The VMC++ Library

Francesco Calcavecchia

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VMC++ (Variational Monte Carlo Plus Plus) is a C++ library which allows with few simple commands for the implementation of a Variational Monte Carlo calculation. It provides the tools for describing a trial wave function and an Hamiltonian, and it uses this information to find the optimal values of the variational parameters embedded in the trial wave function, and therefore find the best approximation of the ground state.

The code has been developed using the standard C++11, and requires the MCI++ (https://github.com/francesco086/MCIntegratorPlusPlus) and NoisyFunMin (https://github.com/francesco086/NoisyFunMin) libraries.

In the following we will present the classes made available by the library. At the beginning we will report the necessary #include call and the prototype of the class. The comment TO DO indicates that the method needs to be implemented (as in the case of a pure virtual class).

First, we will present the virtual classes that should be instantiated for describing the trial wave function and the Hamiltonian. Then, we will introduce the class that performs the whole Variational Monte Carlo calculation.

1 WaveFunction

```
#import "WaveFunction.hpp"
1
2
3
  IMPLEMENTATIONS OF THIS INTERFACE MUST INCLUDE:
5
      - void setVP(const double *vp)
6
               set the variational parameters
7
      - void getVP(double *vp)
9
               get the variational parameters
10
11
        void samplingFunction(const double * in, double * out)
12
               heritage from MCISamplingFunctionInterface, uses Psi
13
14
        double getAcceptance()
15
               heritage from MCISamplingFunctionInterface
```

```
17
      - void computeAllDerivatives(const double *x)
18
19
              use the setters for derivatives values (setD1DivByWF
                  , setD2DivByWF, etc.)
20
21
22
  class WaveFunction: public MCISamplingFunctionInterface, public
23
      MCICallBackOnAcceptanceInterface {
  public:
24
      WaveFunction(const int &nspacedim, const int &npart, const
25
          int &ncomp, const int &nvp,
           bool flag_vd1=true, bool flag_d1vd1=true, bool
26
              flag d2vd1=true);
      virtual ~WaveFunction();
27
28
29
      int getNSpaceDim();
      int getTotalNDim();
30
      int getNPart();
31
      int getNVP();
32
33
34
      // --- interface for manipulating the variational parameters
35
      virtual void setVP(const double *vp) = 0; // --- MUST BE
36
          IMPLEMENTED
      virtual void getVP(double *vp) = 0; // --- MUST BE
37
          IMPLEMENTED
38
39
      // --- computation of the derivatives
40
      // When called, this method computes all the internal values
41
          , such as the derivatives,
      // and stored them internally, ready to be accessed with the
42
           getters methods.
      // It requires the positions as input
43
      virtual void computeAllDerivatives (const double *x) = 0;
44
               - MUST BE IMPLEMENTED
45
46
      // --- getters and setters for the derivatives
47
      // first derivative divided by the wf
48
      void setD1DivByWF(const int &id1, const double &d1_logwf);
49
      double getD1DivByWF(const int &id1);
50
51
      // second derivative divided by the wf
52
      void setD2DivByWF(const int &id2, const double &d2 logwf);
53
      double getD2DivByWF(const int &id2);
      // variational derivative divided by the wf
56
      bool hasVD1();
57
      void setVD1DivByWF(const int &ivd1, const double &vd1 logwf)
58
      double getVD1DivByWF(const int &ivd1);
59
60
```

```
cross derivative: first derivative and first variational
61
          derivative divided by the wf
      bool hasD1VD1();
62
      void setD1VD1DivByWF(const int &id1, const int &ivd1, const
63
          double &d1vd1 logwf);
      double getD1VD1DivByWF(const int &id1, const int &ivd1);
      // cross derivative: second derivative and first variational
66
           derivative divided by the wf
      bool hasD2VD1();
67
      void setD2VD1DivByWF(const int &id2, const int &ivd1, const
68
          double &d2vd1 logwf);
      double getD2VD1DivByWF(const int &id2, const int &ivd1);
69
```

The class WaveFunction is a pure virtual class introduced for representing the trial wave function. The first thing that should be noticed, is that it is a child class of the MCI++ classes MCISamplingFunctionInterface and MCICallBackOnAcceptanceInterface. Please refer to the user manual of MCI++ to see the details of this class. The user must be able to correctly implement the MCISamplingFunctionInterface's methods samplingFunction and getAcceptance.

Let us now see in details the methods of the class WaveFunction:

- WaveFunction: The constructor. It is necessary to specify the number of dimensions of the space in which it is used (nspacedim, typically 3 dimensions), the number of particles that the wave function describes (npart), the number of components of the wave function (ncomp, which corresponds to nproto of the class MCISamplingFunctionInterface), and the number of variational parameters used (nvp). Moreover, with the optional parameters flag_vd1, flag_d1vd1, and flag_d2vd1, one can specify if the variational derivatives $\frac{1}{\psi(x)} \frac{\partial \psi(x)}{\partial \alpha_i}$, $\frac{1}{\psi(x)} \frac{\partial^2 \psi(x)}{\partial x_i \partial \alpha_i}$, and $\frac{1}{\psi(x)} \frac{\partial^3 \psi(x)}{\partial x_i^2 \partial \alpha_i}$ are computed or not;
- getNSpaceDim: Returns nspacedim;
- getNPart: Returns npart;
- getNVP: Returns nvp
- setVP: Set the variational parameters according to the provided nvp-dimensional array vp. Must be implemented by the user;
- getVP: Store in the nvp-dimensional array vp the values of the variational parameters. Must be implemented by the user;
- compute All Derivatives: This method must be implemented to compute all the derivatives that the wave function should implement. Once computed, all the derivatives, divided by the value of the wave function

itself, should be stored internally using the methods setD1DivByWF, setD2DivByWF, setD1VD1DivByWF, setD2VD1DivByWF;

- hasVD1, hasD1VD1, hasD2VD1: Tells whether the wave function implements the variational derivatives or not:
- getD1DivByWF, getD2DivByWF, getVD1DivByWF, getD1VD1DivByWF, getD2VD1DivByWF: In case the values were computed, returns the derivatives divided by the wave function value.

1.1 FFNNWaveFunction

In case you want to use a Neural Network as Wave Function, there is an already prepared WaveFunction. One needs to provide only the number of spacial dimensions (nspacedim) and number of particles (npart), and a Feed-FowardNeuralNetwork (see the library) that has nspacedim × npart inputs and only one output. This FFNN should be already connected, but should not have any derivative substrate. As for the WaveFunction, some flags can be specified in the constructor to tell whether the variational derivatives are computed or not. Internally, this class create two separated instances of this FFNN, a bare one, which does not have any substrate, and is used only for sampling, and a more complex one, that is used for computing all the derivatives.

Of course, it inherits all the methods from the WaveFunction class, and we do not report it in the following.

```
class FFNNWaveFunction: public WaveFunction{
2
3
  private:
      FeedForwardNeuralNetwork * ffnn;
4
5
6
  public:
            - Constructor
      // IMPORTANT: The provided ffnn should be ready to use (
          connected) and have the first, second and variational
          derivatives substrates
      FFNNWaveFunction(const int &nspacedim, const int &npart,
9
          FeedForwardNeuralNetwork * ffnn, bool flag vd1=true, bool
           flag_d1vd1=true, bool flag_d2vd1=true);
10
11
            - Getters
12
      FeedForwardNeuralNetwork * getBareFFNN() { return bare ffnn; }
13
      FeedForwardNeuralNetwork * getDerivFFNN() { return _ deriv_ffnn
          ;}
15
16
  };
```

2 Hamiltonian

```
import "Hamiltonian.hpp"
1
  class Hamiltonian: public MCIObservableFunctionInterface
2
3
  {
     public:
4
         // Constructor and destructor
5
        Hamiltonian (const int &nspacedim, const int &npart,
6
            WaveFunction * wf):
            MCIObservableFunctionInterface (nspacedim*npart,4)
7
         virtual ~Hamiltonian(){}
8
9
         // Getters
10
         int getNSpaceDim();
11
        int getNPart();
12
13
         // Kinetic energy
14
        double localPBKineticEnergy(const double *in);
15
        double localJFKineticEnergy(const double *in);
16
17
         // Potential energy
18
         virtual double localPotentialEnergy(const double *in) = 0;
19
               // TO DO
20
         // Heritage from MCIObservableFunctionInterface
21
         // already implemented
22
         void observableFunction(const double * in, double *out)
24 };
```

This pure virtual class is used to define the Hamiltonian of the system. The user must take care of implementing only the localPotentialEnergy method, while all the rest is already provided.

- Hamiltonian: The constructor. It requires the spacial number of dimensions (nspacedim), the number of particles (npart), and a pointer to an implementation of a WaveFunction. Notice that the constructor inform the constructor of MCIObservableFunctionInterface that the Monte Carlo integral will be performed in a nspacedime × npart space, and that there will be 4 observables, corresponding to the total, potential, kinetic, and Jackson-Feenberg kinetic energies, respectively. All the energies are computed as energy unit per particle;
- getNSpaceDim: Returns nspacedim;
- getNPart: Returns getNPart;
- localPBKineticEnergy: Returns the standard (Pandharipande-Bethe) local kinetic energy, in units of energy per particle. It requires the particle positions, provided through the array in;

- localJFKineticEnergy: Returns the Jackson-Feenberg local kinetic energy;
- localPotentialEnergy: Returns the local potential energy. Must be implemented by the user;
- observableFunction: Returns the 4 observables for the particle coordinates contained in the array in. The observables will be contained in the array out, and are the local total, potential, kinetic, and Jackson-Feenberg kinetic energies.

As example, we report the Hamiltonian for a one-dimensional, one-particle, harmonic oscillator:

$$H = -\frac{\partial^2 \psi}{\partial x^2} + \frac{1}{2}\omega^2 x^2 \tag{1}$$

```
class HarmonicOscialltor1D1P: public Hamiltonian
2
     protected:
3
        double _w;
4
5
     public:
6
        HarmonicOscialltor1D1P(const double w, WaveFunction * wf):
               Hamiltonian(1, 1, wf) \{ w=w; \}
8
10
        double localPotentialEnergy(const double *r)
            return (0.5* w* w*(*r)*(*r));
12
13
14
```

3 VMC

```
// #include "VMC.hpp"
  class VMC{
  public:
4
     VMC(WaveFunction * wf, Hamiltonian * H);
     \sim VMC();
7
     // Monte Carlo Integral within VMC should be performed using
9
         the MCI object provided by VMC
     MCI * getMCI(){return mci;}
10
11
12
     // Computation of the variational energy
13
     void computeVariationalEnergy (const long & Nmc, double * E,
14
         double * dE);
```

```
16
     // Wave Function Optimization Methods
17
18
     void conjugateGradientOptimization(const long & Nmc, const
         long &grad E Nmc);
19
     void stochasticReconfigurationOptimization(const long &Nmc);
20
21
     void simulatedAnnealingOptimization(const long &Nmc, const
22
         double &iota, const double &kappa, const double &lambda,
         gsl siman params t &params);
23
24
```

The Variational Monte Carlo (VMC) method is a method that uses a minimisation method in order to find the variational parameters α of a trial wave function ψ_{α} such that the variational energy

$$E(\psi_{\alpha}) = \frac{\int dR \,\psi_{\alpha}(R) H \psi_{\alpha}(R)}{\int dR \,\psi_{\alpha}(R) \psi_{\alpha}(R)} \tag{2}$$

is minimised. In Eq. (2) H is the Hamiltonian, and we have assumed that both the Hamiltonian and the wave functions are real, as it is done by this library. The minimisation can be achieved by using several optimisation algorithms. At the end of the optimization process, the wave function will be set to have the optimal variational parameters

- VMC: The constructor. It requires a wave function, a Hamiltonian, and the number of sampling points to use for computing the energy (ENmc) and the energy gradient (GNmc) during the optimisation process. Notice that the constructor inform the constructor of NoisyFunctionWithGradient about the number of the number of variational parameters used by the wave function:
- getMCI: Returns a pointer to the MCI object used to compute the variational energy and the wave function derivatives;
- computeVariationalEnergy: Compute the total, kinetic, and potential energies for the given wave function. In fact E is expected to be an array of size 4, where E[0] is the total energy, E[1] is is the potential energy, E[2] is the Pandharipande-Bethe kinetic energy (i.e. the "real" kinetic energy), and E[3] is the Jackson-Feenberg kinetic energy;
- conjugateGradientOptimization: Optimise the trial wave function using the conjugate gradient method of the NoisyFunMin library. It requires the number of sampling points for computing the energy during the linear search, and the number of samplings to use for computing the energy gradient;

- stochasticReconfigurationOptimization: Optimise the trial wave function using the Dynamic Descent method of the NoisyFunMin library using as direction the one obtained using the Stochastic Reconfiguration (SR) approach. It requires the number of sampling points for computing the SR direction;
- simulatedAnnealingOptimization: Optimise the trial wave function using the Simulated Annealing algorithm contained in the GSL library (read here). The simulated annealing will try to minimise the target function

$$iE + \kappa \sigma_E + \lambda \frac{\sqrt{\sum_{i=1}^{N_{\alpha}} \alpha_i^2}}{N_{\alpha}}$$

where E is the energy, σ_E is the energy's standard deviation, and the last term represents a normalization factor, often used in Machine Learning. The weight of each term is controlled by the three parameters ι (iota), κ (kappa), and λ (lambda), which must be provided to the method. Furthermore the method requires Nmc, the number of sampling points for computing the target function integrals (E and σ_E), and the GSL siman library parameters.

Examples can be found in the folder examples.