Homework 3 - Integer Programming

Adv. Analytics and Metaheuristics

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1 - Problem 1

1.1 Mathematical Formulation

1.1.1 Sets

Set Name	Description
GENERATORS PERIODS	Set of generators i that can be used (A,B,C) 2 possible periods p (1, 2) in the production day

1.1.2 Parameters

Parameter Name	Description
$\overline{S_i}$	Fixed cost to start a generator
	$(i \in GENERATORS)$ in the entire day
F_i	Fixed cost to operate a generator
	$(i \in GENERATORS)$ in any period
C_i	Variable cost per megawatt to operator a
	generator $(i \in GENERATORS)$ in any
	period
U_i	Max. megawatts generated for generator
	$(i \in GENERATORS)$ in any period
$demand_p$	Total demanded megawatts for period
r	$(p \in PERIODS)$
M_i	Value to map watts used by each
	generator $(i \in GENERATORS)$

1.1.3 Decision Variables

Variable Name	Description
$watts_{i,p}$	Integer variable: Number of watts to
	produce per generator
	$(i \in GENERATORS)$ per period
	$(p \in PERIODS)$
$x_{i,p}$	Binary variable: 1 if a generator
	$(i \in GENERATORS)$ is in period p
	$(p \in PERIODS)$, 0 if not turned on at all
y_i	Binary variable: 1 if a generator
	$(i \in GENERATORS)$ is used, 0 if not
	turned on at all

1.1.4 Objective Function

$$minimize\ cost: \sum_{i \in GENERATORS} \left(\left(\sum_{p \in PERIODS} (watts_{i,p}) \times C_i \right) + \left(F_i \times \sum_{p \in PERIODS} x_{i,p} \right) + \left(S_i \times y_i \right) \right)$$

1.1.5 Constraints

C1: For each period, meet the demanded megawatts

$$requiredWatts: \sum_{i \in GENERATORS} (watts_{i,p}) = demand_p, \forall \ p \in PERIODS$$

C2: For each generator, don't surpass the allowable megawatts

upperBound:
$$\sum_{p \in PERIODS} (watts_{i,p}) \leq U_i, \forall i \in GENERATORS$$

C3: For each generator, map decision variables together to account for the fixed costs in a given day S_i

$$mapVars: \sum_{p \in PERIODS} (watts_{i,p}) \leq M_i \times y_i, \forall i \in GENERATORS$$

C4: For each generator and period, map decision variables y and watts together to account for the fixed costs in a per period p

$$mapVars2: watts_{i,p} \leq M_i \times x_{i,p}, \forall i \in GENERATORS, p \in PERIODS$$

1.2 Code and Output

1.2.1 Code

```
Fynich/Millians N

| Particle | Control | Cont
```

1.2.2 Output

```
ampl: model 'C:\Users\daniel.carpenter\OneDrive - the Chickasaw
CPLEX 20.1.0.0: optimal integer solution; objective 46100
7 MIP simplex iterations
0 branch-and-bound nodes

Which generators are used?
y [*] :=
A 1
B 1
C 1;

Which periods were the generators used?
x :=
A 1 0
A 2 1
B 1 0
B 2 1
C 1 1
C 2 0;

Optimal Amount of Megawatts for each generator and period:
watts :=
A 1 0
A 2 2100
B 1 0
B 2 1800
C 1 2900
C 2 0;
```

1.2.2.1 Analysis of the Output

- The minimized cost is \$46, 100
- Generator A, B, and C run
- Generator C runs in period 1. Generator A and B run in period 2
- Generator A produces 2, 100 megawatts in total
- Generator B produces 1,800 megawatts in total
- Generator C produces 2,900 megawatts in total

2 - Problem 2

2.1 Mathematical Formulation

2.1.1 Sets

Set Name	Description
PRODUCTS	5 types of landscaping and construction products (e.g., cement, sand, etc.) labeled product (p) A, B, C, D , and E
SILOS	8 different silos s that each product must be stored in $(1, 2,, 8)$

2.1.2 Parameters

Parameter Name	Description
$cost_{s,p}$	Cost of storing one ton of product $p \in PRODUCTS$ in silo $s \in SILOS$
$supply_p$	Total supply in tons available of product $p \in PRODUCTS$
$capacity_s$	Total capacity in tons of silo $s \in SILOS$. Can store products.

2.1.3 Decision Variables

Variable Name	Description
$tonsOfProduct_{p,s}$	Tons of product $p \in PRODUCTS$ to store in silo $s \in SILOS$
$isStored_{p,s}$	Binary variable indicating if product $p \in PRODUCTS$ is stored in silo $s \in SILOS$

2.1.4 Objective Function

2.1.5 Constraints

C1:

- 2.2 Code and Output
- 2.2.1 Code
- 2.2.2 Output