

# The rminer package for regression

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## Abstract

The aim of this work is to have an insight into the *rminer* package for regression analysis. Starting from a brief theoretical introduction, towards the description of the main functions of the package, and concluding with a simple case study to show how the package can be used.

## Introduction

### Regression

Regression is the problem of learning a *functional relationship* between variables using a dataset where the specific functional form learned depends on the choice of the model (it can be linear or not). The parameters of the function are learned using the *explanatory variables (features)* into the training set, and then performance are evaluated testing the model on the test set. The aim of a regression model — as opposed to a classification model — is to perform a *numeric prediction* based on the features in input.

### Linear Regression

### Random Forest

## The rminer package

The goal of this package is to facilitate the use of data mining algorithms for classification and regression. It offers a short and coherent set of functions in order to easily develop a project, letting the user to follow in particular three CRISP-DM stages: *data preparation*, *modeling* and *evaluation*.

The package can be installed and loaded with:

```
install.packages("rminer")
```

And loaded with:

```
library(rminer)
```

As usual, a complete list of all functions available can be found in the documentation of the package:

```
help(package=rminer)
```

For the purpose of this work instead of reporting what can be found easily — and with more details — inside the documentation, I preferred to report a brief list of the function organized by their purpose, in order to quickly move through the practical example that is more useful to show the package capabilities.

## Data Preparation

First of all, for the data preparation phase, after having loaded the dataset, the functions that can be used are mainly:

- `delevels(x, levels, label = NULL)` – reduce or replace factor *x* with *levels*, with an optional new label;
- `imputation(imethod = "value", D, Attribute = NULL, Missing = NA, Value = 1)` – perform imputation to remove missing values from dataset *D* and from a specific attribute, with the value specified.
- `CaseSeries` – create a data.frame from a time series (vector) using a sliding window. This function is not used in this work and its behavior can be further analyzed in official documentation.

## Modeling

When the dataset is ready is possible to proceed with the model definition. For this phase three functions are important:

- `holdout(y, ratio = 2/3, mode = "stratified", ...)` – it computes indexes for holdout data split into training and test sets. Here are reported principal parameters:
  - *ratio* represent the split ratio and if it's a percentage it's used to define the training, if in number it represents the test set number of examples
  - the *mode* is important if one want to have an advanced control on how the splitting is performed
  - other parameters can be found in the documentation
- `fit(x, data = NULL, model = "default", task = "default", ...)` – it fits a supervised data mining model. Principal parameters are:
  - *x* is the formula of the model to fit, from the dataset *data*
  - *model* is the model to be used, there is a great variety of them
  - *task* is to select regression or classification for models that admit both
  - again, more parameters are available in the documentation
- `crossvaldata(x, data, theta.fit, theta.predict, ngroup = 10, model, task, ...)` – compute k-fold cross-validation for models. Main parameters are similar to *fit* function, and there are also:
  - *theta.fit* and *theta.predict* are the rminer function to be used respectively for fitting and prediction
  - *ngroup* represent the number of folds
  - again, more parameters are available in the documentation

## Evaluation

After having fitted the model one can proceed with the evaluation in order to understand the goodness of the model and eventually fix it. Main functions here are:

- `mmetric(y, metric, ...)` – used to get the metrics specified in the parameter *metric* about the model *y*
- `mgraph(y, graph, ...)` – used to print graphs about model accuracy: “RSC” and “REC” are common options for regression
- `mining(x, data = NULL, Runs = 1, method = NULL, model = "default", task = "default", ...)` – it's a powerful function that trains and tests a particular fit model under several *runs* and a given validation *method*

## Case Study: Life Expectancy

In this section it will be given a tour through the main functionalities of rminer by mean of a real life case study.

## The dataset

The dataset is about Life Expectancy and can be found in Kaggle (“Life Expectancy (Who),” n.d.). This dataset is available thanks to the World Health Organization who keeps track of the health status for all countries. It contains data about 193 countries from the year 2000 to 2015. All data column have a pretty self-explanatory name. For more details one can have a look into the official website from which the dataset has been taken.

For the purpose of this work a quick idea about the data can be achieved with the summary function in R, after loading it.

```
lifeexp.df = read.csv("Life Expectancy Data.csv")
str(lifeexp.df)
summary(lifeexp.df) # here we can see NAs
```

```
## 'data.frame': 2938 obs. of 22 variables:
## $ Country : Factor w/ 193 levels "Afghanistan",...: 1 1 1 1 1 ..
## $ Year : int 2015 2014 2013 2012 2011 2010 2009 2008 2007..
## $ Status : Factor w/ 2 levels "Developed","Developing": 2 2 ..
## $ Life.expectancy : num 65 59.9 59.9 59.5 59.2 58.8 58.6 58.1 57.5 5..
## $ Adult.Mortality : int 263 271 268 272 275 279 281 287 295 295 ...
## $ infant.deaths : int 62 64 66 69 71 74 77 80 82 84 ...
## $ Alcohol : num 0.01 0.01 0.01 0.01 0.01 0.01 0.01 0.01 0.03 0.02..
## $ percentage.expenditure : num 71.3 73.5 73.2 78.2 7.1 ...
## $ Hepatitis.B : int 65 62 64 67 68 66 63 64 63 64 ...
## $ Measles : int 1154 492 430 2787 3013 1989 2861 1599 1141 1..
## $ BMI : num 19.1 18.6 18.1 17.6 17.2 16.7 16.2 15.7 15.2..
## $ under.five.deaths : int 83 86 89 93 97 102 106 110 113 116 ...
## $ Polio : int 6 58 62 67 68 66 63 64 63 58 ...
## $ Total.expenditure : num 8.16 8.18 8.13 8.52 7.87 9.2 9.42 8.33 6.73 ..
## $ Diphtheria : int 65 62 64 67 68 66 63 64 63 58 ...
## $ HIV.AIDS : num 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 ...
## $ GDP : num 584.3 612.7 631.7 670 63.5 ...
## $ Population : num 33736494 327582 31731688 3696958 2978599 ...
## $ thinness..1.19.years : num 17.2 17.5 17.7 17.9 18.2 18.4 18.6 18.8 19 1..
## $ thinness.5.9.years : num 17.3 17.5 17.7 18 18.2 18.4 18.7 18.9 19.1 1..
## $ Income.composition.of.resources : num 0.479 0.476 0.47 0.463 0.454 0.448 0.434 0.4..
## $ Schooling : num 10.1 10 9.9 9.8 9.5 9.2 8.9 8.7 8.4 8.1 ...

## Country Year Status
## Afghanistan : 16 Min. :2000 Developed : 512
## Albania : 16 1st Qu.:2004 Developing:2426
## Algeria : 16 Median :2008
## Angola : 16 Mean :2008
## Antigua and Barbuda: 16 3rd Qu.:2012
## Argentina : 16 Max. :2015
## (Other) :2842
## Life.expectancy Adult.Mortality infant.deaths Alcohol
## Min. :36.30 Min. : 1.0 Min. : 0.0 Min. : 0.0100
## 1st Qu.:63.10 1st Qu.: 74.0 1st Qu.: 0.0 1st Qu.: 0.8775
## Median :72.10 Median :144.0 Median : 3.0 Median : 3.7550
## Mean :69.22 Mean :164.8 Mean : 30.3 Mean : 4.6029
## 3rd Qu.:75.70 3rd Qu.:228.0 3rd Qu.: 22.0 3rd Qu.: 7.7025
## Max. :89.00 Max. :723.0 Max. :1800.0 Max. :17.8700
## NA's :10 NA's :10 NA's :194
## percentage.expenditure Hepatitis.B Measles BMI
```

```
## Min. : 0.000 Min. : 1.00 Min. : 0.0 Min. : 1.00
## 1st Qu.: 4.685 1st Qu.:77.00 1st Qu.: 0.0 1st Qu.:19.30
## Median : 64.913 Median :92.00 Median : 17.0 Median :43.50
## Mean : 738.251 Mean :80.94 Mean : 2419.6 Mean :38.32
## 3rd Qu.: 441.534 3rd Qu.:97.00 3rd Qu.: 360.2 3rd Qu.:56.20
## Max. :19479.912 Max. :99.00 Max. :212183.0 Max. :87.30
## NA's :553 NA's :34
## under.five.deaths Polio Total.expenditure Diphtheria
## Min. : 0.00 Min. : 3.00 Min. : 0.370 Min. : 2.00
## 1st Qu.: 0.00 1st Qu.:78.00 1st Qu.: 4.260 1st Qu.:78.00
## Median : 4.00 Median :93.00 Median : 5.755 Median :93.00
## Mean : 42.04 Mean :82.55 Mean : 5.938 Mean :82.32
## 3rd Qu.: 28.00 3rd Qu.:97.00 3rd Qu.: 7.492 3rd Qu.:97.00
## Max. :2500.00 Max. :99.00 Max. :17.600 Max. :99.00
## NA's :19 NA's :226 NA's :19
## HIV.AIDS GDP Population
## Min. : 0.100 Min. : 1.68 Min. :3.400e+01
## 1st Qu.: 0.100 1st Qu.: 463.94 1st Qu.:1.958e+05
## Median : 0.100 Median : 1766.95 Median :1.387e+06
## Mean : 1.742 Mean : 7483.16 Mean :1.275e+07
## 3rd Qu.: 0.800 3rd Qu.: 5910.81 3rd Qu.:7.420e+06
## Max. :50.600 Max. :119172.74 Max. :1.294e+09
## NA's :448 NA's :652
## thinness..1.19.years thinness.5.9.years Income.composition.of.resources
## Min. : 0.10 Min. : 0.10 Min. :0.0000
## 1st Qu.: 1.60 1st Qu.: 1.50 1st Qu.:0.4930
## Median : 3.30 Median : 3.30 Median :0.6770
## Mean : 4.84 Mean : 4.87 Mean :0.6276
## 3rd Qu.: 7.20 3rd Qu.: 7.20 3rd Qu.:0.7790
## Max. :27.70 Max. :28.60 Max. :0.9480
## NA's :34 NA's :34 NA's :167
## Schooling
## Min. : 0.00
## 1st Qu.:10.10
## Median :12.30
## Mean :11.99
## 3rd Qu.:14.30
## Max. :20.70
## NA's :163
```

From here can be seen that there are 22 columns and that some of them have missing values that will need to be taken care of. The purpose is to use the *Life expectancy* variable as dependent, and all the others as predictors.

An important note here about the package is that since the country variable is stores as a factor, using this dataset I've find out that rminer can't handle factors with more than 53 levels, so I transformed the country factor as a numerical.

```
lifeexp.df$Country = as.numeric(lifeexp.df$Country)
```

## Imputation

Here I manage the missing value taking advantage of the `imputation()` function of the package.

```
## IMPUTATION
# save column with missing values indexes
nacol = NULL
for (i in 1:ncol(lifeexp.df)) {
  if ( any(is.na(lifeexp.df[,i])) ) {
    nacol = c(nacol,i)
  }
}

# 1st method: case deletion
lifeexp.na.del = na.omit(lifeexp.df)

# 2nd method: imputation by mode
lifeexp.imp.mode = lifeexp.df
for (i in nacol) {
  lifeexp.imp.mode = imputation("value", lifeexp.imp.mode, i,
                                Value=which.max(table(na.omit(lifeexp.df[,i]))))
}

# 3rd mode: imputation by hotdeck
lifeexp.imp.hotdeck = lifeexp.df
for (i in nacol) {
  lifeexp.imp.hotdeck = imputation("hotdeck", lifeexp.imp.hotdeck, i)
}
```

The first part is for convenience: I extract the column indexes that correspond to variables in which there are missing values. Then, just to check out for different methods, I tried to trivially remove missing values, and then I used the imputation function: firstly substituting NAs with the mode, and secondly then with the hotdeck method implemented inside the rminer package.

After this manipulation it's possible to check the summary of the dataframe again to check the results (for example about the hotdeck method):

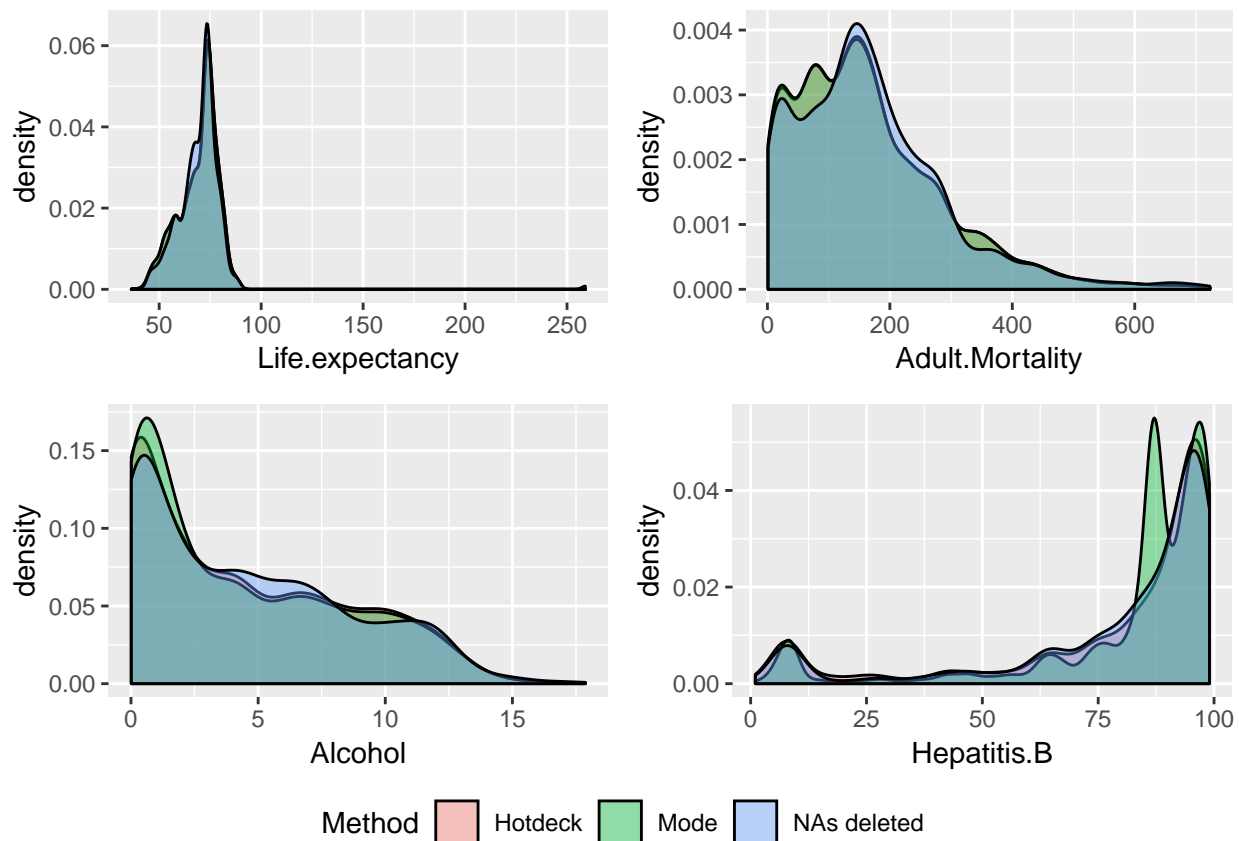
```
summary(lifeexp.imp.hotdeck)
```

```
##      Country      Year      Status      Life.expectancy
## Min.   : 1.0   Min.   :2000   Developed : 512   Min.    :36.30
## 1st Qu.: 47.0   1st Qu.:2004   Developing:2426   1st Qu.:63.20
## Median : 94.0   Median :2008                      Median :72.10
## Mean   : 96.1   Mean   :2008                      Mean   :69.24
## 3rd Qu.:146.0   3rd Qu.:2012                      3rd Qu.:75.67
## Max.   :193.0   Max.   :2015                      Max.   :89.00
## Adult.Mortality infant.deaths      Alcohol      percentage.expenditure
## Min.   : 1.0   Min.   : 0.0   Min.   : 0.0100   Min.    : 0.000
## 1st Qu.: 74.0   1st Qu.: 0.0   1st Qu.: 0.6425   1st Qu.: 4.685
## Median :144.0   Median : 3.0   Median : 3.5650   Median : 64.913
## Mean   :164.7   Mean   : 30.3   Mean   : 4.4763   Mean   : 738.251
## 3rd Qu.:227.0   3rd Qu.: 22.0   3rd Qu.: 7.5600   3rd Qu.: 441.534
## Max.   :723.0   Max.   :1800.0   Max.   :17.8700   Max.   :19479.912
## Hepatitis.B      Measles      BMI      under.five.deaths
## Min.   : 1.00   Min.   : 0.0   Min.   : 1.00   Min.    : 0.00
## 1st Qu.:73.00   1st Qu.: 0.0   1st Qu.:19.20   1st Qu.: 0.00
## Median :91.00   Median : 17.0   Median :43.00   Median : 4.00
## Mean   :78.24   Mean   : 2419.6   Mean   :38.14   Mean   : 42.04
## 3rd Qu.:96.00   3rd Qu.: 360.2   3rd Qu.:56.10   3rd Qu.: 28.00
```

```
## Max. :99.00 Max. :212183.0 Max. :87.30 Max. :2500.00
## Polio Total.expenditure Diphtheria HIV.AIDS
## Min. : 3.00 Min. : 0.370 Min. : 2.00 Min. : 0.100
## 1st Qu.:78.00 1st Qu.: 4.290 1st Qu.:78.00 1st Qu.: 0.100
## Median :93.00 Median : 5.750 Median :93.00 Median : 0.100
## Mean :82.43 Mean : 5.951 Mean :82.29 Mean : 1.742
## 3rd Qu.:97.00 3rd Qu.: 7.470 3rd Qu.:97.00 3rd Qu.: 0.800
## Max. :99.00 Max. :17.600 Max. :99.00 Max. :50.600
## GDP Population thinness..1.19.years
## Min. : 1.68 Min. :3.400e+01 Min. : 0.100
## 1st Qu.: 462.23 1st Qu.:1.816e+05 1st Qu.: 1.600
## Median : 1723.17 Median :1.363e+06 Median : 3.400
## Mean : 6924.41 Mean :1.228e+07 Mean : 4.881
## 3rd Qu.: 5468.43 3rd Qu.:7.538e+06 3rd Qu.: 7.200
## Max. :119172.74 Max. :1.294e+09 Max. :27.700
## thinness.5.9.years Income.composition.of.resources Schooling
## Min. : 0.100 Min. :0.0000 Min. : 0.0
## 1st Qu.: 1.600 1st Qu.:0.4920 1st Qu.:10.1
## Median : 3.400 Median :0.6770 Median :12.3
## Mean : 4.911 Mean :0.6277 Mean :12.0
## 3rd Qu.: 7.300 3rd Qu.:0.7790 3rd Qu.:14.3
## Max. :28.600 Max. :0.9480 Max. :20.7
```

At the end, a brief comparison between the first four columns in which missing values have been managed (similar analysis can be checked for the others but requires more space) suggests that the hotdock method is a better — and less naïf — compromise and tends to be more aligned with original data.

```
plots = list()
j = 1
for (i in nacol[1:4]) {
  meth1=data.frame(v=lifeexp.na.del[[i]])
  meth2=data.frame(v=lifeexp.imp.mode[[i]])
  meth3=data.frame(v=lifeexp.imp.hotdeck[[i]])
  meth1$Method="NAs deleted"
  meth2$Method="Mode"
  meth3$Method="Hotdeck"
  all = rbind(meth1,meth2,meth3)
  plots[[j]] = ggplot(all,aes(v,fill=Method))+
    geom_density(alpha = 0.4)+
    xlab(colnames(lifeexp.df)[i])
  j = j+1
}
ggarrange(plotlist = plots, ncol=2, nrow=2, common.legend = TRUE, legend="bottom")
```

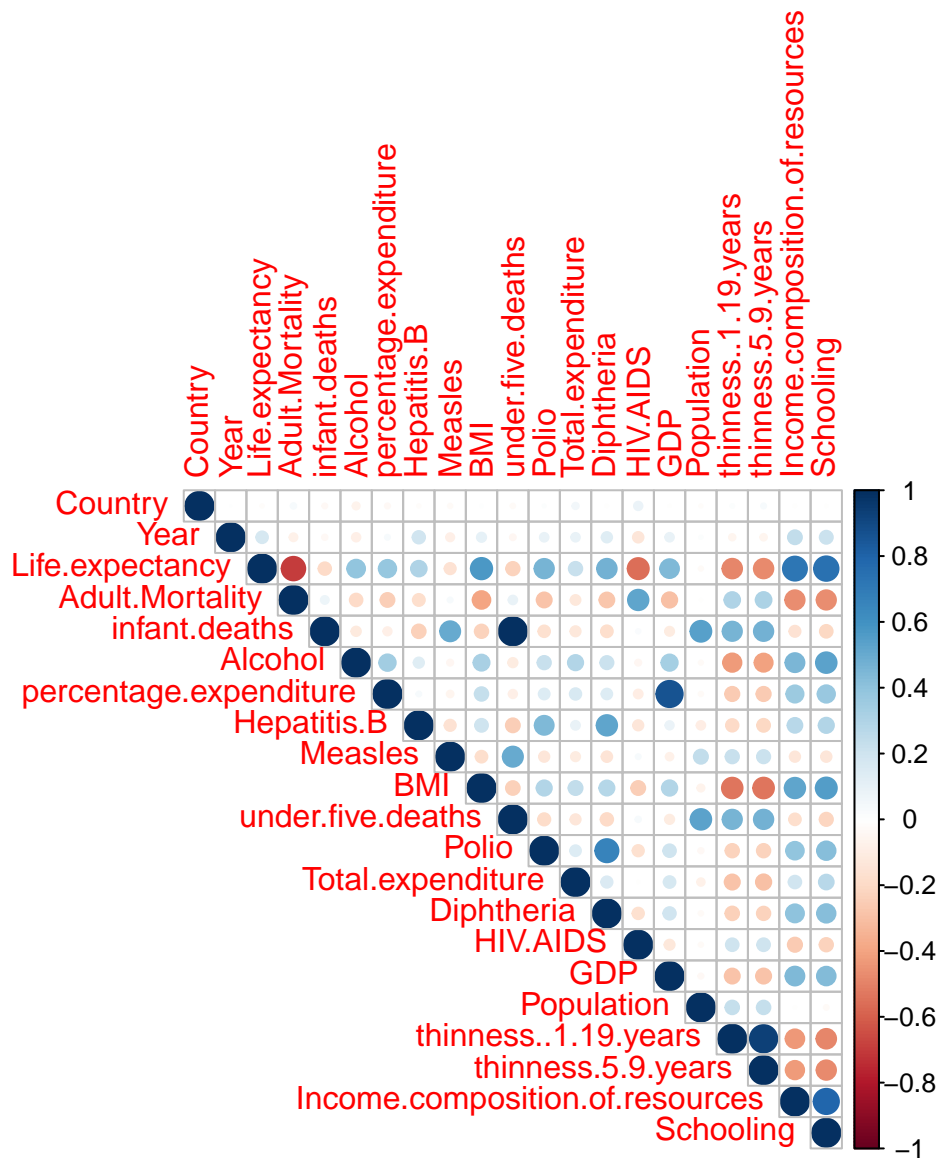


```
# we keep hotdeck version
lifeexp = lifeexp.imp.hotdeck
```

The final dataset is stored in a new variable with a more concise name for further model definition and evaluation.

Another quick insight that can be explored is to check the correlation matrix. Here we can see that there are not serious problem: some correlations are obvious considering the variables meaning, and anyway those with high correlation are the first to check out later in case of poor model.

```
correlation = cor(within(lifeexp, rm("Status")))
corrplot(correlation, type="upper", method="circle")
```



## The model

As described above, the `rminer` package contains different models that can be used for regression analysis. *Random Forest* is only one of them. I've taken it as example of the package capabilities, but with small changes any other model can be used as same as this one.

In order to perform an analysis with a model it's important to have a training set to train the model, but it's necessary to have also a test set to evaluate the performance. Evaluating the model in the training set would lead to over-optimistic results.

For this purpose the package `rminer` lets the user to easily split the dataset into train and test sets, taking care of selecting random units in the right proportions. To this aim, I've trained the model in two different ways: one with the holdout method and one with 10-fold cross-validation.

Here's the code for model training:

```
# Holdout - Random Forest
H = holdout(lifeexp$Life.expectancy, ratio=2/3, seed=42)
```



```
summary(H)
```

```
##      Length Class  Mode
## tr  1958    -none- numeric
## itr    0    -none-  NULL
## val    0    -none-  NULL
## ts   980    -none- numeric
```

```
model1 = fit( Life.expectancy~., lifeexp[H$tr,], model="randomForest")
```

```
# 10-fold Cross-validation - Random Forest
```

```
model2 = crossvaldata(Life.expectancy~., lifeexp, fit, predict, ngroup=10, seed=42,
                      model="randomForest", task="reg")
```

As can be seen, thanks to the rminer package, it's a very easy task to accomplish. After this, one can proceed with model evaluation.

## The Evaluation

The evaluation of the model is easy as the training. Using functions `mgraph` and `mmetric` can be printed the *Regression Scatter Plot* and all the metrics.

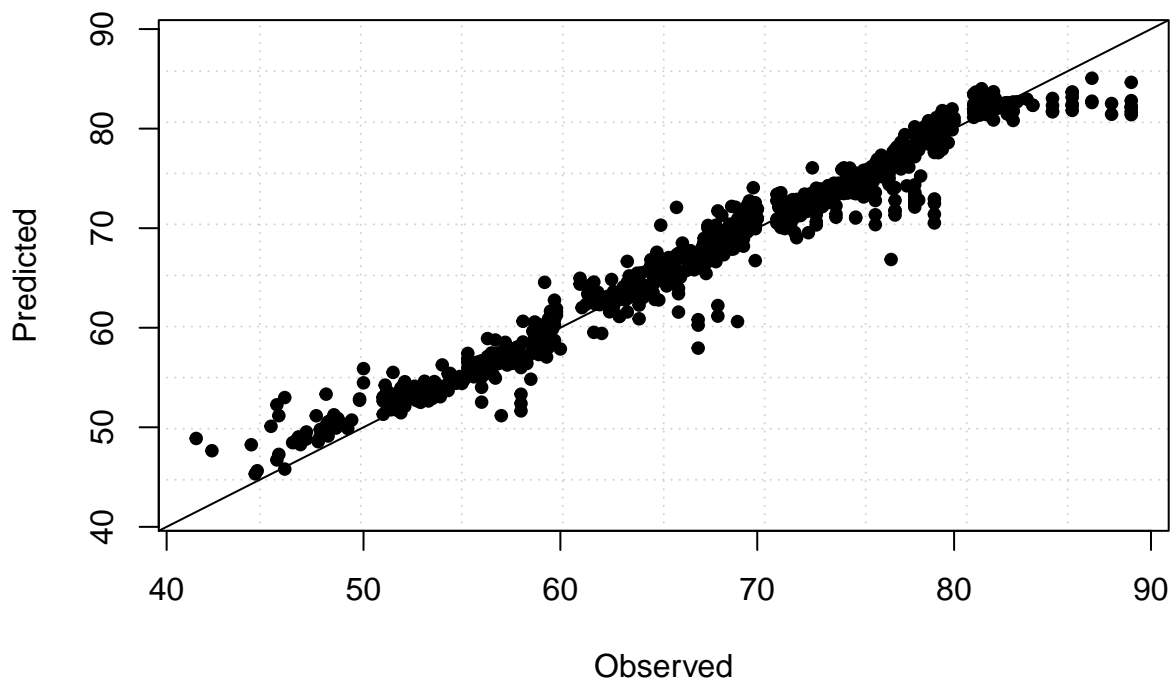
```
# Holdout
```

```
pred1 = predict(model1, lifeexp[H$ts,]) # get predictions on test set (new data)
```

```
target1 = lifeexp[H$ts,]$Life.expectancy
```

```
mgraph(target1, pred1, graph="RSC", Grid=10, main="Random Forest - Holdout 1/3")
```

### Random Forest – Holdout 1/3



```
mmetric(target1, pred1, metric="ALL")
```

```
##          SAE          MAE          MdAE          GMAE          MaxAE
```

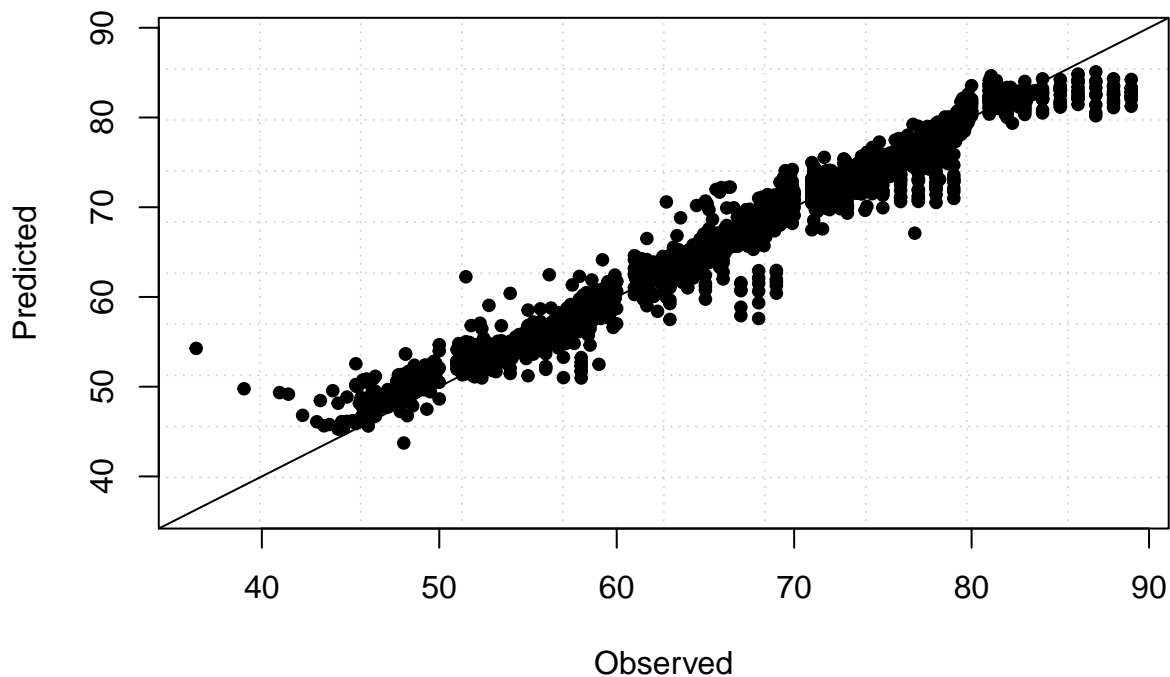
```
## 1.149393e+03 1.172850e+00 6.897750e-01 6.047759e-01 9.945883e+00
## NMAE RAE SSE MSE MdSE
## 2.469158e+00 1.498127e+01 3.344539e+03 3.412795e+00 4.757896e-01
## RMSE GMSE HRMSE RSE RRSE
## 1.847375e+00 0.000000e+00 2.835374e-02 3.756377e+00 1.938137e+01
## ME COR q2 R2 Q2
## -2.278791e-02 9.815993e-01 3.646290e-02 9.635371e-01 3.756377e-02
## NAREC TOLERANCE MAPE MdAPE RMSPE
## 3.647441e-01 6.321942e-01 1.766593e+00 9.992816e-01 2.835374e-01
## RMdSPE SMAPE SMdAPE SMinkowski3 MMinkowski3
## 9.992818e-02 1.766986e+00 9.949653e-01 1.582929e+04 1.582929e+04
## MdMinkowski3
## 1.582929e+04
```

```
# 10-fold cross-validation
```

```
pred2 = model2$cv.fit # k-fold predictions on full dataset
```

```
mgraph(lifeexp$Life.expectancy, pred2, graph="RSC", Grid=10,
main="Random Forest - 10-fold Cross Validation")
```

## Random Forest – 10-fold Cross Validation



```
mmetric(lifeexp$Life.expectancy, pred2, metric="ALL")
```

```
## SAE MAE MdAE GMAE MaxAE
## 3.201716e+03 1.089760e+00 6.322617e-01 0.000000e+00 1.797014e+01
## NMAE RAE SSE MSE MdSE
## 2.067856e+00 1.401288e+01 9.234248e+03 3.143039e+00 3.997553e-01
## RMSE GMSE HRMSE RSE RRSE
## 1.772862e+00 0.000000e+00 2.870430e-02 3.474923e+00 1.864115e+01
## ME COR q2 R2 Q2
## -4.877063e-02 9.827976e-01 3.410884e-02 9.658912e-01 3.474923e-02
## NAREC TOLERANCE MAPE MdAPE RMSPE
## 3.919582e-01 6.639671e-01 1.654958e+00 9.179158e-01 2.870430e-01
```

```
##          RMdSPE          SMAPE          SMdAPE    SMinkowski3    MMinkowski3
## 9.179158e-02 1.649981e+00 9.159594e-01 4.749332e+04 4.749332e+04
## MdMinkowski3
## 4.749332e+04
```

A further very useful function that can be used is the `mining` function. It lets the user to execute several fit and predict runs with a single line of code. After mining, all the metrics are available for examination (note that since there can be a huge number of models, the fitted models are not stored).

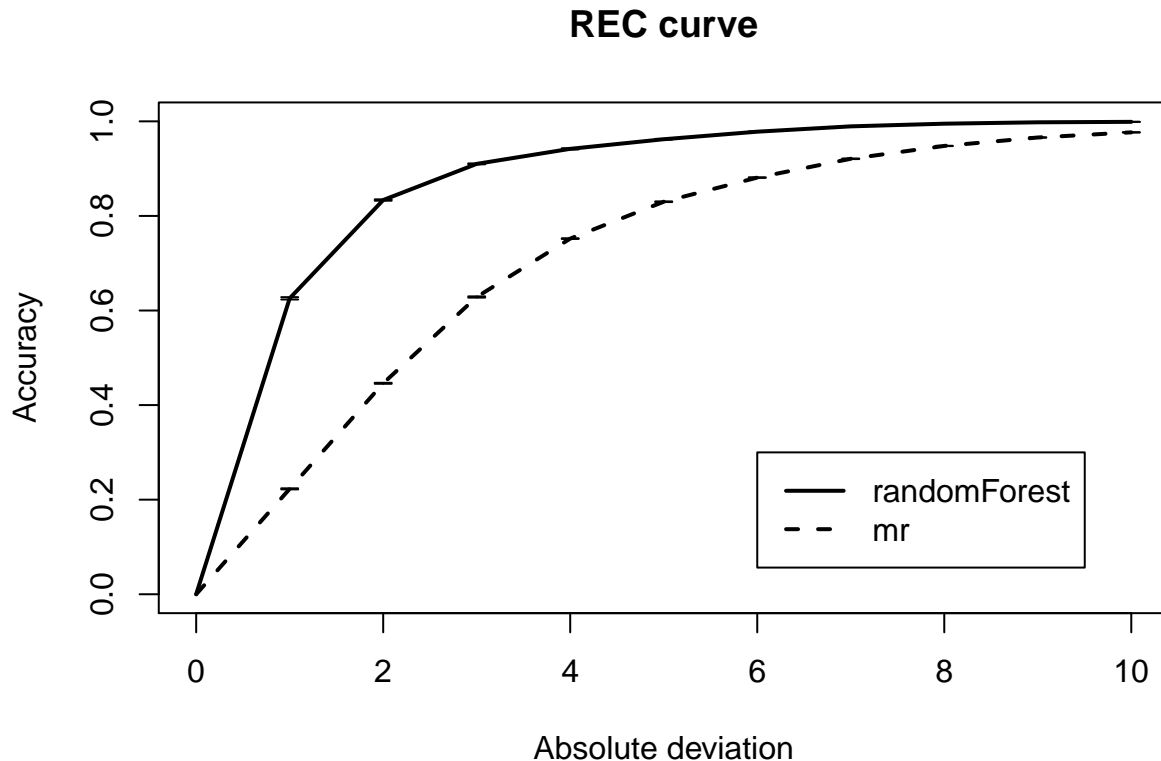
```
# mining for randomForest, external 3-fold, 20 Runs (=60 fitted models)
model3.mining = mining(Life.expectancy~., lifeexp,
                      model="randomForest", method=c("kfold",3,42), Runs=20)
m=mmetric(model3.mining, metric=c("MAE","RMSE","R2"))
print(m) # show metrics for each run
```

```
##          MAE          RMSE          R2
## 1  1.206532 1.939575 0.9592773
## 2  1.186874 1.859235 0.9626054
## 3  1.203920 1.902113 0.9608968
## 4  1.195467 1.885594 0.9613499
## 5  1.209864 1.925625 0.9597574
## 6  1.184972 1.876700 0.9618660
## 7  1.186807 1.883079 0.9616018
## 8  1.202549 1.907914 0.9606777
## 9  1.201508 1.900423 0.9607804
## 10 1.200257 1.903958 0.9607660
## 11 1.200390 1.907964 0.9605318
## 12 1.201168 1.931154 0.9598137
## 13 1.209126 1.904068 0.9608273
## 14 1.200502 1.909922 0.9604048
## 15 1.193869 1.876577 0.9617693
## 16 1.184531 1.879316 0.9617824
## 17 1.183369 1.875478 0.9618425
## 18 1.192731 1.881884 0.9615822
## 19 1.209022 1.917107 0.9600985
## 20 1.183677 1.870401 0.9620338
```

Finally one can be interest in comparing the mining of a model with the mining of another model, and this can be achieved with this commands:

```
# mining for standard multiple linear regression
model4.mining = mining(Life.expectancy~., lifeexp,
                      model="mr", method=c("kfold",3,42), Runs=20)

L=vector("list",2)
L[[1]]=model3.mining
L[[2]]=model4.mining
mgraph(L, graph="REC", leg=c("randomForest","mr"), main="REC curve", xval=10)
```



In this case the Random Forest model is compared with a standard multiple linear regression model. They are compared with REC curves. The Regression Error Characteristic (REC) curve is the corresponding of the ROC curve for regression. It plots the error tolerance on the x-axis versus the percentage of points predicted within the tolerance on the y-axis. More information about the REC curve can be found in (Bi and Bennett 2003).

From the REC curve we can see the two models performance and see the advantage of using a more complex model with the same ease as the standard linear regression model. Of course this is not a detailed comparison, and further improvements in the linear model can be for sure achieved, but the aim here is to place emphasis on the wide spread of tools offered by rminer.

## Conclusions

Eventually, from this work it's evident that the package rminer is a good tool to perform regression analysis. With its small set of functions — but with a wide spread of options and parameters — can be useful to someone who want to do an overall analysis, but also to someone that want a finer granularity for personalization in model hyperparameters. In this brief tour of the package I didn't analyze the details about hyperparameters tuning, but with a quick look into the documentation one can face up this task too as easily as what done here. Must be said also that for an advanced user with very specific requirements, this package can be a bit limiting, but anyway, it's a very good starting point for a regression analysis.

## References

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