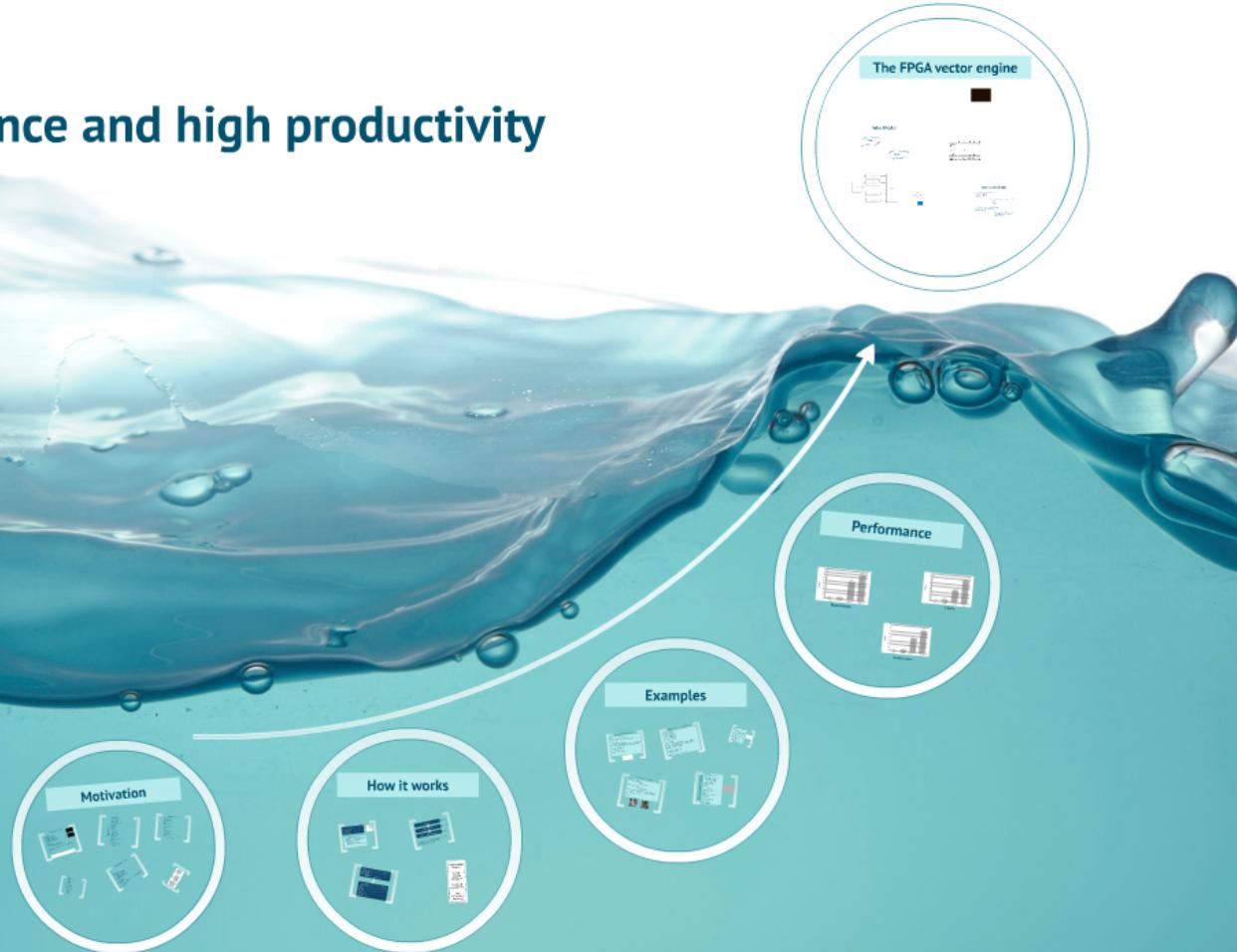


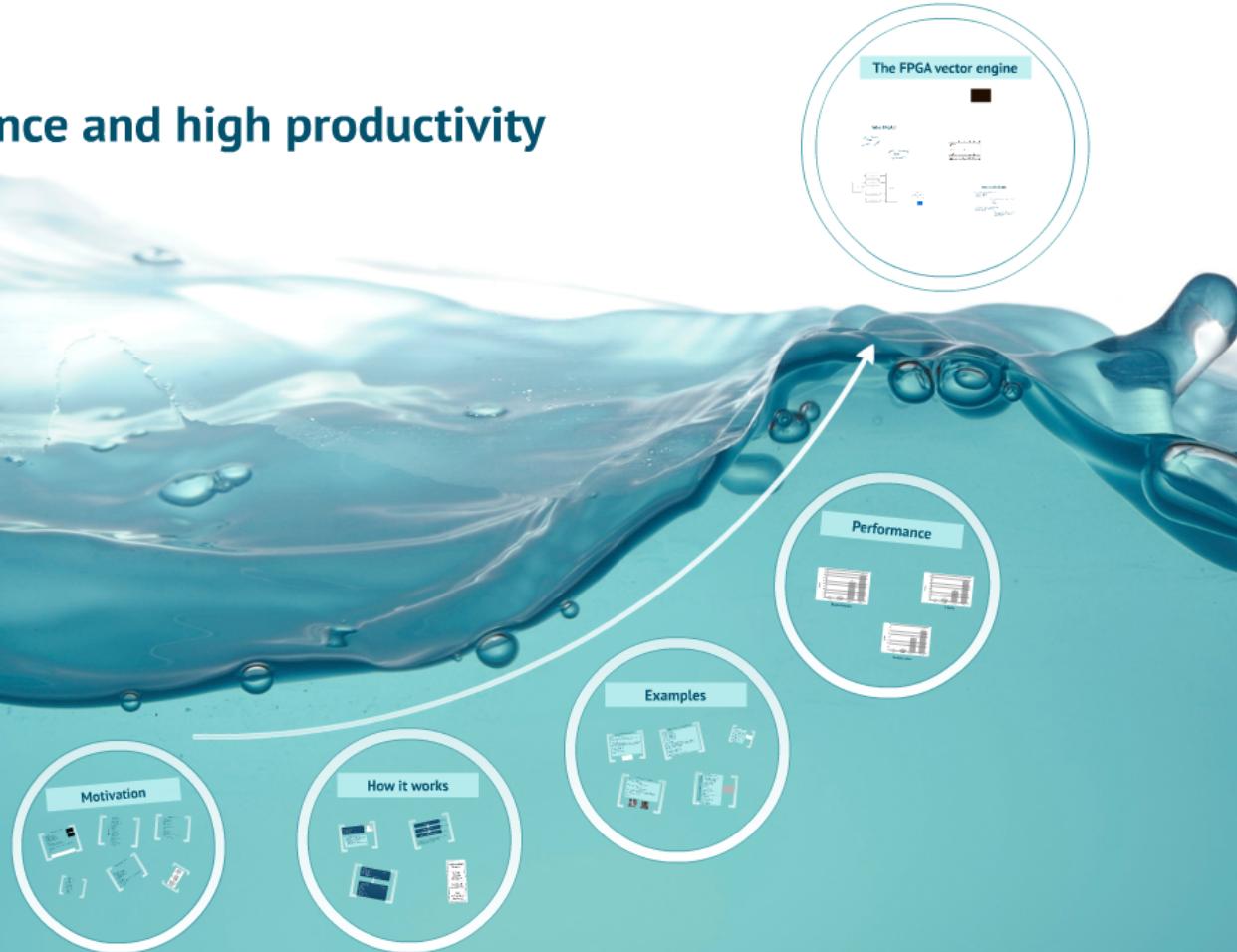
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Motivation

Stencil example in Matlab

- Operators
- Number of iterations
- Initial & Output Matrix
- Temporary array
- SIZE (symmetric Matrix Size)

#Computation

$$I = 2 \times 2 \times 3 \times 3 \text{Center slice vertical}$$
$$J = 1 \times 2 \times 3 \times 3 \text{Center slice horizontal}$$
$$\text{for } m=1:3$$
$$T(I+3, J) = A(I, J) + A(I-1, J) + A(I, J-1) + A(I-1, J-1)$$
$$I = I + 1;$$
$$\text{end}$$

Mat with Operator

```
function [A] = matwithoperator(N)
    % Initialize matrix A
    A = zeros(N);
    % Define operator
    for i = 1:N
        for j = 1:N
            for k = 1:N
                for l = 1:N
                    if (i+j+k+l) == N+1
                        A(i,j,k,l) = 1;
                    end
                end
            end
        end
    end
end
```

Stencil example in C

```
int main()
{
    int i, j, k, l, sum;
    float A[10][10][10][10];
    float T[10][10][10][10];
    for (i = 0; i < 10; i++)
        for (j = 0; j < 10; j++)
            for (k = 0; k < 10; k++)
                for (l = 0; l < 10; l++)
                    A[i][j][k][l] = 0;
    for (i = 0; i < 10; i++)
        for (j = 0; j < 10; j++)
            for (k = 0; k < 10; k++)
                for (l = 0; l < 10; l++)
                    if ((i + j + k + l) == 10)
                        A[i][j][k][l] = 1;
    for (i = 0; i < 10; i++)
        for (j = 0; j < 10; j++)
            for (k = 0; k < 10; k++)
                for (l = 0; l < 10; l++)
                    if ((i + j + k + l) == 10)
                        T[i][j][k][l] = 1;
    for (i = 0; i < 10; i++)
        for (j = 0; j < 10; j++)
            for (k = 0; k < 10; k++)
                for (l = 0; l < 10; l++)
                    if ((i + j + k + l) == 10)
                        sum = A[i][j][k][l] + A[i - 1][j][k][l] + A[i + 1][j][k][l] + A[i][j - 1][k][l] + A[i][j + 1][k][l] + A[i][j][k - 1][l] + A[i][j][k + 1][l];
                        T[i][j][k][l] = sum;
    return 0;
}
```



Stencil example in NumPy

- Operators
- Number of iterations
- Input & Output Matrix
- Temporary array
- SIZE (symmetric Matrix Size)

#Computation

$$I = \text{np.arange}(0, 3)$$
$$J = \text{np.arange}(0, 3)$$
$$T[I+3, J] = A[I, J] + A[I-1, J] + A[I, J-1] + A[I-1, J-1]$$
$$I = I + 1$$

Stencil example in Matlab

#Parameters

I %Number of iterations

A %Input & Output Matrix

T %Temporary array

SIZE %Symmetric Matrix Size



#Computation

i = 2:SIZE+1;%Center slice vertical

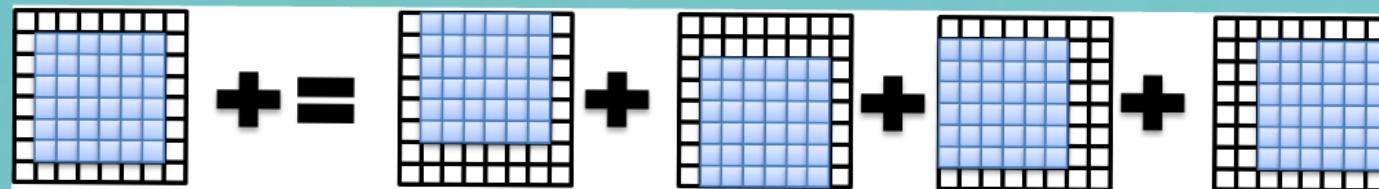
j = 2:SIZE+1;%Center slice horizontal

for n=1:I,

 T(:) = (A(i,j) + A(i+1,j) + A(i-1,j) + A(i,j+1) + A(i,j-1)) / 5.0;

 A(i,j) = T;

end



Stencil example in C

```
//Parameters
int l; //Number of iterations
double *A; //Input & Output Matrix
double *T; //Temporary array
int SIZE; //Symmetric Matrix Size

//Computation
int gsize = SIZE+2; //Size + borders.
for(n=0; n<l; n++)
{
    memcpy(T, A, gsize*gsize*sizeof(double));
    double *a = A;
    double *t = T;
    for(i=0; i<SIZE; ++i)
    {
        double *up    = a+1;
        double *left   = a+gsize;
        double *right  = a+gsize+2;
        double *down   = a+1+gsize*2;
        double *center = t+gsize+1;
        for(j=0; j<SIZE; ++j)
            *center++ = (*center + *up++ + *left++ + *right++ + *down++) / 5.0;
        a += gsize;
        t += gsize;
    }
    memcpy(A, T, gsize*gsize*sizeof(double));
}
```

Stencil example with MPI

```
//Parameters
int l; //Number of iterations
double *A; //Input & Output Matrix (local)
double *T; //Temporary array (local)
int SIZE; //Symmetric Matrix Size (local)

//Computation
int gsize = SIZE+2; //Size + borders.
MPI_Comm_rank(MPI_COMM_WORLD, &myrank);
MPI_Comm_size(MPI_COMM_WORLD, &worldsize);
MPI_Comm comm;
int periods[] = {0};
MPI_Cart_create(MPI_COMM_WORLD, 1, &worldsize,
                periods, 1, &comm);
int L_size = SIZE / worldsize;
if(myrank == worldsize-1)
    L_size += SIZE % worldsize;
int L_gsize = L_size + 2;//Size + borders.
for(n=0; n<l; n++)
{
    int p_src, p_dest;
    //Send/receive - neighbor above
    MPI_Cart_shift(comm,0,1,&p_src,&p_dest);
    MPI_Sendrecv(A+gsize,gsize,MPI_DOUBLE,
                 p_dest,1,A,gsize,MPI_DOUBLE,
                 p_src,1,comm,MPI_STATUS_IGNORE);
    //Send/receive - neighbor below
    MPI_Cart_shift(comm,0,-1,&p_src,&p_dest);
    MPI_Sendrecv(A+(L_gsize-2)*gsize,
                 gsize,MPI_DOUBLE,
                 p_dest,1,A+(L_gsize-1)*gsize,
                 gsize,MPI_DOUBLE,
                 p_src,1,comm,MPI_STATUS_IGNORE);
    memcpy(T, A, L_gsize*gsize*sizeof(double));
    double *a = A;
    double *t = T;
    for(i=0; i<SIZE; ++i)
    {
        int a = i * gsize;
        double *up   = &A[a+1];
        double *left  = &A[a+gsize];
        double *right = &A[a+gsize+2];
        double *down  = &A[a+1+gsize*2];
        double *center = &T[a+gsize+1];
        for(j=0; j<SIZE; ++j)
            *center++ = (*center + *up++ + *left++ + *right++ + *down++) / 5.0;
    }
    MPI_Barrier(MPI_COMM_WORLD);
```

MPI with OpenMP

```
//Parameters
int l; //Number of iterations
double *A; //Input & Output Matrix (local)
double *T; //Temporary array (local)
int SIZE; //Symmetric Matrix Size (local)

//Computation
int gsize = SIZE+2; //Size + borders.
MPI_Comm_rank(MPI_COMM_WORLD, &myrank);
MPI_Comm_size(MPI_COMM_WORLD, &worldsize);
MPI_Comm comm;
int periods[] = {0};
MPI_Cart_create(MPI_COMM_WORLD, 1, &worldsize,
    periods, 1, &comm);
int l_size = SIZE / worldsize;
if(myrank == worldsize-1)
    l_size += SIZE % worldsize;
int l_gsize = l_size + 2;//Size + borders.
for(n=0; n<l; n++)
{
    int p_src, p_dest;
    MPI_Request reqs[4];

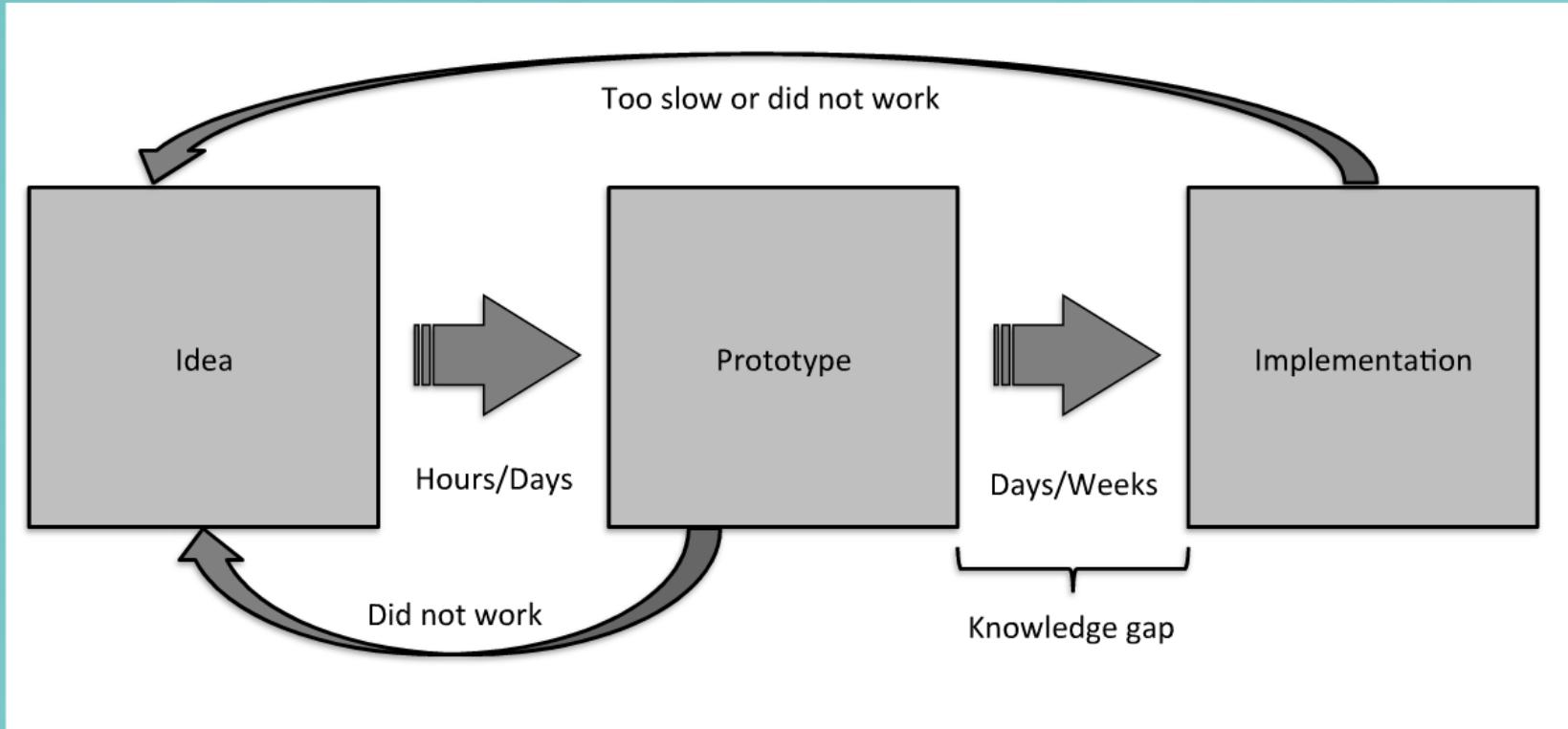
    //Initiate send/receive - neighbor above
    MPI_Cart_shift(comm, 0, 1, &p_src, &p_dest);
    MPI_Isend(A+gsize, gsize, MPI_DOUBLE, p_dest,
        1, comm, &reqs[0]);
    MPI_Irecv(A, gsize, MPI_DOUBLE, p_src,
        1, comm, &reqs[1]);

    //Initiate send/receive - neighbor below
    MPI_Cart_shift(comm, 0, -1, &p_src, &p_dest);
    MPI_Isend(A+(l_gsize-2)*gsize, gsize,
        MPI_DOUBLE,
        p_dest, 1, comm, &reqs[2]);
    MPI_Irecv(A+(l_gsize-1)*gsize, gsize,
        MPI_DOUBLE,
        p_src, 1, comm, &reqs[3]);

    //Handle the non-border elements.
    memcpy(T+gsize, A+gsize, l_size*gsize*sizeof(double));
    #pragma omp parallel for shared(A,T)
    for(i=1; i<l_size-1; ++i)
        compute_row(i,A,T,SIZE,gsize);

    //Handle the upper and lower ghost line
    MPI_Waitall(4, reqs, MPI_STATUSES_IGNORE);
    compute_row(0,A,T,SIZE,gsize);
    compute_row(l_size-1,A,T,SIZE,gsize);

    memcpy(A+gsize, T+gsize, l_size*gsize*sizeof(double));
}
MPI_Barrier(MPI_COMM_WORLD);
```



Stencil example in NumPy

#Parameters

I #Number of iterations
A #Input & Output Matrix
T #Temporary array
SIZE #Symmetric Matrix Size

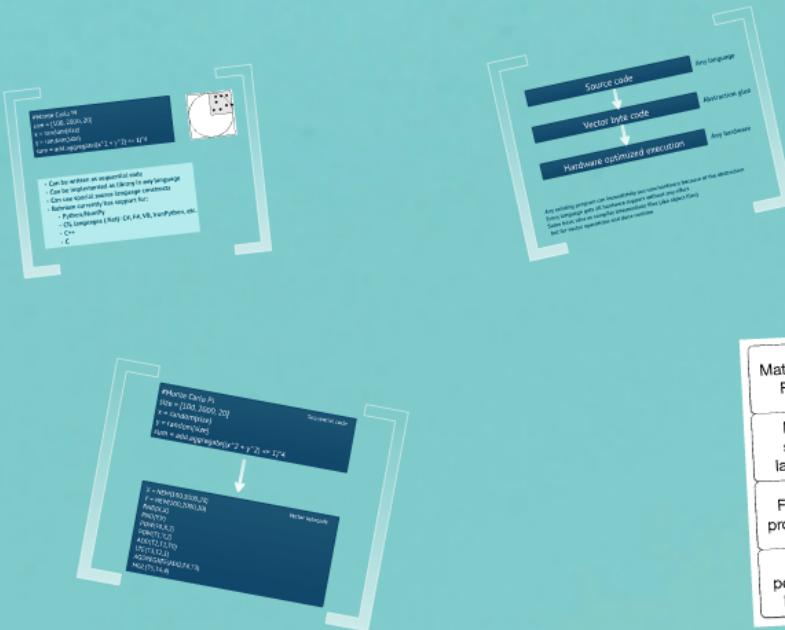
#Computation

for i in xrange(I):

T[:] = (A[1:-1,1:-1] + A[1:-1,:-2] + A[1:-1,2:] + A[:-2,1:-1] \
+ A[2:,1:-1]) / 5.0

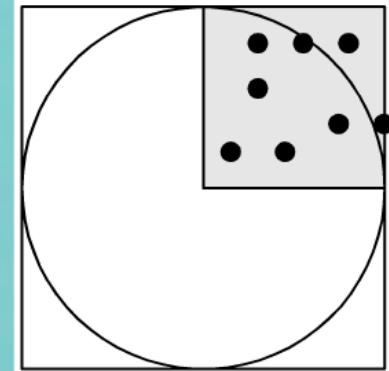
A[1:-1, 1:-1] = T

How it works



Mathematical Finance
Domain specific languages
Functional programming
High performance backends

```
#Monte Carlo PI  
size = [100, 2000, 20]  
x = random(size)  
y = random(size)  
sum = add.aggregate((x^2 + y^2) <= 1)*4
```



- Can be written as sequential code
- Can be implemented as library in any language
- Can use special source language constructs
- Bohrium currently has support for:
 - Python/NumPy
 - CIL languages (.Net): C#, F#, VB, IronPython, etc.
 - C++
 - C

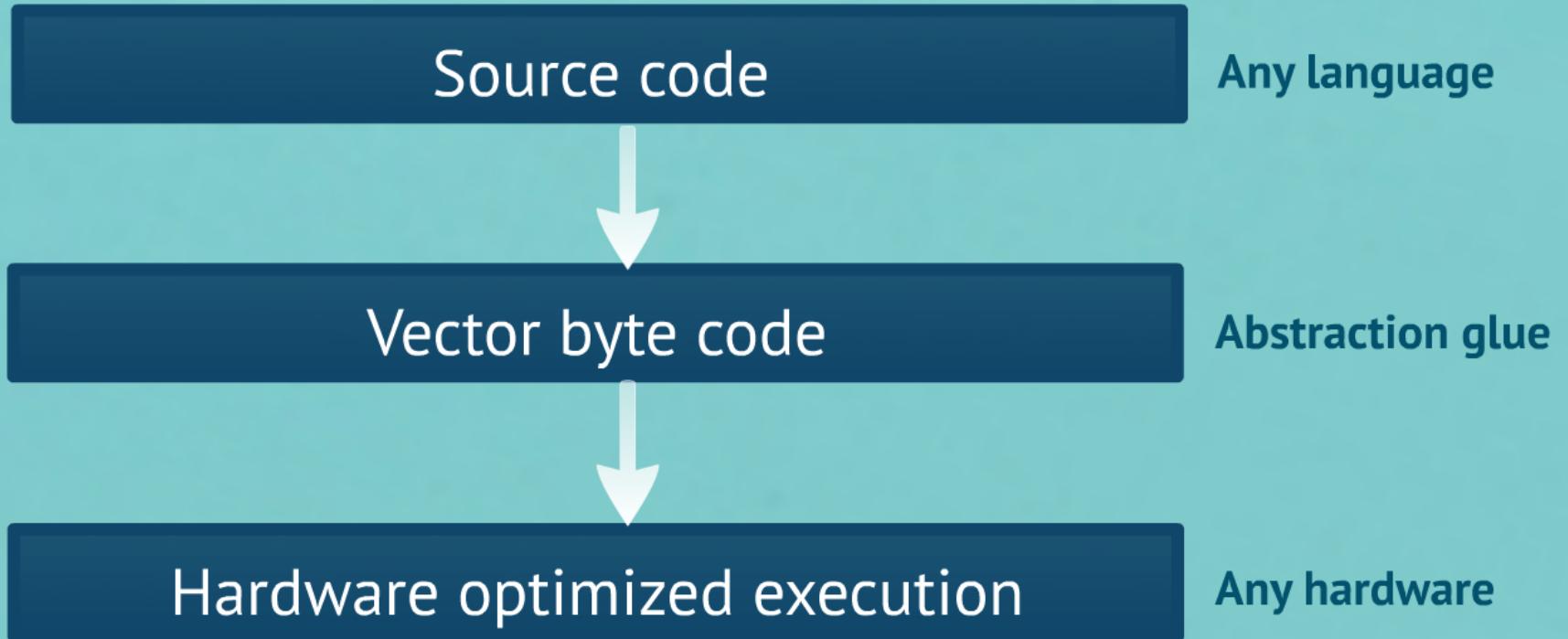
```
#Monte Carlo PI  
size = [100, 2000, 20]  
x = random(size)  
y = random(size)  
sum = add.aggregate((x^2 + y^2) <= 1)*4
```

Sequential code



```
X = NEW(100,2000,20)  
Y = NEW(100,2000,20)  
RND(X,X)  
RND(Y,Y)  
POW(T0,X,2)  
POW(T1,Y,2)  
ADD(T2,T1,T0)  
LTE(T3,T2,1)  
AGGREGATE(ADD,T4,T3)  
MUL(T5,T4,4)
```

Vector bytecode

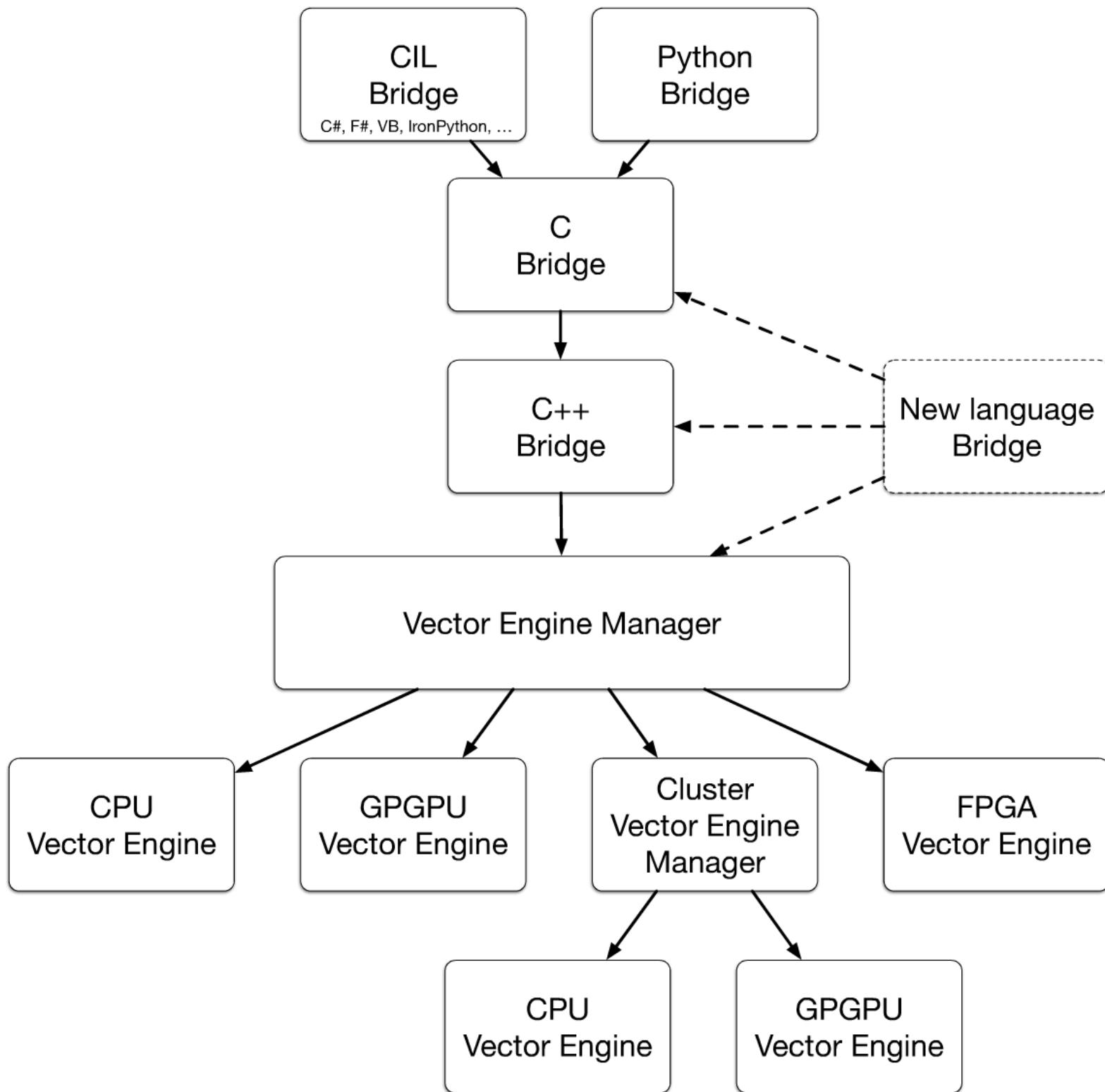


Any existing program can immediately use new hardware because of the abstraction

Every language gets all hardware support without any effort

Same basic idea as compiler intermediate files (aka object files)

but for vector operations and done runtime



Mathematical Finance

Domain
specific
languages

Functional
programming

High
performance
backends



Examples

www.gutenberg.org

```

private static double MatrixChainOrder(int n)
{
    Data a = new Data(1.0, 1.0, 1.0);
    Data b = new Data(1.0, 1.0, 1.0);
    Data c = new Data(1.0, 1.0, 1.0);
    Data d = new Data(1.0, 1.0, 1.0);

    var L = X * AM * B;
    var R = X * A * MB;
    var m = 1.0 / (L + R);
    var S = m * (A * MB + B * AM);
    var P = m * (A * MB * S + B * AM * S);
    var H = 1.0 / (P + S);
    var F = H * (A * MB * S + B * AM * S);
    var G = H * (A * MB * S + B * AM * S);
    var E = H * (A * MB * S + B * AM * S);
    var D = H * (A * MB * S + B * AM * S);
    var C = H * (A * MB * S + B * AM * S);
    var B = H * (A * MB * S + B * AM * S);
    var A = H * (A * MB * S + B * AM * S);
}

```

Implementation of the BlackScholes.cs

Robert Kloss für einige detaillierte

```

def minmax(x,y,z):
    if x < y:
        if y < z:
            return [x,y,z]
        else:
            return [x,z,y]
    else:
        if y < z:
            return [z,y,x]
        else:
            return [z,x,y]

def minmax3(x,y,z,w):
    if x < y:
        if y < z:
            if z < w:
                return [x,y,z,w]
            else:
                return [x,y,w,z]
        else:
            if z < w:
                return [z,y,x,w]
            else:
                return [z,y,w,x]
    else:
        if y < z:
            if z < w:
                return [z,y,x,w]
            else:
                return [z,y,w,x]
        else:
            if z < w:
                return [x,y,z,w]
            else:
                return [x,y,w,z]

```

n-body simulations

C# implementation of BlackScholes core

```
private static NdArray CND(NdArray X)
{
    DATA a1 = 0.31938153f, a2 = -0.356563782f,;
    DATA a3 = 1.781477937f, a4 = -1.821255978f, a5 = 1.330274429f;

    var L = X.Abs();
    var K = 1.0f / (1.0f + 0.2316419f * L);
    var w = 1.0f - 1.0f / ((DATA)Math.Sqrt(2 * Math.PI)) * (-L * L / 2.0f).Exp() * (a1 *
K + a2 * (K.Pow(2)) + a3 * (K.Pow(3)) + a4 * (K.Pow(4)) + a5 * (K.Pow(5)));

    var mask1 = (NdArray)(X < 0);
    var mask2 = (NdArray)(X >= 0);

    w = w * mask2 + (1.0f - w) * mask1;
    return w;
}
```

$$C(S, t) = N(d_1) S - N(d_2) Ke^{-r(T-t)}$$
$$d_1 = \frac{\ln(\frac{S}{K}) + (r + \frac{\sigma^2}{2})(T - t)}{\sigma\sqrt{T - t}}$$
$$d_2 = \frac{\ln(\frac{S}{K}) + (r - \frac{\sigma^2}{2})(T - t)}{\sigma\sqrt{T - t}}$$

F# implementation of the BlackScholes core

```
let CND(X:NdArray) =  
    let a1 = 0.31938153  
    let a2 = -0.356563782  
    let a3 = 1.781477937  
    let a4 = -1.821255978  
    let a5 = 1.330274429  
  
    let L = X.Abs()  
    let K = 1.0 / (1.0 + 0.2316419 * L)  
    let w = 1.0 - 1.0 / ((double(sqrt(2.0 * System.Math.PI)))) * (-L * L /  
        2.0).Exp() * (a1 * K + a2 * (K.Pow(2.0)) + a3 * (K.Pow(3.0)) + a4 *  
        (K.Pow(4.0)) + a5 * (K.Pow(5.0)));  
  
    let mask1 = double(X < 0.0)  
    let mask2 = double(X >= 0.0)  
  
    w * mask2 + (NdArray(1.0) - w) * mask1
```

Sobel filter for edge detection in Python

```
def sobel(input, data_type):
    sobel_window_x = array([[-1, 0, 1],
                           [-2, 0, 2],
                           [-1, 0, 1]]).astype(data_type)

    sobel_window_y = array([[-1, -2, -1],
                           [0, 0, 0],
                           [1, 2, 1]]).astype(data_type)

    sobel_x = convolve2d(input, sobel_window_x, out=None, data_type=data_type)
    sobel_y = convolve2d(input, sobel_window_y, out=None, data_type=data_type)

    result = sqrt(sobel_x**2 + sobel_y**2)

    return result
```



n-body simulation in Python

```
def move(galaxy, dt):
    """Move the bodies
    first find forces and change velocity and then move positions
    """

    n = len(galaxy['x'])
    # Calculate all distances component wise (with sign)
    dx = galaxy['x'][np.newaxis,:,:].T - galaxy['x']
    dy = galaxy['y'][np.newaxis,:,:].T - galaxy['y']
    dz = galaxy['z'][np.newaxis,:,:].T - galaxy['z']

    # Euclidian distances (all bodys)
    r = np.sqrt(dx**2 + dy**2 + dz**2)
    np.diagonal(r)[:] = 1.0

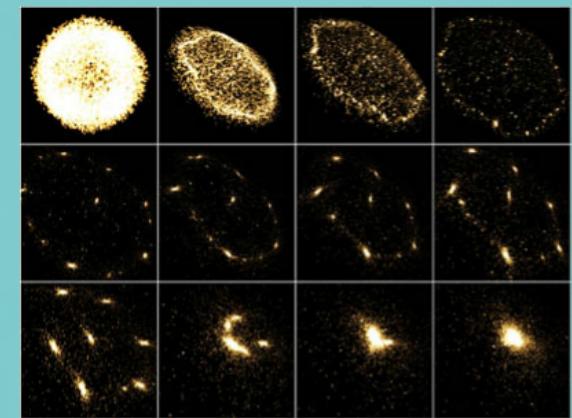
    # prevent collision
    mask = r < 1.0
    r = r * ~mask + 1.0 * mask

    m = galaxy['m'][np.newaxis,:,:].T

    # Calculate the acceleration component wise
    Fx = G*m*dx/r**3
    Fy = G*m*dy/r**3
    Fz = G*m*dz/r**3
    # Set the force (acceleration) a body exerts on it self to zero
    np.diagonal(Fx)[:] = 0.0
    np.diagonal(Fy)[:] = 0.0
    np.diagonal(Fz)[:] = 0.0

    galaxy['vx'] += dt*np.sum(Fx, axis=0)
    galaxy['vy'] += dt*np.sum(Fy, axis=0)
    galaxy['vz'] += dt*np.sum(Fz, axis=0)

    galaxy['x'] += dt*galaxy['vx']
    galaxy['y'] += dt*galaxy['vy']
    galaxy['z'] += dt*galaxy['vz']
```



```

from numpy.lib.stride_tricks import as_strided as ast
import numpy as np
import math

alpha = 0.25 #Input value
epsilon = 0.0001 #Cutoff
raw_data = np.random.random_sample((100000,)) #simulated data

# Determine the window size based on epsilon and alpha
window_size = int(math.ceil(math.log(epsilon) / math.log(1-alpha)))

betas = np.empty(window_size) #Precompute contributions
betas.fill(1-alpha)
rates = np.power(betas, len(betas) - 1 - np.arange(0, len(betas)))
rates[1:] *= alpha

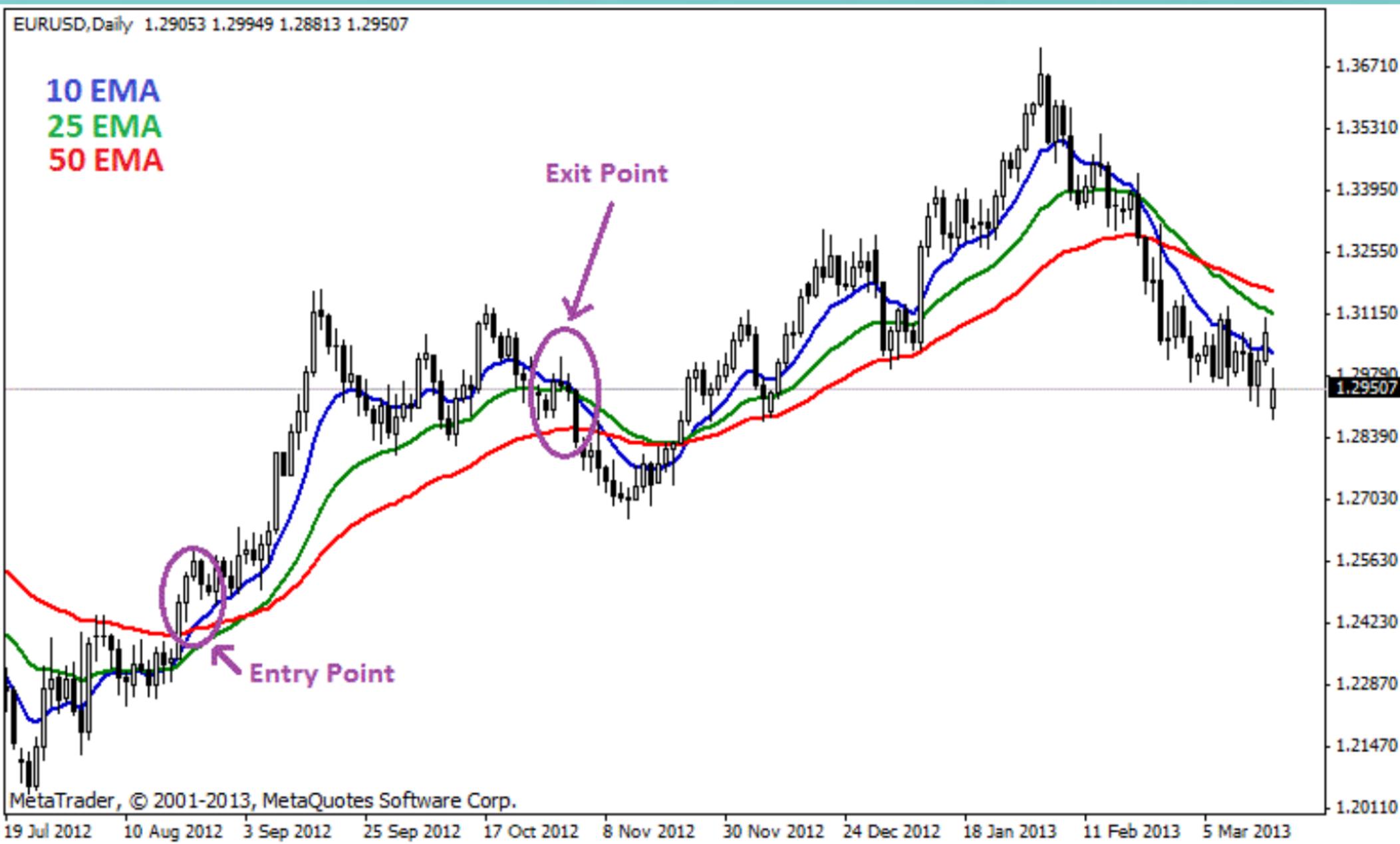
padding = np.empty(window_size - 1) #Produce padding
padding.fill(raw_data[0])
data = np.concatenate((padding, raw_data))

# Transform the data into a set of series
series = ast(data, shape=(len(raw_data), window_size), \
strides=(1*data.itemsize, 1*data.itemsize))

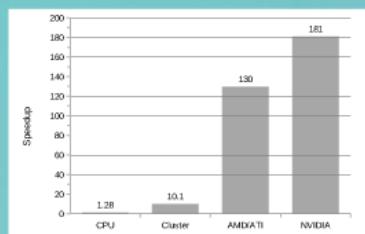
result = np.add.reduce(series * rates, axis=1)

```

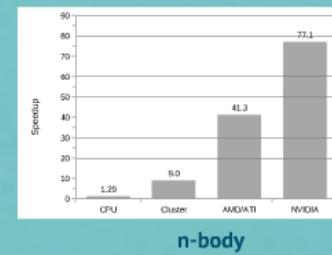




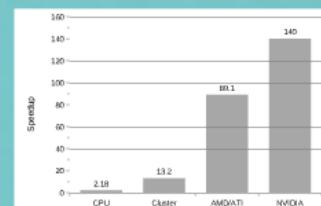
Performance



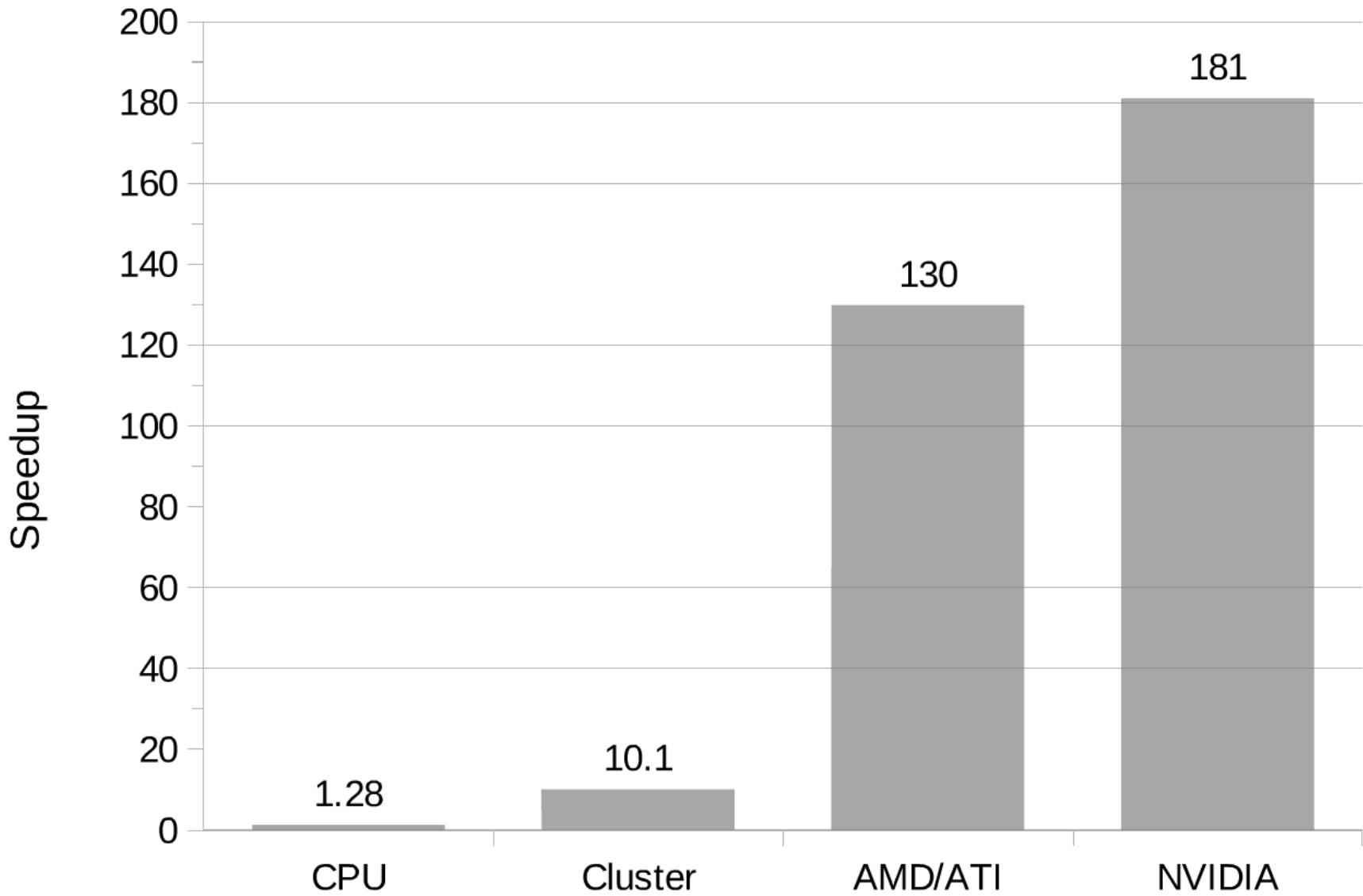
Black-Scholes



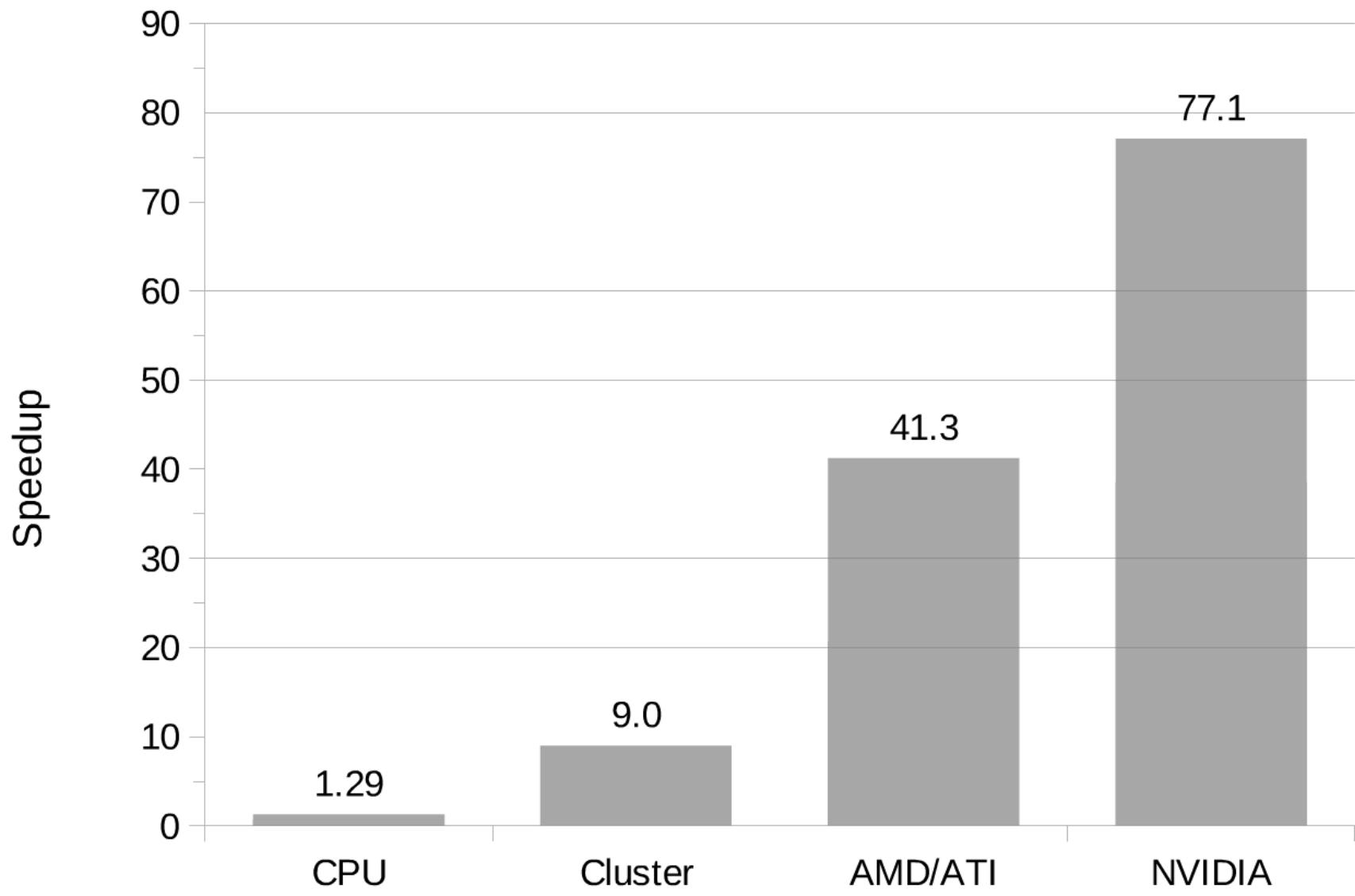
n-body



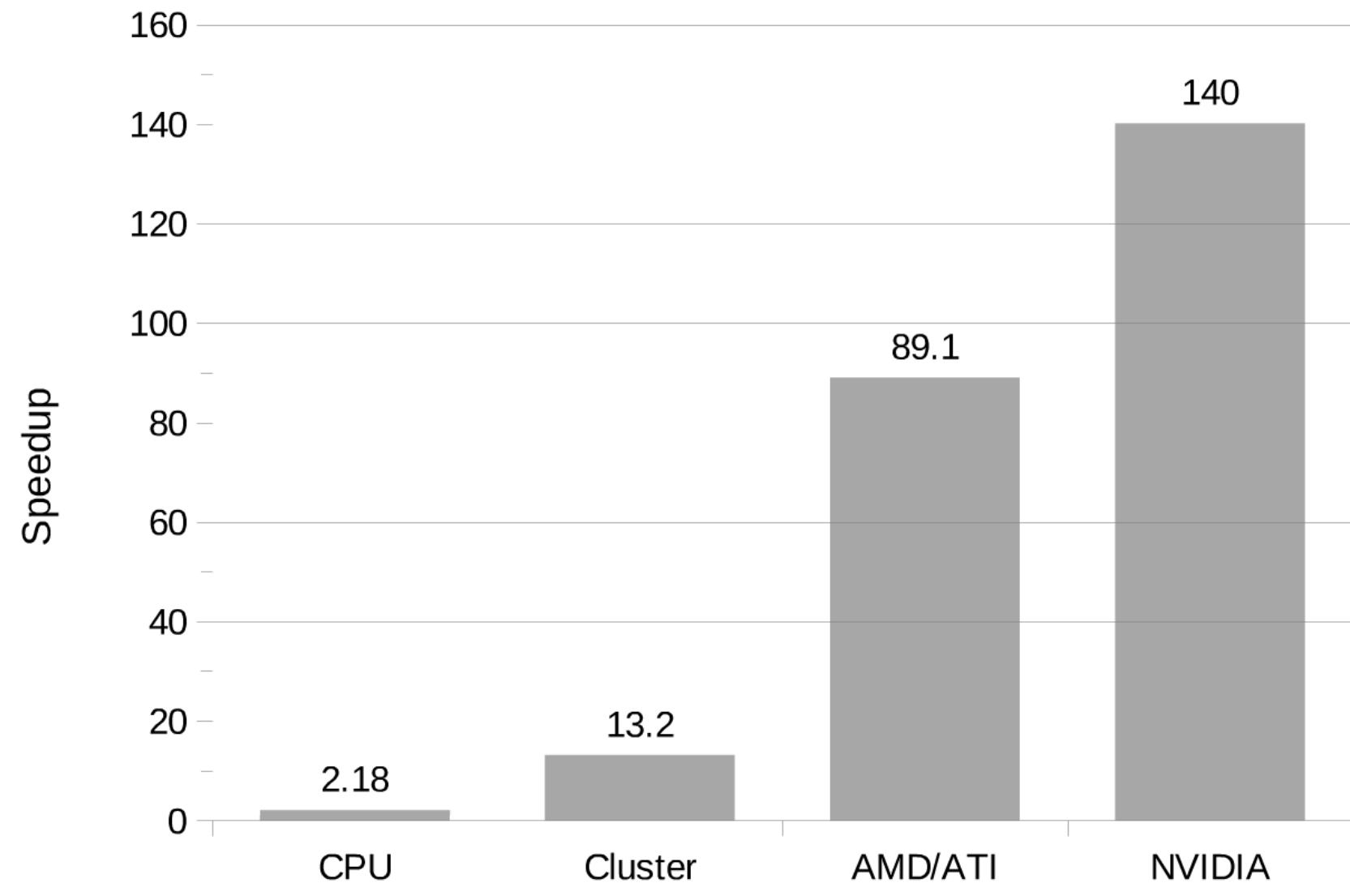
Shallow water



Black-Scholes



n-body

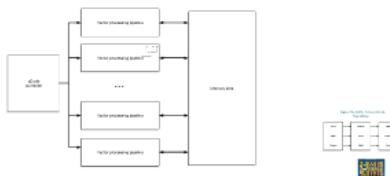


Shallow water

The FPGA vector engine



Why FPGA ?



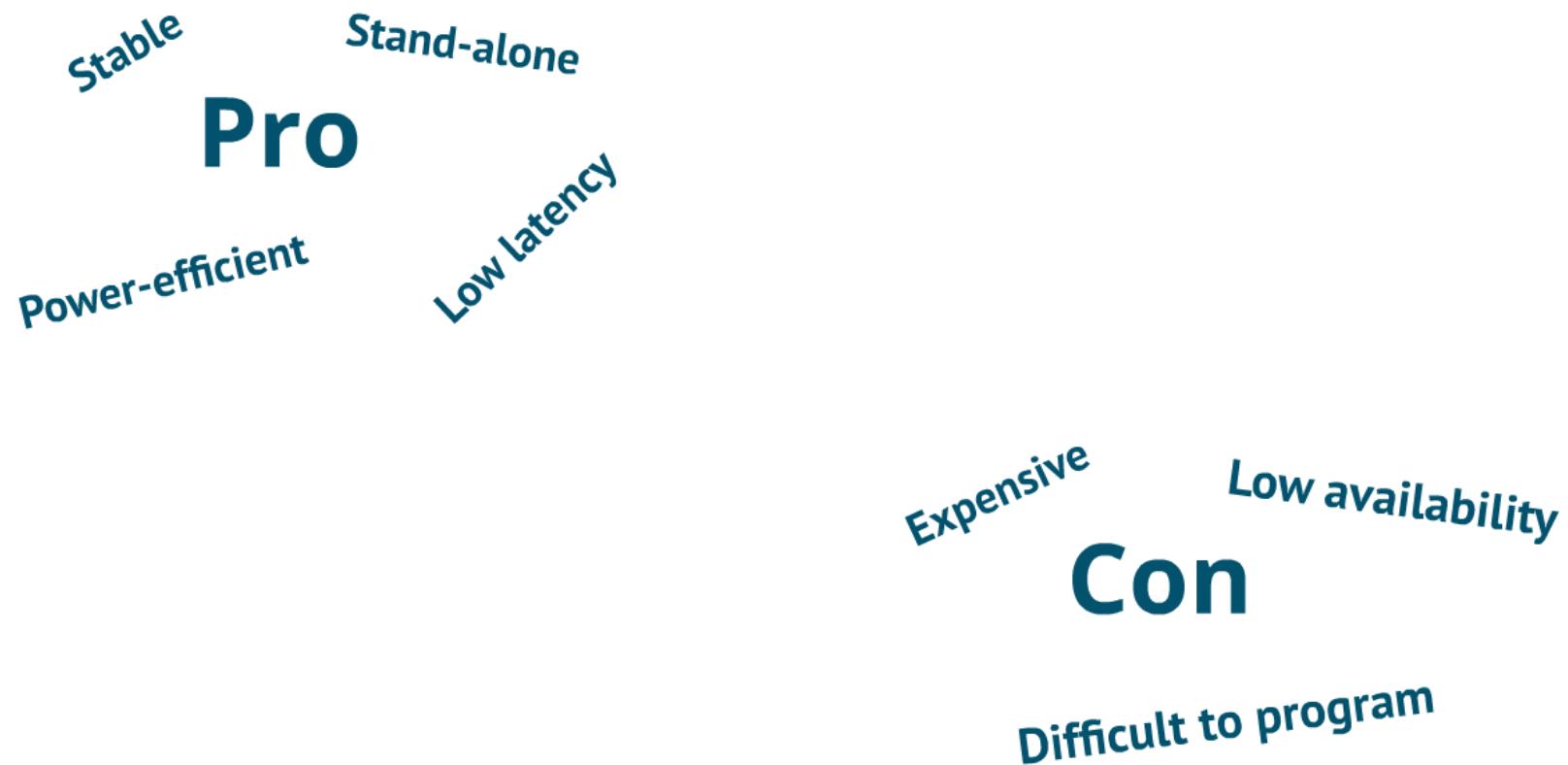
Name	MAX(128)	CORE	MAX(128)
Dependencies	-	-	0 - 160
Width	1	-	160
Height	1	-	2
Depth	-	-	160
Total	2	0	17160
Max width	160	160	160
Max height	160	160	160

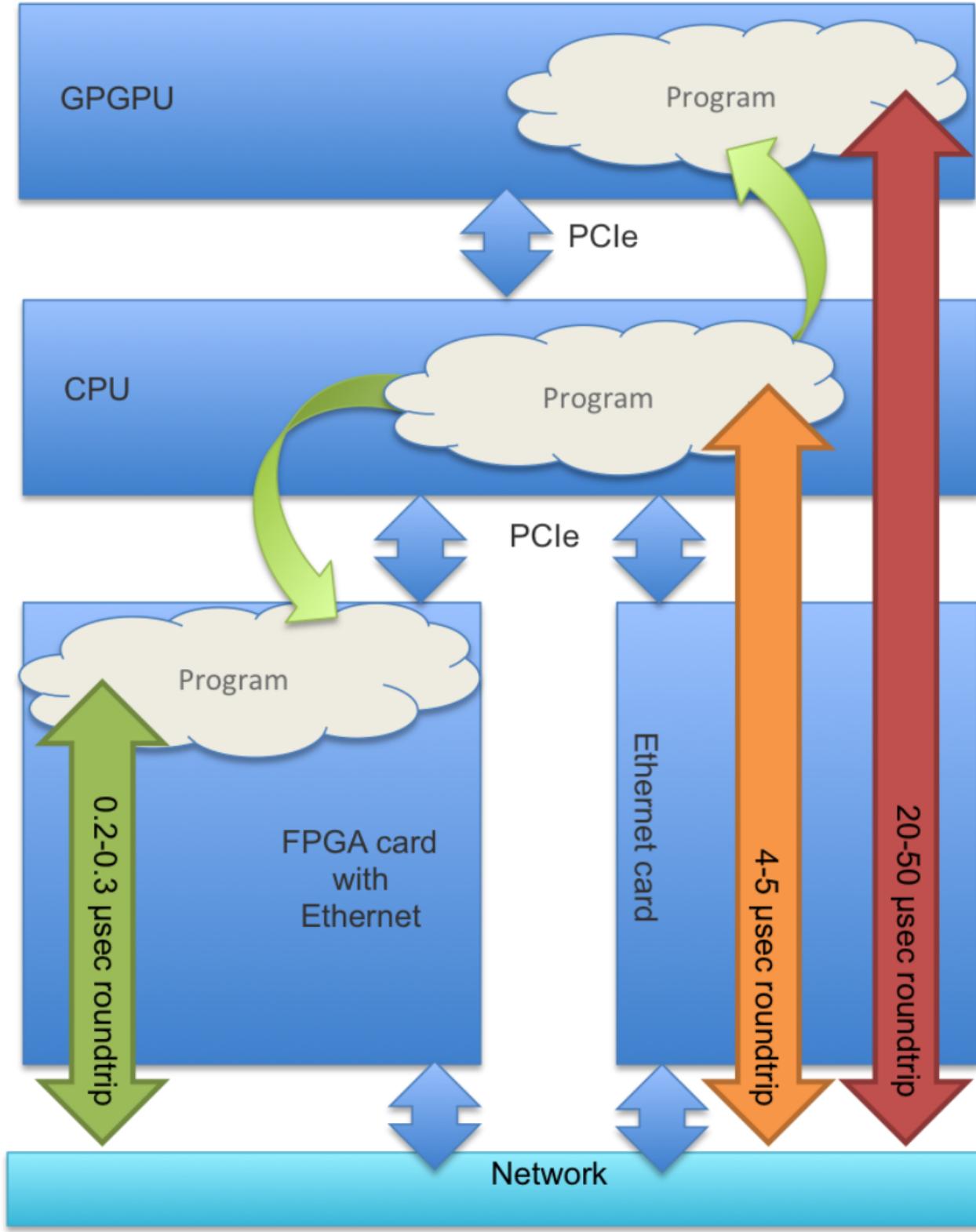


Micro-code design

- Each microcode can execute 2 distinct operations:
 - Vector load memory read
 - Vector load memory write
 - Vector load memory
 - Each microcode can depend on previous instructions:
 - For read
 - For write
 - For store
- The microcode design allows a longer latency on the programmer and is well suited for writing concurrent programs.
- It is a perfect fit for the Bahamut hardware, and especially a processor designed for the programming model.

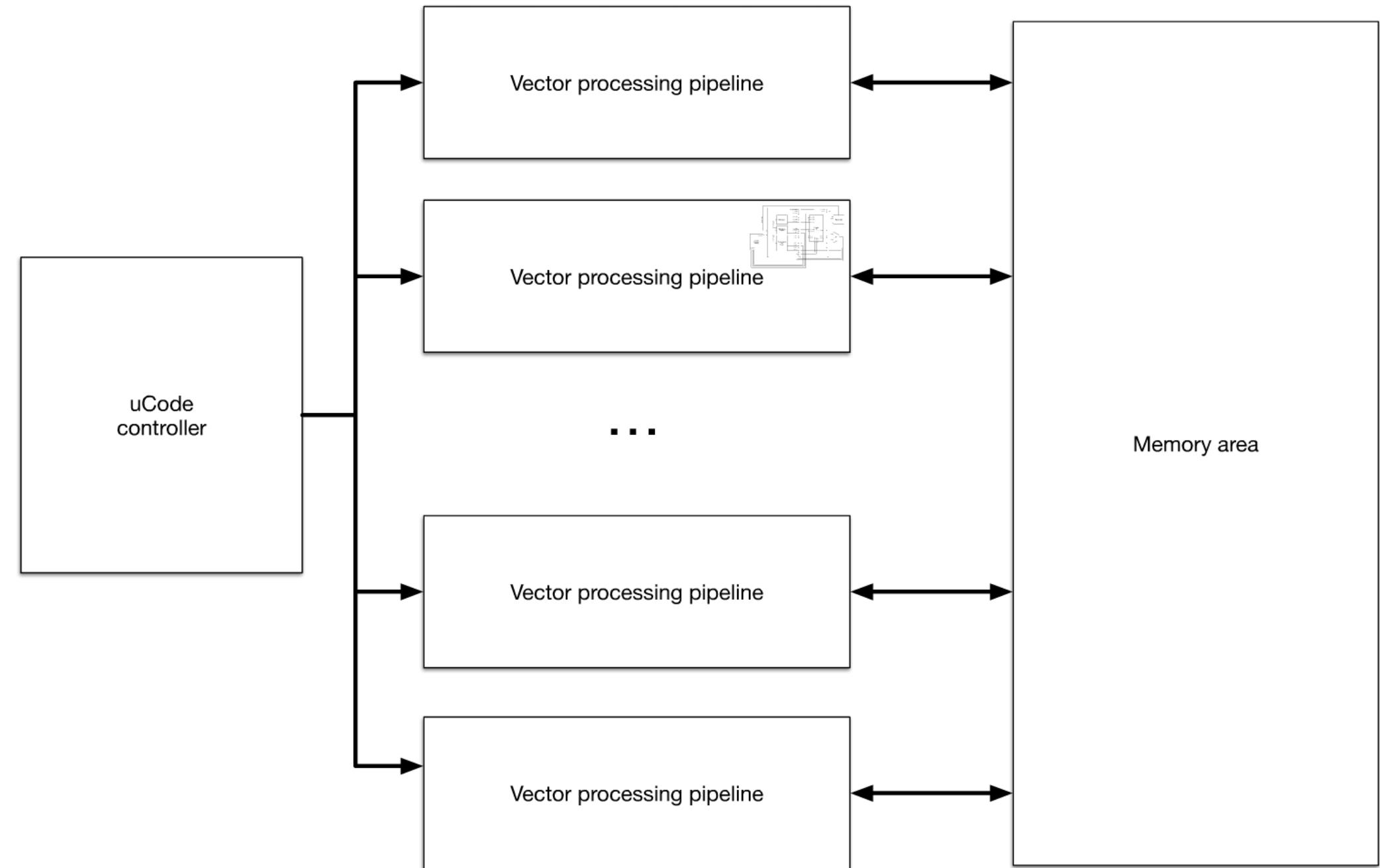
Why FPGA ?

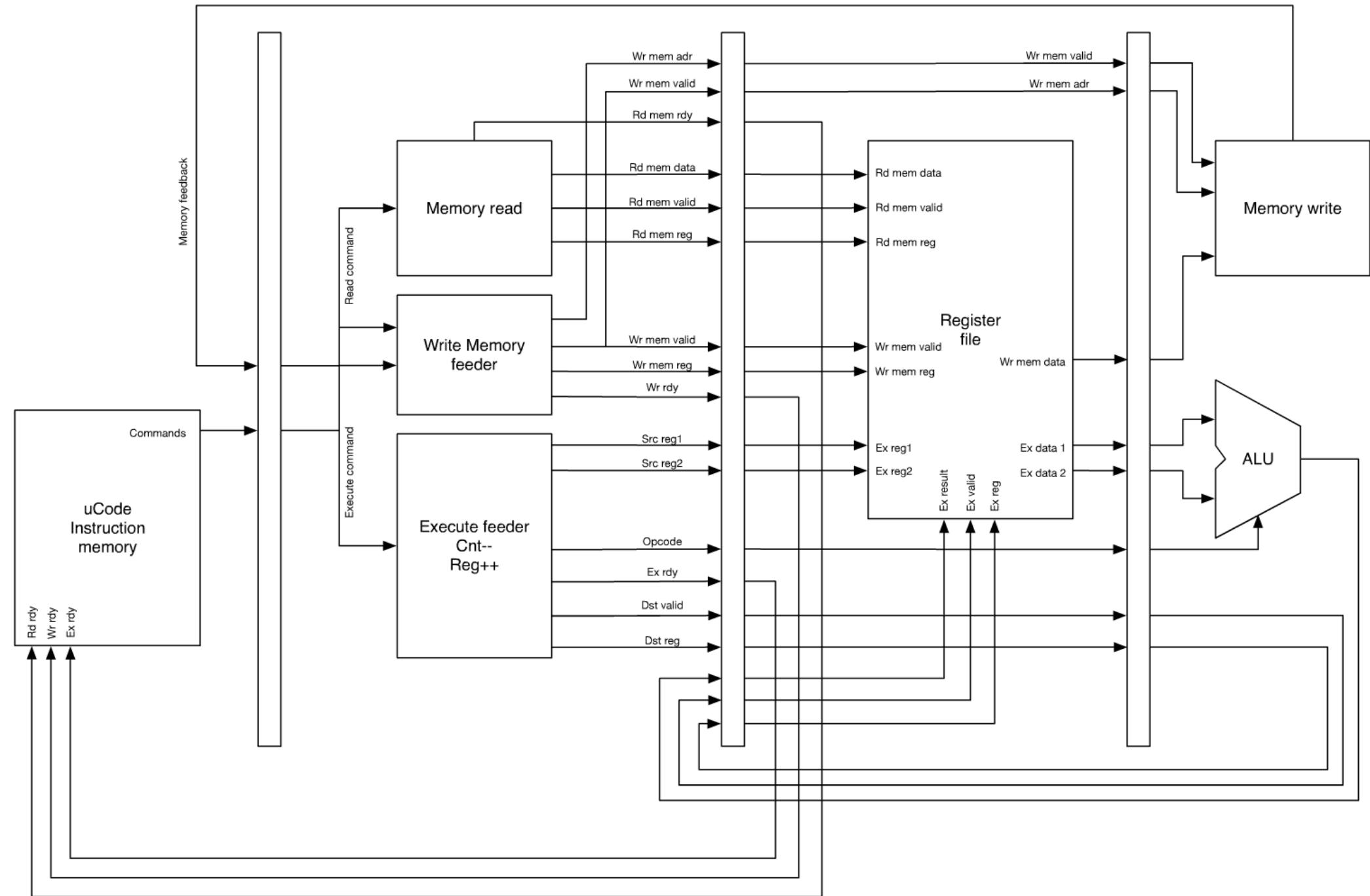






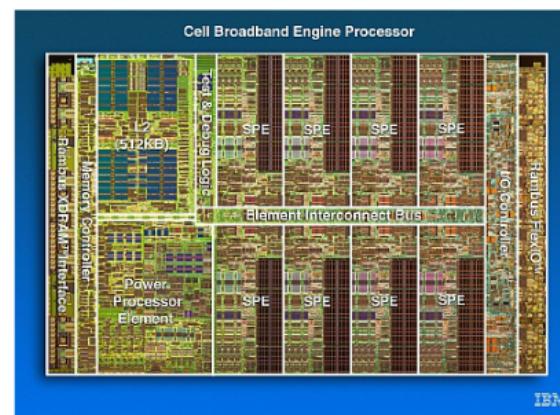
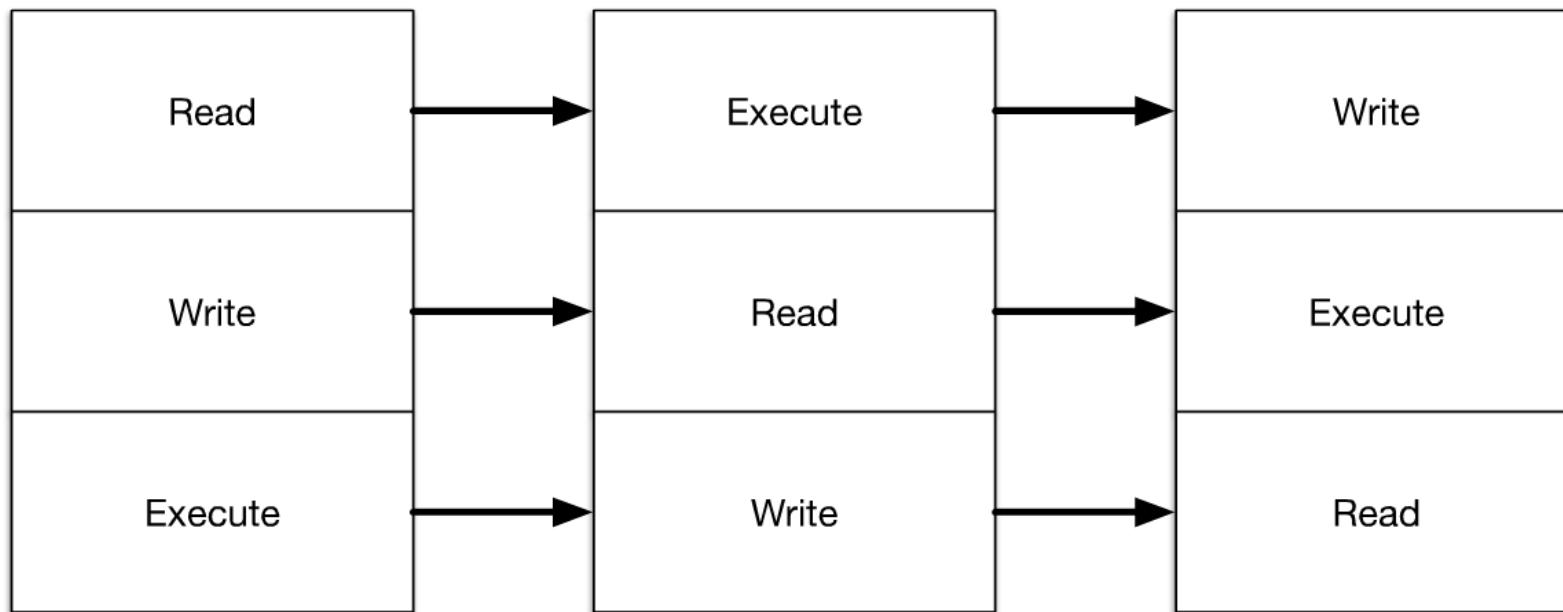






Register file shuffle - 3-state execution

Triple buffering



Micro-code design

Each microcode can express 3 distinct operations:

- Vectorized memory read
- Vectorized memory write
- Vectorized execute

Each microcode can depend on previous instructions

- For read
- For write
- For execute

The micro-code design places a large burden on the programmer and is not suited for writing conventional programs

But it is a perfect fit for the Bohrium bytecode, and essentially a processor designed for the programming model

Name	BRAM_18K	DSP48E	FF	LUT
Expression	-	-	0	4660
FIFO	-	-	-	-
Instance	-	-	2551	4467
Memory	0	-	2	2
Multiplexer	-	-	-	1955
Register	-	-	4172	-
Total	0	0	6725	11084
Available	280	220	106400	53200
Utilization (%)	0	0	6	20

Bohrium

Bridging high performance and high productivity

