

# **Understanding Evolution as a Collective Strategy for Groping in the Dark**

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## **Abstract**

On the one hand side many people admire the often strikingly efficient results of organic evolution. On the other hand side, however, they presuppose mutation and selection to be a rather prodigal and unefficient trial-and-error strategy. Taking into account the parallel processing of a heterogeneous population and sexual propagation with recombination as well as the endogenous adaptation of strategy characteristics, simulated evolution reveals a couple of interesting, sometimes surprising, properties of nature's learning-by-doing algorithm. 'Survival of the fittest', often taken as Darwin's view, turns out to be a bad advice. Individual death, forgetting, and even regression show up to be necessary ingredients of the life game. Whether the process should be named gradualistic or punctualistic, is a matter of the observer's point of view. He even may observe 'long waves'.

## **Introduction**

Evolution can be looked at from a large variety of positions. Beginning with the closest physico-analytic viewpoint, one might focus attention to the molecular and cellular processes. A more distant point of view centers on the behaviour of populations and species. Another difference emerges from whether one emphasizes the homeostatic aspect of the adaptation to a given environment, which is more relevant in the short term, or the euphemistic view of development to the more complex, higher, or even better in the long term.

The instruments used here, will be a microscope and a time accelerator. Moreover, for methodological reasons, an optimistic point of view will be shared by comparing macroevolution with iterative optimization, or, even more adequately, with permanent meliorization techniques, i.e. hill-climbing or ridge-following procedures. By means of a simple algorithmic formulation of the main evolutionary principles, it is possible to reveal some properties of the process which in some cases are striking at the first glance. These findings may not only be helpful for better understanding 'nature's intelligence' but also be beneficial for global long-term planning and other groping-in-the-dark situations.

### Modelling evolution

Ashby's homeostat /1/ was a device which should find back to a feasible state by a sequence of random trials, uniformly distributed over a given parameter space. Many people have made the mistake of thinking of mutations as 'pure' random trials. A couple of them was malignant. They wanted to show that evolution theory never will be able to explain how 'nature' found a way to complex living beings within about  $10^{17}$  seconds - the age of our globe. Montroll's random walk /2/ paradigm, on the other hand, neglects the selection principle of evolution. Both mutation and selection (chance and necessity) are the first principles, which, of course, have to be programmed properly.

Broadly accepted hereditary evidence has led to the proverb 'The apple does not fall far off of the tree'. A better model of mutations therefore is a normal distribution for parameter changes between generations, its maximum being centered at the respective ancestor's position. The rôle of chance in such a model is not explicative, however, but only descriptive. An important question now is the suitable size of the standard deviation(s) of the changes, which may be addressed as mean step size(s) from one generation to the next. This question arises with all optimization or meliorization schemes.

Modelling the selection principle is far more easy, as it seems first. 'Survival of the fittest' is the maxime which Spencer derived from Darwin's observations. Some evolution programmers have taken it for granted: According to a given selection criterion, a descendant is rejected if its vitality is less than that of its ancestor, the ancestor otherwise. This scheme may be called a (1+1)- or two membered evolution strategy (E.S. in the following), resembling the 'struggle for life' between one ancestor and one descendant. Rechenberg /3/ has derived theoretical results for the convergence velocity of that process in an n-dimensional parameter space. Most important was his finding that for an endless ridge following situation as well as for a minimum (or maximum) approaching situation the convergence rate is inversely proportional to the number of parameters. Distances growing with the square root of n, the number of iterations or generations needed to proceed from one to the other arbitrary point in space, increases with  $O(n^{1/2})$  only, and not exponentially as in the case of simple Monte-Carlo strategies.

This type of creeping random search strategy (see e.g. Brooks /4/, Schumer and Steiglitz /5/, or Rastrigin /6/) was first devised for experimental optimization, where measurement inaccuracies drop out one-variable-at-a-time and gradient-following procedures due to their inability of non-local operation.

Bremermann's 'simulated evolution' /7/ does not differ so much from Rechenberg's as e.g. G.E.P. Box's 'Evolutionary Operation' EVOP /8/

does, an experimental design technique, and the so-called Simplex and Complex strategies of Nelder and Mead /9/ and M.J. Box /10/ for numerical optimization. Whereas random trials are vividly rejected by G.E.P. Box, he centers several experiments (at the same time, on principle) in a deterministic way around the position of the current best point in a low-dimensional parameter space. The best of all then is taken as the center of the next trial series. Nelder, Mead, and M.J. Box, however, using a polyhedron for placing the trials, reject the worst position and find a new one by reflecting the worst with respect to the center of the remaining points of the simplex or complex.

The first concept may be called a  $(1+\lambda)$ -, the latter a  $(\mu+1)$ -evolutionary scheme,  $\mu$  denoting the number of parents,  $\lambda$  the number of children within one generation. More general, therefore, is a  $(\mu+\lambda)$ - scheme with  $\mu$  ancestors which have  $\lambda$  descendants, the  $\mu$  best of all become parents of the next generation. The fact that individual life times are limited is reflected by the  $(\mu, \lambda)$ - version, first introduced by Schwefel /11/. Now the  $\mu$  parents are no longer included into the selection, thus  $\lambda$  must be greater than  $\mu$ . Theoretical results so long are available for the  $(1+\lambda)$ - and  $(1, \lambda)$ - evolution strategies only. All further observations in the following, therefore, were found by computer simulation only.

#### Self-adaptation of strategy parameters

As for all optimization techniques, the appropriate step size adjustment is of crucial importance. Rechenberg found that there is a 'window' of one decade only within which the  $(1+1)$ - evolution strategy has a reasonable convergence velocity. He devised a simple rule for exogenously adjusting a near optimum performance of the process, i.e. to control the success probability which should be in the vicinity of one success among five trials. This advice is good for many but not all situations. Moreover, it does not give any hints to adapt the standard deviations of the parameter changes individually. Some may be too large, others too small, at the same time. Only within the multimembered strategy, one can include the step size or even different step sizes (mutation rates) into the set of the individual's genes and adapt them endogenously. There is some evidence that by means of repair enzymes the effective mutation rates are controlled, the rate of premutations due to environmental conditions being constant over long periods.

Let us think at first, however, of one common step size for all object parameters. Within a  $(1, \lambda)$ - E.S. the correct step size turns out to be even more important than within a  $(1+\lambda)$ - version /11/. In the first case regression takes place instead of progress when the step size is too large, whereas stagnation is the worst case in the latter.

At a first glance, therefore, 'survival' of an ancestor might be a good advice. Simulation results, however, show that the opposite is true. This is the first surprise. Figure 1 demonstrates the difference between a (1+10)- and a (1,10)- E.S. when

minimizing the function  $F_i = \sum_{i=1}^n x_i^2$  with  $n=30$ .

The number of variables,  $n$ , was taken as large as 30 in order to avoid improper conclusions. In lower dimensional cases nearly every strategy may achieve good results. One common step size sigma (or standard deviation, more precisely) for all  $x_i$  is changed by mutation, i.e. by multiplying the ancestor's value with a random number, drawn

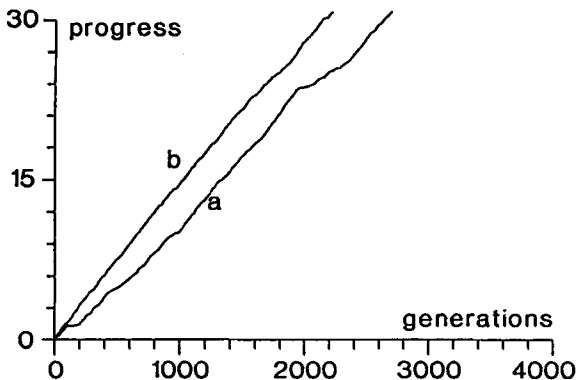


Figure 1:  
Self-learning of the mutation rate (gross mean step size here) for function  $F_i$ ,  $n=30$   
a) (1+10)- evolution strategy  
b) (1,10)- E.S.

The 'progress' is measured in terms of  $\log ((F^0/F^*)^{1/2})$ , where  $F^0$  denotes the start value,  $F^*$  the current value of the objective function.

from a logarithmic normal distribution in order to avoid exogenous drift. The (1,10)- strategy turns out to be superior. An explanation for this surprising fact is the following: if an ancestor happens to arrive at a superior position, this might be - by chance - in spite of a non-optimum step size, or a step size which is not suitable for further generations. The (1+lambda)- scheme preserves the unsuitable step size as long as with it a further success is placed. This leads to periods of stagnation. Within a (1,lambda)- E.S. the good position, occasionally won with an unsuitable step size, is lost, together with the latter, during the next generation. This short term regression, however, enhances the long term velocity of the whole process by a stronger selection with respect to the suitable step size (strategy parameter). Simply speaking: Forgetting is as important as learning, the first must be seen as a necessary ingredient of the latter. One might interpret the fact of an inherent finite life time (preprogrammed maximum number of cell divisions) of living beings as an appropriate measure of nature to overcome the difficulties of undeserved success - or, in a changing environment, of forgetting obsolete 'knowledge'.

### Collective learning of proper scalings

In most cases it is not sufficient to adapt one common step size for all object parameters. For an objective function

like  $F_2 = \sum_{i=1}^{30} (i \times x_i^2)$ , for example, individual standard deviations  $\sigma_{\sigma_i}$ ,

appropriately scaled, could speed up the progress rate considerably. To achieve this kind of flexibility within the multimembered evolution strategy, each individual is characterized by a set of  $n$  step sizes in addition to the  $n$  object parameters. They are mutated by multiplication with two random factors, one being common for all step sizes as before, the other acting individually, however. Thus general and specific scaling can be learned at the same time. Operating with an  $(1, \lambda)$ -strategy - however large  $\lambda$  may be - leads to a second surprise: this kind of process does not work at all, it gets stuck prematurely by approaching a relative optimum in a lower dimensional space. The reason is rather simple: As said above, the convergence rate is inversely proportional to  $n$ , the dimension of the parameter space. Descendants operating in a subspace by sharply reducing one or even some of the step sizes have a short term advantage. Selecting the fittest descendant to become the one and only parent of the next generation, is counterproductive in the long term, as was the survival of the ancestor.

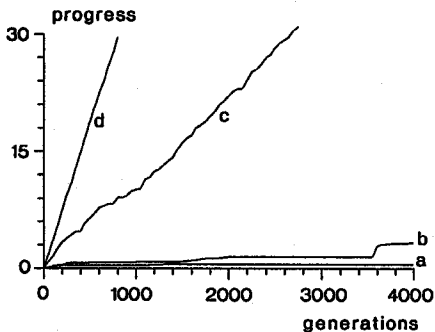


Figure 2:  
Learning of the scaling I  
a) (1,10)- E.S.  
b) (3,10)- E.S. with recombination  
c) (6,30)- E.S. with recombination  
d) (15,100)- E.S. with recombination  
(curve 2d equals 3c )

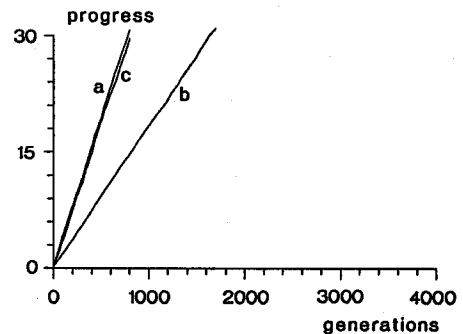


Figure 3:  
Learning of the scaling II  
a) ( 1,100)- E.S.  
b) (15,100)- E.S. without recomb.  
c) (15,100)- E.S. with recomb.  
a) & b) with prefixed optimum  
scalings, c) with scaling learned

Figure 2 demonstrates how to overcome the difficulty. If more than one, i. e. not only the best of the descendants, become parents of the next generation and recombination by sexual propagation takes place, i.e. mixing of the information gathered by different individuals during the course of evolution, then stagnation can be overcome. Now the convergence rate steeply goes up with the population size. On a conventional one-processor computer the parallelism of that scheme cannot be realized, but multi-processor machines are coming. That is why all figures show the progress over the number of generations and not over computing time. The total number of individuals must not increase with the number of object parameters, however, if the problem complexity remains constant like with objective functions  $F_1$  and  $F_2$  above.

The overwhelming success of recombination demonstrated here, may explain the early appearance of sexual propagation on earth. But it is improbable that only the additional variability provokes the success. A better explanation might be the following: The typical situation during the meliorization process is ridge following. Within a population some individuals have a position on one side, others on the other side of the ridge. Mixing genetic information is a means of riding the ridge more efficiently. A similar argument holds for mixing the step sizes: Individuals on one side of the ridge have 'internal models' (made up of the set of step size relations) of the response surface which are different from those on the other side. Even if both models are wrong, at least in the long term, since both may be locally adapted only (if the 'model' learned is not a permanent natural law), some 'mean' model (or better: hypothesis) may turn out to be more useful for the future. Simply speaking, one may say that 'natural intelligence' is distributed.

Now the question of the appropriate selection pressure prevails: How many of the descendants should be selected as new parents. The answer - at least for the objective function chosen - is given by

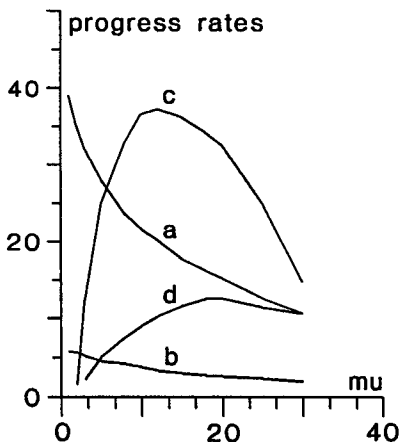


Figure 4:

Comparing progress rates per 1000 generations of different  $(\mu, 100)$ -E.S.'s over  $\mu$ , the number of parents

- a) with prefixed optimum scaling ( $\sigma_{a,i}^0 = c/(i)^{1/2}$ )
- b) with prefixed arbitrary scaling ( $\sigma_{a,i}^0 = c$ )
- c) with adaptive scaling by means of individual learning plus recombination
- d) with adaptive scaling by recombination only

figure 4. All other conditions being held constant, including the number of descendants  $\lambda=100$  within one generation, only  $\mu$ , the number of parents, was changed. Three cases were investigated for function  $F_2$ :

Whereas in both cases a) and b)  $\mu=1$  is the best choice, in a learning situation (cases c and d), it is better, even necessary, to increase  $\mu$  far beyond 1. The diagram moreover demonstrates the effectivity of the collective learning process. Under proper conditions nearly the same convergence rate as with total knowledge of the optimum scaling can be achieved - even with lower selection pressure. This is the third surprise. Recombination alone (case d) is not as successful, however, as together with individual mutations (case c) of the genetically transmitted information about the different step sizes (which represent a simple internal model of the current/local environment).

#### Learning of a metric, and the epigenetic apparatus

Topologies of vitality response surfaces normally are not as simple as assumed above. The next possible complication is to incline the main axes of the hyper-ellipsoids which form the subspaces  $F = \text{const.}$  Now scaling alone does not help in achieving optimum performance. What can nature do, what has it done, to overcome the difficulty? In many cases one has found that a single gene influences several phenotypic characteristics (pleiotropy) and vice versa (polygeny). These are the two sides of the same coin, which is correlation, the perhaps best known example of it being allometric growth. The transmission mechanism between genotype and phenotype, called epigenetic apparatus, in a first order may be approximated by linear correlation. In addition to individual step sizes, now correlation coefficients or

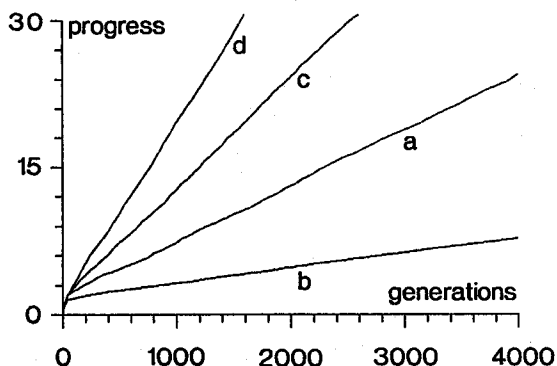


Figure 5: Learning of a metric

- a) (1,100)- E.S. with constant but arbitrary scaling
- b) (15,100)- E.S. under the same conditions, i. e. without recombination
- c) (15,100)- E.S. with recombination and adaptive individual step sizes
- d) (15,100)- E.S. as before, with additional learning of linear correlations between the phenotypic mutations

angles of inclination of the ellipsoid, forming the surface of constant probability density of a mutation, have to be learned. Figure 5 shows first results for the objective function

$$F_3 = \sum_{i=1}^n \left( \sum_{j=1}^i x_j \right)^2$$

Four cases were simulated, three of them corresponding to those of figure 3.

In both cases c) and d), recombination, intermediate for both the object parameters and the step sizes, was used. It is obvious that these sampling conditions bear a variety of possibilities with respect to the mutabilities of step sizes and correlation angles so that simulations c) and d) might not yet represent the best choices. Nevertheless the results show how much may be gained in terms of progress velocity by allowing to learn a simple 'internal model' of the topology of the environment, the 'real world'. Nevertheless, such a model in most cases will not be a correct 'theory', but simply a useful local or temporal hypothesis. Especially and again, no single individual has the best long-term knowledge about the 'correct' world model. This knowledge is partial, temporal only, and distributed.

#### Gradualism or punctualism, and so-called long waves

Up until now all figures showing the evolutionary progress over time or generations were drawn for objective function values only every 50th generation and for the mean of the (parents) population moreover. If we take a closer look by picking out one of the decision variables, e.g.  $x_{15}$  for function  $F_2$ , and look at it at every generation (figure 6, curve a) then the picture reveals more details.

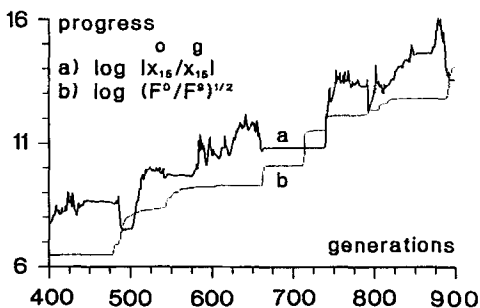


Figure 6: Time cut of one of the variables within a (3,100)-E.S. for  $F_2$ .

It depends on the density of the historical record whether we may speak of a gradual or a punctualistic process (see e. g. Stanley /12/). Due to the fact that the objective function (curve b) depends on many parameters, a single one of them, like  $x_{15}$ , must not

resemble the progress as a whole. Great success in one direction forgives regression in others. And, for sure, looking at some arbitrary cut of the time record, one might get the impression of stochastically disturbed 'long waves' (normally three) with a more or less constant period. Even more aggregated sub-objectives, like the GNP of a nation, could exhibit such behaviour, if the underlying process operates left of the maximum of curve c) in diagram 4, as was the case here with  $\mu=3$  and  $\lambda=100$ .



## Conclusions

Many people today, when speaking about long term planning, environmental forecasting, technology assessment etc., are embarrassed by the degree of our ignorance. Very often then they speak of the uncertainties involved. But looking more precisely, isn't it a fact that there are, at the same time and with access to the same data, different certainties, i.e. different interpretations of the past and different aspirations for the future, or, in other words, different 'internal models' of the world? In the light of the simulation results above, one should appreciate, not regret, that. Due to the findings of a rather new field of science, i.e. nonlinear dynamics, we must admit that knowledge about the long-term future is principally unavailable for an open dissipative system operating far off of equilibria. We really are groping in the dark /13/. Therefore we should not try to establish one best model of the world, but make the best of the different individual ones of the ridge we are trying to follow without clairvoyance. Even if all of them were wrong they might as well be worthwhile to be recombined with each other. Instead of relying upon too strong competition, which leads to stagnation, as we have seen, we better should agree upon further experiments in cooperation. Solidarity should help those who have exploited the situation by means of a-posteriori failures, however.

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