

3D, 4D, ND Arrays Reshape and Rearrange Dimensions

back to [Fan's Intro Math for Econ](#), [Matlab Examples](#), or [MEconTools Repositories](#)

3D Array to Cell Array of Matrix Split by Last Dimension

Convert Multi-dimensional arrays to a cell array consistent of two dimensional arrays. In this example, we split by the 3rd dimension, so the number of output matrixes is equal to the length of the 3rd dimension.

First create a three dimensional array, two matrixes that are 4 by 3 each:

```
% Create a 3D Array
rng(123);
mn_rand = rand(4,3,2);
disp(mn_rand);
```

(:,:,1) =

0.6965	0.7195	0.4809
0.2861	0.4231	0.3921
0.2269	0.9808	0.3432
0.5513	0.6848	0.7290

(:,:,2) =

0.4386	0.1825	0.6344
0.0597	0.1755	0.8494
0.3980	0.5316	0.7245
0.7380	0.5318	0.6110

Now convert the 3 dimensional array to a 2 by 1 cell array that contains matrixes in each cell:

```
% Squeeze 3D array to a Cell array of matrixes
cl_mn_rand = squeeze(num2cell(mn_rand, [1,2]));
celldisp(cl_mn_rand);
```

cl_mn_rand{1} =

0.6965	0.7195	0.4809
0.2861	0.4231	0.3921
0.2269	0.9808	0.3432
0.5513	0.6848	0.7290

cl_mn_rand{2} =

0.4386	0.1825	0.6344
0.0597	0.1755	0.8494
0.3980	0.5316	0.7245
0.7380	0.5318	0.6110

4D Array to Cell Array of Matrix Split by Last Two Dimensions

Convert 4D Multi-dimensional arrays to a cell array consistent of two dimensional arrays. In this example, the first two dimensions determine the resulting matrix size, the 3rd and the 4th dimensions are categorical.

First create a four dimensional array, four matrixes stored each matrix is 2 by 2:

```
% Create a 3D Array
```

```
rng(123);  
mn_rand = rand(2,2,2,2);  
disp(mn_rand);
```

```
(:,:,1,1) =
```

```
    0.6965    0.2269  
    0.2861    0.5513
```

```
(:,:,2,1) =
```

```
    0.7195    0.9808  
    0.4231    0.6848
```

```
(:,:,1,2) =
```

```
    0.4809    0.3432  
    0.3921    0.7290
```

```
(:,:,2,2) =
```

```
    0.4386    0.3980  
    0.0597    0.7380
```

Now convert the 4 dimensional array to a 2 by 2 cell array that contains matrixes in each cell:

```
% Squeeze 3D array to a Cell array of matrixes
```

```
cl_mn_rand = squeeze(num2cell(mn_rand, [1,2]));  
celldisp(cl_mn_rand);
```

```
cl_mn_rand{1,1} =
```

```
    0.6965    0.2269  
    0.2861    0.5513
```

```
cl_mn_rand{2,1} =
```

```
    0.7195    0.9808  
    0.4231    0.6848
```

```
cl_mn_rand{1,2} =
```

```
    0.4809    0.3432  
    0.3921    0.7290
```

```

c1_mn_rand{2,2} =

    0.4386    0.3980
    0.0597    0.7380

```

4D Array to Cell Array of Matrix Split by First and Fourth Dimensions Rearrange Dimensions

Suppose we store policy and value function given four state variables. The first one is age, the second one is asset, the third one is shock, and the fourth one is the number of kids. We start out with a four dimensional matrix. The objective is to create a two dimensional cell array as output where indexed by the 1st and 4th dimension of the underlying numeric array, and the elements of the 2D cell array are matrixes.

This is achieved by the [permute](#) function. We first rearrange the matrix, so that the 2nd and 3rd dimensions become the 1st and 2nd, then we use the technique used above to squeeze out the first two dimensions as matrixes with the last two as categories.

First, generate the 2 by 2 by 2 by 2, (Age, A, Z, Kids Count), matrix:

```

% Create a 3D Array
rng(123);
% (Age, A, Z, Kids Count)
mn_rand = rand(2,2,2,2);

```

Second, loop out the (A,Z) matrix by Age and Kids Count, this shows us what we want to achieve. Note that each row is Age, each column is A, each submatrix is z, and each super-matrix is kid-count. So from slicing, each column printed out are different value of A, the two submatrixes printed out are for each z. For the output structure where we want a (A,Z) matrix, the columns need to become rows, and the submatrix need to become columns.

```

% Show Matrix by Age and Kids
for it_age = 1:size(mn_rand,1)
    for it_kids = 1:size(mn_rand,4)
        disp(strcat(['it_age:' num2str(it_age) ', it_kids:' num2str(it_kids)]))
        disp(mn_rand(it_age,:,: ,it_kids));
    end
end

```

```

it_age:1, it_kids:1
(:, :, 1) =

    0.6965    0.2269

it_age:1, it_kids:2
(:, :, 1) =

    0.7195    0.9808
    0.4809    0.3432

```

```
(:,:,2) =  
    0.4386    0.3980  
it_age:2, it_kids:1  
(:,:,1) =  
    0.2861    0.5513
```

```
(:,:,2) =  
    0.4231    0.6848  
it_age:2, it_kids:2  
(:,:,1) =  
    0.3921    0.7290
```

```
(:,:,2) =  
    0.0597    0.7380
```

Third, we permute the matrix and squeeze to arrive at the 2 by 2 cell, note that step two is just to show via loop what we should get:

```
% Rearrange dimensions  
mn_rand_2314 = permute(mn_rand, [2,3,1,4]);  
% Squeeze the first two dimensions as before  
cl_mn_rand = squeeze(num2cell(mn_rand_2314, [1,2]));  
% show  
celldisp(cl_mn_rand);
```

```
cl_mn_rand{1,1} =  
    0.6965    0.7195  
    0.2269    0.9808
```

```
cl_mn_rand{2,1} =  
    0.2861    0.4231  
    0.5513    0.6848
```

```
cl_mn_rand{1,2} =  
    0.4809    0.4386  
    0.3432    0.3980
```

```
cl_mn_rand{2,2} =  
    0.3921    0.0597  
    0.7290    0.7380
```

ND Array Summarize in Table

Given an ND dataframe, summarize the first two dimensions. For each possible combination of the 3rd and 4th dimension, generate mean, sd, min and max over the matrix of the first two dimensions. This is similar to a tabulation function.

First, we generate several array of information:

```
% Initialize and Squeeze
rng(123);
mn_rand = rand(2,2,2,2);
cln_mt_rand = squeeze(num2cell(mn_rand, [1,2]));
cl_mt_rand = cln_mt_rand(:);
celldisp(cl_mt_rand);
```

```
cl_mt_rand{1} =

    0.6965    0.2269
    0.2861    0.5513
```

```
cl_mt_rand{2} =

    0.7195    0.9808
    0.4231    0.6848
```

```
cl_mt_rand{3} =

    0.4809    0.3432
    0.3921    0.7290
```

```
cl_mt_rand{4} =

    0.4386    0.3980
    0.0597    0.7380
```

Second, create two arrays that tracks for each element of cl_mt_rand, which one of the 3rd and 4th dimensions they correspond to:

```
ar_dim_3 = [31,32]';
ar_dim_4 = [41,42]';
[mt_dim_3, mt_dim_4] = ndgrid(ar_dim_3, ar_dim_4);
ar_dim_3 = mt_dim_3(:);
ar_dim_4 = mt_dim_4(:);
```

Third, summarize each matrix:

```
% Over of matrix and summarize
ar_mean = zeros(size(cl_mt_rand));
ar_std = zeros(size(cl_mt_rand));
```

```

for it_mt=1:length(cl_mt_rand)
    mt_cur = cl_mt_rand{it_mt};
    ar_mean(it_mt) = mean(mt_cur, 'all');
    ar_std(it_mt) = std(mt_cur, [], 'all');
end

```

Fourth Construct a Table

```

% Constructe Table
tb_rowcols_tab = array2table([(1:length(cl_mt_rand))', ...
    ar_dim_3, ar_dim_4, ar_mean, ar_std]);
tb_rowcols_tab.Properties.VariableNames = ...
    matlab.lang.makeValidName(["i", "dim3", "dim4", "mean", "std"]);
disp(tb_rowcols_tab);

```

i	dim3	dim4	mean	std
1	31	41	0.44019	0.22156
2	32	41	0.70204	0.2281
3	31	42	0.48632	0.17157
4	32	42	0.40857	0.27764

ND Array Two-Way Summarize in Table

Given dataframe as above, but we now want to add to the resulting summary table additional columns, rather than taking the means of the entire matrix in the first two dimensions, we only take average with respect to the rows, the first dimension, the second dimension show up as column statistics names, still multiple stats. The results worked out here are embedded in the `fx_summ_nd_array` function of the [MEconTools](#) Package.

First, we generate several array of information:

```

% dimension names
st_title = 'Summarize values over a conditional on z (columns) and kids and marriage (rows)';
st_dim_1 = 'a';
st_dim_2 = 'z';
st_dim_3 = 'kid';
st_dim_4 = 'marriage';
% 3rd and fourth dimension values
ar_dim_2 = [-3, -1, 1, 3];
ar_dim_3 = [1,2,3];
ar_dim_4 = [0,1];
% Initialize and Squeeze
rng(123);
mn_rand = rand(10,4,3,2);
cln_mt_rand = squeeze(num2cell(mn_rand, [1,2]));
cl_mt_rand = cln_mt_rand(:);

```

Second, create two arrays that tracks for each element of `cl_mt_rand`, which one of the 3rd and 4th dimensions they correspond to:

```

[mt_dim_3, mt_dim_4] = ndgrid(ar_dim_3', ar_dim_4');
ar_dim_3 = mt_dim_3(:);
ar_dim_4 = mt_dim_4(:);

```

Third, summarize each matrix:

```
% Over of matrix and summarize
mt_mean = zeros(length(cl_mt_rand), size(mn_rand,2));
mt_std = zeros(length(cl_mt_rand), size(mn_rand,2));
for it_mt=1:length(cl_mt_rand)
    mt_cur = cl_mt_rand{it_mt};
    mt_mean(it_mt,:) = mean(mt_cur, 1);
    mt_std(it_mt,:) = std(mt_cur, [], 1);
end
```

Fourth Construct a Table

```
% Constructe Table
tb_rowcols_tab = array2table([(1:length(cl_mt_rand))', ...
    ar_dim_3, ar_dim_4, mt_mean, mt_std]);
% Column Names
cl_col_names_cate_dims = [string(st_dim_3), string(st_dim_4)];
cl_col_names_mn = strcat('mean_', st_dim_2, string(ar_dim_2));
cl_col_names_sd = strcat('sd_', st_dim_2, string(ar_dim_2));
tb_rowcols_tab.Properties.VariableNames = ...
    matlab.lang.makeValidName(["group", cl_col_names_cate_dims, cl_col_names_mn, cl_col_names_sd]);
% disp(['xxx ' st_title ' xxxxxxxxxxxxxxxxxxxxxxxxxxxxxxxx']);
disp(tb_rowcols_tab);
```

group	kid	marriage	mean_z_3	mean_z_1	mean_z1	mean_z3	sd_z_3	sd_z_1	sd_z1	sd_z
1	1	0	0.5442	0.41278	0.53795	0.49542	0.22935	0.22945	0.21653	0.252
2	2	0	0.51894	0.52262	0.52544	0.45066	0.26787	0.23615	0.25833	0.311
3	3	0	0.48248	0.5238	0.50392	0.46534	0.27009	0.26676	0.26644	0.294
4	1	1	0.58343	0.50529	0.54361	0.5006	0.29578	0.30182	0.30952	0.273
5	2	1	0.58408	0.45941	0.50466	0.40081	0.25026	0.34704	0.31039	0.286
6	3	1	0.51148	0.49531	0.48963	0.47698	0.3271	0.24336	0.34498	0.340