CSCI-1200 Data Structures — Spring 2019 Lecture 20 – Hash Tables

Review from Lecture 19

- Last pieces of ds_set: removing an item, erase, operator++
- Breadth-first and depth-first search

Today's Lecture

- "the single most important data structure known to mankind"
- Hash Tables, Hash Functions, and Collision Resolution
- Performance of: Hash Tables vs. Binary Search Trees
- Collision resolution: separate chaining vs open addressing
- STL's unordered_set (and unordered_map)
- Using a hash table to implement a set/map
 - Hash functions as functors/function objects
 - Iterators, find, insert, and erase

20.1 Definition: What's a Hash Table?

- A table implementation with constant time access.
 - Like a set, we can store elements in a collection. Or like a map, we can store key-value pair associations in the hash table. But it's even faster to do find, insert, and erase with a hash table! However, hash tables do not store the data in sorted order.
- A hash table is implemented with an array at the top level.
- Each element or key is mapped to a slot in the array by a hash function.

20.2 Definition: What's a Hash Function?

- A simple function of one argument (the key) which returns an integer index (a bucket or slot in the array).
- Ideally the function will "uniformly" distribute the keys throughout the range of legal index values $(0 \to k-1)$.
- What's a collision?

When the hash function maps multiple (different) keys to the same index.

• How do we deal with collisions?

One way to resolve this is by storing a linked list of values at each slot in the array.

20.3 Example: Caller ID

- We are given a phonebook with 50,000 name/number pairings. Each number is a 10 digit number. We need to create a data structure to lookup the name matching a particular phone number. Ideally, name lookup should be O(1) time expected, and the caller ID system should use O(n) memory (n = 50,000).
- Note: In the toy implementations that follow we use small datasets, but we should evaluate the system scaled up to handle the large dataset.

• The basic interface:

```
// add several names to the phonebook
add(phonebook, 1111, "fred");
add(phonebook, 2222, "sally");
add(phonebook, 3333, "george");
// test the phonebook
std::cout << identify(phonebook, 2222) << " is calling!" << std::endl;
std::cout << identify(phonebook, 4444) << " is calling!" << std::endl;</pre>
```

• We'll review how we solved this problem in Lab 9 with an STL vector then an STL map. Finally, we'll implement the system with a hash table.

20.4 Caller ID with an STL Vector

```
// create an empty phonebook
std::vector<std::string> phonebook(10000, "UNKNOWN CALLER");

void add(std::vector<std::string> &phonebook, int number, std::string name) {
   phonebook[number] = name; }

std::string identify(const std::vector<std::string> &phonebook, int number) {
   return phonebook[number]; }
```

Exercise: What's the memory usage for the vector-based Caller ID system? What's the expected running time for find, insert, and erase?

20.5 Caller ID with an STL Map

```
// create an empty phonebook
std::map<int,std::string> phonebook;

void add(std::map<int,std::string> &phonebook, int number, std::string name) {
   phonebook[number] = name; }

std::string identify(const std::map<int,std::string> &phonebook, int number) {
   map<int,std::string>::const_iterator tmp = phonebook.find(number);
   if (tmp == phonebook.end()) return "UNKNOWN CALLER"; else return tmp->second;
}
```

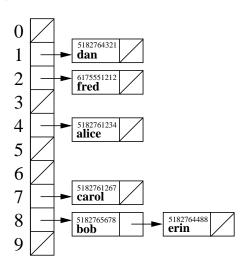
Exercise: What's the memory usage for the map-based Caller ID system? What's the expected running time for identify, add, and erase?

20.6 Now let's implement Caller ID with a Hash Table

```
#define PHONEBOOK_SIZE 10

class Node {
public:
    int number;
    string name;
    Node* next;
};

// create the phonebook, initially all numbers are unassigned
Node* phonebook[PHONEBOOK_SIZE];
for (int i = 0; i < PHONEBOOK_SIZE; i++) {
    phonebook[i] = NULL;
}</pre>
```



```
// corresponds a phone number to a slot in the array
int hash_function(int number) {

// add a number, name pair to the phonebook
void add(Node* phonebook[PHONEBOOK_SIZE], int number, string name) {

// given a phone number, determine who is calling
void identify(Node* phonebook[PHONEBOOK_SIZE], int number) {

// size a phone number of the phonebook into the phoneboo
```

20.7 Exercise: Choosing a Hash Function

- What's a good hash function for this application?
- What's a bad hash function for this application?

20.8 Exercise: Hash Table Performance

- What's the memory usage for the hash-table-based Caller ID system?
- What's the expected running time for find, insert, and erase?

20.9 What makes a Good Hash Function?

- Goals: fast O(1) computation and a random, uniform distribution of keys throughout the table, despite the actual distribution of keys that are to be stored.
- For example, using: f(k) = abs(k)%N as our hash function satisfies the first requirement, but may not satisfy the second.

• Another example of a dangerous hash function on string keys is to add or multiply the ascii values of each char:

```
unsigned int hash(string const& k, unsigned int N) {
  unsigned int value = 0;
  for (unsigned int i=0; i<k.size(); ++i)
    value += k[i]; // conversion to int is automatic
  return value % N;
}</pre>
```

The problem is that different permutations of the same string result in the same hash table location.

• This can be improved through multiplications that involve the position and value of the key:

```
unsigned int hash(string const& k, unsigned int N) {
  unsigned int value = 0;
  for (unsigned int i=0; i<k.size(); ++i)
    value = value*8 + k[i]; // conversion to int is automatic
  return value % N;
}</pre>
```

• The 2nd method is better, but can be improved further. The theory of good hash functions is quite involved and beyond the scope of this course.

20.10 How do we Resolve Collisions? METHOD 1: Separate Chaining

- Each table location stores a linked list of keys (and values) hashed to that location (as shown above in the phonebook hashtable). Thus, the hashing function really just selects which list to search or modify.
- This works well when the number of items stored in each list is small, e.g., an average of 1. Other data structures, such as binary search trees, may be used in place of the list, but these have even greater overhead considering the (hopefully, very small) number of items stored per bin.

20.11 How do we Resolve Collisions? METHOD 2: Open Addressing

- In *open addressing*, when the chosen table location already stores a key (or key-value pair), a different table location is sought in order to store the new value (or pair).
- Here are three different open addressing variations to handle a collision during an *insert* operation:
 - Linear probing: If i is the chosen hash location then the following sequence of table locations is tested ("probed") until an empty location is found:

```
(i+1)%N, (i+2)%N, (i+3)%N, ...
```

Quadratic probing: If i is the hash location then the following sequence of table locations is tested:

```
(i+1)%N, (i+2*2)%N, (i+3*3)%N, (i+4*4)%N, ...
```

More generally, the j^{th} "probe" of the table is $(i+c_1j+c_2j^2) \mod N$ where c_1 and c_2 are constants.

- Secondary hashing: when a collision occurs a second hash function is applied to compute a new table location. This is repeated until an empty location is found.
- For each of these approaches, the *find* operation follows the same sequence of locations as the *insert* operation. The key value is determined to be absent from the table only when an empty location is found.
- When using open addressing to resolve collisions, the *erase* function must mark a location as "formerly occupied". If a location is instead marked empty, *find* may fail to return elements in the table. Formerly-occupied locations may (and should) be reused, but only after the *find* operation has been run to completion.
- Problems with open addressing:
 - Slows dramatically when the table is nearly full (e.g. about 80% or higher). This is particularly problematic for linear probing.
 - Fails completely when the table is full.
 - Cost of computing new hash values.

20.12 Hash Table in STL?

- The Standard Template Library standard and implementation of hash table have been slowly evolving over many years. Unfortunately, the names "hashset" and "hashmap" were spoiled by developers anticipating the STL standard, so to avoid breaking or having name clashes with code using these early implementations...
- STL's agreed-upon standard for hash tables: unordered_set and unordered_map
- Depending on your OS/compiler, you may need to add the -std=c++11 flag to the compile line (or other configuration tweaks) to access these more recent pieces of STL. (And this will certainly continue to evolve in future years!) Also, for many types STL has a good default hash function, so you may not always need to specify both template parameters!

20.13 Our Copycat Version: A Set As a Hash Table

• The class is templated over both the key type and the hash function type.

```
template < class KeyType, class HashFunc >
class ds_hashset { ... };
```

• We use separate chaining for collision resolution. Hence the main data structure inside the class is:

```
std::vector< std::list<KeyType> > m_table;
```

• We will use automatic resizing when our table is too full. Resize is expensive of course, so similar to the automatic reallocation that occurs inside the vector push_back function, we at least double the size of underlying structure to ensure it is rarely needed.

20.14 Our Hash Function (as a Functor or Function Object)

- Next lecture we'll talk about "function objects" or "functors".... A functor is just a class wrapper around a function, and the function is implemented as the overloaded function call operator for the class.
- Often the programmer/designer for the program using a hash function has the best understanding of the distribution of data to be stored in the hash function. Thus, they are in the best position to define a custom hash function (if needed) for the data & application.
- Here's an example of a (generically) good hash function for STL strings, wrapped up inside of a class:

```
class hash_string_obj {
public:
    unsigned int operator() (std::string const& key) const {
        // This implementation comes from
        // http://www.partow.net/programming/hashfunctions/
        unsigned int hash = 1315423911;
        for(unsigned int i = 0; i < key.length(); i++)
            hash ^= ((hash << 5) + key[i] + (hash >> 2));
        return hash;
    }
};
```

• Once our new type containing the hash function is defined, we can create instances of our hash set object containing std::string by specifying the type hash_string_obj as the second template parameter to the declaration of a ds_hashset. E.g.,

```
ds_hashset<std::string, hash_string_obj> my_hashset;
```

• Alternatively, we could use function pointers as a non-type template argument. (We don't show that syntax here!).

20.15 Hash Set Iterators

- Iterators move through the hash table in the order of the storage locations rather than the ordering imposed by (say) an operator<. Thus, the visiting/printing order depends on the hash function and the table size.
 - Hence the increment operators must move to the next entry in the current linked list or, if the end of the current list is reached, to the first entry in the next non-empty list.
- The declaration is nested inside the ds_hashset declaration in order to avoid explicitly templating the iterator
 over the hash function type.

- The iterator must store:
 - A pointer to the hash table it is associated with. This reflects a subtle point about types: even though
 the iterator class is declared inside the ds_hashset, this does not mean an iterator automatically knows
 about any particular ds_hashset.
 - The index of the current list in the hash table.
 - An iterator referencing the current location in the current list.
- Because of the way the classes are nested, the iterator class object must declare the ds_hashset class as a friend, but the reverse is unnecessary.

20.16 Implementing begin() and end()

- begin(): Skips over empty lists to find the first key in the table. It must tie the iterator being created to the particular ds_hashset object it is applied to. This is done by passing the this pointer to the iterator constructor.
- end(): Also associates the iterator with the specific table, assigns an index of -1 (indicating it is not a normal valid index), and thus does not assign the particular list iterator.
- Exercise: Implement the begin() function.

20.17 Iterator Increment, Decrement, & Comparison Operators

- The increment operators must find the next key, either in the current list, or in the next non-empty list.
- The decrement operator must check if the iterator in the list is at the beginning and if so it must proceed to find the previous non-empty list and then find the last entry in that list. This might sound expensive, but remember that the lists should be very short.
- The comparison operators must accommodate the fact that when (at least) one of the iterators is the end, the internal list iterator will not have a useful value.

20.18 Insert & Find

- Computes the hash function value and then the index location.
- If the key is already in the list that is at the index location, then no changes are made to the set, but an iterator is created referencing the location of the key, a pair is returned with this iterator and false.
- If the key is not in the list at the index location, then the key should be inserted in the list (at the front is fine), and an iterator is created referencing the location of the newly-inserted key a pair is returned with this iterator and true.
- Exercise: Implement the insert() function, ignoring for now the resize operation.
- Find is similar to insert, computing the hash function and index, followed by a std::find operation.

20.19 Erase

• Two versions are implemented, one based on a key value and one based on an iterator. These are based on finding the appropriate iterator location in the appropriate list, and applying the list erase function.

20.20 Resize

• Must copy the contents of the current vector into a scratch vector, resize the current vector, and then re-insert each key into the resized vector. **Exercise:** Write resize()

20.21 Hash Table Iterator Invalidation

• Any insert operation invalidates *all* ds_hashset iterators because the insert operation could cause a resize of the table. The erase function only invalidates an iterator that references the current object.

ds_hashset_lec.h

```
// Find the previous entry in the table
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // Find the next entry in the table
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // Otherwise, we are at the end
// increment and decrement
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                                                                                                                                                                                                                                                                                                                                                        iterator & operator--() {
                                      iterator& operator++() {
                                                                                                                                                                            iterator operator++(int)
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                                                                         this->next();
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    this->prev();
                                                                                                         return *this;
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// current iterator at the current index
                                                                                                                                                                                                                                                                                                                                                                                        ^{\prime\prime} The ds_hashset is templated over both the type of key and the type
                                                               // The set class as a hash table instead of a binary search tree. Th
// primary external difference between ds_set and ds_hashset is that
// the iterators do not step through the hashset in any meaningful
// order. It is just the order imposed by the hash function.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      friend bool operator!= (const iterator& lft, const iterator& rgt)
{ return lft.m_hs != rgt.m_hs || lft.m_index != rgt.m_index ||
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iterator(ds_hashset* hs, int index, hash_list_itr loc)
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                               #define ds_hashset_h_
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ds_hashset* m_hs;
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              class ds_hashset {
                                                                                                                                                                                                                                                                               #include <string>
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```

(lft.m_index != -1 && lft.m_list_itr != rgt.m_list_itr); }

```
m_index < int(m_hs->m_table.size()) && m_hs->m_table[m_index].empty();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // non-empty list in the table is found for (--m_index; m_index >= 0 && m_hs->m_table[m_index].empty(); --m_index)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // Go to the last entry in the list.
m_list_itr = m_hs->m_table[m_index].begin();
hash_list_itr p = m_list_itr; ++p;
for (; p != m_hs->m_table[m_index].end(); ++p, ++m_list_itr) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // If we aren't at the start of the current list, just decrement
                                                                                                                                                                                                                                                                                                                                                                                                         // If one is found, assign the m_list_itr to the start
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // Otherwise, back down the table until the previous
                                                                              // If we are at the end of this list
if (m_list_itr == m_hs->m_table[m_index].end()) {
// Find the next non-empty list in the table
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (m_list_itr != m_hs->m_table[m_index].begin())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    m_list_itr = m_hs->m_table[m_index].begin();
                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (m_index != int(m_hs->m_table.size()))
++ m_list_itr; // next item in the list
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // end of ITERATOR CLASS
```

ds_hashset_lec.h

```
int erase(const KeyType& key) {
    // Find the key and use the erase iterator function.
iterator p = find(key);
if (p == end())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (unsigned int i=0; i<m_table.size(); ++i) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // resize the table with the same values but a
                                                                                                                                                                                                                                                                                                                                                                                                                        m_table[ p.m_index ].erase(p.m_list_itr);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void resize_table(unsigned int new_size) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // implemented in lecture or lab
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // implemented in lecture or lab
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // A public print utility.
void print(std::ostream & ostr) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // Create an end iterator.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ostr << ' ' << *p;
                                                                                                                                                                                                                                                                                                                                                               // Erase at the iterator
                                                                                                                                                                                                                                                                                                                                                                                          void erase(iterator p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ostr << i << ": ";
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ostr << std::endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               iterator p(this);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             iterator begin() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   p.m_index = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       iterator end()
                                                                                                                                                                                                            erase(p);
                                                                                                                                                return 0;
                                                                                                                                                                                                                                          return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return p;
                                                                                                                                                                              else (
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           private:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       };
#endif
                                                                                                                                                                                                                                                                                                                                                                                          ds_hashset(unsigned int init_size = 10) : m_table(init_size), m_size(0) {}
                                                                                                                                                                                                                                                                                                                              // Constructor for the table accepts the size of the table. Default // constructor for the hash function object is implicitly used.
                                                                                                                                                                                                                                                                                                                                                                                                                                                   // Copy constructor just uses the member function copy constructors.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ds_hashset& operator=(const ds_hashset<KeyType,HashFunc>& old) {
   if (&old != this)
                                                                                                                                                // number of keys
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // Find the key, using hash function, indexing and list find
                                                                                                                  // hash function
                                                                                    // actual table
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (m_size >= LOAD_FRACTION_FOR_RESIZE * m_table.size())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // Insert the key if it is not already there.
std::pair< iterator, bool > insert(KeyType const& key)
const float LOAD_FRACTION_FOR_RESIZE = 1.25;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ds_hashset(const ds_hashset<KeyType, HashFunc>& old)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               : m_table(old.m_table), m_size(old.m_size) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    unsigned int size() const { return m_size; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            this->resize_table(2*m_table.size()+1);
                                                                                    std::vector< std::list<KeyType> > m_table;
HashFunc m_hash;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return iterator(this, index, p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     iterator find(const KeyType& key) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // implemented in lecture or lab
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (p == m_table[index].end())
                                                         // HASH SET REPRESENTATION
                                                                                                                                                                                                                                                                     // HASH SET IMPLEMENTATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return this->end();
                                                                                                                                                unsigned int m_size;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        "ds_hashset() {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             *this = old;
private:
                                                                                                                                                                                                         public:
```

```
for (hash_list_itr p = m_table[i].begin(); p != m_table[i].end(); ++p)
// Find the first entry in the table and create an associated iterator
```