

Homework 2 - Advanced LP & Network Flow Models

Adv. Analytics and Metaheuristics

Daniel Carpenter and Christopher Ferguson

February 2022

Contents

1 - Problem 1	2
1.1 Problems a and b	2
1.2 Model Assumptions and Overview	2
1.3 Mathematical Formulation	3
1.4 Code and Output	5
1.5 Problems 1 c (ii-vii)	6
1.6 Problems 1 d	7
2 - Problem 2	10
2.1 Model Overview	10
2.2 Mathematical Formulation	10
2.3 Code and Output	11
3 - Problem 3	12
3.1 Model Overview	12
3.2 Mathematical Formulation	13
3.3 Code and Output	14
4 - Problem 4	16
4.1 Model Overview	16
4.2 Mathematical Formulation	18
4.3 Code and Output	19

1 - Problem 1

1.1 Problems a and b

- Below shows how we get to the answer of Problems a and b

Problem 1 (a): Calculating the Upper Bound for the Raisin Product

Total Raisins Calculated	1,240,000	
Less Raisin Dedicated Portion to Grade A	(930,000)	75% <- note this is the % towards A
Grade B Portion Implied*	310,000	25% <- "" B
Total Grade B Available	5,270,000	
% Grade B Used Towards Raisins, i.e. tier 8	5.88%	

Interpretation and Assumptions:

*There must be 5.88% (Total of 310,000) of grade B's total supply that are on tier 8, which raisins are able to use since it satisfies the minimum points.

For raisins, this implies that 25% of the raisin production will stem from Grade B (and 75% towards A)

For juice, this implies that 75% of the juice production will stem from Grade B (and 25% towards A)

Note 100% Grade B used for Jelly.

Problem 1(b): Calculate the Fruit Cost seen in Table 3

Grade	Cost per Pound	
Grade A	\$ 0.45	<- noted in table 3 bullet 4
Grade B	\$ 0.25	

	Raisins	Juice	Jelly	
Pounds per Product	6.5	14.0	18.0	<- Noted in Table 2 footer

% Breakdown of Grades				
Grade A	75.0%	25.0%	0.0%	<- this is from the aboves assumptions text
Grade B	25.0%	75.0%	100.0%	<- 1 minus above
Weighted Avg. Cost per Pound	\$ 0.40	\$ 0.30	\$ 0.25	
Fruit Cost (Pounds * Wt. Avg. Cost)	\$ 2.60	\$ 4.20	\$ 4.50	<- this is how they determine the fruit cost in Table 3

1.2 Model Assumptions and Overview

- This model calculates the maximum profit using varying models from the boards, for a set of products and inputs grades (See below sets).

1.3 Mathematical Formulation

1.3.1 Sets

Set Name	Description
<i>FRUIT</i>	Fruit grade levels of grapes, which are Grade A and Grade B grapes
<i>PRODUCTS</i>	Types of products to be sold, which are Raisins , Juice , and Jelly

1.3.2 Parameters

Parameter Name	Description
$amountOfFruit_f$	<i>Pounds</i> of fruit grade ($f \in FRUIT$) available to use
$avgGradeOfFruit_f$	Avg. point quality of fruit grade ($f \in FRUIT$)
$productLimit_p$	Upper bound of number of products ($p \in PRODUCTS$) to produce
$poundsPerProduct_p$	The amount of pounds associated with a single unit of product ($p \in PRODUCTS$)
$contrToProfit_p$	The contribution to profit of product ($p \in PRODUCTS$)
$netProfit_p$	The net profit (<i>net of OH allocation</i>) of product ($p \in PRODUCTS$)
$productGradeLimit_p$	Requirement of mean point quality of a product ($p \in PRODUCTS$)

1.3.3 Decision Variables

Variable Name	Description
$produce_{f,p}$	Number (<i>as integer</i>) of products ($p \in PRODUCTS$) to be produced by fruit grade ($f \in FRUIT$)

1.3.4 Objective Function

$$\text{Maximize Net_Profit : } \sum_{f \in FRUIT, p \in PRODUCTS} produce_{f,p} \times netProfit_p$$

1.3.5 Constraints

C1: For each fruit grade ($f \in FRUIT$), the number of products produced ($p \in PRODUCTS$) must be equal to numbers of fruit provided

$$maxWeight : \sum_{p \in PRODUCTS} (produce_{f,p} \times numbersPerProduct_p) = amountOfFruit_f, \forall f \in FRUIT$$

C2: For each product produced ($p \in PRODUCTS$), limit the number of products p produced to \leq to the demanded (product numbers)

$$demand : \sum_{f \in FRUIT} produce_{f,p} \leq productLimit_p, \forall p \in PRODUCTS$$

C3: For each product ($p \in PRODUCTS$), the grade of fruit ($f \in FRUIT$) is greater than the minimum required grade of the product ($p \in PRODUCTS$).

minAvgGrade :

$$\sum_{f \in FRUIT} (produce_{f,p} \times avgGradeOfFruit_f) \geq productGradeLimit_p \times \sum_{f \in FRUIT} (produce_{f,p}),$$

$$\forall p \in PRODUCTS$$

C4: Non-negativity constraints

$$produce_{f,p} \geq 0, \forall f \in FRUIT, \forall p \in PRODUCTS$$

1.4 Code and Output

1.4.1 Code

```

group12_HW2_plmod.m X
C:\Users\danielcarpenter> OneDrive - The Chickasaw Nation\Documents\GITHUB\OU-DSA\Metaheuristics\03-Homework\HW02\AMPLModels\group12_1
7
8 # Reset globals
9 options solver cplex; # Using cplex for simplex alg
10
11 # SETS =====
12 set FRUIT circular; # Circular to index the kth element for constraint 2
13 set PRODUCTS circular; # ""
14
15 # PARAMETERS =====
16 param amountOffruit {FRUIT} >= 0; # Pounds of fruit available by grade
17 param avgGradeOffruit {FRUIT}; # Avg fruit grade
18 param productLimit {PRODUCTS} >= 0; # Demand for products
19 param poundsPerProduct {PRODUCTS}; # Pounds associated with a product
20 param contrToProfit {PRODUCTS}; # Product contribution to profit
21 param netProfit {PRODUCTS}; # Net profit per product
22 param productGradeLimit {PRODUCTS}; # The min grade for each product
23
24 # DECISION VARIABLES =====
25 # Include upper and lower bounds
26 var produce {f in FRUIT, p in PRODUCTS} >= 0 integer;
27 # var grade {p in PRODUCTS} >= 0, <= 10;
28
29 # OBJECTIVE FUNCTION =====
30 maximize Total_Profit:
31 sum {f in FRUIT, p in PRODUCTS} produce[f,p] * netProfit[p];
32
33 # CONSTRAINTS =====
34
35 ## C1: Number of pounds of the products produced (p in PRODUCTS) must be <= pounds of fruit
36 ## provided (f in FRUIT)
37 subject to maxWeight {f in FRUIT}:
38 sum {p in PRODUCTS} produce[f,p] * poundsPerProduct[p] == amountOffruit[f];
39
40 ## C2: Limit the number of products to <= the demand
41 subject to demand {p in PRODUCTS}:
42 sum {f in FRUIT} produce[f,p] <= productLimit[p];
43
44 ## C3: For all products (p in PRODUCTS), the weighted-average grade of fruit is greater than the
45 ## minimum required grade
46 subject to minAvgGrade {p in PRODUCTS}:
47 sum {f in FRUIT} produce[f,p] * avgGradeOffruit[f]
48 >= productGradeLimit[p] * (sum {f in FRUIT} produce[f,p]);
49
50 # CONTROLS =====
51 data group12_HW2_pl.dat;
52 solve;
53
54 print;
55 print "At maximum profit, the number of products to produce (by fruit grade)";
56 display produce;
57
group12_HW2_plmod.m X
C:\Users\danielcarpenter> OneDrive - The Chickasaw Nation\Documents\GITHUB\OU-DSA\Metaheuristics\03-Homework\HW02\AMPLModels\group12_1
4
5 # February, 2022
6
7 # Problem 1
8
9 # SETS =====
10 # Fruit grade levels of grapes, which are 'Grade A' and 'Grade B' grapes
11 set FRUIT := gradeA gradeB;
12 # Types of products to be sold, which are 'Raisins', 'Juice', and 'Jelly'
13 set PRODUCTS := raisins juice jelly;
14
15 # PARAMETERS =====
16 # Tons of fruit grade (f in FRUIT) available to use
17 param amountOffruit :=
18 gradeA 930000
19 gradeB 527000;
20
21 # Avg. point quality of fruit grade (f in FRUIT)
22 param avgGradeOffruit :=
23 gradeA 9
24 gradeB 5;
25
26 # Upper bound of production "tons" of product (p in PRODUCTS)
27 param productLimit :=
28 raisins INFINITY
29 juice 190000
30 jelly 210000;
31
32 # The amount of pounds associated with a single unit of product (p in PRODUCTS)
33 param poundsPerProduct :=
34 raisins 6.5
35 juice 14
36 jelly 18;
37
38 # The contribution to profit of a product (p in PRODUCTS)
39 param contrToProfit :=
40 raisins 1.40
41 juice 2.46
42 jelly 2.35;
43
44 # The net profit (net of OH allocation) of a product (p in PRODUCTS) per "ton"
45 param netProfit :=
46 raisins 0.35
47 juice -0.14
48 jelly 0.43;
49
50 # Requirement of mean point quality of a product (p in PRODUCTS)
51 param productGradeLimit :=
52 raisins 8
53 juice 6
54 jelly 0
55

```

1.4.2 Output

CPLEX 20.1.0.0: optimal integer solution within mipgap or absmipgap; objective 107593.36
 14 MIP simplex iterations
 0 branch-and-bound nodes
 absmipgap = 2.60826, relmipgap = 2.42418e-05

At maximum profit, the number of products to produce (by fruit grade):

```

produce :=
gradeA raisins    74996
gradeA juice      31609
gradeA jelly       0
gradeB raisins    24988
gradeB juice      94827
gradeB jelly     210000
;

```

Optimal profit is \$107,600. 74,996 Raisins produced using Grade A, 24,988 of Grade B, and so on for each product. See validation of the weighted-average point constraint below.

		Grade A	Grade B		
Avg Grade of Fruit		9	5		
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799,872 TRUE
Jelly	-	210,000	18	758,616	>= 758,616 TRUE
Total per Grade	930,000	5,270,000		1,050,000	>= - TRUE
Product	Grade A	Grade B	Pounds per Product	Equation using the produce var	
Raisin	74,996	24,988	7	LHS	RHS
Juice	31,609	94,827	14	799,904	>= 799

1.5 Problems 1 c (ii-vii)

i.

```
CPLEX 20.1.0.0: optimal integer solution within mipgap or absmipgap; obje
14 MIP simplex iterations
0 branch-and-bound nodes
absmipgap = 2.60826, relmipgap = 2.42418e-05
```

At maximum profit, the number of products to produce (by fruit grade):

```
produce :=
gradeA raisins    74996
gradeA juice      31609
gradeA jelly       0
gradeB raisins    24988
gradeB juice      94827
gradeB jelly      210000
;
```

Product total = (Amount of Grade A product + Amount of Grade B product) Raisins -

74996 + 24988 = 99984 Raisins

Juice - 31609 + 94827 = 126436 Juice

Jelly - 0 + 210000 = 210000 Jelly

ii. Max contribution of profit = Sum of all products (Product total * contribution to profit of product)

Raisins - 99984 * 1.40 = \$139977.60

+ Juice - 126436 * 2.46 = \$311032.56

+ Jelly - 210000 * 2.35 = \$493500

= Total - \$944510.16

The maximum contribution to profit will be \$944510.16

iii. Grade A grapes left over = Total Grade A - sum of Grade A grapes in products:

930000 - ((74996 * 6.5) + (31609 * 14) + 0) = 0

Grade B grapes left over = Total Grade B - sum of Grade B grapes in products:

5270000 - ((24988 * 6.5) + (94827 * 14) + (210000 * 18)) = 0

There are no grapes left over according to the optimal solution.

iv. Product total points = (# of Grade A in Product * 9 + # of Grade B * 5) / Total Product

Raisins - (74996 * 9 + 24988 * 5) / (99984) = 8

Juice - (31609 * 9 + 94827 * 5) / (126436) = 6

Jelly - (0 * 9 + 210000 * 5) / (210000) = 5

v.

```

ampl: option display_precision 8;
ampl: display Total_Profit;
Total_Profit = 107592.52

ampl: reset;
ampl: model group12_HW2_p1.mod;
CPLEX 20.1.0.0: optimal integer solution
14 MIP simplex iterations
0 branch-and-bound nodes
absmipgap = 2.60826, relmipgap = 2.42

At maximum profit, the number of products to
produce :=
gradeA raisins      74996
gradeA juice        31609
gradeA jelly         0
gradeB raisins      24988
gradeB juice        94827
gradeB jelly       210000
;

ampl: option display_precision 8;
ampl: display Total_Profit;
Total_Profit = 107593.36

ampl:

```

(option display_precision 8): puts the answer in decimal using 8 digits

(Total profit of model + 1 additional pound of Grade A grapes) - (Total profit of original)
 $107592.52 - 107593.36 = .16$

vi. No, they should not buy the additional 300,000 pounds of A-grade grapes at .50 per pound.

vii. The maximum price that Grapes of Wrath should pay for an extra pound of A-grade product would be .16.

The maximum price that Grapes of Wrath should pay for an extra pound of B-grade product would be 2.96. Our model will not show the upper bound on the price per product that can serve the model.

(Total profit of model + 1 additional pound of Grade B grapes) - (Total profit of original)
 $107596.28 - 107593.36 = 2.92$

1.6 Problems 1 d

i. The product mix that would be made by using Thomas's contribution figures are

gradeA raisins 40760

gradeA juice 47503

gradeA jelly 1

gradeB raisins 13582

gradeB juice 142496

gradeB jelly 177043

Thomas's profit contribution is \$959,529.74 The maximum that they should pay for an additional pound of A-grade grapes is .16.

ii.

```

# group12_HW2.plt.mod M.X
C:\Users\daniel.carpenter\OneDrive - the Chickasaw Nation\Documents\GitHub\OU-DA\Mathematics\DS - Homework\HW02\group12_HW2.plt.mod
1 | # Homework 2: Demand and Revenue Flow Models
2 | # Adv. Analytics and Metaheuristics
3 | # Daniel Carpenter and Christopher Ferguson
4 | # February 2022
5 | # Problem 1
6 |
7 | reset; # Reset globals
8 | options solver cplex; # Using cplex for simplex alg
9 |
10 | # SETS =====
11 | set FRUIT circular; # Circular to index the RHS element for constraint 2
12 | set PRODUCTS circular; # ""
13 |
14 | # PARAMETERS =====
15 | param amountOffruit {FRUIT} >= 0; # Pounds of fruit available by grade
16 | param avgGradeOffruit {FRUIT}; # Avg fruit grade
17 | param productLimit {PRODUCTS} >= 0; # Demand for products
18 | param poundsPerProduct {PRODUCTS}; # Pounds associated with a product
19 | param contrToProfit {PRODUCTS}; # Product contribution to profit
20 | param netProfit {PRODUCTS}; # Net profit per product
21 | param productGradeLimit {PRODUCTS}; # The min grade for each product
22 | param sellingPrice {PRODUCTS}; # Selling price of each product
23 | param contrToProfit3 {PRODUCTS}; # Product contribution to profit from Table 3
24 | param marginalProfit3 {PRODUCTS}; # Marginal profit from Table 3
25 |
26 | # DECISION VARIABLES =====
27 | var produce {f in FRUIT, p in PRODUCTS} >= 0 integer;
28 |
29 | # OBJECTIVE FUNCTION =====
30 | maximize Total_Profit:
31 |   sum (f in FRUIT, p in PRODUCTS) produce(f, p) * contrToProfit3(p);
32 |
33 | # CONSTRAINTS =====
34 | # C1: Number of pounds of the products produced (p in PRODUCTS) must be <= pounds of fruit provided (f in FRUIT)
35 | subject to maxWeight (f in FRUIT):
36 |   (sum (p in PRODUCTS) produce(f, p) * poundsPerProduct(p)) <= amountOffruit(f);
37 |
38 | # C2: Limit the number of products to <= the demand
39 | subject to demand (p in PRODUCTS):
40 |   (sum (f in FRUIT) produce(f, p)) <= productLimit(p);
41 |
42 | # C3: For all products (p in PRODUCTS), the weighted-average grade of fruit is greater than the minimum required grade.
43 | subject to minAvgGrade (p in PRODUCTS):
44 |   (sum (f in FRUIT) produce(f, p) * avgGradeOffruit(f))
45 |   >= productGradeLimit(p) * (sum (f in FRUIT) produce(f, p));
46 |
47 | # CONTROLS =====
48 | data group12_HW2.plt.dat;
49 | solve;
50 |
51 | print "At maximum profit, the number of products to produce (by fruit grade).";
52 | display produce;
53 | ndisplay maxweight;
54 | display minAvgGrade;
55 | ndisplay demand;
56 |
57 |
58 |
59 |
60 |
61 |
62 |
63 |
64 |
65 |
66 |
67 |
68 |
69 |
70 |
71 |
72 |
73 |
74 |
75 |
76 |
77 |
78 |
79 |
80 |
81 |
82 |
83 |
84 |
85 |
86 |
87 |
88 |
89 |
90 |
91 |
92 |
93 |
94 |
95 |
96 |
97 |
98 |
99 |
100 |

```

```

# group12_HW2.plt.dat M.X
C:\Users\daniel.carpenter\OneDrive - the Chickasaw Nation\Documents\GitHub\OU-DA\Mathematics\DS - Homework\HW02\group12_HW2.plt.dat
1 |
2 | # SETS =====
3 | # FRUIT grade levels of grapes, which are "grade A" and "grade B" grapes
4 | set FRUIT := gradeA gradeB;
5 | # Types of products to be sold, which are "Raisins", "Juice", and "Jelly"
6 | set PRODUCTS := raisins juice jelly;
7 |
8 | # PARAMETERS =====
9 | # Tons of fruit-grade (f in FRUIT) available to use
10 | param amountOffruit :=
11 |   gradeA 930000
12 |   gradeB 527000;
13 |
14 | # Avg. point quality of fruit grade (f in FRUIT)
15 | param avgGradeOffruit :=
16 |   gradeA 9
17 |   gradeB 5;
18 |
19 | # Upper bound of production "tons" of product (p in PRODUCTS)
20 | param productLimit :=
21 |   raisins 1000000
22 |   juice 100000
23 |   jelly 210000;
24 |
25 | # The amount of pounds associated with a single unit of product (p in PRODUCTS)
26 | param poundsPerProduct :=
27 |   raisins 6.5
28 |   juice 14
29 |   jelly 18;
30 |
31 | # The contribution to profit of a product (p in PRODUCTS)
32 | param contrToProfit :=
33 |   raisins 1.40
34 |   juice 2.44
35 |   jelly 2.35;
36 |
37 | # The net profit (net of an allocation) of a product (p in PRODUCTS) per "ton"
38 | param netProfit :=
39 |   raisins 0.35
40 |   juice -0.14
41 |   jelly 0.43;
42 |
43 | # Requirement of mean point quality of a product (p in PRODUCTS)
44 | param productGradeLimit :=
45 |   raisins 8
46 |   juice 6
47 |   jelly 0;
48 |
49 | # Selling price of each product
50 | param sellingPrice :=
51 |   raisins 8.39
52 |   juice 16.28
53 |   jelly 13.89;
54 |
55 | # Contribution to profit from Table 3
56 | param contrToProfit3 :=
57 |   raisins 3.52
58 |   juice 6.38
59 |   jelly 7.39;
60 |
61 | # Marginal Profit from Table 3
62 | # M3: Data
63 | param marginalProfit3 :=
64 |   raisins 0.62
65 |   juice 2.18
66 |   jelly 3.05;
67 |
68 |
69 |
70 |
71 |
72 |
73 |
74 |
75 |
76 |
77 |
78 |
79 |
80 |
81 |
82 |
83 |
84 |
85 |
86 |
87 |
88 |
89 |
90 |
91 |
92 |
93 |
94 |
95 |
96 |
97 |
98 |
99 |
100 |

```

1.6.1 Output

```

ampl: model 'C:\Users\daniel.carpenter\OneDrive - the Chickasaw Nation\Documents\GitHub\OU-DA\Mathematics\DS - Homework\HW02\group12_HW2.plt.mod';
CPLEX 20.1.0.0: optimal integer solution within mipgap or absmipgap; objective 2695531.61
6 MIP simplex iterations
0 branch-and-bound nodes
absmipgap = 4.89857, relmipgap = 1.81729e-06

```

At maximum profit, the number of products to produce (by fruit grade):

```

produce :=
gradeA raisins 40780
gradeA juice 47495
gradeA jelly 0
gradeB raisins 13592
gradeB juice 142481
gradeB jelly 177051
;

```

```

minAvgGrade [*] :=
raisins 0
juice 0
jelly 0
;
ampl:

```

- The maximum to pay per pound would be equal to the dual variable of the active constraint, which does not show any values.

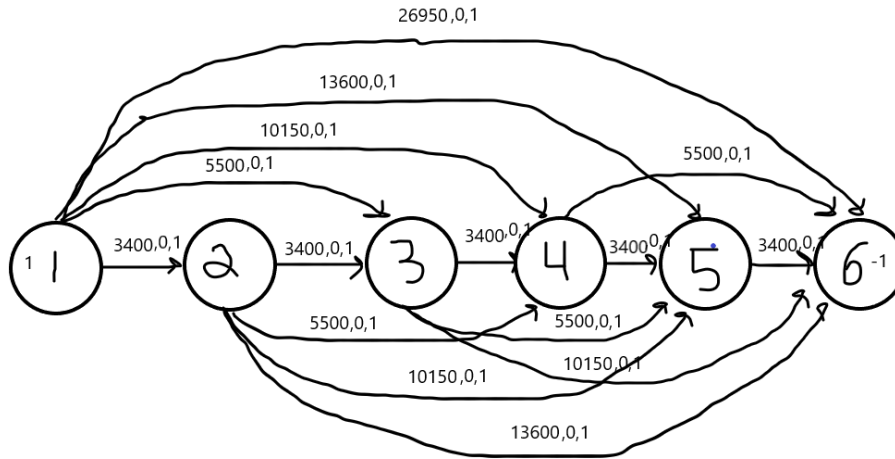
iii.

1.6.2 Code

- The model who should be used is Thomas' method, which yields the highest profit. An enhancement would be to be only compare net profit or contribution margins.

2 - Problem 2

2.1 Model Overview



2.2 Mathematical Formulation

NODES: Set of all nodes in above network flow diagram resembling a time period.

The set A is a set of *arcs*, e.g. (i, j) for $i \in N, j \in N$
each of which may carry *flow of a commodity*

Decision variable: x_{ij} determines the units of flow on arc (i, j)

Arc (i, j)

- cost c_{ij} per unit of flow on arc (i, j)
- upper bound on flow of u_{ij} (capacity)
- lower bound on flow of ℓ_{ij} (usually 0)

2.2.1 Objective, and Constraints

$$\begin{aligned}
 &\text{minimize} \quad \sum_{(i,j) \in A} c_{ij} x_{ij} \\
 &\text{subject to} \quad \sum_{j: (i,j) \in A} x_{ij} - \sum_{j: (j,i) \in A} x_{ji} = b_i \quad \forall i \in N \\
 &\quad \quad \quad l_{ij} \leq x_{ij} \leq u_{ij} \quad \forall (i, j) \in A
 \end{aligned}$$

2.3 Code and Output

2.3.1 Model group12_HW2_p2.mod

- Used mcnpf.txt from course website and renamed to group12_HW2_p2.mod.
- Added data group12_HW2_p2.dat; solve; and display x;

2.3.2 Data group12_HW2_p2.dat

```
#use with MCNFP.txt model
#note: default arc costs and lower bounds are 0
#      default arc upper bounds are infinity
#      default node requirements are 0

set NODES := 1 2 3 4 5 6; #nodes for problem #2

set ARCS := (1,2) (1,3) (1,4) (1,5) (1,6) (2,3) (2,4) (2,5) (2,6) (3,4) (3,5) (3,6) (4,5) (4,6) (5,6); #arcs for problem #2

param b:= 1 1 #for shortest path problem, start node supply = 1
          6 -1; #and the destination node supply = -1

#note: to make things a little more compact, you can use a "template"
# for setting up costs. See Chapter 9 "Specifying Data" in the AMPL textbook

#for example, the first line below: [1, *] 2 5 3 10
#is short hand for: [1, 2] 5 [1,3] 10

#this comes in handy for some larger, more complex data files.

param c:= [1, *] 2 3400 3 5550 4 10150 5 13600 6 26950 #arc cost equals the distance
          [2, *] 3 3400 4 5550 5 10150 6 13600
          [3, *] 4 3400 5 5550 6 10150
          [4, *] 5 3400 6 5550
          [5, *] 6 3400;
```

2.3.3 Output

- The lowest total cost over the 5 years will be \$14,500 by traveling from nodes (1,2), (2,4), (4,6).

```
AMPL
ampl: model HW2Q2.mod;
CPLEX 20.1.0.0: optimal solution; objec
2 dual simplex iterations (0 in phase I
cost = 14500

x :=
1 2 1
1 3 0
1 4 0
1 5 0
1 6 0
2 3 0
2 4 1
2 5 0
2 6 0
3 4 0
3 5 0
3 6 0
4 5 0
4 6 1
5 6 0
.
```

3 - Problem 3

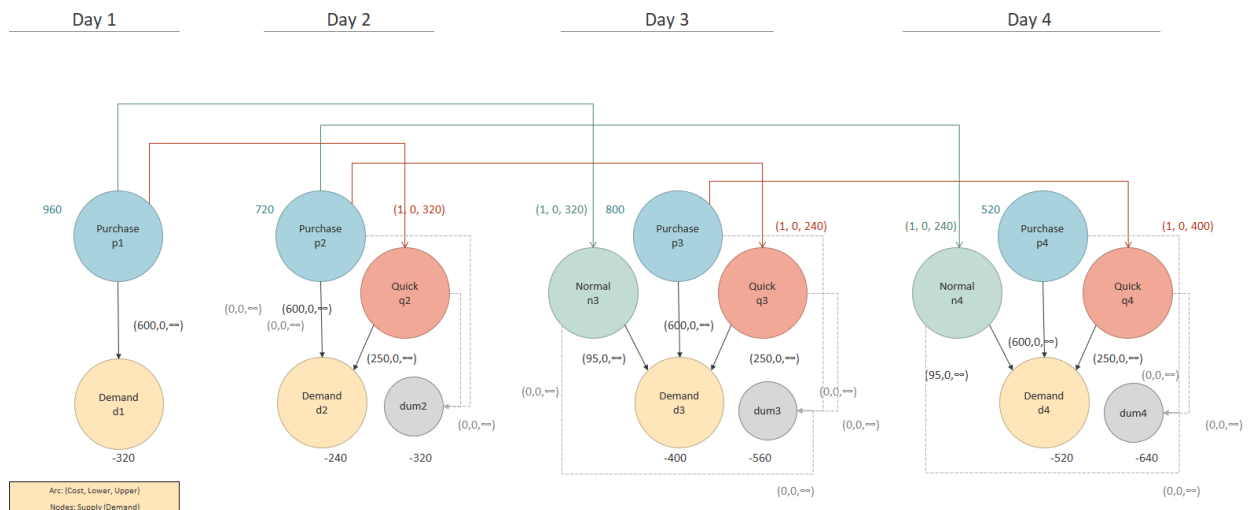
3.1 Model Overview

3.1.1 Assumptions and Calculations for Network Flow Diagram

- Below shows how we decided to balance the network with supply and dummy nodes
- In order to obtain a balanced network (i.e. supply equals demand), we must allow for all possible routes to have enough supply.
- Excess supply allowed on certain days is captured by dummy nodes so that the business does not actually produce the tires.

Determine Supply and Dummy Allocation					
Day	Demand (d)	Incoming Arcs (in)	Potential Supply $in * d$	Dummy Allocation $d_{day-1} + d_{day-2}$	
1	-320	3	960	0	
2	-240	3	720	-320	
3	-400	2	800	-560	
4	-520	1	520	-640	

3.1.2 Network Flow Diagram



3.2 Mathematical Formulation

3.2.1 Sets, Parameters, Decision Vars

Set Name	Description
<i>NODES</i>	Set of all nodes in above network flow diagram:
p1 p2 p3 p4	Number of tires to <i>purchase</i> on day $\in(1-4)$
n1 n2 n3 n4	Number of tires to reshape using the <i>normal</i> service on day $\in(1-4)$
q1 q2 q3 q4	Number of tires to reshape using the <i>quick</i> service on day $\in(1-4)$
d1 d2 d3 d4	Demand of tires on each day $\in(1-4)$
dum2 dum3 dum4	Dummy nodes to balance excess supply for days 2 3 and 4 $\in(2-4)$. Do not need one for day 1 since purchasing

The set A is a set of *arcs*, e.g. (i, j) for $i \in N, j \in N$ each of which may carry *flow of a commodity*

Decision variable: x_{ij} determines the units of flow on arc (i, j)

Arc (i, j)

- cost c_{ij} per unit of flow on arc (i, j)
- upper bound on flow of u_{ij} (capacity)
- lower bound on flow of ℓ_{ij} (usually 0)

3.2.2 Objective, and Constraints

$$\begin{aligned}
 &\text{minimize} && \sum_{(i,j) \in A} c_{ij} x_{ij} \\
 &\text{subject to} && \sum_{j:(i,j) \in A} x_{ij} - \sum_{j:(j,i) \in A} x_{ji} = b_i \quad \forall i \in N \\
 &&& \ell_{ij} \leq x_{ij} \leq u_{ij} \quad \forall (i, j) \in A
 \end{aligned}$$

- Upper and lower bounds use to direct the flow of tires from *purchasing* to *quick* or *normal* service

3.3 Code and Output

3.3.1 Model: group12_HW2_p3.mod

- Used mcnpf.txt from course website and renamed to group12_HW2_p3.mod.
- Added data group12_HW2_p3.dat; solve; and display x;

3.3.2 Data: group12_HW2_p3.dat

```
5 # Problem 4
6
7 data;
8
9 # Set of Nodes for each day (1,2,3,4)
10 set NODES := p1 p2 p3 p4 # Purchases
11             n1 n2 n3 n4 # Normal Service
12             q1 q2 q3 q4 # Quick Service
13             d1 d2 d3 d4 # Demand
14             dum2 dum3 dum4 # Dummy for days 2 3 and 4
15 ;
16
17 # Set of ARCS from Node i to Node j
18 set ARCS :=
19             (p1, *) d1 q2 n3
20             (p2, *) d2 q3 n4 dum2
21             (p3, *) d3 q4 dum3
22             (p4, dum4)
23             (q2, *) d2 dum2
24             (q3, *) d3 dum3
25             (q4, *) d4 dum4
26             (n3, *) d3 dum3
27             (n4, *) d4 dum4
28 ;
29
30 # Number of Products demanded
31 param b :=
32     # "Supply" nodes. Not actually supply but needs to have origin
33     p1 960
34     p2 720
35     p3 800
36     p4 520
37
38     # Transshipment
39     n1 0 n2 0 n3 0 n4 0
40     q1 0 q2 0 q3 0 q4 0
41
42     # Dummy Nodes to take excess supply
43     dum2 -320 # Dif between d2 and p2
44     dum3 -560 # ""3
45     dum4 -640
46
47     # Demand nodes
48     d1 -320
49     d2 -240
50     d3 -400
51     d4 -520
52 ;
53
```

Data Continued:

```

54 # The cost (c), lower (l), and upper (u), from node i to j in IN NODES
55 param:      c      l      u :=
56     [p1, d1] 600    .    .
57     [p2, d2] 600    .    .
58     [p3, d3] 600    .    .
59     [q2, d2] 250    .    .
60     [q3, d3] 250    .    .
61     [q4, d4] 250    .    .
62     [n3, d3] 95     .    .
63     [n4, d4] 95     .    .
64     [p1, q2] 1      .    320
65     [p1, n3] 1      .    320
66     [p2, q3] 1      .    240
67     [p2, n4] 1      .    240
68     [p3, q4] 1      .    400
69     [p2, dum2] 0     .    .
70     [p3, dum3] 0     .    .
71     [p4, dum4] 0     .    .
72     [q2, dum2] 0     .    .
73     [q3, dum3] 0     .    .
74     [q4, dum4] 0     .    .
75     [n3, dum3] 0     .    .
76     [n4, dum4] 0     .    .
77 ;
78

```

3.3.3 Output

- Total minimized cost: 396,720
- Interpretation of the tires purchased on each day:
 1. 320 tires purchased
 2. 240 tires reshaped with Quick Service from previous day
 3. 80 Reshaped with quick service from previous day. 320 tires used from reshaping via Normal service from day 1.
 4. 280 Reshaped with quick service from previous day. 240 tires used from reshaping via Normal service from day 2.

```

ampl: model 'C:\Users\daniel.carpenter\OneDrive - the Chickasaw Na
CPLEX 20.1.0.0: optimal solution; objective 396720
1 dual simplex iterations (0 in phase I)
x [*,*] (tr)
:      n3      n4      p1      p2      p3      p4      q2      q3      q4      :=
d1      .      .      320      .      .      .      .      .      .
d2      .      .      .      0      .      .      240      .      .
d3      320      .      .      .      0      .      .      80      .
d4      .      240      .      .      .      .      .      .      280
dum2      .      .      .      240      .      .      80      .      .
dum3      0      .      .      .      400      .      160      .      .
dum4      .      0      .      .      .      520      .      .      120
n3      .      .      320      .      .      .      .      .      .
n4      .      .      .      240      .      .      .      .      .
q2      .      .      320      .      .      .      .      .      .
q3      .      .      .      240      .      .      .      .      .
q4      .      .      .      .      400      .      .      .      .
;

```

4 - Problem 4

4.1 Model Overview

4.1.1 Assumptions and Calculations for Network Flow Diagram

- Goal of below tables are to put all data on a *per unit of product* basis
- Need to be on per unit basis so that we can effectively minimize the cost
- *Color of tables* correspond to the network nodes on the next page

Labor, Manufacturing, and Transportation Cost Calculations for Arcs

Labor (Cost per Unit Output and Total Supply Available)					
Type	Cost per Person	Unit Output per Person	Cost / Unit	Total Labor Avail	TTL Product Supply
Specialist	\$ 2,000	12	\$ 166.67	100	1,200
Generalist	\$ 1,700	10	\$ 170.00	200	2,000

Cost of Transportation			
	Scranton, PA	Utica, NY	Stamford, CT
Per Person	300	250	275
Per Unit of Product (trans. Cost / unit output by type)			
Specialist	\$ 25.00	\$ 20.83	\$ 22.92
Generalist	\$ 30.00	\$ 25.00	\$ 27.50

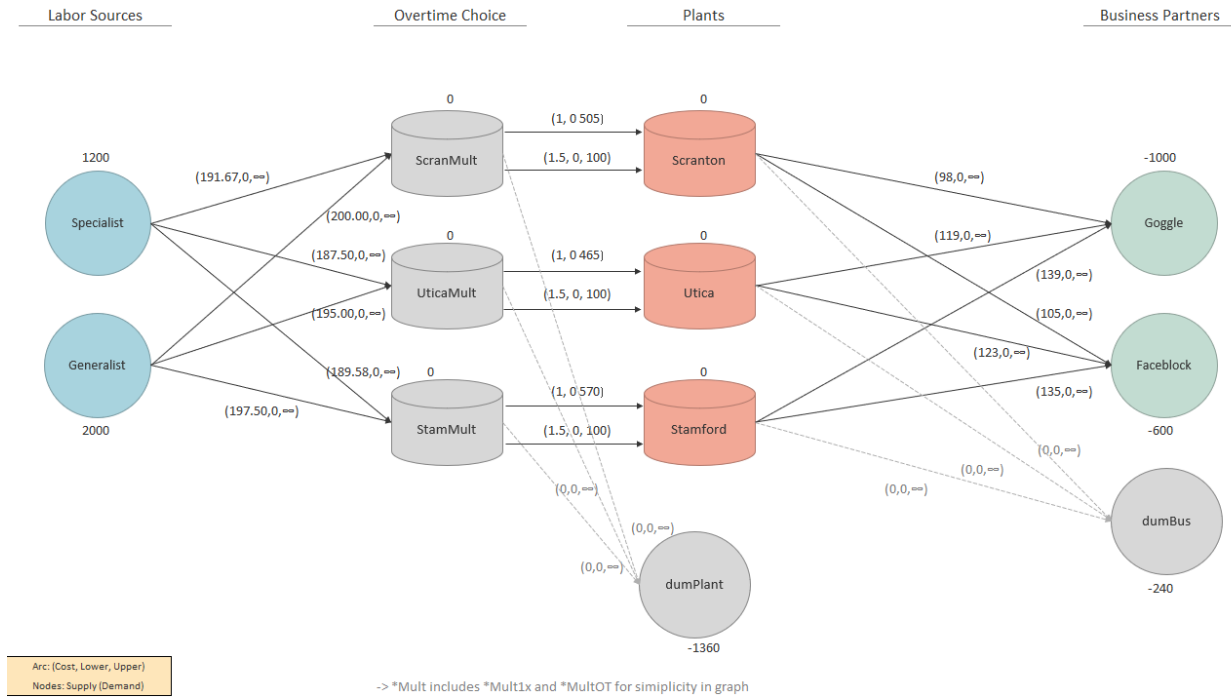
Cost of Transportation + Labor per Unit of Output			
	Scranton, PA	Utica, NY	Stamford, CT
Specialist	\$ 191.67	\$ 187.50	\$ 189.58
Generalist	\$ 200.00	\$ 195.00	\$ 197.50

Plant Production Limits			
	Base	OT	OT Mult
Scranton	505	100	1.5
Utica	465	100	1.5
Stamford	570	100	1.5

Manufacturing and Transportation Costs			
	Manufacture	Goggle	Faceblock
Scranton	\$ 90	\$ 8	\$ 15
Utica	\$ 105	\$ 14	\$ 18
Stamford	\$ 115	\$ 24	\$ 20

Man. + Trans Cost	
Goggle	Faceblock
\$ 98	\$ 105
\$ 119	\$ 123
\$ 139	\$ 135

4.1.2 Network Flow Diagram



4.2 Mathematical Formulation

4.2.1 Sets, Parameters, Decision Vars

Set Name	Description
<i>NODES</i>	Set of all nodes in above network flow diagram:
Specialist, Generalist	The two types of Supply of Labor
ScranMult1x, UticaMult1x, StamMult1x	Passed through if <i>did not</i> use overtime
ScranMultOT, UticaMultOT, StamMultOT	Passed through if <i>did</i> use overtime
Scranton, Utica, Stamford	Transshipment nodes which are the plants
dumPlant, dumBus	Dummy nodes that account for excess supply from unbalanced supply from labor nodes

The set A is a set of *arcs*, e.g. (i, j) for $i \in N, j \in N$
each of which may carry *flow of a commodity*

Decision variable: x_{ij} determines the units of flow on arc (i, j)

Arc (i, j)

- cost c_{ij} per unit of flow on arc (i, j)
- upper bound on flow of u_{ij} (capacity)
- lower bound on flow of ℓ_{ij} (usually 0)

4.2.2 Objective, and Constraints

$$\begin{aligned}
 &\text{minimize} && \sum_{(i,j) \in A} c_{ij} x_{ij} \\
 &\text{subject to} && \sum_{j:(i,j) \in A} x_{ij} - \sum_{j:(j,i) \in A} x_{ji} = b_i \quad \forall i \in N \\
 &&& \ell_{ij} \leq x_{ij} \leq u_{ij} \quad \forall (i, j) \in A
 \end{aligned}$$

- Upper and lower bounds use to direct the flow of the product

4.3 Code and Output

4.3.1 Model: group12_HW2_p4.mod

- Used mcnpf.txt from course website and renamed to group12_HW2_p4.mod.
- Added data group12_HW2_p4.dat; solve; and display x;

4.3.2 Data: group12_HW2_p4.dat

```
group12_HW2_p4.mod M  group12_HW2_p4.dat M
C:\Users\daniel.carpenter> OneDrive - the Chickasaw Nation > Documents > GitHub > OU-DSA > Metaheuristics > 03 - Homework > HW 02 > AMPL Models > gr
1  # Homework 2 - Advanced LP & Network Flow Models
2  # Adv. Analytics and Metaheuristics
3  # Daniel Carpenter and Christopher Ferguson
4  # February 2022
5  # Problem 4
6
7  data;
8
9  # Set of Nodes containing all sources of Labor, Plants, and Business Partners
10 set NODES :=    Specialist Generalist          # Labor
11                ScrantMult1x UticaMult1x StamMult1x # Multiplier dumBus 1x no OT
12                ScrantMultOT UticaMultOT StamMultOT # Multiplier dumBus 1.5x for OT
13                dumPlant                          # Dummy to limit supply before plants
14                Scranton Utica Stamford          # Plants
15                Goggle Facebook dumBus           # Business Partners + dumBus for unbalanced supply/demand
16                ;
17
18 # Set of ARCS from Labor Sources, to Plants, to Business Partners
19 set ARCS :=
20     # No OT used
21     (Specialist, *) ScrantMult1x UticaMult1x StamMult1x
22     (Generalist, *) ScrantMult1x UticaMult1x StamMult1x
23     (ScrantMult1x, *) Scranton dumPlant
24     (UticaMult1x, *) Utica dumPlant
25     (StamMult1x, *) Stamford dumPlant
26
27     # If Use OT
28     (Specialist, *) ScrantMultOT UticaMultOT StamMultOT
29     (Generalist, *) ScrantMultOT UticaMultOT StamMultOT
30     (ScrantMultOT, *) Scranton dumPlant
31     (UticaMultOT, *) Utica dumPlant
32     (StamMultOT, *) Stamford dumPlant
33
34     # Plants to demanders and dumBus for unbalanced network
35     (Scranton, *) Goggle Facebook dumBus
36     (Utica, *) Goggle Facebook dumBus
37     (Stamford, *) Goggle Facebook dumBus
38     ;
39
40 # Number of Products demanded by Business Partner
41 param b :=
42     # Supply
43     Specialist 1200 # 12 units * 100 Labor hours
44     Generalist 2000 # 10 units * 200 Labor hours
45
46     # Transshipment (Plants or OT Multiplier)
47     ScrantMult1x 0 # Not using OT
48     UticaMult1x 0
49     StamMult1x 0
50     ScrantMultOT 0 # Using OT
51     UticaMultOT 0
52     StamMultOT 0
53     Scranton 0 # Plant Arrival
54     Utica 0
55     Stamford 0
56
```

Data Continued:

```

group12_HW2_p4.mod M  group12_HW2_p4.dat M
C: > Users > daniel.carpenter > OneDrive - the Chickasaw Nation > Documents > GitHub > OU-DSA > Metaheuristics > 03 - Homework > HW 02 > AMPL M
57      # Demand
58      dumPlant    -1360  # (505+465+570 + 3*100) - (1200+2000)
59      Goggle      -1000
60      Faceblock   -600
61      dumBus      -240  # (-1000-600) - (-1360)
62      ;
63
64      # The cost (c), lower (l), and upper (u), from node i to j in IN NODES
65      param:                c      l      u :=
66      # Cost of Transportation + Labor per Unit of Output (see screenshot)
67      # PATH **NOT** USING OT -----
68      [Specialist, ScrantMult1x] 191.67 . . # Supply -> Mult
69      [Specialist, UticaMult1x] 187.5 . .
70      [Specialist, StamMult1x] 189.58 . .
71      [Generalist, ScrantMult1x] 200 . .
72      [Generalist, UticaMult1x] 195 . .
73      [Generalist, StamMult1x] 197.5 . .
74      [ScrantMult1x, Scranton] 1 . 505 # Mult -> Plant
75      [UticaMult1x, Utica] 1 . 465
76      [StamMult1x, Stamford] 1 . 570
77      [ScrantMult1x, dumPlant] 0 . . # Mult -> Dummy
78      [UticaMult1x, dumPlant] 0 . .
79      [StamMult1x, dumPlant] 0 . .
80
81      # PATH USING OT -----
82      [Specialist, ScrantMultOT] 191.67 . . # Supply -> Mult
83      [Specialist, UticaMultOT] 187.5 . .
84      [Specialist, StamMultOT] 189.58 . .
85      [Generalist, ScrantMultOT] 200 . .
86      [Generalist, UticaMultOT] 195 . .
87      [Generalist, StamMultOT] 197.5 . .
88      [UticaMultOT, Utica] 1.5 . 100 # Mult -> Plant
89      [ScrantMultOT, Scranton] 1.5 . 100
90      [StamMultOT, Stamford] 1.5 . 100
91      [ScrantMultOT, dumPlant] 0 . . # Mult -> Dummy
92      [UticaMultOT, dumPlant] 0 . .
93      [StamMultOT, dumPlant] 0 . .
94
95      # Plant to Business Partners
96      [Scranton, Goggle] 98 . . # Plant -> Demanders
97      [Scranton, Faceblock] 105 . .
98      [Scranton, dumBus] 0 . .
99      [Utica, Goggle] 119 . .
100     [Utica, Faceblock] 123 . .
101     [Utica, dumBus] 0 . .
102     [Stamford, Goggle] 139 . .
103     [Stamford, Faceblock] 135 . .
104     [Stamford, dumBus] 0 . .
105     ;
106

```

4.3.3 Output

- Total minimized cost: \$806,192.95
- Scranton, Utica, and Stamford produce 0, 430, and 170 units of product for **Facebook**, respectively.
- Scranton, Utica, and Stamford produce 605, 0, and 395 units of product for **Goggle**, respectively.
- All possible products produced (using a portion of the available regular and overtime hours). 200 products produced by Specialists using OT, and 100 from generalists using OT.

```

ampl: model 'C:\Users\daniel.carpenter\OneDrive - the Chickasaw Nation\Documents\Githu
CPLEX 20.1.0.0: optimal solution; objective 806192.95
13 dual simplex iterations (0 in phase I)
x [*,*] (tr)
# $1 = Generalist
# $2 = ScranMult1x
# $3 = ScranMultOT
# $4 = Scranton
# $5 = Specialist
# $6 = StamMult1x
# $7 = StamMultOT
# $8 = Stamford
# $10 = UticaMult1x
# $11 = UticaMultOT
:
      $1      $2      $3      $4      $5      $6      $7      $8      Utica      $10      $11 :=
Facebook      .      .      .      0      .      .      .      430      170      .      .
Goggle      .      .      .      605      .      .      .      0      395      .      .
ScranMult1x      0      .      .      .      505      .      .      .      .      .      .
ScranMultOT      0      .      .      .      100      .      .      .      .      .      .
Scranton      .      505      100      .      .      .      .      .      .      .      .
StamMult1x      75      .      .      .      495      .      .      .      .      .      .
StamMultOT      0      .      .      .      100      .      .      .      .      .      .
Stamford      .      .      .      .      .      570      100      .      .      .      .
Utica      .      .      .      .      .      .      .      .      .      465      100
UticaMult1x      1825      .      .      .      0      .      .      .      .      .      .
UticaMultOT      100      .      .      .      0      .      .      .      .      .      .
dumBus      .      .      .      0      .      .      .      240      0      .      .
dumPlant      .      0      0      .      .      0      0      .      .      1360      0
;

```