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CSCI 2125

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22 October 2021

Homework 3

```
public void inclusivePrintValuesBetween(AnyType k1, AnyType k2){
    printInRange(root, k1, k2);
}

private void printInRange(BinaryNode<AnyType> node, AnyType k1, AnyType k2) {
    if (node == null)
        return;

    if (node.element.compareTo(k1) >= 0)
        printInRange(node.left, k1, k2);

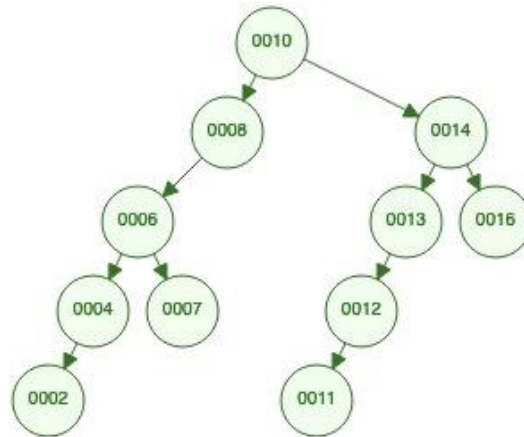
    if (node.element.compareTo(k1) >= 0 && node.element.compareTo(k2) <= 0)
        System.out.print(node.element + " ");

    if (node.element.compareTo(k2) <= 0)
        printInRange(node.right, k1, k2);
}
```

Implementation idea:

In the implementation, I used two methods, `inclusivePrintValuesBetween`, which calls the `printInRange` method with arguments `root`, `k1`, `k2`. In the `printRange` method, I used the inorder traversal algorithm to display the items from `k1` to `k2` in order, where `K` is the number of items, which is $O(K)$. If the node element is greater than or equal to `k1`, then we move along the tree to the left. If the node element is less than or equal to `k2`, then we move along the tree to the right. In general, as we know, the average BST depth is $O(\log N)$ on average, therefore we can say that the time complexity of the algorithm will be $O(K + \log N)$ on average.

Let's look at an example from the first `testFromLeftRight()` method of `RedirectTester_junit4.java` class. The values `k1 = 2` and `k2 = 14`, that is, we want to get all the elements in the tree from 2 to 14. The result should be 2 4 6 7 8 10 11 12 13 14.



We start with the root = 10. Since $10 \geq k_1(2)$, we move to the left through nodes $8 \rightarrow 6 \rightarrow 4 \rightarrow 2$. As soon as we get to 2, the first if-statement is encountered, which is true, because 2 is a leaf. Therefore, we recursively back from 2 to 6. While backtracking occurs, items 2 4 6 will be printed to the screen via `System.out.print`. Further, as soon as we returned to 6, the fourth condition of the if-statement will be true, which means that we are moving to 7. Since 7 is a leaf, we return to the root 10 ($7 \rightarrow 6 \rightarrow 8 \rightarrow 10$) and display the nodes that have not been withdrawn.

When it returns to 10, the fourth if-statement will be checked. It will be true because $10 \leq k_2(14)$. So, we move to the right to 14. As soon as we get to 14, then with a recursive call, everything starts from the beginning of the block of code, therefore the condition of the second if-statement will be true, and we move to the left through $14 \rightarrow 13 \rightarrow 12 \rightarrow 11$. Since 11 is a leaf, we go back and output all the nodes along the path to 14, namely 11, 12, 13, 14. After returning to 14, the fourth condition of the if-statement will be true, which means that we move right to 16. 16 is a leaf, therefore we return recursively from 16 to 14, but $16 \notin [2, 14]$. 16 will not be displayed because the condition of the third if-statement will be false (16 is not in range). After returning to 14, the `printInRange` method exits, thereby completing the `inclusivePrintValuesBetween` method. Actual result is as expected 2 4 6 7 8 10 11 12 13 14.