

```
In[37]:= eq = {
  m (x0''[t] + R (θ'[t] Cos[θ[t]] - θ'[t]^2 Sin[θ[t]])) ==
    -f2[t] Cos[θ[t]] + Fn2[t] Sin[θ[t]],
  m R (-θ''[t] Sin[θ[t]] - θ'[t]^2 Cos[θ[t]]) == f2[t] Sin[θ[t]] + Fn2[t] Cos[θ[t]] - m g,
  f2[t] - f1[t] ==  $\frac{x0''[t]}{R^2} i$ ,
  f1[t] + f2[t] Cos[θ[t]] + Fn2[t] Sin[θ[t]] == m x0''[t]
};
Column[Simplify@eq, Frame → All]
```

```
Out[38]:= 

|                                                                                                                                                                 |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $\text{Cos}[\theta[t]] f2[t] + m (-R \text{Sin}[\theta[t]] \theta'[t]^2 + x0''[t] + R \text{Cos}[\theta[t]] \theta'[t]) == \text{Fn2}[t] \text{Sin}[\theta[t]]$ |
| $g m == \text{Cos}[\theta[t]] \text{Fn2}[t] + f2[t] \text{Sin}[\theta[t]] + m R \text{Cos}[\theta[t]] \theta'[t]^2 + m R \text{Sin}[\theta[t]] \theta'[t]$      |
| $f2[t] == f1[t] + \frac{i x0''[t]}{R^2}$                                                                                                                        |
| $f1[t] + \text{Cos}[\theta[t]] f2[t] + \text{Fn2}[t] \text{Sin}[\theta[t]] == m x0''[t]$                                                                        |


```

## Solve the system

### Solve for $x0''[t]$

```
In[33]:= x0ppsol = First@Simplify@Solve[eq[[3]], x0''[t]]
```

```
Out[33]:=  $\left\{ x0''[t] \rightarrow -\frac{R^2 (f1[t] - f2[t])}{i} \right\}$ 
```

```
In[23]:= Column[eqs2 = Simplify[eq /. x0ppsol], Frame → All]
```

```
Out[23]:= 

|                                                                                                                                                                                       |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $\text{Cos}[\theta[t]] f2[t] == \text{Fn2}[t] \text{Sin}[\theta[t]] + \frac{m R (R f1[t] - R f2[t] + i \text{Sin}[\theta[t]] \theta'[t]^2 - i \text{Cos}[\theta[t]] \theta''[t])}{i}$ |
| $g m == \text{Cos}[\theta[t]] \text{Fn2}[t] + f2[t] \text{Sin}[\theta[t]] + m R \text{Cos}[\theta[t]] \theta'[t]^2 + m R \text{Sin}[\theta[t]] \theta''[t]$                           |
| True                                                                                                                                                                                  |
| $f1[t] + \frac{m R^2 (f1[t] - f2[t])}{i} + \text{Cos}[\theta[t]] f2[t] + \text{Fn2}[t] \text{Sin}[\theta[t]] == 0$                                                                    |


```

### Solve for $\theta''[t]$

```
In[32]:= θppsol = First@Simplify@Solve[eqs2[[1]], θ''[t]]
```

```
Out[32]:=  $\left\{ \theta''[t] \rightarrow \frac{m R^2 f1[t] \text{Sec}[\theta[t]] - f2[t] (i + m R^2 \text{Sec}[\theta[t]]) + i \text{Tan}[\theta[t]] (\text{Fn2}[t] + m R \theta'[t]^2)}{i m R} \right\}$ 
```

In[25]:= **Column[eqs3 = Simplify[eqs2 /. eppsol], Frame → All]**

	True
Out[25]=	$g m == \frac{\text{Sec}[\theta[t]] \left( i \text{Fn2}[t] + m R \left( R f1[t] \text{Sin}[\theta[t]] - R f2[t] \text{Sin}[\theta[t]] + i \theta'[t]^2 \right) \right)}{i}$
	True
	$f1[t] + \frac{m R^2 (f1[t] - f2[t])}{i} + \text{Cos}[\theta[t]] f2[t] + \text{Fn2}[t] \text{Sin}[\theta[t]] == 0$

## Solve for f1[t]

In[31]:= **f1sol = First@Simplify@Solve[eqs2[[4]], f1[t]]**

Out[31]= 
$$\left\{ f1[t] \rightarrow \frac{m R^2 f2[t] - i \text{Cos}[\theta[t]] f2[t] - i \text{Fn2}[t] \text{Sin}[\theta[t]]}{i + m R^2} \right\}$$

In[28]:= **Column[eqs4 = Simplify[eqs3 /. f1sol], Frame → All]**

	True
Out[28]=	$g m == \text{Sec}[\theta[t]] \left( \text{Fn2}[t] + \frac{m R \left( -R (1 + \text{Cos}[\theta[t]]) f2[t] \text{Sin}[\theta[t]] - R \text{Fn2}[t] \text{Sin}[\theta[t]]^2 + (i + m R^2) \theta'[t]^2 \right)}{i + m R^2} \right)$
	True
	True

## Solve for Fn2[t]

In[30]:= **Fn2sol = First@Simplify@Solve[eqs4[[2]], Fn2[t]]**

Out[30]= 
$$\left\{ \text{Fn2}[t] \rightarrow \frac{m \left( R^2 f2[t] (2 \text{Sin}[\theta[t]] + \text{Sin}[2 \theta[t]]) + 2 (i + m R^2) (g \text{Cos}[\theta[t]] - R \theta'[t]^2) \right)}{2 i + m R^2 + m R^2 \text{Cos}[2 \theta[t]]} \right\}$$

In[39]:= **SetDirectory[NotebookDirectory[]]**

**Export["Explicitly solving for Matlab.pdf", EvaluationNotebook[]]**

Out[39]= /home/eric/Documents/School/QEA2/Module 3/QEA-BB8/v2