Feed Mix LP Problem

DSA/ISE 5113

An agricultural mill produces a different feed for cattle, sheep, and chickens by mixing the following raw ingredients: corn, limestone, soybeans, and fish meal. These ingredients contain the following nutrients: vitamins, protein, calcium, and crude fat in the following quantities:

| | Nutrient, k | | | | | |
|---------------|-------------|---------|---------|-----------|--|--|
| Ingredient, i | Vitamins | Protein | Calcium | Crude Fat | | |
| Corn | 8 | 10 | 6 | 8 | | |
| Limestone | 6 | 5 | 10 | 6 | | |
| Soybeans | 10 | 12 | 6 | 6 | | |
| Fish Meal | 4 | 18 | 6 | 9 | | |
| | | | | | | |

The mill has (firm) contracts for the following feed demands:

| | Cattle | Sheep | Chicken |
|-------------|--------|-------|---------|
| Demand (kg) | 10,000 | 6,000 | 8,000 |

There are limited availabilities of the raw ingredients:

| | Corn | Limestone | Soybeans | Fish Meal |
|-------------|-------|-----------|----------|-----------|
| Supply (kg) | 6,000 | 10,000 | 4,000 | 5,000 |

The different feeds have quality bounds per kilogram:

| | Vitamins | | Protein | | Calcium | | Crude fat | |
|---------|-----------------|-----|----------------|-----|---------|-----|------------------|-----|
| | min | max | min | max | min | max | min | max |
| Cattle | 6 | | 6 | | 7 | | 4 | 8 |
| Sheep | 6 | | 6 | | 6 | | 4 | 8 |
| Chicken | 4 | 6 | 6 | | 6 | | 4 | 8 |

Cost per kg of the raw ingredients is as follows:

| | Corn | Limestone | Soybeans | Fish Meal |
|-------------|--------|-----------|----------|-----------|
| $\cos t/kg$ | \$0.20 | \$0.12 | \$0.24 | \$0.12 |