 72
- inprod_analytic::innerproducts, 74
- inprod_analytic::oceanicwavenumber, 78
- inprod_analytic::oceaninnerproducts, 79
- integrator_def, 24
- integrator_def::clean_int, 72
- integrator_def::init_int, 74
- integrator_def::integrator, 76
- integrator_def::step_int, 89
- isin
 - util, 67
- iter
 - stat, 48
- jacobian
 - model_def, 28
- jacobian_mat
 - model_def, 30
- jsparse_mul
 - tensor_def, 56
- jsparse_mul_mat
 - tensor_def, 57
- load_ic
 - model_def, 30
- load_tensor_from_file
 - tensor_def, 57
- mean
 - stat, 48
- model_def, 25
 - ad_tendencies, 26
 - delete_model, 26
 - init_ad_model, 27
 - init_model, 27
 - init_tl_model, 28
 - jacobian, 28
 - jacobian_mat, 30
 - load_ic, 30
 - tendencies, 32
 - tl_tendencies, 33
- model_def::model, 76
- params, 34
 - clean_model_config, 34
 - init_model_config, 35
- params::integrationparameters, 75
- params::modelconfiguration, 77
- params::modesconfiguration, 78
- params::physicsconfiguration, 79
 - cpa, 82
- print_tensor
 - tensor_def, 58
- reset
 - stat, 49
- rk2_ad_integrator, 36
 - ad_step, 36
- rk2_ad_integrator::rk2adintegrator, 82
- rk2_integrator, 37
 - clean, 38
 - init, 38
 - step, 39
- rk2_integrator::rk2integrator, 83
- rk2_tl_integrator, 39
 - tl_step, 40
- rk2_tl_integrator::rk2tlintegrator, 84
- rk4_ad_integrator, 41
 - ad_step, 41
- rk4_ad_integrator::rk4adintegrator, 85
- rk4_integrator, 42
 - clean, 42
 - init, 43
 - step, 43
- rk4_integrator::rk4integrator, 86
- rk4_tl_integrator, 44
 - tl_step, 45
- rk4_tl_integrator::rk4tlintegrator, 87
- simplify
 - tensor_def, 59
- sparse_mul2
 - tensor_def, 60
- sparse_mul3
 - tensor_def, 61
- stat, 45
 - acc, 46
 - clean, 47
 - init_stat, 47
 - iter, 48
 - mean, 48
 - reset, 49
 - var, 49
- stat::stataccumulator, 88
- step
 - rk2_integrator, 39
 - rk4_integrator, 43
- tendencies
 - model_def, 32
- tensor_def, 50
 - add_elem, 51
 - add_from_tensor, 52
 - clean, 53
 - copy, 53
 - empty, 54
 - from_mat, 54
 - init, 55
 - jsparse_mul, 56
 - jsparse_mul_mat, 57
 - load_tensor_from_file, 57
 - print_tensor, 58
 - simplify, 59
 - sparse_mul2, 60

- sparse_mul3, [61](#)
 - tensor_size, [61](#)
 - test_alloc, [62](#)
 - write_tensor_to_file, [62](#)
- tensor_def::coolist, [73](#)
- tensor_def::coolistelem, [73](#)
- tensor_def::tensor, [89](#)
- tensor_size
 - tensor_def, [61](#)
- test_alloc
 - tensor_def, [62](#)
- tl_ad_tensor, [63](#)
 - delete_tensor, [64](#)
 - init_adtensor, [65](#)
 - init_tltensor, [66](#)
- tl_ad_tensor::adtensor, [69](#)
- tl_ad_tensor::tltensor, [90](#)
- tl_step
 - rk2_tl_integrator, [40](#)
 - rk4_tl_integrator, [45](#)
- tl_tendencies
 - model_def, [33](#)
- util, [67](#)
 - isin, [67](#)
- var
 - stat, [49](#)
- write_tensor_to_file
 - tensor_def, [62](#)