Logic Programming and Prolog

Read: Scott, Chapter 12

Lecture Outline

- Logic programming
- Prolog
 - Language constructs: facts, rules, queries
 - Search tree, unification, backtracking, backward chaining

Prolog

- Download and install SWI Prolog on laptop!
 - Write your Prolog program and save in .pl file,
 e.g., snowy.pl
 - Run swip1 (Prolog interpreter) on command line
 - Load your file: ?- [swnowy].
 - Issue query at prompt: ?- snowy (C).

J.R.Fisher's Prolog Tutorial:

http://www.cpp.edu/~jrfisher/www/prolog_tutorial/contents.html

Why Study Prolog?

- Declarative programming and logic programming
- Prolog is useful in a variety of applications
 - Rule-based reasoning
 - Natural-language processing
 - Database systems
 - Prolog and SQL have a lot in common
- Practice of important concepts such as <u>first-order logic</u>

Logic Programming

- Logic programming is declarative programming
- Logic program states what (logic), not how (control)
- Programmer declares axioms
 - In Prolog, facts and rules
- Programmer states a theorem, or a goal (the what)
 - In Prolog, a query
- Language implementation determines how to use the axioms to prove the goal

Logic Programming

Logic programming style is characterized by

- Database of facts and rules that represent logical relations. Computation is modeled as search (queries) over this database
- Use of lists and use of recursion, which turns out very similar to the functional programming style

Logic Programming Concepts

- A Horn Clause is: $H \leftarrow B_1, B_2, ..., B_n$
 - Antecedents (B's): conjunction of zero or more terms in predicate calculus; this is the body of the horn clause
 - Consequent (H): a term in predicate calculus
- Resolution principle: if two Horn clauses

$$A \leftarrow B_1, B_2, B_3, \dots, B_m$$

 $C \leftarrow D_1, D_2, D_3, \dots, D_n$

are such that A matches D_1 ,

then we can replace D_1 with $B_1, B_2, B_3, ..., B_m$

$$C \leftarrow \underline{B_1, B_2, B_3, \dots, B_m, D_2, D_3, \dots, D_n}$$

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Horn Clauses in Prolog

- In Prolog, a Horn clause is written
 h:-b₁,...,b_n.
- Horn Clause is called clause
- Consequent is called goal or head
- Antecedents are called subgoals or tail

- Horn Clause with no tail is a fact
 - E.g., rainy(seattle). Depends on no other conditions
- Horn Clause with a tail is a rule snowy (X) :- rainy (X), cold (X).

Horn Clauses in Prolog

Clause is composed of terms

- Constants
 - Number, e.g., 123, etc.
 - Atoms e.g., seattle, rochester, rainy, foo In Prolog, atoms begin with a lower-case letter!

Variables

X, Foo, My_var, Seattle, Rochester, etc. In Prolog, variables begin with upper-case letter!

Structures

- E.g., rainy(seattle), snowy(X)
- Consists of an atom, called a functor and a list of arguments

Horn Clauses in Prolog

- Variables may appear in the tail and head of a rule:
 - c(X):- h(X,Y).
 For all values of X, c(X) is true if there exist a value of Y such that h(X,Y) is true
 - Call Y an auxiliary variable. Its value will be bound to make consequent true, but not reported by Prolog, because it does not appear in the head

Prolog

- Program has a database of clauses i.e., facts and rules; the rules help derive more facts
- We add simple queries with constants, variables, conjunctions or disjunctions

```
rainy(seattle).
rainy(rochester).
cold(rochester).
snowy(X) :- rainy(X),cold(X).
? - rainy(C).
? - snowy(C).
```

Facts

```
likes(eve, pie). food(pie).
likes(al, eve). food(apple).
likes(eve, tom). person(tom).
likes(eve, eve).
```

The combination of the functor and its arity (i.e., its number of arguments) is called a predicate.

Queries

```
likes(eve, pie).
                       food(pie).
 likes(al, eve).
                       food(apple).
 likes(eve, tom).
                       person(tom).
 likes(eve, eve).
                                   variable
                 query
?-likes(al,eve).
                      ?-likes(al, Who).
true. — answer
                      Who=eve.
                      ?-likes (eve, W) .answer with
?-likes(al,pie).
                                       variable binding
false.
                      W=pie
                      W=tom
?-likes(eve,al).
false.
                      W=eve
```

force search for

more answers

Question

```
likes(eve, pie). food(pie).
likes(al, eve). food(apple).
likes(eve, tom). person(tom).
likes(eve, eve).
```

```
?-likes(eve,W).
W = pie ;
W = tom ;
W = eve .
```

Prolog gives us the answer precisely in this order: first W=pie then W=tom and finally W=eve. Can you guess why?

Harder Queries

```
food(pie).
 likes(eve, pie).
 likes(al, eve). food(apple).
 likes(eve, tom). person(tom).
 likes(eve, eve).
?-likes(al,V) , likes(eve,V).
V=eve.
?-likes(eve,W) , person(W).
W=tom
?-likes(A,B).
A=eve,B=pie ; A=al,B=eve ; A=eve,B=tom ;
A=eve, B=eve.
?-likes(D,D).
D=eve.
```

Harder Queries

```
likes(eve, pie).
                     food(pie).
likes(al, eve).
                     food(apple).
likes(eve, tom). person(tom).
likes(eve, eve).
                    same binding
?-likes(eve, W), likes(W, V).
W=eve, V=pie ; W=eve, V=tom ; W=eve, V=eve.
?-likes(eve,W),person(W),food(V).
W=tom, V=pie; W=tom, V=apple
?-likes(eve, V), (person(V); food(V)).
V=pie ; V=tom
```

Rules

```
likes(eve, pie). food(pie).
likes(al, eve). food(apple).
likes(eve, tom). person(tom).
likes(eve, eve).
```

Add a rule to the database:

```
rule1:-likes(eve,V),person(V).

?-rule1.

true
```

Rules

```
likes(eve, pie). food(pie).
likes(al, eve). food(apple).
likes(eve, tom). person(tom).
likes(eve, eve).
rule1 :- likes(eve, V), person(V).
rule2(V) :- likes(eve, V), person(V).
```

```
?-rule2(H).
H=tom
?-rule2(pie).
false.
rule1 and rule2 are just like any other predicate!
```

Queen Victoria Example

```
male(albert).
                     Put all clauses in file
  male(edward).
  female(alice). family.pl
  female(victoria).
  parents(edward, victoria, albert).
  parents(alice, victoria, albert).
?- [family]. Loads file family.pl
  true.
  ?- male(albert). A query
  true.
  ?- male(alice).
  false.
  ?- parents(edward, victoria, albert).
  true.
  ?- parents(bullwinkle, victoria, albert).
  false.
```

cf Clocksin and Mellish

Queen Victoria Example

```
?-female(X). a query
X = alice ; ; asks for more answers
X = victoria.
```

- Variable x has been unified to all possible values that make female (X) true.
- Variables are upper-case, functors (predicates and constants) are lower-case!

Queen Victoria Example

 Facts alone do not make interesting programs. We need variables and deductive rules.

Another Prolog Program

```
rainy(seattle).
rainy(rochester).
cold(rochester).
snowy(X) :- rainy(X),cold(X).
?- [snowy].
?- rainy(C).
?- snowy(C).
```

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Logical Semantics

Prolog program consists of facts and rules

```
rainy(seattle).
rainy(rochester).
cold(rochester).
snowy(X):-rainy(X),cold(X).
```

Rules like snowy(X):- rainy(X), cold(X).

correspond to logical formulas:

```
\forall X[snowy(X) \leftarrow rainly(X) \land cold(X)]
```

/* For every X, X is snowy, if X is rainy and X is cold */

Logical Semantics

```
rainy(seattle).
rainy(rochester).
cold(rochester).
snowy(X):-rainy(X),cold(X).
```

A query such as ?- rainy(C).
triggers resolution. Logical semantics does
not impose restriction in the order of application
of resolution rules

Procedural Semantics

Find the first clause in the database whose head matches the query. In our case this is clause

```
snowy(X) :- rainy(X),cold(X)
```

Then, find a binding for x that makes rainy(x) true; then, check if cold(x) is true with that binding

- If yes, report binding as successful
- Otherwise, backtrack to the binding of x, unbind and consider the next binding
- Prolog's computation is well-defined procedurally by search tree, rule ordering, unification, backtracking, and backward chaining

Question

```
rainy(seattle).
rainy(rochester).
cold(rochester).
snowy(X):-rainy(X),cold(X).
snowy(troy).
What does this query yield?
?-snowy(C).
Answer:
C = rochester ;
C = troy.
```

Procedural Semantics

```
rainy (seattle).
 rainy (rochester).
 cold(rochester).
 snowy(X) := rainy(X), cold(X).
                          snowy (C)
                                  success
                          snowy (X)
                                            cold(seattle)
                            AND
                                                   $; backtrack.
             rainy(X)
                                                  cold(X)
X = seattle
                            X = rochester
                                              cold(rockester)
                     rainy (rochester)
rainy (seattle)
```

Prolog Concepts: Search Tree

```
OR levels:
 parent: goal (e.g., rainy (X))
                                        rainy(seattle).
 children: heads-of-clauses (rainy (...))
                                        rainy(rochester).
   ORDER: from left to right
                                        cold(rochester).
AND levels:
                                        snowy(X):=rainy(X),cold(X).
 parent: goal (e.g., snowy (X))
 children: subgoals (rainy(X), cold(X))
                                           snowy (C).
   ORDER: from left to right
                             snowy (C)
                             snowy(X)
               rainy(X)
                                                        cold(X)
                                                    cold(rochester)
                       rainy(rochester)
rainy (seattle)
                                                                        30
```

Prolog Concepts: Unification

- At OR levels Prolog performs unification
 - Unifies parent (goal), with child (head-of-clause)
- E.g.,
 - = snowy(C) = snowy(X)
 - \bullet success, C = X
 - rainy(X) = rainy(seattle)
 - success, X = seattle
 - parents(alice,M,F) = parents(edward,victoria,albert)
 - fail
 - parents(alice,M,F) = parents(alice,victoria,albert)
 - success, M = victoria, F = albert

In Prolog, = denotes unification, not assignment!

Prolog Concepts: Unification

- A constant unifies only with itself
 - E.g., alice=alice, but alice=edward fails
- Two structures unify if and only if (i) they have the same functor, (ii) they have the same number of arguments, and (iii) their arguments unify recursively
 - E.g., rainy(X) = rainy(seattle)

A variable unifies with anything. If the other thing has a value, then variable is bound to that value. If the other thing is an unbound variable, then the two variables are associated and if either one gets a value, both do

Prolog Concepts: Backtracking

```
rainy(seattle).
If at some point, a goal fails, Prolog backtracks
                                        rainy(rochester).
to the last goal (i.e., last unification point)
                                        cold(rochester).
where there is an untried binding, undoes
                                        snowy(X):=rainy(X),cold(X).
current binding and tries new binding (an
alternative OR branch), etc.
                                         ?-snowy(C).
                             snowy (C)
                             snowy (X)
                                                  cold(seattle)
                                                     fails; backtrack.
               rainy(X)
                                                        cold(X)
 X = seattle
                                                    cold(rochester)
rainy (seattle)
                       rainy (rochester)
```

Prolog Concepts: Backward Chaining

Backward chaining: starts from goal, towards facts ? - snowy(rochester). snowy(rochester):rainy(rochester), cold(rochester) rainy(rochester) snowy(rochester):cold(rochester) cold(rochester) snowy(rochester).

```
Forward chaining: starts from
  facts towards goal
? - snowy(rochester).
rainy(rochester)
snowy(rochester):-
    rainy(rochester),
    cold(rochester)
cold(rochester)
snowy(rochester):-
    cold(rochester)
snowy(rochester).
```

Exercise

```
takes(jane, his).
takes(jane, cs).
takes(ajit, art).
takes(ajit, cs).
classmates(X,Y):-takes(X,Z),takes(Y,Z).
?- classmates(jane,C).
```

Draw search tree for query.

What are the bindings for **c**?

The End