

# 1 hornerErrorBound

According to [1], p.95, the error bound for evaluating a polynomial using Horner's Algorithm is:

$$|p(x) - \hat{r}_0(x)| \leq \gamma_{2n} \sum_{i=0}^n |a_i| |x|^i \equiv \gamma_{2n} \tilde{p}(|x|)$$

where  $p(x)$  is the exact evaluation at  $x$  and  $\hat{r}_0(x)$  is the result using Horner's Algorithm.

A running error bound, which is tighter, can be calculated via a slight modification:

[1] - N. J. Higham. Accuracy and Stability of Numerical Algorithms. SIAM, second edition, 2002.