

# Data Structures and Dynamic Optimization with Matlab

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# Preface

This is a work-in-progress [website](#) of support files for using matlab. Materials gathered from various [projects](#) in which matlab is used. Matlab files are linked below by section with livescript files. Tested with [Matlab](#) 2019a ([The MathWorks Inc, 2019](#)). This is not a Matlab package, but a list of examples in PDF/HTML/Mlx formats. [MEconTools](#) is a package that can be installed with tools used in projects involving matlab code.

Bullet points in the Appendix show which matlab functions/commands are used to achieve various objectives. The goal of this repository is to make it easier to find/re-use codes produced for various projects. Some functions also rely on or correspond to functions from [MEconTools](#) ([Wang, 2020](#)).

From other repositories: For dynamic borrowing and savings problems, see [Dynamic Asset Repository](#); For code examples, see also [R Example Code](#), and [Stata Example Code](#); For intro stat with R, see [Intro Statistics for Undergraduates](#), and intro Math with Matlab, see [Intro Mathematics for Economists](#). See [here](#) for all of [Fan](#)'s public repositories.

The site is built using [Bookdown](#) ([Xie, 2020](#)).

Please contact [FanWangEcon](#) for issues or problems.



# Chapter 1

## Data Structures

### 1.1 Matrices and Arrays

#### 1.1.1 Array Reshape, Repeat and Expand Examples

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

##### 1.1.1.1 Basic Examples of Reshape

```
a = [1,2,3,4,5,6]';  
b = reshape(a, [3,2])
```

```
b = 3x2  
     1     4  
     2     5  
     3     6
```

```
b(:)
```

```
ans = 6x1  
     1  
     2  
     3  
     4  
     5  
     6
```

```
a = [1,2,3;4,5,6;7,8,9;10,11,12]'
```

```
a = 3x4  
     1     4     7    10  
     2     5     8    11  
     3     6     9    12
```

```
b = reshape(a, [6,2])
```

```
b = 6x2  
     1     7  
     2     8  
     3     9  
     4    10  
     5    11
```

6      12

### 1.1.1.2 Stack Two Matrix of Equal Column Count Together

```
a = [1,2;3,4];
a_stacked = [a;a;a];
disp(a_stacked);
```

```
1     2
3     4
1     2
3     4
1     2
3     4
```

### 1.1.1.3 Repeat/Duplicate Matrix Downwards

There is a 2 by 3 matrix, to be repeated 4 times, downwards. This is useful for replicating data matrix for say counterfactual purposes.

Below, we have two ways of repeating a matrix downwards. Copy as whole, or copy row by row.

```
row_count = 2;
col_count = 3;
repeat_mat_count = 2;

data_vec = 1:(row_count*col_count);
searchMatrix = reshape(data_vec,row_count,col_count);

% To repeat matrix downwards
rep_rows_idx = [1:row_count]*ones(1,repeat_mat_count);
rep_rows_idx = rep_rows_idx(:);

rep_cols_idx = [1:col_count];
rep_cols_idx = rep_cols_idx(:);

searchMatrixRep_stack = searchMatrix(rep_rows_idx, rep_cols_idx);

% To insert repeated rows following original rows
rep_rows_idx = ([1:row_count]*ones(1,repeat_mat_count))';
rep_rows_idx = rep_rows_idx(:);

searchMatrixRep_dup = searchMatrix(rep_rows_idx, rep_cols_idx);

disp(searchMatrix)

1     3     5
2     4     6

disp(searchMatrixRep_stack)

1     3     5
2     4     6
1     3     5
2     4     6

disp(searchMatrixRep_dup)

1     3     5
1     3     5
```



```

2      4      6
2      4      6

```

#### 1.1.1.4 Index Dimension Transform

```

it_inner_fin = 5; it_outter_fin = 3;
it_inner_cur = it_outter_fin it_outter_cur = it_inner_fin
ar_it_cols_idx = 1:1:(it_inner_fin*it_outter_fin) ar_it_cols_inner_dim = repmat(1:it_inner_cur,
                                         it_outter_cur,1
) ar_it_cols_inner_dim(:)'
mt_it_cols_idx = reshape(ar_it_cols_idx,
                         it_inner_cur,it_outter_cur
)' mt_it_cols_idx(:)'
it_inner_fin = 5;
it_outter_fin = 3;

ar_it_cols_idx = 1:1:(it_inner_fin*it_outter_fin)

ar_it_cols_idx = 1x15
    1     2     3     4     5     6     7     8     9    10    11    12    13    14    15

mt_it_cols_idx = reshape(ar_it_cols_idx, [it_outter_fin, it_inner_fin])'

mt_it_cols_idx = 5x3
    1     2     3
    4     5     6
    7     8     9
   10    11    12
   13    14    15

mt_it_cols_idx(:)'

ans = 1x15
    1     4     7    10    13     2     5     8    11    14     3     6     9    12    15

```

### 1.1.2 Array Index Slicing and Subsetting to Replace and Expand

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 1.1.2.1 Index Select Rows and Columns of a 2D matrix

In the example below, select by entire rows and columns:

```

% There is a 2D Matrix
rng(123);
randMatZ = rand(3,6);
disp(randMatZ);

    0.6965    0.5513    0.9808    0.3921    0.4386    0.7380
    0.2861    0.7195    0.6848    0.3432    0.0597    0.1825
    0.2269    0.4231    0.4809    0.7290    0.3980    0.1755

% Duplicate Select Row sand Columns of Elements

```

```
disp(randMatZ([1,2,3,3,3,2], [1,1,2,2,2,1]))
```

0.6965	0.6965	0.5513	0.5513	0.5513	0.6965
0.2861	0.2861	0.7195	0.7195	0.7195	0.2861
0.2269	0.2269	0.4231	0.4231	0.4231	0.2269
0.2269	0.2269	0.4231	0.4231	0.4231	0.2269
0.2269	0.2269	0.4231	0.4231	0.4231	0.2269
0.2861	0.2861	0.7195	0.7195	0.7195	0.2861

### 1.1.2.2 Index Select Set of Elements from 2D matrix

Rather than selecting entire rows and columns, suppose we want to select only one element at row 1 col 2, the element at row 2 col 4, element at row 5 col 1, etc.

```
% Select Subset of Elements
it_row_idx = [1,2,3,1,3,2];
it_col_idx = [1,1,5,4,2,3];
% Select sub2idx
ar_lin_idx = sub2ind(size(randMatZ), it_row_idx, it_col_idx);
ar_sel_val = randMatZ(ar_lin_idx);
disp(ar_sel_val');
```

0.6965
0.2861
0.3980
0.3921
0.4231
0.6848

### 1.1.2.3 Find Closest Element of Array to Each Element of Another Array

Given scalar value, find the closest value in array:

```
fl_a = 3.4;
ar_bb = [1,2,3,4];
[fl_min, it_min_idx] = min(abs(ar_bb-fl_a));
disp(it_min_idx);
```

3

Given a scalar value and an array, find the closest smaller value in the array to the scalar value:

```
fl_a = 2.1;
ar_bb = [1,2,3,4];
disp(sum(ar_bb<fl_a));
```

2

Array A is between 0 and 1, on some grid. Array B is also between 0 and 1, but scattered. Find for each element of B the index of the closest value on A that is smaller than the element in B.

```
rng(1234);
ar_a = linspace(0,10,5);
ar_b = rand([5,1])*10;
mt_a_less_b = ar_a<ar_b;
mt_a_less_b_idx = sum(ar_a<ar_b, 2);
disp(ar_a);
```

0	2.5000	5.0000	7.5000	10.0000
---	--------	--------	--------	---------

```
disp(ar_b);
```

```

1.9152
6.2211
4.3773
7.8536
7.7998

disp(mt_a_less_b);

1   0   0   0   0
1   1   1   0   0
1   1   0   0   0
1   1   1   1   0
1   1   1   1   0

disp(mt_a_less_b_idx);

1
3
2
4
4

```

#### 1.1.2.4 Matlab Index based Replacement of Subset of Matrix Values

```

rng(123);
randMatZ = rand(3,6)+1;
randMat = rand(3,6)-0.5;

output = max(-randMat,0);
randMatZ(output==0) = 999;
min(randMatZ,[],2);
randMatZ((max(-randMat,0))==0) = 999;
disp(randMatZ);

999.0000  999.0000  999.0000    1.3921    1.4386    1.7380
999.0000  999.0000    1.6848    1.3432    1.0597    1.1825
999.0000  999.0000    1.4809  999.0000    1.3980    1.1755

disp(min(randMatZ,[],2));

1.3921
1.0597
1.1755

```

#### 1.1.2.5 Matlab Matrix Index Based Matrix Expansion (Manual)

In the example below, we start with a 4 by 2 matrix, than we expand specific rows and columns of the matrix. Specifically, we expand the matrix such that the result matrix repeats the 1st, 2nd, 1st, 2nd, then 3rd, than 1st, 1st, and 1st rows. And repeats column 1, then 2nd, then 2nd, then 2nd, and finally the first column.

```

% Original Matrix
Z = 2;
N = 2;
Q = 2;
base_mat = reshape(1:(Z*N*Q),Z*N,Q);
disp(base_mat);

```

```

1      5

```

```

2      6
3      7
4      8

% Expanded Matrix
base_expand = base_mat([1,2,1,2,3,1,1,1],[1,2,2,2,1]);
disp(base_expand);

```

```

1      5      5      5      1
2      6      6      6      2
1      5      5      5      1
2      6      6      6      2
3      7      7      7      3
1      5      5      5      1
1      5      5      5      1
1      5      5      5      1

```

### 1.1.2.6 Duplicate Matrix Downwards N times Using Index

The example here has the same idea, but we do the operations above in a more automated way. This could be done using alternative methods.

```

% Original Matrix
Z = 2;
N = 2;
Q = 2;
base_mat = reshape(1:(Z*N*Q),Z*N,Q);
disp(base_mat);

```

```

1      5
2      6
3      7
4      8

```

```

% Generate row Index many times automatically depending on how many times
% to replicate
vmat_repeat_count = 3;
vmat_reindex_rows_repeat = [1:(Z*N)]'* ones(1,vmat_repeat_count);
vmat_reindex_rows_repeat = vmat_reindex_rows_repeat(:);
disp(vmat_reindex_rows_repeat');

```

```

1      2      3      4      1      2      3      4      1      2      3      4

```

```

% Duplicate Matrix by the Rows specified above, and using the same number
% of columns.
mat_repdown = base_mat(vmat_reindex_rows_repeat(:), 1:Q);
disp(mat_repdown');

```

```

1      2      3      4      1      2      3      4      1      2      3      4
5      6      7      8      5      6      7      8      5      6      7      8

```

### 1.1.2.7 Given ND Array, Get Row and Column (and other dimension) Index With Value Conditioning

There is a matrix where some values are equal to 1 (based on some prior selection), get the row and column index of the matrix.

```

% Some matrix with 1s
rng(123);
mt_some_ones = rand(3,3);

```

```

disp(mt_some_ones);

    0.6965    0.5513    0.9808
    0.2861    0.7195    0.6848
    0.2269    0.4231    0.4809

% find the location of the ones
[r_idx, c_idx] = find(mt_some_ones<0.5);
% the set of locations
disp([r_idx,c_idx]);

     2     1
     3     1
     3     2
     3     3

```

Now do the same three with a three dimensional array:

```

% Some matrix with 1s
rng(123);
mn3_some_ones = rand(3,3,3);
disp(mn3_some_ones);

(:, :, 1) =

    0.6965    0.5513    0.9808
    0.2861    0.7195    0.6848
    0.2269    0.4231    0.4809

(:, :, 2) =

    0.3921    0.4386    0.7380
    0.3432    0.0597    0.1825
    0.7290    0.3980    0.1755

(:, :, 3) =

    0.5316    0.8494    0.7224
    0.5318    0.7245    0.3230
    0.6344    0.6110    0.3618

% find the location of the ones
[d1_idx, d2_idx, d3_idx] = ind2sub(size(mn3_some_ones), find(mn3_some_ones<0.5));
% the set of locations
disp([d1_idx, d2_idx, d3_idx]);

     2     1     1
     3     1     1
     3     2     1
     3     3     1
     1     1     2
     2     1     2
     1     2     2
     2     2     2
     3     2     2
     2     3     2
     3     3     2

```

```

2      3      3
3      3      3

```

### 1.1.2.8 Max of Matrix column by Column Linear to 2d Index

Finding max of matrix column by column, then obtain the linear index associated with the max values.

```

randMat = rand(5,3);
disp(randMat);

0.4264    0.1156    0.4830
0.8934    0.3173    0.9856
0.9442    0.4148    0.5195
0.5018    0.8663    0.6129
0.6240    0.2505    0.1206

[maxVal maxIndex] = max(randMat);
linearIndex = sub2ind(size(randMat),maxIndex,(1:1:size(randMat,2)))

linearIndex = 1x3
           3      9     12

randMat(linearIndex)

ans = 1x3
    0.9442    0.8663    0.9856

t_pV = [1,2;3,4;5,6];
t_pV_Ind = [1,1;0,0;1,1];
[maxVal maxIndex] = max(t_pV(t_pV_Ind==1))

maxVal = 6
maxIndex = 4

```

### 1.1.2.9 Given Array of size M, Select N somewhat equi-distance elements

```

% Subset count
it_n = 5;

% Example 1, long array
ar_fl_a = 1:1.1:100;
ar_it_subset_idx = unique(round(((0:1:(it_n-1))/(it_n-1))*(length(ar_fl_a)-1)+1));
ar_fl_a_subset = ar_fl_a(ar_it_subset_idx);
disp(ar_fl_a_subset);

```

```

1.0000    26.3000    50.5000    75.8000   100.0000

```

```

% Example 2, Short Array
ar_fl_a = 1:1.1:3;
ar_it_subset_idx = unique(round(((0:1:(it_n-1))/(it_n-1))*(length(ar_fl_a)-1)+1));
ar_fl_a_subset = ar_fl_a(ar_it_subset_idx);
disp(ar_fl_a_subset);

```

```

1.0000    2.1000

```

```

% Write As function

```

```

f_subset = @(it_subset_n, it_ar_n) unique(round(((0:1:(it_subset_n-1))/(it_subset_n-1))*(it_ar_n-1)+

```

```
% Select 5 out of 10
disp(f_subset(5, 10));
```

```
1      3      6      8     10
```

```
% Select 10 out of 5
disp(f_subset(10, 5));
```

```
1      2      3      4      5
```

```
% Select 5 out of 5
disp(f_subset(5, 5));
```

```
1      2      3      4      5
```

### 1.1.3 3D, 4D, ND Arrays Reshape and Rearrange Dimensions

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 1.1.3.1 3D Array to Cell Array of Matrix Split by Last Dimension

Convert Multi-dimensional arrays to a cell array consistent of two dimensional arrays. In this example, we split by the 3rd dimension, so the number of output matrixes is equal to the length of the 3rd dimension.

First create a three dimensional array, two matrixes that are 4 by 3 each:

```
% Create a 3D Array
rng(123);
mn_rand = rand(4,3,2);
disp(mn_rand);
```

```
(:,:,1) =
```

```
0.6965    0.7195    0.4809
0.2861    0.4231    0.3921
0.2269    0.9808    0.3432
0.5513    0.6848    0.7290
```

```
(:,:,2) =
```

```
0.4386    0.1825    0.6344
0.0597    0.1755    0.8494
0.3980    0.5316    0.7245
0.7380    0.5318    0.6110
```

Now convert the 3 dimensional array to a 2 by 1 cell array that contains matrixes in each cell:

```
% Squeeze 3D array to a Cell array of matrixes
cl_mn_rand = squeeze(num2cell(mn_rand, [1,2]));
celldisp(cl_mn_rand);
```

```
cl_mn_rand{1} =
```

```
0.6965    0.7195    0.4809
```

0.2861	0.4231	0.3921
0.2269	0.9808	0.3432
0.5513	0.6848	0.7290

```
cl_mn_rand{2} =
```

0.4386	0.1825	0.6344
0.0597	0.1755	0.8494
0.3980	0.5316	0.7245
0.7380	0.5318	0.6110

### 1.1.3.2 4D Array to Cell Array of Matrix Split by Last Two Dimensions

Convert 4D Multi-dimensional arrays to a cell array consistent of two dimensional arrays. In this example, the first two dimensions determine the resulting matrix size, the the 3rd and the 4th dimensions are categorical.

First create a four dimensional array, four matrixes stored each matrix is 2 by 2:

```
% Create a 3D Array
```

```
rng(123);
```

```
mn_rand = rand(2,2,2,2);
```

```
disp(mn_rand);
```

```
(:,:,1,1) =
```

0.6965	0.2269
0.2861	0.5513

```
(:,:,2,1) =
```

0.7195	0.9808
0.4231	0.6848

```
(:,:,1,2) =
```

0.4809	0.3432
0.3921	0.7290

```
(:,:,2,2) =
```

0.4386	0.3980
0.0597	0.7380

Now convert the 4 dimensional array to a 2 by 2 cell array that contains matrixes in each cell:

```
% Squeeze 3D array to a Cell array of matrixes
```

```
cl_mn_rand = squeeze(num2cell(mn_rand, [1,2]));
```

```
celldisp(cl_mn_rand);
```

```
cl_mn_rand{1,1} =
```

0.6965	0.2269
0.2861	0.5513



```
cl_mn_rand{2,1} =

    0.7195    0.9808
    0.4231    0.6848
```

```
cl_mn_rand{1,2} =

    0.4809    0.3432
    0.3921    0.7290
```

```
cl_mn_rand{2,2} =

    0.4386    0.3980
    0.0597    0.7380
```

### 1.1.3.3 4D Array to Cell Array of Matrix Split by First and Fourth Dimensions Rearrange Dimensions

Suppose we store policy and value function given four state variables. The first one is age, the second one is asset, the third one is shock, and the fourth one is the number of kids. We start out with a four dimensional matrix. The objective is to create a two dimensional cell array as output where indexed by the 1st and 4th dimension of the underlying numeric array, and the elements of the 2D cell array are matrixes.

This is achieved by the [permute](#) function. We first rearrange the matrix, so that the 2nd and 3rd dimensions become the 1st and 2nd, then we use the technique used above to squeeze out the first two dimensions as matrixes with the last two as categories.

First, generate the 2 by 2 by 2 by 2, (Age, A, Z, Kids Count), matrix:

```
% Create a 3D Array
rng(123);
% (Age, A, Z, Kids Count)
mn_rand = rand(2,2,2,2);
```

Second, loop out the (A,Z) matrix by Age and Kids Count, this shows us what we want to achieve. Note that each row is Age, each column is A, each submatrix is z, and each super-matrix is kid-count. So from slicing, each column printed out are different value of A, the two submatrixes printed out are for each z. For the output structure where we want a (A,Z) matrix, the columns need to become rows, and the submatrix need to become columns.

```
% Show Matrix by Age and Kids
for it_age = 1:size(mn_rand,1)
    for it_kids = 1:size(mn_rand,4)
        disp(strcat(['it_age:' num2str(it_age) ' ', it_kids:' num2str(it_kids)]))
        disp(mn_rand(it_age,:,: ,it_kids));
    end
end

it_age:1, it_kids:1
(:, :, 1) =
```

```
    0.6965    0.2269
```

```
(:,:,2) =

    0.7195    0.9808
it_age:1, it_kids:2
(:,:,1) =
```

```
    0.4809    0.3432
```

```
(:,:,2) =

    0.4386    0.3980
it_age:2, it_kids:1
(:,:,1) =
```

```
    0.2861    0.5513
```

```
(:,:,2) =

    0.4231    0.6848
it_age:2, it_kids:2
(:,:,1) =
```

```
    0.3921    0.7290
```

```
(:,:,2) =

    0.0597    0.7380
```

Third, we permute the matrix and squeeze to arrive at the 2 by 2 cell, note that step two is just to show via loop what we should get:

```
% Rearrange dimensions
mn_rand_2314 = permute(mn_rand, [2,3,1,4]);
% Squeeze the first two dimensions as before
cl_mn_rand = squeeze(num2cell(mn_rand_2314, [1,2]));
% show
celldisp(cl_mn_rand);
```

```
cl_mn_rand{1,1} =

    0.6965    0.7195
    0.2269    0.9808
```

```
cl_mn_rand{2,1} =

    0.2861    0.4231
    0.5513    0.6848
```

```
cl_mn_rand{1,2} =
```

0.4809	0.4386
0.3432	0.3980

```
cl_mn_rand{2,2} =
```

0.3921	0.0597
0.7290	0.7380

#### 1.1.3.4 ND Array Summarize in Table

Given an ND dataframe, summarize the first two dimensions. For each possible combination of the 3rd and 4th dimension, generate mean, sd, min and max over the matrix of the first two dimensions. This is similar to a tabulation function.

First, we generate several array of information:

```
% Initialize and Squeeze
rng(123);
mn_rand = rand(2,2,2,2);
cln_mt_rand = squeeze(num2cell(mn_rand, [1,2]));
cl_mt_rand = cln_mt_rand(:);
celldisp(cl_mt_rand);
```

```
cl_mt_rand{1} =
```

0.6965	0.2269
0.2861	0.5513

```
cl_mt_rand{2} =
```

0.7195	0.9808
0.4231	0.6848

```
cl_mt_rand{3} =
```

0.4809	0.3432
0.3921	0.7290

```
cl_mt_rand{4} =
```

0.4386	0.3980
0.0597	0.7380

Second, create two arrays that tracks for each element of `cl_mt_rand`, which one of the 3rd and 4th dimensions they correspond to:

```
ar_dim_3 = [31,32]';
ar_dim_4 = [41,42]';
[mt_dim_3, mt_dim_4] = ndgrid(ar_dim_3, ar_dim_4);
ar_dim_3 = mt_dim_3(:);
ar_dim_4 = mt_dim_4(:);
```

Third, summarize each matrix:

```
% Over of matrix and summarize
ar_mean = zeros(size(cl_mt_rand));
ar_std = zeros(size(cl_mt_rand));
for it_mt=1:length(cl_mt_rand)
    mt_cur = cl_mt_rand{it_mt};
    ar_mean(it_mt) = mean(mt_cur, 'all');
    ar_std(it_mt) = std(mt_cur, [], 'all');
end
```

Fourth Construct a Table

```
% Constructe Table
tb_rowcols_tab = array2table([(1:length(cl_mt_rand))', ...
    ar_dim_3, ar_dim_4, ar_mean, ar_std]);
tb_rowcols_tab.Properties.VariableNames = ...
    matlab.lang.makeValidName(["i", "dim3", "dim4", "mean", "std"]);
disp(tb_rowcols_tab);
```

i	dim3	dim4	mean	std
1	31	41	0.44019	0.22156
2	32	41	0.70204	0.2281
3	31	42	0.48632	0.17157
4	32	42	0.40857	0.27764

### 1.1.3.5 ND Array Two-Way Summarize in Table

Given dataframe as above, but we now want to add to the resulting summary table additional columns, rather than taking the means of the entire matrix in the first two dimensions, we only take average with respect to the rows, the first dimension, the second dimension show up as counmn statistics names, still multiple stats. The results worked out here are embedded in the [fx\\_summ\\_nd\\_array](#) function of the [MEconTools](#) Package.

First, we generate several array of information:

```
% dimension names
st_title = 'Summarize values over a conditional on z (columns) and kids and marriage (rows)';
st_dim_1 = 'a';
st_dim_2 = 'z';
st_dim_3 = 'kid';
st_dim_4 = 'marriage';
% 3rd and fourth dimension values
ar_dim_2 = [-3, -1, 1, 3];
ar_dim_3 = [1,2,3];
ar_dim_4 = [0,1];
% Initialize and Squeeze
rng(123);
mn_rand = rand(10,4,3,2);
cln_mt_rand = squeeze(num2cell(mn_rand, [1,2]));
cl_mt_rand = cln_mt_rand(:);
```

Second, create two arrays that tracks for each element of cl\_mt\_rand, which one of the 3rd and 4th dimensions they correspond to:

```
[mt_dim_3, mt_dim_4] = ndgrid(ar_dim_3', ar_dim_4');
ar_dim_3 = mt_dim_3(:);
ar_dim_4 = mt_dim_4(:);
```

Third, summarize each matrix:

```
% Over of matrix and summarize
mt_mean = zeros(length(cl_mt_rand), size(mn_rand,2));
mt_std = zeros(length(cl_mt_rand), size(mn_rand,2));
for it_mt=1:length(cl_mt_rand)
    mt_cur = cl_mt_rand{it_mt};
    mt_mean(it_mt,:) = mean(mt_cur, 1);
    mt_std(it_mt,:) = std(mt_cur, [], 1);
end

Fourth Construct a Table

% Constructe Table
tb_rowcols_tab = array2table([(1:length(cl_mt_rand))', ...
    ar_dim_3, ar_dim_4, mt_mean, mt_std]);
% Column Names
cl_col_names_cate_dims = [string(st_dim_3), string(st_dim_4)];
cl_col_names_mn = strcat('mean_', st_dim_2, string(ar_dim_2));
cl_col_names_sd = strcat('sd_', st_dim_2, string(ar_dim_2));
tb_rowcols_tab.Properties.VariableNames = ...
    matlab.lang.makeValidName(["group", cl_col_names_cate_dims, cl_col_names_mn, cl_col_names_sd]);
% disp(['xxx ' st_title ' xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx']);
disp(tb_rowcols_tab);
```

group	kid	marriage	mean_z_3	mean_z_1	mean_z1	mean_z3	sd_z_3	sd_z_1
-----	---	-----	-----	-----	-----	-----	-----	-----
1	1	0	0.5442	0.41278	0.53795	0.49542	0.22935	0.22945
2	2	0	0.51894	0.52262	0.52544	0.45066	0.26787	0.23615
3	3	0	0.48248	0.5238	0.50392	0.46534	0.27009	0.26676
4	1	1	0.58343	0.50529	0.54361	0.5006	0.29578	0.30182
5	2	1	0.58408	0.45941	0.50466	0.40081	0.25026	0.34704
6	3	1	0.51148	0.49531	0.48963	0.47698	0.3271	0.24336

### 1.1.4 Array Broadcast and Expansion Examples

back to [Fan's Reusable Matlab Repository](#) or [Dynamic Asset Repository](#).

Matrix broadcasting was added to matlab's recent editions. This is an important step for vectorizing codes. Proper usage of broadcasting reduces memory allocation requirements for matrix matrix operations.

#### 1.1.4.1 Broadcasting with A Row and a Column

Below we add together a 1 by 3 and 4 by 1 array, that should not work. With broadcasting, it is assumed that we will mesh the arrays and then sum up the meshed matrixes.

```
clear all
ar_A = [1,2,3];
ar_B = [4,3,2,1]';
disp(size(ar_A));

1      3

disp(size(ar_B));

4      1

mt_A_B_broadcast = ar_A + ar_B;
disp(mt_A_B_broadcast);

5      6      7
```

4	5	6
3	4	5
2	3	4

```
mt_A_B_broadcast_product = ar_A.*ar_B;
disp(mt_A_B_broadcast_product);
```

4	8	12
3	6	9
2	4	6
1	2	3

#### 1.1.4.2 Broadcasting with One Row and One Matrix

Below we add together a 1 by 3 and 4 by 3 matrix, that should not work. With broadcasting, it is assumed that we will repeat the array four times, duplicating the single row four times, so the matrix dimensions match up.

```
clear all
ar_A = [1,2,3];
mt_B = [4,3,2,1;5,4,3,2;6,5,4,3]';
disp(size(ar_A));
```

1	3
---	---

```
disp(size(mt_B));
```

4	3
---	---

```
mt_A_B_broadcast = ar_A + mt_B;
disp(mt_A_B_broadcast);
```

5	7	9
4	6	8
3	5	7
2	4	6

```
mt_A_B_broadcast_product = ar_A.*mt_B;
disp(mt_A_B_broadcast_product);
```

4	10	18
3	8	15
2	6	12
1	4	9

#### 1.1.4.3 Broadcasting with One Column and One Matrix

Below we add together a 4 by 1 and 4 by 3 matrix, that should not work. With broadcasting, it is assumed that we will repeat the column three times, duplicating the single column three times, so the matrix dimensions match up.

```
clear all
ar_A = [4,3,2,1]';
mt_B = [4,3,2,1;5,4,3,2;6,5,4,3]';
disp(size(ar_A));
```

4	1
---	---

```
disp(size(mt_B));
```

```

4      3

mt_A_B_broadcast = ar_A + mt_B;
disp(mt_A_B_broadcast);

8      9      10
6      7      8
4      5      6
2      3      4

mt_A_B_broadcast_product = ar_A.*mt_B;
disp(mt_A_B_broadcast_product);

16     20     24
9      12     15
4       6      8
1       2      3

```

#### 1.1.4.4 Expand with Broadcast, Percentage Choice grids

```

clear all
ar_w_perc = [0.1,0.5,0.9]

ar_w_perc = 1x3
    0.1000    0.5000    0.9000

ar_w_level = [-2,0,2]

ar_w_level = 1x3
    -2         0         2

fl_b_bd = -4

fl_b_bd = -4

ar_k_max = ar_w_level - fl_b_bd

ar_k_max = 1x3
         2         4         6

ar_ak_perc = [0.1,0.3,0.7,0.9]

ar_ak_perc = 1x4
    0.1000    0.3000    0.7000    0.9000

mt_k = (ar_k_max'*ar_ak_perc)

mt_k = 4x3
    0.2000    0.4000    0.6000
    0.6000    1.2000    1.8000
    1.4000    2.8000    4.2000
    1.8000    3.6000    5.4000

mt_a = (ar_w_level - mt_k)

mt_a = 4x3
   -2.2000   -0.4000    1.4000
   -2.6000   -1.2000    0.2000

```

```
-3.4000  -2.8000  -2.2000
-3.8000  -3.6000  -3.4000
```

#### 1.1.4.5 Expand Matrix Twice

```
clear all
% Same as above
ar_w_level = [-2,-1,-0.1]

ar_w_level = 1x3
    -2.0000    -1.0000    -0.1000

fl_b_bd = -4

fl_b_bd = -4

ar_k_max = ar_w_level - fl_b_bd

ar_k_max = 1x3
     2.0000     3.0000     3.9000

ar_ak_perc = [0.001, 0.1,0.3,0.7,0.9, 0.999]

ar_ak_perc = 1x6
     0.0010     0.1000     0.3000     0.7000     0.9000     0.9990

mt_k = (ar_k_max'*ar_ak_perc)'

mt_k = 6x3
     0.0020     0.0030     0.0039
     0.2000     0.3000     0.3900
     0.6000     0.9000     1.1700
     1.4000     2.1000     2.7300
     1.8000     2.7000     3.5100
     1.9980     2.9970     3.8961

mt_a = (ar_w_level - mt_k)

mt_a = 6x3
    -2.0020    -1.0030    -0.1039
    -2.2000    -1.3000    -0.4900
    -2.6000    -1.9000    -1.2700
    -3.4000    -3.1000    -2.8300
    -3.8000    -3.7000    -3.6100
    -3.9980    -3.9970    -3.9961

% fraction of borrowing for bridge loan
ar_coh_bridge_perc = [0, 0.5, 0.999];

% Expand matrix to include coh percentage dimension
mt_k = repmat(mt_k, [1, length(ar_coh_bridge_perc)])

mt_k = 6x9
     0.0020     0.0030     0.0039     0.0020     0.0030     0.0039     0.0020     0.0030     0.0039
     0.2000     0.3000     0.3900     0.2000     0.3000     0.3900     0.2000     0.3000     0.3900
     0.6000     0.9000     1.1700     0.6000     0.9000     1.1700     0.6000     0.9000     1.1700
     1.4000     2.1000     2.7300     1.4000     2.1000     2.7300     1.4000     2.1000     2.7300
```



```

1.8000    2.7000    3.5100    1.8000    2.7000    3.5100    1.8000    2.7000    3.5100
1.9980    2.9970    3.8961    1.9980    2.9970    3.8961    1.9980    2.9970    3.8961

mt_a = repmat(mt_a, [1, length(ar_coh_bridge_perc)])

mt_a = 6x9
-2.0020   -1.0030   -0.1039   -2.0020   -1.0030   -0.1039   -2.0020   -1.0030   -0.1039
-2.2000   -1.3000   -0.4900   -2.2000   -1.3000   -0.4900   -2.2000   -1.3000   -0.4900
-2.6000   -1.9000   -1.2700   -2.6000   -1.9000   -1.2700   -2.6000   -1.9000   -1.2700
-3.4000   -3.1000   -2.8300   -3.4000   -3.1000   -2.8300   -3.4000   -3.1000   -2.8300
-3.8000   -3.7000   -3.6100   -3.8000   -3.7000   -3.6100   -3.8000   -3.7000   -3.6100
-3.9980   -3.9970   -3.9961   -3.9980   -3.9970   -3.9961   -3.9980   -3.9970   -3.9961

mt_a = mt_a

mt_a = 6x9
-2.0020   -1.0030   -0.1039   -2.0020   -1.0030   -0.1039   -2.0020   -1.0030   -0.1039
-2.2000   -1.3000   -0.4900   -2.2000   -1.3000   -0.4900   -2.2000   -1.3000   -0.4900
-2.6000   -1.9000   -1.2700   -2.6000   -1.9000   -1.2700   -2.6000   -1.9000   -1.2700
-3.4000   -3.1000   -2.8300   -3.4000   -3.1000   -2.8300   -3.4000   -3.1000   -2.8300
-3.8000   -3.7000   -3.6100   -3.8000   -3.7000   -3.6100   -3.8000   -3.7000   -3.6100
-3.9980   -3.9970   -3.9961   -3.9980   -3.9970   -3.9961   -3.9980   -3.9970   -3.9961

% bridge loan component of borrowing
ar_brdige_a = (ar_coh_bridge_perc'*ar_w_level)'

ar_brdige_a = 3x3
    0   -1.0000   -1.9980
    0   -0.5000   -0.9990
    0   -0.0500   -0.0999

ar_brdige_a = ar_brdige_a(:)

ar_brdige_a = 1x9
    0         0         0   -1.0000   -0.5000   -0.0500   -1.9980   -0.9990   -0.0999

% borrowing choices excluding bridge loan
mt_a_nobridge = mt_a - ar_brdige_a

mt_a_nobridge = 6x9
-2.0020   -1.0030   -0.1039   -1.0020   -0.5030   -0.0539   -0.0040   -0.0040   -0.0040
-2.2000   -1.3000   -0.4900   -1.2000   -0.8000   -0.4400   -0.2020   -0.3010   -0.3901
-2.6000   -1.9000   -1.2700   -1.6000   -1.4000   -1.2200   -0.6020   -0.9010   -1.1701
-3.4000   -3.1000   -2.8300   -2.4000   -2.6000   -2.7800   -1.4020   -2.1010   -2.7301
-3.8000   -3.7000   -3.6100   -2.8000   -3.2000   -3.5600   -1.8020   -2.7010   -3.5101
-3.9980   -3.9970   -3.9961   -2.9980   -3.4970   -3.9461   -2.0000   -2.9980   -3.8962

```

### 1.1.5 Grid States, Choices and Optimal Choices Example

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

#### 1.1.5.1 Generate State Grid

There many multiple individuals, each individual's value for each state space variable is different. We duplicate that by shockCount and choicecount:

```

stateCount = 2;
shockCount = 3;
choiceCount = 4;

state1 = rand(1,stateCount)

state1 = 1x2
    0.0571    0.6694

states1ShkDup = state1(ones(shockCount*choiceCount,1), :)

states1ShkDup = 12x2
    0.0571    0.6694
    0.0571    0.6694
    0.0571    0.6694
    0.0571    0.6694
    0.0571    0.6694
    0.0571    0.6694
    0.0571    0.6694
    0.0571    0.6694
    0.0571    0.6694
    0.0571    0.6694
    0.0571    0.6694
    0.0571    0.6694

states1ShkDup(:)

ans = 24x1
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571
    0.0571

```

### 1.1.5.2 Generate Choices

Generate Choice Grid, Example: Each individual has minimal protein and maximal protein they can get. Generate a evenly set grid of choices for each individual from min to max. Individual min and max choice is a function of some component of their state-space, such as wealth/income level, and choice is the quantity of good to purchase.

```

stateCount = 2;
shockCount = 3;
choiceCount = 4;

% 1. Min and Max Choices for each state
minprot_n = floor(rand(1,stateCount)*10)

minprot_n = 1x2
     7     7

maxprot_n = minprot_n + floor(rand(1,stateCount)*10)

maxprot_n = 1x2
    14    12

```

```

% 2. Choice Ratios, ratios of max-min difference
protChoiceGrid = linspace(0,1,choiceCount)

protChoiceGrid = 1x4
    0    0.3333    0.6667    1.0000

% 3. Each column is a different state.
searchMatrix = (protChoiceGrid*(maxprot_n-minprot_n)+minprot_n(ones(choiceCount,1),:))

searchMatrix = 4x2
    7.0000    7.0000
    9.3333    8.6667
   11.6667   10.3333
   14.0000   12.0000

% 4. Each column is a different state, each set of rows is a different shock% for the state. In this
searchMatrix = searchMatrix([1:choiceCount]'* ones(1,shockCount), [1:stateCount]' * ones(1,1))

searchMatrix = 12x2
    7.0000    7.0000
    9.3333    8.6667
   11.6667   10.3333
   14.0000   12.0000
    7.0000    7.0000
    9.3333    8.6667
   11.6667   10.3333
   14.0000   12.0000
    7.0000    7.0000
    9.3333    8.6667

searchMatrix(:)

ans = 24x1
    7.0000
    9.3333
   11.6667
   14.0000
    7.0000
    9.3333
   11.6667
   14.0000
    7.0000
    9.3333

```

### 1.1.5.3 Average Utility over Shocks

Average of Shocks,  $E(\text{value})$  For each STATE and CHOICE, x number of shocks. Need to average over shocks; The raw value output is: STATES \* SHOCKS \* CHOICES; Code below turn into various things, see MATLAB CODE STRUCTURE in oneNOTE GCC working notes

```

shockCount = 2;
choiceCount = 3;
stateCount = 4;

```

```

% 1. VALUE vector (STATES * SHOCKS * CHOICES by 1), this is generated by utility% evaluation function
valuesOri = sort(rand(choiceCount*shockCount*stateCount,1))

```

```

valuesOri = 24x1
    0.0296

```

```

0.1141
0.1472
0.1514
0.1826
0.1936
0.2526
0.2911
0.3257
0.3352

% 2. CHOICES by STATES * SHOCKS (ST1 SK1, ST1 SK2; ST2 SK1, etc), each% column are values for differ
values = reshape(valuesOri,[choiceCount,shockCount*stateCount])

values = 3x8
    0.0296    0.1514    0.2526    0.3352    0.5939    0.7065    0.8791    0.9204
    0.1141    0.1826    0.2911    0.3480    0.5992    0.7267    0.9001    0.9508
    0.1472    0.1936    0.3257    0.4578    0.6576    0.7792    0.9018    0.9658

% 3. SHOCKS by CHOICES * STATES (CH1 ST1, CH1 ST2; CH2 ST1, etc), each% column are two shocks for ea
values = reshape(values',[shockCount, choiceCount*stateCount])

values = 2x12
    0.0296    0.2526    0.5939    0.8791    0.1141    0.2911    0.5992    0.9001    0.1472    0.3257
    0.1514    0.3352    0.7065    0.9204    0.1826    0.3480    0.7267    0.9508    0.1936    0.4578

% 4. AVG: 1 by CHOICES * STATES (CH1 ST1, CH1 ST2; CH2 ST1, etc), take% average over shocks for each
valuesMn = mean(values,1)

valuesMn = 1x12
    0.0905    0.2939    0.6502    0.8997    0.1483    0.3196    0.6629    0.9254    0.1704    0.3918

% 5. AVG: CHOICES * STATES. From this matrix, one can now pick maximum% utility, and match that to t
valuesMn = reshape(valuesMn, [stateCount, choiceCount])'

valuesMn = 3x4
    0.0905    0.2939    0.6502    0.8997
    0.1483    0.3196    0.6629    0.9254
    0.1704    0.3918    0.7184    0.9338

```

#### 1.1.5.4 Pick Optimal Choice

```

choiceCount = 3;
stateCount = 4;

% 1. Matrix, each column is a state, each row is a choice
randMat = rand(choiceCount,stateCount)

randMat = 3x4
    0.0733    0.5905    0.1731    0.1795
    0.0550    0.8539    0.1340    0.3175
    0.3232    0.2871    0.9947    0.5683

% 2. Maximum Value and Maximum Index
[maxVal maxIndex] = max(randMat)

maxVal = 1x4
    0.3232    0.8539    0.9947    0.5683

```

```

maxIndex = 1x4
    3     2     3     3

% 3. Linear index
linearIdx = maxIndex + ((1:stateCount)-1)*choiceCount

linearIdx = 1x4
    3     5     9    12

% 4. Optimal Choices
randMat(linearIdx)

ans = 1x4
    0.3232    0.8539    0.9947    0.5683

```

### 1.1.6 Accumarray Examples

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 1.1.6.1 Accumarray Basic Example

There are three unique values in `ar_a`, sum up the probabilities for each of the unique states. This is equivalent to sorting a matrix with `a` and `prob`, and computing sum for each.

```

ar_a = [3,2,1,3]';
ar_prob = [0.1,0.2,0.31,0.39]';
ar_sumprob = accumarray(ar_a, ar_prob);
tb_summed_prob = table(sort(unique(ar_a)), ar_sumprob);
disp(tb_summed_prob);

```

Var1	ar_sumprob
----	-----
1	0.31
2	0.2
3	0.49

#### 1.1.6.2 Accumarray For Discrete Random Variable

Upon solving a model, if we look for the mass at certain choices or states, `accumarray` could help aggregate up probabilities

```

a1 = [1,1,2,2]

a1 = 1x4
    1     1     2     2

a2 = [3,2,1,3]

a2 = 1x4
    3     2     1     3

a3 = [1,2,3,3]

a3 = 1x4
    1     2     3     3

a = [a1;a2;a3]'/2

```

```

a = 4x3
    0.5000    1.5000    0.5000
    0.5000    1.0000    1.0000
    1.0000    0.5000    1.5000
    1.0000    1.5000    1.5000

prob_a = zeros(size(a)) + 1/12

prob_a = 4x3
    0.0833    0.0833    0.0833
    0.0833    0.0833    0.0833
    0.0833    0.0833    0.0833
    0.0833    0.0833    0.0833

[ar_idx_full, ~, ar_idx_of_unique] = unique(a)

ar_idx_full = 3x1
    0.5000
    1.0000
    1.5000

ar_idx_of_unique = 12x1
     1
     1
     2
     2
     3
     2
     1
     3
     1
     2

mt_idx_of_unique = reshape(ar_idx_of_unique, size(a))

mt_idx_of_unique = 4x3
     1     3     1
     1     2     2
     2     1     3
     2     3     3

accumarray(mt_idx_of_unique(:,1), prob_a(:,1))

ans = 2x1
    0.1667
    0.1667

accumarray(mt_idx_of_unique(:,2), prob_a(:,2))

ans = 3x1
    0.0833
    0.0833
    0.1667

accumarray(mt_idx_of_unique(:,3), prob_a(:,3))

```

```
ans = 3x1
    0.0833
    0.0833
    0.1667
```

### 1.1.7 Array Draw Random Index and Find Combinations or Permutations

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 1.1.7.1 Matlab Draw Random with and without Replacement

```
%Generate a matrix named foo, with limited numbers
rng(1234);
foo = unique((round((randn(5,1)+1)*100)));
disp(foo);
```

```
    5
   78
  154
  219
  232
```

```
% draw 10 random samples without replacement
index = randsample(1:length(foo), 4);
bar_rand_noreplace = foo(index,:);
```

```
% draw 1000 random samples with replacement
index = randsample(1:length(foo), 4, true);
bar_rand_replace = foo(index,:);
```

```
% Display
disp(table(bar_rand_noreplace, bar_rand_replace));
```

bar_rand_noreplace	bar_rand_replace
5	78
78	154
154	219
232	219

#### 1.1.7.2 Matrix Meshgrid to Loop Permutated Vectors

Meshgrid to generate all permutations of arrays.

```
k = linspace(1,10,10);
kp = linspace(1,10,10);
z = linspace(0,1,10);

[kM kpM zM] = meshgrid(k,kp,z);
kMVec = kM(:);
kpMVec = kpM(:);
zMVec = zM(:);
```

```
outputVec = zeros(size(zMVec));
for a=1:length(zMVec)
```

```
outputVec(a) = kMVec(a)+kMpVec(a)+zMVec(a);
end
```

```
outputTens = reshape(outputVec,size(kM));
disp(outputTens);
```

```
(:,:,1) =
```

2	3	4	5	6	7	8	9	10	11
3	4	5	6	7	8	9	10	11	12
4	5	6	7	8	9	10	11	12	13
5	6	7	8	9	10	11	12	13	14
6	7	8	9	10	11	12	13	14	15
7	8	9	10	11	12	13	14	15	16
8	9	10	11	12	13	14	15	16	17
9	10	11	12	13	14	15	16	17	18
10	11	12	13	14	15	16	17	18	19
11	12	13	14	15	16	17	18	19	20

```
(:,:,2) =
```

2.1111	3.1111	4.1111	5.1111	6.1111	7.1111	8.1111	9.1111	10.1111	11.1111
3.1111	4.1111	5.1111	6.1111	7.1111	8.1111	9.1111	10.1111	11.1111	12.1111
4.1111	5.1111	6.1111	7.1111	8.1111	9.1111	10.1111	11.1111	12.1111	13.1111
5.1111	6.1111	7.1111	8.1111	9.1111	10.1111	11.1111	12.1111	13.1111	14.1111
6.1111	7.1111	8.1111	9.1111	10.1111	11.1111	12.1111	13.1111	14.1111	15.1111
7.1111	8.1111	9.1111	10.1111	11.1111	12.1111	13.1111	14.1111	15.1111	16.1111
8.1111	9.1111	10.1111	11.1111	12.1111	13.1111	14.1111	15.1111	16.1111	17.1111
9.1111	10.1111	11.1111	12.1111	13.1111	14.1111	15.1111	16.1111	17.1111	18.1111
10.1111	11.1111	12.1111	13.1111	14.1111	15.1111	16.1111	17.1111	18.1111	19.1111
11.1111	12.1111	13.1111	14.1111	15.1111	16.1111	17.1111	18.1111	19.1111	20.1111

```
(:,:,3) =
```

2.2222	3.2222	4.2222	5.2222	6.2222	7.2222	8.2222	9.2222	10.2222	11.2222
3.2222	4.2222	5.2222	6.2222	7.2222	8.2222	9.2222	10.2222	11.2222	12.2222
4.2222	5.2222	6.2222	7.2222	8.2222	9.2222	10.2222	11.2222	12.2222	13.2222
5.2222	6.2222	7.2222	8.2222	9.2222	10.2222	11.2222	12.2222	13.2222	14.2222
6.2222	7.2222	8.2222	9.2222	10.2222	11.2222	12.2222	13.2222	14.2222	15.2222
7.2222	8.2222	9.2222	10.2222	11.2222	12.2222	13.2222	14.2222	15.2222	16.2222
8.2222	9.2222	10.2222	11.2222	12.2222	13.2222	14.2222	15.2222	16.2222	17.2222
9.2222	10.2222	11.2222	12.2222	13.2222	14.2222	15.2222	16.2222	17.2222	18.2222
10.2222	11.2222	12.2222	13.2222	14.2222	15.2222	16.2222	17.2222	18.2222	19.2222
11.2222	12.2222	13.2222	14.2222	15.2222	16.2222	17.2222	18.2222	19.2222	20.2222

```
(:,:,4) =
```

2.3333	3.3333	4.3333	5.3333	6.3333	7.3333	8.3333	9.3333	10.3333	11.3333
3.3333	4.3333	5.3333	6.3333	7.3333	8.3333	9.3333	10.3333	11.3333	12.3333
4.3333	5.3333	6.3333	7.3333	8.3333	9.3333	10.3333	11.3333	12.3333	13.3333
5.3333	6.3333	7.3333	8.3333	9.3333	10.3333	11.3333	12.3333	13.3333	14.3333
6.3333	7.3333	8.3333	9.3333	10.3333	11.3333	12.3333	13.3333	14.3333	15.3333
7.3333	8.3333	9.3333	10.3333	11.3333	12.3333	13.3333	14.3333	15.3333	16.3333
8.3333	9.3333	10.3333	11.3333	12.3333	13.3333	14.3333	15.3333	16.3333	17.3333
9.3333	10.3333	11.3333	12.3333	13.3333	14.3333	15.3333	16.3333	17.3333	18.3333



10.3333	11.3333	12.3333	13.3333	14.3333	15.3333	16.3333	17.3333	18.3333	19.3333
11.3333	12.3333	13.3333	14.3333	15.3333	16.3333	17.3333	18.3333	19.3333	20.3333

(:, :, 5) =

2.4444	3.4444	4.4444	5.4444	6.4444	7.4444	8.4444	9.4444	10.4444	11.4444
3.4444	4.4444	5.4444	6.4444	7.4444	8.4444	9.4444	10.4444	11.4444	12.4444
4.4444	5.4444	6.4444	7.4444	8.4444	9.4444	10.4444	11.4444	12.4444	13.4444
5.4444	6.4444	7.4444	8.4444	9.4444	10.4444	11.4444	12.4444	13.4444	14.4444
6.4444	7.4444	8.4444	9.4444	10.4444	11.4444	12.4444	13.4444	14.4444	15.4444
7.4444	8.4444	9.4444	10.4444	11.4444	12.4444	13.4444	14.4444	15.4444	16.4444
8.4444	9.4444	10.4444	11.4444	12.4444	13.4444	14.4444	15.4444	16.4444	17.4444
9.4444	10.4444	11.4444	12.4444	13.4444	14.4444	15.4444	16.4444	17.4444	18.4444
10.4444	11.4444	12.4444	13.4444	14.4444	15.4444	16.4444	17.4444	18.4444	19.4444
11.4444	12.4444	13.4444	14.4444	15.4444	16.4444	17.4444	18.4444	19.4444	20.4444

(:, :, 6) =

2.5556	3.5556	4.5556	5.5556	6.5556	7.5556	8.5556	9.5556	10.5556	11.5556
3.5556	4.5556	5.5556	6.5556	7.5556	8.5556	9.5556	10.5556	11.5556	12.5556
4.5556	5.5556	6.5556	7.5556	8.5556	9.5556	10.5556	11.5556	12.5556	13.5556
5.5556	6.5556	7.5556	8.5556	9.5556	10.5556	11.5556	12.5556	13.5556	14.5556
6.5556	7.5556	8.5556	9.5556	10.5556	11.5556	12.5556	13.5556	14.5556	15.5556
7.5556	8.5556	9.5556	10.5556	11.5556	12.5556	13.5556	14.5556	15.5556	16.5556
8.5556	9.5556	10.5556	11.5556	12.5556	13.5556	14.5556	15.5556	16.5556	17.5556
9.5556	10.5556	11.5556	12.5556	13.5556	14.5556	15.5556	16.5556	17.5556	18.5556
10.5556	11.5556	12.5556	13.5556	14.5556	15.5556	16.5556	17.5556	18.5556	19.5556
11.5556	12.5556	13.5556	14.5556	15.5556	16.5556	17.5556	18.5556	19.5556	20.5556

(:, :, 7) =

2.6667	3.6667	4.6667	5.6667	6.6667	7.6667	8.6667	9.6667	10.6667	11.6667
3.6667	4.6667	5.6667	6.6667	7.6667	8.6667	9.6667	10.6667	11.6667	12.6667
4.6667	5.6667	6.6667	7.6667	8.6667	9.6667	10.6667	11.6667	12.6667	13.6667
5.6667	6.6667	7.6667	8.6667	9.6667	10.6667	11.6667	12.6667	13.6667	14.6667
6.6667	7.6667	8.6667	9.6667	10.6667	11.6667	12.6667	13.6667	14.6667	15.6667
7.6667	8.6667	9.6667	10.6667	11.6667	12.6667	13.6667	14.6667	15.6667	16.6667
8.6667	9.6667	10.6667	11.6667	12.6667	13.6667	14.6667	15.6667	16.6667	17.6667
9.6667	10.6667	11.6667	12.6667	13.6667	14.6667	15.6667	16.6667	17.6667	18.6667
10.6667	11.6667	12.6667	13.6667	14.6667	15.6667	16.6667	17.6667	18.6667	19.6667
11.6667	12.6667	13.6667	14.6667	15.6667	16.6667	17.6667	18.6667	19.6667	20.6667

(:, :, 8) =

2.7778	3.7778	4.7778	5.7778	6.7778	7.7778	8.7778	9.7778	10.7778	11.7778
3.7778	4.7778	5.7778	6.7778	7.7778	8.7778	9.7778	10.7778	11.7778	12.7778
4.7778	5.7778	6.7778	7.7778	8.7778	9.7778	10.7778	11.7778	12.7778	13.7778
5.7778	6.7778	7.7778	8.7778	9.7778	10.7778	11.7778	12.7778	13.7778	14.7778
6.7778	7.7778	8.7778	9.7778	10.7778	11.7778	12.7778	13.7778	14.7778	15.7778
7.7778	8.7778	9.7778	10.7778	11.7778	12.7778	13.7778	14.7778	15.7778	16.7778
8.7778	9.7778	10.7778	11.7778	12.7778	13.7778	14.7778	15.7778	16.7778	17.7778
9.7778	10.7778	11.7778	12.7778	13.7778	14.7778	15.7778	16.7778	17.7778	18.7778
10.7778	11.7778	12.7778	13.7778	14.7778	15.7778	16.7778	17.7778	18.7778	19.7778
11.7778	12.7778	13.7778	14.7778	15.7778	16.7778	17.7778	18.7778	19.7778	20.7778

```
(:,:,9) =
```

```

2.8889    3.8889    4.8889    5.8889    6.8889    7.8889    8.8889    9.8889   10.8889   11.8889
3.8889    4.8889    5.8889    6.8889    7.8889    8.8889    9.8889   10.8889   11.8889   12.8889
4.8889    5.8889    6.8889    7.8889    8.8889    9.8889   10.8889   11.8889   12.8889   13.8889
5.8889    6.8889    7.8889    8.8889    9.8889   10.8889   11.8889   12.8889   13.8889   14.8889
6.8889    7.8889    8.8889    9.8889   10.8889   11.8889   12.8889   13.8889   14.8889   15.8889
7.8889    8.8889    9.8889   10.8889   11.8889   12.8889   13.8889   14.8889   15.8889   16.8889
8.8889    9.8889   10.8889   11.8889   12.8889   13.8889   14.8889   15.8889   16.8889   17.8889
9.8889   10.8889   11.8889   12.8889   13.8889   14.8889   15.8889   16.8889   17.8889   18.8889
10.8889   11.8889   12.8889   13.8889   14.8889   15.8889   16.8889   17.8889   18.8889   19.8889
11.8889   12.8889   13.8889   14.8889   15.8889   16.8889   17.8889   18.8889   19.8889   20.8889
```

```
(:,:,10) =
```

```

3     4     5     6     7     8     9     10    11    12
4     5     6     7     8     9     10    11    12    13
5     6     7     8     9     10    11    12    13    14
6     7     8     9     10    11    12    13    14    15
7     8     9     10    11    12    13    14    15    16
8     9     10    11    12    13    14    15    16    17
9     10    11    12    13    14    15    16    17    18
10    11    12    13    14    15    16    17    18    19
11    12    13    14    15    16    17    18    19    20
12    13    14    15    16    17    18    19    20    21
```

### 1.1.7.3 Given Integer Arrays, All Possible Combinations

given any sizes arrays, N of them, create all possible combinations

```

ar_it_a = 1:3;
ar_it_b = 1:2;
ar_it_c = 2:4;
ar_it_d = -1:-1:-2;
ar_it_e = 0.1;

cl_ar_all = {ar_it_a, ar_it_b, ar_it_c, ar_it_d, ar_it_e};
cl_mt_all = cl_ar_all;
[cl_mt_all{:}] = ndgrid(cl_ar_all{:});
mt_it_allcombo = cell2mat(cellfun(@(m) m(:), cl_mt_all, 'uni', 0));

disp(mt_it_allcombo)
```

```

1.0000    1.0000    2.0000   -1.0000    0.1000
2.0000    1.0000    2.0000   -1.0000    0.1000
3.0000    1.0000    2.0000   -1.0000    0.1000
1.0000    2.0000    2.0000   -1.0000    0.1000
2.0000    2.0000    2.0000   -1.0000    0.1000
3.0000    2.0000    2.0000   -1.0000    0.1000
1.0000    1.0000    3.0000   -1.0000    0.1000
2.0000    1.0000    3.0000   -1.0000    0.1000
3.0000    1.0000    3.0000   -1.0000    0.1000
1.0000    2.0000    3.0000   -1.0000    0.1000
2.0000    2.0000    3.0000   -1.0000    0.1000
3.0000    2.0000    3.0000   -1.0000    0.1000
1.0000    1.0000    4.0000   -1.0000    0.1000
```

2.0000	1.0000	4.0000	-1.0000	0.1000
3.0000	1.0000	4.0000	-1.0000	0.1000
1.0000	2.0000	4.0000	-1.0000	0.1000
2.0000	2.0000	4.0000	-1.0000	0.1000
3.0000	2.0000	4.0000	-1.0000	0.1000
1.0000	1.0000	2.0000	-2.0000	0.1000
2.0000	1.0000	2.0000	-2.0000	0.1000
3.0000	1.0000	2.0000	-2.0000	0.1000
1.0000	2.0000	2.0000	-2.0000	0.1000
2.0000	2.0000	2.0000	-2.0000	0.1000
3.0000	2.0000	2.0000	-2.0000	0.1000
1.0000	1.0000	3.0000	-2.0000	0.1000
2.0000	1.0000	3.0000	-2.0000	0.1000
3.0000	1.0000	3.0000	-2.0000	0.1000
1.0000	2.0000	3.0000	-2.0000	0.1000
2.0000	2.0000	3.0000	-2.0000	0.1000
3.0000	2.0000	3.0000	-2.0000	0.1000
1.0000	1.0000	4.0000	-2.0000	0.1000
2.0000	1.0000	4.0000	-2.0000	0.1000
3.0000	1.0000	4.0000	-2.0000	0.1000
1.0000	2.0000	4.0000	-2.0000	0.1000
2.0000	2.0000	4.0000	-2.0000	0.1000
3.0000	2.0000	4.0000	-2.0000	0.1000

### 1.1.8 Matlab Array Basics and Miscellaneous

back to [Fan's Reusable Matlab Repository](#) or [Dynamic Asset Repository](#).

#### 1.1.8.1 Compare Array Values That are Approximately Similar

[What is the best way to compare floats for almost-equality in Python?](#)

- `rel_tol` is a relative tolerance, it is multiplied by the greater of the magnitudes of the two arguments; as the values get larger, so does the allowed difference between them while still considering them equal.
- `abs_tol` is an absolute tolerance that is applied as-is in all cases. If the difference is less than either of those tolerances, the values are considered equal.

```
rel_tol=1e-09;
abs_tol=0.0;
if_is_close = @(a,b) (abs(a-b) <= max(rel_tol * max(abs(a), abs(b)), abs_tol));
disp(['1 and 1, if_is_close:' num2str(if_is_close(1,1))]);

1 and 1, if_is_close:1

disp(['1e-300 and 1e-301, if_is_close:' num2str(if_is_close(1e-300,1e-301))]);

1e-300 and 1e-301, if_is_close:0

disp(['1+1e-9 and 1+1e-10, if_is_close:' num2str(if_is_close(1+1e-9,1+1e-10))]);

1+1e-9 and 1+1e-10, if_is_close:1
```

#### 1.1.8.2 Imaginary Number Examples

```
rng(123);

% Imaginary array
```

```

ar_img = rand([1,7]) + 1i*rand([1,7]);

% Regular Array
ar_real = rand([1,10]);

% Combine arrays
ar_full = [ar_real ar_img];
ar_full = ar_full(randperm(length(ar_full))));
disp(ar_full);

Columns 1 through 7

    0.6344 + 0.0000i    0.1755 + 0.0000i    0.5316 + 0.0000i    0.2861 + 0.4809i    0.7380 + 0.0000i    0.

Columns 8 through 14

    0.2269 + 0.3921i    0.7245 + 0.0000i    0.8494 + 0.0000i    0.6110 + 0.0000i    0.4231 + 0.4386i    0.

Columns 15 through 17

    0.3980 + 0.0000i    0.5513 + 0.3432i    0.7195 + 0.7290i

% real index
disp(~imag(ar_full));

    1     1     1     0     1     1     0     0     1     1     1     0     0     1     1     0     0

% Get Real and not real Components
disp(ar_full(imag(ar_full) == 0));

    0.6344    0.1755    0.5316    0.7380    0.1825    0.7245    0.8494    0.6110    0.5318    0.3980

disp(ar_full(imag(ar_full) ~= 0));

    0.2861 + 0.4809i    0.6965 + 0.6848i    0.2269 + 0.3921i    0.4231 + 0.4386i    0.9808 + 0.0597i    0.

```

## 1.2 Cells

### 1.2.1 List Comprehension with Cells

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 1.2.1.1 Find Index of Elements of String Cells in a larger String Cells

the function below returns the position of `cl_st_param_keys` in `ls_st_param_key` should only include in `cl_st_param_keys` strings that also exist in `ls_st_param_key`.

```

ls_st_param_key = {'fl_crra', 'fl_beta', ...
                  'fl_w', 'fl_r_save', ...
                  'fl_a_max', 'it_z_n', 'it_a_n'};

cl_st_param_keys = {'fl_w', 'fl_beta', 'it_z_n'};

cell2mat(cellfun(@(m) find(strcmp(ls_st_param_key, m)), ...
                 cl_st_param_keys, 'UniformOutput', false))

```

```
ans = 1x3
      3      2      6
```

### 1.2.1.2 Given Container of Arrays, Find Total Length of All Arrays for Selected Keys

```
cl_st_param_keys = {'fl_crra', 'fl_beta'};

param_tstar_map = containers.Map('KeyType','char', 'ValueType','any');
it_simu_vec_len = 5;

param_tstar_map('fl_crra') = linspace(1, 2, 5);
param_tstar_map('fl_beta') = linspace(0.94, 0.98, 10);
param_tstar_map('w') = linspace(1.1, 1.4, it_simu_vec_len);
param_tstar_map('r') = linspace(0.01, 0.04, it_simu_vec_len);

ar_it_array_len = cell2mat(cellfun(@(m) length(param_tstar_map(m)), ...
                                   cl_st_param_keys, 'UniformOutput', false));

it_total_length = sum(ar_it_array_len);
disp(['ar_it_array_len: ' num2str(ar_it_array_len)])

ar_it_array_len: 5  10

disp(['it_total_length: ' num2str(it_total_length)])

it_total_length: 15
```

### 1.2.1.3 Given Container of Arrays, Find Min and Max of Each and Draw Random N sets

```
cl_st_param_keys = {'fl_crra', 'fl_beta'};

param_tstar_map = containers.Map('KeyType','char', 'ValueType','any');
it_simu_vec_len = 5;

param_tstar_map('fl_crra') = linspace(1, 2, 5);
param_tstar_map('fl_beta') = linspace(0.94, 0.98, 10);
param_tstar_map('w') = linspace(1.1, 1.4, it_simu_vec_len);
param_tstar_map('r') = linspace(0.01, 0.04, it_simu_vec_len);

rng(123);
it_simu_length = 20;
mt_param_rand = cell2mat(cellfun(@(m) ...
                                   rand([it_simu_length,1]).*(max(param_tstar_map(m)) - min(param_tstar_map(m))
                                   + min(param_tstar_map(m)), ...
                                   cl_st_param_keys, 'UniformOutput', false));

tb_rand_draws = array2table(mt_param_rand, 'VariableNames', cl_st_param_keys);

disp(tb_rand_draws);

    fl_crra    fl_beta
    -----    -
    1.6965    0.96538
    1.2861    0.97398
    1.2269    0.96898
    1.5513    0.96444
    1.7195    0.9689
    1.4231    0.95292
```

1.9808	0.95447
1.6848	0.94913
1.4809	0.95175
1.3921	0.96524
1.3432	0.94368
1.729	0.95735
1.4386	0.95723
1.0597	0.95975
1.398	0.95703
1.738	0.95249
1.1825	0.95705
1.1755	0.97574
1.5316	0.97777
1.5318	0.96007

## 1.2.2 All Possible Combinations of Multiple Arrays

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

### 1.2.2.1 Given Several Arrays of Possibly different Length in Container, all Possible combinations

```
param_tstar_map = containers.Map('KeyType','char','ValueType','any');
param_tstar_map('a') = linspace(1, 5, 5);
param_tstar_map('b') = linspace(0.87, 0.97, 6);
param_tstar_map('c') = linspace(0, 0.5, 10);

cl_st_param_keys = {'a','c'};
cl_ar_param_subset_values = values(param_tstar_map, {'a','c'});

cl_mt_all = cl_ar_param_subset_values;
[cl_mt_all{:}] = ndgrid(cl_ar_param_subset_values{:});
mt_param_vals_combi = cell2mat(cellfun(@(m) m(:), cl_mt_all, 'uni', 0));

tb_all_combi = array2table(mt_param_vals_combi, 'VariableNames', cl_st_param_keys);

disp(tb_all_combi);
```

a	c
-	-----
1	0
2	0
3	0
4	0
5	0
1	0.055556
2	0.055556
3	0.055556
4	0.055556
5	0.055556
1	0.11111
2	0.11111
3	0.11111
4	0.11111
5	0.11111
1	0.16667
2	0.16667

```

3      0.16667
4      0.16667
5      0.16667
1      0.22222
2      0.22222
3      0.22222
4      0.22222
5      0.22222
1      0.27778
2      0.27778
3      0.27778
4      0.27778
5      0.27778
1      0.33333
2      0.33333
3      0.33333
4      0.33333
5      0.33333
1      0.38889
2      0.38889
3      0.38889
4      0.38889
5      0.38889
1      0.44444
2      0.44444
3      0.44444
4      0.44444
5      0.44444
1          0.5
2          0.5
3          0.5
4          0.5
5          0.5

```

### 1.2.3 Combine Cells Together

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 1.2.3.1 String Combine with string cell

```

ls_st_param_key = {'fl_crra', 'fl_beta', ...
                  'fl_w', 'fl_r_save', ...
                  'fl_a_max', 'it_z_n', 'it_a_n'};

cl_st_param_keys = {'fl_wad', 'fl_betart', 'it_z_nfg'};

st_param = 'asdjfl';

[st_param, ls_st_param_key, cl_st_param_keys]

ans =
    {'asdjfl'}    {'fl_crra'}    {'fl_beta'}    {'fl_w'}    {'fl_r_save'}    {'fl_a_max'}    {'it_z_n'}

```

### 1.2.4 Nested Cells

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

### 1.2.4.1 Nested Cells and access

```

cl_st_param_keys = {'fl_crra', 'fl_beta'};

it_simu_vec_len = 3;
clns_parm_tstar = cell([4,1]);
clns_parm_tstar{1} = {'fl_crra', 'CRRa', linspace(1, 2, it_simu_vec_len)};
clns_parm_tstar{2} = {'fl_beta', 'Discount', linspace(0.94, 0.98, it_simu_vec_len)};
clns_parm_tstar{3} = {'w', 'Wage', linspace(1.1, 1.4, it_simu_vec_len)};
clns_parm_tstar{4} = {'r', 'Save Interest', linspace(0.01, 0.04, it_simu_vec_len)};

disp(clns_parm_tstar(1));

    {1x3 cell}

disp(clns_parm_tstar{1}{1})

fl_crra

disp(clns_parm_tstar{1}{2});

CRRa

disp(clns_parm_tstar{1}{3});

    1.0000    1.5000    2.0000

```

## 1.3 Characters and Strings

### 1.3.1 Basic String Operations

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 1.3.1.1 Combine String, Numeric values etc, Single and Double Quotes

Convert a string array into a single string, note the double quotes, and the auto space between:

```

st_a = "another string";
ar_st = ["abc", num2str(2), "opq", st_a];
disp(strjoin(ar_st));

```

```
abc 2 opq another string
```

If we do not want to have spaces between words, the second parameter for strjoin allows for string connectors:

```

st_a = "another string";
ar_st = ["abc", num2str(2), "opq", st_a];
disp(strjoin(ar_st, ""));

```

```
abc2opqanother string
```

With single quotes, the str element is not an array, so does not need strjoin, but not need to have spaces:

```

st_a = 'another string';
str = ['abc ', num2str(2), ' opq ', st_a];
disp((str));

```

```
abc 2 opq another string
```



### 1.3.1.2 Construct String Array and String Elements of String Array

In the example below, we have a number of strings we want to put inside a string array, then join with `strjoin`, but two of the strings need to be constructed as strings first. Note below that double quotes are own strings, single quotes in brackets constructing additional strings.

```
st_a = "another string";
ar_st = strjoin(...
    ["Completed SNW_DS_MAIN", ...
    ['SNW_MP_PARAM=' num2str(123.345)], ...
    ['SNW_MP_CONTROL=' num2str(678.90)], ...
    st_a...
    ], ";");
disp(ar_st);
```

```
Completed SNW_DS_MAIN;SNW_MP_PARAM=123.345;SNW_MP_CONTROL=678.9;another string
```

### 1.3.1.3 Paste Join Strings Together with Separator

Join strings together with separator, this is similar to the `paste0` function in R.

```
ar_st = ["abc", "efg", "opq"];
disp(strjoin(ar_st, '-'));
```

```
abc-efg-opq
```

### 1.3.1.4 Combine Char with Numeric Value

Compose a string with words and numerical values

```
st_title = strcat("Figure Title ", ...
    "(", ...
    "threedeci=%.3f", ...
    "twodeci=%.2f", ...
    "int=%.0f", ...
    ")");
ar_params = 123.4567 + zeros(1,3);
st_combo = compose(st_title, ar_params);
disp(st_combo);
```

```
Figure Title (threedeci=123.457,twodeci=123.46,int=123)
```

### 1.3.1.5 Search if String Contains Substring

Does string contain substring?

```
st_long1 = 'simu_dense';
st_long2 = 'simu_denser';
st_long3 = 'simuverydense';
st_long4 = 'simu_medium';
st_long5 = 'simuverysmall';
disp([contains(st_long1, 'dense'), contains(st_long2, 'dense'), contains(st_long3, 'dense'), ...
    contains(st_long4, 'dense'), contains(st_long5, 'dense')]);
```

```
1    1    1    0    0
```

### 1.3.1.6 Change File Name MLX to M

```
st_file_name_mlx = 'continuous_differentiable.mlx';
at_st_split_file_name = split(st_file_name_mlx, ".");
st_file_name_m = strcat(at_st_split_file_name{1}, '_m.m');
disp(st_file_name_m);
```

```
continuous_differentiable_m.m
```

### 1.3.2 String Manipulations with Arrays

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 1.3.2.1 String Array

Three title lines, with double quotes:

```
ar_st_titles = ["Title1","Title2","Title3"]';
disp(ar_st_titles);
```

```
"Title1"
"Title2"
"Title3"
```

Three words, joined together, now single quotes, this creates one string, rather than a string array:

```
st_titles = ['Title1','Title2','Title3'];
disp(st_titles);
```

```
Title1Title2Title3
```

#### 1.3.2.2 String Cell Array

Create a string array:

```
ar_st_title_one = {'Title One Line'};
ar_st_titles = {'Title1','Title2','Title3'};
disp(ar_st_title_one);
```

```
{'Title One Line'}
```

```
disp(ar_st_titles);
```

```
{'Title1'}    {'Title2'}    {'Title3'}
```

Add to a string array:

```
ar_st_titles{4} = 'Title4';
disp(ar_st_titles);
```

```
{'Title1'}    {'Title2'}    {'Title3'}    {'Title4'}
```

Update one of the strings:

```
ar_st_title_one{1} = strcat('log(', ar_st_title_one{1},')');
ar_st_titles{1} = strcat('log(', ar_st_titles{1},')');
disp(ar_st_title_one);
```

```
{'log(Title One Line)'}
```

```
disp(ar_st_titles);
```

```
{'log(Title1)'}    {'Title2'}    {'Title3'}    {'Title4'}
```

#### 1.3.2.3 Joint String Cell Array with Suffix

```
ar_st_titles = {'Title1','Title2','Title3'};
disp(strcat(ar_st_titles, '_init'));
```

```
{'Title1_init'}    {'Title2_init'}    {'Title3_init'}
```

#### 1.3.2.4 Duplicate String

```
it_duplicate_n = 10;
disp(repmat({'String'}, [1, it_duplicate_n]));
```

Columns 1 through 9

```
{'String'}    {'String'}    {'String'}    {'String'}    {'String'}    {'String'}    {'String'}
```

Column 10

```
{'String'}
```

#### 1.3.2.5 String Join to form Single Element

using `char()` is safe

```
st_var_name = "abc"
```

```
st_var_name = "abc"
```

```
st_var_name = [st_var_name ' percentile values']
```

```
st_var_name = 1x2 string
"abc"          " percentile values"
```

```
strjoin(st_var_name)
```

```
ans = "abc percentile values"
```

```
st_var_name = "abc"
```

```
st_var_name = "abc"
```

```
st_var_name = [char(st_var_name) ' percentile values']
```

```
st_var_name = 'abc percentile values'
```

```
st_var_name = 'abc'
```

```
st_var_name = 'abc'
```

```
st_var_name = [char(st_var_name) ' percentile values']
```

```
st_var_name = 'abc percentile values'
```

#### 1.3.2.6 String Join dash (Paste)

This is similar to R's `paste` function:

```
st_var_name = "abc";
st_var_name = [st_var_name, 'efg', 'mqo'];
disp(strjoin(st_var_name, "_"));
```

```
abc_efg_mqo
```

```
disp(strjoin(st_var_name, ","));

abc,efg,mqo
```

### 1.3.2.7 Numeric Array to String without Space

String replace

```
ar_it_test_grp = [3, 8, 9];
strrep(num2str(ar_it_test_grp), ' ', '_')

ans = '3_8_9'
```

### 1.3.2.8 Substring replace in Cell Array

```
ar_st_cells = {'shock=0.35','shock=0.40','shock=0.46'};
ar_st_updated_cells = strrep(ar_st_cells, 'shock', '$\epsilon$');
disp(ar_st_updated_cells);

{'$\epsilon$=0.35'} {'$\epsilon$=0.40'} {'$\epsilon$=0.46'}
```

### 1.3.2.9 Find position of String in String Cell

```
ls_st_param_key = {'fl_crra', 'fl_beta', ...
                  'fl_w', 'fl_r_save', ...
                  'fl_a_max', 'it_z_n', 'it_a_n'};
st_param_key = 'fl_a_max';
find(strcmp(ls_st_param_key, st_param_key))

ans = 5
```

### 1.3.2.10 Find the positions of String Cells in Full String Cells

Find the positions of `fl_w`, `fl_beta`, and `it_z_n` in `ls_st_param_key`. Then just find the position of `fl_crra`. When looking for the position of something that does not exist, generate an find outcome array of length 0.

```
ls_st_param_key = {'fl_crra', 'fl_beta', ...
                  'fl_w', 'fl_r_save', ...
                  'fl_a_max', 'it_z_n', 'it_a_n'};

cl_st_param_keys = {'fl_w', 'fl_beta', 'it_z_n'};

cell2mat(cellfun(@(m) find(strcmp(ls_st_param_key, m)), ...
                cl_st_param_keys, 'UniformOutput', false))

ans = 1x3
      3      2      6

find(strcmp(ls_st_param_key, 'fl_crra'))

ans = 1

length(find(strcmp(ls_st_param_key, 'fl_crra_not_exist'))))

ans = 0

~sum(strcmp(ls_st_param_key, 'fl_crra_not_exist'))
```

```
ans =
    1
```

### 1.3.2.11 Cell to string Paste and Replace dash

```
cl_st_param_keys = {'fl_crra', 'fl_beta'};
display(strrep(strjoin(cl_st_param_keys, '-'), '_', '\_'));

fl\_crra-fl\_beta
```

## 1.3.3 Concatenate Strings Arrays with Numbers and Number Arrays with Strings

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

### 1.3.3.1 Combine A String Array with A Numeric Array using Compose

String array and numeric array, combine together using the compose function, and test different formatting functions. Formatting with leading empty spaces, leading zeros, and convert to integer or not.

```
st_titles = ["%.3f",    "%.1f",    "%.0f";...
             "%6.3f",  "%6.1f",   "%6.0f";...
             "%06.3f", "%06.1f", "%06.0f"];
ar_params = 123.4567890 + zeros(3,3);
st_combo = compose(st_titles, ar_params);
disp(st_combo);

    "123.457"    "123.5"    "123"
    "123.457"    " 123.5"    "   123"
    "123.457"    "0123.5"    "000123"
```

A string array and a numeric array combined

```
ls_st_param_esti = {'ar_mu_pos_1', 'ar_COEF_U_gamma'};
ar_params = [1213,456];
st_combo = strcat(ls_st_param_esti, '=', num2str(ar_params));
disp(st_combo);

{'ar_mu_pos_1=1213'    }
{'ar_COEF_U_gamma= 456'}
```

### 1.3.3.2 Title from an Array of Values

There is a vector of parameter values and a vector of names for these parameter values, I want to include these in the title of a figure with the same decimal formatting.

```
% Inputs
rng(123);
ar_params = rand(1,3);
ar_st_parms_names = ["param1", "param2", "param3"];
st_rounding = '.2f';
st_title_main = "this is the figure title";
% Rounding and combining
ar_st_params = strcat(ar_st_parms_names, compose(strcat("=%", st_rounding), ar_params));
% Generate a Single String that is comma separated:
st_param_pasted = strjoin(ar_st_params, ', ');
% Generate title with parameters
st_title_wth_params = strcat(st_title_main, ' (', st_param_pasted, ')');
% Display:
disp(st_title_wth_params);
```

this is the figure title (param1=0.70, param2=0.29, param3=0.23)

### 1.3.3.3 Combine String with Numeric Array

Example 1:

```
ar_fl_abc1 = [0.4 0.1 0.25 0.3 0.4];
disp([num2str(ar_fl_abc1', 'zw=%3.2f;'), num2str(ar_fl_abc1', 'zr=%3.2f')]);
```

Example 2:

```
close all;

rng(123);
ar_z_r_borr_mesh_wage = rand([1,5]);
ar_z_wage_mesh_r_borr = rand([1,5]);
ar_it_rows = round(rand([1,5])*10);
cl_st_full_rowscols = cellstr([num2str(ar_z_r_borr_mesh_wage', 'zr=%3.2f;'), ...
                               num2str(ar_z_wage_mesh_r_borr', 'zw=%3.2f')]);
cl_col_names = strcat('zi=', num2str(ar_it_rows([1,3,5]')), ':', cl_st_full_rowscols([1,3,5]));
disp(ar_z_r_borr_mesh_wage);

    0.6965    0.2861    0.2269    0.5513    0.7195

disp(ar_z_wage_mesh_r_borr);

    0.4231    0.9808    0.6848    0.4809    0.3921

disp(cl_st_full_rowscols);

    'zr=0.70;zw=0.42'
    'zr=0.29;zw=0.98'
    'zr=0.23;zw=0.68'
    'zr=0.55;zw=0.48'
    'zr=0.72;zw=0.39'

disp(cl_col_names);

    'zi=3:zr=0.70;zw=0.42'
    'zi=4:zr=0.23;zw=0.68'
    'zi=4:zr=0.72;zw=0.39'
```

### 1.3.3.4 Combine Number with String Cell Array

We have a string cell array we created from the previous section, now append numbers to it

```
% Append Common Numbers
cl_col_names_append = strcat(cl_col_names, '-String-Cell-With-Numeric-', num2str(123));
disp(cl_col_names_append);

    'zi=3:zr=0.70;zw=0.42-String-Cell-With-Numeric-123'
    'zi=4:zr=0.23;zw=0.68-String-Cell-With-Numeric-123'
    'zi=4:zr=0.72;zw=0.39-String-Cell-With-Numeric-123'
```

### 1.3.3.5 Combine Numeric Array with String Cell Array

Append an array of numeric values

```
% Append Common Numbers
cl_col_names_append = strcat(cl_col_names, '-String-Cell-With-Numeric-Array-', ...
    num2str(transpose(1:length(cl_col_names))));
```

```
disp(cl_col_names_append);

'zi=3:zr=0.70;zw=0.42-String-Cell-With-Numeric-Array-1'
'zi=4:zr=0.23;zw=0.68-String-Cell-With-Numeric-Array-2'
'zi=4:zr=0.72;zw=0.39-String-Cell-With-Numeric-Array-3'
```

### 1.3.3.6 Convert Numeric Array to String, Apeend Prefix to all elements.

```
ar_fl_abc1 = [0.4 0.1 0.25 0.3 0.4];
ar_st_wth_prefix = strcat('row=', string(ar_fl_abc1));
disp(ar_st_wth_prefix);

% Does Array Exist in Longer Array as Subset
ar_abc1 = [0.4 0.1 0.25 0.3 0.4];
ar_abc2 = [0.4 0.1 0.2 0.3 0.4];
ar_efg = [0.1 0.2 0.3 0.4 0.1 0.2 0.3 0.4 0.1 0.2 0.3 0.4 0.1 0.2 0.3 0.4];
st_abc1 = strjoin(string(num2str(ar_abc1)));
st_abc2 = strjoin(string(num2str(ar_abc2)));
st_efg = strjoin(string(num2str(ar_efg)));
contains(st_efg, st_abc1)
contains(st_efg, st_abc2)

% Display Convert to String
fprintf('Display string [%s]', num2str([1,2,3]));
fprintf('Display string [%s]', num2str(1.1));
fprintf('Display string [%s]', 'abc');
```

## 1.4 Map Containers

### 1.4.1 Container Map Basics

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 1.4.1.1 Container Integer Keys

Given some matrix, I want to store matrix column names as well as labels for what each row and column correspond to. Achieve this using a cell array of container maps. Cell dimensions correspond to the first, second, etc dimensions, any dimension specific information can be stored in this fashion.

Can access information associated with the label value of the row values:

```
% Define Matrix Row and Column and additional dimension information
cl_mp_datasetdesc = {};
cl_mp_datasetdesc{1} = containers.Map({'dim', 'name', 'labval'}, {1, 'kids', [0,1,2,3]});
cl_mp_datasetdesc{2} = containers.Map({'dim', 'name', 'labval'}, {2, 'age', [18,19,20]});
% get variable labels for the first dimension (rows)
disp([...
    string(['dim 1 var name:' cl_mp_datasetdesc{1}('name') ]), ...
    string(['dim 2 var name:' cl_mp_datasetdesc{2}('name') ])...
]);

"dim 1 var name:kids"    "dim 2 var name:age"
```

#### 1.4.1.2 Is Key In Container

```
param_map_a = containers.Map('KeyType','char', 'ValueType','any');
param_map_a('fl_b_bd') = -3;
param_map_a('fl_w_max') = 50;
param_map_a('fl_kp_min') = 0;
```

```

param_map_a('it_w_i') = 100;

disp([...
    string(['has it_w_i as key? ' num2str(isKey(param_map_a, 'it_w_i'))]), ...
    string(['has it_w_i1 as key? ' num2str(isKey(param_map_a, 'it_w_i1'))]) ...
]);

    "has it_w_i as key? 1"      "has it_w_i1 as key? 0"

```

### 1.4.1.3 Container Key Loop

Generate new container key within loop dynamically

```

param_map_a = containers.Map('KeyType', 'char', 'ValueType','any');

rng(123);
for st_cur = ["abc", "efg", "qqq"]

    if (strcmp(st_cur, "abc"))
        data = rand([1,1]);
    elseif (strcmp(st_cur, "efg"))
        data = 123.123;
    elseif (strcmp(st_cur, "qqq"))
        data = -123;
    end

    % common function
    fl_sh_0p1pc_j = data*2 + 1;
    fl_sh_5pc_j = data/2 - 1;

    % generate map keys
    st_key_sh_0p1pc_j = strjoin([st_cur, 'sh_0p1pc_j'], "_");
    st_key_sh_5pc_j = strjoin([st_cur, 'sh_5pc_j'], "_");

    % store
    param_map_a(st_key_sh_0p1pc_j) = fl_sh_0p1pc_j;
    param_map_a(st_key_sh_5pc_j) = fl_sh_5pc_j;

end

disp([...
    string(['param_map_a.keys:' param_map_a.keys]), ...
    string(['param_map_a.values:' string(param_map_a.values)]) ...
]);

Columns 1 through 7

    "param_map_a.keys:"      "abc_sh_0p1pc_j"      "abc_sh_5pc_j"      "efg_sh_0p1pc_j"      "efg_sh_5pc_j"

Columns 8 through 14

    "param_map_a.values:"      "2.3929"      "-0.65177"      "247.246"      "60.5615"      "-245"      "-62.5"

```

## 1.4.2 Container Map Display Key and Values and Subsetting

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).



### 1.4.2.1 Print Keys and Values

Define container:

```
% Define Container
param_map = containers.Map('KeyType','char', 'ValueType','any');
param_map('share_unbanked_j') = 12;
param_map('equi_r_j') = 2;
param_map('equi_w_j') = 'abc';
param_map('equi_P_j') = 1.2;
```

Print the key and values of the container:

```
param_map_keys = keys(param_map);
param_map_vals = values(param_map);
for i = 1:length(param_map)
    st_key = param_map_keys{i};
    ob_val = param_map_vals{i};
    st_display = strjoin(['pos = ' num2str(i) ' ; key = ' string(st_key) ' ; val = ' string(ob_val)]);
    disp(st_display);
end
```

```
pos = 1 ; key = equi_P_j ; val = 1.2
pos = 2 ; key = equi_r_j ; val = 2
pos = 3 ; key = equi_w_j ; val = abc
pos = 4 ; key = share_unbanked_j ; val = 12
```

### 1.4.2.2 Select of Subset of Key/Values from a Container Map

There is a larger container map, I want to create a new container map, that keeps a subset of the keys/values of the full container map.

```
% Original Container map
param_map = containers.Map('KeyType','char', 'ValueType','any');
param_map('equi_r_j') = 0.05;
param_map('equi_w_j') = 1.05;
param_map('equi_P_j') = 1;
% To select a subset of keys
ls_st_keys_select = {'equi_w_j', 'equi_P_j'};
% Select
param_map_subset = containers.Map(ls_st_keys_select, values(param_map, ls_st_keys_select));
% display
disp(param_map_subset.keys);

    'equi_P_j'    'equi_w_j'

disp(param_map_subset.values);

    [1]    [1.0500]
```

## 1.4.3 Generate Container Maps

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

### 1.4.3.1 Generate a Container map with any time of data

Create a container map with float, int, string, and matrix

```
close all;
clear all;
```

```
% Create A Map with String Keys and any values
param_map = containers.Map('KeyType','char', 'ValueType','any');
param_map('share_unbanked_j') = 12;
param_map('equi_r_j') = 2;
param_map('equi_w_j') = 'abc';
param_map('equi_P_j') = zeros(2,3);
disp(param_map.keys);

    'equi_P_j'    'equi_r_j'    'equi_w_j'    'share_unbanked_j'

disp(param_map.values);

    [2x3 double]    [2]    'abc'    [12]
```

### 1.4.3.2 Access Multiple Values of a container map

Values been accessed need to be of the same type

```
% Parameter Dealing from Map
params_group = values(param_map, {'share_unbanked_j', 'equi_r_j'});
[equi_P_j, equi_r_j] = params_group{:};
disp(['equi_P_j:' num2str(equi_P_j) ', equi_r_j:' num2str(equi_r_j)]);

equi_P_j:12, equi_r_j:2

% Access Scalar Elements of Map and Convert the Array
disp(cell2mat(values(param_map, {'share_unbanked_j', 'equi_r_j'}))));

    12    2
```

Create a container map of color values and generate a array of color choices:

```
% Container map with three colors
mp_colors = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_colors('blue') = [57 106 177]./255;
mp_colors('red') = [204 37 41]./255;
mp_colors('black') = [83 81 84]./255;
% An selection array
ar_st_colors_pick = {'blue', 'blue', 'red', 'black', 'blue'};
ar_colors = values(mp_colors, ar_st_colors_pick);
% Print selected colors
celldisp(ar_colors);

ar_colors{1} =

    0.2235    0.4157    0.6941

ar_colors{2} =

    0.2235    0.4157    0.6941

ar_colors{3} =

    0.8000    0.1451    0.1608
```

```
ar_colors{4} =

    0.3255    0.3176    0.3294
```

```
ar_colors{5} =

    0.2235    0.4157    0.6941
```

### 1.4.4 Container Map Example Overriding

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

#### 1.4.4.1 Update Container Map

There is one map with values, Container Map A. There is another container Map, Container Map B. Container Maps A and B share keys. For keys that exist in B and A, B Key value supercede values for the same keys in A. For new keys in B, they superced keys in A.

```
param_map_a = containers.Map('KeyType','char', 'ValueType','any');
param_map_a('fl_bd') = -3;
param_map_a('fl_w_max') = 50;
param_map_a('fl_kp_min') = 0;
param_map_a('it_w_i') = 100;

param_map_b = containers.Map('KeyType','char', 'ValueType','any');
param_map_b('fl_w_max') = 77;
param_map_b('fl_kp_min') = -231;
param_map_b('it_z_n') = 5;
param_map_b('fl_z_mu') = 0;

param_map_c = [param_map_a; param_map_b];
param_map_c.keys

ans =

    'fl_bd'    'fl_kp_min'    'fl_w_max'    'fl_z_mu'    'it_w_i'    'it_z_n'

param_map_c.values

ans =

    [-3]    [-231]    [77]    [0]    [100]    [5]
```



# Chapter 2

## Functions

### 2.1 varargin Default Parameters

#### 2.1.1 varargin as a Function Parameter

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

##### 2.1.1.1 Call Function with Two Parameters and Defaults

Call function below without overriding

```
ff_varargin(1.1, 2)

fl_a = 1.1000
it_b = 2
mt_data = 3x4
    0.6965    0.5513    0.9808    0.3921
    0.2861    0.7195    0.6848    0.3432
    0.2269    0.4231    0.4809    0.7290

ar_st_colnames = 1x4 string
"col1"         "col2"         "col3"         "col4"

ar_st_rownames = 1x4 string
"row1"         "row2"         "row3"         "row4"

st_table_name = "Table Name"
it_table_ctr = 1021
```

##### 2.1.1.2 Override Subset of Varargin

```
rng(789);
mt_data_ext = rand(5,2);
ar_st_colnames = ["col1", "col2"];
ar_st_rownames = ["row1", "row2", "row3", "row4", "row5"];
ff_varargin(param_map, support_map, mt_data_ext, ar_st_colnames, ar_st_rownames);

fl_a =
    Map with properties:
        Count: 2
        KeyType: char
        ValueType: any
```

```

it_b =
    Map with properties:

        Count: 1
        KeyType: char
        ValueType: any

mt_data = 5x2
    0.3233    0.7589
    0.2302    0.0106
    0.7938    0.0247
    0.6244    0.1110
    0.9754    0.5381

ar_st_colnames = 1x2 string
"col1"         "col2"

ar_st_rownames = 1x5 string
"row1"         "row2"         "row3"         "row4"         "row5"

st_table_name = "Table Name"
it_table_ctr = 1021

```

### 2.1.1.3 Function with varargin as Inputs

Basic default structure with varargin.

```

function ff_varargin(fl_a, it_b, varargin)
% This is an example of how to use varargin:
% 1. includes array matrix
% 2. includes array
% 3. includes scalar
% 4. includes string
% 5. includes cell array

%% Catch Error
cl_params_len = length(varargin);
if cl_params_len > 5
    error('ff_mat2tab:TooManyOptionalParameters', ...
        'allows at most 5 optional parameters');
end

%% Default Folder Parameters
% by default all go to Sandbox folder with sub folders by dates
rng(123);
mt_data = rand(3,4);
% String array requires double quotes
ar_st_colnames = ["col1", "col2", "col3", "col4"];
ar_st_rownames = ["row1", "row2", "row3", "row4"];
% Others
st_table_name = "Table Name";
it_table_ctr = 1021;
cl_params = {mt_data ar_st_colnames ar_st_rownames ...
             st_table_name it_table_ctr};

%% Parse Parameters
% numvarargs is the number of varargin inputted
[cl_params{1:cl_params_len}] = varargin{:};

```

```
% cell2mat(cl_params(1)) works with array
mt_data = cell2mat(cl_params(1));
% The structure below works with cell array
ar_st_colnames = cl_params{2};
ar_st_rownames = cl_params{3};
% Others
st_table_name = cl_params{4};
it_table_ctr = cl_params{5};

% Build Basic Matlab Table
% Suppose we want to store matrix results in a table,
% there are Q columns and N rows, The Q columns each is a different variable.
fl_a
it_b
mt_data
ar_st_colnames
ar_st_rownames
st_table_name
it_table_ctr

end
```

### 2.1.2 Map Based Default Parameter Structure with varargin

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 2.1.2.1 Call Function with Default Parameters

Call function below without overriding

```
ff_defaultmap()

'c_gap'      'c_max'      'c_min'      'c_min_for_util'      'fl_crra'      'it_rown'      'st_single_double'

[1.0000e-03]      [60]      [1.0000e-03]      [1.0000e-03]      [1.5000]      [100]      'double'

Elapsed time is 0.000896 seconds.
```

#### 2.1.2.2 Call Function overriding some Parameters

```
param_map = containers.Map('KeyType','char', 'ValueType','any');
param_map('fl_w_max') = 1.11;
param_map('it_w_i') = 2.22;

support_map = containers.Map('KeyType','char', 'ValueType','any');
support_map('bl_display') = true;
ff_defaultmap(param_map, support_map)

'c_gap'      'c_max'      'c_min'      'c_min_for_util'      'fl_crra'      'fl_w_max'      'it_rown'      'it

[1.0000e-03]      [60]      [1.0000e-03]      [1.0000e-03]      [1.5000]      [1.1100]      [100]      [2.2200]

Elapsed time is 0.000667 seconds.
```

#### 2.1.2.3 Function with Map Defaults and Overriding

This default parameter style is fairly succinct, allows for program testability, and easy adjustments/addition of additional parameters to models.

```

function ff_defaultmap(varargin)

% Parameters
params_len = length(varargin);
if params_len > 3
    error('ff_defaultmap:Can only have 3 container map parameters');
end
bl_input_override = 0;
if (params_len == 3)
    bl_input_override = varargin{3};
end

% Defaults
if (bl_input_override)
    % this relies on externally generated parameters, defaults do not have to be generated
    % if this file has to be invoked many times, then this saves time by avoiding
    % regenerating defaults over and over again
    [param_map, support_map, ~] = varargin{:};
else
    param_map = containers.Map('KeyType','char', 'ValueType','any');
    param_map('fl_crra') = 1.5;
    param_map('c_min') = 0.001;
    param_map('c_min_for_util') = 0.001;
    param_map('c_gap') = 10^-3;
    param_map('c_max') = 60;
    param_map('it_rown') = 100;
    param_map('st_single_double') = 'double';

    support_map = containers.Map('KeyType','char', 'ValueType','any');
    support_map('bl_display') = true;
    support_map('bl_graph') = true;
    support_map('bl_graph_onebyones') = true;
    support_map('bl_time') = true;
    support_map('bl_profile') = false;
    support_map('st_profile_path') = [pwd '/profile'];
    default_maps = {param_map, support_map};
end

% Parse Parameters
% see: C:\Users\fan\M4Econ\support\dtype\map_override.m
[default_maps{1:params_len}] = varargin{:};
param_map = [param_map; default_maps{1}];
support_map = [support_map; default_maps{2}];

params_group = values(param_map, {'fl_crra', 'c_min', 'c_min_for_util', 'c_gap', 'c_max'});
[fl_crra, c_min, c_min_for_util, c_gap, c_max] = params_group{:};
params_group = values(param_map, {'it_rown'});
[it_rown] = params_group{:};
params_group = values(param_map, {'st_single_double'});
[st_single_double] = params_group{:};

% support
params_group = values(support_map, {'bl_display', 'bl_graph', 'bl_graph_onebyones'});
[bl_display, bl_graph, bl_graph_onebyones] = params_group{:};
params_group = values(support_map, {'bl_time', 'bl_profile', 'st_profile_path'});
[bl_time, bl_profile, st_profile_path] = params_group{:};

% Tic toc starts

```



```
if (bl_time); tic; end

% Print Parameters
if (bl_display)
    disp(param_map.keys);
    disp(param_map.values);
end

% Profile On
if (bl_profile)
    close all;
    profile off;
    profile on;
end

%% Profiling
if (bl_profile)
    profile off
    profile viewer
    profsave(profile('info'), st_profile_path);
end

if (bl_time); toc; end

end
```



# Chapter 3

## Panel

### 3.1 Time Series

#### 3.1.1 Simulate AR(1) Autoregressive Processes

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

##### 3.1.1.1 Mean and Standard Deviation for AR(1) Autoregressive Process

A first-order autoregressive process can be written as:

- AR1:  $X_t = \text{constant} + \text{persistence} \cdot x_{t-1} + \epsilon$
- AR1:  $X_t = C + \rho \cdot x_{t-1} + \epsilon$

Assume that  $\epsilon$  is mean zero

Note that, we know the mean of  $X$ :

- $\mu_X = C + \rho \cdot \mu_X + 0$
- $\mu_x = \frac{C}{1 - \rho}$

Note that, we also know the standard deviation of  $X$ :

- $\text{var}(X) = \rho^2 \cdot \text{var}(X) + \text{var}(\epsilon)$
- $\sigma_x = \sqrt{\frac{\sigma_\epsilon^2}{1 - \rho^2}}$

We will let the initial point of the time series follow the stationary distribution of the AR(1) process, then we simulate the time series over 100 periods, in the example below, we use a highly persistent shock process with  $\rho = 0.98$ ,  $\sigma_\epsilon = 0.02$ ,  $C = 0.02$ . Note that for this process:

- $\mu_x^{\rho=0.98, \sigma_\epsilon=0.02, C=0.02} = \frac{0.02}{1 - 0.98} = 1$
- $\sigma_x^{\rho=0.98, \sigma_\epsilon=0.02, C=0.02} = \sqrt{\frac{0.02^2}{1 - 0.98^2}} \approx 0.10$

##### 3.1.1.2 Simulated one First-Order Autoregressive Time-Series

In the Example below, we simulate an individual for 1000 periods, given  $\rho = 0.98$ ,  $\sigma_\epsilon = 0.02$ ,  $C = 0.02$ . Given that the process is highly persistent, the individual stays rich or poor for dozens of periods at a time. If each period is a year, look at the results below, and suppose the simulated time series is income, what is the process saying about this person's income rise and fall. Note that we have the same person through all 1000 periods, but if you only look at 50 periods (years), you might think this person during

one span is really successful, another segment of 50 years, doing really bad, but actually there is nothing changing in the person's type, all that is changing is the person's luck.

First Set Parameters:

```
% Number of Time Periods
it_T = 1000;
% Mean and SD of the Shock Process
fl_constant = 0.02;
fl_normal_sd = 0.02;
% Persistence
fl_persistence = 0.98;
% Bounds on Shocks
fl_shk_bnds = 3;
% Initialize with exo fed point or not, if false initialize at Random Point
% from the stationary distribution
bl_init = true;
fl_init = fl_constant/(1 - fl_persistence);
```

Second, generate a vector of normal shocks:

```
% Generate a normal shock vector (the first draw will be ignored)
it_draws = it_T;
rng(789);
ar_fl_shocks = normrnd(0, fl_normal_sd, 1, it_draws);
disp(ar_fl_shocks(1:20));
```

Columns 1 through 13

```
-0.0060    -0.0047     0.0168     0.0118     0.0380     0.0062    -0.0616    -0.0485    -0.0192     0.0023
```

Columns 14 through 20

```
-0.0089     0.0160     0.0099    -0.0200    -0.0206    -0.0090    -0.0069
```

Third, replace any values exceeding bounds:

```
% out of bounds indicators
fl_shk_bds_lower = 0 - fl_normal_sd*fl_shk_bnds;
fl_shk_bds_upper = 0 + fl_normal_sd*fl_shk_bnds;
ar_bl_outofbounds = (ar_fl_shocks <= fl_shk_bds_lower | ar_fl_shocks >= fl_shk_bds_upper);
% count out of bounds
disp(strcat('lower:', num2str(fl_shk_bds_lower), ', upper:', num2str(fl_shk_bds_upper)));
```

```
lower:-0.06, upper:0.06
```

```
disp(sum(ar_bl_outofbounds));
```

4

```
ar_fl_shocks(ar_fl_shocks <= fl_shk_bds_lower) = fl_shk_bds_lower;
ar_fl_shocks(ar_fl_shocks >= fl_shk_bds_upper) = fl_shk_bds_upper;
```

Fourth, generate the AR(1) time series:

```
% Initialize Output Array
ar_fl_time_series = zeros(size(ar_fl_shocks));
% Loop over time
for it_t=1:length(ar_fl_shocks)
    if (it_t == 1)
        % initialize using the mean of the process
        ar_fl_time_series(1) = fl_constant/(1 - fl_persistence);
```

```

        if (bl_init)
            ar_fl_time_series(1) = fl_init;
        end
    else
        fl_ts_t = fl_constant + ar_fl_time_series(it_t-1)*fl_persistence + ar_fl_shocks(it_t);
        ar_fl_time_series(it_t) = fl_ts_t;
    end
end
end

```

Fifth, show the mean and sd of the process (these are very close to the analytical results):

```

disp(mean(ar_fl_time_series));

    1.0104

disp(std(ar_fl_time_series));

    0.1000

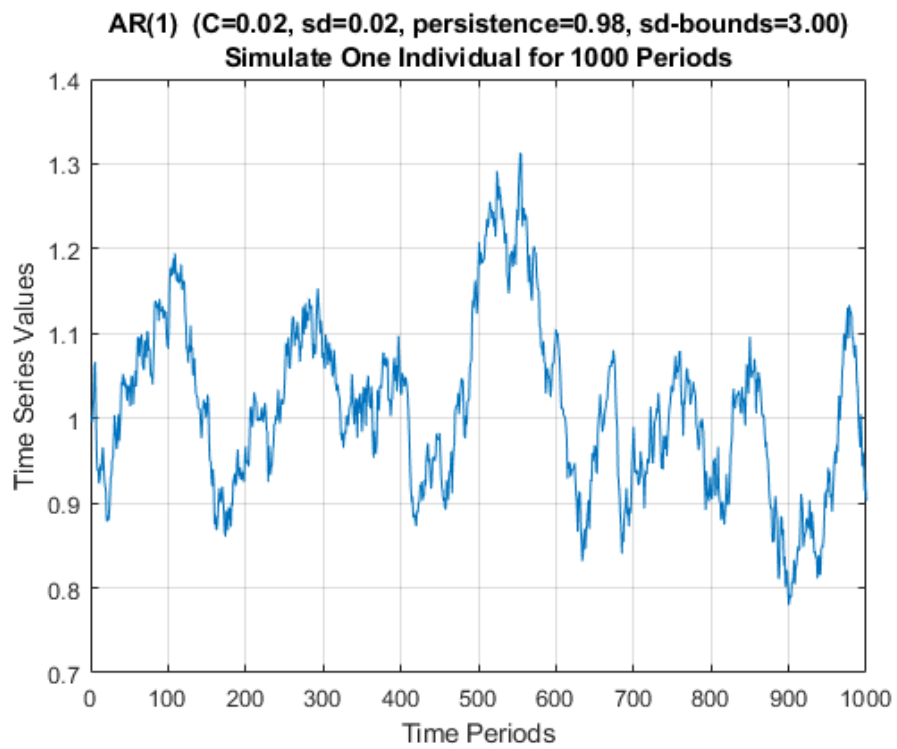
```

Sixth, plot the results:

```

figure();
% x-axis
ar_it_time = 1:1:length(ar_fl_shocks);
% plot
plot(ar_it_time, ar_fl_time_series);
% Generate Title
ar_fl_params_values = [fl_constant, fl_normal_sd, fl_persistence, fl_shk_bnds];
ar_st_parms_names = ["C", "sd", "persistence", "sd-bounds"];
st_rounding = '.2f';
st_title_main = "AR(1) ";
ar_st_params = strcat(ar_st_parms_names, compose(strcat("=%", st_rounding), ar_fl_params_values));
st_param_pasted = strjoin(ar_st_params, ', ');
st_title_wth_params = strcat(st_title_main, ' (' , st_param_pasted, ')');
title({st_title_wth_params, 'Simulate One Individual for 1000 Periods'});
% X and Y labels
ylabel({'Time Series Values'});
xlabel('Time Periods');
grid on;

```



## Chapter 4

# Simulation

### 4.1 Normal Distribution

#### 4.1.1 Compute CDF for Normal and Bivariate Normal Distributions

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

CDF for normal random variable through simulation and with NORMCDF function. CDF for bivariate normal random variables through simulation and with NORMCDF function.

- [fs\\_cholesky\\_decomposition](#)
- [fs\\_cholesky\\_decomposition\\_d5](#)
- [fs\\_bivariate\\_normal](#)

##### 4.1.1.1 Simulate Normal Distribution Probability with Uniform Draws

Mean score is 0, standard deviation is 1, we want to know what is the chance that children score less than -2, -1, 0, 1, and 2 respectively. We have a solution to the normal CDF cumulative distribution problem, it is:

```
mu = 0;
sigma = 1;
ar_x = [-2,-1,0,1,2];
for x=ar_x
    cdf_x = normcdf(x, mu, sigma);
    disp([strjoin(...
        ["CDF with normcdf", ...
        ['x=' num2str(x)] ...
        ['cdf_x=' num2str(cdf_x)] ...
        ], ";")]);
end
```

```
CDF with normcdf;x=-2;cdf_x=0.02275
CDF with normcdf;x=-1;cdf_x=0.15866
CDF with normcdf;x=0;cdf_x=0.5
CDF with normcdf;x=1;cdf_x=0.84134
CDF with normcdf;x=2;cdf_x=0.97725
```

We can also approximate the probabilities above, by drawing many points from a uniform:

1. Draw from uniform distribution 0 to 1, N times.
2. Invert these using `invnorm`. This means our uniform draws are now effectively drawn from the normal distribution.

3. Check if each draw inverted is below the  $x$  threshold or above, count fractions.

We should get very similar results as in the example above (especially if  $N$  is large)

```
% set seed
rng(123);
% generate random numbers
N = 10000;
ar_unif_draws = rand(1,N);
% invert
ar_normal_draws = norminv(ar_unif_draws);
% loop over different x values
for x=ar_x
    % index if draws below x
    ar_it_idx_below_x = (ar_normal_draws < x);
    fl_frac_below_x = (sum(ar_it_idx_below_x))/N;
    disp([strjoin(...
        ["CDF with normcdf", ...
        ['x=' num2str(x)] ...
        ['fl_frac_below_x=' num2str(fl_frac_below_x)] ...
        ], ";"))]);
end

CDF with normcdf;x=-2;fl_frac_below_x=0.023
CDF with normcdf;x=-1;fl_frac_below_x=0.1612
CDF with normcdf;x=0;fl_frac_below_x=0.4965
CDF with normcdf;x=1;fl_frac_below_x=0.847
CDF with normcdf;x=2;fl_frac_below_x=0.9789
```

#### 4.1.1.2 Simulate Bivariate-Normal Distribution Probability with Uniform Draws

There are two tests now, a math test and an English test. Student test scores are correlated with correlation 0.5 from the two tests, mean and standard deviations are 0 and 1 for both tests. What is the chance that a student scores below -2 and -2 for both, below -2 and 0 for math and English, below 2 and 1 for math and English, etc?

```
% timer
tm_start_mvncdf = tic;
% mean, and varcov
ar_mu = [0,0];
mt_varcov = [1,0.5;0.5,1];
ar_x = linspace(-3,3,101);
% initialize storage
mt_prob_math_eng = zeros([length(ar_x), length(ar_x)]);
% loop over math and english score thresholds
it_math = 0;
for math=ar_x
    it_math = it_math + 1;
    it_eng = 0;
    for eng=ar_x
        it_eng = it_eng + 1;
        % points below which to compute probability
        ar_scores = [math, eng];
        % volumn of a mountain to the southwest of north-south and east-west cuts
        cdf_x = mvncdf(ar_scores, ar_mu, mt_varcov);
        mt_prob_math_eng(it_math, it_eng) = cdf_x;
    end
end
% end timer
tm_end_mvncdf = toc(tm_start_mvncdf);
```



```
st_complete = strjoin(...
    ["MVNCDF Completed CDF computes", ...
    ['number of points=' num2str(numel(mt_prob_math_eng))] ...
    ['time=' num2str(tm_end_mvncdf)] ...
    ], ";");
disp(st_complete);
```

```
MVNCDF Completed CDF computes;number of points=10201;time=1.1957
```

```
% show results
```

```
tb_prob_math_eng = array2table(round(mt_prob_math_eng, 4));
cl_col_names_a = strcat('english <=', string(ar_x'));
cl_row_names_a = strcat('math <=', string(ar_x'));
tb_prob_math_eng.Properties.VariableNames = cl_col_names_a;
tb_prob_math_eng.Properties.RowNames = cl_row_names_a;
```

```
% subsetting function
```

```
% https://fanwangecon.github.io/M4Econ/amto/array/htmlpdfm/fs\_slicing.html#19\_Given\_Array\_of\_size\_M,
f_subset = @(it_subset_n, it_ar_n) unique(round(((0:1:(it_subset_n-1))/(it_subset_n-1))*(it_ar_n-1)+
disp(tb_prob_math_eng(f_subset(7, length(ar_x)), f_subset(7, length(ar_x))));
```

	english <=-3	english <=-1.98	english <=-1.02	english <=0	english <=1
	-----	-----	-----	-----	-----
math <=-3	0.0001	0.0005	0.001	0.0013	0.0013
math <=-1.98	0.0005	0.0043	0.0136	0.0217	0.0237
math <=-1.02	0.001	0.0136	0.0598	0.1239	0.1505
math <=0	0.0013	0.0217	0.1239	0.3333	0.4701
math <=1.02	0.0013	0.0237	0.1505	0.4701	0.7521
math <=1.98	0.0013	0.0238	0.1537	0.4978	0.8359
math <=3	0.0013	0.0239	0.1539	0.5	0.8458

We can also approximate the probabilities above, by drawing many points from two iid uniforms, and translating them to correlated normal using cholesky decomposition:

1. Draw from two random uniform distribution 0 to 1, N times each
2. Invert these using invnorm for both iid vectors from unifom draws to normal draws
3. Choleskey decompose and multiplication

This method below is faster than the method above when the number of points where we have to evaluat probabilities is large.

Generate randomly drawn scores:

```
% timer
tm_start_chol = tic;
% Draws unifom and invert to standard normal draws
N = 10000;
rng(123);
ar_unif_draws = rand(1,N*2);
ar_normal_draws = norminv(ar_unif_draws);
ar_draws_eta_1 = ar_normal_draws(1:N);
ar_draws_eta_2 = ar_normal_draws((N+1):N*2);

% Choesley decompose the variance covariance matrix
mt_varcov_chol = chol(mt_varcov, 'lower');

% Generate correlated random normals
mt_scores_chol = ar_mu' + mt_varcov_chol*([ar_draws_eta_1; ar_draws_eta_2]);
ar_math_scores = mt_scores_chol(1,:);
ar_eng_scores = mt_scores_chol(2,:);
```

Approximate probabilities from randomly drawn scores:

```
% initialize storage
mt_prob_math_eng_approx = zeros([length(ar_x), length(ar_x)]);
% loop over math and english score thresholds
it_math = 0;
for math=ar_x
    it_math = it_math + 1;
    it_eng = 0;
    for eng=ar_x
        it_eng = it_eng + 1;

        % points below which to compute probability
        % index if draws below x
        ar_it_idx_below_x_math = (ar_math_scores < math);
        ar_it_idx_below_x_eng = (ar_eng_scores < eng);
        ar_it_idx_below_x_joint = ar_it_idx_below_x_math.*ar_it_idx_below_x_eng;
        fl_frac_below_x_approx = (sum(ar_it_idx_below_x_joint))/N;

        % volumn of a mountain to the southwest of north-south and east-west cuts
        mt_prob_math_eng_approx(it_math, it_eng) = fl_frac_below_x_approx;
    end
end
% end timer
tm_end_chol = toc(tm_start_chol);
st_complete = strjoin(...
    ["UNIF+CHOL Completed CDF computes", ...
    ['number of points=' num2str(numel(mt_prob_math_eng_approx))] ...
    ['time=' num2str(tm_end_chol)] ...
    ], ";");
disp(st_complete);
```

UNIF+CHOL Completed CDF computes;number of points=10201;time=0.28661

```
% show results
tb_prob_math_eng_approx = array2table(round(mt_prob_math_eng_approx, 4));
cl_col_names_a = strcat('english <=', string(ar_x'));
cl_row_names_a = strcat('math <=', string(ar_x'));
tb_prob_math_eng_approx.Properties.VariableNames = cl_col_names_a;
tb_prob_math_eng_approx.Properties.RowNames = cl_row_names_a;
disp(tb_prob_math_eng_approx(f_subset(7, length(ar_x)), f_subset(7, length(ar_x))));
```

	english <=-3	english <=-1.98	english <=-1.02	english <=0	english <=1
-----	-----	-----	-----	-----	-----
math <=-3	0.0001	0.0005	0.001	0.0016	0.0016
math <=-1.98	0.0003	0.004	0.0132	0.0218	0.0237
math <=-1.02	0.0008	0.0131	0.061	0.1272	0.1529
math <=0	0.0009	0.0202	0.1236	0.334	0.4661
math <=1.02	0.0009	0.0215	0.1493	0.4724	0.754
math <=1.98	0.0009	0.0217	0.1526	0.4989	0.8344
math <=3	0.0009	0.0217	0.1526	0.5007	0.8425

#### 4.1.2 Cholesky Decomposition Correlated Bivariate Normal from IID Random Draws

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

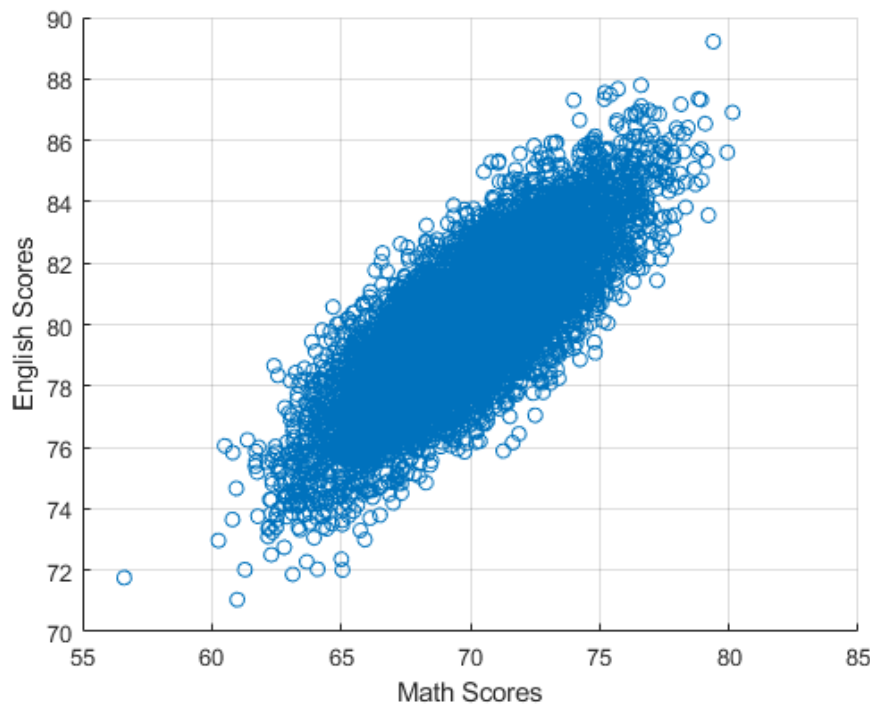
Draw two correlated normal shocks using the MVNRND function. Draw two correlated normal shocks from uniform random variables using Cholesky Decomposition.

- [fs\\_cholesky\\_decomposition](#)
- [fs\\_cholesky\\_decomposition\\_d5](#)
- [fs\\_bivariate\\_normal](#)

#### 4.1.2.1 Positively Correlated Scores MVNRND

We have English and Math scores, and we draw from a bivariate normal distribution, assuming the two scores are positively correlated. These are  $x_1$  and  $x_2$ .

```
% mean, and varcov
ar_mu = [70,80];
mt_varcov = [8,5;5,5];
% Generate Scores
rng(123);
N = 10000;
mt_scores = mvnrnd(ar_mu, mt_varcov, N);
% graph
figure();
scatter(mt_scores(:,1), mt_scores(:,2));
ylabel('English Scores');
xlabel('Math Scores')
grid on;
```



What are the covariance and correlation statistics?

```
disp([num2str(cov(mt_scores(:,1), mt_scores(:,2))))]);

8.0557      5.0738
5.0738      5.0638

disp([num2str(corrcoef(mt_scores(:,1), mt_scores(:,2))))]);
```

```

1      0.79441
0.79441      1

```

#### 4.1.2.2 Bivariate Normal from Uncorrelated Draws via Cholesky Decomposition

We can get the same results as above, without having to explicitly draw from a multivariate distribution by (For more details see [Train \(2009\)](#)):

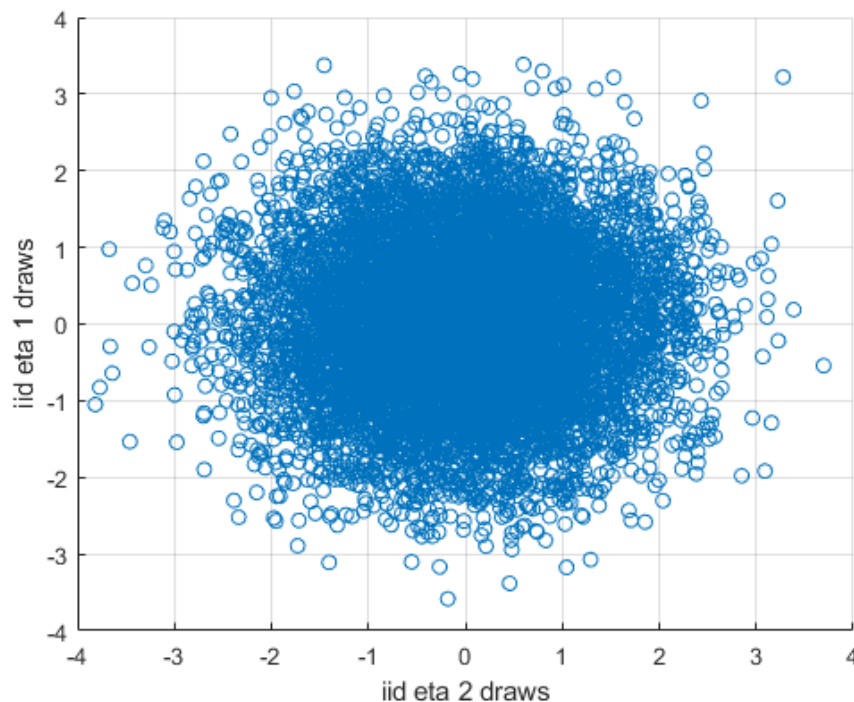
1. Draw 2 uniform random iid vectors.
2. Convert to normal iid vectors.
3. Generate the test scores as a function of the two random variables, using Cholesky matrix.

, draw two uncorrelated normal random variables, with mean 0, sd 1,  $\eta_1$  and  $\eta_2$ .

```

% Draw Two Uncorrelated Normal Random Variables
% use the same N as above
rng(123);
% uniform draws, uncorrelated
ar_unif_draws = rand(1,N*2);
% normal draws, english and math are uncorrelated
% ar_draws_eta_1 and ar_draws_eta_2 are uncorrelated by construction
ar_normal_draws = norminv(ar_unif_draws);
ar_draws_eta_1 = ar_normal_draws(1:N);
ar_draws_eta_2 = ar_normal_draws((N+1):N*2);
% graph
figure();
scatter(ar_draws_eta_1, ar_draws_eta_2);
ylabel('iid eta 1 draws');
xlabel('iid eta 2 draws')
grid on;

```



```

% Show Mean 1, cov = 0
disp([num2str(cov(ar_draws_eta_1, ar_draws_eta_2))]);

```

```

0.99075    0.0056929

```

```

0.0056929      0.98517

disp([num2str(corrcoef(ar_draws_eta_1, ar_draws_eta_2))]);

      1      0.0057623
0.0057623      1

```

, now using the variance-covariance we already have, decompose it, we will have:

- $c_{aa}, 0$   
 $c_{ab}, c_{bb}$

```

% Cholesley decompose the variance covariance matrix
mt_varcov_chol = chol(mt_varcov, 'lower');
disp([num2str(mt_varcov_chol)]);

2.8284      0
1.7678      1.3693

% The cholesky decomposed matrix factorizes the original varcov matrix
disp([num2str(mt_varcov_chol*mt_varcov_chol')]);

8      5
5      5

```

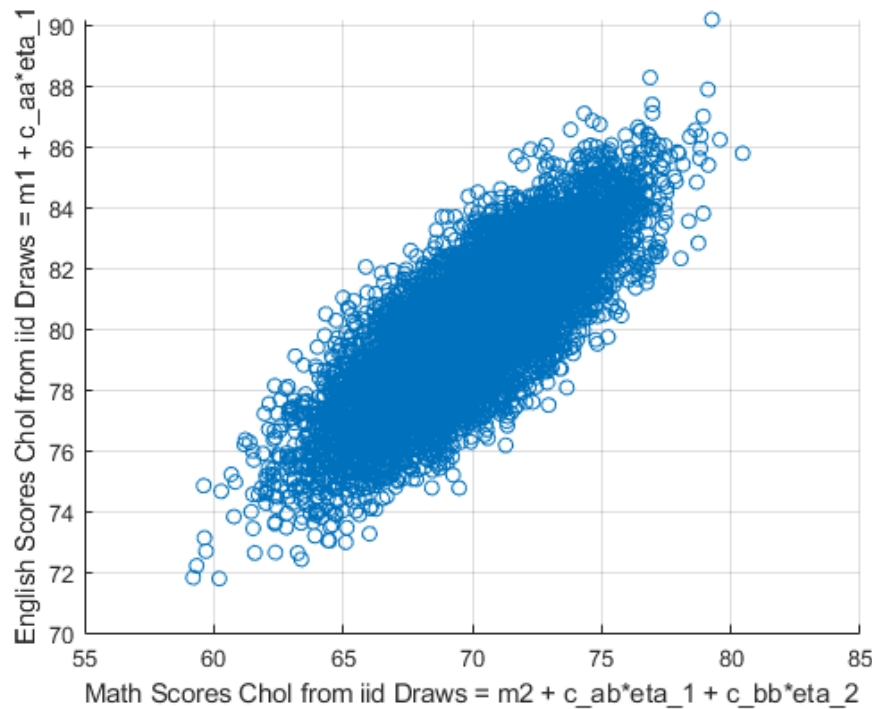
, We can get back to the original  $x_1$  and  $x_2$  variables:

- $x_1 = \mu_1 + c_{aa} * \eta_1$
- $x_2 = \mu_2 + c_{ab} * \eta_1 + c_{bb} * \eta_2$

```

% multiple the cholesky matrix by the eta draws
mt_scores_chol = ar_mu' + mt_varcov_chol*([ar_draws_eta_1; ar_draws_eta_2]);
mt_scores_chol = mt_scores_chol';
% graph
figure();
scatter(mt_scores_chol(:,1), mt_scores_chol(:,2));
ylabel('English Scores Chol from iid Draws = m1 + c\_aa*eta\_1');
xlabel('Math Scores Chol from iid Draws = m2 + c\_ab*eta\_1 + c\_bb*eta\_2')
grid on;

```



```
disp([num2str(cov(mt_scores_chol(:,1), mt_scores_chol(:,2))))];

7.926      4.9758
4.9758      4.9708

disp([num2str(corrcoef(mt_scores_chol(:,1), mt_scores_chol(:,2))))];

1      0.79272
0.79272      1
```

### 4.1.3 Cholesky Decomposition Correlated Five Dimensional Multivariate Normal Shock

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

Generate variance-covariance matrix from correlation and standard deviation. Draw five correlated normal shocks using the MVNRND function. Draw five correlated normal shocks from uniform random variables using Cholesky Decomposition.

- [fs\\_cholesky\\_decomposition](#)
- [fs\\_cholesky\\_decomposition\\_d5](#)
- [fs\\_bivariate\\_normal](#)

#### 4.1.3.1 Correlation and Standard Deviations to Variance Covariance Matrix

Given correlations and standard deviations, what is the variance and covariance matrix? Assume mean 0. The first three variables are correlated, the final two are iid.

First the ingredients:

```
% mean array
ar_mu = [0,0,0,0,0];
% standard deviations
ar_sd = [0.3301, 0.3329, 0.3308, 2312, 13394];
```

```
% correlations
mt_cor = ...
    [1,0.1226,0.0182,0,0;...
     0.1226,1,0.4727,0,0;...
     0.0182,0.4727,1,0,0;...
     0,0,0,1,0;...
     0,0,0,0,1];
% show
disp(mt_cor);
```

1.0000	0.1226	0.0182	0	0
0.1226	1.0000	0.4727	0	0
0.0182	0.4727	1.0000	0	0
0	0	0	1.0000	0
0	0	0	0	1.0000

Second, we know that variance is the square of standard deviation. And we know the formula for covariance, which is variance divided by two standard deviations. So for the example here, we have:

```
% initialize
mt_varcov = zeros([5,5]);
% variance
mt_varcov(eye(5)==1) = ar_sd.^2;
% covariance
mt_varcov(1,2) = mt_cor(1,2)*ar_sd(1)*ar_sd(2);
mt_varcov(2,1) = mt_varcov(1,2);
mt_varcov(1,3) = mt_cor(1,3)*ar_sd(1)*ar_sd(3);
mt_varcov(3,1) = mt_varcov(1,3);
mt_varcov(2,3) = mt_cor(2,3)*ar_sd(2)*ar_sd(3);
mt_varcov(3,2) = mt_varcov(2,3);
% show
disp(mt_varcov(1:3,1:3));
```

0.1090	0.0135	0.0020
0.0135	0.1108	0.0521
0.0020	0.0521	0.1094

```
disp(mt_varcov(4:5,4:5));
```

5345344	0
0	179399236

#### 4.1.3.2 Draw Five Correlated Shocks Using MVNRND

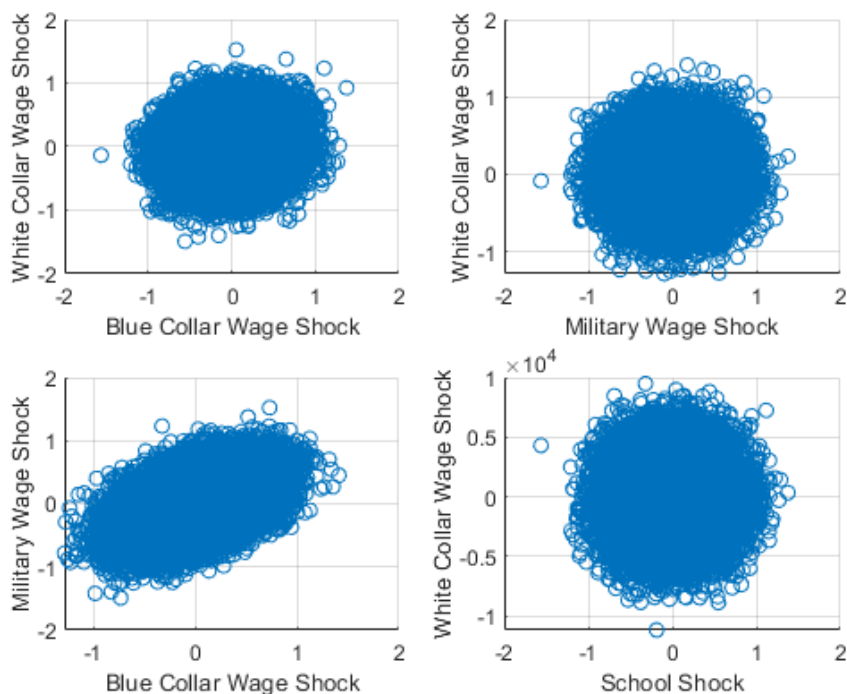
Generate N5 correlated shock structure

```
% Generate Scores
rng(123);
N = 50000;
mt_kw97_eps = mvnrnd(ar_mu, mt_varcov, N);
% graph
figure();
% subfigure 1
subplot(2,2,1);
scatter(mt_kw97_eps(:,1), mt_kw97_eps(:,2));
ylabel('White Collar Wage Shock');
xlabel('Blue Collar Wage Shock')
grid on;
% subfigure 2
subplot(2,2,2);
```

```

scatter(mt_kw97_eps(:,1), mt_kw97_eps(:,3));
ylabel('White Collar Wage Shock');
xlabel('Military Wage Shock')
grid on;
% subfigure 3
subplot(2,2,3);
scatter(mt_kw97_eps(:,3), mt_kw97_eps(:,2));
ylabel('Military Wage Shock');
xlabel('Blue Collar Wage Shock')
grid on;
% subfigure 4
subplot(2,2,4);
scatter(mt_kw97_eps(:,1), mt_kw97_eps(:,4));
ylabel('White Collar Wage Shock');
xlabel('School Shock')
grid on;

```



What are the covariance and correlation statistics?

```
disp([num2str(round(corrcoef(mt_kw97_eps),3))]);
```

1	0.119	0.016	0.002	-0.003
0.119	1	0.468	-0.003	0.004
0.016	0.468	1	-0.003	0.001
0.002	-0.003	-0.003	1	-0.005
-0.003	0.004	0.001	-0.005	1

```
disp([num2str(round(corrcoef(mt_kw97_eps),2))]);
```

1	0.12	0.02	0	0
0.12	1	0.47	0	0
0.02	0.47	1	0	0
0	0	0	1	-0.01
0	0	0	-0.01	1



### 4.1.3.3 Draw Five Correlated Shocks Using Cholesky Decomposition

Following what we did for bivariate normal distribution, we can now do the same for five different shocks at the same time (For more details see [Train \(2009\)](#)):

1. Draw 5 normal random variables that are uncorrelated
2. Generate 5 correlated shocks

Draw the shocks

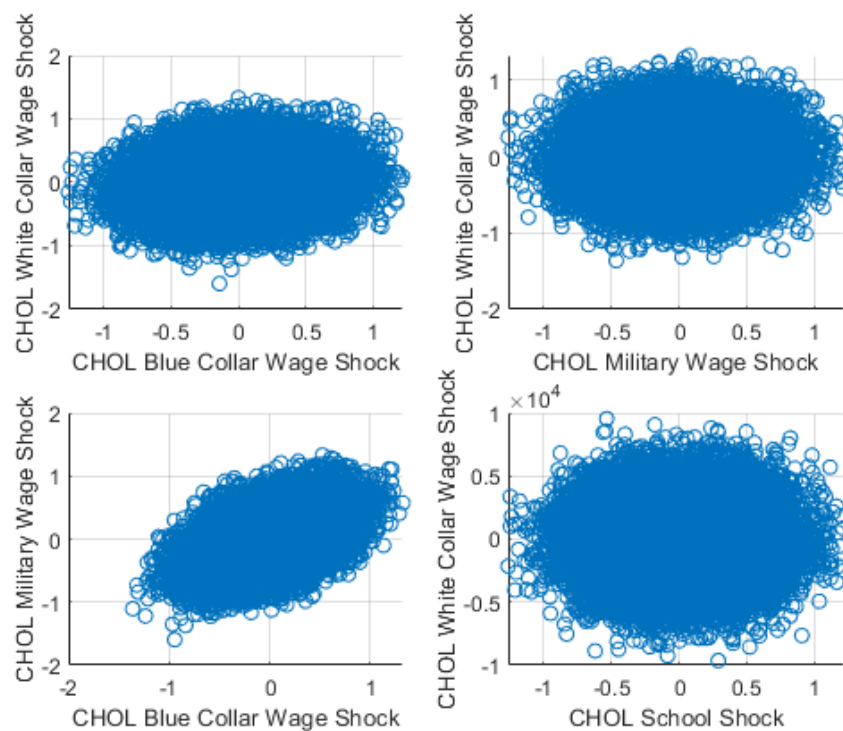
```
% Draws uniform and invert to standard normal draws
rng(123);
ar_unif_draws = rand(1,N*5);
ar_normal_draws = norminv(ar_unif_draws);
ar_draws_eta_1 = ar_normal_draws((N*0+1):N*1);
ar_draws_eta_2 = ar_normal_draws((N*1+1):N*2);
ar_draws_eta_3 = ar_normal_draws((N*2+1):N*3);
ar_draws_eta_4 = ar_normal_draws((N*3+1):N*4);
ar_draws_eta_5 = ar_normal_draws((N*4+1):N*5);

% Cholesley decompose the variance covariance matrix
mt_varcov_chol = chol(mt_varcov, 'lower');

% Generate correlated random normals
mt_kp97_eps_chol = ar_mu' + mt_varcov_chol*([...
    ar_draws_eta_1; ar_draws_eta_2; ar_draws_eta_3; ar_draws_eta_4; ar_draws_eta_5]);
mt_kp97_eps_chol = mt_kp97_eps_chol';
```

Graph:

```
% graph
figure();
% subfigure 1
subplot(2,2,1);
scatter(mt_kp97_eps_chol(:,1), mt_kp97_eps_chol(:,2));
ylabel('CHOL White Collar Wage Shock');
xlabel('CHOL Blue Collar Wage Shock')
grid on;
% subfigure 2
subplot(2,2,2);
scatter(mt_kp97_eps_chol(:,1), mt_kp97_eps_chol(:,3));
ylabel('CHOL White Collar Wage Shock');
xlabel('CHOL Military Wage Shock')
grid on;
% subfigure 3
subplot(2,2,3);
scatter(mt_kp97_eps_chol(:,3), mt_kp97_eps_chol(:,2));
ylabel('CHOL Military Wage Shock');
xlabel('CHOL Blue Collar Wage Shock')
grid on;
% subfigure 4
subplot(2,2,4);
scatter(mt_kp97_eps_chol(:,1), mt_kp97_eps_chol(:,4));
ylabel('CHOL White Collar Wage Shock');
xlabel('CHOL School Shock')
grid on;
```



What are the covariance and correlation statistics?

```
disp([num2str(round(corrcoef(mt_kp97_eps_chol),3))]);
```

1	0.119	0.021	0.008	-0.003
0.119	1	0.479	0.008	-0.003
0.021	0.479	1	0.002	0
0.008	0.008	0.002	1	-0.004
-0.003	-0.003	0	-0.004	1

```
disp([num2str(round(corrcoef(mt_kp97_eps_chol),2))]);
```

1	0.12	0.02	0.01	0
0.12	1	0.48	0.01	0
0.02	0.48	1	0	0
0.01	0.01	0	1	0
0	0	0	0	1

# Chapter 5

## Graphs

### 5.1 Figure Components

#### 5.1.1 Matlab Graph Safe Colors for Web, Presentation and Publications Examples

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

##### 5.1.1.1 Good Colors to Use Darker

Nice darker light colors to use in matlab.

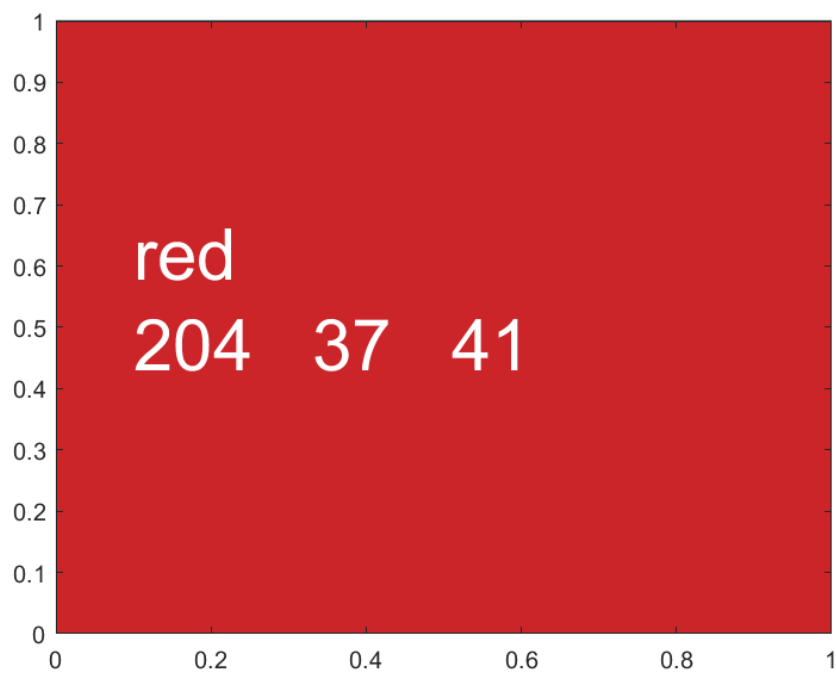
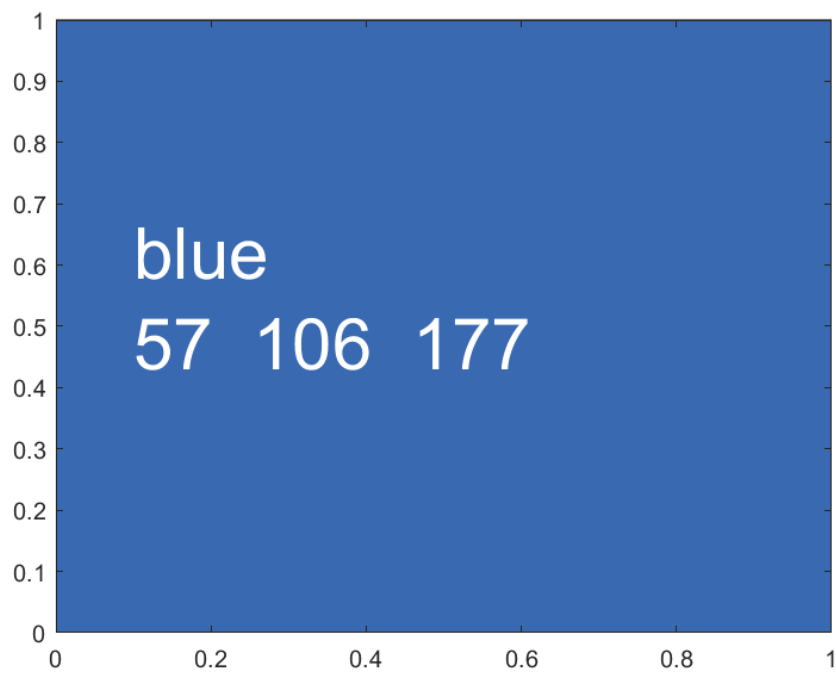
```
close all

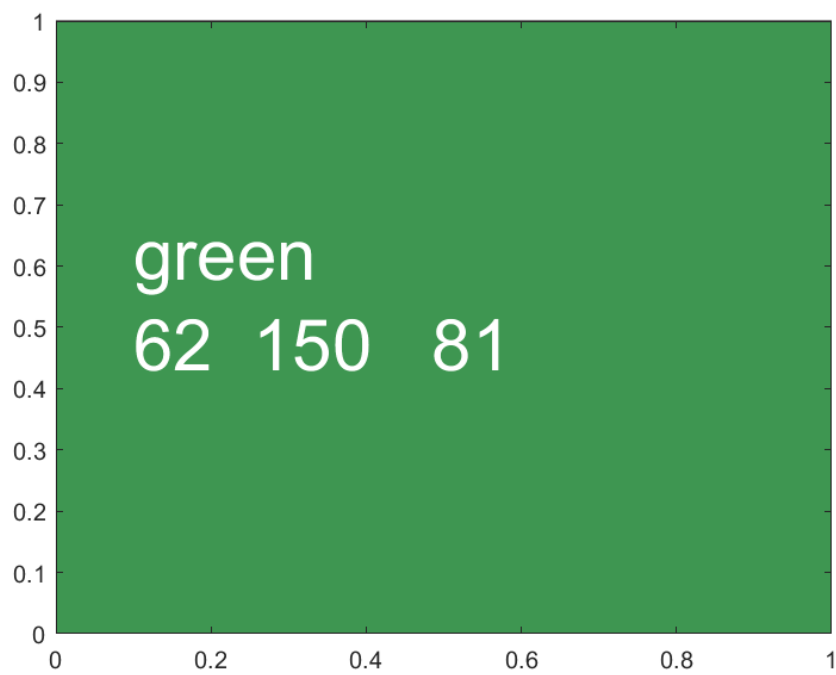
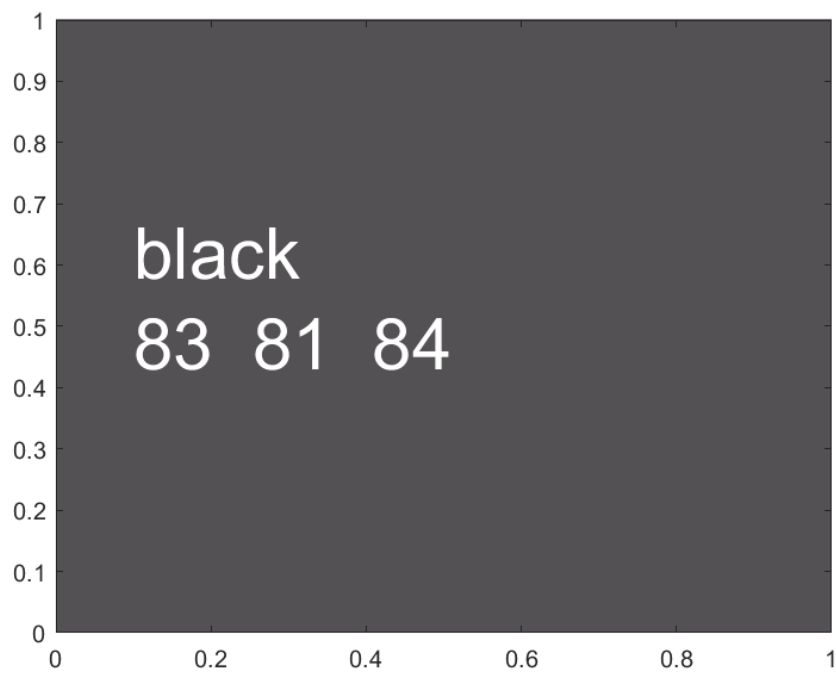
blue = [57 106 177]./255;
red = [204 37 41]./255;
black = [83 81 84]./255;
green = [62 150 81]./255;
brown = [146 36 40]./255;
purple = [107 76 154]./255;
cl_colors = {blue, red, black, ...
             green, brown, purple};
cl_str_clr_names = ["blue", "red", "black", "green", "brown", "purple"];

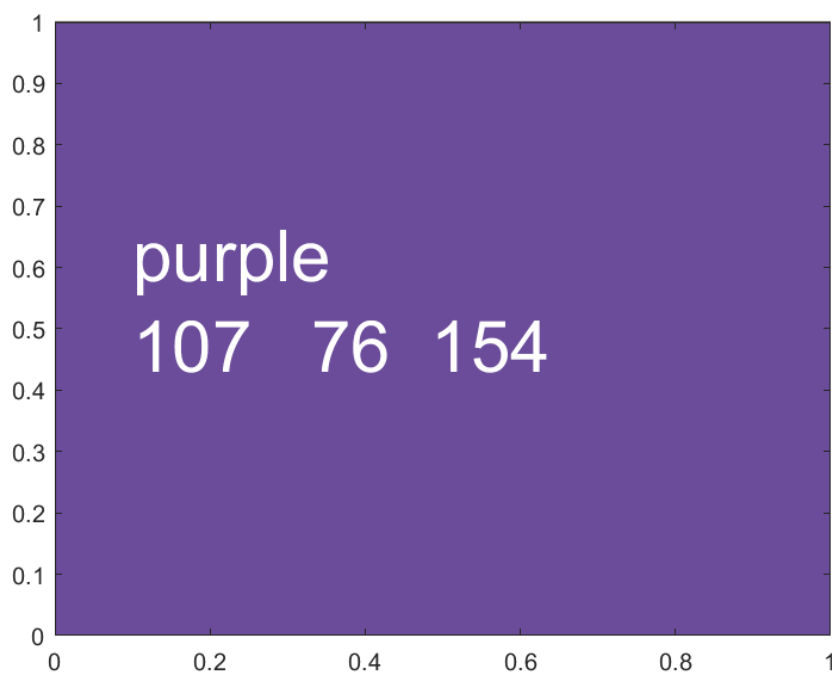
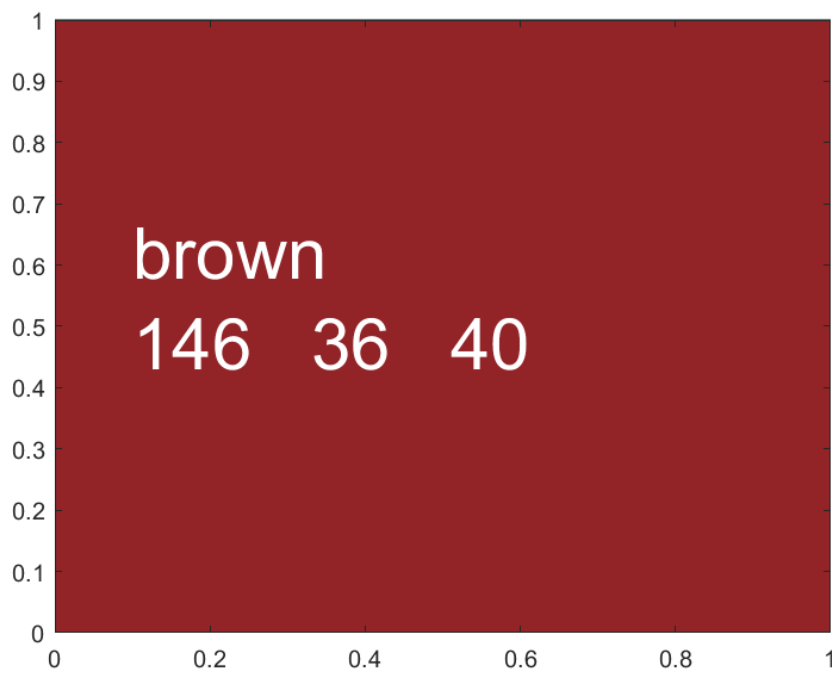
for it_color=1:length(cl_colors)

    figure();
    x = [0 1 1 0];
    y = [0 0 1 1];
    fill(x, y, cl_colors{it_color});
    st_text = [cl_str_clr_names(it_color) num2str(round(cl_colors{it_color}*255))];
    hText = text(.10,.55, st_text);
    hText.Color = 'white';
    hText.FontSize = 30;
    snapnow;

end
```







#### 5.1.1.2 Good Colors to Use Lighter

Nice lighter colors to use in matlab.

```
close all
```

```
blue = [114 147 203]./255;  
red = [211 94 96]./255;  
black = [128 133 133]./255;  
green = [132 186 91]./255;
```

```

brown = [171 104 87]./255;
purple = [144 103 167]./255;
cl_colors = {blue, red, black, ...
             green, brown, purple};
cl_str_clr_names = ["blue", "red", "black", "green", "brown", "purple"];

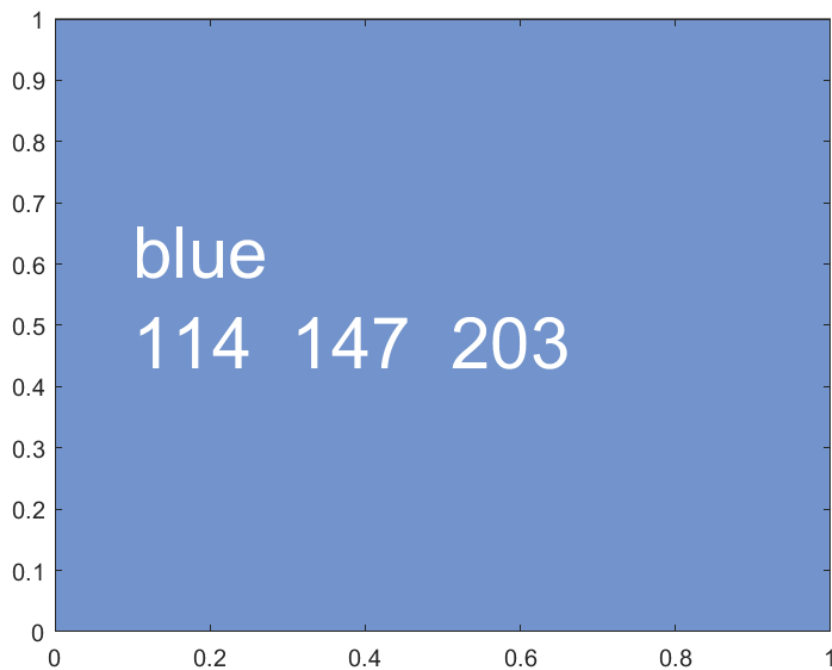
for it_color=1:length(cl_colors)

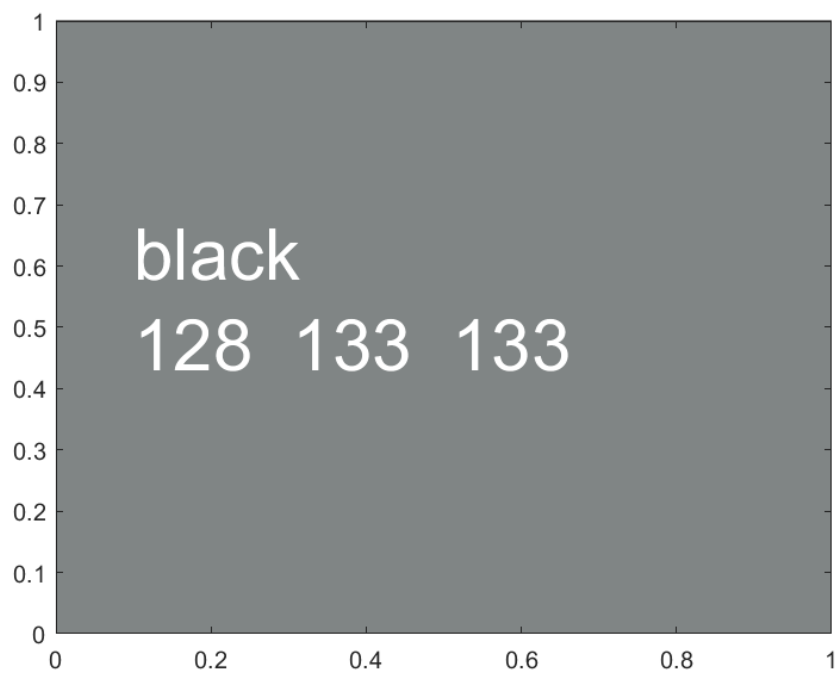
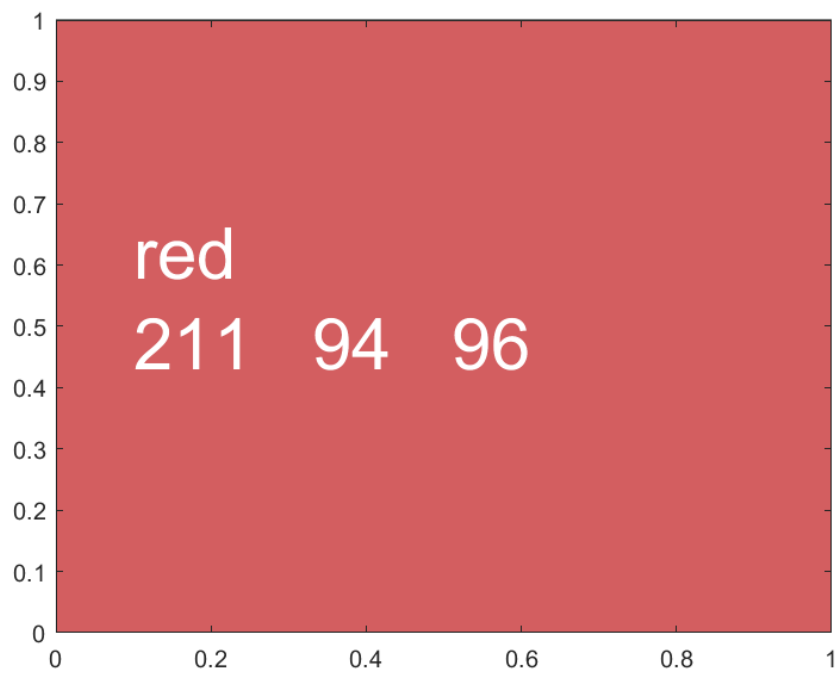
    figure();
    x = [0 1 1 0];
    y = [0 0 1 1];
    fill(x, y, cl_colors{it_color});

    st_text = [cl_str_clr_names(it_color) num2str(round(cl_colors{it_color}*255))];
    hText = text(.10,.55, st_text);
    hText.Color = 'white';
    hText.FontSize = 30;
    snapnow;

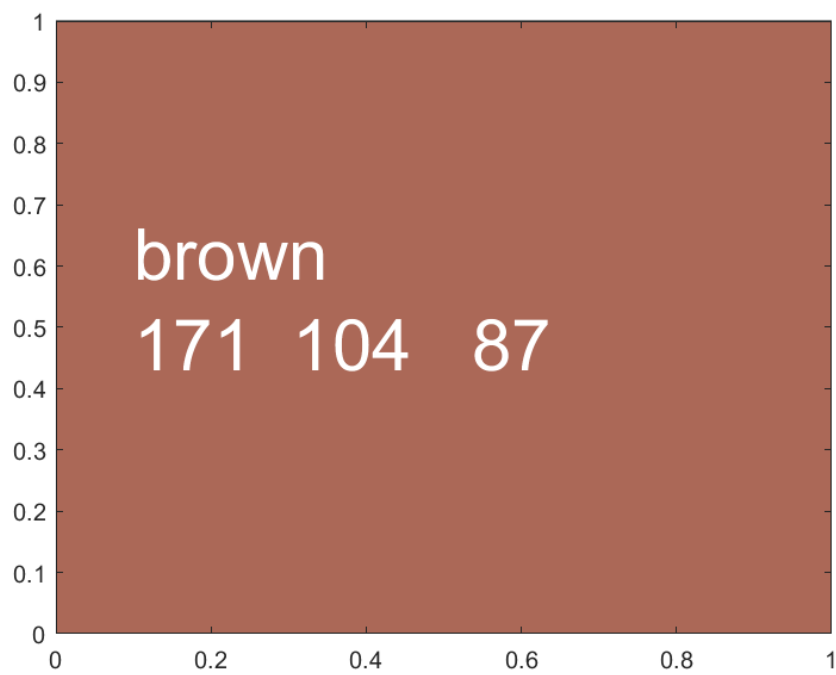
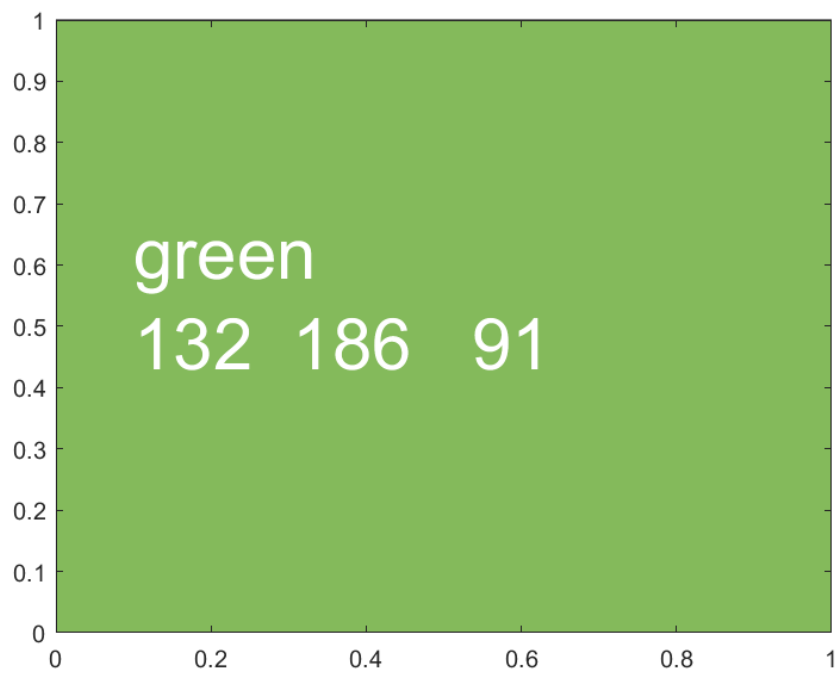
end

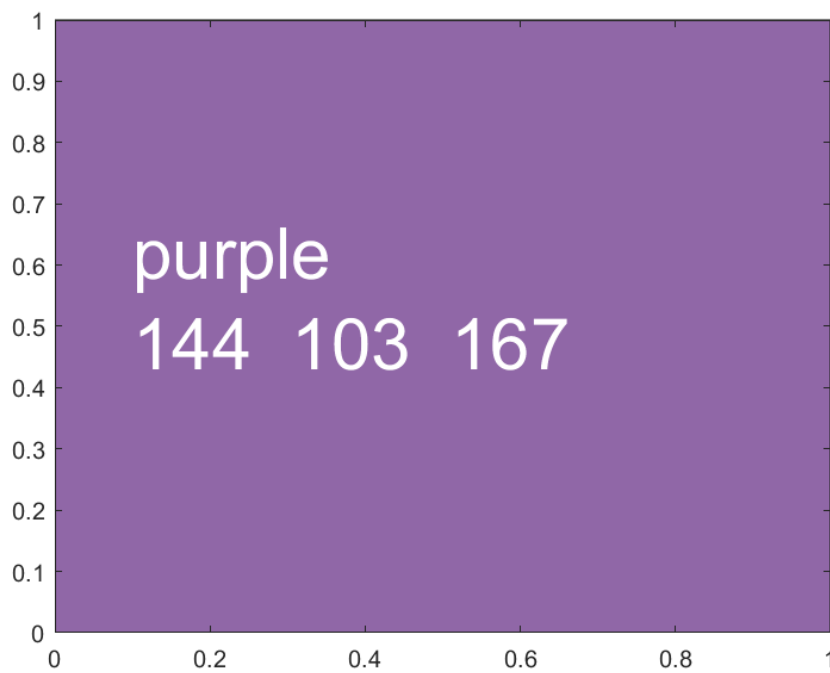
```











### 5.1.1.3 Matlab has a graphical tool for picking color

Enter `uigetcolor` pick color from new window and color values will appear `uigetcolor`

```
% Color Pickers
% uigetcolor
```

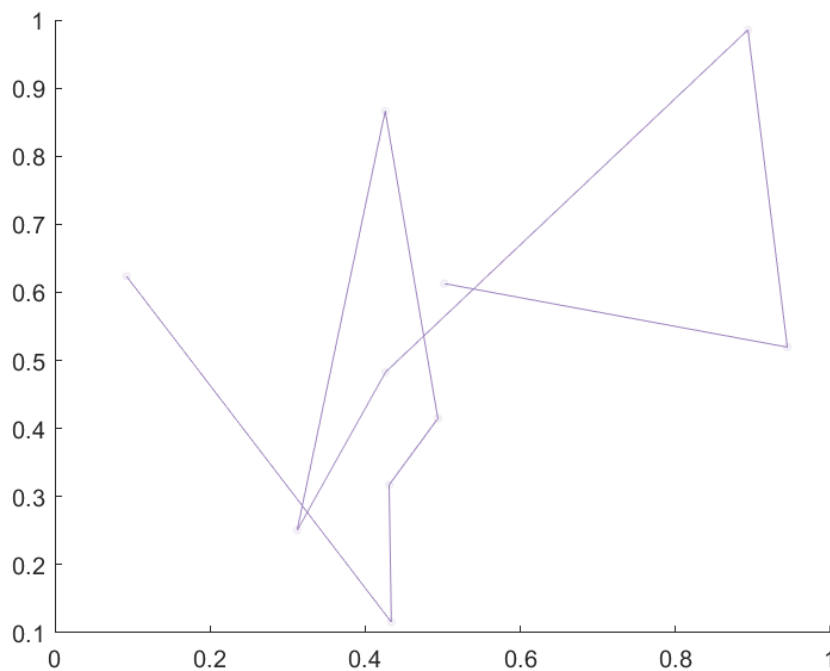
Picked Color use

```
figure();
hold on;

x = rand([10,1]);
y = rand([10,1]);

% Then can use for plot
plot(x,y,'Color',[.61 .51 .74]);

% Can use for Scatter
scatter(x, y, 10, ...
    'MarkerEdgeColor', [.61 .51 .74], 'MarkerFaceAlpha', 0.1, ...
    'MarkerFaceColor', [.61 .51 .74], 'MarkerEdgeAlpha', 0.1);
```



### 5.1.2 Matlab Graph Titling, Labels and Legends Examples

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

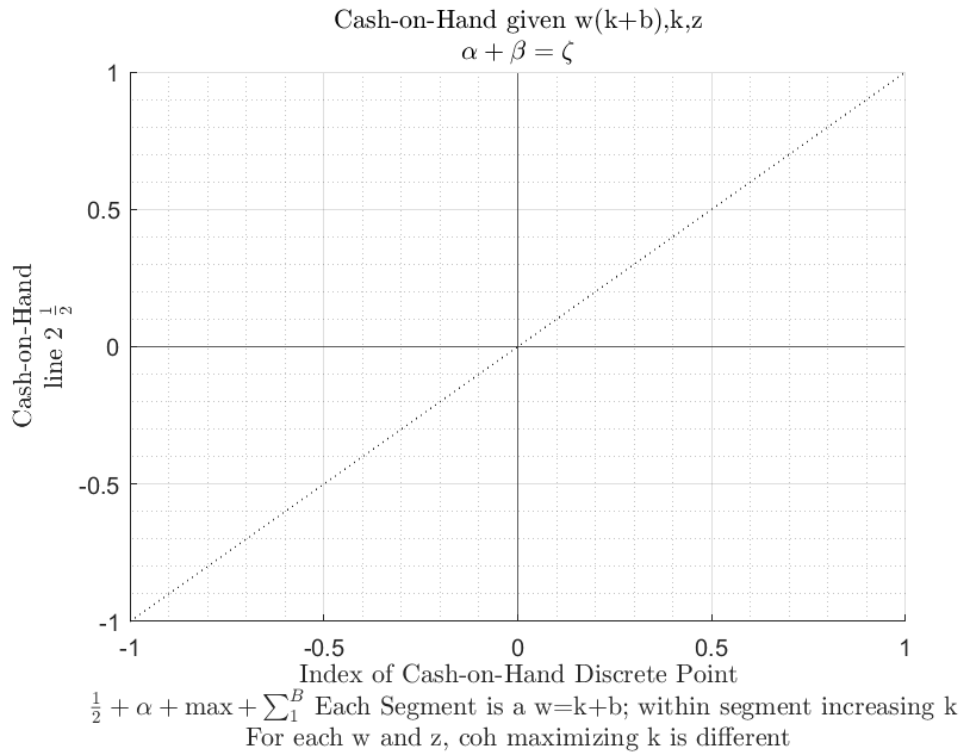
#### 5.1.2.1 Draw A figure Label Title, X and Y Axes with Latex Equations

```
clear all;
close all;
figure();

% draw some lines
xline0 = xline(0);
xline0.HandleVisibility = 'off';
yline0 = yline(0);
yline0.HandleVisibility = 'off';
hline = refline([1 0]);
hline.Color = 'k';
hline.LineStyle = ':';
hline.HandleVisibility = 'off';

% Titling with multiple lines
title({'Cash-on-Hand given  $w(k+b)$ ,  $k$ ,  $z$ ' '$\alpha + \beta = \zeta$', 'Interpreter', 'latex');
ylabel({'Cash-on-Hand' 'line 2 $\frac{1}{2}$'}, 'Interpreter', 'latex');
xlabel({'Index of Cash-on-Hand Discrete Point'...
' $\frac{1}{2} + \alpha + \max + \sum_1^B$ Each Segment is a  $w=k+b$ ; within segment increases by  $b$ '
'For each  $w$  and  $z$ ,  $coh$  maximizing  $k$  is different'}, 'Interpreter', 'latex');

grid on;
grid minor;
```



### 5.1.2.2 Matlab Graph Specify Legends Manually

Specify labels manually, note we can use `HandleVisibility` to control what part of figure show up in legends.

```
% Generate Random Data
rng(123);
it_x_n = 10;
it_x_groups_n = 3;
mat_y = rand([it_x_n, it_x_groups_n]);
mat_y = mat_y + sqrt(1:it_x_groups_n);
mat_y = mat_y + log(1:it_x_n)';
ar_x = 1:1:it_x_n;

% Start Figure
figure('PaperPosition', [0 0 10 10]);

hold on;

g1 = scatter(ar_x, mat_y(:,1), 30, 'filled');
g2 = scatter(ar_x, mat_y(:,2), 30, 'filled');
g3 = scatter(ar_x, mat_y(:,3), 30, 'filled');

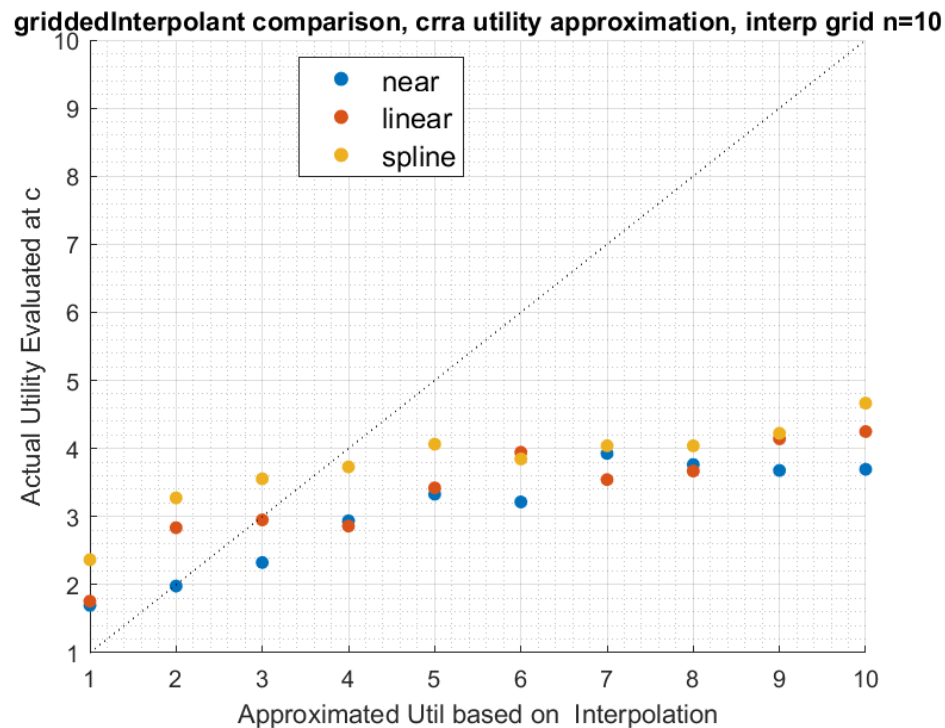
legend([g1, g2, g3], {'near', 'linear', 'spline'}, 'Location', 'best', ...
    'NumColumns', 1, 'FontSize', 12, 'TextColor', 'black');

% PLOT this line, but this line will not show up in legend
hline = reline([1 0]);
hline.Color = 'k';
hline.LineStyle = ':';
% not to show up in legend
hline.HandleVisibility = 'off';
grid on;
grid minor;
```

```

title(sprintf('griddedInterpolant comparison, crra utility approximation, interp grid n=%d', it_x_n))
ylabel('Actual Utility Evaluated at c')
xlabel('Approximated Util based on Interpolation')

```



```

snapnow;

```

### 5.1.2.3 Given Graph, Graph Subset of Lines and Add Extra Line with Legend

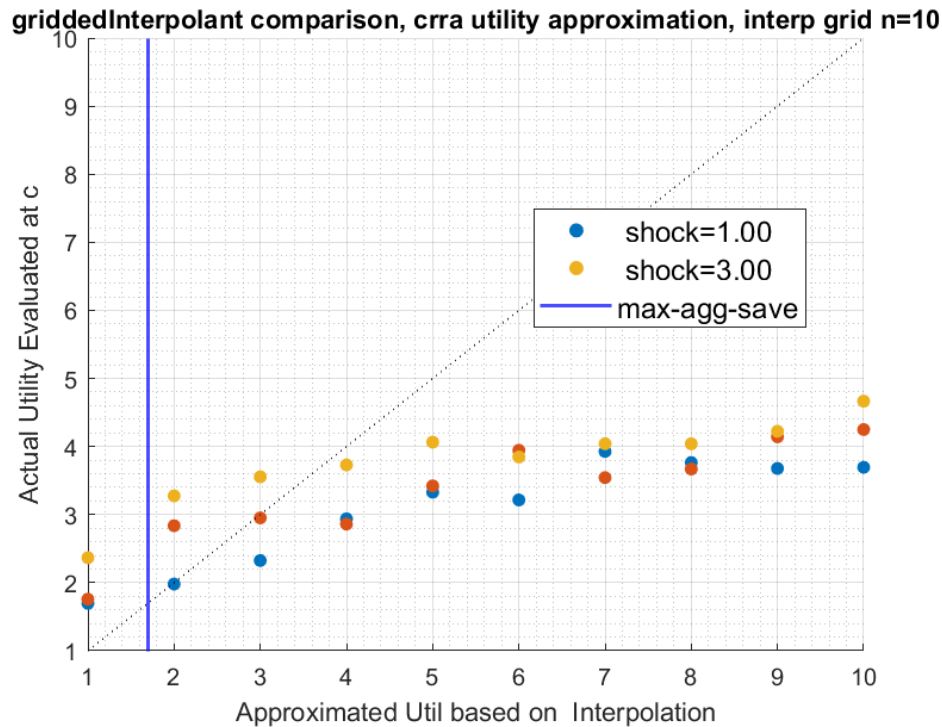
Same plot as before, except we plot only 2 of the three lines and add another line with associated legend entry.

```

legendCell = cellstr(num2str(ar_x', 'shock=%3.2f'));
xlinemax = xline(min(mat_y, [], 'all'));
xlinemax.Color = 'b';
xlinemax.LineWidth = 1.5;

legendCell[length(legendCell) + 1] = 'max-agg-save';
legend([g1, g3, xlinemax], legendCell([1,3,length(legendCell)]), 'Location', 'best');

```



```
snapnow;
```

### 5.1.3 Matlab Graph Matrix with Jet Spectrum Color, Label a Subset Examples

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 5.1.3.1 Plot a Subset of Data Matrix with Appropriate Legends

Sometimes we solve a model across many states, but we can only plot at a subset of states, or perhaps we plot at all states, but only show legends/labels for a subset.

In the example below, many lines are plotted, however, only a subset of lines are labeled in the legend.

```
clear all;
close all;

% Generate Random Data
rng(123);
it_x_n = 10;
it_y_groups_n = 100;
ar_y = linspace(1,2,it_y_groups_n);
mat_y = rand([it_x_n, it_y_groups_n]);
mat_y = mat_y + sqrt(1:it_y_groups_n);
mat_y = mat_y + log(1:it_x_n)' + ar_y;
ar_x = 1:1:it_x_n;

% Jet color Graph All
figure('PaperPosition', [0 0 7 4]);
chart = plot(mat_y);
clr = jet(numel(chart));
for m = 1:numel(chart)
    set(chart(m),'Color',clr(m,:))
end
```

```

% zero lines
xline(0);
yline(0);

% invalid points separating lines
yline_borrbound = yline(3);
yline_borrbound.HandleVisibility = 'on';
yline_borrbound.LineStyle = ':';
yline_borrbound.Color = 'black';
yline_borrbound.LineWidth = 3;

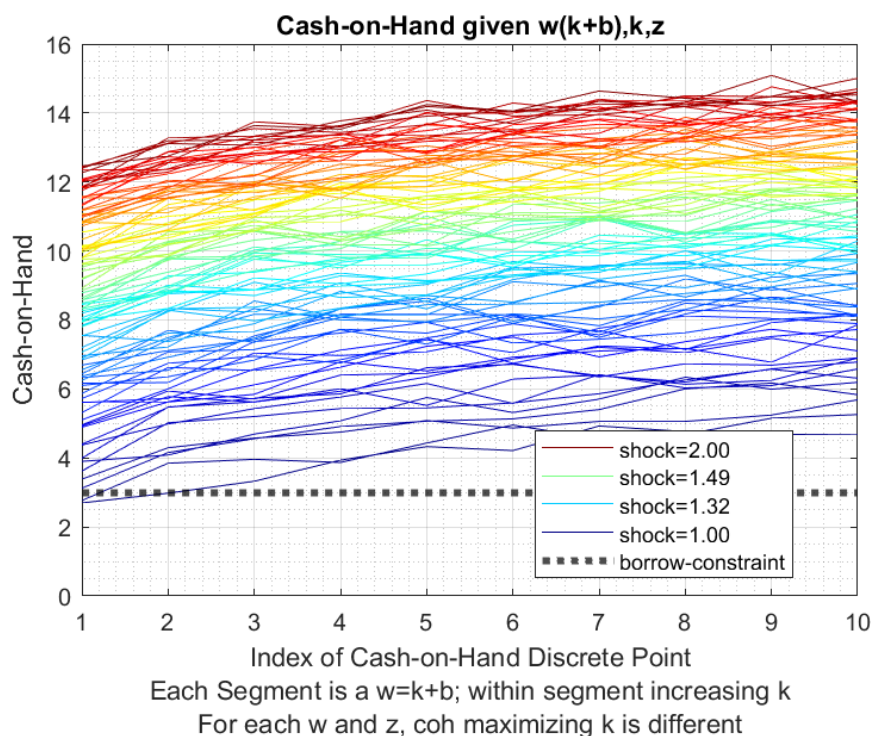
% Titling
title('Cash-on-Hand given w(k+b),k,z');
ylabel('Cash-on-Hand');
xlabel({'Index of Cash-on-Hand Discrete Point'...
    'Each Segment is a w=k+b; within segment increasing k'...
    'For each w and z, coh maximizing k is different'});

% Xlim controls
xlim([min(ar_x), max(ar_x)]);

% Grid ons
grid on;
grid minor;
% Legends
legend2plot = fliplr([1 round(numel(chart))/3 round((2*numel(chart))/4) numel(chart)]);
legendCell = cellstr(num2str(ar_y', 'shock=%3.2f'));

legendCell{length(legendCell) + 1} = 'borrow-constraint';
chart(length(chart)+1) = yline_borrbound;
legend(chart([legend2plot length(legendCell)]), ...
    legendCell([legend2plot length(legendCell)]), ...
    'Location', 'best');

```



## 5.2 Basic Figure Types

### 5.2.1 Matlab Graph Scatter Plot Examples

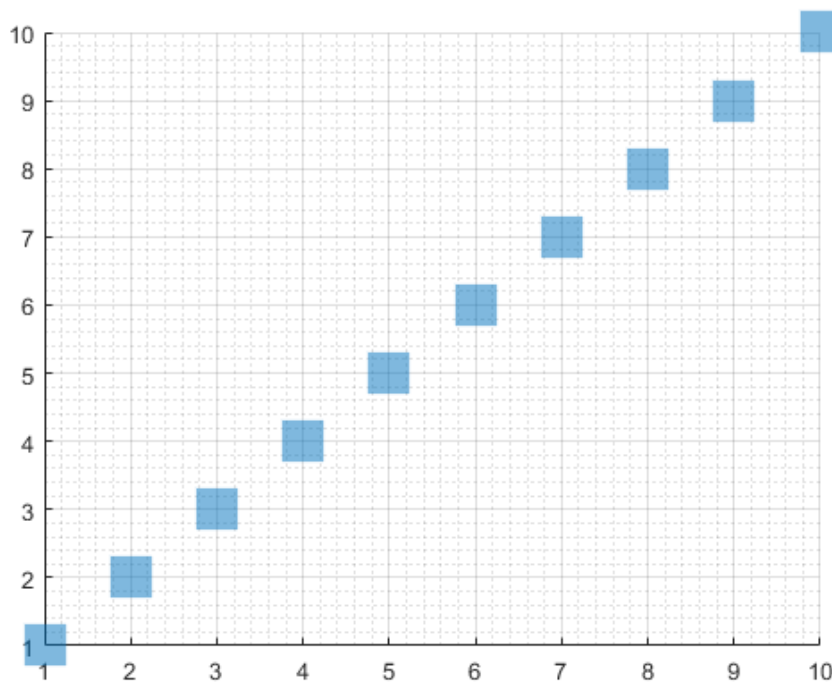
Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 5.2.1.1 Scatter Plot Example

The plot below as square scatter points, each one with thick border. Can set transparency of border/edge and inside separately.

```
close all;
figure();
size = 100;
s = scatter(1:10,1:10,size);

s.Marker = 's';
% color picked by using: uisetcolor
s.MarkerEdgeColor = [0 0.4471 0.7412];
s.MarkerEdgeAlpha = 0.5;
s.MarkerFaceColor = [.61 .51 .74];
s.MarkerFaceAlpha = 1.0;
s.LineWidth = 10;
grid on;
grid minor;
```



```
% 'o'   Circle
% '+'   Plus sign
% '*'   Asterisk
% '.'   Point
% 'x'   Cross
% 'square' or 's'   Square
% 'diamond' or 'd'   Diamond
% '^'   Upward-pointing triangle
% 'v'   Downward-pointing triangle
```



```
% '>'   Right-pointing triangle
% '<'   Left-pointing triangle
% 'pentagram' or 'p'   Five-pointed star (pentagram)
% 'hexagram' or 'h'   Six-pointed star (hexagram)
% 'none'   No markers
```

### 5.2.1.2 Scatter with Edge and Face Color and Transparency

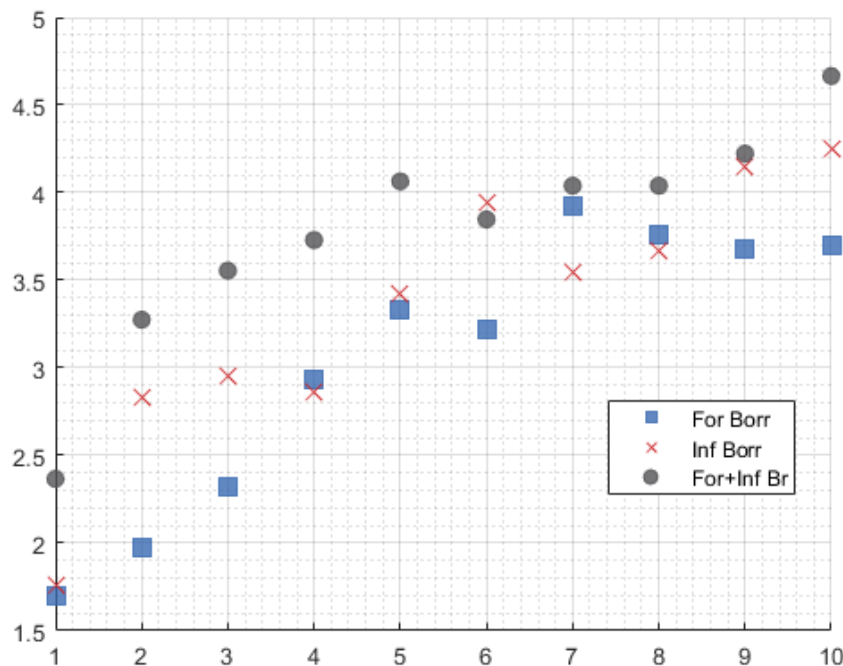
Here is another way to Set Scatter Edge and Fac Colors and Transparencies.

```
% Generate Data
rng(123);
it_x_n = 10;
it_x_groups_n = 3;
mat_y = rand([it_x_n, it_x_groups_n]);
mat_y = mat_y + sqrt(1:it_x_groups_n);
mat_y = mat_y + log(1:it_x_n)';
ar_x = 1:1:it_x_n;

% Colors
blue = [57 106 177]./255;
red = [204 37 41]./255;
black = [83 81 84]./255;
green = [62 150 81]./255;
brown = [146 36 40]./255;
purple = [107 76 154]./255;
cl_colors = {blue, red, black, ...
             green, brown, purple};

% Scatter Shapes
cl_scatter_shapes = {'s','x','o','d','p','*'};
% Scatter Sizes
cl_scatter_sizes = {100,100,50,50,50,50};
% Legend Keys
cl_legend = {'For Borr', 'Inf Borr', 'For+Inf Br'};

% Plot
figure();
hold on;
for it_m = 1:it_x_groups_n
    scatter(ar_x, mat_y(:,it_m), cl_scatter_sizes{it_m}, ...
           'Marker', cl_scatter_shapes{it_m}, ...
           'MarkerEdgeColor', cl_colors{it_m}, 'MarkerFaceAlpha', 0.8, ...
           'MarkerFaceColor', cl_colors{it_m}, 'MarkerEdgeAlpha', 0.8);
    cl_legend{it_m} = cl_legend{it_m};
end
legend(cl_legend, 'Location', 'best');
grid on;
grid minor;
```



## 5.2.2 Matlab Line and Scatter Plot with Multiple Lines and Axis Lines

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

### 5.2.2.1 Six lines Plot

Colors from [optimal colors](#). Generate A line plot with multiple lines using safe colors, with differencing shapes. Figures include lines as well as scatter overlayed jointly.

```
close all
figure();
hold on;

blue = [57 106 177]./255;
red = [204 37 41]./255;
black = [83 81 84]./255;
green = [62 150 81]./255;
brown = [146 36 40]./255;
purple = [107 76 154]./255;
cl_colors = {blue, red, black, ...
             green, brown, purple};
cl_legend = {'For Borr', 'Inf Borr', 'For+Inf Br', 'For+Br+Save', 'Bridge Loan', 'For Save'};
cl_scatter_shapes = {'s','x','o','d','p','*'};
cl_linestyle = {'--','-',':','-.-','--','-'};
it_sca_bs = 20;
cl_scatter_csizes = {10*it_sca_bs, 20*it_sca_bs, 10*it_sca_bs, 10*it_sca_bs, 5*it_sca_bs, 8*it_sca_bs};
it_line_bs = 2;
cl_line_csizes = {1*it_line_bs, 2*it_line_bs, 1*it_line_bs, 1*it_line_bs, 1*it_line_bs, 2*it_line_bs};

it_x_groups_n = length(cl_scatter_csizes);
it_x_n = 10;
```

```
% Generate Random Data
```

```

rng(123);
mat_y = rand([it_x_n, it_x_groups_n]);
mat_y = mat_y + sqrt(1:it_x_groups_n);
mat_y = mat_y + log(1:it_x_n)';
ar_x = 1:1:it_x_n;

ar_it_graphs_run = 1:6;
it_graph_counter = 0;
ls_chart = [];
for it_fig = ar_it_graphs_run

    % Counter
    it_graph_counter = it_graph_counter + 1;

    % Y Outcome
    ar_y = mat_y(:, it_fig)';

    % Color and Size etc
    it_csize = cl_scatter_csizes{it_fig};
    ar_color = cl_colors{it_fig};
    st_shape = cl_scatter_shapes{it_fig};
    st_lnsty = cl_linestyle{it_fig};
    st_lnwth = cl_line_csizes{it_fig};

    % plot scatter and include in legend
    ls_chart(it_graph_counter) = scatter(ar_x, ar_y, it_csize, ar_color, st_shape);

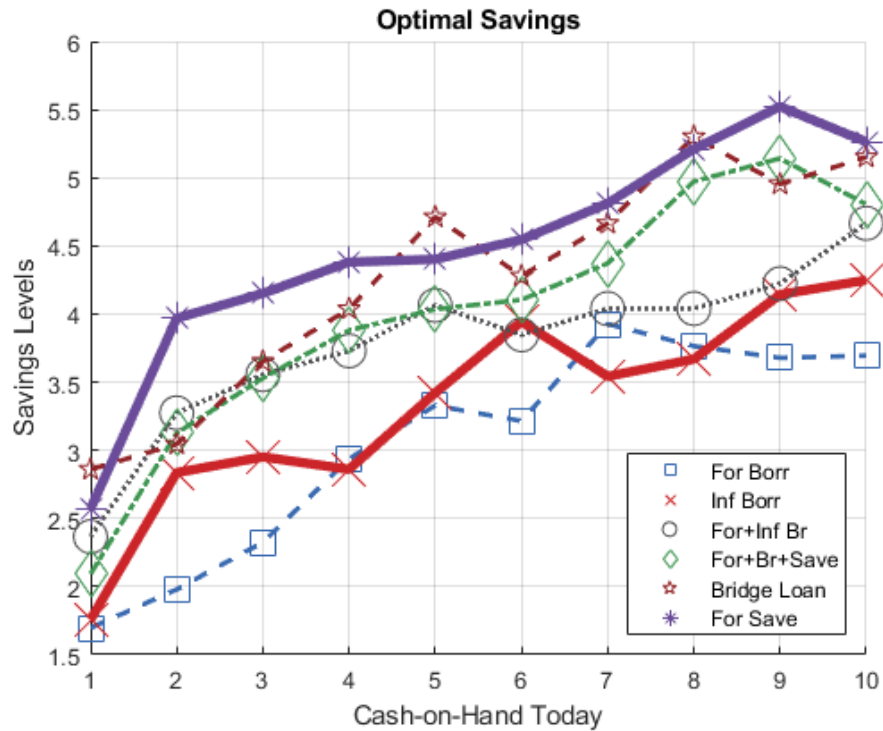
    % plot line do not include in legend
    line = plot(ar_x, ar_y);
    line.HandleVisibility = 'off';
    line.Color = ar_color;
    line.LineStyle = st_lnsty;
    line.HandleVisibility = 'off';
    line.LineWidth = st_lnwth;

    % Legend to include
    cl_legend{it_graph_counter} = cl_legend{it_fig};
end

% Legend
legend(ls_chart, cl_legend, 'Location', 'southeast');

% labeling
title('Optimal Savings');
ylabel('Savings Levels');
xlabel('Cash-on-Hand Today');
grid on;

```



```
snapnow;
```

### 5.2.2.2 Horizontal and Vertical Lines and 45 Degree

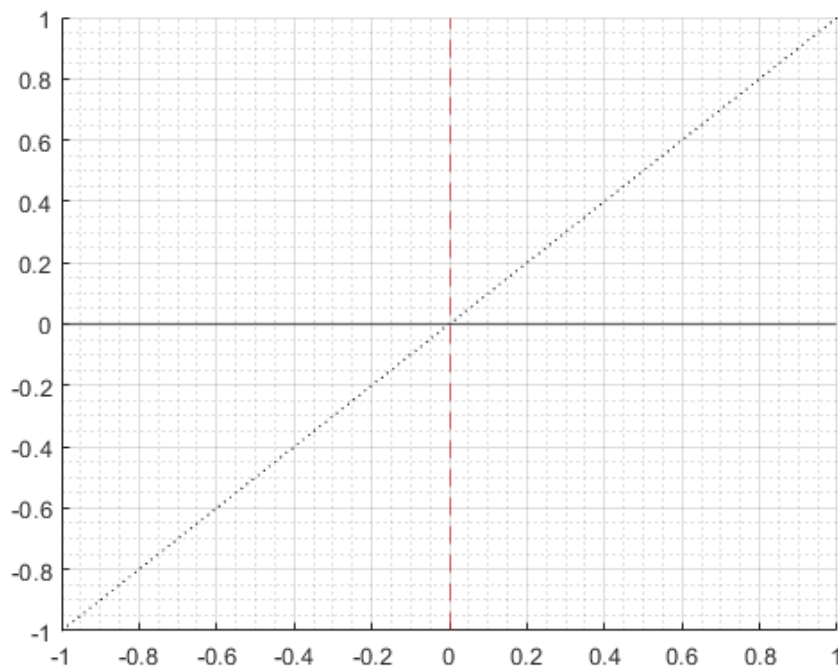
Draw x and y axis, and draw a 45 degree line.

```
figure();

xline0 = xline(0);
xline0.HandleVisibility = 'off';
xline0.Color = red;
xline0.LineStyle = '--';
yline0 = yline(0);
yline0.HandleVisibility = 'off';
yline0.LineWidth = 1;

hline = refile([1 0]);
hline.Color = 'k';
hline.LineStyle = ':';
hline.HandleVisibility = 'off';

snapnow;
grid on;
grid minor;
```



### 5.2.3 Matlab Graph Scatter and Line Spectrum with Three Variables

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

Generate  $k + b = w$ , color for each  $w$ , vectors of  $k$  and  $b$  such that  $k + b = w$  for each  $w$

There are two  $N$  by  $M$  matrix,  $A$  and  $B$ .

Values in Matrix  $A$  correspond to the x-axis, values in Matrix  $B$  correspond to the y-axis.

The rows and columns in matrix  $A$  and  $B$  have some other meanings. In this case, we will give color to the columns.

The columns is represented by vector  $C$ , which is another variable.

1. Each line a different color representing variable 3
2. Legend labeling a subset of colors
3.  $X$  and  $Y$  could be asset choices, color could be utility, consumption etc.

#### 5.2.3.1 Setting Up Data

```
close all
clear all

% Bounds
fl_b_bd = -10;
% Max and Mins
fl_w_max = 50;
fl_w_min = fl_b_bd;
fl_kp_max = fl_w_max - fl_b_bd;
fl_kp_min = 0;

% Grid Point Counts
it_w_i = 30;
it_kb_j = 30;
```

```

% Grids
ar_w = linspace(fl_w_min, fl_w_max, it_w_i);
ar_kp = linspace(fl_kp_min, fl_kp_max, it_kb_j);
mt_bp = ar_w - ar_kp';
mt_kp = ar_w - mt_bp;
mt_bl_constrained = (mt_bp < fl_b_bd);
mt_bp_wth_na = mt_bp;
mt_kp_wth_na = mt_kp;
mt_bp_wth_na(mt_bl_constrained) = nan;
mt_kp_wth_na(mt_bl_constrained) = nan;

% Flatten
ar_bp_mw_wth_na = mt_bp_wth_na(:);
ar_kp_mw_wth_na = mt_kp_wth_na(:);
ar_bp_mw = ar_bp_mw_wth_na(~isnan(ar_bp_mw_wth_na));
ar_kp_mw = ar_kp_mw_wth_na(~isnan(ar_kp_mw_wth_na));

```

### 5.2.3.2 Graphing

```

figure('PaperPosition', [0 0 7 4]);
hold on;

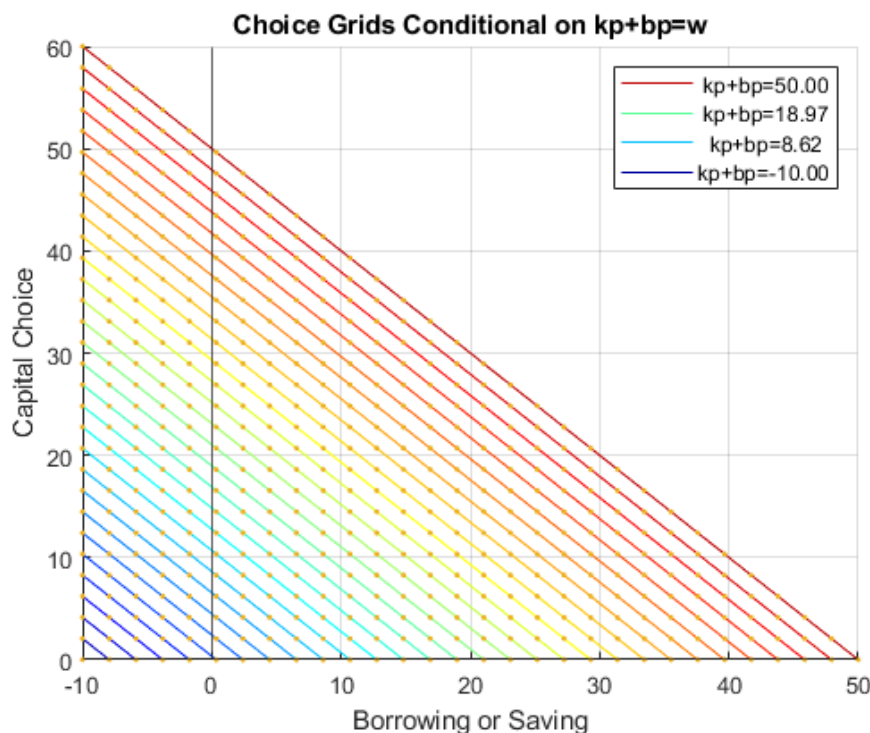
chart = plot(mt_bp_wth_na, mt_kp_wth_na, 'blue');

clr = jet(numel(chart));
for m = 1:numel(chart)
    set(chart(m), 'Color', clr(m,:))
end
if (length(ar_w) <= 50)
    scatter(ar_bp_mw, ar_kp_mw, 5, 'filled');
end
xline(0);
yline(0);

title('Choice Grids Conditional on kp+bp=w')
ylabel('Capital Choice')
xlabel({'Borrowing or Saving'})
legend2plot = fliplr([1 round(numel(chart)/3) round((2*numel(chart))/4) numel(chart)]);
legendCell = cellstr(num2str(ar_w', 'kp+bp=%3.2f'));
legend(chart(legend2plot), legendCell(legend2plot), 'Location','northeast');

grid on;

```



## 5.3 Write and Read Plots

### 5.3.1 Matlab Graph Generate EPS postscript figures in matlab

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 5.3.1.1 Properly Save EPS with Scatter and Other Graphing Methods: `Renderer = Painters`

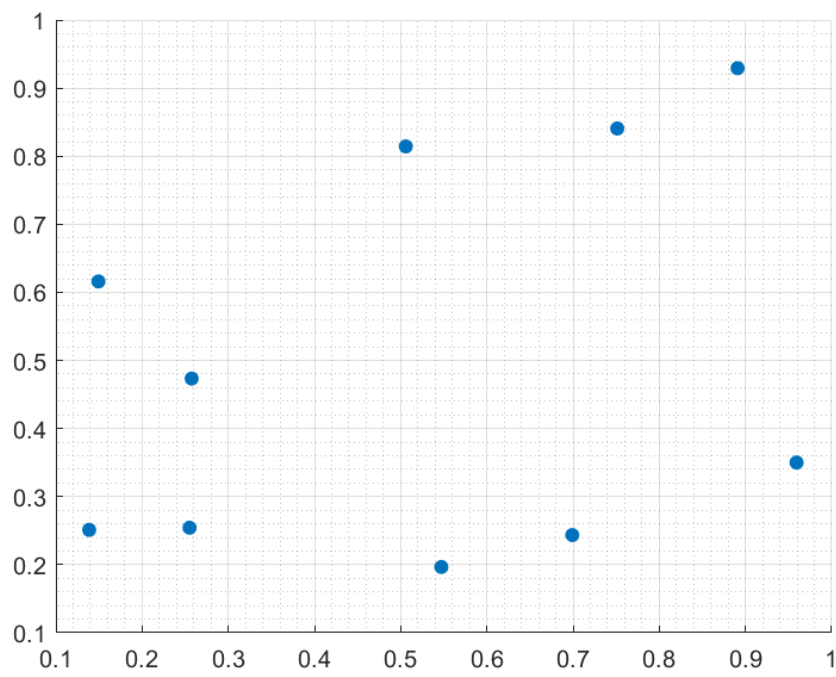
scatter plot saving as eps seems to only work when `Renderer` is set to `Painters`

```
fl_fig_wdt = 3;
fl_fig_hgt = 2.65;

figure('PaperPosition', [0 0 fl_fig_wdt fl_fig_hgt], 'Renderer', 'Painters');
x = rand([10,1]);
y = rand([10,1]);
scatter(x, y, 'filled');
grid on;
grid minor;

st_img_path = 'C:/Users/fan/M4Econ/graph/export/_img/';
st_file_name = 'fs_eps_scatter_test';

% eps figure save with tiff preview
print(strcat(st_img_path, st_file_name), '-depsc', '-tiff');
```





# Chapter 6

## Tables

### 6.1 Basic Table Generation

#### 6.1.1 Named Tables with Random Data

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

##### 6.1.1.1 Generate A Table with M Variables

Generate a numeric table with random varlues and a string column

```
% Numeric Matrix
it_num_cols = 4;
it_num_rows = 5;
mt_data = rand([it_num_rows, it_num_cols]);

% Generate Table
tb_test = array2table(mt_data);

% Generate Row and Column Names
cl_col_names = strcat('col_', string((1:it_num_cols)));
cl_row_names = strcat('row_', string((1:it_num_rows)));

tb_test.Properties.VariableNames = matlab.lang.makeValidName(cl_col_names);
tb_test.Properties.RowNames = matlab.lang.makeValidName(cl_row_names);

% Generate two string variable
rng(456);
cl_st_var1 = strcat('data=', string(rand([it_num_rows,1])));
cl_st_var2 = strcat('data=', string(rand([it_num_rows,1])));
tb_test = addvars(tb_test, cl_st_var1, cl_st_var2);

% Display Table
disp(tb_test);
```

	col_1	col_2	col_3	col_4	cl_st_var1	cl_st_var2
	-----	-----	-----	-----	-----	-----
row_1	0.43568	0.4688	0.18092	0.14604	"data=0.24876"	"data=0.60411"
row_2	0.38527	0.57	0.11816	0.54272	"data=0.16307"	"data=0.8857"
row_3	0.57571	0.6457	0.24273	0.8571	"data=0.78364"	"data=0.75912"
row_4	0.14609	0.72334	0.0081834	0.20021	"data=0.80852"	"data=0.18111"
row_5	0.68659	0.68067	0.36007	0.13463	"data=0.62563"	"data=0.15017"

### 6.1.2 Tables Order, Sort, Add, Rename and Drop Columns

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

#### 6.1.2.1 Given Table, Show Some Columns First

```
% Generate Table
it_num_cols = 4;
it_num_rows = 5;
mt_data = rand([it_num_rows, it_num_cols]);
tb_test = array2table(mt_data);
cl_col_names = strcat('col_', string((1:it_num_cols)));
cl_row_names = strcat('row_', string((1:it_num_rows)));
tb_test.Properties.VariableNames = matlab.lang.makeValidName(cl_col_names);
tb_test.Properties.RowNames = matlab.lang.makeValidName(cl_row_names);

rng(123);
mean = strcat('data=', string(rand([it_num_rows,1])));
sd = strcat('data=', string(rand([it_num_rows,1])));
tb_test_ori = addvars(tb_test, mean, sd);

% Move Variable
tb_test_varmove = movevars(tb_test_ori, {'mean', 'sd'}, 'Before', 'col_1');

% Display
disp(tb_test_ori);
```

	col_1	col_2	col_3	col_4	mean	sd
row_1	0.34318	0.738	0.6344	0.32296	"data=0.69647"	"data=0.42311"
row_2	0.72905	0.18249	0.84943	0.36179	"data=0.28614"	"data=0.98076"
row_3	0.43857	0.17545	0.72446	0.22826	"data=0.22685"	"data=0.68483"
row_4	0.059678	0.53155	0.61102	0.29371	"data=0.55131"	"data=0.48093"
row_5	0.39804	0.53183	0.72244	0.63098	"data=0.71947"	"data=0.39212"

```
disp(tb_test_varmove);
```

	mean	sd	col_1	col_2	col_3	col_4
row_1	"data=0.69647"	"data=0.42311"	0.34318	0.738	0.6344	0.32296
row_2	"data=0.28614"	"data=0.98076"	0.72905	0.18249	0.84943	0.36179
row_3	"data=0.22685"	"data=0.68483"	0.43857	0.17545	0.72446	0.22826
row_4	"data=0.55131"	"data=0.48093"	0.059678	0.53155	0.61102	0.29371
row_5	"data=0.71947"	"data=0.39212"	0.39804	0.53183	0.72244	0.63098

#### 6.1.2.2 Rename Table Columns

Rename the first Column, rename the 'sd' column, then rename the 3rd and 4th Columns. Note for multiple column renaming, use parenthesis, but for single column renaming, use bracket.

```
tb_test_varmove.Properties.VariableNames{1} = 'RenameMean';
tb_test_varmove.Properties.VariableNames{'sd'} = 'RenameSDCol';
tb_test_varmove.Properties.VariableNames([3 4]) = {'3rd' '4th'};
disp(tb_test_varmove);
```

	RenameMean	RenameSDCol	3rd	4th	col_3	col_4
row_1	"data=0.69647"	"data=0.42311"	0.34318	0.738	0.6344	0.32296
row_2	"data=0.28614"	"data=0.98076"	0.72905	0.18249	0.84943	0.36179
row_3	"data=0.22685"	"data=0.68483"	0.43857	0.17545	0.72446	0.22826
row_4	"data=0.55131"	"data=0.48093"	0.059678	0.53155	0.61102	0.29371
row_5	"data=0.71947"	"data=0.39212"	0.39804	0.53183	0.72244	0.63098

row_1	"data=0.69647"	"data=0.42311"	0.34318	0.738	0.6344	0.32296
row_2	"data=0.28614"	"data=0.98076"	0.72905	0.18249	0.84943	0.36179
row_3	"data=0.22685"	"data=0.68483"	0.43857	0.17545	0.72446	0.22826
row_4	"data=0.55131"	"data=0.48093"	0.059678	0.53155	0.61102	0.29371
row_5	"data=0.71947"	"data=0.39212"	0.39804	0.53183	0.72244	0.63098

### 6.1.2.3 Remove Table Column

Remove columns from the Table

```
tb_test_varmove_drop = removevars(tb_test_varmove, {'3rd', 'col_3'});
disp(tb_test_varmove_drop);
```

	RenameMean	RenameSDCol	4th	col_4
	-----	-----	-----	-----
row_1	"data=0.69647"	"data=0.42311"	0.738	0.32296
row_2	"data=0.28614"	"data=0.98076"	0.18249	0.36179
row_3	"data=0.22685"	"data=0.68483"	0.17545	0.22826
row_4	"data=0.55131"	"data=0.48093"	0.53155	0.29371
row_5	"data=0.71947"	"data=0.39212"	0.53183	0.63098

## 6.1.3 Row and Column Names for Table based on Arrays

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository \(bookdown site\)](#), or [Math for Econ with Matlab Repository \(bookdown site\)](#).

### 6.1.3.1 Generate Table with Row and Column Names based on Multiple Numeric Array

Two numeric arrays describe the column names, combine numeric arrays together to form string array which becomes table variable/column names.

```
close all;
```

```
% Generate Table 1
ar_fl_abc1 = [0.4 0.1 0.25 0.3 0.4];
ar_fl_abc2 = [0.4 0.1 0.2 0.3 0.4];
number1 = '123';
number2 = '456';
mt_data_a = [ar_fl_abc1' ar_fl_abc2'];

tb_test_a = array2table(mt_data_a);
cl_col_names_a = {'col' num2str(number1)}, ['col' num2str(number2)];
cl_row_names_a = strcat('rowA=', string((1:size(mt_data_a,1)))));

tb_test_a.Properties.VariableNames = cl_col_names_a;
tb_test_a.Properties.RowNames = cl_row_names_a;
disp(tb_test_a);
```

	col123	col456
	-----	-----
rowA=1	0.4	0.4
rowA=2	0.1	0.1
rowA=3	0.25	0.2
rowA=4	0.3	0.3
rowA=5	0.4	0.4

### 6.1.3.2 Include Row Names as a String Cell Variable

```
% a and b must have the same row names
cl_st_varrownames = tb_test_a.Properties.RowNames;
tb_test_a = addvars(tb_test_a, cl_st_varrownames, 'Before', 1);

disp(tb_test_a);
```

	cl_st_varrownames	col123	col456
	-----	-----	-----
rowA=1	{'rowA=1'}	0.4	0.4
rowA=2	{'rowA=2'}	0.1	0.1
rowA=3	{'rowA=3'}	0.25	0.2
rowA=4	{'rowA=4'}	0.3	0.3
rowA=5	{'rowA=5'}	0.4	0.4

### 6.1.3.3 Include Row Names as a String Variable

```
% a and b must have the same row names
st_varrownames = string(cl_st_varrownames);
tb_test_a = addvars(tb_test_a, st_varrownames, 'Before', 1);
disp(tb_test_a);
```

	st_varrownames	cl_st_varrownames	col123	col456
	-----	-----	-----	-----
rowA=1	"rowA=1"	{'rowA=1'}	0.4	0.4
rowA=2	"rowA=2"	{'rowA=2'}	0.1	0.1
rowA=3	"rowA=3"	{'rowA=3'}	0.25	0.2
rowA=4	"rowA=4"	{'rowA=4'}	0.3	0.3
rowA=5	"rowA=5"	{'rowA=5'}	0.4	0.4

### 6.1.3.4 Remove Row Names

Remove row names

```
tb_test_a.Properties.RowNames = {};
disp(tb_test_a);
```

st_varrownames	cl_st_varrownames	col123	col456
-----	-----	-----	-----
"rowA=1"	{'rowA=1'}	0.4	0.4
"rowA=2"	{'rowA=2'}	0.1	0.1
"rowA=3"	{'rowA=3'}	0.25	0.2
"rowA=4"	{'rowA=4'}	0.3	0.3
"rowA=5"	{'rowA=5'}	0.4	0.4

## 6.1.4 Select Subset of Rows and Columns

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

### 6.1.4.1 Generate a Table

```
close all;
% Generate Table 1
ar_fl_abc1 = [0.4 0.1 0.25 0.3 0.4];
ar_fl_abc2 = [0.4 0.1 0.2 0.3 0.4];
```

```

number1 = '123';
number2 = '456';
mt_data_a = [ar_fl_abc1' ar_fl_abc2'];
tb_test_a = array2table(mt_data_a);
cl_col_names_a = {'col' num2str(number1)}, {'col' num2str(number2)};
cl_row_names_a = strcat('rowA=', string((1:size(mt_data_a,1))));
tb_test_a.Properties.VariableNames = cl_col_names_a;
tb_test_a.Properties.RowNames = cl_row_names_a;
% a and b must have the same row names
cl_st_varrownames = tb_test_a.Properties.RowNames;
tb_test_a = addvars(tb_test_a, cl_st_varrownames, 'Before', 1);
% a and b must have the same row names
st_varrownames = string(cl_st_varrownames);
tb_test_a = addvars(tb_test_a, st_varrownames, 'Before', 1);
tb_test_a = addvars(tb_test_a, ["a", "b", "cc", "aa", "b"], 'Before', 1);
disp(tb_test_a);

```

	Var1	st_varrownames	cl_st_varrownames	col123	col456
	----	-----	-----	-----	-----
rowA=1	"a"	"rowA=1"	{'rowA=1'}	0.4	0.4
rowA=2	"b"	"rowA=2"	{'rowA=2'}	0.1	0.1
rowA=3	"cc"	"rowA=3"	{'rowA=3'}	0.25	0.2
rowA=4	"aa"	"rowA=4"	{'rowA=4'}	0.3	0.3
rowA=5	"b"	"rowA=5"	{'rowA=5'}	0.4	0.4

#### 6.1.4.2 Select Rows if ColX is Equal to Something

Select a subset of rows based on the variable value in one column

```

% select the rows where Var1="b"
disp(tb_test_a(strcmp(tb_test_a.Var1, "b"),:));

```

	Var1	st_varrownames	cl_st_varrownames	col123	col456
	----	-----	-----	-----	-----
rowA=2	"b"	"rowA=2"	{'rowA=2'}	0.1	0.1
rowA=5	"b"	"rowA=5"	{'rowA=5'}	0.4	0.4

```

% select the rows where col123=0.4
disp(tb_test_a(tb_test_a.col123==0.4,:));

```

	Var1	st_varrownames	cl_st_varrownames	col123	col456
	----	-----	-----	-----	-----
rowA=1	"a"	"rowA=1"	{'rowA=1'}	0.4	0.4
rowA=5	"b"	"rowA=5"	{'rowA=5'}	0.4	0.4

## 6.2 Table Joining

### 6.2.1 Row and Column Combine Stack Tables and Matrices

Go back to [fan's MEconTools Package](#), [Matlab Code Examples Repository](#) ([bookdown site](#)), or [Math for Econ with Matlab Repository](#) ([bookdown site](#)).

#### 6.2.1.1 Generate Some Tables and Matrixes for Combination

```
close all;
```

```
% Generate Table 1
ar_fl_abc1 = [0.4 0.1 0.25 0.3 0.4];
ar_fl_abc2 = [0.4 0.1 0.2 0.3 0.4];
number1 = '123';
number2 = '456';
mt_data_a = [ar_fl_abc1' ar_fl_abc2'];

tb_test_a = array2table(mt_data_a);
cl_col_names_a = {'col' num2str(number1)}, ['col' num2str(number2)]};
cl_row_names_a = strcat('rowA=', string((1:size(mt_data_a,1)))));

tb_test_a.Properties.VariableNames = cl_col_names_a;
tb_test_a.Properties.RowNames = cl_row_names_a;
disp(tb_test_a);
```

	col123	col456
	-----	-----
rowA=1	0.4	0.4
rowA=2	0.1	0.1
rowA=3	0.25	0.2
rowA=4	0.3	0.3
rowA=5	0.4	0.4

```
% Generate Table 2
rng(123);
ar_fl_abc3 = rand(size(ar_fl_abc1));
ar_fl_abc4 = rand(size(ar_fl_abc1));
ar_fl_abc5 = rand(size(ar_fl_abc1));

mt_data_b = [ar_fl_abc3' ar_fl_abc4' ar_fl_abc5'];

tb_test_b = array2table(mt_data_b);
cl_col_names_b = {'col' num2str(33)}, ['col' num2str(44)}, ['col' num2str(55)]};
cl_row_names_b = strcat('rowB=', string((1:size(mt_data_a,1)))));

tb_test_b.Properties.VariableNames = cl_col_names_b;
tb_test_b.Properties.RowNames = cl_row_names_b;
disp(tb_test_b);
```

	col33	col44	col55
	-----	-----	-----
rowB=1	0.69647	0.42311	0.34318
rowB=2	0.28614	0.98076	0.72905
rowB=3	0.22685	0.68483	0.43857
rowB=4	0.55131	0.48093	0.059678
rowB=5	0.71947	0.39212	0.39804

### 6.2.1.2 Combine Tables Together Stack Columns

Tables with the same number of rows, add more columns with named variables

```
% a and b must have the same row names
tb_test_b_withArownames = tb_test_b;
tb_test_b_withArownames.Properties.RowNames = tb_test_a.Properties.RowNames;
tb_ab_col_stacked = [tb_test_a tb_test_b_withArownames];
disp(tb_ab_col_stacked);
```

	col123	col456	col133	col144	col155
	-----	-----	-----	-----	-----
rowA=1	0.4	0.4	0.69647	0.42311	0.34318
rowA=2	0.1	0.1	0.28614	0.98076	0.72905
rowA=3	0.25	0.2	0.22685	0.68483	0.43857
rowA=4	0.3	0.3	0.55131	0.48093	0.059678
rowA=5	0.4	0.4	0.71947	0.39212	0.39804

### 6.2.1.3 Combine Tables Together Stack Rows

Tables with the same number of columns, dd more rows variables

```
% Select only 2 columns to match table a column count
```

```
tb_test_b_subset = tb_test_b(:,1:2);
```

```
% Make Column Names consistent
```

```
tb_test_b_subset.Properties.VariableNames = cl_col_names_a;
```

```
% Reset Row Names, can not have identical row names
```

```
tb_test_a.Properties.RowNames = strcat('row=', string((1:size(mt_data_a,1))));
```

```
tb_test_b_subset.Properties.RowNames = ...
```

```
    strcat('row=', string(((size(mt_data_a,1)+1):(size(mt_data_a,1)+size(tb_test_b_subset,1)))));
```

```
% tb_test_b_subset.Properties.RowNames =
```

```
% Stack Rows
```

```
tb_ab_row_stacked = [tb_test_a; tb_test_b_subset];
```

```
disp(tb_ab_row_stacked);
```

	col123	col456
	-----	-----
row=1	0.4	0.4
row=2	0.1	0.1
row=3	0.25	0.2
row=4	0.3	0.3
row=5	0.4	0.4
row=6	0.69647	0.42311
row=7	0.28614	0.98076
row=8	0.22685	0.68483
row=9	0.55131	0.48093
row=10	0.71947	0.39212

### 6.2.1.4 ND Dimensional Parameter Arrays, Simulate Model and Stack Output Tables

Now we will first column combine matrixes, model parameters and model outcomes, and then row combine matrixes from different simulations.

A model takes a N parameters, solve the model over M sets of parameters. Each time when the model is solved, a P by Q table of results is generated. Each column is a different statistics (mean, std, etc.), and each row is a different outcome variable (consumption, asset choices, etc.). Stack these P by Q Tables together, and add in information about the N parameters, each of the tables been stacked initially had the same column and row names.

The resulting table should have P times M rows, for M sets of model simulations each with P rows of results. And there should be N + Q columns, storing the N parameters as well as the Q columns of different outcomes.

```
rng(123);
```

```
% Generate A P by Q matrix of random parameter Values
```

```
it_param_groups_m = 5;
```

```

it_params_n = 2;
it_outcomes_p = 3;
it_stats_q = 3;

% Parameter Matrix and Names
ar_param_names = strcat('param_', string(1:it_params_n));
mt_param_m_by_n = round(rand([it_param_groups_m, it_params_n])*5, 2);

% Loop over the parameters
for it_cur_param_group=1:1:it_param_groups_m

    % Current Parameters
    ar_param = mt_param_m_by_n(it_cur_param_group,:);

    % Some Model is simulated
    mt_model_simu = normrnd(mean(ar_param), std(ar_param), [it_outcomes_p, it_stats_q]);

    % Model Results are Saved As Table With Column and Row Information
    tb_model_simu = array2table(mt_model_simu);
    cl_col_names = strcat('stats_', string((1:size(mt_model_simu,2))));
    cl_row_names = strcat('outvar_', string((1:size(mt_model_simu,1))));
    tb_model_simu.Properties.VariableNames = cl_col_names;
    tb_model_simu.Properties.RowNames = cl_row_names;

    % Convert Row Variable Names to a Column String
    outvar = string(tb_model_simu.Properties.RowNames);
    tb_model_simu = addvars(tb_model_simu, outvar, 'Before', 1);

    % Parameter Information Table that Shares Row Names as Simu Results
    mt_param_info = zeros([it_outcomes_p,it_params_n]) + ar_param;
    tb_param_info = array2table(mt_param_info);
    tb_param_info.Properties.VariableNames = ar_param_names;
    tb_param_info.Properties.RowNames = cl_row_names;

    % Combine Parameter Information and Simulation Contents
    tb_model_simu_w_info = [tb_param_info tb_model_simu];
    % Update Row Names based on total row available
    ar_rows_allsimu = (1:it_stats_q)' + (it_cur_param_group-1)*it_stats_q;
    tb_model_simu_w_info.Properties.RowNames = strcat('row=', string(ar_rows_allsimu));

    % Show One Example Table before Stacking
    if (it_cur_param_group == round(it_param_groups_m/2))
        disp(tb_model_simu);
        disp(tb_param_info);
        disp(tb_model_simu_w_info);
    end

    % Stack all results
    if(it_cur_param_group == 1)
        tb_model_allsimu_w_info = tb_model_simu_w_info;
    else
        tb_model_allsimu_w_info = [tb_model_allsimu_w_info; tb_model_simu_w_info];
    end

end

```

outvar	stats_1	stats_2	stats_3
-----	-----	-----	-----



outvar_1	"outvar_1"	0.056853	2.1703	2.1098		
outvar_2	"outvar_2"	3.1545	2.0634	0.7798		
outvar_3	"outvar_3"	-0.49033	2.2566	1.7896		
	param_1	param_2				
	-----	-----				
outvar_1	1.13	3.42				
outvar_2	1.13	3.42				
outvar_3	1.13	3.42				
	param_1	param_2	outvar	stats_1	stats_2	stats_3
	-----	-----	-----	-----	-----	-----
row=7	1.13	3.42	"outvar_1"	0.056853	2.1703	2.1098
row=8	1.13	3.42	"outvar_2"	3.1545	2.0634	0.7798
row=9	1.13	3.42	"outvar_3"	-0.49033	2.2566	1.7896

Show all Simulation Joint Table Outputs:

```
disp(tb_model_allsimu_w_info);
```

	param_1	param_2	outvar	stats_1	stats_2	stats_3
	-----	-----	-----	-----	-----	-----
row=1	3.48	2.12	"outvar_1"	2.2665	1.1885	1.924
row=2	3.48	2.12	"outvar_2"	3.3427	2.4647	2.3548
row=3	3.48	2.12	"outvar_3"	2.6714	3.6132	2.918
row=4	1.43	4.9	"outvar_1"	3.3859	5.3759	1.5816
row=5	1.43	4.9	"outvar_2"	3.9499	3.8698	2.2693
row=6	1.43	4.9	"outvar_3"	5.7745	4.6871	1.7334
row=7	1.13	3.42	"outvar_1"	0.056853	2.1703	2.1098
row=8	1.13	3.42	"outvar_2"	3.1545	2.0634	0.7798
row=9	1.13	3.42	"outvar_3"	-0.49033	2.2566	1.7896
row=10	2.76	2.4	"outvar_1"	2.9611	2.6847	2.4986
row=11	2.76	2.4	"outvar_2"	2.9333	2.3457	3.0629
row=12	2.76	2.4	"outvar_3"	2.5814	2.4372	2.4806
row=13	3.6	1.96	"outvar_1"	2.7199	3.3129	3.0577
row=14	3.6	1.96	"outvar_2"	3.9804	1.4529	2.9285
row=15	3.6	1.96	"outvar_3"	2.8445	4.4117	2.6576



# Appendix A

## Index and Code Links

### A.1 Data Structures links

#### A.1.1 Section 1.1 Matrices and Arrays links

1. [Array Reshape, Repeat and Expand](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Reshape and flatten arrays.
  - **m**: `reshape()`
2. [Array Index Slicing and Subsetting to Replace and Expand](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Index based column and row expansions.
  - Anonymous function to slice array subsets.
  - **m**: `sub2ind() + @(it_subset_n, it_ar_n) unique(round(((0:1:(it_subset_n-1))/(it_subset_n-1)) times (it_ar_n-1)+1))`
3. [3D, 4D, ND Arrays Reshape and Summarize](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Slice 2D matrixes out of ND matrixes. The 2D matrix is contiguous, but can be intermediate dimensions.
  - Summarize a nd dimensional matrix along one or two dimensions group by various other dimensions.
  - **m**: `permute(mn, [3,1,2,4]) + squeeze(num2cell(mn, [1,2])) + celldisp() + ndgrid()`
4. [Array Broadcasting Examples](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - broadcast means: `array + array' + matrix = matrix`.
5. [Grid States, Choices and Optimal Choices Example](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - States, choices, and find max.
6. [Accumarray Examples](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Accumarray to sum up probabilities/values for discrete elements of arrays.
  - **m**: `unique() + reshape() + accumarray()`
7. [Array Random Draws and Permutation](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Draw randomly from array, permute arrays.
  - **m**: `ndgrid() + cell2mat(cellfun(@(m) m(:), cl_mt_all, 'uni', 0))`
8. [Matlab Array Miscellaneous](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Compare approximately similar values.
  - Find imaginary elements of array.
  - **m**: `imag()`

#### A.1.2 Section 1.2 Cells links

1. [List Comprehension with Cells](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Cell2mat, cellfun, anonymous function list comprehension over cells.
  - Find min and max of all arrays in cells.
  - Find length of all arrays in cells; find index of elements of one array in another cell array.
  - **m**: `cell2mat() + cellfun() + strcmp() + find() + cell2mat(cellfun(@(m) find(strcmp(ls_st_param_key, m)), cl_st_param_keys, 'UniformOutput', false))`
2. [Permutate Cells](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)

- Generate all possible combinations of various arrays contained in cell array.
  - **m**: `ndgrid() + cell2mat() + array2table() + cell2mat(cellfun(@(m) m(:), cl_mt_all, 'uni', 0))`
3. **Combine Cells**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
    - Combine string cell arrays and string.
    - **m**: `[{st_param}, ls_st_param_key, cl_st_param_keys]`
  4. **Nested Cells**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
    - Cell of cells with inner cell having multiple types.
    - **m**: `linspace() + cell([4,1]) + cns_parm_tstar{1} = {'fl_crra', 'CRRa', linspace(1, 2, it_simu_vec_len)} + disp(cns_parm_tstar(1)) + disp(cns_parm_tstar{1}{1})`

### A.1.3 Section 1.3 Characters and Strings links

1. **String Basics**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Compose string and rounded numeric array.
  - Cut string suffix and append new suffix.
  - **m**: `*compose() + strjoin() + str_sub = split(string, ".") + strcat(str_sub{1}, '_m.m')*`
2. **String Arrays Operations**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - String arrays and cell strings.
  - Duplicate strings, concatenate string, and paste strings jointly with separator.
  - Find string element positions, replace substrings.
  - **m**: `repmat() + num2str() + strcat() + strjoin() + fprintf() + strcmp() + strrep() + cel2mat(cellfun(@(m) find(strcmp())))`
3. **String and Numeric Array Concatenations**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Generate rounded string array matrix with leading zero, leading space, decimal round from numeric matrix.
  - Create a title string by joining rounded parameter and parameter names.
  - Concatenate multiple numeric arrays together with strings and format.
  - **m**: `compose() + cellstr() + strcat() + strjoin() + %.2f`

### A.1.4 Section 1.4 Map Containers links

1. **Container Map Basics**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Numeric container map, dynamically filled container map.
  - **m**: `isKey() + strjoin() + containers.Map('KeyType', 'char', 'ValueType', 'any')`
2. **Display Container Map Keys, Values and Subsetting**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Loop over map, display keys and values.
  - Select Container map subset by keys.
  - **m**: `strjoin() + keys(map) + values(map) + containers.Map(keys, values)`
3. **Container Map Varied Value Type**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Numeric scalar, string, matrix as values for map container.
  - Get values for multiple keys in map.
  - **m**: `map.keys() + map.values() + values(param_map, {'share_unbanked_j', 'equi_r_j'})`
4. **Cell Override**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Override default map with externally fed map, update existing and add new keys.
  - **m**: `param_map_updated = [param_map_old; param_map_updates_new]`

## A.2 Functions links

### A.2.1 Section 2.1 varargin Default Parameters links

1. **Use varargin as a Function Parameter**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Default parameters allow for maintaining code testability.
  - Use varargin for functions with limited parameters.
  - **m**: `varargin + cell2mat() + function [out_put] = func_name(varargin)`
2. **Use varargin as a Function Parameter**: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - The varargin structure could lead to excessive code lines. Container Map works well with large parameter structure.

- Core model functions with potentially many parameters, possibly override default generation to save time.
- **m**: *varargin* + function [out\_put] = func\_name(varargin) + cm\_defaults = {cm\_a, cm\_b} + [cm\_defaults{1:optional\_params\_len}] = varargin{:} + cm\_c = [cm\_a;cm\_b]

## A.3 Panel links

### A.3.1 Section 3.1 Time Series links

1. Autoregressive Process AR(1): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - The Mean and standard deviation of an AR(1) process.
  - Simulate and graph an AR(1) persistent process.
  - **m**: *normrnd()* + for *it\_t=1:1:length(ar\_shk)* + *plot(ar\_t, ar\_y)*

## A.4 Simulation links

### A.4.1 Section 4.1 Normal Distribution links

1. Compute CDF for Normal and Bivariate Normal Distributions: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - CDF for normal random variable through simulation and with NORMCDF function.
  - CDF for bivariate normal random variables through simulation and with NORMCDF function, using cholesky decomposition to model correlation from uniform random draws.
  - **m**: *mvncdf* + *norminv*
2. Cholesky Decomposition Correlated Two Dimensional Normal Shock: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Draw two correlated normal shocks using the MVNRND function.
  - Draw two correlated normal shocks from uniform random variables using Cholesky Decomposition.
  - **m**: *mvnrnd* + *corrcoef* + *norminv*
3. Cholesky Decomposition Correlated Five Dimensional Normal Shock: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Generate variance-covariance matrix from correlation and standard deviation.
  - Draw five correlated normal shocks using the MVNRND function.
  - Draw five correlated normal shocks from uniform random variables using Cholesky Decomposition.
  - **m**: *mvnrnd* + *corrcoef* + *norminv* + *subplot*

## A.5 Graphs links

### A.5.1 Section 5.1 Figure Components links

1. Image Pick Safe Colors: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Display safe colors.
  - **m**: *blue = [57 106 177]./255 + fill(x, y, cl\_colors{it\_color})*
2. Figure Titling and Legend: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Multi-line titles, add legend lines.
  - Add to legend, select legend to show.
  - **m**: *title({'Cash-on-Hand' 'α + β = ζ'}, 'Interpreter', 'latex') + legend([g1, g2, g3], {'near', 'linear', 'spline'}, 'Location', 'best', 'NumColumns', 1, 'FontSize', 12, 'TextColor', 'black');*
3. Graph Many Lines Legend for Subset: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - State-space plots with color spectrum: can not show all states in legend, show subset, add additional line to plot and legend.
  - **m**: *jet() + numel() + flipr() + jet(numel(chart)), set(chart(m), 'Color', clr(m,:))*

### A.5.2 Section 5.2 Basic Figure Types links

1. Scatter Plot Examples: [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Scatter multiple lines different colors, shapes and sizes.

- **m**: `scatter(x, y, size) + Marker + MarkerEdgeColor + MarkerEdgeAlpha + MarkerFaceColor + MarkerFaceAlpha`
- 2. [Scatter Plot Examples](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Scatter and lines multiple lines different colors, shapes and sizes.
  - X axis, Y axis, and 45 degree line.
  - **m**: `xline(0) + yline(0) + reffline([1 0]) + plot(x,y) + HandleVisibility + Color + LineStyle + LineWidth`
- 3. [Three variables Scatter and Lines with Color Spectrum](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Two dimensional matrix for x and y, a third variable with color spectrum set via loop.
  - **m**: `plot(2d, 2d) + jet + set(chart(m), 'Color', clr)`

### A.5.3 Section 5.3 Write and Read Plots links

1. [Graph Generate EPS Postscript Figures](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - EPS vector graphics, avoid bitmap (jpg, png), use vector graphics.
  - **m**: `figure('Renderer', 'Painters')`

## A.6 Tables links

### A.6.1 Section 6.1 Basic Table Generation links

1. [Named Tables with Random Data](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Convert a random matrix to a table with column and row names defined with arrays.
  - **m**: `array2table() + strcat() + addvars() + matlab.lang.makeValidName()`
2. [Order, Sort and Rename Columns](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Convert a matrix to table with mean and sd columns. Rearrange and rename columns.
  - **m**: `array2table() + rng() + addvars() + movevars() + removevars() + matlab.lang.makeValidName() + tb.Properties.VariableNames + tb.Properties.RowNames`
3. [Array Based Row and Column Names](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Generate a column and row named table. Convert row names to a column as strings. Remove Row Names.
  - **m**: `array2table() + string() + strcat('rowA=', string((1:size(mt, 1)))) + tb_test_a.Properties.VariableNames + tb_test_a.Properties.RowNames + addvars(tb, rownames, 'Before', 1)`
4. [Select Subset of Rows and Columns](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Conditional selection based on cell values and column and row names.
  - **m**: `tb(strcmp(tb.v1, "b"), :) + tb(tb.va==0.4, :)`

### A.6.2 Section 6.2 Table Joining links

1. [Stack Matlab Tables](#): [mlx](#) | [m](#) | [pdf](#) | [html](#)
  - Append columns to existing table. Stack tables vertically and horizontally.
  - Simulate a model, column combine simulation parameters with multi-row simulation results. Then row stack results from multiple simulations together.
  - **m**: `array2table() + [tb_a tb_b] + [tb_a; tb_b] + tb.Properties.VariableNames + tb.Properties.RowNames`

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