

# Special topics in Logic and Security I

Master Year II, Sem. I, 2022-2023

Ioana Leuştean  
FMI, UB

# Formal analysis of security protocols

- In formal analysis we define and analyze a protocol within a consistent mathematical theory.
- One studies abstract versions of real protocols (for example the (real, computer-network authentication) protocol Kerberos is based on the (academic) protocol Needham-Schroeder.
- Verification based on:
  - epistemic logics, for example [BAN logic, 1990](#)
  - model-checking tools: Proverif, AVISPA, Scyther, Tamarin, ...
  - ...

In the following we shall present the *operational semantics approach* from [\[OSVSP\]](#):

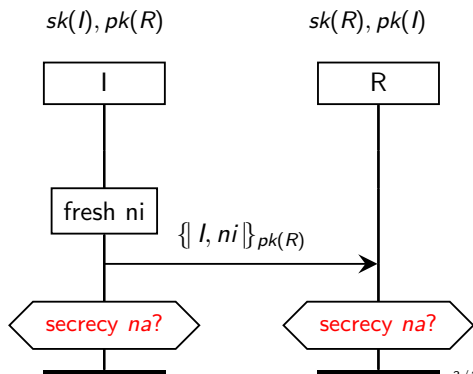
- Cremers C. and Mauw S. Operational Semantics and Verification of Security Protocols. Springer, 2012.
- Cremers, C. J. F. (2006). Scyther : semantics and verification of security protocols Eindhoven: Technische Universiteit Eindhoven DOI: 10.6100/IR614943

# Example: OSS Protocol

## One-Sided Secrecy Protocol (OSS)

$I \longrightarrow R : \{ \{ I, ni \} \}_{pk(R)}$

What does **secrecy** mean?

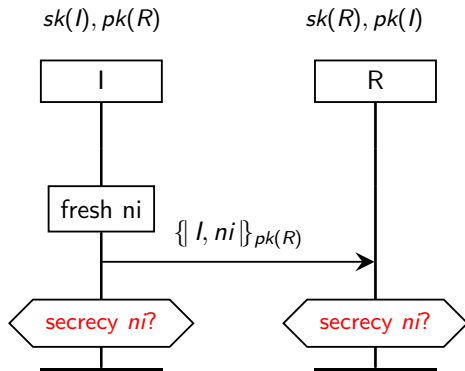


# Example: OSS Protocol

What does **secrecy ni** mean?

[OSVSP]

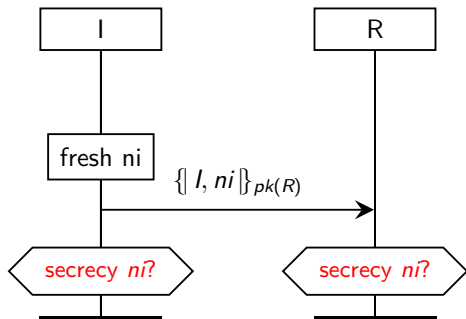
We say that the claim **secrecy ni** holds *for the role i* whenever a run of the *i* role is completed with trusted communication partners and the nonce *ni* generated in the run does not become known to the intruder



# Scyther: OSS Protocol

```
protocol oss(I,R)
{role I
{fresh ni: Nonce;
send_1(I,R, {[I,ni]}pk(R) );
claim(I,Secret,ni);}

role R
{var ni: Nonce;
recv_1(I,R, {[I,ni]}pk(R) );
claim(R,Secret,ni);
}}
```



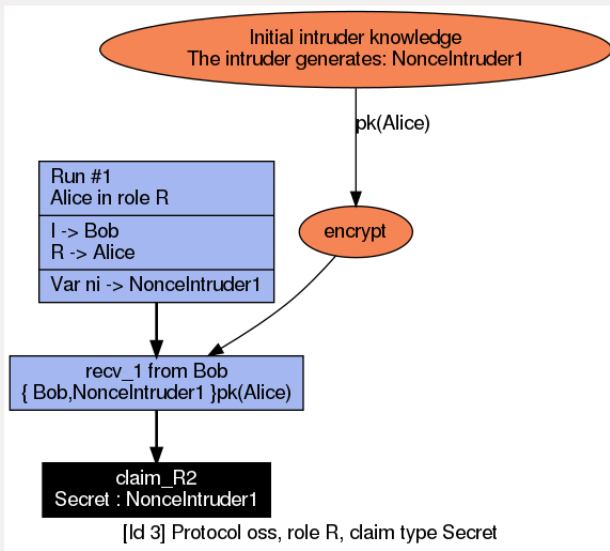
# Scyther: OSS Protocol

```
protocol oss(I,R)
{role I
{fresh ni: Nonce;
send_1(I,R, {I,ni}pk(R) );
claim(I,Secret,ni);}
```

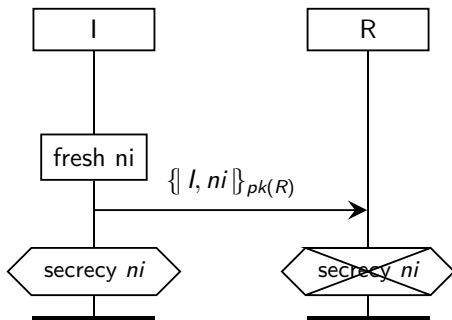
```
role R
{var ni: Nonce;
recv_1(I,R, {I,ni}pk(R));
claim(R,Secret,ni);
}}
```

Scyther results : verify							
Claim				Status		Comments	Pattern
oss	I	oss,I1	Secret ni	Ok	Verified	No attacks.	
	R	oss,R1	Secret ni	Fail	Falsified	Exactly 1 attack.	1 attack
Done.							

# Scyther: OSS Protocol



# Scyther: OSS Protocol



The claims are locally analyzed!



# Formal analysis of security protocols

- A formal approach should:
  - specify the security protocol,
  - provide a model for agents,
  - provide a model for communication,
  - provide a threat model,
  - express the security requirements.
- In the following, we shall use a *many-sorted language*:
  - *the roles and the messages are represented by terms,*
  - *a protocol is defined by specifying each role,*
  - *the (adversary) knowledge is derived using a deduction system,*
  - *the protocol execution is defined as a (complex) transition system,*
  - *the security properties are formally defined and analyzed.*

# Basic elements

- There are few types of variables and constants:
  - *Var* :  $V, X, Y, Z, \dots$  (variables for messages),
  - *Fresh* :  $ni, nr, sessionkey, \dots$  (local constants, freshly generated for each instance of a role),
  - *Role* :  $i, r, s, \dots$  ( variables for roles: initiator, respondent, server etc.)
- *Func* is a set of function symbols
  - each symbol has a fixed arity;
  - the global constants are functions of arity zero;
  - example: hash functions.

# Terms: *RoleTerm*

We use *role terms* to specify: *messages, nonces, roles, keys*.

$$\begin{aligned} \textit{RoleTerm} \quad ::= \quad & \textit{Var} \mid \textit{Fresh} \mid \textit{Role} \\ & \mid \textit{Func}(\textit{RoleTerm}^*) \\ & \mid (\textit{RoleTerm}, \textit{RoleTerm}) \\ & \mid \{ \{ \textit{RoleTerm} \} \}_{\textit{RoleTerm}} \\ & \mid \textit{sk}(\textit{RoleTerm}) \mid \textit{pk}(\textit{RoleTerm}) \mid \textit{k}(\textit{RoleTerm}, \textit{RoleTerm}) \end{aligned}$$

We denote  $\{ \{ (t_1, t_2) \} \}$  by  $\{ \{ t_1, t_2 \} \}$ .

# The inverse function. Encryption

$$^{-1} : RoleTerm \rightarrow RoleTerm$$

- for any term  $rt \in RoleTerm$  we define the inverse  $rt^{-1} \in RoleTerm$  as follows:

$$rt^{-1} = \begin{cases} sk(t) & \text{if } rt = pk(t) \text{ for some } t \in RoleTerm \\ pk(t) & \text{if } rt = sk(t) \text{ for some } t \in RoleTerm \\ rt & \text{otherwise} \end{cases}$$

We further assume that  $sk$  and  $pk$  are the secret and, respectively, the public key for asymmetric encryption, while  $k$  defines a symmetric key.

## Example: digital signature

Assume that  $m \in RoleTerm$  is a message and  $R \in Role$  is a role.

- $\{ \{ m \} \}_{pk(R)}$  is the encryption of  $m$  with the public key of  $R$
- a digitally signed message is a pair

$$(m, \{ \{ h(m) \} \}_{sk(R)})$$

where

- $h(m)$  is the message digest, computed using the hash function  $h$ ,
  - $\{ \{ h(m) \} \}_{sk(R)}$ , the signed message digest, is computed with the signer's private key  $sk(R)$ ,
  - the message in plain text together with the signed message digest form the digitally signed message.
- 
- One can verify the digital signature, in order to prove who the signer was and the integrity of the document: find the message digest using the signer's public key and compare the message digest with the result obtained by applying the hash function to the plain message.

# Deduction on *RoleTerm*

$$\vdash \subseteq \mathcal{P}(\text{RoleTerm}) \times \text{RoleTerm}$$

$M \vdash t$  means that  $t$  can be deduced knowing  $M$

$\vdash$  is the least relation with the following properties:

- if  $t \in M$  then  $M \vdash t$
- if  $M \vdash t_1$  and  $M \vdash t_2$  then  $M \vdash (t_1, t_2)$
- if  $M \vdash (t_1, t_2)$  then  $M \vdash t_1$  and  $M \vdash t_2$
- if  $M \vdash t$  and  $M \vdash k$  then  $M \vdash \{ t \}_k$
- if  $M \vdash \{ t \}_k$  and  $M \vdash k^{-1}$  then  $M \vdash t$
- if  $M \vdash t_1$  and  $\dots$  and  $M \vdash t_n$  then  $M \vdash f(t_1, \dots, t_n)$   
where  $n$  is the arity of  $f \in \text{Func}$ .

Notation:  $\text{Cons}(M) = \{ t \in \text{RoleTerm} \mid M \vdash t \}$

**Exercise:** Find  $\text{Cons}(M)$  where  $M = \{ \{ m \}_k, \{ k^{-1} \}_{pk(b)}, \{ h(m) \}_m, sk(b) \}$ .

# Terms: *RoleEvent*

We use *role events* to specify protocol actions and claims.

- Given two disjoint sets:
  - *Label* : 1, 2, 3, ... (labels)
  - *Claim* : *secret*, *alive*, ... (denotations for security properties)

and  $R \in \text{Role}$  we define

$$\begin{aligned} \text{RoleEvent}_R \quad ::= & \text{send}_{\text{Label}}(R, \text{Role}, \text{RoleTerm}) \\ & | \text{recv}_{\text{Label}}(\text{Role}, R, \text{RoleTerm}) \\ & | \text{claim}_{\text{Label}}(R, \text{Claim}[, \text{RoleTerm}]) \end{aligned}$$

$$\text{RoleEvent} = \bigcup_{R \in \text{Role}} \text{RoleEvent}_R$$

## Termeni: *RoleEvent*

$$\begin{aligned} \text{RoleEvent}_R \quad ::= & \text{send}_{\text{Label}}(R, \text{Role}, \text{RoleTerm}) \\ & | \text{recv}_{\text{Label}}(\text{Role}, R, \text{RoleTerm}) \\ & | \text{claim}_{\text{Label}}(R, \text{Claim}[, \text{RoleTerm}]) \end{aligned}$$

- $\text{send}_l(R, R', rt)$  means that  $R$  sends the message  $rt$  to  $R'$ ,
- $\text{recv}_l(R', R, rt)$  means that  $R$  receives the message  $rt$  (apparently) sent by  $R'$ ,
- $\text{claim}_l(R, c, rt)$  is the security property that should be satisfied after the execution of the role  $R$ .
- The labels uniquely identify the events and establish the correspondence between *send* and *receive* events.



# Protocol specification

Informally, in order to specify a protocol one should describe each role.

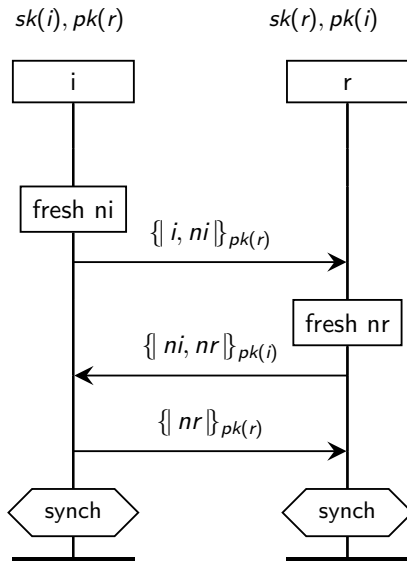
$NS(i) = (\{i, r, ni, sk(i), pk(i), pk(r)\},$

$[send_1(i, r, \{\{ni, i\}_{pk(r)}\},$

$recv_2(r, i, \{\{ni, V\}_{pk(i)}\},$

$send_3(i, r, \{\{V\}_{pk(r)}\},$

$claim_4(i, synch))]$



$$NS(i) = (\{i, r, ni, sk(i), pk(i), pk(r)\},$$
$$\begin{aligned} &[send_1(i, r, \{\{ni, i\}_{pk(r)}\}, \\ &recv_2(r, i, \{\{ni, V\}_{pk(i)}\}, \\ &send_3(i, r, \{\{V\}_{pk(r)}\}, \\ &claim_4(i, synch)]) \end{aligned}$$

- $\{i, r, ni, sk(i), pk(i), sk(r)\}$  is the *initial knowledge* of the role  $i$ ,
- $s = [send_1(\dots), \dots, claim_4(\dots)]$  is the sequence of events that are executed by  $i$  during a protocol session.

# Protocol specification

Let  $P$  be a protocol and  $R$  a role in  $P$ .

The specification of the role  $R$  in  $P$ , denoted  $P(R)$ , is a pair from  $\mathcal{P}(\text{RoleTerm}) \times \text{RoleEvent}_R^*$ .

**Example:** The roles  $i$  and  $r$  of NSPK are specified as follows:

$$\begin{aligned} NS(i) = & (\{i, r, ni, sk(i), pk(i), pk(r)\}, & NS(r) = & (\{i, r, nr, sk(r), pk(r), pk(i)\}, \\ & [send_1(i, r, \{\{ ni, i \}_{pk(r)}\}), & & [recv_1(i, r, \{\{ W, i \}_{pk(r)}\}), \\ & recv_2(r, i, \{\{ ni, V \}_{pk(i)}\}), & & send_2(r, i, \{\{ W, nr \}_{pk(i)}\}), \\ & send_3(i, r, \{\{ V \}_{pk(r)}\}), & & recv_3(i, r, \{\{ nr \}_{pk(r)}\}), \\ & claim_4(i, synch))] & & claim_5(r, synch))] \end{aligned}$$

Thank you!

- Cremers, C. J. F. (2006). Scyther : semantics and verification of security protocols Eindhoven: Technische Universiteit Eindhoven DOI: 10.6100/IR614943
- Cremers C. and Mauw S. Operational Semantics and Verification of Security Protocols. Springer, 2012.