Homework Assignment 2

Greg Forkutza Student ID: 400277514

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1 Introduction

This data set comprises details of simulated samples associated with 23 species of gilled mushrooms from the Agaricus and Lepiota Family. Each species is categorized as either definitely edible, definitely poisonous, or of unknown edibility and thus, not advised for consumption. The latter category is subsumed under definitely inedible, thereby defining a binary classification problem. The idea is to use the mushrooms qualitative characteristics to identify it as edible or not. This data set is sourced from the machine learning repository mis [1987].

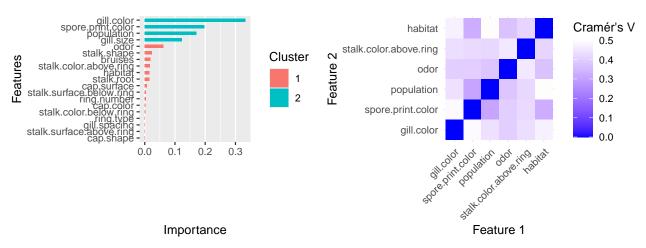


Figure 1: Feature importance by Xtreme Gradient Boosting training and a heatmap of Cramer's V statistic for the features selected by xgboost.

2 Methodology

The 22 categorical features are transformed into integer factor variables. One feature, veil-type, was removed as it had many NA's (30%) and it had very low importance as determined below. No other features had missing values. The data is split into a training and test set. We use xgboost::xbg.train() to perform feature selection on the training data and subset in accordance with the results (Figure 1). The sub-setted training data is checked for collinearity via Cramer's V statistic. The top 10 most important features were cross referenced with the Cramers V statistic and features greater than a threshold of 0.5 were removed (Figure 1).

We used silence::isolationForests to detect outliers in the data. It provides a score for each data point indicating how anomalous it is. We classify a point as analomous if it has a score > 0.99. This resulted in 48 potential outliers. This high dimensional data is vizualized using Uniform Manifold Approximation and Projection (UMAP) via umap::umap (Figure 2). None of the analomous points appear outside the main cluster so none were excluded.

In total there are 6 features and 8124 observations.

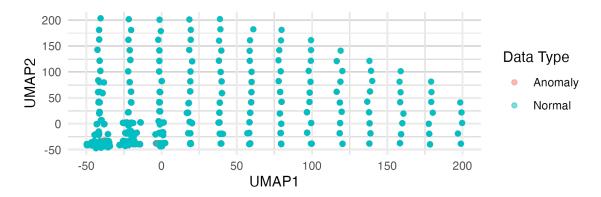


Figure 2: Low dimensional approximation of data by UMAP and classified according to anomalousness via isolation forests.

3 Data Splitting

The data was split into training and test data using random sampling in a (70/30) split. It was done before pre-processing to ensure there was no data leakage. This resulted in 5686 training observations and 2438 test observations.

4 Model Fitting

KNN does not work for categorical features using the euclidean distance metric because it does not make sense to take the distance of integer valued categories when the ordinal ranking has no meaning. This can be overcome in two steps. First the data is one-hot encoded to create numeric valued features. This means each level of each feature is transformed into a binary variable. Then the jaccard metric is used instead of the euclidean metric. It is defined as the distance between two sets, A and B as

$$D_J(A,B) = 1 - \frac{|A \cap B|}{|A \cup B|}.$$

This custom distance function is specified using kknn:train.kknn. This function automatically performs cross-validation for the the number of neighbors k.

kNN is a non-parametric algorithm, meaning that it is based on the entire data and not parameters estimated from the data. The observation of each observation is determined by its "neighbors" and therefore all features play a role. The model does not rank them. On the other hand we can see from (Figure 1) that xgboost ranks gill.color as the most important feature.

Logistic regression is a parametric method and we can compare magnitude of estimated coefficients with the corresponding statistical significance. Prioritizing magnitude population is the most important feature and prioritizing statistical significance gill.color is the most important feature. Both are easily observable traits of a mushroom for an expert picking them. Since gill.color is the most important in both methods we can look at its interpretation as follows. The coefficient for gill.color is -0.388. This means that for a one-unit increase in gill.color, the log odds of the dependent variable occurring decrease by 0.3884028 units, holding all else constant. The odds ratio for gill.color would be $e^{-0.388}$, which is less than 1. This implies that as gill.color increases by one unit, the odds of the event (edible) occurring decrease.

5 Model Analysis and Comparison

Table 1: Classification Comparison

Metric	First Classifier	knn Classifier
Accuracy	0.8404	1.0000
Kappa	0.6761	1.0000
Pos Pred Value (Class 0)	0.7899	1.0000
Neg Pred Value (Class 0)	0.9282	1.0000

There is distinct performance differences between the two classifiers. The first classifier achieves an accuracy of 0.8404 with a κ statistic of 0.6761, indicating moderate agreement beyond chance. At the computed threshold of 0.6901, the specificity of the model is approximately 0.9502, meaning that it correctly identifies about 95.02% of the negative instances as negative. At the same threshold, the sensitivity of the model is approximately 0.7179, meaning that it correctly identifies about 71.79% of the positive instances as positive. The classifier thus performs relatively well, but there's a notable trade-off between sensitivity and specificity. Conversely, the knn classifier achieves a perfect accuracy of 1 with a κ of 1 signifying total agreement. Its sensitivity and specificity are both 1, implying no errors in classification.

6 Logistic Regression with Shrinkage

The best shrinkage value is $\lambda = 8.3 \times 10^{-4}$. Without shrinkage every coefficient in the data set will get a coefficient. With lasso shrinkage some coefficients get shrunk to zero by penalizing the coefficients. The accuracy of the lasso model is 81.16%, which is less than without shrinkage.

7 Conclusion

kNN is able to predict whether a mushroom is edible or not based off of six easily observable characteristics with 100% accuracy. It is a more flexible algorithm as it makes no assumptions about the functional form of the decision boundary, instead it uses local information based on the nearest data points in the feature space. On the other hand logistic regression is a global method and finds a single boundary to separate classes. Since we carefully pre-processed the data to include only the most important features, it enabled us to take advantage of the flexibility of kNN by avoiding the curse of dimensionality.

8 Supplemntary Material

```
# Packages
knitr::opts_chunk$set(echo = TRUE)
require(tidyverse)
library(patchwork)
library(vcd)
library(reshape2)
library(xgboost)
library(solitude)
library(umap)
library(caret)
library(proxy)
library(class)
library(pROC)
library(knitr)
library(glmnet)
# Data tidying
set.seed(123)
data <- read.csv("agaricus-lepiota.data", header = FALSE)</pre>
#Missing colnames
column_names <- c("poisonous","cap-shape", "cap-surface", "cap-color",</pre>
                  "bruises", "odor",
                  "gill-attachment", "gill-spacing", "gill-size", "gill-color",
                  "stalk-shape", "stalk-root", "stalk-surface-above-ring",
                  "stalk-surface-below-ring", "stalk-color-above-ring",
                  "stalk-color-below-ring", "veil-type", "veil-color",
                   "ring-number", "ring-type", "spore-print-color", "population",
                   "habitat")
# Assign these names to dataframe
```

```
colnames(data) <- column_names</pre>
# Remove variable with NA's
data <- data %>% select(-`veil-type`)
# Make features into factor variables
data_numeric <- as.data.frame(lapply(data,</pre>
                 function(x) as.numeric(as.factor(x))))
train_indices <- sample(1:nrow(data_numeric), nrow(data_numeric)*0.7)</pre>
train_data <- data_numeric[train_indices, ]</pre>
test_data <- data_numeric[-train_indices, ]</pre>
train_labels <- train_data$poisonous - 1</pre>
test_labels <- test_data$poisonous - 1</pre>
# Remove the label from train_data and test_data
train_data <- train_data[, -which(names(train_data) == "poisonous")]</pre>
test_data <- test_data[, -which(names(test_data) == "poisonous")]</pre>
#Feature Selection
model <- xgboost(data = as.matrix(train_data),</pre>
                  label = train_labels,
                  nrounds = 100,
                  objective = "binary:logistic",
                  verbose = 0)
importance <- xgb.importance(feature_names = colnames(train_data),</pre>
                               model = model)
top_features <- importance %>%
                 filter(Feature != "gill.size") %>%
                 filter(Feature %in% c("gill.color", "spore.print.color",
                                         "population", "odor",
                          "stalk.color.above.ring", "habitat"))
top_features <- top_features$Feature</pre>
```

```
print(top_features)
## [1] "gill.color"
                                  "spore.print.color"
                                                             "population"
## [4] "odor"
                                  "stalk.color.above.ring" "habitat"
p1 <- xgb.ggplot.importance(importance) + ggplot2::labs(title = NULL)</pre>
# Applying feature selection
train_data_selected <- train_data %>%
  select(all_of(top_features))
test_data_selected <- test_data %>%
  select(all_of(top_features))
#Correlation Analysis
  # Remove predictor
  data2 <- train_data %>%
          select(all_of(importance$Feature[1:10]))
  # Create an empty matrix to store Cramers V values
  n <- ncol(data2)</pre>
  cramer_matrix <- matrix(0, n, n)</pre>
  colnames(cramer_matrix) <- colnames(data2)</pre>
  rownames(cramer_matrix) <- colnames(data2)</pre>
  # Loop through all pairs of variables
  for (i in 1:n) {
    for (j in 1:n) {
      # Skip the diagonal (variable with itself)
      if (i != j) {
        table_data <- table(data2[, i], data2[, j])</pre>
        cramers_v <- assocstats(table_data)$cramer</pre>
        cramer_matrix[i, j] <- cramers_v</pre>
      }
    }
```

```
}
 # Melt the matrix for ggplot2
 melted_matrix <- melt(cramer_matrix)</pre>
 p2 <- ggplot(melted_matrix, aes(Var1, Var2, fill=value)) +
   geom_tile() +
   scale fill gradient2(low="blue", mid="white", high="red", midpoint=0.5) +
   theme_minimal() +
   labs(title= NULL, x="Feature 1", y="Feature 2",
         fill="Cramér's V") +
   theme(axis.text.x = element_text(angle = 45, hjust = 1))
# Define function to extract pairs of features that exceed threshold in
 # cramer matrix
 extract_high_assoc <- function(cramer_matrix, threshold) {</pre>
    # Obtain indices where Cramer's V exceeds threshold
   high_assoc_ind <- which(cramer_matrix > threshold, arr.ind = TRUE)
   # Convert matrix indices to column names
   high_assoc_pairs <- apply(high_assoc_ind, 1, function(idx) {</pre>
      c(rownames(cramer_matrix)[idx[1]], colnames(cramer_matrix)[idx[2]])
   })
    # Remove duplicated pairs and self-associations (pair[1] == pair[2])
 high_assoc_pairs <- unique(t(high_assoc_pairs))</pre>
 high_assoc_pairs <- high_assoc_pairs[high_assoc_pairs[,1] !=
                                          high_assoc_pairs[,2], ]
    # Convert matrix to list of pairs
    #pair_list <- apply(high_assoc_pairs,1, function(pair) {</pre>
    # list(pair[1], pair[2])
    #})
```

```
# return(pair_list)
high_associations_df <- as.data.frame(high_assoc_pairs)
colnames(high_associations_df) <- c("Feature_1", "Feature_2")
rownames(high_associations_df) <- NULL
return(high_associations_df)
}
threshold_value = 0.5
high_associations <- extract_high_assoc(cramer_matrix, threshold_value)
print(high_associations)</pre>
```

##		Feature_1	Feature_2
##	1	gill.size	gill.color
##	2	stalk.shape	gill.color
##	3	bruises	gill.color
##	4	stalk.root	gill.color
##	5	gill.size	spore.print.color
##	6	bruises	spore.print.color
##	7	stalk.root	spore.print.color
##	8	gill.size	population
##	9	habitat	population
##	10	stalk.root	population
##	11	gill.color	gill.size
##	12	spore.print.color	gill.size
##	13	population	gill.size
##	14	odor	gill.size
##	15	habitat	gill.size
##	16	stalk.root	gill.size
##	17	gill.size	odor
##	18	stalk.shape	odor
##	19	bruises	odor
##	20	stalk.root	odor
##	21	gill.color	stalk.shape
##	22	odor	stalk.shape
##	23	stalk.color.above.ring	stalk.shape

```
## 25
           spore.print.color
                                              bruises
## 26
                                              bruises
                         odor
                      habitat
                                              bruises
## 27
## 28
                   stalk.root
                                              bruises
                  stalk.shape stalk.color.above.ring
## 29
## 30
                                              habitat
                   population
## 31
                                              habitat
                    gill.size
## 32
                      bruises
                                              habitat
## 33
                   stalk.root
                                              habitat
## 34
                   gill.color
                                           stalk.root
           spore.print.color
## 35
                                           stalk.root
## 36
                   population
                                           stalk.root
## 37
                    gill.size
                                           stalk.root
## 38
                         odor
                                           stalk.root
## 39
                      bruises
                                           stalk.root
## 40
                      habitat
                                           stalk.root
# Train Isolation Forest on training data
iso_forest <- isolationForest$new()</pre>
iso_forest$fit(train_data_selected)
         [19:36:50.013] dataset has duplicated rows
## INFO
        [19:36:50.025] Building Isolation Forest ...
## INFO [19:36:50.053] done
## INFO
        [19:36:50.053] Computing depth of terminal nodes ...
## INFO
        [19:36:50.145] done
         [19:36:50.199] Completed growing isolation forest
## INFO
scores.iso_train <- iso_forest$predict(train_data_selected)</pre>
scores.iso_test <- iso_forest$predict(test_data_selected)</pre>
train_scores <- scores.iso_train$anomaly_score</pre>
threshold <- quantile(train_scores, 0.99)</pre>
anomalies <- which(train_scores > threshold)
print(anomalies)
```

bruises

24

gill.color

[1] 175 317 337 386 423 555 557 577 846 882 1104 1150 1180 1194 1252 ## [16] 1359 1492 1701 2116 2193 2582 2604 2622 2639 2702 2825 2970 3145 3434 3507

```
## [31] 3590 3597 3648 3959 4368 4517 4553 4599 4634 4651 4695 4717 4819 4932 4986
## [46] 5011 5602 5673
```

```
# UMAP transformation on training data
umap_model_train <- umap(train_data_selected, n_neighbors = 5, min.dist = 0.01)</pre>
umap data <- as.data.frame(umap model train$layout)</pre>
colnames(umap_data) <- c("UMAP1", "UMAP2")</pre>
umap_data$is_anomaly <- ifelse(rownames(umap_data) %in% anomalies,</pre>
                                 "Anomaly", "Normal")
p3 <- ggplot(umap_data, aes(x = UMAP1, y = UMAP2, color = is_anomaly)) +
  geom_point(alpha = 0.5) +
  theme_minimal() +
  labs(title = NULL, color = "Data Type")
# have to save file as islationForest messages cant be turned off
ggsave(filename = "umap.png", plot = p3, width = 6, height = 2)
# One hot encode features
dummy_train <- dummyVars(" ~ .", data= train_data_selected)</pre>
dummy_test <- dummyVars(" ~ .", data= test_data_selected)</pre>
onehot_train <- data.frame(predict(dummy_train, newdata =train_data_selected))</pre>
onehot_test <- data.frame(predict(dummy_test, newdata =test_data_selected))</pre>
# Fit kNN
\# Define jaccard function
jaccard_dist <- function(a, b) {</pre>
    intersection = sum(a & b)
    union = sum(a | b)
    if (union == 0) return (0) # to avoid division by zero
    return (1 - intersection/union)
}
knn_model_jaccard <- kknn::train.kknn(formula = train_labels ~ .,</pre>
                                        data = data.frame(onehot_train,
```

```
train_labels = train_labels),
                                        kmax = 21,
                                        distance = 1,
                                        kernel = "optimal",
                                        scale = FALSE,
                                        customDist = jaccard_dist)
knn_predictions <- predict(knn_model_jaccard, newdata = onehot_test)</pre>
knn_predictions <- factor(knn_predictions, levels = c(0, 1))</pre>
test_labels <- factor(test_labels, levels = c(0, 1))</pre>
knn_conf_matrix <- confusionMatrix(knn_predictions, test_labels)</pre>
print(knn_conf_matrix)
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction
            0 1286
##
                       0
                 0 1152
##
            1
##
                   Accuracy: 1
##
                     95% CI : (0.9985, 1)
##
       No Information Rate: 0.5275
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                      Kappa: 1
##
   Mcnemar's Test P-Value : NA
##
##
##
               Sensitivity: 1.0000
##
               Specificity: 1.0000
            Pos Pred Value : 1.0000
##
##
            Neg Pred Value : 1.0000
                Prevalence: 0.5275
##
```

```
Detection Rate: 0.5275
##
##
      Detection Prevalence: 0.5275
##
         Balanced Accuracy: 1.0000
##
          'Positive' Class : 0
##
##
# Fit log model
# Convert features to factors
train_labels <- as.factor(train_labels)</pre>
test_labels <- as.factor(test_labels)</pre>
logistic_model <- train(onehot_train, train_labels,</pre>
                         method = "glm",
                         family = "binomial",
                         trControl = trainControl(method = "cv", number = 5),
                         metric = "Accuracy")
log_predictions <- predict(logistic_model, newdata = onehot_test)</pre>
log_conf_matrix <- confusionMatrix(log_predictions, test_labels)</pre>
# For kNN with Jaccard
knn_misclass_error <- 1 - knn_conf_matrix$overall['Accuracy']</pre>
print(knn_misclass_error)
## Accuracy
##
# For Logistic Regression
log_conf_matrix <- confusionMatrix(log_predictions, test_labels)</pre>
logistic_misclass_error <- 1 - log_conf_matrix$overall['Accuracy']</pre>
print(logistic_misclass_error)
## Accuracy
## 0.1837572
# Get predicted probabilities for the positive class
logistic_probs <- predict(logistic_model, newdata = onehot_test,</pre>
```

```
type = "prob")$`1`
# Compute ROC curve
roc_obj <- suppressMessages(roc(test_labels, logistic_probs))</pre>
# Find optimal cutoff using Youden's Index
cutoff <- coords(roc_obj, "best")</pre>
print(cutoff)
     threshold specificity sensitivity
##
## 1 0.6900856
                0.9502333
                              0.7178819
predicted_probs <- predict(logistic_model, newdata = onehot_test, type = "prob")</pre>
predicted_labels <- ifelse(predicted_probs[,2] >= cutoff$threshold, 1, 0)
predicted_labels <- factor(predicted_labels, levels = c(0, 1))</pre>
conf_matrix <- confusionMatrix(predicted_labels, test_labels)</pre>
print(conf_matrix)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                 0
##
            0 1222 325
                64 827
##
##
                   Accuracy : 0.8404
##
                     95% CI: (0.8253, 0.8548)
##
       No Information Rate: 0.5275
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                      Kappa : 0.6761
##
    Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.9502
##
##
               Specificity: 0.7179
```

```
Pos Pred Value: 0.7899
##
##
             Neg Pred Value: 0.9282
##
                 Prevalence: 0.5275
            Detection Rate: 0.5012
##
##
      Detection Prevalence: 0.6345
         Balanced Accuracy: 0.8341
##
##
           'Positive' Class : 0
##
##
X_train <- as.matrix(train_data_selected)</pre>
y_train <- train_labels</pre>
cv.lasso <- cv.glmnet(X_train, y_train, family="binomial", alpha=1)</pre>
best_lambda <- cv.lasso$lambda.min</pre>
print(best_lambda)
## [1] 0.0008328795
X_test <- as.matrix(test_data_selected)</pre>
y_test <- test_labels</pre>
# Predict on the test set using the best lambda
lasso_probs <- predict(cv.lasso, s = best_lambda, newx = X_test,</pre>
                        type = "response")
# Convert probabilities to binary predictions
lasso_preds <- ifelse(lasso_probs > 0.5, 1, 0)
# Measure performance
accuracy_lasso <- mean(lasso_preds == y_test)</pre>
print(accuracy_lasso)
```

[1] 0.8162428

References

 $Mushroom.\ UCI\ Machine\ Learning\ Repository,\ 1987.\ DOI:\ https://doi.org/10.24432/C5959T.$