

# Analysis and Design of an LCL-T Resonant Converter as a Constant-Current Power Supply

Mangesh Borage, Sunil Tiwari, and Swarna Kotaiah

**Abstract**—An LCL-T resonant converter (LCL-T RC) is shown to behave as a current source when operated at resonant frequency. A detailed analysis of the LCL-T RC for this property is presented. Closed-form expressions for converter gain, component stresses, and the condition for converter design optimized for minimum size of resonant network is derived. A design procedure is illustrated with a prototype 200-W 20-A current-source power supply and experimental results are presented. The LCL-T RC as a current source offers many advantages such as easy parallel operation and low circulating currents at light load. Additionally, with appropriate phase shift in paralleled modules, the peak–peak ripple in output current is reduced and the ripple frequency is increased, reducing filtering requirements. The leakage inductance of a transformer can be advantageously integrated into the resonant network. These merits make the topology applicable in various applications such as magnet power supply, capacitor charging power supply, laser diode drivers, etc.

**Index Terms**—Current supplies, dc–dc power conversion, resonant power conversion, soft switching.

## NOMENCLATURE

$A$	A term defined by (13).
$C$	Capacitance value of resonant capacitor, $C$ .
$E_n$	Normalized total inductor energy.
$f$	Switching frequency.
$f_o$	Resonant frequency.
$H$	Current gain.
$I_B$	Base current.
$I_{C,rms}$	RMS value of current in capacitor $C$ .
$I_{CN}$	Normalized rms current in capacitor $C$ .
$I_{L,rms}$	RMS value of current in inductor $L$ .
$I_{LN}$	Normalized rms current in inductor $L$ .
$I_{L_a,rms}$	RMS value of current in inductor $L_a$ .
$I_{L_aN}$	Normalized rms current in inductor $L_a$ .
$I_o$	Output dc current.
$L$	Inductance value of resonant inductor $L$ .
$L_a$	Inductance value of resonant inductor $L_a$ .
$M$	Voltage gain.
$N_1$	Number of primary turns in transformer.
$N_2$	Number of secondary turns in transformer.
$p$	Number of parallel-connected converters.
$Q$	The $Q$ -value of the resonant circuit.
$Q_{opt}$	Optimum value of $Q$ .

$R_{ac}$	Equivalent ac resistance.
$R_L$	Load resistance.
$V_B$	Base voltage.
$V_{C,rms}$	RMS value of voltage across capacitor $C$ .
$V_{CN}$	Normalized rms voltage across capacitor $C$ .
$V_d$	Input dc voltage.
$V_{in,rms}$	RMS value of the fundamental component of input square-wave voltage.
$V_{L,rms}$	RMS value of voltage across inductor $L$ .
$V_{LN}$	Normalized rms voltage across inductor $L$ .
$V_{L_a,rms}$	RMS value of voltage across inductor $L_a$ .
$V_{L_aN}$	Normalized rms voltage across inductor $L_a$ .
$V_o$	Output dc voltage.
$Z_n$	Characteristic impedance of the resonant circuit.
$\gamma$	Ratio of inductors $L_a$ and $L$ .
$\phi$	Phase angle between inverter output voltage and current.
$\omega$	$\equiv 2\pi f$ , angular switching frequency (in radians per second).
$\omega_i$	Normalized switching frequency where $H$ is independent of $Q$ .
$\omega_n$	Normalized switching frequency.
$\omega_o$	$\equiv 2\pi f_o$ , angular resonant frequency (in radians per second).
$\omega_v$	Normalized switching frequency where $M$ is independent of $Q$ .

## I. INTRODUCTION

**R**ESONANT converters (RCs) feature zero voltage switching (ZVS), zero current switching (ZCS), high-frequency operation, high efficiency, small size, and low electromagnetic interference (EMI). They have been successfully applied to dc power supplies for industrial, commercial, and domestic applications, high-frequency ac power supplies for induction heating, power-factor correction, and discharge lamp ballast. The series [1] and parallel [2] RC (SRC and PRC, respectively) are basic resonant-converter topologies with two reactive elements. The merits of SRC include better part-load efficiency and inherent dc blocking of the isolation transformer due to the series capacitor in the resonant network. However, its part-load regulation is poor and output-voltage regulation at no load is not possible by switching frequency variation. On the other hand, PRC offers no-load regulation but suffers from poor part-load efficiency and lack of inherent dc blocking for the isolation transformer. To remove these limitations, RCs with three and four reactive components were investigated in [3] and [4], respectively.

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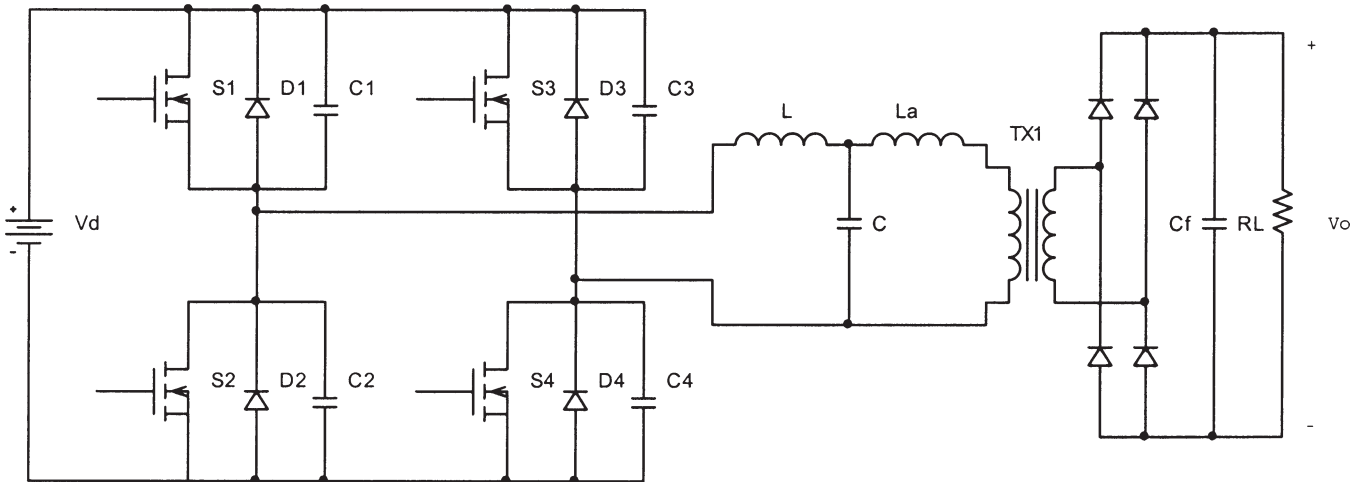


Fig. 1. Circuit diagram of the LCL-T RC.

It has been shown that the addition of an inductor to the SRC significantly improves the no-load-regulation characteristics. The resulting converter, called the LCL RC [5], [6], offers load-independent output voltage when operated at the switching frequency equal to the resonant frequency of the series arm. Therefore, the output voltage can be regulated against wide line and load variations with a moderate sweep of switching frequency. The magnetic components of the RC can also be integrated [7]. Therefore, the LCL RC is deemed as a strong candidate for the output-voltage-regulated power supplies [8].

The addition of an inductor to PRC also changes its characteristics. Because of the T-type resonant network, the resulting topology is referred in this paper as the LCL-T RC. The circuit diagram of this topology is shown in Fig. 1. The LCL-T resonant network composed of inductors  $L$ ,  $L_a$  and capacitor  $C$  is driven by a high-frequency full-bridge square-wave inverter. The antiparallel diodes and capacitors shown in Fig. 1 are inherent to each MOSFET switch of the inverter. It has been shown that the LCL-T RC also offers load-independent output voltage and no-load regulation, which is useful for voltage-regulated power supplies [9]. Another interesting property of the LCL-T RC has been pointed out in [10]. When operated at the resonant frequency, the LCL-T RC behaves like a current source. That is, under these conditions, the output current is constant irrespective of load variations. Furthermore, for operation at resonance with  $L = L_a$ , the inverter output current (that is, current in inductor  $L$ ) is in phase with the voltage, which further reduces under the part-load condition. This maximizes full-load and part-load converter efficiency due to lower conduction losses. The same property of the LCL-T RC is reported in [11] for realizing a high-power-factor rectifier. The property that the LCL-T RC converts a high-frequency constant-voltage source to a high-frequency constant-current (CC) source using a passive  $LC$  element is also signified in [12] and [13].

A CC or an output-current-regulated power supply is required in many commercial, industrial, and research applications such as electromagnets [14], capacitor charging [15], battery charging [16], arc welding [17], semiconductor laser diode drivers [18], etc. The LCL-T RC, by virtue of its current-

source property, can become a potential candidate for such application. Although [10]–[13] mention the current-source property of this topology, the detailed analysis, optimization, and design guidelines are not reported in the literature. Therefore, the major objectives of this paper are:

- 1) to perform a detailed study of the LCL-T RC for its operation as a CC source;
- 2) to derive and simplify the expressions for voltage and current ratings of different components;
- 3) present an optimum design of the converter;
- 4) to validate the analysis with experimental results.

The ac analysis [19] is followed to derive closed-form expressions, discuss the performance characteristics, and derive the condition for optimized design of the converter in Section II. Section III discusses the control-related issues and experimental results on a laboratory prototype are presented in Section IV.

## II. CONVERTER ANALYSIS

In the ac analysis, the output rectifier and filter are replaced by the equivalent ac resistance and the square-wave input-voltage source is replaced by its fundamental sinusoidal equivalent. The power transfer from input to output is assumed to be only via the fundamental component and the contribution of all the harmonics is neglected. Without losing generality, the turns ratio ( $N_1/N_2$ ) of the isolation transformer  $T_{x1}$  is assumed to be unity. The equivalent ac resistance for the rectifier with capacitive filter [19] and the rms value of the fundamental component of input square-wave voltage are given by

$$R_{ac} = \frac{8}{\pi^2} R_L \quad \text{and} \quad V_{in,rms} = \frac{2\sqrt{2}}{\pi} V_d. \quad (1)$$

The resonant frequency and the normalized switching frequency are defined as

$$\omega_o = \frac{1}{\sqrt{LC}} \quad \text{and} \quad \omega_n = \frac{\omega}{\omega_o}. \quad (2)$$

The characteristic impedance and  $Q$  of the resonant network are

$$Z_n = \sqrt{\frac{L}{C}} \quad \text{and} \quad Q = \frac{\omega_o L}{R_L} = \frac{Z_n}{R_L}. \quad (3)$$

The ratio of inductors is defined as

$$\gamma = \frac{L_a}{L}. \quad (4)$$

The voltage and current gain are defined as

$$M = \frac{V_o}{V_d} \quad \text{and} \quad H = \frac{I_o}{\left(\frac{V_d}{Z_n}\right)}. \quad (5)$$

The voltage gain can be derived as

$$M = \frac{1}{(1 - \omega_n^2) + j \frac{\pi^2}{8} Q [(1 + \gamma)\omega_n - \gamma\omega_n^3]}. \quad (6)$$

A close examination of (6) shows that the value of  $M$  is independent of load (that is,  $Q$ ) if

$$\omega_n = \omega_v = \sqrt{\frac{1 + \gamma}{\gamma}} \quad (7)$$

where  $\omega_v$  is defined as the normalized switching frequency where  $M$  is independent of  $Q$ . Furthermore, at  $\omega_n = \omega_v$ , the converter gain can be expressed as

$$M|_{\omega_n=\omega_v} = \gamma. \quad (8)$$

Next, the current gain of LCL-T RC can be derived as

$$H = \frac{1}{\frac{1}{Q} (1 - \omega_n^2) + j \frac{\pi^2}{8} [(1 + \gamma)\omega_n - \gamma\omega_n^3]}. \quad (9)$$

We see from (9) that the load current is independent of the load if operated at  $\omega_n = \omega_i = 1$ ,  $\omega_i$  being the normalized switching frequency where  $H$  is independent of  $Q$ . And

$$H|_{\omega_n=\omega_i} = \frac{8}{\pi^2}. \quad (10)$$

Generalized expressions for normalized voltage and current ratings of different components are derived subsequently. The following base values are defined for the normalization

$$\text{Base voltage : } V_B = V_d \quad (11)$$

$$\text{Base current : } I_B = \frac{V_d}{Z_n} \quad (12)$$

$$\text{If } A = (1 - \omega_n^2) + j \frac{\pi^2}{8} Q [(1 + \gamma)\omega_n - \gamma\omega_n^3] \quad (13)$$

then

$$I_{LN} = \frac{I_{L,\text{rms}}}{I_B} = \frac{\pi}{2\sqrt{2}} \left( \frac{Q(1 - \gamma\omega_n^2) + j \frac{8}{\pi^2} \omega_n}{A} \right) \quad (14)$$

$$I_{CN} = \frac{I_{C,\text{rms}}}{I_B} = \frac{\pi}{2\sqrt{2}} \left( \frac{-Q\gamma\omega_n^2 + j \frac{8}{\pi^2} \omega_n}{A} \right) \quad (15)$$

$$I_{L_aN} = \frac{I_{L_a,\text{rms}}}{I_B} = \frac{\pi}{2\sqrt{2}} \left( \frac{Q}{A} \right) \quad (16)$$

$$V_{LN} = \frac{V_{L,\text{rms}}}{V_B} = \frac{2\sqrt{2}}{\pi} \left( \frac{-\omega_n^2 + j \frac{\pi^2}{8} Q (\omega_n - \gamma\omega_n^3)}{A} \right) \quad (17)$$

$$V_{CN} = \frac{V_{C,\text{rms}}}{V_B} = \frac{2\sqrt{2}}{\pi} \left( \frac{1 + j \frac{\pi^2}{8} Q \gamma \omega_n}{A} \right) \quad (18)$$

$$V_{L_aN} = \frac{V_{L_a,\text{rms}}}{V_B} = \frac{2\sqrt{2}}{\pi} \left( \frac{j \frac{\pi^2}{8} Q \gamma \omega_n}{A} \right). \quad (19)$$

For operation at  $\omega_n = \omega_i = 1$ , (14) can be simplified as

$$I_{LN}|_{\omega_n=\omega_i} = \frac{\pi}{2\sqrt{2}} \left( \frac{Q(1 - \gamma) + j \frac{8}{\pi^2}}{j \frac{\pi^2}{8} Q} \right). \quad (20)$$

Therefore, the phase angle between the inverter output voltage and current can be derived as

$$\phi|_{\omega_n=\omega_i} = \tan^{-1} \left( \frac{Q(\gamma - 1)}{\frac{8}{\pi^2}} \right) \quad (21)$$

$$\phi|_{\omega_n=\omega_i} = 0, \quad \text{if } \gamma = 1$$

$$\phi|_{\omega_n=\omega_i} < 0, \quad \text{if } \gamma < 1$$

$$\phi|_{\omega_n=\omega_i} > 0, \quad \text{if } \gamma > 1. \quad (22)$$

Thus, the converter can operate in lagging power-factor mode if  $\gamma < 1$ . The advantages of an RC operating in lagging power-factor mode are very well known [20]. For the operation in lagging power-factor mode, the antiparallel diode conducts prior to the switch in every cycle to ensure zero voltage turn on. For reliable ZVS of the switch, it is essential that the diode conducts before the switch does. Although  $\gamma = 1$  gives a zero phase angle that would result in lowest conduction loss, in practice, the required phase lag can be realized by keeping  $\gamma$  slightly less than unity. Nevertheless, theoretically preferred operating parameters can be decided as  $\omega_n = 1$  and  $\gamma = 1$ , and the magnitude of the above-derived expressions can be written in simplified form as below. The resulting error will not be significant as long as  $\gamma$  is close to unity.

$$M|_{\omega_n=\gamma=1} = \frac{8}{\pi^2} \left( \frac{1}{Q} \right) \quad \text{and} \quad H|_{\omega_n=\gamma=1} = \frac{8}{\pi^2} \quad (23)$$

$$I_{LN}|_{\omega_n=\gamma=1} = V_{LN}|_{\omega_n=\gamma=1} = \frac{16\sqrt{2}}{\pi^3} \left( \frac{1}{Q} \right) \quad (24)$$

$$I_{L_aN}|_{\omega_n=\gamma=1} = V_{L_aN}|_{\omega_n=\gamma=1} = \frac{2\sqrt{2}}{\pi} \quad (25)$$

$$I_{CN}|_{\omega_n=\gamma=1} = V_{CN}|_{\omega_n=\gamma=1} = \frac{2\sqrt{2}}{\pi} \left( \frac{\sqrt{\left(\frac{8}{\pi^2}\right)^2 + Q^2}}{Q} \right). \quad (26)$$

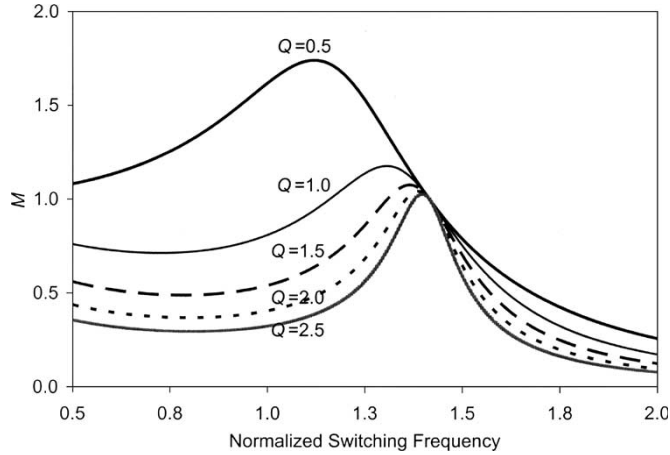


Fig. 2. Converter voltage gain ( $M$ ) versus normalized switching frequency for  $\gamma = 1$ .

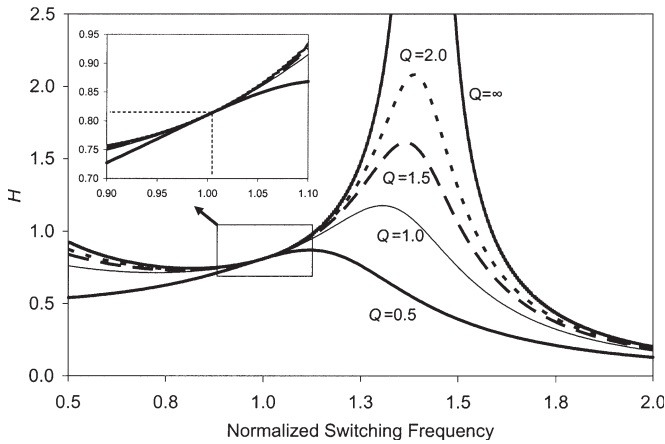


Fig. 3. Converter current gain ( $H$ ) versus normalized switching frequency for  $\gamma = 1$ . In the inset: details about the operating point  $\omega_n = 1$ .

Normally, the resonant inductor is a bigger and heavier component than the capacitor. It is known that the physical size of an inductor is indicated by the area product, which is directly proportional to the energy handled by the inductor. The normalized total inductor energy can be derived as

$$E_n|_{\omega_n=\gamma=1} = \frac{\left(\frac{1}{2}LI_{L,rms}^2 + \frac{1}{2}L_a I_{L_a,rms}^2\right)}{\left(\frac{V_d^2}{\omega_o R_L}\right)} \bigg|_{\omega_n=\gamma=1} = \frac{256}{\pi^6} \frac{1}{Q^3} + \frac{4}{\pi^2} \frac{1}{Q}. \quad (27)$$

#### A. Performance Characteristics

The plots of voltage gain  $M$  of LCL-T RC as a function of  $\omega_n$  are shown in Fig. 2 for  $\gamma = 1$ . The converter offers load-independent voltage gain at a particular operating frequency; the operating frequency ( $\omega_v$ ) and the voltage gain both are functions of  $\gamma$ , as described by (7) and (8). The plots of current gain  $H$  are shown in Fig. 3 for different values of  $Q$  and  $\gamma = 1$ . The plot for  $Q = \infty$  corresponding to load short circuit is also included to demonstrate current-source behavior.  $H$  is seen to

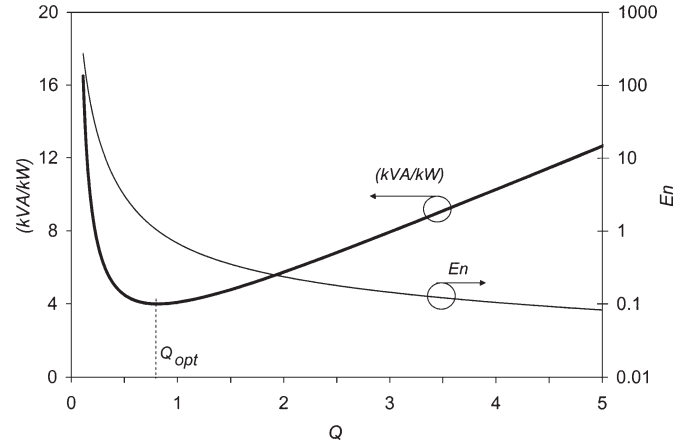


Fig. 4. (kVA/kW) and  $E_n$  rating of the LCL-T RC as a function of  $Q$  for  $\gamma = 1$  and  $\omega_n = 1$ .

be load independent at  $\omega_n = \omega_i = 1$  under all conditions. The region around  $\omega_n = 1$  in Fig. 3 is magnified and shown as inset. It can be noticed that the load current is nearly independent of load even for operation in the vicinity of  $\omega_n = 1$ . This can be achieved by keeping full-load  $Q \geq 1$ . At no load, the load resistance is 0 for a current-source power supply or, in other words, at no load,  $Q = \infty$ . Note from (24) that under the no-load condition, the inverter output current is 0. This shows that the input current reduces proportionately from full load to no load and thus, the converter maintains excellent efficiency.

#### B. Optimization

The reactive components in a RC increase its size. Therefore, the RCs are optimized for minimum size of resonant network. The (kVA/kW) rating of resonant network is considered as an index for the physical size of the resonant network. Using expressions (23)–(26), the (kVA/kW) rating of LCL-T RC can be derived from

$$\frac{\text{kVA}}{\text{kW}} \bigg|_{\omega_n=\gamma=1} = \frac{V_{CN} \cdot I_{CN} + V_{LN} \cdot I_{LN} + V_{LaN} \cdot I_{LaN}}{M \cdot H} \bigg|_{\omega_n=\gamma=1}. \quad (28)$$

The plot of (28) is shown in Fig. 4 as a function of  $Q$  for  $\gamma = 1$  and  $\omega_n = 1$ . The plot shows the existence of a particular value of  $Q$  where (kVA/kW) is minimum. This is termed as the optimum value of  $Q$  ( $Q_{opt}$ ). It can be shown that  $Q_{opt} = (8/\pi^2)$ . For the design of the converter, full-load  $Q$  should be taken equal to  $Q_{opt}$ . Also shown in Fig. 4 is the normalized total inductor energy  $E_n$ , which decreases with increase in  $Q$ .

### III. CONVERTER CONTROL

Although the output current of LCL-T RC is seen to be constant irrespective of changes in the load, for practical application as a current-source power supply, it should be possible to regulate the output current against input-voltage variations. In some applications, wide conversion range is desired. Since the LCL-T RC behaves as a current source only when operated

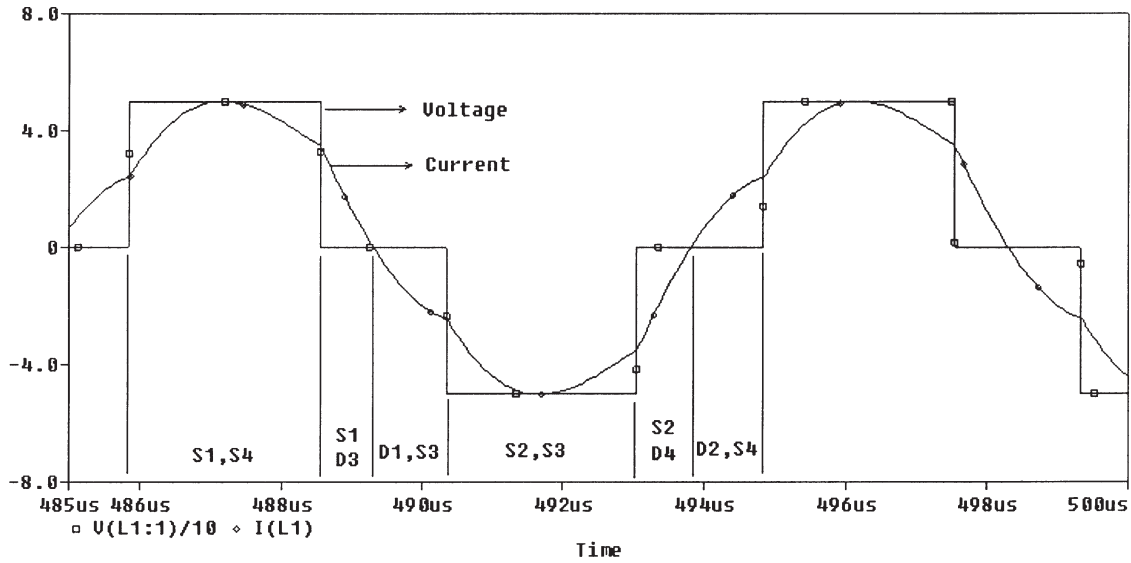


Fig. 5. Simulated waveforms of inverter output voltage and current with clamped-mode control. Also shown are the devices conducting in various subintervals.

at  $\omega_n = 1$ , the method using variation of switching frequency to control the output cannot be applied—or else current-source behavior will be lost. Besides, Fig. 3 shows that the current gain characteristics is relatively flat in the vicinity of  $\omega_n = 1$ . Thus, variation of switching frequency will not provide wide conversion range and output-current regulation against large input-voltage variations. Constant frequency control must therefore be applied. Various fixed-frequency control strategies for SRC have been reported in the literature [21], [22], namely, clamped-mode (CM) control, asymmetrical duty-cycle (ADC) control, and asymmetrical voltage cancellation (AVC) control. They can be applied to the LCL-T RC. Loss of ZVS of the switches under certain operating conditions may be a limitation of these methods. Illustratively, Fig. 5 shows simulated waveforms of inverter output voltage and current with CM control for operation with  $\omega_n = 1$ ,  $\gamma = 1$ , and  $Q = Q_{opt}$ . Since the LCL-T RC is designed to operate in unity or slightly lagging power-factor mode of operation, the ZVS of switches in the bridge inverter is seen to be lost with CM control. The ZVS of switches is expected to be maintained over a wider range of operation with ADC and AVC control than with the CM control. However, ADC and AVC control methods necessitate a capacitor in series with  $L$  to block the dc component of high-frequency excitation voltage resulting from the asymmetrical operation.

Alternatively, the output current of the LCL-T RC can be varied over a wide range by controlling its input dc voltage by a front-end converter, which can be a soft switching PWM topology—with or without isolation. The second stage is the LCL-T RC free running at  $\omega_n = 1$ . This method allows flexibility in the design. The resonant network can be designed with optimum parameters for maximum efficiency. However, two cascaded converters reduce the overall conversion efficiency and increase complexity, component count, and cost.

Since LCL-T RC is a current source, it lends itself for easy paralleling without any additional care for equal current sharing. A parallel connection of low-power modules instead of a single high-power converter is known to provide modu-

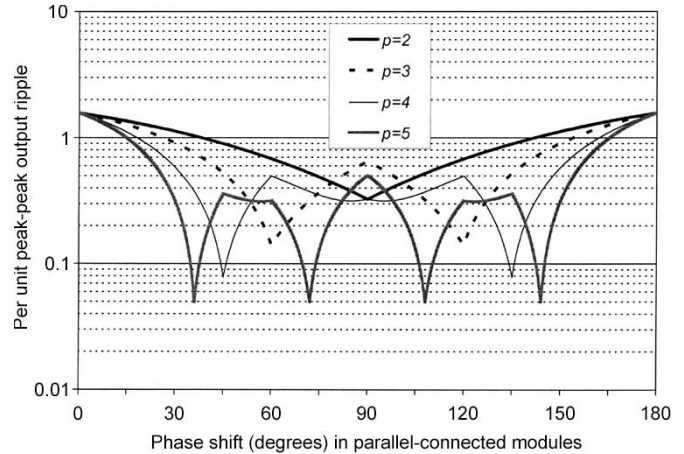


Fig. 6. Parallel operation of LCL-T RC modules: The per-unit peak-peak ripple as a function of phase shift.  $p$  is the number of paralleled modules.

larity, standardization, redundancy, and high reliability. With transformer-isolated LCL-T RC, two or more modules can be connected in parallel. Furthermore, if the operation of two modules is phase shifted, the average total output current is doubled and the peak-peak ripple is reduced. It can be shown that for two paralleled modules, the ripple will be minimum, equal to 32.53% of average total current, when the phase shift between two modules is  $90^\circ$ . Similarly, for three modules, the ripple will be minimum, equal to 14.03%, when the phase shift is  $60^\circ$  or  $120^\circ$ . The peak-peak ripple will be 7.81% and 4.97% for four and five parallel-connected phase-shifted modules, respectively. In general, the optimum phase shift among the modules is given by  $(180/p)$  degrees, where  $p$  is the number of paralleled connected modules. The per-unit peak-peak ripple as a function of phase shift is shown in Fig. 6 for different values of  $p$ . The graph assumes sinusoidal current waveshape. For  $p$  modules in parallel, the ripple frequency of output as well as input current will be  $2p$  times the switching frequency. The filtering requirement is thus significantly reduced, and in some applications, filter can be eliminated.

TABLE I  
DESIGN PARAMETERS FOR THE EXPERIMENTAL CONVERTER

Parameter	Value
$L$ ( $\mu\text{H}$ )	14.47
$L_a$ ( $\mu\text{H}$ )	14.47
$C$ ( $\mu\text{F}$ )	0.141
$N_1/N_2$	5
$I_{L,rms}$ (A)	4.45
$I_{La,rms}$ (A)	4.45
$I_{C,rms}$ (A)	6.28
$V_{L,rms}$ (V)	45
$V_{La,rms}$ (V)	45
$V_{C,rms}$ (V)	63

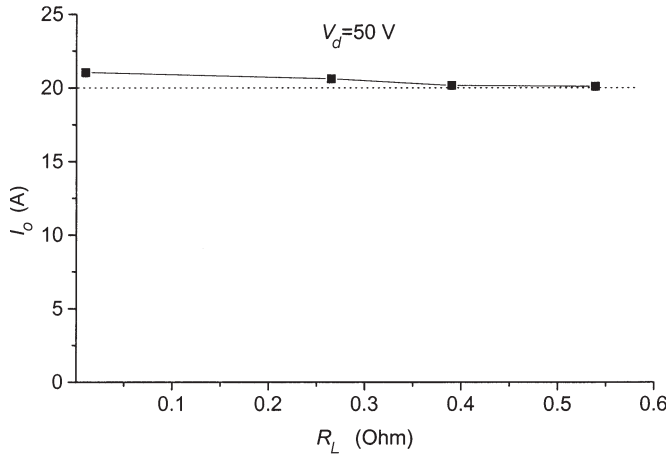


Fig. 7. Open-loop output characteristics of the prototype experimental converter.

#### IV. EXPERIMENTAL RESULTS

A laboratory prototype of the LCL-T RC dc current-source power supply is designed, built, and tested to validate the current-source property of the LCL-T RC. The converter has the following specifications: input dc supply voltage = 50 V, maximum output current = 20 A, maximum load resistance (full load) = 0.5  $\Omega$ , and switching frequency = 100 kHz. In the analysis of previous sections, the transformer turns ratio ( $N_1/N_2$ ) was assumed to be unity. In the design procedure to follow, the transformer is included. The previous results still apply; however, they are scaled suitably by transformer turns ratio. The optimum value of  $Q$  is derived as

$$Q_{opt} = \frac{8}{\pi^2} = \frac{\omega_o L}{R_L \left(\frac{N_1}{N_2}\right)^2} = \frac{Z_n}{R_L \left(\frac{N_1}{N_2}\right)^2}. \quad (29)$$

Rewriting (10)

$$I_o = \frac{8}{\pi^2} \left(\frac{V_d}{Z_n}\right) \left(\frac{N_1}{N_2}\right). \quad (30)$$

From (29) and (30)

$$\frac{N_1}{N_2} = \frac{V_d}{I_o R_L}. \quad (31)$$

In the present design example,  $N_1/N_2 = 5$ . Then, the values of  $L$  and  $C$  can be calculated as 16.11  $\mu\text{H}$  and 0.157  $\mu\text{F}$ , respectively, for the design with  $Q = Q_{opt}$  at full load and

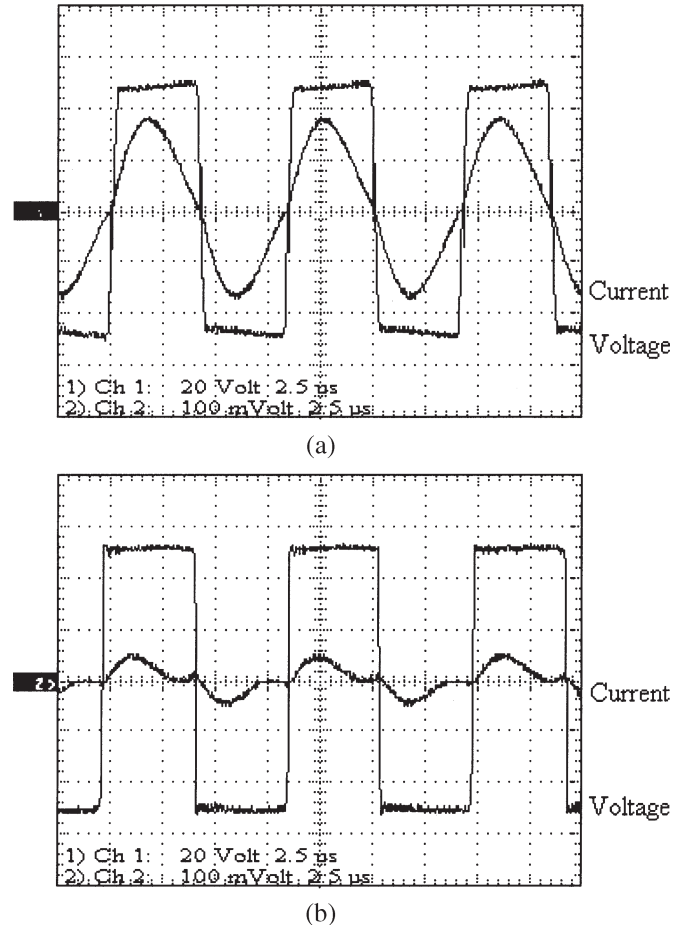


Fig. 8. Voltage and current waveforms at the output of the inverter bridge. (a)  $R_L = 0.53 \Omega$ , and, (b)  $R_L = 0.1 \Omega$ . Scale: 20 V/div (voltage), 5 A/div (current), and 2.5  $\mu\text{s}$ /div.

resonant frequency of 100 kHz. However, 0.157  $\mu\text{F}$  is an odd value and could not be realized with available capacitors. Connecting three 0.047- $\mu\text{F}$  capacitors in parallel, the closest realizable value is 0.141  $\mu\text{F}$ . Accordingly, the value of  $L$  is scaled to 14.47  $\mu\text{H}$  to retain equal  $Z_n$ . The resonant and switching frequency is consequently changed to 111.43 kHz. The component values and their computed ratings at full load are summarized in Table I. The input bridge inverter is realized with 200-V MOSFET switches. A secondary center-tap transformer is used to reduce losses in the output rectifier stage. A common-cathode Schottky module rated for 45 V and 40 A is used for output rectification. A 20- $\mu\text{F}$  capacitor forms the output filter in the prototype. The measured transformer leakage inductance reflected on the primary side was 2.5  $\mu\text{H}$ . Hence, an additional 11.5- $\mu\text{H}$  inductance is added to make  $L_a = 14 \mu\text{H}$ .  $L = 14.5 \mu\text{H}$ , resulting in  $\gamma$  slightly less than unity. In fact, to reduce the circuit components, the leakage inductance of the transformer can be beneficially used as the resonant inductor  $L_a$ . Various techniques allow predictable and controlled leakage inductance in a transformer [23]–[25].

Fig. 7 shows the open-loop output characteristics of the prototype converter. The converter operates at a 50-V dc input. The load was varied from short-circuit condition to full load. The output current is seen to be approximately constant



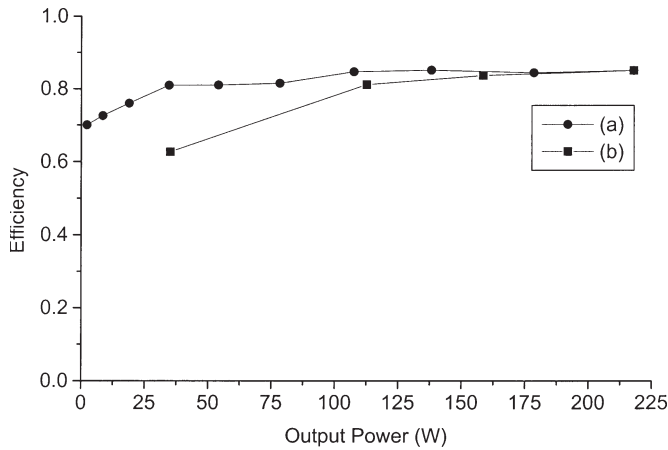


Fig. 9. Efficiency of the experimental converter as a function of output power. Plot (a):  $R_L = 0.53 \Omega$  and  $V_d$  is varied from 5 to 50 V. Plot (b):  $V_d = 50$  V and load resistance is varied.

at 20 A. The slight droop in the characteristics is due to the increase in conduction losses in the bridge inverter and resonant network. The voltage and current waveforms at the output of the inverter bridge are shown in Fig. 8(a) and (b) for  $R_L = 0.53$  and  $0.1 \Omega$ , respectively. Besides being in phase with the voltage, the inverter output current is seen to reduce with load, as predicted in the analysis, resulting in high part-load efficiency. Fig. 9 shows the experimental converter efficiency as a function of output power. In plot (a),  $R_L = 0.53 \Omega$  and input dc voltage is varied from 5 V to 50 V. This plot indicates high efficiency over the entire conversion range. The maximum efficiency is 0.85 at 217-W output power, which drops to 0.7 when the output power is reduced to 2.25 W. The highest efficiency is limited to 0.85 because drops in the circuit (output rectifier and MOSFETs) become comparable with the low output voltage (10 V) of the experimental prototype. Plot (b) shows the efficiency of the experimental converter when operated at 50-V input and load resistance is varied to change the output power.

## V. CONCLUSION

A detailed analysis of the LCL-T RC is presented in this paper for its application as a CC power supply. Closed-form expressions for converter gain and component stresses are derived. It is seen that the converter exhibits load-independent voltage and current gain at certain operating frequencies, the latter being useful for a CC power supply. The condition for converter design optimized for minimum size of resonant network is derived. Various methods for the control of output current over a wide conversion range and against variation in input dc voltage are discussed. Being an inherent current source, the converter lends itself for easy paralleling without any complex control for equal current sharing. If the paralleled modules are phase shifted, the peak-peak ripple in output and input currents is reduced and the ripple frequency is increased. This reduces the filtering requirement. If sufficient number of modules are connected in parallel, the additional filter can be eliminated. The leakage inductance of the transformer can be advantageously integrated into the LCL-T resonant network.

Part-load efficiency is better due to lower circulating currents. Experimental results on the prototype converter validates the merits of the converter topology. These merits make the topology applicable as a CC power supply in various applications.

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