Hamiltonian Zoo

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No Matter Where They're From

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I. MODEL HAMILTONIANS

1. Coulomb

$$H_{\text{Coulomb}} = \frac{q_1 q_2}{4\pi\epsilon_0 r} \tag{1}$$

A. Electronic Structure

1. Molecular Hamiltonian

$$H_{\rm BO} = -\sum_{A} \frac{1}{2M_A} \nabla_A^2 - \sum_{i} \frac{1}{2} \nabla_i^2 - \sum_{iA} \frac{Z_A}{r_{iA}} + \sum_{i>j} \frac{1}{r_{ij}} + \sum_{B>A} \frac{Z_A Z_B}{R_{AB}}$$
 (2)

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- 2. Born-Oppenheimer Model
 - 3. Watson Model

B. Fine and Hyperfine Structure

- 1. Stark
- 2. Zeeman

$$H_{\text{Zeeman}} = -\frac{\mu_B \left(g_l \vec{L} + g_s \vec{S} \right)}{\hbar} \cdot \vec{B}$$
 (3)

3. Complete magnetic dipole interaction

$$H_{\text{Magnetic Dipole}} = \frac{g_{I}\mu_{N}\mu_{B}\mu_{0}}{2\pi} \left(\frac{1}{L_{z}} \sum_{i} \frac{\hat{l}_{zi}}{r_{i}^{3}} \vec{I} \cdot \vec{L} + \frac{2g_{s}}{S_{z}} \sum_{i} \frac{\hat{s}_{zi}}{r_{i}^{3}} \left(3\left(\vec{I} \cdot \hat{r}\right)\left(\vec{S} \cdot \hat{r}\right) - \vec{I} \cdot \vec{S} \right) + \frac{g_{s}}{3S_{z}} \sum_{i} \hat{s}_{zi} \delta^{3}\left(\vec{r}_{i}\right) \vec{I} \cdot \vec{S} \right)$$

$$(4)$$

4. Frosch-Foley

$$H_{\text{Frosch-Foley},1} = \frac{e\hbar}{2mc} \frac{2\mu \cdot \mathbf{L}}{r_1^3} + \frac{i2\mu_0}{\hbar} \mathbf{S} \cdot \left[\mathbf{p} \times \mathbf{A}\right] + \frac{2e^2\hbar}{4m^2c^3} \mathbf{S} \cdot \left[\epsilon' \times \mathbf{A}\right]. \tag{5}$$

$$H_{\text{Frosch-Foley},2} = aI_zL_z + b\vec{I} \cdot \vec{S} + cI_zS_z, \tag{6}$$

where

$$a = 2g_I \mu_0 \mu_N \sum_i \left\langle \frac{1}{r_i^3} \right\rangle, \tag{7}$$

$$b = 2g_I \mu_0 \mu_N \sum_i \left(\frac{2e^2 mc^2 \mathcal{E}_r}{\left(E + eV + mc^2\right)^2} \frac{\left(\frac{1}{2}\sin^2 \chi + \cos^2 \chi\right)}{r_i^2} - \frac{1}{2} \left(\frac{3\cos^2 \chi - 1}{r_i^3} \right) \right), \text{ and}$$
 (8)

$$c = 2g_I \mu_0 \mu_N \sum_i \left(\frac{2e^2 mc^2 \mathcal{E}_r}{(E + eV + mc^2)^2} \frac{(1/2\sin^2 \chi - \cos^2 \chi)}{r_i^2} + \frac{3}{2} \left(\frac{3\cos^2 \chi - 1}{r_i^3} \right) \right). \tag{9}$$

- 5. Spin-orbit
- 6. Orbit-orbit
- 7. Spin-other-orbit (Gaunt)
 - 8. Fermi Contact

C. Special Relativity

1. Dirac

$$H = \beta mc^2 - eV + c\alpha \cdot (\mathbf{p} - \frac{e}{c}\mathbf{A}). \tag{10}$$

- 2. Klein-Gordon
- 3. Darwin (1e⁻)

$$H_{\text{Darwin-1}} = \alpha_{\text{FS}}^2 \frac{\pi Z}{2} \sum_i \delta(\vec{r}_i)$$
 (11)

4. Darwin (2e⁻)

$$H_{\text{Darwin-2}} = \alpha_{\text{FS}}^2 \pi \sum_{i < j} \delta(\vec{r}_{ij})$$
 (12)

5. Mass Velocity

$$H_{\text{Mass-Velocity}} = -\alpha_{\text{FS}}^2 \frac{1}{8} \sum_{i} \nabla_i^4. \tag{13}$$

- 6. Breit-Pauli
- 7. Dirac-Coulomb-Breit

D. Quantum Electrodynamics

1. Aracki-Sucher

$$H_{\text{Aracki-Sucher}} = -\alpha_{\text{FS}}^3 \frac{7}{6\pi} \sum_{i>j} \lim_{a \to 0} \left(\frac{\theta \left(r_{ij} - a \right)}{r_{ij}^3} + 4\pi \left(\gamma + \ln a \right) \delta(\vec{r}_{ij}) \right)$$
(14)

2. One-Loop

$$H_{1-\text{loop}} = \alpha_{\text{FS}}^4 \pi Z^2 \left(\frac{427}{96} - \ln 2 \right) \sum_i \delta \left(\vec{r}_i \right)$$
 (15)

- 3. Schwinger-Dyson
- E. Nuclear Motion

$$H_{\text{Nuc}} = -\frac{\hbar^2}{2} \sum_{i=1}^{N} \sum_{\alpha=1}^{3} \frac{1}{M_i} \frac{\partial^2}{\partial R_{i\alpha}^2} + V(\mathbf{R}_1, \dots, \mathbf{R}_N)$$
(16)

- 1. Rigid Rotor Harmonic Oscillator
 - 2. Centrifugal distortion
 - 3. Centrifugal distortion

F. Long-range Interactions

- 1. van der Waals
- 2. Lenard-Jones
- 3. Casimir-Polder
- 4. Resonance dipole-dipole
 - 5. Meath
 - 6. Axilrod-Teller

G. Hubbard Models

1. Non-interacting Hubbard model

$$H = \sum_{\mathbf{k}} \sum_{\sigma} (\varepsilon_{\mathbf{k}} - \mu) n_{\mathbf{k},\sigma}$$
 (17)

2. 1D Hydrogen chain Hubbard model

$$H = -t \sum_{\langle i,j \rangle} \sum_{\sigma} \left(\hat{c}_{i,\sigma}^{\dagger} \hat{c}_{j,\sigma} + \hat{c}_{j,\sigma}^{\dagger} \hat{c}_{i,\sigma} \right) + U \sum_{i=1}^{N} \hat{n}_{i\uparrow} \hat{n}_{i\downarrow}, \quad t > 0, U > 0$$

$$\tag{18}$$

3. 1D Hydrogen chain Hubbard model with μ term

$$H = -t \sum_{\langle i,j \rangle} \sum_{\sigma} \left(\hat{c}_{i,\sigma}^{\dagger} \hat{c}_{j,\sigma} + \hat{c}_{j,\sigma}^{\dagger} \hat{c}_{i,\sigma} \right) + U \sum_{i=1}^{N} \hat{n}_{i\uparrow} \hat{n}_{i\downarrow} - \mu \sum_{i} \left(n_{i\uparrow} + n_{i\downarrow} \right)$$

$$\tag{19}$$

4. With particle-hole symmetry

$$H = -t \sum_{\langle i,j \rangle} \sum_{\sigma} \left(\hat{c}_{i,\sigma}^{\dagger} \hat{c}_{j,\sigma} + \hat{c}_{j,\sigma}^{\dagger} \hat{c}_{i,\sigma} \right) + U \sum_{i=1}^{N} \left(\hat{n}_{i\uparrow} - \frac{1}{2} \right) \left(\hat{n}_{i\downarrow} - \frac{1}{2} \right) - \mu \sum_{i} \left(n_{i\uparrow} + n_{i\downarrow} \right)$$
 (20)

5. Bose-Hubbard (Boson Hubbard)

$$H = -t \sum_{\langle i,j \rangle} \hat{b}_i^{\dagger} \hat{b}_j + \frac{1}{2} U \sum_i \hat{n}_i \left(\hat{n}_i - 1 \right) - \mu \sum_i \hat{n}_i$$
 (21)

6. Fermi-Hubbard (Fermi Hubbard)

- $7. \quad Bose-Fermi-Hubbard$
- 8. Jaynes-Cummings-Hubbard
- 9. Tavis-Cummings-Hubbard
- 10. Periodic Anderson Model

$$H = -t \sum_{\langle i,j \rangle} \sum_{\sigma} \left(\hat{c}_{i,\sigma}^{\dagger} \hat{c}_{j,\sigma} + \hat{c}_{j,\sigma}^{\dagger} \hat{c}_{i,\sigma} \right) + V \sum_{\langle i,j \rangle} \sum_{\sigma} \left(c_{j\sigma}^{\dagger} d_{i\sigma} + d_{i\sigma}^{\dagger} c_{j\sigma} \right)$$

$$+ U \sum_{i=1}^{N} \left(\hat{n}_{di\uparrow} - \frac{1}{2} \right) \left(\hat{n}_{di\downarrow} - \frac{1}{2} \right) - \mu \sum_{i} \left(n_{di\uparrow} + n_{di\downarrow} + n_{ci\uparrow} + n_{ci\downarrow} \right),$$

$$(22)$$

where $d_{i\sigma}$ is the annihilation operator for an electron in the localized band at site i, $c_{i\sigma}$ is the annihilation operator for an electron in the conduction band at site i, V is termed the hybridization and is the transition amplitude of an electron moving from the localized band at site i to the conduction band at site i or vice versa.

H. Disorder Models

1. Tight-binding Model with Onsite Disorder

$$H = \sum_{i} \omega_i \hat{c}_i^{\dagger} \hat{c}_i + t \sum_{\langle i,j \rangle} \hat{c}_i^{\dagger} \hat{c}_j, \tag{23}$$

where ω_i is drawn from a unifrom distribution of width W, the disorder strength, and the angular brackets indicate a sum over nearest-neighbours only.

- 2. Tight-binding Model with Continuous Off-diagonal Disorder
 - 3. Tight-binding Model with Binary Off-diagonal Disorder
 - 4. Long-range Disorder Models

I. Mean-field Hamiltonians

1. Clean Bose-Hubbard

$$H_{\text{MF}} = \sum_{i} \left[-\mu \hat{n}_i + \frac{U}{2} \hat{n}_i (\hat{n}_i - 1) - zt(\psi^* \hat{b}_i + \psi \hat{b}_i^{\dagger}) + zt\psi^* \psi \right]$$
 (24)

J. Spin lattices

1. XY model

$$H = -J\sum_{i} \left(\frac{1+\gamma}{2} \sigma_{x,i} \sigma_{x,i+1} + \frac{1-\gamma}{2} \sigma_{y,i} \sigma_{y,i+1} \right) - h\sum_{i} \sigma_{z,i}$$
 (25)

$$H = -J\sum_{i} \left(\frac{1+\gamma}{2} x_{i} x_{i+1} + \frac{1-\gamma}{2} y_{i} y_{i+1} \right) - h\sum_{i} z_{i}$$
 (26)

K. Open Quantum Systems

- 1. Rabi model
- 2. Spin-Boson
- 3. Feynman-Vernon
- 4. Leggett-Caldeira
- 5. Ishizaki-Fleming
- 6. Jaynes-Cummings

L. Models of Superconductivity

1. BCS

$$H_{\text{BCS}} = \sum_{i} \epsilon_{i} n_{i} + g \sum_{ij} c_{i\uparrow}^{\dagger} c_{-i\downarrow}^{\dagger} c_{-j\downarrow} c_{j\uparrow}$$
(27)

- 2. Richardson-Gaudin
- 3. Exactly solvable pairing Hamiltonians

SU(2), Rank 1 algebra

$$H_{SU(2)} = \sum_{i} \epsilon_i n_i - g \sum_{ij} P_i^+ P_j \tag{28}$$

SO(5), Rank 2 algebra

$$H_{SO(5)} = \sum_{i} \epsilon_i n_i - g \sum_{ijk} P_{ik}^+ P_{jk}$$
 (29)

SO(8), Rank 4 algebra

$$H_{SO(8)} = \sum_{i} \epsilon_{i} n_{i} - g_{T} \sum_{ijk} P_{ik}^{+} P_{jk} - g_{S} \sum_{ijk} D_{ik}^{+} D_{jk}$$
(30)

4. t-J model

M. Models of Superfluidity

1. 2D p-wave Fermi superfluid

$$H_{2DFSF} = \sum_{i} \epsilon_{i} a_{i}^{\dagger} a_{i} + \frac{i\Delta_{i}}{2} \left(a_{i}^{\dagger} a_{-i}^{\dagger} + \text{H.c.} \right)$$
 (31)

N. Spin models

- 1. Ising
- 2. Transverse Ising
 - 3. XY
 - 4. XYZ
- O. Heisenberg
- P. J1-J2 Model
- Q. Majumdar-Ghosh
 - R. AKLT Model
 - S. Kitaev Models
 - 1. Toric Code
 - 2. Ocko-Yoshida
- 3. Honeycomb Model

$$H_{\text{Honeycomb}} = -J_x \sum_{x-\text{links}} x_i x_j - J_y \sum_{y-\text{links}} y_i y_j - J_z \sum_{z-\text{links}} z_i z_j$$
 (32)

T. Miscellaneous

1. Fertitta-Booth auxiliary Hamiltonian

$$H_{\rm FB} = \sum_{x=0}^{N_{\rm cells}-1} \sum_{\alpha}^{N_{\rm Impurities}} \sum_{k}^{N_{\rm aux}} \nu_{\alpha k} \left(\hat{c}_{\alpha+x}^{\dagger} \hat{c}_{k+x} + \hat{c}_{k+x}^{\dagger} \hat{c}_{\alpha+x} \right) + \varepsilon_{k} \hat{c}_{k+x}^{\dagger} \hat{c}_{k+x}$$
(33)

Matrix Zoo

U. 2-level systems (spin-1/2 particles)

$$x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \qquad y = \begin{pmatrix} 0 & -\mathrm{i} \\ \mathrm{i} & 0 \end{pmatrix} \qquad z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$A_1 = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \qquad A_2 = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix} \qquad A_3 = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \qquad A_4 = \begin{pmatrix} 0 & \mathrm{i} \\ -\mathrm{i} & 0 \end{pmatrix}$$

$$s_+ = \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix} = \frac{x + \mathrm{i}y}{2} \quad s_- = \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} = \frac{x - \mathrm{i}y}{2} \quad s_\alpha = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} = \frac{1 + z}{2} = b \quad s_\beta = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix} = \frac{1 - z}{2}$$

V. 3-level systems (spin-1 particles)

$$x_{3} = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \qquad y_{3} = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & -i \\ 0 & i & 0 \end{pmatrix} \quad z_{3} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix} \quad s_{3+} = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{pmatrix} \quad s_{3-} = \begin{pmatrix} 0 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} \quad x_{3}^{2} = \begin{pmatrix} 1 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 1 \end{pmatrix} \quad y_{3}^{2} = \begin{pmatrix} 1 & 0 & -1 \\ 0 & 2 & 0 \\ -1 & 0 & 1 \end{pmatrix}$$

$$\lambda_{1} = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \lambda_{2} = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \lambda_{3} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \lambda_{4} = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} \quad \lambda_{5} = \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ i & 0 & 0 \end{pmatrix} \quad \lambda_{6} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \quad \lambda_{7} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix}$$

$$\lambda_{8} = \begin{pmatrix} \frac{1}{\sqrt{3}} & 0 & 0 \\ 0 & \frac{1}{\sqrt{3}} & 0 \\ 0 & 0 & -\frac{2}{\sqrt{3}} \end{pmatrix} \quad s_{3}^{1} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad s_{3}^{2} = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad s_{3}^{3} = \begin{pmatrix} 0 & 0 & i \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad B_{1} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad B_{2} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$B_{3} = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad B_{5} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{pmatrix} \quad B_{7} = \begin{pmatrix} 0 & 0 & i \\ 0 & 0 & 0 \\ -i & 0 & 0 \end{pmatrix} \quad B_{8} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \quad B_{9} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & i \\ 0 & -i & 0 \end{pmatrix}$$

$$\begin{split} \lambda_1 &= \frac{1}{2}(x_3 + z_3x_3 + x_3z_3) \\ \lambda_3 &= 21 + \frac{1}{2}(z_3 - \frac{3}{2}x_3^2 - \frac{3}{2}y_3^2) \\ \lambda_5 &= \frac{1}{2}(x_3y_3 + y_3x_3) \\ \lambda_7 &= \frac{1}{2}(y_3 - y_3z_3 - z_3y_3) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2)) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}(z_3 + \frac{1}{2}x_3^2 + \frac{1}{2}y_3^2) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}z_3^2 + \frac{1}{2}y_3^2) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}z_3^2 + \frac{1}{2}y_3^2) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}z_3^2 + \frac{1}{2}y_3^2 + \frac{1}{2}y_3^2) \\ \lambda_8 &= \frac{1}{\sqrt{3}}(-211 + \frac{3}{2}z_3^2 + \frac{1}{2}y_3^2 + \frac{1$$

W. 4-level systems (spin-3/2 particles)

X. 5-level systems (spin-2 particles)

Y. 6-level systems (spin-3/2 particles)

Z. 7-level systems (spin-3 particles)

II. OTHER HAMILTONIANS

A. Feynman Hamiltonian

Wavefunction Zoo

B. Electronic Structure Ansatze

- 1. Hartree Product
- 2. Configuration Interaction
 - 3. Coupled Cluster

CC(n)

Bruckner-CC(n)

EOM-CC(n)

EOM-IP-CC(n)

FS-CC(n)

DLPNO-CC(n)

MR-EOM

4. Geminals

AP1roG/pCCD

APIG

APSetG

APG

Potential Zoo

PolyMLR

Harmonic Oscillator Morse $Lenard ext{-}Jones$ Morse/Long-range TiemannMorse-RosenTriatomics Jensen Schwenke

E. Torsion Potentials

C. Diatomics

Functional Zoo

Function Zoo

Master Equation Zoo

Particle Zoo

https://en.wikipedia.org/wiki/Particle_zoo

$Complexity \ Zoo \ \ ({\rm founded} \ {\rm by} \ {\rm Scott} \ {\rm Aarsonson} \ {\rm of} \ {\rm UWaterloo})$

 $https://complexityzoo.uwaterloo.ca/Complexity_Zoo$

$Algorithms \ Zoo \ \ ({\rm founded} \ {\rm by} \ {\rm Stephen} \ {\rm Jordan} \ {\rm of} \ {\rm NIST})$

https://math.nist.gov/quantum/zoo/