

Final Exam

Adv. Analytics and Metaheuristics

Daniel Carpenter

March 2022

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1 - Question 1 (Version 1)

1.1 Mathematical Formulation

1.1.1 Sets

NewBuildTypes: Set of new build types $b \in (Homes, Duplex, MiniPark)$

1.1.2 Parameters

Parameter	Description	Default Value
<i>budget</i>	Federal grant allocation to revitalize neighborhoods	\$15MM total budget
<i>maxBuildingDemod</i>	Max amount of buildings that can be demolished	300 total buildings
<i>demoCost</i>	Cost of demolishing a building	\$4,000 per building
<i>freedUpSpace</i>	Acreage generated from demolishing a building	0.25 per building
<i>newBuildSpace_b</i>	Amount of acreage that a new building ($b \in NewBuildTypes$) consumes	<i>Homes</i> : 0.2, <i>Duplex</i> : 0.4, <i>MiniPark</i> : 1.0
<i>newBuildTax_b</i>	Amount of tax dollars generated from a new building ($b \in NewBuildTypes$)	<i>Homes</i> : 1,500, <i>Duplex</i> : 2,750, <i>MiniPark</i> : 500
<i>newBuildCost_b</i>	Amount of dollars used to create a new building ($b \in NewBuildTypes$)	<i>Homes</i> : 150,000, <i>Duplex</i> : 190,000, <i>MiniPark</i> : 20,000
<i>newBuildPercShare_b</i>	Minimum required percentage share of new buildings ($b \in NewBuildTypes$) created	<i>Homes</i> : 20%, <i>Duplex</i> : 10%, <i>MiniPark</i> : 5%

1.1.3 Decision Variables

Variable	Description
$numOldBuildsDemod$	Number of old buildings to demolish
$numNewBuilds_b$	Number of new buildings ($b \in NewBuildTypes$) to produce

1.1.4 Objective

Maximize the tax revenue from the projects

$$maximize\ taxRevenue : \sum_{b \in NewBuildTypes} (numNewBuilds_b \times newBuildTax_b)$$

1.1.5 Constraints

C1 Spend less than or equal to the federal budget
meetTheBudget :

$$\sum_{b \in NewBuildTypes} [(numNewBuilds_b \times newBuildCost_b) + (numOldBuildsDemod \times demoCost)] \leq budget$$

C2 Can only produce new builds using the demolished buildings land

$$useAvailLand : \sum_{b \in NewBuildTypes} (numNewBuilds_b \times newBuildSpace_b) \leq numOldBuildsDemod \times freedUpSpace$$

C3 Can only clear a certain amount of old buildings

$$maxBuildingsCleared : numOldBuildsDemod \leq maxBuildingDemod$$

C4 For each new build type ($b \in NewBuildTypes$), the percentage share of the new build type must meet the minimum required

$$share : numNewBuilds_b \geq newBuildPercShare_b \times \sum_{b \in NewBuildTypes} (numNewBuilds_b), \\ \forall b \in Businesses$$

C5 Non-negativity constraints

$$numOldBuildsDemod \geq 0 \\ numNewBuilds_b \geq 0, \forall b \in NewBuildTypes$$

1.2 Code

1.2.1 AMPL Code

Code here

1.2.2 AMPL Solution

Defined on a directed network: $G = (N, A)$
where N is a set of n nodes: $\{1, 2, \dots, n\}$
and A is a set of m arcs as a subset of $N \times N$

Each node i has an associated value $b(i)$

Arc (i, j) has certain characteristics:

- cost c_{ij} per unit of flow on arc (i, j)
- upper bound on flow of u_{ij} (capacity)
- lower bound on flow of ℓ_{ij} (usually 0)
- **multiplier $\mu_{ij} \geq 0$ such that if 1 unit of flow leaves node i , then μ_{ij} units arrive at node j**

Figure 1: Problem 1 AMPL Output of Optimal Solution and Variables

2 - *Question 2* (Version 6)

3 - *Question 3* (Version 2)

4 - *Question 4* (Version 3)

5 - *Question 5* (Version 2)