# Reference Manual

Generated by Doxygen 1.8.3.1

Thu Mar 24 2016 14:02:17

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# **Chapter 1**

# **Main Page**

### **About**

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This software is provided as supplementary material with:

De Cruz, L., Demaeyer, J. and Vannitsem, S.: A modular arbitrary-order ocean-atmosphere model: MAOOA-M, Geosci. Model Dev. Discuss., doi:xx/xxx, 2016.

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The authors would appreciate it if you could also send a reprint of your paper to lesley.decruz@meteo.be, jonathan.demaeyer@meteo.be and svn@meteo.be.

Consult the MAOOAM code repository at doi:yy/yyy for updates, and our website for additional resources. A pdf version of this manual is available here.

# Installation

The code should be compiled with gfortran 4.7+ (allows for allocatable arrays in namelists). Unpack the archive in a folder, and run: make

Remark: The command "make clean" removes the compiled files.

For Windows users, a minimalistic GNU development environment (including gfortran and make) is available at <a href="https://www.mingw.org">www.mingw.org</a>.

# **Description of the files**

The model tendencies are represented through a tensor called aotensor which includes all the coefficients. This tensor is computed once at the program initialization.

- maooam.f90 : Main program.
- aotensor\_def.f90 : Tensor aotensor computation module.
- IC\_def.f90 : A module which loads the user specified initial condition.
- inprod\_analytic.f90 : Inner products computation module.
- integrator.f90 : A module which contains the integrator for the model equations.

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- · Makefile: The Makefile.
- params.f90 : The model parameters module.
- · maooam tl ad.f90: Tangent Linear (TL) and Adjoint (AD) model tensors definition module
- tl\_ad\_integrator.f90 : Tangent Linear (TL) and Adjoint (AD) model integrators module
- test\_tl\_ad.f90 : Tests for the Tangent Linear (TL) and Adjoint (AD) model versions
- · README.md: A read me file.
- LICENSE.txt: The license text of the program.
- util.f90 : A module with various useful functions.
- · stat.f90 : A module for statistic accumulation.
- · params.nml : A namelist to specify the model parameters.
- int params.nml : A namelist to specify the integration parameters.
- modeselection.nml : A namelist to specify which spectral decomposition will be used.

# **Usage**

The user first has to fill the params.nml and int params.nml namelist files according to their needs.

The modeselection.nml namelist can then be filled:

- NBOC and NBATM specify the number of blocks that will be used in respectively the ocean and the atmosphere. Each block corresponds to a given x and y wavenumber.
- The OMS and AMS arrays are integer arrays which specify which wavenumbers of the spectral decomposition
  will be used in respectively the ocean and the atmosphere. Their shapes are OMS(NBOC,2) and AMS(NBATM,2).
- The first dimension specifies the number attributed by the user to the block and the second dimension specifies the x and the y wavenumbers.
- The VDDG model, described in Vannitsem et al. (2015) is given as an example in the archive.
- Note that the variables of the model are numbered according to the chosen order of the blocks.

Model and integration parameters can be specified in the params.nml namelist file.

Finally, the IC.nml file specifying the initial condition should be defined. To obtain an example of this configuration file corresponding to the model you have previously defined, simply delete the current IC.nml file (if it exists) and run the program :

./maooam

It will generate a new one and start with the 0 initial condition. If you want another initial condition, stop the program, fill the newly generated file and restart :

./maooam

It will generate two files:

- · evol field.dat: the recorded time evolution of the variables.
- mean\_field.dat : the mean field (the climatology)

The tangent linear and adjoint models of MAOOAM are provided in the maooam\_tl\_ad and tl\_ad\_integrator module. It is documented here.

# Implementation notes

As the system of differential equations is at most bilinear in  $y_j$  ( j = 1..n), y being the array of variables, it can be expressed as a tensor contraction :

$$\frac{dy_i}{dt} = \sum_{j,k=0}^{ndim} \mathcal{T}_{i,j,k} y_k y_j$$

with  $y_0 = 1$ .

The tensor  $aotensor_def$ :: $aotensor_def$ ::a

- $\mathcal{T}_{i,j,k}$  contains the contribution of  $dy_i/dt$  proportional to  $y_j y_k$ .
- Furthermore,  $y_0$  is always equal to 1, so that  $\mathcal{T}_{i,0,0}$  is the constant contribution to  $dy_i/dt$
- $\mathcal{T}_{i,j,0} + \mathcal{T}_{i,0,j}$  is the contribution to  $dy_i/dt$  which is linear in  $y_j$ .

Ideally, the tensor aotensor\_def::aotensor is composed as an upper triangular matrix (in the last two coordinates).

The tensor for this model is composed in aotensor\_def and uses the inner products defined in inprod\_analytic .

# **Final Remarks**

The authors would like to thank Kris for help with the lua2fortran project. It has greatly reduced the amount of (error-prone) work.

No animals were harmed during the coding process.

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# **Chapter 2**

# Modular arbitrary-order ocean-atmosphere model: The Tangent Linear and Adjoint model

# **Description:**

The Tangent Linear and Adjoint model model are implemented in the same way as the nonlinear model, with a tensor storing the different terms. The Tangent Linear (TL) tensor  $\mathscr{T}^{TD}_{i,j,k}$  is defined as:

$$\mathscr{T}_{i,j,k}^{TL} = \mathscr{T}_{i,k,j} + \mathscr{T}_{i,j,k}$$

while the Adjoint (AD) tensor  $\mathscr{T}^{AD}_{i,j,k}$  is defined as:

$$\mathscr{T}_{i,j,k}^{AD} = \mathscr{T}_{j,k,i} + \mathscr{T}_{j,i,k}.$$

where  $\mathcal{T}_{i,j,k}$  is the tensor of the nonlinear model.

These two tensors are used to compute the trajectories of the models, with the equations

$$\frac{d\delta y_i}{dt} = \sum_{i=1}^{ndim} \sum_{k=0}^{ndim} \mathscr{T}_{i,j,k}^{TL} y_k^* \, \delta y_j.$$

$$-\frac{d\delta y_i}{dt} = \sum_{i=1}^{ndim \, ndim} \sum_{k=0}^{AD} \mathcal{T}_{i,j,k}^{AD} y_k^* \, \delta y_j.$$

where  $y^*$  is the point where the Tangent model is defined (with  $y_0^* = 1$ ).

# Implementation:

The two tensors are implemented in the module maooam\_tl\_ad and must be initialized (after calling params::init\_params and aotensor\_def::aotensor) by calling maooam\_tl\_ad::init\_tltensor() and maooam\_tl\_ad::init\_adtensor(). The tendencies are then given by the routine tl(t,ystar,deltay,buf) and ad(t,ystar,deltay,buf). An integrator with the Heun method is available in the module tl\_ad\_maooam. An example on how to use it can be found in the test file test\_tl\_ad.f90

| 6 | Modular arbitrary-order ocean-atmosphere model: The Tangent Linear and Adjoint model |
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# **Chapter 3**

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# Chapter 4

# File Index

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# **Chapter 5**

# **Data Type Documentation**

# 5.1 aotensor\_def Module Reference

The equation tensor for the coupled ocean-atmosphere model with temperature which allows for an extensible set of modes in the ocean and in the atmosphere.

# **Public Member Functions**

• subroutine, public init\_aotensor

Subroutine to initialise the aotensor tensor.

# **Public Attributes**

 type(coolist), dimension(:), allocatable, public aotensor

 $\mathscr{T}_{i,j,k}$  - Tensor representation of the tendencies.

# **Private Member Functions**

• integer function psi (i)

Translate the  $\psi_{a,i}$  coefficients into effective coordinates.

• integer function theta (i)

Translate the  $\theta_{a,i}$  coefficients into effective coordinates.

• integer function a (i)

Translate the  $\psi_{o,i}$  coefficients into effective coordinates.

• integer function t (i)

Translate the  $\delta T_{o,i}$  coefficients into effective coordinates.

• integer function kdelta (i, j)

Kronecker delta function.

• subroutine coeff (i, j, k, v)

Subroutine to add element in the aotensor  $\mathcal{T}_{i,j,k}$  structure.

• subroutine add\_count (i, j, k, v)

Subroutine to count the elements of the aotensor  $\mathcal{T}_{i,j,k}$ . Add +1 to count\_elems(i) for each value that is added to the tensor i-th component.

• subroutine compute\_aotensor (func)

Subroutine to compute the tensor aotensor.

# **Private Attributes**

integer, dimension(:), allocatable count\_elems

Vector used to count the tensor elements.

• real(kind=8), parameter real\_eps = 2.2204460492503131e-16

Epsilon to test equality with 0.

# 5.1.1 Detailed Description

The equation tensor for the coupled ocean-atmosphere model with temperature which allows for an extensible set of modes in the ocean and in the atmosphere.

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### Remarks

Generated Fortran90/95 code from ../../lua/aomodel extended/aotensor.lua

Definition at line 21 of file aotensor\_def.f90.

# 5.1.2 Member Function/Subroutine Documentation

**5.1.2.1** integer function aotensor\_def::a ( integer *i* ) [private]

Translate the  $\psi_{o,i}$  coefficients into effective coordinates.

Definition at line 75 of file aotensor\_def.f90.

5.1.2.2 subroutine aotensor\_def::add\_count ( integer, intent(in) *i*, integer, intent(in) *j*, integer, intent(in) *k*, real(kind=8), intent(in) *v* ) [private]

Subroutine to count the elements of the aotensor  $\mathcal{T}_{i,j,k}$ . Add +1 to count\_elems(i) for each value that is added to the tensor i-th component.

# **Parameters**

| i | tensor i index           |
|---|--------------------------|
| j | tensor j index           |
| k | tensor k index           |
| V | value that will be added |

Definition at line 123 of file aotensor\_def.f90.

5.1.2.3 subroutine aotensor\_def::coeff ( integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v ) [private]

Subroutine to add element in the aotensor  $\mathcal{T}_{i,j,k}$  structure.

# **Parameters**

| i | tensor i index   |
|---|------------------|
| j | tensor $j$ index |
| k | tensor k index   |
| V | value to add     |

Definition at line 98 of file aotensor\_def.f90.

**5.1.2.4** subroutine aotensor\_def::compute\_aotensor ( external func ) [private]

Subroutine to compute the tensor aotensor.

#### **Parameters**

```
func External function to be used
```

Definition at line 131 of file aotensor def.f90.

5.1.2.5 subroutine, public aotensor\_def::init\_aotensor ( )

Subroutine to initialise the aotensor tensor.

### Remarks

This procedure will also call params::init\_params() and inprod\_analytic::init\_inprod() . It will finally call inprod\_analytic::deallocate\_inprod() to remove the inner products, which are not needed anymore at this point.

Definition at line 201 of file aotensor def.f90.

**5.1.2.6** integer function aotensor\_def::kdelta ( integer *i*, integer *j* ) [private]

Kronecker delta function.

Definition at line 87 of file aotensor\_def.f90.

**5.1.2.7** integer function aotensor\_def::psi(integer i) [private]

Translate the  $\psi_{a,i}$  coefficients into effective coordinates.

Definition at line 63 of file aotensor\_def.f90.

**5.1.2.8** integer function aotensor\_def::t(integer i) [private]

Translate the  $\delta T_{o,i}$  coefficients into effective coordinates.

Definition at line 81 of file aotensor\_def.f90.

**5.1.2.9** integer function aotensor\_def::theta ( integer *i* ) [private]

Translate the  $\theta_{a,i}$  coefficients into effective coordinates.

Definition at line 69 of file aotensor def.f90.

# 5.1.3 Member Data Documentation

5.1.3.1 type(coolist), dimension(:), allocatable, public aotensor\_def::aotensor

 $\mathcal{T}_{i,j,k}$  - Tensor representation of the tendencies.

Definition at line 45 of file aotensor\_def.f90.

```
5.1.3.2 integer, dimension(:), allocatable aotensor_def::count_elems [private]
```

Vector used to count the tensor elements.

Definition at line 37 of file aotensor\_def.f90.

5.1.3.3 real(kind=8), parameter aotensor\_def::real\_eps = 2.2204460492503131e-16 [private]

Epsilon to test equality with 0.

Definition at line 40 of file aotensor def.f90.

The documentation for this module was generated from the following file:

· aotensor def.f90

# 5.2 inprod\_analytic::atm\_tensors Type Reference

Type holding the atmospheric inner products tensors.

### **Private Attributes**

```
    real(kind=8), dimension(:,:),
allocatable a
```

- real(kind=8), dimension(:,:), allocatable c
- real(kind=8), dimension(:,:), allocatable d
- real(kind=8), dimension(:,:), allocatable s
- real(kind=8), dimension(:,:,:), allocatable b
- real(kind=8), dimension(:,:,:), allocatable g

# 5.2.1 Detailed Description

Type holding the atmospheric inner products tensors.

Definition at line 52 of file inprod\_analytic.f90.

# 5.2.2 Member Data Documentation

**5.2.2.1** real(kind=8), dimension(:,:), allocatable inprod\_analytic::atm\_tensors::a [private]

Definition at line 53 of file inprod\_analytic.f90.

**5.2.2.2** real(kind=8), dimension(:,:,:), allocatable inprod\_analytic::atm\_tensors::b [private]

Definition at line 54 of file inprod\_analytic.f90.

**5.2.2.3** real(kind=8), dimension(:,:), allocatable inprod\_analytic::atm\_tensors::c [private]

Definition at line 53 of file inprod\_analytic.f90.

```
5.2.2.4 real(kind=8), dimension(:,:), allocatable inprod_analytic::atm_tensors::d [private]
```

Definition at line 53 of file inprod\_analytic.f90.

```
5.2.2.5 real(kind=8), dimension(:,,,:), allocatable inprod_analytic::atm_tensors::g [private]
```

Definition at line 54 of file inprod\_analytic.f90.

```
5.2.2.6 real(kind=8), dimension(:,:), allocatable inprod_analytic::atm_tensors::s [private]
```

Definition at line 53 of file inprod\_analytic.f90.

The documentation for this type was generated from the following file:

· inprod analytic.f90

# 5.3 inprod\_analytic::atm\_wavenum Type Reference

Atmospheric bloc specification type.

### **Private Attributes**

- · character typ
- integer m =0
- integer p =0
- integer h =0
- real(kind=8) nx =0.
- real(kind=8) ny =0.

# 5.3.1 Detailed Description

Atmospheric bloc specification type.

Definition at line 39 of file inprod\_analytic.f90.

# 5.3.2 Member Data Documentation

```
5.3.2.1 integer inprod_analytic::atm_wavenum::h =0 [private]
```

Definition at line 41 of file inprod\_analytic.f90.

**5.3.2.2** integer inprod\_analytic::atm\_wavenum::m =0 [private]

Definition at line 41 of file inprod\_analytic.f90.

**5.3.2.3** real(kind=8) inprod\_analytic::atm\_wavenum::nx =0. [private]

Definition at line 42 of file inprod\_analytic.f90.

**5.3.2.4** real(kind=8) inprod\_analytic::atm\_wavenum::ny =0. [private]

Definition at line 42 of file inprod\_analytic.f90.

**5.3.2.5** integer inprod\_analytic::atm\_wavenum::p =0 [private]

Definition at line 41 of file inprod\_analytic.f90.

**5.3.2.6** character inprod\_analytic::atm\_wavenum::typ [private]

Definition at line 40 of file inprod\_analytic.f90.

The documentation for this type was generated from the following file:

• inprod\_analytic.f90

# 5.4 tensor::coolist Type Reference

Coordinate list. Type used to represent the sparse tensor.

# **Public Attributes**

 type(coolist\_elem), dimension(:), allocatable elems

Lists of elements tensor::coolist\_elem.

• integer nelems = 0

Number of elements in the list.

# 5.4.1 Detailed Description

Coordinate list. Type used to represent the sparse tensor.

Definition at line 27 of file tensor.f90.

# 5.4.2 Member Data Documentation

5.4.2.1 type(coolist\_elem), dimension(:), allocatable tensor::coolist::elems

Lists of elements tensor::coolist\_elem.

Definition at line 28 of file tensor.f90.

5.4.2.2 integer tensor::coolist::nelems = 0

Number of elements in the list.

Definition at line 29 of file tensor.f90.

The documentation for this type was generated from the following file:

• tensor.f90

# 5.5 tensor::coolist\_elem Type Reference

Coordinate list element type. Elementary elements of the sparse tensors.

# **Private Attributes**

integer j

Index j of the element.

integer k

Index k of the element.

• real(kind=8) v

Value of the element.

# 5.5.1 Detailed Description

Coordinate list element type. Elementary elements of the sparse tensors.

Definition at line 20 of file tensor.f90.

# 5.5.2 Member Data Documentation

**5.5.2.1** integer tensor::coolist\_elem::j [private]

Index j of the element.

Definition at line 21 of file tensor.f90.

**5.5.2.2** integer tensor::coolist\_elem::k [private]

Index k of the element.

Definition at line 22 of file tensor.f90.

**5.5.2.3** real(kind=8) tensor::coolist\_elem::v [private]

Value of the element.

Definition at line 23 of file tensor.f90.

The documentation for this type was generated from the following file:

• tensor.f90

# 5.6 ic\_def Module Reference

Module to load the initial condition.

# **Public Member Functions**

• subroutine, public load\_ic

Subroutine to load the initial condition if IC.nml exists. If it does not, then write IC.nml with 0 as initial condition.

# **Public Attributes**

 real(kind=8), dimension(:), allocatable, public ic Initial condition vector.

# **Private Attributes**

· logical exists

Boolean to test for file existence.

# 5.6.1 Detailed Description

Module to load the initial condition.

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Definition at line 12 of file ic def.f90.

# 5.6.2 Member Function/Subroutine Documentation

5.6.2.1 subroutine, public ic\_def::load\_ic ( )

Subroutine to load the initial condition if IC.nml exists. If it does not, then write IC.nml with 0 as initial condition. Definition at line 31 of file ic\_def.f90.

### 5.6.3 Member Data Documentation

**5.6.3.1 logicalic\_def::exists** [private]

Boolean to test for file existence.

Definition at line 21 of file ic\_def.f90.

5.6.3.2 real(kind=8), dimension(:), allocatable, public ic\_def::ic

Initial condition vector.

Definition at line 23 of file ic def.f90.

The documentation for this module was generated from the following file:

• ic def.f90

# 5.7 inprod\_analytic Module Reference

Inner products between the truncated set of basis functions for the ocean and atmosphere streamfunction fields. These are partly calculated using the analytical expressions from Cehelsky, P., & Tung, K. K.: Theories of multiple equilibria and weather regimes-A critical reexamination. Part II: Baroclinic two-layer models. Journal of the atmospheric sciences, 44(21), 3282-3303, 1987.

# **Data Types**

· type atm\_tensors

Type holding the atmospheric inner products tensors.

· type atm wavenum

Atmospheric bloc specification type.

• type ocean\_tensors

Type holding the oceanic inner products tensors.

· type ocean wavenum

Oceanic bloc specification type.

# **Public Member Functions**

• subroutine, public init\_inprod

Initialisation of the inner product.

• subroutine, public deallocate\_inprod

Deallocation of the inner products.

### **Public Attributes**

 type(atm\_wavenum), dimension(:), allocatable, public awavenum

Atmospheric blocs specification.

• type(ocean\_wavenum), dimension(:), allocatable, public owavenum

Oceanic blocs specification.

• type(atm\_tensors), public atmos

Atmospheric tensors.

• type(ocean\_tensors), public ocean

Oceanic tensors.

# **Private Member Functions**

• REAL(KIND=8) function b1 (Pi, Pj, Pk)

Cehelsky & Tung Helper functions.

• REAL(KIND=8) function b2 (Pi, Pj, Pk)

Cehelsky & Tung Helper functions.

• REAL(KIND=8) function delta (r)

Integer Dirac delta function.

• REAL(KIND=8) function flambda (r)

"Odd or even" function

• REAL(KIND=8) function s1 (Pj, Pk, Mj, Hk)

Cehelsky & Tung Helper functions.

• REAL(KIND=8) function s2 (Pj, Pk, Mj, Hk)

Cehelsky & Tung Helper functions.

• REAL(KIND=8) function s3 (Pj, Pk, Hj, Hk)

Cehelsky & Tung Helper functions.

REAL(KIND=8) function s4 (Pj, Pk, Hj, Hk)

Cehelsky & Tung Helper functions.

• subroutine calculate\_a

Eigenvalues of the Laplacian (atmospheric)

· subroutine calculate b

Streamfunction advection terms (atmospheric)

• subroutine calculate c atm

Beta term for the atmosphere.

· subroutine calculate d

Forcing of the ocean on the atmosphere.

subroutine calculate g

Temperature advection terms (atmospheric)

• subroutine calculate s

Forcing (thermal) of the ocean on the atmosphere.

subroutine calculate k

Forcing of the atmosphere on the ocean.

subroutine calculate\_m

Forcing of the ocean fields on the ocean.

• subroutine calculate n

Beta term for the ocean.

· subroutine calculate o

Temperature advection term (passive scalar)

subroutine calculate\_c\_oc

Streamfunction advection terms (oceanic)

· subroutine calculate\_w

Short-wave radiative forcing of the ocean.

# 5.7.1 Detailed Description

Inner products between the truncated set of basis functions for the ocean and atmosphere streamfunction fields. These are partly calculated using the analytical expressions from Cehelsky, P., & Tung, K. K.: Theories of multiple equilibria and weather regimes-A critical reexamination. Part II: Baroclinic two-layer models. Journal of the atmospheric sciences, 44(21), 3282-3303, 1987.

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# Remarks

Generated Fortran90/95 code from ../../lua/aomodel\_extended/inprod\_analytic.lua

Definition at line 23 of file inprod\_analytic.f90.

# 5.7.2 Member Function/Subroutine Documentation

5.7.2.1 REAL(KIND=8) function inprod\_analytic::b1 ( integer Pi, integer Pj, integer Pk ) [private]

Cehelsky & Tung Helper functions.

Definition at line 90 of file inprod analytic.f90.

5.7.2.2 REAL(KIND=8) function inprod\_analytic::b2 ( integer Pi, integer Pk ) [private]

Cehelsky & Tung Helper functions.

Definition at line 96 of file inprod\_analytic.f90.

**5.7.2.3 subroutine inprod\_analytic::calculate\_a()** [private]

Eigenvalues of the Laplacian (atmospheric)

$$a_{i,j} = (F_i, \nabla^2 F_j)$$
.

Definition at line 154 of file inprod analytic.f90.

**5.7.2.4 subroutine inprod\_analytic::calculate\_b ( )** [private]

Streamfunction advection terms (atmospheric)

$$b_{i,j,k} = (F_i, J(F_j, \nabla^2 F_k))$$
.

### Remarks

Atmospheric g and a tensors must be computed before calling this routine

Definition at line 181 of file inprod\_analytic.f90.

**5.7.2.5 subroutine inprod\_analytic::calculate\_c\_atm()** [private]

Beta term for the atmosphere.

$$c_{i,j} = (F_i, \partial_x F_j)$$
.

### Remarks

Strict function !! Only accepts KL type. For any other combination, it will not calculate anything

Definition at line 215 of file inprod\_analytic.f90.

**5.7.2.6 subroutine inprod\_analytic::calculate\_c\_oc()** [private]

Streamfunction advection terms (oceanic)

$$C_{i,j,k} = (\eta_i, J(\eta_j, \nabla^2 \eta_k))$$
.

# Remarks

Requires O\_{i,j,k} and M\_{i,j} to be calculated beforehand.

Definition at line 567 of file inprod\_analytic.f90.

**5.7.2.7 subroutine inprod\_analytic::calculate\_d()** [private]

Forcing of the ocean on the atmosphere.

$$d_{i,j} = (F_i, \nabla^2 \eta_j)$$
.

# Remarks

Atmospheric s tensor and oceanic M tensor must be computed before calling this routine!

Definition at line 254 of file inprod\_analytic.f90.

**5.7.2.8 subroutine inprod\_analytic::calculate\_g( )** [private]

Temperature advection terms (atmospheric)

$$g_{i,j,k} = (F_i, J(F_j, F_k))$$
.

Definition at line 287 of file inprod analytic.f90.

5.7.2.9 subroutine inprod\_analytic::calculate\_k( ) [private]

Forcing of the atmosphere on the ocean.

$$K_{i,j} = (\eta_i, \nabla^2 F_j)$$
.

Remarks

atmospheric a and s tensors must be computed before calling this function!

Definition at line 433 of file inprod\_analytic.f90.

**5.7.2.10 subroutine inprod\_analytic::calculate\_m( )** [private]

Forcing of the ocean fields on the ocean.

$$M_{i,j} = (eta_i, \nabla^2 \eta_j)$$
.

Definition at line 463 of file inprod analytic.f90.

**5.7.2.11 subroutine inprod\_analytic::calculate\_n()** [private]

Beta term for the ocean.

$$N_{i,j} = (\eta_i, \partial_x \eta_j).$$

Definition at line 486 of file inprod\_analytic.f90.

 $\textbf{5.7.2.12} \quad \textbf{subroutine inprod\_analytic::calculate\_o ( )} \quad [\texttt{private}]$ 

Temperature advection term (passive scalar)

$$O_{i,j,k} = (\eta_i, J(\eta_j, \eta_k))$$
.

Definition at line 515 of file inprod\_analytic.f90.

 $\textbf{5.7.2.13} \quad \textbf{subroutine inprod\_analytic::calculate\_s ( )} \quad \texttt{[private]}$ 

Forcing (thermal) of the ocean on the atmosphere.

$$s_{i,j}=(F_i,\eta_j)$$
.

Definition at line 379 of file inprod\_analytic.f90.

**5.7.2.14 subroutine inprod\_analytic::calculate\_w()** [private]

Short-wave radiative forcing of the ocean.

$$W_{i,j}=(\eta_i,F_j)$$
.

```
Remarks
```

atmospheric s tensor must be computed before calling this function!

Definition at line 604 of file inprod\_analytic.f90.

5.7.2.15 subroutine, public inprod\_analytic::deallocate\_inprod ( )

Deallocation of the inner products.

Definition at line 721 of file inprod analytic.f90.

**5.7.2.16 REAL(KIND=8)** function inprod\_analytic::delta ( integer *r* ) [private]

Integer Dirac delta function.

Definition at line 102 of file inprod\_analytic.f90.

**5.7.2.17 REAL(KIND=8)** function inprod\_analytic::flambda ( integer *r* ) [private]

"Odd or even" function

Definition at line 112 of file inprod analytic.f90.

5.7.2.18 subroutine, public inprod\_analytic::init\_inprod ( )

Initialisation of the inner product.

Definition at line 638 of file inprod\_analytic.f90.

5.7.2.19 REAL(KIND=8) function inprod\_analytic::s1 ( integer Pj, integer Pk, integer Mj, integer Hk ) [private]

Cehelsky & Tung Helper functions.

Definition at line 122 of file inprod\_analytic.f90.

5.7.2.20 REAL(KIND=8) function inprod\_analytic::s2 ( integer Pj, integer Pk, integer Mj, integer Hk ) [private]

Cehelsky & Tung Helper functions.

Definition at line 128 of file inprod\_analytic.f90.

5.7.2.21 REAL(KIND=8) function inprod\_analytic::s3 ( integer Pj, integer Pk, integer Hj, integer Hk ) [private]

Cehelsky & Tung Helper functions.

Definition at line 134 of file inprod analytic.f90.

5.7.2.22 REAL(KIND=8) function inprod\_analytic::s4 ( integer *Pj*, integer *Pk*, integer *Hj*, integer *Hk* ) [private]

Cehelsky & Tung Helper functions.

Definition at line 140 of file inprod\_analytic.f90.

# 5.7.3 Member Data Documentation

5.7.3.1 type(atm\_tensors), public inprod\_analytic::atmos

Atmospheric tensors.

Definition at line 69 of file inprod\_analytic.f90.

5.7.3.2 type(atm\_wavenum), dimension(:), allocatable, public inprod\_analytic::awavenum

Atmospheric blocs specification.

Definition at line 64 of file inprod\_analytic.f90.

5.7.3.3 type(ocean\_tensors), public inprod\_analytic::ocean

Oceanic tensors.

Definition at line 71 of file inprod\_analytic.f90.

5.7.3.4 type(ocean\_wavenum), dimension(:), allocatable, public inprod\_analytic::owavenum

Oceanic blocs specification.

Definition at line 66 of file inprod\_analytic.f90.

The documentation for this module was generated from the following file:

· inprod\_analytic.f90

# 5.8 integrator Module Reference

Module with the integration routines.

# **Public Member Functions**

• subroutine, public init\_integrator

Routine to initialise the integration buffers.

• subroutine, public step (y, t, dt, res)

Routine to perform an integration step (Heun algorithm). The incremented time is returned.

# **Private Member Functions**

• subroutine tendencies (t, y, res)

Routine computing the tendencies of the model.

# **Private Attributes**

 real(kind=8), dimension(:), allocatable buf\_y1

Buffer to hold the intermediate position (Heun algorithm)

 real(kind=8), dimension(:), allocatable buf\_f0 Buffer to hold tendencies at the initial position.

 real(kind=8), dimension(:), allocatable buf\_f1

Buffer to hold tendencies at the intermediate position.

# 5.8.1 Detailed Description

Module with the integration routines.

# Copyright

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# Remarks

This module actually contains the Heun algorithm routines. The user can modify it according to its preferred integration scheme. For higher-order schemes, additional buffers will probably have to be defined.

Definition at line 19 of file integrator.f90.

# 5.8.2 Member Function/Subroutine Documentation

5.8.2.1 subroutine, public integrator::init\_integrator ( )

Routine to initialise the integration buffers.

Definition at line 36 of file integrator.f90.

5.8.2.2 subroutine, public integrator::step ( real(kind=8), dimension(0:ndim), intent(in) y, real(kind=8), intent(inout) t, real(kind=8), intent(in) dt, real(kind=8), dimension(0:ndim), intent(out) res )

Routine to perform an integration step (Heun algorithm). The incremented time is returned.

### **Parameters**

| У   | Initial point.              |
|-----|-----------------------------|
| t   | Actual integration time     |
| dt  | Integration timestep.       |
| res | Final point after the step. |

Definition at line 60 of file integrator.f90.

5.8.2.3 subroutine integrator::tendencies ( real(kind=8), intent(in) t, real(kind=8), dimension(0:ndim), intent(in) y, real(kind=8), dimension(0:ndim), intent(out) res ) [private]

Routine computing the tendencies of the model.

# **Parameters**

| t   | Time at which the tendencies have to be computed. Actually not needed for autonomous |
|-----|--|
|     | systems.   |
| У   | Point at which the tendencies have to be computed.                                   |
| res | vector to store the result.  |

#### Remarks

Note that it is NOT safe to pass y as a result buffer, as this operation does multiple passes.

Definition at line 48 of file integrator.f90.

# 5.8.3 Member Data Documentation

**5.8.3.1** real(kind=8), dimension(:), allocatable integrator::buf\_f0 [private]

Buffer to hold tendencies at the initial position.

Definition at line 28 of file integrator.f90.

5.8.3.2 real(kind=8), dimension(:), allocatable integrator::buf\_f1 [private]

Buffer to hold tendencies at the intermediate position.

Definition at line 29 of file integrator.f90.

5.8.3.3 real(kind=8), dimension(:), allocatable integrator::buf\_y1 [private]

Buffer to hold the intermediate position (Heun algorithm)

Definition at line 27 of file integrator.f90.

The documentation for this module was generated from the following file:

• integrator.f90

# 5.9 maooam\_tl\_ad Module Reference

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Tensors definition module.

# **Public Member Functions**

- subroutine, public init\_tltensor
  - Routine to initialize the TL tensor.
- subroutine, public init\_adtensor

Routine to initialize the AD tensor.

· subroutine, public init\_adtensor\_ref

Alternate method to initialize the AD tensor from the TL tensor.

• subroutine, public ad (t, ystar, deltay, buf)

Tendencies for the AD of MAOOAM in point ystar for perturbation deltay.

• subroutine, public tl (t, ystar, deltay, buf)

Tendencies for the TL of MAOOAM in point ystar for perturbation deltay.

# **Public Attributes**

 type(coolist), dimension(:), allocatable, public tltensor

Tensor representation of the Tangent Linear tendencies.

 type(coolist), dimension(:), allocatable, public adtensor

Tensor representation of the Adjoint tendencies.

#### **Private Member Functions**

 type(coolist) function, dimension(ndim) jacobian (ystar)

Compute the Jacobian of MAOOAM in point ystar.

 real(kind=8) function, dimension(ndim, ndim) jacobian\_mat (ystar)

Compute the Jacobian of MAOOAM in point ystar.

• subroutine compute\_tltensor (func)

Routine to compute the TL tensor from the original MAOOAM one.

• subroutine tl\_add\_count (i, j, k, v)

Subroutine used to count the number of TL tensor entries.

• subroutine tl\_coeff (i, j, k, v)

Subroutine used to compute the TL tensor entries.

• subroutine compute\_adtensor (func)

Subroutine to compute the AD tensor from the original MAOOAM one.

• subroutine ad\_add\_count (i, j, k, v)

Subroutine used to count the number of AD tensor entries.

- subroutine ad coeff (i, j, k, v)
- subroutine compute\_adtensor\_ref (func)

Alternate subroutine to compute the AD tensor from the TL one.

• subroutine ad\_add\_count\_ref (i, j, k, v)

Alternate subroutine used to count the number of AD tensor entries from the TL tensor.

• subroutine ad\_coeff\_ref (i, j, k, v)

Alternate subroutine used to compute the AD tensor entries from the TL tensor.

#### **Private Attributes**

• real(kind=8), parameter real\_eps = 2.2204460492503131e-16

Epsilon to test equality with 0.

integer, dimension(:), allocatable count\_elems

Vector used to count the tensor elements.

### 5.9.1 Detailed Description

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Tensors definition module.

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### Remarks

The routines of this module should be called only after params::init\_params() and aotensor\_def::init\_aotensor() have been called !

Definition at line 19 of file maooam\_tl\_ad.f90.

#### 5.9.2 Member Function/Subroutine Documentation

5.9.2.1 subroutine, public maooam\_tl\_ad::ad ( real(kind=8), intent(in) *t*, real(kind=8), dimension(0:ndim), intent(in) *ystar*, real(kind=8), dimension(0:ndim), intent(in) *deltay*, real(kind=8), dimension(0:ndim), intent(out) *buf* )

Tendencies for the AD of MAOOAM in point ystar for perturbation deltay.

#### **Parameters**

| t      | time  |
|--------|---|
| ystar  | vector with the variables (current point in trajectory) |
| deltay | vector with the perturbation of the variables at time t |
| buf    | vector (buffer) to store derivatives.                   |

Definition at line 390 of file maooam\_tl\_ad.f90.

5.9.2.2 subroutine maooam\_tl\_ad::ad\_add\_count ( integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v ) [private]

Subroutine used to count the number of AD tensor entries.

#### **Parameters**

| i | tensor i index           |
|---|--------------------------|
| j | tensor $j$ index         |
| k | tensor k index           |
| V | value that will be added |

Definition at line 249 of file maooam tl ad.f90.

5.9.2.3 subroutine maooam\_tl\_ad::ad\_add\_count\_ref ( integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v ) [private]

Alternate subroutine used to count the number of AD tensor entries from the TL tensor.

#### **Parameters**

| i | tensor i index           |
|---|--------------------------|
| j | tensor $j$ index         |
| k | tensor k index           |
| V | value that will be added |

Definition at line 352 of file maooam\_tl\_ad.f90.

5.9.2.4 subroutine maooam\_tl\_ad::ad\_coeff ( integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v ) [private]

#### **Parameters**

| i | tensor i index   |
|---|------------------|
| j | tensor $j$ index |
| k | tensor k index   |
| V | value to add     |

Definition at line 263 of file maooam\_tl\_ad.f90.

5.9.2.5 subroutine maooam\_tl\_ad::ad\_coeff\_ref ( integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v ) [private]

Alternate subroutine used to compute the AD tensor entries from the TL tensor.

#### **Parameters**

| i | tensor i index   |
|---|------------------|
| j | tensor $j$ index |
| k | tensor k index   |
| V | value to add     |

Definition at line 364 of file maooam\_tl\_ad.f90.

5.9.2.6 subroutine maooam\_tl\_ad::compute\_adtensor ( external func ) [private]

Subroutine to compute the AD tensor from the original MAOOAM one.

#### **Parameters**

| func | subroutine used to do the computation |
|------|---------------------------------------|

Definition at line 223 of file maooam\_tl\_ad.f90.

5.9.2.7 subroutine maooam\_tl\_ad::compute\_adtensor\_ref( external func ) [private]

Alternate subroutine to compute the AD tensor from the TL one.

#### **Parameters**

| func | subroutine used to do the computation |
|------|---------------------------------------|

Definition at line 324 of file maooam tl ad.f90.

5.9.2.8 subroutine maooam\_tl\_ad::compute\_tltensor( external func ) [private]

Routine to compute the TL tensor from the original MAOOAM one.

#### **Parameters**

| _ |      |                                       |
|---|------|---------------------------------------|
|   | func | subroutine used to do the computation |

Definition at line 127 of file maooam\_tl\_ad.f90.

5.9.2.9 subroutine, public maooam\_tl\_ad::init\_adtensor()

Routine to initialize the AD tensor.

Definition at line 199 of file maooam tl ad.f90.

5.9.2.10 subroutine, public maooam\_tl\_ad::init\_adtensor\_ref ( )

Alternate method to initialize the AD tensor from the TL tensor.

#### Remarks

The tltensor must be initialised before using this method.

Definition at line 300 of file maooam\_tl\_ad.f90.

5.9.2.11 subroutine, public maooam\_tl\_ad::init\_tltensor()

Routine to initialize the TL tensor.

Definition at line 103 of file maooam\_tl\_ad.f90.

5.9.2.12 type(coolist) function, dimension(ndim) maooam\_tl\_ad::jacobian ( real(kind=8), dimension(0:ndim), intent(in) ystar ) [private]

Compute the Jacobian of MAOOAM in point ystar.

#### **Parameters**

| ystar | array with variables in which the jacobian should be evaluated. |
|-------|---|

#### Returns

Jacobian in coolist-form (table of tuples {i,j,0,value})

Definition at line 81 of file maooam\_tl\_ad.f90.

Compute the Jacobian of MAOOAM in point ystar.

#### **Parameters**

| ystar | array with variables in which the jacobian should be evaluated. |
|-------|---|

#### Returns

Jacobian in matrix form

Definition at line 90 of file maooam\_tl\_ad.f90.

5.9.2.14 subroutine, public maooam\_tl\_ad::tl ( real(kind=8), intent(in) t, real(kind=8), dimension(0:ndim), intent(in) ystar, real(kind=8), dimension(0:ndim), intent(in) deltay, real(kind=8), dimension(0:ndim), intent(out) buf )

Tendencies for the TL of MAOOAM in point ystar for perturbation deltay.

#### **Parameters**

| t      | time  |
|--------|---|
| ystar  | vector with the variables (current point in trajectory) |
| deltay | vector with the perturbation of the variables at time t |
| buf    | vector (buffer) to store derivatives.                   |

Definition at line 402 of file maooam tl ad.f90.

5.9.2.15 subroutine maooam\_tl\_ad::tl\_add\_count ( integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v ) [private]

Subroutine used to count the number of TL tensor entries.

#### **Parameters**

| i | tensor i index           |
|---|--------------------------|
| j | tensor $j$ index         |
| k | tensor k index           |
| V | value that will be added |

Definition at line 153 of file maooam\_tl\_ad.f90.

5.9.2.16 subroutine maooam\_tl\_ad::tl\_coeff ( integer, intent(in) i, integer, intent(in) j, integer, intent(in) k, real(kind=8), intent(in) v ) [private]

Subroutine used to compute the TL tensor entries.

#### **Parameters**

| i | tensor i index   |
|---|------------------|
| j | tensor $j$ index |
| k | tensor k index   |
| V | value to add     |

Definition at line 167 of file maooam\_tl\_ad.f90.

#### 5.9.3 Member Data Documentation

5.9.3.1 type(coolist), dimension(:), allocatable, public maooam\_tl\_ad::adtensor

Tensor representation of the Adjoint tendencies.

Definition at line 51 of file maooam\_tl\_ad.f90.

**5.9.3.2** integer, dimension(:), allocatable maooam\_tl\_ad::count\_elems [private]

Vector used to count the tensor elements.

Definition at line 45 of file maooam\_tl\_ad.f90.

 $\textbf{5.9.3.3} \quad \textbf{real(kind=8), parameter maooam\_tl\_ad::real\_eps = 2.2204460492503131e-16} \quad \texttt{[private]}$ 

Epsilon to test equality with 0.

Definition at line 42 of file maooam\_tl\_ad.f90.

5.9.3.4 type(coolist), dimension(:), allocatable, public maooam\_tl\_ad::tltensor

Tensor representation of the Tangent Linear tendencies.

Definition at line 48 of file maooam tl ad.f90.

The documentation for this module was generated from the following file:

• maooam\_tl\_ad.f90

### 5.10 inprod\_analytic::ocean\_tensors Type Reference

Type holding the oceanic inner products tensors.

#### **Private Attributes**

```
    real(kind=8), dimension(:,:),
allocatable k
```

- real(kind=8), dimension(:,:), allocatable m
- real(kind=8), dimension(:,:), allocatable n
- real(kind=8), dimension(:,:), allocatable w
- real(kind=8), dimension(:,:,:), allocatable o
- real(kind=8), dimension(:,:,:), allocatable c

### 5.10.1 Detailed Description

Type holding the oceanic inner products tensors.

Definition at line 58 of file inprod\_analytic.f90.

#### 5.10.2 Member Data Documentation

5.10.2.1 real(kind=8), dimension(:,:,:), allocatable inprod\_analytic::ocean\_tensors::c [private]

Definition at line 60 of file inprod\_analytic.f90.

5.10.2.2 real(kind=8), dimension(:,:), allocatable inprod\_analytic::ocean\_tensors::k [private]

Definition at line 59 of file inprod\_analytic.f90.

5.10.2.3 real(kind=8), dimension(:,:), allocatable inprod\_analytic::ocean\_tensors::m [private]

Definition at line 59 of file inprod\_analytic.f90.

**5.10.2.4** real(kind=8), dimension(:,:), allocatable inprod\_analytic::ocean\_tensors::n [private]

Definition at line 59 of file inprod\_analytic.f90.

5.10.2.5 real(kind=8), dimension(:,:,:), allocatable inprod\_analytic::ocean\_tensors::o [private]

Definition at line 60 of file inprod\_analytic.f90.

**5.10.2.6** real(kind=8), dimension(:,:), allocatable inprod\_analytic::ocean\_tensors::w [private]

Definition at line 59 of file inprod\_analytic.f90.

The documentation for this type was generated from the following file:

• inprod\_analytic.f90

### 5.11 inprod\_analytic::ocean\_wavenum Type Reference

Oceanic bloc specification type.

#### **Private Attributes**

- integer p
- integer h
- real(kind=8) nx
- real(kind=8) ny

#### 5.11.1 Detailed Description

Oceanic bloc specification type.

Definition at line 46 of file inprod\_analytic.f90.

#### 5.11.2 Member Data Documentation

**5.11.2.1** integer inprod\_analytic::ocean\_wavenum::h [private]

Definition at line 47 of file inprod\_analytic.f90.

**5.11.2.2** real(kind=8) inprod\_analytic::ocean\_wavenum::nx [private]

Definition at line 48 of file inprod\_analytic.f90.

**5.11.2.3** real(kind=8) inprod\_analytic::ocean\_wavenum::ny [private]

Definition at line 48 of file inprod\_analytic.f90.

**5.11.2.4** integer inprod\_analytic::ocean\_wavenum::p [private]

Definition at line 47 of file inprod\_analytic.f90.

The documentation for this type was generated from the following file:

· inprod\_analytic.f90

### 5.12 params Module Reference

The model parameters module.

#### **Public Member Functions**

• subroutine init\_params

Parameters initialisation routine.

#### **Public Attributes**

• real(kind=8) g

```
 real(kind=8) n

      n = 2L_y/L_x - Aspect ratio
• real(kind=8) phi0
      Latitude in radian.
• real(kind=8) rra
      Earth radius.
• real(kind=8) sig0
      \sigma_0 - Non-dimensional static stability of the atmosphere.
• real(kind=8) k
      Bottom atmospheric friction coefficient.

 real(kind=8) kp

      k' - Internal atmospheric friction coefficient.
• real(kind=8) r
      Frictional coefficient at the bottom of the ocean.

 real(kind=8) d

      Merchanical coupling parameter between the ocean and the atmosphere.
• real(kind=8) f0
      f_0 - Coriolis parameter
• real(kind=8) gp
      g' Reduced gravity
real(kind=8) h
      Depth of the active water layer of the ocean.

    real(kind=8) phi0 npi

      Latitude exprimed in fraction of pi.
• real(kind=8) lambda
      \lambda - Sensible + turbulent heat exchange between the ocean and the atmosphere.
• real(kind=8) co
      C_a - Constant short-wave radiation of the ocean.
• real(kind=8) go
      \gamma_o - Specific heat capacity of the ocean.
• real(kind=8) ca
      C_a - Constant short-wave radiation of the atmosphere.
• real(kind=8) to0
      T_o^0 - Stationary solution for the 0-th order ocean temperature.
• real(kind=8) ta0
      T_a^0 - Stationary solution for the 0-th order atmospheric temperature.
• real(kind=8) epsa
      arepsilon_a - Emissivity coefficient for the grey-body atmosphere.
• real(kind=8) ga
      \gamma_a - Specific heat capacity of the atmosphere.
• real(kind=8) rr
      R - Gas constant of dry air
• real(kind=8) scale
      L_{\scriptscriptstyle 
m V} = L\,\pi - The characteristic space scale.
• real(kind=8) pi

 real(kind=8) lr

      L<sub>R</sub> - Rossby deformation radius
```

```
γ

 real(kind=8) rp

      r^\prime - Frictional coefficient at the bottom of the ocean.

 real(kind=8) dp

      d^\prime - Non-dimensional mechanical coupling parameter between the ocean and the atmosphere.

 real(kind=8) kd

      k_d - Non-dimensional bottom atmospheric friction coefficient.

    real(kind=8) kdp

      k_d^\prime - Non-dimensional internal atmospheric friction coefficient.
• real(kind=8) cpo
      C_a' - Non-dimensional constant short-wave radiation of the ocean.

 real(kind=8) lpo

      \lambda'_o - Non-dimensional sensible + turbulent heat exchange from ocean to atmosphere.
• real(kind=8) cpa
      C_a' - Non-dimensional constant short-wave radiation of the atmosphere.

    real(kind=8) lpa

      \lambda_a' - Non-dimensional sensible + turbulent heat exchange from atmosphere to ocean.

    real(kind=8) sbpo

      \sigma'_{B,o} - Long wave radiation lost by ocean to atmosphere & space.

    real(kind=8) sbpa

      \sigma'_{B,a} - Long wave radiation from atmosphere absorbed by ocean.
• real(kind=8) Isbpo
      S'_{B,o} - Long wave radiation from ocean absorbed by atmosphere.
• real(kind=8) Isbpa
      S'_{B,a} - Long wave radiation lost by atmosphere to space & ocean.
real(kind=8)
      L - Domain length scale
• real(kind=8) sc
      Ratio of surface to atmosphere temperature.
• real(kind=8) sb
      Stefan-Boltzmann constant.

    real(kind=8) betp

• real(kind=8) t_trans
      Transient time period.
real(kind=8) t_run
      Effective intergration time (length of the generated trajectory)
• real(kind=8) dt
      Integration time step.
• real(kind=8) tw
      Write all variables every tw time units.
· logical writeout
      Write to file boolean.

    integer nboc

      Number of atmospheric blocks.

    integer nbatm

      Number of oceanic blocks.
• integer natm =0
      Number of atmospheric basis functions.
• integer noc =0
```

integer ndim

Number of oceanic basis functions.

Number of variables (dimension of the model)

 integer, dimension(:,:), allocatable oms

Ocean mode selection array.

 integer, dimension(:,:), allocatable ams

Atmospheric mode selection array.

#### **Private Member Functions**

• subroutine, private init nml

Read the basic parameters and mode selection from the namelist.

#### 5.12.1 Detailed Description

The model parameters module.

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#### Remarks

Once the init\_params() subroutine is called, the parameters are loaded globally in the main program and its subroutines and function

Definition at line 18 of file params.f90.

### 5.12.2 Member Function/Subroutine Documentation

```
5.12.2.1 subroutine, private params::init_nml( ) [private]
```

Read the basic parameters and mode selection from the namelist.

Definition at line 90 of file params.f90.

5.12.2.2 subroutine params::init\_params ( )

Parameters initialisation routine.

Definition at line 134 of file params.f90.

#### 5.12.3 Member Data Documentation

5.12.3.1 integer, dimension(:,:), allocatable params::ams

Atmospheric mode selection array.

Definition at line 81 of file params.f90.

5.12.3.2 real(kind=8) params::betp

Definition at line 67 of file params.f90.

5.12.3.3 real(kind=8) params::ca

 $C_a$  - Constant short-wave radiation of the atmosphere.

Definition at line 40 of file params.f90.

5.12.3.4 real(kind=8) params::co

 $C_a$  - Constant short-wave radiation of the ocean.

Definition at line 38 of file params.f90.

5.12.3.5 real(kind=8) params::cpa

 $C_a'$  - Non-dimensional constant short-wave radiation of the atmosphere.

Remarks

Cpa acts on psi1-psi3, not on theta.

Definition at line 58 of file params.f90.

5.12.3.6 real(kind=8) params::cpo

 $C_a'$  - Non-dimensional constant short-wave radiation of the ocean.

Definition at line 56 of file params.f90.

5.12.3.7 real(kind=8) params::d

Merchanical coupling parameter between the ocean and the atmosphere.

Definition at line 31 of file params.f90.

5.12.3.8 real(kind=8) params::dp

d' - Non-dimensional mechanical coupling parameter between the ocean and the atmosphere.

Definition at line 52 of file params.f90.

5.12.3.9 real(kind=8) params::dt

Integration time step.

Definition at line 71 of file params.f90.

5.12.3.10 real(kind=8) params::epsa

 $arepsilon_a$  - Emissivity coefficient for the grey-body atmosphere.

Definition at line 43 of file params.f90.

5.12.3.11 real(kind=8) params::f0

 $f_0$  - Coriolis parameter

Definition at line 32 of file params.f90.

5.12.3.12 real(kind=8) params::g

γ

Definition at line 50 of file params.f90.

5.12.3.13 real(kind=8) params::ga

 $\gamma_a$  - Specific heat capacity of the atmosphere.

Definition at line 44 of file params.f90.

5.12.3.14 real(kind=8) params::go

 $\gamma_o$  - Specific heat capacity of the ocean.

Definition at line 39 of file params.f90.

5.12.3.15 real(kind=8) params::gp

g'Reduced gravity

Definition at line 33 of file params.f90.

5.12.3.16 real(kind=8) params::h

Depth of the active water layer of the ocean.

Definition at line 34 of file params.f90.

5.12.3.17 real(kind=8) params::k

Bottom atmospheric friction coefficient.

Definition at line 28 of file params.f90.

5.12.3.18 real(kind=8) params::kd

 $\ensuremath{k_{\!d}}$  - Non-dimensional bottom atmospheric friction coefficient.

Definition at line 53 of file params.f90.

5.12.3.19 real(kind=8) params::kdp

 $k_d^\prime$  - Non-dimensional internal atmospheric friction coefficient.

Definition at line 54 of file params.f90.

5.12.3.20 real(kind=8) params::kp

k' - Internal atmospheric friction coefficient.

Definition at line 29 of file params.f90.

5.12.3.21 real(kind=8) params::I

L - Domain length scale

Definition at line 64 of file params.f90.

5.12.3.22 real(kind=8) params::lambda

 $\lambda$  - Sensible + turbulent heat exchange between the ocean and the atmosphere.

Definition at line 37 of file params.f90.

5.12.3.23 real(kind=8) params::lpa

 $\lambda_a^\prime$  - Non-dimensional sensible + turbulent heat exchange from atmosphere to ocean.

Definition at line 59 of file params.f90.

5.12.3.24 real(kind=8) params::lpo

 $\lambda_o'$  - Non-dimensional sensible + turbulent heat exchange from ocean to atmosphere.

Definition at line 57 of file params.f90.

5.12.3.25 real(kind=8) params::lr

 $L_R$  - Rossby deformation radius

Definition at line 49 of file params.f90.

5.12.3.26 real(kind=8) params::lsbpa

 $S'_{B,a}$  - Long wave radiation lost by atmosphere to space & ocean.

Definition at line 63 of file params.f90.

5.12.3.27 real(kind=8) params::lsbpo

 $S'_{B,o}$  - Long wave radiation from ocean absorbed by atmosphere.

Definition at line 62 of file params.f90.

5.12.3.28 real(kind=8) params::n

 $n = 2L_y/L_x$  - Aspect ratio

Definition at line 24 of file params.f90.

5.12.3.29 integer params::natm =0

Number of atmospheric basis functions.

Definition at line 77 of file params.f90.

5.12.3.30 integer params::nbatm

Number of oceanic blocks.

Definition at line 76 of file params.f90.

5.12.3.31 integer params::nboc

Number of atmospheric blocks.

Definition at line 75 of file params.f90.

5.12.3.32 integer params::ndim

Number of variables (dimension of the model)

Definition at line 79 of file params.f90.

5.12.3.33 integer params::noc =0

Number of oceanic basis functions.

Definition at line 78 of file params.f90.

5.12.3.34 integer, dimension(:,:), allocatable params::oms

Ocean mode selection array.

Definition at line 80 of file params.f90.

5.12.3.35 real(kind=8) params::phi0

Latitude in radian.

Definition at line 25 of file params.f90.

5.12.3.36 real(kind=8) params::phi0\_npi

Latitude exprimed in fraction of pi.

Definition at line 35 of file params.f90.

5.12.3.37 real(kind=8) params::pi

 $\pi$ 

Definition at line 48 of file params.f90.

5.12.3.38 real(kind=8) params::r

Frictional coefficient at the bottom of the ocean.

Definition at line 30 of file params.f90.

5.12.3.39 real(kind=8) params::rp

r' - Frictional coefficient at the bottom of the ocean.

Definition at line 51 of file params.f90.

5.12.3.40 real(kind=8) params::rr

R - Gas constant of dry air

Definition at line 45 of file params.f90.

5.12.3.41 real(kind=8) params::rra

Earth radius.

Definition at line 26 of file params.f90.

5.12.3.42 real(kind=8) params::sb

Stefan-Boltzmann constant.

Definition at line 66 of file params.f90.

5.12.3.43 real(kind=8) params::sbpa

 $\sigma_{B,a}^{\prime}$  - Long wave radiation from atmosphere absorbed by ocean.

Definition at line 61 of file params.f90.

5.12.3.44 real(kind=8) params::sbpo

 $\sigma'_{B,o}$  - Long wave radiation lost by ocean to atmosphere & space.

Definition at line 60 of file params.f90.

5.12.3.45 real(kind=8) params::sc

Ratio of surface to atmosphere temperature.

Definition at line 65 of file params.f90.

5.12.3.46 real(kind=8) params::scale

 $L_{\rm y} = L \, \pi$  - The characteristic space scale.

Definition at line 47 of file params.f90.

5.12.3.47 real(kind=8) params::sig0

 $\sigma_0$  - Non-dimensional static stability of the atmosphere.

Definition at line 27 of file params.f90.

5.12.3.48 real(kind=8) params::t\_run

Effective intergration time (length of the generated trajectory)

Definition at line 70 of file params.f90.

5.12.3.49 real(kind=8) params::t\_trans

Transient time period.

Definition at line 69 of file params.f90.

5.12.3.50 real(kind=8) params::ta0

 $T_a^0$  - Stationary solution for the 0-th order atmospheric temperature.

Definition at line 42 of file params.f90.

5.12.3.51 real(kind=8) params::to0

 $T_o^0$  - Stationary solution for the 0-th order ocean temperature.

Definition at line 41 of file params.f90.

5.12.3.52 real(kind=8) params::tw

Write all variables every tw time units.

Definition at line 72 of file params.f90.

5.12.3.53 logical params::writeout

Write to file boolean.

Definition at line 73 of file params.f90.

The documentation for this module was generated from the following file:

• params.f90

### 5.13 stat Module Reference

Statistics accumulators.

#### **Public Member Functions**

- subroutine, public init\_stat
   Initialise the accumulators.
- subroutine, public acc (x)

Accumulate one state.

 real(kind=8) function, dimension(0:ndim), public mean ()

Function returning the mean.

 real(kind=8) function, dimension(0:ndim), public var () 5.13 stat Module Reference 43

Function returning the variance.

• integer function, public iter ()

Function returning the number of data accumulated.

· subroutine, public reset

Routine resetting the accumulators.

#### **Private Attributes**

```
• integer i =0
```

Number of stats accumulated.

 real(kind=8), dimension(:), allocatable m

Vector storing the inline mean.

 real(kind=8), dimension(:), allocatable mprev

Previous mean vector.

 real(kind=8), dimension(:), allocatable v

Vector storing the inline variance.

 real(kind=8), dimension(:), allocatable mtmp

#### 5.13.1 Detailed Description

Statistics accumulators.

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Definition at line 14 of file stat.f90.

### 5.13.2 Member Function/Subroutine Documentation

5.13.2.1 subroutine, public stat::acc ( real(kind=8), dimension(0:ndim), intent(in) x )

Accumulate one state.

Definition at line 47 of file stat.f90.

5.13.2.2 subroutine, public stat::init\_stat ( )

Initialise the accumulators.

Definition at line 34 of file stat.f90.

5.13.2.3 integer function, public stat::iter ( )

Function returning the number of data accumulated.

Definition at line 71 of file stat.f90.

```
5.13.2.4 real(kind=8) function, dimension(0:ndim), public stat::mean ( )
Function returning the mean.
Definition at line 59 of file stat.f90.
5.13.2.5 subroutine, public stat::reset ( )
Routine resetting the accumulators.
Definition at line 77 of file stat.f90.
5.13.2.6 real(kind=8) function, dimension(0:ndim), public stat::var ( )
Function returning the variance.
Definition at line 65 of file stat.f90.
5.13.3 Member Data Documentation
5.13.3.1 integer stat::i = 0 [private]
Number of stats accumulated.
Definition at line 20 of file stat.f90.
5.13.3.2 real(kind=8), dimension(:), allocatable stat::m [private]
Vector storing the inline mean.
Definition at line 23 of file stat.f90.
5.13.3.3 real(kind=8), dimension(:), allocatable stat::mprev [private]
Previous mean vector.
Definition at line 24 of file stat.f90.
5.13.3.4 real(kind=8), dimension(:), allocatable stat::mtmp [private]
Definition at line 26 of file stat.f90.
5.13.3.5 real(kind=8), dimension(:), allocatable stat::v [private]
Vector storing the inline variance.
Definition at line 25 of file stat.f90.
The documentation for this module was generated from the following file:
```

tensor Module Reference

Tensor utility module.

• stat.f90

5.14

### **Data Types**

· type coolist

Coordinate list. Type used to represent the sparse tensor.

type coolist\_elem

Coordinate list element type. Elementary elements of the sparse tensors.

#### **Public Member Functions**

• subroutine, public copy\_tensor (src, dst)

Routine to copy a tensor.

• subroutine, public mat\_to\_coo (src, dst)

Routine to convert a matrix to a tensor.

• subroutine, public sparse\_mul3 (coolist\_ijk, arr\_j, arr\_k, res)

Sparse multiplication of a tensor with two vectors:  $\sum_{j,k=0}^{ndim} \mathscr{T}_{i,j,k} a_j b_k$ .

• subroutine, public jsparse\_mul (coolist\_ijk, arr\_j, jcoo\_ij)

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} \left( \mathscr{T}_{i,j,k} + \mathscr{T}_{i,k,j} \right) a_k.$$

It's implemented slightly differently: for every  $\mathcal{T}_{i,j,k}$ , we add to  $J_{i,j}$  as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a coolist (sparse tensor).

• subroutine, public jsparse\_mul\_mat (coolist\_ijk, arr\_j, jcoo\_ij)

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} \left( \mathscr{T}_{i,j,k} + \mathscr{T}_{i,k,j} \right) a_k.$$

It's implemented slightly differently: for every  $\mathcal{T}_{i,j,k}$ , we add to  $J_{i,j}$  as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a matrix.

• subroutine, public sparse\_mul2 (coolist\_ij, arr\_j, res)

Sparse multiplication of a 2d sparse tensor with a vectors:  $\sum_{i=0}^{ndim} \mathscr{T}_{i,j,k} a_j b_k$ .

• subroutine, public simplify (tensor)

Routine to simplify a coolist (sparse tensor). For each index i, it upper triangularize the matrix

$$\mathcal{T}_{i,j,k}$$
  $0 \le j,k \le ndim$ .

#### **Public Attributes**

• real(kind=8), parameter real\_eps = 2.2204460492503131e-16

Parameter to test the equality with zero.

### 5.14.1 Detailed Description

Tensor utility module.

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Definition at line 13 of file tensor.f90.

#### 5.14.2 Member Function/Subroutine Documentation

5.14.2.1 subroutine, public tensor::copy\_tensor ( type(coolist), dimension(ndim), intent(in) *src*, type(coolist), dimension(ndim), intent(out) *dst* )

Routine to copy a tensor.

#### **Parameters**

| src | Source tensor      |
|-----|--------------------|
| dst | Destination tensor |

#### Remarks

The destination tensor have to be an empty tensor, i.e. with unallocated list of elements and nelems set to 0.

Definition at line 43 of file tensor.f90.

5.14.2.2 subroutine, public tensor::jsparse\_mul ( type(coolist), dimension(ndim), intent(in) coolist\_ijk, real(kind=8), dimension(0:ndim), intent(in) arr\_j, type(coolist), dimension(ndim), intent(out) jcoo\_ij )

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} \left( \mathscr{T}_{i,j,k} + \mathscr{T}_{i,k,j} \right) a_k.$$

It's implemented slightly differently: for every  $\mathcal{T}_{i,j,k}$ , we add to  $J_{i,j}$  as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a coolist (sparse tensor).

#### **Parameters**

| _,      | a coordinate list (sparse tensor) of which index 2 or 3 will be contracted. |
|---------|---|
| arr_j   | the vector to be contracted with index 2 and then index 3 of ffi_coo_ijk    |
| jcoo_ij | a coolist (sparse tensor) to store the result of the contraction            |

Definition at line 122 of file tensor.f90.

5.14.2.3 subroutine, public tensor::jsparse\_mul\_mat ( type(coolist), dimension(ndim), intent(in) coolist\_ijk, real(kind=8), dimension(0:ndim), intent(in) arr\_j, real(kind=8), dimension(ndim,ndim), intent(out) jcoo\_ij )

Sparse multiplication of two tensors to determine the Jacobian:

$$J_{i,j} = \sum_{k=0}^{ndim} \left( \mathscr{T}_{i,j,k} + \mathscr{T}_{i,k,j} \right) \, a_k.$$

It's implemented slightly differently: for every  $\mathcal{T}_{i,j,k}$ , we add to  $J_{i,j}$  as follows:

$$J_{i,j} = J_{i,j} + \mathcal{T}_{i,j,k} a_k J_{i,k} = J_{i,k} + \mathcal{T}_{i,j,k} a_j$$

This version return a matrix.

#### **Parameters**

| coolist_ijk | a coordinate list (sparse tensor) of which index 2 or 3 will be contracted. |
|-------------|---|
| arr_j       | the vector to be contracted with index 2 and then index 3 of ffi_coo_ijk    |
| jcoo_ij     | a matrix to store the result of the contraction                             |

Definition at line 165 of file tensor.f90.

5.14.2.4 subroutine, public tensor::mat\_to\_coo ( real(kind=8), dimension(0:ndim,0:ndim), intent(in) *src*, type(coolist), dimension(ndim), intent(out) *dst* )

Routine to convert a matrix to a tensor.

#### **Parameters**

| src | Source matrix      |
|-----|--------------------|
| dst | Destination tensor |

#### Remarks

The destination tensor have to be an empty tensor, i.e. with unallocated list of elements and nelems set to 0.

Definition at line 65 of file tensor.f90.

5.14.2.5 subroutine, public tensor::simplify (type(coolist), dimension(ndim), intent(inout) tensor)

Routine to simplify a coolist (sparse tensor). For each index i, it upper triangularize the matrix

$$\mathscr{T}_{i,j,k}$$
  $0 \leq j,k \leq ndim$ .

#### **Parameters**

tensor a coordinate list (sparse tensor) which will be simplified.

Definition at line 207 of file tensor.f90.

5.14.2.6 subroutine, public tensor::sparse\_mul2 ( type(coolist), dimension(ndim), intent(in) coolist\_ij, real(kind=8), dimension(0:ndim), intent(in) arr\_j, real(kind=8), dimension(0:ndim), intent(out) res )

Sparse multiplication of a 2d sparse tensor with a vectors:  $\sum_{j=0}^{ndim} \mathscr{T}_{i,j,k} a_j b_k$ .

#### **Parameters**

| coolist_ij | a coordinate list (sparse tensor) of which index 2 will be contracted. |
|------------|--|
| arr_j      | the vector to be contracted with index 2 of coolist_ijk                |
| res        | vector (buffer) to store the result of the contraction                 |

#### Remarks

Note that it is NOT safe to pass arr\_j as a result buffer, as this operation does multiple passes.

Definition at line 190 of file tensor.f90.

5.14.2.7 subroutine, public tensor::sparse\_mul3 ( type(coolist), dimension(ndim), intent(in) coolist\_ijk, real(kind=8), dimension(0:ndim), intent(in) arr\_k, real(kind=8), dimension(0:ndim), intent(out) res )

Sparse multiplication of a tensor with two vectors:  $\sum_{j,k=0}^{ndim} \mathscr{T}_{i,j,k} a_j b_k.$ 

#### **Parameters**

| coolist_ijk | a coordinate list (sparse tensor) of which index 2 and 3 will be contracted. |
|-------------|--|
| arr_j       | the vector to be contracted with index 2 of coolist_ijk                      |
| arr_k       | the vector to be contracted with index 3 of coolist_ijk                      |
| res         | vector (buffer) to store the result of the contraction                       |

#### Remarks

Note that it is NOT safe to pass arr\_j/arr\_k as a result buffer, as this operation does multiple passes.

Definition at line 98 of file tensor.f90.

#### 5.14.3 Member Data Documentation

5.14.3.1 real(kind=8), parameter tensor::real\_eps = 2.2204460492503131e-16

Parameter to test the equality with zero.

Definition at line 33 of file tensor.f90.

The documentation for this module was generated from the following file:

• tensor.f90

### 5.15 tl\_ad\_integrator Module Reference

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Integrators module.

#### **Public Member Functions**

• subroutine, public init\_ad\_integrator

Routine to initialise the adjoint model integration buffers.

• subroutine, public ad\_step (y, ystar, t, dt, res)

Routine to perform an integration step (Heun algorithm) of the adjoint model. The incremented time is returned.

• subroutine, public init\_tl\_integrator

Routine to initialise the tangent linear model integration buffers.

• subroutine, public tl\_step (y, ystar, t, dt, res)

Routine to perform an integration step (Heun algorithm) of the tangent linear model. The incremented time is returned.

#### **Private Attributes**

```
    real(kind=8), dimension(:),
allocatable ad_buf_y1
```

Buffer to hold the intermediate position (Heun algorithm) of the adjoint model.

 real(kind=8), dimension(:), allocatable ad\_buf\_f0

Buffer to hold tendencies at the initial position of the adjoint model.

 real(kind=8), dimension(:), allocatable ad buf f1

Buffer to hold tendencies at the intermediate position of the adjoint model.

 real(kind=8), dimension(:), allocatable tl\_buf\_y1

Buffer to hold the intermediate position (Heun algorithm) of the tangent linear model.

 real(kind=8), dimension(:), allocatable tl buf f0

Buffer to hold tendencies at the initial position of the tangent linear model.

 real(kind=8), dimension(:), allocatable tl\_buf\_f1

Buffer to hold tendencies at the intermediate position of the tangent linear model.

#### 5.15.1 Detailed Description

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Integrators module.

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#### Remarks

This module actually contains the Heun algorithm routines. The user can modify it according to its preferred integration scheme. For higher-order schemes, additional buffers will probably have to be defined.

Definition at line 22 of file tl\_ad\_integrator.f90.

#### 5.15.2 Member Function/Subroutine Documentation

5.15.2.1 subroutine, public tl\_ad\_integrator::ad\_step ( real(kind=8), dimension(0:ndim), intent(in) y, real(kind=8), dimension(0:ndim), intent(in) ystar, real(kind=8), intent(inout) t, real(kind=8), intent(in) dt, real(kind=8), dimension(0:ndim), intent(out) res )

Routine to perform an integration step (Heun algorithm) of the adjoint model. The incremented time is returned.

### **Parameters**

| У     | Initial point.                    |
|-------|-----------------------------------|
| ystar | Adjoint model at the point ystar. |
| t     | Actual integration time           |
| dt    | Integration timestep.             |
| res   | Final point after the step.       |

Definition at line 62 of file tl ad integrator.f90.

5.15.2.2 subroutine, public tl\_ad\_integrator::init\_ad\_integrator()

Routine to initialise the adjoint model integration buffers.

Definition at line 50 of file tl\_ad\_integrator.f90.

5.15.2.3 subroutine, public tl\_ad\_integrator::init\_tl\_integrator ( )

Routine to initialise the tangent linear model integration buffers.

Definition at line 82 of file tl\_ad\_integrator.f90.

5.15.2.4 subroutine, public tl\_ad\_integrator::tl\_step ( real(kind=8), dimension(0:ndim), intent(in) y, real(kind=8), dimension(0:ndim), intent(in) ystar, real(kind=8), intent(inout) t, real(kind=8), intent(in) dt, real(kind=8), dimension(0:ndim), intent(out) res )

Routine to perform an integration step (Heun algorithm) of the tangent linear model. The incremented time is returned.

#### **Parameters**

| У     | Initial point.                    |
|-------|-----------------------------------|
| ystar | Adjoint model at the point ystar. |
| t     | Actual integration time           |
| dt    | Integration timestep.             |
| res   | Final point after the step.       |

Definition at line 94 of file tl\_ad\_integrator.f90.

#### 5.15.3 Member Data Documentation

5.15.3.1 real(kind=8), dimension(:), allocatable tl\_ad\_integrator::ad\_buf\_f0 [private]

Buffer to hold tendencies at the initial position of the adjoint model.

Definition at line 31 of file tl ad integrator.f90.

**5.15.3.2** real(kind=8), dimension(:), allocatable tl\_ad\_integrator::ad\_buf\_f1 [private]

Buffer to hold tendencies at the intermediate position of the adjoint model.

Definition at line 32 of file tl ad integrator.f90.

5.15.3.3 real(kind=8), dimension(:), allocatable tl\_ad\_integrator::ad\_buf\_y1 [private]

Buffer to hold the intermediate position (Heun algorithm) of the adjoint model.

Definition at line 30 of file tl\_ad\_integrator.f90.

5.15.3.4 real(kind=8), dimension(:), allocatable tl\_ad\_integrator::tl\_buf\_f0 [private]

Buffer to hold tendencies at the initial position of the tangent linear model.

Definition at line 35 of file tl\_ad\_integrator.f90.

5.16 util Module Reference 51

5.15.3.5 real(kind=8), dimension(:), allocatable tl\_ad\_integrator::tl\_buf\_f1 [private]

Buffer to hold tendencies at the intermediate position of the tangent linear model.

Definition at line 36 of file tl\_ad\_integrator.f90.

**5.15.3.6** real(kind=8), dimension(:), allocatable tl\_ad\_integrator::tl\_buf\_y1 [private]

Buffer to hold the intermediate position (Heun algorithm) of the tangent linear model.

Definition at line 34 of file tl\_ad\_integrator.f90.

The documentation for this module was generated from the following file:

• tl ad integrator.f90

### 5.16 util Module Reference

Utility module.

#### **Public Member Functions**

- CHARACTER(len=20) function, public str (k)
   Convert an integer to string.
- CHARACTER(len=40) function, public rstr (x, fm)

  Convert a real to string with a given format.

#### 5.16.1 Detailed Description

Utility module.

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Definition at line 13 of file util.f90.

### 5.16.2 Member Function/Subroutine Documentation

5.16.2.1 CHARACTER(len=40) function, public util::rstr ( real(kind=8), intent(in) x, character(len=20), intent(in) fm )

Convert a real to string with a given format.

Definition at line 35 of file util.f90.

5.16.2.2 CHARACTER(len=20) function, public util::str ( integer, intent(in) k )

Convert an integer to string.

Definition at line 28 of file util.f90.

The documentation for this module was generated from the following file:

• util.f90

| Data Type Documentatio | or |
|------------------------|----|
|------------------------|----|

## **Chapter 6**

## **File Documentation**

### 6.1 aotensor\_def.f90 File Reference

### **Data Types**

· module aotensor\_def

The equation tensor for the coupled ocean-atmosphere model with temperature which allows for an extensible set of modes in the ocean and in the atmosphere.

- 6.2 doc/gen\_doc.md File Reference
- 6.3 doc/tl\_ad\_doc.md File Reference
- 6.4 ic\_def.f90 File Reference

#### **Data Types**

• module ic\_def

Module to load the initial condition.

### 6.5 inprod\_analytic.f90 File Reference

#### **Data Types**

• module inprod\_analytic

Inner products between the truncated set of basis functions for the ocean and atmosphere streamfunction fields. These are partly calculated using the analytical expressions from Cehelsky, P., & Tung, K. K.: Theories of multiple equilibria and weather regimes-A critical reexamination. Part II: Baroclinic two-layer models. Journal of the atmospheric sciences, 44(21), 3282-3303, 1987.

• type inprod\_analytic::atm\_wavenum

Atmospheric bloc specification type.

type inprod\_analytic::ocean\_wavenum

Oceanic bloc specification type.

· type inprod\_analytic::atm\_tensors

Type holding the atmospheric inner products tensors.

type inprod\_analytic::ocean\_tensors

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Type holding the oceanic inner products tensors.

### 6.6 integrator.f90 File Reference

#### **Data Types**

· module integrator

Module with the integration routines.

#### 6.7 LICENSE.txt File Reference

#### **Functions**

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### 6.8 maooam.f90 File Reference

#### **Functions/Subroutines**

program maooam

Fortran 90 implementation of the modular arbitrary-order ocean-atmosphere! model MAOOAM.!

#### 6.8.1 Function/Subroutine Documentation

6.8.1.1 program maooam ( )

Fortran 90 implementation of the modular arbitrary-order ocean-atmosphere! model MAOOAM.!

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Definition at line 13 of file maooam.f90.

### 6.9 maooam\_tl\_ad.f90 File Reference

### **Data Types**

• module maooam\_tl\_ad

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Tensors definition module.

### 6.10 params.f90 File Reference

### **Data Types**

module params

The model parameters module.

### 6.11 stat.f90 File Reference

### **Data Types**

· module stat

Statistics accumulators.

### 6.12 tensor.f90 File Reference

### **Data Types**

· module tensor

Tensor utility module.

• type tensor::coolist\_elem

Coordinate list element type. Elementary elements of the sparse tensors.

· type tensor::coolist

Coordinate list. Type used to represent the sparse tensor.

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#### 6.13 test aotensor.f90 File Reference

#### **Functions/Subroutines**

• program test\_aotensor

Small program to print the inner products.

#### 6.13.1 Function/Subroutine Documentation

```
6.13.1.1 program test_aotensor ( )
```

Small program to print the inner products.

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Definition at line 13 of file test\_aotensor.f90.

### 6.14 test\_inprod\_analytic.f90 File Reference

#### **Functions/Subroutines**

program inprod\_analytic\_test
 Small program to print the inner products.

#### 6.14.1 Function/Subroutine Documentation

```
6.14.1.1 program inprod_analytic_test ( )
```

Small program to print the inner products.

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Definition at line 13 of file test inprod analytic.f90.

### 6.15 test\_tl\_ad.f90 File Reference

#### **Functions/Subroutines**

program test\_tl\_ad

Tests for the Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM.

- real(kind=8) function gasdev (idum)
- real(kind=8) function ran2 (idum)

#### 6.15.1 Function/Subroutine Documentation

6.15.1.1 real(kind=8) function gasdev (integer idum)

Definition at line 149 of file test\_tl\_ad.f90.

```
6.15.1.2 real(kind=8) function ran2 ( integer idum )
```

Definition at line 174 of file test\_tl\_ad.f90.

```
6.15.1.3 program test_tl_ad ( )
```

Tests for the Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM.

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Definition at line 14 of file test\_tl\_ad.f90.

## 6.16 tl\_ad\_integrator.f90 File Reference

### **Data Types**

• module tl\_ad\_integrator

Tangent Linear (TL) and Adjoint (AD) model versions of MAOOAM. Integrators module.

### 6.17 util.f90 File Reference

### **Data Types**

· module util

Utility module.

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