Comprehensive Final Exam

Adv. Analytics and Metaheuristics

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1 - Question 1 (Version 1)

1.1 Part (1): Mathematical Formulation

1.1.1 Sets

NewBuildTypes: Set of new build types $b \in (Homes, Duplex, MiniPark)$

1.1.2 Parameters

Parameter	Description	Default Value
budget	Federal grant allocation to revitalize neighborhoods	\$15MM total budget
maxBuildingDemod	Max amount of buildings that can be demolished	300 total buildings
demoCost	Cost of demolishing a building	\$4,000 per building
freed Up Space	Acreage generated from demolishing a building	0.25 per building
$newBuildSpace_b$	Amount of acreage that a new build $(b \in NewBuildTypes)$ consumes	Homes: 0.2, Duplex: 0.4, MiniPark: 1.0
$newBuildTax_{b}$	Amount of tax dollars generated from a new build $(b \in NewBuildTypes)$	Homes: 1,500, Duplex: 2,750, MiniPark: 500
$newBuildCost_b$	Amount of dollars used to create a new build $(b \in NewBuildTypes)$	Homes: 150,000, Duplex: 190,000, MiniPark: 20,000
$new Build Perc Share_b \\$	Minimum required percentage share of new builds $(b \in NewBuildTypes)$ created	Homes: 20%, Duplex: 10%, MiniPark: 5%

1.1.3 Decision Variables

Variable	Description
numOldBuildsDemod	Number $\in \mathbb{Z}$ of old buildings to demolish
$numNewBuilds_b$	Number $\in \mathbb{Z}$ of new buildings $(b \in NewBuildTypes)$ to produce
new Build Total Cost	Variables to hold total cost of new builds
	$(b \in NewBuildTypes)$. Calculation:
	$\sum_{b \in NewBuildTypes} (numNewBuilds_b \times newBuildCost_b)$
old DemoTotal Cost	Variables to hold total cost of old demolitions. Calculation:
	$numOldBuildsDemod \times demoCost$
sum Of New Builds	Variable to hold the number of all new build types over all New
	build types $(b \in NewBuildTypes)$. Calculation:
	$\sum_{b \in NewBuildTypes} (numNewBuilds_b)$

1.1.4 Objective

Maximize the total tax revenue from the new builds $(b \in NewBuildTypes)$

$$maximize~taxRevenue: \sum_{b \in NewBuildTypes} (numNewBuilds_b \times newBuildTax_b)$$

1.1.5 Constraints

C1 Spend less than or equal to the federal budget (variable definitions above define below)

 $meetTheBudget: newBuildTotalCost + oldDemoTotalCost \leq budget$

C2 Can only produce new builds using the demolished buildings' generated land

$$useAvailLand: \sum_{b \in NewBuildTypes} (numNewBuilds_b \times newBuildSpace_b)$$

 $\leq numOldBuildsDemod \times freedUpSpace$

C3 Can only clear a certain amount of old buildings

 $maxBuildingsCleared: numOldBuildsDemod \leq maxBuildingDemod$

C4 For each new build type $(b \in NewBuildTypes)$, the percentage share of the new build type must meet the minimum required (see variables)

$$share: numNewBuilds_b \geq newBuildPercShare_b \times sumOfNewBuilds, \\ \forall \ b \in NewBuildTypes$$

C5 Non-negativity and integer constraints

 $numOldBuildsDemod \in \mathbb{Z}^+$ $numNewBuilds_b \in \mathbb{Z}^+, \ \forall \ b \in NewBuildTypes$

1.2 Part (2): AMPL Code & Output

1.2.1 AMPL Code

Data problem1.dat

```
data;
# Set of new build types
set NewBuildTypes := Homes Duplex MiniPark;
:= 15000000; # federal budget
param budget
param maxBuildingDemod := 300;
                               # max buildings can be demo'd
                    := 4000; # Cost of each demolition
param demoCost
param freedUpSpace
                    := 0.25;  # Freed up space from demolition
# Amount of acreage that a new building (b in NewBuildTypes) consumes
param: newBuildSpace :=
              0.2
      Homes
              0.4
      Duplex
      MiniPark 1.0
# Amount of tax dollars generated from a new building (b in NewBuildTypes)
param: newBuildTax :=
      Homes
              1500
      Duplex
              2750
      MiniPark 500
# Amount of dollars used to create a new building (b in NewBuildTypes)
param: newBuildCost :=
      Homes
              150000
      Duplex 190000
      MiniPark 20000
# Minimum required percentage share of new buildings (b in NewBuildTypes) created
param: newBuildPercShare :=
      Homes
             0.20
              0.10
      Duplex
      MiniPark 0.05
```

;

Model problem1.mod

```
# Reset globals
reset:
options solver cplex; # Using cplex for simplex alg
# SETS ------
set NewBuildTypes; # Set of new build types
param budget
                  >= 0; # federal budget
param maxBuildingDemod >= 0; # max buildings can be demo'd
                 >= 0; # Cost of each demolition
param demoCost
param freedUpSpace >= 0; # Freed up space from demolition
param newBuildSpace
                  {NewBuildTypes} >= 0; # new build acreage
param newBuildTax
                  {NewBuildTypes} >= 0; # n.b. tax generation
param newBuildCost
                  {NewBuildTypes} >= 0; # n.b. cost
param newBuildPercShare{NewBuildTypes} >= 0; # n.b. min % share
var numOldBuildsDemod
                              >= 0 integer; # Num old builds to demo
var numNewBuilds
                 {NewBuildTypes} >= 0 integer; # Num new builds to create
# Variables to hold total cost of new builds over all types
var newBuildTotalCost = sum{b in NewBuildTypes} ( (numNewBuilds[b] * newBuildCost[b]));
# Variables to hold total cost of old demolitions
var oldDemoTotalCost = (numOldBuildsDemod * demoCost) ;
# Variable to hold the sum of all new build types over all New build types
var sumOfNewBuilds = sum{b in NewBuildTypes}( numNewBuilds[b] );
maximize taxRevenue: sum{b in NewBuildTypes}( numNewBuilds[b] * newBuildTax[b] );
# C1 Spend less than or equal to the federal budget
s.t. meetTheBudget:
   newBuildTotalCost + oldDemoTotalCost <= budget ;</pre>
# C2 Can only produce new builds using the demolished buildings land
```

```
s.t. useAvailLand:
   sum{b in NewBuildTypes}( numNewBuilds[b] * newBuildSpace[b] )
   <= numOldBuildsDemod * freedUpSpace ;</pre>
# C3 Can only clear a certain amount of old buildings
s.t. maxBuildingsCleared: numOldBuildsDemod <= maxBuildingDemod ;</pre>
# C4 For each new build type (b in NewBuildTypes),
     the percentage share of the new build type must meet the minimum required
s.t. share {b in NewBuildTypes}:
   numNewBuilds[b] >= newBuildPercShare[b] * sumOfNewBuilds;
data problem1.dat; # retreive data file with sets/param. values
   solve:
   print;
   print "Number of old buildings to demolish and cost (dollars):";
   display numOldBuildsDemod, oldDemoTotalCost;
   print "Number of new buildings produced and cost (dollars):";
   display numNewBuilds , newBuildTotalCost ;
   print "Total Budget Used (dollars):";
   display newBuildTotalCost + oldDemoTotalCost;
   print "Part 3: Max Tax Revenue generated (dollars):";
   display taxRevenue;
```

1.2.2 Part 2/3: Solve AMPL Model and Display Solution w/Commentary

```
CPLEX 20.1.0.0: optimal integer solution; objective 199000 6 MIP simplex iterations 0 branch-and-bound nodes

Number of old buildings to demolish and cost (dollars): numOldBuildsDemod = 137 oldDemoTotalCost = 548000

Number of new buildings produced and cost (dollars): numNewBuilds [*] := Duplex 62 Homes 17 MiniPark 6; newBuildTotalCost = 14450000

Total Budget Used (dollars): newBuildTotalCost + oldDemoTotalCost = 14998000

Part 3: Max Tax Revenue generated (dollars): taxRevenue = 199000
```

2 - Question 2 (Version 6)

2.1 Code to get Root Node

Root Node is Node 1 in the diagram

2.1.1 Root Node AMPL Model problem2.mod

• Note code below also used/altered to test upper and lower bounds of child nodes.

```
reset;
option solver cplex; # Solver

var x >= 0; # Not integer because this is used to check the optimal when fixing a var
var y >= 0; # ""

# Original problem:
maximize theSolution: 2.5*x + 6*y;
    s.t. first: 3*x + 5*y <= 26;
    s.t. second: x >= 4;

# Used to check the BnB nodes
# Fixing x = 4 to solve for initial values of y
s.t. checkNode: x = 4;

# Solve and display
solve;
display theSolution, x,y;
```

2.1.2 Output of Root Node AMPL Model (fixing x=4 & solving for y)

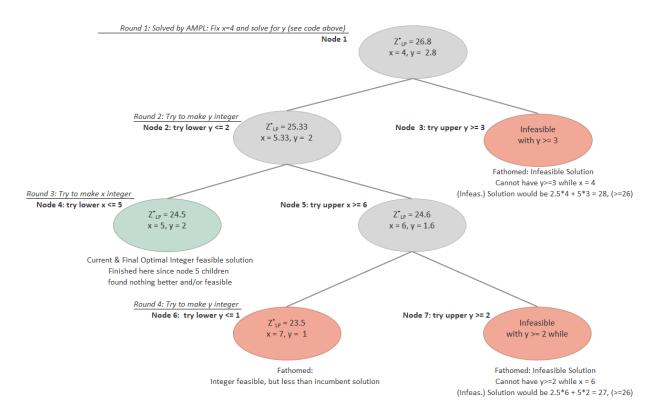
```
CPLEX 20.1.0.0: optimal solution; objective 26.8 0 dual simplex iterations (0 in phase I) the Solution = 26.8 x = 4 y = 2.8
```

2.2 Branch and Bound Diagram

2.2.1 Summary of Diagram

- Optimal solution reached at node 4 with integer feasible values of x=5, and y=2, optimal of 24.5
- Checked 7 total nodes
- Fathomed 3 nodes (see description of "why" in diagram)
- Each "Round" label shows which variable is being checked and for what integer value (lower or upper bound of the parent node)
- Please note that the AMPL model above was used as a calculator to test upper and lower bounds.

2.2.2 Branch and Bound Diagram



3 - Question 3 (Version 2)

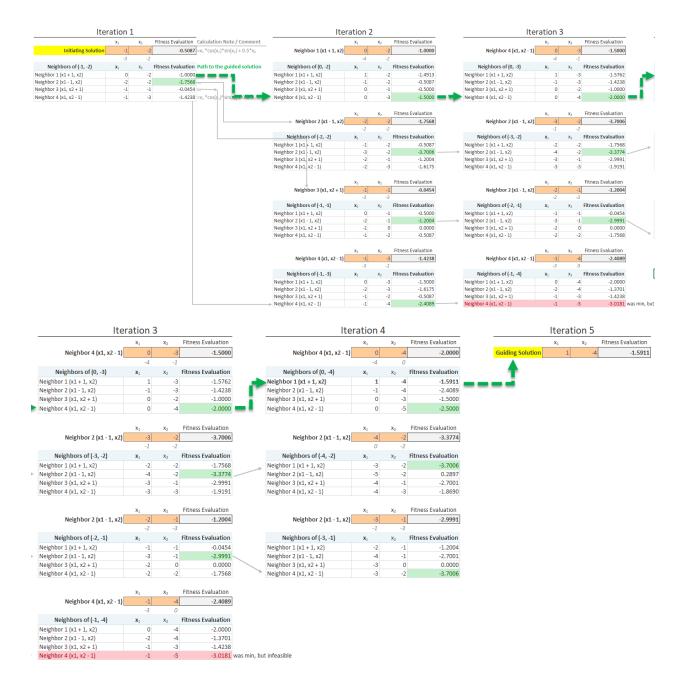
3.1 Part (i): Hill Climbing

- Please see the below snippet on rightmost comments about the algorithm
- Ended at iteration 3 with minimum value of -1.9991 due to no change in best neighbor

	X_1	X_2	Fitness Evaluation	Calculation Note / Comment
Starting Solution, So	2	2		$=x_1 * cos(x_1) * sin(x_2) + 0.5 * x_2$
starting solution, s ₀	۷		0.2432	-X1 COS(X1) SIN(X2) + 0.5 X2
	X_1	X ₂	Fitness Evaluation	
Current Solution	2	2		$=x_1*\cos(x_1)*\sin(x_2) + 0.5*x_2$
Done?	FALSE		0.2432	λ1 cos(λ1) sin(λ2) · c.s λ2
Done:	TALSE			
lf.	teration 1			
Best Neighbor (current)	2	2	0.2432	current solution from past iteration
Neighbors of (2, 2)	\mathbf{x}_1	x_2	Fitness Evaluation	
Neighbor 1 (x1 + 1, x2)	3	2	-1.7006	$=x_1 * cos(x_1) * sin(x_2) + 0.5 * x_2$
Neighbor 2 (x1 - 1, x2)	1	2	1.4913	
Neighbor 3 (x1, x2 + 1)	2	3	1.3825	1
Neighbor 4 (x1, x2 - 1)	2	1	-0.2004	
(New) Best Neighbor	3	2	-1.7006	=min(neighbors, best_neighbor)
is Best Neighbor Same as Old?	FALSE			
Done?	FALSE			done if same
			E1	
	x ₁	X ₂	Fitness Evaluation	1
Current Solution	3	2	-1.7006	$=x_1*\cos(x_1)*\sin(x_2) + 0.5*x_2$
	teration 2	2	1 7006	
Best Neighbor (current)	3	2	-1.7006	current solution from past iteration
Neighbors of (3, 2)	\mathbf{x}_1	X ₂	Fitness Evaluation	
	x ₁	x ₂ 2		$=x_1*\cos(x_1)*\sin(x_2) + 0.5*x_2$
Neighbor 1 (x1 + 1, x2)	4		-1.3774	
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2)	_	2	-1.3774 0.2432	
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1)	4	2	-1.3774 0.2432 1.0809	
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1)	4 2 3	2 2 3	-1.3774 0.2432 1.0809	
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor	4 2 3 3	2 2 3	-1.3774 0.2432 1.0809 -1.9991	
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old?	4 2 3 3 3 FALSE	2 2 3 1	-1.3774 0.2432 1.0809 -1.9991	=min(neighbors, best_neighbor)
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor	4 2 3 3	2 2 3 1	-1.3774 0.2432 1.0809 -1.9991	
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old?	4 2 3 3 FALSE	2 2 3 1	-1.3774 0.2432 1.0809 -1.9991	=min(neighbors, best_neighbor)
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done?	4 2 3 3 3 FALSE FALSE x ₁	2 2 3 1 1	-1.3774 0.2432 1.0809 -1.9991 -1.9991	=min(neighbors, best_neighbor) done if same
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old?	4 2 3 3 FALSE	2 2 3 1	-1.3774 0.2432 1.0809 -1.9991 -1.9991	=min(neighbors, best_neighbor)
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution	4 2 3 3 3 FALSE FALSE x ₁ 3	2 2 3 1 1	-1.3774 0.2432 1.0809 -1.9991 -1.9991	=min(neighbors, best_neighbor) done if same
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution	4 2 3 3 3 FALSE FALSE x ₁ 3	2 2 2 3 3 1 1 1 1 x ₂ 1	-1.3774 0.2432 1.0809 -1.9991 -1.9991 Fitness Evaluation -1.9991	=min(neighbors, best_neighbor) done if same $=x_1*\cos(x_1)*\sin(x_2) + 0.5*x_2$
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution	4 2 3 3 3 FALSE FALSE x ₁ 3	2 2 3 1 1	-1.3774 0.2432 1.0809 -1.9991 -1.9991 Fitness Evaluation -1.9991	=min(neighbors, best_neighbor) done if same $=x_1*\cos(x_1)*\sin(x_2) + 0.5*x_2$
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution	4 2 3 3 3 FALSE FALSE x ₁ 3 steration 3 3	2 2 3 3 1 1 1 1 x ₂ 1	-1.3774 0.2432 1.0809 -1.9991 -1.9991 Fitness Evaluation -1.9991	=min(neighbors, best_neighbor) done if same $=x_1*\cos(x_1)*\sin(x_2) + 0.5*x_2$
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution Best Neighbor (current) Neighbors of (3, 1)	4 2 3 3 3 FALSE FALSE x ₁ 3 teration 3 3	2 2 3 3 1 1 1 1 x ₂ 1 1 x ₂	-1.3774 0.2432 1.0809 -1.9991 -1.9991 Fitness Evaluation -1.9991 Fitness Evaluation	=min(neighbors, best_neighbor) done if same $=x_1*\cos(x_1)*\sin(x_2) + 0.5*x_2$ current solution from past iteration
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution Best Neighbor (current) Neighbors of (3, 1) Neighbor 1 (x1 + 1, x2)	4 2 3 3 3 FALSE FALSE x ₁ 3 teration 3 3	2 2 3 3 1 1 1	-1.3774 0.2432 1.0809 -1.9991 -1.9991 Fitness Evaluation -1.9991 Fitness Evaluation -1.7001	=min(neighbors, best_neighbor) done if same $=x_1*\cos(x_1)*\sin(x_2)+0.5*x_2$ current solution from past iteration $=x_1*\cos(x_1)*\sin(x_2)+0.5*x_2$
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution Best Neighbor (current) Neighbors of (3, 1) Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2)	4 2 3 3 3 FALSE FALSE x ₁ 3 cteration 3 3 4 4 2	2 2 3 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-1.3774	=min(neighbors, best_neighbor) done if same $=x_1*\cos(x_1)*\sin(x_2) + 0.5*x_2$ current solution from past iteration $=x_1*\cos(x_1)*\sin(x_2) + 0.5*x_2$
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution Best Neighbor (current) Neighbors of (3, 1) Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1)	4 2 3 3 3 FALSE FALSE x ₁ 3 4 teration 3 3 x ₁ 4 2 3	2 2 3 3 1 1 1	-1.3774	=min(neighbors, best_neighbor) done if same $=x_1*\cos(x_1)*\sin(x_2)+0.5*x_2$ current solution from past iteration $=x_1*\cos(x_1)*\sin(x_2)+0.5*x_2$
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution Best Neighbor (current) Neighbors of (3, 1) Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2)	4 2 3 3 3 FALSE FALSE x ₁ 3 cteration 3 3 4 4 2	2 2 3 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-1.3774	=min(neighbors, best_neighbor) done if same $=x_1*\cos(x_1)*\sin(x_2)+0.5*x_2$ current solution from past iteration $=x_1*\cos(x_1)*\sin(x_2)+0.5*x_2$
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution Best Neighbor (current) Neighbors of (3, 1) Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1)	4 2 3 3 3 FALSE FALSE x ₁ 3 4 teration 3 3 x ₁ 4 2 3	2 2 3 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-1.3774	=min(neighbors, best_neighbor) done if same $=x_1*\cos(x_1)*\sin(x_2)+0.5*x_2$ current solution from past iteration $=x_1*\cos(x_1)*\sin(x_2)+0.5*x_2$
Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1) (New) Best Neighbor is Best Neighbor Same as Old? Done? Current Solution Neighbors of (3, 1) Neighbor 1 (x1 + 1, x2) Neighbor 2 (x1 - 1, x2) Neighbor 3 (x1, x2 + 1) Neighbor 4 (x1, x2 - 1)	4 2 3 3 FALSE FALSE x ₁ 3 teration 3 3 x ₁ 4 2 3 3 3	2 2 3 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-1.3774	=min(neighbors, best_neighbor) done if same $=x_1*\cos(x_1)*\sin(x_2)+0.5*x_2$ current solution from past iteration $=x_1*\cos(x_1)*\sin(x_2)+0.5*x_2$

3.2 Part (ii): Path Relinking

- Below shows two images with the path re-linking process iterations (from initiation to guided solution).
- Green arrow highlights the path to the guided solution
- Logic overview: Evaluates neighbors of initiation solution, then moves along path of each neighbor. Makes best move for each neighbor, then checks difference between current and guided solution. Repeats until finding the guided solution
- Iteration 3 duplicated for ease of viewing



3.3 Part (iii): Simulated Annealing

Using the evaluation function for this question (note language below is R)

```
# Create an Evaluation function to evaluate fitness
evaluateFitness <- function(x1, x2) { x1*cos(x1)*sin(x2) + 0.5*x2 }</pre>
```

The probability **p** of accepting a move uses the following formula: $p = e^{\frac{-(f(s_1) - f(s_2))}{T}}$.

Where $f(s_1)$ is the current solution, and $f(s_2)$ is the candidate solution since minimization. See calculation below (using evaluateFitness() function)

```
# Uses the evaluation function to return the probability (see above formula)
calculateProb <- function(temperature, currentPosition, newPosition) {
    # Assuming minimization, evaluation of the Current and Candidate solutions:
    f_s1 = evaluateFitness(currentPosition[1], currentPosition[2]) # f(s[1]) current sol.
    f_s2 = evaluateFitness(newPosition[1], newPosition[2]) # f(s[2]) candidate so

# If Candidate evaluation is WORSE than the current, accept with prob. p
if (f_s2 < f_s1) { # '<' since minimization
    p = exp((-(f_s1-f_s2) / temperature)))
} else { p = 1 } # Else accept move since better

return(round(p, 3)) # Round to 3 decimal places
}</pre>
```

Now calculate the probability p from the current to the candidate solutions

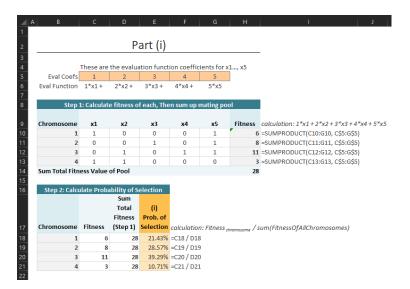
[1] "At temp. 3, the probability from (4, 0) to (4, 1) is 0.567"

[1] "At temp. 3, the probability from (4, 0) to (4, -1) is 1"

4 - Question 4 (Version 3)

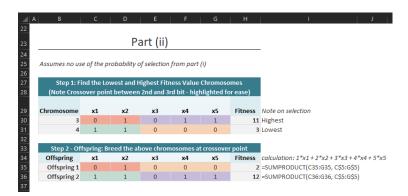
4.1 Part (i) - Roulette Probability

- Evaluates the fitness for each chromosome $c \in Chromosomes$ using $f(x) = x_1 + 2x_2 + 3x_3 + 4x_4 + 5x_5$ as evaluation function.
- Then computes the probability based on the following equation: $\frac{f_c}{\sum_{c \in Chromosomes} f_c}$
- See yellow highlighted cells for final roulette wheel probabilities for each chromosome



4.2 Part (ii/iii) - Breed Offspring

- Select the highest (Chrom. 3) and lowest (Chrom. 4) fitness valued chromosomes, then split at crossover point to produce offspring
- Offspring split between the second and third bit (highlighted for ease)
- \bullet Highest fitness valued offspring: <code>Offspring</code> 2 with fitness value of 12



5 - Question 5 (Version 2)

5.1 Part (i) - Global Best

5.1.1 Assumptions

- Uses all calculations and parameter values from the problem question. See header in picture as well for the calculation
- Parameters of interest highlighted in orange
- See global best logic in picture below

5.1.2 Solution

• Particle 1's Next Velocity: (-1.90, 3.55, 3.70)

• Particle 1's Next Position: (12.10, 8.55, 5.70)

5.1.3 Relevant Work

					Par	't (i)								
				Ine	rtia			Cog	nitive				Sc	ocial	
	Next Position	Next Vel.		I. Weight	Curr. Vel.			nn	P. Best	Curr. Pos.		nn n	nn	G. Best	Curr. Pos.
Particle 1's: Position Index	X[t+1] = V[t+1] + X[t]	V[t+1]	=	w	V[t]	+	phi[1]	r[1]	(P[i]	- X[t])	+	phi[2]	r[2]	(P[g]	- X[t])
Position Idx. 1	12.10	-1.90		1	1		1	0.5	10	14		1	0.15	8	14
Position Idx. 2	8.55	3.55		1	0		1	0.5	13	5		1	0.15	2	5
Position Idx. 3	5.70	3.70		1	1		1	0.5	8	2		1	0.15	0	2
Particle 1's Next Velocit Particle 1's Next Position										est Logic: personal bes cle 4's perso					

5.2 Part (ii) - Local Best w/Ring

5.2.1 Assumptions

- Local best paramaters highlighted in yellow
- See local best logic with ring structure in picture below

5.2.2 Solution

• Particle 1's Next Velocity: (-0.40, 4.30, 4.45)

• Particle 1's Next Position: (13.60, 9.30, 6.45)

5.2.3 Relevant Work

					Par	t (i	ii)										
			Inertia			Cognitive						Social					
	Next Position	Next Vel.		I. Weight	Curr. Vel.	-	nn	""	P. Best	Curr. Pos.		""	""	L. Best	Curr. Pos		
Particle 1's: Position Index)	X[t+1] = V[t+1] + X[t]	V[t+1]	=	w	V[t]	+	phi[1]	r[1]	(P[i]	- X[t])	+	phi[2]	r[2]	(P[1]	- X[t])		
Position Idx. 1	13.60	-0.40	1	1	1		1	0.5	10	14		1	0.15	18	14		
Position Idx. 2	9.30	4.30	1	1	0		1	0.5	13	5		1	0.15	7	5		
Position Idx. 3	6.45	4.45		1	1		1	0.5	8	2		1	0.15	5	2		
Particle 1's Next Velocit	y: (-0.40, 4.30, 4.45)								Local Bes	_							
Particle 1's Next Position	n: (13.60, 9.30, 6.45)								Neighbors of particle 1 are:								
										Particle 2	Personal Best Fitness value: 120						
									Particle 5 Personal Best Fitness value: 150								
									Use 5's n	hest nositi	on s	ince it has	the highes	t nersonal	hest		

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