# Homework 4 Hill Climbing Methods

# Daniel Carpenter & Kyle (Chris) Ferguson

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## Question 1: Strategies

#### (a) Initial Solution

Define and defend a strategy for determining an initial solution to this knapsack problem for a neighborhood-based heuristic.

- Our algorithm for the initial\_solution() function randomly generates a list of binary ∈ (0, 1) values for the knapsack problem, 1 if an item is included in the knapsack and 0 if the item is excluded
- Since the solution could randomly generate an infeasible solution (i.e., the totalWeight ≥ maxWeight),
  the initial\_solution() function handles it by randomly removing items from the knapsack until it
  is under the maxWeight.
- After the generation of the initial solution, the evaluate function searches for better solutions.
- We considered beginning with nothing in the knapsack (list of 0's from item 0 to n), but we researched
  and found that a common approach is to begin with a randomly generated solution.

#### (b) Neighborhood Structures

Describe 3 neighborhood structure definitions that you think would work well for this problem. Compute the size of each neighborhood.

- 1. Without any adjustment to the neighborhoods: For each neighborhood, there are 150 neighbors. Since the knapsack problem uses a n-dimensional binary vector, the total solution space is  $2^n$ , which is  $2^{150}$
- 2. **TODO**
- 3. **TODO**

#### (c) Infeasibility

During evaluation of a candidate solution, it may be discovered to be infeasible. In this case, provide 2 strategies for handling infeasible solutions:

Note both approaches are similar:

- 1. Chosen Method in model: If the solution is infeasible (i.e., the totalWeight ≥ maxWeight), then we will randomly remove values from the knapsack until the bag's weight is less than the max allowable weight.
- 2. If the solution is infeasible, then we will *iteratively* (from last item in list to beginning) remove values from the knapsack until the bag's weight is less than the max allowable weight.

### Global Variables

Input variables like the  $random\ seed,\ values\ and\ weights$  data for knapsack, and the  $maximum\ allowable\ weight$ 

```
# Import python libraries
from random import Random # need this for the random number generation -- do not change
import numpy as np
# Set the seed
seed = 51132021
myPRNG = Random(seed)
n = 150 # number of elements in a solution
# create an "instance" for the knapsack problem
value = []
for i in range(0, n):
   value.append(round(myPRNG.triangular(150, 2000, 500), 1))
weights = []
for i in range(0, n):
    weights.append(round(myPRNG.triangular(8, 300, 95), 1))
# define max weight for the knapsack
maxWeight = 2500
```

## **Key Functions**

Functions to provide initial solution, create a neighborhood and evaluate better solutions

```
# Randomly remove ann item. If not feasible, then try evaluating again until feasible
      randIdx = myPRNG.randint(0,n-1) # generate random item index to remove
                                  # Don't include the index r from the knapsack
      x[r] = 0
      evaluate(x, r=randIdx)
                                  # Try again on the next to last element
   else:
      # Finish the process if the total weight is satisfied
       # (returns a list of both total value and total weight)
      return [totalValue, totalWeight]
   # returns a list of both total value and total weight
   return [totalValue, totalWeight]
# ------
# NEIGHBORHOOD FUNCTION - simple function to create a neighborhood
# 1-flip neighborhood of solution x
def neighborhood(x):
   nbrhood = []
   # Set up n number of neighbors with list of lists
   for i in range(0, n):
      nbrhood.append(x[:])
      # Flip the neighbor from 0 to 1 or 1 to 0
      if nbrhood[i][i] == 1:
          nbrhood[i][i] = 0
      else:
          nbrhood[i][i] = 1
   return nbrhood
# INITIAL SOLUTION FUNCTION - create the initial solution
# create a feasible initial solution
def initial_solution():
   x = [] # empty list for x to hold binary values indicating if item i is in knapsack
   # Create a initial solution for knapsack (Could be infeasible), by
   # randomly create a list of binary values from 0 to n. 1 if item is in the knapsack
   for item in range(0, n):
      x.append(myPRNG.randint(0,1))
   totalWeight = np.dot(np.array(x), np.array(weights)) # Sumproduct of weights and is included
```

```
# While the bag is infeasible, randomly remove items from the bag.
# Stop once a feasible solution is found.
knapsackSatisfiesWeight = totalWeight <= maxWeight # True if the knapsack is a feasible solution, e
while not knapsackSatisfiesWeight:

randIdx = myPRNG.randint(0,n-1) # Generate random index of item in knapsack and remove item
x[randIdx] = 0

# If the knapsack is feasible, then stop the loop and go with the solution
totalWeight = np.dot(np.array(x), np.array(weights)) # Recalc. Sumproduct of weights and is inc
if (totalWeight <= maxWeight):
    knapsackSatisfiesWeight = True

return x</pre>
```

## Question 2: Local Search with Best Improvement

```
## GET INITIAL SOLUTION -----
# variable to record the number of solutions evaluated
solutionsChecked = 0
x_curr = initial_solution() # x_curr will hold the current solution
x_best = x_curr[:] # x_best will hold the best solution
r = -1 # last element in list
# f_curr will hold the evaluation of the current soluton
f_curr = evaluate(x_curr, r)
f_best = f_curr[:]
## BEGIN LOCAL SEARCH LOGIC -----
done = 0
while done == 0:
    # create a list of all neighbors in the neighborhood of x_curr
   Neighborhood = neighborhood(x_curr)
   for s in Neighborhood: # evaluate every member in the neighborhood of x_curr
       solutionsChecked = solutionsChecked + 1
       if evaluate(s, r)[0] > f_best[0]:
           # find the best member and keep track of that solution
           x_best = s[:]
           f_best = evaluate(s, r)[:] # and store its evaluation
    # Checks for platueau and feasibility
   if f_best == f_curr and (f_curr[1] < maxWeight): # if there were no improving solutions in the nei
```

```
done = 1
    else:
       x_curr = x_best[:] # else: move to the neighbor solution and continue
       f_curr = f_best[:] # evalute the current solution
       print("\nTotal number of solutions checked: ", solutionsChecked)
       print("Best value found so far: ", f_best)
##
## Total number of solutions checked: 150
## Best value found so far: [20960.6, 2492.0]
print("\nFinal number of solutions checked: ", solutionsChecked, '\n',
      "Best value found: ", f_best[0], '\n',
      "Weight is: ", f_best[1], '\n',
     "Total number of items selected: ", np.sum(x_best), '\n\n',
     "Best solution: ", x_best)
##
## Final number of solutions checked: 300
## Best value found: 20960.6
## Weight is: 2492.0
## Total number of items selected: 21
## Best solution: [0, 1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0
```