Statistical Methods Fall 2019

Assignment 4: Correlation, regression and contingency tables

Deadline: December 12, 21.59h

Topics of this assignment

The exercises below concern topics that were covered in Lectures 9 and 10: correlation, regression and contingency tables (see Sections 9.2 (incl. Part 2), 9.3 (incl. Part 3), 9.4, 10.2 and 10.3 (incl. Part 2) of the book and the slides of Lectures 9 and 10). Before making the assignment, study these topics. Numbers of exercises in the book refer to the twelfth edition (Pearson New International Edition).

How to make the exercises? See Assignment 1.

If you are asked to perform a test, do not only give the conclusion of your test, but report:

- the hypotheses in terms of the population parameter of interest;
- the significance level;
- the test statistic and its distribution under the null hypothesis;
- the observed value of the test statistic (the observed score);
- the *P*-value or the critical region;
- whether or not the null hypothesis is rejected and why.

If applicable, also phrase your conclusion in terms of the context of the problem.

Theoretical exercises

For the two theoretical exercises below use Tables 3 and 4 from the Appendix in the book to find probabilities and/or critical values. Do not use R. If you need to use a t-distribution with the number of degrees of freedom not included in Table 3, report the number of degrees of freedom, and use the critical value based on a t-distribution with the next lower number of degrees of freedom found in the table.

Exercise 4.1

Exercise 6 from Section 9.2 (Old Faithful).

The exercise description begins with the words "For 40 eruptions..."

(Note that Exercise 5 begins with the same words.)

Take significance level $\alpha = 10\%$ for hypothesis testing.

The value in the table is the sample linear correlation coefficient r = 0.091548.

(Follow the detailed instructions about testing presented above).

Exercise 4.2

Exercise 8 from Section 10.2 (Flat tire and missed class).

The exercise description begins with the words "A classic story..."

Take significance level $\alpha = 10\%$ for hypothesis testing.

(Follow the detailed instructions about testing presented above).

R-exercises

Do not use tables from the Appendix in the book. Use R to find probabilities and/or critical values.

Hints concerning R:

- The R-function cor() computes the sample linear correlation coefficient. The R-function cor.test() can be used to compute a confidence interval for the population correlation coefficient, and to perform a test concerning the population correlation coefficient. At the same time it also gives the sample correlation coefficient; here it is called 'sample estimate' (for the population linear correlation coefficient).
- For analysis of the linear regression model the R-function lm() can be used. Let the measurements of the explanatory variable be in the vector x and the measurements of the outcome variable be in y. Then lmsim=lm(y~x) fits a simple linear regression model and stores the output in lmsim. The output is a list, which can be studied using summary(lmsim). To obtain the estimated coefficients for the intercept and slope the command lmsim\$coef can be used. Similarly, lmsim\$res provides the residuals. The standard errors of the estimated coefficients can be obtained (apart from inspection of summary(lmsim)) with the command summary(lmsim)\$coef[,2]. To visualise the regression equation, the command abline(lmsim\$coef) can be used. See also the slides of Lecture 9.
- For the analysis of contingency tables the function chisq.test() can be used.

 The command chisq.test(table) \$exp provides the expected frequency count of the data in the fictitious contingency table table under the null hypothesis. See also the slides of Lecture 10.
- Recall: for computing probabilities and quantiles of normally, t-, chisquare, etc. distributed random variables the R-functions pnorm, pt, pchisq, ..., and qnorm, qt, qchisq, ... can be used. For the t- and chisquare distributions the number of degrees of freedom needs to be specified.
- You can load an .RData file into the workspace using the command load(...).

Exercise 4.3 There is considerable variation among individuals in their perception of crime, and in particular of which specific acts constitute a crime. A study was made to investigate which variables, like age, level of education, parental income, etc., may influence this perception. The file crimemale.txt contains part of the results of this study: data are given for 18 male college students who were asked how many of the following 25 acts they perceive as being a crime: aggravated assault, armed robbery, arson, atheism, auto theft, burglary, civil disobedience, communism, drug addiction, embezzlement, forcible rape, gambling, homosexuality, land fraud, nazism, payola, price fixing, prostitution, sexual abuse of child, sex discrimination, shoplifting, striking, strip mining, treason, vandalism. The column crimes contains the number of acts the students perceive as crimes, age the ages of the students, and income the incomes of the parents (in \$1000).

- a) Make for the data of the male students a scatterplot in which the x variable is **age** and the y variable is **crimes**. Compute also the sample linear correlation coefficient. Based on the plot and the sample linear correlation coefficient, do you think there is linear correlation between the two variables?
- b) Repeat part a with income as the x variable.
- c) Perform a linear regression analysis—i.e. formulate the regression model and compute the estimates of the unknown parameter values—with the variable <code>income</code> as the explanatory variable and the variable <code>crimes</code> as the response variable. Report the estimated values of the intercept and slope that determine the 'best' line and draw this 'best' line in the corresponding scatterplot.
- d) Using the results of the regression analysis of part c, test the claim that there is no linear relationship between the two variables income and crimes. Take significance level 5%. (See the first page of the assignment for detailed instructions about testing).
- e) In order to perform the test of part d, certain requirements have to be met. What are these requirements? Provide a suitable plot (or plots) and report whether the requirements are indeed met.

Exercise 4.4 During the previous Christmas party, the statistics teacher was asked to give an estimate of the general chances that Germany would win (or lose) against Italy in matches of the national men's soccer teams. He always thought that he knew a lot about soccer, so he was confident that the following guess was appropriate (from a German point of view):

	Wins	Draws	Defeats	(*)
men	30%	40%	30%	(*)

The following table shows the actual results (of both German men's and women's national soccer results against Italy):

	Wins	Draws	Defeats
men	8	12	15
women	16	8	4

- a) Compute the expected frequency of German men's wins against Italy under the assumption that the teacher's guess (*) was true.
- b) Use the significance level $\alpha = 5\%$ to test the teacher's guess (*) with a goodness-of-fit test. (See the first page of the assignment for detailed instructions about testing).

Furthermore, the teacher claimed that the German men and women have the same chances of winning or losing against or tie with the Italians. (**)

- c) Should you use a test of independence or a test of homogeneity to test the teacher's second claim (**)? Motivate your answer and formulate the null and alternative hypothesis.
- d) Create a matrix results containing the data and use it to perform the test of part c). Take significance level $\alpha = 5\%$. (See the first page of the assignment for detailed instructions about testing).
- e) Supposing the second claim (**) is true, what is the expected number of wins of the German men?
- f) Now combine Draws and Defeats among each, men and women. This results in this 2×2 table:

	Draws/Defeats	Wins
men	27	8
women	12	16

Use Fisher's exact test and significance level $\alpha = 1\%$ to test the directed claim

 H_a : "The German men are more likely to lose against/tie with Italy than the German women."

(See the first page of the assignment for detailed instructions about testing).