
MATHEMATICS

9709/62

Paper 6 Probability & Statistics 1 (S1)

May/June 2016

1 hour 15 minutes

Additional Materials: List of Formulae (MF9)

READ THESE INSTRUCTIONS FIRST

An answer booklet and a graph paper booklet are provided inside this question paper. You should follow the instructions on the front cover of both booklets. If you need additional answer paper or graph paper ask the invigilator for a continuation booklet or graph paper booklet.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 50.

This document consists of **3** printed pages, **1** blank page and **2** inserts.

- 1 Ayman's breakfast drink is tea, coffee or hot chocolate with probabilities 0.65, 0.28, 0.07 respectively. When he drinks tea, the probability that he has milk in it is 0.8. When he drinks coffee, the probability that he has milk in it is 0.5. When he drinks hot chocolate he always has milk in it.

(i) Draw a fully labelled tree diagram to represent this information. [2]

(ii) Find the probability that Ayman's breakfast drink is coffee, given that his drink has milk in it. [3]

- 2 When visiting the dentist the probability of waiting less than 5 minutes is 0.16, and the probability of waiting less than 10 minutes is 0.88.

(i) Find the probability of waiting between 5 and 10 minutes. [1]

A random sample of 180 people who visit the dentist is chosen.

(ii) Use a suitable approximation to find the probability that more than 115 of these people wait between 5 and 10 minutes. [5]

- 3 A particular type of bird lays 1, 2, 3 or 4 eggs in a nest each year. The probability of x eggs is equal to kx , where k is a constant.

(i) Draw up a probability distribution table, in terms of k , for the number of eggs laid in a year and find the value of k . [3]

(ii) Find the mean and variance of the number of eggs laid in a year by this type of bird. [3]

- 4 When people visit a certain large shop, on average 34% of them do not buy anything, 53% spend less than \$50 and 13% spend at least \$50.

(i) 15 people visiting the shop are chosen at random. Calculate the probability that at least 14 of them buy something. [3]

(ii) n people visiting the shop are chosen at random. The probability that none of them spends at least \$50 is less than 0.04. Find the smallest possible value of n . [3]

- 5 The following are the maximum daily wind speeds in kilometres per hour for the first two weeks in April for two towns, Bronlea and Rogate.

Bronlea	21	45	6	33	27	3	32	14	28	24	13	17	25	22
Rogate	7	5	4	15	23	7	11	13	26	18	23	16	10	34

(i) Draw a back-to-back stem-and-leaf diagram to represent this information. [5]

(ii) Write down the median of the maximum wind speeds for Bronlea and find the interquartile range for Rogate. [3]

(iii) Use your diagram to make one comparison between the maximum wind speeds in the two towns. [1]

- 6** The time in minutes taken by Peter to walk to the shop and buy a newspaper is normally distributed with mean 9.5 and standard deviation 1.3.
- (i) Find the probability that on a randomly chosen day Peter takes longer than 10.2 minutes. [3]
 - (ii) On 90% of days he takes longer than t minutes. Find the value of t . [3]
 - (iii) Calculate an estimate of the number of days in a year (365 days) on which Peter takes less than 8.8 minutes to walk to the shop and buy a newspaper. [3]
- 7** (a) Find the number of different arrangements which can be made of all 10 letters of the word WALLFLOWER if
- (i) there are no restrictions, [1]
 - (ii) there are exactly six letters between the two Ws. [4]
- (b) A team of 6 people is to be chosen from 5 swimmers, 7 athletes and 4 cyclists. There must be at least 1 from each activity and there must be more athletes than cyclists. Find the number of different ways in which the team can be chosen. [4]

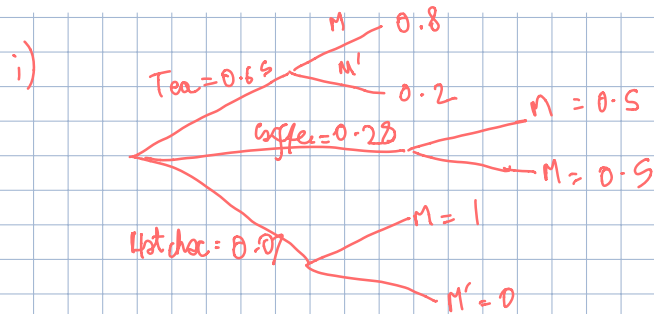
- 1 Ayman's breakfast drink is tea, coffee or hot chocolate with probabilities 0.65, 0.28, 0.07 respectively. When he drinks tea, the probability that he has milk in it is 0.8. When he drinks coffee, the probability that he has milk in it is 0.5. When he drinks hot chocolate he always has milk in it.

(i) Draw a fully labelled tree diagram to represent this information.

[2]

(ii) Find the probability that Ayman's breakfast drink is coffee, given that his drink has milk in it.

[3]



ii) $P(\text{coffee} | \text{milk}) = \frac{0.28 \times 0.5}{(0.65 \times 0.8) + (0.28 \times 0.5) + (0.07 \times 1)} = \frac{14}{73} = 0.1917$

- 2 When visiting the dentist the probability of waiting less than 5 minutes is 0.16, and the probability of waiting less than 10 minutes is 0.88.

(i) Find the probability of waiting between 5 and 10 minutes.

[1]

A random sample of 180 people who visit the dentist is chosen.

(ii) Use a suitable approximation to find the probability that more than 115 of these people wait between 5 and 10 minutes.

[5]

i) 0.72

ii) $X \sim B(180, 0.72)$
 $X \sim N(129.6, 36.288)$



$$\phi\left(\frac{143.7 - 129.6}{\sqrt{36.288}}\right) = \phi(2.340656) = 0.9909 \approx 0.991$$

- 3 A particular type of bird lays 1, 2, 3 or 4 eggs in a nest each year. The probability of x eggs is equal to kx , where k is a constant.

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i)

x	1	2	3	4
$P(X=x)$	k	$2k$	$3k$	$4k$

$$10k = 1$$

$$k = \frac{1}{10} \checkmark$$

ii)

$$\frac{1}{10} + \frac{2}{10} + \frac{9}{10} + \frac{16}{10} = 3 = \mu$$

$$\sum x^2 p = \frac{1}{10} + \frac{8}{10} + \frac{27}{10} + \frac{64}{10} = 10 \checkmark$$

$$10 - 9 = 1 = \text{variance}$$

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i)

$$X \sim B(15, 0.66)$$

$$P(X \geq 14) = P(15, 14)$$

$$= {}^{15}C_{13} \times 0.66^{13} \times 1 = 0.00196407$$

$${}^{15}C_{14} \times 0.66^{14} \times 0.34 = 0.0151769$$

ii)

$${}^nC_0 \times 0.04^n \times 0.96^{n-0} < 0.04 = \underline{0.04}$$

$$n \ln 0.96 < \ln 0.04$$

$$n > \frac{\ln 0.04}{\ln 0.96}$$

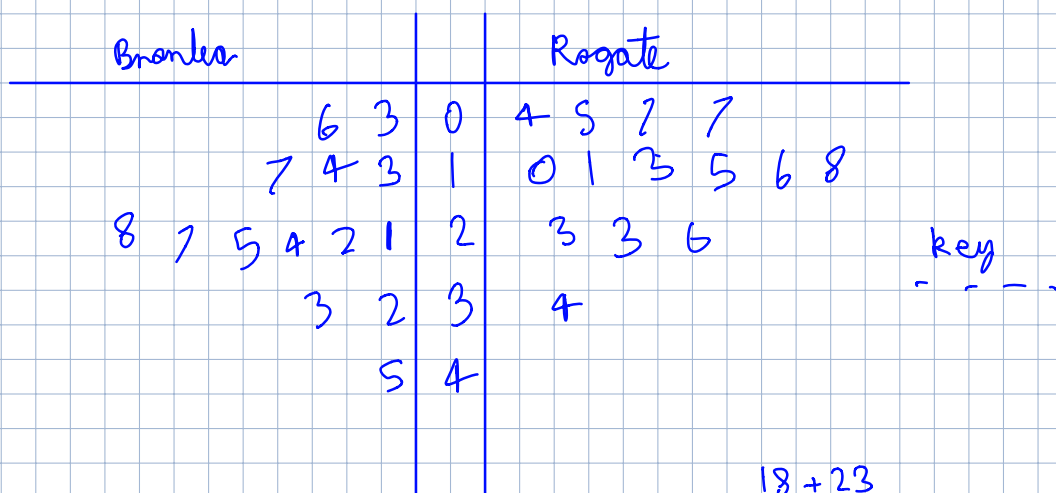
$$n = 24$$

- 5 The following are the maximum daily wind speeds in kilometres per hour for the first two weeks in April for two towns, Bronlea and Rogate.

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- (i) Draw a back-to-back stem-and-leaf diagram to represent this information. [5]
- (ii) Write down the median of the maximum wind speeds for Bronlea and find the interquartile range for Rogate. [3]
- (iii) Use your diagram to make one comparison between the maximum wind speeds in the two towns. [1]

i)



ii) median for Bronlea = 23

UQ for Rogate = 23

LQ " " = 7

IQR = 16

$$\frac{18 + 23}{2}$$

iii) ~~Bronlea has wider range of max wind speeds~~

11

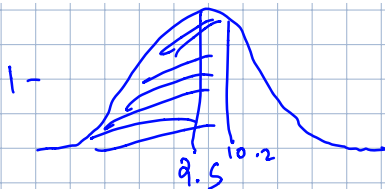
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(i) Find the probability that on a randomly chosen day Peter takes longer than 10.2 minutes. [3]

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(iii) Calculate an estimate of the number of days in a year (365 days) on which Peter takes less than 8.8 minutes to walk to the shop and buy a newspaper. [3]

i)

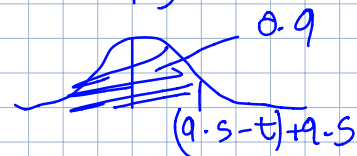
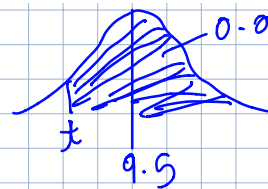


$$X \sim N(9.5, 1.3^2)$$

$$\Phi\left(\frac{0.7}{1.3}\right) = \Phi(0.53846)$$

$$1 - 0.7046 = 0.295$$

ii)



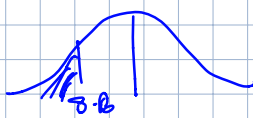
$$\Phi\left(\frac{9.5 - t}{1.3}\right) = 0.9$$

$$\frac{9.5 - t}{1.3} = 1.2815$$

$$t = 7.83405$$

$$= \underline{\underline{7.83}}$$

iii)



$$0.295 \times 365 = 107.821$$

$$= \underline{\underline{108 \text{ days}}}$$

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(i) there are no restrictions, [1]

(ii) there are exactly six letters between the two Ws. [4]

- (b) A team of 6 people is to be chosen from 5 swimmers, 7 athletes and 4 cyclists. There must be at least 1 from each activity and there must be more athletes than cyclists. Find the number of different ways in which the team can be chosen. [4]

a i) $\frac{10!}{3! \times 2!} = 302400$ ✓ W/W ALLFLOWER

ii) W _ _ _ _ W _ _ _ or _ W _ _ _ W _
 $3 \times \frac{8!}{3!} = 20160$ or _ _ W _ _ _ W

b) #1

S	A	C			
S	A	C	A	A	A
S	A	C	A	A	C
S	A	C	S	A	A
S	A	C	S	S	A

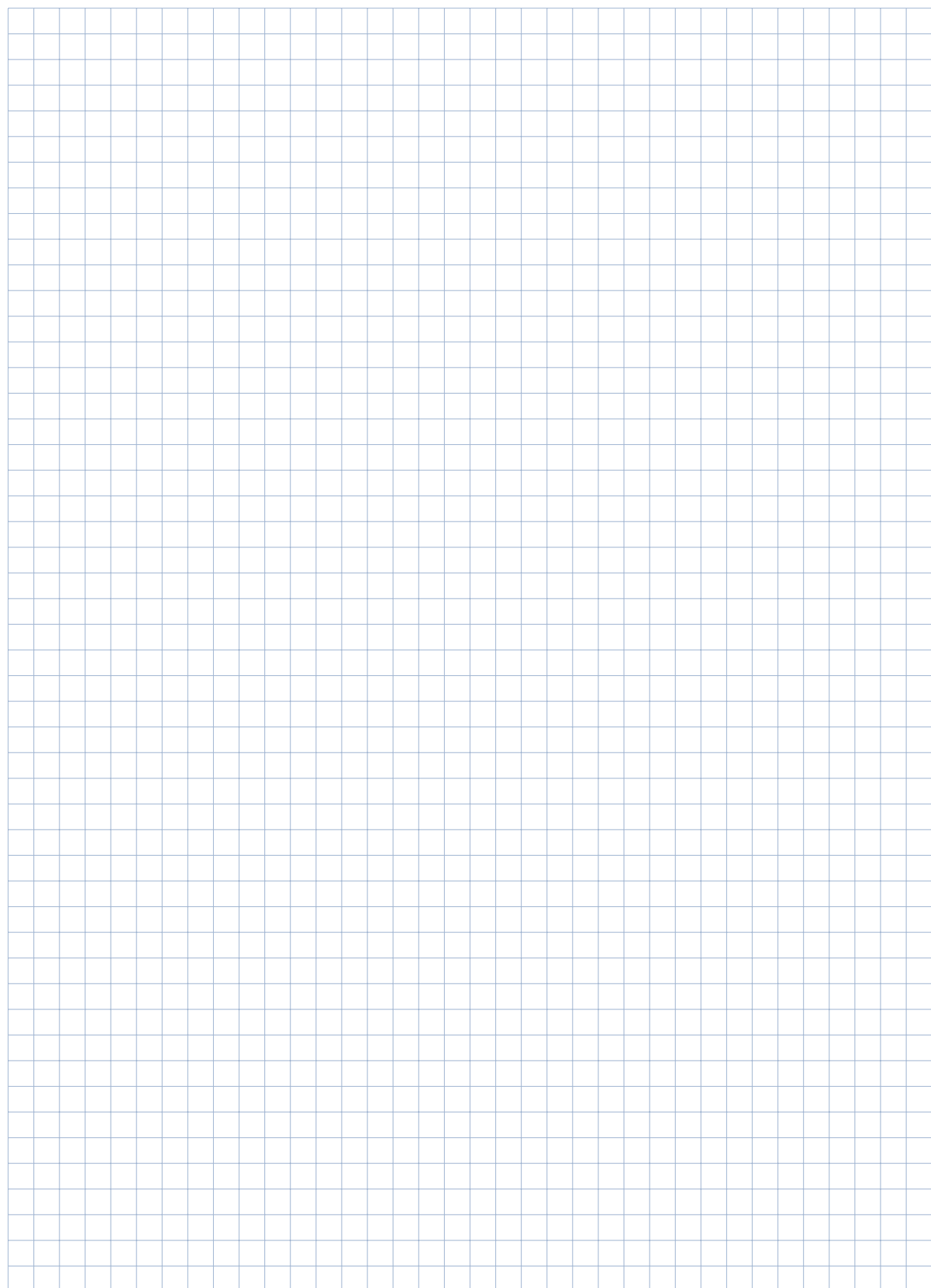
${}^7C_4 \times {}^4C_1 \times {}^9C_1 = 200$

${}^7C_3 \times {}^4C_2 \times {}^5C_1 = 1050$

${}^7C_3 \times {}^4C_1 \times {}^5C_2 = 1400$

${}^7C_2 \times {}^4C_1 \times {}^5C_3 = 840$

3090



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