

```
In[1]:= eq = {
  m (x0''[t] + R (θ'[t] Cos[θ[t]] - θ'[t]^2 Sin[θ[t]])) ==
    -f2[t] Cos[θ[t]] + Fn2[t] Sin[θ[t]],
  m R (-θ'[t] Sin[θ[t]] - θ'[t]^2 Cos[θ[t]]) == f2[t] Sin[θ[t]] + Fn2[t] Cos[θ[t]] - m g,
  f2[t] - f1[t] ==  $\frac{x0''[t]}{R^2} i$ ,
  f1[t] + f2[t] Cos[θ[t]] + Fn2[t] Sin[θ[t]] == m x0''[t]
}
```

```
Out[1]= {m (x0''[t] + R (-Sin[θ[t]] θ'[t]^2 + Cos[θ[t]] θ''[t])) == -Cos[θ[t]] f2[t] + Fn2[t] Sin[θ[t]],
  m R (-Cos[θ[t]] θ'[t]^2 - Sin[θ[t]] θ''[t]) == -g m + Cos[θ[t]] Fn2[t] + f2[t] Sin[θ[t]],
  -f1[t] + f2[t] ==  $\frac{i x0''[t]}{R^2}$ , f1[t] + Cos[θ[t]] f2[t] + Fn2[t] Sin[θ[t]] == m x0''[t]}
```

## Solve the system

### Solve for $x0''[t]$

```
In[33]:= x0ppsol = First@Simplify@Solve[eq[[3]], x0''[t]]
```

```
Out[33]= {x0''[t] → - $\frac{R^2 (f1[t] - f2[t])}{i}$ }
```

```
In[23]:= Column[eqs2 = Simplify[eq /. x0ppsol], Frame → All]
```

```
Out[23]= 

|                                                                                                                                                                                       |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $\text{Cos}[\theta[t]] f2[t] == \text{Fn2}[t] \text{Sin}[\theta[t]] + \frac{m R (R f1[t] - R f2[t] + i \text{Sin}[\theta[t]] \theta'[t]^2 - i \text{Cos}[\theta[t]] \theta''[t])}{i}$ |
| $g m == \text{Cos}[\theta[t]] \text{Fn2}[t] + f2[t] \text{Sin}[\theta[t]] + m R \text{Cos}[\theta[t]] \theta'[t]^2 + m R \text{Sin}[\theta[t]] \theta''[t]$                           |
| True                                                                                                                                                                                  |
| $f1[t] + \frac{m R^2 (f1[t] - f2[t])}{i} + \text{Cos}[\theta[t]] f2[t] + \text{Fn2}[t] \text{Sin}[\theta[t]] == 0$                                                                    |


```

### Solve for $\theta''[t]$

```
In[32]:= θppsol = First@Simplify@Solve[eqs2[[1]], θ''[t]]
```

```
Out[32]= {θ''[t] →  $\frac{m R^2 f1[t] \text{Sec}[\theta[t]] - f2[t] (i + m R^2 \text{Sec}[\theta[t]]) + i \text{Tan}[\theta[t]] (\text{Fn2}[t] + m R \theta'[t]^2)}{i m R}$ }
```

```
In[25]:= Column[eqs3 = Simplify[eqs2 /. θppsol], Frame → All]
```

```
Out[25]= 

|                                                                                                                                                   |
|---------------------------------------------------------------------------------------------------------------------------------------------------|
| True                                                                                                                                              |
| $g m == \frac{\text{Sec}[\theta[t]] (i \text{Fn2}[t] + m R (R f1[t] \text{Sin}[\theta[t]] - R f2[t] \text{Sin}[\theta[t]] + i \theta'[t]^2))}{i}$ |
| True                                                                                                                                              |
| $f1[t] + \frac{m R^2 (f1[t] - f2[t])}{i} + \text{Cos}[\theta[t]] f2[t] + \text{Fn2}[t] \text{Sin}[\theta[t]] == 0$                                |


```

## Solve for f1[t]

In[31]:= **f1sol = First@Simplify@Solve[eqs2[[4]], f1[t]]**

Out[31]=  $\left\{ f1[t] \rightarrow \frac{m R^2 f2[t] - i \cos[\theta[t]] f2[t] - i F n2[t] \sin[\theta[t]]}{i + m R^2} \right\}$

In[28]:= **Column[eqs4 = Simplify[eqs3 /. f1sol], Frame → All]**

	True
Out[28]=	$g m == \sec[\theta[t]] \left( F n2[t] + \frac{m R (-R (1 + \cos[\theta[t]]) f2[t] \sin[\theta[t]] - R F n2[t] \sin[\theta[t]]^2 + (i + m R^2) \theta'[t]^2)}{i + m R^2} \right)$
	True
	True

## Solve for Fn2[t]

In[30]:= **F n2sol = First@Simplify@Solve[eqs4[[2]], F n2[t]]**

Out[30]=  $\left\{ F n2[t] \rightarrow \frac{m \left( R^2 f2[t] (2 \sin[\theta[t]] + \sin[2 \theta[t]]) + 2 (i + m R^2) (g \cos[\theta[t]] - R \theta'[t]^2) \right)}{2 i + m R^2 + m R^2 \cos[2 \theta[t]]} \right\}$

In[35]:= **SetDirectory[NotebookDirectory[]]**

**Export["Explicitly solving for Matlab.pdf", EvaluationNotebook[]]**

Out[35]= /home/eric/Documents/School/QEA2/Module 3/QEA-BB8/v2