

Formal Verification in K

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Outline

RV and K: an overview

The K Framework

Symbolic Execution in K

Using the Haskell Backend

RV and K: an overview

Who is Runtime Verification, Inc.?



- ▶ **Runtime Verification Inc.** is a startup headquartered in Urbana, Illinois, USA, with staff around the world, including Bucharest, Romania.
- ▶ The company specialises in security for the **blockchain** and **embedded** domains. Our services include code audits and verification using a **formal methods**-based approach.
- ▶ The company is named after **runtime verification** as a technique for analysing programs as they execute, observing the results of the execution and using those results to find bugs.
- ▶ One of our unique technologies is the **K Framework**, a semantic framework for design, implementation and formal reasoning.

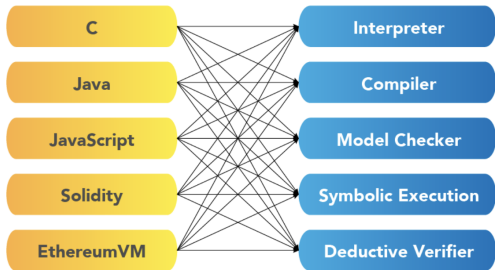
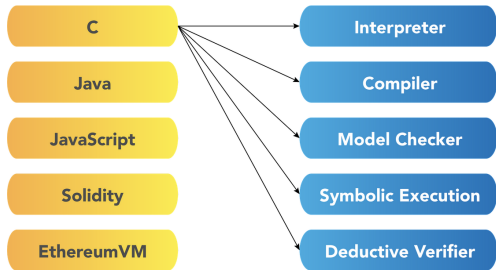
What is K?

- ▶ K is a framework for deriving programming languages tools from their **semantic specifications**.
- ▶ What is a semantic specification?

What is K?

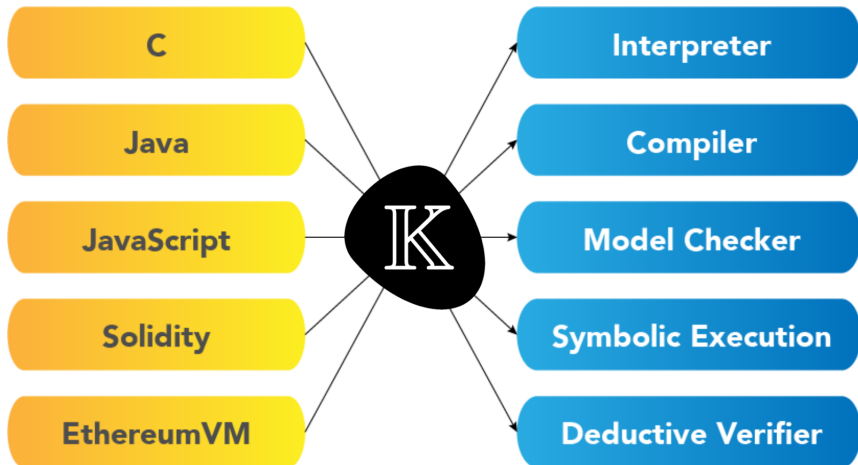
- ▶ K is a framework for deriving programming languages tools from their **semantic specifications**.
- ▶ What is a semantic specification?
- ▶ For a programming language L , a semantic specification (or just semantics) is a mathematical model of the language and its behaviour.
- ▶ Specifying a semantics in K is similar to specifying the **operational semantics** of a programming language.
- ▶ Historically, when designing programming languages people skipped specifying their semantics: it was generally considered time consuming and useless.
- ▶ This resulted in the implementation of programming languages dictating the behaviour they should have. A direct corollary of this is that **different implementations can have different behaviours**.

The Problem

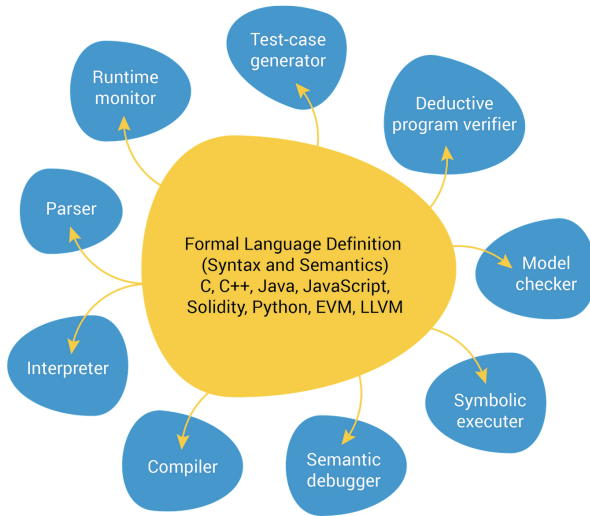


The K Solution

A language independent framework



Semantics-driven PL design



The K Framework

Defining Semantics in K

Three main components:

- ▶ **Syntax**: encodes the system primitives
- ▶ **Configuration**: encodes the system state
- ▶ **Transition Rules**: encode the system behavior

Defining Semantics in K

Defining Syntax

```
1 syntax AExp ::= Int | Id ...
2
3 syntax Stmt ::= Id "=" AExp ";" | ...
```

- ▶ K allows defining language syntax using Backus-Naur form
- ▶ The primitive constructs of the language inhabit user-defined **sorts** (categories of primitive constructs)

```
1 syntax BExp ::= Bool
2               | BExp "&&" BExp      [left, strict(1)]
3               | ...
```

- ▶ Users can specify **attributes** which provide parsing/execution hints to K

Defining Semantics in K

Defining Configurations

```
1 configuration <T>
2     <k> Stmt </k>
3     <state> .Map </state>
4 </T>
```

- ▶ Configurations are split into **cells**, which describe the different components of the program state
- ▶ The contents of the cells contain syntactical constructs defined earlier

Defining Semantics in K

Defining Transition Rules

```
1 rule
2   <k> X:Id => I ...</k>
3   <state>... X |-> I ...</state>
4 [label(variable_lookup)]
5
6
7 rule
8   <k> X = I:Int; => . ...</k>
9   <state>... X |-> (_ => I) ...</state>
10 [label(variable_assignment)]
```

- ▶ Transition rules describe how the configuration (program state) evolves during execution
- ▶ We say "the LHS configuration is rewritten to the RHS configuration"
- ▶ Rules apply by **unifying** the LHS configuration with the configuration which describes the program being executed
- ▶ K is built for making writing these rules as **efficient and maintainable** as possible: "local" description of state transformation, possibility of omitting parts of the state which do not get modified etc.

Defining Semantics in K

An example (1)

(Simplified) K definition:

```
1 syntax AExp ::= Int | Id
2
3 syntax Stmt ::= Id "=" AExp ";"          [strict(2)]
4
5 configuration <T>
6     <k> Stmt </k>
7     <state> .Map </state>
8 </T>
9
10 rule
11     <k> X = I:Int; => . ...</k>
12     <state>... X |-> (_ => I) ...</state>
13 [label(variable_assignment)]
```

Program:

```
1 n = 10;
```

Defining Semantics in K

An example (2)

Program in K:

```
1 <T>
2   <k> n = 10; </k>
3   <state> .Map </state>
4 </T>
```

Program state after applying the transition rule:

```
1 <T>
2   <k> .K </k>
3   <state> n |-> 10 </state>
4 </T>
```

The rule unifies with the configuration, meaning that it finds a way in which the LHS "overlaps" with the program. Specifically, this overlap exists when the variable X is equal to n and the variable l is equal to 10. A more technical detail is that the rest of the map inside the rule will be equal to the empty map. These associations form a [substitution](#).

K's Program Execution Capabilities

What if we had a program like:

```
1 n = N:Int;
```

- ▶ Can this be executed using K?

K's Program Execution Capabilities

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- ▶ Can this be executed using K?
- ▶ The answer is yes! What is this kind of execution called, when the program contains elements which are not concrete?

K's Program Execution Capabilities

What if we had a program like:

```
1 n = N:Int;
```

- ▶ Can this be executed using K?
- ▶ The answer is yes! What is this kind of execution called, when the program contains elements which are not concrete?
- ▶ One of the most important features of K is that it can do **symbolic execution**. Configurations become templates for programs, abstracting over a set of concrete programs which match it.

K's Program Execution Capabilities

What if we had a program like:

```
1 n = N: Int;
```

- ▶ Can this be executed using K?
- ▶ The answer is yes! What is this kind of execution called, when the program contains elements which are not concrete?
- ▶ One of the most important features of K is that it can do **symbolic execution**. Configurations become templates for programs, abstracting over a set of concrete programs which match it.
- ▶ The innovative aspect here is that defining the semantics in K gives us a description of how programs execute, and using this K is able to do symbolic execution and check on all paths if execution reaches a specified state.
- ▶ This means that K can naturally do **deductive verification** as well!

Symbolic Execution in K

- ▶ K's modern symbolic execution engine: the [Haskell backend](#)
- ▶ Developed and maintained by a dedicated team at RV
- ▶ Based on the logical formalisms for K, [matching logic](#) and [reachability logic](#)

Using the Haskell Back-end

Example: the IMP Language

Definition and program specification in K

- ▶ `imp.k`
- ▶ `sum-spec.k`

Proving with the Haskell backend

- ▶ First, kompile the definition for the Haskell backend:

```
1 $ kompile --backend haskell imp.k  
2
```

- ▶ Then, use kprove on the specification file:

```
1 $ kprovex sum-spec.k  
2
```

Proving with the Haskell backend

- ▶ First, kompile the definition for the Haskell backend:

```
1 $ kompile --backend haskell imp.k
2
```

- ▶ Then, use kprove on the specification file:

```
1 $ kprovex sum-spec.k
2
```

- ▶ The output we get is:

```
1 #Top
2
```

- ▶ That means the proof passed, but it doesn't give us much information about how it managed to prove the specification.

Proving with the Haskell backend

The Interactive Proof Debugger

- ▶ Thankfully, the Haskell backend has an interactive debugger mode which allows us to execute each semantic step separately and inspect the state of the proof

```
1 $ kprovex sum-spec.k --debugger
2 Welcome to the Kore Repl! Use 'help' to get started.
3
4 Kore (0)>
5
```

- ▶ The [help](#) command will give you a list of all the available commands in the [kore-repl](#)
- ▶ [Kore](#) = the internal language of the Haskell backend

Proving with the Haskell backend

The Interactive Proof Debugger



- ▶ Each claim is proven separately, so to start we can use the following command to see which one we are currently proving

```
1  Kore (0)> claim
2  You are currently proving claim 0
3  \implies{SortGeneratedTopCell{}}(
4    \and{SortGeneratedTopCell{}}(
5      /*... requires predicate ...*/ ,
6      /*... left term ...*/
7    ),
8    weakAlwaysFinally{SortGeneratedTopCell{}}(
9      /*... right pattern ...*/
10   )
11 )
12
```

- ▶ The whole output: **claim0.kore**

Proving with the Haskell backend

The Interactive Proof Debugger



- ▶ The previous command resulted in a big pattern in the Kore language
- ▶ Fortunately, we don't need to understand Kore to use the interactive debugger

```
1 Kore (0)> load kast.kscript
2 Kore (0)> kclaim
3 You are currently proving claim 0
4   /* left term */
5   #And
6   /* requires predicate */
7 #Implies
8   #wAF (
9     /* right pattern */
10   )
11
```

- ▶ The whole output: **claim0.k**

Proving with the Haskell backend

Observations until now

- ▶ The K produced by the previous command differs from the original K claim
- ▶ This K comes from a verbatim translation of Kore
- ▶ We're closer to the internal representation of claims in the Haskell backend
- ▶ We're proving the claim with `while` at the top, this means we're proving the invariant
- ▶ Let's go back to the proof!

Proving with the Haskell backend

The first step

- Using the debugger, we can take a single execution step and inspect the new configuration

```
1 Kore (0)> step
2 Kore (1)> konfig
3 Config at node 1 is:
4   <T>
5     <k>
6       if ( ! n <= 0 ) { { sum = sum + n ; n = n + -1 ; } while ( ! n <= 0 ) { sum = sum + n ; n =
7         n + -1 ; } } else { } ~> _DotVar2 ~> .
8     </k>
9     <state>
10       n |-> N:Int
11       sum |-> S:Int
12     </state>
13   </T>
14 #And
15 {
16   true
17   #Equals
18   N >=Int 0
19 }
```

Proving with the Haskell backend

The first step



- Let's look at the rule which was applied to reach this new configuration

```
1 Kore (1)> krule
2   #Top
3 #And
4   <T>
5     <k>
6       while ( RuleVarB ) RuleVarS ~> RuleVar_DotVar2 ~> .
7     </k>
8     RuleVar_DotVar1
9   </T> => <T>
10  <k>
11    if ( RuleVarB ) { RuleVarS:Block while ( RuleVarB ) RuleVarS } else { } ~> RuleVar_DotVar2 ~>
12    .
13  </k>
14  RuleVar_DotVar1
15 </T>
16 /Users/anapantilie/RV/LOSPresentation/ImpDemo/imp.k:69:10-69:55
17 Axiom 28
```


Proving with the Haskell backend

The second step

- Let's run another step to see how the `if` at the top starts getting rewritten

```
1 Kore (1)> step
2 Kore (2)> konfig
3 Config at node 2 is:
4   <T>
5     <k>
6       ! n <= 0 ~> #freezerif( )_else__IMP-SYNTAX_Stmt_BExp_Block_Block0_ ( { { sum = sum + n ; n =
          n + -1 ; } while ( ! n <= 0 ) { sum = sum + n ; n = n + -1 ; } } ~> . , { } ~> . ) ~>
          _DotVar2 ~> .
7     </k>
8     <state>
9       n |-> N:Int
10      sum |-> S:Int
11    </state>
12  </T>
13 #And
14 {
15   true
16 #Equals
17   N >=Int 0
18 }
19
```

Proving with the Haskell backend

The second step

► Let's see the rule that applied

```
1 Kore (2)> krule
2   <T>
3   <k>
4     if ( RuleVarHOLE ) RuleVarK1 else RuleVarK2 ~> RuleVar_DotVar2 ~> .
5   </k>
6   RuleVar_DotVar1
7 </T>
8 #And
9 {
10   true andBool notBool isKResult ( RuleVarHOLE:BExp ~> . )
11 #Equals
12   true
13 } => <T>
14 <k>
15   RuleVarHOLE:BExp ~> #freezerif(_)_else__IMP-SYNTAX Stmt_BExp_Block_Block0_ ( RuleVarK1:Block
16     ~> . , RuleVarK2:Block ~> . ) ~> RuleVar_DotVar2 ~> .
17 </k>
18 RuleVar_DotVar1
19 </T>
20 /Users/anapantilie/RV/LOSPresentation/ImpDemo/imp.k:18:22-19:59
21 Axiom 8
```

Proving with the Haskell backend

K and contextual evaluation

- ▶ We didn't actually define this rule in the semantics
- ▶ The previous rule was generated by `if`'s strictness annotation
- ▶ What needs to be evaluated first gets pushed to the top of the K cell
- ▶ The remaining computations (which depend on these evaluations) are remembered and sequenced later in the computation list
- ▶ All the necessary rules to achieve this are generated by `K's frontend`, the **backend doesn't do this sort of "magic"**
- ▶ For this presentation, we will skip all these steps related to contextual evaluation
- ▶ If you're interested in understanding K better, I recommend studying these steps as an exercise!

Proving with the Haskell backend

Rewriting the if

- ▶ The steps between node 2 and node 10 take care of evaluating the **if**'s condition

```
1 Kore (10)> konfig
2 Config at node 10 is:
3   <T>
4     <k>
5       if ( notBool N <=Int 0 ) { { sum = sum + n ; n = n + -1 ; } while ( ! n <= 0 ) { sum = sum +
6         n ; n = n + -1 ; } } else { } ~> _DotVar2 ~> .
7     </k>
8     <state>
9       n |-> N:Int
10      sum |-> S:Int
11    </state>
12  </T>
13 #And
14 {
15   true
16   #Equals
17   N >=Int 0
18 }
```

- ▶ If we run another execution step, what do you expect will happen?

Proving with the Haskell backend

Rewriting the if

- ▶ The proof branches, and by inspecting the two new configurations we can see on which condition

```
1 Kore (10)> step
2 Stopped after 0 step(s) due to branching on [11,12]
3
```

- ▶ In $config_{11}$ we get $N >_{Int} 0$

```
1 #And
2 {
3   false
4   #Equals
5     N <=Int 0
6 }
7
```

- ▶ In $config_{12}$ we get $N ==_{Int} 0$

```
1 #And
2 {
3   true
4   #Equals
5     N <=Int 0
6 }
7
```

Proving with the Haskell backend

The "base case"

- Let's look at the configuration when $N \equiv_{Int} 0$

```
1 Kore (13)> konfig
2 Config at node 13 is:
3   <T>
4     <k>
5       _DotVar2
6     </k>
7     <state>
8       n |-> N:Int
9       sum |-> S:Int
10    </state>
11  </T>
12 #And
13 {
14   true
15 #Equals
16   N <=Int 0
17 }
18 #And
19 {
20   true
21 #Equals
22   N >=Int 0
23 }
24
```

Proving with the Haskell backend

The "base case"

- ▶ By looking at the destination, with some simplification the two are identical
- ▶ We can expect the proof is trivial on this branch

```
1 Kore (13)> dest | kast -i kore -o pretty -d . /dev/stdin
2 Destination at node 13 is:
3 <T>
4   <k>
5     _DotVar2
6   </k>
7   <state>
8     n |-> 0
9     sum |-> S +Int ( N +Int 1 ) *Int N /Int 2
10  </state>
11 </T>
12
```

- ▶ The backend will unify the configuration and the destination, and see that the condition is also satisfied

Proving with the Haskell backend

The "base case"

- ▶ Stepping again will only tell us that the proof has been finished on this branch

```
1 Kore (13)> step
2 Stopped after 0 step(s) due to reaching end of proof on current branch.
3
```


Proving with the Haskell backend

The "inductive case"

- Let's go back to the branch we haven't yet started proving, where $N >_{Int} 0$

```
1 Kore (11)> konfig
2 Config at node 11 is:
3   <T>
4     <k>
5       { { sum = sum + n ; n = n + -1 ; } while ( ! n <= 0 ) { sum = sum + n ; n = n + -1 ; } } ~>
6       _DotVar2 ~> .
7     </k>
8     <state>
9       n |-> N:Int
10      sum |-> S:Int
11    </state>
12  </T>
13 #And
14 {
15   false
16   #Equals
17   N <=Int 0
18 }
19 #And
20 {
21   true
22   #Equals
23   N >=Int 0
24 }
```

Proving with the Haskell backend

The "inductive case"

- We see that we have one *while* loop iteration to execute, for brevity we will skip till we reach the *while* again

```
1 Kore (11)> step 100
2 Kore (35)> konfig
3 Config at node 35 is:
4   <T>
5     <k>
6       while ( ! n <= 0 ) { sum = sum + n ; n = n + -1 ; } ~> _DotVar2 ~> .
7     </k>
8     <state>
9       n |-> N +Int -1
10      sum |-> S +Int N
11    </state>
12  </T>
13 #And
14 {
15   false
16   #Equals
17   N <=Int 0
18 }
19 #And
20 {
21   true
22   #Equals
23   N >=Int 0
24 }
25
```

Proving with the Haskell backend

The "inductive case"

- ▶ Stepping now will apply the claim itself as a circularity
- ▶ It applies because the two terms unify, and the precondition is satisfied
- ▶ The unification results in the following substitution:
$$\sigma = \{N_R = N_C +_{Int} -1, S_R = S_C +_{Int} N_C\}$$
- ▶ The LHS and the RHS of the claim also unify, the conditions hold therefore the claim is proven
- ▶ We'll see the resulting configuration on the next slide

Proving with the Haskell backend

The "inductive case"

```
1 Kore (36)> konfig
2 Config at node 36 is:
3   <T>
4     <k>
5       _DotVar2
6     </k>
7     <state>
8       n |-> 0
9       sum |-> S +Int N +Int N *Int ( N +Int -1 ) /Int 2
10    </state>
11  </T>
12 #And
13 {
14   false
15   #Equals
16   N <=Int 0
17 }
18 #And
19 {
20   true
21   #Equals
22   N +Int -1 >=Int 0
23 }
24 #And
25 {
26   true
27   #Equals
28   N >=Int 0
29 }
30
```

Proving with the Haskell backend

The "inductive case"

► The destination:

```
1 Kore (36)> dest | kast -i kore -o pretty -d . /dev/stdin
2 Destination at node 36 is:
3 <T>
4   <k>
5     _DotVar2
6   </k>
7   <state>
8     n |-> 0
9     sum |-> S +Int ( N +Int 1 ) *Int N /Int 2
10  </state>
11 </T>
12
```

► And the last step in the claim's proof:

```
1 Kore (36)> step
2 Stopped after 0 step(s) due to reaching end of proof on current branch.
```

Proving with the Haskell backend

The main claim

- ▶ Let's use the following command to see the whole proof status

```
1 Kore (36)> proof-status
2 Current proof status:
3   claim 1: NotStarted
4   claim 0: Completed
5
```

- ▶ We can switch to proving the second claim, which we know is our main claim as follows

```
1 Kore (36)> prove 1
2 Switched to proving claim 1
3 Kore (0)>
4
```

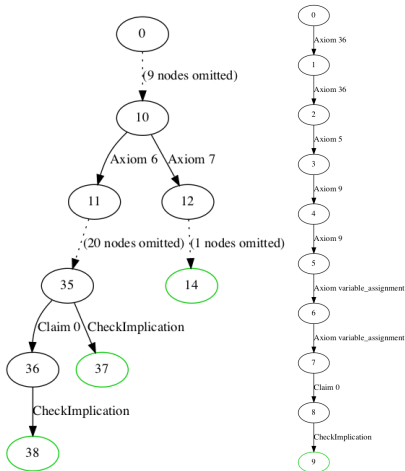
- ▶ Let's not study each step of this proof, but it can be useful as an exercise!

```
1 Kore (0)> step 100
2 Stopped after 8 step(s) due to reaching end of proof on current branch.
3 Kore (8)>
4
```

Proving with the Haskell backend

Visualising the proof

The `graph` command inside the debugger generates a graph visualisation of the proof for the currently selected claim.



Proving with the Haskell backend

Conclusions

- ▶ We've seen that K provides a general solution to defining programming languages
- ▶ K generates the necessary tooling for free, providing a semantics-based approach to PL development
- ▶ K offers symbolic execution and deductive verification based on a sound, mathematical formalism, again, for free
- ▶ We've seen how to use this verifier in practice on a toy example

The background features several thin, light gray concentric circles centered on the slide. In the middle of these circles is a large, solid yellow, irregular blob shape.

Thank you!

References and Further Reading

References and Further Reading

- 1 GitHub repository for the Haskell Backend
 - 2 GitHub repository for the K Framework
 - 3 The K User Manual
 - 4 The K Overview
 - 5 Verifying Wasm Programs with K, Stephen Skeirik, 2019
 - 6 X. Chen, G. Rosu, *Matching μ -Logic*, LICS'19 ACM/IEEE, pp 1-13, June 2019
 - 7 T. Serbanuta, V. Serbanuta, X. Chen, *Proving All-Path Reachability Claims*
- For any questions feel free to reach out at ana.pantilie@runtimeverification.com!