Formal Specification of the Cardano Ledger for the Conway era

Andre Knispel andre.knispel@iohk.io

William DeMeo william.demeo@iohk.io

Joosep Jääger joosep.jaager@iohk.io

Carlos Tomé Cortiñas carlos.tome-cortinas@iohk.io

Abstract

This document presents the modifications to the previous specifications of the Cardano ledger (see [1]–[4]) for the Conway era. The additions mostly relate to the implementation of the governance framework described in CIP-1694 [5].

List of Contributors

Alasdair Hill, Ulf Norell, Orestis Melkonian, Jared Corduan, Alexey Kuleshevich

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1 Introduction

This is the specification of the Conway era of the Cardano ledger. As with previous specifications, this document is an incremental specification, so everything that isn't defined here refers to the most recent definition from an older specification.

Note: As of now, this specification is still a draft. Some details and explanations may be missing or wrong.

1.1 A Note on Agda

This specification is written using the Agda programming language and proof assistant [6]. We have made a considerable effort to ensure that this document is readable by people unfamiliar with Agda (or other proof assistants, functional programming languages, etc.). However, by the nature of working in a formal language we have to play by its rules, meaning that some instances of uncommon notation are very difficult or impossible to avoid. Some are explained in Sec. 2 and Appendix A, but there is no guarantee that those sections are complete. If the meaning of an expression is confusing or unclear, please open an issue in the formal ledger GitHub repository with the 'notation' label.

1.2 Separation of Concerns

The Cardano Node consists of three pieces,

- a networking layer responsible for sending messages across the internet,
- a consensus layer establishing a common order of valid blocks, and
- a ledger layer which determines whether a sequence of blocks is valid.

Because of this separation, the ledger gets to be a state machine,

$$s \xrightarrow{b} s'$$
.

More generally, we will consider state machines with an environment,

$$\Gamma \vdash s \xrightarrow{b} s'$$
.

These are modelled as 4-ary relations between the environment Γ , an initial state s, a signal b and a final state s'. The ledger consists of roughly 25 (depending on the version) such relations that depend on each other, forming a directed graph that is almost a tree. Thus each such relation represents the transition rule of the state machine; X is simply a placeholder for the name of the transition rule.

1.3 Reflexive-transitive Closure

Some state transition rules need to be applied as many times as possible to arrive at a final state. Since we use this pattern multiple times, we define a closure operation which takes a transition rule and applies it as many times as possible.

The closure $_\vdash_ \rightharpoonup \llbracket_\rrbracket *_$ of a relation $_\vdash_ \rightharpoonup \llbracket_\rrbracket__$ is defined in Fig. 1. In the remainder of the text, the closure operation is called ReflexiveTransitiveClosure.

```
module _ (_\top-\top^\[_]__ : C \top S \top Sig \to S \to Type) where

Closure type

data _\top-\top^\[_]*_ : C \top S \top List Sig \to S \to Type where

Closure rules

RTC-base :

\Gamma \vdash s \to [\ ]\ ]* s

RTC-ind :

\circ \Gamma \vdash s \to [\ sig \ ]* s''

\circ \Gamma \vdash s' \to [\ sigs \ ]* s''

\Gamma \vdash s \to [\ sigs \ ]* s''
```

Figure 1: Reflexive transitive closure

Figure 2: Computational relations

1.4 Computational

Since all such state machines need to be evaluated by the nodes and all nodes should compute the same states, the relations specified by them should be computable by functions. This can be captured by the definition in Fig. 2 which is parametrized over the state transition relation.

Unpacking this, we have a compute function that computes a final state from a given environment, state and signal. The second piece is correctness: compute succeeds with some final state if and only if that final state is in relation to the inputs.

This has two further implications:

- Since compute is a function, the state transition relation is necessarily a (partial) function; i.e., there is at most one possible final state for each input data. Otherwise, we could prove that compute could evaluates to two different states on the same inputs, which is impossible since it is a function.
- The actual definition of compute is irrelevant—any two implementations of compute have to produce the same result on any input. This is because we can simply chain the equivalences for two different compute functions together.

What this all means in the end is that if we give a Computational instance for every relation defined in the ledger, we also have an executable version of the rules which is guaranteed to be correct. This is indeed something we have done, and the same source code that generates this document also generates a Haskell library that lets anyone run this code.

1.5 Sets & Maps

The ledger heavily uses set theory. For various reasons it was necessary to implement our own set theory (there will be a paper on this some time in the future). Crucially, the set theory is completely abstract (in a technical sense—Agda has an abstract keyword) meaning that implementation details of the set theory are irrelevant. Additionally, all sets in this specification are finite.

We use this set theory to define maps as seen below, which are used in many places. We usually think of maps as partial functions (i.e., functions not necessarily defined everywhere—equivalently, "left-unique" relations) and we use the harpoon arrow \rightarrow to distinguish such maps from standard Agda functions which use \rightarrow . The figure below also gives notation for the powerset operation, \mathbb{P} , used to form a type of sets with elements in a given type, as well as the subset relation and the equality relation for sets.

```
_C_ : {A : Type} → P A → P A → Type

X \subseteq Y = \forall \{x\} \rightarrow x \in X \rightarrow x \in Y

_=e_ : {A : Type} → P A → P A → Type

X \equiv ^e Y = X \subseteq Y \times Y \subseteq X

Rel : Type → Type → Type

Rel A B = P (A × B)

left-unique : {A B : Type} → Rel A B → Type

left-unique R = \forall \{a \ b \ b'\} \rightarrow (a \ , b) \in R \rightarrow (a \ , b') \in R \rightarrow b \equiv b'

___ : Type → Type → Type

A \to B = r \in Rel A B \, left-unique r
```

1.6 Propositions as Types, Properties and Relations

In type theory we represent propositions as types and proofs of a proposition as elements of the corresponding type. A unary predicate is a function that takes each x (of some type A) and returns a proposition P(x). Thus, a predicate is a function of type $A \to Type$. A binary relation P(x) between P(x) and P(x) are taken a pair of values P(x) and P(x) and returns a proposition asserting that the relation P(x) holds between P(x) and P(x). Thus, such a relation is a function of type P(x) and P(x) are the proposition as P(x) are the proposition as P(x) and P(x) are the proposition as P(x) are the proposition as P(x) and P(x) are the proposition as P(x) and P(x) are the proposition as P(x) and P(x) are the proposit

2 Notation

This section introduces some of the notation we use in this document and in our Agda formalization.

Propositions, sets and types. In this document the abstract notions of "set" and "type" are essentially the same, despite having different formal definitions in our Agda code. We represent sets as a special type, which we denote by Set A, for A an arbitrary type. (See Sec. 1.5 for details and Nordström, Petersson, and Smith [7, Ch. 19] for background.) Agda denotes the primitive notion of type by Set. To avoid confusion, throughout this document and in our Agda code we call this primitive Type, reserving the name Set for our set type. All of our sets are finite, and when we need to convert a list 1 to its set of elements, we write from List 1.

- **Lists** We use the notation a :: as for the list with head a and tail as; [] denotes the empty list, and 1 :: x appends the element x to the end of the list 1.
- Sums and products. The sum (or disjoint union, coproduct, etc.) of A and B is denoted by $A \uplus B$, and their product is denoted by $A \times B$. The projection functions from products are denoted proj_1 and proj_2 , and the injections are denoted inj_1 and inj_2 respectively. The properties whether an element of a coproduct is in the left or right component are called isInj_1 and isInj_2 .
- Addition of map values. The expression $\sum [x \in m] f x$ denotes the sum of the values obtained by applying the function f to the values of the map m.
- **Record types** are explained in Appendix A.
- **Postfix projections.** Projections can be written using postfix notation. For example, we may write x .proj₁ instead of proj₁ x.
- **Restriction, corestriction and complements.** The restriction of a function or map f to some domain A is denoted by $f \mid A$, and the restriction to the complement of A is written $f \mid A$. Corestriction or range restriction is denoted similarly, except that \mid is replaced by $\mid \land$.
- **Inverse image.** The expression m^{-1} B denotes the inverse image of the set B under the map m.
- **Left-biased union.** For maps m and m', we write $m \cup^1 m'$ for their left-biased union. This means that key-value pairs in m are guaranteed to be in the union, while key-value pairs in m' will be in the union if and only if the keys don't collide.
- **Map addition.** For maps m and m', we write $m \cup^+ m'$ for their union, where keys that appear in both maps have their corresponding values added.
- **Mapping a partial function.** A partial function is a function on A which may not be defined for all elements of A. We denote such a function by $f:A \to B$. If we happen to know that the function is total (defined for all elements of A), then we write $f:A \to B$. The mapPartialoperation takes such a function f and a set S of elements of A and applies f to the elements of S at which it is defined; the result is the set $\{f \mid x \mid x \in S \text{ and } f \text{ is defined at } x\}$.
- The Maybe type represents an optional value and can either be just x (indicating the presence of a value, x) or nothing (indicating the absence of a value). If x has type X, then just x has type Maybe X.
 - The symbol \sim denotes (pseudo)equality of two values x and y of type Maybe X: if x is of the form just x' and y is of the form just y', then x' and y' have to be equal. Otherwise, they are considered "equal".
- The unit type τ has a single inhabitant tt and may be thought of as a type that carries no information; it is useful for signifying the completion of an action, the presence of a trivial value, a trivially satisfied requirement, etc.

2.1 Superscripts and Other Special Notations

In the current version of this specification, superscript letters are heavily used for things such as disambiguations or type conversions. These are essentially meaningless, only present for technical reasons and can safely be ignored. However there are the two exceptions:

- \cup^1 for left-biased union
- c in the context of set restrictions, where it indicates the complement

Also, non-letter superscripts do carry meaning.¹

Finally, there are some ? and $\dot{\epsilon}$ operations. These relate to decision procedures and can also safely be ignored.²

¹At some point in the future we hope to be able to remove all those non-essential superscripts. Since we prefer doing this by changing the Agda source code instead of via hiding them in this document, this is a non-trivial problem that will take some time to address.

²We plan on refactoring the code so that these special symbols will also disappear from this document.

3 Protocol Parameters

This section is part of the Ledger.PParams module of the formal ledger specification, in which we define the adjustable protocol parameters of the Cardano ledger.

Protocol parameters are used in block validation and can affect various features of the system, such as minimum fees, maximum and minimum sizes of certain components, and more.

```
data PParamGroup: Type where

NetworkGroup: PParamGroup
EconomicGroup: PParamGroup
TechnicalGroup: PParamGroup
GovernanceGroup: PParamGroup
SecurityGroup: PParamGroup
```

Figure 3: Protocol parameter group definition

```
record DrepThresholds: Type where
field
P1 P2a P2b P3 P4 P5a P5b P5c P5d P6: 

record PoolThresholds: Type where
field
Q1 Q2a Q2b Q4 Q5: 

Q
```

Figure 4: Protocol parameter threshold definitions

PParams contains parameters used in the Cardano ledger, which we group according to the general purpose that each parameter serves.

- NetworkGroup: parameters related to the network settings;
- EconomicGroup: parameters related to the economic aspects of the ledger;
- TechnicalGroup: parameters related to technical settings;
- GovernanceGroup: parameters related to governance settings;
- SecurityGroup: parameters that can impact the security of the system.

The purpose of these groups is to determine voting thresholds for proposals aiming to change parameters. Given a proposal to change a certain set of parameters, we look at which groups those parameters fall into and from this we determine the voting threshold for that proposal. (The voting threshold calculation is described in detail in Sec. 12.1; in particular, the definition of the threshold function appears in Fig. 41.)

The first four groups have the property that every protocol parameter is associated to precisely one of these groups. The SecurityGroup is special: a protocol parameter may or may not be in the SecurityGroup. So, each protocol parameter belongs to at least one and at most two groups. Note that in CIP-1694 there is no SecurityGroup, but there is the concept of security-relevant protocol parameters (see Corduan, Knispel, Benkort, et al. [5]). The difference between these notions is only social, so we implement security-relevant protocol parameters as a group.

The new protocol parameters are declared in Fig. 5 and denote the following concepts:

- drepThresholds: governance thresholds for DReps; these are rational numbers named P1, P2a, P2b, P3, P4, P5a, P5b, P5c, P5d, and P6;
- poolThresholds: pool-related governance thresholds; these are rational numbers named Q1, Q2a, Q2b, Q4 and Q5;
- ccMinSize: minimum constitutional committee size;
- ccMaxTermLength: maximum term limit (in epochs) of constitutional committee members;
- govActionLifetime: governance action expiration;
- govActionDeposit: governance action deposit;
- drepDeposit: DRep deposit amount;
- drepActivity: DRep activity period;
- minimumAVS: the minimum active voting threshold.

Fig. 5 also defines the function paramsWellFormed which performs some sanity checks on protocol parameters. Fig. 7 defines types and functions to update parameters. These consist of an abstract type UpdateT and two functions applyUpdate and updateGroups. The type UpdateT is to be instantiated by a type that

- can be used to update parameters, via the function applyUpdate
- can be queried about what parameter groups it updates, via the function updateGroups

An element of the type UpdateT is well formed if it updates at least one group and applying the update preserves well-formedness.

```
record PParams : Type where
   field
Network group
     maxBlockSize
                               : N
     maxTxSize
                               : N
     maxHeaderSize
                               : N
     maxTxExUnits
                               : ExUnits
     maxBlockExUnits
                               : ExUnits
     maxValSize
                               : IN
     maxCollateralInputs
                               : N
Economic group
     а
                                : IN
                               : N
     keyDeposit
                               : Coin
     poolDeposit
                               : Coin
     coinsPerUTxOByte
                               : Coin
                               : Prices
     prices
     minFeeRefScriptCoinsPerByte: @
     maxRefScriptSizePerTx
     maxRefScriptSizePerBlock : N
     refScriptCostStride
                                : N
     refScriptCostMultiplier
                               : Q
Technical group
     Emax
                                : Epoch
     nopt
                                : IN
                                : 0
     collateralPercentage
                               : N
     costmdls
                               : CostModel
Governance group
                               : PoolThresholds
     poolThresholds
     drepThresholds
                               : DrepThresholds
     ccMinSize
                               : IN
     ccMaxTermLength
                               : N
     govActionLifetime
                               : IN
     govActionDeposit
                               : Coin
     drepDeposit
                               : Coin
     drepActivity
                               : Epoch
Security group
maxBlockSize maxTxSize maxHeaderSize maxValSize maxBlockExUnits a b minFeeRefScript-
CoinsPerByte coinsPerUTxOByte govActionDeposit
```

Figure 5: Protocol parameter definitions

Figure 6: Protocol parameter well-formedness

```
Abstract types & functions

UpdateT : Type
applyUpdate : PParams → UpdateT → PParams
updateGroups : UpdateT → P PParamGroup

Well-formedness condition

ppdWellFormed : UpdateT → Type
ppdWellFormed u = updateGroups u ≠ ∅
x ∀ pp → paramsWellFormed pp → paramsWellFormed (applyUpdate pp u)
```

Figure 7: Abstract type for parameter updates

Figure 8: Calculation of fees for reference scripts

4 Fee Calculation

This section is part of the Ledger. Fees module of the formal ledger specification, where we define the functions used to compute the fees associated with reference scripts.

The function scriptsCost (Fig. 8) calculates the fee for reference scripts in a transaction. It takes as input the total size of the reference scripts in bytes—which can be calculated using refScriptsSize (Fig. 17)—and uses a function (scriptsCostAux) that is piece-wise linear in the size, where the linear constant multiple grows with each refScriptCostStride bytes. In addition, scriptsCost depends on the following constants (which are bundled with the protocol parameters; see Fig. 5):

- refScriptCostMultiplier, a rational number, the growth factor or step multiplier that determines how much the price per byte increases after each increment;
- refScriptCostStride, an integer, the size in bytes at which the price per byte grows linearly;
- minFeeRefScriptCoinsPerByte, a rational number, the base fee or initial price per byte.

5 Governance Actions

This section is part of the Ledger.GovernanceActions module of the formal ledger specification. We introduce the following distinct bodies with specific functions in the new governance framework:

- 1. a constitutional committee (henceforth called CC);
- 2. a group of delegate representatives (henceforth called DReps);
- 3. the stake pool operators (henceforth called SPOs).

Fig. 9 defines several data types used to represent governance actions. The type DocHash is abstract but in the implementation it will be instantiated with a 32-bit hash type (like e.g. ScriptHash). We keep it separate because it is used for a different purpose.

- GovActionID: a unique identifier for a governance action, consisting of the TxId of the proposing transaction and an index to identify a proposal within a transaction;
- GovRole (governance role): one of three available voter roles defined above (CC, DRep, SPO);
- VDeleg (voter delegation): one of three ways to delegate votes: by credential, abstention, or no confidence (credVoter, abstainRep, or noConfidenceRep);
- Anchor: a url and a document hash;
- GovAction (governance action): one of seven possible actions (see Fig. 10 for definitions);

The governance actions carry the following information:

- UpdateCommittee: a map of credentials and terms to add and a set of credentials to remove from the committee;
- NewConstitution: a hash of the new constitution document and an optional proposal policy;
- TriggerHF: the protocol version of the epoch to hard fork into;
- ChangePParams: the updates to the parameters; and
- TreasuryWdrl: a map of withdrawals.

5.1 Hash Protection

For some governance actions, in addition to obtaining the necessary votes, enactment requires that the following condition is also satisfied: the state obtained by enacting the proposal is in fact the state that was intended when the proposal was submitted. This is achieved by requiring actions to unambiguously link to the state they are modifying via a pointer to the previous modification. A proposal can only be enacted if it contains the <code>GovActionID</code> of the previously enacted proposal modifying the same piece of state. <code>NoConfidence</code> and <code>UpdateCommittee</code> modify the same state, while every other type of governance action has its own state that isn't shared with any other action. This means that the enactibility of a proposal can change when other proposals are enacted.

However, not all types of governance actions require this strict protection. For TreasuryWdrl and Info, enacting them does not change the state in non-commutative ways, so they can always be enacted.

Types related to this hash protection scheme are defined in Fig. 11.

³There are many varying definitions of the term "hard fork" in the blockchain industry. Hard forks typically refer to non-backwards compatible updates of a network. In Cardano, we attach a bit more meaning to the definition by calling any upgrade that would lead to *more blocks* being validated a "hard fork" and force nodes to comply with the new protocol version, effectively rendering a node obsolete if it is unable to handle the upgrade.

5.2 Votes and Proposals

The data type Vote represents the different voting options: yes, no, or abstain. For a Vote to be cast, it must be packaged together with further information, such as who votes and for which governance action. This information is combined in the GovVote record. An optional Anchor can be provided to give context about why a vote was cast in a certain manner.

To propose a governance action, a GovProposal needs to be submitted. Beside the proposed action, it requires:

- potentially a pointer to the previous action (see Sec. 5.1),
- potentially a pointer to the proposal policy (if one is required),
- a deposit, which will be returned to returnAddr, and
- an Anchor, providing further information about the proposal.

While the deposit is held, it is added to the deposit pot, similar to stake key deposits. It is also counted towards the voting stake (but not the block production stake) of the reward address to which it will be returned, so as not to reduce the submitter's voting power when voting on their own (and competing) actions. For a proposal to be valid, the deposit must be set to the current value of <code>govActionDeposit</code>. The deposit will be returned when the action is removed from the state in any way.

GovActionState is the state of an individual governance action. It contains the individual votes, its lifetime, and information necessary to enact the action and to repay the deposit.

```
data GovRole: Type where
 CC DRep SPO : GovRole
           = GovRole × Credential
GovActionID = TxId \times N
data VDeleg: Type where
 credVoter
                 : GovRole → Credential → VDeleg
 abstainRep
                                         VDeleg
 noConfidenceRep :
                                         VDeleg
record Anchor: Type where
 field
   url : String
   hash: DocHash
data GovActionType : Type where
 NoConfidence : GovActionType
 UpdateCommittee : GovActionType
 NewConstitution : GovActionType
 TriggerHF : GovActionType
 ChangePParams : GovActionType
 TreasuryWdrl : GovActionType
                 : GovActionType
GovActionData: GovActionType → Type
GovActionData NoConfidence
                           = T
GovActionData UpdateCommittee = (Credential → Epoch) × P Credential × ℚ
GovActionData NewConstitution = DocHash x Maybe ScriptHash
GovActionData TriggerHF
                           = ProtVer
GovActionData ChangePParams = PParamsUpdate
GovActionData TreasuryWdrl = RwdAddr → Coin
GovActionData Info
record GovAction : Type where
 constructor [_,_]ga
 field
   gaType : GovActionType
   gaData : GovActionData gaType
open GovAction public
```

Figure 9: Governance actions

Action	Description
NoConfidence	a motion to create a <i>state of no-confidence</i> in the current constitutional committee
UpdateCommittee	changes to the members of the constitutional committee and/or to its signature threshold and/or terms
NewConstitution	a modification to the off-chain Constitution and the proposal policy script
TriggerHF ³	triggers a non-backwards compatible upgrade of the network; requires a prior software upgrade
ChangePParams	a change to <i>one or more</i> updatable protocol parameters, excluding changes to major protocol versions ("hard forks")
TreasuryWdrl	movements from the treasury
Info	an action that has no effect on-chain, other than an on-chain record

Figure 10: Types of governance actions

```
NeedsHash : GovActionType → Type
NeedsHash NoConfidence = GovActionID
NeedsHash UpdateCommittee = GovActionID
NeedsHash NewConstitution = GovActionID
NeedsHash TriggerHF = GovActionID
NeedsHash ChangePParams = GovActionID
NeedsHash TreasuryWdrl = T
NeedsHash Info = T
HashProtected : Type → Type
HashProtected A = A × GovActionID
```

Figure 11: NeedsHash and HashProtected types

```
data Vote: Type where
 yes no abstain : Vote
record GovVote: Type where
 field
   gid
             : GovActionID
             : Voter
   voter
   vote
             : Vote
   anchor : Maybe Anchor
record GovProposal : Type where
 field
            : GovAction
   action
   prevAction : NeedsHash (gaType action)
   policy : Maybe ScriptHash
   deposit
             : Coin
   returnAddr : RwdAddr
            : Anchor
   anchor
record GovActionState : Type where
 field
   votes
            : Voter → Vote
   returnAddr : RwdAddr
   expiresIn : Epoch
            : GovAction
   action
   prevAction : NeedsHash (gaType action)
```

Figure 12: Vote and proposal types

```
getDRepVote : GovVote → Maybe Credential
getDRepVote record { voter = (DRep , credential) } = just credential
getDRepVote _ = nothing

proposedCC : GovAction → P Credential
proposedCC [ UpdateCommittee , (x , _ , _ ) ] ga = dom x
proposedCC _ = ∅
```

Figure 13: Governance helper function

6 Transactions

This section is part of the Ledger. Transaction module of the formal ledger specification, where we define transactions.

A transaction consists of a transaction body, a collection of witnesses and some optional auxiliary data.

Ingredients of the transaction body introduced in the Conway era are the following:

- txvote, the list of votes for governnce actions;
- txprop, the list of governance proposals;
- txdonation, amount of Coin to donate to treasury, e.g., to return money to the treasury after a governance action;
- curTreasury, the current value of the treasury. This field serves as a precondition to executing Plutus scripts that access the value of the treasury;
- txsize and txid, the size and hash of the serialized form of the transaction that was included in the block.

```
Abstract types
 Ix TxId AuxiliaryData : Type
Transaction types
 record TxBody: Type where
   field
     txins
                   : P TxIn
                  : P TxIn
     refInputs
                  : Ix → TxOut
     txouts
     txfee
                   : Coin
     mint
                   : Value
     txvldt
                   : Maybe Slot × Maybe Slot
     txcerts
                  : List DCert
     txwdrls
                  : Wdrl
     txvote
                  : List GovVote
                  : List GovProposal
     txprop
     txdonation
                  : Coin
                  : Maybe Update
     txup
     txADhash
                  : Maybe ADHash
     txNetworkId : Maybe Network
     curTreasury : Maybe Coin
     txsize
                   : N
     txid
                  : TxId
     collateral
                  : P TxIn
     reqSigHash
                  : ℙ KeyHash
     scriptIntHash : Maybe ScriptHash
```

Figure 14: Transactions and related types

7 UTxO

This section is part of the Ledger. Utxo module of the formal ledger specification, where we define types and functions needed for the UTxO transition system.

7.1 Accounting

Figs. 15 to 17 define types and functions needed for the UTxO transition system.

The deposits have been reworked since the original Shelley design. We now track the amount of every deposit individually. This fixes an issue in the original design: An increase in deposit amounts would allow an attacker to make lots of deposits before that change and refund them after the change. The additional funds necessary would have been provided by the treasury. Since changes to protocol parameters were (and still are) known publicly and guaranteed before they are enacted, this comes at zero risk for an attacker. This means the deposit amounts could realistically never be increased. This issue is gone with the new design.

Similar to ScriptPurpose, DepositPurpose carries the information what the deposit is being made for. The deposits are stored in the deposits field of UTxOState (the type Deposits is defined in Fig. 29). updateDeposits is responsible for updating this map, which is split into updateCertDeposits and updateProposalDeposits, responsible for certificates and proposals respectively. Both of these functions iterate over the relevant fields of the transaction body and insert or remove deposits depending on the information seen. Note that some deposits can only be refunded at the epoch boundary and are not removed by these functions.

There are two equivalent ways to introduce this tracking of the deposits. One option would be to populate the deposits field of UTxOState with the correct keys and values that can be extracted from the state of the previous era at the transition into the Conway era. Alternatively, we can effectively treat the old handling of deposits as an erratum in the Shelley specification, which we fix by implementing the new deposits logic in older eras and then replaying the chain. (The handling of deposits in the Shelley era is discussed in Corduan, Vinogradova, and Güdemann [1, Sec 8] and IOHK Formal Methods Team [8, Sec B.2].)

```
record UTxOState: Type where
field
  utxo : UTxO
  fees : Coin
  deposits : Deposits
  donations : Coin
```

Figure 15: UTxO transition-system types

As seen in Figs. 16 and 17, we redefine depositRefunds and newDeposits via depositsChange, which computes the difference between the total deposits before and after their application. This simplifies their definitions and some correctness proofs. We then add the absolute value of depositsChange to consumed or produced depending on its sign. This is done via negPart and posPart, which satisfy the key property that their difference is the identity function.

Fig. 16 defines the function minfee. In Conway, minfee includes the cost for reference scripts. This is calculated using scriptsCost (see Fig. 8).

Fig. 16 also shows the signature of ValidCertDeposits. Inhabitants of this type are constructed in one of eight ways, corresponding to seven certificate types plus one for an empty list of certificates. Suffice it to say that ValidCertDeposits is used to check the validity of the

```
refScriptsSize : UTxO \rightarrow Tx \rightarrow \mathbb{N}
refScriptsSize utxo tx = sum $ map scriptSize (refScripts tx utxo)
minfee : PParams → UTxO → Tx → Coin
minfee pp utxo tx = pp .a * tx .body .txsize + pp .b
                  + txscriptfee (pp .prices) (totExUnits tx)
                  + scriptsCost pp (refScriptsSize utxo tx)
certDeposit : DCert → PParams → Deposits
certDeposit (delegate c - v) = { CredentialDeposit c \cdot v }
                          pp = { CredentialDeposit c , pp .keyDeposit }
certDeposit (reg c _)
certDeposit (regpool kh _) pp = { PoolDeposit kh , pp .poolDeposit }
certDeposit (regdrep c v_{-}) = { DRepDeposit c , v }
certDeposit _
                                = 0
certRefund : DCert → P DepositPurpose
certRefund (dereg c _)
                          = { CredentialDeposit c }
certRefund (deregdrep c _) = { DRepDeposit c }
certRefund _
                           = Ø
data ValidCertDeposits (pp : PParams) (deps : Deposits) : List DCert → Set
```

Figure 16: Functions used in UTxO rules

```
depositRefunds : PParams → UTxOState → TxBody → Coin
depositRefunds pp st txb = negPart (depositsChange pp txb (st .deposits))

newDeposits : PParams → UTxOState → TxBody → Coin
newDeposits pp st txb = posPart (depositsChange pp txb (st .deposits))

consumed : PParams → UTxOState → TxBody → Value
consumed pp st txb
= balance (st .utxo | txb .txins)
+ txb .mint
+ inject (depositRefunds pp st txb)
+ inject (getCoin (txb .txwdrls))

produced : PParams → UTxOState → TxBody → Value
produced pp st txb = balance (outs txb)
+ inject (txb .txfee)
+ inject (newDeposits pp st txb)
+ inject (txb .txdonation)
```

Figure 17: Functions used in UTxO rules, continued

deposits in a transaction so that the function updateCertDeposits can correctly register and deregister deposits in the UTxO state based on the certificates in the transaction.

```
Scripts-Yes:

let pp = Γ.pparams

sLst = collectPhaseTwoScriptInputs pp tx utxo

in

• ValidCertDeposits pp deposits txcerts

• evalScripts tx sLst = isValid

• isValid = true

Γ⊢ [ utxo , fees , deposits , donations ] → ( tx ,UTXOS) [ (utxo | txins °) ∪¹ (outs txb) , fees

Scripts-No:

let pp = Γ.pparams

sLst = collectPhaseTwoScriptInputs pp tx utxo

in

• evalScripts tx sLst = isValid

• isValid = false

Γ⊢ [ utxo , fees , deposits , donations ] → ( tx ,UTXOS) [ utxo | collateral ° , fees + cbalance
```

Figure 18: UTXOS rule

Fig. 19 ties all the pieces of the UTXO rule together (The symbol **≡?** is explained in Sec. 2).

```
UTXO-inductive:
  let pp = \Gamma .pparams
      slot
               =\Gamma .slot
      treasury = \Gamma \cdot treasury
               = s .UTxOState.utxo
      txouts h = mapValues txOutHash txouts
      overhead = 160
  in
                              • txins ∪ refInputs ⊆ dom utxo
  • txins ≢ ∅
  • txins ∩ refInputs = ∅ • inInterval slot txvldt
  • feesOK pp tx \ utxo • consumed pp s \ txb \equiv produced pp s \ txb
  • coin mint ≡ 0

    txsize ≤ maxTxSize pp

  • refScriptsSize utxo tx ≤ pp .maxRefScriptSizePerTx
  • \forall [(\_, txout) \in txouts^h .proj_1]
      inject ((overhead + utxoEntrySize txout) * coinsPerUTxOByte pp) ≤ t getValue txout
  • \forall [(\_, txout) \in txouts^h.proj_1]
      serSize (getValue<sup>h</sup> txout) ≤ maxValSize pp
  • ∀[ (a , _) ∈ range txouts h ]
      Sum.All (const \tau) (\lambda a \rightarrow a .BootstrapAddr.attrsSize \leq 64) \alpha
  • \forall [ (a, \_) \in \text{range } txouts^h ] \text{ netId } a
                                                ■ NetworkId
  • \forall [a \in dom \ txwdrls]
                               a .RwdAddr.net ≡ NetworkId
  • txNetworkId ~ just NetworkId
  • curTreasury ~ just treasury
  • \Gamma \vdash s \rightharpoonup \emptyset tx ,UTXOSD s'
    \Gamma \vdash s \rightharpoonup \emptyset tx , UTX00 s'
```

Figure 19: UTXO inference rules

7.2 Witnessing

This section is part of the Ledger. Utxow module of the formal ledger specification, in which we define witnessing.

The purpose of witnessing is make sure the intended action is authorized by the holder of the signing key. (For details see Corduan, Vinogradova, and Güdemann [1, Sec 8.3].) Fig. 20 defines functions used for witnessing. witsVKeyNeeded and scriptsNeeded are now defined by projecting the same information out of credsNeeded. Note that the last component of credsNeeded adds the script in the proposal policy only if it is present.

allowedLanguages has additional conditions for new features in Conway. If a transaction contains any votes, proposals, a treasury donation or asserts the treasury amount, it is only allowed to contain Plutus V3 scripts. Additionally, the presence of reference scripts or inline scripts does not prevent Plutus V1 scripts from being used in a transaction anymore. Only inline datums are now disallowed from appearing together with a Plutus V1 script.

7.3 Plutus script context

CIP-0069 unifies the arguments given to all types of Plutus scripts currently available (spending, certifying, rewarding, minting, voting, proposing).

The formal specification permits running spending scripts in the absence datums in the Conway era. However, since the interface with Plutus is kept abstract in this specification, changes to the representation of the script context which are part of CIP-0069 are not included here. To provide a CIP-0069-conformant implementation of Plutus to this specification, an additional step processing the List Data argument we provide would be required.

In Fig. 22, the line *inputHashes* \subseteq *txdatsHashes* compares two inhabitants of $\mathbb P$ DataHash. In the Alonzo spec, these two terms would have inhabited $\mathbb P$ (Maybe DataHash), where a nothing is thrown out [3, Sec 3.1].

```
getVKeys: P Credential → P KeyHash
getVKeys = mapPartial isKeyHashObj
allowedLanguages : Tx \rightarrow UTx0 \rightarrow P Language
allowedLanguages tx utxo =
  if (\exists [o \in os] isBootstrapAddr (proj_1 o))
    then ø
  else if UsesV3Features txb
    then fromList (PlutusV3 :: [])
  else if \exists [o \in os] HasInlineDatum o
    then fromList (PlutusV2 :: PlutusV3 :: [])
    fromList (PlutusV1 :: PlutusV2 :: PlutusV3 :: [])
  where
    txb = tx . Tx.body; open TxBody txb
    os = range (outs txb) U range (utxo | (txins U refInputs))
getScripts : P Credential → P ScriptHash
getScripts = mapPartial isScriptObj
credsNeeded : UTxO → TxBody → P (ScriptPurpose × Credential)
credsNeeded utxo txb
  = map<sup>s</sup> (\lambda (i, o) \rightarrow (Spend i, payCred (proj_1 o))) ((utxo | (txins \cup collateral)) s)
                    \rightarrow (Rwrd a, stake a)) (dom (txwdrls .proj<sub>1</sub>))
  U mapPartial (\lambda c \rightarrow (Cert c_{,-}) < s > cwitness c) (fromList txcerts)
  U map^s (\lambda x)
                    \rightarrow (Mint x, ScriptObj x)) (policies mint)
  U map<sup>s</sup> (λ v
                     → (Vote v , proj₂ v)) (fromList (map voter txvote))
  U mapPartial (\lambda p \rightarrow \text{case } p \cdot \text{policy of}
                              (just sh) \rightarrow just (Propose p, ScriptObj sh)
                              nothing → nothing) (fromList txprop)
witsVKeyNeeded: UTxO → TxBody → P KeyHash
witsVKeyNeeded = getVKeys o map s proj2 o credsNeeded
scriptsNeeded : UTxO → TxBody → P ScriptHash
scriptsNeeded = getScripts o maps proj2 o credsNeeded
```

Figure 20: Functions used for witnessing

```
_⊢_→(_,UTXOW)_: UTxOEnv → UTxOState → Tx → UTxOState → Type
```

Figure 21: UTxOW transition-system types

```
UTXOW-inductive:
  let utxo
                          = s .utxo
      witsKeyHashes
                         = map s hash (dom vkSigs)
      witsScriptHashes = map s hash scripts
      inputHashes
                          = getInputHashes tx utxo
      refScriptHashes = fromList $ map hash (refScripts tx utxo)
      neededHashes = scriptsNeeded utxo txb
      txdatsHashes
                         = dom txdats
      allOutHashes
                        = getDataHashes (range txouts)
      nativeScripts
                          = mapPartial isInj<sub>1</sub> (txscripts tx utxo)
  in
  • \forall [ (vk, \sigma) \in vkSigs ] isSigned vk (txidBytes txid) \sigma
  • \forall[ s \in nativeScripts ] (hash s \in neededHashes \rightarrow validP1Script witsKeyHashes txvldt <math>s)
  • witsVKeyNeeded utxo txb ⊆ witsKeyHashes
  • neededHashes \ refScriptHashes ≡ e witsScriptHashes
  • inputHashes ⊆ txdatsHashes
  • txdatsHashes ⊆ inputHashes ∪ allOutHashes ∪ getDataHashes (range (utxo | refInputs))
  • languages tx utxo ⊆ allowedLanguages tx utxo
  • txADhash \equiv map hash txAD
  • \Gamma \vdash s \rightharpoonup \emptyset tx ,UTX00 s'
    \Gamma \vdash s \rightharpoonup \emptyset tx ,UTXOWD s'
```

Figure 22: UTXOW inference rules

```
Derived types

GovState = List (GovActionID × GovActionState)

record GovEnv : Type where
  field
    txid : TxId
    epoch : Epoch
    pparams : PParams
    ppolicy : Maybe ScriptHash
    enactState : EnactState
    certState : CertState
    rewardCreds : P Credential
```

Figure 23: Types used in the GOV transition system

8 Governance

This section is part of the Ledger.Gov module of the formal ledger specification, where we define the types required for ledger governance.

The behavior of GovState is similar to that of a queue. New proposals are appended at the end, but any proposal can be removed at the epoch boundary. However, for the purposes of enactment, earlier proposals take priority. Note that EnactState used in GovEnv is defined in Sec. 11.

- addVote inserts (and potentially overrides) a vote made for a particular governance action (identified by its ID) by a credential with a role.
- addAction adds a new proposed action at the end of a given GovState.
- The validHFAction property indicates whether a given proposal, if it is a TriggerHF action, can potentially be enacted in the future. For this to be the case, its prevAction needs to exist, be another TriggerHF action and have a compatible version.

Fig. 26 shows some of the functions used to determine whether certain actions are enactable in a given state. Specifically, allEnactable passes the GovState to getAidPairsList to obtain a list of GovActionID-pairs which is then passed to enactable. The latter uses the _connects_to_function to check whether the list of GovActionID-pairs connects the proposed action to a previously enacted one.

The function <code>govActionPriority</code> assigns a priority to the various types of governance actions. This is useful for ordering lists of governance actions (see <code>insertGovAction</code> in Fig. 24). Priority is also used to check if two actions <code>Overlap</code>: that is, they potentially modify the same piece of <code>EnactState</code>.

```
govActionPriority : GovActionType → N
govActionPriority NoConfidence
govActionPriority UpdateCommittee = 1
govActionPriority NewConstitution = 2
govActionPriority TriggerHF
govActionPriority ChangePParams = 4
govActionPriority TreasuryWdrl = 5
govActionPriority Info
                                       = 6
Overlap : GovActionType → GovActionType → Type
Overlap NoConfidence UpdateCommittee = T
Overlap UpdateCommittee NoConfidence = T
                       a'
Overlap a
                                          = a \equiv a'
insertGovAction: GovState → GovActionID × GovActionState → GovState
insertGovAction [] gaPr = [ gaPr ]
insertGovAction ((gaID_0, gaSt_0) :: gaPrs) (gaID_1, gaSt_1)
  = if (govActionPriority (action gaSt_0 .gaType)) \le ? (govActionPriority (action gaSt_1 .gaType))
    then (gaID_0, gaSt_0) :: insertGovAction gaPrs (gaID_1, gaSt_1)
    else (gaID_1, gaSt_1) :: (gaID_0, gaSt_0) :: gaPrs
mkGovStatePair : Epoch \rightarrow GovActionID \rightarrow RwdAddr \rightarrow (a : GovAction) \rightarrow NeedsHash (a .gaType)
                   → GovActionID × GovActionState
mkGovStatePair e aid addr a prev = (aid , record
  { votes = \( \phi \); returnAddr = addr; expiresIn = e; action = a; prevAction = prev })
addAction: GovState
           \rightarrow Epoch \rightarrow GovActionID \rightarrow RwdAddr \rightarrow (a: GovAction) \rightarrow NeedsHash (a .gaType)
addAction s e aid addr a prev = insertGovAction s (mkGovStatePair e aid addr a prev)
  addVote : GovState → GovActionID → Voter → Vote → GovState
  addVote s aid voter v = map modifyVotes s
    where modifyVotes : GovActionID × GovActionState → GovActionID × GovActionState
           modifyVotes = \lambda (gid , s') \rightarrow gid , record s'
             { votes = if gid ≡ aid then insert (votes s') voter v else votes s'}
  isRegistered : GovEnv → Voter → Type
  isRegistered \Gamma (r, c) = case r of \lambda where
           \rightarrow just c \in \text{range (gState .ccHotKeys)}
    DRep \rightarrow c \in \text{dom (gState .dreps)}
    SPO \rightarrow c \in \text{map}^s \text{ KeyHashObj (dom (pState .pools))}
        open CertState (GovEnv.certState Γ) using (gState; pState)
  validHFAction : GovProposal → GovState → EnactState → Type
  validHFAction (record { action = [ TriggerHF , v ] ga ; prevAction = prev }) s e =
    (let (v', aid) = EnactState.pv e in aid = prev \times pvCanFollow v'v)
    \forall \exists_2 [x, v'] (prev, x) \in \text{fromList } s \times x \text{ .action} \equiv [TriggerHF, v']^{ga} \times pvCanFollow v'v
  validHFAction _ _ = T
```

Figure 24: Functions used in the GOV transition system

```
Transition relation types

_⊢_→(_,GOV)_ : GovEnv × N → GovState → GovVote ⊎ GovProposal → GovState → Type
_⊢_→(_,GOVS)_ : GovEnv → GovState → List (GovVote ⊎ GovProposal) → GovState → Type
```

Figure 25: Type signature of the transition relation of the GOV transition system

```
enactable : EnactState → List (GovActionID × GovActionID)
            → GovActionID × GovActionState → Type
enactable e aidPairs = \lambda (aidNew, as) \rightarrow case getHashES e (action as .gaType) of
  nothing
                  \rightarrow T
  (just\ aidOld) \rightarrow \exists [t]\ fromList\ t \subseteq fromList\ aidPairs
                            \times Unique t \times t connects aidNew to aidOld
allEnactable : EnactState → GovState → Type
allEnactable e aid×states = All (enactable e (getAidPairsList aid×states)) aid×states
hasParentE : EnactState → GovActionID → GovActionType → Type
hasParentE e aid gaTy = case getHashES e gaTy of
  nothing → T
  (just id) \rightarrow id \equiv aid
hasParent : EnactState \rightarrow GovState \rightarrow (gaTy : GovActionType) \rightarrow NeedsHash gaTy \rightarrow Type
hasParent e s gaTy aid = case getHash aid of
nothing
             → T
(just aid') → hasParentE e aid' gaTy
                \forall Any (\lambda (gid, gas) \rightarrow gid \equiv aid' \times Overlap (gas.action.gaType) gaTy) s
```

Figure 26: Enactability predicate

```
actionValid: P Credential → Maybe ScriptHash → Maybe ScriptHash → Epoch → GovAction → Type actionValid rewardCreds p ppolicy epoch [ ChangePParams , _ ] ga = p = ppolicy actionValid rewardCreds p ppolicy epoch [ TreasuryWdrl , x ] ga = p = ppolicy × maps RwdAddr.stake (dom x) crewardCreds actionValid rewardCreds p ppolicy epoch [ UpdateCommittee , (new , rem , q) ] ga = p = nothing × (∀[ e ∈ range new ] epoch < e) × (dom new ∩ rem = e) actionValid rewardCreds p ppolicy epoch _ = p = nothing

actionWellFormed: GovAction → Type actionWellFormed [ ChangePParams , x ] ga = ppdWellFormed x actionWellFormed [ TreasuryWdrl , x ] ga = (∀[ a ∈ dom x ] RwdAddr.net a ≡ NetworkId) × (∃[ v ∈ range x ] ¬ (v ≡ 0)) actionWellFormed _ = T
```

Figure 27: Validity and wellformedness predicates

Fig. 27 defines predicates used in the GOV-Propose case of the GOV rule to ensure that a governance action is valid and well-formed.

- actionValid ensures that the proposed action is valid given the current state of the system:
 - a ChangePParams action is valid if the proposal policy is provided;
 - a TreasuryWdrl action is valid if the proposal policy is provided and the reward stake credential is registered;
 - an UpdateCommittee action is valid if credentials of proposed candidates have not expired, and the action does not propose to both add and remove the same candidate.
- actionWellFormed ensures that the proposed action is well-formed:
 - a ChangePParams action must preserve well-formedness of the protocol parameters;
 - a TreasuryWdrl action is well-formed if the network ID is correct and there is at least one non-zero withdrawal amount in the given $RwdAddr \rightarrow Coin$ map.

```
data _⊢_→ (_,GOV)_ where
  GOV-Vote:
    • (aid, ast) \in fromLists
    • canVote (Γ .pparams) (action ast) (proj<sub>1</sub> voter)
    • isRegistered Γ voter
    • ¬ expired (Γ .epoch) ast
      (\Gamma, k) \vdash s \rightharpoonup \emptyset \text{ inj}_1 [\text{aid}, \text{voter}, \text{v}, \text{machr}], GOVD addVote s aid voter v
  GOV-Propose:
    let pp
                      = \Gamma .pparams
                      =\Gamma .epoch
         enactState = \Gamma .enactState
         rewardCreds = Γ .rewardCreds
                      = record { returnAddr = addr ; action = a ; anchor = achr
                                 ; policy = p; deposit = d; prevAction = prev }
    in

    actionWellFormed a

    actionValid rewardCreds p (Γ .ppolicy) e a

    • d \equiv pp .govActionDeposit
    • validHFAction prop s enactState

    hasParent enactState s (a .gaType) prev

    • addr .RwdAddr.net ≡ NetworkId
    • addr .RwdAddr.stake ∈ rewardCreds
      (\Gamma, k) \vdash s \rightharpoonup \emptyset \text{ inj}_2 \text{ prop ,GOVD addAction } s \text{ (pp .govActionLifetime } +^e e)
                                                       (\Gamma . txid, k) addr a prev
```

Figure 28: Rules for the GOV transition system

The GOVS transition system is now given as the reflexitive-transitive closure of the system GOV, described in Fig. 28.

For GOV-Vote, we check that the governance action being voted on exists; that the voter's role is allowed to vote (see canVote in Fig. 41); and that the voter's credential is actually associated with their role (see isRegistered in Fig. 25).

For GOV-Propose, we check the correctness of the deposit along with some and some conditions that ensure the action is well-formed and valid; naturally, these checks depend on the type of action being proposed (see Fig. 27).

9 Certificates

This section is part of the Ledger.Certs module of the formal ledger specification.

```
Derived types

data DepositPurpose : Type where
   CredentialDeposit : Credential → DepositPurpose
   PoolDeposit : KeyHash → DepositPurpose
   DRepDeposit : Credential → DepositPurpose
   GovActionDeposit : GovActionID → DepositPurpose

Deposits = DepositPurpose → Coin
```

Figure 29: Deposit types

```
data DCert : Type where
  delegate : Credential → Maybe VDeleg → Maybe KeyHash → Coin → DCert
  dereg : Credential → Maybe Coin → DCert
  regpool : KeyHash → PoolParams → DCert
  retirepool : KeyHash → Epoch → DCert
  regdrep : Credential → Coin → Anchor → DCert
  deregdrep : Credential → Coin → DCert
  ccreghot : Credential → Maybe Credential → DCert
```

Figure 30: Delegation definitions

9.1 Changes Introduced in Conway Era

9.1.1 Delegation

Registered credentials can now delegate to a DRep as well as to a stake pool. This is achieved by giving the delegate certificate two optional fields, corresponding to a DRep and stake pool.

Stake can be delegated for voting and block production simultaneously, since these are two separate features. In fact, preventing this could weaken the security of the chain, since security relies on high participation of honest stake holders.

9.1.2 Removal of Pointer Addresses, Genesis Delegations and MIR Certificates

Support for pointer addresses, genesis delegations and MIR certificates is removed (see CIP-1694 and Corduan, Knispel, Benkort, et al. [5]). In DState, this means that the four fields relating to those features are no longer present, and DelegEnv contains none of the fields it used to in the Shelley era (see Corduan, Vinogradova, and Güdemann [1, Sec 9.2]).

Note that pointer addresses are still usable, only their staking functionality has been retired. So all funds locked behind pointer addresses are still accessible, they just don't count towards the stake distribution anymore. Genesis delegations and MIR certificates have been superceded by the new governance mechanisms, in particular the TreasuryWdrl governance action in case of the MIR certificates.

```
record CertEnv: Type where
 field
   epoch: Epoch
        : PParams
   votes : List GovVote
   wdrls : RwdAddr → Coin
   coldCreds : P Credential
record DState: Type where
 field
   voteDelegs : Credential → VDeleg
   stakeDelegs : Credential → KeyHash
               : Credential → Coin
   rewards
record GState: Type where
 field
             : Credential → Epoch
   ccHotKeys : Credential → Maybe Credential
record CertState : Type where
 field
   dState: DState
   pState: PState
   gState: GState
record DelegEnv: Type where
 field
   pparams
              : PParams
              : KeyHash → PoolParams
   delegatees : P Credential
GovCertEnv = CertEnv
PoolEnv
          = PParams
```

Figure 31: Types used for CERTS transition system

9.1.3 Explicit Deposits

Registration and deregistration of staking credentials are now required to explicitly state the deposit that is being paid or refunded. This deposit is used for checking correctness of transactions with certificates. Including the deposit aligns better with other design decisions such as having explicit transaction fees and helps make this information visible to light clients and hardware wallets.

While not shown in the figures, the old certificates without explicit deposits will still be supported for some time for backwards compatibility.

9.2 Governance Certificate Rules

The rules for transition systems dealing with individual certificates are defined in Figs. 33 and 34.GOVCERT deals with the new certificates relating to DReps and the constitutional committee.

- GOVCERT-regdrep registers (or re-registers) a DRep. In case of registration, a deposit needs to be paid. Either way, the activity period of the DRep is reset.
- GOVCERT-deregdrep deregisters a DRep.
- GOVCERT-ccreghot registers a "hot" credential for constitutional committee members. We check that the cold key did not previously resign from the committee. We allow this delegation for any cold credential that is either part of EnactState or is is a proposal. This allows a newly elected member of the constitutional committee to immediately delegate their vote to a hot key and use it to vote. Since votes are counted after previous actions have been enacted, this allows constitutional committee members to act without a delay of one epoch.

```
_⊢_→ (_,DELEG)_
                    : DelegEnv
                                 → DState
                                              → DCert
                                                           → DState
                                                                       → Type
_⊢_→(_,P00L)_
                    : PoolEnv
                                 → PState
                                              → DCert
                                                           → PState
                                                                       → Type
_⊢_ → (_,GOVCERT)_
                   : GovCertEnv → GState
                                              → DCert
                                                           → GState
                                                                       → Type
_⊢_ → ( _ , CERT) _
                    : CertEnv
                                 → CertState → DCert
                                                           → CertState → Type
_⊢_→(_,CERTBASE)_: CertEnv
                                 → CertState → T
                                                           → CertState → Type
_⊢_→(_,CERTS)_
                                 → CertState → List DCert → CertState → Type
                    : CertEnv
```

Figure 32: Types for the transition systems relating to certificates

Fig. 35 assembles the CERTS transition system by bundling the previously defined pieces together into the CERT system, and then taking the reflexive-transitive closure of CERT together with CERTBASE as the base case. CERTBASE does the following:

- check the correctness of withdrawals and ensure that withdrawals only happen from credentials that have delegated their voting power;
- set the rewards of the credentials that withdrew funds to zero;
- and set the activity timer of all DReps that voted to <code>drepActivity</code> epochs in the future.

⁴By "hot" and "cold" credentials we mean the following: a cold credential is used to register a hot credential, and then the hot credential is used for voting. The idea is that the access to the cold credential is kept in a secure location, while the hot credential is more conveniently accessed. If the hot credential is compromised, it can be changed using the cold credential.

```
DELEG-delegate:
  let \Gamma = [pp, pools, delegatees]
  • (c \notin dom \ rwds \rightarrow d \equiv pp \ .keyDeposit)
  • (c \in dom\ rwds \rightarrow d \equiv 0)
  • mv ∈ map s (just ∘ credVoter DRep) delegatees U
      fromList ( nothing :: just abstainRep :: just noConfidenceRep :: [] )

    mkh ∈ map<sup>s</sup> just (dom pools) ∪ { nothing }

    \Gamma \vdash [vDelegs, sDelegs, rwds] \rightarrow (delegate c mv mkh d, DELEG)
        [ insertIfJust c mv vDelegs , insertIfJust c mkh sDelegs , rwds ∪¹ { c , 0 } ]
DELEG-dereg:
  • (c , 0) ∈ rwds
    [ pp , pools , delegatees ] ⊢ [ vDelegs , sDelegs , rwds ] → ( dereg c md ,DELEG)
      [ vDelegs | { c } c , sDelegs | { c } c , rwds | { c } c ]
DELEG-reg :
  • c ∉ dom rwds
  • d \equiv pp .keyDeposit \forall d \equiv 0
    pp , pools , delegatees | ⊢
      [ vDelegs , sDelegs , rwds ] → ( reg c d ,DELEG)
      [ vDelegs , sDelegs , rwds ∪¹ { c , 0 } ]
```

Figure 33: Auxiliary DELEG transition system

```
GOVCERT-regdrep:

let Γ = [e , pp , vs , wdrls , cc]

in

• (d ≡ pp .drepDeposit × c ∉ dom dReps) ⊎ (d ≡ 0 × c ∈ dom dReps)

Γ ⊢ [ dReps , ccKeys ] → ( regdrep c d an ,GOVCERT)

[ { c , e + pp .drepActivity } ∪¹ dReps , ccKeys ]

GOVCERT-deregdrep:

• c ∈ dom dReps

[e , pp , vs , wdrls , cc] ⊢ [ dReps , ccKeys ] → ( deregdrep c d ,GOVCERT) [ dReps ] { c } c , ccKeys

GOVCERT-ccreghot:

• (c , nothing) ∉ ccKeys

• c ∈ cc

[e , pp , vs , wdrls , cc] ⊢ [ dReps , ccKeys ] → ( ccreghot c mc ,GOVCERT) [ dReps , { c , mc } ∪¹ cc
```

Figure 34: Auxiliary GOVCERT transition system

```
CERT transitions
  CERT-deleg:
    • [ pp , PState.pools st^p , dom (GState.dreps st^g) ] \vdash st^d \rightharpoonup \emptyset dCert ,DELEGD st^{d'}
      [e, pp, vs, wdrls, cc] \vdash [st<sup>d</sup>, st<sup>p</sup>, st<sup>g</sup>] \rightharpoonup (dCert, CERT) [st<sup>d'</sup>, st<sup>p</sup>, st<sup>g</sup>]
  CERT-pool :
    • pp \vdash st^p \rightharpoonup \emptyset dCert , POOLD st^p'
      [ e , pp , vs , wdrls , cc ] \vdash [ st^d , st^p , st^g ] \rightharpoonup ( dCert , CERT) [ st^d , st^{p'} , st^g ]
  CERT-vdel:
    • \Gamma \vdash st^g \rightharpoonup \emptyset dCert ,GOVCERTD st^g'
      \Gamma \vdash [st^d, st^p, st^g] \rightarrow (dCert, CERT) [st^d, st^p, st^g']
CERTBASE transition
  CERT-base:
    let refresh
                             = mapPartial getDRepVote (fromList vs)
         refreshedDReps = mapValueRestricted (const (e + pp .drepActivity)) dReps refresh
                             = map s stake (dom wdrls)
         validVoteDelegs = voteDelegs | ^ ( map* (credVoter DRep) (dom dReps)
                                                 U fromList (noConfidenceRep : abstainRep : []) )
    • filter isKeyHash wdrlCreds ⊆ dom voteDelegs

    map<sup>s</sup> (map<sub>1</sub> stake) (wdrls <sup>s</sup>) ⊆ rewards <sup>s</sup>

       [e, pp, vs, wdrls, cc] \vdash
         [ [ voteDelegs , stakeDelegs , rewards ]
         , stp
         , [ dReps , ccHotKeys ]
         _ ,CERTBASED
         [ [ validVoteDelegs , stakeDelegs , constMap wdrlCreds 0 ∪ l rewards ]
         , [ refreshedDReps , ccHotKeys ]
```

Figure 35: CERTS rules

10 Ledger

This section is part of the Ledger.Ledger module of the formal ledger specification, where the entire state transformation of the ledger state caused by a valid transaction can now be given as a combination of the previously defined transition systems.

As there is nothing new to the Conway era in this part of the ledger, we do not present any details of the Agda formalization.

```
record LEnv: Type where
  field
    slot
                 : Slot
    ppolicy
                 : Maybe ScriptHash
    pparams
                 : PParams
    enactState : EnactState
    treasury : Coin
record LState: Type where
  field
    utxoSt
               : UTxOState
                : GovState
    govSt
    certState : CertState
txgov: TxBody → List (GovVote ⊎ GovProposal)
txgov txb = map inj<sub>2</sub> txprop ++ map inj<sub>1</sub> txvote
  where open TxBody txb
rmOrphanDRepVotes : CertState → GovState → GovState
rmOrphanDRepVotes cs govSt = L.map (map<sub>2</sub> go) govSt
  where
    ifDRepRegistered : Voter → Type
    ifDRepRegistered (r, c) = r \equiv DRep \rightarrow c \in dom (cs.gState.dreps)
    go : GovActionState → GovActionState
    go gas = record gas { votes = filterKeys ifDRepRegistered (gas .votes) }
\verb|allColdCreds|: GovState| \rightarrow \verb|EnactState| \rightarrow \verb|P| Credential|
allColdCreds govSt es =
  ccCreds (es.cc) U concatMap<sup>s</sup> (\lambda (_ , st) \rightarrow proposedCC (st.action)) (fromList govSt)
```

Figure 36: Types and functions for the LEDGER transition system

```
data _⊢_→(_,LEDGER)_ : LEnv → LState → Tx → LState → Type where

LEDGER-V:

let txb = tx .body
    rewards = certState .dState .rewards

in

isValid tx ≡ true

[slot , pp , treasury] ⊢ utxoSt → (tx ,UTXOW) utxoSt'

[epoch slot , pp , txvote , txwdrls , allColdCreds govSt enactState] ⊢ certState → (txcerts ,CE)

[txid , epoch slot , pp , ppolicy , enactState , certState' , dom rewards] ⊢ rmOrphanDRepVotes ce

[slot , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx ,LEDGER) [utxoSt , pp , treasury] ⊢ utxoSt → (tx ,UTXOW) utxoSt'

[slot , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx ,LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx ,LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx ,LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx ,LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx ,LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx ,LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx ,LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx ,LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx , LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx , LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx , LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , govSt , certState] → (tx , LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , ppolicy , pp , enactState ] → (tx , LEDGER) [utxoSt , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , ppolicy , pp , enactState ] → (tx , ppolicy , pp , enactState , treasury] ⊢ [utxoSt , ppolicy , pp , enactState ] → (tx , ppolicy , pp , ena
```

Figure 37: LEDGER transition system

11 Enactment

This section is part of the Ledger. Enact module of the formal ledger specification

Fig. 38 contains some definitions required to define the ENACT transition system. EnactEnv is the environment and EnactState the state of ENACT, which enacts a governance action. All governance actions except TreasuryWdrl and Info modify EnactState permanently, which of course can have further consequences. TreasuryWdrl accumulates withdrawal temporarily in EnactState, but this information is applied and discarded immediately in EPOCH. Also, enacting these governance actions is the *only* way of modifying EnactState. The withdrawals field of EnactState is special in that it is ephemeral—ENACT accumulates withdrawals there which are paid out at the next epoch boundary where this field will be reset.

Note that all other fields of EnactState also contain a GovActionID since they are HashProtected.

Figs. 39 and 40 define the rules of the ENACT transition system. Usually no preconditions are checked and the state is simply updated (including the GovActionID for the hash protection scheme, if required). The exceptions are UpdateCommittee and TreasuryWdrl:

- UpdateCommittee requires that maximum terms are respected, and
- TreasuryWdrl requires that the treasury is able to cover the sum of all withdrawals (old and new).

```
record EnactEnv : Type where
   field
     gid
              : GovActionID
     treasury : Coin
     epoch : Epoch
 record EnactState : Type where
   field
                   : HashProtected (Maybe ((Credential → Epoch) × ℚ))
     СС
     constitution : HashProtected (DocHash x Maybe ScriptHash)
                   : HashProtected ProtVer
                   : HashProtected PParams
     withdrawals : RwdAddr → Coin
 ccCreds : HashProtected (Maybe ((Credential → Epoch) × ℚ)) → P Credential
 ccCreds (just x , _) = dom (x \cdot proj_1)
 ccCreds (nothing , _) = ∅
 getHash : \forall \{a\} \rightarrow \text{NeedsHash } a \rightarrow \text{Maybe GovActionID}
 getHash {NoConfidence}
                            h = just h
 getHash {UpdateCommittee} h = just h
 getHash {NewConstitution} h = just h
 getHash {TriggerHF}
                            h = just h
 getHash {ChangePParams} h = just h
 getHash {TreasuryWdrl} _ = nothing
 getHash {Info}
                             _ = nothing
 getHashES : EnactState → GovActionType → Maybe GovActionID
 getHashES es NoConfidence
                                  = just (es .cc .proj<sub>2</sub>)
 getHashES es (UpdateCommittee) = just (es .cc .proj<sub>2</sub>)
 getHashES es (NewConstitution) = just (es .constitution .proj2)
 getHashES es (TriggerHF)
                             = just (es .pv .proj<sub>2</sub>)
 getHashES es (ChangePParams) = just (es .pparams .proj<sub>2</sub>)
 getHashES es (TreasuryWdrl)
                                  = nothing
 getHashES es Info
                                  = nothing
Type of the ENACT transition system
   _⊢_→ (_,ENACT)_: EnactEnv → EnactState → GovAction → EnactState → Type
```

Figure 38: Types and function used for the ENACT transition system

Figure 39: ENACT transition system

```
Enact-HF:

[ gid , t , e ] ⊢ s → ( [ TriggerHF , v ] ga ,ENACT) record s { pv = v , gid }

Enact-PParams:

[ gid , t , e ] ⊢ s → ( [ ChangePParams , up ] ga ,ENACT) record s { pparams = applyUpdate (s .pparams .proj_1) up , gid }

Enact-Wdrl: let newWdrls = s .withdrawals U+ wdrl in ∑[ x ← newWdrls ] x ≤ t

[ gid , t , e ] ⊢ s → ( [ TreasuryWdrl , wdrl ] ga ,ENACT) record s { withdrawals = newWdrls }

Enact-Info:

[ gid , t , e ] ⊢ s → ( [ Info , _ ] ga ,ENACT) s
```

Figure 40: ENACT transition system (continued)

12 Ratification

This section is part of the Ledger.Ratify module of the formal ledger specification

Governance actions are *ratified* through on-chain votes. Different kinds of governance actions have different ratification requirements but always involve at least two of the three governance bodies.

A successful motion of no-confidence, election of a new constitutional committee, a constitutional change, or a hard-fork delays ratification of all other governance actions until the first epoch after their enactment. This gives a new constitutional committee enough time to vote on current proposals, re-evaluate existing proposals with respect to a new constitution, and ensures that the (in principle arbitrary) semantic changes caused by enacting a hard-fork do not have unintended consequences in combination with other actions.

12.1 Ratification Requirements

Fig. 41 details the ratification requirements for each governance action scenario. For a governance action to be ratified, all of these requirements must be satisfied, on top of other conditions that are explained further down. The threshold function is defined as a table, with a row for each type of GovAction and the column representing the CC, DRep and SPO roles in that order.

The symbols mean the following:

- vote x: For an action to pass, the fraction of stake associated with yes votes with respect to that associated with yes and no votes must exceed the threshold x.
- -: The body of governance does not participate in voting.
- \checkmark : The constitutional committee needs to approve an action, with the threshold assigned to it.
- \checkmark t: Voting is possible, but the action will never be enacted. This is equivalent to vote 2 (or any other number above 1).

Two rows in this table contain functions that compute the DRep and SPO thresholds simultaneously: the rows for UpdateCommittee and ChangePParams.

For UpdateCommittee, there can be different thresholds depending on whether the system is in a state of no-confidence or not. This information is provided via the ccThreshold argument: if the system is in a state of no-confidence, then ccThreshold is set to nothing.

In case of the ChangePParams action, the thresholds further depend on what groups that action is associated with. pparamThreshold associates a pair of thresholds to each individual group. Since an individual update can contain multiple groups, the actual thresholds are then given by taking the maximum of all those thresholds.

Note that each protocol parameter belongs to exactly one of the four groups that have a DRep threshold, so a DRep vote will always be required. A protocol parameter may or may not be in the SecurityGroup, so an SPO vote may not be required.

Finally, each of the P_x and Q_x in Fig. 41 are protocol parameters.

12.2 Protocol Parameters and Governance Actions

Voting thresholds for protocol parameters can be set by group, and we do not require that each protocol parameter governance action be confined to a single group. In case a governance action carries updates for multiple parameters from different groups, the maximum threshold of all the groups involved will apply to any given such governance action.

The purpose of the SecurityGroup is to add an additional check to security-relevant protocol parameters. Any proposal that includes a change to a security-relevant protocol parameter must also be accepted by at least half of the SPO stake.

```
threshold: PParams → Maybe Q → GovAction → GovRole → Maybe Q
threshold pp ccThreshold =
                     , \, \_ \, ] g a \rightarrow | \, -
  NoConfidence
                                    | vote P1 | vote Q1 |
  [ UpdateCommittee , _ ]ga → | -
                                    ∥ P/Q2a/b
  | vote P3 | -
                     , \, \_ \, ]^{ga} \rightarrow | \checkmark
  TriggerHF
                                   | vote P4 | vote Q4 |
                     X \parallel^{ga} \rightarrow \downarrow \checkmark
                                    ∥ P/Q5 x
  ChangePParams
  [ TreasuryWdrl
                     , \, \_ \, ] g a \rightarrow \, | \, \checkmark
                                    | vote P6 | -
                     Info
    where
    P/Q2a/b: Maybe Q × Maybe Q
    P/Q2a/b = case ccThreshold of
              (just \_) \rightarrow (vote P2a, vote Q2a)
              nothing → (vote P2b , vote Q2b)
    pparamThreshold: PParamGroup → Maybe ℚ × Maybe ℚ
    pparamThreshold NetworkGroup
                                    = (vote P5a , -
    pparamThreshold EconomicGroup = (vote P5b , -
    pparamThreshold TechnicalGroup = (vote P5c , -
    pparamThreshold GovernanceGroup = (vote P5d , -
    pparamThreshold SecurityGroup = (-
                                                 , vote Q5 )
    P/Q5 : PParamsUpdate → Maybe @ × Maybe @
    P/Q5 ppu = maxThreshold (map<sup>s</sup> (proj₁ ∘ pparamThreshold) (updateGroups ppu))
             , maxThreshold (map⁵ (proj₂ ∘ pparamThreshold) (updateGroups ppu))
canVote : PParams → GovAction → GovRole → Type
canVote pp \ a \ r = Is-just (threshold pp \ nothing a \ r)
```

Figure 41: Functions related to voting

12.3 Ratification Restrictions

As mentioned earlier, most governance actions must include a GovActionID for the most recently enacted action of its given type. Consequently, two actions of the same type can be enacted at the same time, but they must be *deliberately* designed to do so.

Fig. 42 defines some types and functions used in the RATIFY transition system. CCData is simply an alias to define some functions more easily.

Fig. 43 defines the actualVotes function. Given the current state about votes and other parts of the system it calculates a new mapping of votes, which is the mapping that will actually be used during ratification. Things such as default votes or resignation/expiry are implemented in this way.

actualVotes is defined as the union of four voting maps, corresponding to the constitutional committee, predefined (or auto) DReps, regular DReps and SPOs.

- roleVotes filters the votes based on the given governance role and is a helper for definitions further down.
- if a CC member has not yet registered a hot key, has expired, or has resigned, then actualCCVote returns abstain; if none of these conditions is met, then
 - if the CC member has voted, then that vote is returned;

```
record StakeDistrs : Type where
  field
    stakeDistr : VDeleg → Coin
record RatifyEnv: Type where
 field
    stakeDistrs : StakeDistrs
   currentEpoch : Epoch
                : Credential → Epoch
   ccHotKeys : Credential → Maybe Credential
    treasury
                 : Coin
                : KeyHash → PoolParams
    pools
    delegatees : Credential → VDeleg
record RatifyState : Type where
  field
            : EnactState
    removed : P (GovActionID × GovActionState)
   delay : Bool
CCData: Type
CCData = Maybe ((Credential → Epoch) × ℚ)
govRole : VDeleg → GovRole
govRole (credVoter gv _) = gv
govRole abstainRep
                       = DRep
govRole noConfidenceRep = DRep
IsCC IsDRep IsSPO : VDeleg → Type
       v = govRole v \equiv CC
IsDRep v = govRole v \equiv DRep
IsSPO v = govRole v \equiv SPO
```

Figure 42: Types and functions for the RATIFY transition system

- if the CC member has not voted, then the default value of no is returned.
- actualDRepVotes adds a default vote of no to all active DReps that didn't vote.
- actual SPOVotes adds a default vote to all SPOs who didn't vote, with the default depending on the action.

Let us discuss the last item above—the way SPO votes are counted—as the ledger specification's handling of this has evolved in response to community feedback. Previously, if an SPO did not vote, then it would be counted as having voted abstain by default. Members of the SPO community found this behavior counterintuitive and requested that non-voters be assigned a no vote by default, with the caveat that an SPO could change its default setting by delegating its reward account credential to an AlwaysNoConfidence DRep or an AlwaysAbstain DRep. (This change applies only after the bootstrap period; during the bootstrap period the logic is unchanged; see Appendix C.) To be precise, the agreed upon specification is the following: an SPO that did not vote is assumed to have vote no, except under the following circumstances:

• if the SPO has delegated its reward credential to an AlwaysNoConfidence DRep, then

their default vote is yes for NoConfidence proposals and no for other proposals;

• if the SPO has delegated its reward credential to an AlwaysAbstain DRep, then its default vote is abstain for all proposals.

It is important to note that the credential that can now be used to set a default voting behavior is the credential used to withdraw staking rewards, which is not (in general) the same as the credential used for voting.

Fig. 44 defines the accepted and expired functions (together with some helpers) that are used in the rules of RATIFY.

- getStakeDist computes the stake distribution based on the given governance role and the corresponding delegations. Note that every constitutional committe member has a stake of 1, giving them equal voting power. However, just as with other delegation, multiple CC members can delegate to the same hot key, giving that hot key the power of those multiple votes with a single actual vote.
- acceptedStakeRatio is the ratio of accepted stake. It is computed as the ratio of yes votes over the votes that didn't abstain. The latter is equivalent to the sum of yes and no votes. The special division symbol /o indicates that in case of a division by 0, the numbers 0 should be returned. This implies that in the absence of stake, an action can only pass if the threshold is also set to 0.
- acceptedBy looks up the threshold in the threshold table and compares it to the result of acceptedStakeRatio.
- accepted then checks if an action is accepted by all roles; and
- expired checks whether a governance action is expired in a given epoch.

Fig. 45 defines functions that deal with delays and the acceptance criterion for ratification. A given action can either be delayed if the action contained in EnactState isn't the one the given action is building on top of, which is checked by verifyPrev, or if a previous action was a delayingAction. Note that delayingAction affects the future: whenever a delayingAction is accepted all future actions are delayed. delayed then expresses the condition whether an action is delayed. This happens either because the previous action doesn't match the current one, or because the previous action was a delaying one. This information is passed in as an argument.

The RATIFIES transition system is defined as the reflexive-transitive closure of RATIFY, which is defined via three rules, defined in Fig. 46.

- RATIFY-Accept checks if the votes for a given GovAction meet the threshold required for acceptance, that the action is accepted and not delayed, and RATIFY-Accept ratifies the action.
- RATIFY-Reject asserts that the given GovAction is not accepted and expired; it removes the governance action.
- RATIFY-Continue covers the remaining cases and keeps the GovAction around for further voting.

Note that all governance actions eventually either get accepted and enacted via RATIFY-Accept or rejected via RATIFY-Reject. If an action satisfies all criteria to be accepted but cannot be enacted anyway, it is kept around and tried again at the next epoch boundary.

We never remove actions that do not attract sufficient yes votes before they expire, even if it is clear to an outside observer that this action will never be enacted. Such an action will simply keep getting checked every epoch until it expires.

```
actualVotes : RatifyEnv → PParams → CCData → GovActionType
             → (GovRole × Credential → Vote) → (VDeleg → Vote)
actualVotes Γ pparams cc gaTy votes
  = mapKeys (credVoter CC) actualCCVotes U<sup>1</sup> actualPDRepVotes gαTy
  U<sup>l</sup> actualDRepVotes
                                              U<sup>l</sup> actualSPOVotes gaTy
  where
  roleVotes : GovRole → VDeleg → Vote
  roleVotes r = \text{mapKeys} (uncurry credVoter) (filter (\lambda (x, \_) \rightarrow r \equiv \text{proj}_1 x) \text{ votes})
  activeDReps = dom (filter (\lambda (\_, e) \rightarrow currentEpoch \le e) dreps)
  spos = filter* IsSPO (dom (stakeDistr stakeDistrs))
  getCCHotCred : Credential × Epoch → Maybe Credential
  getCCHotCred (c, e) = case \dot{c} currentEpoch \leq e \dot{c}^b, lookup<sup>m</sup>? ccHotKeys c of
       (true , just (just c')) \rightarrow just c'
                                 → nothing -- expired, no hot key or resigned
  SPODefaultVote : GovActionType → VDeleg → Vote
  SPODefaultVote gaT (credVoter SPO (KeyHashObj kh)) = case lookup<sup>m</sup>? pools kh of
       nothing → Vote.no
       (just p) \rightarrow case lookup^m? delegatees (PoolParams.rewardAddr p), gaTy of
                                      , TriggerHF)
                                                      → Vote.no
              (just noConfidenceRep , NoConfidence) → Vote.yes
              (just abstainRep , _ )
                                                        → Vote.abstain
                                                        → Vote.no
  SPODefaultVote _ _ = Vote.no
  actualCCVote : Credential → Epoch → Vote
  actualCCVote c e = case getCCHotCred (c , e) of
       (just c') → maybe id Vote.no (lookup<sup>m</sup>? votes (CC , c'))
                    → Vote.abstain
  actualCCVotes : Credential → Vote
  actualCCVotes = case cc of
       nothing
                     → Ø
       (\text{just } (m, q)) → if ccMinSize \leq length<sup>s</sup> (mapFromPartialFun getCCHotCred (m^{s}))
                         then mapWithKey actualCCVote m
                         else constMap (dom m) Vote.no
  actualPDRepVotes : GovActionType → VDeleg → Vote
  actualPDRepVotes NoConfidence
                       = { abstainRep , Vote.abstain } U<sup>1</sup> { noConfidenceRep , Vote.yes }
  actualPDRepVotes _ = { abstainRep , Vote.abstain } Ul { noConfidenceRep , Vote.no }
  actualDRepVotes : VDeleg → Vote
  actualDRepVotes = roleVotes DRep
                    U<sup>1</sup> constMap (map<sup>s</sup> (credVoter DRep) activeDReps) Vote.no
  actualSPOVotes : GovActionType → VDeleg → Vote
  actual SPOV otes gaTy = roleVotes SPO U^1 mapFromFun (SPODefaultVote gaTy) spos
```

Figure 43: Vote counting

```
getStakeDist : GovRole → P VDeleg → StakeDistrs → VDeleg → Coin
getStakeDist CC     cc sd = constMap (filter* IsCC cc) 1
getStakeDist DRep _ sd = filterKeys IsDRep (sd .stakeDistr)
getStakeDist SPO _ sd = filterKeys IsSPO (sd .stakeDistr)
acceptedStakeRatio : GovRole → P VDeleg → StakeDistrs → (VDeleg → Vote) → ℚ
acceptedStakeRatio r cc dists votes = acceptedStake /o totalStake
  where
    dist : VDeleg → Coin
    dist = getStakeDist r cc dists
    acceptedStake totalStake : Coin
    acceptedStake = \sum [x \leftarrow \text{dist} \mid \text{votes}^{-1} \text{ Vote.yes}] x
    totalStake = \sum [x \in \text{dist} \mid \text{dom} (votes \mid ^(\{ \text{Vote.yes} \} \cup \{ \text{Vote.no} \}))] x
acceptedBy : RatifyEnv → EnactState → GovActionState → GovRole → Type
acceptedBy Γ (record { cc = cc , _; pparams = pparams , _ }) gs role =
  let open GovActionState gs; open PParams pparams
      votes' = actualVotes Γ pparams cc (gaType action) votes
      mbyT = threshold pparams (proj<sub>2</sub> <$> cc) action role
              = maybe id 00 mbyT
  in acceptedStakeRatio role (dom votes') (stakeDistrs Γ) votes' ≥ t
    \land (role ≡ CC → maybe (λ (m , _) → length<sup>s</sup> m) 0 cc ≥ ccMinSize \forall Is-nothing mbyT)
accepted : RatifyEnv → EnactState → GovActionState → Type
accepted \Gamma es gs = acceptedBy \Gamma es gs CC \Lambda acceptedBy \Gamma es gs DRep \Lambda acceptedBy \Gamma es gs SPO
expired : Epoch → GovActionState → Type
expired current record { expiresIn = expiresIn } = expiresIn < current</pre>
```

Figure 44: Functions used in RATIFY rules, without delay

```
verifyPrev : (a : GovActionType) \rightarrow NeedsHash a \rightarrow EnactState \rightarrow Type
verifyPrev NoConfidence h = es.cc.proj_2
verifyPrev UpdateCommittee h es = h ≡ es .cc .proj₂
verifyPrev NewConstitution h es = h \equiv es .constitution .proj<sub>2</sub>
verifyPrev TriggerHF h = es.pv.proj_2
verifyPrev ChangePParams h = es \cdot pparams \cdot proj_2
verifyPrev TreasuryWdrl _ _ = T
verifyPrev Info
delayingAction : GovActionType → Bool
delayingAction NoConfidence
                                 = true
delayingAction UpdateCommittee = true
delayingAction NewConstitution = true
delayingAction TriggerHF
delayingAction ChangePParams = false
delayingAction TreasuryWdrl = false
delayingAction Info
                                   = false
delayed : (a : GovActionType) \rightarrow NeedsHash a \rightarrow EnactState \rightarrow Bool \rightarrow Type
delayed gaTy \ h \ es \ d = \neg \ verifyPrev \ gaTy \ h \ es \ ⊎ \ d \equiv true
acceptConds: RatifyEnv → RatifyState → GovActionID × GovActionState → Type
acceptConds \Gamma st^{\tau} (id, st) =
    accepted \Gamma es st

x ¬ delayed (gaType action) prevAction es delay

  \times 3[ es' ] [ id , treasury , currentEpoch ] \vdash es \rightarrow 0 action ,ENACTD es'
```

Figure 45: Functions related to ratification

```
data _⊢_→ (_,RATIFY)_:
  RatifyEnv → RatifyState → GovActionID × GovActionState → RatifyState → Type where
  RATIFY-Accept:
    let treasury = \Gamma .treasury
                      = Γ .currentEpoch
        (gaId, gaSt) = a
        action
                      = gaSt .action
    • acceptConds Γ [ es , removed , d ] a
    • [ gaId , treasury , e ] \vdash es \rightharpoonup ( action ,ENACT) es'
     \Gamma \vdash [es, removed, d] \rightarrow (a, RATIFY)
          [ es', { a } U removed , delayingAction (gaType action) ]
  RATIFY-Reject:
                      = Γ .currentEpoch
    let e
        (gaId, gaSt) = a
    • ¬ acceptConds Γ [ es , removed , d ] α
    • expired e gaSt
     \Gamma \vdash [es, removed, d] \rightarrow (a, RATIFY) [es, {a} \cup removed, d]
  RATIFY-Continue:
    let e
                       = Γ .currentEpoch
        (gaId, gaSt) = a
    • ¬ acceptConds Γ [ es , removed , d ] α
    • ¬ expired e gaSt
     \Gamma \vdash [es, removed, d] \rightharpoonup (a, RATIFY) [es, removed, d]
_⊢_→ (_,RATIFIES)_: RatifyEnv → RatifyState → List (GovActionID × GovActionState)
 → RatifyState → Type
_⊢_→(_,RATIFIES)_ = ReflexiveTransitiveClosure {sts = _⊢_→(_,RATIFY)_}
```

Figure 46: The RATIFY transition system

13 Epoch Boundary

This section is part of the Ledger. Epoch module of the formal ledger specification

```
record EpochState : Type where
field
  acnt : Acnt
  ss : Snapshots
  ls : LState
  es : EnactState
  fut : RatifyState
```

Figure 47: Definitions for the EPOCH and NEWEPOCH transition systems

```
stakeDistr : UTxO → DState → PState → Snapshot
stakeDistr utxo st<sup>d</sup> pState = [ aggregate+ (stakeRelation fs) , stakeDelegs ]
where
open DState st<sup>d</sup> using (stakeDelegs; rewards)
m = map<sup>s</sup> (λ α → (α , cbalance (utxo | ^' λ i → getStakeCred i ≡ just α))) (dom rewards)
stakeRelation = m ∪ proj₁ rewards

gaDepositStake : GovState → Deposits → Credential → Coin
gaDepositStake govSt ds = aggregateBy
(map<sup>s</sup> (λ (gaid , addr) → (gaid , addr) , stake addr) govSt')
(mapFromPartialFun (λ (gaid , _ ) → lookup<sup>m</sup>? ds (GovActionDeposit gaid)) govSt')
where govSt' = map<sup>s</sup> (map₂ returnAddr) (fromList govSt)

mkStakeDistrs : Snapshot → GovState → Deposits → (Credential → VDeleg) → StakeDistrs
mkStakeDistrs ss govSt ds delegations .StakeDistrs.stakeDistr =
aggregateBy (proj₁ delegations) (Snapshot.stake ss U* gaDepositStake govSt ds)
```

Figure 48: Functions for computing stake distributions

Fig. 49 defines the EPOCH transition rule. Currently, this incorporates logic that was previously handled by POOLREAP in the Shelley specification [1, Sec 11.6]; POOLREAP is not implemented here.

The EPOCH rule now also needs to invoke RATIFIES and properly deal with its results by carrying out each of the following tasks.

- Pay out all the enacted treasury withdrawals.
- Remove expired and enacted governance actions & refund deposits.
- If govSt' is empty, increment the activity counter for DReps.
- Remove all hot keys from the constitutional committee delegation map that do not belong to currently elected members.
- Apply the resulting enact state from the previous epoch boundary fut and store the resulting enact state fut'.

```
EPOCH : let
           = record esW { withdrawals = ∅ }
  tmpGovSt = filter (\lambda x \rightarrow i proj_1 x \notin map^s proj_1 removed i) govSt
  orphans = fromList $ getOrphans es tmpGovSt
  removed' = removed U orphans
  removedGovActions = flip concatMap<sup>s</sup> removed' \lambda (gaid, gaSt) \rightarrow
    map<sup>s</sup> (returnAddr gaSt ,_) ((utxoSt .deposits | { GovActionDeposit gaid }) *)
  govActionReturns = aggregate + (map<sup>s</sup> (\lambda (\alpha, _-, d) \rightarrow \alpha, d) removedGovActions <sup>fs</sup>)
  trWithdrawals = esW .withdrawals
  totWithdrawals = \sum [x \leftarrow trWithdrawals] x
  retired = (pState .retiring) -1 e
  payout
             = govActionReturns U⁺ trWithdrawals
             = pullbackMap payout toRwdAddr (dom (dState .rewards))
  refunds
  unclaimed = getCoin payout - getCoin refunds
  govSt' = filter (λ x → ¿ proj₁ x ∉ map<sup>s</sup> proj₁ removed' ¿) govSt
  dState' = [dState .voteDelegs , dState .stakeDelegs , dState .rewards ∪* refunds ]
  pState' = [ pState .pools | retired c , pState .retiring | retired c ]
  gState' = [ (if null govSt' then mapValues (1 +_) (gState .dreps) else (gState .dreps))
             , gState .ccHotKeys | ccCreds (es .cc) ]
  certState' : CertState
  certState' = [ dState' , pState' , gState' ]
 utxoSt' = [ utxoSt .utxo , utxoSt .fees , utxoSt .deposits | maps (proj1 o proj2) removedGovActions c
 acnt' = record acnt
    { treasury = acnt .treasury - totWithdrawals + utxoSt .donations + unclaimed }
in
record { currentEpoch = e
        ; stakeDistrs = mkStakeDistrs (Snapshots.mark ss') govSt'
                                         (utxoSt' .deposits) (voteDelegs dState)
        ; treasury = acnt .treasury ; GState gState
        ; pools = pState .pools ; delegatees = dState .voteDelegs }
    ⊢ [ es , ∅ , false ] → ( govSt' ,RATIFIES) fut'
 \rightarrow 1s \vdash ss \rightarrow 0 tt ,SNAPD ss'
\_\vdash [acnt, ss, ls, es_0, fut] \rightarrow (e, EPOCH)
    [ acnt' , ss' , [ utxoSt' , govSt' , certState' ] , es , fut' ]
```

Figure 49: EPOCH transition system

References

- [1] J. Corduan, P. Vinogradova, and M. Güdemann, A Formal Specification of the Cardano Ledger, https://github.com/intersectmbo/cardano-ledger/releases/latest/down load/shelley-ledger.pdf, LATEXsource: https://github.com/intersectmbo/cardan o-ledger/tree/master/eras/shelley/formal-spec/shelley-ledger.tex; Accessed: 2024-07-30, 2019. [Online]. Available: https://github.com/intersectmbo/cardano-ledger/releases/latest/download/shelley-ledger.pdf.
- [2] P. Vinogradova and A. Knispel, A Formal Specification of the Cardano Ledger with a Native Multi-Asset Implementation, https://github.com/intersectmbo/cardano-ledger/releases/latest/download/mary-ledger.pdf, IATEXsource: https://github.com/intersectmbo/cardano-ledger/tree/master/eras/shelley-ma/formal-spec/mary-ledger.tex; Accessed: 2024-07-30, 2019. [Online]. Available: https://github.com/intersectmbo/cardano-ledger/releases/latest/download/mary-ledger.pdf.
- [3] P. Vinogradova and A. Knispel, A Formal Specification of the Cardano Ledger integrating Plutus Core, https://github.com/intersectmbo/cardano-ledger/releases/latest/download/alonzo-ledger.pdf, Accessed: 2024-07-30, 2021. [Online]. Available: https://github.com/intersectmbo/cardano-ledger/releases/latest/download/alonzo-ledger.pdf.
- [4] A. Knispel and J. Corduan, Formal Specification of the Cardano Ledger for the Babbage era, https://github.com/intersectmbo/cardano-ledger/releases/latest/download/babbage-ledger.pdf, Accessed: 2024-07-15, 2022. [Online]. Available: https://github.com/intersectmbo/cardano-ledger/releases/latest/download/babbage-ledger.pdf.
- [5] J. Corduan, A. Knispel, M. Benkort, K. Hammond, C. Hoskinson, and S. Leathers, A first step towards on-chain decentralized governance, https://cips.cardano.org/cip/CIP-16 94, 2023.
- [6] Agda development team, Agda 2.7.0 documentation, https://agda.readthedocs.io/en/v2.7.0/, Dec. 2024.
- [7] B. Nordström, K. Petersson, and J. M. Smith, *Programming in Martin-Löf's type theory: An introduction*, https://www.cse.chalmers.se/research/group/logic/book/book.pdf, previously published as [9], Jul. 1990.
- [8] IOHK Formal Methods Team, Design Specification for Delegation and Incentives in Cardano, IOHK Deliverable SL-D1, 2018. [Online]. Available: https://github.com/intersectmbo/cardano-ledger/releases/latest/download/shelley-delegation.pdf.
- [9] B. Nordström, K. Petersson, and J. M. Smith, *Programming in Martin-Löf's Type Theory:* An Introduction (International series of monographs on computer science). Clarendon Press; Oxford University Press, Jul. 1990, ISBN: 0198538146; 9780198538141. [Online]. Available: https://books.google.com/books?id=mZhQAAAAMAAJ.

A Agda Essentials

Here we describe some of the essential concepts and syntax of the Agda programming language and proof assistant. The goal is to provide some background for readers who are not already familiar with Agda, to help them understand the other sections of the specification. For more details, the reader is encouraged to consult the official Agda documentation [6].

A.1 Record Types

A *record* is a product with named accessors for the individual fields. It provides a way to define a type that groups together inhabitants of other types.

Example.

```
record Pair (A B : Type) : Type where
  constructor (_,_)
  field
   fst : A
  snd : B
```

We can construct an element of the type Pair N N (i.e., a pair of natural numbers) as follows:

```
p23 : Pair N N
p23 = record { fst = 2; snd = 3 }
```

Since our definition of the Pair type provides an (optional) constructor (-,-), we can have defined p23 as follows:

```
p23': Pair N N p23' = (2,3)
```

Finally, we can "update" a record by deriving from it a new record whose fields may contain new values. The syntax is best explained by way of example.

```
p24 : Pair N N
p24 = record p23 { snd = 4 }
```

This results a new record, p24, which denotes the pair (2, 4).

See also agda.readthedocs.io/record-types.

B Bootstrapping EnactState

To form an EnactState, some governance action IDs need to be provided. However, at the time of the initial hard fork into Conway there are no such previous actions. There are effectively two ways to solve this issue:

- populate those fields with IDs chosen in some manner (e.g. random, all zeros, etc.), or
- add a special value to the types to indicate this situation.

In the Haskell implementation the latter solution was chosen. This means that everything that deals with GovActionID needs to be aware of this special case and handle it properly.

This specification could have mirrored this choice, but it is not necessary here: since it is already necessary to assume the absence of hash-collisions (specifically first pre-image resistance) for various properties, we could pick arbitrary initial values to mirror this situation. Then, since GovActionID contains a hash, that arbitrary initial value behaves just like a special case.

C Bootstrapping the Governance System

As described in CIP-1694, the governance system needs to be bootstrapped. During the bootstrap period, the following changes will be made to the ledger described in this document.

- Transactions containing any proposal except TriggerHF, ChangePParams or Info will be rejected.
- Transactions containing a vote other than a CC vote, a SPO vote on a TriggerHF action or any vote on an Info action will be rejected.
- Q4, P5 and Q5e are set to 0.
- An SPO that does not vote is assumed to have voted abstain.

This allows for a governance mechanism similar to the old, Shelley-era governance during the bootstrap phase, where the constitutional committee is mostly in charge [8]. These restrictions will be removed during a subsequent hard fork, once enough DRep stake is present in the system to properly govern and secure itself.