

## Introduction to Telecommunications

### Question 1

Let a signal  $sq\_triangle(t)$  which is the square of the triangular periodic table. This signal has amplitude  $A = 4$  V and frequency  $f_m$  in kHz which  $f_m$  is the sum of the last three digits of each student's Registration Number. If the sum exceeds 9 then the sum of the digits continues until a single digit number occurs. Figure 1 illustrates an example of a triangular periodic pulse series of amplitude  $A = 1$  V and frequency 1 Hz.

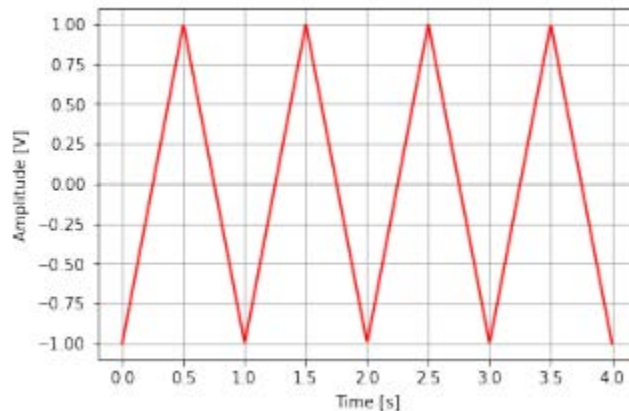


Figure 1

- The above signal  $sq\_triangle(t)$  to be sampled with two different frequencies, first with  $f_{s1} = 25f_m$  and then with  $f_{s2} = 60f_m$ . Present the following three graphs:
  - Samples after sampling with frequency  $f_{s1}$ .
  - Samples after sampling with frequency  $f_{s2}$ .
  - The samples from questions (i) and (ii) in a common diagram.
- What do you notice if the signal  $sq\_triangle(t)$  is sampled with  $f_s = 5f_m$ ? How would you find the minimum theoretical  $f_s$  so that the exact signal under discussion can be accurately reconstructed? Approach it theoretically and numerically.
- Let be a halftone  $z(t) = A \sin(2\pi f_m t)$  of width  $A = 1$  V and frequency  $f_m$  in kHz. The frequency  $f_m$  is the sum of the last three digits of the Registration Number of each student. If the sum exceeds 9 then the sum of the digits continues until it occurs a single digit number.
  - Repeat questions (a) and (b) for signal  $z(t)$ .
  - Repeat questions (a) and (b) for signal  $q(t) = z(t) + A \sin(2\pi(f_m + \Lambda)t)$ , where  $A = 1$  V and  $\Lambda = 1$  kHz. What is the resultant signal? Explain briefly.

Note: In the diagrams the horizontal axis should express time (sec) and the samples should not be joined together. In the diagrams of queries a and c (i) to present four (4) periods while in c (ii) one (1) period.

## Question 2

Consider as input to a uniform quantizer (mid riser) the signal  $y(t)$  of the 1st question after sampling frequency  $f_{s1} = 45f_m$ . If the frequency  $f_m$  is even (based on the Registration Number) to be quantized with 4 bits, otherwise (if it is unnecessary) to be quantized with 5 bits.

- a) Diagram the output of the quantum. The vertical axis will display the quantization levels (not as a decimal number but as a binary one, having coded Gray) and the horizontal axis the time (in sec).
- b) Calculate the standard deviation of the quantization error
  - i) for the first 10 samples
  - ii) for the first 20 samples
  - iii) Calculate the quantization SNR for cases (i) and (ii) as well as its theoretical value and explain any differences in the resulting values.
- c) After the quantization, present in a diagram for a period the corresponding transmission flow from bits (bit stream) considering a line coding of BIPOLAR RZ with a bit duration of 1 msec. The amplitude (in Volts) is numerically equal to the frequency of the signal (eg for a frequency of 1 kHz, the amplitude is 1 V).

## Question 3

Considering the sine signal  $z(t)$  of the 1st question with  $f_{s2} = 130f_m$  as a carrier in AM configuration with modulation index 0.5 and information signal  $m(t) = \sin(2\pi 35t)$ :

- a) Present the AM signal modulated signal for four (4) periods of the information signal  $m(t)$ .
- b) Implement a demodulator / ambient light and plot the signal after demodulation. The final signal at the demodulator output should coincide with the original pre-configuration information signal. It is recommended to use Python's SciPy library and more specifically the `signal.firwin()` and `signal.lfilter()` commands.